

Spectroscopy of exotic states (Experimental aspects)

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OUTLINE

- Lecture 1: The Past and Present
 - How it all began (on a parking lot)
 - The X, the Y and the Z
 - What is „beam constraint“?
- Lecture 2: The Future
 - Dalitz formalism: how to „see“ quantum numbers
 - (Bottomonium: recoil mass, kinematic reflections
→ BACKUP)
 - Belle II (ready to take data ?)
 - Panda, an X factory! („detailed balance“)

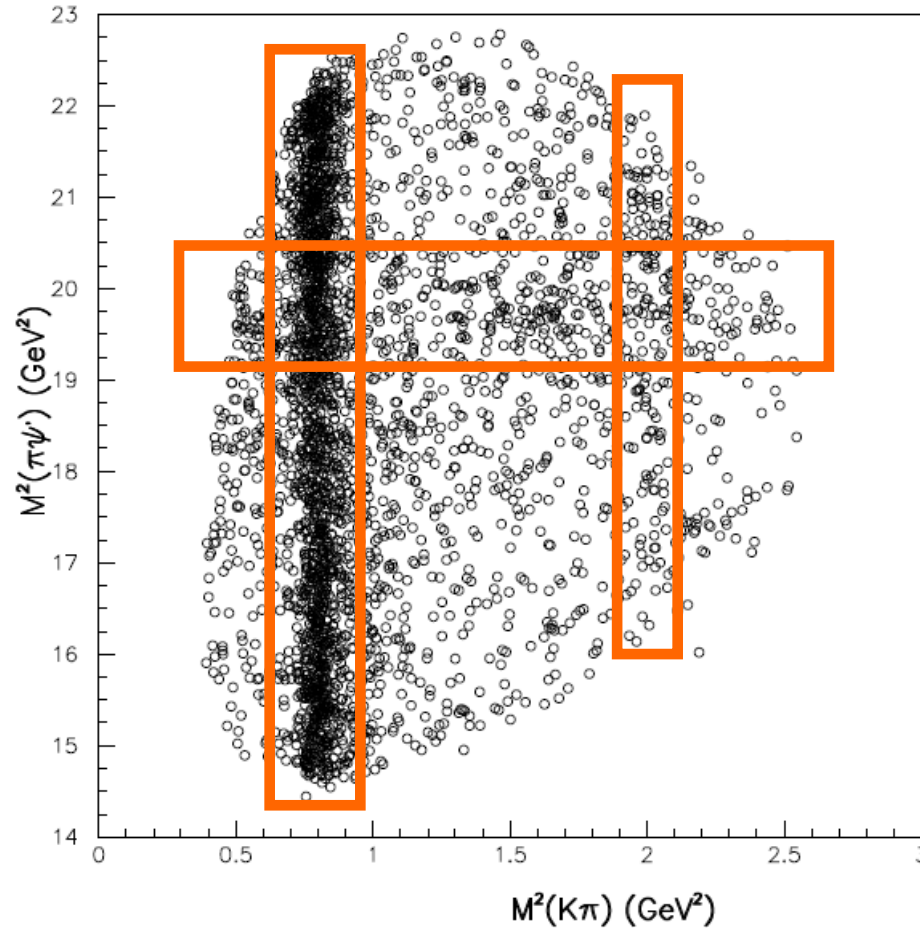
Lecture 2

$$B^0 \rightarrow K^+ \psi' \pi^-$$

$$\psi' \rightarrow J/\psi \pi^+ \pi^-$$

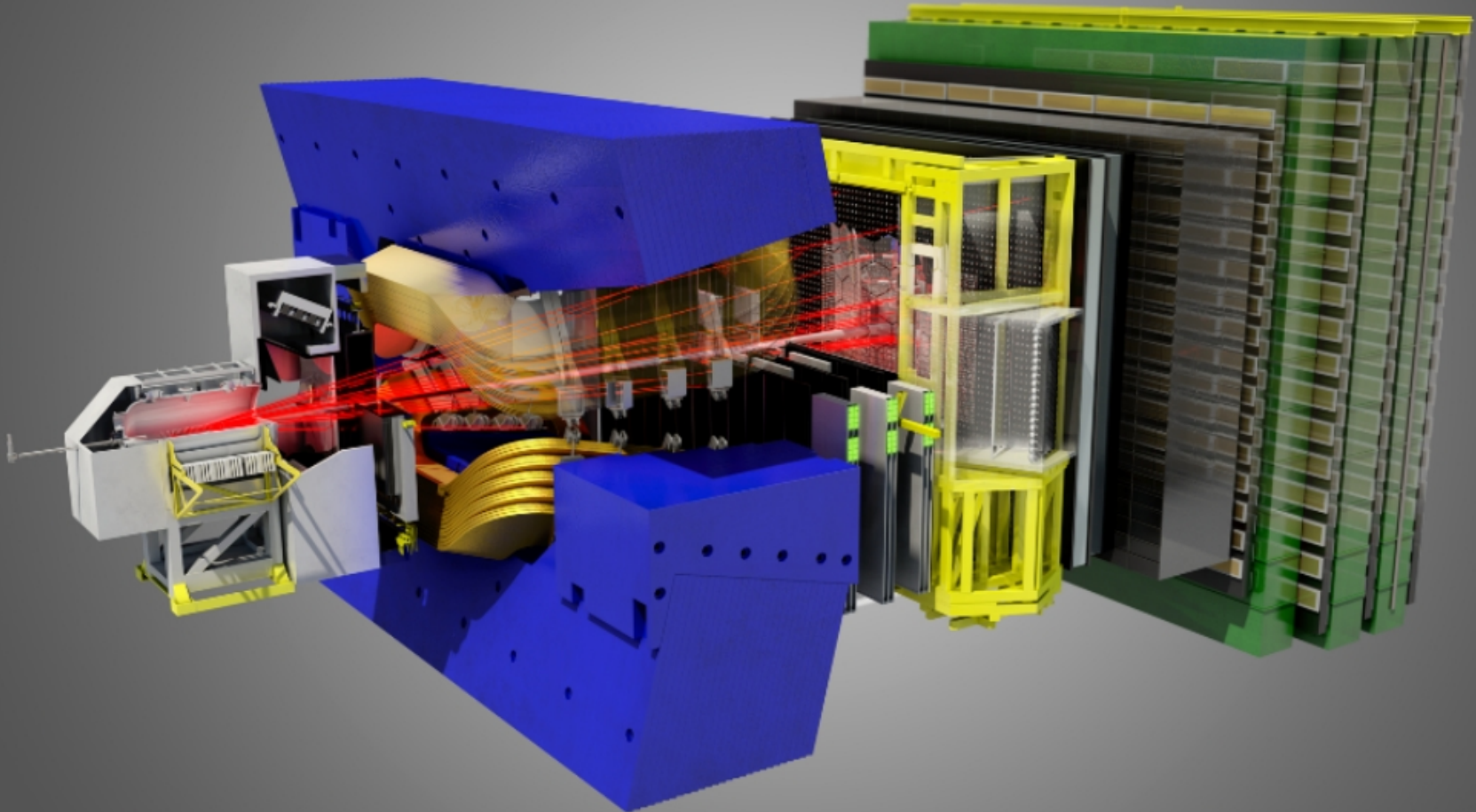
K*(892)

K*(1430)



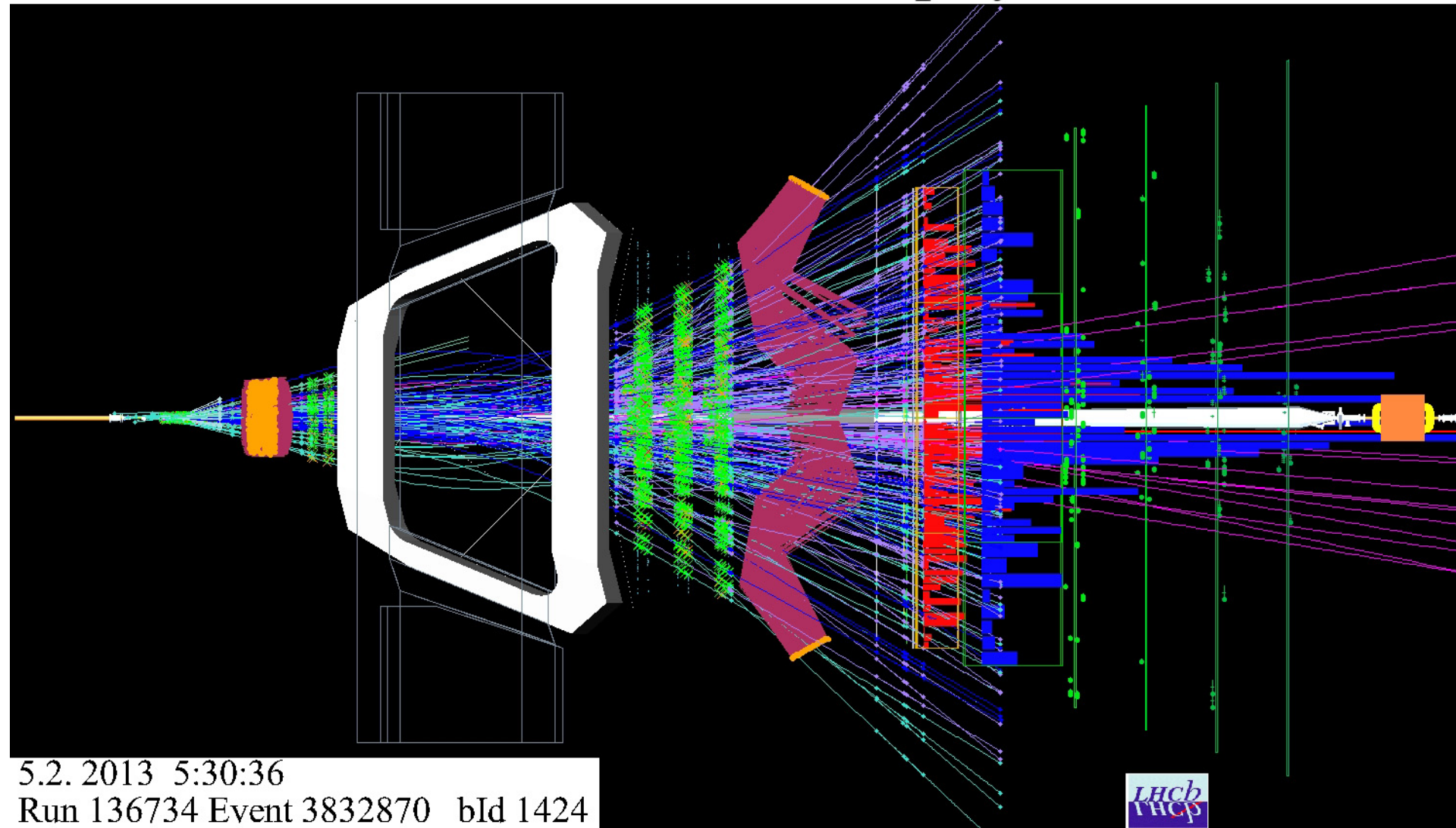
Confirmation of the $Z(4430)^+$ at LHCb

LHCb



Velo RICH1 MAGNET RICH2 MUON System
Tracking Stations Calorimeters

LHCb Event Display



Why forward boost?

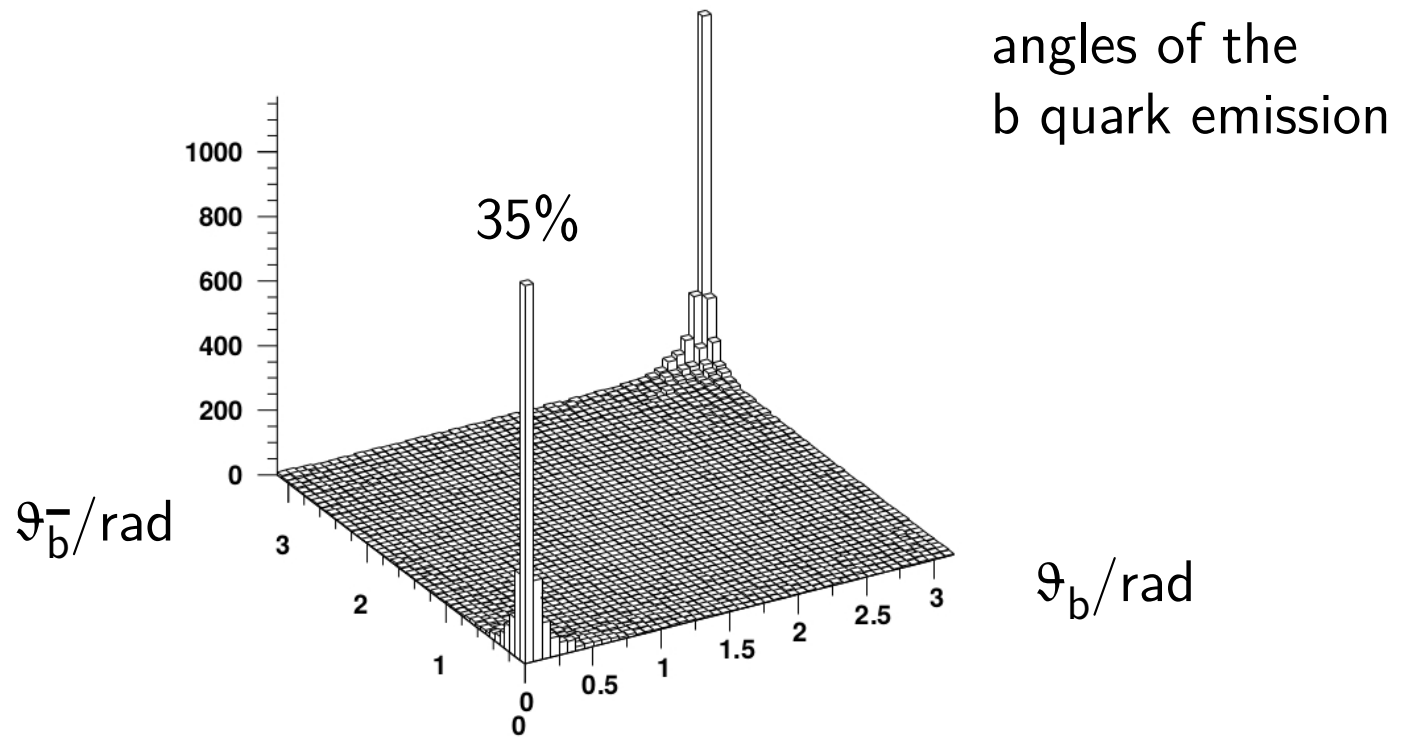
Is it a fixed target experiment?

N.B. the predecessor experiment, HERA-B,
was fixed target
with wire targets, moved into the beam.

No!

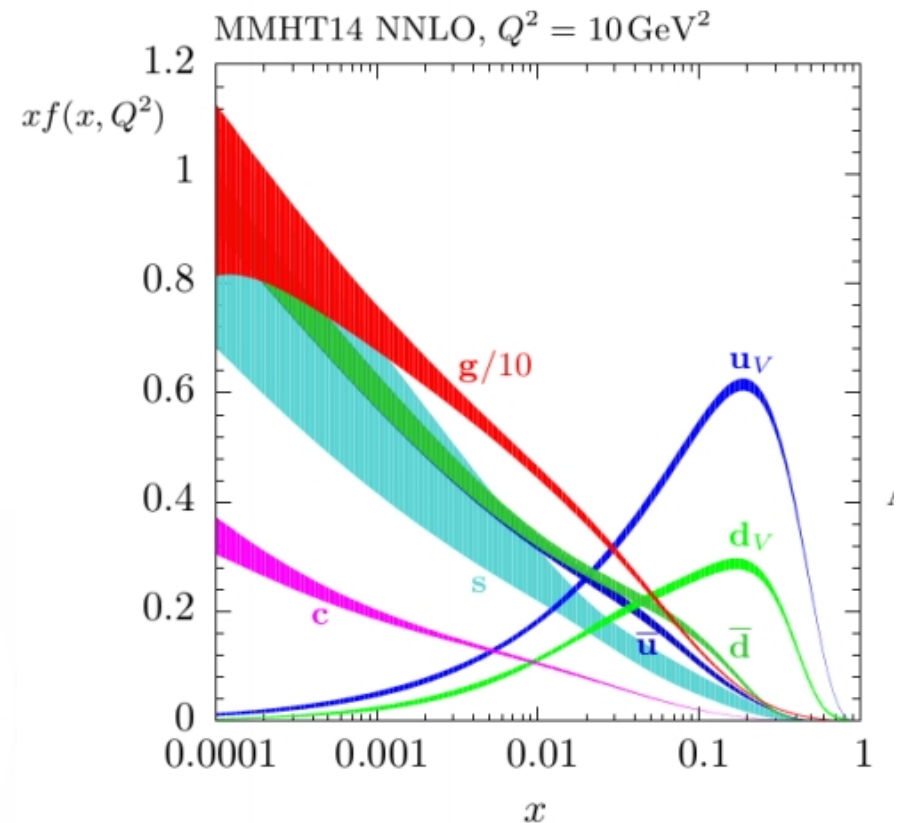
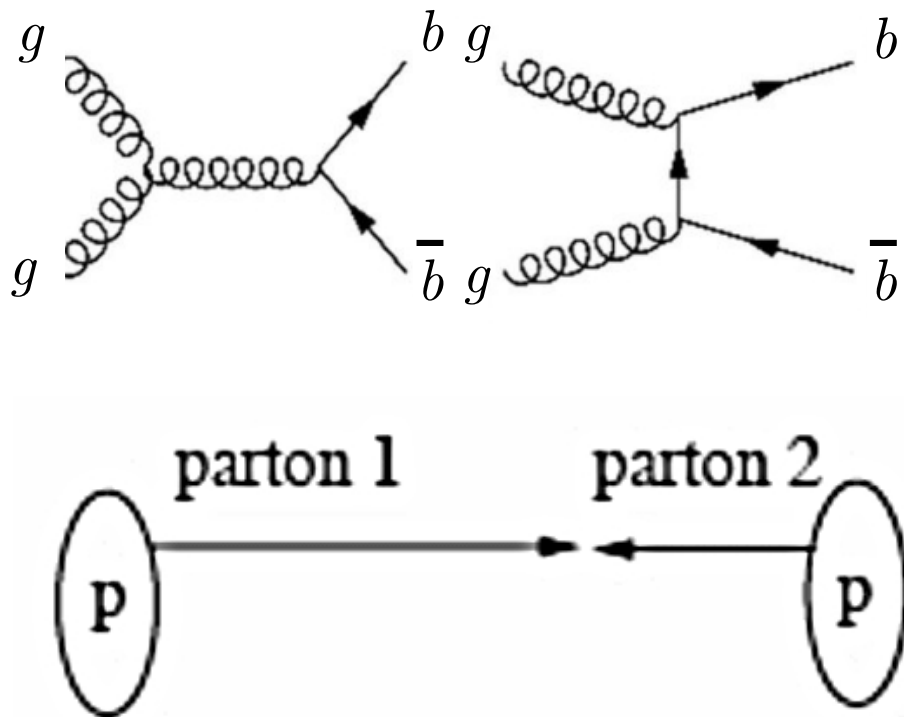
It is a pp interaction.

So, why is LHCb „peaked forward“?



b quark production at LHCb is dominated by gluon gluon fusion
 $\sqrt{s'} = x_1 x_2 \sqrt{s}$, average product is 0.1

prefers asymmetric parton momentum fractions



LHCb

Cross sections at 14 TeV:

Total	100 mb
Inelastic	80 mb
$c\bar{c}$	3.5 mb
$b\bar{b}$	$500 \mu\text{b}$

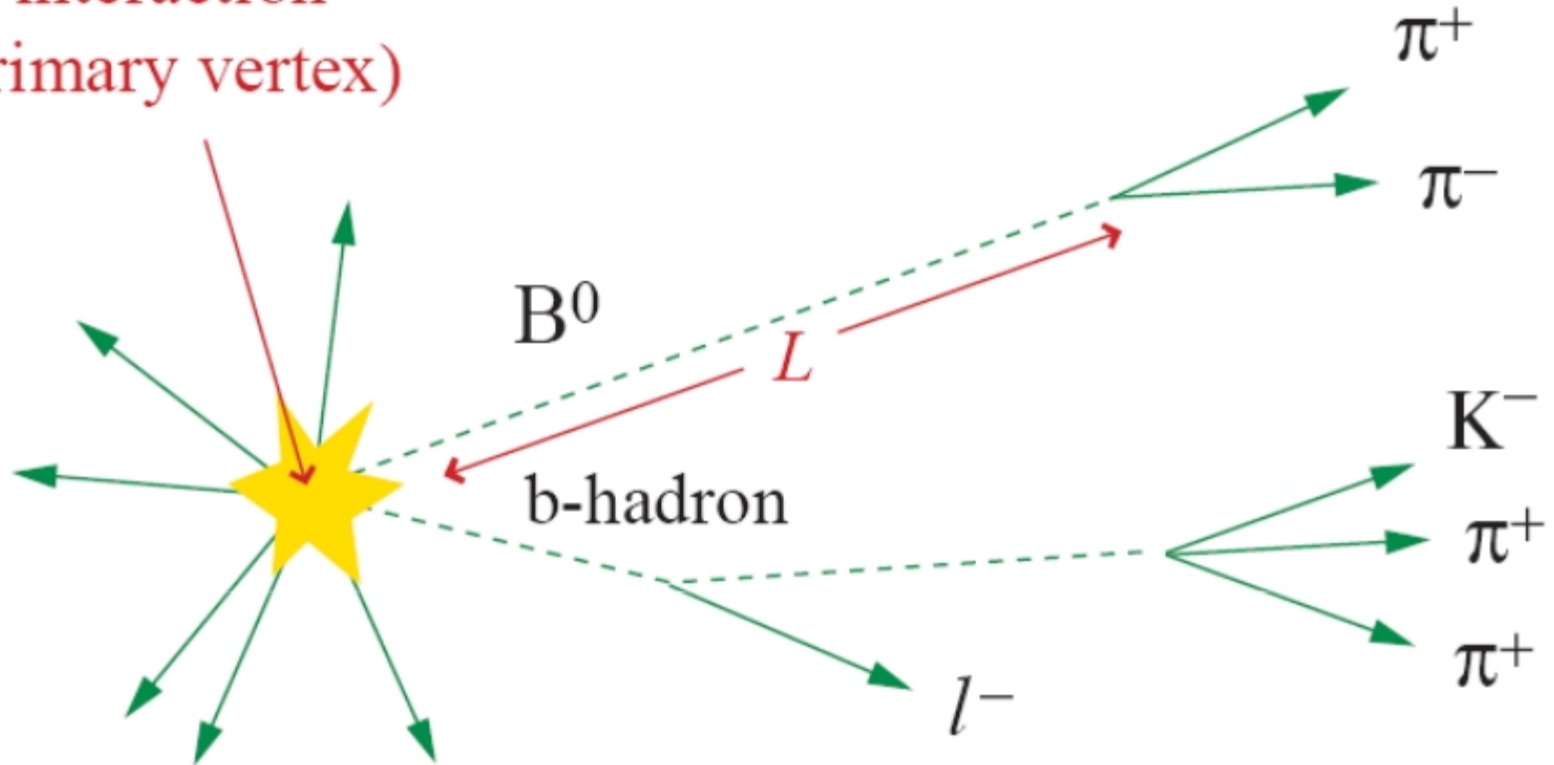
remember Belle: 1.2 nb

In 1 in every 200 collisions a
 $b\bar{b}$ pair is produced

} needs a clever trigger
(„High level trigger“)

LHCb

pp interaction
(primary vertex)

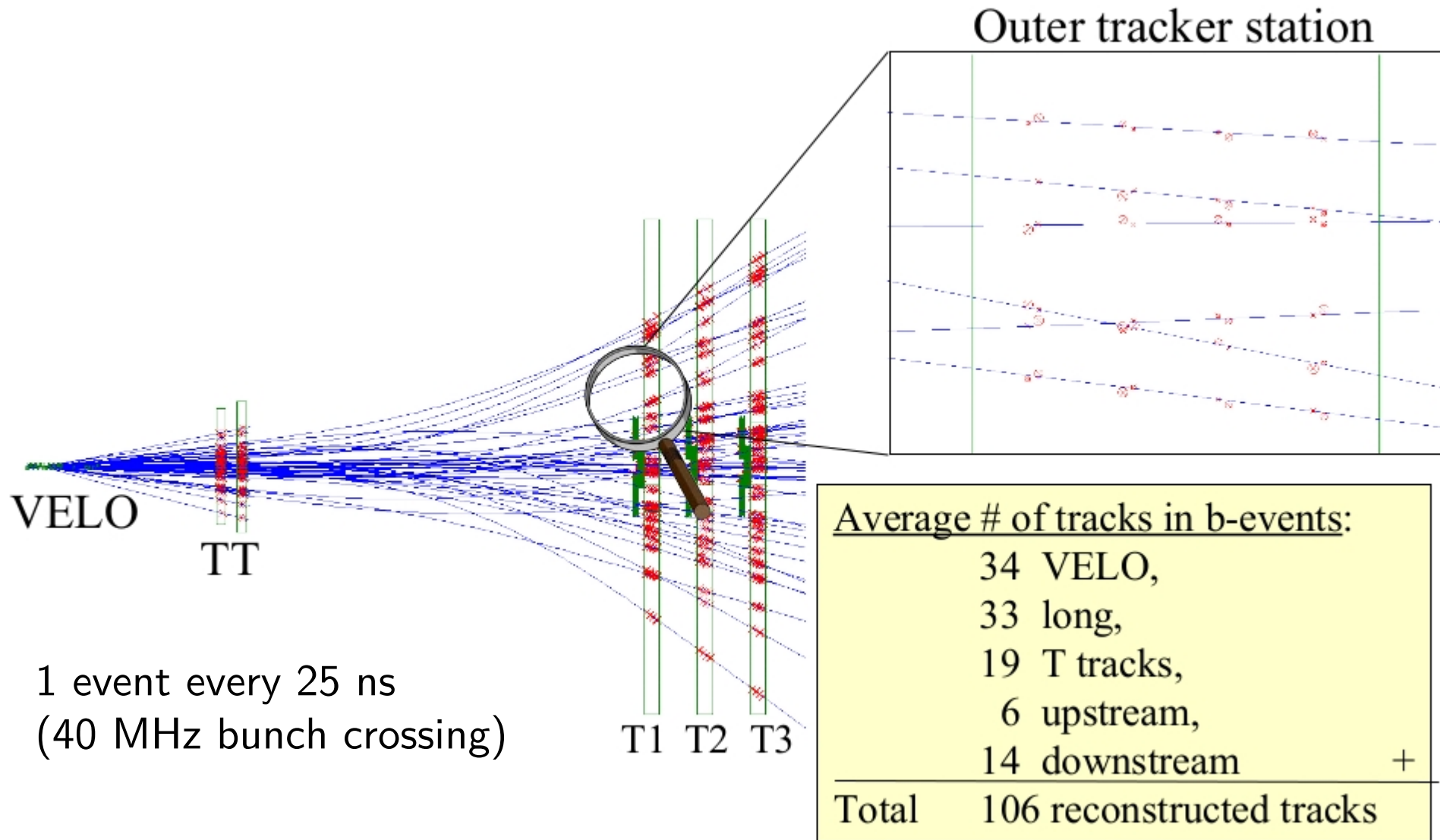


- Typical decay length of B hadron ~ 7 mm
- Decay products with $p \sim 1 - 200$ GeV

Advantage: high momentum
detector materials don't have to be very thin!

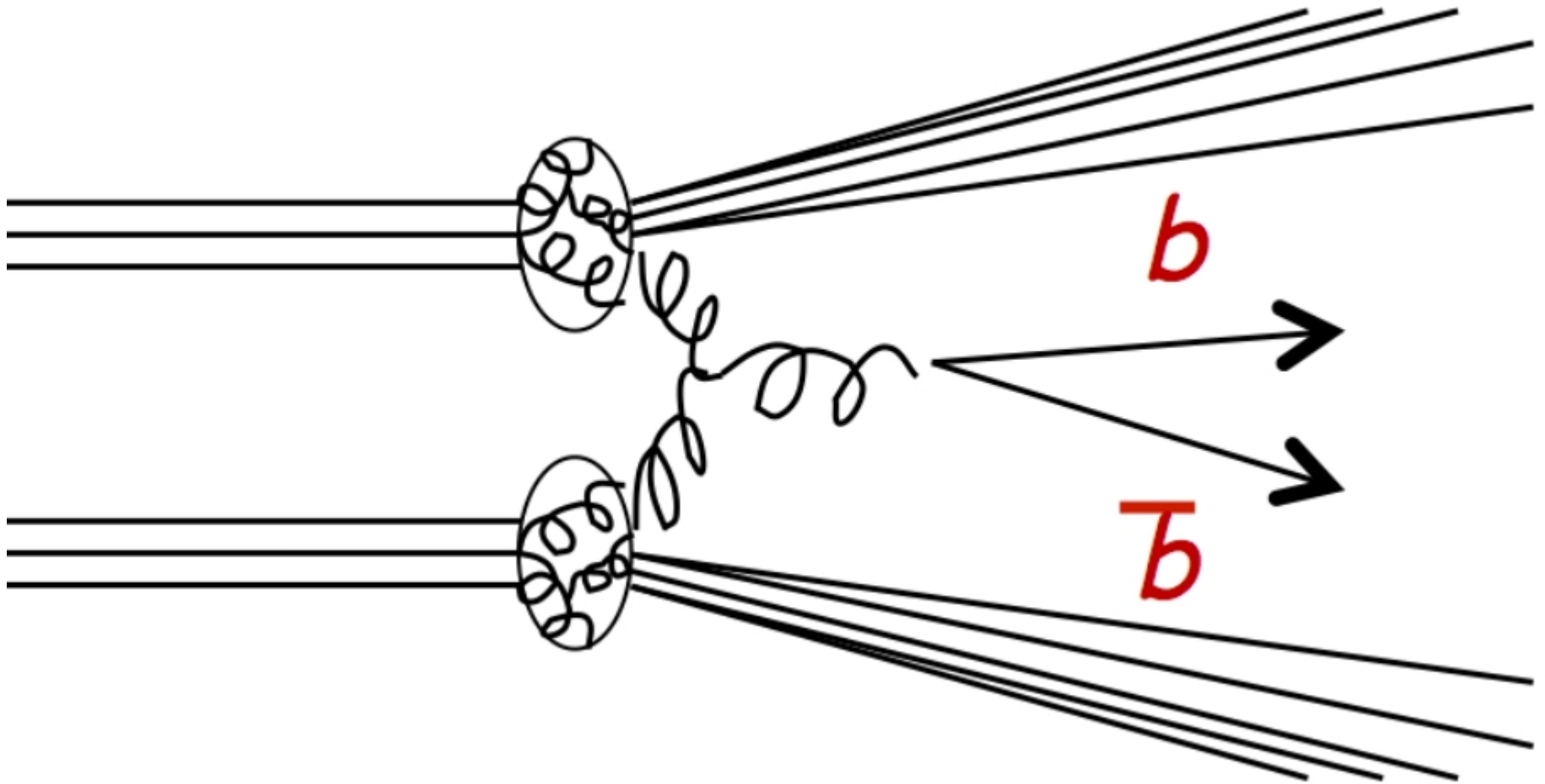
Belle
 ~ 200 μm
1-4 GeV

LHCb

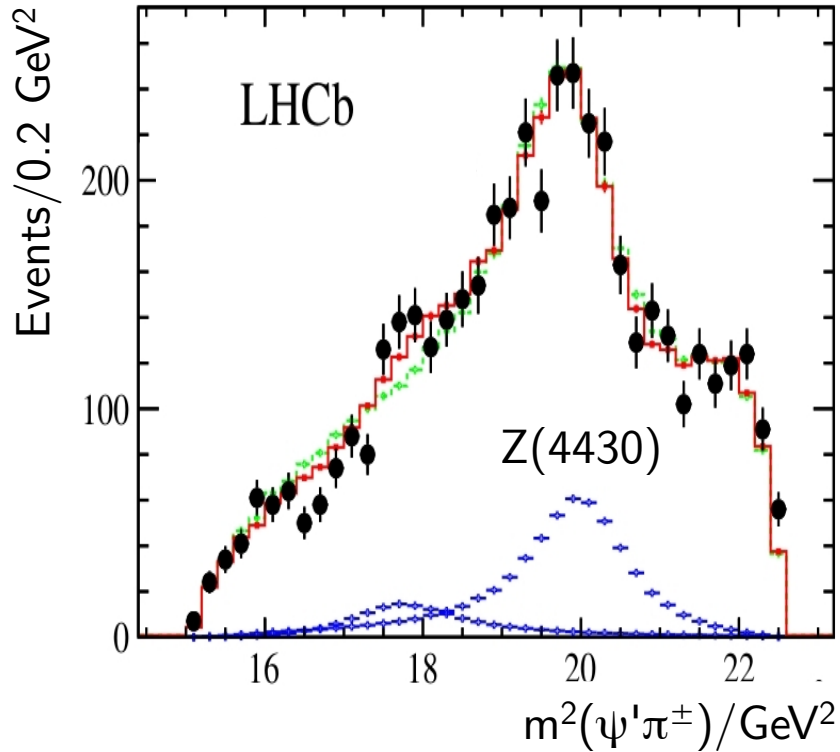


Uli Uwer, Heidelberg

Why so many tracks at LHCb ?



Confirmation of the $Z_c(4430)^+$ in B meson decays



$$B^0 \rightarrow K^\pm \underbrace{\psi' \pi^\mp}_{\text{resonant state?}}$$

LHCb, PRL 112(2014)222002

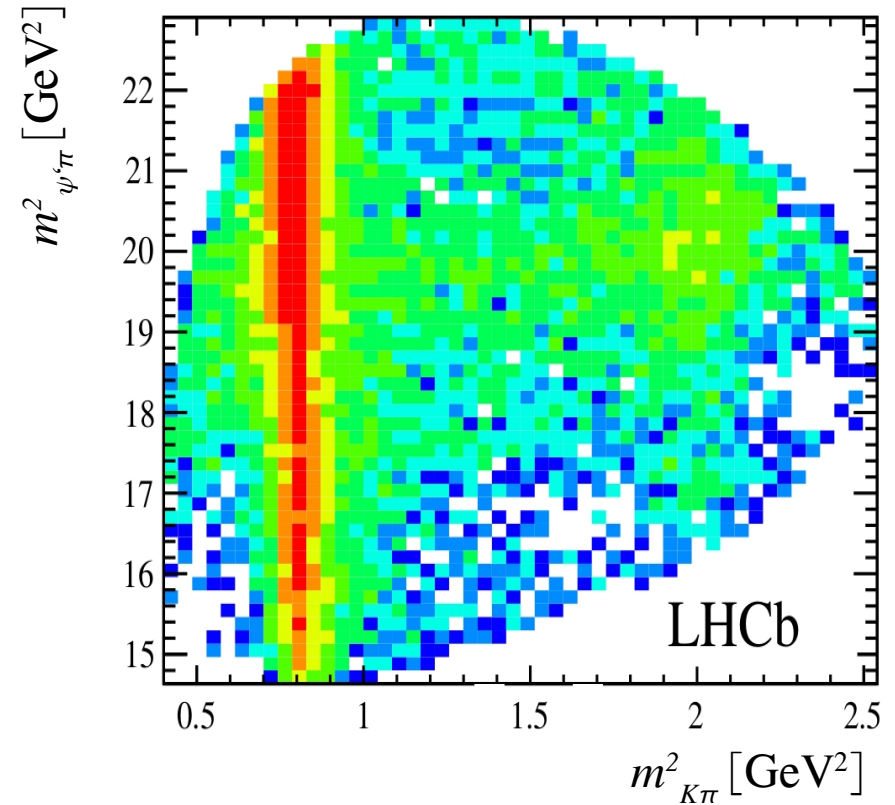
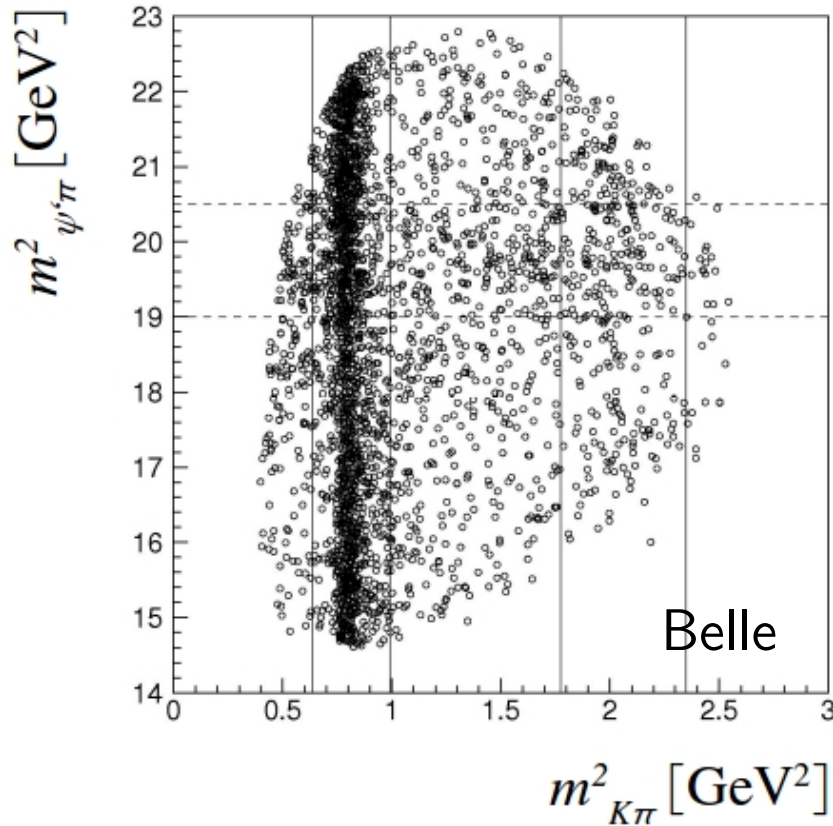
significance $\geq 13.9\sigma$

$J^P = \mathbf{1}^+$ established
(other J^P rejected by $\geq 9.7\sigma$)

4-dim Dalitz Fit

$$\Phi = (M_{K\pi}^2, M_{J/\psi\pi}^2, \theta_{J/\psi}, \varphi)$$

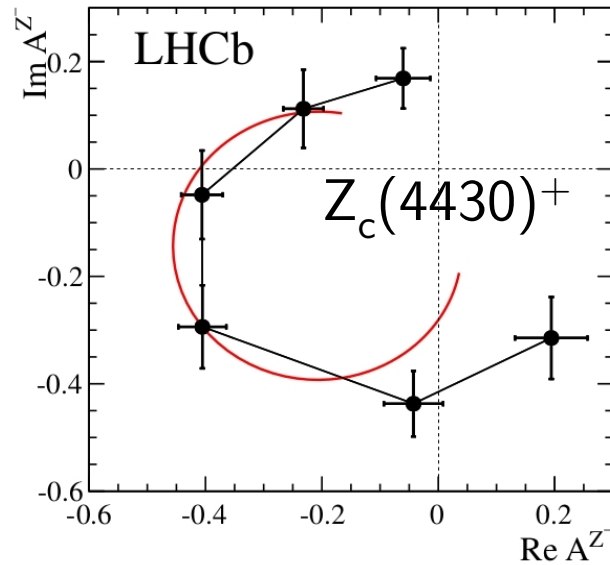
Z(4430)



25176 $\pm$ 174 events
factor 10 more than Belle

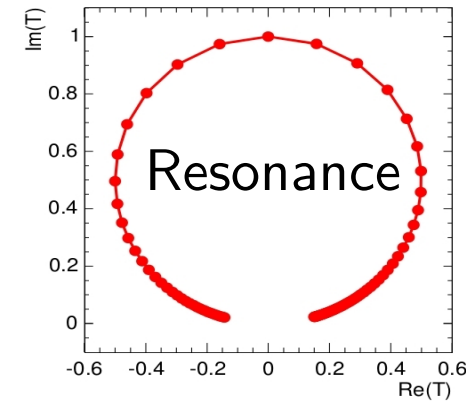
ARGAND PLOT: resonant character of Z^+ states

LHCb, PRL 112(2014)222002

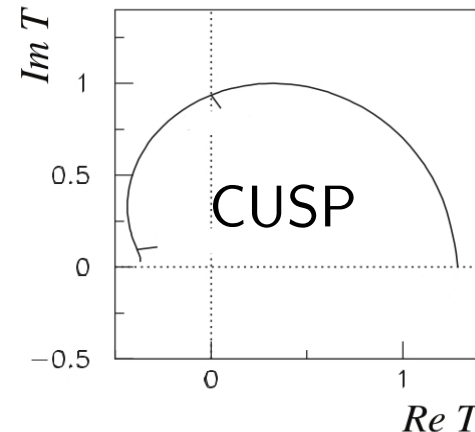


$$\frac{m\Gamma}{s - m^2 - im\Gamma}$$

clockwise
or
counter-clockwise?



phase motion 180°



positive $\text{Im}(T)$ only
phase motion not 180°

K. Peters,
arXiv:hep-ph/0412069

D. Bugg,
EPL 96(2011)11002

Why a Breit-Wigner has counter clockwise phase motion.

$$\frac{m\Gamma}{s - m^2 + im\Gamma} = \frac{m\Gamma s - m^3\Gamma}{(s - m^2)^2 + m^2\Gamma^2} - i \frac{m^2\Gamma^2}{(s - m^2)^2 + m^2\Gamma^2}$$



PDG convention

Belle and LHCb convention is minus

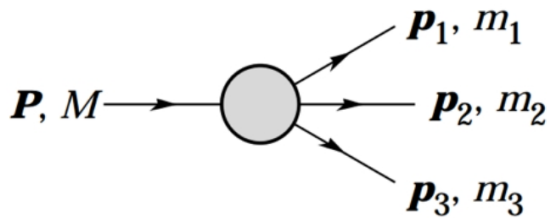
$$\mathcal{M}_{ba}^{\text{pole}} \Big|_{N=1} = - \frac{g_b g_a}{s - M_{\text{BW}}^2 + i\sqrt{s}\Gamma_{\text{BW}}}$$

PDG, Review „Resonances“, 2016 version, p. 8

**Howto determine
the quantum number
of the $Z(4430)$?**

DALITZ FORMALISM

Example: decay of a scalar to 3 scalars



Constraint

3 four-vectors

masses m_1, m_2, m_3 fixed

Energy and momentum conserved

rotational invariance (Euler angles)

DOF

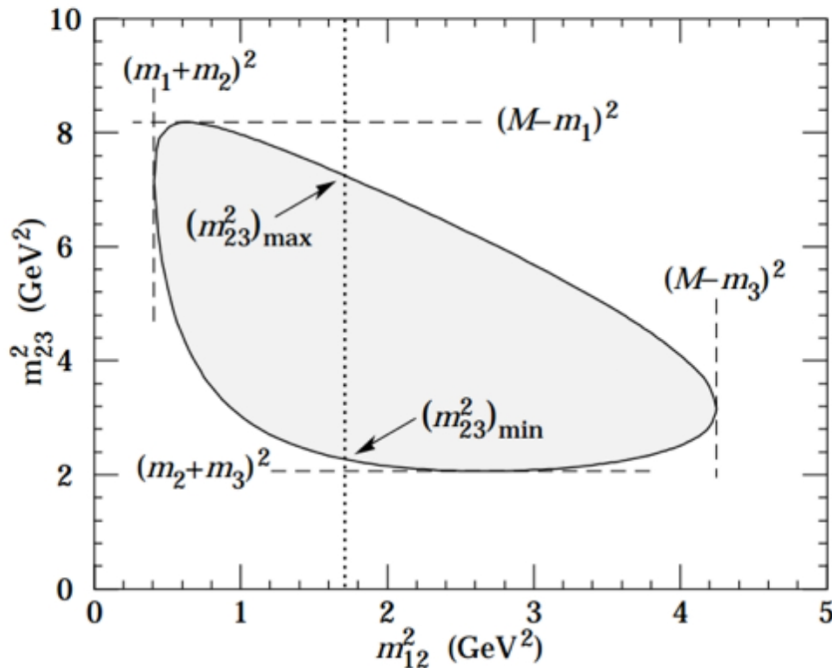
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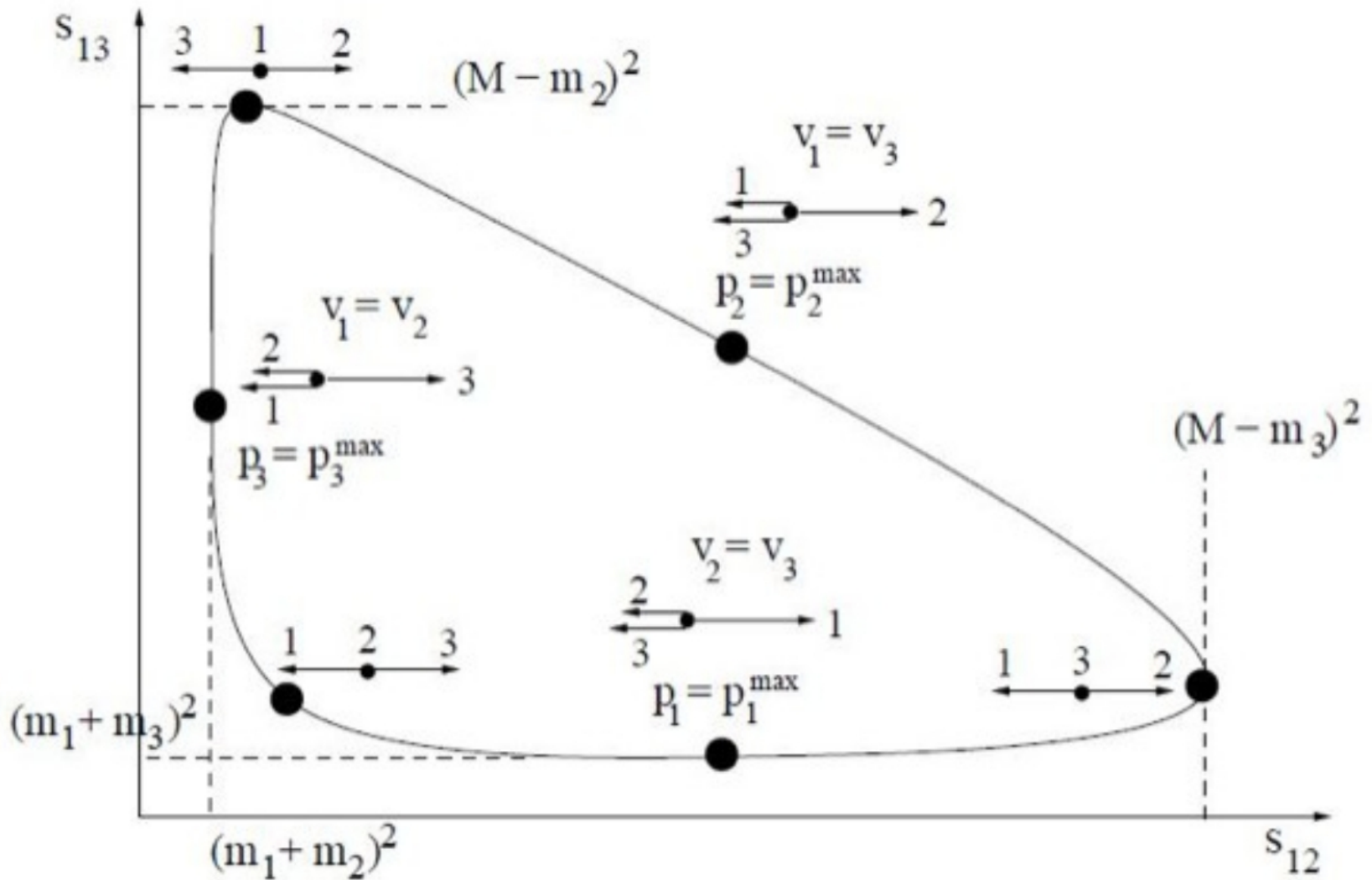
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2

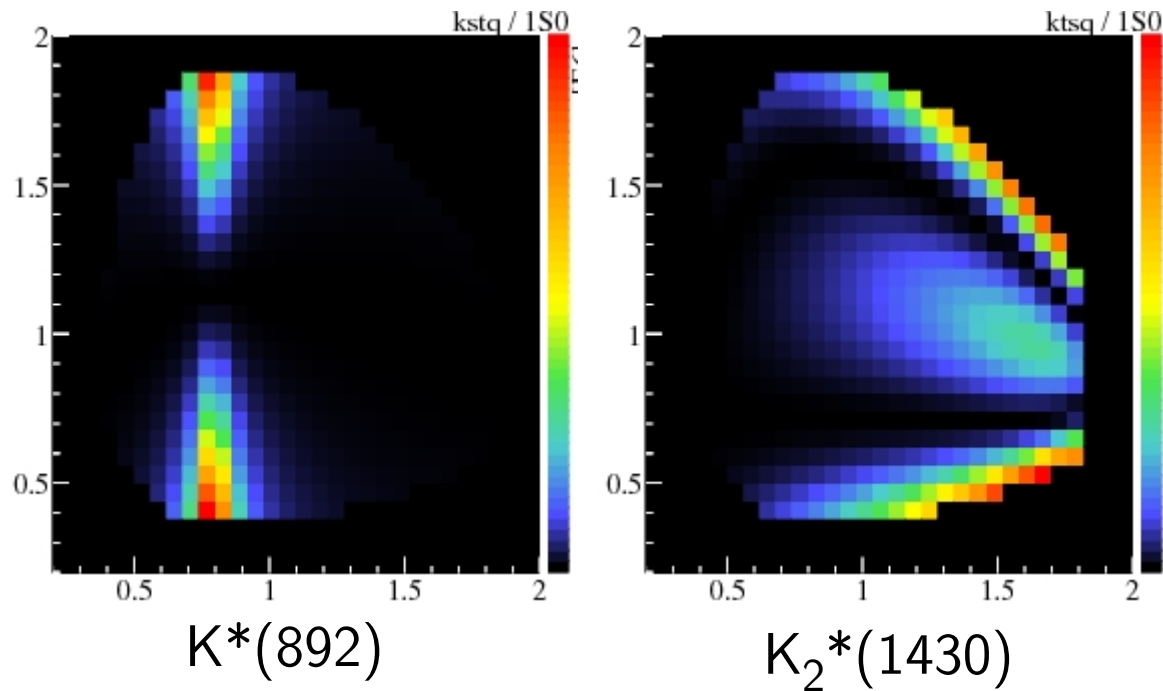


Kinematics fully determined
by 2 variables!

3-particle kinematics, mapped onto Dalitz space



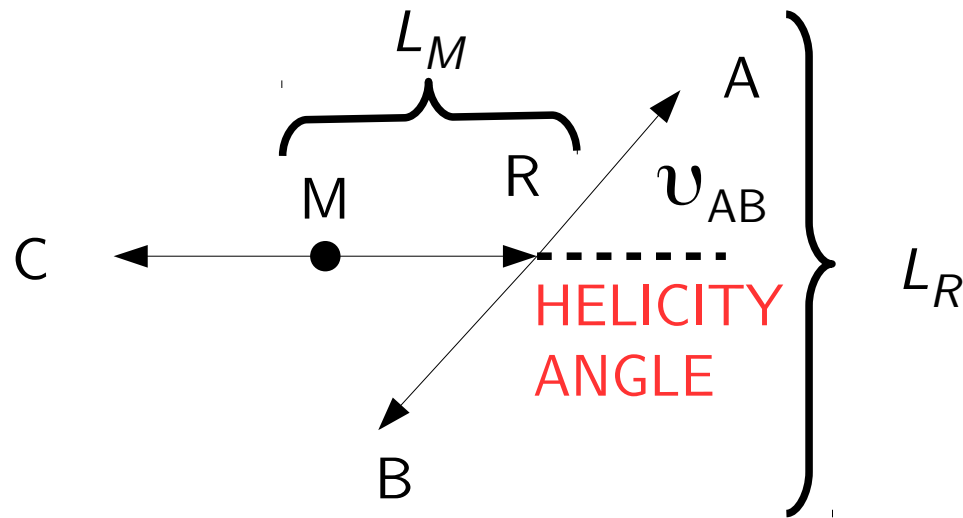
Dalitz plot example: $p \bar{p} \rightarrow K K \pi$



J	L	1	Angular distribution
0	0	0	1
0	1	1	$\cos^2 \theta$
0	2	2	$(\cos^2 \theta - \frac{1}{3})^2$

M. T. Lakata, Ph. D. Thesis,
University of California Berkeley, 1998

**Why do we „see“
angular distributions
in m^2 distributions
in a Dalitz plot?**



$$f(m_{AB}, m_{BC}) = f_S(m_{AB}, m_{BC}) \times \varepsilon(m_{AB}, m_{BC}) + f_B(m_{AB}, m_{BC})$$

COMPLEX NUMBERS

$$f_S(m_{AB}, m_{BC}) = \sum_{\lambda} \left| \sum_R T_{fi}^{R, \lambda} \right|^2$$

signal density in Dalitz plot
(number of events in a bin)

Polarisations
e.g. $\lambda = -1, 0, 1$ for $J=1$

$$\begin{aligned}
 T_{fi}(m_{AB}, m_{BC}) = & \frac{1}{m_R^2 - s_R - im_R \Gamma_{tot}(s_R)} \\
 & \cdot F_M^{L_M} \cdot F_R^{L_R} \cdot \underbrace{\left(\frac{p_M}{m_M}\right)^{L_M} \cdot \left(\frac{p_R}{\sqrt{s_R}}\right)^{L_R}}_{\text{Angular dependance}} \cdot T_\lambda \cdot
 \end{aligned}$$

Formfactors

Momenta in the center-of-mass frames
Momentum dependance enters explicitly !

Formfactors

often: Blatt-Weisskopf barrier factors

$$F^0(z) = 1$$

$$F^1(z) = \frac{\sqrt{1 + z_0}}{1 + z}$$

$$F^2(z) = \frac{\sqrt{z_0^2 + 3z_0 + 9}}{z^2 + 3z + 9}$$

$$F^3(z) = \frac{\sqrt{z_0^3 + 6z_0^2 + 45z_0 + 225}}{z^3 + 6z^2 + 45z + 225}$$

Here $z=r^2p^2$ with a scale parameter representing the radius of the centrifugal barrier and usually set to $R\simeq 1.6 \text{ (GeV/c)}^{-1}$, which is $R\simeq 3\text{-}4 \text{ fm}$. For z_0 we use p_{R0} which is the R resonance daughters momentum calculated for the pole mass of R .

Width (in the Breit–Wigner Term)

$$\Gamma(s_R) = \Gamma_0 \left(\frac{p_R}{p_{R0}} \right)^{2L_R+1} \frac{m_R}{\sqrt{s_R}} \cdot F_R^2$$

(again, using Blatt-Weisskopf)

Angular dependant term

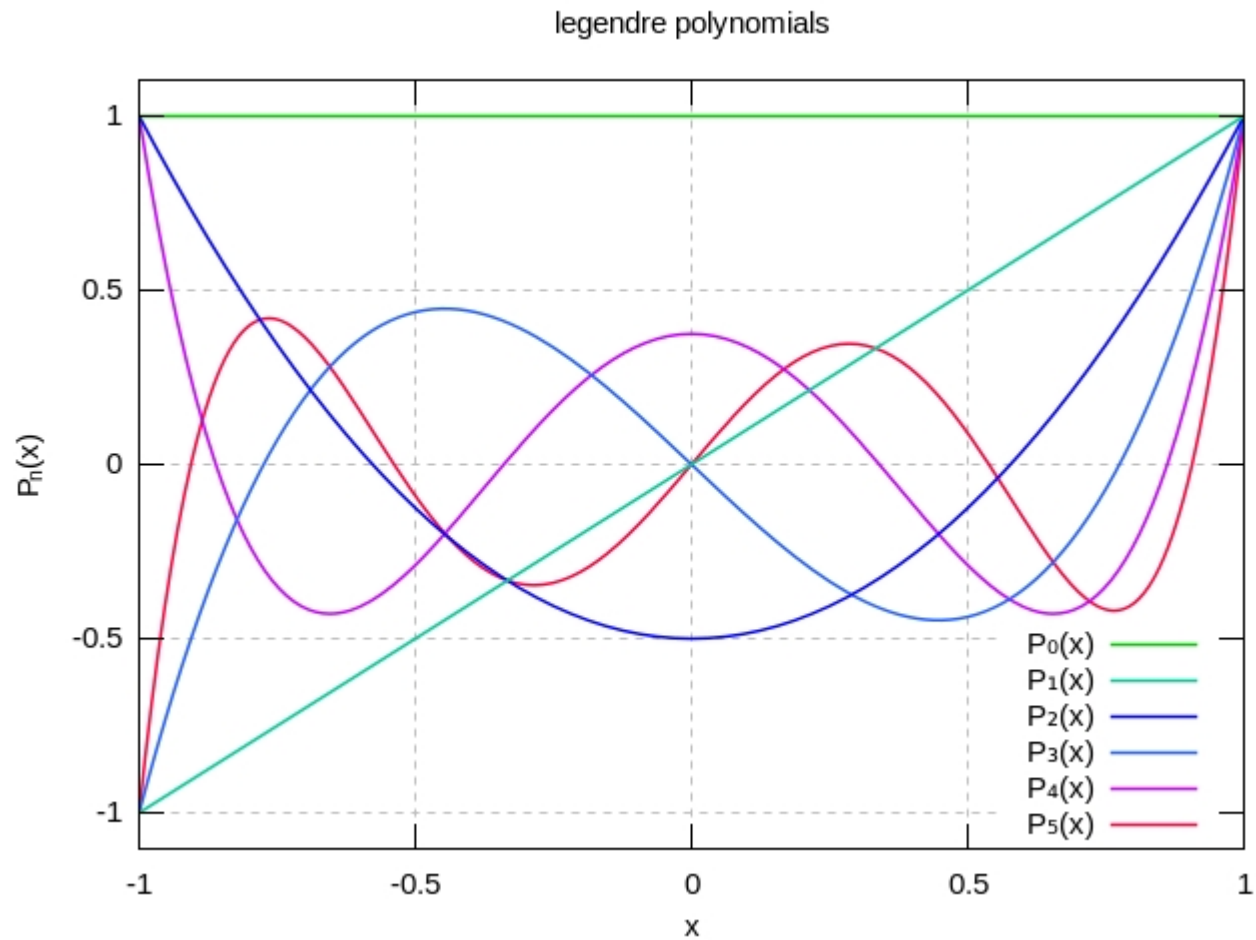
$$T_\lambda = d_{\lambda\lambda'}^J(\vartheta_{AB})$$

where J is the spin of the $R \rightarrow AB$ resonance and ϑ_{AB} its polar angle ("helicity angle"). $d_{\lambda\lambda'}^J$ are the Wigner D functions, which for $\lambda'=0$ can be expressed by the spherical harmonics

$$d_{\lambda 0}^J = \frac{4\pi}{2J+1} (-1)^\lambda Y_J^{-\lambda}$$

and for $\lambda=0$ and $\lambda'=0$ by the Legendre polynoms

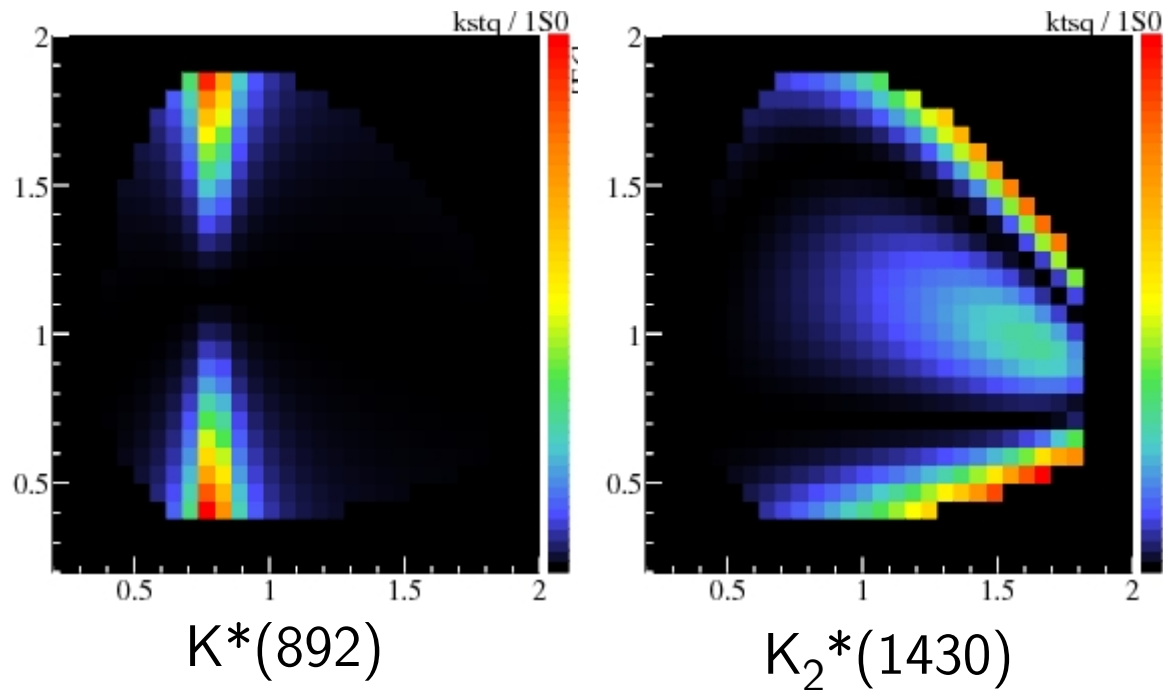
$$d_{00}^J = P_J(\cos\vartheta_{AB}) .$$



J is spin of resonance R

L_1	L_2	J	T_λ
0	0	0	1
1	1	0	$\cos^2(\vartheta_{AC})$
2	2	0	$(\cos^2(\vartheta_{AC})-1/3)^2$
1	0	1	1
0	1	1	1
1	1	1	$\sin^2(\vartheta_{AC})$
1	2	1	$\cos^2(\vartheta_{AC})+1/3$
2	1	1	$\cos^2(\vartheta_{AC})+1/3$
2	2	1	$(\cos(\vartheta_{AC})\sin(\vartheta_{AC}))^2$
2	0	2	1
0	2	2	1
1	1	2	$(\sin^2(\vartheta_{AC})+1/3)^2$
2	1	2	$\sin^2(\vartheta_{AC})$
2	2	2	$\cos^2(\vartheta_{AC})$

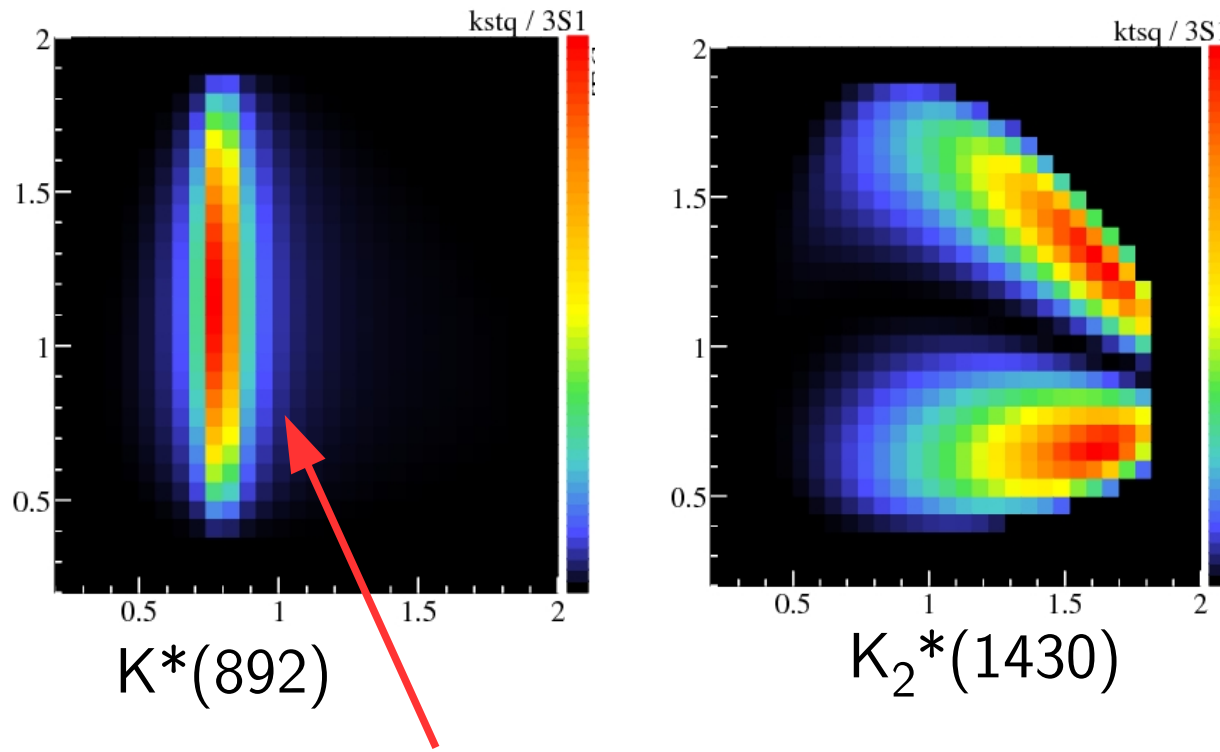
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M. T. Lakata, Ph. D. Thesis,
University of California Berkeley, 1998

If $J_{total}=1$, then distributions change



we reach K^* by $L=0$

$B \rightarrow \psi' K \pi$
 (search for $Z(4430)$ is $[\psi \pi']$)
 scalar $\rightarrow$ **vector** scalar scalar

Constraint

3 four-vectors
 masses m_1, m_2, m_3 fixed
 energy and momentum conserved
 rotational invariance (Euler angles)
vector helicity

DOF

12

-3

-4

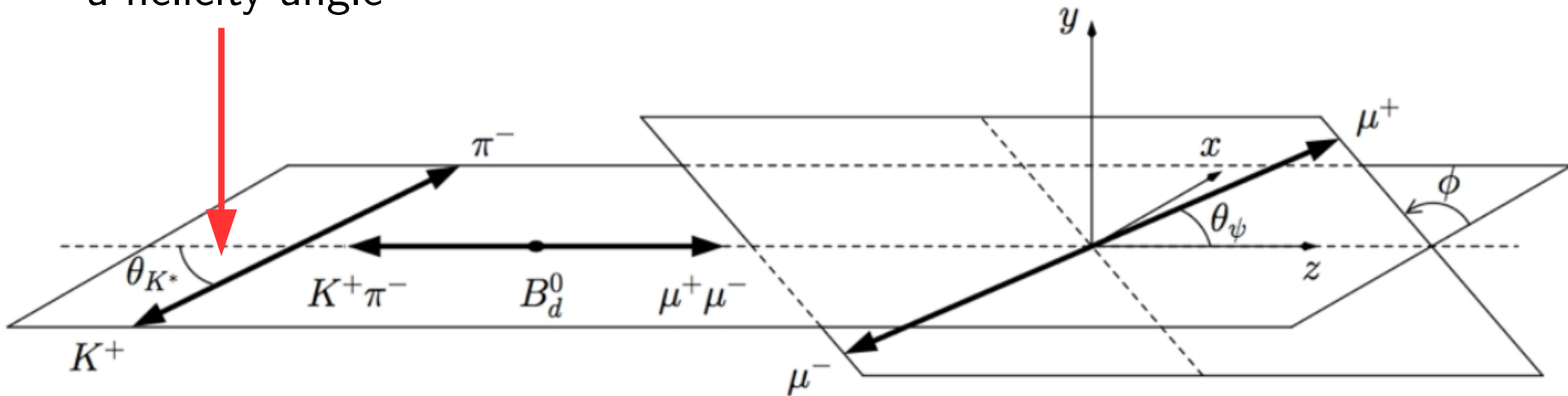
-3

2

—

4

a helicity angle



requires 4-dim analysis!

If more than 2 variables: Dalitz plot shape becomes
a function of the 3rd or 4th variable ...

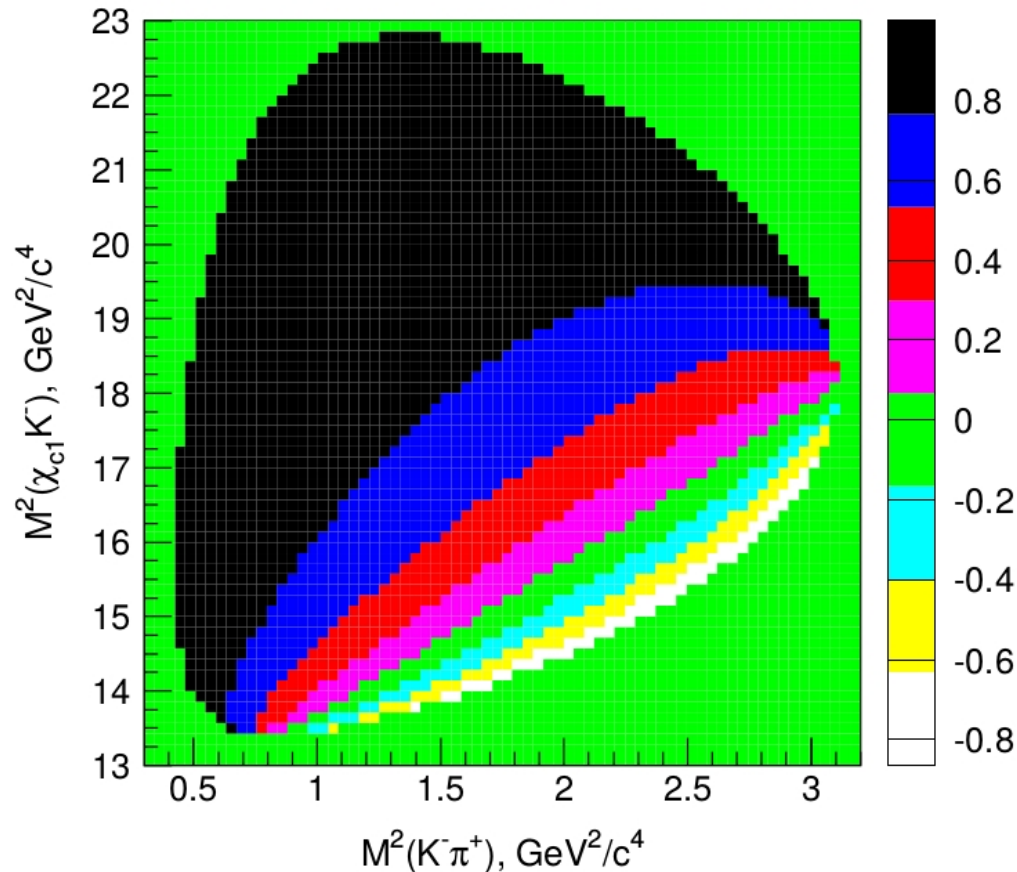


FIG. 5: $\cos \theta$ as a function of the Dalitz plot variables, where θ is the angle between the helicity axes for $K\pi$ and $\pi\chi_{c1}$ intermediate resonances.

Belle, Phys. Rev. D78(2008)072004

Legendre decomposition of $Z(4430)^+$ data („model independent“)

LHCb, Phys. Rev. D 92(2015)112009

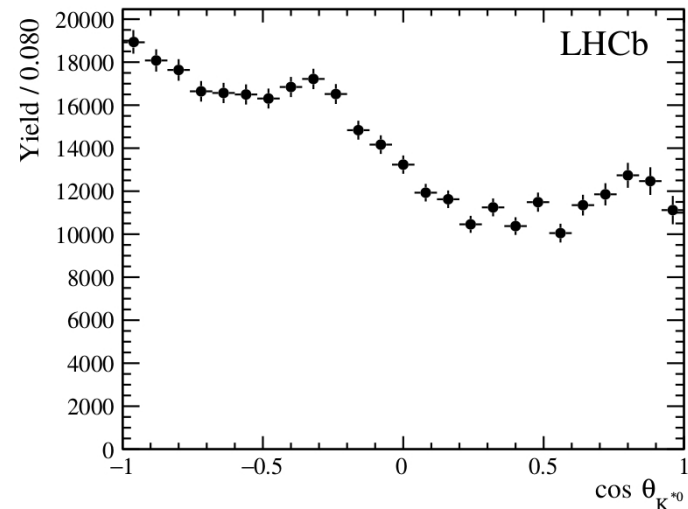
$$\frac{dN}{d \cos \theta_{K^*0}} = \sum_{j=0}^{l_{\max}} \langle P_j^U \rangle P_j(\cos \theta_{K^*0})$$

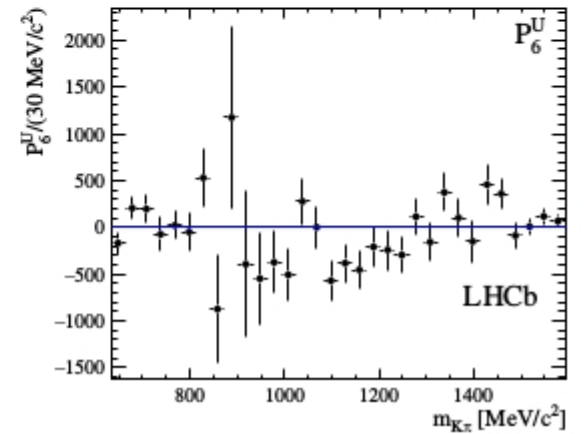
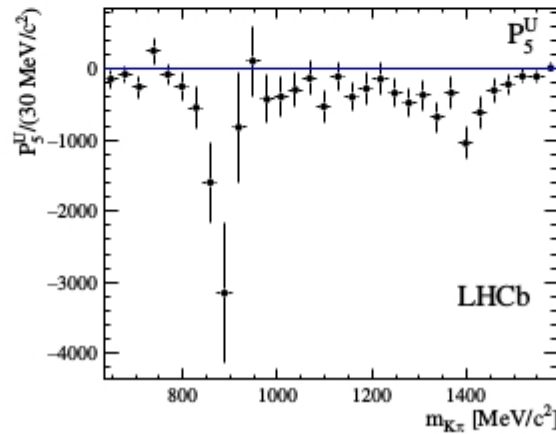
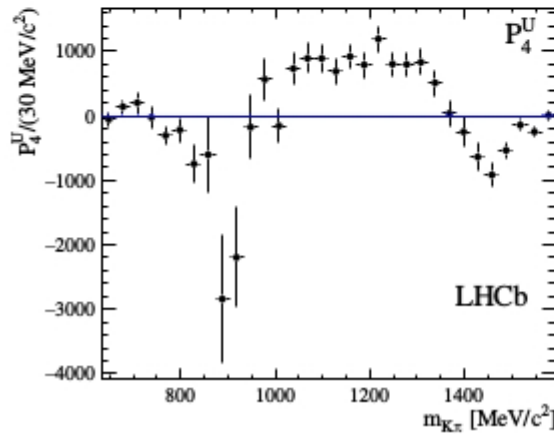
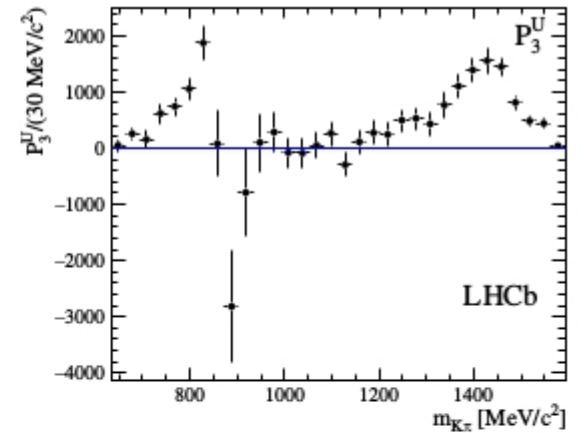
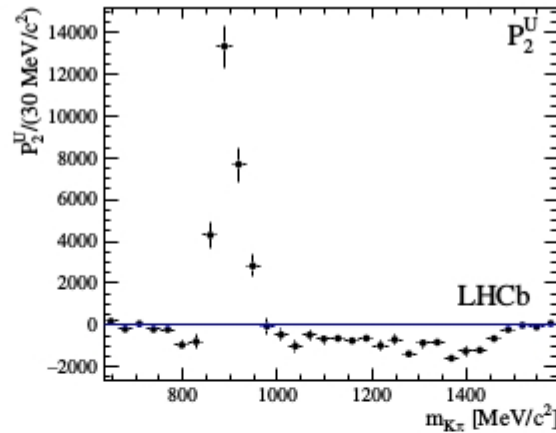
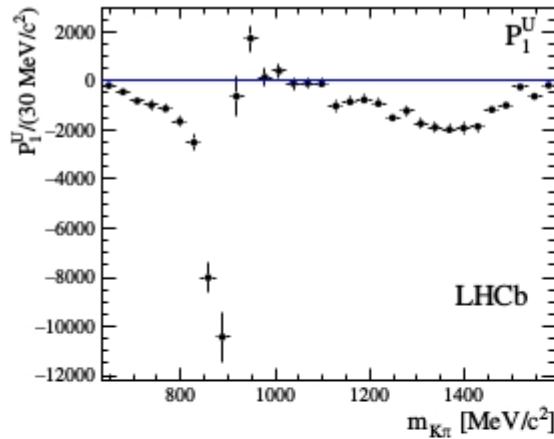
↑ „moments“

select a certain bin in $m(K\pi)$

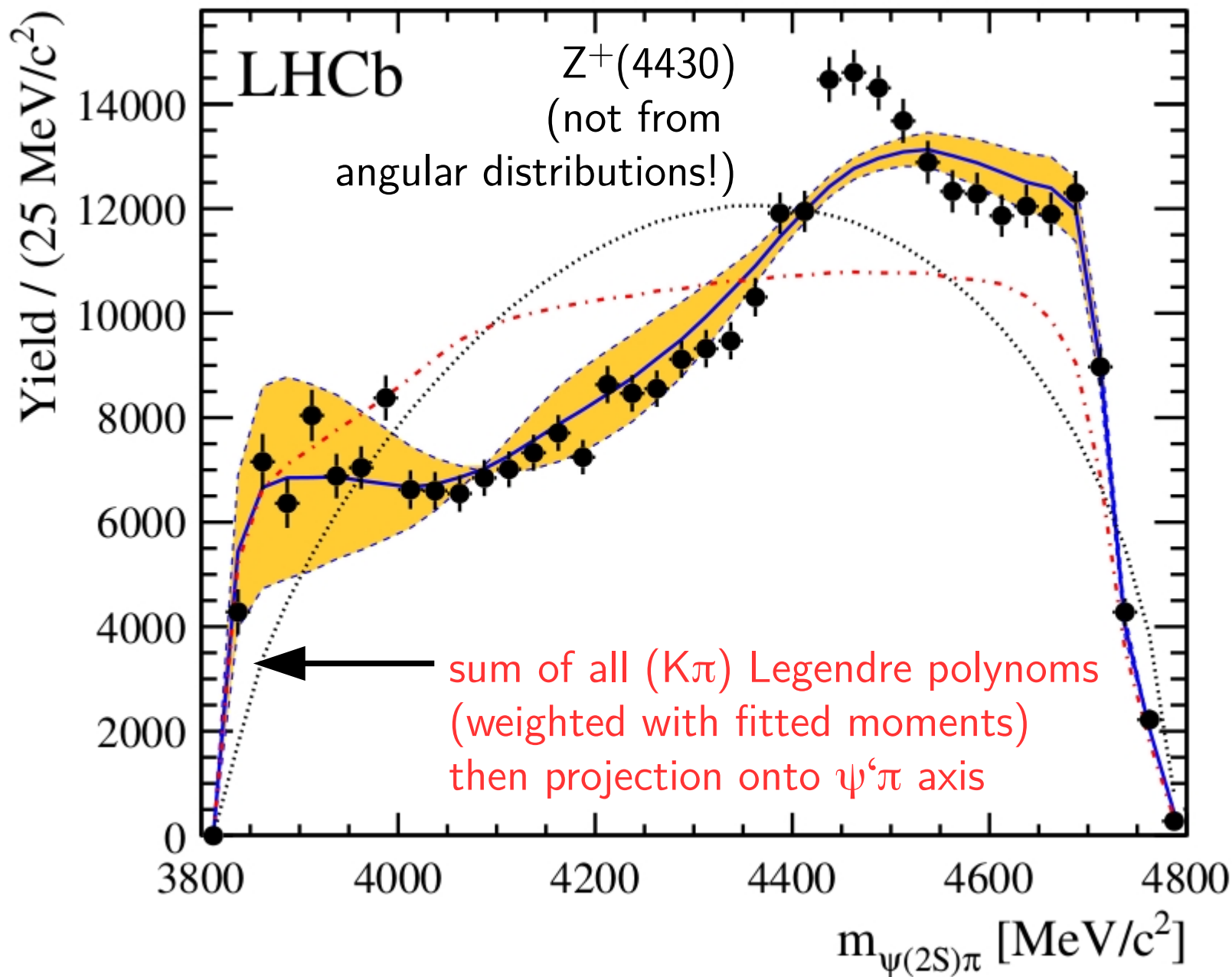
find the decomposition in
Legendre polynomials
in $\cos(\theta_{K^*})$

this works, because it is an orthogonal system

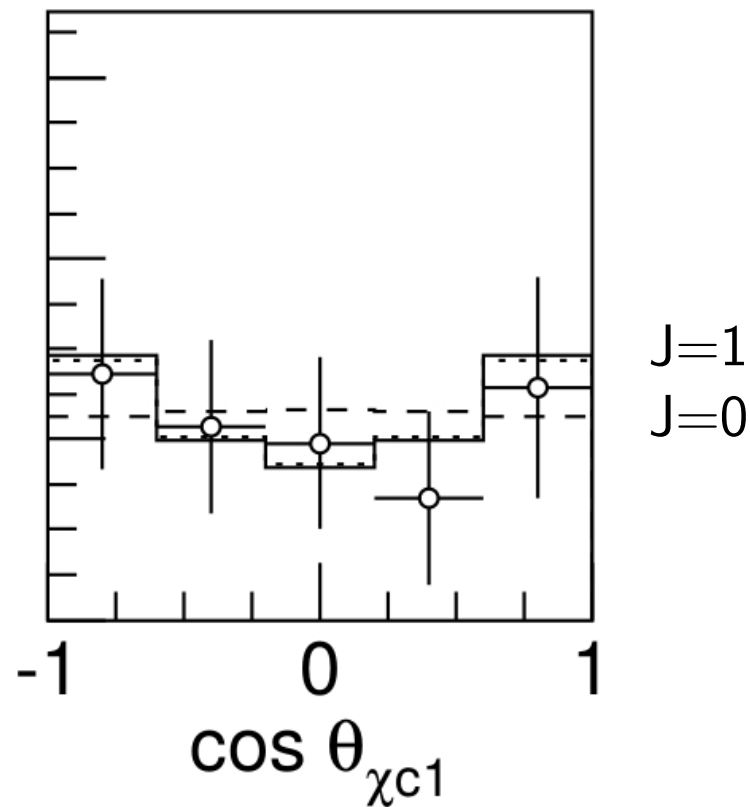




LHCb, Phys. Rev. D 92(2015)112009



Let's assume, we established $J=1$ for a charged Z state
by Legendre polynomials in the angular distribution
here: Belle, PRD 78, 072004 (2008)





How to determine, that the Z state has $J^P=1^+$?
(positive parity)

$B \rightarrow K Z(4430)$
 $0^- \rightarrow 0^- 1(+ \text{ or } -)$

is a weak decay.

Parity may be violated!

Solution:

$B \rightarrow K Z(4430)$ is a weak decay
but

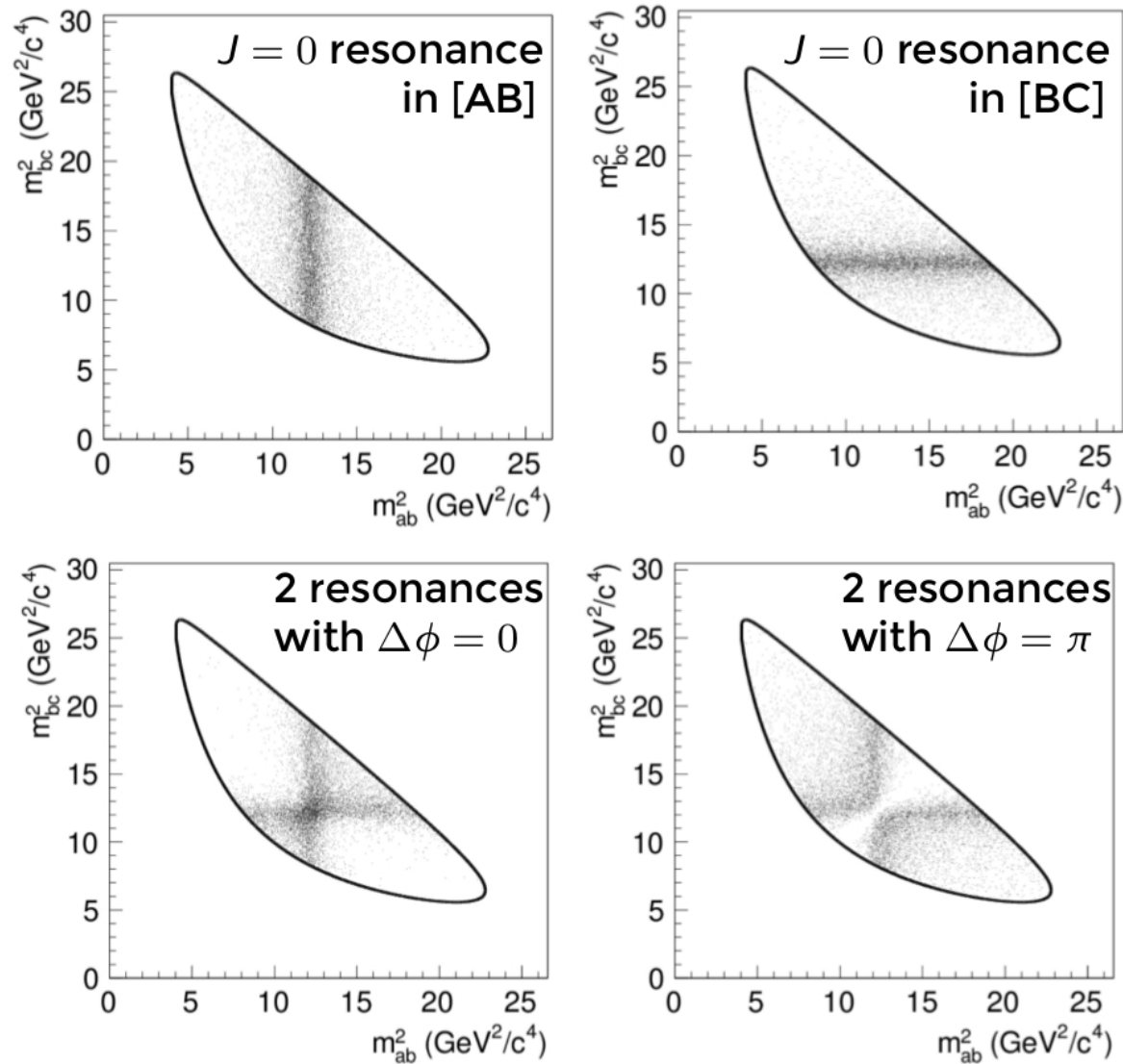
$Z(4430) \rightarrow \psi\pi$ is a strong decay
parity conserving !

need to check the angular distribution
of the ψ (or the π)
in the rest frame of the Z state

$1^- 0^-$ in S-wave $\rightarrow 1^+$

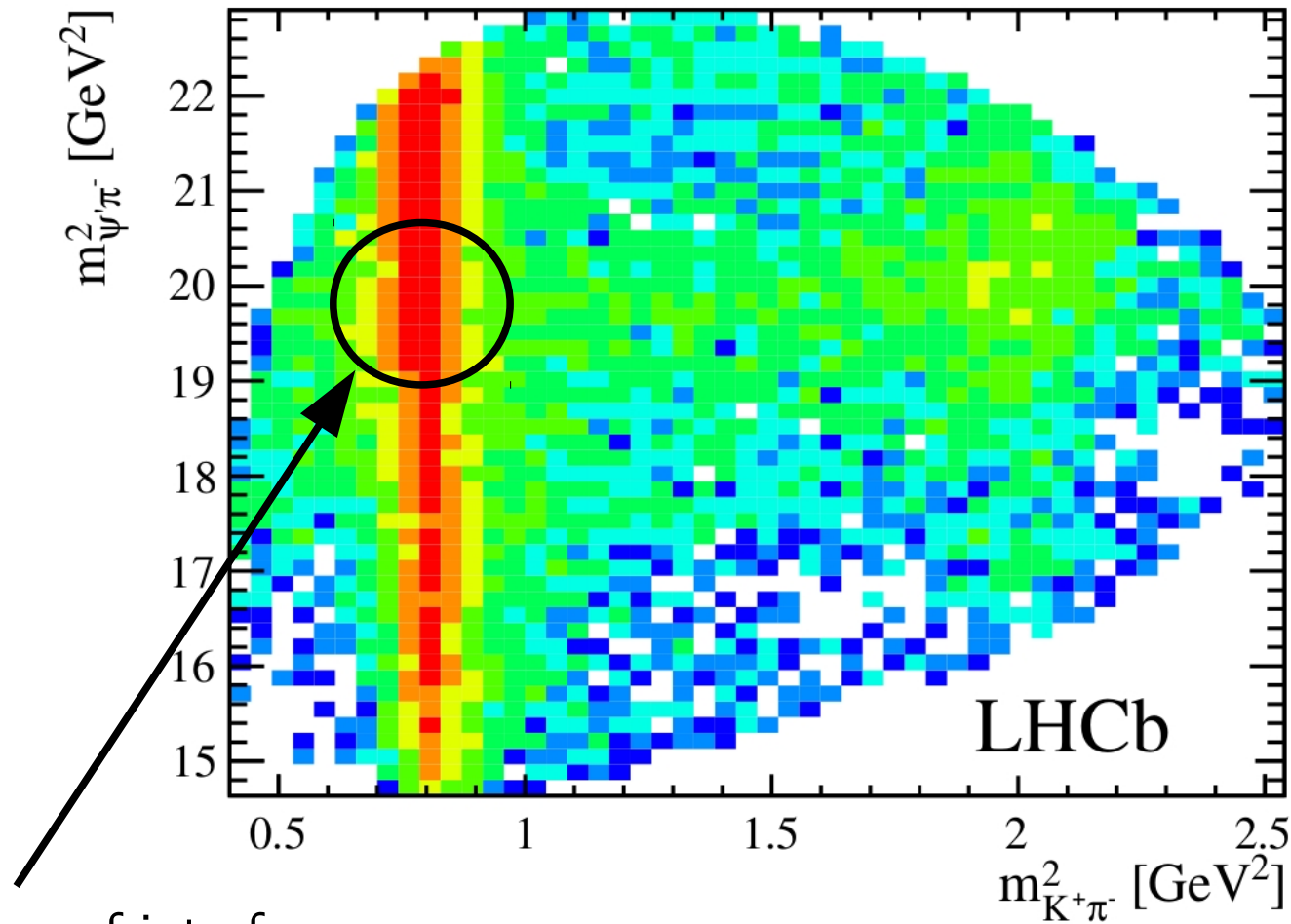
$1^- 0^-$ in P-wave $\rightarrow 1^-$ (or 0^- or 2^-)

Interlude: interference in a Dalitz plot



plots by
A. Palano,
S. Neubert
see also book
„Physics of the
B factories“

An easy way to see that the $Z(4430)$ is $1+$.

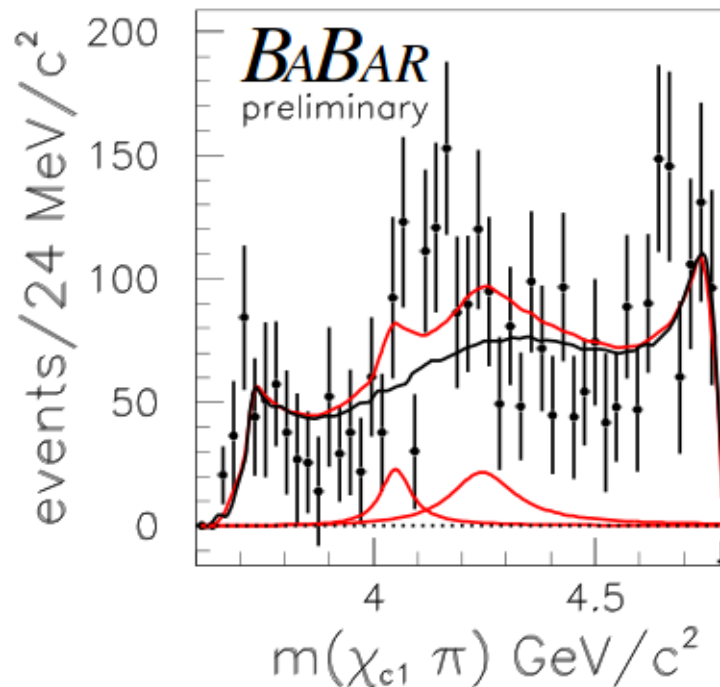
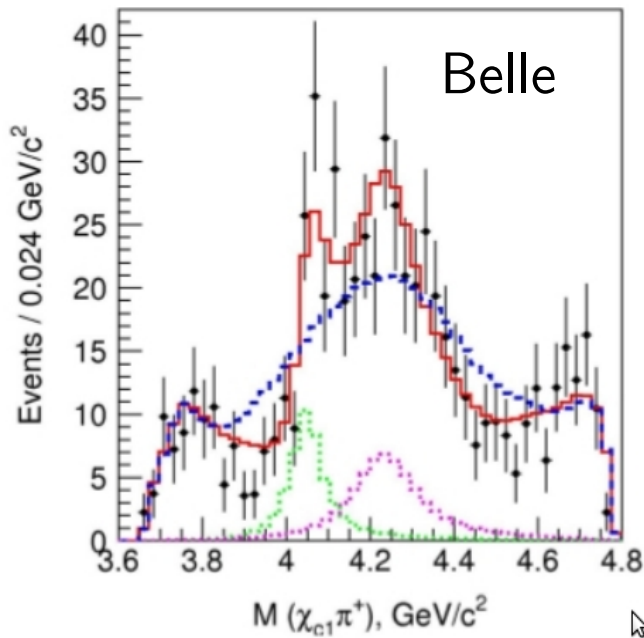


No sign of interference.

We know that the K^* is $1-$.

If the $Z(4430)$ is $J=1$ and there is no interference, then $1+$!

Interference plays an important role:
significance is higher, if **destructive interference**
is allowed in the fit



A final remark about Breit-Wigner

relativistic

$$A = \frac{m\Gamma}{s - m^2 + im\Gamma}$$

PDG convention

$$\sigma = A^2 = \frac{m^2\Gamma^2}{(s - m^2)^2 + m^2\Gamma^2}$$

non-relativistic

$$A = \frac{\Gamma/2}{\sqrt{s} - m + i\Gamma/2}$$

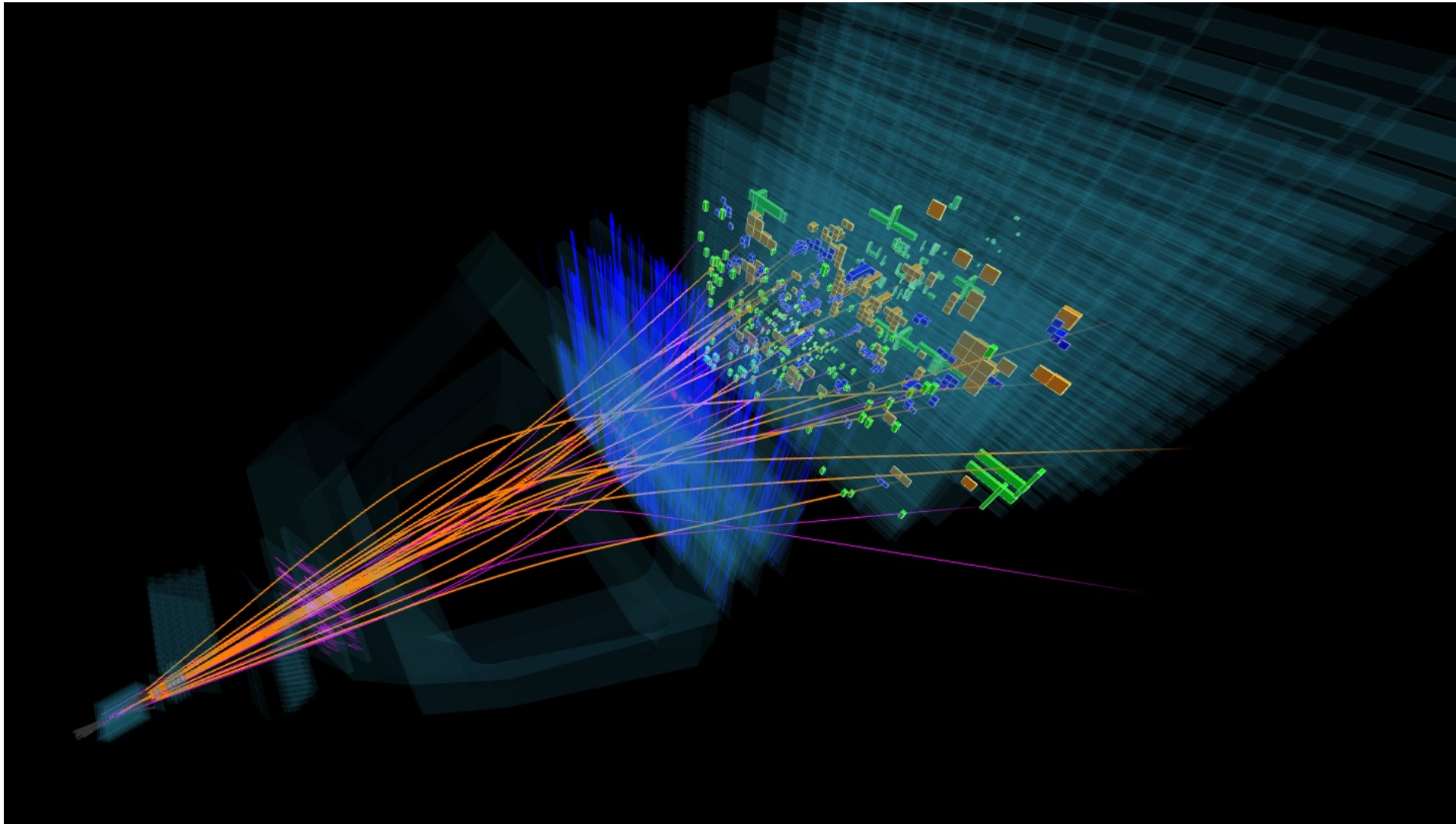
$$\sigma = \frac{\Gamma^2/4}{(\sqrt{s} - m)^2 + \Gamma^2/4}$$

not Lorentz invariant,
but sufficient in many cases

Almost all the observed, narrow Z states
are $J^P=1^+$

Why?

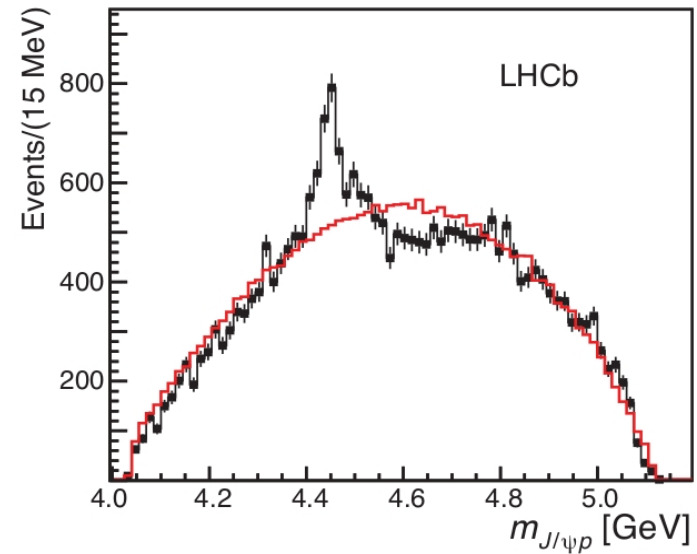
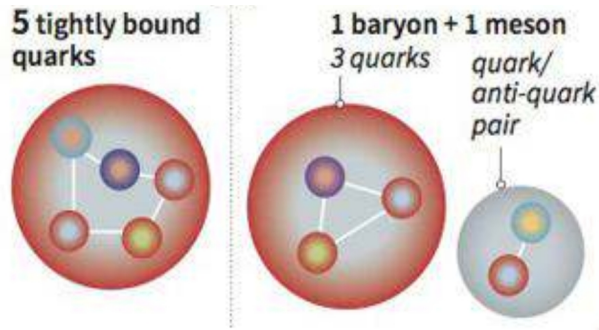
Pentaquark decay



The $P(4450)$ pentaquark

LHCb, arXiv:1507.03414

Phys. Rev. Lett. 115(2015)072001



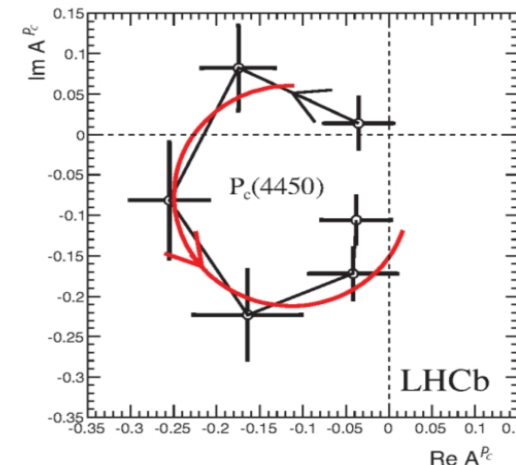
26007 ± 166 Λ_b candidates

$\Lambda_b \rightarrow K [J/\psi p]$

[MeV]	$P_c(4450)^+$
Mass	$4449.8 \pm 1.7 \pm 2.5$
$\chi_{c1}(1P)p$	4448.93 ± 0.07
$\Lambda_c^{+*} \bar{D}^0$	4457.09 ± 0.35
$\Sigma_c \bar{D}^{0*}$	4459.9 ± 0.5
$\Sigma_c \bar{D}^0 \pi^0$	4452.7 ± 0.5

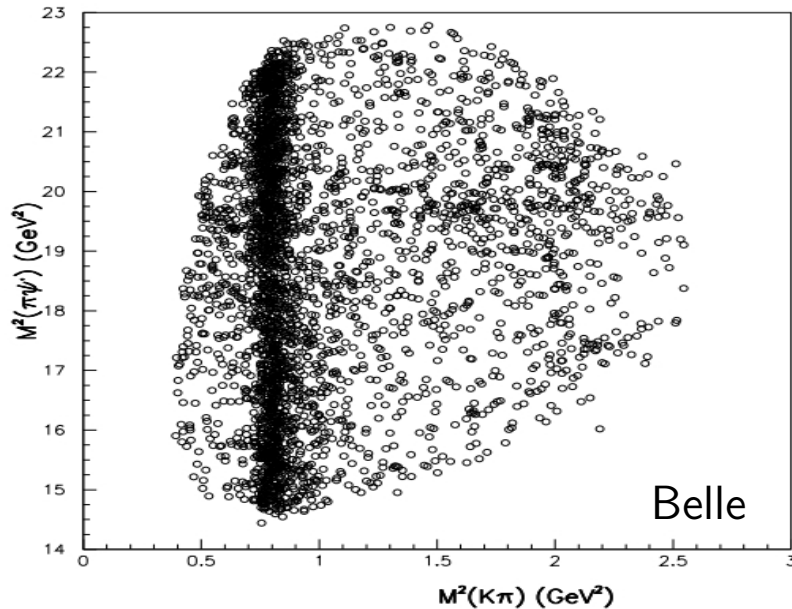
several thresholds
in the vicinity

resonant
character

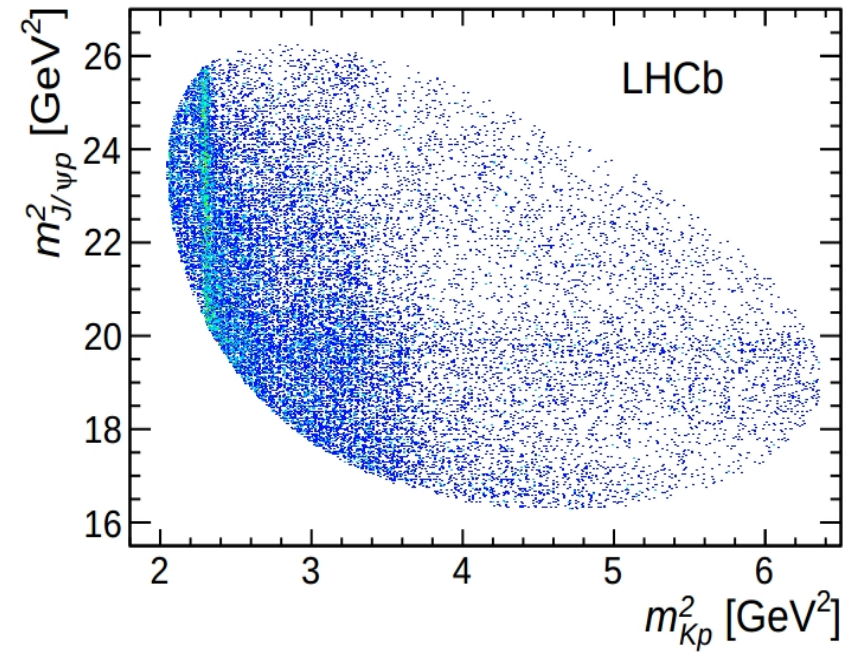


Similarities of „tetraquark“ and „pentaquark“

$B^0 \rightarrow K^- \psi' \pi^+$
Phys. Rev D80(2009)031104



$\Lambda_b^0 \rightarrow K^- J/\psi p$
Phys. Rev. Lett. 115(2015)072001



$c \bar{c} u \bar{d}$ (minimal content) $\rightarrow Z(4430)^+$
 $c \bar{c} u u \bar{d}$ (minimal content) $\rightarrow P(4450)^+$
 similar mass (?)

Why is LHCb better
for the pentaquark
than Belle II?

Reminder: decay to J/ψ p.

Belle II



Bundesministerium
für Bildung
und Forschung



Mt. Tsukuba

SuperKEKB asymmetric B meson factory, $e^+ e^- \rightarrow B \bar{B}$

adjusted to $\Upsilon(4S)$ resonance, $\sqrt{s}=10.6$ GeV

different beam energies

8 GeV $\rightarrow$ 7 GeV (lower emittance)

3.5 GeV $\rightarrow$ 4 GeV (Touschek lifetime)

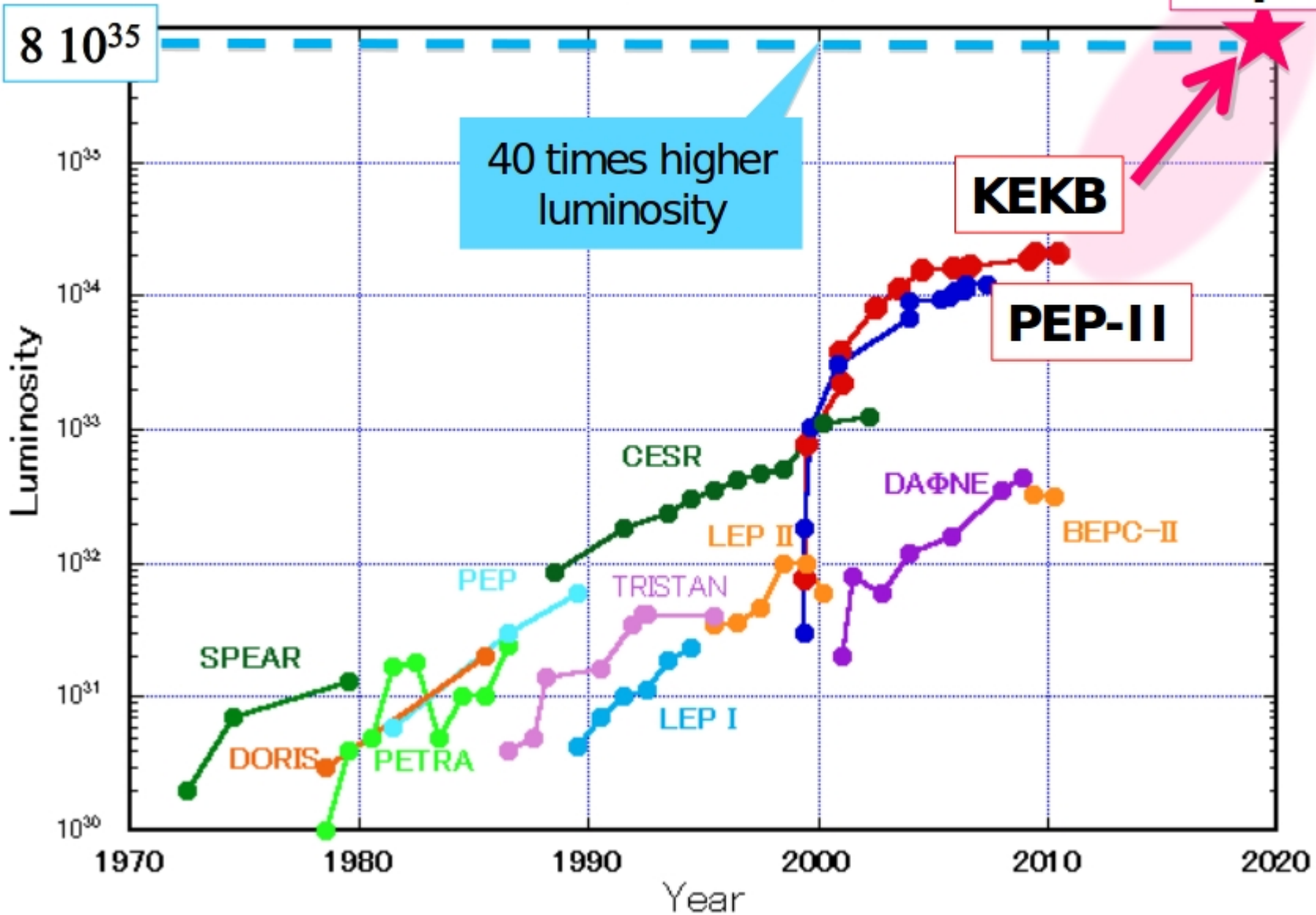
Upgrade: luminosity peak $\times 40$, integrated $\times 50$

Belle II Detector

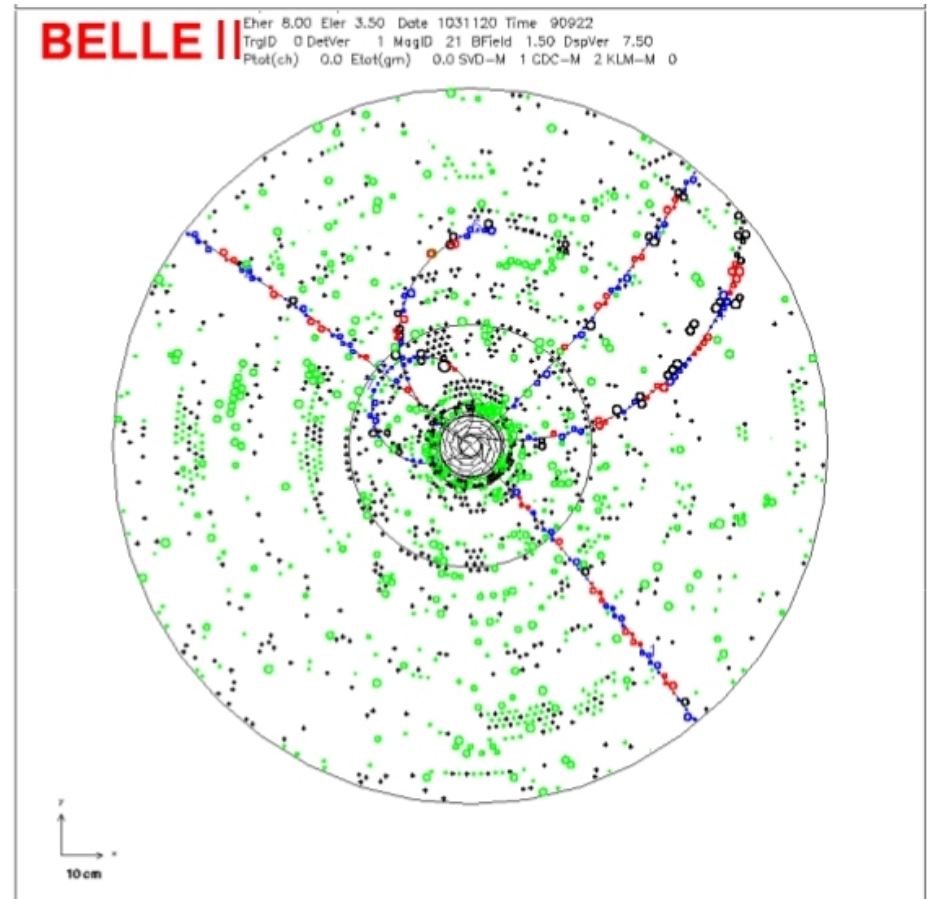
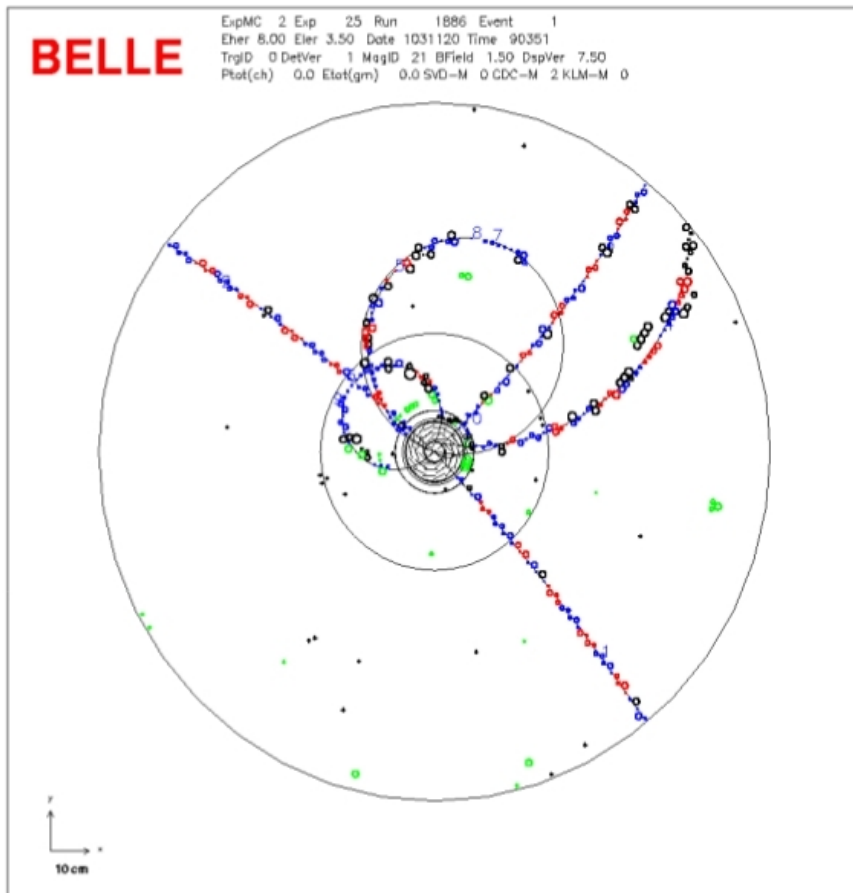
Linac

Peak Luminosity Trends (e^+e^- collider)

SuperKEKB



Background increase x factor 10–20

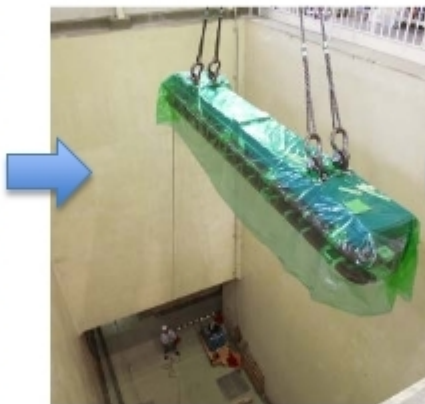


Trigger rate ~ 400 Hz (Belle) $\rightarrow 30.000$ Hz (Belle II)

Installation of 100 new LER Dipole Magnets



field measurement



move into tunnel



carry on an air-pallet

Installation of 100 new LER
bending magnets done



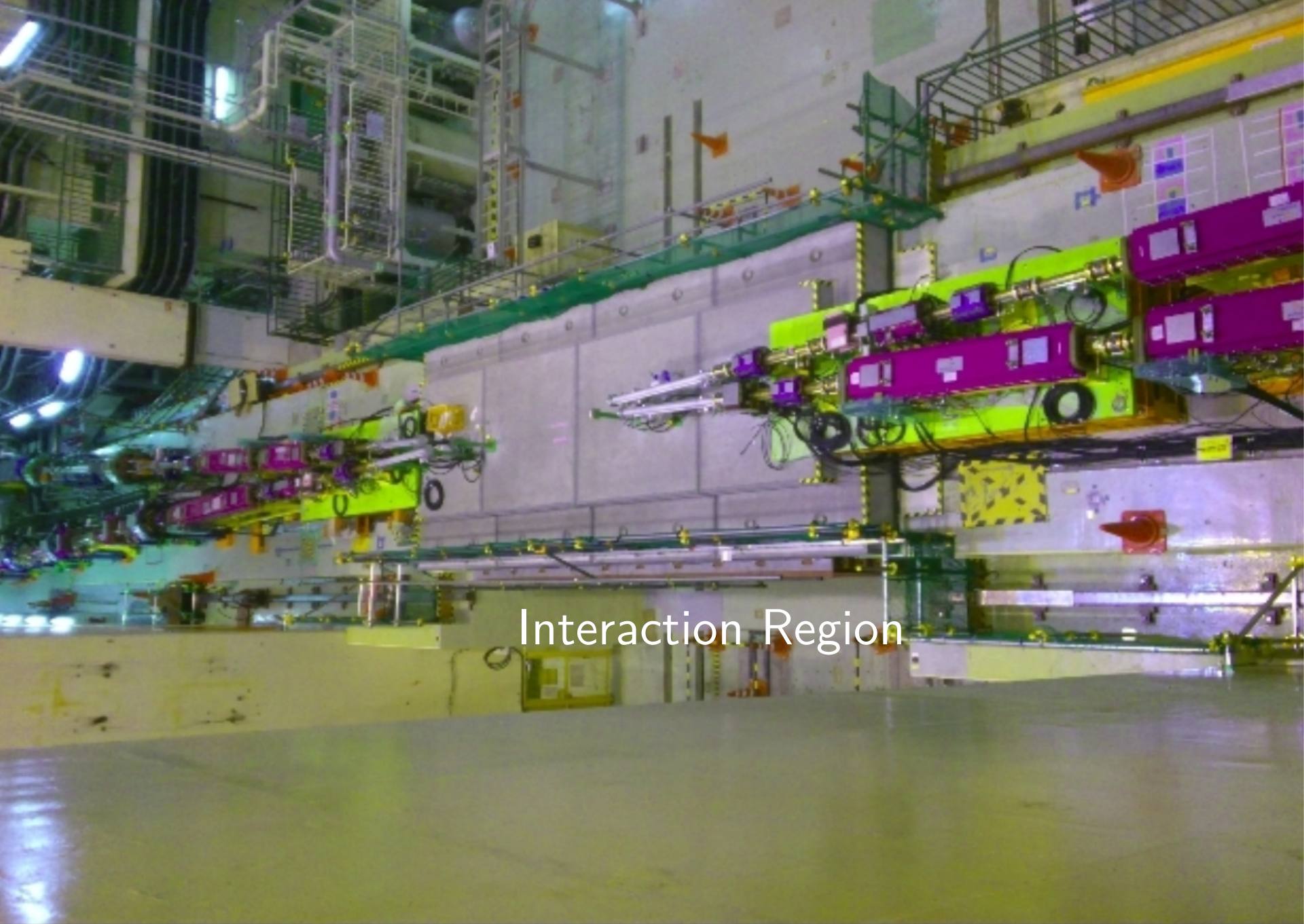
Install over
HER magnets

install done

~3 magnets per day



SuperKEKB Status, 7th BPAC, Mar. 11, 2013, K. Akai



Interaction Region

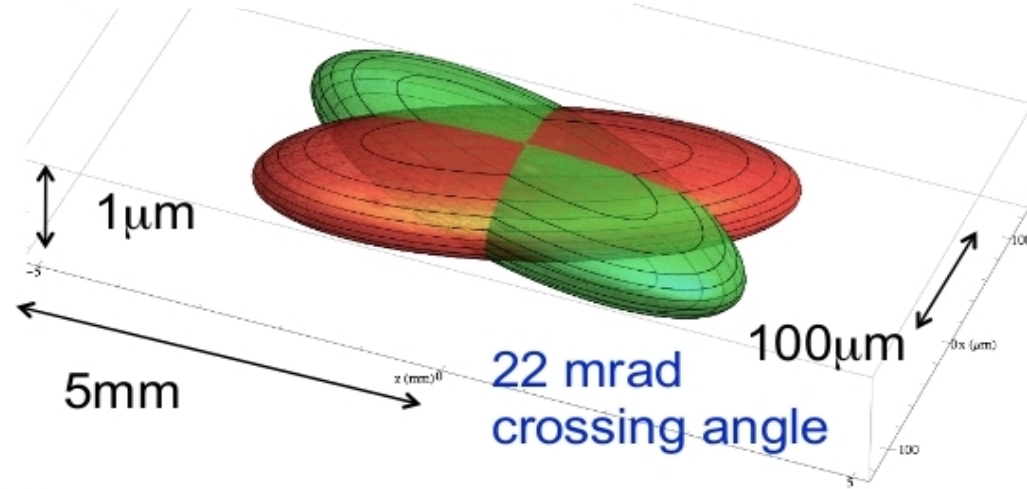
Nano-Beam Scheme

Belle $\rightarrow$ Belle II

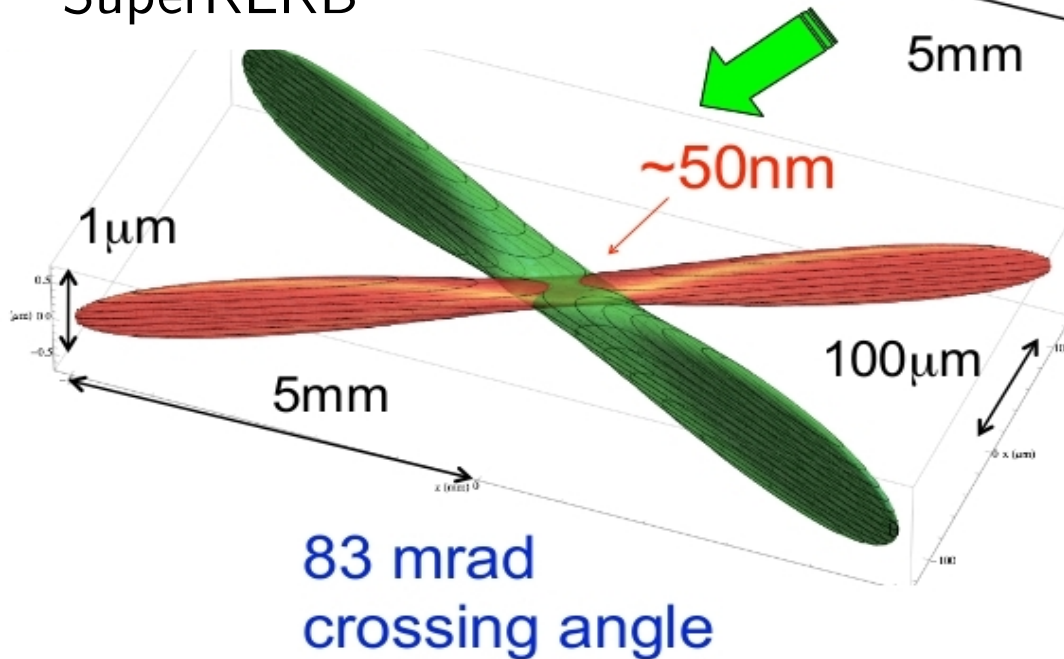
Luminosity $\times 40$

$$L \leq 0.8 \times 10^{36} \text{ cm}^{-2} \text{ s}^{-1}$$

KEKB (*without crab*)



SuperKEKB

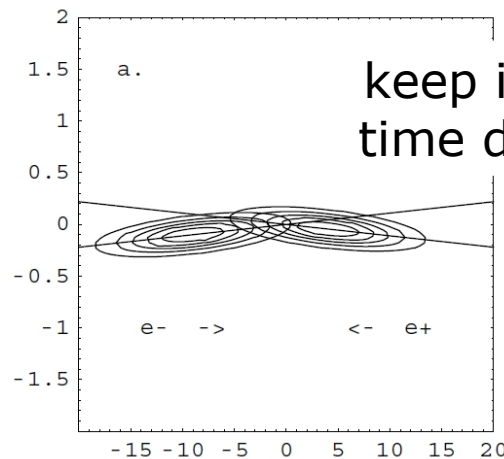
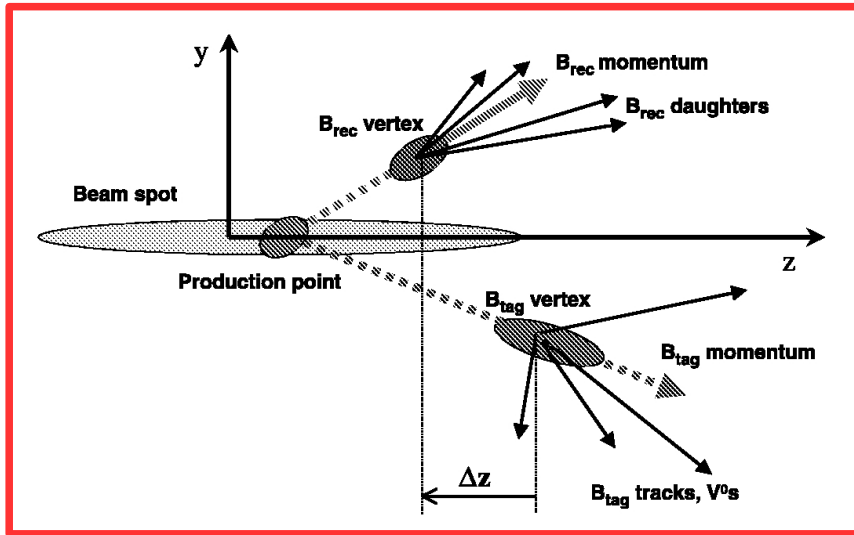


originally proposed for SuperB
by P. Raimondi (INFN)

graphics E. Paoloni (Pisa)

IP Profile for Belle and Belle II („nanobeam“)

$$100\mu\text{m}(H) \times 2\mu\text{m}(V) \rightarrow 10\mu\text{m}(H) \times 59\text{nm}(V)$$



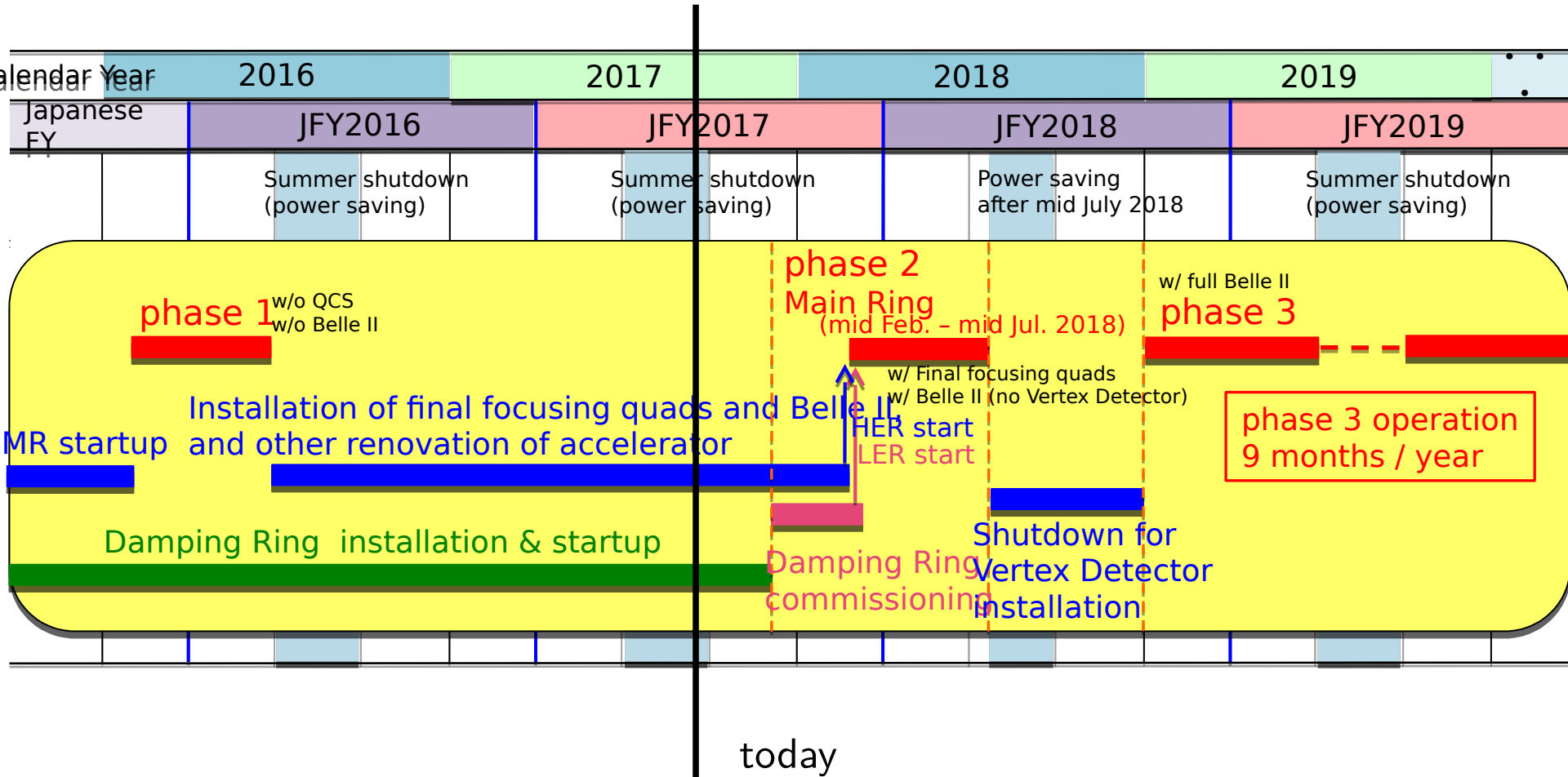
Belle Rotation 03/2013

for larger crossing angle $22 \text{ mrad} \rightarrow 83 \text{ mrad}$ (nanobeam)



18.6 cm @ end of platform (accuracy 0.5 mm)

SuperKEKB/Belle II schedule





Inter-University Research Institute Corporation
High Energy Accelerator Research Organization

Press Release



First turns and successful storage of beams in the SuperKEKB electron and positron rings

March 2nd, 2016

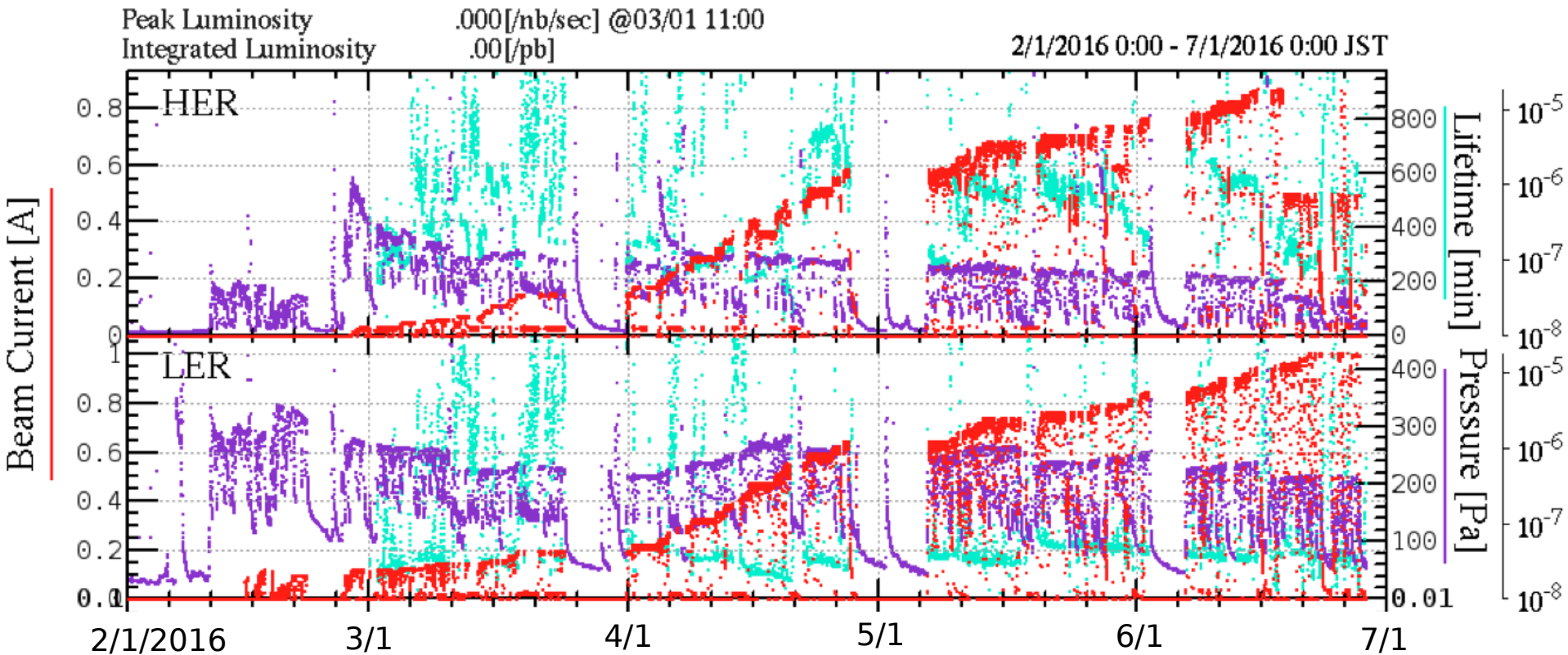
High Energy Accelerator Research Organization (KEK)

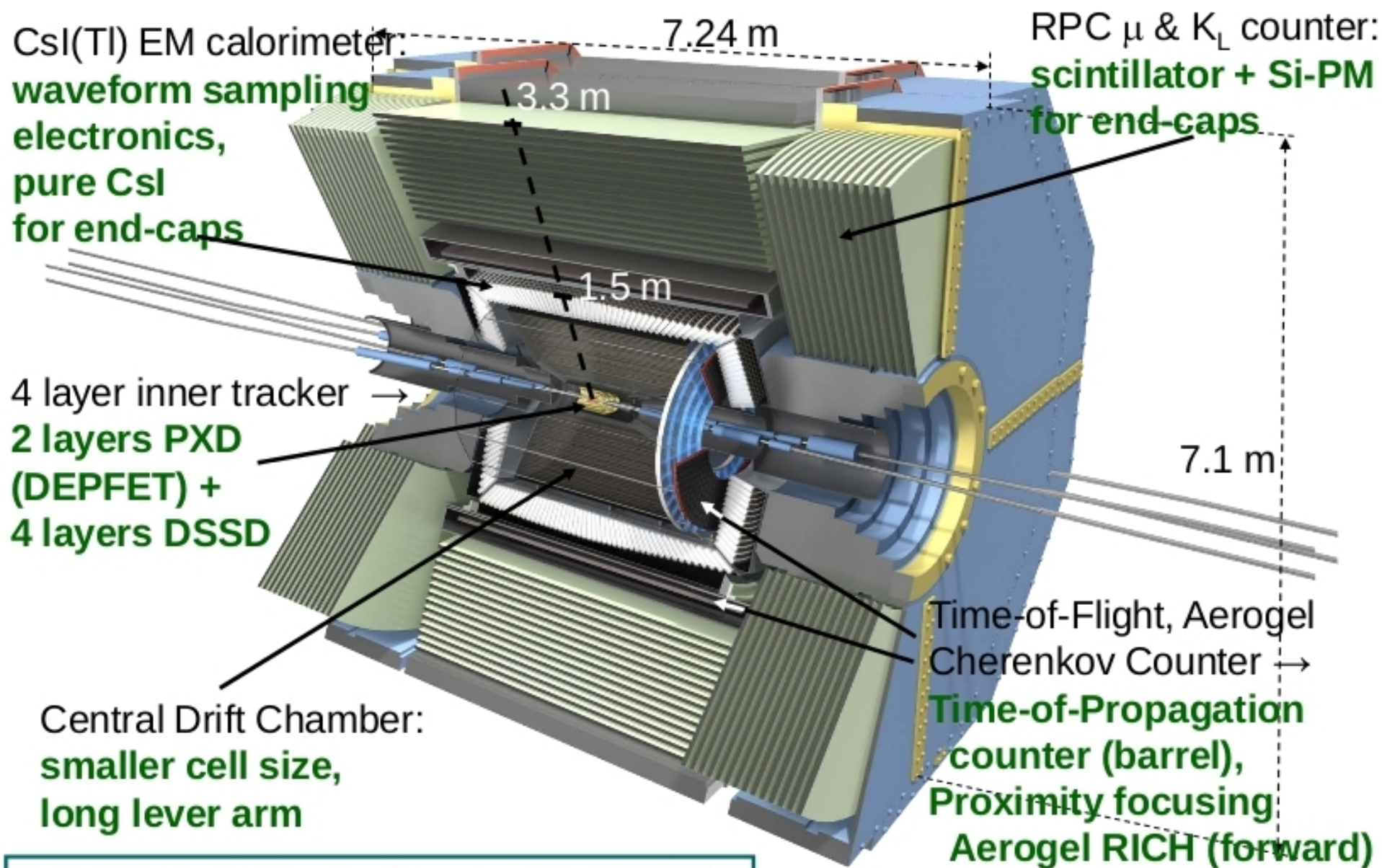
Phase I operation history

max. stored beam current 870 mA (HER), 1010 mA (LER)

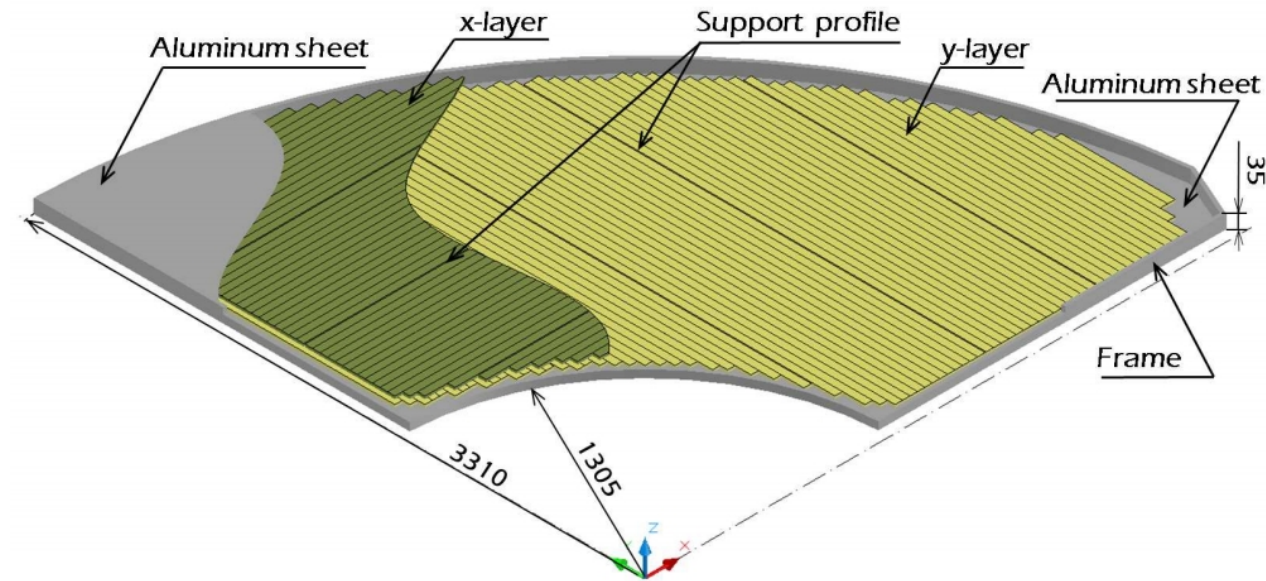
red: beam current

purple: vacuum pressure



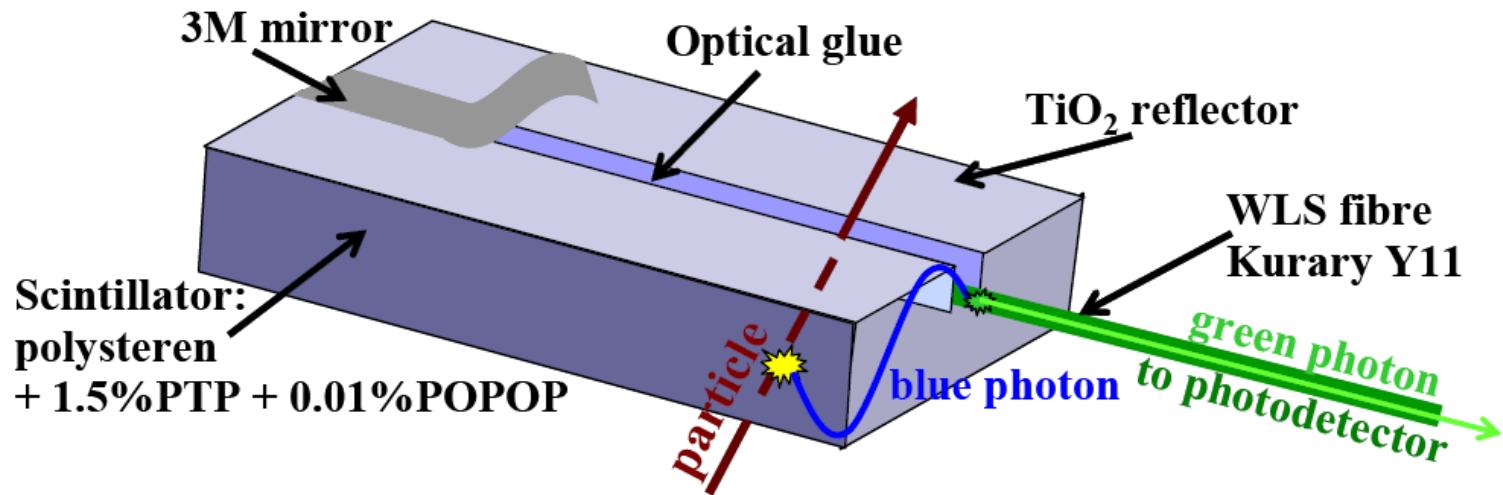






KLM

replace RPCs
by scintillators
total area $\sim 1400 \text{ m}^2$
16.800 readout fibres



B-KLM Installation



completed 11/2013
RPCs exchanged
by scintillator
in endcap and
2 inner layers in barrel

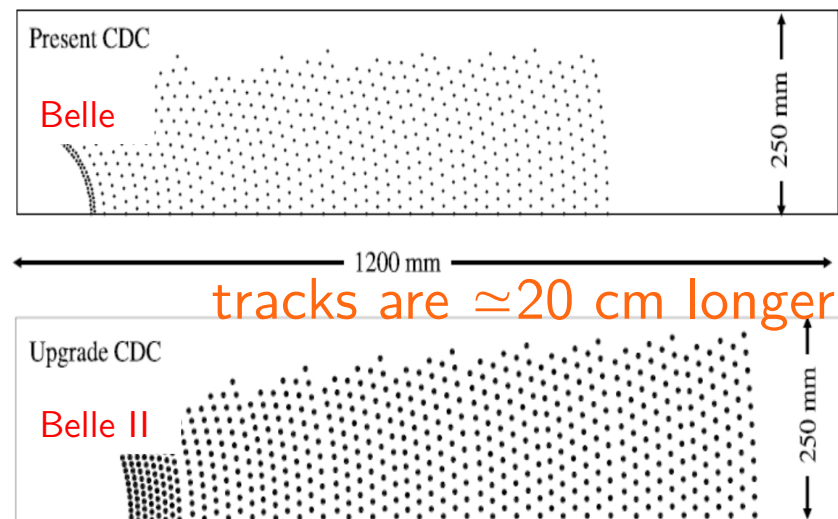
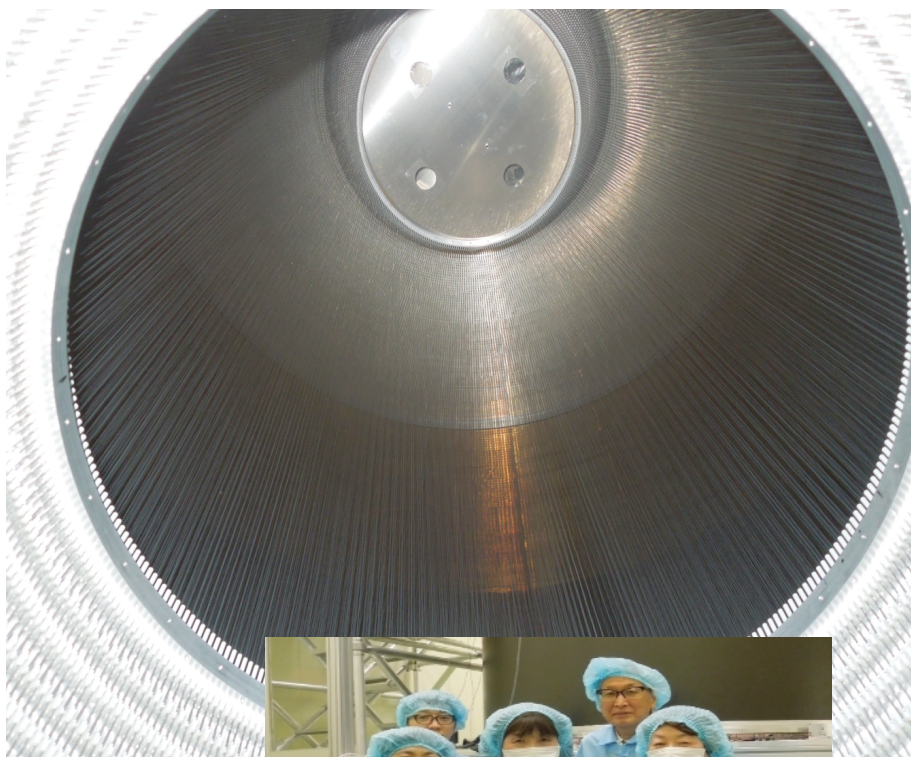


During installation, modules
have been checked, found to
be healthy.

The 1st New Detector Installed !!

CDC (Charged Drift Chamber)

wire stringing finished (01/2014), 51456 wires



Improved resolution:

$$\sigma(p_T)/p_T =$$

$$0.19 \, p_T \oplus 0.30/\beta \text{ (Belle)}$$

$$0.11 \, p_T \oplus 0.30/\beta \text{ (Belle II)}$$

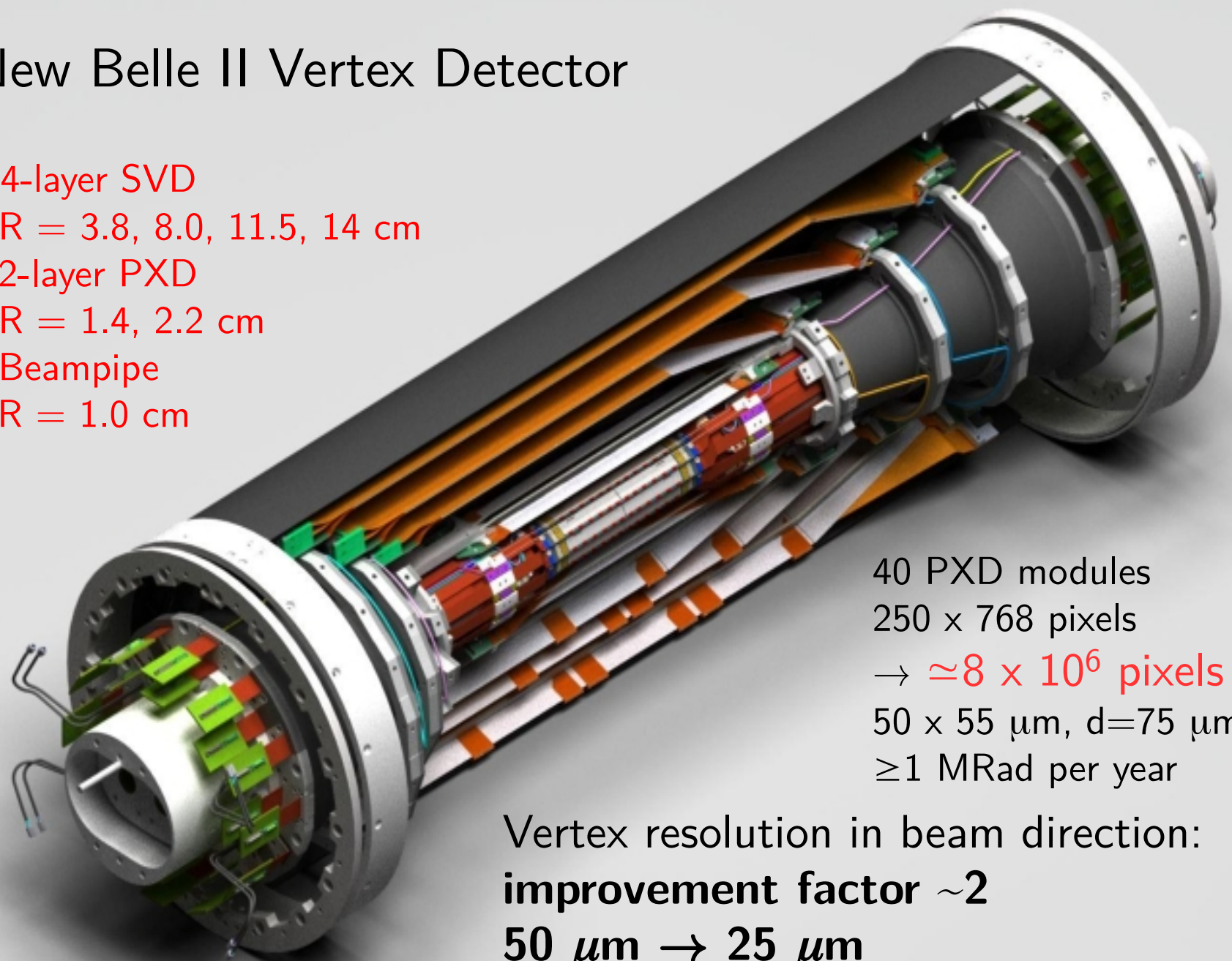
$$dE/dx \, 6.8\% \rightarrow 4.8\%$$

CDC transport from Fuji Hall to Tsukuba Hall, 21.01.2015



New Belle II Vertex Detector

- 4-layer SVD
 $R = 3.8, 8.0, 11.5, 14 \text{ cm}$
- 2-layer PXD
 $R = 1.4, 2.2 \text{ cm}$
- Beampipe
 $R = 1.0 \text{ cm}$

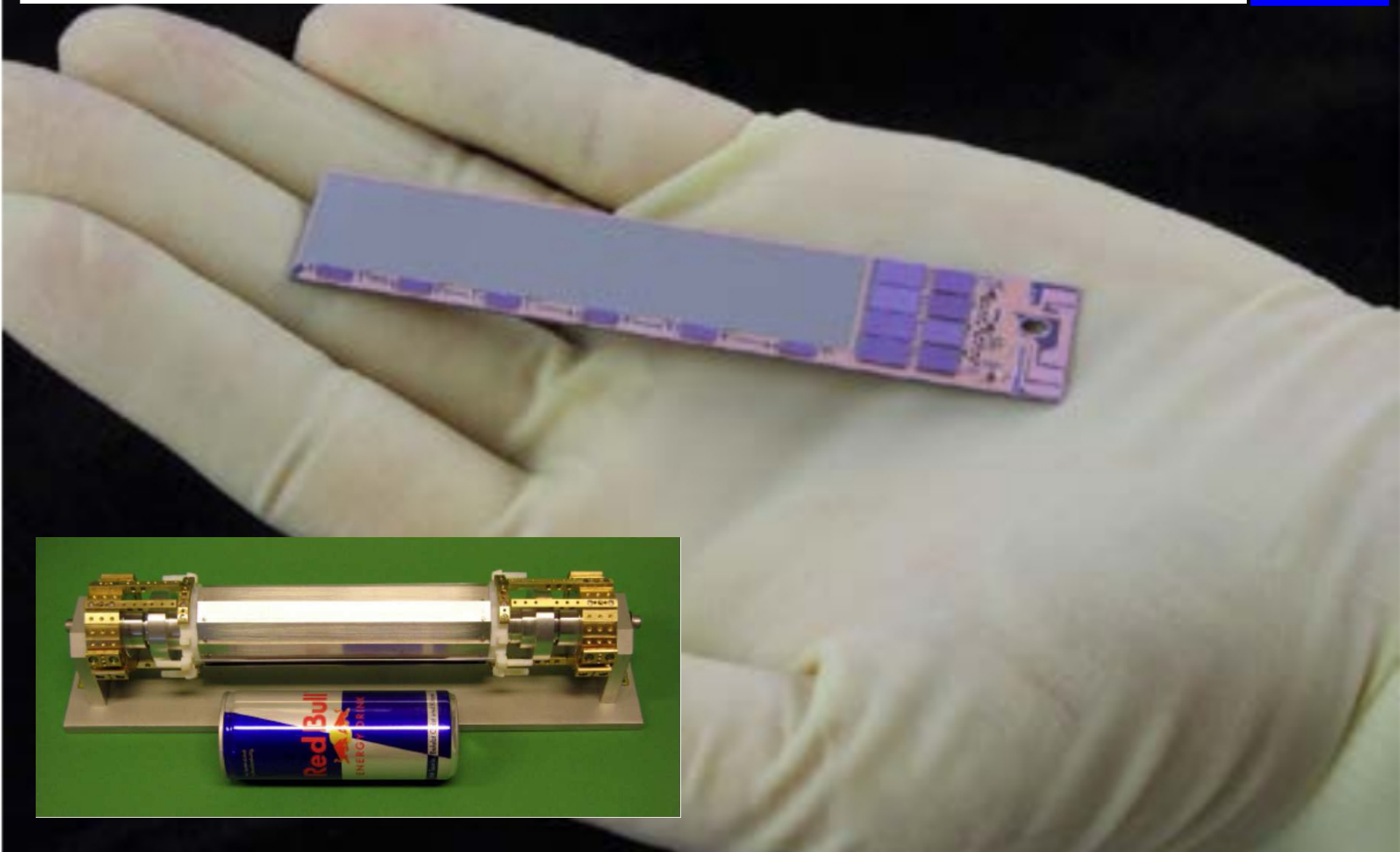


40 PXD modules
 $250 \times 768 \text{ pixels}$
 $\rightarrow \simeq 8 \times 10^6 \text{ pixels}$
 $50 \times 55 \mu\text{m}, d=75 \mu\text{m}$
 $\geq 1 \text{ MRad per year}$

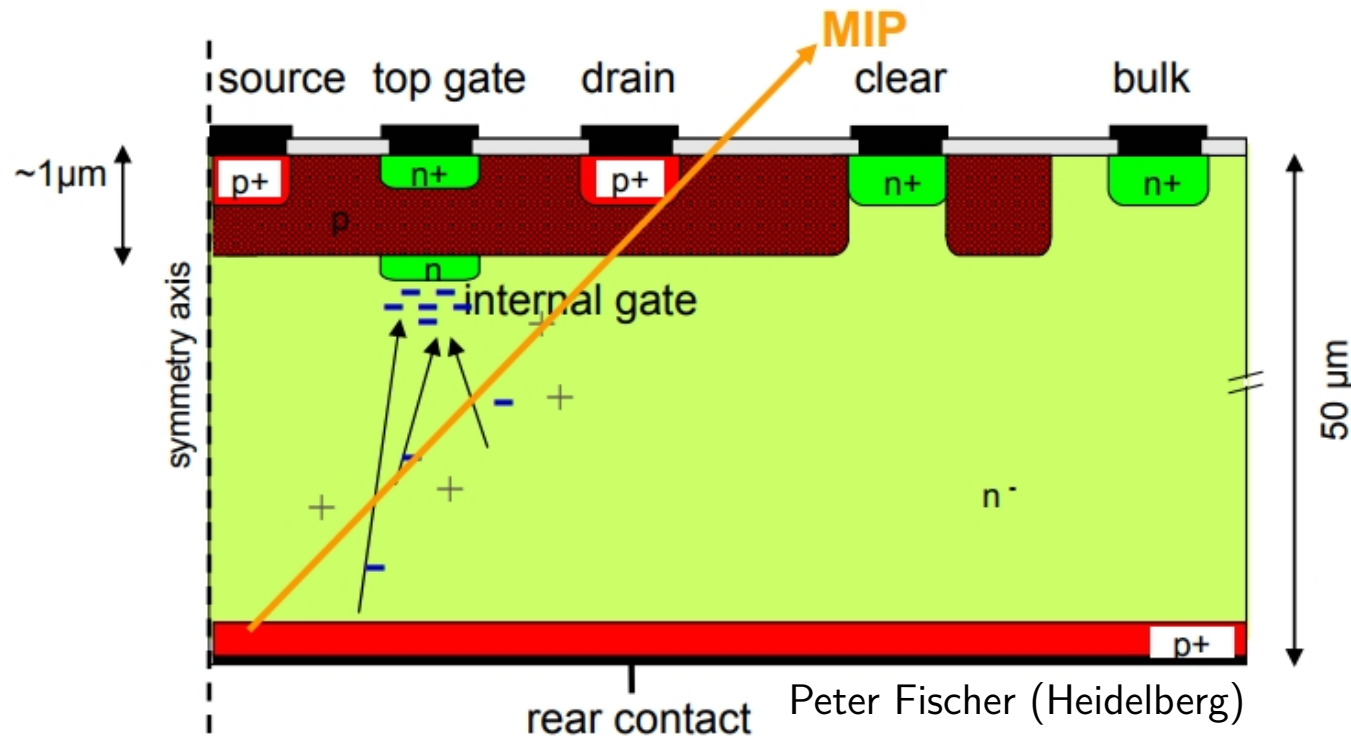
Vertex resolution in beam direction:
improvement factor ~ 2
 $50 \mu\text{m} \rightarrow 25 \mu\text{m}$

Belle II DEPFET Pixel Detector

Univ. Bonn, DESY, Univ. Giessen, Univ. Göttingen, Univ. Hamburg, Univ. Heidelberg, KIT Karlsruhe, Univ. Mainz, HLL München, MPI München, LMU München, TU München



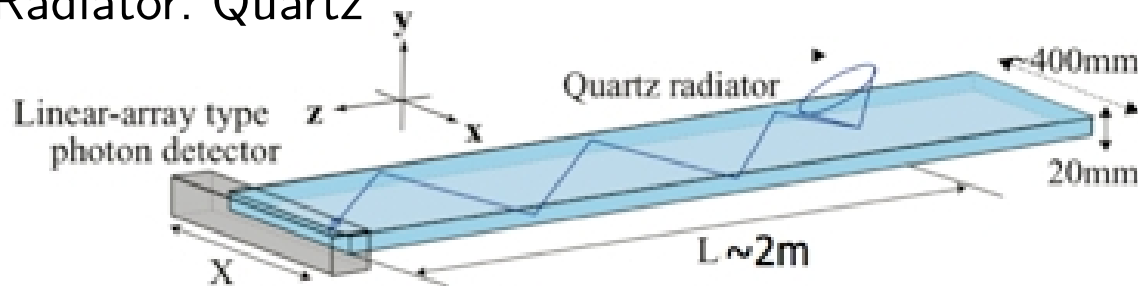
DEPFET Principle



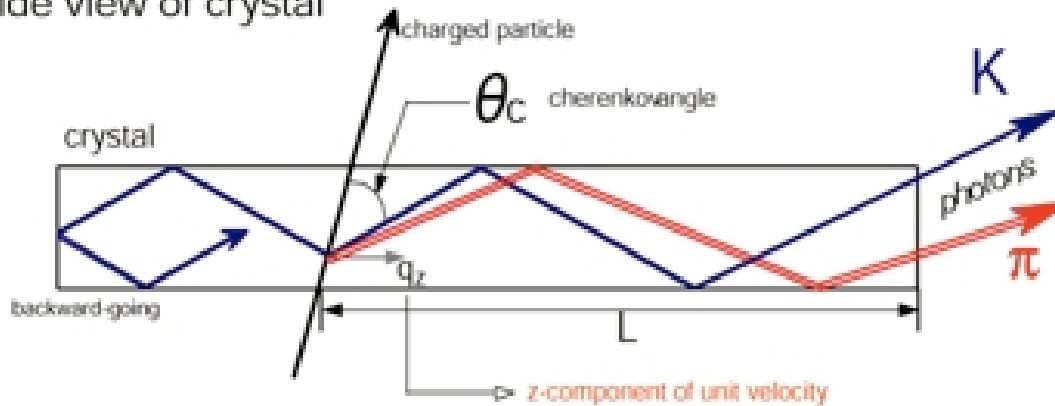
every pixel contains a p-FET (on n-substrate)
clear can be operated at high rates (30 kHz at Belle II)
then current flows to drain and is measured by an ADC (ASIC)
Belle II PXD has $\sim 8 \times 10^6$ pixels

TOP (Time-of-Propagation Counter)

Radiator: Quartz

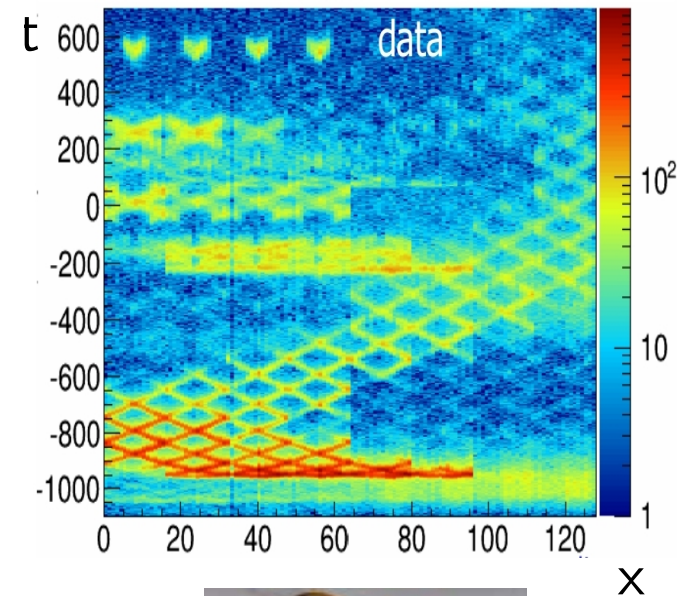


Side view of crystal



reconstruct Cherenkov angle from

- (X,Y)
- time of propagation



- Photon detector: Hamamatsu SL10 MCP-PMT
 - $\Delta t \leq 50 \text{ ps}$
 - single photon sensitivity
 - operated in $B=1.5 \text{ T}$ field
- Estimated kaon fake rate factor 2-5 smaller than Belle (@ 95% kaon efficiency)



Mirror

TOP Assembly of 1st Module

Lifting jig
with
vacuum
chucks

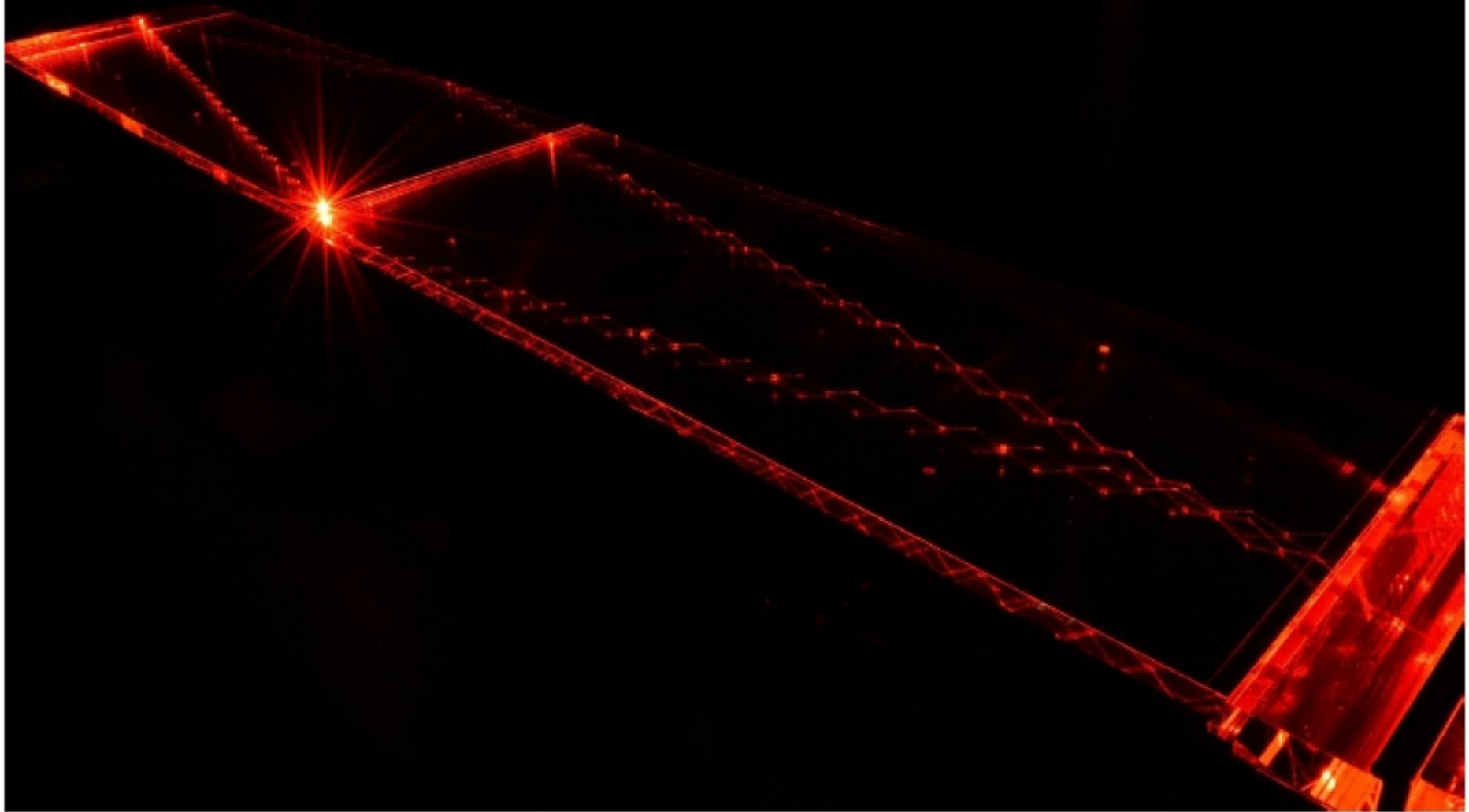
Glue joint
between two
bars

2014/10/29 16:32

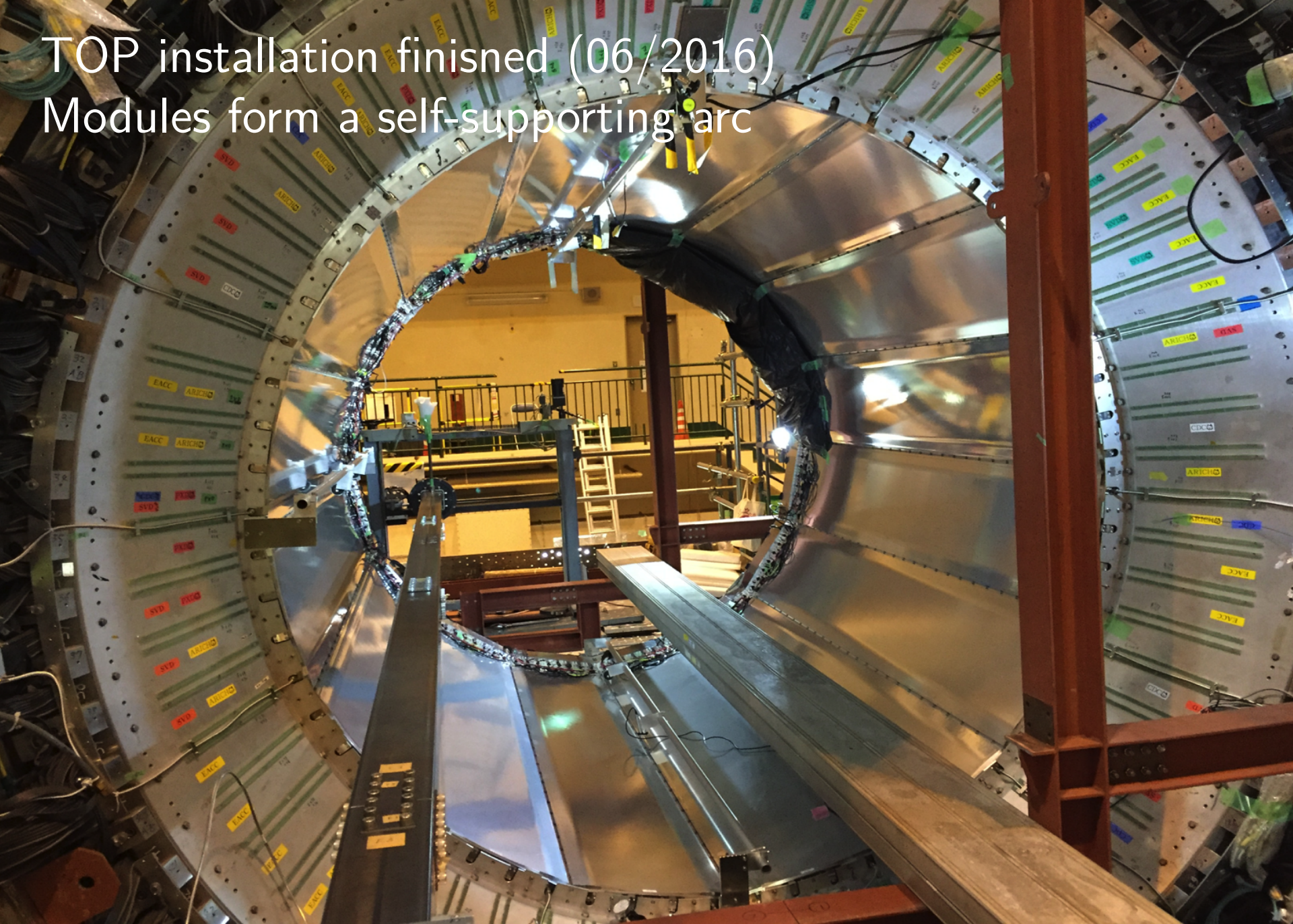
Clean Room @ KEK, Fuji Hall

Prism

Laser in TOP module
Photo: K. Inami (Nagoya)



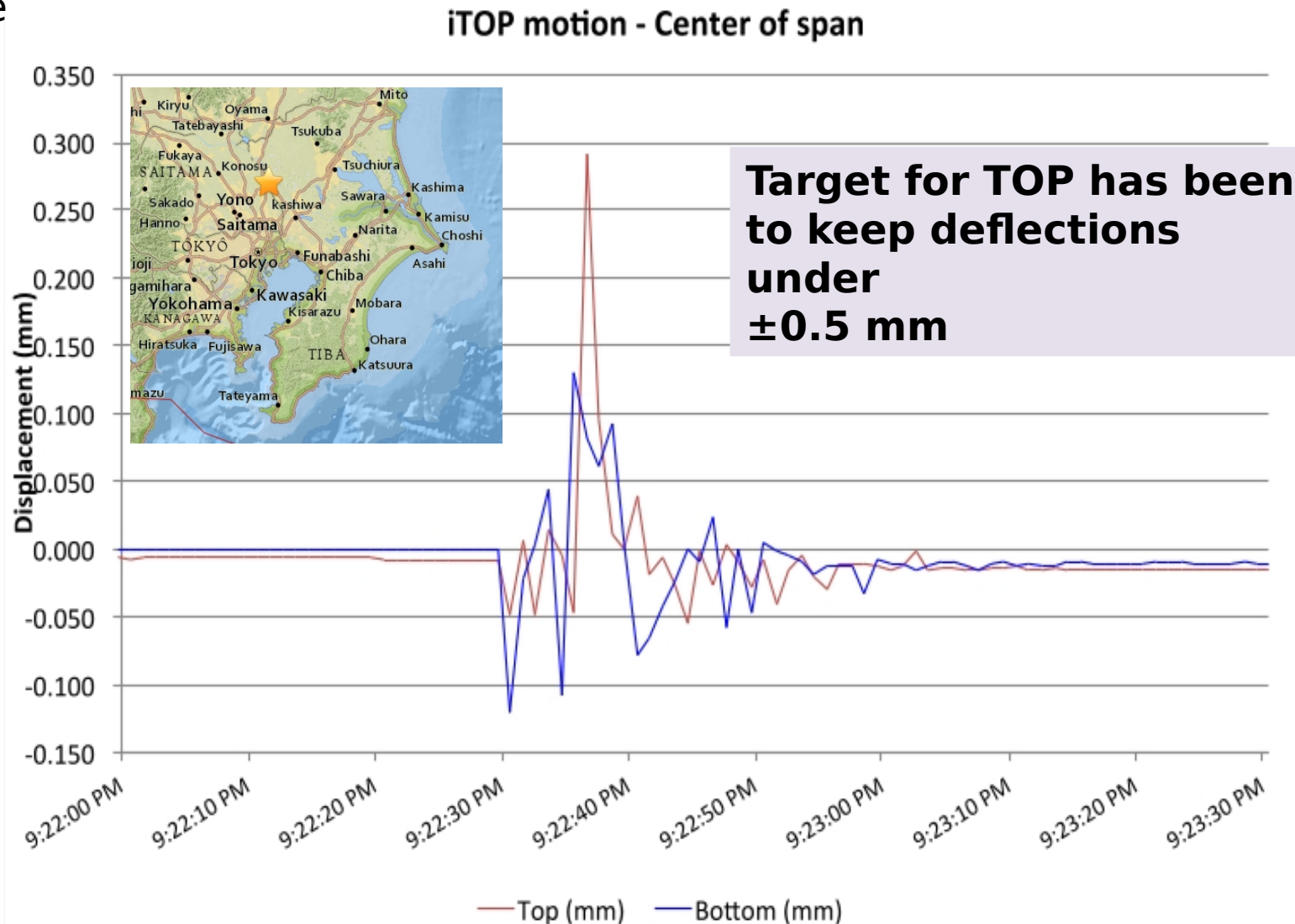
TOP installation finished (06/2016)
Modules form a self-supporting arc



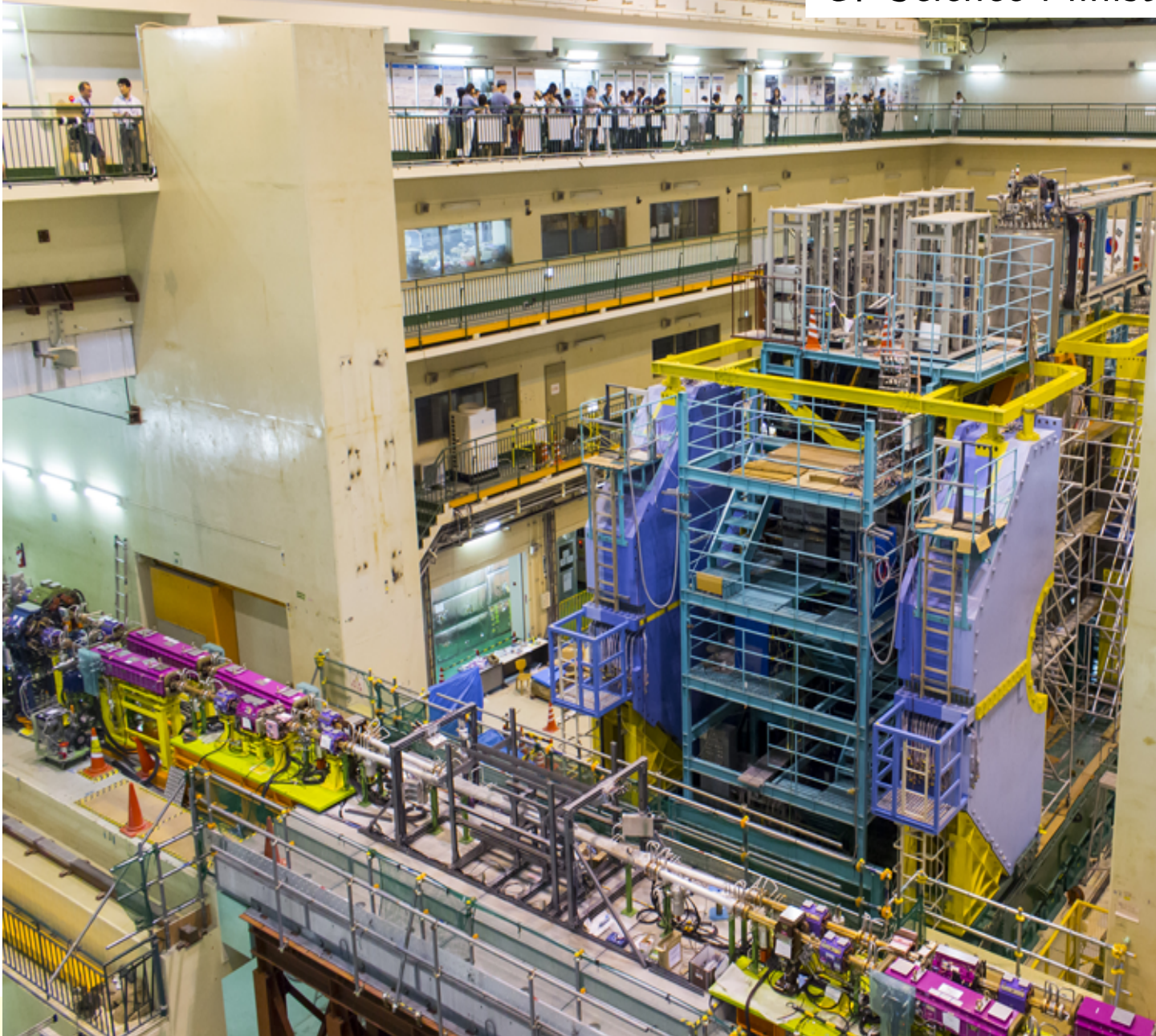
16.05.2016 First night after „strongback“ support were removed

→ a M5.4 earthquake with epicenter in Ibaraki prefecture !

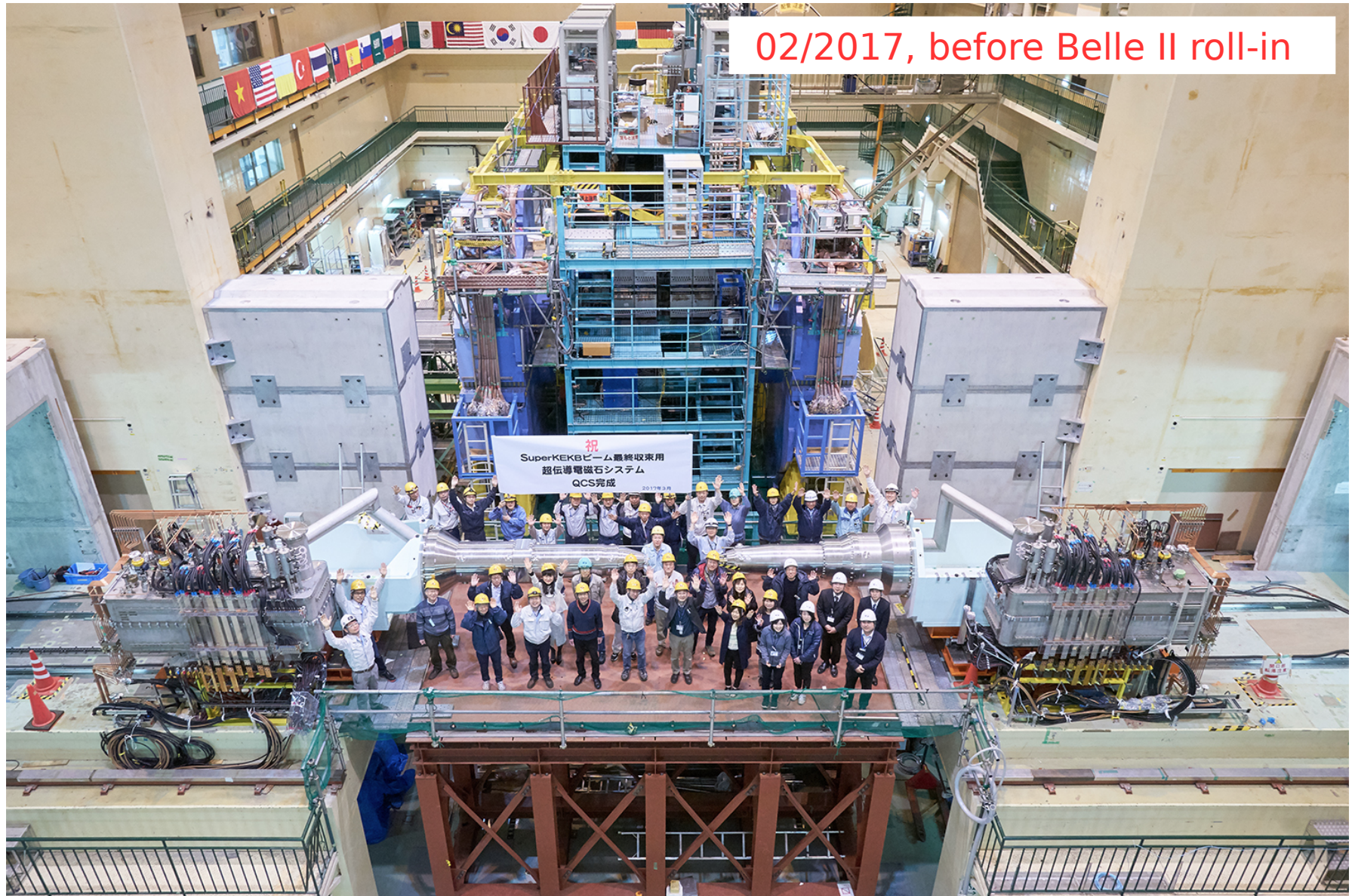
<http://earthquake.usgs.gov/earthquakes/eventpage/us10005hgy#executive>



17.05.2016 One day after earthquake
G7 Science Ministers visit Belle II

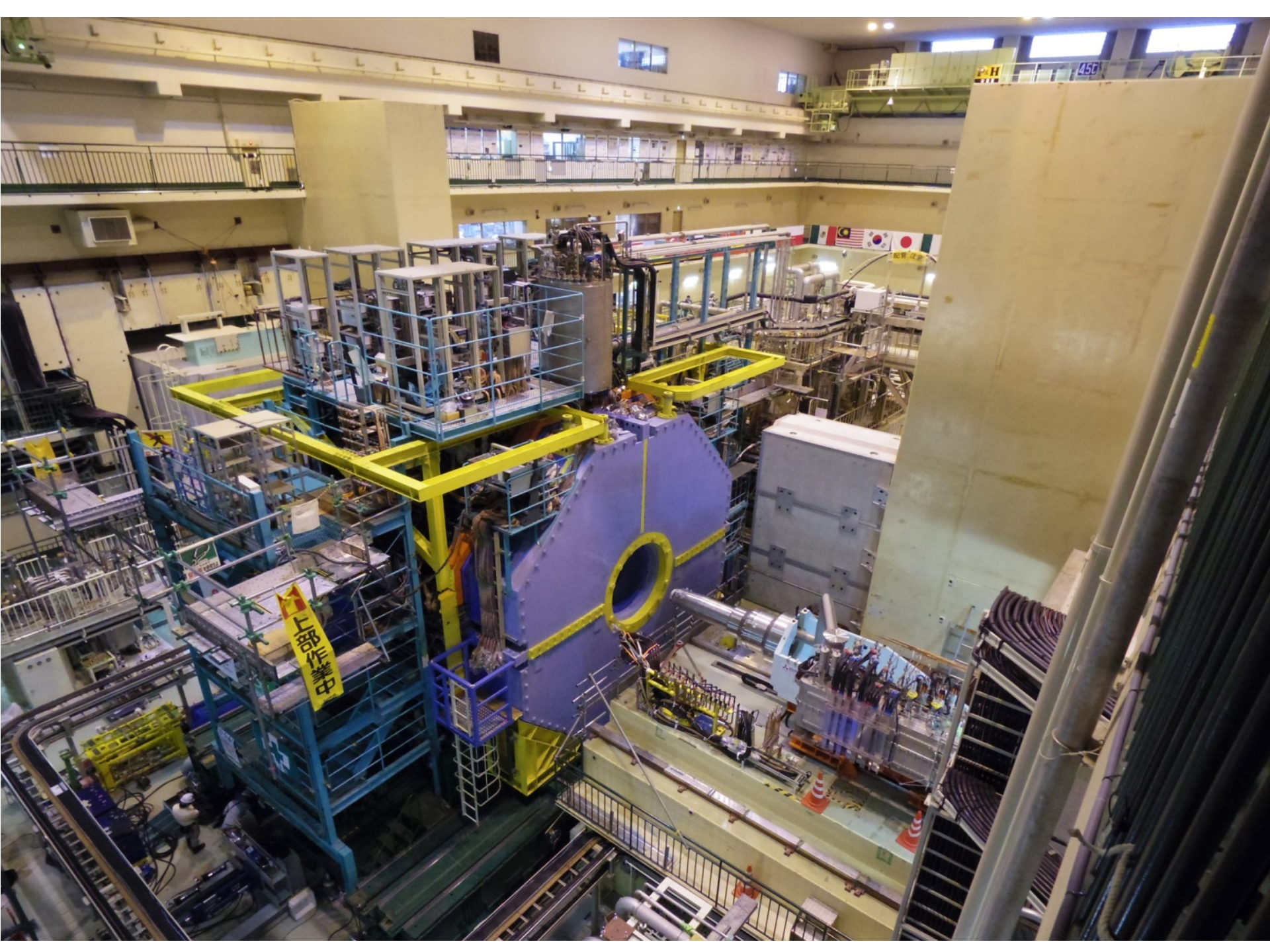


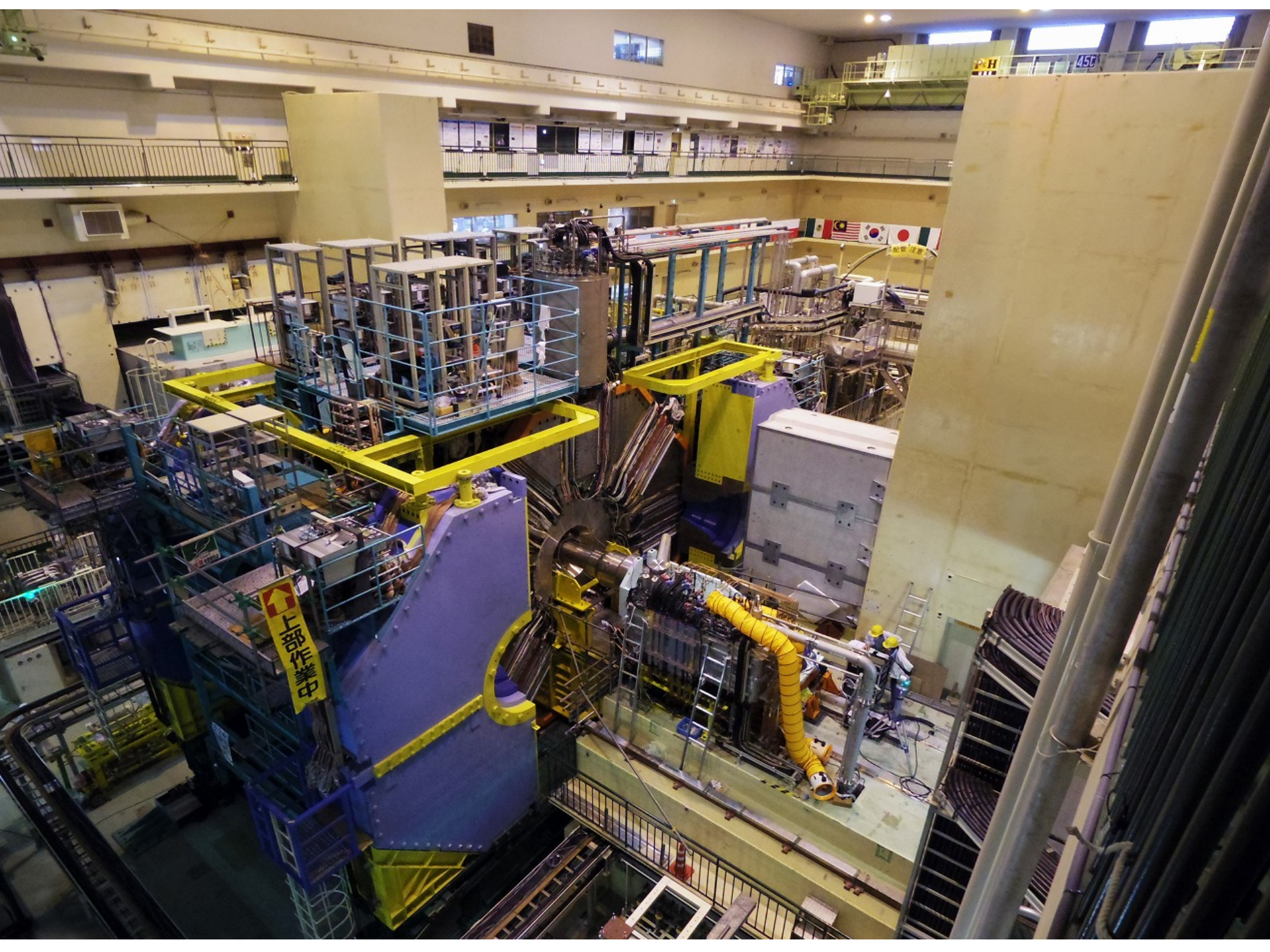
Final focusing quadrupoles (QCS) installed at IR, 55 superconducting coils, 2 cryostats



ROLL-IN, 11.04.2017





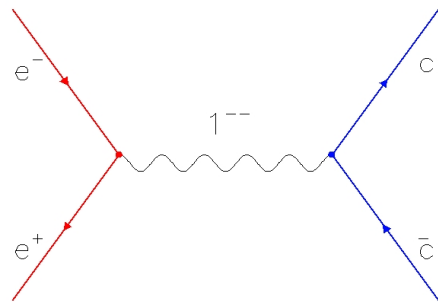


$\bar{P}$ ANDA

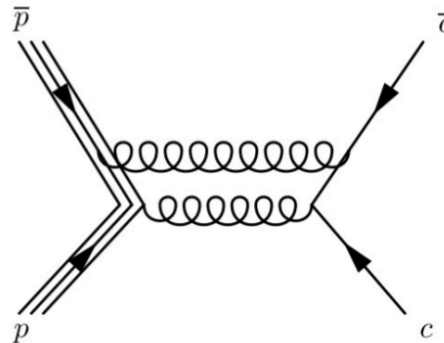
X(3872) factory

Charmonium(-like) Production in $\bar{p}p$ collisions

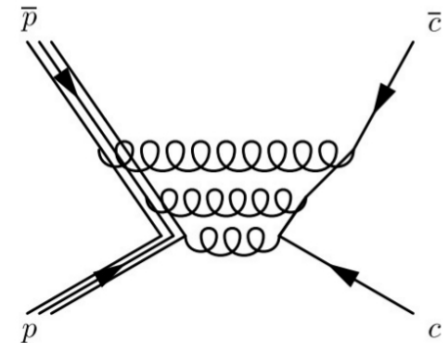
- X(3872) has 1^{++} ($C=+$)
- In e^+e^- collisions only $J^{PC}=1^{--}$ can be produced directly
in $\bar{p}p$ collisions any quantum number



2 gluons: $0^{-+}, 0^{++}, 2^{++}$



3 gluons: $1^{--}, 1^{+-}$



- 2 mechanisms:

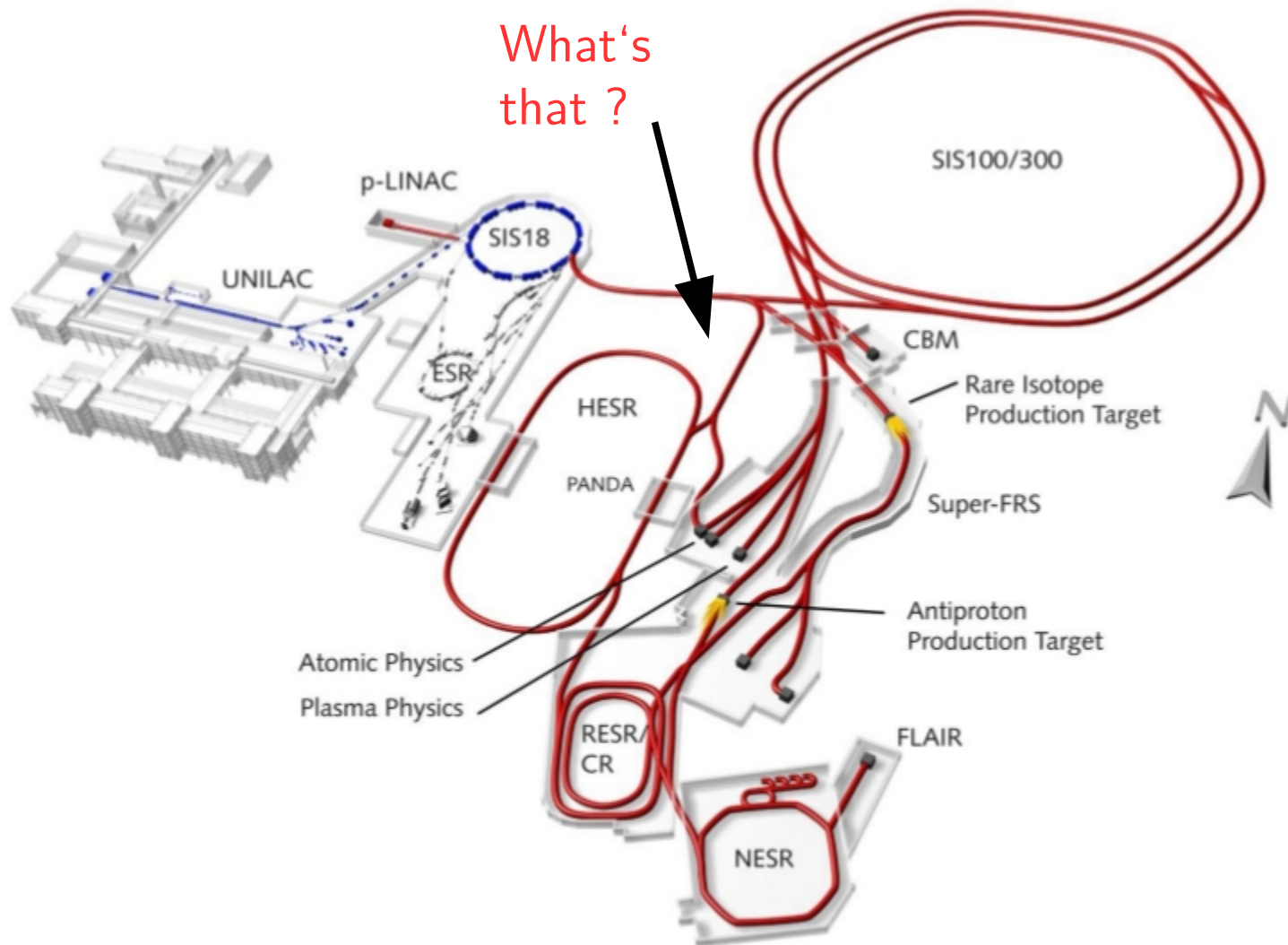
Formation $\bar{p}p \rightarrow X(3872)$

Production $\bar{p}p \rightarrow X(3872) + \text{meson(s)} @ \text{ higher energy}$



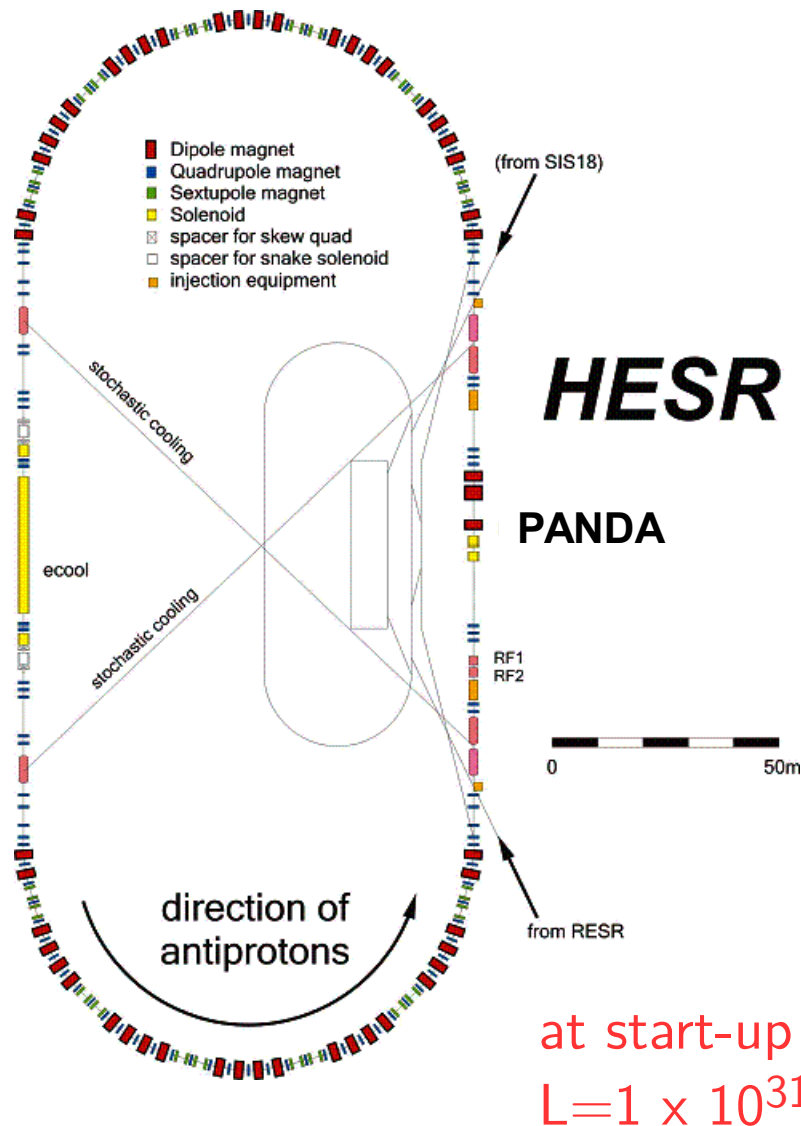
(no parking lot)

FAIR (Facility for Anti-Proton and Ion Research) Helmholtz Center GSI Darmstadt (Germany)



HESR (High Energy Storage Ring)

For Anti-Protons



High intensity mode

- $10^{11} \bar{p}$
- $\delta p/p \approx 10^{-4}$ (stochastic cooling)

High resolution mode

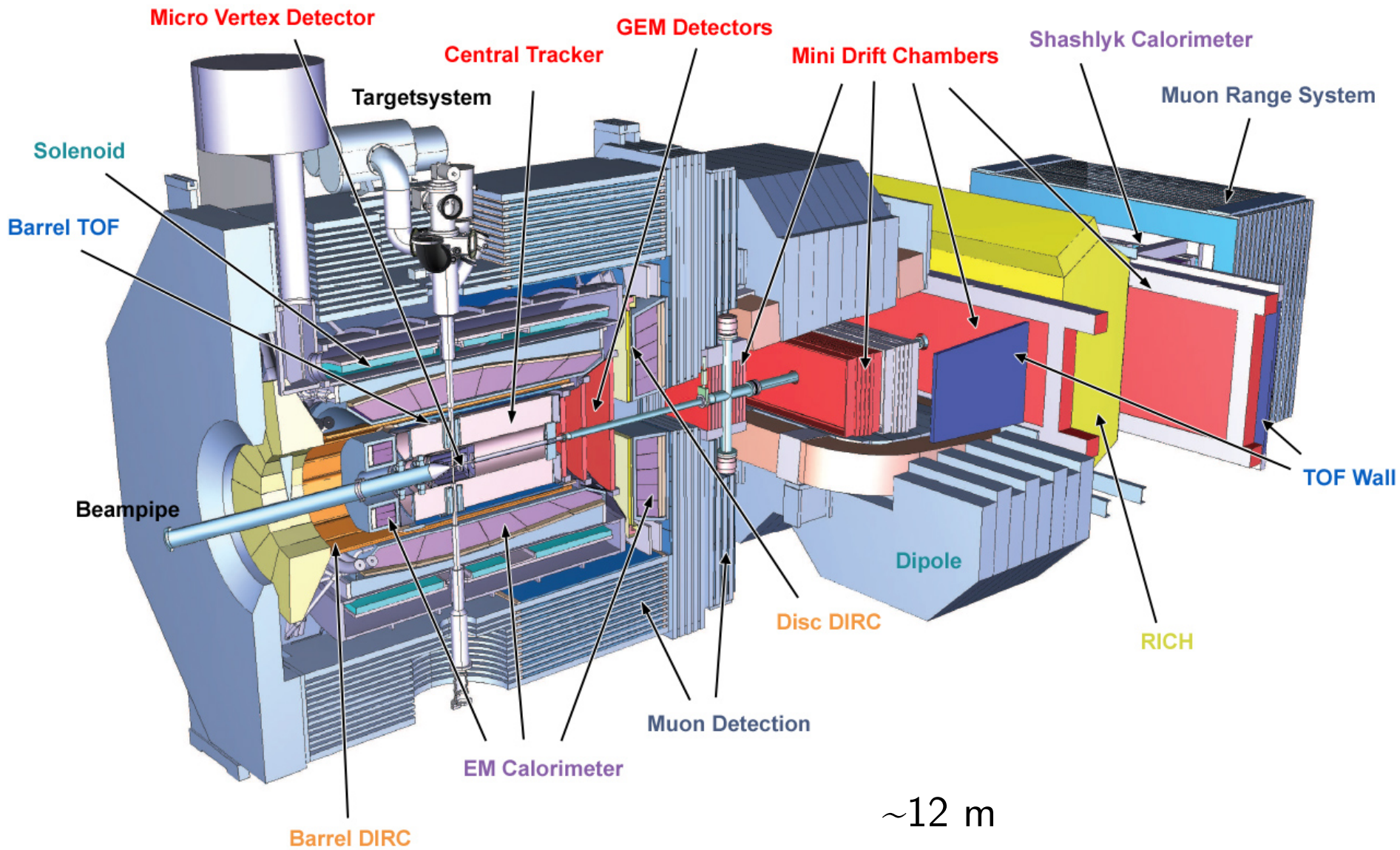
- $10^{10} \bar{p}$
- $\delta p/p \approx 10^{-5}$ (e^- cooling)

Internal targets

- $\mathcal{L} = 2 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$
- H_2 Pellets
- Cluster jet
- Nuclei: Be, C, Si, Al

at start-up planned
 $L = 1 \times 10^{31} \text{ cm}^{-2} \text{ s}^{-1}$

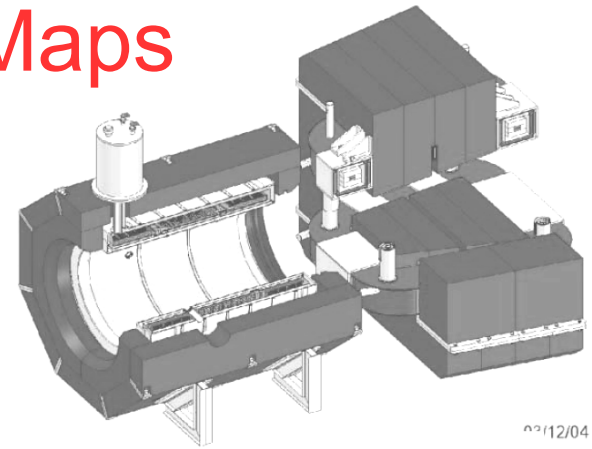
Question:
what's that large dipole magnet
behind Panda good for?



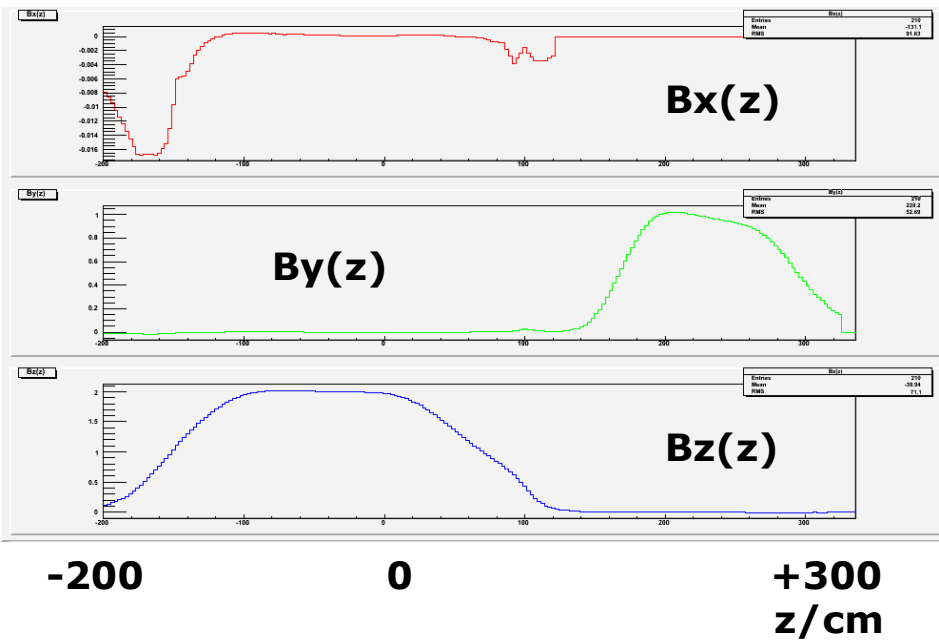
Target spectrometer
 $B_z = 2\text{ T}$

Forward spectrometer
 Dipole $B \cdot L = 2\text{ Tm}$

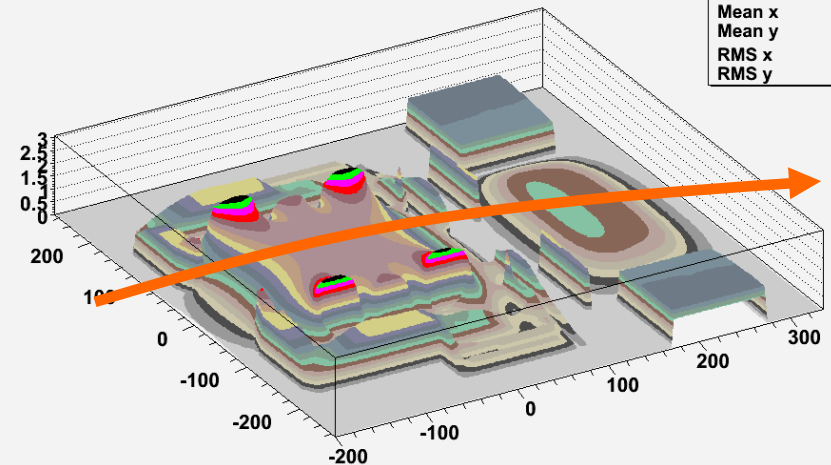
Panda B Field Maps



B field in kG



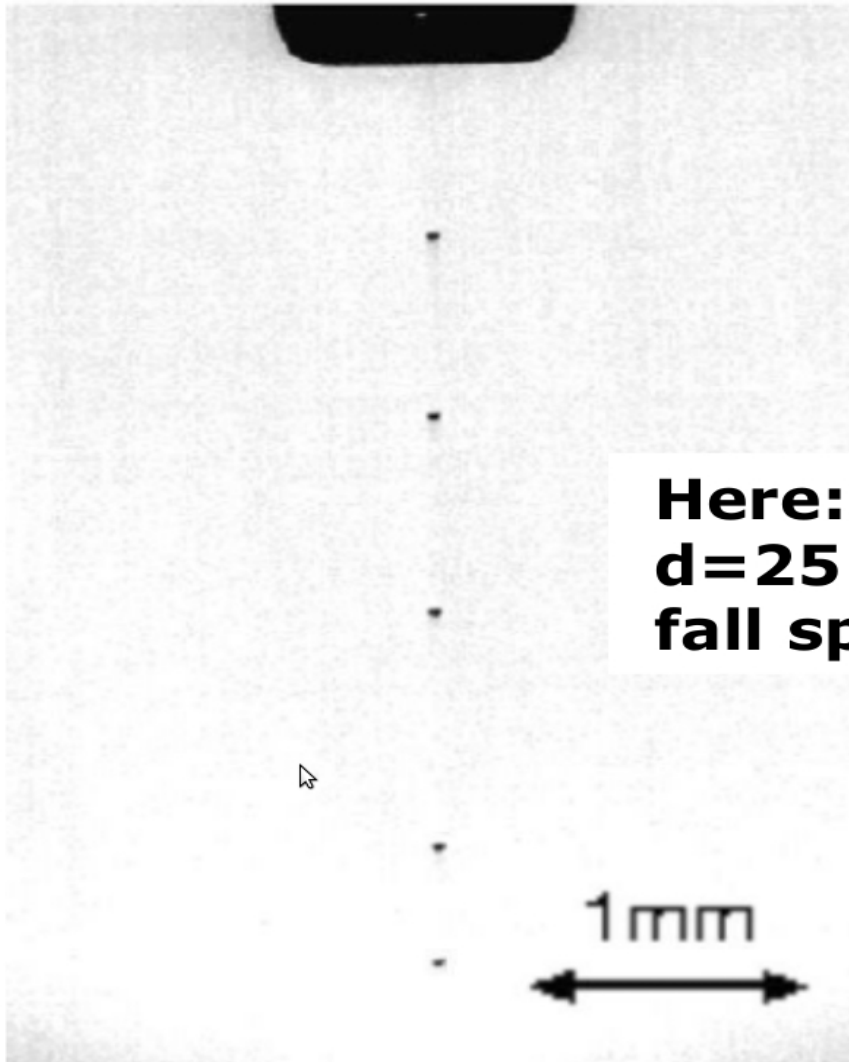
B mod y=0 plane



**→ beam deflection for $p_{\text{beam}} = 15 \text{ GeV}/c$
4.2 cm @ $z = 6\text{m}$ (end of dipole)**

Question:
why is the HESR an „accelerator“
and not (only) a „storage ring“ ?

The Panda Pellet Target



Here: WASA Target
 $d=25\ \mu\text{m}$
fall speed $\geq 60\ \text{m/s}$

Anti-proton beam momentum $p \leq 15 \text{ GeV}/c$

$\rightarrow \sqrt{s} \leq 5.5 \text{ GeV}$

access to states higher than 5 GeV !

not available in Belle II (B decays) neither at BESIII

$B = 2 \text{ T}$ (high!)

fixed target

$\rightarrow$ high p_z of tracks (boosted)

NO TRIGGER

full reconstruction online

with interaction rate $2 \times 10^7 /s$

Panda is a fixed target experiment

$$\sqrt{s} = \sqrt{2m_p^2 + 2m_p \sqrt{p_{beam}^2 + m_p^2}} \quad \text{Homework}$$

$p_{beam} / \text{GeV}/c$	$\sqrt{s} / \text{GeV}$	Resonance
4.064	3.096	J/ψ
6.234	3.686	ψ'
6.571	3.770	ψ''
6.991	3.872	X(3872)
7.277	3.940	Y(3940)
7.705	4.040	ψ'''
8.685	4.260	Y(4260)

$$\beta_{cms}=0.89 \text{ (very high!)}$$

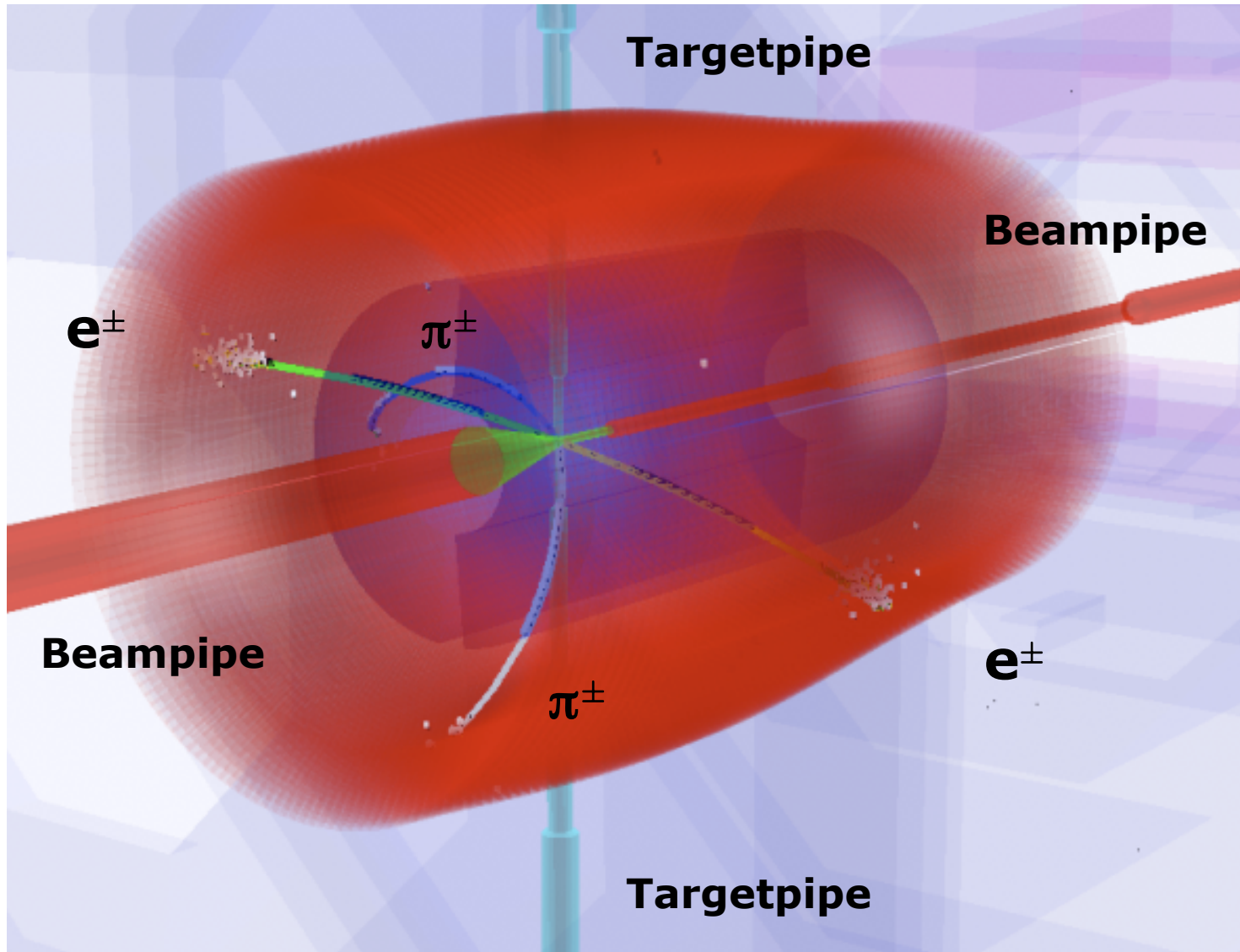
$$\beta\gamma=1.95$$

$$\beta\gamma=0.43 \text{ (Belle), } 0.28 \text{ (Belle II)}$$



Beam operators „tune“ antiproton momentum energy (for resonance scan) is a non-linear function

$X(3872) \rightarrow J/\psi \pi^+ \pi^-$ Event, PandaRoot Simulation



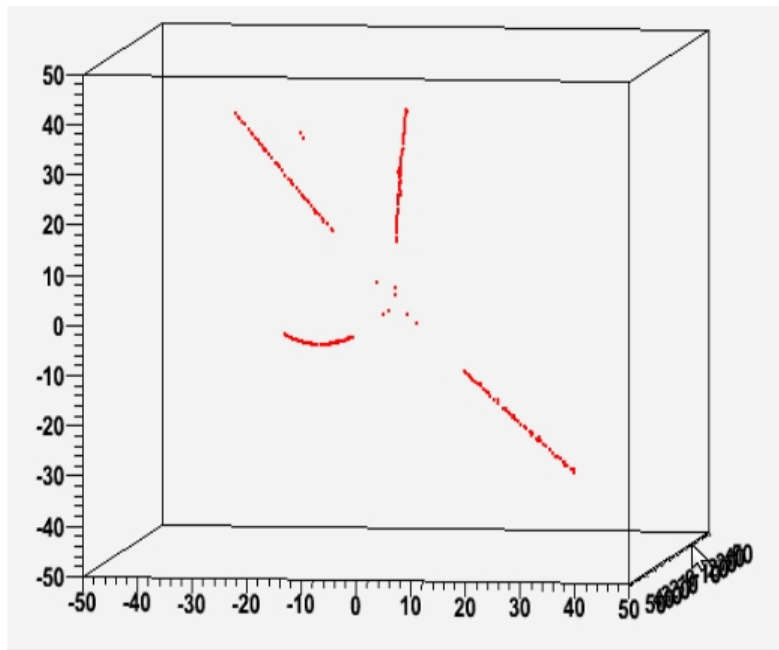
PandaRoot Framework Simulation

$X(3872) \rightarrow J/\psi \pi^+ \pi^-$

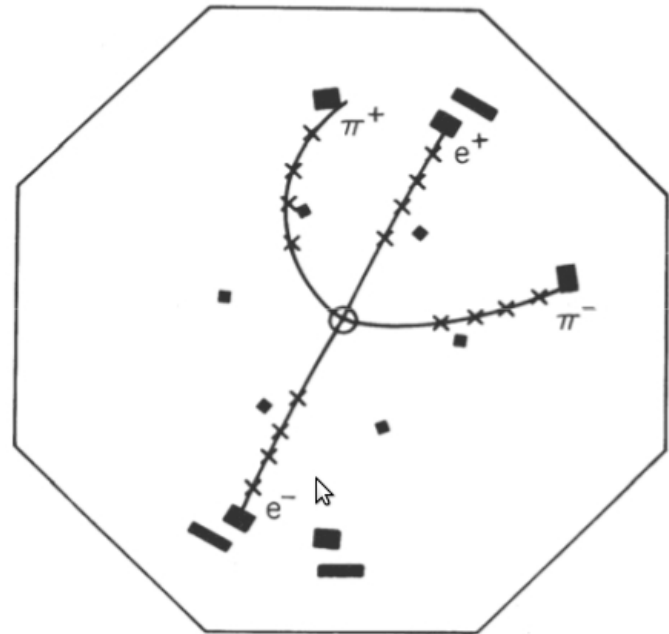
TPC digitization,

MVD Silicon Tracker digitization

XYZ coordinates / cm

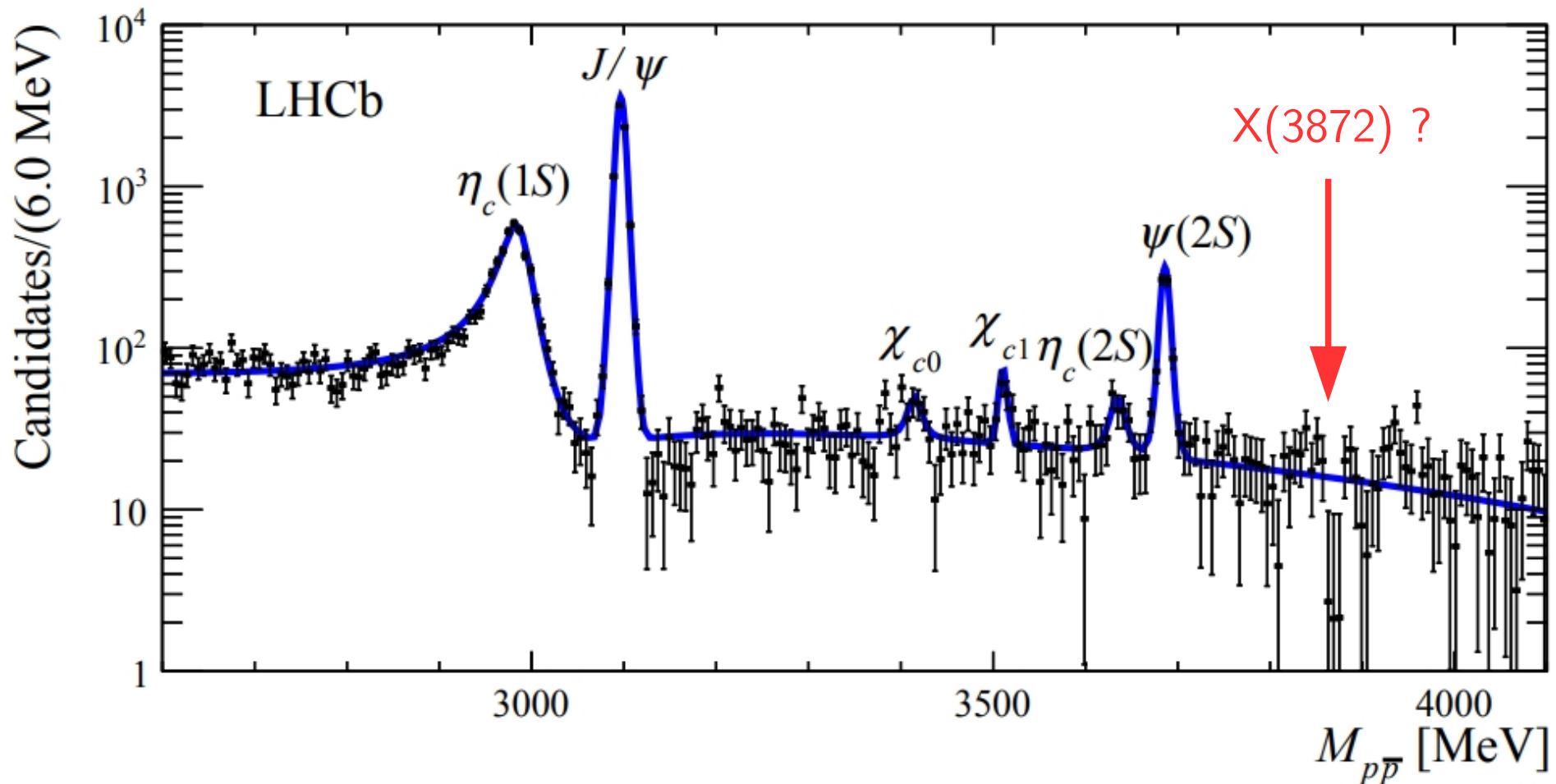


$\psi' \rightarrow J/\psi \pi^+ \pi^-$
Mark II, 1973



How can we estimate
cross sections at PANDA ?
DETAILED BALANCE.

$B^+ \rightarrow [\text{charmonium}]K^+$ decays, with $[\text{charmonium}] \rightarrow p\bar{p}$
 LHCb, arXiv:1303.7133 [hep-ex], Eur. Phys. J. C73 (2013) 2462
 LHCb, arXiv:1607.06446 [hep-ex], Phys.Lett. B769 (2017) 305



Remember Breit–Wigner?

From PDG,
Review Section „Kinematics“

This is SQUARED
(there is no „i“ anymore)

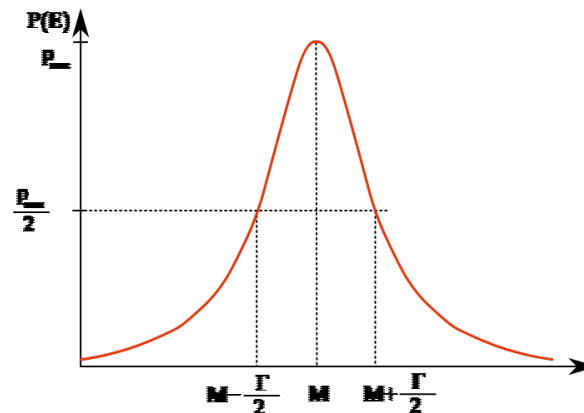
The spin-averaged Breit-Wigner cross section for a spin- J resonance produced in the collision of particles of spin S_1 and S_2 is

$$\sigma_{BW}(E) = \frac{(2J+1)}{(2S_1+1)(2S_2+1)} \frac{\pi}{k^2} \frac{B_{\text{in}} B_{\text{out}} \Gamma_{\text{tot}}^2}{(E - E_R)^2 + \Gamma_{\text{tot}}^2/4}, \quad (46.55)$$

where k is the c.m. momentum, E is the c.m. energy, and B_{in} and B_{out} branching fractions of the resonance into the entrance and exit channels. The $2S+1$

k is wave number,
for a matter wave

$$k \equiv \frac{2\pi}{\lambda} = \frac{p}{\hbar} = \frac{\sqrt{2mE}}{\hbar}$$



The (squared) Breit-Wigner formula relates the cross section and the branching fraction.

N.b. this is more a „coupling strength“ but time-reversed it gives a branching fraction.

Cross section for $p \bar{p} \rightarrow X(3872)$

Branching fraction
of $X(3872)$ as
detected in Panda

Branching fraction
 $X(3872) \rightarrow p \bar{p}$

spin $X(3872)$

$$\sigma_{\text{BW}}(E_{\text{cm}}) = \frac{(2J+1)}{(2S_1+1) \cdot (2S_2+1)} \cdot \frac{\pi}{k^2} \cdot \frac{\mathcal{B}_{\text{in}}(i) \cdot \mathcal{B}_{\text{out}}(f) \cdot \Gamma_R^2}{(E_{\text{cm}} - M_R)^2 + \Gamma_R^2/4}$$

spin
proton

spin
antiproton

width of $X(3872)$
unknown!
(we need a trick)

$$k = \sqrt{\frac{E_{\text{cm}}^2 - 4m_p^2}{4}}$$

How do we know cross sections @ $\bar{P}$ ANDA ?

→ Detailed Balance

Production @ Panda

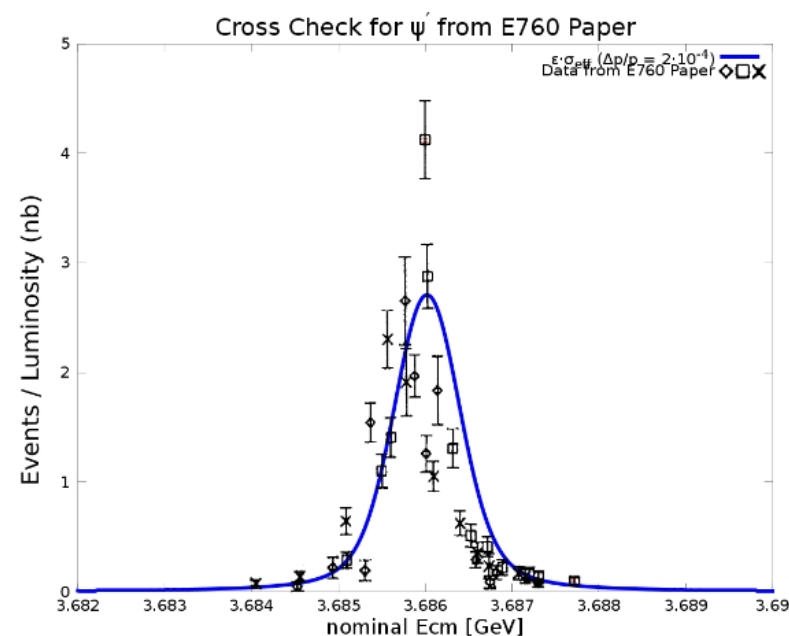
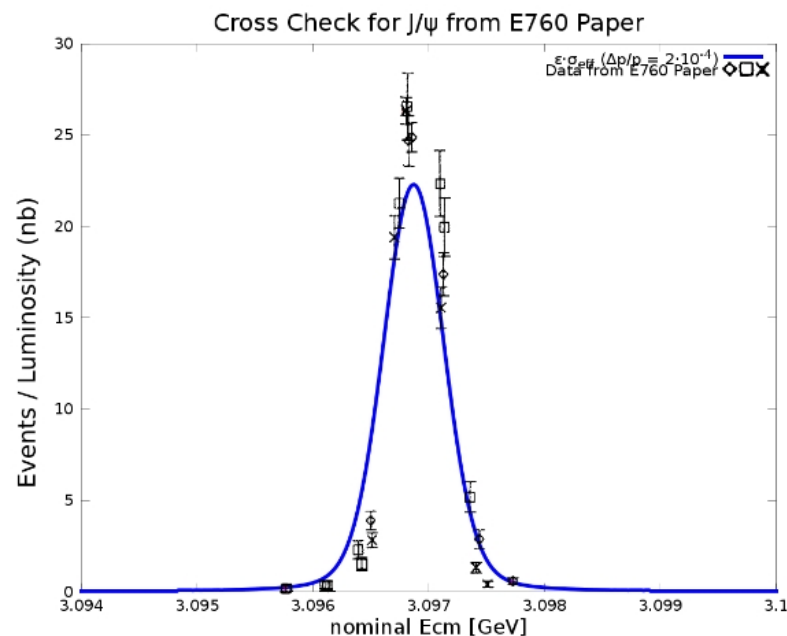
$$\begin{aligned}
 \sigma[p\bar{p} \rightarrow X(3872)] &= \sigma_{BW}[p\bar{p} \rightarrow X \rightarrow \text{all}](m_{X(3872)}) \\
 &= \frac{(2J+1) \cdot 4\pi}{m_{X(3872)}^2 - 4m_p^2} \cdot \frac{\mathcal{B}(X(3872) \rightarrow p\bar{p}) \cdot \overbrace{\mathcal{B}(X(3872) \rightarrow f)}^{=1} \cdot \Gamma_{X(3872)}^2}{\underbrace{4(m_{X(3872)} - m_{X(3872)})^2}_{=0} + \Gamma_{X(3872)}^2} \\
 &\stackrel{(J=1)}{=} \frac{3 \cdot 4\pi}{m_{X(3872)}^2 - 4m_p^2} \cdot \mathcal{B}(X(3872) \rightarrow p\bar{p})
 \end{aligned}$$

Decay
@ Belle, BaBar, Bes3, LHCb



Trick: if sitting on the resonance, the width cancels out

Crosscheck of detailed balance with data from E760



Data points from E760, Phys. Rev. D47 (1993) 772
blue curves from detailed balance (LHCb as input)
M. Galuska (Giessen)

Table: Peak cross sections $\sigma_{[\text{p}\bar{\text{p}} \rightarrow R]}^{\text{peak}}$ for $\text{p}\bar{\text{p}} \rightarrow R$ assuming Breit Wigner distributions with constant small width Γ_R .

Res. R	J	Mass m [MeV]	$\mathcal{B}(R \rightarrow \text{p}\bar{\text{p}})$	$\sigma_{[\text{p}\bar{\text{p}} \rightarrow R]}^{\text{peak}} \pm \text{err. fr. } \mathcal{B}(R \rightarrow \text{p}\bar{\text{p}}) \pm \text{err. fr. } m_R$
$J/\psi(1S)$	1	3096.916 ± 0.011	$(2.17 \pm 0.07) \cdot 10^{-3}$	$5.25 \pm 0.17 \pm 0.00 \mu\text{b}$
$\psi(2S)$	1	$3686.109^{+0.012}_{-0.014}$	$(2.76 \pm 0.12) \cdot 10^{-4}$	$402 \pm 18 \pm 4 \text{ nb}$
$\eta_c(1S)$	0	2981.0 ± 1.1	$(1.41 \pm 0.17) \cdot 10^{-3}$	$1.29 \pm 0.16 \pm 0.00 \mu\text{b}$
$\eta_c(1S)$	0	2981.0 ± 1.1	$(1.32 \pm 0.19) \cdot 10^{-3}$	$1.21 \pm 0.17 \pm 0.00 \mu\text{b}$
$\eta_c(2S)$	0	3638.9 ± 1.3	$(1.85 \pm 1.26) \cdot 10^{-4}$	$93 \pm 63 \pm 0 \text{ nb}$
$\eta_c(2S)$	0	3638.9 ± 1.3	$(3.12 \pm 1.65) \cdot 10^{-4}$	$< 157 \pm 83 \pm 0 \text{ nb (95\% CL)}$
$\chi_{c0}(1P)$	0	3414.75 ± 0.31	$(2.23 \pm 0.13) \cdot 10^{-4}$	$134.1 \pm 7.8 \pm 0 \text{ nb}$
$h_c(1P)$	1	3525.41 ± 0.16	$(8.95 \pm 5.21) \cdot 10^{-4}$	$1.47 \pm 0.86 \pm 0 \mu\text{b}$
$h_c(1P)$	1	3525.41 ± 0.16	$(1.68 \pm 0.05) \cdot 10^{-3}$	$< 2776 \pm 87 \pm 0 \text{ nb (95\% CL)}$
$X(3872)$	1	3871.68 ± 0.17	$(5.31 \pm 0.00) \cdot 10^{-4}$	$< 68.0 \pm 4.0 \pm 0.0 \text{ nb (95\% CL)}$
$X(3915)$	?	3917.5 ± 2.7	$(27 \pm 10) \cdot 10^3$	not isolated

Let's assume 50 nb (conservative)

Cross sections at $\overline{\text{P}}\text{ANDA}$

$$L = 1 \times 10^{31} \text{ cm}^{-2} \text{ s}^{-1} \text{ (start-up phase)}$$

$$1 \text{ nb} = 1 \times 10^{-9} \times 10^{-24} \text{ cm}^2$$

$$1 \text{ nb}^{-1} = 10^{33} \text{ cm}^{-2}$$

$L=0.01$ collisions per nanobarn and per second

for 1 nb production cross section

$$0.01 * 3600 * 24 = 864 \text{ events per 1 day}$$

for $X(3872)$: estimate 50 nb

43.500 per 1 day

Decay into $J/\psi\pi\pi$ (assume 5% branching fraction)

→ 2160 events per day (in Panda start-up phase!)

Belle recorded ~150 events in ~10 years

End of Lecture 2
Thank you!

Backup Slides

Bottomonium-like States

RECOIL MASS

$$m_B = \sqrt{E_B^{*2} - \vec{p}_B^{*2}} \quad (1)$$

where * indicates the center-of-mass system.

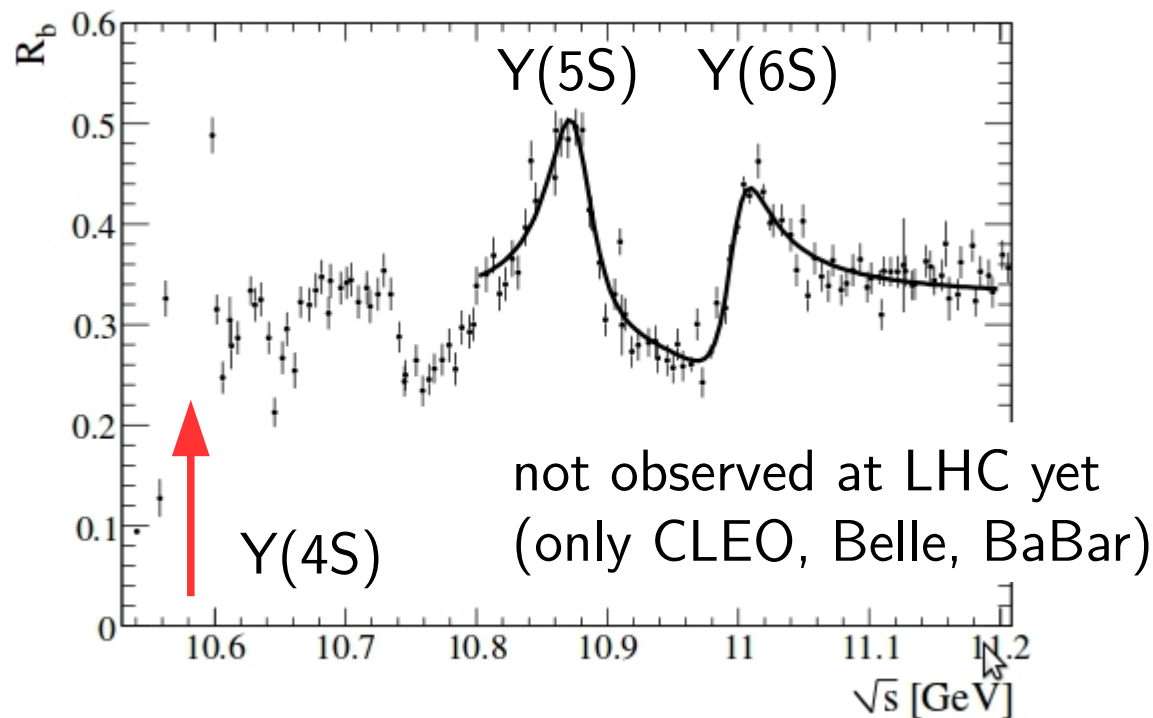
In a two-body system: $\vec{p}_A^* = -\vec{p}_B^*$ and $E_A^* + E_B^* = \sqrt{s}$.
(back-to-back in cms)

$$m_B = \sqrt{(\sqrt{s} - E_A^*)^2 - p_A^{*2}} \quad (2)$$

This implies: the mass of B can be calculated from measurements of A only. B does not need to be measured.

→ sometimes also referred to as „missing mass“

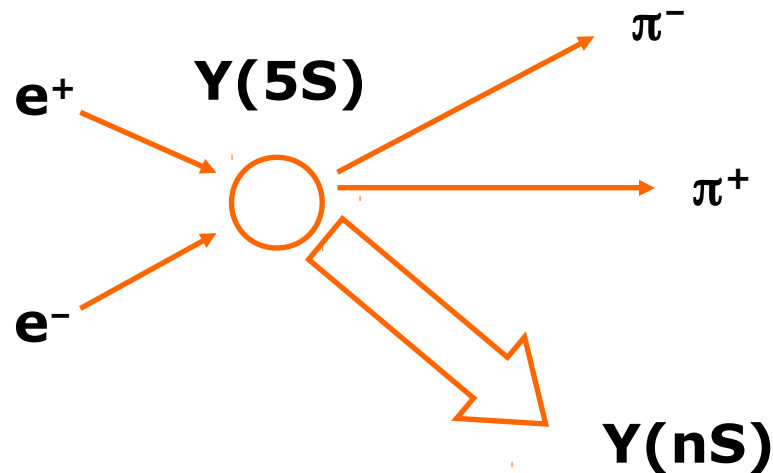
	$\Upsilon(10860)$	$\Upsilon(11020)$
mass (GeV)	10.876 ± 0.002	10.996 ± 0.002
width (MeV)	43 ± 4	37 ± 3
ϕ (rad)	2.11 ± 0.12	0.12 ± 0.07
PDG mass (GeV)	10.865 ± 0.008	11.019 ± 0.008
PDG width (MeV)	110 ± 13	79 ± 16



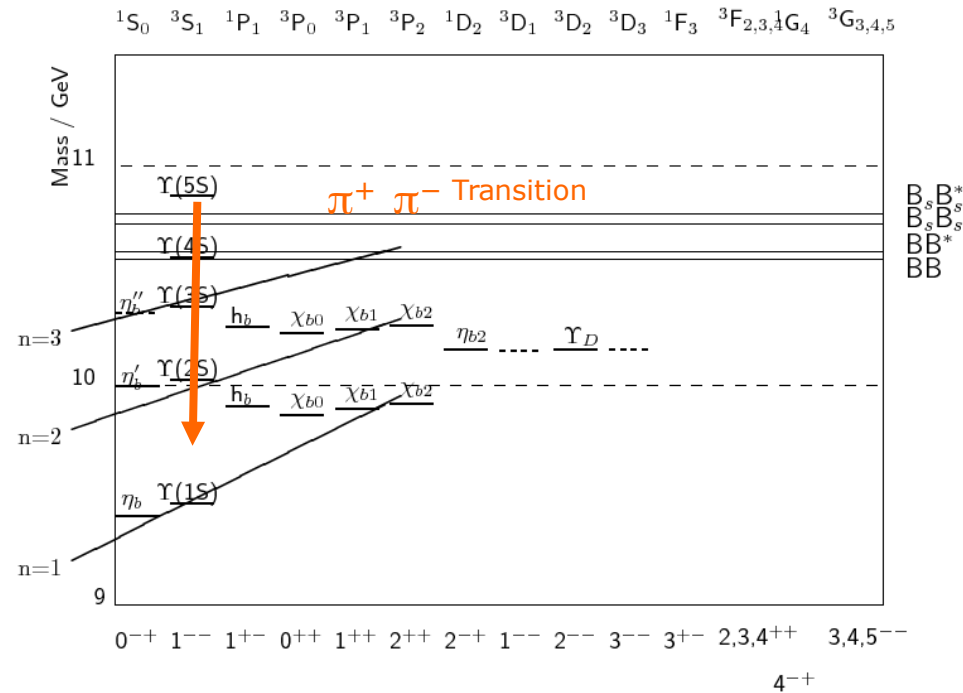
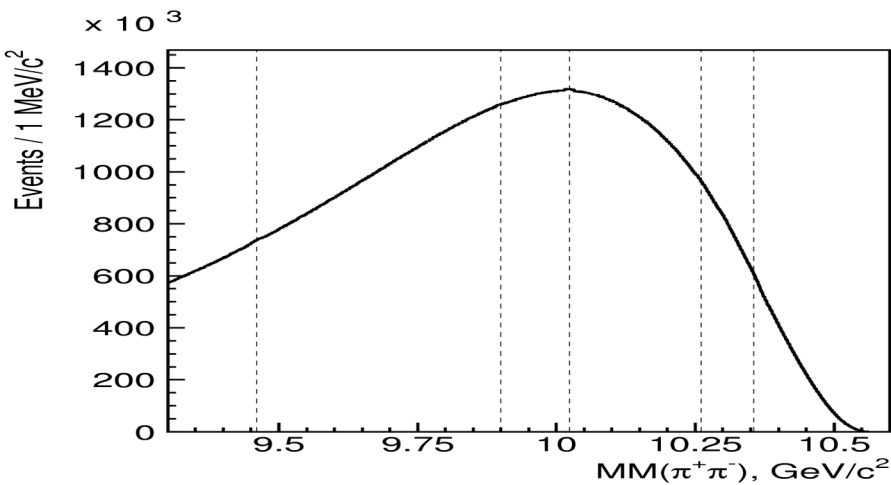
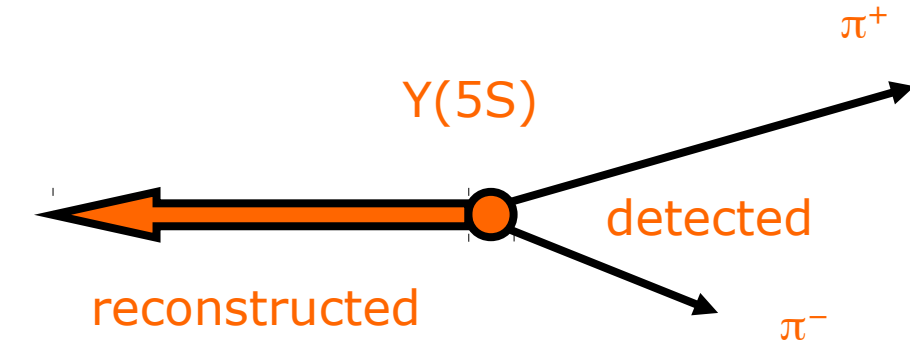
BaBar, 0809.4120[hep-ex], Phys. Rev. Lett. 102(2009)012001
 Events „tagged“ with a B meson ($N_{\text{track}} \geq 3$, $E_{\text{vis}} > 4.5$ GeV, $R_2 < 0.2$)

Y(5S) data taking

- KEK-B and Belle changed beam energy to Y(5S)
- 22 points, 1 fb^{-1} per point, 5 MeV apart
61 points, 0.5 fb^{-1} per point, 1 MeV apart
- investigate **[vector $\rightarrow$ vector $\pi \pi$]**
as an analogy to $Y(4260) \rightarrow J/\psi \pi \pi$



$\Upsilon(5S) \rightarrow X \pi^+ \pi^-$ reconstruction



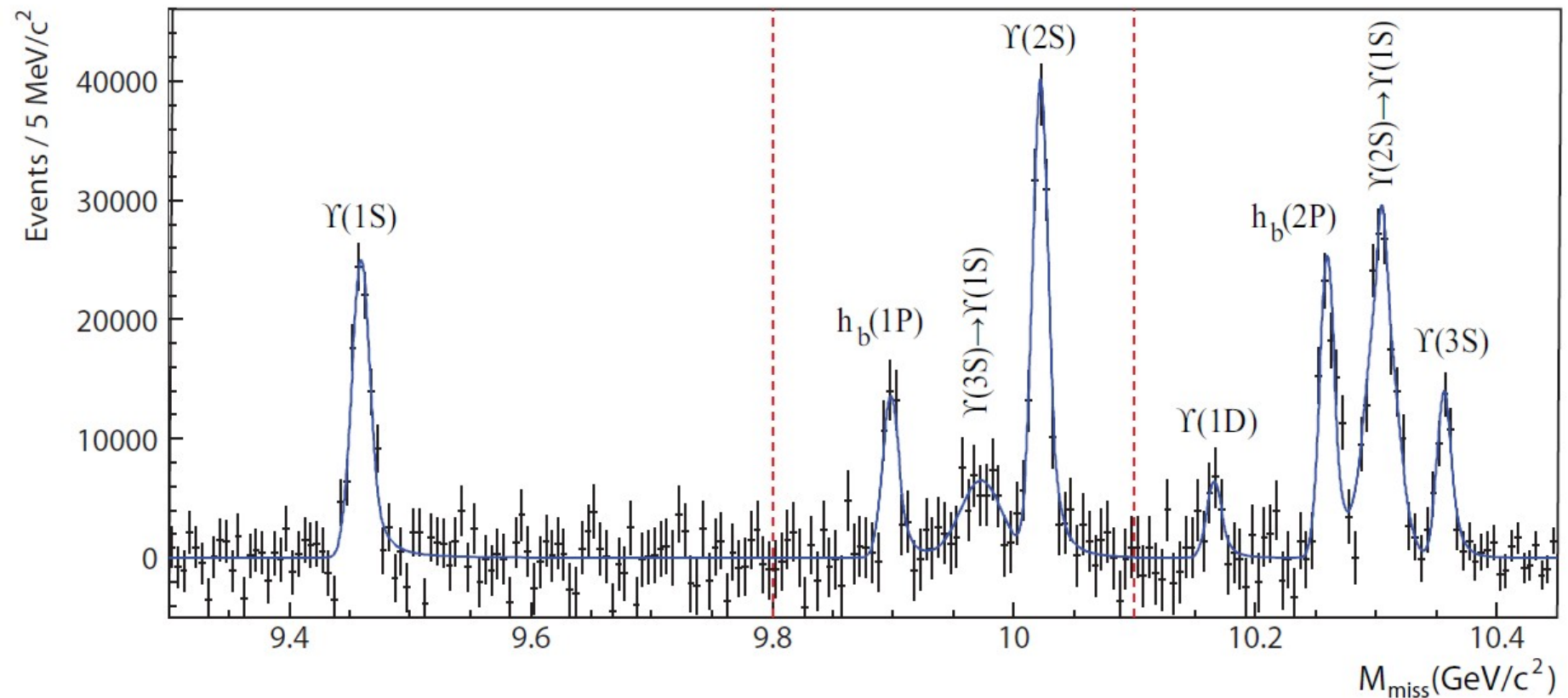
$$M_{\text{miss}}(X) = \sqrt{(E_{\text{c.m.}} - E_X^*)^2 - p_X^{*2}}$$

$\Upsilon(5S)$ Decays

$\pi^+ \pi^-$ missing mass

First observation of
 $h_b(1P)$ and $h_b(2P)$

Belle, 121.4 fb⁻¹
Phys. Rev. Lett 108(2011)032001
arXiv:1103.3419



Advantage of recoil mass technique:

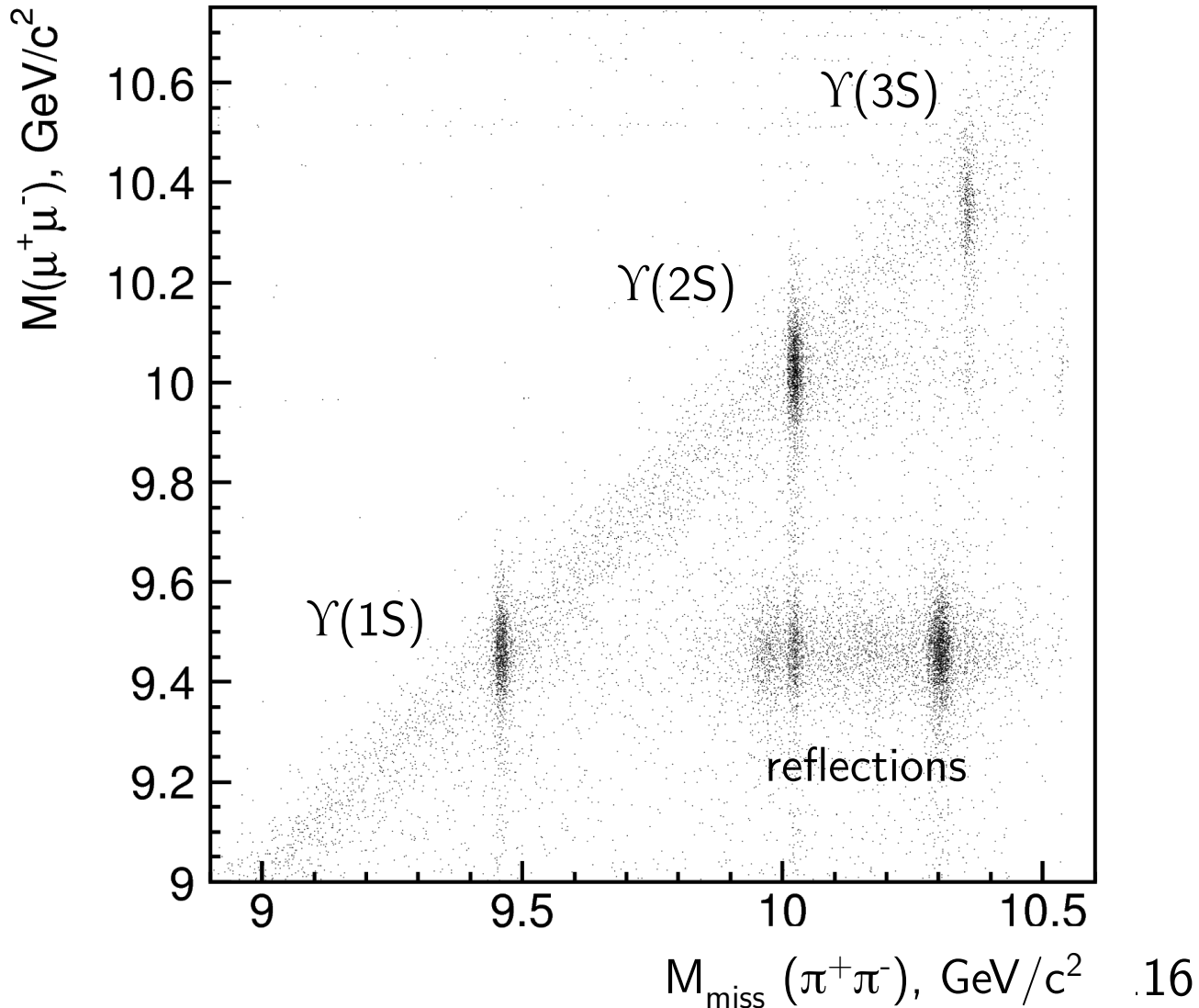
reconstruction of decay (final state particles)
on recoil side not required
→ 100% reconstruction efficiency

Resonant substructure of
 $\Upsilon(5S) \rightarrow \Upsilon(nS) \pi^+ \pi^-$
($n=1,2,3$)

$$\Upsilon(5S) \rightarrow \Upsilon(nS) \pi^+ \pi^- \quad (n = 1, 2, 3)$$

$$\quad \quad \quad \downarrow$$

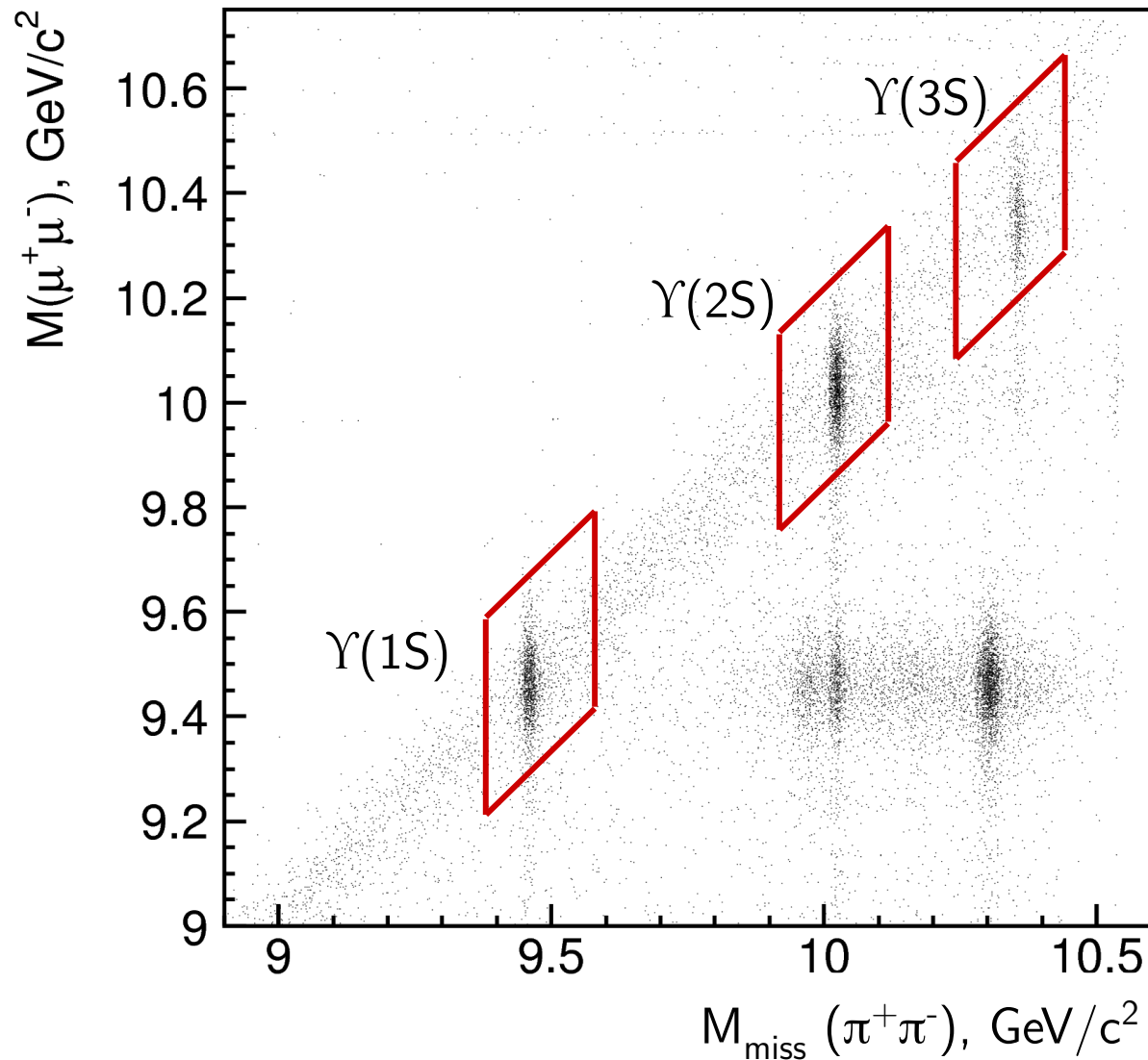
$$\quad \quad \quad \mu^+ \mu^-$$



$$\Upsilon(5S) \rightarrow \Upsilon(nS) \pi^+ \pi^- \quad (n = 1, 2, 3)$$

$$\quad \quad \quad \downarrow$$

$$\quad \quad \quad \mu^+ \mu^-$$



Reflections
 $\Upsilon(5S)$
 $\rightarrow \Upsilon(2S, 3S) \pi \pi$
 $\rightarrow \Upsilon(1S) \pi \pi \pi \pi$

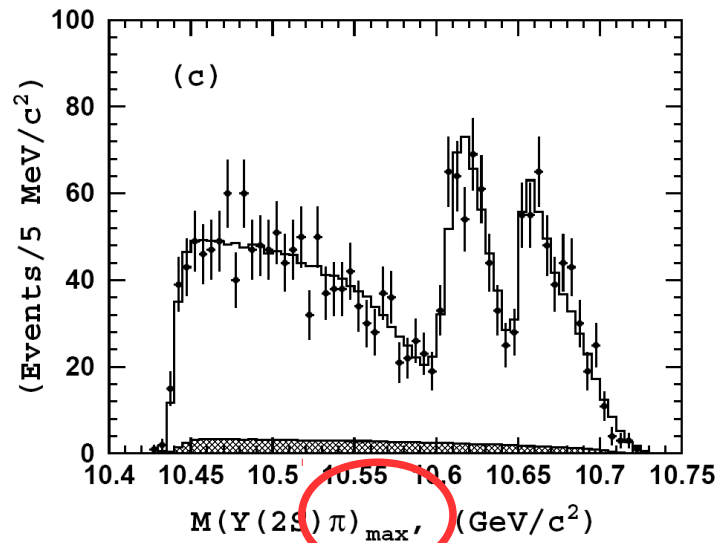
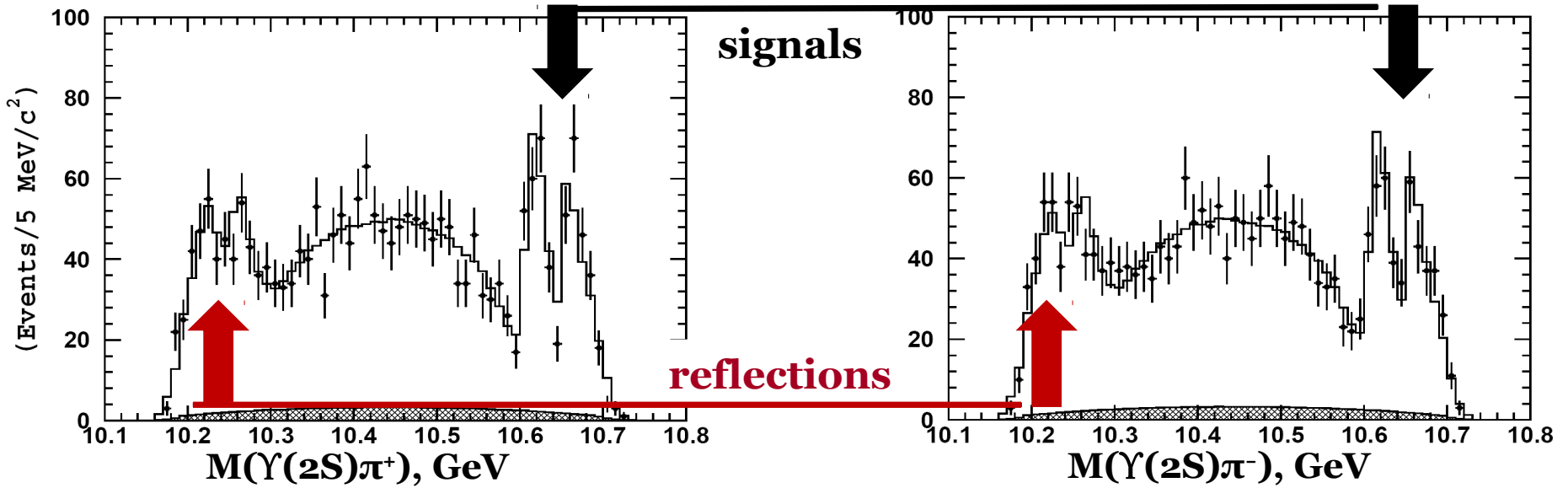
.17

REFLECTION

$$Y(5S) \rightarrow Y(3S) \pi_1^+ \pi_1^- \rightarrow Y(1S) \underbrace{\pi_2^+ \pi_2^-}_{\text{monoenergetic } Y(3S) \rightarrow Y(1S)} \underbrace{\pi_1^+ \pi_1^-}_{\text{monoenergetic } Y(5S) \rightarrow Y(3S)}$$

Now we combine $Y(1S)$ with $\pi_1^+ \pi_1^-$
gives a (wrong) peak!

$\Upsilon(2S)\pi^+\pi^-$



A different type of reflection

$$\begin{array}{ll} \Upsilon(5S) \rightarrow \Upsilon(2S)\pi^+\pi^- & \Upsilon(5S) \rightarrow \Upsilon(2S)\pi^+\pi^- \\ \Upsilon(5S) \rightarrow Z^+\pi^- & \Upsilon(5S) \rightarrow Z^-\pi^+ \\ Z^+ \rightarrow \Upsilon(2S)\pi^+ & Z^- \rightarrow \Upsilon(2S)\pi^- \end{array}$$

π^+ from Z^+ decay is monoenergetic (in Z rest frame),
because of two-body kinematics

π^+ from $\Upsilon(5S)$ decay in case of Z^- is monoenergetic,
because two-body decay and initial energy is fixed

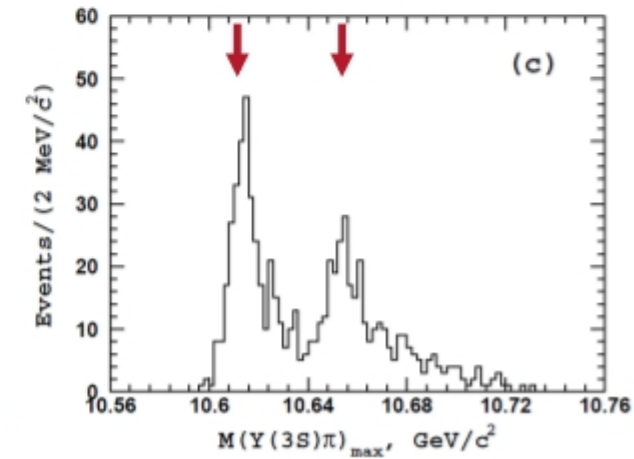
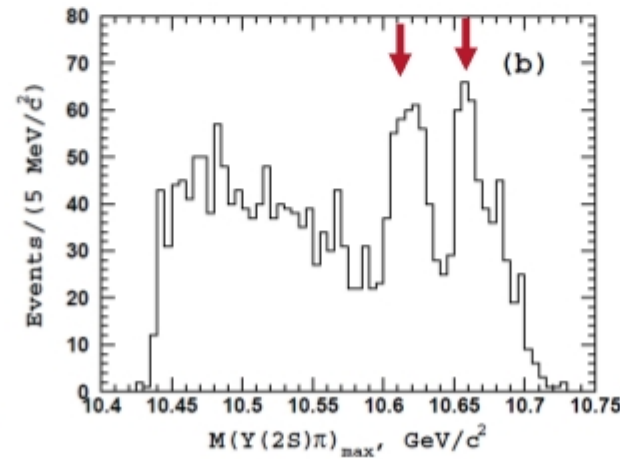
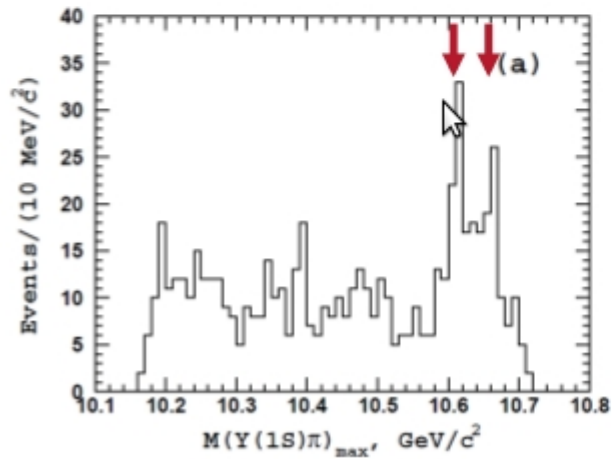
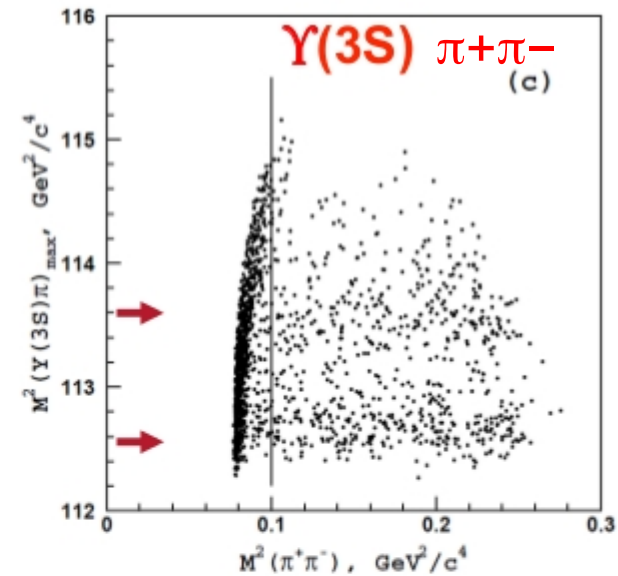
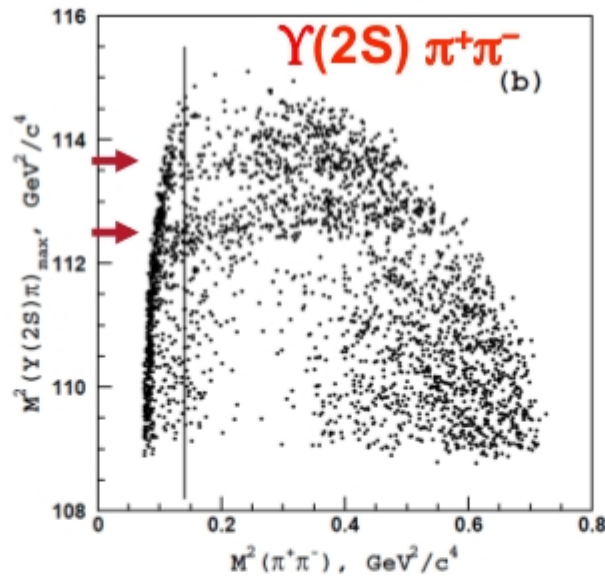
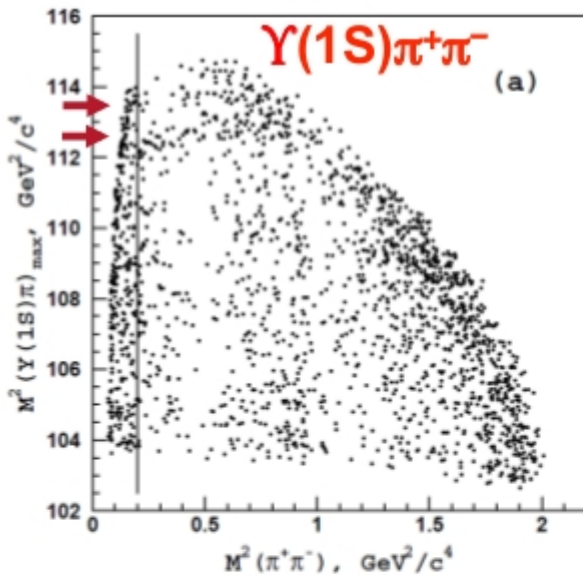
→ $[\Upsilon(2S)\pi^+(\text{from } \Upsilon(5S) \text{ decay})]$ combination gives a (wrong) peak

Solution: the one (the other) π^+ is high (low) momentum

→ "identify" the pions (subscript "max")

Side remark: the pure observation of these reflections tell us,
that there is a Z^+ and a Z^-

$\Upsilon(5S) \rightarrow \Upsilon(nS) \pi^+ \pi^-$ Dalitz plots



→ Signals of $Z_b(10610)$ and $Z_b(10650)$ **CHARGED STATES**

Summary of Z_b parameters

Thresholds (PDG)

BB* 10,604 GeV

B*B* 10,650 GeV

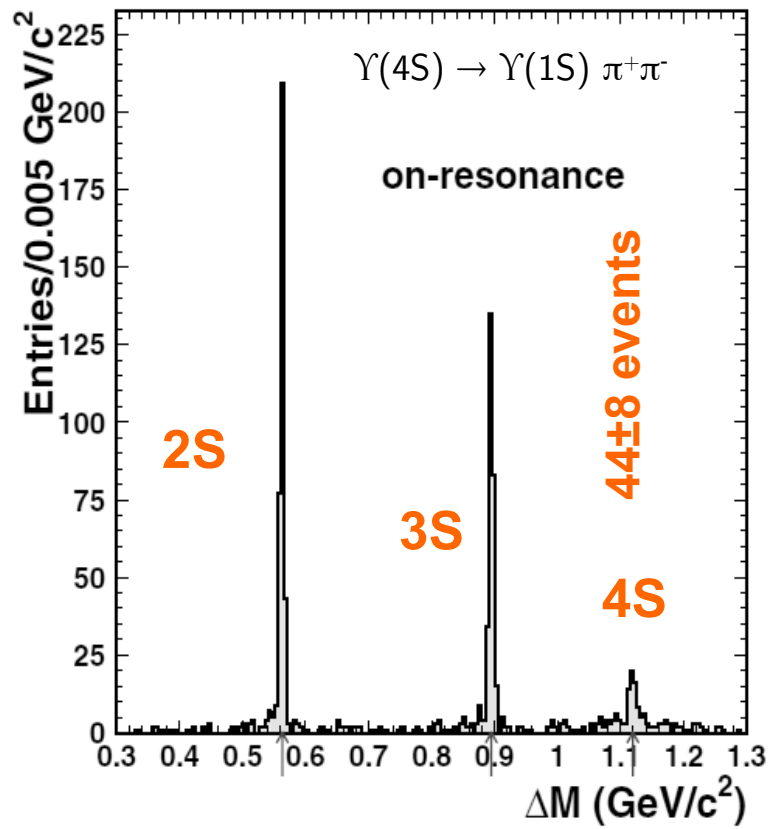
Final state	$\Upsilon(1S)\pi^+\pi^-$	$\Upsilon(2S)\pi^+\pi^-$	$\Upsilon(3S)\pi^+\pi^-$	$h_b(1P)\pi^+\pi^-$	$h_b(2P)\pi^+\pi^-$
$M[Z_b(10610)], \text{ MeV}/c^2$	$10611 \pm 4 \pm 3$	$10609 \pm 2 \pm 3$	$10608 \pm 2 \pm 3$	$10605 \pm 2_{-1}^{+3}$	10599_{-3-4}^{+6+5}
$\Gamma[Z_b(10610)], \text{ MeV}$	$22.3 \pm 7.7_{-4.0}^{+3.0}$	$24.2 \pm 3.1_{-3.0}^{+2.0}$	$17.6 \pm 3.0 \pm 3.0$	$11.4_{-3.9-1.2}^{+4.5+2.1}$	13_{-8-7}^{+10+9}
$M[Z_b(10650)], \text{ MeV}/c^2$	$10657 \pm 6 \pm 3$	$10651 \pm 2 \pm 3$	$10652 \pm 1 \pm 2$	$10654 \pm 3_{-2}^{+1}$	10651_{-3-2}^{+2+3}
$\Gamma[Z_b(10650)], \text{ MeV}$	$16.3 \pm 9.8_{-2.0}^{+6.0}$	$13.3 \pm 3.3_{-3.0}^{+4.0}$	$8.4 \pm 2.0 \pm 2.0$	$20.9_{-4.7-5.7}^{+5.4+2.1}$	$19 \pm 7_{-7}^{+11}$
Rel. normalization	$0.57 \pm 0.21_{-0.04}^{+0.19}$	$0.86 \pm 0.11_{-0.10}^{+0.04}$	$0.96 \pm 0.14_{-0.05}^{+0.08}$	$1.39 \pm 0.37_{-0.15}^{+0.05}$	$1.6_{-0.4-0.6}^{+0.6+0.4}$
Rel. phase, degrees	$58 \pm 43_{-9}^{+4}$	$-13 \pm 13_{-8}^{+17}$	$-9 \pm 19_{-26}^{+11}$	187_{-57-12}^{+44+3}	$181_{-105-109}^{+65+74}$

The two charged states are observed in 5 decays channels.

Reminder:
any of these results
were only possible
because of one reason:
we have factor $\geq 10^3$
too many events ...

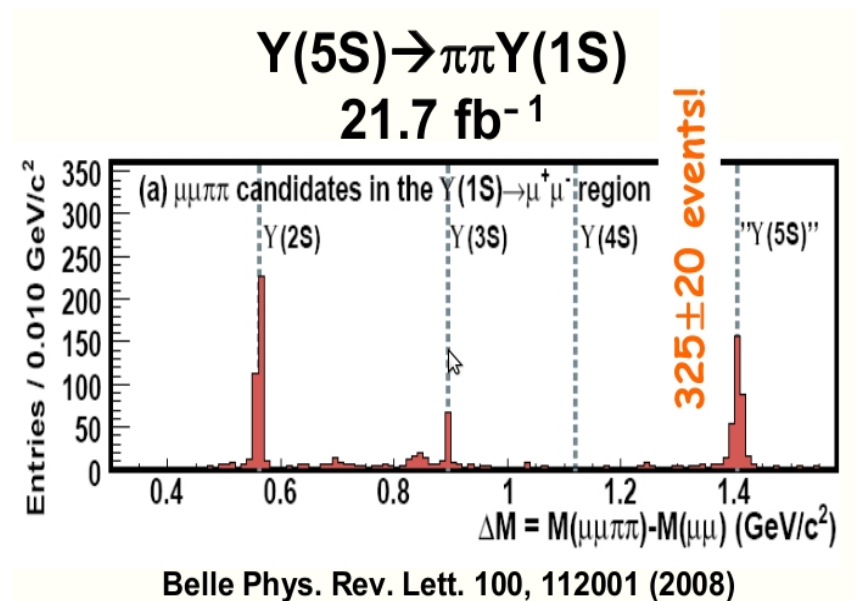
$\Gamma[Y(5S) \rightarrow \pi\pi Y(nS)]$ is huge

$Y(4S) \rightarrow \pi\pi Y(1S)$
477 fb⁻¹



Phys. Rev. D75(2007)071103

*8 times as many events
integrated for Y(nS)
1/20 times the data &
~1/10th the crosssection*



Not only $Y(5S) \rightarrow Y(1S)\pi\pi$ is large,
but also $Y(5S) \rightarrow Y(2S)\pi\pi$

