

The **BabaYaga** event generator

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in collaboration with
G. Montagna, O. Nicrosini, F. Piccinini

- ★ Motivations for precise luminometry
- ★ QED processes & radiative corrections
- ★ The **BabaYaga** and **BabaYaga@NLO** event generators
 - theoretical framework
 - improving theoretical accuracy:
QED Parton Shower and matching with NLO corrections
- ★ Results, tuned comparisons, theoretical accuracy
- ★ Conclusions

Relevant references

★ Website

<http://www.pv.infn.it/hepcomplex/babayaga.html>
(or better ask the authors!)

★ BabaYaga main references:

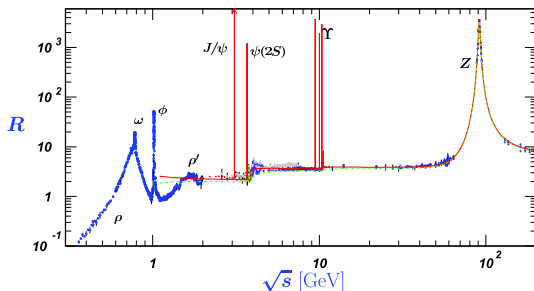
- Barzè et al., Eur. Phys. J. C **71** (2011) 1680 BabaYaga with dark photon
- Balossini et al., Phys. Lett. **663** (2008) 209 BabaYaga@NLO for $e^+e^- \rightarrow \gamma\gamma$
- Balossini et al., Nucl. Phys. **B758** (2006) 227 BabaYaga@NLO for Bhabha
- C.M.C.C. et al., Nucl. Phys. Proc. Suppl. **131** (2004) 48 BabaYaga@NLO
- C.M.C.C., Phys. Lett. B **520** (2001) 16 improved PS BabaYaga
- C.M.C.C. et al., Nucl. Phys. B **584** (2000) 459 BabaYaga

★ Related work:

- S. Actis et al.
“Quest for precision in hadronic cross sections at low energy: Monte Carlo tools vs. experimental data”, Eur. Phys. J. C **66** (2010) 585
Report of the Working Group on Radiative Corrections and Monte Carlo Generators for Low Energies
- C.M.C.C. et al., JHEP **1107** (2011) 126
NNLO massive pair corrections

Why high precision generators for luminosity?

- Precision measurements require a precise knowledge of the machine luminosity
- *e.g.*, the measurement of the $R(s)$ ratio is a key ingredient for the predictions of $a_\mu = (g_\mu - 2)/2$ and $\Delta\alpha_{\text{had}}(M_Z)$ and in turn for SM precision tests



$$a_\mu = \frac{\alpha^2}{3\pi^2} \int_{m_\pi^2}^{\infty} ds K(s) \frac{R(s)}{s} \quad \Delta\alpha_{\text{had}}^{(5)}(M_Z^2) = -\frac{\alpha M_Z^2}{3\pi} \text{Re} \int_{m_\pi^2}^{\infty} \frac{R(s) ds}{s(s - M_Z^2 - i\epsilon)}$$

Reference processes for luminosity

- Instead of getting the luminosity from machine parameters, it's more effective to exploit the relation

$$\sigma = \frac{N}{L} \quad \rightarrow \quad L = \frac{N_{\text{ref}}}{\sigma_{\text{theory}}} \quad \frac{\delta L}{L} = \frac{\delta N_{\text{ref}}}{N_{\text{ref}}} \oplus \frac{\delta \sigma_{\text{theory}}}{\sigma_{\text{theory}}}$$

- Normalization processes are required to have a clean topology, high statistics and **be calculable with high theoretical accuracy**
- ★ Large-angle QED processes as $e^+e^- \rightarrow e^+e^-$ (Bhabha), $e^+e^- \rightarrow \gamma\gamma$, $e^+e^- \rightarrow \mu^+\mu^-$ are golden processes at flavour factories to achieve a typical precision at the level of $1 \div 0.1\%$
 - ↪ **QED RC corrections are mandatory**
- ↪ **BabaYaga** has been developed for high-precision simulation of QED processes at flavour factories (primarily for luminosity determination)

Theory of QED corrections into MC generators

- ★ The most precise MC generators include **exact $\mathcal{O}(\alpha)$ (NLO) photonic corrections matched with higher-order leading logarithmic contributions [multiple photon corrections]** [+ **vacuum polarization**, using a data driven routine for the calculation of the non-perturbative $\Delta\alpha_{\text{had}}^{(5)}(q^2)$ hadronic contribution]
- ★ Common methods used to account for multiple photon corrections are the **analytical collinear QED Structure Functions (SF)**, **YFS exponentiation** and **QED Parton Shower (PS)**
- The QED PS [implemented in **BabaYaga/BabaYaga@NLO**] is an **exact MC solution** of the QED DGLAP equation for the electron SF $D(x, Q^2)$

$$Q^2 \frac{\partial}{\partial Q^2} D(x, Q^2) = \frac{\alpha}{2\pi} \int_x^1 \frac{dt}{t} P_+(t) D\left(\frac{x}{t}, Q^2\right)$$

- The PS solution can be cast into the form

$$D(x, Q^2) = \Pi(Q^2) \sum_{n=0}^{\infty} \int \frac{\delta(x-x_1 \cdots x_n)}{n!} \prod_{i=0}^n \left[\frac{\alpha}{2\pi} P(x_i) L dx_i \right]$$

→ $\Pi(Q^2) \equiv e^{-\frac{\alpha}{2\pi} LI}$ Sudakov form factor, $I_+ \equiv \int_0^{1-\epsilon} P(x) dx$, $L \equiv \ln Q^2/m^2$ collinear log, ϵ soft-hard separator and Q^2 virtuality scale

→ **the kinematics of the photon emissions can be recovered** → **exclusive photons generation**

- The accuracy is improved by **matching exact NLO with higher-order leading log corrections**
 - ★ **theoretical error starts at $\mathcal{O}(\alpha^2)$ (NNLO) QED corrections, for all QED channels [Bhabha, $\gamma\gamma$ and $\mu^+\mu^-$]**

Summary of QED (photonic) radiative corrections

Loosely and schematically, the corrections to the LO cross section can be arranged as (collinear $\log L \equiv \log \frac{s_-}{m_e^2}$)

| | | | |
|------|---|---|-----------------------|
| LO | α^0 | | |
| NLO | αL | α | |
| NNLO | $\frac{1}{2}\alpha^2 L^2$ | $\frac{1}{2}\alpha^2 L$ | $\frac{1}{2}\alpha^2$ |
| h.o. | $\sum_{n=3}^{\infty} \frac{\alpha^n}{n!} L^n$ | $\sum_{n=3}^{\infty} \frac{\alpha^n}{n!} L^{n-1}$ | \dots |

Blue: Leading-Log PS, Leading-Log YFS, SF

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| h.o. | $\sum_{n=3}^{\infty} \frac{\alpha^n}{n!} L^n$ | $\sum_{n=3}^{\infty} \frac{\alpha^n}{n!} L^{n-1}$ | \dots |

Red: matched PS, YFS, SF + NLO

Summary of QED (photonic) radiative corrections

Loosely and schematically, the corrections to the LO cross section can be arranged as (collinear $\log L \equiv \log \frac{s_-}{m_e^2}$)

| | | | |
|------|-------|-------|-------|
| LO | 90% | | |
| NLO | 10% | 0.5% | |
| NNLO | 0.5% | 0.05% | 0.01% |
| h.o. | 0.01% | ... | ... |

Typically at flavour factories (on integrated σ)

Matching NLO and PS in BabaYaga@NLO

Exact $\mathcal{O}(\alpha)$ (NLO) soft+virtual (SV) corrections and hard-bremsstrahlung (H) matrix elements can be combined with QED PS *via* a matching procedure

- $d\sigma_{LL}^{\infty} = \Pi(Q^2, \varepsilon) \sum_{n=0}^{\infty} \frac{1}{n!} |\mathcal{M}_{n,LL}|^2 d\Phi_n$
- $d\sigma_{LL}^{\alpha} = [1 + C_{\alpha,LL}] |\mathcal{M}_0|^2 d\Phi_0 + |\mathcal{M}_{1,LL}|^2 d\Phi_1 \equiv d\sigma_{LL}^{SV}(\varepsilon) + d\sigma_{LL}^H(\varepsilon)$
- $d\sigma_{NLO}^{\alpha} = [1 + C_{\alpha}] |\mathcal{M}_0|^2 d\Phi_0 + |\mathcal{M}_1|^2 d\Phi_1 \equiv d\sigma_{NLO}^{SV}(\varepsilon) + d\sigma_{NLO}^H(\varepsilon)$
- $F_{SV} = 1 + (C_{\alpha} - C_{\alpha,LL}) \quad F_H = 1 + \frac{|\mathcal{M}_1|^2 - |\mathcal{M}_{1,LL}|^2}{|\mathcal{M}_{1,LL}|^2}$

$$d\sigma_{\text{matched}}^{\infty} = F_{SV} \Pi(Q^2, \varepsilon) \sum_{n=0}^{\infty} \frac{1}{n!} \left(\prod_{i=0}^n F_{H,i} \right) |\mathcal{M}_{n,LL}|^2 d\Phi_n$$

$d\Phi_n$ is the **exact** phase space for $n + 2$ final-state particles

Matching NLO and PS in BabaYaga@NLO

- F_{SV} and $F_{H,i}$ are infrared/collinear safe and account for missing $\mathcal{O}(\alpha)$ non-logs, **avoiding double counting of LL**
- $\left[\sigma_{matched}^{\infty} \right] \mathcal{O}(\alpha) = \sigma_{\text{NLO}}^{\alpha}$
- resummation of higher orders LL contributions is preserved
- **the cross section is still fully differential in the momenta of the final state particles (e^+ , e^- and $n\gamma$)**
(F 's correction factors are applied on an event-by-event basis)
- as a by-product, **part of photonic $\alpha^2 L$** included by means of terms of the type $F_{SV | H,i} \times LL$

G. Montagna et al., **PLB** 385 (1996)

- the theoretical error is shifted to $\mathcal{O}(\alpha^2)$ (**NNLO, 2 loop**) **not infrared, singly collinear terms**: very naively and roughly (for photonic corrections)

$$\frac{1}{2} \alpha^2 L \equiv \frac{1}{2} \alpha^2 \log \frac{s}{m_e^2} \sim 5 \times 10^{-4}$$

- to show the typical size of RC, the following setups and definitions are used (for Bhabha)

- a $\sqrt{s} = 1.02 \text{ GeV}$, $E_{min} = 0.408 \text{ GeV}$, $20^\circ < \theta_{\pm} < 160^\circ$, $\xi_{max} = 10^\circ$
- b $\sqrt{s} = 1.02 \text{ GeV}$, $E_{min} = 0.408 \text{ GeV}$, $55^\circ < \theta_{\pm} < 125^\circ$, $\xi_{max} = 10^\circ$
- c $\sqrt{s} = 10 \text{ GeV}$, $E_{min} = 4 \text{ GeV}$, $20^\circ < \theta_{\pm} < 160^\circ$, $\xi_{max} = 10^\circ$
- d $\sqrt{s} = 10 \text{ GeV}$, $E_{min} = 4 \text{ GeV}$, $55^\circ < \theta_{\pm} < 125^\circ$, $\xi_{max} = 10^\circ$

$$\begin{aligned}\delta_{VP} &\equiv \frac{\sigma_{0,VP} - \sigma_0}{\sigma_0} & \delta_{\alpha} &\equiv \frac{\sigma_{\alpha}^{NLO} - \sigma_0}{\sigma_0} \\ \delta_{HO} &\equiv \frac{\sigma_{matched}^{PS} - \sigma_{\alpha}^{NLO}}{\sigma_0} & \delta_{HO}^{PS} &\equiv \frac{\sigma^{PS} - \sigma_{\alpha}^{PS}}{\sigma_0} \\ \delta_{\alpha}^{non-log} &\equiv \frac{\sigma_{\alpha}^{NLO} - \sigma_{\alpha}^{PS}}{\sigma_0} & \delta_{\infty}^{non-log} &\equiv \frac{\sigma_{matched}^{PS} - \sigma^{PS}}{\sigma_0}\end{aligned}$$

| setup | (a) | (b) | (c) | (d) |
|-----------------------------|--------|--------|--------|--------|
| δ_{VP} | 1.76 | 2.49 | 4.81 | 6.41 |
| δ_{α} | -11.61 | -14.72 | -16.03 | -19.57 |
| δ_{HO} | 0.39 | 0.82 | 0.73 | 1.44 |
| δ_{HO}^{PS} | 0.35 | 0.74 | 0.68 | 1.34 |
| $\delta_{\alpha}^{non-log}$ | -0.34 | -0.56 | -0.34 | -0.56 |
| $\delta_{\infty}^{non-log}$ | -0.30 | -0.49 | -0.29 | -0.46 |

Table: Relative corrections (in per cent) to the Bhabha cross section for the four setups

- ★ in short, the fact that $\delta_{\alpha}^{non-log} \simeq \delta_{\infty}^{non-log}$ and $\delta_{HO} \simeq \delta_{HO}^{PS}$ means that the matching algorithm preserves both the advantages of exact NLO calculation and PS approach:
 - it includes the missing NLO RC to the PS
 - it adds the missing higher-order RC to the NLO

Estimating the theoretical accuracy

S. Actis et al. Eur. Phys. J. C **66** (2010) 585

- It is extremely important to compare independent calculations/implementations/codes, in order to
 - ★ assess the technical precision, spot bugs (with the same th. ingredients)
 - ★ estimate the theoretical “error” when including partial/incomplete higher-order corrections
- A number of generators are available, some of them including QED h.o. and NLO corrections according to different approaches (collinear SF + NLO, YFS exponentiation, . . .)

| Generator | Processes | Theory | Accuracy | Web address |
|---------------|------------------------------------|-----------------------------------|--------------|--|
| BHAGENF/BKQED | $e^+e^-/\gamma\gamma, \mu^+\mu^-$ | $\mathcal{O}(\alpha)$ | 1% | www.lnf.infn.it/~graziano/bhagenf/bhabha.html |
| BabaYaga v3.5 | $e^+e^-, \gamma\gamma, \mu^+\mu^-$ | Parton Shower | $\sim 0.5\%$ | www.pv.infn.it/hepcomplex/babayaga.html |
| BabaYaga@NLO | $e^+e^-, \gamma\gamma, \mu^+\mu^-$ | $\mathcal{O}(\alpha) + \text{PS}$ | $\sim 0.1\%$ | www.pv.infn.it/hepcomplex/babayaga.html |
| BHWIDE | e^+e^- | $\mathcal{O}(\alpha) \text{ YFS}$ | 0.5% (LEP1) | placzek.home.cern.ch/placzek/bhwide |
| MCGPJ | $e^+e^-, \gamma\gamma, \mu^+\mu^-$ | $\mathcal{O}(\alpha) + \text{SF}$ | $< 0.2\%$ | cmd.inp.nsk.su/~sibid |

Large angle Bhabha: tuned comparisons & technical precision

Without vacuum polarization, to compare QED corrections consistently

At the Φ and τ -charm factories (cross sections in nb)

By BabaYaga group, Ping Wang and A. Sibidanov

| setup | BabaYaga@NLO | BHWIDE | MCGPJ | $\delta(\%)$ |
|---|--------------|-----------|-----------|--------------|
| $\sqrt{s} = 1.02 \text{ GeV}, 20^\circ \leq \vartheta_{\mp} \leq 160^\circ$ | 6086.6(1) | 6086.3(2) | — | 0.005 |
| $\sqrt{s} = 1.02 \text{ GeV}, 55^\circ \leq \vartheta_{\mp} \leq 125^\circ$ | 455.85(1) | 455.73(1) | — | 0.030 |
| $\sqrt{s} = 3.5 \text{ GeV}, \vartheta_+ + \vartheta_- - \pi \leq 0.25 \text{ rad}$ | 35.20(2) | — | 35.181(5) | 0.050 |

★ Agreement well below 0.1%! ★

At BaBar (cross sections in nb)

By A. Hafner and A. Denig

| angular acceptance cuts | BabaYaga@NLO | BHWIDE | $\delta(\%)$ |
|---------------------------|--------------|-----------|--------------|
| $15^\circ \div 165^\circ$ | 119.5(1) | 119.53(8) | 0.025 |
| $40^\circ \div 140^\circ$ | 11.67(3) | 11.660(8) | 0.086 |
| $50^\circ \div 130^\circ$ | 6.31(3) | 6.289(4) | 0.332 |
| $60^\circ \div 120^\circ$ | 3.554(6) | 3.549(3) | 0.141 |

★ Agreement at the $\sim 0.1\%$ level! ★

Theoretical accuracy, comparisons with NNLO

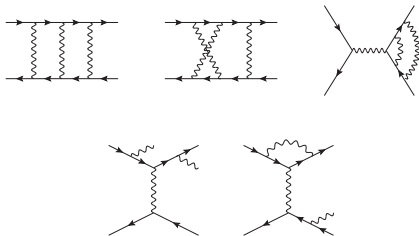
- NLO RC being included, the theoretical error starts at $\mathcal{O}(\alpha^2)$ (NNLO)
 - ↪ anyway large NNLO RC already included by h.o. exponentiation (and by $\mathcal{O}(\alpha)$ LL \times non-log-NLO)
- ★ The full set of NNLO QED corrections to Bhabha scattering has been calculated in the last years
- **BabaYaga@NLO** formulae can be truncated at $\mathcal{O}(\alpha^2)$ to be consistently and systematically compared with all the classes of NNLO corrections

$$\sigma^{\alpha^2} = \sigma_{\text{SV}}^{\alpha^2} + \sigma_{\text{SV,H}}^{\alpha^2} + \sigma_{\text{HH}}^{\alpha^2}$$

- $\sigma_{\text{SV}}^{\alpha^2}$: soft+virtual photonic corrections up to $\mathcal{O}(\alpha^2)$
 - ↪ compared with the corresponding available NNLO QED calculation
- $\sigma_{\text{SV,H}}^{\alpha^2}$: one-loop soft+virtual corrections to single hard bremsstrahlung
 - ↪ **presently** estimated relying on existing (partial) results
- $\sigma_{\text{HH}}^{\alpha^2}$: double hard bremsstrahlung
 - ↪ compared with the exact $e^+e^- \rightarrow e^+e^-\gamma\gamma$ cross section, to register **really negligible differences (at the 1×10^{-5} level)**

NNLO Bhabha calculations

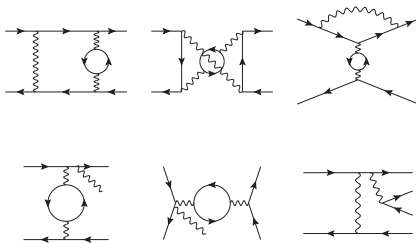
- **Photonic corrections** A. Penin, PRL **95** (2005) 010408 & Nucl. Phys. **B734** (2006) 185



- **Electron loop corrections**

R. Bonciani *et al.*, Nucl. Phys. **B701** (2004) 121 & Nucl. Phys. **B716** (2005) 280

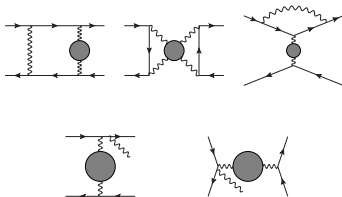
S. Actis, M. Czakon, J. Gluza and T. Riemann, Nucl. Phys. **B786** (2007) 26



- Heavy fermion and hadronic loops

R. Bonciani, A. Ferroglia and A. Penin, PRL **100** (2008) 131601
S. Actis, M. Czakon, J. Gluza and T. Riemann, PRL **100** (2008) 131602

J.H. Kühn and S. Uccirati, Nucl. Phys. **B806** (2009) 300



- One-loop soft+virtual corrections to single hard bremsstrahlung

S. Actis, P. Mastrolia and G. Ossola, Phys. Lett. **B682** (2010) 419

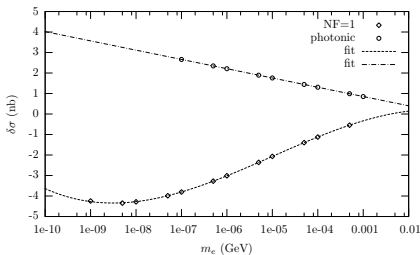
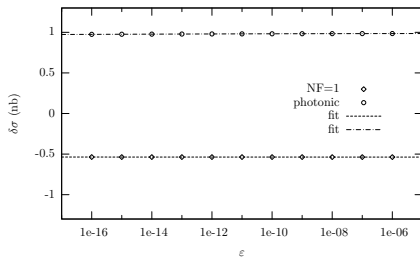


Comparison with NNLO calculation for $\sigma_{SV}^{\alpha^2}$

Using realistic cuts for luminosity @ KLOE

Comparison of $\sigma_{SV}^{\alpha^2}$ calculation of **BabaYaga@NLO** with

- Penin (photonic): function of the logarithm of the soft photon cut-off (left plot) and a fictitious electron mass (right plot)



★ differences are infrared safe, as expected

★ $\delta\sigma(\text{photonic})/\sigma_0 \propto \alpha^2 L$, as expected

- Numerically, for various selection criteria at the Φ and B factories

$$\sigma_{SV}^{\alpha^2}(\text{Penin}) - \sigma_{SV}^{\alpha^2}(\text{BabaYaga@NLO}) < 0.02\% \times \sigma_0$$

Lepton and hadron loops & pairs at NNLO

- The exact NNLO soft+virtual corrections and $2 \rightarrow 4$ matrix elements $e^+e^- \rightarrow e^+e^-(l^+l^-)$ [$l = e, \mu, \tau$], $e^+e^- \rightarrow e^+e^-(\pi^+\pi^-)$ are available
- Compared to the *approximation* in **BabaYaga@NLO**, using realistic luminosity cuts ($S_i \equiv \sigma_i^{\text{NNLO}}/\sigma_{\text{BY}}$)

| | \sqrt{s} | | σ_{BY} | $S_{e^+e^-}$ [%] | S_{lep} [%] | S_{had} [%] | S_{tot} [%] |
|-------|------------|--------|----------------------|------------------|---------------|---------------|---------------|
| KLOE | 1.020 | NNLO | | -3.935(4) | -4.472(4) | 1.02(2) | -3.45(2) |
| | | BB@NLO | 455.71 | -3.445(2) | -4.001(2) | 0.876(5) | -3.126(5) |
| BES | 3.650 | NNLO | | -1.469(9) | -1.913(9) | -1.3(1) | -3.2(1) |
| | | BB@NLO | 116.41 | -1.521(4) | -1.971(4) | -1.071(4) | -3.042(5) |
| BaBar | 10.56 | NNLO | | -1.48(2) | -2.17(2) | -1.69(8) | -3.86(8) |
| | | BB@NLO | 5.195 | -1.40(1) | -2.09(1) | -1.49(1) | -3.58(2) |
| Belle | 10.58 | NNLO | | -4.93(2) | -6.84(2) | -4.1(1) | -10.9(1) |
| | | BB@NLO | 5.501 | -4.42(1) | -6.38(1) | -3.86(1) | -10.24(2) |

- ★ The uncertainty due to lepton and hadron pair NNLO corrections is at the level of a few units in 10^{-4}

Carlone, Czyz, Gluza, Gunia, Montagna, Nicosini, Piccinini, Riemann *et al.*, JHEP **1107** (2011) 126

Error budget for Bhabha luminometry

main conclusion of the Luminosity Section of the WG Report

Putting the sources of uncertainties (in large-angle Bhabha) all together:

| Source of error (%) | Φ -factories | $\sqrt{s} = 3.5$ GeV | B -factories |
|--|-------------------|----------------------|----------------|
| $ \delta_{VP}^{err} $ [Jegerlehner] | 0.00 | 0.01 | 0.03 |
| $ \delta_{VP}^{err} $ [HMNT] | 0.02 | 0.01 | 0.02 |
| $ \delta_{SV,\alpha^2}^{err} $ | 0.02 | 0.02 | 0.02 |
| $ \delta_{HH,\alpha^2}^{err} $ | 0.00 | 0.00 | 0.00 |
| $ \delta_{SV,H,\alpha^2}^{err} $ | 0.05 | 0.05 | 0.05 |
| $ \delta_{pairs}^{err} $ | 0.03 | 0.016 | 0.03 |
| $ \delta_{total}^{err} $ linearly | 0.12 | 0.1 | 0.13 |
| $ \delta_{total}^{err} $ in quadrature | 0.07 | 0.06 | 0.06 |

- ★ The present error estimate appears to be rather robust and sufficient for high-precision luminosity measurements. It is comparable with that achieved for small-angle Bhabha luminosity monitoring at LEP/SLC
- For the experiments on top of and closely around the narrow resonances (J/ψ , Υ , ...), the accuracy quickly deteriorates, because of the differences between the predictions of independent $\Delta\alpha_{had}^{(5)}(q^2)$ parameterizations and/or their intrinsic error [see extra slides]

Conclusions

- ★ In the last 15(+) years **BabaYaga/BabaYaga@NLO** has been developed for high-precision luminometry at flavour factories

- ★ It simulates QED processes

$$\hookrightarrow e^+e^- \rightarrow e^+e^- (+n\gamma)$$

$$\hookrightarrow e^+e^- \rightarrow \mu^+\mu^- (+n\gamma)$$

$$\hookrightarrow e^+e^- \rightarrow \gamma\gamma (+n\gamma)$$

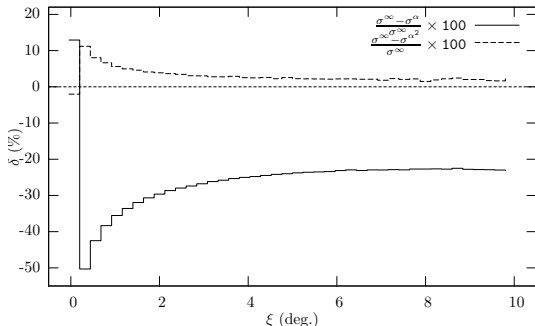
with **multiple-photon emission in a QED Parton Shower framework, matched with exact NLO matrix elements**

- ★ **A theoretical precision at the 0.5×10^{-3} level is achieved** (at least for Bhabha), with a systematic comparison to independent calculations/codes and assessing the size of missing higher-order corrections
- ★ Improving the accuracy of QED processes would imply the inclusion of exact **full 2-loop corrections**, which is (in principle) feasible with a non trivial effort, if needed by experiments

EXTRAS

Resummation beyond α^2

- ★ with a complete 2-loop generator at hand, (leading-log) resummation beyond α^2 can be neglected?

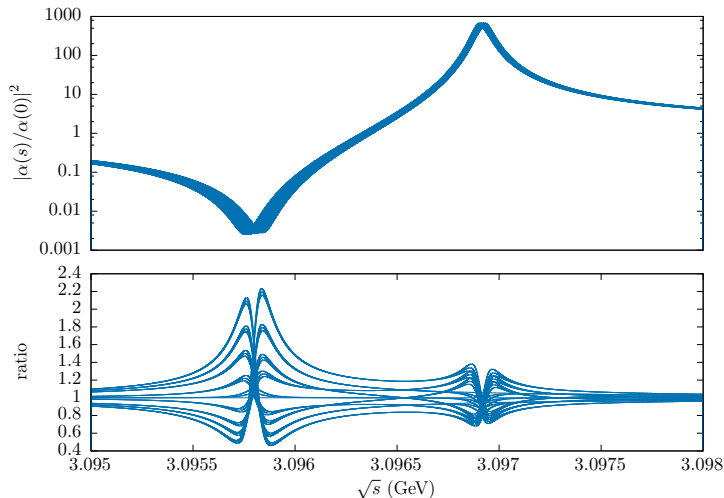


Impact of α^2 (solid line) and resummation of higher order ($\geq \alpha^3$) (dashed line) corrections on the **acollinearity distribution**

- ★ Resummation beyond α^2 still important!

Around J/Ψ

- s -channel diagram(s) $\propto |\alpha(s)|^2$
- e.g. HLMNT (Teubner et al.) VP routine, varying $M_{J/\Psi}$, $\Gamma_{J/\Psi}$, $\Gamma_{J/\Psi}^{ee}$ within PDG values



BabaYaga for dark photon searches at low-energies

- From normalization to “discovery” tool \rightarrow

$$e^+e^- \rightarrow \gamma + \gamma^{\text{dark}} \rightarrow l^+l^-\gamma (n\gamma)$$

- dark photon (U -boson) production via **radiative return, including ISR** (with LL collinear structure-functions)

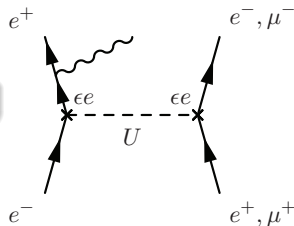
- Implemented model:

“secluded” $U(1)_S$ symmetry with a **light vector gauge field**, heavy DM, complex Higgs field for $U(1)_S$ SSB

\leftrightarrow coupling to SM fields through $\gamma^{\text{dark}}/\gamma$ mixing

$$\mathcal{L}_{mix} = \frac{\epsilon}{2} F_{\gamma^{\text{dark}}}^{\mu\nu} F_{\mu\nu}^{\gamma}$$

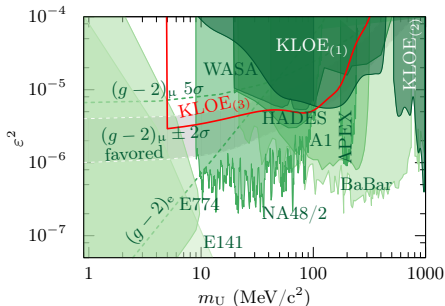
- extremely weak signal \rightarrow control of background mandatory



KLOE-2 results

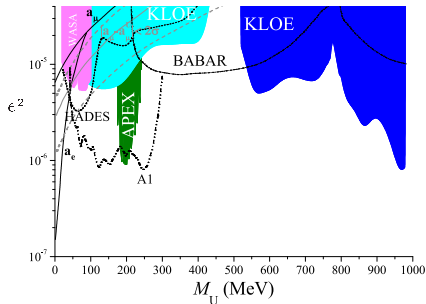
- **BabaYaga** with dark-photon production used in KLOE-2 analyses for exclusion plots

$$e^+e^- \rightarrow \gamma U, U \rightarrow e^+e^-$$



A. Anastasi *et al.*, Phys. Lett. B **750** (2015) 633

$$e^+e^- \rightarrow \gamma U, U \rightarrow \mu^+\mu^-$$



D. Babusci *et al.* Phys. Lett. B **736** (2014) 459