

Theory of hadronic molecules applied to the XYZ states

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Key reference: Review article

F. K. Guo, C. Hanhart, U.-G. Meißner, Q. Wang, Q. Zhao and
B. S. Zou, “Hadronic molecules”, arXiv:1705.00141 [hep-ph]

Hadronic Molecules

- are few-hadron states, **bound by the strong force**
- **do exist**: light nuclei.
e.g. **deuteron as pn & hypertriton as Λd bound state**
- are located typically **close to relevant continuum threshold**;

e.g., for $E_B = m_1 + m_2 - M$

$$\triangleright E_B^{\text{deuteron}} = 2.22 \text{ MeV}$$

$$\triangleright E_B^{\text{hypertriton}} = (0.13 \pm 0.05) \text{ MeV (to } \Lambda d)$$

- **can be identified in observables (Weinberg compositeness)**:

$$\frac{g_{\text{eff}}^2}{4\pi} = \frac{4M^2\gamma}{\mu}(1-\lambda^2) \rightarrow a = -2 \left(\frac{1-\lambda^2}{2-\lambda^2} \right) \frac{1}{\gamma}; \quad r = - \left(\frac{\lambda^2}{1-\lambda^2} \right) \frac{1}{\gamma}$$

where $(1 - \lambda^2)$ = **probability to find molecular component** in bound state wave function

Are there mesonic molecules?

Properties of molecular states

→ Potential the strongest in *S*-waves

→ Potential i.g. contains short and long ranged contributions

Filin et al., PRL 105 (2010) 019101

→ Interaction channel dependent

▷ isovector meson exchanges give

$$\langle \vec{\tau}_{(1)} \cdot \vec{\tau}_{(2)} \rangle = 2I(I + 1) - 3$$

Thus: Either $I = 1$ or $I = 0$ states (not both) for given J^{PC} ,
if, e.g., ρ -exchange or π -exchange significant

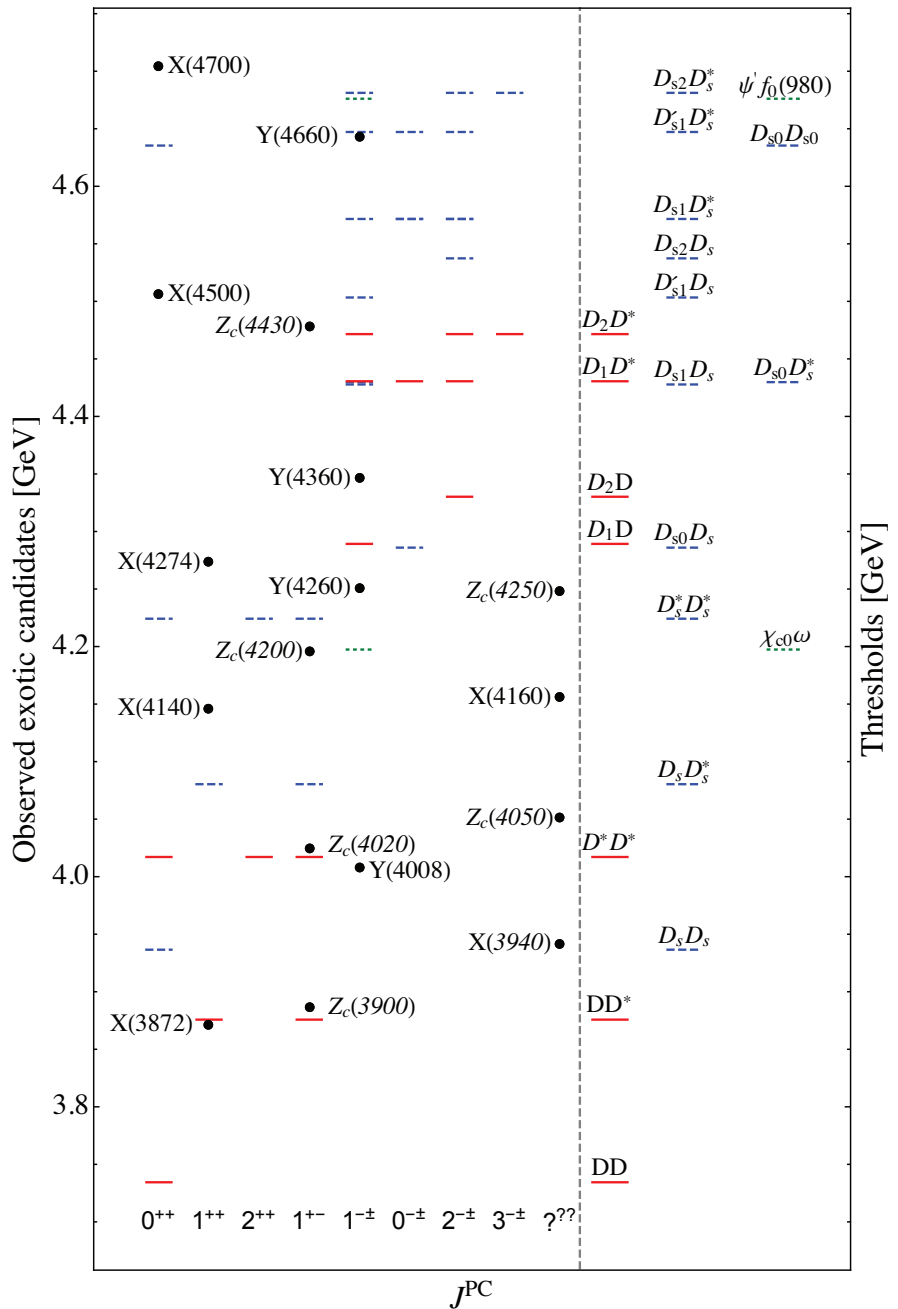
Voloshin & Okun, JETPL 23 (1976) 333; Tornqvist, PRL 67 (1991) 556.

▷ Switching C also induces sign change

▷ Potentially large coupled channel effects

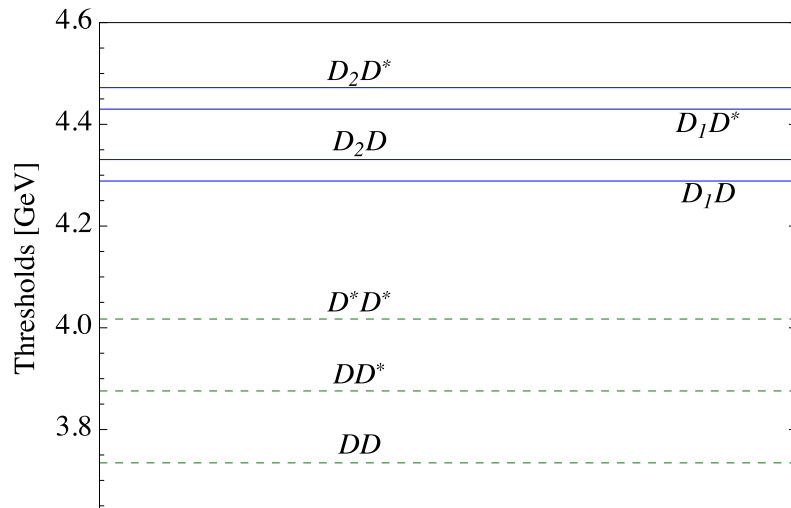
→ Interaction particle dependent (no $\pi D\bar{D}$ vertex)

Here: Heavy Quarkonium Sector



- All exotic candidates above open flavor thresholds
 - Many (not all) states near *S*-wave thresholds of narrow states Filin et al., PRL 105, 019101 (2010)
Guo et al., PRD84, 014013 (2011)
 - States not near all those thresholds
 - Lightest negative parity exotic (*Y*(4260)) significantly heavier than lightest positive parity exotics (*X*(3872) & *Z_c*(3900))
- ... does *Y*(4008) exist?

Example: $1/2^-$ multiplet $\{D, D^*\}$ and $3/2^+$ multiplet $\{D_1, D_2\} \rightarrow$



$3^-_{\pm}: D^* D_2$
 $0^-_{\pm}: D^* D_1$
 $2^-_{\pm}: D^* D_1 - D^* D_2 - DD_2$
 $1^-_{\pm}: DD_1 - D^* D_1 - D^* D_2$ ($Y(4260), Y(4360)$ ($I=0$))
 $2^{++}: D^* D^*$
 $1^{++}: DD^*$ ($X(3872)$ ($I=0$))
 $1^{+-}: DD^* - D^* D^*$ ($Z_c(3900)^+, Z_c(4020)^+$ ($I=1$))
 $0^{++}: DD - D^* D^*$;

\rightarrow **Explains** mass gap between $J^P = 1^+$ and 1^- states:

$$M_{Y(4260)} - M_{X(3872)} = 388 \text{ MeV} \simeq M_{D_1(2420)} - M_{D^*} = 410 \text{ MeV}$$

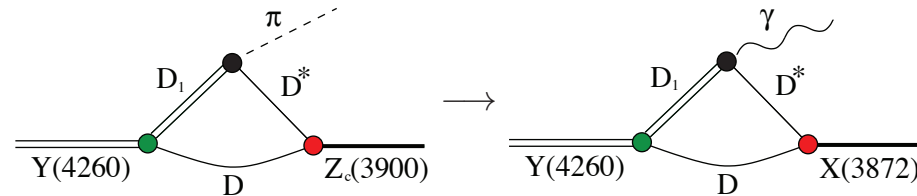
\rightarrow **Predicts**, e.g., $M(0^-) - M(1^-) \simeq M_{D^*} - M_D \simeq +100 \text{ MeV}$,
if it exists

c.f. for hadrocharmonium: $M(0^-) - M(1^-) \simeq -100 \text{ MeV}$

Cleven et al., PRD 92 (2015) 014005

→ Natural explanation for $Y(4260) \rightarrow \pi Z_c(3900)$ and

Wang, C. H., Zhao, PRL111 (2013) no.13, 132003



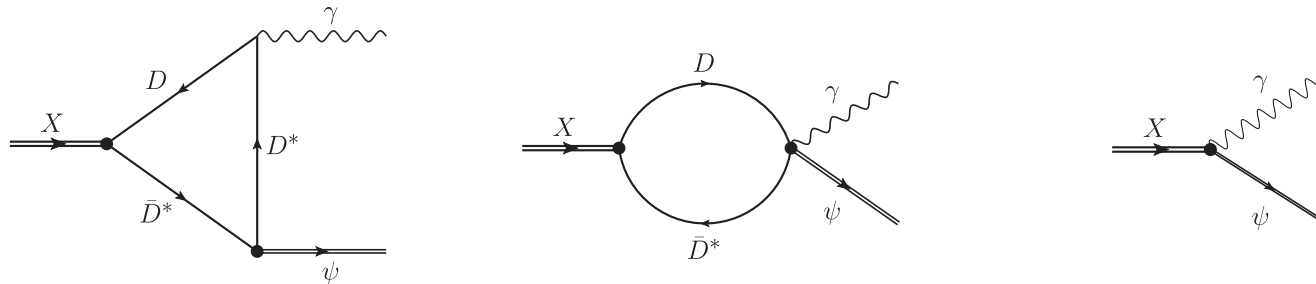
prediction of $Y(4260) \rightarrow \gamma X(3872)$

Guo et al., PLB 725 (2013) 127-133

confirmed at BESIII Ablikim et al. PRL 112 (2014), 092001

→ Not all observables sensitive to molecular component!

e.g. $X(3872) \rightarrow \gamma \psi(nS)$ has leading order counter term



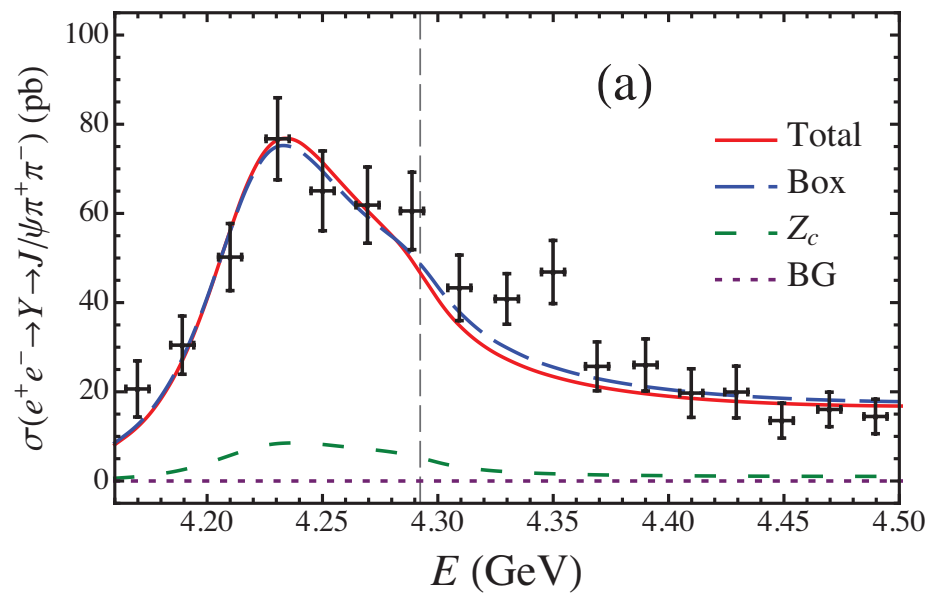
In particular:
$$R = \frac{\mathcal{B}(X(3872) \rightarrow \gamma \psi')}{\mathcal{B}(X(3872) \rightarrow \gamma J/\psi)} \simeq 2.5$$

Aaij et al. [LHCb],
NPB 886 (2014) 665

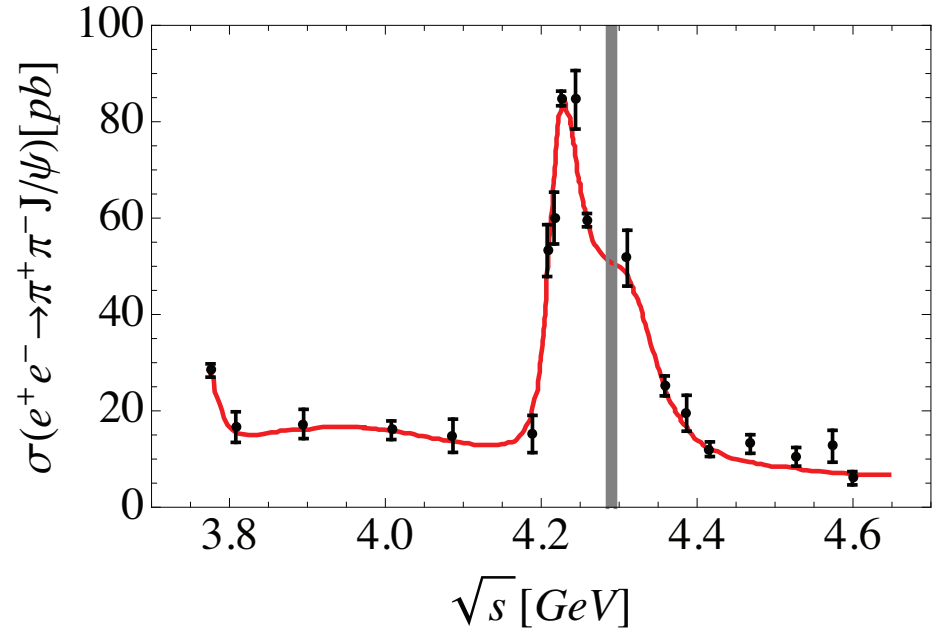
can be easily described within molecular approach

Guo et al., PLB 742 (2015) 394

Lineshapes of $Y(4260)$



Cleven et al., PRD90 (2014) 074039

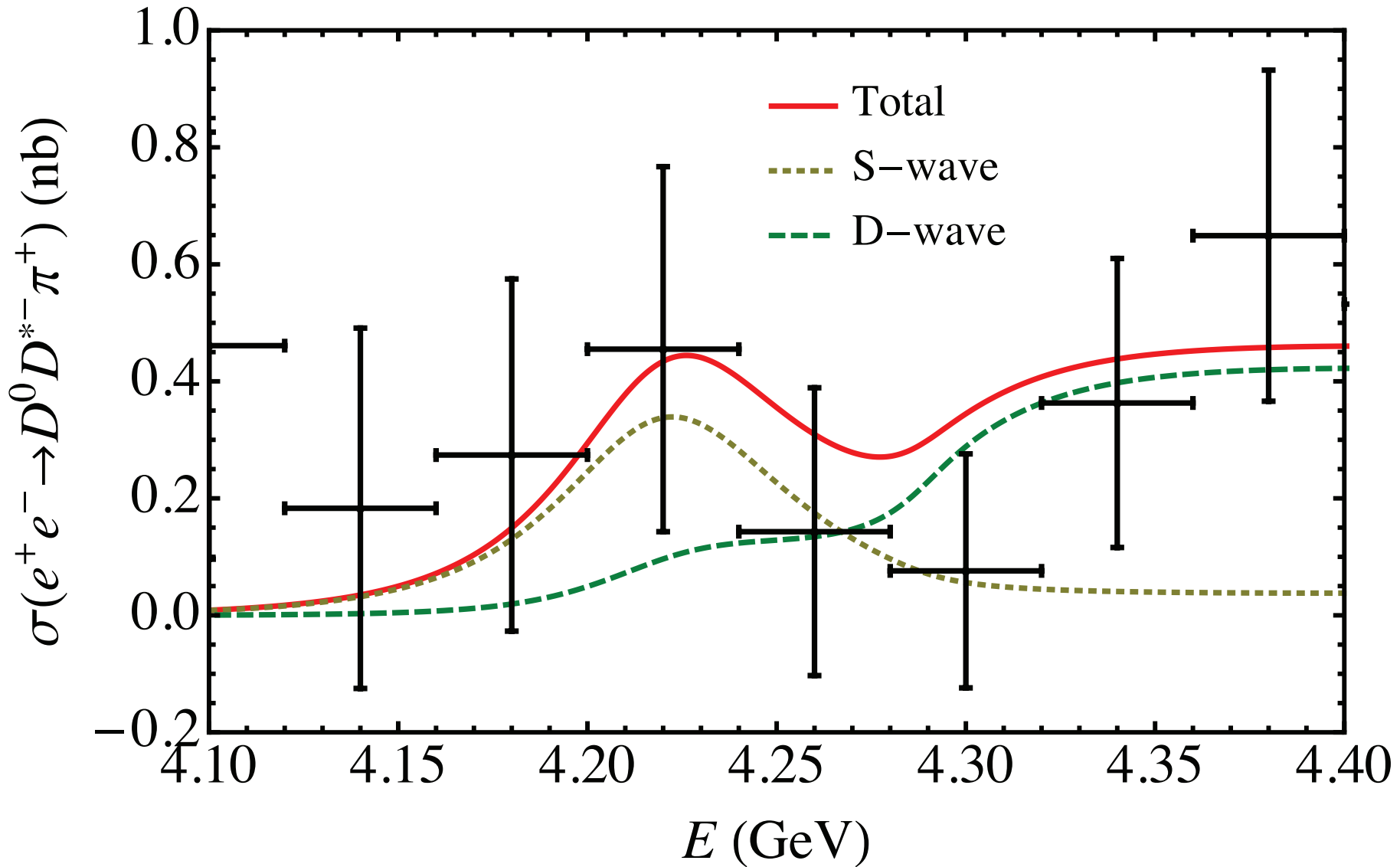
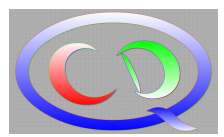


talk by Zhentian SUN for BESIII this morning

IF the $Y(4260)$ were a $D_1 \bar{D}$ molecule

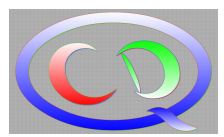
- it **MUST** have a **large coupling to this channel**
- this must have an **impact on lineshapes**

$$Y(4260) \rightarrow D_1 \bar{D} \rightarrow [D^* \pi] \bar{D}$$

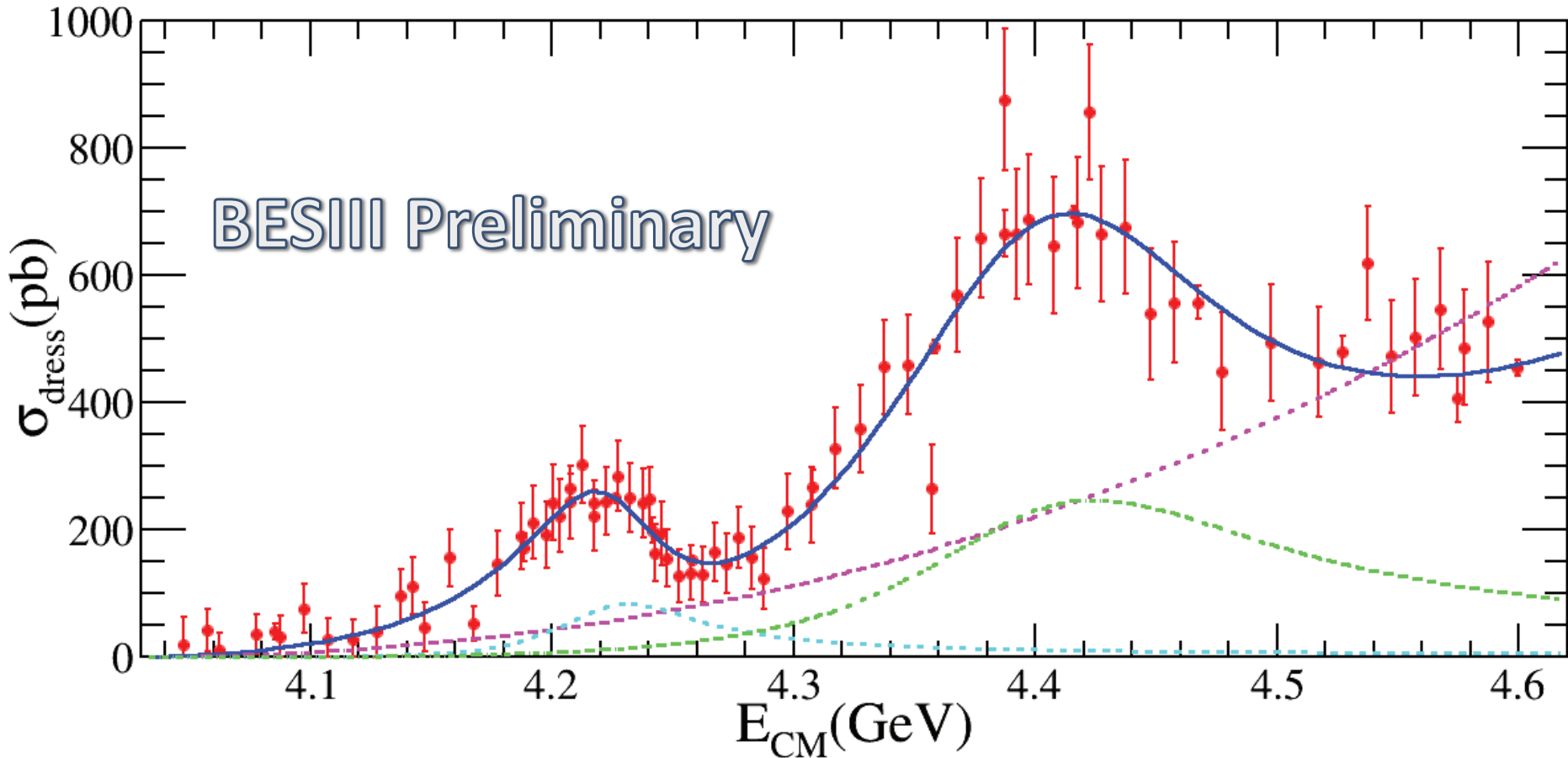


Cleven et al., PRD90 (2014) 074039; Data: Belle, PRD80 (2009) 091101

$$Y(4260) \rightarrow D_1 \bar{D} \rightarrow [D^* \pi] \bar{D}$$



Soon there will be new data from BESIII



talk by Zhentian SUN for BESIII this morning

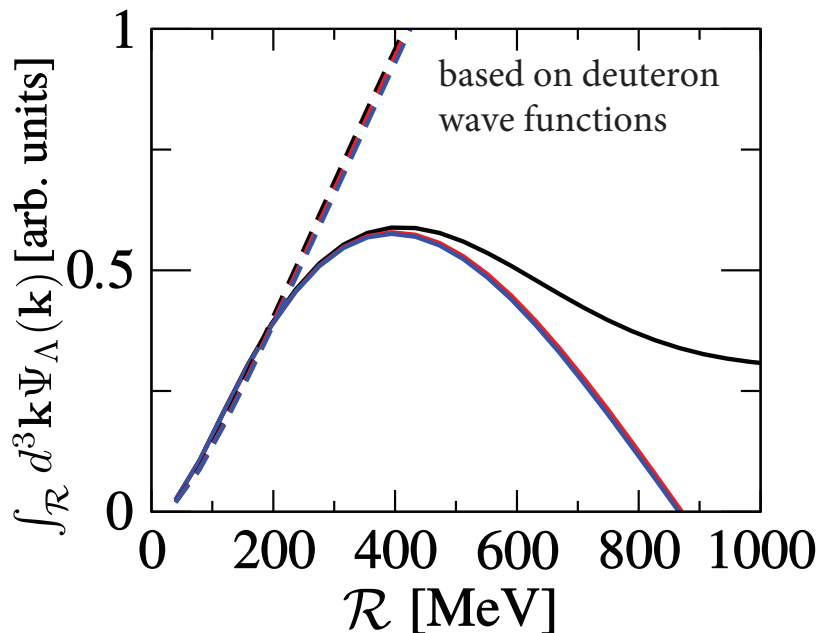
... that confirm the general features!

Strong support for molecular picture of $Y(4260)$

Production at high P_T

$$\begin{aligned} & \sigma(\bar{p}p \rightarrow X) \\ & \sim \left| \int d^3\mathbf{k} \langle X | D^0 \bar{D}^{*0}(\mathbf{k}) \rangle \langle D^0 \bar{D}^{*0}(\mathbf{k}) | \bar{p}p \rangle \right|^2 \\ & \simeq \left| \int_{\mathcal{R}} d^3\mathbf{k} \langle X | D^0 \bar{D}^{*0}(\mathbf{k}) \rangle \langle D^0 \bar{D}^{*0}(\mathbf{k}) | \bar{p}p \rangle \right|^2 \\ & \leq \int_{\mathcal{R}} d^3\mathbf{k} |\Psi(\mathbf{k})|^2 \int_{\mathcal{R}} d^3\mathbf{k} |\langle D^0 \bar{D}^{*0}(\mathbf{k}) | \bar{p}p \rangle|^2 \\ & \leq \int_{\mathcal{R}} d^3\mathbf{k} |\langle D^0 \bar{D}^{*0}(\mathbf{k}) | \bar{p}p \rangle|^2, \end{aligned}$$

Bignamini et al., PRL 103 (2009) 162001



\mathcal{R} must be large enough to saturate wave function

Bignamini et al.:

$$\mathcal{R} \sim \sqrt{m E_b} \sim 40 \text{ MeV}$$

→ Test on deuteron

Albaladejo et al. subm. to PRL

One finds: $\mathcal{R} \sim 400 \text{ MeV}$ using Herwig (Pythia)

$$\mathcal{R} \sim 60 \text{ MeV} \rightarrow \sigma_X \sim 0.1(0.04) \text{ nb}$$

$$\mathcal{R} \sim 300 \text{ MeV} \rightarrow \sigma_X \sim 13(4) \text{ nb}^\dagger$$

$$\mathcal{R} \sim 600 \text{ MeV} \rightarrow \sigma_X \sim 55(15) \text{ nb}^\dagger$$

†: $D^+ D^-$ channel included

$$\text{vs } \sigma_{\text{exp}}^{\text{CMS}} \sim 13 - 39 \text{ nb} \rightarrow$$

fully consistent!

- So far large bulk of **properties of XYZ states consistent with hadronic molecule picture** Guo et al., arXiv:1705.00141 [hep-ph]
- Spin symmetry violations **different for different scenarios** (more **pronounced for negative parity** states) Cleven et al., PRD 92 (2015) 014005
 - ▷ Z_b spin partners **sensitive to input parameters**
 - ▷ Detailed modeling calls for **inclusion of π exchange**
- To disentangle compact tetraquarks from hadronic molecules, **existence of $Y(4008)$ must be clarified**
- We need information for **various quantum numbers for both bottomonia and charmonia**

Thanks a lot for your attention