



Tel Aviv University



# Recent issues in heavy quark spectroscopy

Marek Karliner  
Tel Aviv University

PHI2PSI, Mainz, June 28, 2017

hadrons w. heavy quarks are *much simpler*:

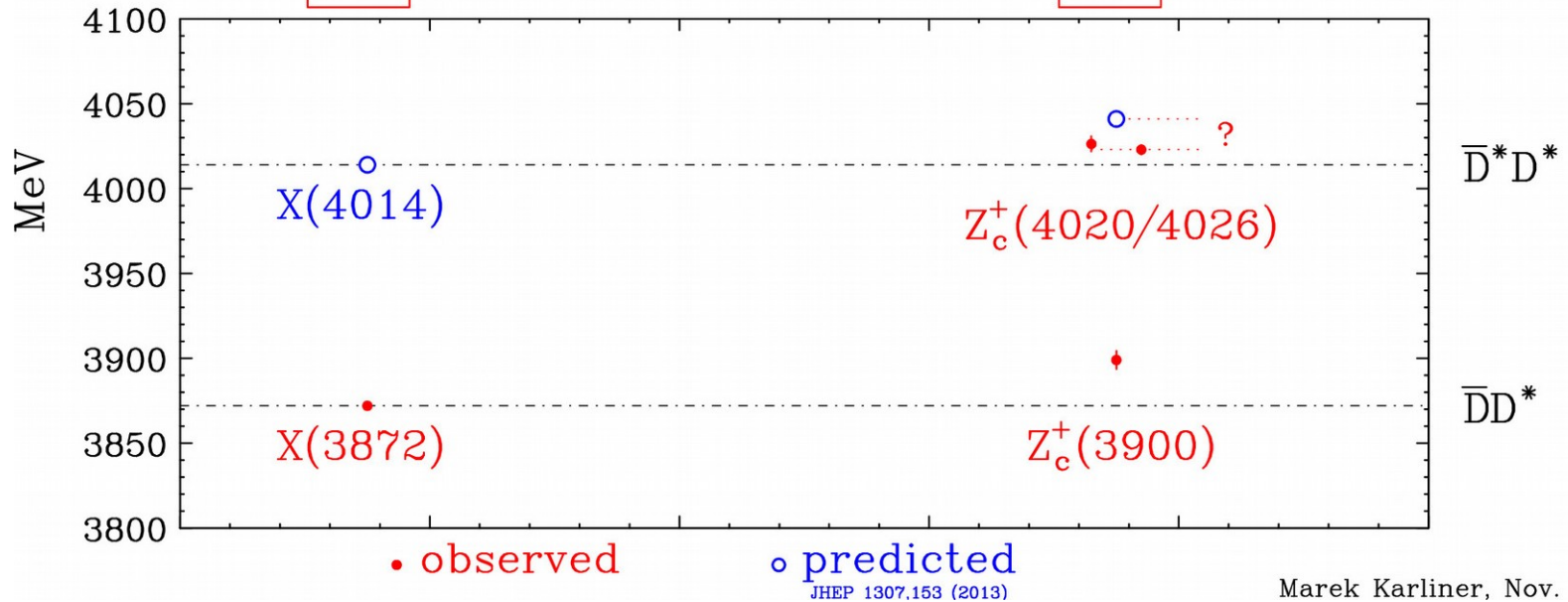
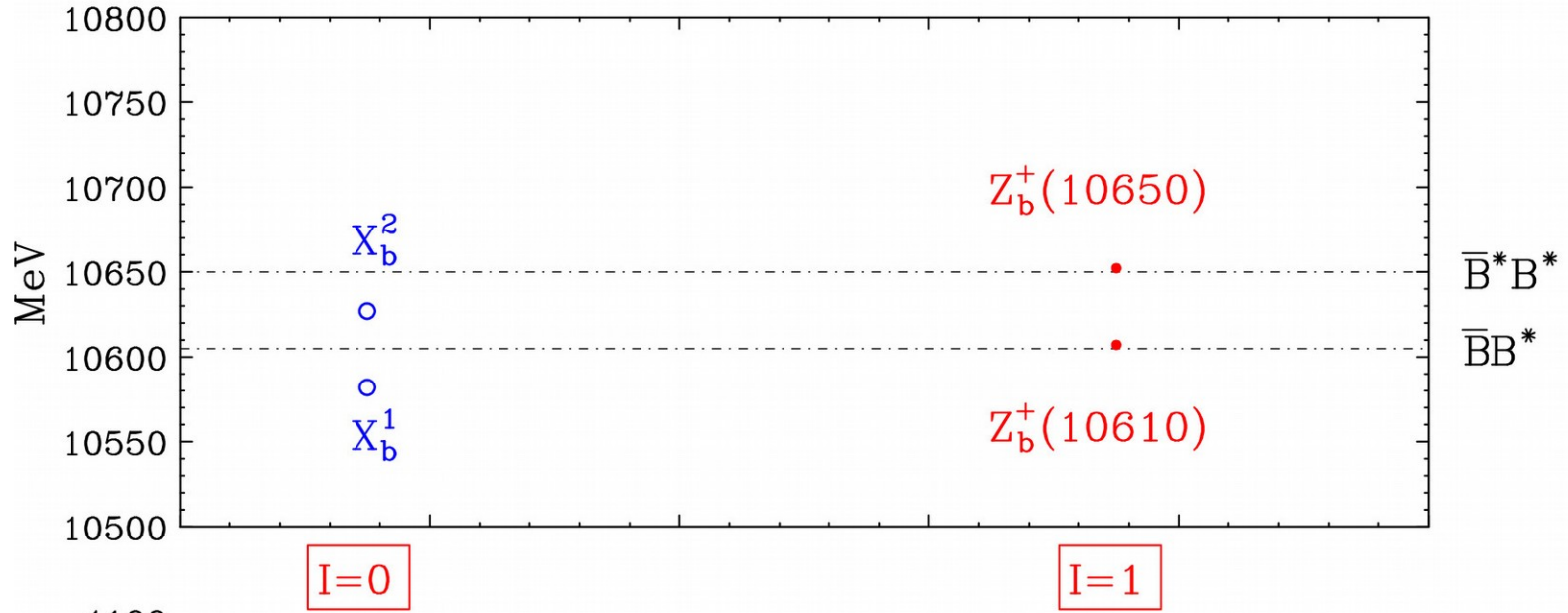
- heavy quarks almost static
- smaller spin-dep. interaction  $\propto 1/m_Q$
- key to accurate prediction of  $b$  quark baryons

## 5 narrow exotic states close to meson-meson thresholds

state	mass MeV	width MeV	$\bar{Q}Q$ decay mode	phase space MeV	nearby threshold	$\Delta E$ MeV
$X(3872)$	3872	$< 1.2$	$J/\psi \pi^+ \pi^-$	495	$\bar{D}D^*$	$< 1$
$Z_b(10610)$	10608	21	$\gamma \pi$	1008	$\bar{B}B^*$	$2 \pm 2$
$Z_b(10650)$	10651	10	$\gamma \pi$	1051	$\bar{B}^*B^*$	$2 \pm 2$
$Z_c(3900)$	3900	24 – 46	$J/\psi \pi$	663	$\bar{D}D^*$	24
$Z_c(4020)$	4020	8 – 25	$J/\psi \pi$	783	$\bar{D}^*D^*$	6
$\times$					$\bar{D}D$	
$\times$					$\bar{B}B$	

- masses and widths approximate
- quarkonium decays mode listed have max phase space
- offset from threshold for orientation only, v. sensitive to exact mass

# exotic heavy quarkonia vs. two meson thresholds



Marek Karliner, Nov. 2013

The  $Z_Q$  resonances decay into

$\bar{Q}Q\pi$

$\implies$  must contain both  $\bar{Q}Q$  and  $\bar{q}q$ ,  $q = u, d$

$\implies$  manifestly exotic

$X(3872)$ : a mixture of  $\bar{D}D^*$  and  $\chi_{c1}(2P)$

# tetraquarks or a “hadronic molecules” ?

The molecule idea has a long history:

Voloshin Okun (1976),

de Rujula, Georgi Glashow (1977)

Tornqvist, Z. Phys. C61,525 (1993)

all states close to two-meson thresholds

despite large phase space (hundreds of MeV)

narrow widths in decays into  $\bar{Q}Q\pi$

$\implies$  very small overlap of wave functions:  $|\langle i|f\rangle|^2 \ll 1$

strong hint in favor of molecular interpretation

Belle, PRL 116, 212001 (2016):

$$\frac{\Gamma(Z_b(10610) \rightarrow \bar{B}B)}{\Gamma(Z_b(10610) \rightarrow \Upsilon(1S)\pi)} \approx \frac{86\%}{0.54\%} = \mathcal{O}(100)$$

despite 1000 MeV of phase space

for  $\Upsilon(1S)\pi$  vs few MeV for  $\bar{B}B^*$  !

overlap of  $Z_c$  wave function with  $J/\psi\pi$

much smaller than with  $\bar{D}D \Rightarrow$  indicates an extended object

also

$$\frac{\Gamma(Z_c(3885) \rightarrow \bar{D}D^*)}{\Gamma(Z_c(3885) \rightarrow J/\psi\pi)} = 6.2 \pm 1.1 \pm 2.7$$

(BESIII/Yu-Ping Guo @EQCD, Jinan 6/2015)

BR-s of  $X(3872)$  to  $J/\psi$  and pions vs “fall apart” mode  $\bar{D}D^*$

$\text{BR}(\bar{D}D^*) \sim 10 \times \text{BR}(J/\psi + X)$

despite  $-1$  MeV vs  $400-500$  MeV phase space

Citation: K.A. Olive *et al.* (Particle Data Group), *Chin. Phys.* **C38**, 090001 (2014) (URL: <http://pdg.lbl.gov>)

## $X(3872)$ DECAY MODES

	Mode	Fraction ( $\Gamma_i/\Gamma$ )
$\Gamma_1$	$e^+ e^-$	
$\Gamma_2$	$\pi^+ \pi^- J/\psi(1S)$	$> 2.6 \%$
$\Gamma_3$	$\rho^0 J/\psi(1S)$	
$\Gamma_4$	$\omega J/\psi(1S)$	$> 1.9 \%$
$\Gamma_5$	$D^0 \bar{D}^0 \pi^0$	$> 32 \%$
$\Gamma_6$	$\bar{D}^{*0} D^0$	$> 24 \%$
-		



## 4 pieces of experimental evidence in support of molecular interpretation of $Z_Q$ and $X(3872)$ :

1. masses near thresholds and  $J^P$  of S-wave
2. narrow width despite very large phase space
3.  $\text{BR}(\text{fall apart mode}) \gg \text{BR}(\text{quarkonium} + X)$
4. no states which require binding through 3 pseudoscalar coupling

## binding two hadrons through $\pi$ exchange<sup>†</sup>:

explains conspicuous absence of  $\bar{D}D$  and  $\bar{B}B$  resonances

e.g.  $\bar{D}D$  resonance through  $\pi$  would require  $DD\pi$  vertex. But 3-pseudoscalar vertex is forbidden in QCD by parity conservation.

another way to understand why no  $D \rightarrow D\pi$ :  
 $J^P = 0^-$ , so parity demands  $D \rightarrow D\pi$  in  $P$ -wave;  
but  $D$  and  $\pi$  in  $P$ -wave give  $J = 1$

---

$\pi$  = shorthand for a light pseudoscalar, not necessarily physical pion

Heavy-light  $Q\bar{q}$  mesons have  $l = 1$

$\Rightarrow$  they couple to pions;  $m_{Q\bar{q}} \gg m_N$

$\Rightarrow$  deuteron-like meson-meson bound states, “deusons”

pion exchange  $\rightarrow$  no  $\bar{D}D$ , only  $\bar{D}D^*$ ,  $\bar{D}^*D^*$

crucial test:  $X(J^P = 0^{++}) \xrightarrow{?} J/\psi\gamma$  near  $\bar{D}D$

$\bar{D}D^*$  ( $l = 0$ ) at threshold:  $X(3872)$  !

$S$ -wave  $\rightarrow J^P = 1^+$ , confirmed by BESIII

$l = 1$ :  $3\times$  weaker than  $l = 0$

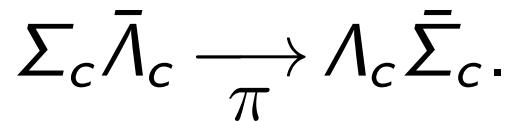
$\Rightarrow l = 1$  well above threshold

What about  $\bar{B}B^*$  analogue ?....

necessary\* conditions for existence of a resonance

(a) both hadrons heavy, as  $E_{kin} \sim 1/\mu_{RED}$

(b) both couple to pions;  
one of them can have  $l = 0$ , e.g.



(c) spin & parity which allow the state  
go into itself under one  $\pi$  exchange

(d)  $\Gamma(h_1) + \Gamma(h_2) \ll \Gamma(\text{molecule})$

---

\* may not be sufficient

the binding mechanism can in principle  
apply to any two heavy hadrons  
which couple to isospin  
and satisfy these conditions,  
*be they mesons or baryons*

doubly-heavy hadronic molecules:

most likely candidates with  $Q\bar{Q}'$ ,  $Q = c, b$ ,  $\bar{Q}' = \bar{c}, \bar{b}$ :

$D\bar{D}^*$ ,  $D^*\bar{D}^*$ ,  $D^*B^*$ ,  $\bar{B}B^*$ ,  $\bar{B}^*B^*$ ,

$\Sigma_c\bar{D}^*$ ,  $\Sigma_c B^*$ ,  $\Sigma_b\bar{D}^*$ ,  $\Sigma_b B^*$ , **the lightest of new kind**

$\Sigma_c\bar{\Sigma}_c$ ,  $\Sigma_c\bar{\Lambda}_c$ ,  $\Sigma_c\bar{\Lambda}_b$ ,  $\Sigma_b\bar{\Sigma}_b$ ,  $\Sigma_b\bar{\Lambda}_b$ , and  $\Sigma_b\bar{\Lambda}_c$ .

$c\bar{c}$  and  $b\bar{b}$  states decay strongly to  $\bar{c}c$  or  $\bar{b}b$  and  $\pi$ -(s)

$b\bar{c}$  and  $c\bar{b}$  states decay strongly to  $B_c^\pm$  and  $\pi$ -(s)

$QQ'$  candidates – dibaryons:

$\Sigma_c\Sigma_c$ ,  $\Sigma_c\Lambda_c$ ,  $\Sigma_c\Lambda_b$ ,  $\Sigma_b\Sigma_b$ ,  $\Sigma_b\Lambda_b$ , and  $\Sigma_b\Lambda_c$ .

prediction of doubly heavy baryon with hidden charm:

$$\Sigma_c \bar{D}^* \equiv \Theta_{\bar{c}c}, \quad m_{\Theta_{\bar{c}c}} \approx 4460 \text{ MeV},$$

possible decay mode:  $\Theta_{cc} \rightarrow J/\psi p$

$(S_1 \cdot S_2) (l_1 \cdot l_2)$  interaction:  $l = 1/2 \rightarrow J = 3/2$

S-wave  $\rightarrow J^P = 3/2^-$

small overlap of molecular state with  $J/\psi p$

$\Rightarrow$  narrow width  $\lesssim$  few tens of MeV

despite  $> 400$  MeV phase space

$\Theta_{\bar{c}c}$  minimal quark content:  $\bar{c}c uud$

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$\Theta_{\bar{c}c}$  minimal quark content:  $\bar{c}c uud \equiv P_c(4450)$

a molecule, not a tightly-bound pentaquark



## Thresholds for $Q\bar{Q}'$ molecular states

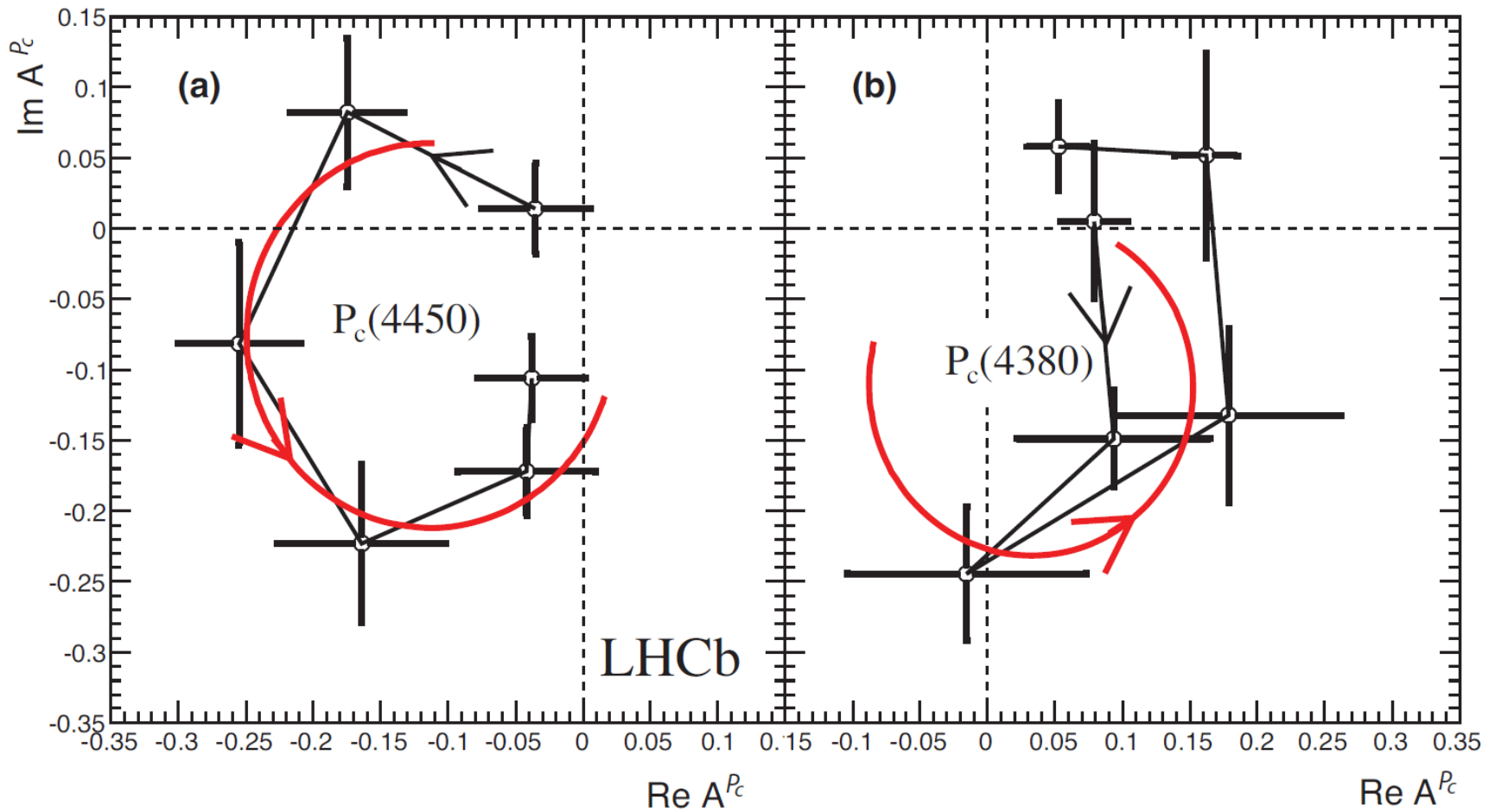
Channel	Minimum isospin	Minimal quark content <sup>a,b</sup>	Threshold (MeV) <sup>c</sup>	Example of decay mode
$D\bar{D}^*$	0	$c\bar{c}q\bar{q}$	3875.8	$J/\psi \pi\pi$
$D^*\bar{D}^*$	0	$c\bar{c}q\bar{q}$	4017.2	$J/\psi \pi\pi$
$D^*B^*$	0	$c\bar{b}q\bar{q}$	7333.8	$B_c^+ \pi\pi$
$\bar{B}B^*$	0	$b\bar{b}q\bar{q}$	10604.6	$\Upsilon(nS)\pi\pi$
$\bar{B}^*B^*$	0	$b\bar{b}q\bar{q}$	10650.4	$\Upsilon(nS)\pi\pi$
$\Sigma_c\bar{D}^*$	1/2	$c\bar{c}qqq'$	4462.4	$J/\psi p$
$\Sigma_c B^*$	1/2	$c\bar{b}qqq'$	7779.5	$B_c^+ p$
$\Sigma_b\bar{D}^*$	1/2	$b\bar{c}qqq'$	7823.0	$B_c^- p$
$\Sigma_b B^*$	1/2	$b\bar{b}qqq'$	11139.6	$\Upsilon(nS)p$
$\Sigma_c\bar{\Lambda}_c$	1	$c\bar{c}qq' \bar{u}\bar{d}$	4740.3	$J/\psi \pi$
$\Sigma_c\bar{\Sigma}_c$	0	$c\bar{c}qq' \bar{q}\bar{q}'$	4907.6	$J/\psi \pi\pi$
$\Sigma_c\bar{\Lambda}_b$	1	$c\bar{b}qq' \bar{u}\bar{d}$	8073.3 <sup>d</sup>	$B_c^+ \pi$
$\Sigma_b\bar{\Lambda}_c$	1	$b\bar{c}qq' \bar{u}\bar{d}$	8100.9 <sup>d</sup>	$B_c^- \pi$
$\Sigma_b\bar{\Lambda}_b$	1	$b\bar{b}qq' \bar{u}\bar{d}$	11433.9	$\Upsilon(nS)\pi$
$\Sigma_b\bar{\Sigma}_b$	0	$b\bar{b}qq' \bar{q}\bar{q}'$	11628.8	$\Upsilon(nS)\pi\pi$

<sup>a</sup>Ignoring annihilation of quarks.

<sup>b</sup>Plus other charge states when  $I \neq 0$ .

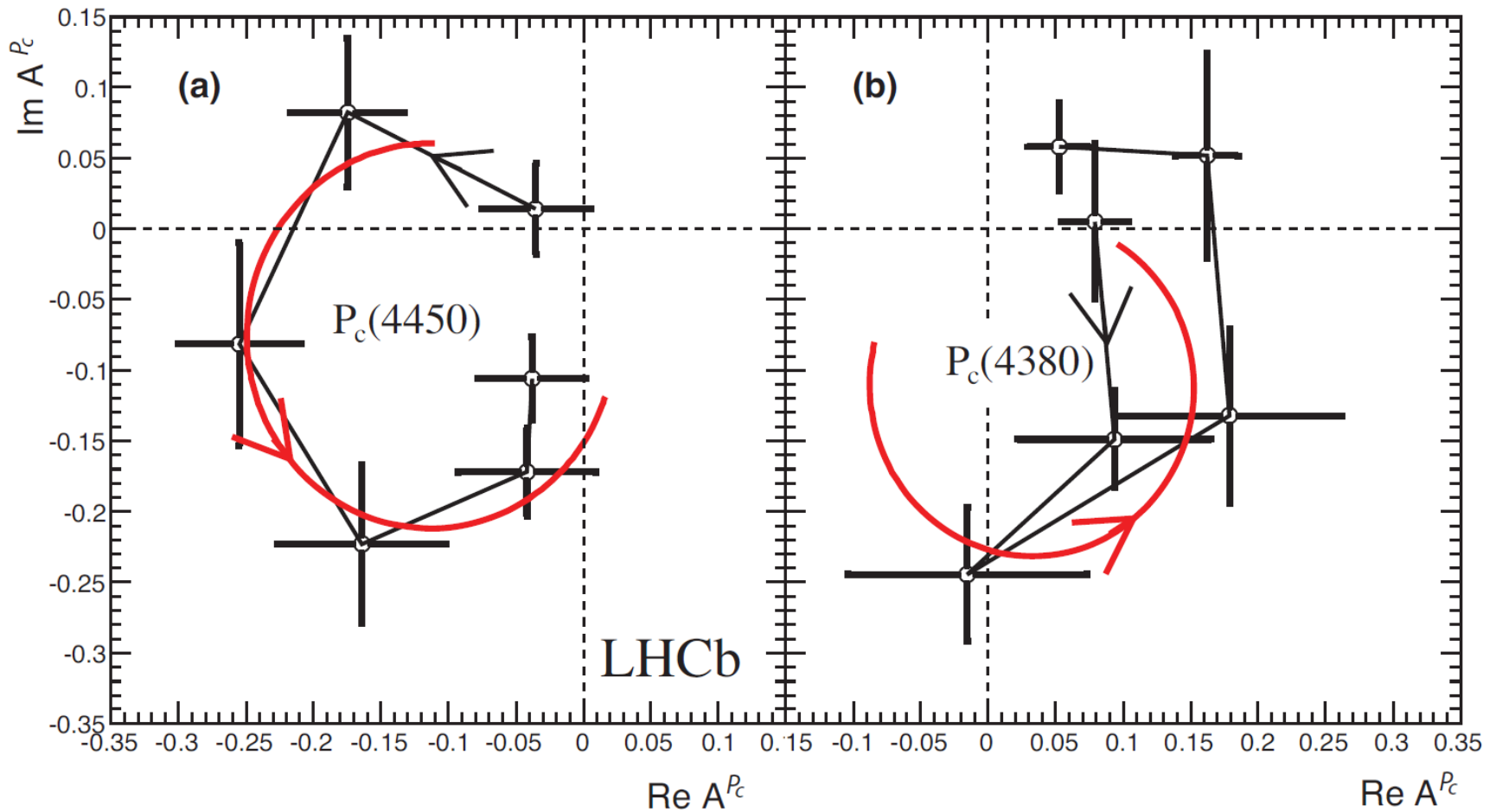
<sup>c</sup>Based on isospin-averaged masses.

<sup>d</sup>Thresholds differ by 27.6 MeV.



$P_c(4450)$ : predicted,  
 narrow:  $\Gamma = 39 \pm 5 \pm 19$ ,  
 10 MeV from  $\Sigma_c \bar{D}^*$  threshold  
 perfect Argand plot: a molecule

$P_c(4380)$ : not predicted,  
 wide:  $\Gamma = 205 \pm 18 \pm 86$  MeV,  
 Argand plot not resonance-like  
 ???



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 ???

**$P_c(4450)$  might be just the first of many “heavy deuterons”**

The narrow width, 39 MeV, is a problem for pentaquark interpretation, given the large phase space of 400 MeV

$$\Gamma (P_c(4450) \rightarrow J/\psi p) = \left| \langle P_c(4450) | J/\psi p \rangle \right|^2 \times (\text{phase space})$$

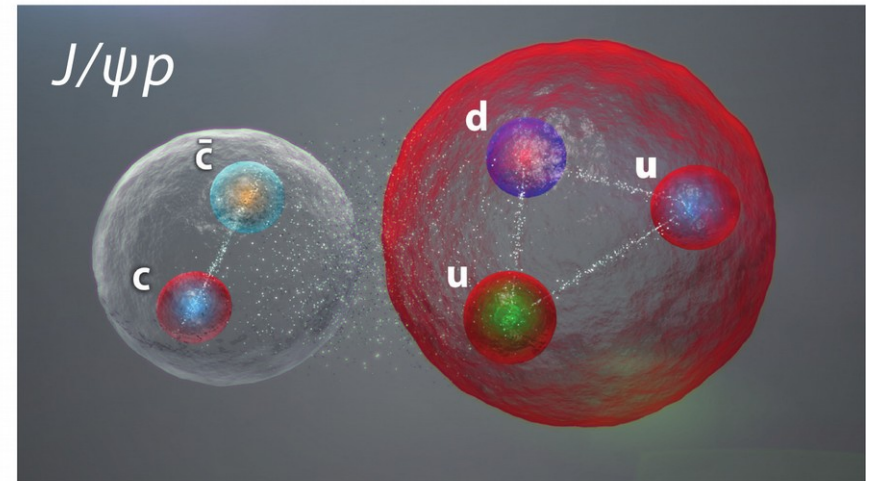
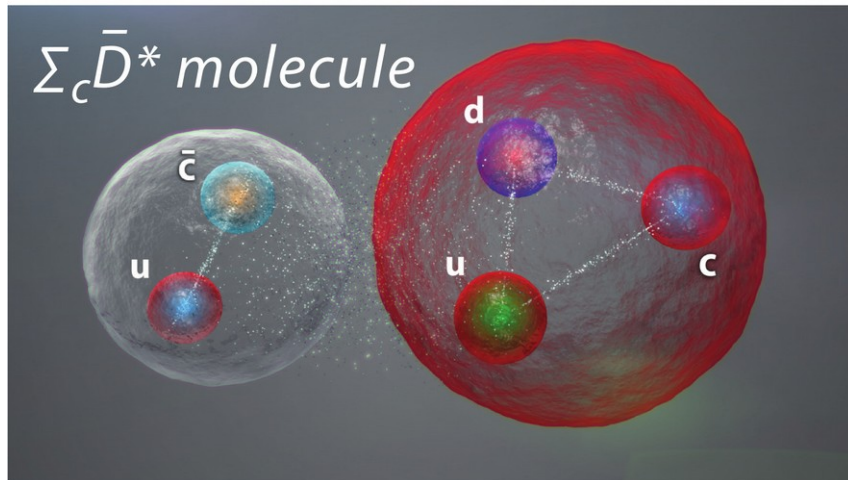
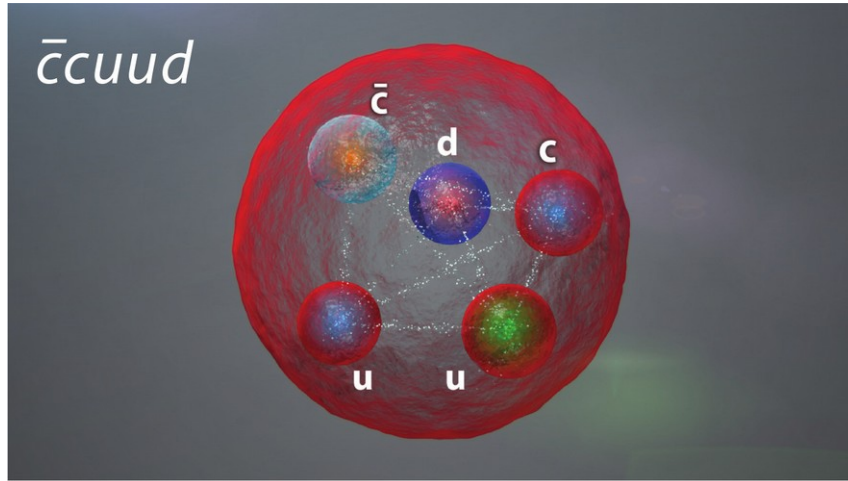
To get  $\Gamma = 39$  MeV, the matrix element must be small .

But in a pentaquark  $c$  and  $\bar{c}$  are close to each other within the same confinement volume, so overlap with  $J/\psi$  is generically large.

In a molecule narrow width is automatic:

$c$  is in  $\Sigma_c$ ,  $\bar{c}$  is in  $\bar{D}^*$ ; they are from each other, so overlap with  $J/\psi$  is generically small.

# Decay of a tightly bound pentaquark vs. hadronic molecule to $J/\psi p$



$$|\langle \Sigma_c \bar{D}^* | J/\psi p \rangle| \ll |\langle \bar{c}cuud | J/\psi p \rangle|$$

2  $J/\psi p$  resonances with  $> 9 \sigma$  in  $\Lambda_b \rightarrow J/\psi p K^-$

$P_c(4450)$  very clean, but:

- $P_c(3380)$  ?
- $J$ :  $(3/2, 5/2)$  or  $(5/2, 3/2)$  ?
- $P$ :  $(-, +)$  or  $(+, -)$  ?
- $m(P_c(4450)) = m_p + m_{\chi_{c1}}$
- “triangle singularity”

$\implies$  need a different production mechanism

# Photoproduction of exotic baryon resonances

MK & J. Rosner, arXiv:1508.01496

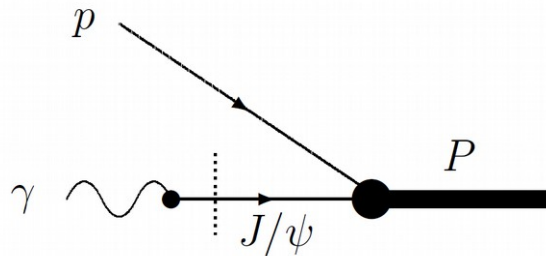
Q. Wang, X. H. Liu and Q. Zhao, arXiv:1508.00339

V. Kubarovsky and M. B. Voloshin, arXiv:1508.00888

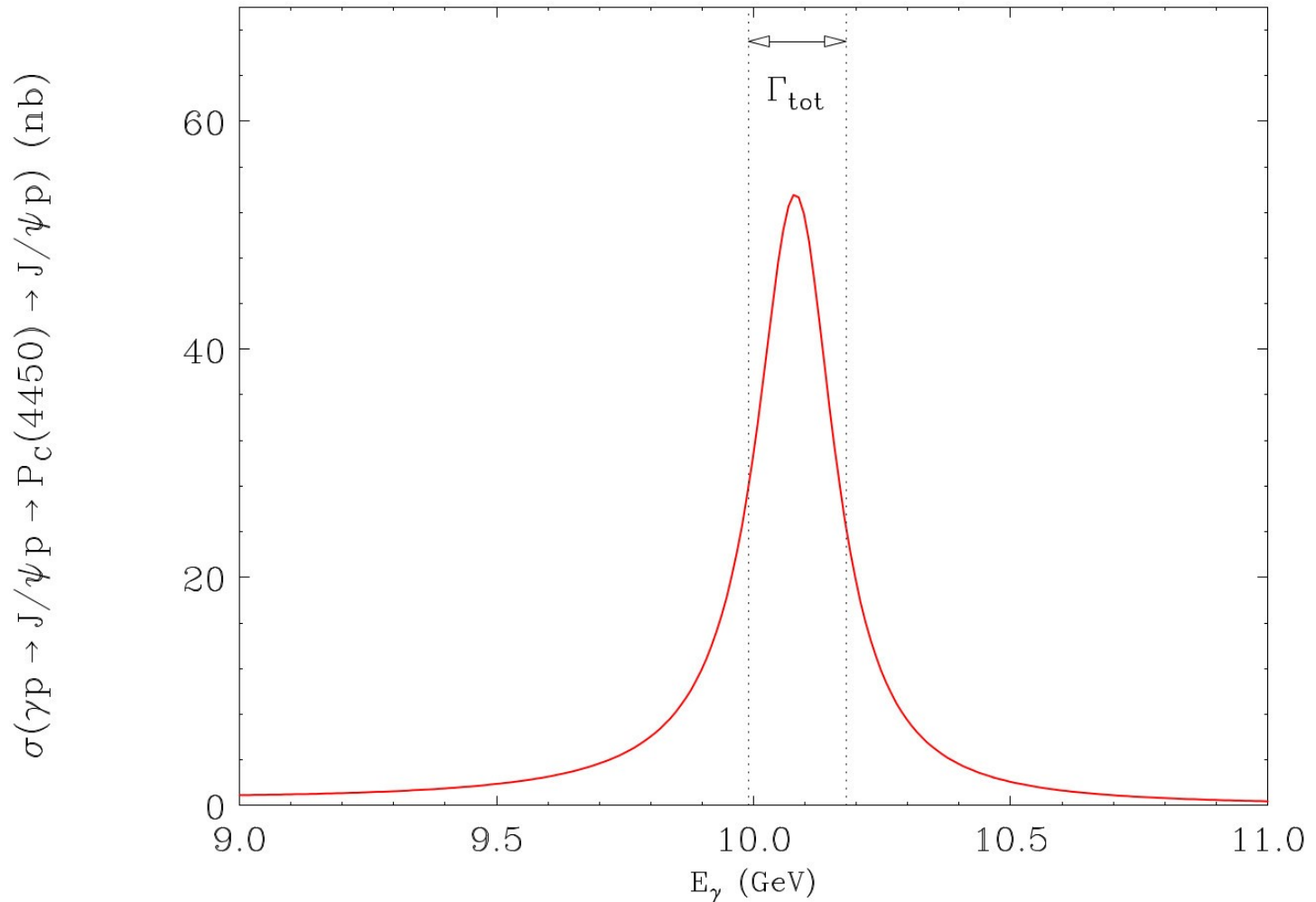
LHCb: new exotic resonances in  $J/\psi p$  channel:

$\implies$  natural candidates for photoproduction

- estimate  $\sigma(\gamma p \rightarrow P_c \rightarrow J/\psi p)$  from vector dominance:



- $E_\gamma = 10 \text{ GeV} \implies \text{CLAS12 \& GlueX @JLab \& ...}$
- $\sigma \sim 50 \text{ nb} \gg \sigma_{\text{diffractive}} \sim 1 \text{ nb}$



Cross section for resonant photoproduction  $\gamma p \rightarrow J/\psi p \rightarrow P_c(4450) \rightarrow J/\psi p$ , assuming  $B_{\text{out}} = 0.1$ , plotted as function of the incident photon energy  $E_\gamma$ . The vertical dotted lines indicate the width of the  $P_c(4450)$  resonance.

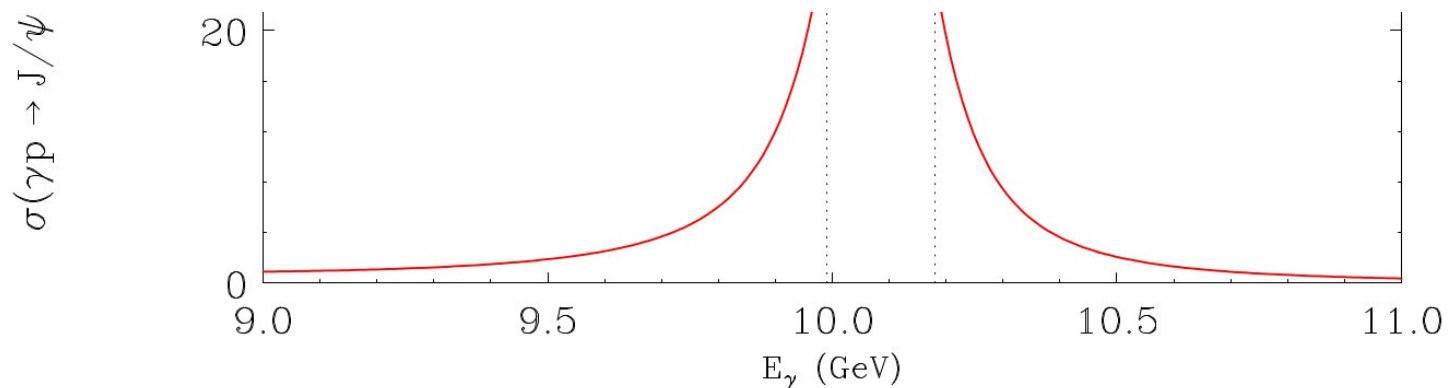


Caveat:

$$BR(P_c(4450) \rightarrow J/\psi p) \ll BR(P_c(4450) \rightarrow \Sigma_c \bar{D}^*)$$

$$BR(\text{quarkonium mode}) \ll BR(\text{“fall apart” mode})$$

with significantly more data LHCb might be able to look for  $P_c \rightarrow \Sigma_c^{++} D^{-*}$



Cross section for resonant photoproduction  $\gamma p \rightarrow J/\psi p \rightarrow P_c(4450) \rightarrow J/\psi p$ , assuming  $B_{\text{out}} = 0.1$ , plotted as function of the incident photon energy  $E_\gamma$ . The vertical dotted lines indicate the width of the  $P_c(4450)$  resonance.

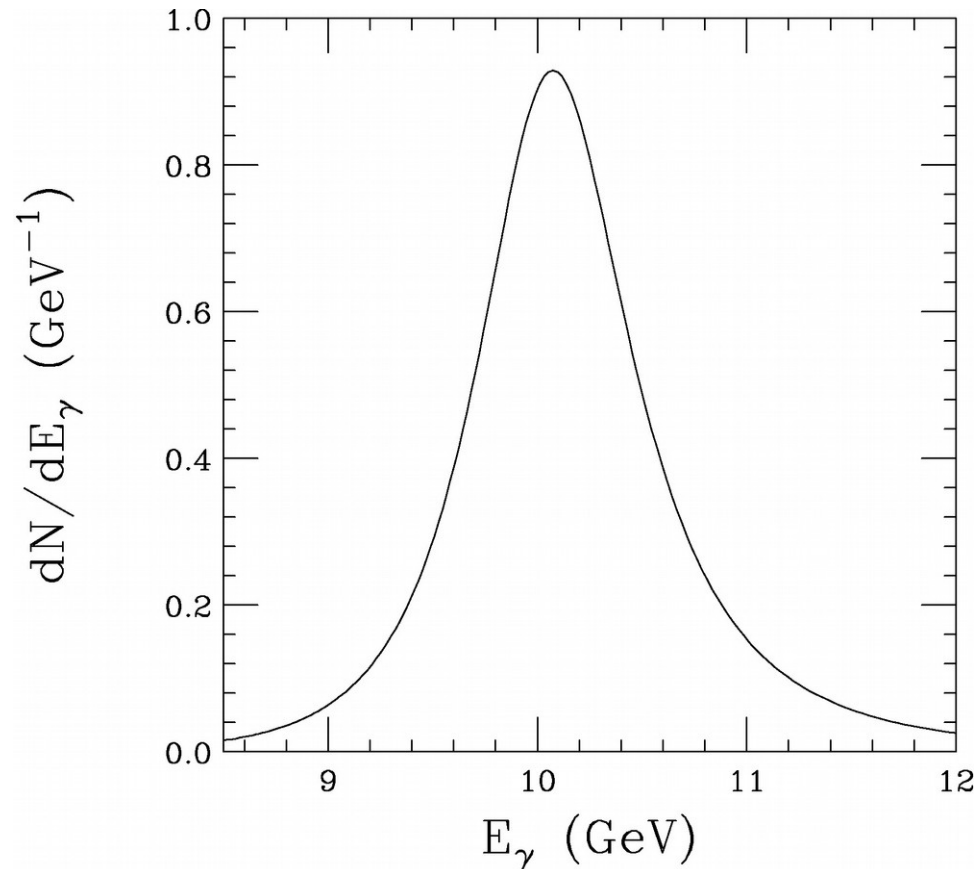
$$P_c(4380) \text{ and } P_c^+(4450) \rightarrow J/\psi p \Rightarrow I_3 = +\frac{1}{2}$$

If genuine resonances,  $I_3 = -\frac{1}{2}$  partner must exist

$$\Rightarrow \gamma d \rightarrow J/\psi n p$$

- $\sigma(\gamma n \rightarrow P_c \rightarrow J/\psi n) = \sigma(\gamma p \rightarrow P_c \rightarrow J\psi p)$
- $M(P_c^0) = M(P_c^+)$
- w/o Fermi motion  $\sigma(\gamma d) = 2\sigma(\gamma p)$
- Fermi motion effects significant:  
smearing, FF suppression, offshellness
- recoil  $N$  momentum  $\lesssim 100$  MeV,  
so detection problematic

convolution of  $\sigma(\gamma N \rightarrow P_c)$  with Fermi motion results in significant broadening of the peak



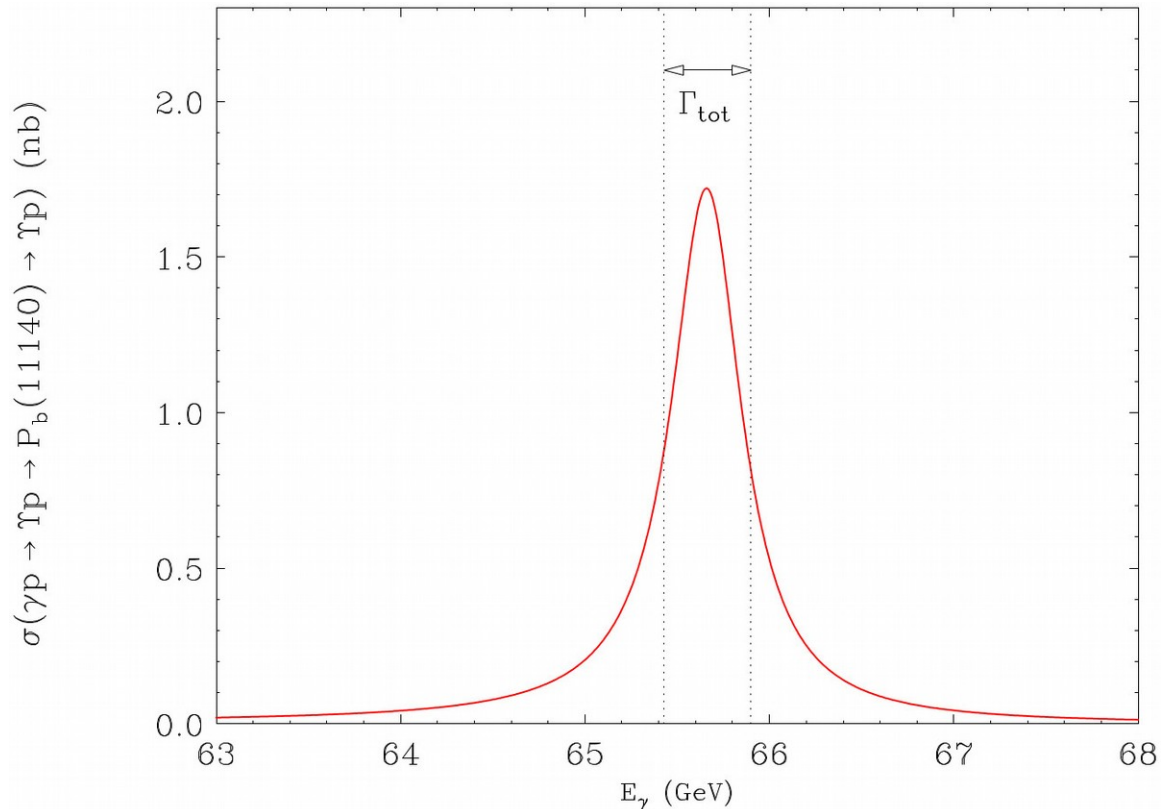
MK and J.L. Rosner,  
arXiv:1705.07691 [hep-ph].

Spread in incident photon energy for photoproduction of a narrow  $P_c(4450)$  on a deuteron target. The curve is normalized so that its integral over  $E_\gamma$  is 1.

bottomonium analogue:  
 $\Sigma_b B^*$  molecule at 11.14 GeV

$$E_\gamma = 65.66 \text{ GeV},$$

$$\sigma \sim 1 \text{ nb} \gg \sigma_{\text{diffractive}} \sim 50 \text{ pb}$$



$X(3872) \rightarrow J/\psi \pi^+ \pi^-$  seen in LHC exps,

$\sigma^{\text{prompt}}(pp \rightarrow X(3872) + \text{anything}) \cdot \mathcal{B}(X(3872) \rightarrow J/\psi \pi^+ \pi^-) \sim \text{few nb}$

so perhaps LHC can also see continuum production

$P_c(4450) \rightarrow J/\psi p$

$P_b(11140) \rightarrow \gamma p ?$

## bottom analogue of $X(3872)$ :

- $X_b$  and  $\chi_{b1}(3P)$  have the same quantum numbers
  - their masses are close
- $\Rightarrow$  mixing is inevitable

$\Rightarrow$   $X_b$  might have been seen already,  
by ATLAS, D0 and LHCb,  
camouflaging as  $\chi_{1b}(3P)$

$\Rightarrow$  measure  $R_{\gamma\gamma} \equiv \frac{\mathcal{B}(\chi_{b1}(3P) \rightarrow \Upsilon(2S)\gamma)}{\mathcal{B}(\chi_{b1}(3P) \rightarrow \Upsilon(1S)\gamma)}$

## $\Sigma_b^+ \Sigma_b^-$ dibaryon:

$\Sigma_b^+ \Sigma_b^-$  vs.  $\bar{B}B^*$ :

$m_{\Sigma_b} > m_B$ ,  $l = 1$  vs.  $l = \frac{1}{2}$   $\rightarrow$  stronger binding via  $\pi$

$\Rightarrow$  deuteron-like  $J = 1$ ,  $l = 0$  bound state, “*beautron*”

extra  $\sim 3$  MeV binding from EM interaction

EXP signature:  $\rightarrow \Lambda_b \Lambda_b \pi^+ \pi^-$

$\Gamma(\Sigma_b) \sim 5 \div 10$  MeV, so might be visible

should be seen in lattice QCD

also  $\Sigma_c^+ \Sigma_c^-$ , etc.

# Exotic resonances due to $\eta$ exchange

- Mesons w/o  $u$  and  $d$  light quarks, e.g.  $D_s$  :
- cannot exchange  $\pi$
- but under suitable circumstances can bind as a result of  $\eta$  exchange.

$\Rightarrow$  exotic  $D_s^{(*)} \bar{D}_s^{(*)}$  ( $c\bar{s} \bar{c}s$ ) mesons  $\rightarrow J/\psi \phi$   
in  $B \rightarrow XK \rightarrow J/\psi \phi K$

MK and J. Rosner, Nucl. Phys. A **954**, 365 (2016)



Table 1: Possible S-wave resonances with two  $D_s$  mesons below 5 GeV.

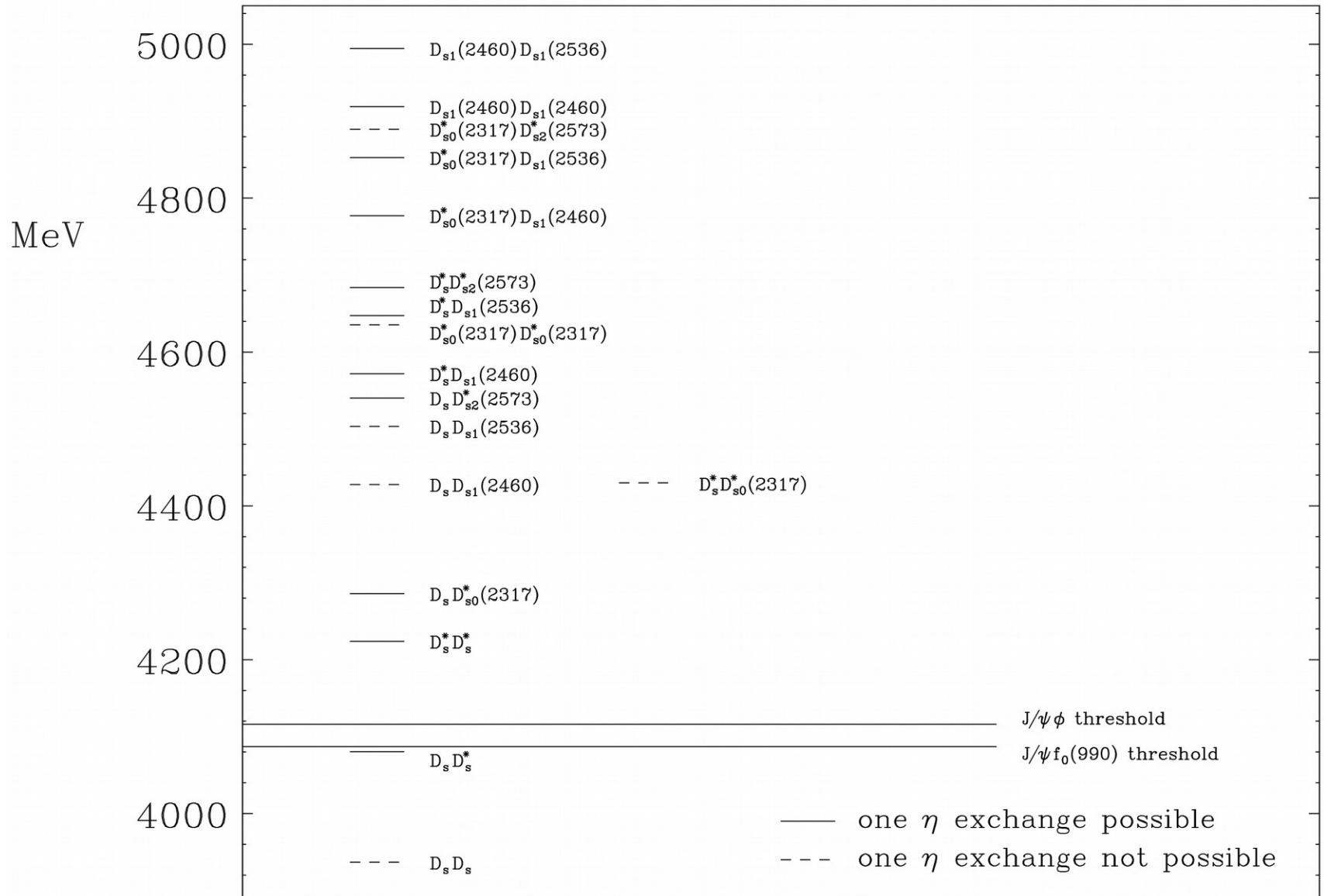
States ( $J^P$ )	$M$ (MeV)	$M - M(J/\psi)$ $-M(\phi)$	Binding by $\eta$ ?	Allowed $J^P$
$D_s^+(0^-) D_s^-(0^-)$	3936.6	-179.8	No	-
$D_s^+(0^-) D_s^{*-}(1^-)$	4080.4	-36.0	Yes	$1^+$
$D_s^{*+}(1^-) D_s^{*-}(1^-)$	4224.2	107.8	Yes	$0^+, 2^+{}^a$
$D_s^+(0^-) D_{s0}^{*-}(2317)(0^+)$	4286.0	169.6	Yes	$0^-$
$D_s^+(0^-) D_{s1}^-(2460)(1^+)$	4427.8	311.4	No <sup>b</sup>	$[1^-]{}^b$
$D_s^{*+}(1^-) D_{s0}^{*-}(2317)(0^+)$	4429.8	313.4	No <sup>b</sup>	$[1^-]{}^b$
$D_s^+(0^-) D_{s1}^-(2536)(1^+)$	4503.4	387.0	No	-
$D_s^+(0^-) D_{s2}^{*-}(2573)(2^+)$	4540.2	423.8	Yes	$2^-$
$D_s^{*+}(1^-) D_{s1}^-(2460)(1^+)$	4571.6	455.2	Yes	$0^-, 1^-, 2^-$
$D_{s0}^{*+}(2317)(0^+) D_{s0}^{*-}(2317)(0^+)$	4635.4	519.0	No	-
$D_s^{*+}(1^-) D_{s1}^-(2536)(1^+)$	4647.2	530.8	Yes	$0^-, 1^-, 2^-$
$D_s^{*+}(1^-) D_{s2}^{*-}(2573)(2^+)$	4684.0	567.6	Yes	$1^-, 2^-, 3^-$
$D_{s0}^{*+}(2317)(0^+) D_{s1}^-(2460)(1^+)$	4777.2	660.8	Yes	$1^+$
$D_{s0}^{*+}(2317)(0^+) D_{s1}^-(2536)(1^+)$	4852.8 <sup>c</sup>	736.4	Yes	$1^+$
$D_{s0}^{*+}(2317)(0^+) D_{s2}^{*-}(2573)(2^+)$	4889.6 <sup>c</sup>	773.2	No	-
$D_{s1}^+(2460)(1^+) D_{s1}^-(2460)(1^+)$	4919.0 <sup>c</sup>	802.6	Yes	$0^+, 2^+{}^a$
$D_{s1}^+(2460)(1^+) D_{s1}^-(2536)(1^+)$	4994.6 <sup>c</sup>	878.2	Yes	$0^+, 1^+, 2^+$

<sup>a</sup>  $J^P = 1^+$  forbidden by symmetry.

<sup>b</sup> Proximity of these two channels may lead to binding. See text.

<sup>c</sup> Cannot be produced in  $B \rightarrow KX$  because of kinematic mass limit.

# Thresholds involving two $D_s$ mesons



doubly heavy baryons  $QQq$ :

$ccq, bcq, bbq, \quad q = u, d$

must exist, but have never been seen

fascinating challenge for EXP & TH

LHCb sees thousands of  $B_c$ -s

$\implies$  should see  $bcq, ccq, \text{ etc.}$

$QQq$  baryons are the simplest baryons:

when  $m_Q \rightarrow \infty$ ,  $QQ$  form a static  $\bar{3}_c$  diquark

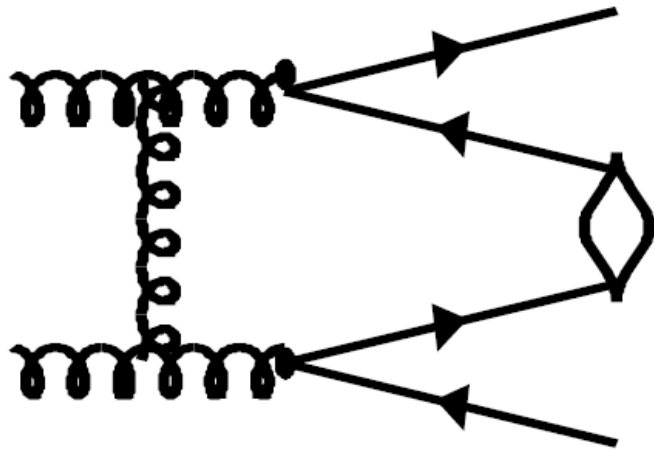
so  $QQq$  baryon  $\sim \bar{Q}q$  meson

e.g. form factors:  $F_{QQq}(q^2) = F_{\bar{Q}q}(q^2)$

corrections:  $f\left(\frac{\Lambda_{QCD}}{m_Q}\right)$ , calculable in QCD

hydrogen atom of baryon physics!

## $B_c$ production in LHCb: $gg$ fusion



v. hard to compute reliably  
from first principles, but...

$\Xi_{bc}$  production: same diagram,

but  $b$  needs to pick up  $c$ , instead of  $\bar{c}$ :  $\bar{\mathbf{3}}_c \mathbf{3}_c$  vs.  $\mathbf{3}_c \mathbf{3}_c$

$$\Rightarrow \sigma(pp \rightarrow \Xi_{bc} + X) \stackrel{<}{\sim} \sigma(pp \rightarrow B_c + X)$$

LHCb is making a lot of  $B_c$ -s  $\sigma \approx 0.4 \mu\text{b}$

$\Rightarrow$  LHCb is making a lot of  $(QQq)$  baryons !!!

$\Xi_{cc}$  is the lightest doubly-heavy baryon

is it LHCb's best bet for  $(QQq)$  ?

$$\sigma(\bar{c}c \bar{c}c) \gg \sigma(\bar{b}b \bar{c}c) \gg \sigma(\bar{b}b, \bar{b}b)$$

but  $\tau(b) \sim 7\tau(c)$  (Cabibbo),

e.g.  $\tau(\Lambda_b) \approx 1.4 \times 10^{-12}$  sec.

vs.  $\tau(\Lambda_c) \approx 0.2 \times 10^{-12}$  sec.

verified by detailed lifetime calculation

masses of doubly-heavy baryons:  
use same toolbox that predicted  
b baryon masses.

# doubly heavy baryons: masses and lifetimes

our mass predictions (in MeV) for lowest-lying baryons with two heavy quarks. States without a star have  $J = 1/2$ ; states with a star are their  $J = 3/2$  hyperfine partners. The quark  $q$  can be either  $u$  or  $d$ . The square or curved brackets around  $cq$  denote coupling to spin 0 or 1.

State	Quark content	$M(J = 1/2)$	$M(J = 3/2)$
$\Xi_{cc}^{(*)}$	$ccq$	$3627 \pm 12$	$3690 \pm 12$
$\Xi_{bc}^{(*)}$	$b[cq]$	$6914 \pm 13$	$6969 \pm 14$
$\Xi'_{bc}$	$b(cq)$	$6933 \pm 12$	–
$\Xi_{bb}^{(*)}$	$bbq$	$10162 \pm 12$	$10184 \pm 12$

summary of lifetime predictions for baryons containing two heavy quarks. Values given are in fs.

Baryon	This work	[27]	[51]	[70]	[71]
$\Xi_{cc}^{++} = ccu$	185	$430 \pm 100$	$460 \pm 50$	500	$\sim 200$
$\Xi_{cc}^{+} = ccd$	53	$120 \pm 100$	$160 \pm 50$	150	$\sim 100$
$\Xi_{bc}^{+} = bcu$	244	$330 \pm 80$	$300 \pm 30$	200	–
$\Xi_{bc}^{0} = bcd$	93	$280 \pm 70$	$270 \pm 30$	150	–
$\Xi_{bb}^{0} = bbu$	370	–	$790 \pm 20$	–	–
$\Xi_{bb}^{-} = bbd$	370	–	$800 \pm 20$	–	–



Predicted isospin splittings (MeV) in  $QQq$  baryons.

$$\begin{array}{ccc} M(ccu) - M(ccd) & M(bbu) - M(bbd) & M(bcu) - M(bcd) \\ \hline 1.41 \pm 0.12^{+0.76} & -4.78 \pm 0.06^{+0.03} & -1.69 \pm 0.07^{+0.39} \end{array}$$

arXiv:1706.06961

# Likely decay modes of $QQq$ baryons

- $\Xi_{cc}^{+++} = ccu$

$$\Xi_{cc}^{+++} \rightarrow (csu) W^+ \rightarrow (csu) (\pi^+, \rho^+, a_1^+)$$

e.g.

$$\Xi_{cc}^{+++} \rightarrow 3\pi^+ \Xi^- \quad (\text{missed by CDF trigger})$$

$$\Xi_{cc}^{+++} \rightarrow \Lambda_c K^- 2\pi^+$$

lifetime: each  $c$  quark can decay independently

$$\Gamma(\Xi_{cc}^{+++}) = 3.56 \times 10^{-12} \text{ GeV}$$

$$\tau(\Xi_{cc}^{+++}) = 185 \text{ fs}$$

- $\Xi_{cc}^+ = ccd$

In addition to  $c \rightarrow sud$ , have  $cd \rightarrow su$

$$\implies \tau(\Xi_{cc}^+) = 50 \div 100 \text{ fs}$$

- $\Xi_{bc}^+ = bcu$

$b \rightarrow cdu$  and  $c \rightarrow sud$

e.g.  $\Xi_{bc} \rightarrow J/\psi \Xi_c$

$$\tau(\Xi_{bc}^+) \approx 240 \text{ fs}$$

- $\Xi_{bc}^0 = bcd$

$$\tau(\Xi_c^+) = (4.42 \pm 0.26) \times 10^{-13} \text{ s}$$

the difference due to  $cd \rightarrow su$

$$\tau(\Xi_c^0) = (1.12^{+0.13}_{-0.10}) \times 10^{-13} \text{ s}$$

$$\implies \tau(\Xi_{bc}^0) = 93 \text{ fs}$$

e.g.  $\Xi_{bc}^0 \rightarrow j/\psi \Xi^0$  or  $\Xi_{bc}^0 \rightarrow J/\psi \Xi^- \pi^+$

- $\Xi_{bb} = bbq$

$bu \rightarrow cd$  possible for  $\Xi_{bb}^0$ , but

$\tau(\Xi_b^0)$  not much different from  $\tau(\Xi_b^-)$   
 so treat  $\Xi_{bb}^0$  and  $\Xi_{bb}^-$  generically as  $\Xi_{bb}$

$$\implies \tau(\Xi_{bb}) \approx 376 \text{ fs}$$

rare but spectacular decay mode:

$$(bbq) \rightarrow (\bar{c}cs) (\bar{c}cs)q \rightarrow J/\psi J\psi \Xi$$

rough estimate of  $\Xi_{cc}$  production rate

assume suppression due to  $s \rightarrow c$   
indep. of spectators, i.e.

$\Xi_{cc}$  suppressed vs.  $\Xi_c$  as  $\Xi_c$  vs.  $\Xi$ :

$$\sigma(pp \rightarrow \Xi_{cc} + X) \sim \sigma(pp \rightarrow \Xi_c + X) \cdot \frac{\sigma(pp \rightarrow \Xi_c + X)}{\sigma(pp \rightarrow \Xi + X)}$$

perhaps can generalize to  $\Xi_{bc}$  and  $\Xi_{bb}$  production rate

$$\sigma(pp \rightarrow \Xi_{bc} + X) \sim \sigma(pp \rightarrow \Xi_b + X) \cdot \frac{\sigma(pp \rightarrow \Xi_c + X)}{\sigma(pp \rightarrow \Xi + X)}$$

or

$$\sigma(pp \rightarrow \Xi_{bc} + X) \sim \sigma(pp \rightarrow \Xi_c + X) \cdot \frac{\sigma(pp \rightarrow \Xi_b + X)}{\sigma(pp \rightarrow \Xi + X)}$$

and

$$\sigma(pp \rightarrow \Xi_{bb} + X) \sim \sigma(pp \rightarrow \Xi_b + X) \cdot \frac{\sigma(pp \rightarrow \Xi_b + X)}{\sigma(pp \rightarrow \Xi + X)}$$

a possible way to check if  $\Xi_{bc}$  and  $B_c$

production rates are comparable:

compare analogous prod. rates of  $\Xi_c$  and  $D_s$

(or  $\Xi_b$  and  $B_s$ ) in the same setup,

and large enough  $E_{CM}$

be it  $e^+e^-$ ,  $\bar{p}p$  or  $pp$

# $QQ\bar{Q}\bar{Q}$ States

Phys. Rev. D **95**, 034011 (2017) MK, J.L. Rosner, S.Nussinov

Toolbox borrowed from  $QQq$  baryons

$M_{(cc\bar{c}\bar{c})} = 6,192 \pm 25$  MeV,  $225 \pm 25$  MeV above  $\eta_c\eta_c$

unlikely to be narrow, nor to have significant non-hadronic decays

$M_{(bb\bar{b}\bar{b})} = 18,826 \pm 25$  MeV,  $28 \pm 25$  MeV above  $\eta_b\eta_b$

could be narrow & exhibit non-hadronic decays if estim.  $> 1\sigma$  high

production of an extra  $Q\bar{Q}$ : probability  $\sim 0.1\%$

CMS (arXiv:1610.07095) sees double  $\Upsilon(1S)$ ; production;  
38 events, each  $\Upsilon \rightarrow \mu^+\mu^-$ , in  $20.7 \text{ fb}^{-1}$  at  $\sqrt{s} = 8$  TeV

$\Rightarrow$  Inspect neutral  $4\ell$  final states for possible evidence  
of  $bb\bar{b}\bar{b}$  state; most likely  $J^{PC} = 0^{++}$



$$\Xi_c^+ = csu, \quad K^- = s\bar{u}$$

$$\Rightarrow css: \text{ excited } \Omega_c$$

## Observation of five new narrow $\Omega_c^0$ states decaying to $\Xi_c^+ K^-$

The LHCb collaboration<sup>†</sup>

### Abstract

The  $\Xi_c^+ K^-$  mass spectrum is studied with a sample of  $pp$  collision data corresponding to an integrated luminosity of  $3.3 \text{ fb}^{-1}$ , collected by the LHCb experiment. The  $\Xi_c^+$  is reconstructed in the decay mode  $pK^-\pi^+$ . Five new, narrow excited  $\Omega_c^0$  states are observed: the  $\Omega_c(3000)^0$ ,  $\Omega_c(3050)^0$ ,  $\Omega_c(3066)^0$ ,  $\Omega_c(3090)^0$ , and  $\Omega_c(3119)^0$ . Measurements of their masses and widths are reported.

Submitted to Phys. Rev. Lett.

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<sup>†</sup>Authors are listed at the end of this paper.

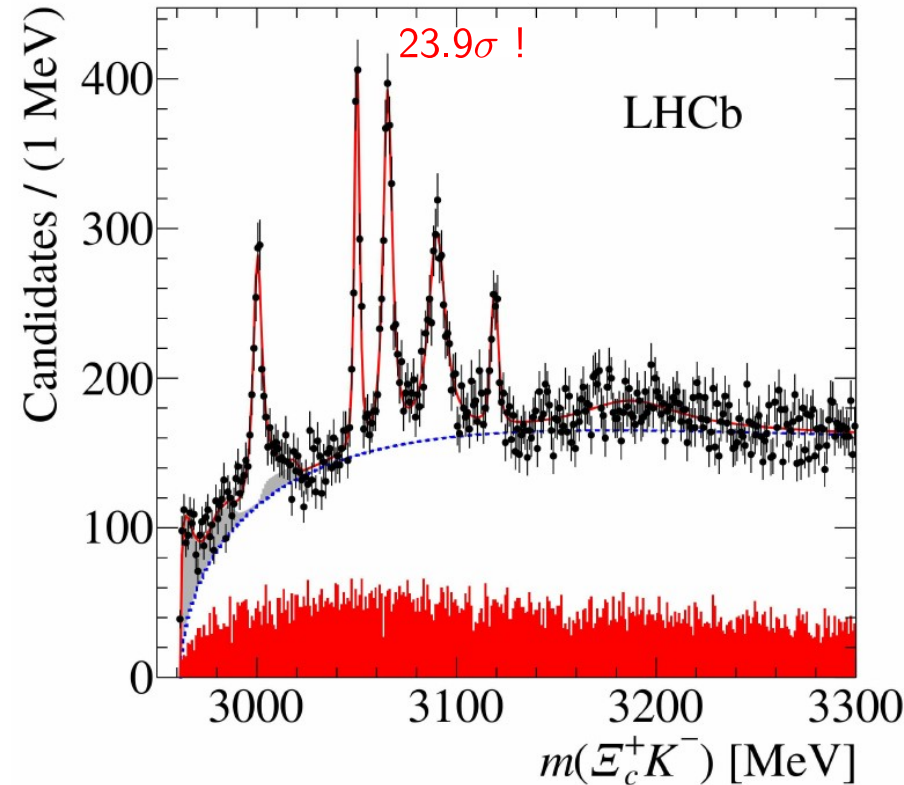


Figure 2: Distribution of the reconstructed invariant mass  $m(\Xi_c^+ K^-)$  for all candidates passing the likelihood ratio selection; the solid (red) curve shows the result of the fit, and the dashed (blue) line indicates the fitted background. The shaded (red) histogram shows the corresponding mass spectrum from the  $\Xi_c^+$  sidebands and the shaded (light gray) distributions indicate the feed-down from partially reconstructed  $\Omega_c(X)^0$  resonances.

- interpret as bound states of a  $c$ -quark and a  $P$ -wave  $ss$ -diquark.
- ⇒ exactly 5 possible combinations of **S** and **L** splitting due to spin-orbit, spin-spin and tensor
- narrowness:  
diquark hard to split and/or  $D$ -wave suppression
- predict 5 states:  
 $J^P = 1/2^-, 1/2^-, 3/2^-, 3/2^-, 5/2^-$
- assign to 5 observed resonances  
(*a priori*  $5! = 120$  possibilities)
- $\Omega_b$  analogues
- alternative interpretations

some immediate questions:

- (a) Why five states? Are there more ?
- (b) Why are they so narrow?
- (c) What are their spin-parity assignments?
- (d) Can one understand the mass pattern?
- (e) Other similar states ?  
e.g. very narrow excited  $\Omega_b$  baryons?

## $P$ -wave $c(ss)$ system

$c(ss)$ : if  $ss$   $S$ -wave  $\bar{3}_c$  diquark  $\Rightarrow S_{ss} = 1$

combine  $S_{ss} = 1$  with  $S_c = \frac{1}{2} \Rightarrow$  total  $S = \frac{1}{2}$  or  $\frac{3}{2}$

take  $L = 1$  for  $c$ - $ss$  system

combine  $L = 1$  with  $S = \frac{1}{2} \Rightarrow J = \frac{1}{2}, \frac{3}{2}$

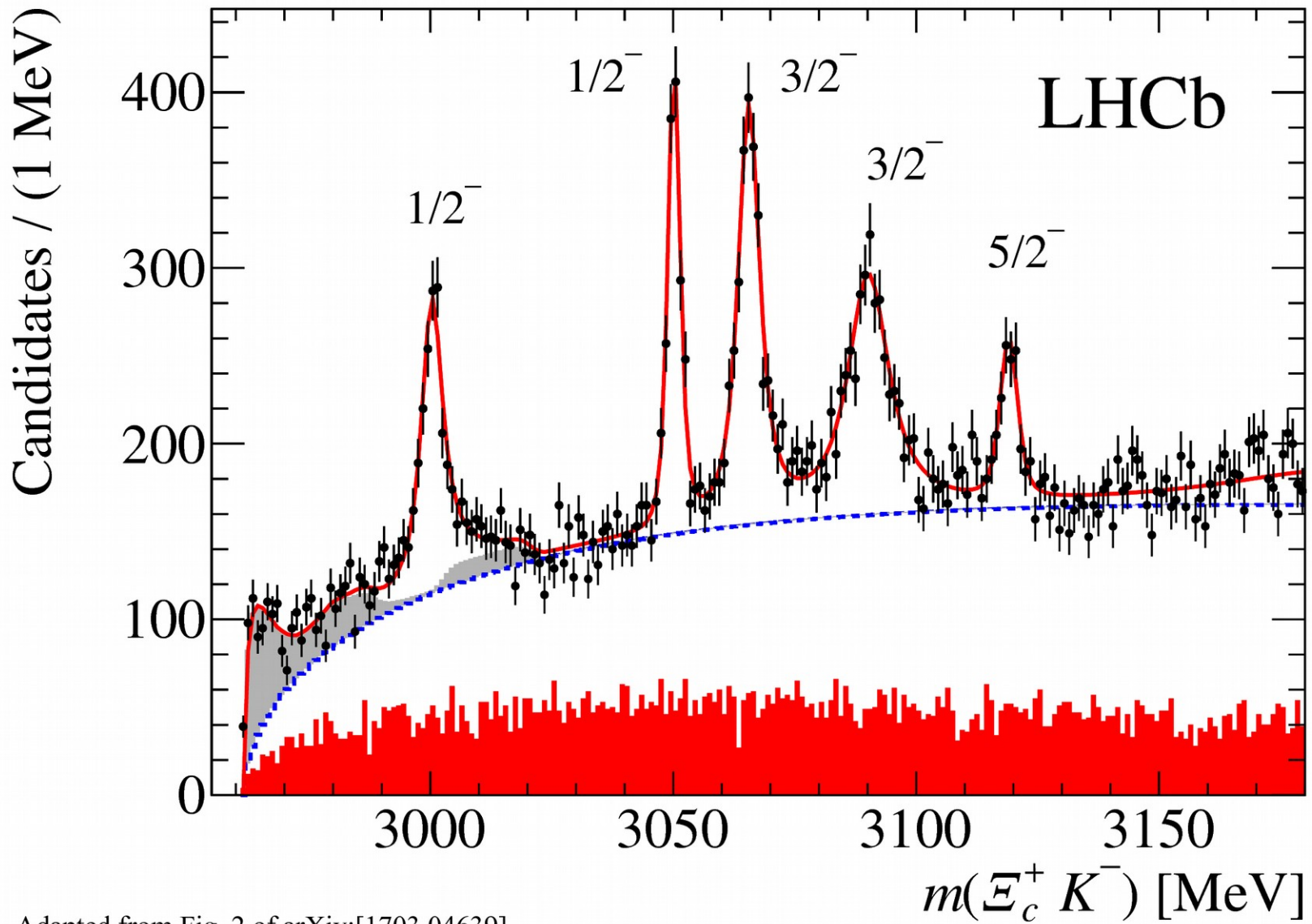
combine  $L = 1$  with  $S = \frac{3}{2} \Rightarrow J = \frac{1}{2}, \frac{3}{2}, \frac{5}{2}$

all with  
negative parity

$\Rightarrow J^P = 1/2^-, 1/2^-, 3/2^-, 3/2^-, 5/2^-$

$J^P = 1/2^-$  decay to  $\Xi_c^+ K^-$  in  $S$ -wave,   
  $\bullet$  partially confirmed by preferred  $J^P$   
  $\bullet$  consistent w. alternate assignment

$J^P = 3/2^-, 5/2^-$  decay to  $\Xi_c^+ K^-$  in  $D$ -wave



Adapted from Fig. 2 of arXiv:[1703.04639]

Masses and widths of  $\Omega_c = c s s$  candidates reported by LHCb.  
 The proposed values of spin-parity  $J^P$  are ours.  
 An alternative set of assignments is shown in parentheses.

State	Mass (MeV) <sup>a</sup>	Width (MeV)	Proposed $J^P$
$\Omega_c(3000)^0$	$3000.4 \pm 0.2 \pm 0.1$	$4.5 \pm 0.6 \pm 0.3$	$1/2^-$ ( $3/2^-$ )
$\Omega_c(3050)^0$	$3050.2 \pm 0.1 \pm 0.1$	$0.8 \pm 0.2 \pm 0.1$	$1/2^-$ ( $3/2^-$ )
		$< 1.2$ MeV, 95% CL	
$\Omega_c(3066)^0$	$3065.6 \pm 0.1 \pm 0.3$	$3.5 \pm 0.4 \pm 0.2$	$3/2^-$ ( $5/2^-$ )
$\Omega_c(3090)^0$	$3090.2 \pm 0.3 \pm 0.5$	$8.7 \pm 1.0 \pm 0.8$	$3/2^-$ ( $1/2^+$ )
$\Omega_c(3119)^0$	$3119.1 \pm 0.3 \pm 0.9$	$1.1 \pm 0.8 \pm 0.4$	$5/2^-$ ( $3/2^+$ )
		$< 2.6$ MeV, 95% CL	

<sup>a</sup>Additional common error of  $+0.3, -0.5$  MeV from  $M(\Xi_c^+)$  uncertainty.

spin-dependent potential  
between a heavy quark  $Q$  and the  $(ss)$  spin-1 diquark

$$\begin{aligned} V_{SD} &= a_1 \mathbf{L} \cdot \mathbf{S}_{ss} + a_2 \mathbf{L} \cdot \mathbf{S}_Q \quad \text{spin orbit} \\ &+ b[-\mathbf{S}_{ss} \cdot \mathbf{S}_Q + 3(\mathbf{S}_{ss} \cdot \mathbf{r})(\mathbf{S}_Q \cdot \mathbf{r})/r^2] \quad \text{tensor force} \\ &+ c \mathbf{S}_{ss} \cdot \mathbf{S}_Q, \quad \text{color hyperfine} \end{aligned}$$

$\mathbf{L}$  = angular momentum = 1

$\mathbf{S}_{ss}$  =  $ss$  diquark spin = 1

$\mathbf{S}_Q$  = heavy quark spin = 1/2

## criteria for parameters

(i)  $\mathbf{S}_{ss} \cdot \mathbf{S}_Q :$

$c$  should be small, as it depends on  $P$ -wave near the origin.

(ii)  $\mathbf{L} \cdot \mathbf{S}_Q :$

$a_2$  should be close to estimate from  $\Lambda_c$ ,  $a_2 = 23.9$  MeV

(iii)  $\mathbf{L} \cdot \mathbf{S}_{ss} :$

$a_1$  should be  $< 40$  MeV, from previous  $\Sigma_c(cuu)$  analysis

examine all  $5! = 120$  *a priori* possible assignments of  $P$ -wave states

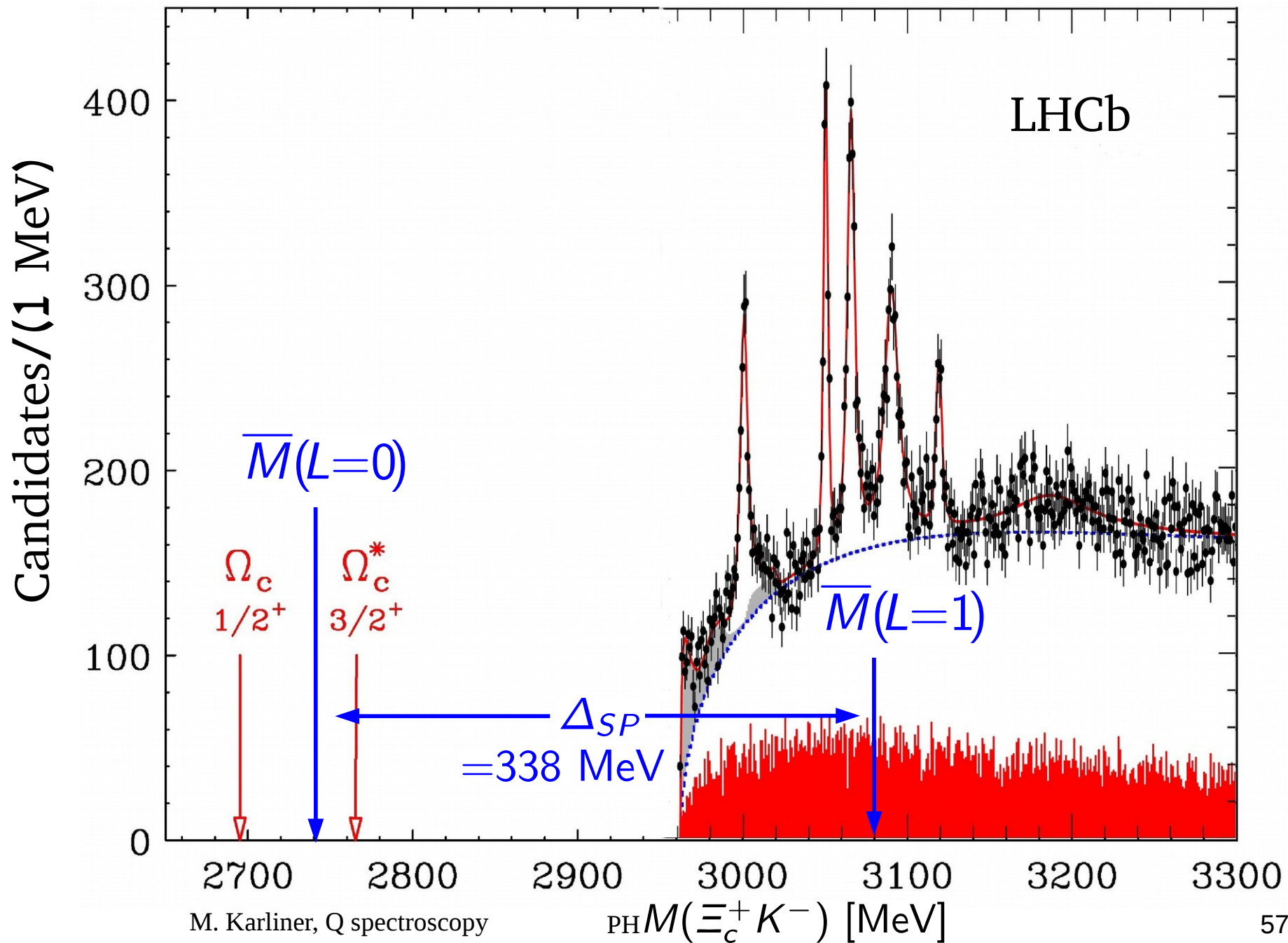
$\Rightarrow$  assignment in Table favored, with parameters

$$a_1 = 26.95 \text{ MeV} , \quad a_2 = 25.74 \text{ MeV} , \quad b = 13.52 \text{ MeV} , \quad c = 4.07 \text{ MeV} .$$

$\Rightarrow$  the spin-averaged mass:

$$\bar{M} = (1/18) \sum_J (2J + 1) M(J) = 3079.94 \text{ MeV} .$$





## predictions for $\Omega_b = b(ss)$ states

$$\frac{m_c}{m_b} \sim \frac{1}{3} \Rightarrow \text{expect lin. approx. much better}$$

- set HF parameter  $c = 0$ .
- $a_1 = 26.95$  MeV as for  $c(ss)$ , as coeff. of  $\mathbf{L} \cdot \mathbf{S}_{(ss)}$ .
- $a_2 = 8.72$  MeV, rescaled by  $m_c/m_b$ .
- $-20$  MeV  $< b < 20$  MeV.
- $S$ - $P$  splitting:  $\Delta E_{PS}(\Omega_b) \sim 300$  MeV.

# predictions for $\Omega_b = b(ss)$ states

leading to mass shifts  $\Delta M(J, j)$  in MeV:

$$\Delta M(1/2, 0) = -53.9 ,$$

$$\Delta M(1/2, 1) = -31.3 - b ,$$

$$\Delta M(3/2, 1) = -24.8 + \frac{1}{2}b ,$$

$$\Delta M(3/2, 2) = 20.4 + \frac{3}{10}b ,$$

$$\Delta M(5/2, 2) = 31.3 - \frac{1}{5}b .$$

$$\frac{1}{18} \sum_J (2J+1) M(J, j) = \bar{M}(\Omega_b) \approx [6062 + \Delta E_{PS}(\Omega_b)] \text{ MeV} \sim 6362 \text{ MeV}$$

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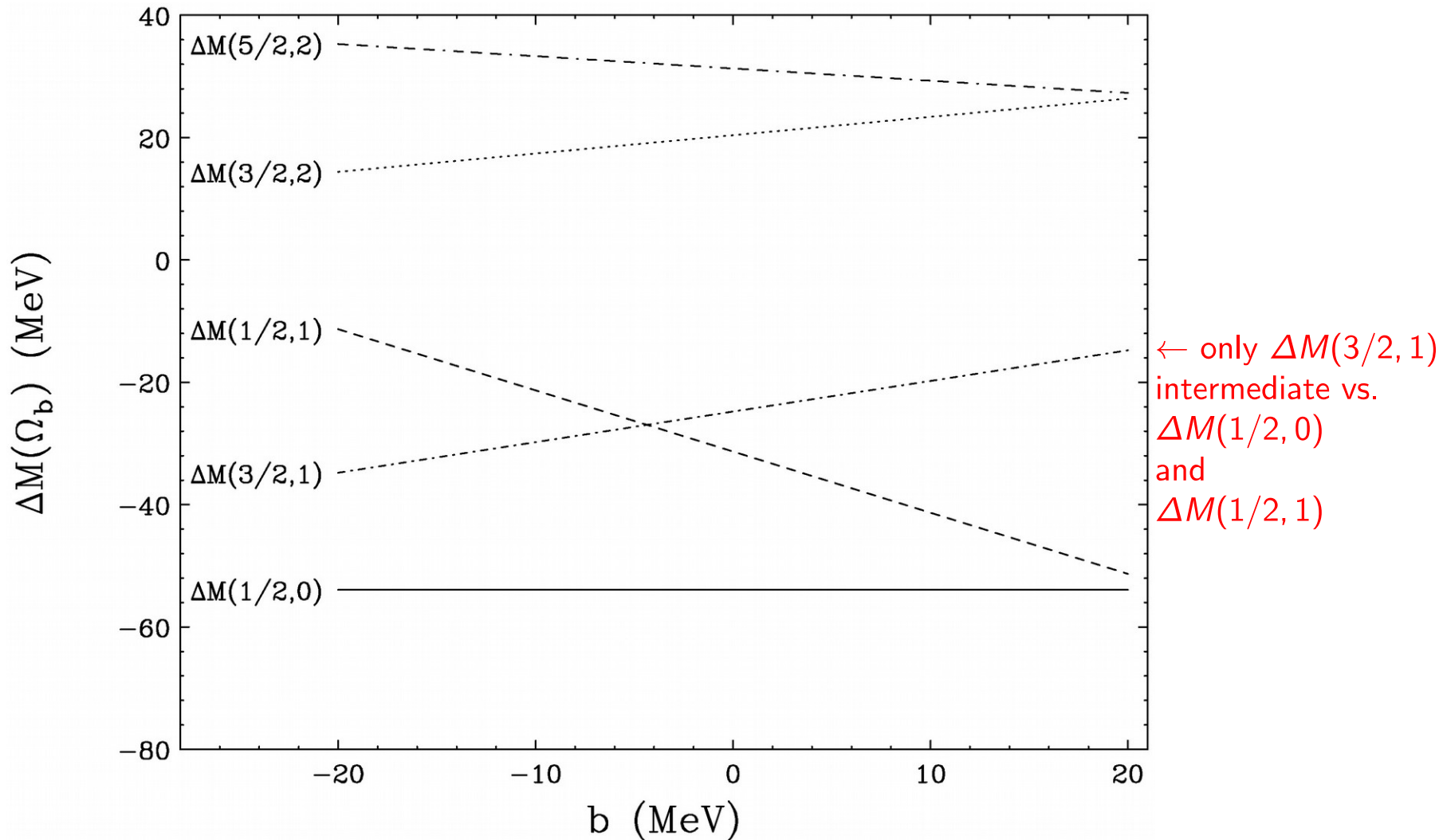
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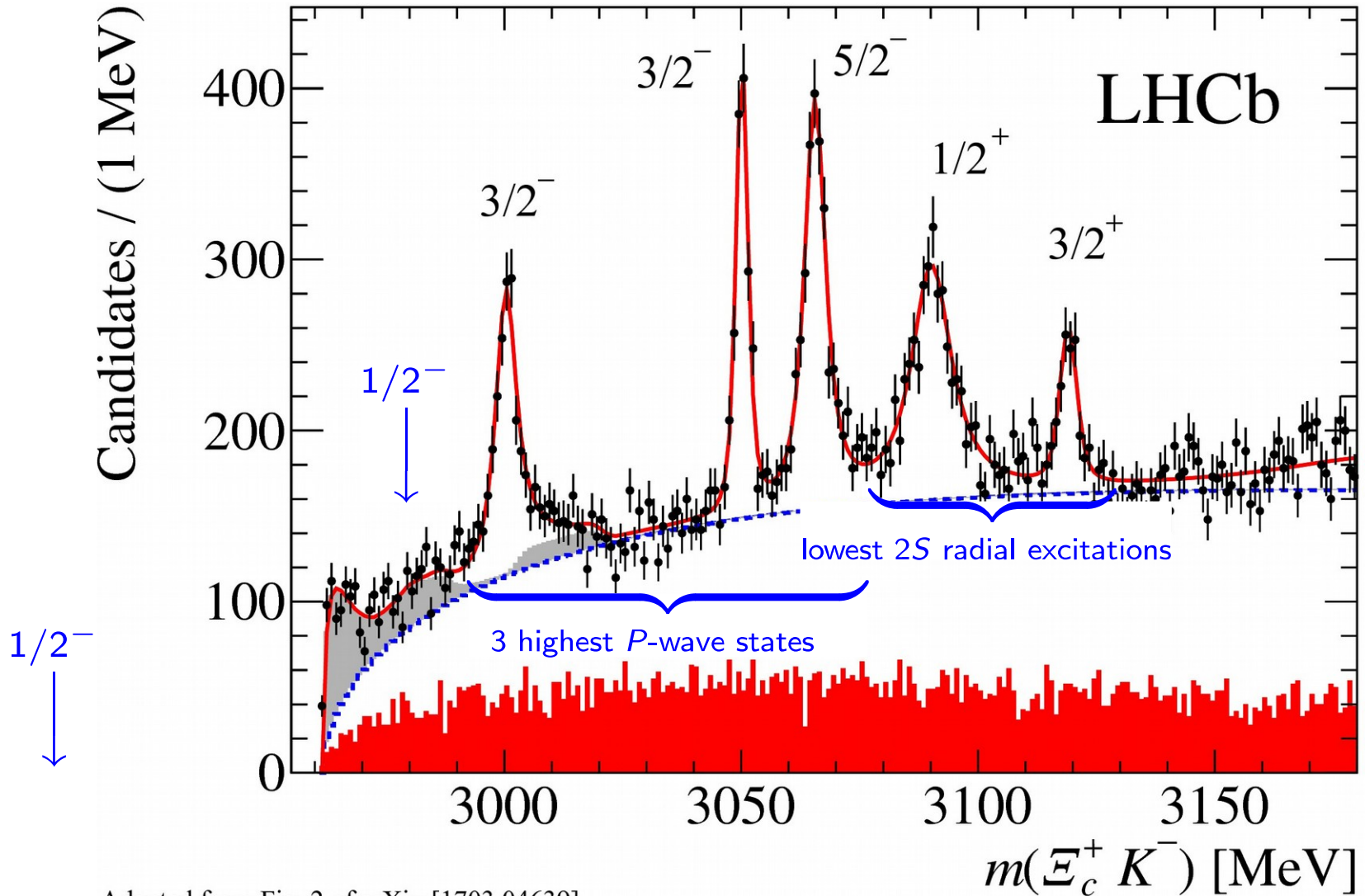
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caveat:  $\Xi_b^0 K^-$  threshold at 6286 MeV  
so lowest states might be below threshold



Masses of  $P$ -wave  $\Omega_b$  states as functions of tensor force parameter  $b$  in scenario with all five peaks observed by LHCb corresponding to  $P$ -wave excitations of the  $(ss)$  diquark with respect to the charmed quark.

# alternate $J^P$ assignment



Adapted from Fig. 2 of arXiv:[1703.04639]

# Upshot on new $\Omega_c$ states

- LHCb: 5 new excited  $\Omega_c$  states: v. narrow & v. high stats
- interpret as 5 states expected in  $P$ -wave  $c(ss)$  system :  
 $J^P = 1/2^-, 1/2^-, 3/2^-, 3/2^-, 5/2^-$   
awaits exp. confirmation, spin & parity meas.
- if instead 2 highest states are  $2S$ ,  $1/2^+$  and  $3/2^+$   
then 3 lowest are likely  $J^P = 3/2^-, 3/2^-, 5/2^-$
- then expect  $1/2^-$  near 2978 MeV  $\rightarrow \Xi_c^+ K^-$  in  $S$ -wave  
and  $1/2^-$  near 2904 MeV  $\rightarrow \Omega_c$  and/or  $\Omega_c/\pi^0$
- predictions for excited  $\Omega_b$ -s in  $b(ss)$  system

# narrow $B_{sJ}$ states

$b$ -quark analogues of the very narrow  $D_{sJ}$  states  
 $D_{s0}^*(2317)$  and  $D_{s1}(2460)$  (BaBar, CLEO and Belle)

e.g.  $D_{s0}^*(2317)$ ,  $J^P = 0^+$ , likely chiral partner of  $D_s$ :

$$m[D_{s0}^*(2317)] - m[D_s] = 345 \text{ MeV} \approx m_q^{\text{const.}}$$

below  $DK$  threshold  $\Rightarrow$  very narrow,  $\Gamma < 3.8 \text{ MeV}$ ,

decay: mainly  $D_{s0}^*(2317) \rightarrow D_s^+ \pi^0$

through v. small isospin-violating  $\eta-\pi^0$  mixing

detailed v. interesting predictions for  $b$  analogues  
 $\Rightarrow$  opportunity to test our understanding of  $\chi$ SB



# narrow $B_{sJ}$ states

$$J^P = 0^+: m(B_{s0}^*) \approx m(B_s) + 345 \text{ MeV} = 5712 \text{ MeV}$$

$$J^P = 1^+: m(B_{s1}) \approx m(B_s^*) + 345 \text{ MeV} = 5760 \text{ MeV}$$

both below relevant thresholds:

$$m(B) + m(K) = 5777 \text{ MeV}$$

$$m(B^*) + m(K) = 5822 \text{ MeV}$$

$\Rightarrow$  expect v. narrow widths

dominant decay modes:

$$B_{s0}^* \rightarrow B_s \pi^0, B_s^* \gamma$$

$$B_{s1} \rightarrow B_s^* \pi^0, B_s^{(*)} \gamma$$

# narrow $B_{sJ}$ states

$$J^P = 0^+: m(B_{s0}^*) \approx m(B_s) + 345 \text{ MeV} = 5712 \text{ MeV}$$

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dominant decay modes:

$$B_{s0}^* \rightarrow B_s \pi^0, B_s^* \gamma$$

$$B_{s1} \rightarrow B_s^* \pi^0, B_s^{(*)} \gamma$$

challenging @LHCb:  
soft  $\pi^0$  and  $\gamma$ , so  
large combinatorial  
background

• Belle II ?

$$e^+ e^- \rightarrow B_{s0}^* B_s^*$$

@11,127  $\pm$  10 MeV

# SUMMARY

- the new narrow exotic resonances are loosely bound states of  $\bar{D}D^*$ ,  $\bar{D}^*D^*$ ,  $\bar{B}^*B^*$ ,  $\Sigma_c\bar{D}^*$

predictions:

- $\bar{D}^*D^*$  in  $l = 0$  and  $l = 1$  channels;  $l = 1$  seen!
- *heavy deuterons*:  $\Sigma_c D^*$ : LHCb  $P_c(4450) \Rightarrow$  photoproduction  $\Sigma_c B^*$ ,  $\Sigma_b \bar{D}^*$ ,  $\Sigma_b B^*$ ,  $\Sigma_Q \bar{\Lambda}_{Q'}$ ,  $\Sigma_Q^+ \Sigma_Q^-$ , ...
- new isosinglet  $\bar{B}B^*$  and  $\bar{B}^*B^*$  states below threshold; hiding as  $\chi_{1b}(3P)$  ?
- $\eta$ -mediated:  $D_s \bar{D}_s^*$ ,  $\Lambda_c \bar{D}_s^*$ , ...
- doubly & triply heavy baryons  $QQq$ ,  $QQQ$  @  $pp$  &  $e^+e^-$
- $cc\bar{c}\bar{c}$  @  $6,192 \pm 25$  MeV and  $bb\bar{b}\bar{b}$  @  $18,826 \pm 25$  MeV  $\Rightarrow 4\ell$
- new excited  $\Omega_c$  states: spin dep. splittings  $\Rightarrow J^P$  prediction,  $\Omega_b$  analogues
- v. narrow  $B_{s0}^* \rightarrow B_s \pi^0$ ,  $B_s \gamma$  and  $B_{s1} \rightarrow B_s^* \pi^0$ ,  $B_s^{(*)} \gamma$

**exciting new spectroscopy awaiting discovery**