

# Heavy-quark spin-symmetry partners of $Z_b(10610)$ and $Z_b(10650)$ molecules

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Key Refs: PLB 763, 20 (2016) and arXiv:1704.07332 (JHEP 2017)



# Heavy quark spin symmetry

The XYZ states contain heavy quark and antiquark  $\implies$  employ heavy quark spin symmetry

☞ HQSS implies:

In the limit  $\Lambda_{\text{QCD}}/m_Q \rightarrow 0$  strong interactions are independent of HQ spin

☞ Consequences of HQSS — number of partner states, location and decay properties — are different for different scenarios Cleven et al. (2015)  
(talk by Christoph Hanhart)

$\implies$  Search for spin partner states  $\implies$  useful insights into the nature of XYZ states

This Talk: Discuss HQSS predictions for the molecular scenario

# Molecular partners: contact theory

- Basis states  $\mathbf{J}^{\mathbf{PC}}$  made of a Pseudoscalar (P) and a Vector (V):

C-parity states:  $C = \pm$        $PV(\pm) = \frac{1}{\sqrt{2}} (P\bar{V} \pm V\bar{P})$

$P = D$  or  $B$ ,       $V = D^*$  or  $B^*$

$$\begin{aligned} 0^{++} &: \{P\bar{P}(^1S_0), V\bar{V}(^1S_0)\}, \\ 1^{+-} &: \{P\bar{V}(^3S_1, -), V\bar{V}(^3S_1)\}, \\ 1^{++} &: \{P\bar{V}(^3S_1, +)\}, \\ 2^{++} &: \{V\bar{V}(^5S_2)\}. \end{aligned}$$

- Consequences of HQSS for S-wave contact interactions

Grinstein et al. (1992),  
AlFiky et al. (2006),  
Nieves and Valderrama (2012)

☞ only two parameters at LO: LECs  $C$  and  $C'$

☞  $V_{\text{LO}}^{(1^{++})}$  and  $V_{\text{LO}}^{(2^{++})}$  are the same!

☞  $C$  and  $C'$  –different for isoscalars and isovectors

$$\begin{aligned} V_{\text{LO}}^{(0^{++})} &= \frac{1}{4} \begin{pmatrix} 3C + C' & -\sqrt{3}(C - C') \\ -\sqrt{3}(C - C') & C + 3C' \end{pmatrix}, \\ V_{\text{LO}}^{(1^{+-})} &= \frac{1}{2} \begin{pmatrix} C + C' & C - C' \\ C - C' & C + C' \end{pmatrix}, \\ V_{\text{LO}}^{(1^{++})} &= V_{\text{LO}}^{(2^{++})} \equiv C \end{aligned}$$

- strict HQSS limit:  $V$ - $P$  mass splitting much smaller than all other scales

$$\delta = m_* - m \ll E_{\text{Bound}} \ll m$$

⇒ solutions of coupled-channel problem: two decoupled sets of partner states

$$E_{1^{++}}^{(0)} = E_{2^{++}}^{(0)} = E_{1^{+-}}^{(0)} = E_{0^{++}}^{(0)} \quad \text{and} \quad E_{0^{++}}^{(0)'} = E_{1^{+-}}^{(0)'}$$

our work (2016)

our finding is in line with Hidalgo-Duque et al. (2013)

# Contact theory with HQSS breaking

- Bondar et al. (2011), Voloshin (2011), Mehen and Powell (2011) propose a different expansion to account for HQSS breaking

$$E_{\text{Bound}} \ll \delta \ll m \quad \text{with}$$

$$\delta \simeq 140 \text{ MeV} \quad \delta/m \simeq 7\% \quad \text{in the c-sector}$$

$$\delta \simeq 45 \text{ MeV} \quad \delta/m \simeq 1\% \quad \text{in the b-sector}$$

- Leading effect — the states reside near their thresholds:  $P\bar{P}$ ,  $P\bar{V}$  and  $V\bar{V}$

For example:

$$M_{2^{++}} = M_{1^{++}} + \delta$$

- Next-to-leading terms  $O(\delta)$  and  $o\left(\frac{\gamma^2}{\sqrt{m\delta}}\right) \simeq o\left(\sqrt{\frac{E_{\text{bound}}}{\delta}}\gamma\right)$  our work (2016)

➡ Binding energies of  $1^{+-}$  and  $0^{++}$  states acquire an  $Im$  part due to coupled-channels

$$D^* \bar{D}^* \rightarrow D \bar{D}^* \rightarrow D^* \bar{D}^*$$

$$B^* \bar{B}^* \rightarrow B \bar{B}^* \rightarrow B^* \bar{B}^*$$

➡  $2^{++}$  tensor state is uncoupled  $\implies$  has no  $Im$  part in the contact problem

# Contact + one-pion exchange (OPE) interactions

- Extended basis states:

$$0^{++} : \{P\bar{P}(^1S_0), V\bar{V}(^1S_0), V\bar{V}(^5D_0)\},$$

$$1^{+-} : \{P\bar{V}(^3S_1, -), P\bar{V}(^3D_1, -), V\bar{V}(^3S_1), V\bar{V}(^3D_1)\},$$

$$1^{++} : \{P\bar{V}(^3S_1, +), P\bar{V}(^3D_1, +), V\bar{V}(^5D_1)\},$$

$$2^{++} : \{P\bar{P}(^1D_2), P\bar{V}(^3D_2), V\bar{V}(^5S_2), V\bar{V}(^1D_2), V\bar{V}(^5D_2), V\bar{V}(^5G_2)\}$$

- Coupled-channel transitions in S, D and even G-waves

- coupled-channel dynamics is very important: inconsistent omission

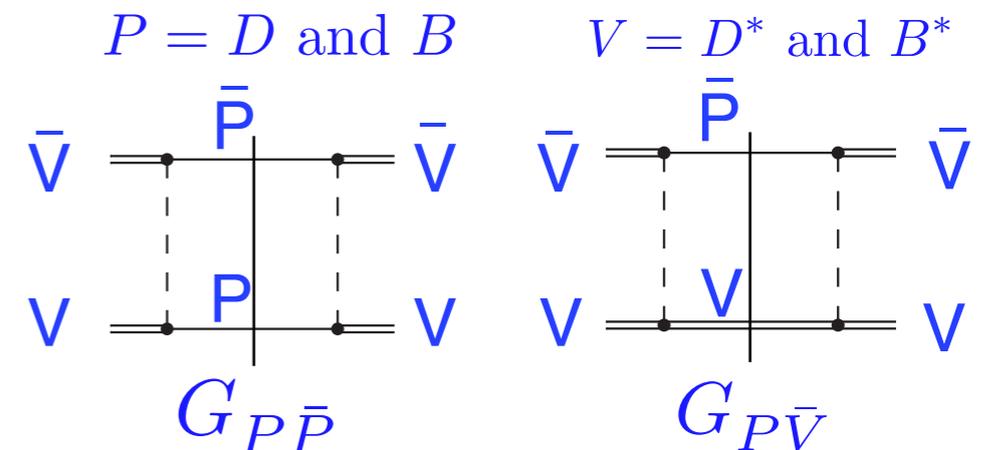
our work (2016)

(as done by Nieves, Valderrama (2012))  $\implies$  strongly cutoff dependent results

- Pions enhance HQSS violation due to V-P mass splitting

$P\bar{P}$  and  $P\bar{V}$  intermediate states can go on shell

$\implies$  also  $2^{++}$   $V\bar{V}$  states acquire finite widths



- pionic (S-D) tensor forces play dominant role due to relatively large momentum scales

$\implies$  Non-perturbative pion dynamics is to be important

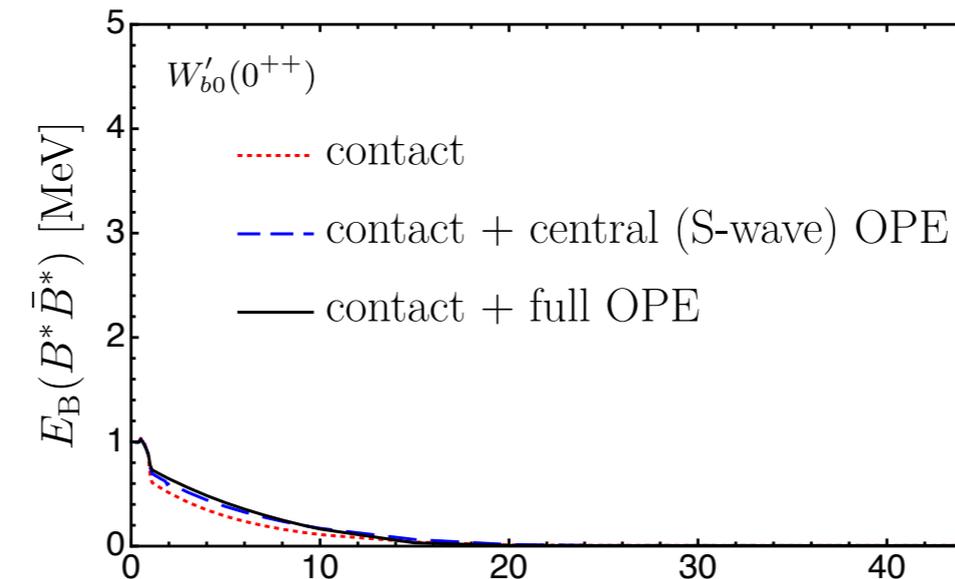
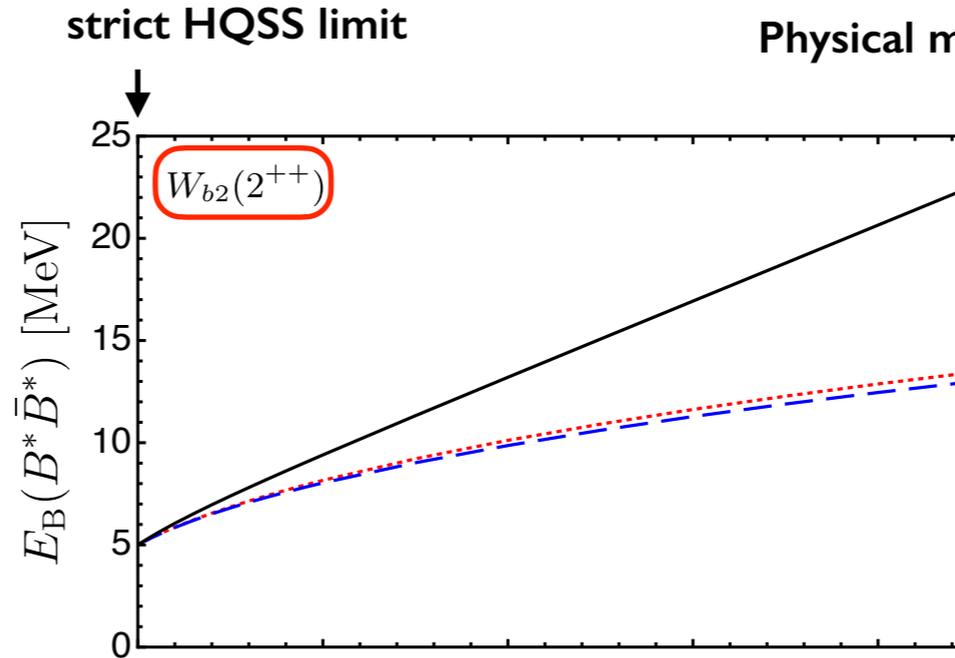
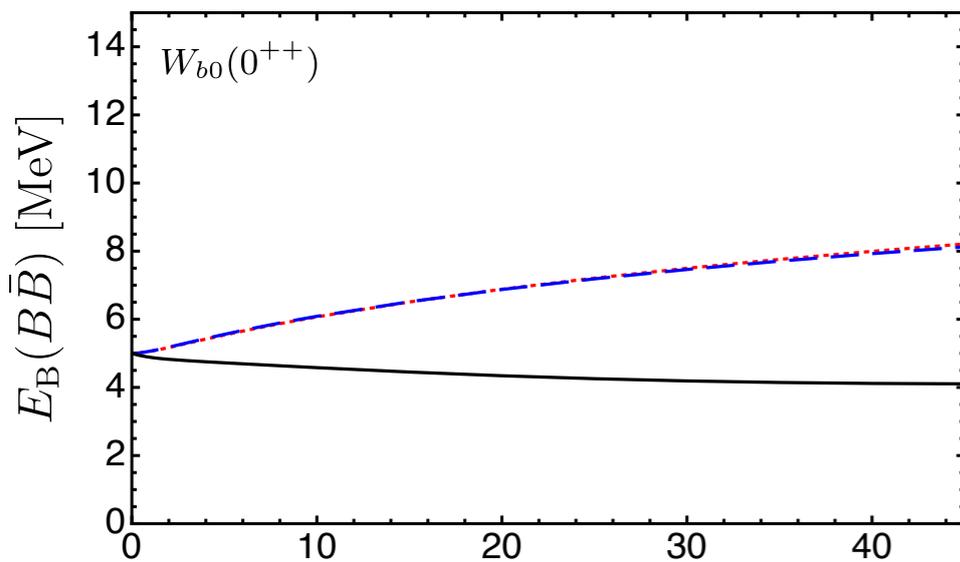
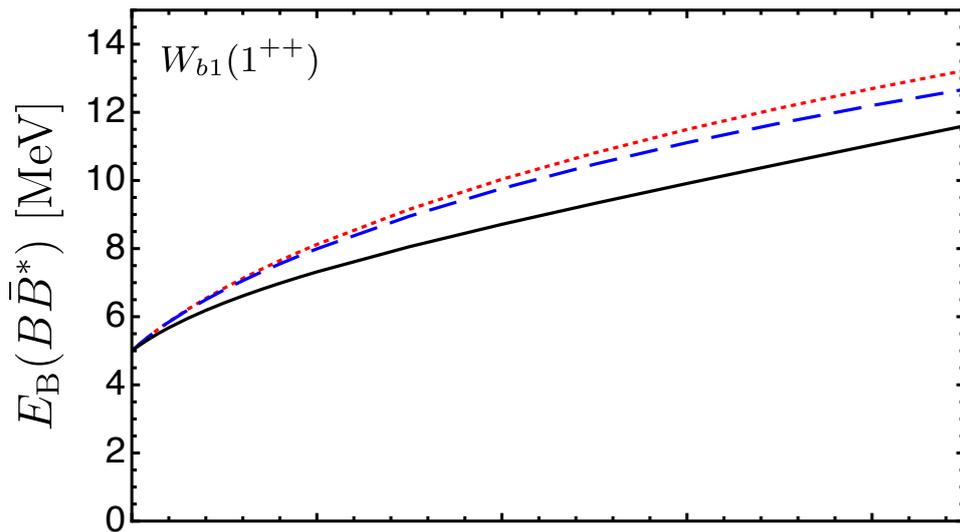
# Chiral EFT based approach for hadronic molecules

Our works: PLB 763, 20 (2016), arXiv:1704.07332 (JHEP 2017)

- A systematic approach for studying various molecular candidates with special emphasis on:
  - ☞ pionic dof, coupled-channel dynamics, HQSS and the pattern of its breaking
  - ☞ three-body effects ( $P\bar{P}\pi$ ) and the  $\eta$ -meson from SU(3) GB octet are included also
- nonperturbative solutions of the LS integral Eqs. for various  $J^{PC} = 1^{++}, 2^{++}, 0^{++}$  and  $1^{+-}$ 
  - ☞ Potential: contact operators (2 parameters) + OPE  $\Rightarrow$  input is needed!
  - ☞ leading HQSS violation is included via the  $V$ - $P$  mass splitting
- Can be applied to study very different aspects of light quark dynamics:
  - ☞ identification of the long-distance modes in the resonance w.f. Our works (2010)
  - ☞ implications of HQSS:  $1^{++}$  X(3872),  $1^{+-}$  Zb(10610)/Zb(10650), ... 
  - ☞ chiral extrapolations of lattice results Our works (2013), (2015)

# Application: HQSS partners of Zb(10610)/Zb(10650)

Our work: arXiv:1704.07332 (JHEP 2017)



$\delta$  [MeV] ← **B\*-B mass splitting** →  $\delta$  [MeV]

Input:  
 $E_{Zb} = 5 \text{ MeV}$   
 $E_{Zb'} = 1 \text{ MeV}$   
 consistent with Belle  
 Cleven et al. (2011)

Refit contact terms  
 for each value of  $\delta$ !

•  $W_{b2}(0^{++})$ ,  $W_{b2}(1^{++})$  and  $W_{b2}(2^{++})$  remain bound for physical  $\delta$ ,  $W'_{b2}(0^{++})$  turn to be virtual

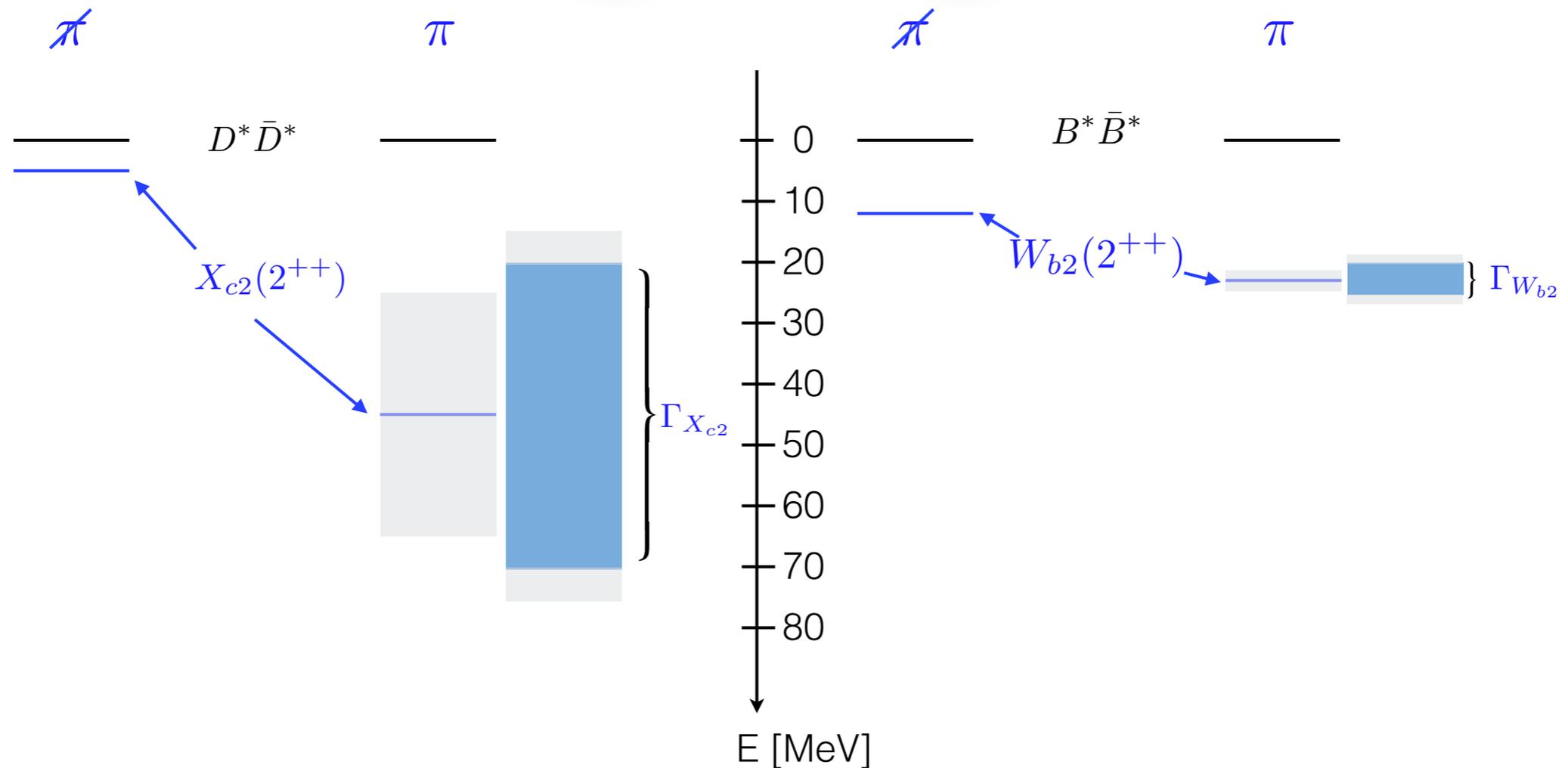
- $W_{b2}(2^{++})$  state:
  - ➡ Binding energy exhibits large HQSS violation
  - ➡ OPE Tensor forces: large shift of  $E_B$
  - ➡ Effect of  $\eta$ -meson is opposite to OPE but minor

# HQSS implications: $X(3872)$ vs $Z_b(10610)/Z_b(10650)$

Our works: PLB 763, 20 (2016), arXiv:1704.07332 (JHEP 2017)

$2^{++}$  tensor partner

$X_{c2}$  vs  $W_{b2}$



Impact of HQSS violation together with nonperturbative pions on the tensor:

- ➡ much larger than with perturbative pions
- ➡ much stronger in the c-sector than in the b-sector

For perturbative approach see Albaladejo et al. (2015)

# Summary

- We propose a systematic approach consistent with chiral and heavy quark symmetries and including all relevant scales to probe various molecular candidates in  $c$  and  $b$ -sectors
- Applied in this talk to predict HQSS partners of  $X(3872)$  and  $Z_b(10610)/Z_b(10650)$
- ➡ HQSS breaking and non-perturbative pions have significant impact on the partner states
- ➡ The effect from OPE is stronger in the  $c$ -quark sector, than in the  $b$ -quark one.

$X_{c2^{++}}$  is significantly shifted from  $D^*D^*$  threshold and has the width  $\Gamma_{X_{c2^{++}}} \simeq 50 \pm 10$  MeV

$W_{b2^{++}}$  is still located around  $B^*\bar{B}^*$  threshold and has a few MeV width

⇒ should be detectable in  $BB^{(*)}$  and also in  $\chi_{b1}\pi$  and  $\chi_{b2}\pi$  channels

- To predict other partners of the  $X(3872)$  one more experimental input is needed

Could  $X(3915)$  be a  $0^{++}$  molecule — spin partner of  $X(3872)$ ?



# Spares

# HQSS partners of the $Z_b(10610)$ and $Z_b(10650)$

A comment on the sign of the OPE potential in isoscalar and isovector channels:

- Isospin coefficient:  $3 - 2 I (I + 1) = \begin{cases} 3 & I=0 \\ -1 & I=1 \end{cases}$  — different signs

- sign also depends on C-parity

☞ central (S-wave) OPE for **isospin-0**  $0^{++}$ ,  $1^{++}$  and  $2^{++}$  states is attractive for  $1^{+-}$  — repulsive

☞ central (S-wave) OPE for **isospin-1**  $0^{++}$ ,  $1^{++}$  and  $2^{++}$  states is repulsive for  $1^{+-}$  — attractive

⇒ Naively, OPE should reduce the binding energies of the partner states

$W_{b2}(0^{++})$ ,  $W_{b2}(1^{++})$  and  $W_{b2}(2^{++})$

⇒ But tensor forces (off diagonal transitions) bring additional attraction!