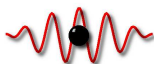




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Physique Quantique



fnrs
FREEDOM TO RESEARCH

Study of corrections to the eikonal approximation

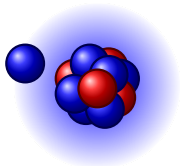
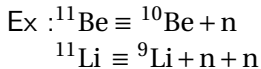
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Motivation

- **Halo nuclei** exhibit a very large matter radius
Compact core + one or two loosely-bound neutrons

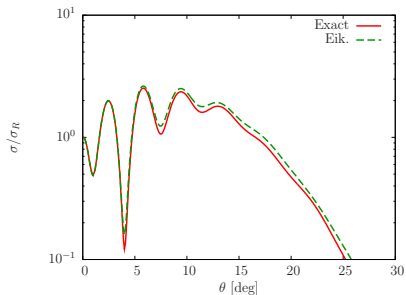


- Short-lived : Studied through **reactions processes**
(elastic scattering, breakup reactions,...)

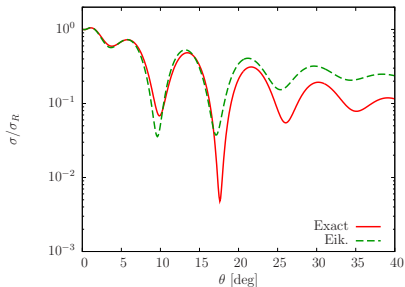
⇒ **Need an accurate reaction model to infer reliable information**

- **The eikonal approximation :**
 - ⊕ **reduced computational time**
 - ⊕ **simple interpretation of the reaction**
 - ⊖ **valid only at high energies**

Elastic scattering ^{10}Be off ^{12}C



67A MeV



10A MeV

Is it possible to improve the accuracy of the eikonal approximation at low energies?

See my poster to find out !

Study of corrections to the eikonal approximation

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Motivation

- **Heavy nuclei:** exotic structures with large neutron radius due to one or two heavily bound neutrons
- **Exotic as a magnetic state with one or two valence neutrons**

Ex. ¹²Be is ¹²Be + n



¹²Be + ¹²C → α + α

Short-fused:

→ Cannot be studied through spectroscopic methods

→ Studied through reaction processes

elastic scattering, breakup reactions...

→ Need an accurate reaction model to infer

valuable information

• **The eikonal model** is a quasilocal approximation which

□ has a **reduced computational time**

□ (since it only uses exact calculations)

□ provides a **simple interpretation** of the reaction

□ is **valid only at high energies**

□ or **Aim of this study:**

extend its range of validity to low energies

The eikonal approximation and its corrections

Assumptions:

- Central potential V simulating the projectile (P) - target (T) interaction
- In a first step, **elastic scattering** of structure and spinless nuclei

Schrodinger equation: $\left(\frac{\partial^2}{\partial r^2} + k^2 + V(r) \right) \Psi(r) = k^2 \Psi(r)$, where μ is the P - T reduced mass and E the energy

The eikonal approximation: at high energy, the wave function is plane wave [1]

$$\Psi(r) \approx e^{i\mathbf{k} \cdot \mathbf{r}} \Psi(b) \quad \text{with } |\mathbf{k}_\perp| \ll k \ll |\mathbf{k}|$$

→ **Solutions:** $\Psi(r) \approx e^{i\mathbf{k} \cdot \mathbf{r}} \exp(i\chi(b))$ with $\chi(b) = -\frac{1}{k} \int_{-\infty}^{\infty} V(\sqrt{b^2 + z^2}) dz$ the **eikonal phase**

P is seen as following a **straight-line** (blue) which it accumulates a phase through its interaction with T .

At low energy, P is deflected by T → eikonal approximation not valid

→ **Two corrections to account for the deflection:**

□ **Widline's correction:** perturbation development of the T matrix [2]

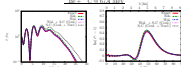
$$T = (1 + V\chi^2)^{-1} + V\chi^2(1 + \dots) \quad \text{where } \chi \text{ is the eikonal propagation}$$

□ **The semi-classical correction:** $\chi(b) \rightarrow \chi^s(b)$, where V is the P - T distance of closest approach computed using the real part of the potential [3,6]

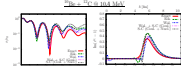


Cross sections and eikonal phases of the elastic scattering of ²⁰Ne off ¹²C

²⁰Ne + ¹²C → ²⁰Ne + ¹²C



²⁰Ne + ¹²C → ²⁰Ne + ¹²C



□ **Widline's correction** [Wid.]

□ **semi exact results** at 60 & 80 MeV but low deflection at 10 & 20 MeV

□ **better reproduction** of the oscillation pattern of the cross sections

□ **shift of the results** θ to forward angles

□ $\chi^s(b)$ to large b

□ $\chi^s(b)$ to large b

□ **Semi-classical correction** to only the Coulomb interaction (Wid. + S-C (Coul.))

□ **compensation of the shift** θ to large angles

□ **better agreement with the exact results**

□ **inaccurate at low energies and large angles**

□ **lack of absorption at small b**

□ **The semi-classical correction to the whole interaction** (S-C (Coul. + Nul.))

□ **more accurate results** at forward scattering angles

□ **better reproduction** of the oscillations

□ **insufficient at large angles**

□ **lack of absorption at small b**

Conclusions and prospects

□ **Widline's correction:** small extension to low energies

□ not sufficient at very low energies and large angles

□ **The semi-classical correction:** not accurate at large angles

□ **Lack of absorption** at small b and large angles

□ **To overcome absorption** use a complex distance of closest approach computed with the whole optical potential

□ **Generalization** to two- and three-body projectile and breakup reactions

References

- [1] R. J. Glauber, High energy collision theory, Lecture in theoretical physics, (1962)
- [2] S. J. Widline, Ann. Phys. **78**, 100 (1972)
- [3] C. R. Adams, F. Zach and A. Vignani, Phys. Rev. C **56**, 1531 (1997)
- [4] T. Fink, K. Ogata, and P. Capel, Phys. Rev. C **90**, 034617 (2014)



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