**Evgeny Epelbaum, RUB** 

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# Status and perspectives of nuclear chiral EFT



- Chiral NN forces
- Uncertainty quantification
- Few-N systems and the quest for 3NF
- Electroweak current operators





## **EFTs for nuclear physics**



A = 0,1: Chiral perturbation theory



A > 1: Halo-EFT (Q << ( $\Delta E_{core} m$ )<sup>1/2</sup>), pionless EFT (Q << M<sub> $\pi$ </sub>), chiral EFT (Q ~ M<sub> $\pi$ </sub>)



A >> 1: In-medium chiral EFT; EFTs using collective DOFs (e.g. to describe deformed nuclei)



### **Chiral perturbation theory**

• Ideal world [ $m_u = m_d = 0$ ], zero-energy limit: non-interacting massless GBs (+ strongly interacting massive hadrons)

• Real world [ $m_u$ ,  $m_d \ll \Lambda_{QCD}$ ], low energy: weakly interacting light GBs (+ strongly interacting massive hadrons)

expand about the ideal world (ChPT)

### Chiral Perturbation Theory Weinberg, Gasser, Leutwyler, Meißner, ...

#### Expansion of the scattering amplitude in powers of

 $Q = \frac{\text{momenta of pions and nucleons or } M_{\pi} \sim 140 \text{ MeV}}{\text{hard scales [at best } \Lambda_{\chi} = 4\pi F_{\pi} \sim 1 \text{ GeV}]} \text{ Manohar, Georgi '84}$ 

Tool: Feynman calculus using the effective chiral Lagrangian



#### Pion-nucleon scattering up to Q<sup>4</sup>

Fettes, Meißner '00; Becher, Leutwyler '01; Krebs, Gasparyan, EE '12; Alarcon, Camalich, Oller '12; Chen, Yao, Zheng '13; Wendt et al. '14; Siemens et al. '16; Yao et al. '16, ...



### **Nuclear chiral EFT**

Chiral EFT for nuclear systems: expansion for nuclear forces + resummation (Schrödinger eq.) Weinberg, van Kolck, Kaiser, EE, Glöckle, Meißner, Entem, Machleidt, Krebs, ...

$$\left[\left(\sum_{i=1}^{A} \frac{-\vec{\nabla}_{i}^{2}}{2m_{N}} + \mathcal{O}(m_{N}^{-3})\right) + \underbrace{V_{2N} + V_{3N} + V_{4N} + \dots}_{\text{derived in ChPT}}\right] |\Psi\rangle = E|\Psi\rangle \qquad \boxed{\mathbf{T}} = \underbrace{\mathbf{V}_{\text{eff}}}_{\mathbf{V}} + \underbrace{\mathbf{$$

#### Notice:

- Much more involved than calculating Feynman diagrams (unitary trafos, TOPT, S-matrixmatching, ...), potentials are not unique, renormalizability is not guaranteed a priori...
- LS equation is linearly divergent already at LO 
   —> infinitely many CTs are needed to absorb all UV divergences from iterations!

Commonly used approach [EGM, EM, EKM, Gezerlis et al.'14, Piarulli et al.'15, Carlsson et al.'16, ...]:

- Introduce a finite UV regulator R  $\sim R_b~(\Lambda_b \sim 600~MeV)$
- Include short-range operators in V<sub>NN</sub> according to NDA ← <sup>minimal possible set;</sup> alternatives have been proposed...
- Solve the LS equation & tune the **bare** LECs C<sub>i</sub>(R) to data (implicit renormalization)
- (Numerical) self-consistency checks via error analysis and R-variation
   See: Lepage, "How to renormalize the Schrödinger equation", nucl-th/9607029 and talk@INT in 2000

Alternative: renormalizable approach based on the Lorentz invariant  $\mathcal{L}_{eff}$  [EE, Gegelia '12]

See also: *Nuclear Effective Field Theories — the crux of the matter*, open discussion by Mike Birse and EE at the KITP program "Frontiers in Nuclear Physics", August 22 - November 4, 2016, available at <u>http://online.kitp.ucsb.edu/online/nuclear16/</u>

### Chiral expansion of the nuclear forces



Why go to fifth order (N<sup>4</sup>LO) in the chiral expansion?

- no additional parameters in the NN force (except for 1 IB term)  $\rightarrow$  testing the theory
- there is evidence that  $\chi$ -expansion for the 3NF is not yet converged at Q<sup>4</sup>

### The long-range part of the nuclear forces

Long-range nuclear forces are completely determined by the chiral symmetry of QCD + experimental information on  $\pi N$  scattering



The TPE potential can be derived by taking the phase-space integral of the  $\pi$ N amplitudes computed in ChPT (Lorentz-transformed to the proper kinematics...) Kaiser '00

### Determination of the low-energy constants

#### All relevant LECs (in GeV<sup>-n</sup>) extracted from $\pi N$ scattering Krebs, Gasparyan, EE '12

	$c_1$	$c_2$	C <sub>3</sub>	$c_4$	$\bar{d}_1 + \bar{d}_2$	$\bar{d}_3$	$\bar{d}_5$	$\bar{d}_{14} - \bar{d}_{15}$	$\bar{e}_{14}$	$\bar{e}_{17}$
$[Q^4]_{\rm HB, NN},  {\rm GW  PWA}$	-1.13	3.69	-5.51	3.71	5.57	-5.35	0.02	-10.26	1.75	-0.58
$[Q^4]_{\rm HB,NN},{\rm KH}$ PWA	-0.75	3.49	-4.77	3.34	6.21	-6.83	0.78	-12.02	1.52	-0.37
$[Q^4]_{\rm covariant},{\rm data}$	-0.82	3.56	-4.59	3.44	5.43	-4.58	-0.40	-9.94	-0.63	-0.90

Related recent work (all calculations lead to similar values of the LECs ):

- determination of the LECs from  $\pi N$  data wendt et al. '14; Siemens et al. '16
- LECs from Roy-Steiner-eq. analysis of  $\pi$ N-scattering Hoferichter et al. '15; Yao et al. '16; Siemens et al. '16

With the LECs taken from  $\pi N$ , the long-range NN force is completely fixed (parameter-free)

#### The short-range part of the nuclear force (contact interactions)

Organizational principle for contact terms according to NDA (Weinberg's counting)



#### Local r-space regulator for $V_{\pi}$ [R = 0.8...1.2 fm], nonlocal Gaussian regulator for $V_{cont}$

### NN phase shifts order by order [R = 0.9 fm]

EE, Krebs, Meißner, EPJ A51 (2015) 5, 53; PRL 115 (2015) 122301



#### Other chiral NN potentials on the market:

- 1st generation χ N<sup>3</sup>LO forces (nonlocal) [Epelbaum-Glöckle-Meißner '04, Entem-Machleidt '03]
- fully local potentials up to N<sup>2</sup>LO [Gezerlis et al. '14]; minimally nonlocal N<sup>3</sup>LO potential including N<sup>2</sup>LO Δ(1232) contributions [Piarulli et al.'15]
- N<sup>2</sup>LO potentials by the Oak Ridge group tuned to heavier nuclei [Ekström, Carlsson et al.]

### Evidence of the $2\pi$ -exchange

#### Predictive power?

Long-range interactions are completely determined by the chiral symmetry & experimental information on  $\pi N$  scattering



predicted in a parameter-free way

	TO	NT O	N2T O		MAT O	
Energy bin	LO	NLO	N <sup>2</sup> LO	NºLO	N⁴LO	
neutron-proton dat	a					
$0-100~{\rm MeV}$	130.11	3.79 no new	1.46	1.08 +1 LEC	1.08	
$0-200~{\rm MeV}$	104.71	19.88	3.21	1.14 ( <sup>1</sup> S <sub>0</sub> )	1.09	
$0-300~{\rm MeV}$	111.24	52.03	8.78	1.51	1.15	
proton-proton data						
$0-100~{\rm MeV}$	2046.58	33.68	6.67	0.86 no new	0.84	
$0-200~{\rm MeV}$	1649.58	115.60	81.11	$1.95 \xrightarrow{LECs}$	1.34	
$0-300 { m MeV}$	1301.41	104.38	84.24	2.73	1.46	
	2 LECs	+ 7 + 2 IB LECs		+ 15 LECs	+ 1 IB LE(	C

#### preliminary: Reinert et al., in preparation

Clear evidence of the (parameter-free) chiral  $2\pi$ -exchange!

### **Uncertainty quantification**

A simple algorithm for estimating uncertainty from the truncation of the chiral expansion: EE, Krebs, Meißner, EPJA 51 (2015) 53

For any observable: 
$$X^{(i)}(p) = X^{(0)} + \Delta X^{(2)} + \dots + \Delta X^{(i)}$$
  
 $\sim Q^2 X^{(0)} + \dots + \Delta X^{(i)}$   
 $\sim Q^i X^{(0)}$  with  $Q = \max(p/\Lambda_b, M_\pi/\Lambda_b)$ 

Use the explicitly calculated  $\Delta X^{(i)}$  to estimate the uncertainty  $\delta X^{(i)}$  at order Q<sup>i</sup>:

 $\delta X^{(0)} = Q^2 |X^{(0)}|,$ 

 $\delta X^{(i)} = \max_{2 \leq j \leq i} \left( Q^{i+1} | X^{(0)} |, \, Q^{i+1-j} | \Delta X^{(j)} | 
ight)$ 

subject to the additional constraint

 $\delta X^{(i)} \, \geq \, \max_{j,k} ig( |X^{(j \geq i)} - X^{(k \geq i)}| ig).$ 

- no reliance on the cutoff variation (not reliable)
- easily applicable to any observable (scattering, bound states, 3N, ...)
- of course, no reliance on exp. data
- for σ<sub>tot</sub>, errors found to be consistent with 68% degree-of-belief intervals
   Furnstahl et al., PRC 92 (2015) 024005

#### proton-neutron scattering observables at Elab=143 MeV



### **Examples in the NN sector**

#### What accuracy is achievable?

#### Chiral expansion of the neutron-proton total cross section



#### Scattering lengths and effective range parameters extracted from the data

	predictions at N <sup>4</sup> LO	Experimental/Empirical values
neutron-proton		
$a_{^{1}S_{0}}$ [fm]	-23.733(6)	-23.740(20)
$r_{^{1}\mathrm{S}_{0}}$ [fm]	2.677(7)	2.77(5)
$a_{^{3}S_{1}}$ [fm]	5.419(1)	5.419(7)
$r_{^{3}\mathbf{S}_{1}}$ [fm]	1.752(0)	1.753(8)
proton-proton		
$a_{^{1}S_{0}}$ [fm]	-7.816(1)	-7.817(4)
$r_{^{1}S_{0}}$ [fm]	2.773(2)	2.78(2)

preliminary: Reinert et al., in preparation

# **Beyond the 2N system**

**LENPIC Collaboration** 

Goal: precision tests of chiral nuclear forces & currents in light nuclei

Strategy: go to high orders, do not compromise the  $\pi$ N LECs, no fine tuning to heavy nuclei, careful error analysis



### **Few-N results without 3NF**

LENPIC Collaboration (Binder et al.), PRC 93 (2016) 04402

#### Is there evidence for missing 3N forces effects? Yes!



• Discrepancies between theory and data well outside the range of quantified uncertainties

→ clear evidence for missing 3NF effects

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• Magnitude of the required 3NF contributions matches well the estimated size of N<sup>2</sup>LO terms

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National Laboratory

→ consistent with the chiral power counting

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LENPIC: Low Energy Nuclear Physics International Collaboration

### **Few-N results without 3NF**

LENPIC Collaboration (Maris et al.), EPJ Web of Conf. 113 (2016) 04015



### **Brueckner-Hartree-Fock without 3NF**

Jinniu Hu, Ying Zhang, EE, Ulf-G. Meißner, Jie Meng, arXiv:1612.05433 [nucl-th]



----- Estima

Estimated accuracy at N<sup>4</sup>LO at the saturation density:

± 0.3 MeV for SNM, ± 0.7 MeV for PNM

$$a_{
m symm}(
ho) = \left(rac{E}{A}
ight)_{
m PNM} - \left(rac{E}{A}
ight)_{
m SNM}$$

$$L=3
horac{\partial(E/A)_{
m SNM}}{\partial
ho}$$

### **Chiral expansion of the 3NF**



## Some PRELIMINARY results with 3NF

The LECs D, E are determined from the <sup>3</sup>H and the Nd cross section minimum @70 MeV (RIKEN data)

#### The results are **preliminary**:

 still have to analyze different ways to determine D and E, check other sources of uncertainties, ...

 $c_i$ 



### Nuclear systems from lattice χEFT

#### **Nuclear lattice simulations:**

A novel ab initio approach to nuclei and nuclear reactions D. Lee, EE, H. Krebs, T. Lähde, T. Luu, U.-G. Meißner, G. Rupak, ...

#### Some recent highlights:

Ab initio calculation of the Hoyle state

EE, H. Krebs, D. Lee, U.-G. Meißner, PRL 106 (11) 192501; EE, H. Krebs, T.A.Lähde, D. Lee, U.-G. Meißner, PRL 109 (12) 252501

Viability of Carbon-based life as a function of light quark masses EE, H. Krebs, T. A. Lähde, D. Lee, U.-G. Meißner, PRL 110 (13) 112502; EPJA 49 (13) 82

Ab initio calculation of the spectrum and structure of <sup>16</sup>O EE, H. Krebs, T. A. Lähde, D. Lee, U.-G. Meißner, G. Rupak, PRL 112 (14) 102501

Lattice EFT for medium-mass nuclei ("triangulation" method for Euclidean-time extrapol.)

T. A. Lähde, EE, H. Krebs, D. Lee, U.-G. Meißner, G. Rupak, PLB 732 (14) 110

 $E_{8Be, old} = -55(2) \text{ MeV}$  $E_{8Be, new} = -56.4(2) \text{ MeV}$ 

### Symmetry-sign extrapol.

T.A. Lähde, T. Luu, D. Lee, U.-G. Meißner, EE, H. Krebs, G. Rupak, EPJ A51 (15) 92

Nuclear binding energy near a quantum phase transition

Elhatisari et al., PRL 117 (2016) 132501





### Nuclear systems from lattice χEFT

Lab

### nature

#### Ab initio alpha-alpha scattering

Serdar Elhatisari<sup>1</sup>, Dean Lee<sup>2</sup>, Gautam Rupak<sup>3</sup>, Evgeny Epelbaum<sup>4</sup>, Hermann Krebs<sup>4</sup>, Timo A. Lähde<sup>5</sup>, Thomas Luu<sup>1,5</sup> & Ulf–G. Meißner<sup>1,5,6</sup>

Nature 528, 111–114 (03 December 2015) | doi:10.1038/nature16067 Received 12 June 2015 | Accepted 30 September 2015 | Published online 02 December 2015

#### First ab initio calculation of alpha-alpha scattering!

Used lattice EFT to extract the effective Hamiltonian for two interacting α-clusters (adiabatic projection method [A. Rokash et al., PRC 92 (15) 054612])



Phase shifts obtained  $[emp] = [N_{\tau}^{-1/2}H_{\tau}N_{\tau}^{-1/2}]_{R,R}^{\ell,\ell_2}$ loying a hard spherical wall boundary at asymptotically large distances

Promising scaling with respect to the number of particles as  $\sim (A_1 + A_2)^2$ 



6

E<sub>Lab</sub> (MeV)

8

10

12

0

2

### Neutron skin of <sup>48</sup>Ca

#### nature physics

#### ARTICLES

PUBLISHED ONLINE: 2 NOVEMBER 2015 | DOI: 10.1038/NPHYS352

### Neutron and weak-charge distributions of the <sup>48</sup>Ca nucleus

G. Hagen<sup>1,2\*</sup>, A. Ekström<sup>1,2</sup>, C. Forssén<sup>1,2,3</sup>, G. R. Jansen<sup>1,2</sup>, W. Nazarewicz<sup>1,4,5</sup>, T. Papenbrock<sup>1,2</sup>,
 K. A. Wendt<sup>1,2</sup>, S. Bacca<sup>6,7</sup>, N. Barnea<sup>8</sup>, B. Carlsson<sup>3</sup>, C. Drischler<sup>9,10</sup>, K. Hebeler<sup>9,10</sup>,
 M. Hjorth-Jensen<sup>4,11</sup>, M. Miorelli<sup>6,12</sup>, G. Orlandini<sup>13,14</sup>, A. Schwenk<sup>9,10</sup> and J. Simonis<sup>9,10</sup>

- First ab-initio (coupled-cluster) calculation of the neutron distribution in <sup>48</sup>Ca
- Used NNLO<sub>sat</sub> NN + 3NF tuned to energies and radii of up to A ~ 25 nuclei (also EM N<sup>3</sup>LO NN + N<sup>2</sup>LO 3NF)



• Neutron skin significantly smaller than expected from DFT and robust (correlations)

 $\bullet$  Prediction of the electric dipole polarizability  $\alpha_D$ 

# Nuclear current operators in chiral EFT



#### **EM currents:**

- Kölling, EE, Krebs, Meißner (method of UT), PRC 80 (09) 045502; 86 (12) 047001
- Jlab-Pisa group (TOPT), Pastore et al. '08 '11

#### **Axial currents:**

- Krebs, EE, Meißner (MUT), arXiv:1610.03569, to appear in Annals of Physics
- Jlab-Pisa group (TOPT), Baroni et al. '16
- Hoferichter, Klos, Schwenk '15



### (Our) requirements on the current operators:

- must be off-shell consistent with the forces
- should be **renormalized** (exploit unitary ambiguity)
- (cutoff) regularization of the forces and currents should **maintain the symmetry** (cont. equation)

### **Electromagnetic currents**

### Chiral expansion of the electromagnetic current and charge operators



### Electromagnetic exchange currents

Skibinski, Golak, Topolnicki, Witala, EE, Krebs, Kamada, Meißner, Nogga, PRC 93 (2016) 064002

- To maintain consistency between currents and forces (symmetry), we generate regularized longitudinal terms in the current via the continuity equation (i.e. Siegert approach).
- Transverse terms in the currents are to be regularized and included explicitly (in progress...)



### Magnetic form factors of <sup>3</sup>He, <sup>3</sup>H

Piarulli, Girlanda, Marcucci, Pastore, Schiavilla, Viviani, Phys. Rev. C87 (2013) 014006



• <sup>3</sup>He/<sup>3</sup>H m.m's used to fix EM LECs; ~15% correction from two-body currents

• Exchange currents crucial to improve agreement with exp data

### Magnetic moments of light nuclei

Pastore, Pieper, Schiavilla, Wiringa, Phys. Rev. C87 (2013) 035503



- Hybrid GFMC calculations using AV18 + Urbana 3NF
- Magnetic moments of A = 2, 3 nuclei used to fix EM LECs
- Theoretical uncertainties?

### Exchange axial currents Krebs, EE, Meißner, arXiv:1610.03569

### Chiral expansion of the axial current and charge operators



### **Tritium \beta-decay** [Skibinski et al., in progress]

5

 $C_D$ 

JÜLICH 💦

-5

0

- Half-life of <sup>3</sup>H (up to known radiative corrections): constraints on the Gamow-Teller ME
- Using 1N current, the *ft* value is off by ~ 5% ← exchange current contribution! Up to Q<sup>1</sup> (i.e. N<sup>3</sup>LO), no LECs except for known c<sub>i</sub> and c<sub>D</sub> involved. Fixing c<sub>D</sub> in the strong sector allows one to predict ft! (it is crucial to maintain the symmetry)

→ test axial exchange currents

- Within the LENPIC, work is in progress on the determination of **c**<sub>D</sub>.
- Being validated in <sup>3</sup>H  $\beta$ -decay, the same currents can be used to predict the  $\mu$  capture rate on <sup>2</sup>H being measured in MuSun

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### **Relevance for WIMP-nucleus scattering**

Assuming the WIMP  $\chi$  to be fermion and a SM singlet, the dimension-6 and -7 effective Lagrangian for  $\chi$ -SM fields has the form [Goodman et al. '10; Hoferichter et al. '15]:



#### ...can be viewed as external sources in QCD...

- Vector, axial-vector and pseudoscalar 2N currents have been worked out at order Q<sup>4</sup> (leading 1-loop) [Pastore et al.'08; Kölling et al.'09,'11; Krebs et al.'15; Hoferichter et al.'15]
- Scalar exchange currents are only available at tree level [Cirigliano et al.'14], derivation of the leading loop corrections in progress [Krebs et al., in preparation...]

### The future

What are the frontiers/challenges for the near future?

Precision physics beyond the 2N system: challenge the theory

- Lots of predictive power (N<sup>3</sup>LO contributions to the 3NF and 4NF are parameter-free, <sup>3</sup>H β-decay & μ-capture reactions are parameter-free up to N<sup>3</sup>LO once the short-range 3NF@N<sup>2</sup>LO is fixed, ...)
- 3NF & long-standing puzzles in 3N continuum
- Push theory to heavier nuclei (underbinding? radii?)
- More reliable error analysis
- Test different power counting schemes

### Nuclear reactions

Chiral EFT as a tool to deal with nuclear effects when looking at physics of/beyond the SM (parity violation, EDM,  $0\nu\beta\beta$ , proton charge radius,...)

EFT for lattice QCD (extrapolations), lattice QCD for EFT (quark mass dependence, "data", …)