Theoretical Description of the X(3872) and Y(4260) Decays

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SFB School, Boppard October, 2016







Motivation

Exotic Mesons



X(3872)

Breit-Wigner Method



Y(4260)

- Breit-Wigner Method
- Mirror-Partner
- $\pi\pi$ Rescattering



Perspectives

• Steps in Progress



Conclusions

Preliminary Conclusions

Motivation		



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Exotic Mesons		

- Discovery 2003
 - Belle at KEK Japan
 - e^+e^- collisions
- Seen by
 - CDF, D0(Fermilab USA), LHCb, CMS (Cerne-Switzerland), Babar (SLAC - USA), BESIII (IHEP - China)
- 1^{st} exotic in $c\bar{c}$ spectrum

Y(4260)

- Discovery 2005
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 - e⁺e⁻ annihilation through initial state radiation

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S. L. Olsen Front. Phys. (2015)



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Alternative explanations:

tetraquark, molecular state, hybrids of quarkonium and gluons, quarkonium-glueballs mixtures ...

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No Unique Structure

Pure Molecular or tetraquark explanations cannot explain the exotic states







Motivation	X(3872)	Y(4260)	

	X(3872) ●		
Breit-Wigner Method			



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Breit-Wigner Method			



🕼 Belle-2011

	X(3872) ●		
Breit-Wigner Method			



$$V_{\rho\pi\pi})^{\mu} \underbrace{\frac{\left(-g_{\mu\nu}+q_{\mu}q_{\nu}/m_{\rho}^{2}\right)}{q^{2}-m_{\rho}^{2}+im_{\rho}\Gamma_{\rho}}} (V_{X\psi\rho})^{\alpha\beta\nu} \epsilon_{\alpha}(p_{X})\epsilon_{\beta}(p_{\psi})$$





	X(3872)		
Breit-Wigner Method			



Belle-2011

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Breit-Wigner Propagator

Vertex $V_{x\psi\rho}$

 $V_{x\psi\rho} \rightarrow 3$ couplings: 1 longitudinal (helicity = 0) 2 transversal (helicity = ±1)

Vertex $V_{\rho\pi\pi}$

 $C_{
ho\pi\pi}$ can be obtained directly from the experimental howidth: $\Gamma_{
ho\pi\pi} = 147.8(9) \text{ MeV}$ $\implies C_{
ho\pi\pi} = 5.98(2)$

Dimensionless Couplings!

	X(3872)		
Breit-Wigner Method			



Belle-2011

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Fit Parameters $\chi^2_{red} \simeq 0.73$ Norm $\simeq 104.08$ $\frac{\textit{Ca}_{x\psi\rho}^{(1)}}{\textit{C}_{x\psi\rho}^{(0)}} \sim 2 \cdot 10^{-7}$ $\sim 8 \cdot 10^{-7}$

■ Belle-2011



Motivation	X(3872)	Y(4260)	



		Y(4260) ⊙●⊙○○○○		
Breit-Wigner Method				
	$I \neq \psi$	_)/ψ	<i>π</i> ⁻	· <i>π</i> *





Motivation 00	X(3872) o	Y(4260) ⊙●○○○○		
Breit-Wigner Method				
Y(4260) /b л	ψ Υ(4260) *	α, α, , , , , , , , , , , , , , , , , ,	Υ(4260) Υ(4260) Υ(4260) <i>Υ</i> (4260) <i>Υ</i> (4260) <i>Υ</i> (4260) <i>Υ</i> (4260)	
$\left(\frac{1}{3}\sum_{spin} \mathcal{M} ^2\right)$	$ =rac{1}{3}ig \mathcal{M}_{f_0}+\mathcal{M}_{\sigma_0}$	$+ M_{Z_{c}^{+}} + M_{Z_{c}^{-}} ^{2}$	$\begin{bmatrix} \underbrace{\epsilon_{\alpha}(p_{Y})\epsilon_{\alpha'}^{*}(p_{Y})}_{-g^{\alpha\alpha'}} \end{bmatrix} \begin{bmatrix} \epsilon_{\beta}(p_{\psi})\epsilon_{\beta'}^{*}(p_{\psi}) \end{bmatrix} \\ \underbrace{-g^{\alpha\alpha'} + \frac{p_{Y}^{\alpha}p_{Y}^{\alpha'}}{m_{Y}^{2}}}_{-g^{\beta\beta'}} \underbrace{-g^{\beta\beta'} + \frac{p_{\psi}^{\beta}p_{\psi}^{\beta'}}{m_{\psi}^{2}}}_{-g^{\beta\beta'}} \end{bmatrix}$	
	$dM_{\psi\pi}^2 dN$	$\frac{\Lambda_{\pi\pi}^2}{\Lambda_{\pi\pi}^2} = \frac{1}{32 (2\pi m_Y)^3}$	$\left(\frac{1}{3}\sum_{spin} \mathcal{M} ^{-}\right)$	
Knov	vn Coupling	s	Couplings to fit	
$\Gamma_{f_0} = 50(15)$ $\Gamma_{\sigma_0} = 552(10)$ $\Gamma_z = \underbrace{4.9(2.2)}_{\text{MeV}}$	$\implies C_{f_0\pi\pi} = \\ \implies C_{\sigma_0\pi\pi} = \\ \implies C_{Z_{c}\psi\pi} = \\$	1.32(13) = 7.29(7) = 0.41(9)	$egin{array}{lll} C_{Y\psi f_0}^{\mathcal{T}} & C_{Y\psi f_0}^{\mathcal{L}} \ C_{Y\psi \sigma_0}^{\mathcal{T}} & C_{Y\psi \sigma_0}^{\mathcal{L}} \ C_{Y\psi \sigma_0} & C_{Y\psi \sigma_0} \ \end{array}$	









	Y(4260) ○○○●○○	
Mirror-Partner		



3.6

*M*_{J/ψ π⁻} (GeV)

3.8

4.0

20 0

3.4



	Y(4260) ○○○●○○	
Mirror-Partner		



*M*_{J/ψ π⁻} (GeV)



$$M_{\psi\pi^{\pm}}
ightarrow M_{z_c^{\pm}}$$

$$\implies$$
 3.40 < $M_{\psi\pi^{\mp}}$ < 3.55

Mirror Partner (Z_c^+, Z_c^-)

The bump in this region is due to the kinematic reflection of the mirror partner!

		Y(4260) ○○○○●○		
$\pi\pi$ Rescattering				
	6) was a Math	ad	





		Y(4260) ○○○○●○		
$\pi\pi$ Rescattering				
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Analyticity: Dispersion Relation

$$\mathcal{M}=rac{1}{\pi}\int\limits_{4m_{\pi}^{2}}^{\infty}ds'\;rac{\textit{Im}\;(\mathcal{M})}{s'-s}$$

		Y(4260) ○○○○●○	
$\pi\pi$ Rescattering			
	0		



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Cutskovsky (Cutting) Rule:				

$$rac{1}{p^2-m^2+i\epsilon}
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Imaginary Part \rightarrow Propagators On-Shell

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Unitarity: p. w. Amplitude

 $Im\mathcal{M}_j(s) =
ho_j(s)\mathcal{M}_j(s)t^{*\,I}_{\pi\pi\,j}\, heta(s>4\pi^2)$

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 S-wave and Isospin = 0

$$t^* = rac{e^{i\delta(s)}\sin\delta(s)}{
ho(s)}$$
 $\mathcal{M}(s) = |\mathcal{M}(s)|e^{i\delta(s)}$

Watson Final State Theorem

$$Arg[\mathcal{M}(s)] = \delta(s)$$

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Omnes Function

$$\Omega(s) = exp\left[rac{s}{\pi}\int\limits_{4m^2}^{\infty}rac{ds'}{s'}rac{\delta(s')}{s'-s}
ight]$$

One subtraction and normalization

 $\Omega(0) = 1$

Analyticity: Dispersion Relation

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$$Im\mathcal{M}_j(s) = \rho_j(s)\mathcal{M}_j(s)t^{*\,l}_{\pi\pi\,j}\,\theta(s>4\pi^2)$$

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	Perspectives	



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Steps in Progress			



- Analytic structure of the process with *t* and *u* channel diagrams
- As important as the others diagrams
- Inclusion of neutral Z_c^0
- Development of the formalism in progress

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Preliminary Conclusions		

- Simple Breit-Wigner method explain the dynamics of the decay:
- Meaning that $X \to \rho^0 + J/\psi$, then $\rho^0 \to \pi^- + \pi^+$
- C_{xψρ} longitudinal dominates the transverse one, and can be determined as soon as the absolute mass spectra are known.

- Breit-Wigner Method:
 - $J/\psi\pi^{\pm}$ invariant mass distribution can be (well) explained!
 - First step: approximate estimate for f_0 and σ_0
- $\pi\pi$ rescattering (via Omnes method):
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Thank you for listening!





