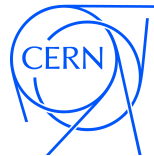


MITP 2014

High precision fundamental constants at the TeV scale

Top quark mass determination
from kinematic distributions

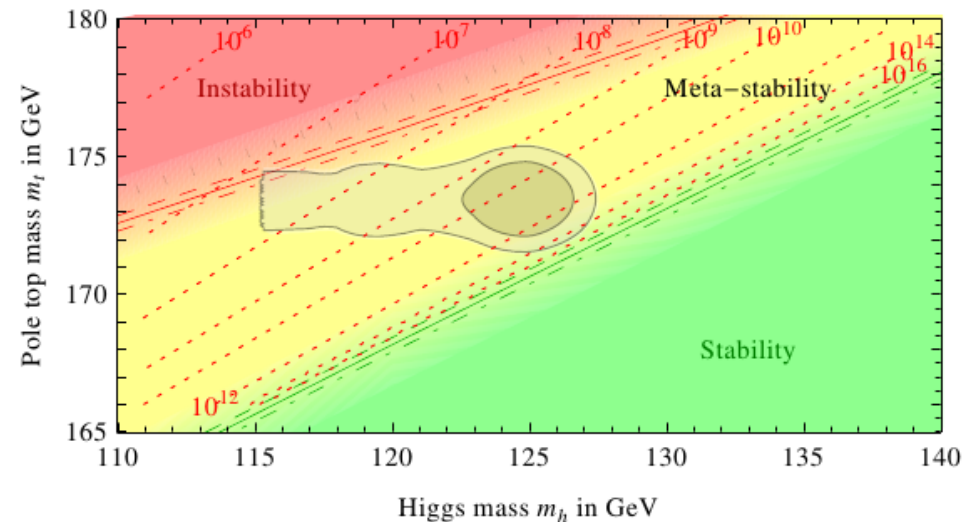
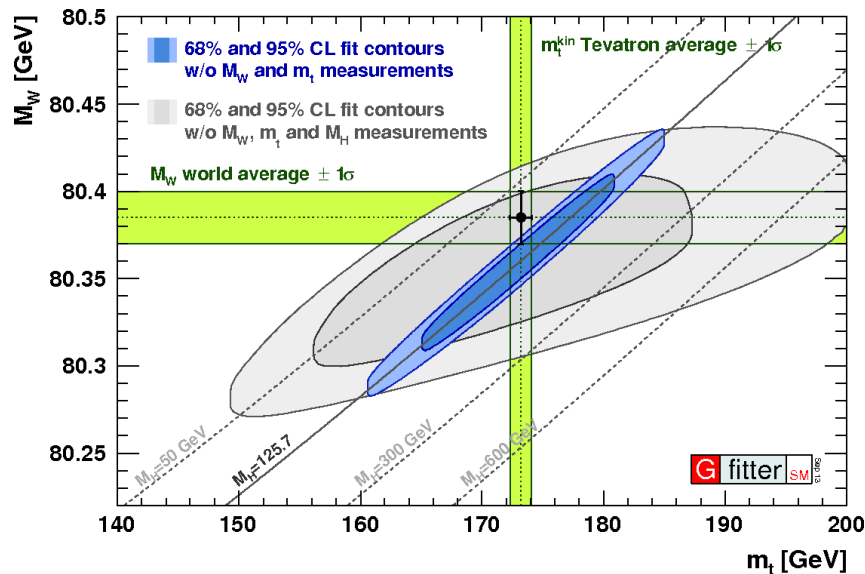
Markus Schulze



Top quark mass determination from kinematic distributions

General motivation

$$\mathcal{L}_{\text{mass}} = -v \left(\lambda_e^i \bar{e}_L^i e_R^i + \lambda_u^i \bar{u}_L^i u_R^i + \lambda_d^i \bar{d}_L^i d_R^i + \text{h.c.} \right) - M_W^2 W_\mu^+ W^{-\mu} - \frac{M_W^2}{2 \cos^2 \theta_W} Z_\mu Z^\mu ;$$



- El. weak precision test: 5.4 MeV uncertainty in $M_W \leftrightarrow 0.9$ GeV uncertainty in m_{top}
- El. weak vacuum stability: Change of m_{top} by ± 2.1 GeV $\leftrightarrow \mu_{\text{neg}} = 10^8 - 10^{16}$ GeV

Top quark mass determination from kinematic distributions

$$\mathcal{O}^{\text{exp}}(\{\mathbf{Q}\}) = \mathcal{O}^{\text{theor}}(\mathbf{m}_t, \{\mathbf{Q}\})$$

Top quark mass determination from kinematic distributions

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$$\mathcal{O}^{\text{exp}}(\{\mathbf{Q}\}) = \mathcal{O}^{\text{theor}}(\mathbf{m}_t, \{\mathbf{Q}\}, \alpha_s, \text{RS}, \Lambda_{\text{QCD}}, \{\mathbf{p}_t, \mathbf{p}_{\bar{t}}\}, \Gamma_t, \text{MC})$$

- Higher orders, renormalization scheme
- Non-perturbative effects (*e.g.* bound state, renormalons)
- Reconstruction of top quark momenta
- Finite width effects
- Monte Carlo modeling, tunes
- Contamination from New Physics

Top quark mass determination from kinematic distributions

Top mass extraction at hadron colliders

- Total cross section

Known at NNLO QCD;
Relatively low sensitivity to m_{top}

- Matrix element method

Method which gave smallest uncertainties at Tevatron;
Currently only LO matrix elements are used in likelihood functions;
Difficult to identify leading uncertainties

- Kinematic distributions

Known to NLO QCD; Good sensitivity to m_{top} ;
Reduces dependence on uncertainties of production mechanism;
Sensitive to finite width effects, details of b -jet fragmentation

Top quark mass determination from kinematic distributions

Kinematic distributions

- End-point methods
- J/ψ method
- $m_{lb/lB}$ distribution

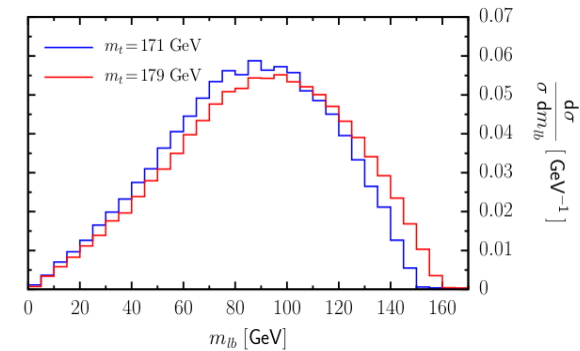
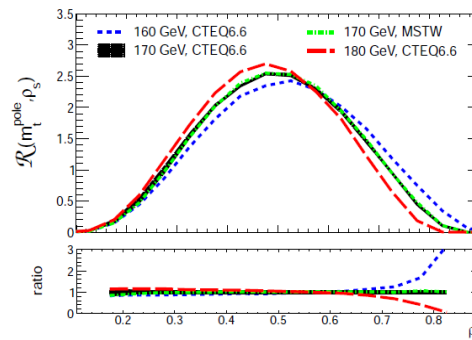
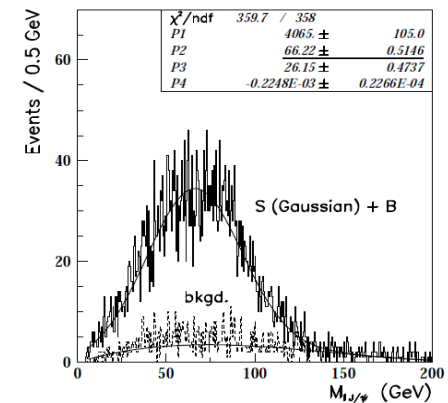
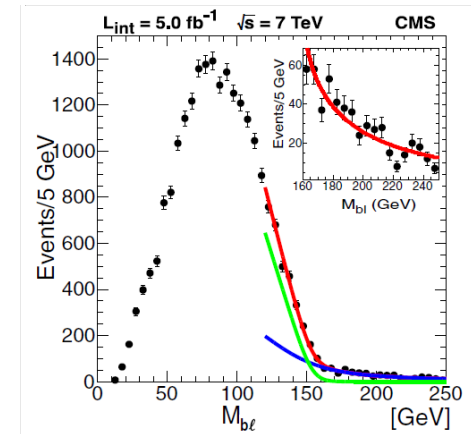
- Other lepton-related observables (E_l, E_b)

- “Threshold scan” ($t\bar{t}b$ +jet)

Top quark mass determination from kinematic distributions

Kinematic distributions

- End-point methods [CMS `13]
- J/ψ method [Kharchilava `99]
- $m_{lb/lB}$ distribution [Corcella,Mangano,Seymour,Mescia `00]
[Biswas,Melnikov,M.S. `10]
[Heinrich,Maier,Nisius,Schlenk,Winter `13]
- Other lepton-related observables (E_l, E_b)
[Beneke,Efthymiopoulos,Mangano,Womersley `00]
[Biswas,Melnikov,M.S. `10]
- “Threshold scan” ($t\bar{t}b$ +jet)
[Alioli,Fuster,Irles,Moch,Uwer,Vos `13]



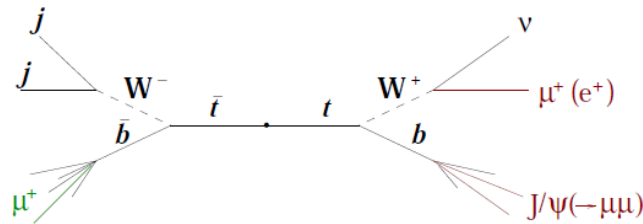
Top quark mass determination from kinematic distributions

The J/ψ method

- Basic idea:

Study $m_{l,J/\psi}$ from top quark decay in a “very” leptonic decay channel

→ Clean final state **vs.** low event rate



- One in 10^5 top quark pairs decays in this channel.

Hence, an integr. luminosity of $\sim 100 \text{ fb}^{-1}$ is required to obtain $\mathcal{O}(1 \text{ GeV})$

- With relaxed assumptions, uncert. of $\mathcal{O}(1.5 \text{ GeV})$ seems possible with 20 fb^{-1}

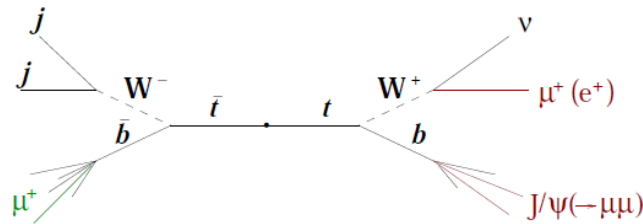
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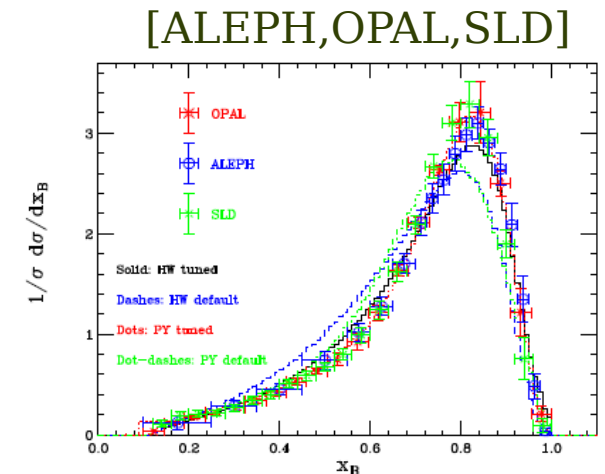


- Theoretical treatment:

Include B -meson fragmentation function

$$D_{b \rightarrow B}(\mu, x) = \int_x^1 \frac{d\xi}{\xi} D_b(\mu, \xi) D_{np} \left(\frac{x}{\xi} \right)$$

$B \rightarrow J/\psi$ transition is well studied in B -factories



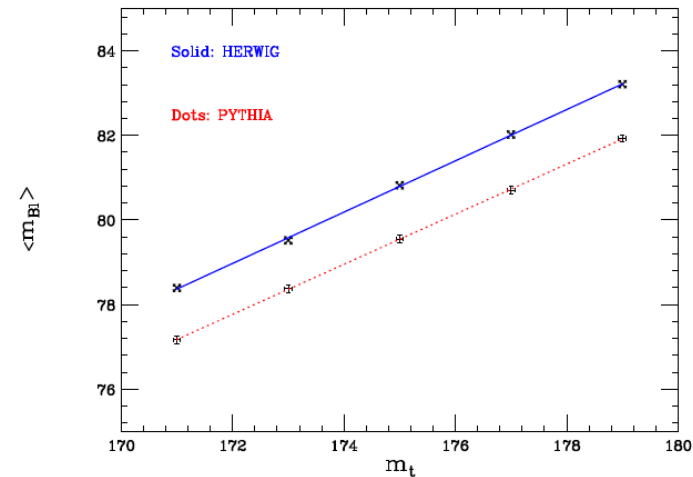
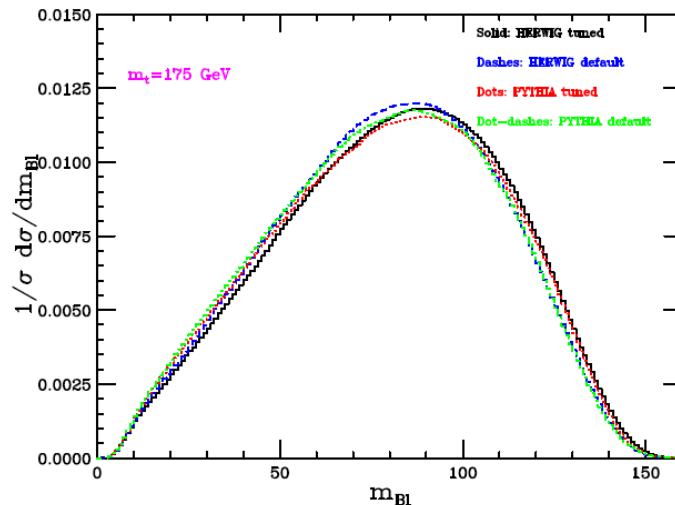
Top quark mass determination from kinematic distributions

The J/ψ method

- Early studies show promising sensitivity to m_{top}

[Corcella, Mangano, Seymour, Mescia '00]

Consider m_{lB} from $t \rightarrow Wb \rightarrow l\nu B$, assume $\Delta\langle m_{lB} \rangle = 0.4$ GeV



$$\langle m_{Bl} \rangle_{\text{Pythia}} = 0.59 m_t - 24.11 \text{ GeV}, \quad \langle m_{Bl} \rangle_{\text{Herwig}} = 0.61 m_t - 25.31 \text{ GeV}$$

→ Uncertainty from comparing HERWIG vs. PYTHIA

$$\Delta m_{\text{top}} = 1.5\text{-}2 \text{ GeV}$$

Top quark mass determination from kinematic distributions

The J/ψ method

- Similar analysis at NLO QCD [Biswas,Melnikov,M.S. `10]

$$D_b(\mu, x) = \delta(1-x) + \frac{\alpha_s(\mu)C_F}{2\pi} \left[\frac{1+x^2}{1-x} \ln\left(\frac{\mu^2}{m_b^2}\right) - 2\log(1-x) - 1 \right]_+ + \mathcal{O}(\alpha_s^2)$$

$$D_{\text{np}} = \begin{cases} x^\alpha(1-x)^\beta/B(\alpha+1, \beta+1), \\ (1+\delta)(2+\delta)(1-x)x^\delta. \end{cases}$$

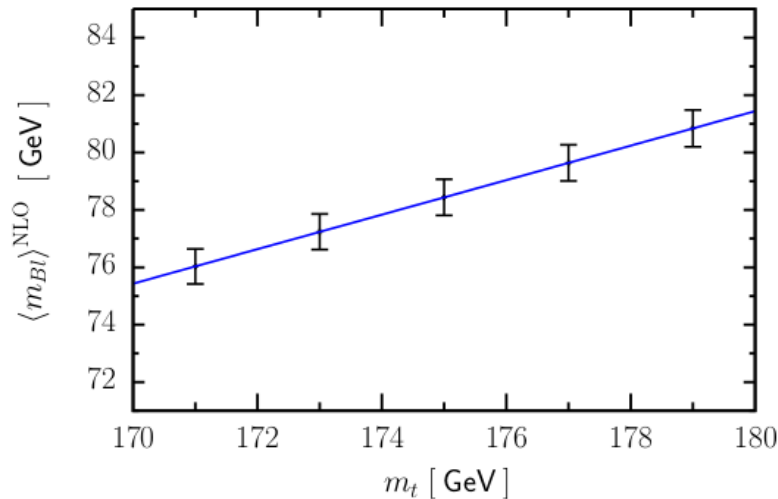
Top quark mass determination from kinematic distributions

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$$\langle m_{Bl} \rangle^{\text{NLO}} = 0.601 m_t - 26.7 \text{ GeV}, \quad \delta_{\text{rms}} = 0.004;$$

$$\langle m_{Bl} \rangle_{\text{Pythia}} = 0.59 m_t - 24.11 \text{ GeV},$$

$$\langle m_{Bl} \rangle_{\text{Herwig}} = 0.61 m_t - 25.31 \text{ GeV}$$

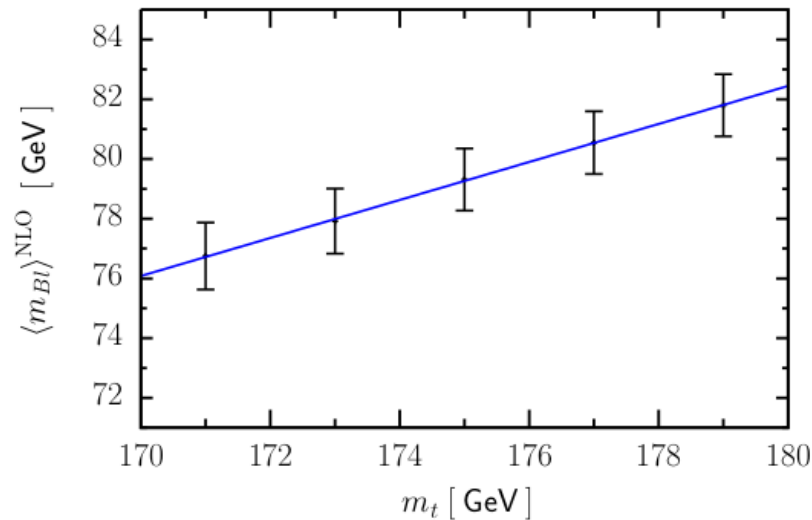
→ Uncertainty from NLO scale variation and variation of D_{np} parameters

$$\Delta m_{\text{top}} = 0.8 \text{ GeV}$$

Top quark mass determination from kinematic distributions

The J/ψ method

- Include full production and decay process at NLO QCD including realistic selection cuts [Biswas,Melnikov,M.S. `10]

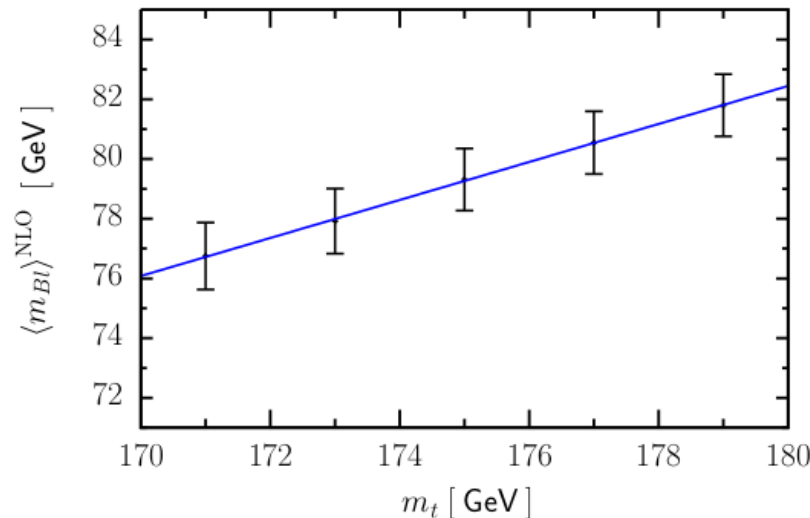


$$\langle m_{Bl} \rangle_{\text{prod}}^{\text{NLO}} = 0.6365 m_t - 32.12 \text{ GeV}, \quad \delta_{\text{rms}} = 0.053$$

Top quark mass determination from kinematic distributions

The J/ψ method

- Include full production and decay process at NLO QCD including realistic selection cuts [Biswas,Melnikov,M.S. `10]



$$\langle m_{Bl} \rangle_{\text{prod}}^{\text{NLO}} = 0.6365 m_t - 32.12 \text{ GeV}, \quad \delta_{\text{rms}} = 0.053$$

- Uncertainty budget from scale variation ($\mu_{\text{ren}}, \mu_{\text{fac}}, \mu_{\text{frag}}$ independently), two different parameters of D_{np} , and two different pdf sets (MSTW,CTEQ)

$$\Delta m_{\text{top}} = 1.5 \text{ GeV}$$

Top quark mass determination from kinematic distributions

m_{top} estimator

- Basic idea: Construct an estimator for m_{top}

[Beneke, Efthymiopoulos, Mangano, Womersley '00]

$$M_{\text{est}}^2 = m_W^2 + \frac{2\langle m_{lb}^2 \rangle}{1 - \langle \cos \theta_{lb} \rangle}$$

→ at LO, $M_{\text{est}} = m_{\text{top}}$

$$\langle m_{lb}^2 \rangle = \frac{m_t^2 - m_W^2}{2} (1 - \langle \cos \theta_{lb} \rangle), \quad \langle \cos \theta_{lb} \rangle = \frac{m_W^2}{m_t^2 + 2m_W^2}$$

Hence, we expect a strong correlation.

Top quark mass determination from kinematic distributions

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Hence, we expect a strong correlation. In reality $M_{\text{est}} \neq m_{\text{top}}$ due to:

- kinematic selection cuts
- higher orders
- lepton b-jet pairing
- experimental effects (JES, b-tagging, ...)

Accounting for the first three points is possible within pert. QCD

Top quark mass determination from kinematic distributions

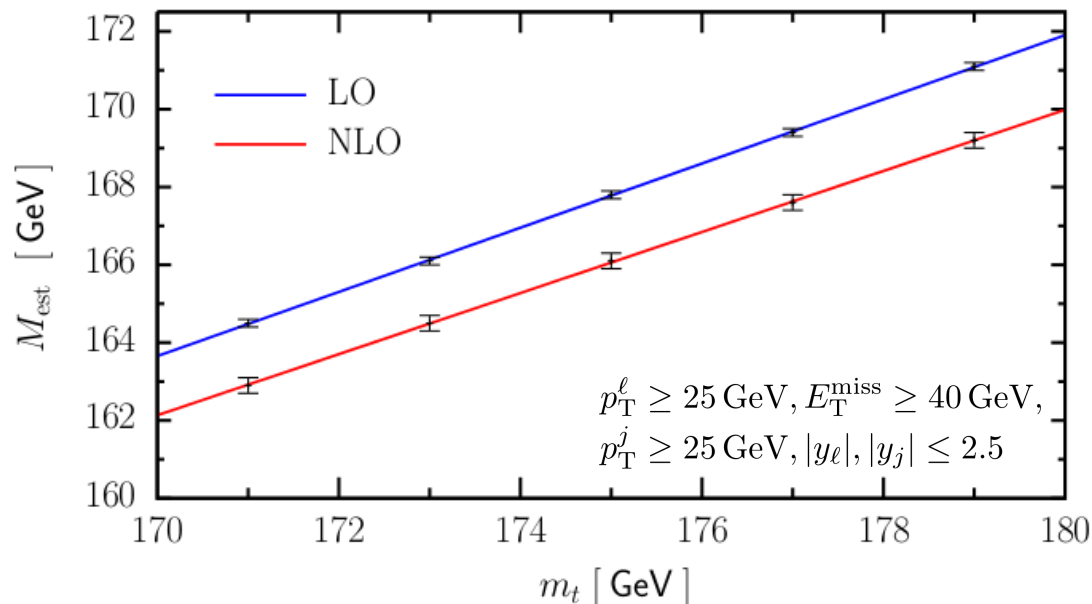
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$$M_{\text{est}}^2 = m_W^2 + \frac{2\langle m_{lb}^2 \rangle}{1 - \langle \cos \theta_{lb} \rangle}$$

[Biswas, Melnikov, M.S. '10]

NLO QCD results (14 TeV) for $pp \rightarrow t\bar{t} \rightarrow (bW \rightarrow bl\nu) (\bar{b}W \rightarrow bj\bar{j})$



$$M_{\text{est}}^{\text{LO}} = 0.8262m_t + 23.22 \text{ GeV}$$

$$M_{\text{est}}^{\text{NLO}} = 0.7850m_t + 28.70 \text{ GeV}$$

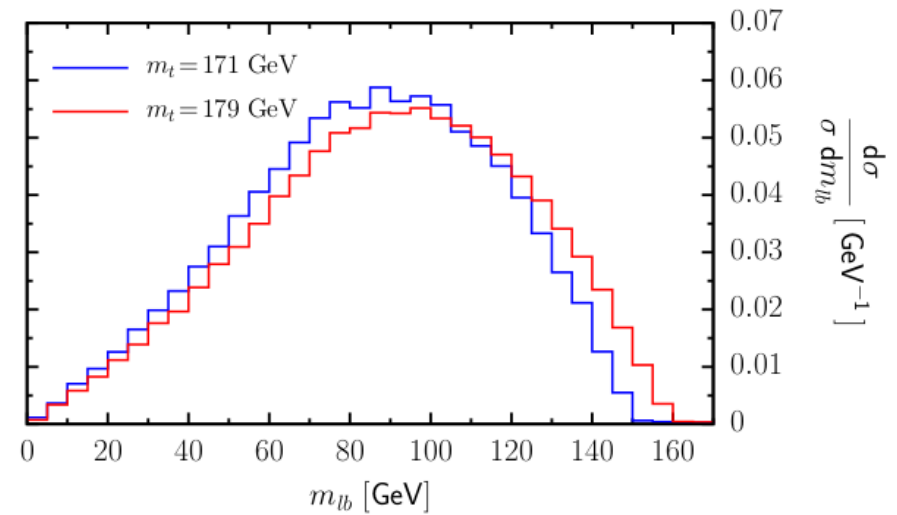
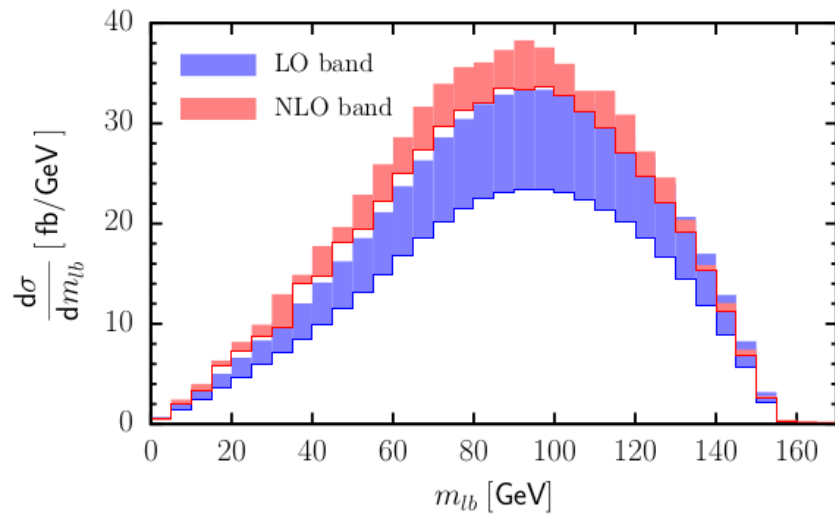
$$\rightarrow \Delta m_{\text{top}} = 0.25 \text{ GeV}$$

expect additional uncert. of
 $\pm 0.7 \text{ GeV}$ (b -fragm.)
 $\pm 0.6 \text{ GeV}$ (JES)

Top quark mass determination from kinematic distributions

m_{lb} distribution

- Shape of m_{lb} distribution

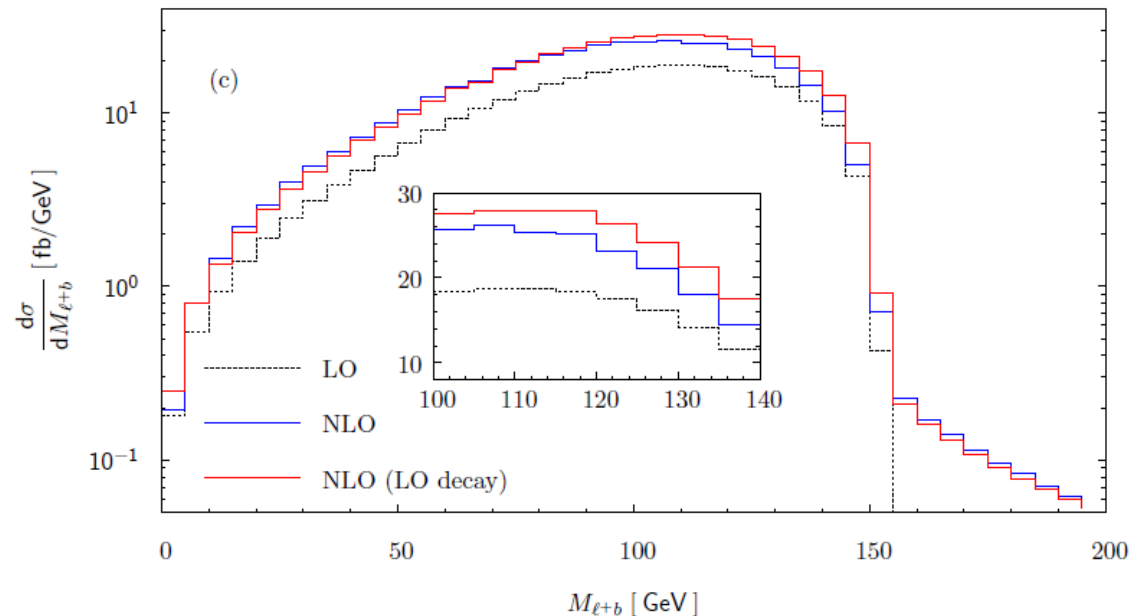


→ Good sensitivity within the range $m_{\text{top}} \in [171..179]$ GeV

Top quark mass determination from kinematic distributions

m_{1b} distribution

- Shape of m_{1b} distribution



NLO correction to decay leads to shape changes
[Melnikov, M.S. `10]

Top quark mass determination from kinematic distributions

m_{tb} distribution

Finite width effects and non-factorizable corrections

thanks to $WWb\bar{b}$ calculations by [Denner,Dittmaier,Kallweit,Pozzorini]
+ HELAC and GOSAM+Sherpa groups

Collider	\sqrt{s} [TeV]	approx.	$\sigma_{t\bar{t}}$ [fb]	$\sigma_{WWb\bar{b}}$ [fb]	$\sigma_{t\bar{t}}/\sigma_{WWb\bar{b}} - 1$
Tevatron	1.96	LO	$44.691(8)^{+19.81}_{-12.58}$	$44.310(3)^{+19.68}_{-12.49}$	+ 0.861(19)%
		NLO	$42.16(3)^{+0.00}_{-2.91}$	$41.75(5)^{+0.00}_{-2.63}$	+ 0.98(14)%
LHC	7	LO	$659.5(1)^{+261.8}_{-173.1}$	$662.35(4)^{+263.4}_{-174.1}$	- 0.431(16)%
		NLO	$837(2)^{+42}_{-87}$	$840(2)^{+41}_{-87}$	- 0.41(31)%
LHC	14	LO	$3306.3(1)^{+1086.8}_{-763.6}$	$3334.6(2)^{+1098.5}_{-771.2}$	- 0.849(7)%
		NLO	$4253(3)^{+282}_{-404}$	$4286(7)^{+283}_{-407}$	- 0.77(19)%

Top quark mass determination from kinematic distributions

m_{tb} distribution

Finite width effects and non-factorizable corrections

thanks to $WWb\bar{b}$ calculations by [Denner,Dittmaier,Kallweit,Pozzorini]
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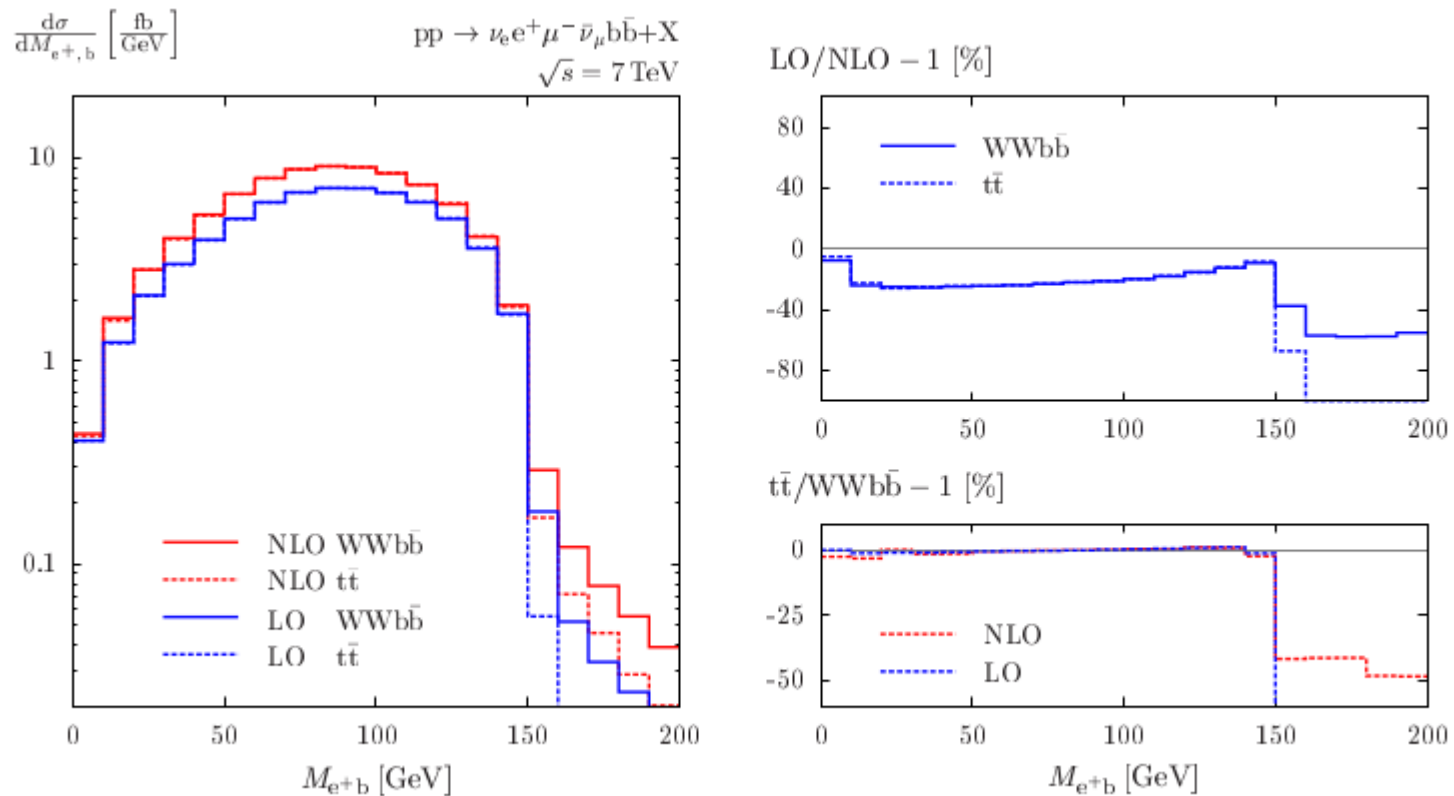
Collider	\sqrt{s} [TeV]	approx.	$\sigma_{t\bar{t}}$ [fb]	$\sigma_{WWb\bar{b}}$ [fb]	$\sigma_{t\bar{t}}/\sigma_{WWb\bar{b}} - 1$
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Top quark mass determination from kinematic distributions

m_{1b} distribution

Study of finite width effects and non-factorizable corrections

[Denner, Dittmaier, Kallweit, Pozzorini, M. S.]

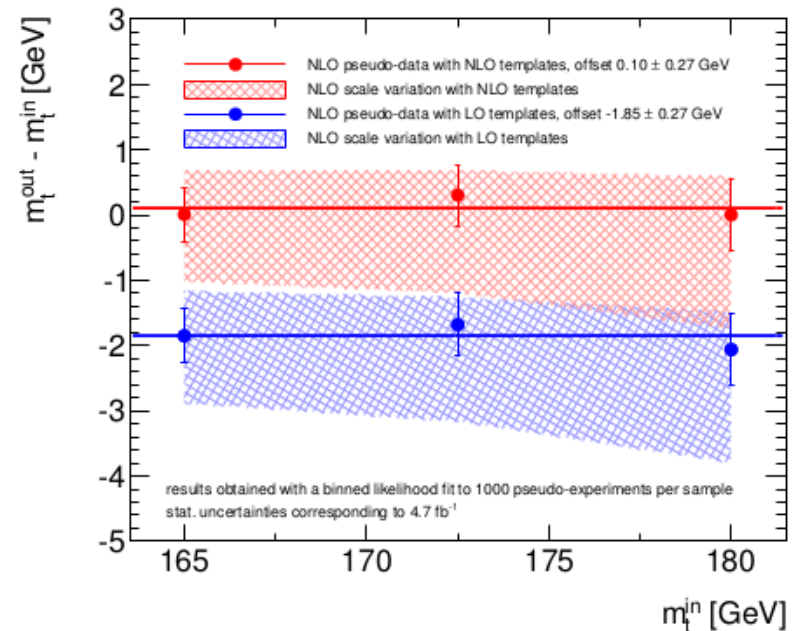
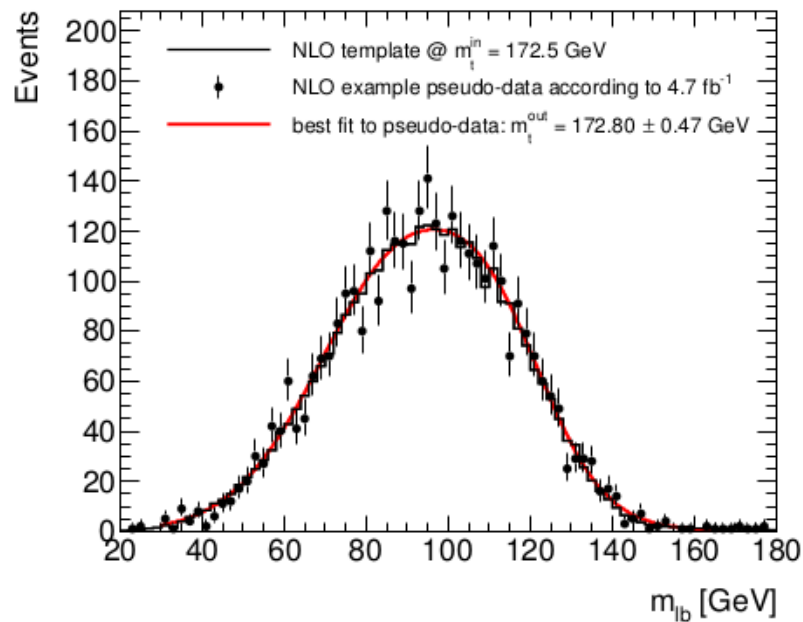


Top quark mass determination from kinematic distributions

m_{lb} distribution

- Template fit to (pseudo) data

[Heinrich, Maier, Nisius, Schlenk, Winter '13]



Pseudo data always generated with NLO QCD.

Templates are either generated at **NLO** (red) or **LO** (blue).

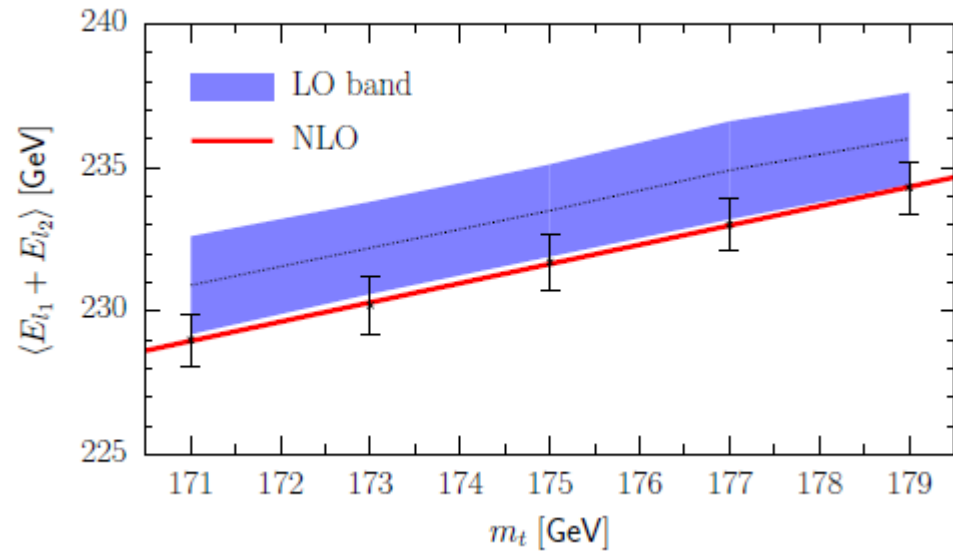
SUMMARY

- Certain types of kinematic distributions have good sensitivity to m_{top} .
Up to know those methods have been rarely applied to real data.
- Uncertainty estimates from kinematic distributions $\sim \pm 1.5$ GeV.
Good theoretical control. No obvious show stopper.
- Reducing uncertainties to $\sim \pm 0.5$ GeV will probably require
a combination of several methods (\rightarrow study correlated errors).
- Significant improvements require more precise B -meson frag. function.
- Possibility of BSM physics hiding in top data (*e.g.* $t\bar{t}b + E_{\text{T,miss}}$)
which shifts m_{top} is not fully excluded.

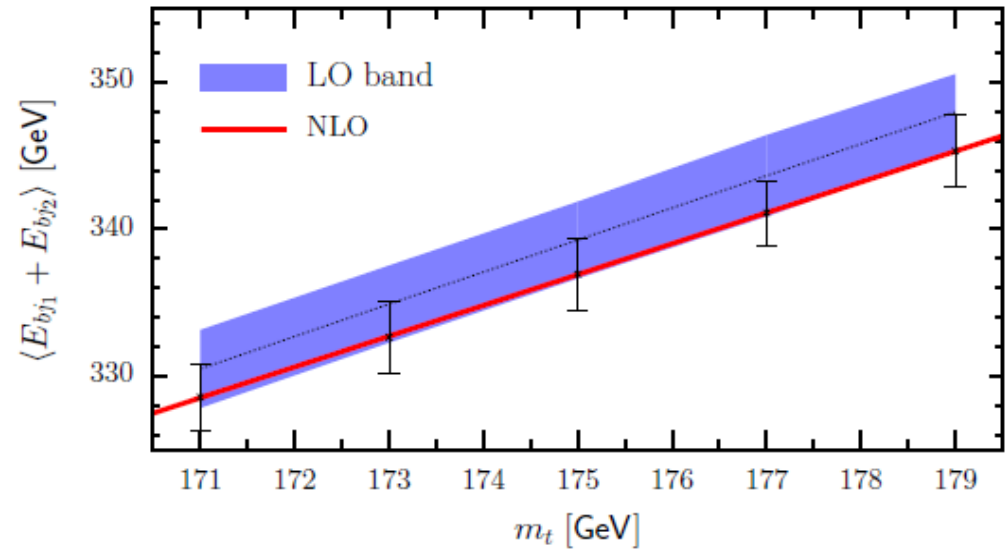
EXTRAS

EXTRAS

[Biswas,Melnikov,M.S. `10]



$\rightarrow \Delta m_{\text{top}} = 1.5 \text{ GeV}$



$\rightarrow \Delta m_{\text{top}} = 1.2 \text{ GeV}$

EXTRAS

	Ref. analysis	Projections				
CM Energy	8 TeV	14 TeV			33 TeV	100 TeV
Cross Section	240 pb	951 pb			5522 pb	25562 pb
Luminosity	$20 fb^{-1}$	$100 fb^{-1}$	$300 fb^{-1}$	$3000 fb^{-1}$	$3000 fb^{-1}$	$3000 fb^{-1}$
Theory (GeV)	-	1.5	1.5	1.0	1.0	0.6
Stat. (GeV)	7.00	1.8	1.0	0.3	0.1	0.1
Total	-	2.3	1.8	1.1	1.0	0.6
Total (%)	-	1.3	1.0	0.6	0.6	0.4

Table 6. Extrapolations based on the J/Ψ method.