Microphysics for supernova simulations and neutrino signals



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Selected examples of microphysics that may impact the neutrino signals from a galactic core collapse SN

- I. Equation of state
- 2. Neutrino opacities

Equation of state (EOS)

- Is a large table with many different parts that extends over many decades in density ρ , temperature T, and proton fraction Y_p. EOS includes:
- **P=P(\rho, T, Y_P)** and other thermodynamic functions E, S, μ ...
- **Composition** $Y_i = Y_i(\rho, T, Y_p)$ for many species i [often p, n, ⁴He, A]. Important for neutrino V interactions.
- EOS and \boldsymbol{v} opacities should be consistent.
 - Attractive strong interactions at just below nuclear density lead to correlations between nucleons that enhance vector response S_V .
 - Effective mass M^* in EOS gives density of states for v opacities.
 - Spin dependent interactions in EOS important for axial response S_A, but poorly constrained (Skyrme forces can have ferromagnetic phases)

EOS and Neutron Star radii

- **Two very different radii**: Neutron star radius **R**_{NS} and Proto-neutron star **R**_{PNS}
- R_{NS}: radius of cold, beta equilibrated NS.
 - Is irrelevant for SN dynamics during first second because star is hot and lepton rich.
 - R_{NS} determines binding E of NS and total
 E radiated in V. Etotal ~ 0.6 GM²/R_{NS}
 - R_{NS} determined by P of cold EOS at ~ $2\rho_0$.
 - Presently R_{NS} =10 to 14 km. Optimistic: assume by next galactic SN that R_{NS} known to 10% from X-rays (NICER) or Gravitational Waves (GW).



Neutron star interior composition explorer (NICER), aims to determine R_{NS} from curvature of space implied by Xray light curve. Launched to space station June 3, 2017.

Total E in Neutrinos

- Constrains distance to SN, mass of new NS, cooling by new particles such as axions, sterile neutrinos ...
- Can we measure E_{tot} to 10%? Or better?
- Option I: Individual flavors. Measure anti-Ve very well in Super-K..., measure Ve well in DUNE. Constrain Vx via theory or indirect observations such as ¹⁶O(V,V'γ). Good statistics, but some systematic errors.
- Option 2: flavor independent neutral current detector. V-nucleus elastic scattering in dark matter detectors has very *large yield of tens of events per ton* (for SN at 10 kpc). Clean systematics, independent of (active) V oscillations, but may have limited statistics.

Observation of v-nucleus elastic scattering from CsI at SNS



D. Akimov et al, Science, Aug. 3

Proto-neutron star radius RPNS

- R_{PNS} = radius of neutrinosphere around warm, lepton rich, proto-NS, and is very important for SN dynamics.
- Depends on thermal/ degeneracy pressure of leptons. Not so sensitive to strong interactions at high density.
- Smaller R_{PNS} gives deeper gravitational well so that accretion powers larger V luminosities, to re-energize shock.
- Faster transport of heat, lepton #, out of star can lead to faster contraction of R_{PNS} .
- Also converting some electrons to muons reduces lepton pressure and R_{PNS}.



R_{PNS} vs time after core bounce in 2D SN simulations by Bolig et al, arXiv:1706.04630

SN Quantum Numbers

	Precollapse	SN	Neutron Star
# nu radiated		10 ⁵⁸	
Baryon #	10 ⁵⁷	1057	10 ⁵⁷
Electron #	10 ⁵⁷	—>	10 ⁵⁶
Muon #	0	—>	10 ⁵⁵
Tau #	0	10 ⁵⁴	0
Strangeness	0	—>	?

- **Deleptonization**: During SN electron # of 10⁵⁷ is radiated.
- Muonization: During SN muon # of minus 10⁵⁵ is radiated.
- Tau #: Produce equal numbers of nu-tau, anti-nu-tau. However anti-nu_tau leave faster because of weak magnetism leaving star nu-tau rich [PLB 443 (1998) 58].

Macroscopic next generation matter and the changing of the generations

- A SN contains astronomical numbers of 2nd and third generation particles. It may be uniquely sensitive to new flavor physics.
- Example: muon to electron conversion: μ +A —> e+A could increase the role of muons.

Neutrino Opacities

v interactions in SN matter

 $v_e + n \rightarrow p + e$ (Charged current capture rxn)

v + N --> v + N (Neutral current elastic scattering, important opacity source for mu and tau v)

- Neutrino-nucleon neutral current cross section in SN is modified by axial or spin response S_A , and vector response S_V , of the medium.

$$\frac{1}{V}\frac{d\sigma}{d\Omega} = \frac{G_F^2 E_\nu^2}{16\pi^2} \Big(g_a^2 (3 - \cos\theta)(n_n + n_p)S_A + (1 + \cos\theta)n_n S_V\Big)$$

- Responses S_A , $S_V \longrightarrow I$ in free space. Normally S_A dominates because of $3g_a^2$ factor.

Neutrinosphere as unitary gas

- Much of the action in SN at *low densities* near neutrinosphere at n $\sim n_0/100$ (nuclear density n_0).
- Average distance between two neutrons near neutrinosphere is less than NN scattering length.



- \leftarrow 8.5 fm \rightarrow Average distance between two neutrons at n₀/100
- \leftrightarrow I.4 fm Range of NN force
- Unitary gas is a system with near infinite scattering length and near zero effective range. Neutrinosphere is close to a unitary gas.
- Because of the long scattering length one can have important correlations in a unitary gas even at low densities.
- Two neutrons are correlated into spin zero 1S_0 state that reduces spin response $S_A{<}1.$

Can the spin response of a unitary gas help a supernova to explode?

- Well posed question.
- Helpful to think of neutrinos interacting with a unitary gas as a special reference system for nuclear matter.
 Better to model neutrinosphere region as a unitary gas instead of a free (Fermi) gas as is often done.
- Many theoretical results for a unitary gas and many **experimental results** for cold atoms.
- Spin response <1 reduces scattering opacity.
- Effect may be important even at low ~10¹² g/cm³ densities because of the large scattering length.
- Probably helps 2D (and 3D?) simulations explode perhaps somewhat earlier???



Dynamic Spin Response of a Strongly Interacting Fermi Gas [S. Hoinka, PRL **109**, 050403]



 $S_A(k,w)$ is solid line and squares, while dashed line is $S_V(k,w)$. Static structure factors: $S_V(k) = \int dw S_V(k,w)$, $S_A(k) = \int dw S_A(k,w)$

Virial Expansion for Unitary Gas

 In high T and or low density limit, expand P in powers of fugacity z=Exp[chemical pot/T]

$$P = \frac{2T}{\lambda^3} \sum_{n=1}^4 b_n z^n \qquad \qquad n = \frac{z}{T} \frac{dP}{dz}$$

- Long wavelength response:

$$S_V(q \to 0) = T/(\partial P/\partial n)_T = z(\partial n/\partial z)/n,$$
$$S_V(q \to 0) = \frac{1 + 4zb_2 + 9z^2b_3 + 16z^3b_4}{1 + 2zb_2 + 3z^2b_3 + 4z^3b_4}$$

- Axial response: $S_A(q \to 0) = \frac{2z}{n} \frac{\partial}{\partial(z_1 - z_2)} (n_1 - n_2) \Big|_{z_1 = z_2}$

Axial Response in Virial Expansion

- At low densities *n* and or high temperatures *T* one can expand equation of state in powers of the fugacity $z=e^{\mu/T}$ with μ the chemical potential.
- Generalize to partially spin polarized gas to determine long wavelength limit of axial response: $S_A \sim 1 + \lambda^3 n b_a$ with $b_a 2^{nd}$ viral coefficient for spin polarization gas.
- *b_a* is about -0.64 from observed nucleon-nucleon elastic scattering phase shifts.



In Phys. Rev. C **95** (2017) 025801 we provide a simple fit $S_A{}^f(n, T, Y_p)$, valid for all densities, that reproduces viral result at low densities and a common Random Phase Approximation model at high densities. Fit can easily be used in SN simulation.

4th order Unitary results



Unitary gas response arXiv:1708.01788





Shock radius vs time for 2D SN simulations

All 2-D SN simulations by Burrows [arXiv:1611.05859] with correlations (S_A <1) explode (solid lines) while 12 and 15 M_{sun} stars fail to explode, and 20, 25 M_{sun} explode later, without correlations (S_A =1).

Preliminary 2D SN simulations by Evan O'Connor and Sean Couch for 12 to 25 M_{sun} stars explode earlier (lighter color) if correlations (S_A<1) included.

Sensitivity of SN dynamics motivates better treatments of neutrino interactions in SN matter.



Bolig et al, arXiv:1706.04630



SN signal at 10 kpc in Super-K



 Neutrino-pasta coherent scattering slows neutrino diffusion and leads to a significant increase in counts at late times (>10 sec after core collapse) compared to a simulation without pasta. Important to observe neutrinos for as long as possible, helped by large Hyper-K statistics.

Neutrino-nucleon elastic scattering

- Multi-D SN simulations sensitive to ~ 10% changes in Vnucleon neutral current cross sections.
- Spin correlations between nucleons, from interactions with large scattering lengths, reduce neutral current opacities even at low neutrinosphere densities.
- These correlations can be calculated accurately with model independent virial expansions.

Neutrino-proton elastic scattering experiment at the SNS?

- Can one measure v-p elastic scattering cross sections to ~10% in lab with (~ 30 MeV) neutrinos from pion decay at rest?
- This cross section is important for SN simulations.
- Constrain strange quark contributions to nucleon spin.
- Constrain nonstandard neutrino interactions that could impact SN dynamics.
- Note V-p primarily involves axial currents and may provide complementary constraints to V-A elastic scattering which probes vector currents.

SN neutrinos and r-process nucleosynthesis

- Possible site of r-process (makes Au, Pt, U,...) is the neutrino driven wind in SN.
- Ratio of neutrons to protons in wind set by capture rates that depend on neutrino and anti-neutrino energies.

 $\nu_e + n \to p + e \qquad \bar{\nu}_e + p \to n + e^+$

- Measure difference in average energy of antineutrinos and neutrinos. If large, wind will be neutron rich. If it is small, wind will be proton rich and likely a problem for r-process.
- Composition (Y_e) of wind depends on anti-neutrino energy (Y-axis) [results from ~20 SN1987A events shown] and energy of neutrinos (X-axis). Energy of neutrinos, not yet measured, depends on properties of n rich gas (nu-sphere).



SN simulations find too few neutrons for main or 3rd peak (Au, actinides) r-process. SN likely make lighter rprocess nuclei.

Learn about impact of neutrinos on nucleosynthesis from a galactic SN. Neutrinos may be important in other r-process sites.

Microphysics for supernova simulations and neutrino signals

- Neutrino interactions in supernovae: Zidu Lin, Liliana Caballero, Achim Schwenk, Luke Roberts, Evan O'Connor, Tobias Fischer, W. Newton ...
- Muons: R. Bollig, H.-T. Janka, A. Lohs, G. Martinez-Pinedo, and T. Melson





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