

# Symmetry violations in $\beta$ decay

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Theor. Physik 1



**DFG** FOR 1873

# Motivation

- Recently non-SM interactions studied using SM EFT Cirigliano *et al.* [2010, 2013]
  - Model independent (\*)
  - All fields obey SM symmetry groups
  - New physics generated by higher-dimensional operators

$$\mathcal{L}_{\text{eff}} = \mathcal{L}^{(4)} + \frac{1}{\Lambda} \mathcal{L}^{(5)} + \frac{1}{\Lambda^2} \mathcal{L}^{(6)}$$

- Interplay between different searches for new physics
  - What is the role of  $\beta$  decay?
  - Can we study Lorentz-symmetry breaking?

$$\begin{aligned}
 \mathcal{L}^{(\text{eff})} = \frac{G_F V_{ud}}{\sqrt{2}} & \left[ \sum_{\epsilon, \delta=L,R} a_{\epsilon\delta} \bar{e} \gamma^\mu \nu_e^\epsilon \cdot \bar{u} \gamma_\mu d_\delta \right. \\
 & + A_L \bar{e} (1 - \gamma_5) \nu_e^\epsilon \cdot \bar{u} d_\delta + A_R \bar{e} (1 + \gamma_5) \nu_e^\epsilon \cdot \bar{u} d_\delta \\
 & \left. + \alpha_R \bar{e} \frac{\sigma^{\mu\nu}}{\sqrt{2}} (1 + \gamma_5) \nu_e^\epsilon \cdot \bar{u} + \alpha_L \bar{e} \frac{\sigma^{\mu\nu}}{\sqrt{2}} (1 - \gamma_5) \nu_e^\epsilon \cdot \bar{u} \right],
 \end{aligned}$$

SM + "V+A"  
Scalar  
Tensor

- Related to "Lee-Yang" formalism using form factors  $g_A, g_S, g_T$
- T (CP)-violation probed by imaginary couplings

# Correlation coefficients

Jackson et al. [1957]

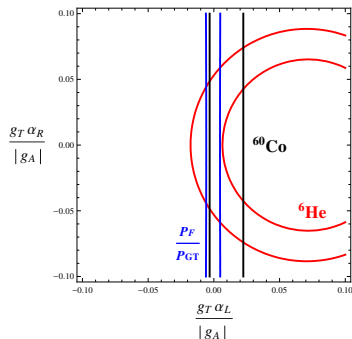
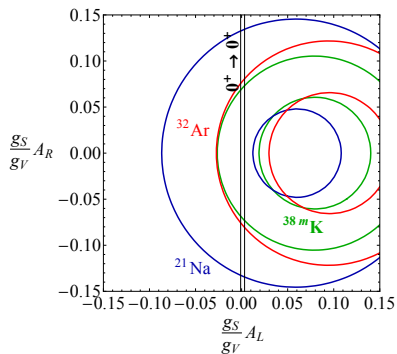
$$\frac{dW}{dW_0} \propto 1 + a \frac{\vec{p}_e \vec{p}_\nu}{E_e E_\nu} + b \frac{m_e}{E_e} + \frac{\langle \vec{J} \rangle}{J} \cdot \left[ A \frac{\vec{p}_e}{E_e} + D \frac{\vec{p}_e \times \vec{p}_\nu}{E_e E_\nu} \right] + \dots$$

- Correlations coefficients measure deviations from “V-A”
  - Scalar/Vector: Fermi transitions
  - Axial-Vector/Tensor: Gamow-Teller transitions
- Only Fierz-interference term  $b$  depends linearly on left-handed scalar and tensor couplings
- Usually measured

$$\tilde{A} = \frac{A}{1 + b \langle m_e / E_e \rangle}$$

# Searches for exotic couplings - Current limits

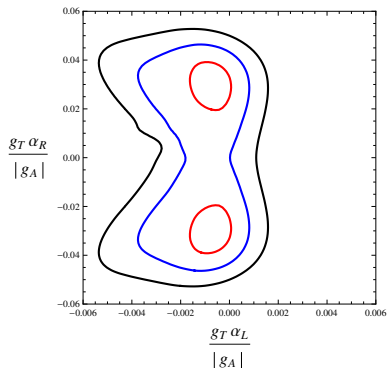
KKV, Wilschut, Timmermans [2015]



$$\frac{1}{ft_F} \propto V_{ud}^2 \left( 1 + \frac{g_S^2}{g_V^2} [A_L^2 + A_R^2] - 2\sqrt{1 - Z^2\alpha^2} \left\langle \frac{m_e}{E_e} \right\rangle \frac{g_S}{g_V} A_L \right)$$

# Searches for exotic couplings - Global fit

KKV, Wilschut, Timmermans [2015]



- Neutron decay can also be used to study new physics
  - Tensor limits improve
  - But issues with neutron life time
  - $g_A$  as input from lattice ?

# Interplay with LHC constraints

Cirigliano *et al.* [2013]

Bhattacharya *et al.* [2012, 2014]

Gonzalez-Alonso and Camalich [2014]

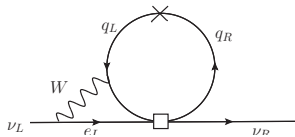
- New particles with high mass would also give deviations from SM predictions at LHC
- $pp \rightarrow e + \text{MET} + X$  same quark process as  $\beta$  decay
  - sensitive to same scalar and tensor interactions
- Upper limit on new physics events can be translated into constraint on exotic couplings
- Values for  $g_S$  and  $g_T$  important/limiting factor

$$g_S = \frac{\delta M^{QCD}}{\delta m_q} = 1.02 \pm 0.11 \quad \text{and} \quad g_T = 1.047 \pm 0.061$$

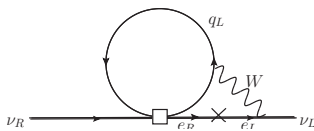
CVC-relation Lattice

# Interplay with neutrino mass

Ito and Prezeau [2005]



Constraint on  $A_{RR}$ ,  $A_{RL}$  and  $\alpha_R$



Constraint on  $a_{RL}$

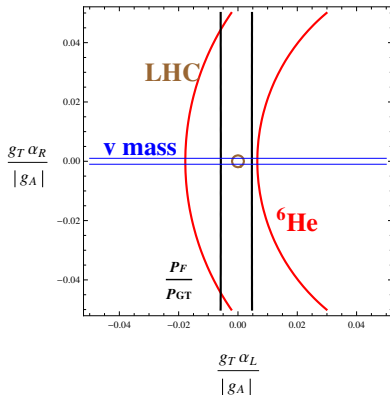
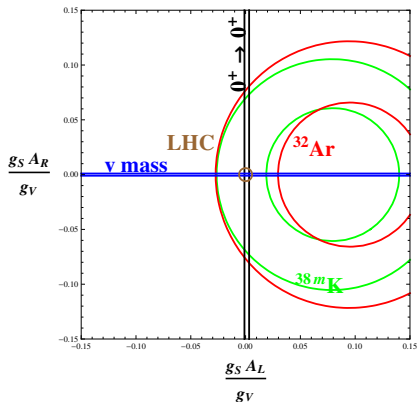
- Electroweak radiative corrections constrain right-handed couplings neutrino couplings
  - Two-loop  $W$  contribution dominant
  - Simple estimate considering only logarithmic part

$$\delta m_\nu \sim 3g^2 G_F \bar{a} \frac{m_f M_W^2}{(4\pi)^4} \left( \ln \frac{\mu^2}{M_W^2} \right)^2$$



# Combined limits on exotic couplings

KKV, Wilschut, Timmermans[2015]



# Time-reversal violation in $\beta$ decay

Chupp et al. [2012]  
Kozela [2012]

- Imaginary couplings probed by triple-correlation coefficients in  $\beta$  decay

$$D\vec{J} \cdot (\vec{p}_e \times \vec{p}_\nu) \text{ and } R\vec{\sigma}_e \cdot (\vec{J} \times \vec{p}_e)$$

where  $D \propto \text{Im } a_{LR}$  and  $R \propto c'g_T \text{Im } \alpha_L - c''g_S \text{Im } A_L$

- Final-state-interactions mimic time-reversal violation:  $D = D_t + D_f$
- For neutron decay  $D_f \sim 10^{-5}$  and  $|\text{Im } a_{LR}| < 4 \times 10^{-4}$
- From neutron and pure GT  ${}^8\text{Li}$   
 $g_T|\text{Im } \alpha_L| < 3^{-3}$  and  $g_S|\text{Im } A_L| < 6 \times 10^{-2}$

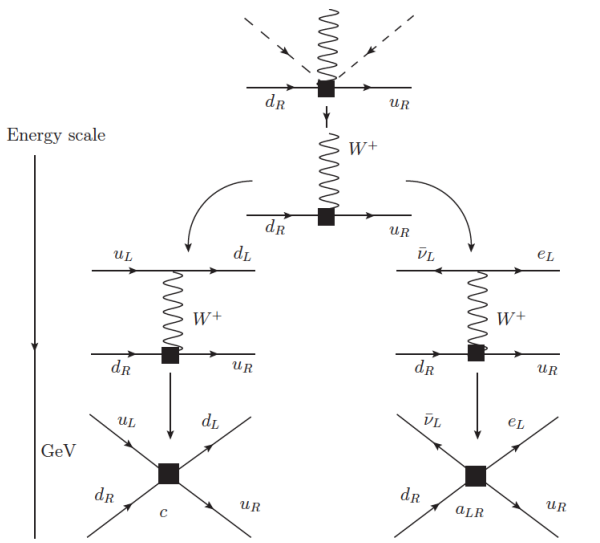
# Time-reversal violation in EDMs

Ng and Tulin [2005]  
Khriplovich [1991, 1997]

- Atomic and molecular EDM measurements limit same couplings
  - Any coupling imaginary part  $a_{LR}$  always contributes to neutron EDM
  - $C_S$  and  $C_T$  couplings linked to electron-quark interactions in  $\beta$  decay

EDM	e cm (90% C.L.)	Coeff. $\beta$ decay
$n$	$2.9 \times 10^{-26}$	$D$
$^{199}\text{Hg}$	$2.6 \times 10^{-29}$	$D, R$
$^{205}\text{Tl}$	$0.9 \times 10^{-24}$	$R$
YbF	$ d_e  < 10.5 \times 10^{-28}$	$R$
ThO	$ d_e  < 8.7 \times 10^{-29}$	$R$

# Time reversal violation in EDMs



$$\mathcal{L} = \frac{c}{\Lambda^2} \bar{u}_R \gamma^\mu d_R \tilde{\varphi}^\dagger i D_\mu \varphi$$

Using  $\chi$ PT and NDA

$$d_n = -10^{-20} \frac{\text{Im}c}{2\sqrt{2}G_F\Lambda^2} \text{e cm}$$

De Vries *et al.*, Seng *et al.*

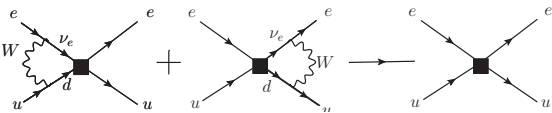
# Time-reversal violation in EDMs

KKV, Wilschut, Timmermans [2015]  
Khriplovich [1991, 1997]

- Molecular EDMs constrain  $C_S$  and  $C_T < 10^{-8}$

$$\mathcal{L} = \sum_N \frac{G_f}{\sqrt{2}} [C_S \bar{N} N \bar{e} i \gamma_5 e + C_T \bar{N} \sigma_{\mu\nu} N \bar{e} i \gamma_5 \sigma^{\mu\nu} e]$$

- Can be linked to  $e$ - $u$  coupling



$$-\frac{G_F}{\sqrt{2}} \frac{\alpha}{4\pi} \ln \left( \frac{\mu^2}{M_W^2} \right) V_{ud} \text{Im} (2A_L + 24\alpha_L) \left[ \bar{e} i \gamma_5 e \bar{u} u + \frac{1}{2} \bar{e} i \gamma_5 \sigma_{\mu\nu} e \bar{u} \sigma^{\mu\nu} u \right]$$

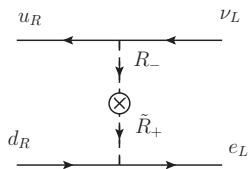
- Very rough estimate

# T-violation: Current constraints

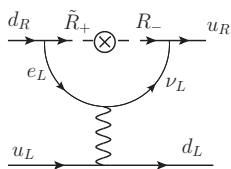
KKV, Wilschut, Timmermans[2015]

	$\text{Im } a_{LR}$	$\text{Im } A_L$	$\text{Im } \alpha_L$
$\beta$ decay	$4 \times 10^{-4}$	$6 \times 10^{-2}$	$3 \times 10^{-3}$
EDM	$3 \times 10^{-6}$	$10^{-5}$	$10^{-6}$

- EDM constraints beyond the FSIs
- Limits for  $a_{LR}$  apply to  $R$ -parity violating MSSM, LRSM ...



dim-8 contribution to  $\beta$  decay



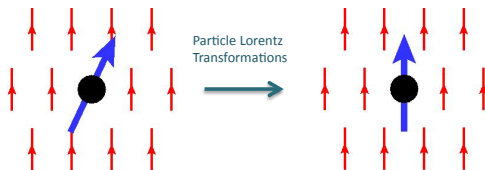
Loop contribution to EDM

- Example: Leptoquarks also not “EDM-safe”

- LHC experiments will give stronger constraints
- EDMs will be improved with factor 10 – 100
- $\beta$  decay experiments should focus on left-handed new couplings
  - $\beta$  shape measurements
  - Super allowed Fermi decays (also  $V_{ud}$ ) and mirror nuclei
  - Neutron lifetime and  $g_A$
  - Theory updates needed
- Cancellation between coefficients  $\rightarrow$  strong finetuning
- Specific models  $\rightarrow$  no dim-6 operators
- Light new degrees of freedom?

# Lorentz-Symmetry Breaking: Motivation

- Standard Model + General Relativity  $\rightarrow$  Quantum Gravity?
- Viable scenarios for Lorentz symmetry breaking
  - Mechanism for CPT violation
- Use effective field theory approach
  - Can be probed in low-energy precision experiments



- Observer invariance maintained
- Breaking of particle Lorentz invariance



# EFT approach: SME

Colladay and Kostelecky[1988]

- SME = SM + all Lorentz symmetry breaking terms
- Most general EFT and gauge invariant (also dim-3 and dim-4)

$$\mathcal{L}^{(3)} = -m\bar{\varphi}\varphi - a_{\mu}\bar{\varphi}\gamma^{\mu}\phi - b_{\mu}\bar{\varphi}\gamma^{\mu}\gamma_5\varphi$$

$$\mathcal{L}^{(4)} = i\bar{\varphi}\gamma_{\nu}\partial^{\nu}\varphi + c_{\mu\nu}\bar{\varphi}\gamma^{\mu}\partial^{\nu}\varphi + d_{\mu\nu}\bar{\varphi}\gamma_5\gamma^{\mu}\partial^{\nu}\varphi$$

CPT-odd Lorentz violating

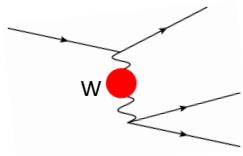
CPT-even Lorentz violating

- Fundamental theory is still Lorentz invariant
- Unique experimental signatures
- Weak interaction mainly unexplored

# Lorentz Violation in the weak interaction

J.P. Noordmans *et al.* [2013]  
KKV *et al.* [2015]

Theoretical framework  $\rightarrow$  modified  $W$ -boson propagator



General Lorentz violating tensor

$$\langle W^{\mu+}(p)W^{\nu-}(-p) \rangle = \frac{-i(g^{\mu\nu} + \chi^{\mu\nu})}{M_W^2}$$

- In the minimal SME  $\chi^{\mu\nu} = -k_{\phi\phi}^{\mu\nu} - \frac{i}{2g}k_{\phi W}^{\mu\nu} + \frac{2p_\rho p_\sigma}{M_W^2}k_W^{\rho\mu\sigma\nu}$
- Best constraints  $\mathcal{O}(10^{-7})$  from forbidden  $\beta$  decay searches in 70s
  - Enhancement of Lorentz-violating effects
  - High intensity sources

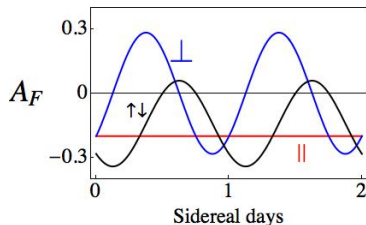
# Lorentz violation in $\beta$ decay

## Example Fermi decay

KKV *et al.* [2015]

$$\frac{dW_F}{dW_0} = \left( 1 + b \frac{m_e}{E_e} + 2\chi_r^{00} + 2\chi_r^{0i} \frac{p_e^i}{E_e} + (a + \chi_r^{00}) \frac{\vec{p}_e \cdot \vec{p}_\nu}{E_e E_\nu} + 2\chi_i^{0j} \frac{(\vec{p}_e \times \vec{p}_\nu)^j}{E_e E_\nu} + \dots \right)$$

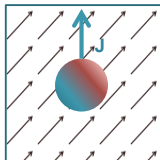
- Many new correlations
- Possible to probe different components directly
- Anisotropic emission
  - Preferred fermion direction or reaction plane
- Study in parallel with  $\beta\nu$ -correlation  $a$



# Lorentz violation in $\beta$ decay - Experiment

First experiment in allowed  $\beta$  decay

Muller *et al.* [2013]  
Sytema *et al.* [2016]



$$\frac{dW}{dW_0} = \left( 1 + A \left[ \vec{\beta} \cdot \hat{J} + \tilde{\chi}_i \hat{J}^i \right] \right)$$

- Spin  $J$  flip of polarized Gamow-Teller decay
  - search for sidereal variation to reduce systematic errors
  - sensitive to imaginary part of  $\chi$
- Final result  $\tilde{\chi}_i < 10^{-4}$

# Discussion

- Established a program to test Lorentz Violation in weak decays
- Lorentz violation could be studied parallel to BSM physics in  $\beta$  decay

## Outlook

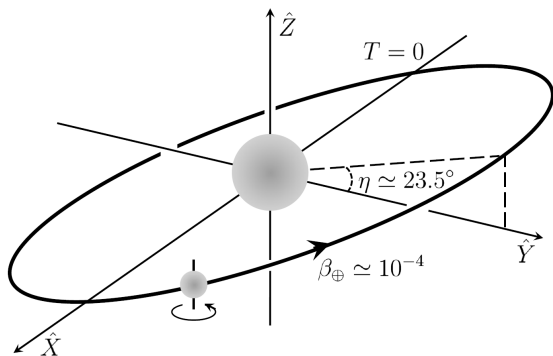
High statistics necessary to improve existing constraints topologies

- Use  $\gamma^2$  enhancement at LHC or future beta beam facilities

$$\frac{dW}{dW_0} = 1 + 2\gamma^2(\chi_r^{00} + 2\chi_r^{0l}\hat{v}_l + \chi_r^{lk}\hat{v}_l\hat{v}_k)$$

- Electron capture

## Backup Slides



# Backup: Forbidden $\beta$ decay

J.P. Noordmans *et al.* [2013]

Best current bounds from forbidden  $\beta$ -decay experiments

- enhancement of Lorentz-violating effects
- high intensity sources still allowed in the 70s

$$\chi_r^{\mu\nu} = \begin{bmatrix} 10^{-6} & 10^{-7} & 10^{-7} & 10^{-8} \\ 10^{-7} & 10^{-6} & 10^{-6} & 10^{-6} \\ 10^{-7} & 10^{-6} & 10^{-6} & 10^{-6} \\ 10^{-8} & 10^{-6} & 10^{-6} & 10^{-6} \end{bmatrix} \quad \chi_i^{\mu\nu} = \begin{bmatrix} \times & - & - & - \\ - & \times & 10^{-8} & 10^{-7} \\ - & 10^{-8} & \times & 10^{-7} \\ - & 10^{-7} & 10^{-7} & \times \end{bmatrix}$$

- High statistics necessary to improve existing constraints
- Unconstrained coefficients

# Backup: Search for Lorentz Violation

Kostelecky and Russell [2011]

More than 70 pages of limits in "Data Tables"

- Window on Quantum Gravity
- Weak interaction relatively unexplored

Particle-antiparticle comparisons  
Spectroscopy of hydrogen and antihydrogen

Baryon asymmetry  
Laboratory tests of gravity  
Clock-comparison measurements

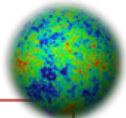
High-energy astrophysical observations  
Tests with microwave cavities and lasers

Muon  $g-2$   
Neutrino oscillations  
Matter interferometry  
Oscillations of K, B, D mesons  
QED tests in Penning traps



Neutrino experiments

CMB Polarization



CMB polarization  
Collider experiments  
Cosmological birefringence  
Dispersion from cosmological sources  
High-energy astrophysical observations



# Backup: Efforts in weak decays

S.E. Muller *et al.* [2013]

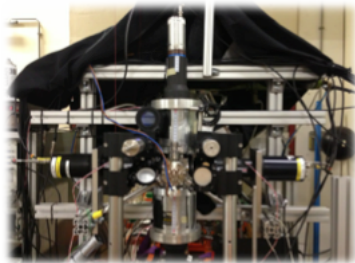
J.P. Noordmans *et al.* [2013, 2014]

KKV *et al.* [2015]

A. Syttema *et al.* [2016]

- Allowed  $\beta$  decay
- Forbidden  $\beta$  decay
- Pion decay at MINOS
- Kaon decay at KLOE
- Muon decay at  $g - 2$
- Electron capture

Setup for allowed  $\beta$  decay experiment



$\chi$  momentum-independent and CPT-even

- 15 independent components

# Backup: Naturalness

Pospelov *et al.* [2005,2008]

$$\underline{a_\mu, b_\mu} \sim \Lambda \quad \underline{c_{\mu\nu}, d_{\mu\nu}} \sim 1$$

- Dim-3 and 4 operators forbidden by SUSY
  - Generated by radiative corrections
- Dim-3 and 4 operators naturally suppressed

$$a_\mu, b_\mu \sim \frac{M_{\text{NP}}^2}{\Lambda} \quad c_{\mu\nu}, d_{\mu\nu} \sim \frac{M_{\text{NP}}}{\Lambda}$$

- No assumptions on new theories between the electroweak and Planck scale