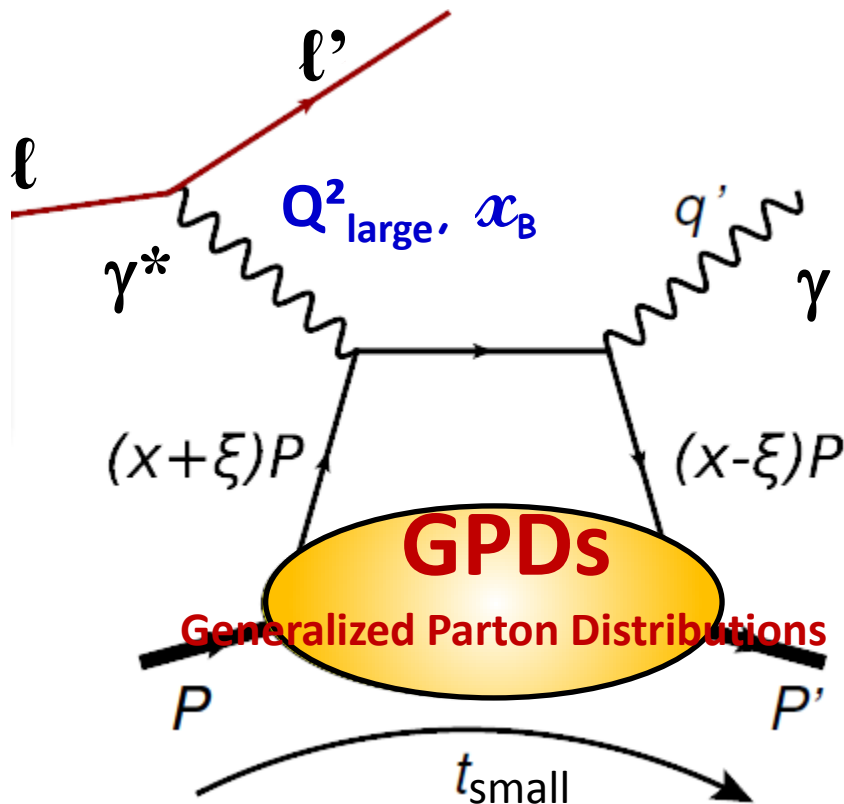


# DVCS OVERVIEW



Workshop New Vistas in Low-Energy precision Physics (LEPP)  
Nicole d'Hose, Mainz, 5 April 2016

# Deeply virtual Compton scattering (DVCS)



Definition of variables:

$x$ : average long. momentum

$\xi$ : long. mom. difference  $\simeq x_B/(2 - x_B)$

$t$ : four-momentum transfer  
related to  $b_{\perp}$  via Fourier transform

D. Mueller *et al*, Fortsch. Phys. 42 (1994)

X.D. Ji, PRL 78 (1997), PRD 55 (1997)

A. V. Radyushkin, PLB 385 (1996), PRD 56 (1997)

**DVCS:  $\ell p \rightarrow \ell' p' \gamma$**

the golden channel

because it interferes with  
the Bethe-Heitler process

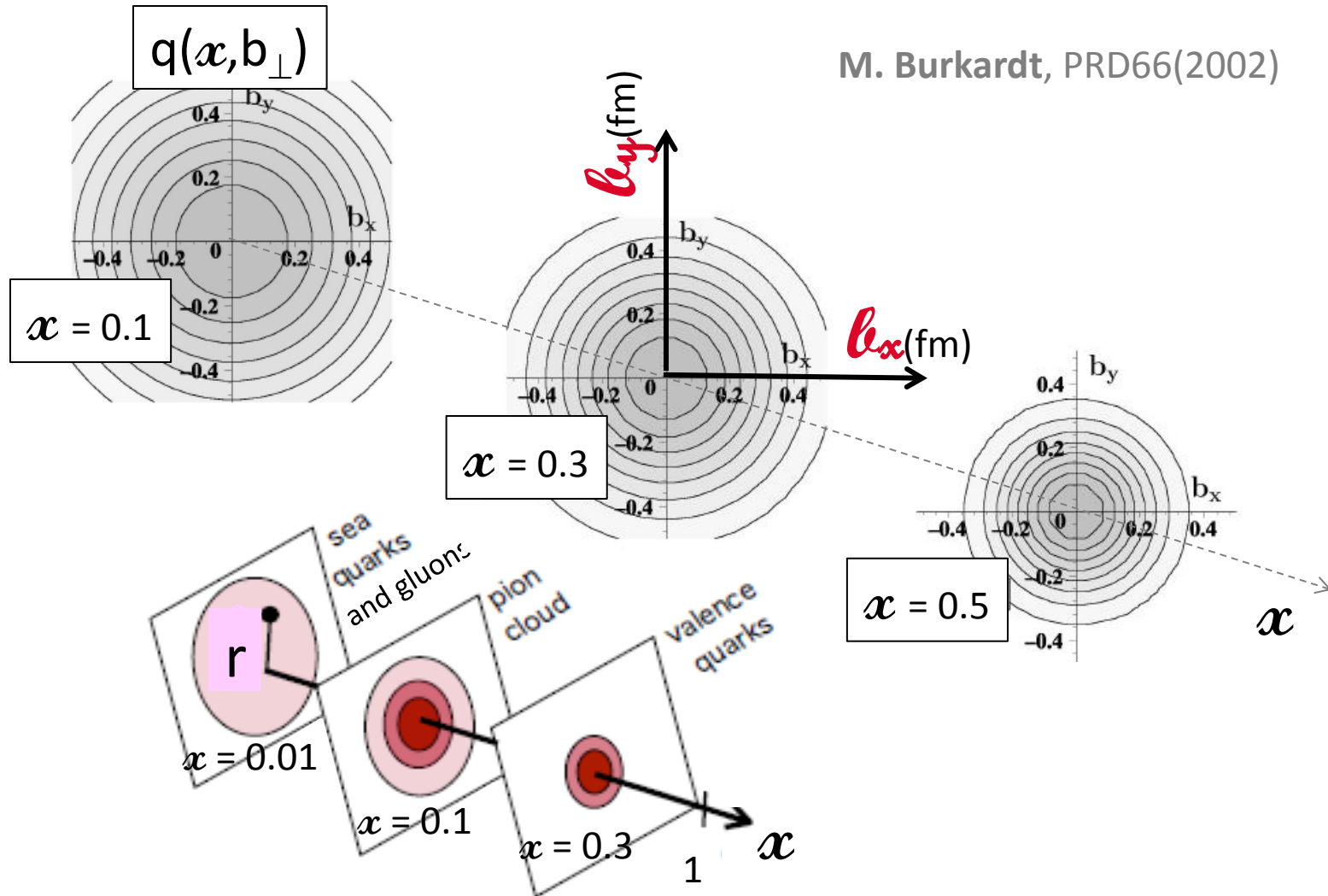
also meson production

$\ell p \rightarrow \ell' p' \pi, \rho$  or  $\phi$  or  $J/\psi \dots$

# 3D imaging: mapping in the transverse plane

Proton  
moving  
towards us

M. Burkardt, PRD66(2002)

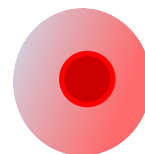


Correlation between the spatial distribution of partons  
and its longitudinal momentum fraction



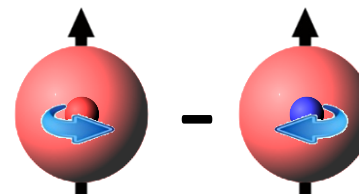
# The 2 most famous GPDs

$$H(x, \xi, t) \xrightarrow{t \rightarrow 0} q(x) \text{ or } f_1(x)$$



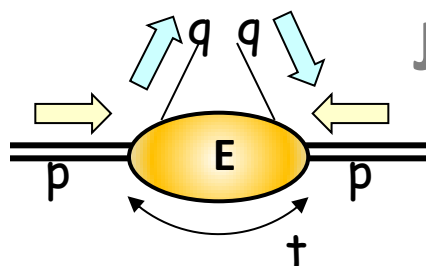
"Elusive"

$$E(x, \xi, t) \leftrightarrow f_{1T}^\perp(x, k_T)$$



**Sivers:** quark  $k_T$  & nucleon transv. Spin

$$2J^q = \lim_{t \rightarrow 0} \int x (H^q(x, \xi, t) + E^q(x, \xi, t)) dx$$



Ji sum rule: PRL78 (1997) cited 1404 times

**Relation to OAM**

$$\frac{1}{2} = \frac{1}{2} \Delta\Sigma + \Delta G + \mathcal{L}$$

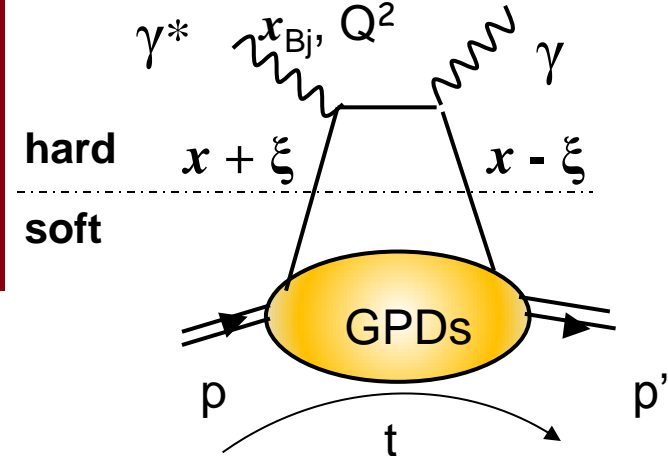
Jaffe and Manohar  
NPB337 (1990)

$\frac{1}{2} \Delta\Sigma \sim 0.15$  well known from DIS/SIDIS

$\Delta G \sim 0.2$  known from DIS/pp

$\mathcal{L}$  unknown

# Compton Form Factors are measured in DVCS

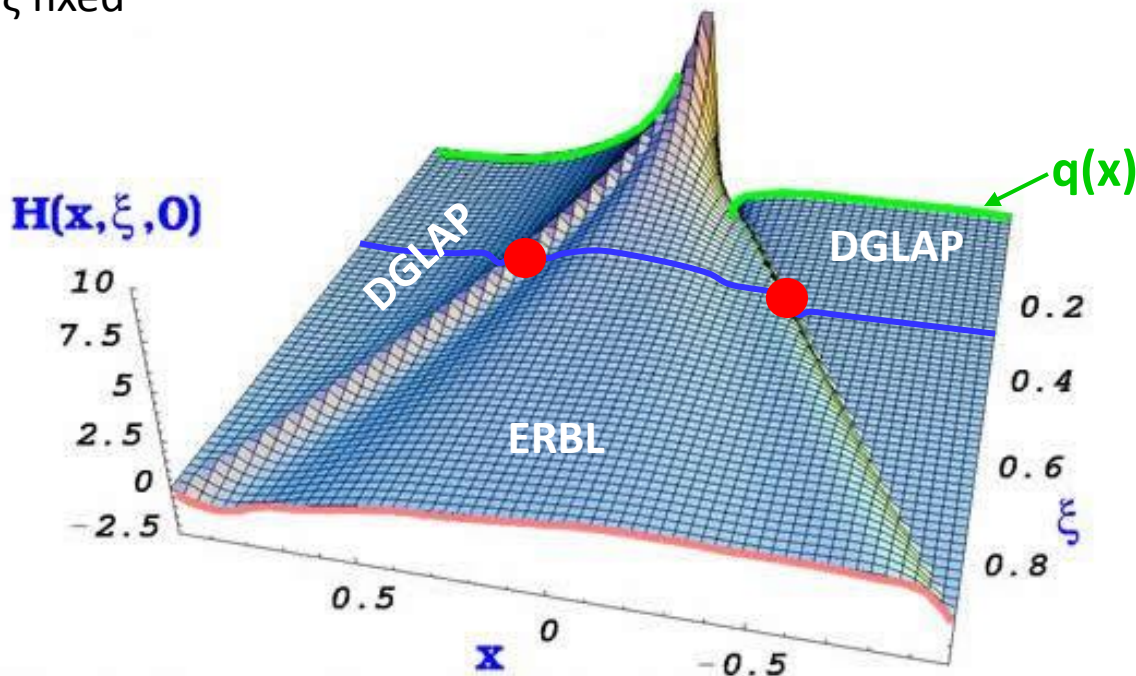


The amplitude DVCS at LT & LO in  $\alpha_s$ :

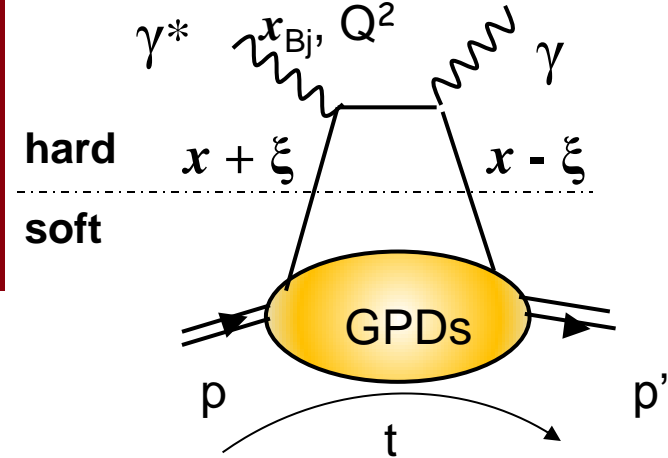
$$\mathcal{H} = \int_{-1}^{+1} dx \frac{H(x, \xi, t)}{x - \xi + i\epsilon} = \mathcal{P} \int_{-1}^{+1} dx \frac{H(x, \xi, t)}{x - \xi} - i \pi H(x = \pm \xi, \xi, t)$$

Real part
Imaginary part

$t, \xi$  fixed



# Compton Form Factors are measured in DVCS



The amplitude DVCS at LT & LO in  $\alpha_s$ :

$$\mathcal{H} = \int_{-1}^{+1} dx \frac{H(x, \xi, t)}{x - \xi + i\varepsilon} = \mathcal{P} \int_{-1}^{+1} dx \frac{H(x, \xi, t)}{x - \xi} - i \pi H(x = \pm \xi, \xi, t)$$

$t, \xi$  fixed

**Real part** **Imaginary part**

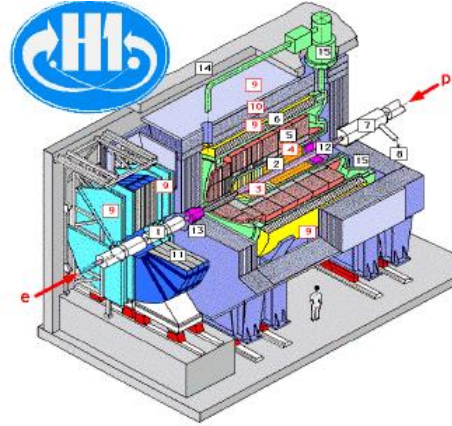
$$\mathcal{Re} \mathcal{H}(\xi, t) = \mathcal{P} \int dx \frac{\mathcal{Im} \mathcal{H}(x, t)}{x - \xi} + \mathcal{D}(t)$$

**$\mathcal{D}$  term** related to the Energy-Momentum Tensor :  
Polyakov, PLB 555 (2003) 57-62

**Im part** measured in  
**Beam Spin**  
or **Target Spin** asymmetries

**Real part** measured in  
**Beam Charge** asymmetry  
or Int. term in DVCS **x- sect.**

# The past and future experiments



**Collider mode e-p** forward fast proton

**HERA: H1** and **ZEUS**

Polarised 27 GeV e-/e+

Unpolarized 920 GeV proton

~ Full event reconstruction

**Fixed target mode** slow recoil proton

**HERMES:** Polarised 27 GeV e-/e+

Long, Trans polarised p, d target

Missing mass technique

2006-07 with recoil detector



**Jlab: Hall A, C, CLAS** High lumi, polar. 6 & **12 GeV e-**

Long, (Trans) polarised p, d target

Missing mass technique



**COMPASS @ CERN:** Polarised **160 GeV  $\mu^+/\mu^-$**

p target, (Trans) polarised target

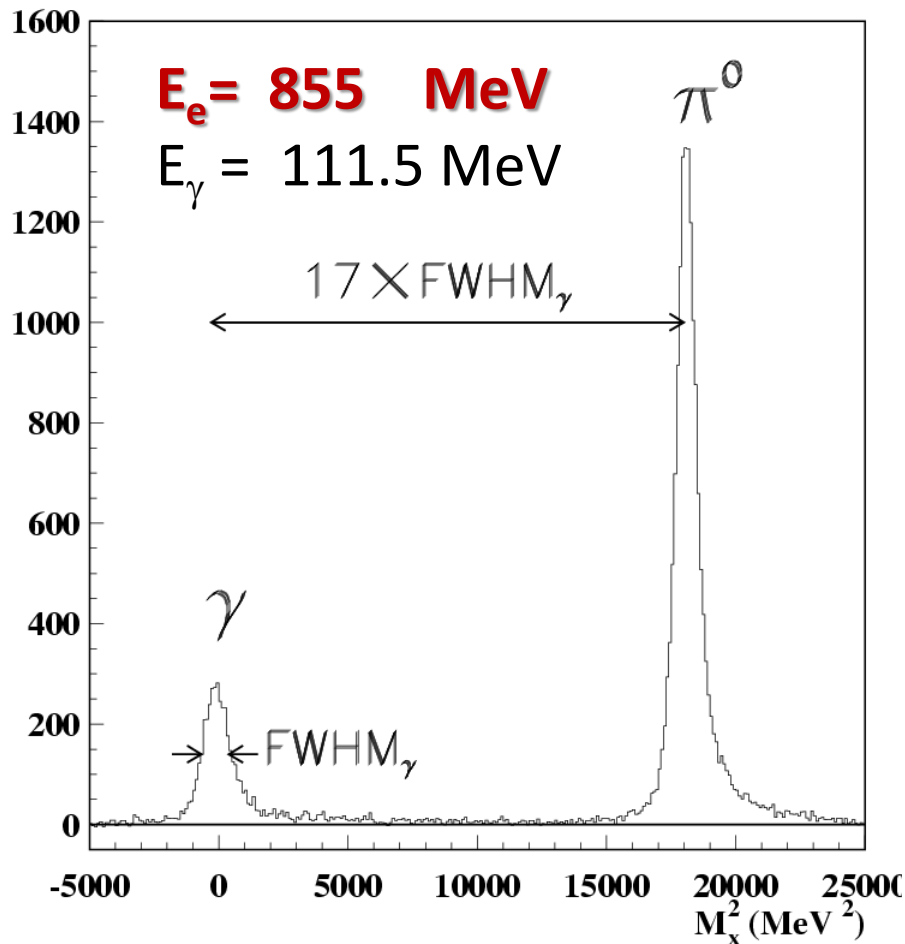
with recoil detection





# Exclusivity : $\ell p \rightarrow \ell + \gamma + p$

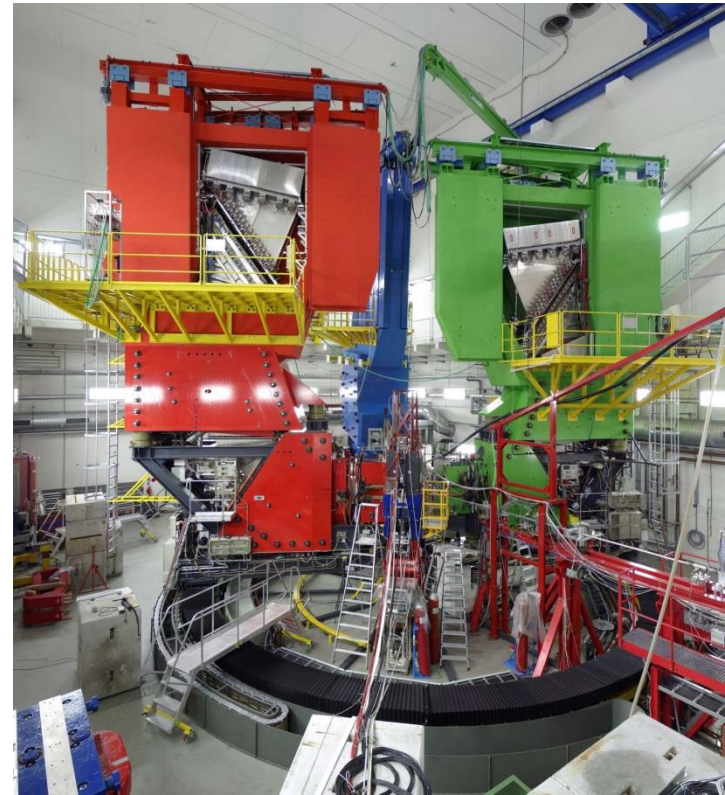
$$M_x^2 = (P_\ell + P_p - P_{\ell'} - P_{p'})^2$$



$ep \rightarrow e' p' \gamma$

$ep \rightarrow e' p' \pi^0$

VCS @ MAMI 1995



Very good separation due to the excellent resolutions

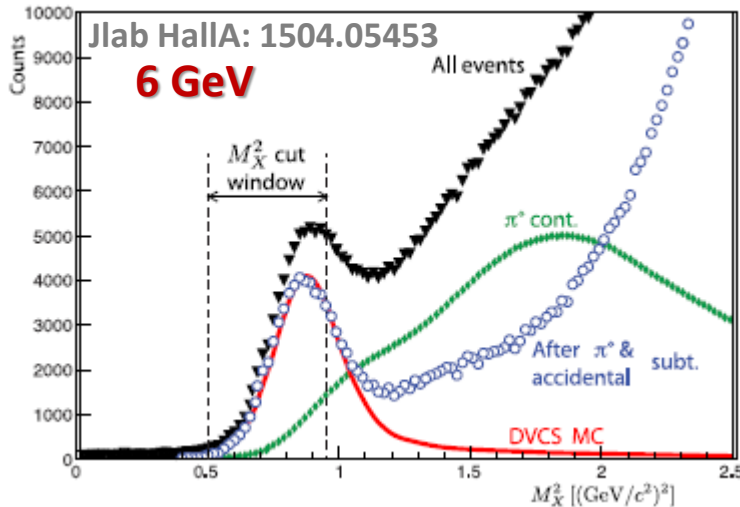
Beam  $\Delta E_e/E_e = 10^{-4}$

Spectros  $\Delta P/P = 10^{-4}$   $\Delta\theta < 3 \text{ mrad}$



# Exclusivity : $\ell p \rightarrow \ell + \gamma + p$

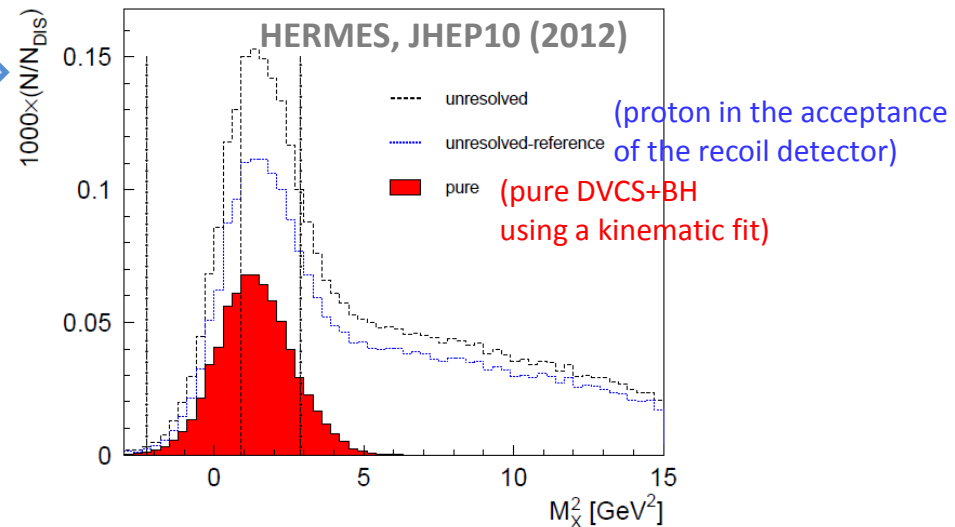
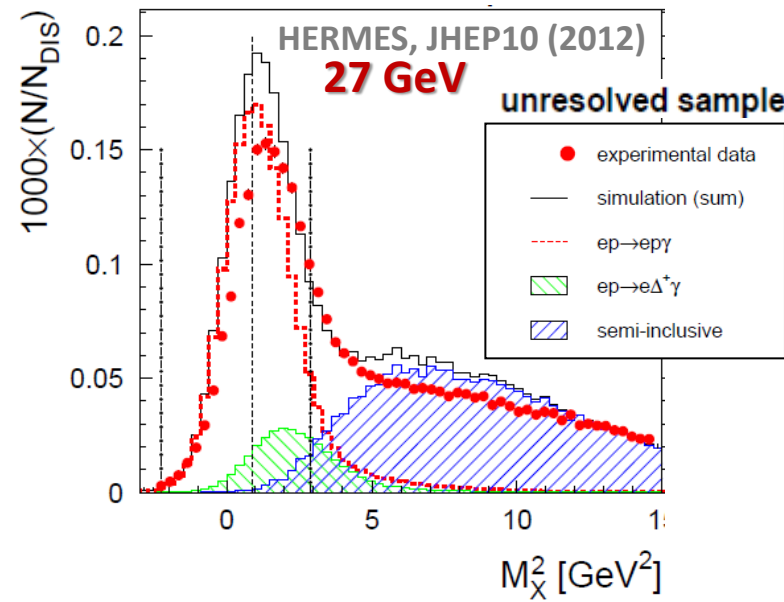
$M_x^2 = (P_\ell + P_p - P_{\ell'} - P_\gamma)^2$   $\Delta M_x^2$  increases with the beam energy !



$\ell p \rightarrow \ell' + \gamma (+p')$  for DVCS + BH

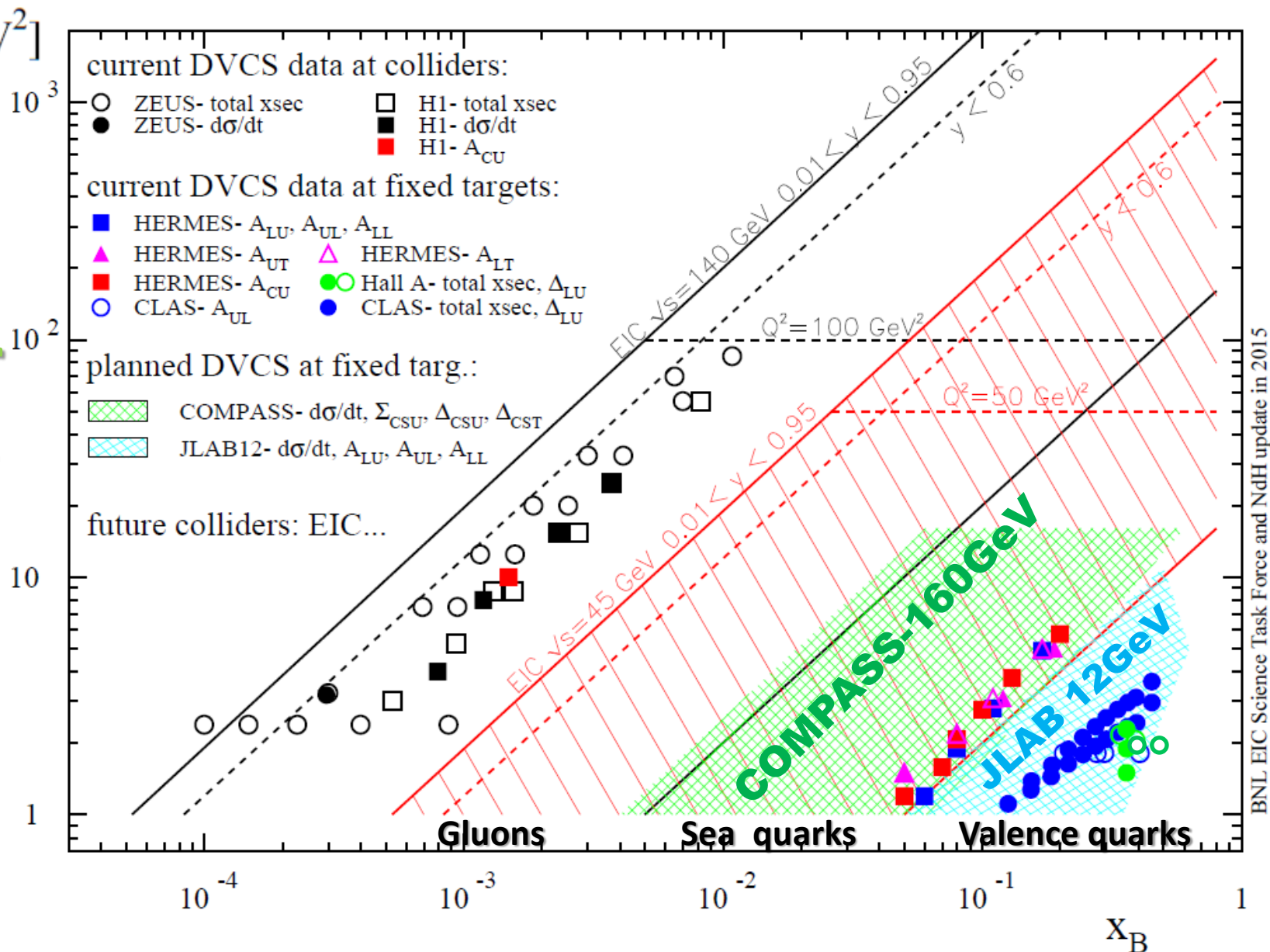
Contamination from  $\pi^0$  decay:

- $\ell p \rightarrow \ell' + \gamma (+\Delta^+)$  associated DVCS + BH
- $\ell p \rightarrow \ell' + \gamma (+\gamma + p')$  exclusive  $\pi^0$
- $\ell p \rightarrow \ell' + \gamma (+\gamma + p' + \dots)$  SIDIS  $\pi^0$

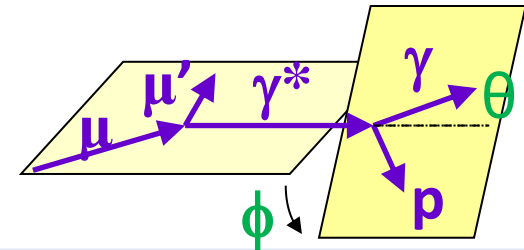
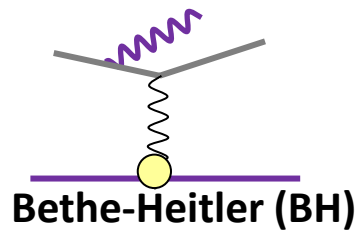
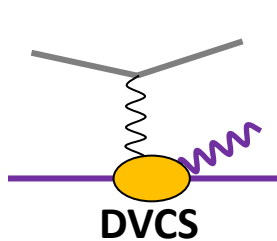


# The past and future DVCS experiments

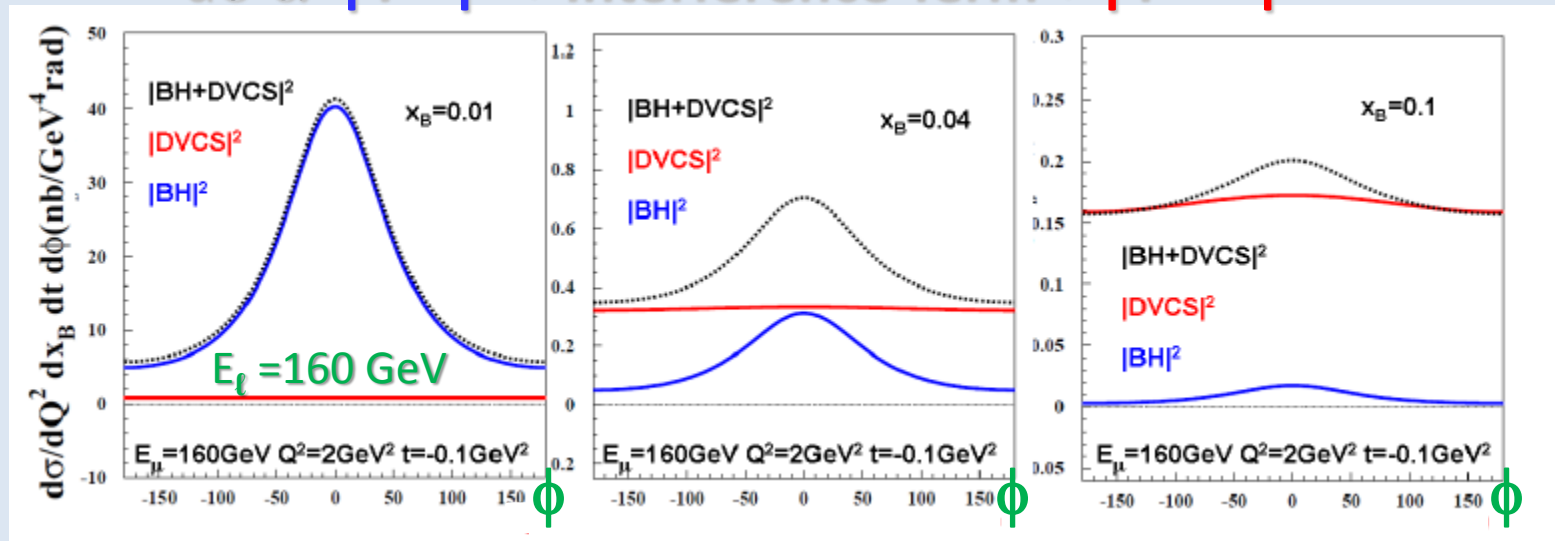
Start  
2001  
  
After  
2016



# Impact of the beam energy for DVCS



$$d\sigma \propto |T^{BH}|^2 + \text{Interference Term} + |T^{DVCS}|^2$$



BH dominates  
Reference yield

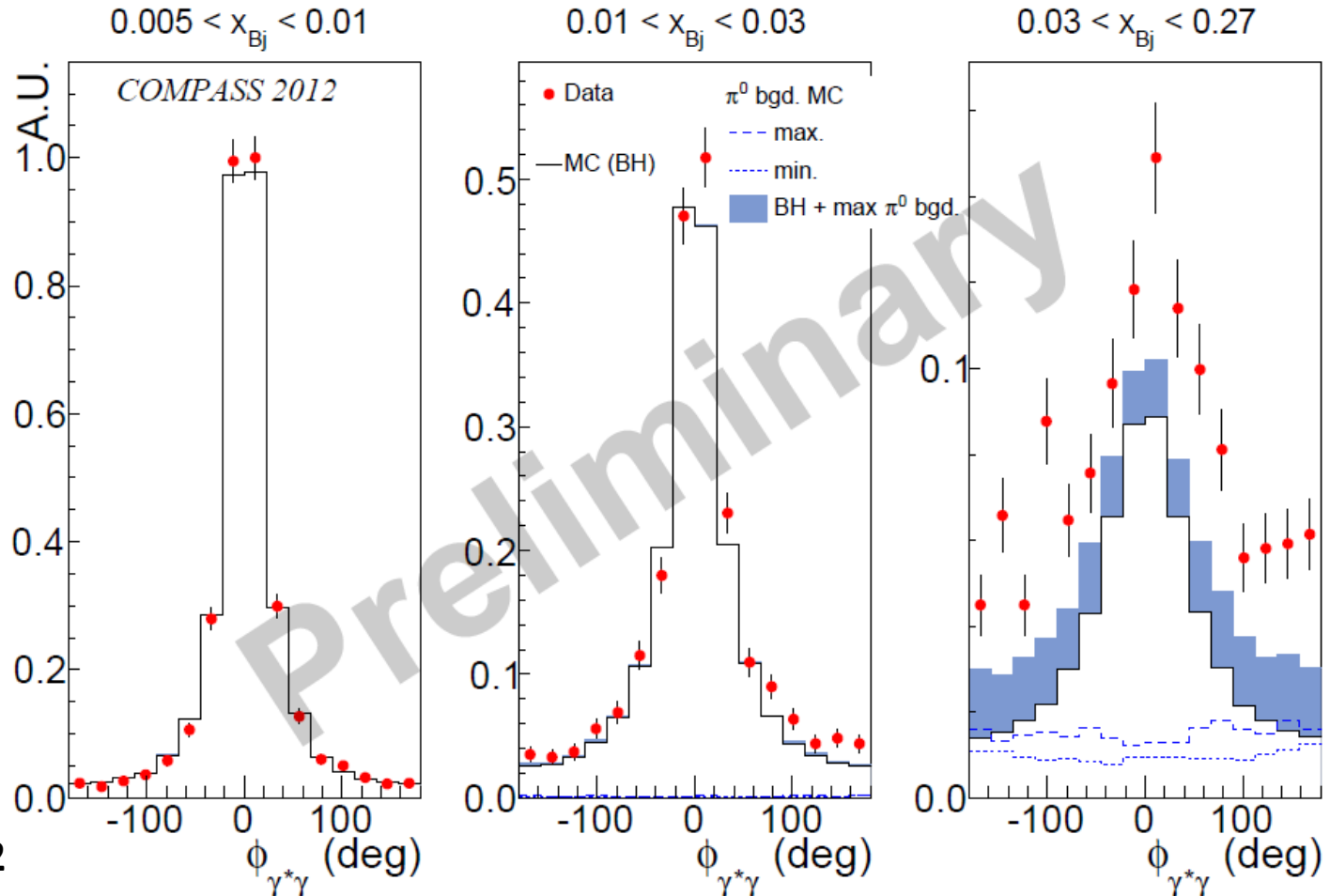
DVCS ampl. via interference  
Jlab, HERMES, H1, COMPASS

DVCS dominates - Study of  $d\sigma^{DVCS}/dt$   
Only for H1, ZEUS, COMPASS



# DVCS and BH contributions @ COMPASS

$\mu^+$  and  $\mu^-$   
160 GeV



Pilot run in 2012

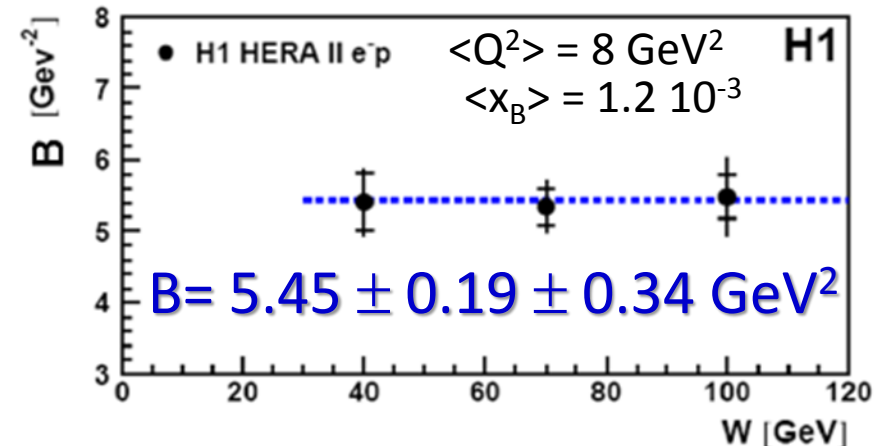
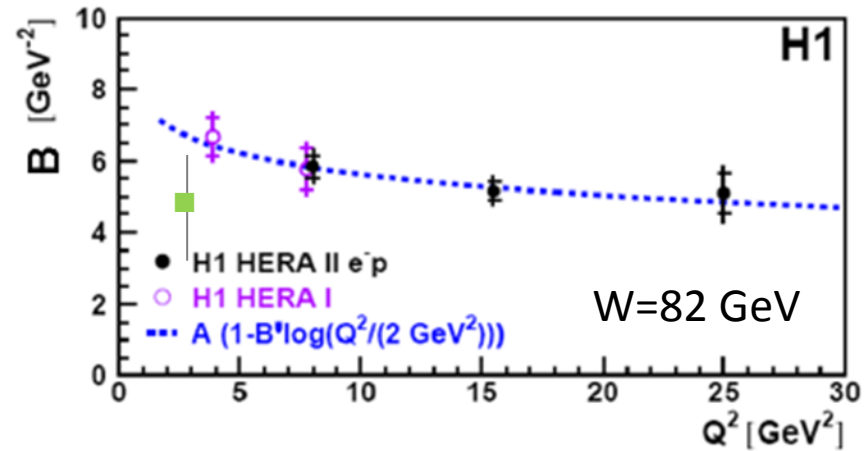
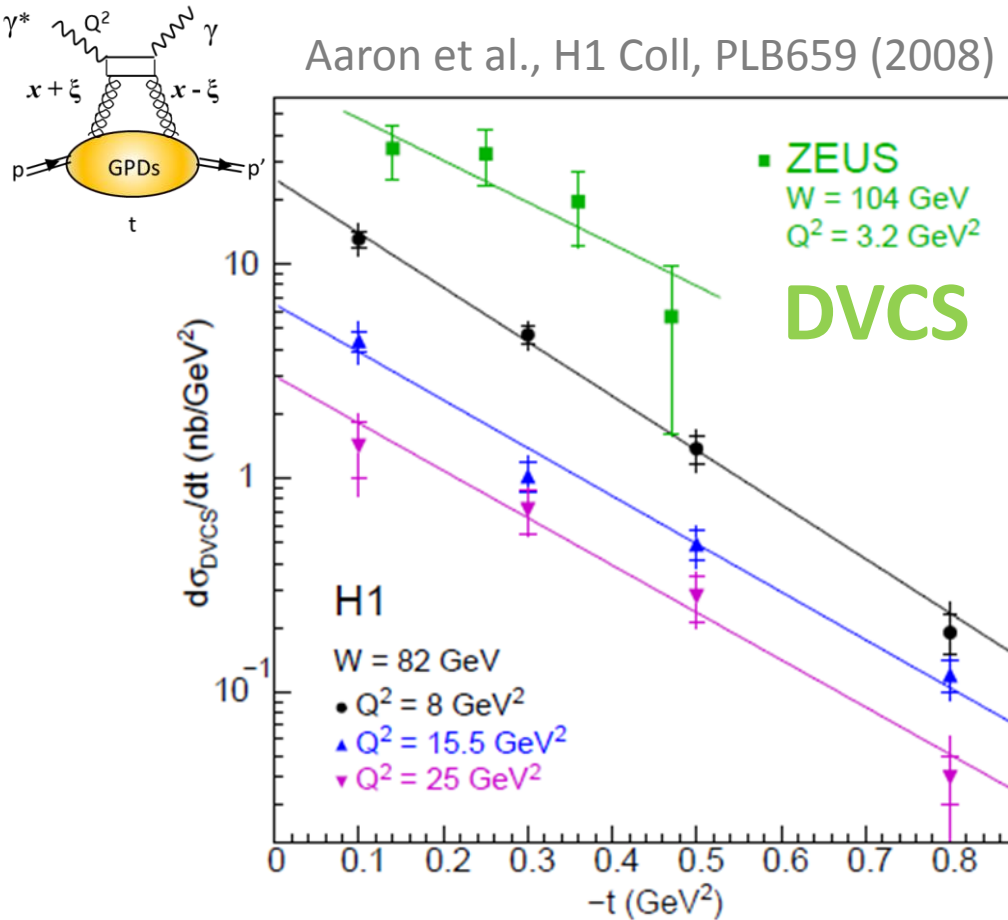
- ✓ Dominant Bethe-Heitler process clearly visible at small  $x_{Bj}$
- ✓ Maximum  $\pi^0$  background (from exclusive and SIDIS  $\pi^0$  production) estimated in blue
- ✓ The data at large  $x_{Bj}$  show an excess compared to BH+Background (for pure DVCS)

**COMPASS ready to take DVCS data in 2016 and 2017**

# Gluon imaging @ HERA

$$d\sigma^{\text{DVCS}}/dt = e^{-B|t|}$$

B is related to the transversed size of the scattering objects

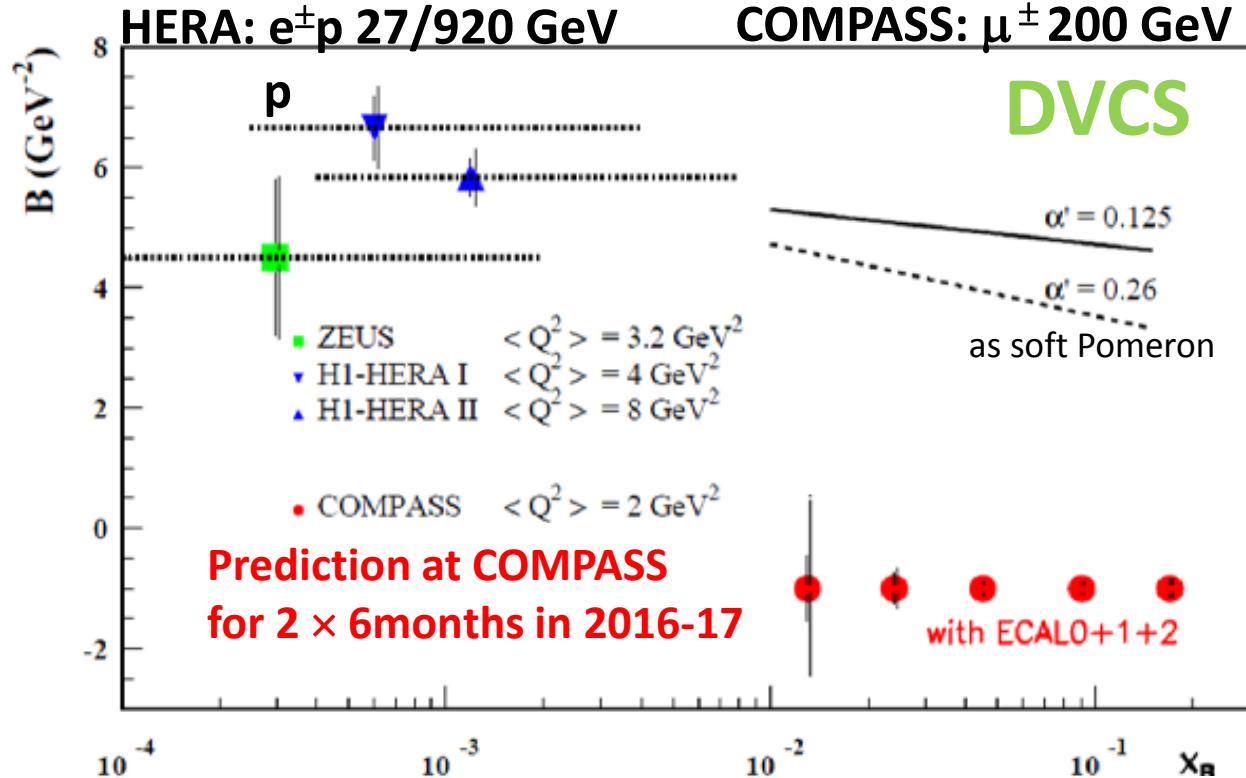


$$\langle r_{\perp}^2 \rangle \approx 2 B$$

$$\sqrt{\langle r_{\perp}^2 \rangle} = 0.65 \pm 0.02 \text{ fm}$$

to be compared to  $\sqrt{4 \frac{d}{dt} F_1^p} \Big|_{t=0} = 0.67 \pm 0.02 \text{ fm}$

# Sea quark imaging @ COMPASS



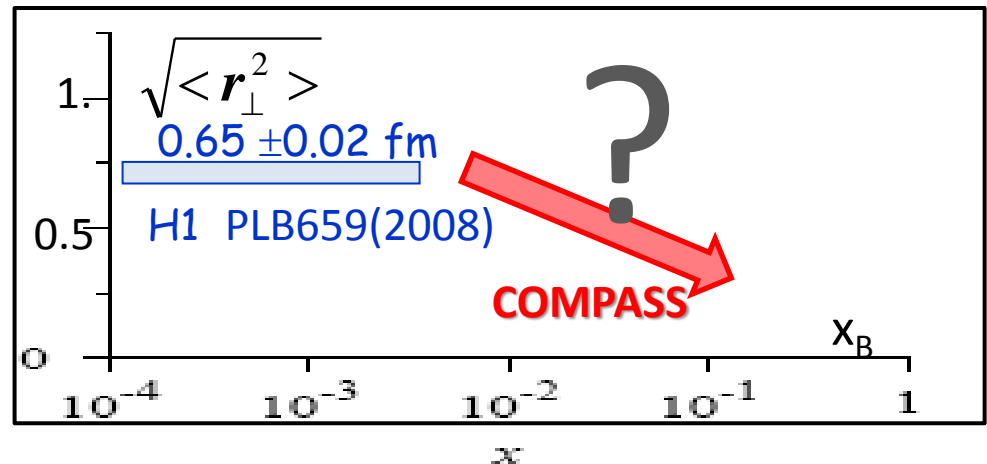
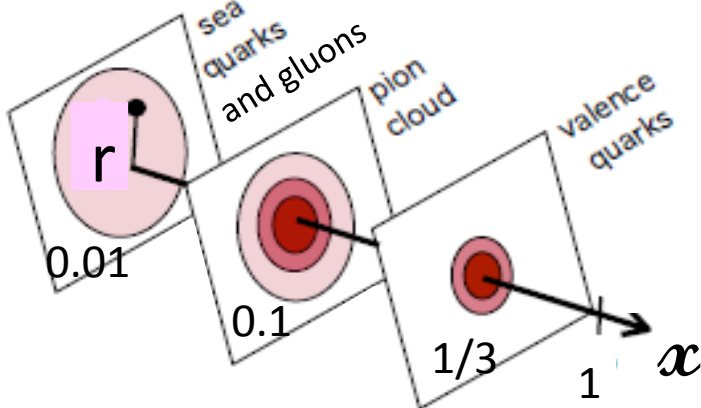
$$d\sigma^{\text{DVCS}}/dt = e^{-B|t|}$$

ansatz inspired by  
Regge Phenomenology:

$$B(x_B) = b_0 + 2 \alpha' \ln(x_0/x_B)$$

$\alpha'$  slope of Regge trajectory

$$\langle r_\perp^2(x_B) \rangle \approx 2B(x_B)$$



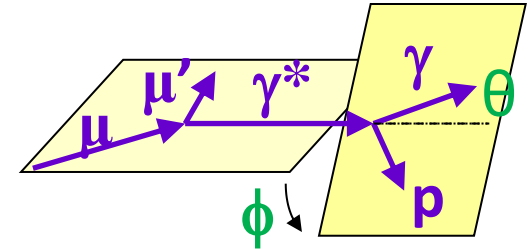


# DVCS-BH interference on the proton

- $Im$  DVCS with BSA or Beam Spin difference
- $Re$  DVCS with BCA or Beam Charge difference
- mainly constrains on the GPD H

# Azimuthal dependence of BH+DVCS

$$\frac{d^4\sigma(\ell p \rightarrow \ell p \gamma)}{dx_B dQ^2 d|t| d\phi} = \underset{\text{Well known}}{d\sigma^{BH}} + \left( d\sigma_{unpol}^{DVCS} + P_\ell d\sigma_{pol}^{DVCS} \right) + (e_\ell \text{Re } I + e_\ell P_\ell \text{Im } I)$$



Twist-2 >>

■ Twist-3,

■ Twist-2  
double helicity flip  
for gluons

$$\begin{aligned} d\sigma^{BH} &\propto c_0^{BH} + c_1^{BH} \cos \phi + c_2^{BH} \cos 2\phi \\ d\sigma_{unpol}^{DVCS} &\propto c_0^{DVCS} + c_1^{DVCS} \cos \phi + c_2^{DVCS} \cos 2\phi \\ d\sigma_{pol}^{DVCS} &\propto s_1^{DVCS} \sin \phi \\ \text{Re } I &\propto c_0^I + c_1^I \cos \phi + c_2^I \cos 2\phi + c_3^I \cos 3\phi \\ \text{Im } I &\propto s_1^I \sin \phi + s_2^I \sin 2\phi \end{aligned}$$

$$s_1^I = \text{Im } \mathcal{F} \quad c_1^I = \text{Re } \mathcal{F}$$

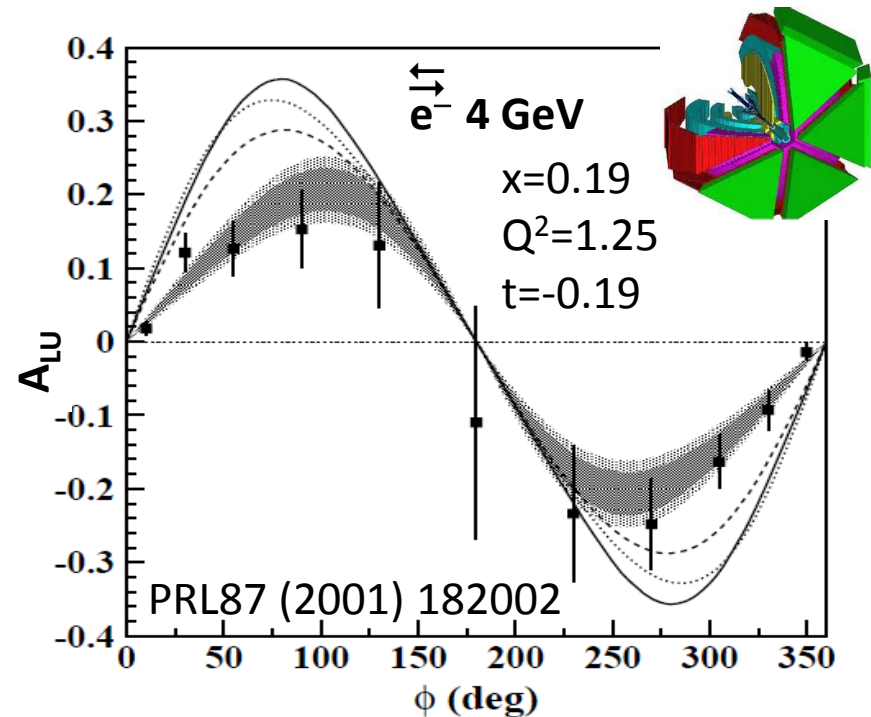
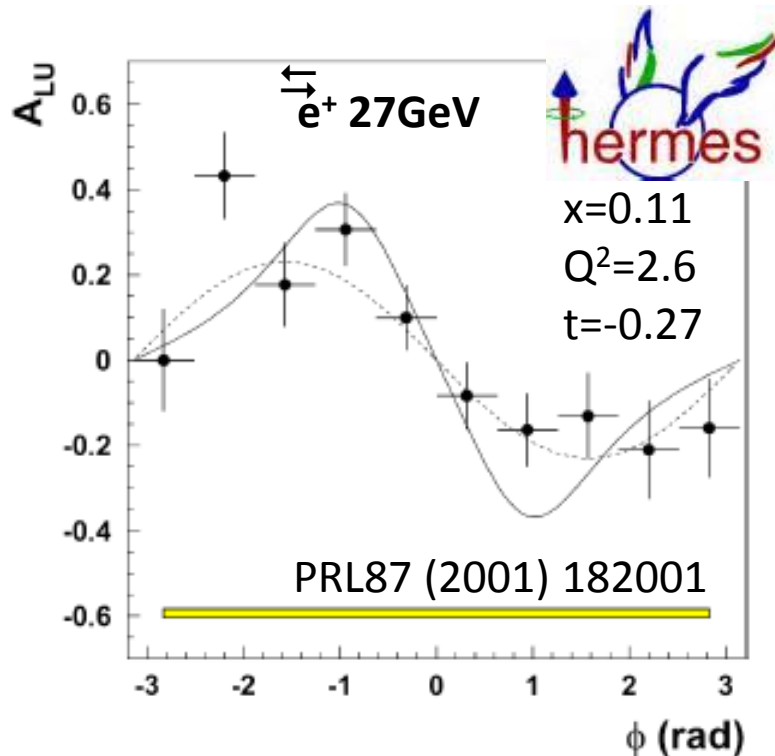
$$\mathcal{F} = F_1 \mathcal{H} + \xi (F_1 + F_2) \tilde{\mathcal{H}} - t/4m^2 F_2 \mathcal{E} \xrightarrow{\text{at small } x_B} F_1 \mathcal{H} \quad \text{for proton}$$

NB: to extract  $\mathcal{E}$  use a neutron (deuteron) target or a transversely pol. target

to extract  $\tilde{\mathcal{H}}$  use a longitudinally polarized target

# First Beam Spin Asymmetries in 2001

$$d\sigma^{\leftarrow} - d\sigma^{\rightarrow} = 2[d\sigma_{pol}^{DVCS} + \text{Im } I] \xrightarrow{L.T.} s_1^I \sin \phi$$



Validate the dominance of the handbag contribution

Fit and **VGG** model: Vanderhaeghen, Guichon, Guidal,...

PRL80(1998), PRD60(1999), PPNP47(2001), PRD72(2005)



# Beam Spin Sum and Diff of DVCS - HallA

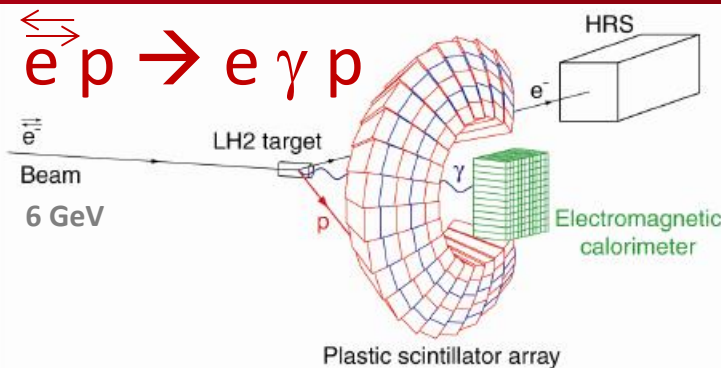
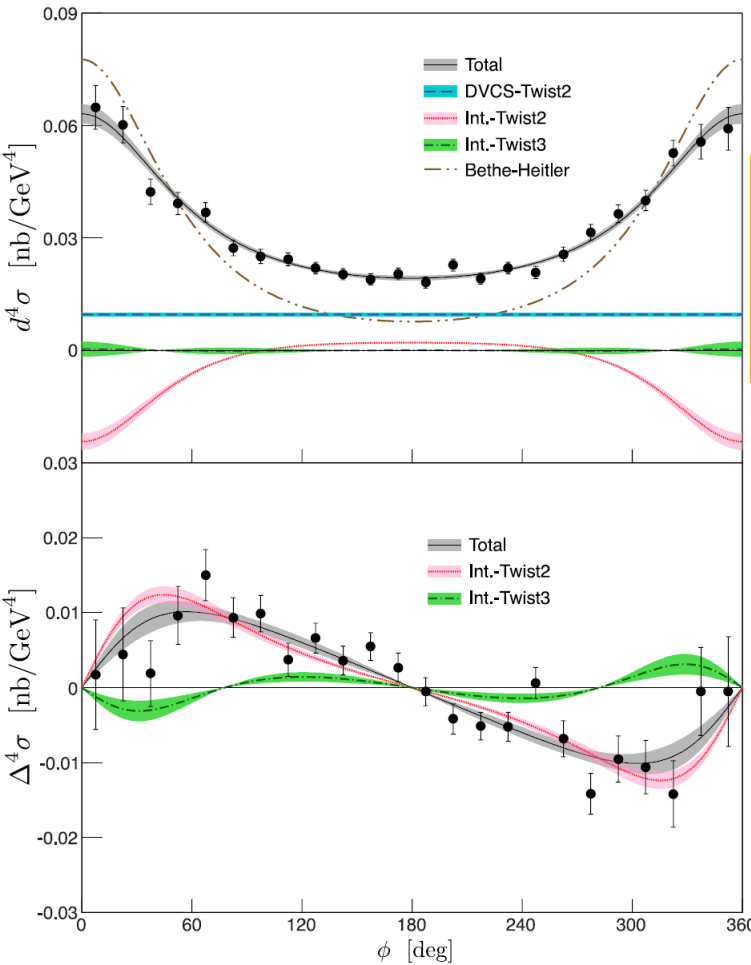
E00-110 pioneer experiment with magnetic spectrometer

$x_B=0.36$   $Q^2= 1.5, 1.9, 2.3 \text{ GeV}^2$  Munoz et al. PRL97, 262002 (2006)

$x_B=0.34, x_B=0.39$   $Q^2= 2.1 \text{ GeV}^2$  Defurne et al. arXiv: 1504.05453

new improved analysis

$x_B=0.36, Q^2= 2.3 \text{ GeV}^2, -t= 0.32 \text{ GeV}^2$



## Unpolarized cross section

$$\begin{aligned} d\sigma^{\leftarrow} + d\sigma^{\rightarrow} &\propto d\sigma^{BH} + d\sigma_{unpol}^{DVCS} + \text{Re } I \\ &\rightarrow d\sigma^{BH} + \underbrace{c_0^{DVCS}} + \underbrace{c_0^I + c_1^I \cos \phi}_{\text{pink}} + \underbrace{c_2^I \cos 2\phi}_{\text{green}} \end{aligned}$$

Further separation  $\rightarrow$  need of different  $\varepsilon$  or beam energies

## Helicity dependent cross section

$$\begin{aligned} d\sigma^{\leftarrow} - d\sigma^{\rightarrow} &\propto d\sigma_{pol}^{DVCS} + \text{Im } I \\ &\rightarrow \underbrace{s_1^I \sin \phi}_{\text{pink}} + \underbrace{s_2^I \sin 2\phi}_{\text{green}} \end{aligned}$$

These results supersede the previous publication

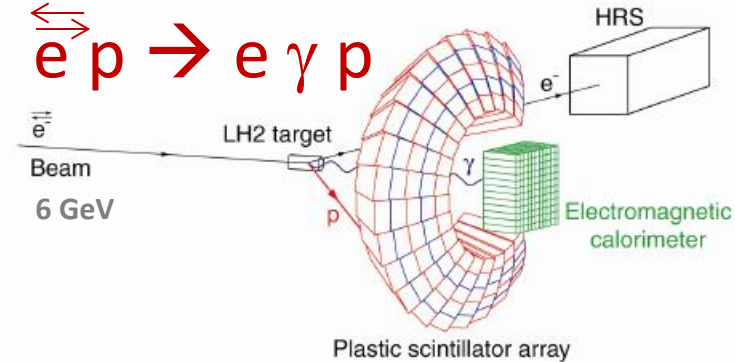
# Beam Spin Sum and Diff of DVCS - HallA

E00-110 pioneer experiment with magnetic spectrometer

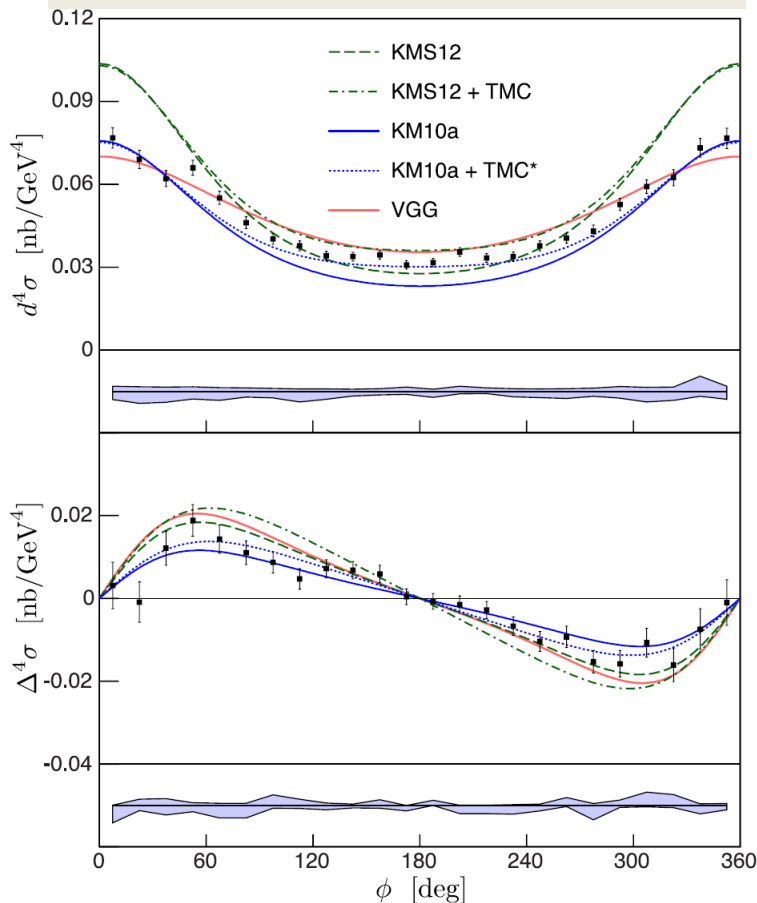
$x_B=0.36$   $Q^2=1.5, 1.9, 2.3 \text{ GeV}^2$  Munoz et al. PRL97, 262002 (2006)

$x_B=0.34, x_B=0.39$   $Q^2=2.1 \text{ GeV}^2$  Defurne et al. arXiv: 1504.05453

new improved analysis



$x_B=0.36, Q^2=1.9 \text{ GeV}^2, -t=0.23 \text{ GeV}^2$



## Comparison to models:

**VGG** popular model of GPD

**KMS12** Kroll, Moutarde, Sabatié, EPJC73 (2013)  
using the **GK** model of GPD adjusted on  
the hard exclusive meson production at small  $x_B$   
“universality” of GPD

**KM10a** fit including all the world DVCS data  
from HERA to HERMES and JLab

Difficulties to reproduce the total cross section at  $\phi=180^\circ$

+ **TMC** twist-4 corrections for kinematic effects due to  
target-mass and finite- $t$ , Braun et al., PRD79 (2014)

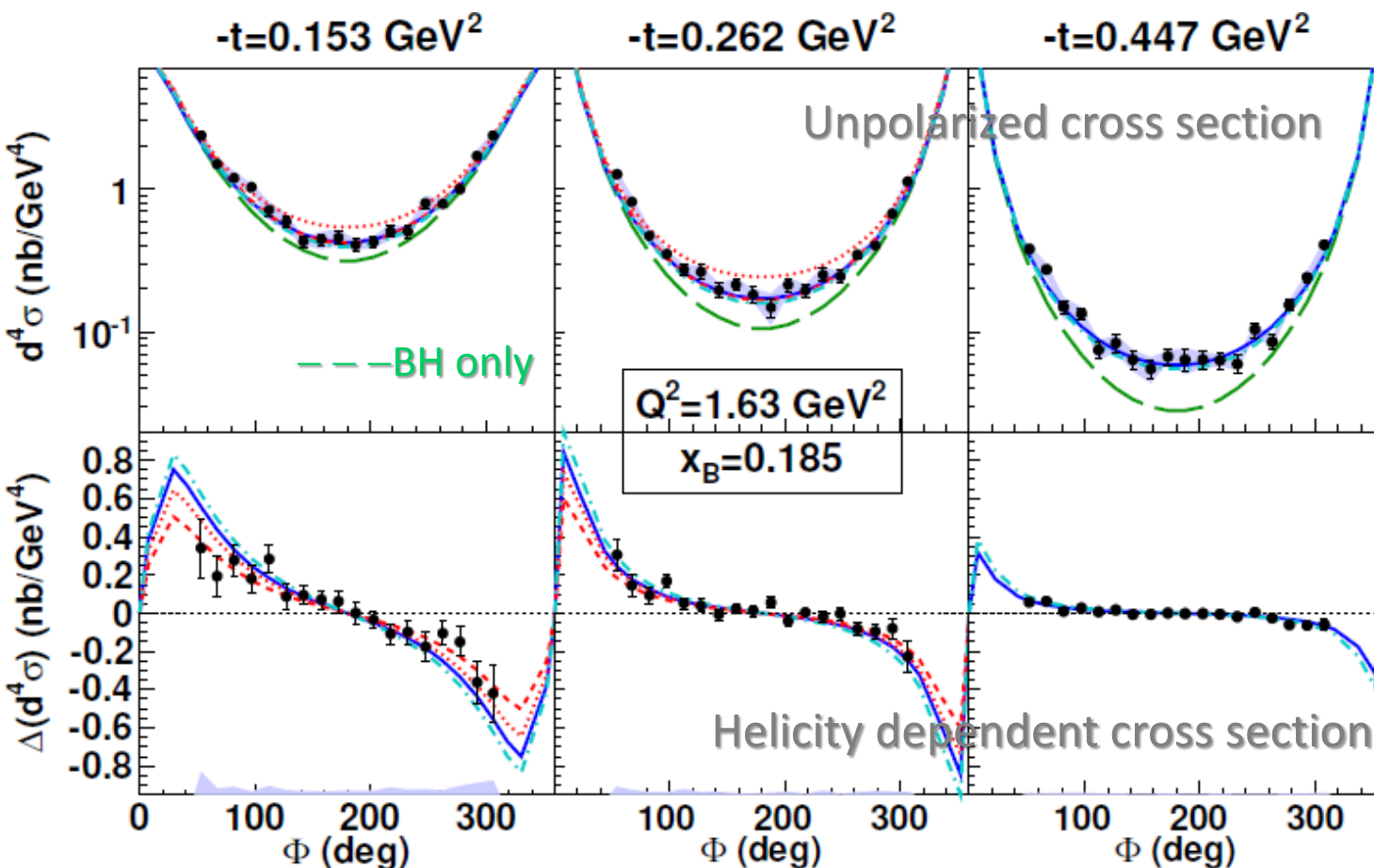
# Beam Spin Sum and Diff of DVCS - CLAS

21 bins in  $(x_B, Q^2)$  or 110 bins  $(x_B, Q^2, t)$

- Girod et al. PRL100, 162002 (2008)

- Jo et al. arXiv: 1504.02009 **new analysis**

$$\vec{e} p \rightarrow e \gamma p$$



models:

VGG

KMS12

KM10a ---

KM10 .....

old fit including  
the first data set  
of Jlab HallA



# Valence quark imaging at Jlab

Fit of only two CFFs at L.O and L.T.

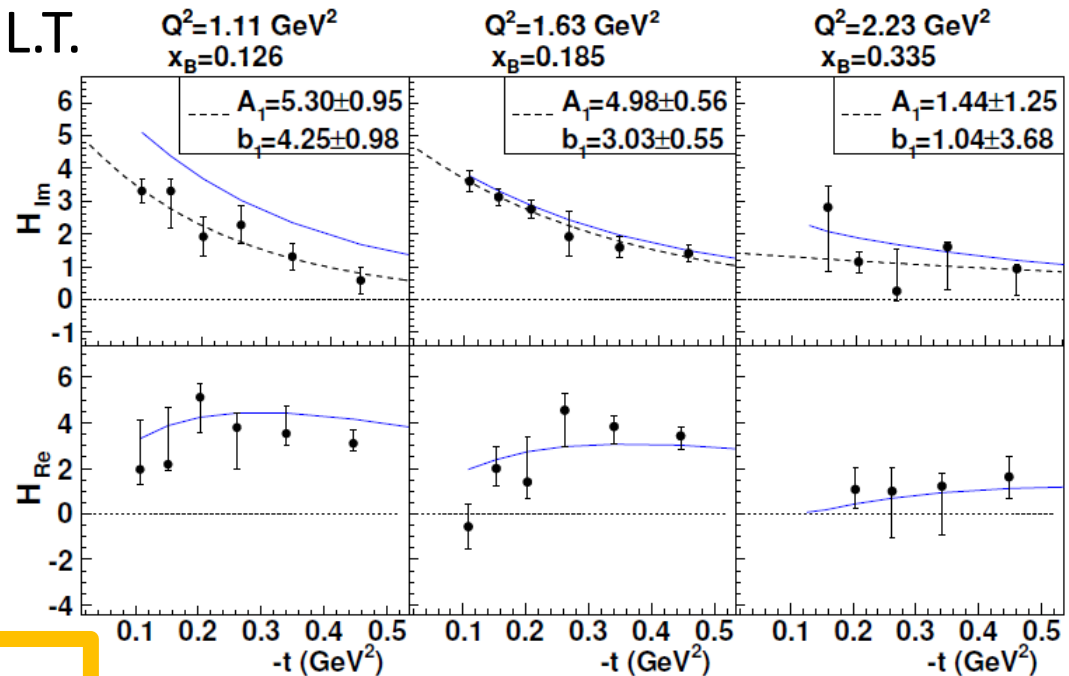
Jo et al. arXiv: 1504.02009

$$s_1^I = \text{Im } F_1 \mathcal{H}$$

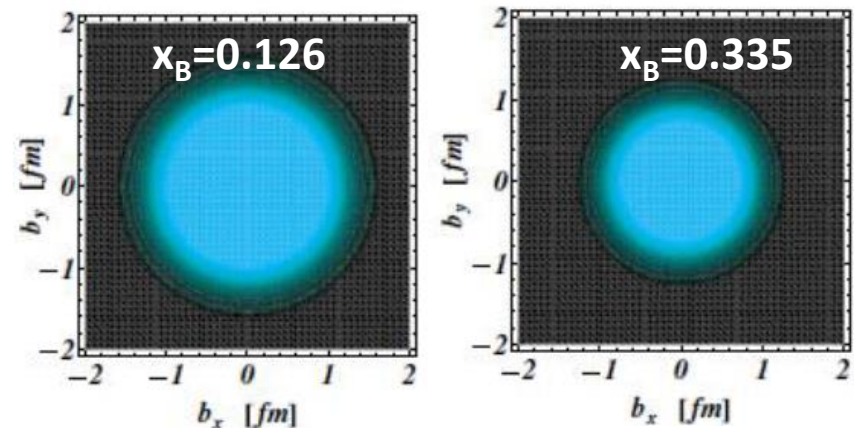
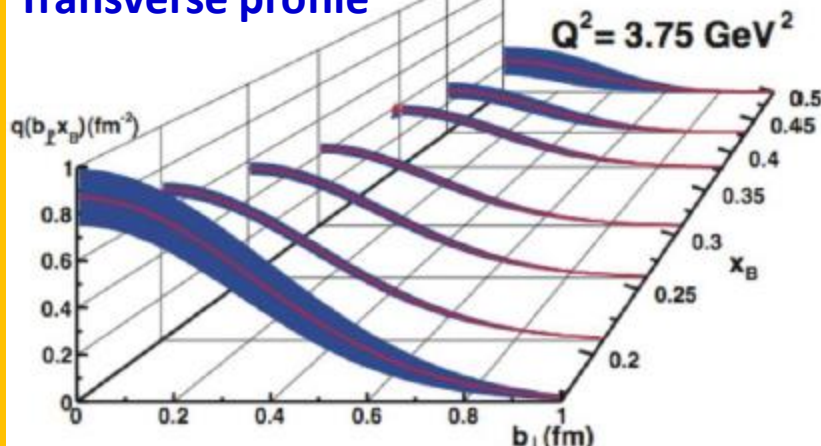
$$c_1^I = \text{Re } F_1 \mathcal{H}$$

— VGG model

..... Fit  $A e^{-b|t|}$



Projection for Jlab 12 GeV  
Transverse profile



# Future Beam Spin Sum and Diff @JLab12

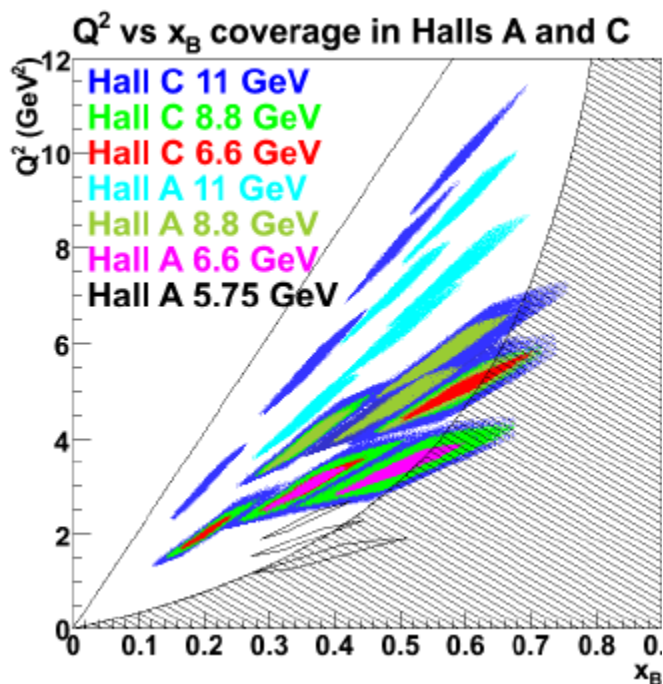
with high resolution magnetic spectrometer+ Calorimeter in Halls A and C

Exp. 2010: run E07-007

Now 2015: Hall A

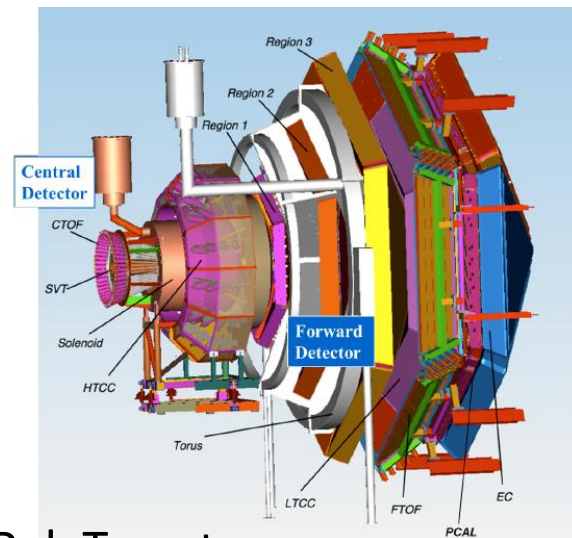
~2018: Hall C

Different beam energies for a Rosenbluth-like DVCS<sup>2</sup>/Interf. separation

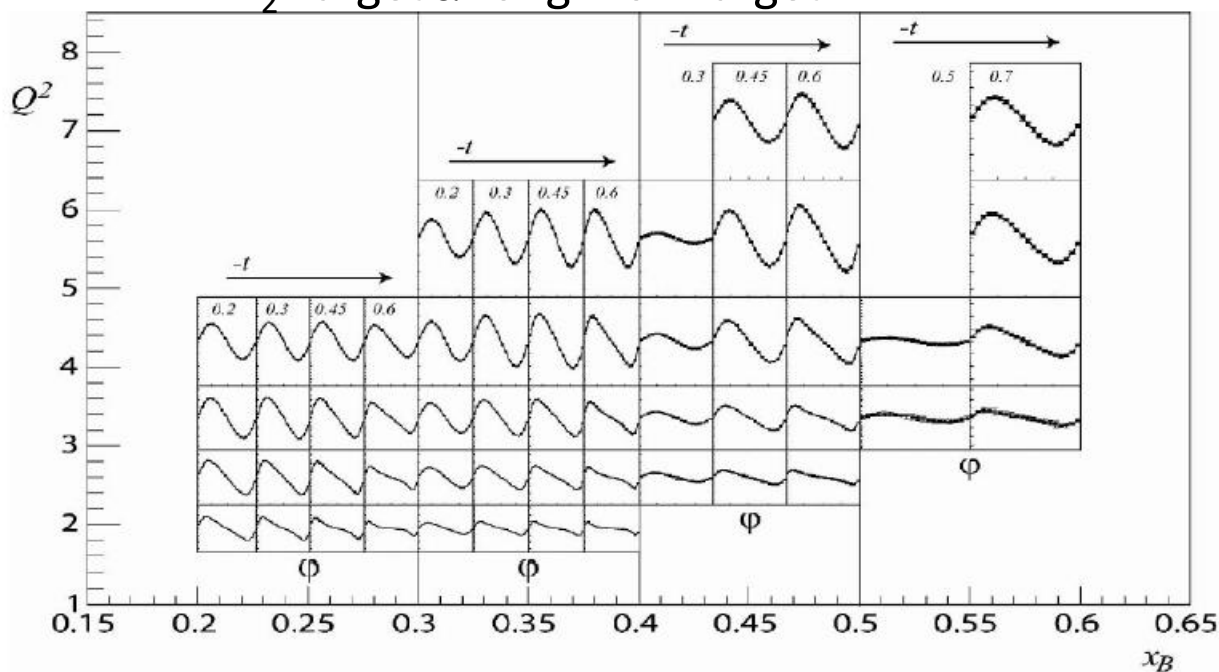


with CLAS12  
In 2016

E12-06-119



LH<sub>2</sub> Target & Long. Pol. Target

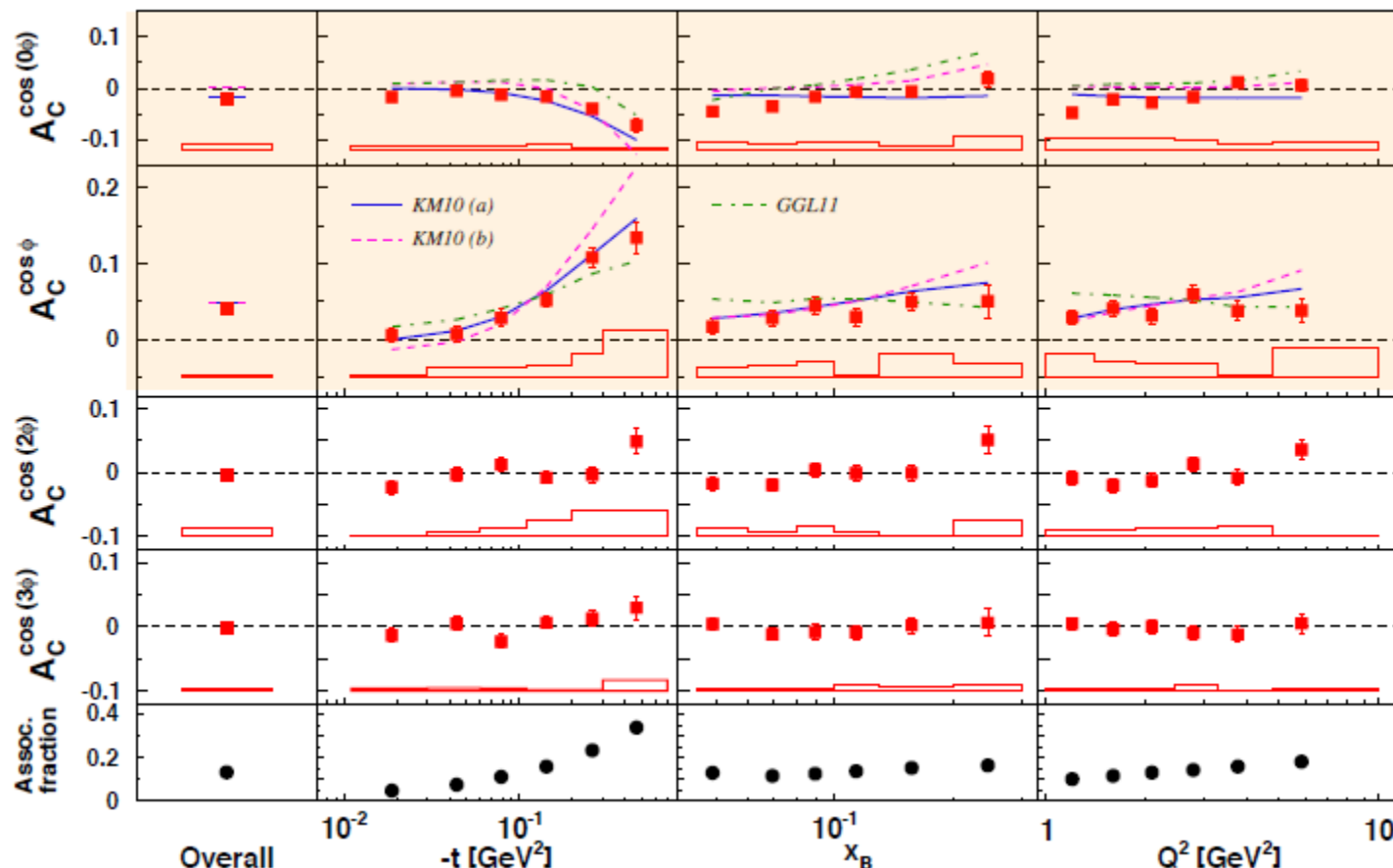


# Beam Charge Asymmetry @ HERMES

Complete data set including 2006-07 without recoil detection

A. Airapetian et al, JHEP 07 (2012) 032

<http://arxiv.org/abs/1203.6287>



Dominant Twist-2

$$c_0^I + c_1^I \cos \phi$$

$$c_1^I = \text{Re } F_1 \mathcal{H}$$

Twist-3 for Int

$$c_2^I \cos 2\phi$$

Twist-2 gluons for Int

$$c_3^I \cos 3\phi$$

resonant fraction

$$ep \rightarrow e\gamma\Delta^+$$

KM10a: <http://arxiv.org/abs/0904.0458>

Kumerički and Müller, Nucl. Phys. **B841** (2010)

GHL11: another flexible parameterization

<http://arxiv.org/abs/1012.3776>

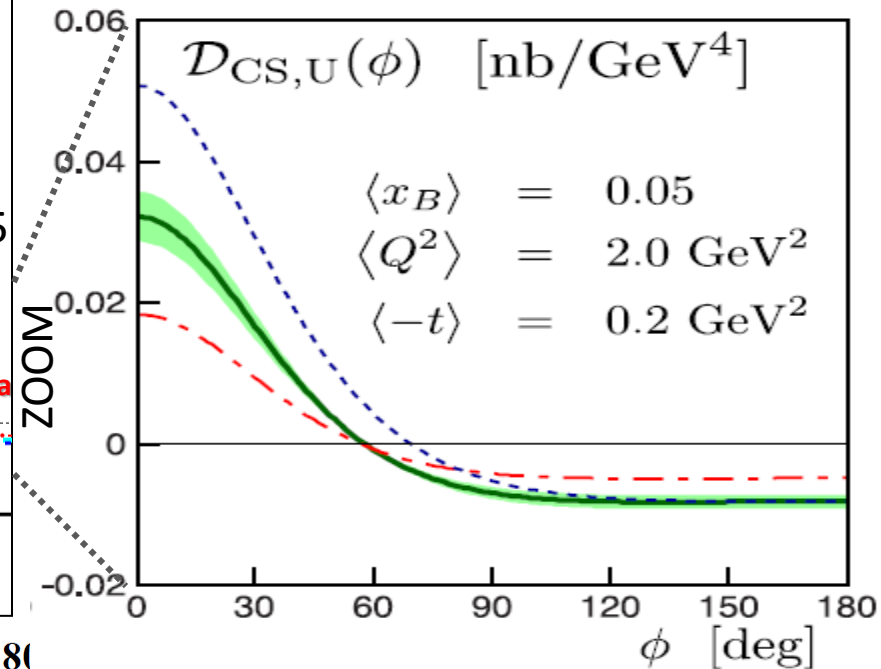
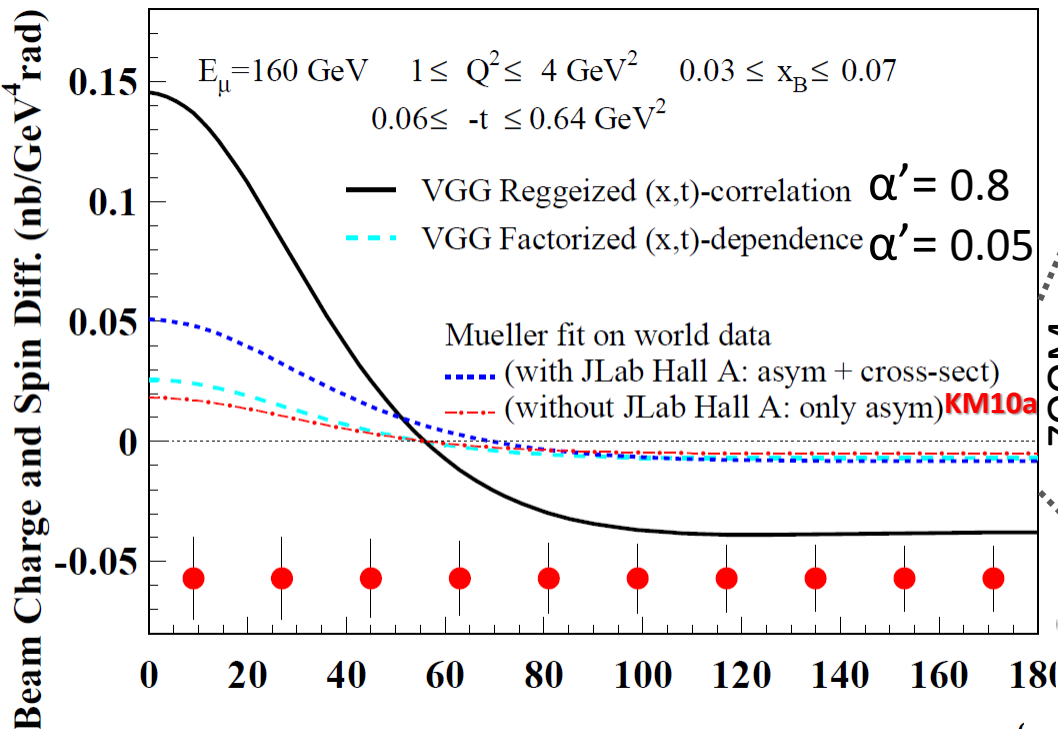
G. Goldstein, J. Hernandez and S. Liuti, Phys. Rev. **D84** (2011)

# Beam Charge and Spin Diff. @ COMPASS




$$\mathcal{D}_{CS,U} \equiv d\sigma^{\leftarrow+} - d\sigma^{\rightarrow-} = 2[d\sigma_{pol}^{DVCS} + \text{Re } I] \xrightarrow{L.T.} c_0^I + c_1^I \cos \phi$$

Comparison to different models

$$c_1^I = \text{Re } F_1 \mathcal{H}$$



**DVCS Prediction at COMPASS**  
**For  $2 \times 6$  months in 2016-17**

-  KMS12: Kroll, Moutarde, Sabatié  
EPJC 73 (2013) 2278
-  KM10a
-  KM10b (old fit with the 1st data set Hall A)

# Beam Charge and Spin Diff. @ COMPASS

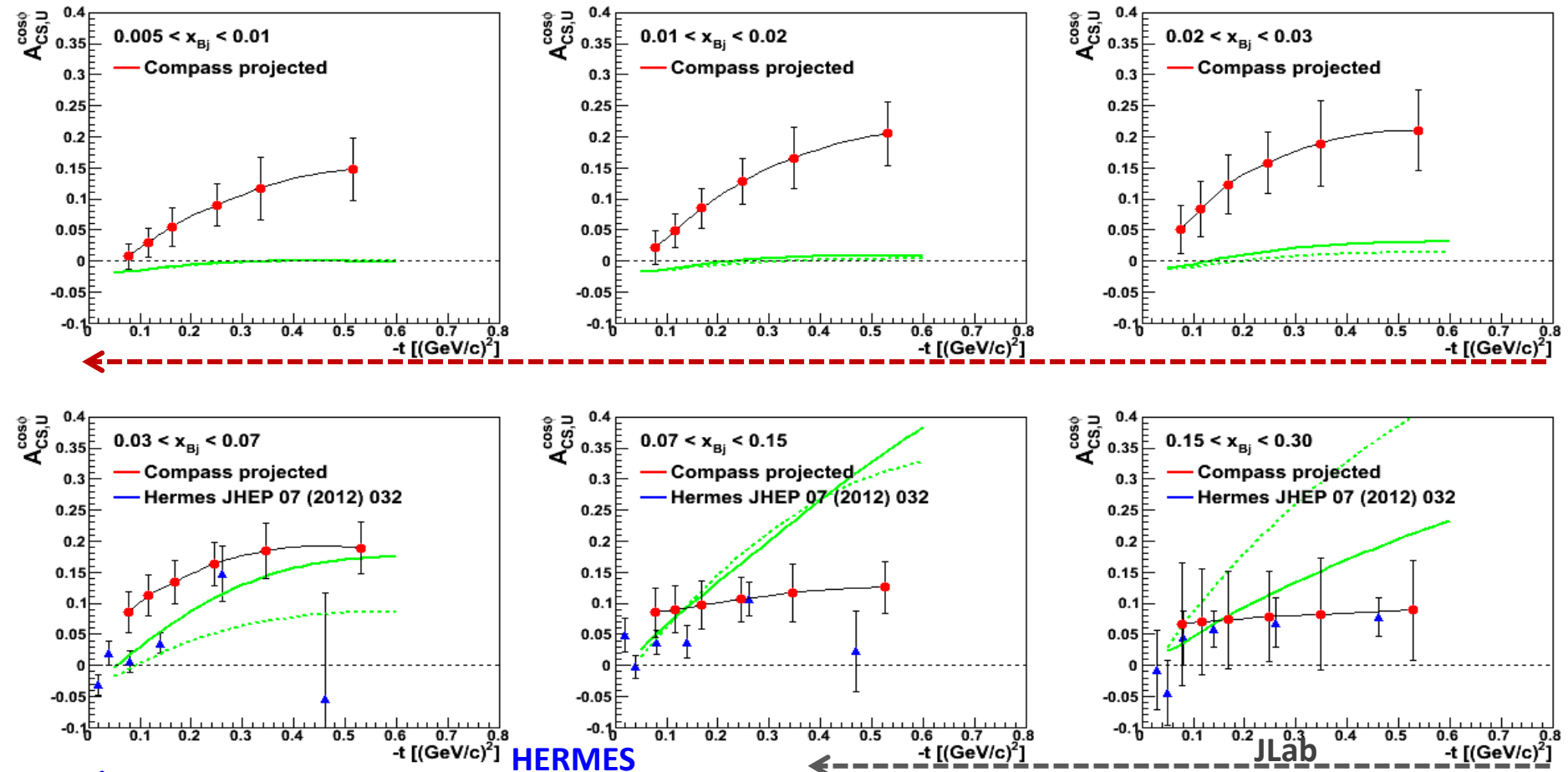
$$c_1^I = \text{Re } F_1 \mathcal{H}$$

Predictions with  
**VGG** and **D.Mueller KM10**

$\text{Re } \mathcal{H} > 0$  at H1

$< 0$  at HERMES

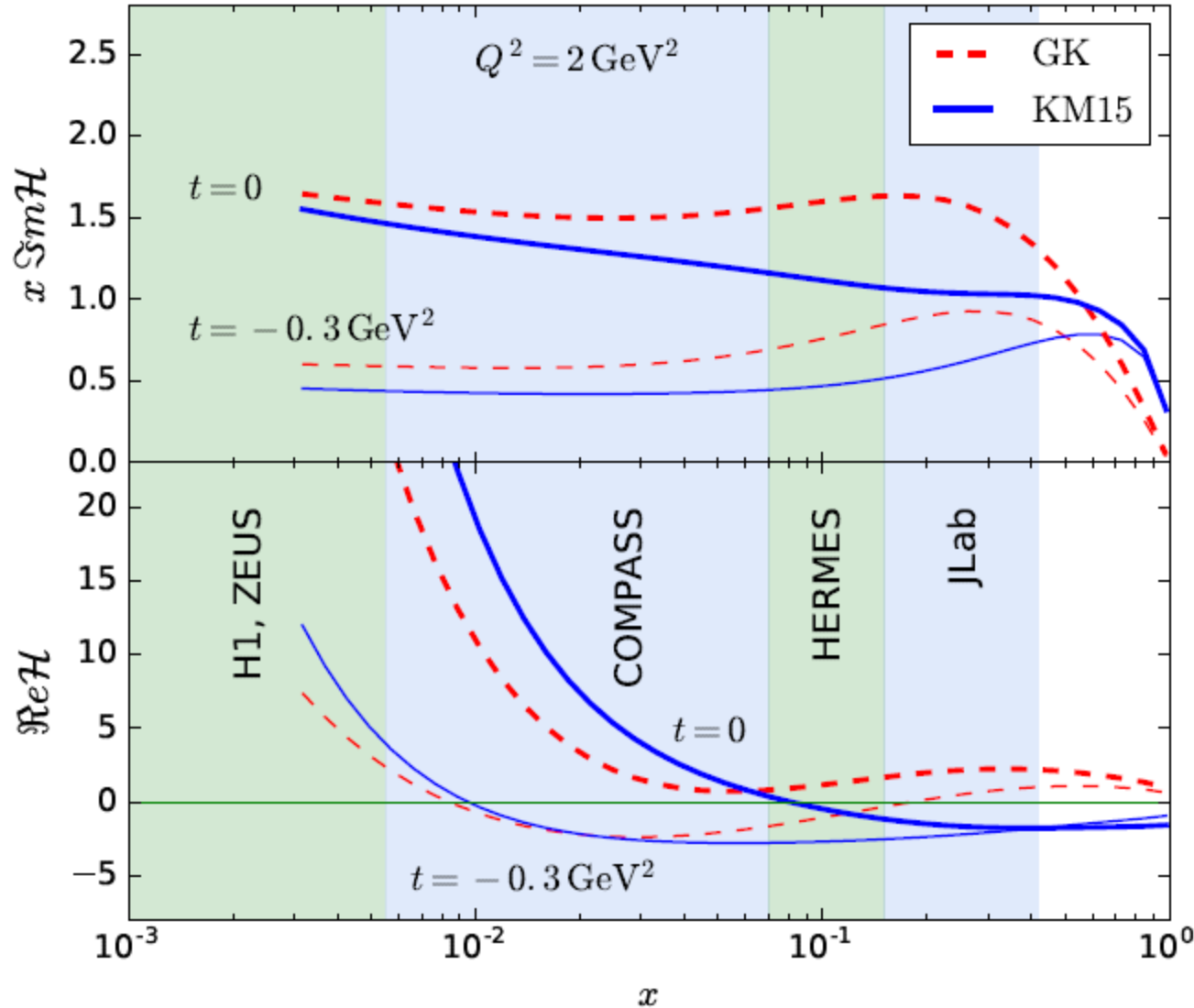
Value of  $x_B$  for the node?



**COMPASS** 2 years of data  $E_\mu = 160$  GeV  $1 < Q^2 < 8$  GeV<sup>2</sup> with ECAL2 + ECAL1 + ECAL0



# Impact of DVCS @ COMPASS in global analysis ?



*Im  $\mathcal{H}$*

Is it rather  
well known ?

*Re  $\mathcal{H}$*  linked  
to the  *$\mathcal{D}$  term*  
is still poorly  
constrained

**KM15** K Kumericki and D Mueller [arXiv:1512.09014v1](https://arxiv.org/abs/1512.09014v1)

**GK** S.V. Goloskokov, P. Kroll, EPJC53 (2008), EPJA47 (2011)

# Hunting the GPD E, holy grail for OAM

$$\vec{\ell} d \rightarrow \ell n \gamma (p)$$

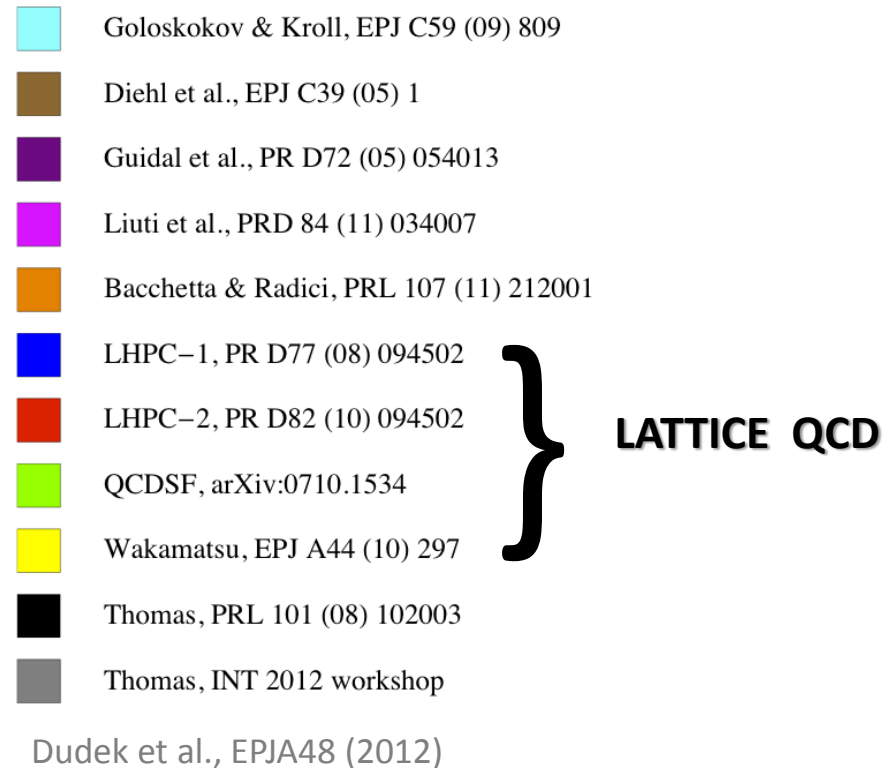
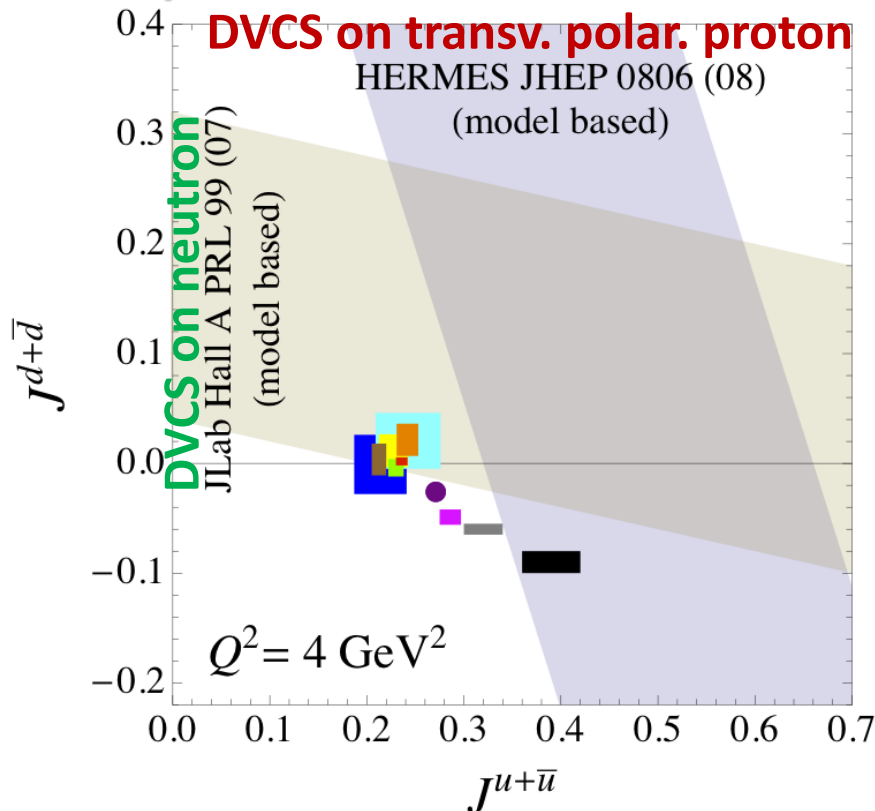
$$\Delta\sigma_{LU} \sim \text{Im} (F_{1n} \mathcal{H} - F_{2n} \mathcal{E})$$

$$\vec{\ell} p \rightarrow \ell p \gamma$$

$$\Delta\sigma_{UT} \sin(\phi - \phi_S) \cos \phi = \text{Im} (F_2 \mathcal{H} - F_1 \mathcal{E})$$

$$\Delta\sigma_{LT} \sin(\phi - \phi_S) \cos \phi = \text{Re} (F_2 \mathcal{H} - F_1 \mathcal{E})$$

Model dependent extraction of  $J^u$  and  $J^d$



Future program - under discussion at COMPASS - selected at JLab12 as  
 "High impact" experiments (CLAS 12 + neutron detector + HDice or ND<sub>3</sub> target)

Only selected results.

Prospects for Time-like Compton Scattering and Double DVCS.

Precise Data in a large kinematic domain are necessary.

A large theoretical effort:

- to extract the GPD information from the experiments
- to still improve the GPD models

**GPD programs with DVCS, HEMP (from light mesons to  $J/\Psi$ ) are a priority for COMPASS @ CERN, JLab 12 GeV, and for a future electron-proton collider**

**Understanding the structure of the nucleon is still an exciting and vibrant area of research**



# Proton picture: 1D $\rightarrow$ 1+2D

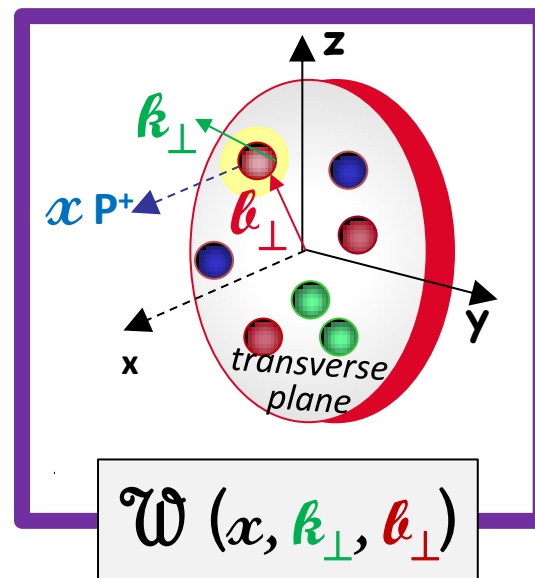
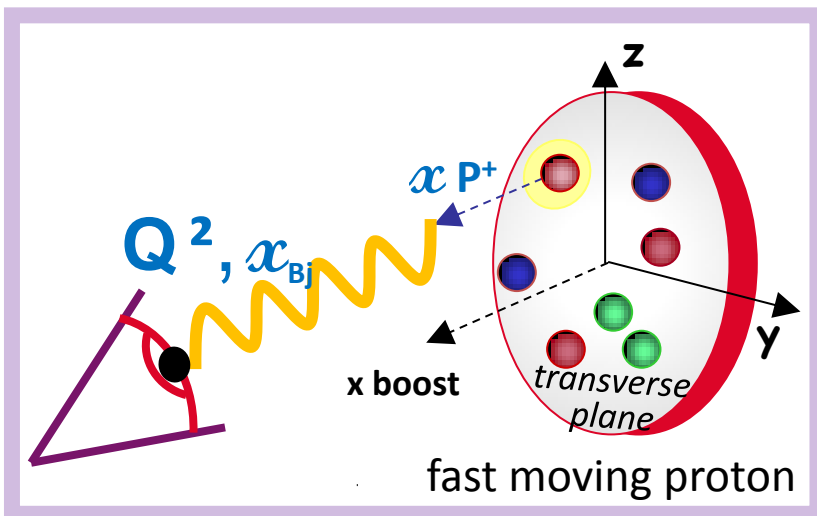


## Quantum tomography of the nucleon

Ji, PRL91 (2003)

Belitsky, Ji, Yuan, PRD69 (2004)

Lorcé et al, JHEP1105 (2011)



$$\mathcal{W}(x, \mathbf{k}_\perp, \mathbf{l}_\perp)$$

### Parton Distribution Functions PDFs ( $x$ )

#### Longitudinal momentum

$$q(x) \text{ or } f_1^q(x)$$

#### Longitudinal spin

$$\Delta q(x) = \vec{q}(x) - \bar{q}(x)$$

#### Transverse spin

$$\Delta_T q \text{ or } h_1(x)$$

#### Transverse momentum

$$\int d\mathbf{k}_\perp$$

$$8 \text{ TMDs } (x, \mathbf{k}_\perp)$$

Sivers,  
the most famous TMD

#### Transverse position

$$\int d\mathbf{k}_\perp$$

$$8 \text{ GPDs } (x, \mathbf{l}_\perp)$$

$$\int dx$$

Form  
Factors

$$H(x, x', \mathbf{t})$$

$$E(x, x', \mathbf{t})$$

**holy grail for OAM**