

Flavor Physics

Part 2

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Abtei Frauenwörth, September 20, 2016

Summary of the First Lecture

- ▶ In the SM, all flavor violation is due to the Higgs
- ▶ At tree level there are no FCNCs; flavor violation occurs only in charged currents, parametrized by the CKM matrix
- ▶ FCNCs arise at the 1-loop level. Example: meson mixing; gives access to CKM elements V_{td} and V_{ts} and their phases
- ▶ Where do the hierarchies in the CKM elements and the fermion masses come from?

Outline of the Lectures

① Flavor Physics in the Standard Model

- Flavor Symmetry and Flavor Symmetry Breaking
- The CKM Matrix
- Meson Mixing and CP Asymmetries
- The Standard Model Flavor Puzzle

② Flavor Physics Beyond the Standard Model

- The New Physics Flavor Puzzle
- Flavor in BSM Models
- Flavor Anomalies

Part 2

Flavor Physics Beyond the Standard Model

The Standard Model as Effective Theory

$$\begin{aligned}\mathcal{L}_{\text{SM}} \sim & \Lambda^4 + \Lambda^2 H^2 + \lambda H^4 \\ & + \bar{\Psi} D\Psi + (D_\mu H)^2 + (F_{\mu\nu})^2 + F_{\mu\nu} \tilde{F}^{\mu\nu} \\ & + Y H \bar{\Psi} \Psi + \frac{1}{\Lambda} (LH)^2 + \frac{1}{\Lambda^2} \sum_i \mathcal{O}_i^{\text{dim6}}\end{aligned}$$

The Standard Model as Effective Theory

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CC problem Hierarchy problem Vacuum stability?
Strong CP problem
SM flavor puzzle Neutrino masses NP flavor puzzle ...

The Hierarchy Problem

What gives mass to the Higgs itself?

The Higgs mass parameter
is not forbidden by any
symmetry of the Standard Model

$$m^2 = m_{(0)}^2 + \Delta m^2 \sim (125\text{GeV})^2$$

- 1) can be added by hand
- 2) not protected from
quantum corrections

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quantum corrections to
the Higgs mass are
sensitive to the largest scales

$$\Delta m^2 \sim \frac{1}{16\pi^2} M_{\text{Planck}}^2 \simeq 10^{36}\text{GeV}^2$$

fine tuned cancellation between the
quantum corrections and the “bare mass” is required

The Hierarchy Problem



Canada
 $9,984,670 \text{ km}^2$



United States
 $9,826,675 \text{ km}^2$ = $157,995 \text{ km}^2$

The Hierarchy Problem



—



$$= 1 \text{ \AA}^2$$

Canada
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—

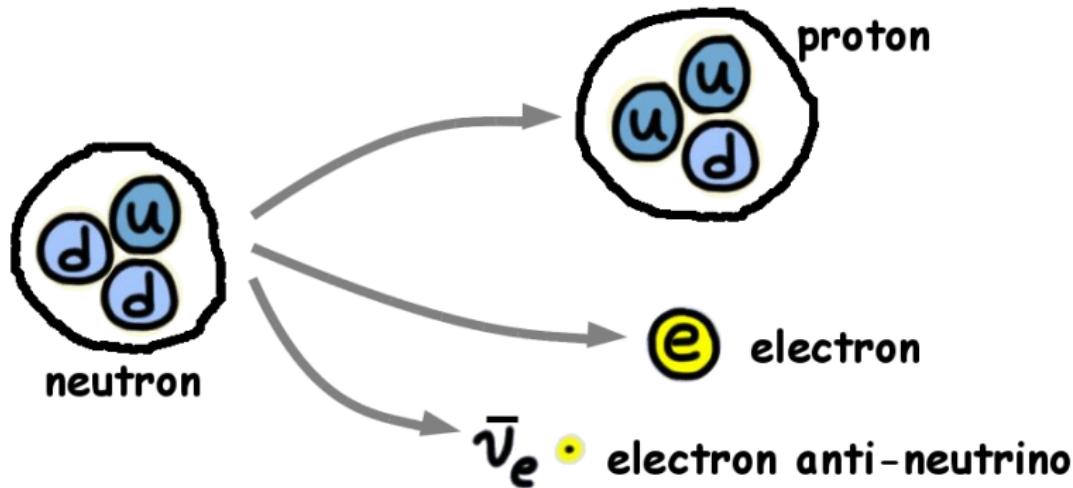
United States
 $9,826,675 \text{ km}^2$ $= 157,995 \text{ km}^2$

tuning of the Higgs mass would correspond to
the surface area of Canada and the United States
differing by approximately the size of an atom!

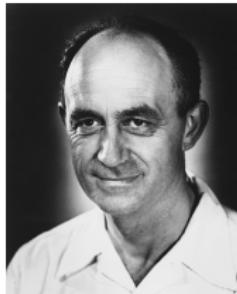
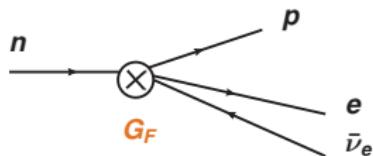
In order to **protect the Higgs mass**
from huge quantum corrections and to avoid finetuning,
we expect **New Physics at the TeV scale**

How can we get information
on New Physics at high scales
from low energy experiments?

Beta Decay



Beta Decay



effective low energy description
of nuclear beta decay by a
4 fermion contact interaction

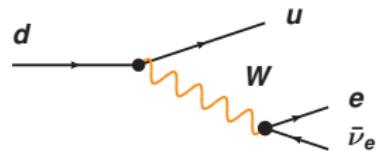
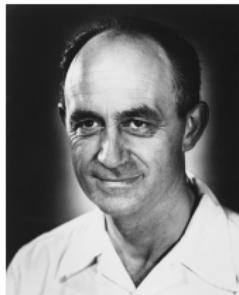
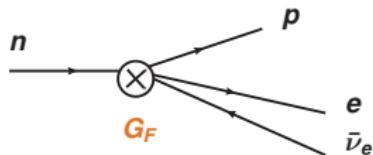
the interaction strength is given by
the Fermi constant

$$G_F \simeq 1.17 \times 10^{-5} \text{ GeV}^{-2}$$

this defines an energy scale

$$\Lambda = (G_F \sqrt{2})^{-1/2} \simeq 246 \text{ GeV}$$

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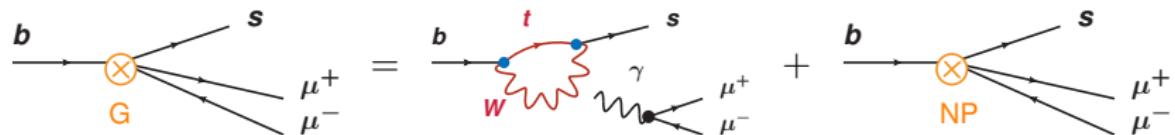
$$\Lambda = (G_F \sqrt{2})^{-1/2} \simeq 246 \text{ GeV}$$

in the Standard Model
we understand beta decay
as consequence of
the exchange of virtual
weak gauge bosons

$$\frac{G_F}{\sqrt{2}} = \frac{g_2^2}{8m_W^2}$$

$$m_W \simeq 80 \text{ GeV}$$

New Physics in Flavor Changing Neutral Currents



$$G \sim \frac{1}{16\pi^2} \frac{g^4}{m_W^2} \frac{m_t^2}{m_W^2} V_{tb} V_{ts}^* + \frac{C_{NP}}{\Lambda_{NP}^2}$$

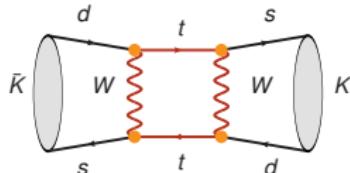
measure
precisely

calculate precisely
the SM contribution

get information on
NP coupling and scale

Example: CP Violation in Kaon mixing

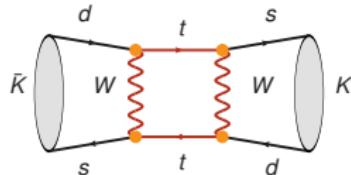
- Standard Model amplitude is **loop suppressed** and **CKM suppressed**



$$\propto \frac{g^4}{16\pi^2} \frac{m_t^2}{M_W^4} (V_{td} V_{ts}^*)^2$$

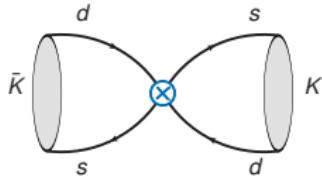
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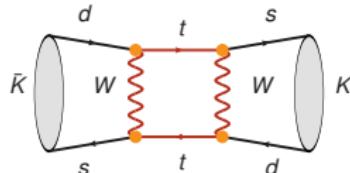
- Generic New Physics amplitude only suppressed by **New Physics scale**



$$\propto \frac{1}{\Lambda_{NP}^2}$$

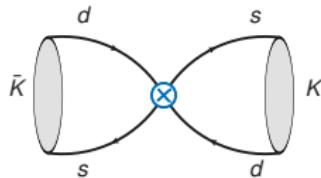
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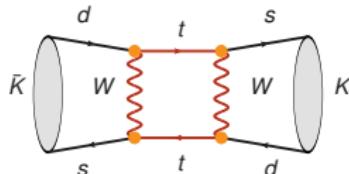
$$\propto \frac{1}{\Lambda_{NP}^2}$$

- CP Violation in Kaon Mixing can probe **extremely high scales**

$$\Lambda_{NP} \sim \frac{M_W^2}{m_t} \frac{4\pi}{g^2} \frac{1}{|V_{td} V_{ts}^*|} \sim 10^4 \text{ TeV}$$

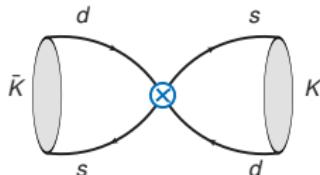
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[Exercise: estimate the scale that can be probed with rare B decays]

Many Flavor Violating Dimension Six Operators

	$1 : X^3$	$2 : H^6$	$3 : H^4 D^2$	$5 : \psi^2 H^3 + \text{h.c.}$
Q_G	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_H (H^\dagger H)^3$	$Q_{H\square} (H^\dagger H) \square (H^\dagger H)$	$Q_{eH} (H^\dagger H) (\bar{l}_p e_r, H)$
$Q_{\bar{G}}$	$f^{ABC} \bar{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$		$Q_{HD} (H^\dagger D_\mu H)^* (H^\dagger D_\mu H)$	$Q_{uH} (H^\dagger H) (\bar{q}_p u_r, \tilde{H})$
Q_W	$e^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$			$Q_{dH} (H^\dagger H) (\bar{q}_p d_r, H)$
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	$4 : X^2 H^2$	$6 : \psi^2 X H + \text{h.c.}$	$7 : \psi^2 H^2 D$
Q_{HG}	$H^\dagger H G_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eW} (\bar{l}_p \gamma^{\mu\nu} e_r) \tau^I H W_{\mu\nu}^I$	$Q_{Hl}^{(1)} (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{l}_p \gamma^\mu l_r)$
$Q_{H\bar{G}}$	$H^\dagger H \bar{G}_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eB} (\bar{l}_p \sigma^{\mu\nu} e_r) H B_{\mu\nu}$	$Q_{Hl}^{(3)} (H^\dagger i \overleftrightarrow{D}_\mu^T H) (\bar{l}_p \tau^I \gamma^\mu l_r)$
Q_{HW}	$H^\dagger H W_\mu^I W_\nu^I \mu\nu$	$Q_{uG} (\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{H} G_\mu^A$	$Q_{He} (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{e}_p \gamma^\mu e_r)$
$Q_{H\bar{W}}$	$H^\dagger H \bar{W}_\mu^I W_\nu^I \mu\nu$	$Q_{uW} (\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{H} W_\mu^I$	$Q_{Hq}^{(1)} (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{q}_p \gamma^\mu q_r)$
Q_{HB}	$H^\dagger H B_{\mu\nu} B^{\mu\nu}$	$Q_{uB} (\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{H} B_{\mu\nu}$	$Q_{Hq}^{(3)} (H^\dagger i \overleftrightarrow{D}_\mu^T H) (\bar{q}_p \tau^I \gamma^\mu q_r)$
$Q_{H\bar{B}}$	$H^\dagger H \bar{B}_{\mu\nu} B^{\mu\nu}$	$Q_{dG} (\bar{q}_p \sigma^{\mu\nu} T^A d_r) H G_\mu^A$	$Q_{Hu} (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{u}_p \gamma^\mu u_r)$
Q_{HWB}	$H^\dagger \tau^I H W_\mu^I B^{\mu\nu}$	$Q_{dW} (\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I H W_\mu^I$	$Q_{Hd} (H^\dagger i \overleftrightarrow{D}_\mu H) (\bar{d}_p \gamma^\mu d_r)$
$Q_{H\bar{W}B}$	$H^\dagger \tau^I H \bar{W}_\mu^I B^{\mu\nu}$	$Q_{dB} (\bar{q}_p \sigma^{\mu\nu} d_r) H B_{\mu\nu}$	$Q_{Hud} + \text{h.c.} i(\bar{H}^\dagger D_\mu H) (\bar{u}_p \gamma^\mu d_r)$

	$8 : (\bar{L}L)(\bar{L}L)$	$8 : (\bar{R}R)(\bar{R}R)$	$8 : (\bar{L}L)(\bar{R}R)$
Q_{ll}	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	$Q_{ee} (\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$	$Q_{le} (\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{uu} (\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{lu} (\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{dd} (\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{ld} (\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{eu} (\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{qe} (\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{ed} (\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)} (\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
		$Q_{ud}^{(1)} (\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)} (\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$
		$Q_{ud}^{(8)} (\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)} (\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$
			$Q_{qd}^{(8)} (\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$

	$8 : (\bar{L}R)(\bar{R}L) + \text{h.c.}$	$8 : (\bar{L}R)(\bar{L}R) + \text{h.c.}$
Q_{ledq}	$(\bar{l}_p^I e_r)(\bar{d}_s q_t)$	$Q_{quqd}^{(1)} (\bar{q}_p^I u_r) \epsilon_{jk} (q_s^k d_t)$
		$Q_{quqd}^{(8)} (\bar{q}_p^I T^A u_r) \epsilon_{jk} (q_s^k T^A d_t)$
Q_{lequ}		$Q_{lequ}^{(1)} (\bar{l}_p^I e_r) \epsilon_{jk} (q_s^k u_t)$
$Q_{lequ}^{(3)}$		$Q_{lequ}^{(3)} (\bar{l}_p^I \sigma_{\mu\nu} e_r) \epsilon_{jk} (q_s^k \sigma^{\mu\nu} u_t)$

2499 baryon number conserving
dim. 6 operators in total

Grzadkowski et al. 1008.4884,

Alonso et al 1312.2014

Many Flavor Violating Dimension Six Operators

$1 : X^3$	$2 : H^6$	$3 : H^4 D^2$	$5 : \psi^2 H^3 + \text{h.c.}$
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$Q_{\tilde{G}} F^{ABC} \tilde{G}_\mu^{Ab} G_\nu^{Bc} G_\rho^{C\mu}$		$Q_{HD} (H^\dagger D_\mu H)^* (H^\dagger D_\mu H)$	$Q_{uH} (H^\dagger H) (\bar{q}_p u, \tilde{H})$
$Q_W e^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$			$Q_{dH} (H^\dagger H) (\bar{q}_p d, H)$
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$Q_{HG} H^\dagger H G_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eW} (\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I H W_{\mu\nu}^I$	$Q_{Hl}^{(1)} (H^\dagger i \overleftrightarrow{D}_{\mu} l) (\bar{l}_p \gamma^\mu l_r)$
$Q_{HG} H^\dagger H \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eB} (\bar{l}_p \sigma^{\mu\nu} e_r) H B_{\mu\nu}$	$Q_{Hl}^{(3)} (H^\dagger i \overleftrightarrow{D}_{\mu}^T H) (\bar{l}_p \tau^I \gamma^\mu l_r)$
$Q_{HW} H^\dagger H W_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uG} (\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{H} G_{\mu\nu}^A$	$Q_{Hs} (H^\dagger i \overleftrightarrow{D}_{\mu} H) (\bar{e}_p \gamma^\mu e_r)$
$Q_{H\tilde{W}} H^\dagger H \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uW} (\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{H} W_{\mu\nu}^I$	$Q_{Hq}^{(1)} (H^\dagger i \overleftrightarrow{D}_{\mu} H) (\bar{q}_p \gamma^\mu q_r)$
$Q_{HR} H^\dagger H B_{\mu\nu} B^{\mu\nu}$	$Q_{uR} (\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{H} B_{\mu\nu}$	$Q_{Hq}^{(3)} (H^\dagger i \overleftrightarrow{D}_{\mu}^T H) (\bar{q}_p \tau^I \gamma^\mu q_r)$
$Q_{H\tilde{B}} H^\dagger H \tilde{B}_{\mu\nu} B^{\mu\nu}$	$Q_{gG} (\bar{q}_p \sigma^{\mu\nu} T^A d_r) H G_{\mu\nu}^A$	$Q_{Hu} (H^\dagger i \overleftrightarrow{D}_{\mu} H) (\bar{u}_p \gamma^\mu u_r)$
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$Q_{H\tilde{W}B} H^\dagger \tau^I H \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	$Q_{IB} (\bar{q}_p \sigma^{\mu\nu} d_r) H B_{\mu\nu}$	$Q_{Hud} + \text{h.c.} i(\tilde{H}^* D_\mu H)(\bar{u}_p \gamma^\mu d_r)$

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	$Q_{nd}^{(1)} (\bar{u}_p \gamma_\mu u_r) (\bar{d}_s \gamma^\mu d_t)$	$Q_{qg}^{(8)} (\bar{q}_p \gamma_\mu T^A q_r) (\bar{u}_s \gamma^\mu T^A u_t)$
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	$Q_{qapd}^{(8)} (\bar{q}_p^2 T^A e_r) \epsilon_{ijk} (\bar{q}_s^k T^A d_t)$
	$Q_{lcpa}^{(1)} (\bar{l}_p^2 e_r) \epsilon_{jik} (\bar{q}_s^k u_t)$
	$Q_{lcpa}^{(3)} (\bar{l}_p^2 \sigma_{ij} e_r) \epsilon_{jik} (\bar{q}_s^k \gamma^\mu \nu_t)$

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4 fermion interactions

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$Q_W e^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$			$Q_{dH} (H^\dagger H) (\bar{q}_p d, H)$
$Q_{\tilde{W}} e^{IJK} \tilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$			

$4 : X^2 H^2$	$6 : \psi^2 X H + \text{h.c.}$	$7 : \psi^2 H^2 D$
$Q_{HG} H^\dagger H G_{\mu\nu}^A G^{A\mu\nu}$	$Q_{cW} (\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I H W_{\mu\nu}^I$	$Q_{Hl}^{(1)} (H^\dagger i \overleftrightarrow{D}_{\mu} l) (\bar{l}_p \gamma^\mu l_r)$
$Q_{HG} H^\dagger H \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	$Q_{sB} (\bar{l}_p \sigma^{\mu\nu} e_r) H B_{\mu\nu}$	$Q_{Hl}^{(3)} (H^\dagger i \overleftrightarrow{D}_{\mu}^T H) (\bar{l}_p \tau^I \gamma^\mu l_r)$
$Q_{HW} H^\dagger H W_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uG} (\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{H} G_{\mu\nu}^A$	$Q_{Hs} (H^\dagger i \overleftrightarrow{D}_{\mu} H) (\bar{e}_p \gamma^\mu e_r)$
$Q_{H\tilde{W}} H^\dagger H \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uW} (\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{H} W_{\mu\nu}^I$	$Q_{Hq}^{(1)} (H^\dagger i \overleftrightarrow{D}_{\mu} H) (\bar{q}_p \gamma^\mu q_r)$
$Q_{HR} H^\dagger H B_{\mu\nu} B^{\mu\nu}$	$Q_{uR} (\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{H} B_{\mu\nu}$	$Q_{Hq}^{(3)} (H^\dagger i \overleftrightarrow{D}_{\mu}^T H) (\bar{q}_p \tau^I \gamma^\mu q_r)$
$Q_{H\tilde{B}} H^\dagger H \tilde{B}_{\mu\nu} B^{\mu\nu}$	$Q_{gG} (\bar{q}_p \sigma^{\mu\nu} T^A d_r) H G_{\mu\nu}^A$	$Q_{Hu} (H^\dagger i \overleftrightarrow{D}_{\mu} H) (\bar{u}_p \gamma^\mu u_r)$
$Q_{HWB} H^\dagger \tau^I H W_{\mu\nu}^I B^{\mu\nu}$	$Q_{dW} (\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I H W_{\mu\nu}^I$	$Q_{Hd} (H^\dagger i \overleftrightarrow{D}_{\mu} H) (\bar{d}_p \gamma^\mu d_r)$
$Q_{H\tilde{W}B} H^\dagger \tau^I H \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	$Q_{IB} (\bar{q}_p \sigma^{\mu\nu} d_r) H B_{\mu\nu}$	$Q_{Hud} + \text{h.c.} i(\bar{l}_p \gamma^\mu H) (\bar{u}_p \gamma^\mu d_r)$

$8 : (\bar{L}L)(\bar{L}L)$	$8 : (\bar{R}R)(\bar{R}R)$	$8 : (\bar{L}L)(\bar{R}R)$
$Q_{ll} (\bar{l}_p \gamma_\mu l_r) (\bar{l}_s \gamma^\mu l_t)$	$Q_{ee} (\bar{e}_p \gamma_\mu e_r) (\bar{e}_s \gamma^\mu e_t)$	$Q_{le} (\bar{l}_p \gamma_\mu l_r) (\bar{e}_s \gamma^\mu e_t)$
$Q_{qq}^{(1)} (\bar{q}_p \gamma_\mu q_r) (\bar{q}_s \gamma^\mu q_t)$	$Q_{uu} (\bar{u}_p \gamma_\mu u_r) (\bar{u}_s \gamma^\mu u_t)$	$Q_{lu} (\bar{l}_p \gamma_\mu l_r) (\bar{u}_s \gamma^\mu u_t)$
$Q_{qq}^{(3)} (\bar{q}_p \gamma_\mu \tau^I q_r) (\bar{q}_s \gamma^{\mu\tau^I} q_t)$	$Q_{dd} (\bar{d}_p \gamma_\mu d_r) (\bar{d}_s \gamma^\mu d_t)$	$Q_{ld} (\bar{l}_p \gamma_\mu l_r) (\bar{d}_s \gamma^\mu d_t)$
$Q_{lq}^{(1)} (\bar{l}_p \gamma_\mu l_r) (\bar{q}_s \gamma^\mu q_t)$	$Q_{eu} (\bar{e}_p \gamma_\mu e_r) (\bar{u}_s \gamma^\mu u_t)$	$Q_{qe} (\bar{q}_p \gamma_\mu q_r) (\bar{e}_s \gamma^\mu e_t)$
$Q_{lq}^{(3)} (\bar{l}_p \gamma_\mu \tau^I l_r) (\bar{q}_s \gamma^{\mu\tau^I} q_t)$	$Q_{ed} (\bar{e}_p \gamma_\mu e_r) (\bar{d}_s \gamma^\mu d_t)$	$Q_{qd}^{(1)} (\bar{q}_p \gamma_\mu q_r) (\bar{u}_s \gamma^\mu u_t)$
	$Q_{nd}^{(1)} (\bar{u}_p \gamma_\mu u_r) (\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)} (\bar{q}_p \gamma_\mu T^A q_r) (\bar{u}_s \gamma^\mu T^A u_t)$
	$Q_{nd}^{(8)} (\bar{u}_p \gamma_\mu T^A u_r) (\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)} (\bar{q}_p \gamma_\mu q_r) (\bar{d}_s \gamma^\mu d_t)$
		$Q_{qd}^{(8)} (\bar{q}_p \gamma_\mu T^A q_r) (\bar{d}_s \gamma^\mu T^A d_t)$

$8 : (\bar{L}R)(\bar{R}L) + \text{h.c.}$	$8 : (\bar{L}R)(\bar{L}R) + \text{h.c.}$
$Q_{led} (\bar{l}_p e_r) (\bar{d}_s q_t)$	$Q_{qapd}^{(1)} (\bar{q}_p^T u_r) \epsilon_{ijk} (\bar{q}_s^k d_t)$
	$Q_{qapd}^{(8)} (\bar{q}_p^T T^A u_r) \epsilon_{ijk} (\bar{q}_s^k T^A d_t)$
	$Q_{lceq}^{(1)} (\bar{l}_p^T e_r) \epsilon_{jik} (\bar{q}_s^k u_t)$
	$Q_{lceq}^{(3)} (\bar{l}_p^T \sigma_{\mu\nu} e_r) \epsilon_{jik} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$

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$1 : X^3$	$2 : H^6$	$3 : H^4 D^2$	$5 : \psi^2 H^3 + \text{h.c.}$
$Q_G F^{ABC} G_\mu^{Ab} G_\nu^{Bc} G_\rho^{C\mu}$	$Q_H (H^\dagger H)^5$	$Q_{H\square} (H^\dagger H) \square (H^\dagger H)$	$Q_{eH} (H^\dagger H) (\bar{l}_p e, H)$
$Q_{\tilde{G}} F^{ABC} \tilde{G}_\mu^{Ab} G_\nu^{Bc} G_\rho^{C\mu}$		$Q_{HD} (H^\dagger D_u H)^* (H^\dagger D_\mu H)$	$Q_{uH} (H^\dagger H) (\bar{q}_p u, \tilde{H})$
$Q_W e^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$			$Q_{dH} (H^\dagger H) (\bar{q}_p d, H)$
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$Q_{HG} H^\dagger H \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	$Q_{sB} (\bar{l}_p \sigma^{\mu\nu} e_r) H B_{\mu\nu}$	$Q_{Hl}^{(3)} (H^\dagger i \overleftrightarrow{D}_{\mu}^T H) (\bar{l}_p \tau^I \gamma^\mu l_r)$
$Q_{HW} H^\dagger H W_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uG} (\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{H} G_{\mu\nu}^A$	$Q_{H\bar{s}} (H^\dagger i \overleftrightarrow{D}_{\mu} H) (\bar{c}_p \gamma^\mu c_r)$
$Q_{H\bar{W}} H^\dagger H \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uW} (\bar{q}_p \sigma^{\mu\nu} e_r) \tau^I \tilde{H} W_{\mu\nu}^I$	$Q_{Hq}^{(1)} (H^\dagger i \overleftrightarrow{D}_{\mu} H) (\bar{q}_p \gamma^\mu q_r)$
$Q_{HR} H^\dagger H B_{\mu\nu} B^{\mu\nu}$	$Q_{uR} (\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{H} B_{\mu\nu}$	$Q_{Hq}^{(3)} (H^\dagger i \overleftrightarrow{D}_{\mu}^T H) (\bar{q}_p \tau^I \gamma^\mu q_r)$
$Q_{H\bar{B}} H^\dagger H \tilde{B}_{\mu\nu} B^{\mu\nu}$	$Q_{gG} (\bar{q}_p \sigma^{\mu\nu} T^A d_r) \tilde{H} G_{\mu\nu}^A$	$Q_{H\bar{u}} (H^\dagger i \overleftrightarrow{D}_{\mu} H) (\bar{u}_p \gamma^\mu u_r)$
$Q_{HWB} H^\dagger \tau^I H W_{\mu\nu}^I B^{\mu\nu}$	$Q_{dW} (\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I H W_{\mu\nu}^I$	$Q_{H\bar{d}} (H^\dagger i \overleftrightarrow{D}_{\mu} H) (\bar{d}_p \gamma^\mu d_r)$
$Q_{H\bar{W}B} H^\dagger \tau^I H \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	$Q_{IB} (\bar{q}_p \sigma^{\mu\nu} d_r) H B_{\mu\nu}$	$Q_{H\bar{u}d} + \text{h.c.} i(\tilde{H} D_{\mu} H) (\bar{u}_p \gamma^\mu d_r)$

$8 : (\bar{L}L)(\bar{L}L)$	$8 : (\bar{R}R)(\bar{R}R)$	$8 : (\bar{L}L)(\bar{R}R)$
$Q_{ll} (\bar{l}_p \gamma_\mu l_r) (\bar{l}_s \gamma^\mu l_t)$	$Q_{ee} (\bar{e}_p \gamma_\mu e_r) (\bar{e}_s \gamma^\mu e_t)$	$Q_{le} (\bar{l}_p \gamma_\mu l_r) (\bar{e}_s \gamma^\mu e_t)$
$Q_{qq}^{(1)} (\bar{q}_p \gamma_\mu q_r) (\bar{q}_s \gamma^\mu q_t)$	$Q_{uu} (\bar{u}_p \gamma_\mu u_r) (\bar{u}_s \gamma^\mu u_t)$	$Q_{lu} (\bar{l}_p \gamma_\mu l_r) (\bar{u}_s \gamma^\mu u_t)$
$Q_{qq}^{(3)} (\bar{q}_p \gamma_\mu \tau^I q_r) (\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{dd} (\bar{d}_p \gamma_\mu d_r) (\bar{d}_s \gamma^\mu d_t)$	$Q_{ld} (\bar{l}_p \gamma_\mu l_r) (\bar{d}_s \gamma^\mu d_t)$
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$Q_{nd}^{(1)} (\bar{u}_p \gamma_\mu u_r) (\bar{d}_s \gamma^\mu d_t)$		$Q_{qg}^{(8)} (\bar{q}_p \gamma_\mu T^A q_r) (\bar{u}_s \gamma^\mu T^A u_t)$
$Q_{nd}^{(8)} (\bar{u}_p \gamma_\mu T^A u_r) (\bar{d}_s \gamma^\mu d_t)$		$Q_{qd}^{(1)} (\bar{q}_p \gamma_\mu q_r) (\bar{d}_s \gamma^\mu d_t)$
		$Q_{qd}^{(8)} (\bar{q}_p \gamma_\mu T^A q_r) (\bar{d}_s \gamma^\mu T^A d_t)$

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$Q_{led} (\bar{l}_p e_r) (\bar{d}_s q_t)$	$Q_{qapd}^{(1)} (\bar{q}_p^a u_r) \epsilon_{ijk} (\bar{q}_s^k d_t)$
	$Q_{qapd}^{(8)} (\bar{q}_p^a T^A u_r) \epsilon_{ijk} (\bar{q}_s^k T^A d_t)$
	$Q_{lcpa}^{(1)} (\bar{l}_p^i e_r) \epsilon_{jkl} (\bar{q}_s^k u_t)$
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$1 : X^3$	$2 : H^6$	$3 : H^4 D^2$	$5 : \psi^2 H^3 + \text{h.c.}$
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$Q_{\tilde{G}} F^{ABC} \tilde{G}_\mu^{Ab} G_\nu^{Bc} G_\rho^{C\mu}$		$Q_{HD} (H^\dagger D_u H)^* (H^\dagger D_\mu H)$	$Q_{uH} (H^\dagger H) (\bar{q}_p u, \tilde{H})$
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$Q_{HG} H^\dagger H \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eB} (\bar{l}_p \sigma^{\mu\nu} e_r) H B_{\mu\nu}$	$Q_{Hl}^{(3)} (H^\dagger i \overleftrightarrow{D}_{\mu}^I H) (\bar{l}_p \tau^I \gamma^\mu l_r)$
$Q_{HW} H^\dagger H W_{\mu\nu}^T W^{T\mu\nu}$	$Q_{uG} (\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{H} G_{\mu\nu}^A$	$Q_{Hs} (H^\dagger i \overleftrightarrow{D}_{\mu} H) (\bar{e}_p \gamma^\mu e_r)$
$Q_{H\tilde{W}} H^\dagger H \tilde{W}_{\mu\nu}^T W^{T\mu\nu}$	$Q_{uW} (\bar{q}_p \sigma^{\mu\nu} e_r) \tau^I \tilde{H} W_{\mu\nu}^I$	$Q_{Hq}^{(1)} (H^\dagger i \overleftrightarrow{D}_{\mu} H) (\bar{q}_p \tau^I \gamma^\mu q_r)$
$Q_{HR} H^\dagger H B_{\mu\nu} B^{\mu\nu}$	$Q_{uR} (\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{H} B_{\mu\nu}$	$Q_{Hq}^{(3)} (H^\dagger i \overleftrightarrow{D}_{\mu} H) (\bar{q}_p \tau^I \gamma^\mu q_r)$
$Q_{H\tilde{B}} H^\dagger H \tilde{B}_{\mu\nu} B^{\mu\nu}$	$Q_{gG} (\bar{q}_p \sigma^{\mu\nu} T^A d_r) H G_{\mu\nu}^A$	$Q_{Hu} (H^\dagger i \overleftrightarrow{D}_{\mu} H) (\bar{u}_p \gamma^\mu u_r)$
$Q_{HWB} H^\dagger \tau^I H W_{\mu\nu}^I B^{\mu\nu}$	$Q_{dW} (\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I H W_{\mu\nu}^I$	$Q_{Hd} (H^\dagger i \overleftrightarrow{D}_{\mu} H) (\bar{d}_p \gamma^\mu d_r)$
$Q_{H\tilde{W}B} H^\dagger \tau^I H \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	$Q_{IB} (\bar{q}_p \sigma^{\mu\nu} d_r) H B_{\mu\nu}$	$Q_{Hud} + \text{h.c.} i(\tilde{H}^* D_\mu H) (\bar{u}_p \gamma^\mu d_r)$

$8 : (\bar{L}L)(\bar{L}L)$	$8 : (\bar{R}R)(\bar{R}R)$	$8 : (\bar{L}L)(\bar{R}R)$
$Q_{ll} (\bar{l}_p \gamma_\mu l_r) (\bar{l}_s \gamma^\mu l_t)$	$Q_{ee} (\bar{e}_p \gamma_\mu e_r) (\bar{e}_s \gamma^\mu e_t)$	$Q_{le} (\bar{l}_p \gamma_\mu l_r) (\bar{e}_s \gamma^\mu e_t)$
$Q_{qq}^{(1)} (\bar{q}_p \gamma_\mu q_r) (\bar{q}_s \gamma^\mu q_t)$	$Q_{uu} (\bar{u}_p \gamma_\mu u_r) (\bar{u}_s \gamma^\mu u_t)$	$Q_{lu} (\bar{l}_p \gamma_\mu l_r) (\bar{u}_s \gamma^\mu u_t)$
$Q_{qq}^{(3)} (\bar{q}_p \gamma_\mu \tau^I q_r) (\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{dd} (\bar{d}_p \gamma_\mu d_r) (\bar{d}_s \gamma^\mu d_t)$	$Q_{ld} (\bar{l}_p \gamma_\mu l_r) (\bar{d}_s \gamma^\mu d_t)$
$Q_{lq}^{(1)} (\bar{l}_p \gamma_\mu l_r) (\bar{q}_s \gamma^\mu q_t)$	$Q_{eu} (\bar{e}_p \gamma_\mu e_r) (\bar{u}_s \gamma^\mu u_t)$	$Q_{qe} (\bar{q}_p \gamma_\mu q_r) (\bar{e}_s \gamma^\mu e_t)$
$Q_{lq}^{(3)} (\bar{l}_p \gamma_\mu \tau^I l_r) (\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{ed} (\bar{e}_p \gamma_\mu e_r) (\bar{d}_s \gamma^\mu d_t)$	$Q_{qg}^{(1)} (\bar{q}_p \gamma_\mu q_r) (\bar{u}_s \gamma^\mu u_t)$
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Higgs penguins

Higgs Penguin Operators

Higgs penguin operators

$$\mathcal{O}_{eh} = (H^\dagger H)(\bar{\ell}_1 P_R e_2)H$$

$$\mathcal{O}_{uh} = (H^\dagger H)(\bar{q}_1 P_R u_2)H^c$$

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[Exercise: show that these interactions lead indeed to flavor violating Higgs couplings]

Higgs Penguin Operators

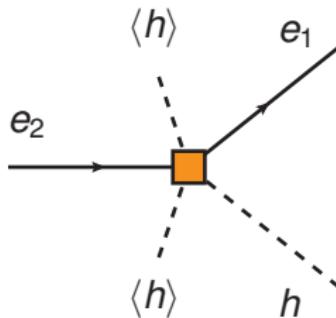
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$$h \rightarrow \tau \mu, \quad \tau \rightarrow \mu \gamma, \quad \tau \rightarrow 3\mu, \dots$$

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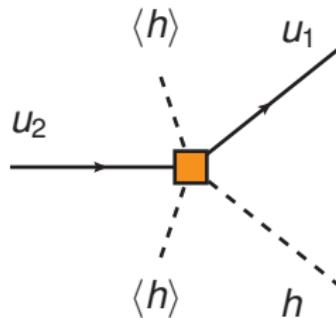
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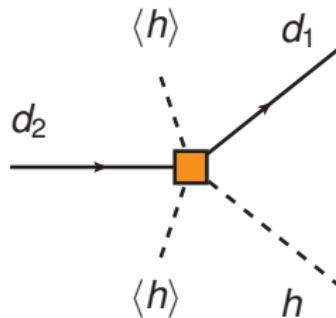
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$$h \rightarrow bs, \quad B \text{ meson mixing}, \quad B_s \rightarrow \mu^+ \mu^-, \dots$$

Z Penguin Operators

Z-penguin operators

$$\mathcal{O}_{hl}^{(3)} = (H^\dagger i \overleftrightarrow{D}_\mu^a H)(\bar{\ell}_1 \gamma^\mu \sigma_a P_L \ell_2)$$

$$\tilde{\mathcal{O}}_{hl}^{(1)} = (H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{\ell}_1 \gamma^\mu P_L \ell_2)$$

$$\mathcal{O}_{he} = (H^\dagger i \overleftrightarrow{D}_\mu H)(\bar{e}_1 \gamma^\mu P_R e_2)$$

...

Z Penguin Operators

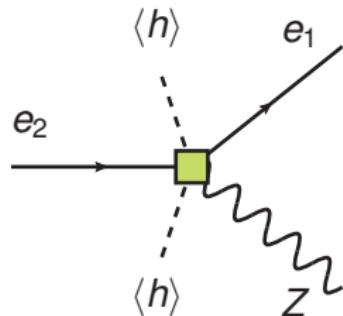
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induced processes:

$Z \rightarrow \tau \mu$, $\tau \rightarrow 3\mu$, $\mu \rightarrow e$ conversion , ...

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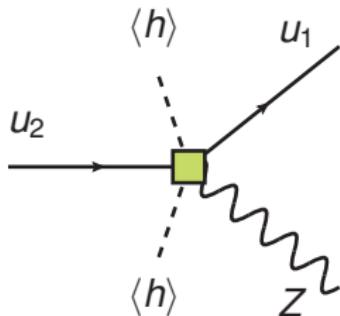
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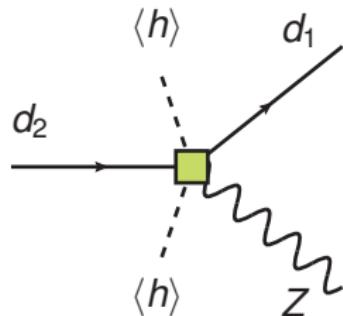
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Dipole Operators

dipole operators

$$\mathcal{O}_{dG} = (\bar{q}_1 \sigma^{\mu\nu} T^A P_R d_2) H \ G_{\mu\nu}^A$$

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Dipole Operators

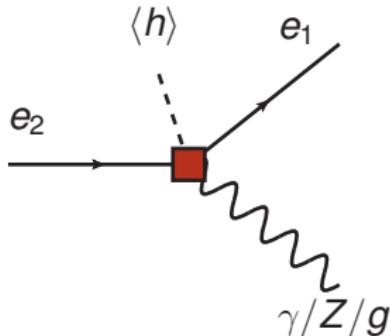
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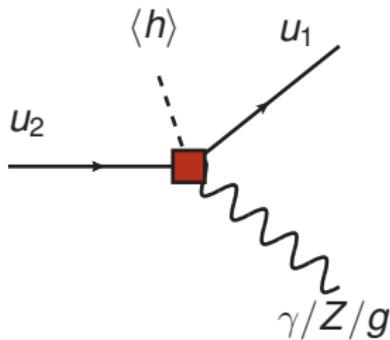
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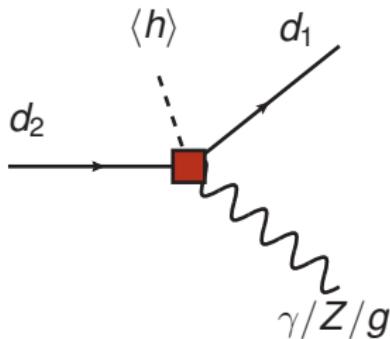
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Four Fermion Contact Interactions

4 fermion interactions

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+ many other Dirac and flavor structures

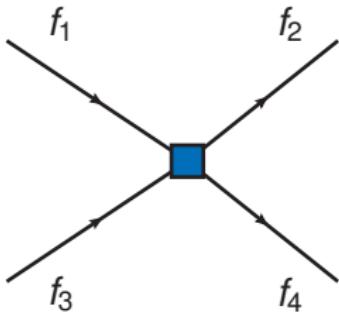
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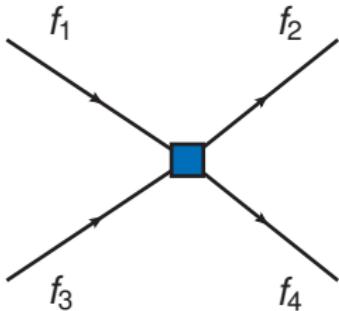
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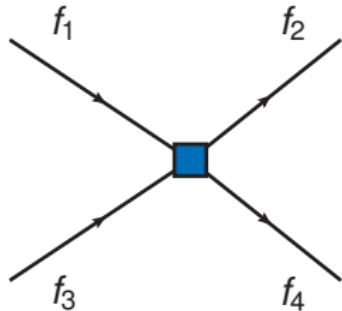
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(analogous for other meson systems)

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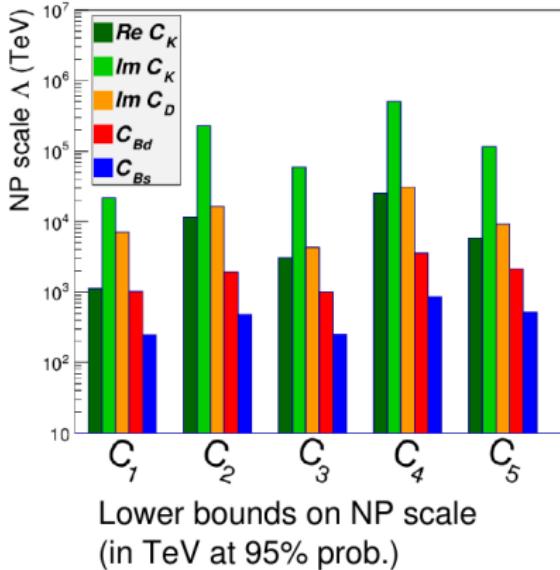
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(bounds on Λ assuming $|C_i| = 1$)

The New Physics Flavor Puzzle

Low energy **flavor observables** are sensitive to
New Physics far beyond the TeV scale



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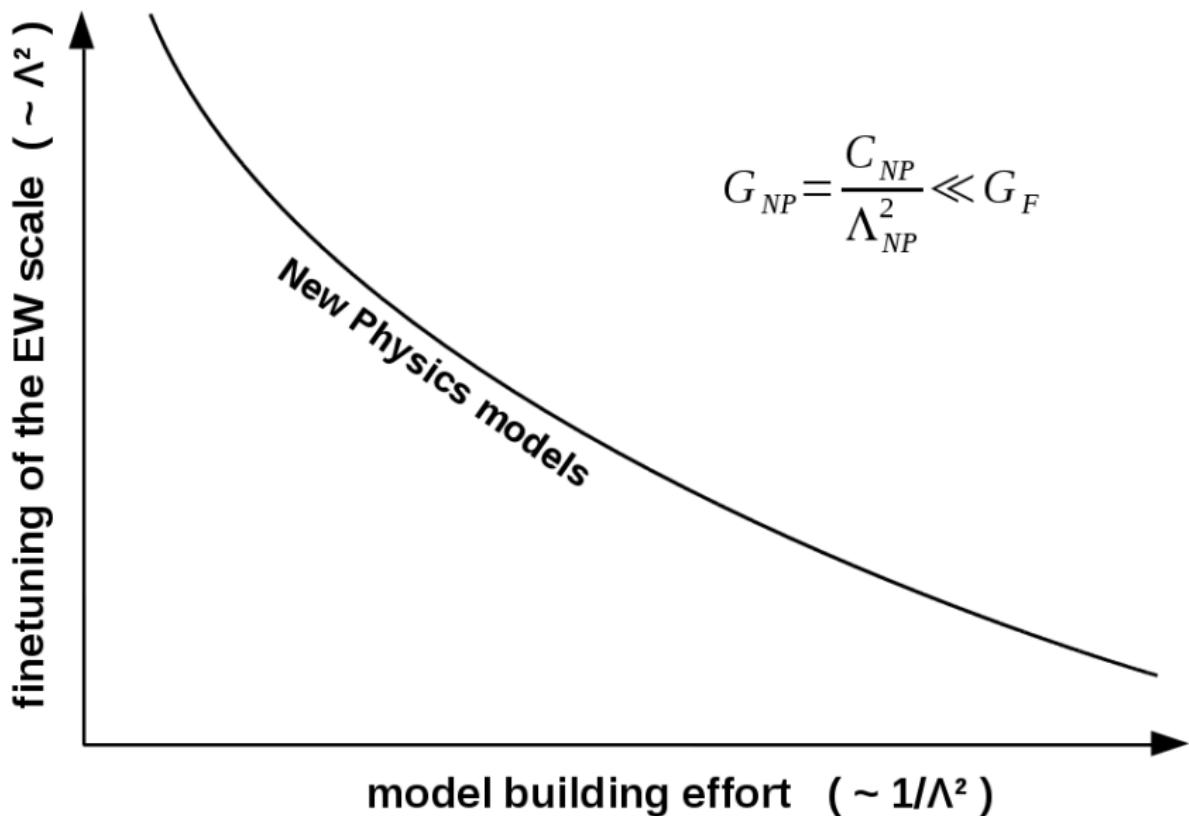


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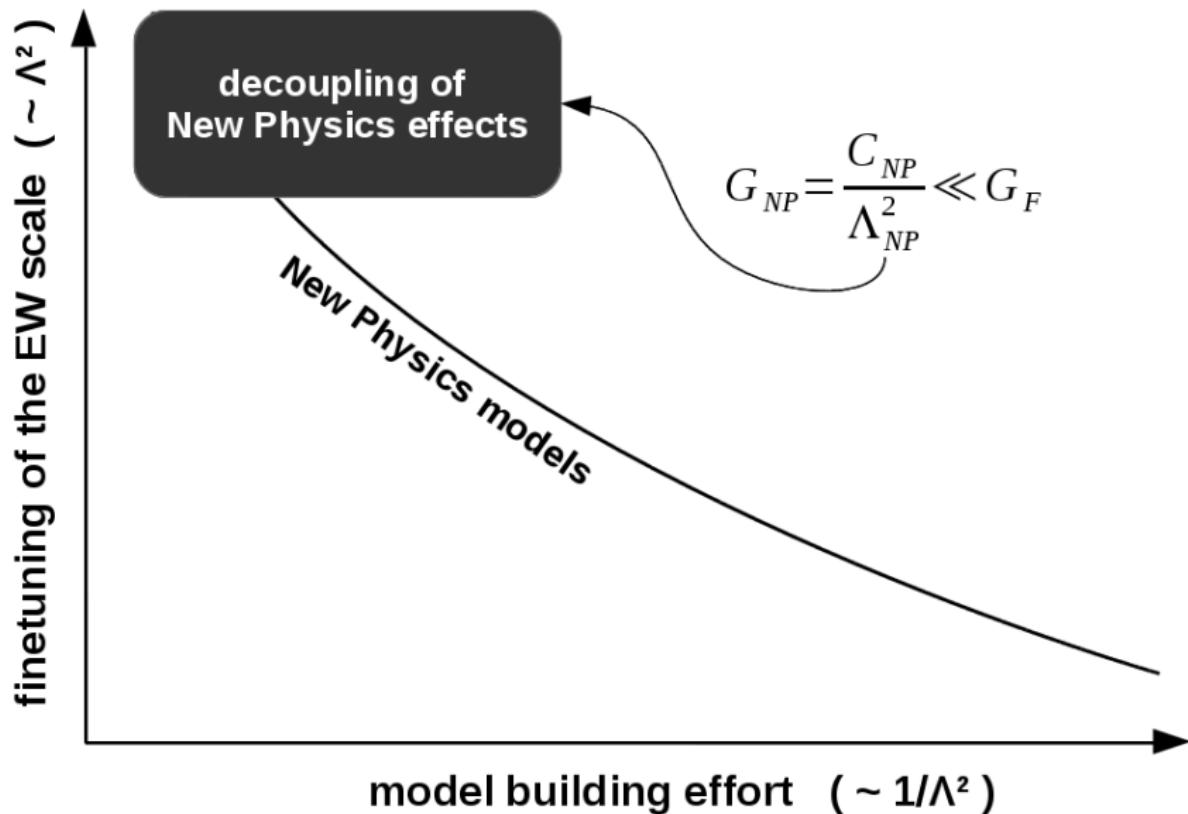
If there is New Physics
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solutions of the hierarchy problem require
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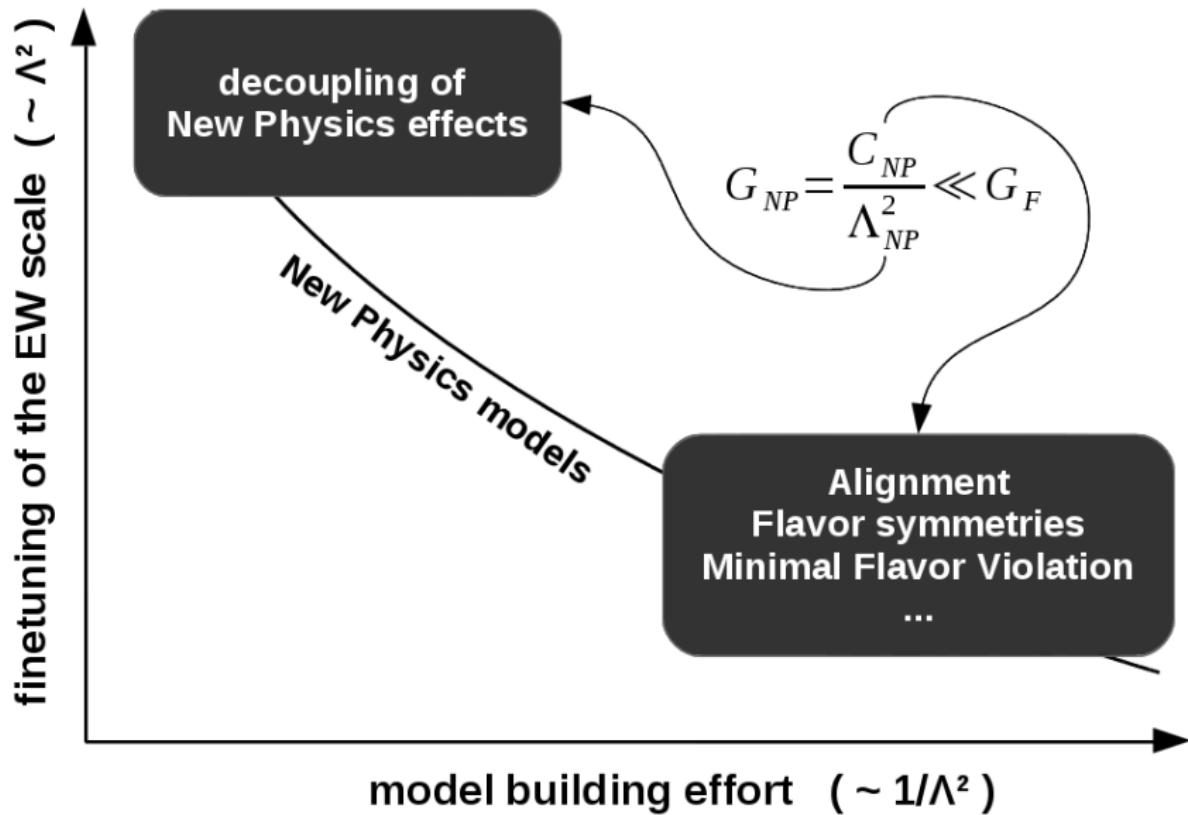
Reactions to the New Physics Flavor Puzzle



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Minimal Flavor Violation

recall from the first lecture that without the Yukawa couplings, the SM has a large global flavor symmetry

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The $SU(3)^5$ symmetry can be formally restored if one promotes the Yukawa couplings to “spurions” that transform in the following way

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the Yukawa interactions are now formally flavor invariant

$$\mathcal{L} \supset H^c(\bar{Q} Y_u U) + H^c(\bar{Q} Y_d D) + H(\bar{L} Y_\ell E)$$

Minimal Flavor Violation

the SM Yukawas remain the only sources of flavor breaking
also in theories beyond the SM

Chivukula, Georgi '87; D'Ambrosio et al. '02

Minimal Flavor Violation and FCNCs

What happens to flavor changing interactions among down quarks?

$$d^L = \mathbf{3}_Q, \quad d^R = \mathbf{3}_D, \quad Y_u = \mathbf{3}_Q \times \bar{\mathbf{3}}_U, \quad Y_d = \mathbf{3}_Q \times \bar{\mathbf{3}}_D$$

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flavor changing transitions are proportional to **small CKM elements**
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transitions involving right handed quarks are
further suppressed by small Yukawa couplings

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Meson mixing constraints are strongly relaxed in the MFV framework

The couplings C_i are now suppressed

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new physics can be at the TeV scale without violating the bounds

Flavor Violation in Models of New Physics

Two Higgs Doublet Models

one of the simplest extensions of the SM Higgs sector

- ▶ two Higgs doublets H_1 and H_2 with hypercharges -1/2 and +1/2

$$H_2 = \begin{pmatrix} H_2^+ \\ \frac{1}{\sqrt{2}}(v s_\beta + h_2 + i a_2) \end{pmatrix}, \quad H_1 = \begin{pmatrix} \frac{1}{\sqrt{2}}(v c_\beta + h_1 + i a_1) \\ H_1^- \end{pmatrix}$$

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- ▶ 5 physical degrees of freedom: h and H, A , and H^\pm

assuming CP conservation:

$$\begin{pmatrix} G^\pm \\ H^\pm \end{pmatrix} = \begin{pmatrix} s_\beta & -c_\beta \\ c_\beta & s_\beta \end{pmatrix} \begin{pmatrix} H_2^\pm \\ H_1^\pm \end{pmatrix}$$

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FCNCs at Tree Level

both Higgs doublets can couple to the SM fermions

$$\begin{aligned}\mathcal{L} \supset & (y_u)_{ik} H_2 \bar{Q}_i U_k + (\tilde{y}_u)_{ik} H_1^\dagger \bar{Q}_i U_k \\ & + (y_d)_{ik} H_1 \bar{Q}_i D_k + (\tilde{y}_d)_{ik} H_2^\dagger \bar{Q}_i D_k \\ & + (y_\ell)_{ik} H_1 \bar{L}_i E_k + (\tilde{y}_\ell)_{ik} H_2^\dagger \bar{L}_i E_k + \text{h.c.}\end{aligned}$$

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- for generic couplings y and \tilde{y} ,
quark masses and Higgs couplings are **not aligned**, e.g.

$$(m_d)_{ik} = \frac{v}{\sqrt{2}} \left(\mathbf{c}_\beta (y_d)_{ik} + \mathbf{s}_\beta (\tilde{y}_d)_{ik} \right), \quad (g_d^A)_{ik} = \frac{1}{\sqrt{2}} \left(\mathbf{s}_\beta (y_d)_{ik} - \mathbf{c}_\beta (\tilde{y}_d)_{ik} \right)$$

FCNCs at Tree Level

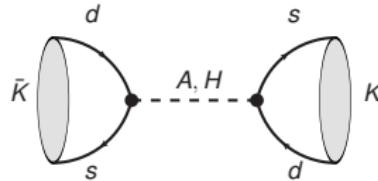
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- for generic couplings y and \tilde{y} ,
quark masses and Higgs couplings are **not aligned**, e.g.

$$(m_d)_{ik} = \frac{v}{\sqrt{2}} \left(\mathbf{c}_\beta (y_d)_{ik} + \mathbf{s}_\beta (\tilde{y}_d)_{ik} \right), \quad (g_d^A)_{ik} = \frac{1}{\sqrt{2}} \left(\mathbf{s}_\beta (y_d)_{ik} - \mathbf{c}_\beta (\tilde{y}_d)_{ik} \right)$$

- tree level FCNCs
- incredible strong constraints
from meson mixing



2HDMs with Natural Flavor Conservation

- ▶ **Natural Flavor Conservation:** no tree level FCNCs if all types of fermions couple only to one Higgs doublet (Glashow, Weinberg '77)
- ▶ Can be enforced by:
(softly broken) continuous symmetries (Peccei-Quinn)
or discrete symmetries (Z_2)
- ▶ 4 possibilities: $(y_u)_{ik} H_2 \bar{Q}_i U_k + (\tilde{y}_d)_{ik} H_2^\dagger \bar{Q}_i D_k + (\tilde{y}_\ell)_{ik} H_2^\dagger \bar{L}_i E_k$

type I	
up quarks	H_2
down quarks	H_2
leptons	H_2

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	type I	type II
up quarks	H_2	H_2
down quarks	H_2	H_1
leptons	H_2	H_1

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	type I	type II	type III
up quarks	H_2	H_2	H_2
down quarks	H_2	H_1	H_2
leptons	H_2	H_1	H_1

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	type I	type II	type III	type IV
up quarks	H_2	H_2	H_2	H_2
down quarks	H_2	H_1	H_2	H_1
leptons	H_2	H_1	H_1	H_2

2HDMs with Minimal Flavor Violation

- expansion of the “wrong” Higgs couplings

$$\begin{aligned}\tilde{y}_u &= \epsilon_u \textcolor{red}{y_u} + \epsilon'_u \textcolor{red}{y_u} \textcolor{blue}{y_u^\dagger} \textcolor{red}{y_u} + \epsilon''_u \textcolor{blue}{y_d} \textcolor{blue}{y_d^\dagger} \textcolor{red}{y_u} + \dots \\ \tilde{y}_d &= \epsilon_d \textcolor{blue}{y_d} + \epsilon'_d \textcolor{blue}{y_d} \textcolor{blue}{y_d^\dagger} \textcolor{blue}{y_d} + \epsilon''_d \textcolor{red}{y_u} \textcolor{red}{y_u^\dagger} \textcolor{blue}{y_d} + \dots \\ \tilde{y}_\ell &= \epsilon_\ell \textcolor{green}{y_\ell} + \epsilon'_\ell \textcolor{green}{y_\ell} \textcolor{green}{y_\ell^\dagger} \textcolor{green}{y_\ell} + \dots\end{aligned}$$

- still Flavor Changing Neutral Currents at tree level, but controlled by small Yukawas and CKM elements

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Exercise part 1:

demonstrate that these terms are formally invariant under the flavor group

- still Flavor Changing Neutral Currents at tree level, but controlled by small Yukawas and CKM elements

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Exercise part 1:

demonstrate that these terms are formally invariant under the flavor group

Exercise part 2:

rotate into the quark mass eigenstate basis and show that off-diagonal entries in \tilde{y}_u and \tilde{y}_d are suppressed by small CKM elements

- ▶ still Flavor Changing Neutral Currents at tree level, but controlled by small Yukawas and CKM elements

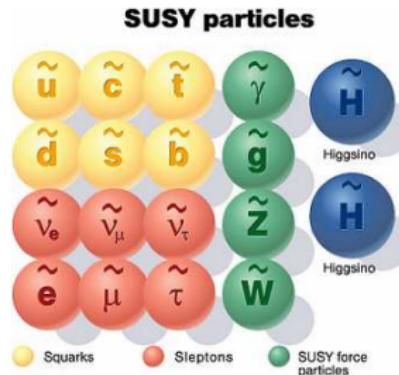
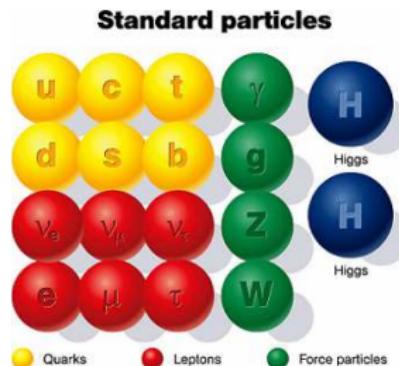
The Minimal Supersymmetric Standard Model

Supersymmetry (SUSY) implies:
every fermion has a bosonic partner
and vice versa

requires 2 Higgs doublets to give mass
to up-type and down-type fermions
(2HDM type II)

$$\tan \beta = \langle H_u \rangle / \langle H_d \rangle$$

expect at least some SUSY particles
(Higgsinos, stops, gluinos)
at or below $O(\text{TeV})$ for a
natural electro-weak scale



Flavor and CP Violation in the MSSM

The MSSM can contain many new sources of flavor and CP violation

Flavor and CP Violation in the MSSM

The MSSM can contain many new sources of flavor and CP violation

Higgsino and Higgs masses
→ 2 phases

$$\mu \tilde{H}_u \tilde{H}_d + B\mu H_u H_d + m_{H_u}^2 |H_u|^2 + m_{H_d}^2 |H_d|^2$$

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squark and slepton masses
→ 15 angles + 15 phases

$$m_Q^2 \tilde{Q}_L^\dagger \tilde{Q}_L + m_U^2 \tilde{U}_R^\dagger \tilde{U}_R + m_D^2 \tilde{D}_R^\dagger \tilde{D}_R \\ + m_L^2 \tilde{L}_L^\dagger \tilde{L}_L + m_E^2 \tilde{E}_R^\dagger \tilde{E}_R$$

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gaugino masses
→ 3 phases

$$m_1 \tilde{B} \tilde{B} + m_2 \tilde{W} \tilde{W} + m_3 \tilde{g} \tilde{g}$$

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$$m_1 \tilde{B} \tilde{B} + m_2 \tilde{W} \tilde{W} + m_3 \tilde{g} \tilde{g}$$

trilinear couplings
→ 18 angles + 27 phases

$$A_u H_u \tilde{Q}_L^\dagger \tilde{U}_R + A_d H_d \tilde{Q}_L^\dagger \tilde{D}_R + A_\ell H_d \tilde{L}_L^\dagger \tilde{E}_R$$

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not all phases are physical! (like in the case of the CKM matrix)

Flavor and CP Violation in the MSSM

The MSSM can contain many new sources of flavor and CP violation

Higgsino and Higgs masses
→ 2 phases

$$\mu \tilde{H}_u \tilde{H}_d + B\mu H_u H_d + m_{H_u}^2 |H_u|^2 + m_{H_d}^2 |H_d|^2$$

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not all phases are physical! (like in the case of the CKM matrix)

2 phases can be rotated away...

The SUSY Flavor Problem

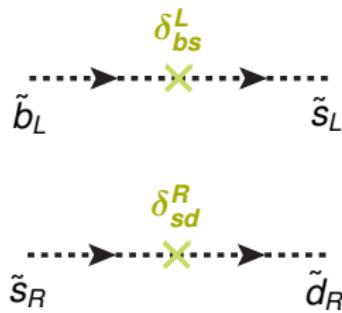
squark flavor mixing can lead to large FCNCs at the 1-loop level

most transparent parametrization in terms of “mass insertions”

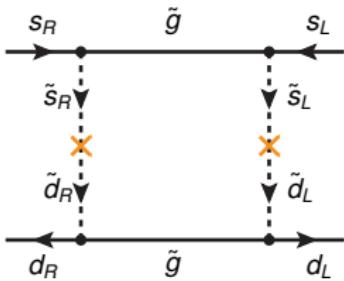
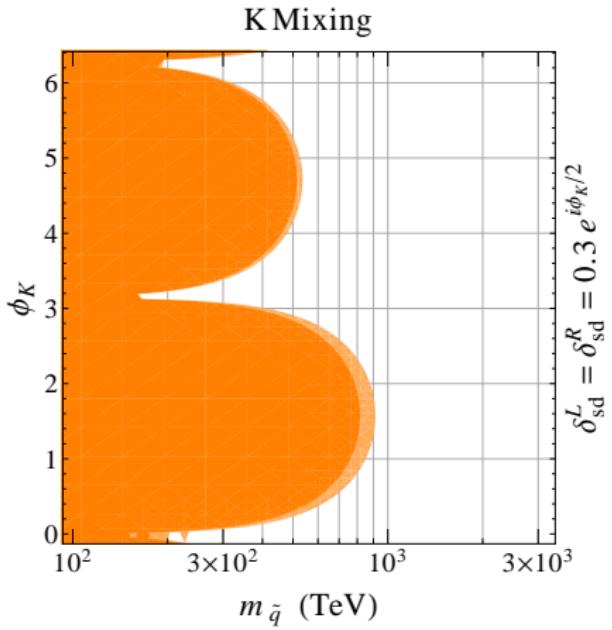
$$m_Q^2 = \tilde{m}_Q^2 (\mathbb{1} + \delta_q)$$

$$m_U^2 = \tilde{m}_U^2 (\mathbb{1} + \delta_u)$$

$$m_D^2 = \tilde{m}_D^2 (\mathbb{1} + \delta_d)$$



Probing PeV Scale Squarks



$$M_{12}^K \propto \frac{\alpha_s^2}{m_{\tilde{q}}^2} (\delta_{sd}^L \delta_{sd}^R)$$

- squarks of several 100 - 1000 TeV can be probed if relevant phases are not suppressed

Minimal Flavor Violation in the MSSM

soft masses
of squarks and sleptons

$$m_Q^2 = \tilde{m}_Q^2 \left(\mathbb{1} + b_1 Y_u Y_u^\dagger + b_2 Y_d Y_d^\dagger + \right. \\ \left. + b_3 Y_d Y_d^\dagger Y_u Y_u^\dagger + b_3^* Y_u Y_u^\dagger Y_d Y_d^\dagger + \dots \right)$$

$$m_U^2 = \tilde{m}_U^2 \left(\mathbb{1} + b_4 Y_u^\dagger Y_u + \dots \right)$$

$$m_D^2 = \tilde{m}_D^2 \left(\mathbb{1} + b_5 Y_d^\dagger Y_d + \dots \right)$$

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$$m_U^2 = \tilde{m}_U^2 \left(\mathbb{1} + b_4 Y_u^\dagger Y_u + \dots \right)$$
$$m_D^2 = \tilde{m}_D^2 \left(\mathbb{1} + b_5 Y_d^\dagger Y_d + \dots \right)$$

trilinear couplings

$$A_u = \tilde{A}_u \left(\mathbb{1} + b_6 Y_d Y_d^\dagger + b_7 Y_u Y_u^\dagger + \dots \right) Y_u$$
$$A_d = \tilde{A}_d \left(\mathbb{1} + b_8 Y_u Y_u^\dagger + b_9 Y_d Y_d^\dagger + \dots \right) Y_d$$

Minimal Flavor Violation in the MSSM

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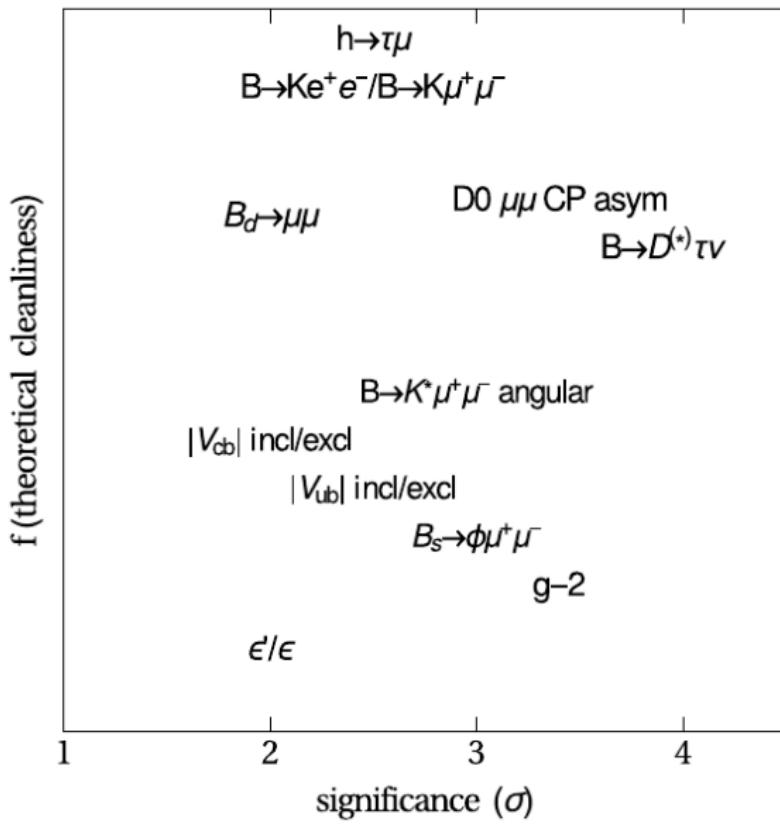
gaugino/higgsino/higgs
masses

$$m_1, m_2, m_3, \mu, B\mu$$

- ▶ flavor violation controlled by small CKM elements
- ▶ sources of CP violation beyond the CKM are allowed in MFV

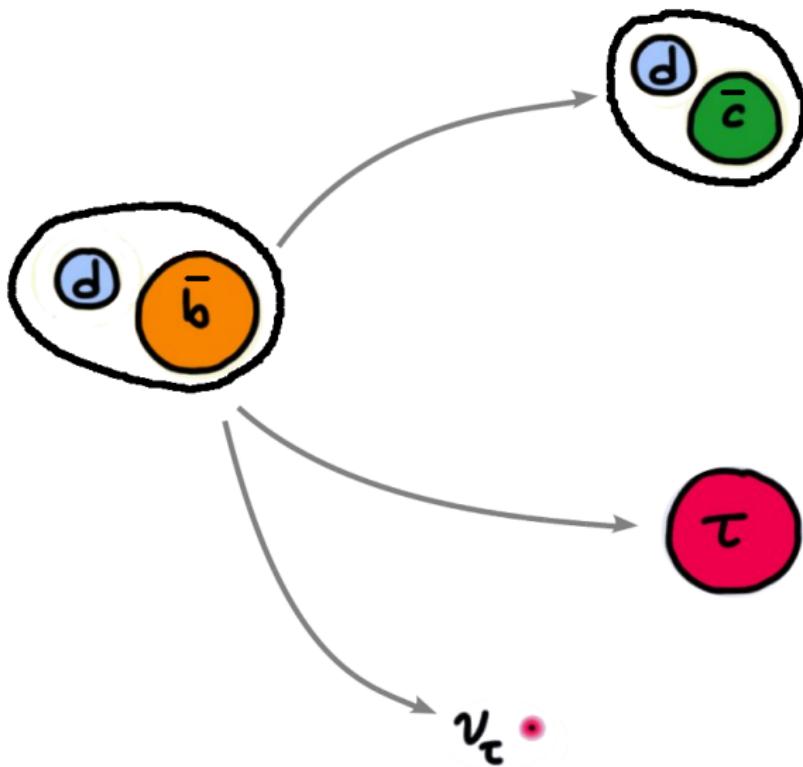
Flavor Anomalies

Overview of Current Flavor Anomalies



Z. Ligeti

The $B \rightarrow D^{(*)}\tau\nu$ Decays



“The R_D and R_{D^*} Anomalies”

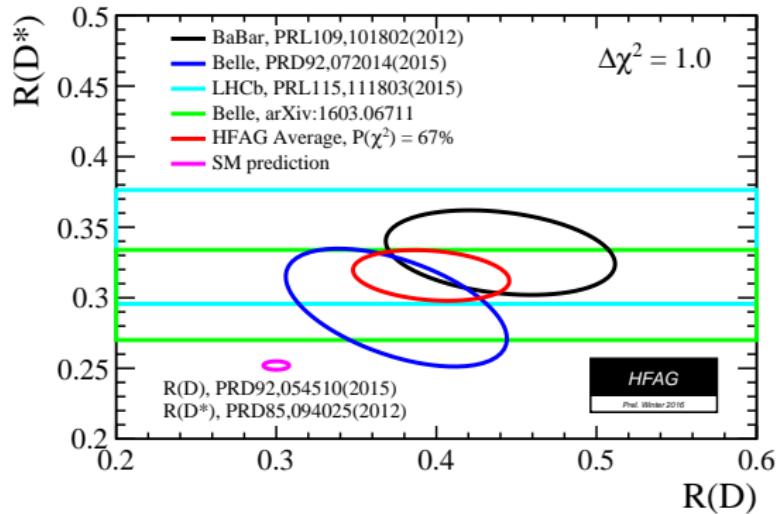
$$R_D = \frac{\text{BR}(B \rightarrow D\tau\nu)}{\text{BR}(B \rightarrow D\ell\nu)}$$

$$R_{D^*} = \frac{\text{BR}(B \rightarrow D^*\tau\nu)}{\text{BR}(B \rightarrow D^*\ell\nu)}$$

SM predictions very well under control

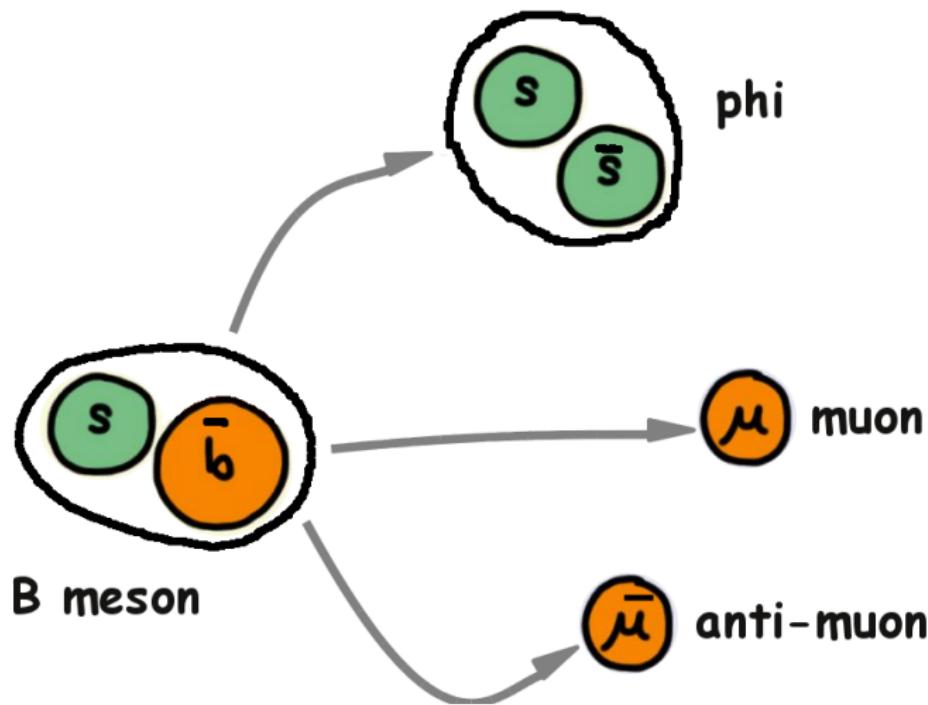
Fajfer, Kamenik, Nisandzic '12

HPQCD collaboration '15



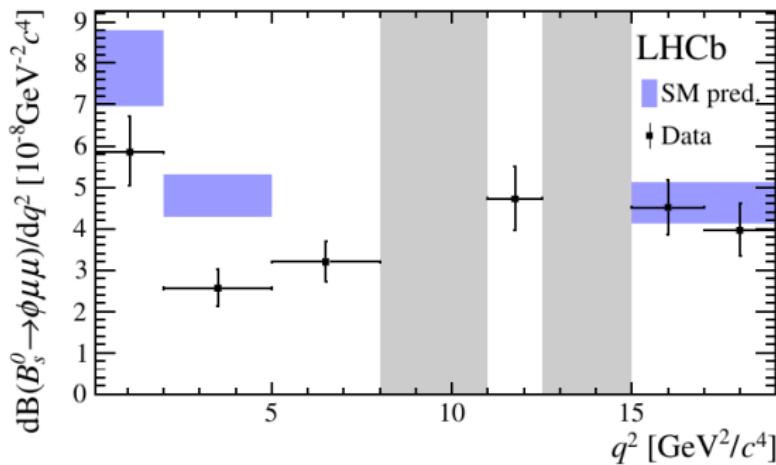
Belle, BaBar and LHCb results are all high
combined significance $\sim 4\sigma$

The $B_s \rightarrow \phi\mu^+\mu^-$ Decay



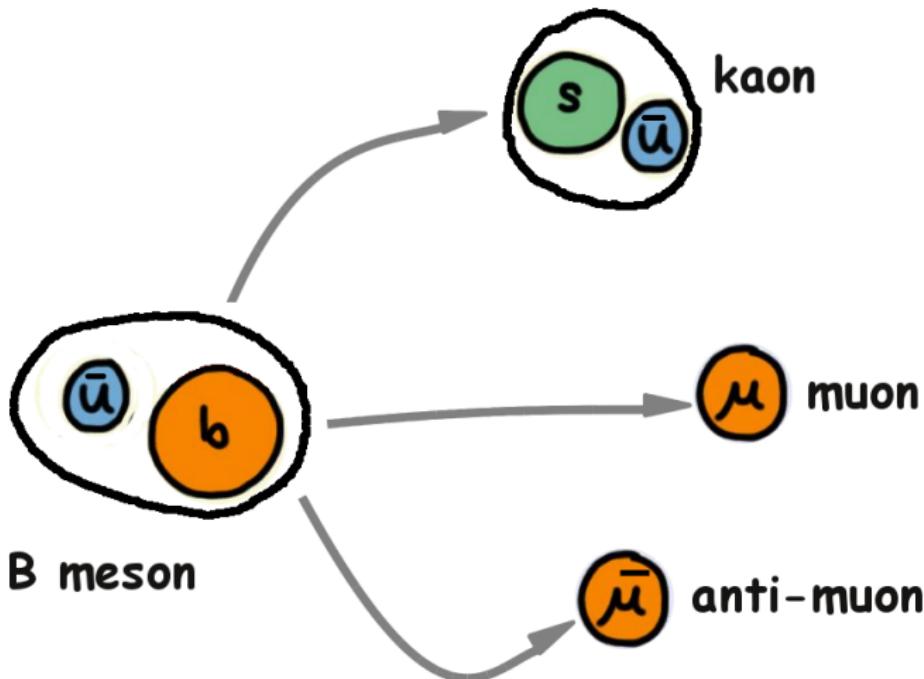
“The $B_s \rightarrow \phi\mu^+\mu^-$ Anomaly”

LHCb 1506.08777

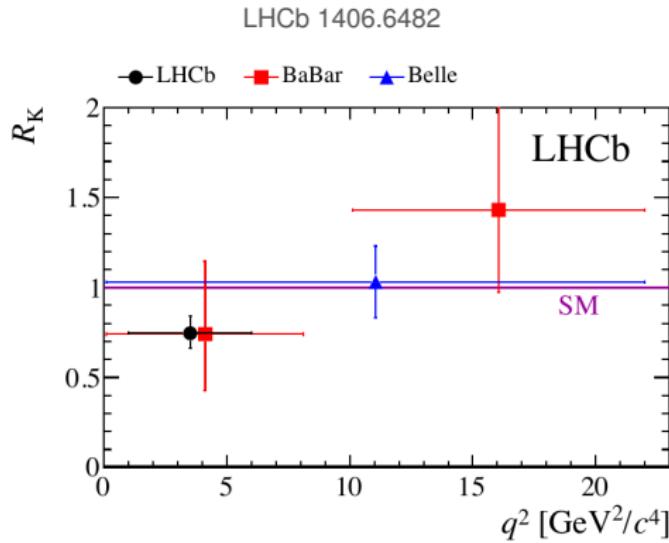


branching ratio is 3.5σ below SM prediction for $1 \text{ GeV}^2 < q^2 < 6 \text{ GeV}^2$

The $B \rightarrow K\mu^+\mu^-$ Decay



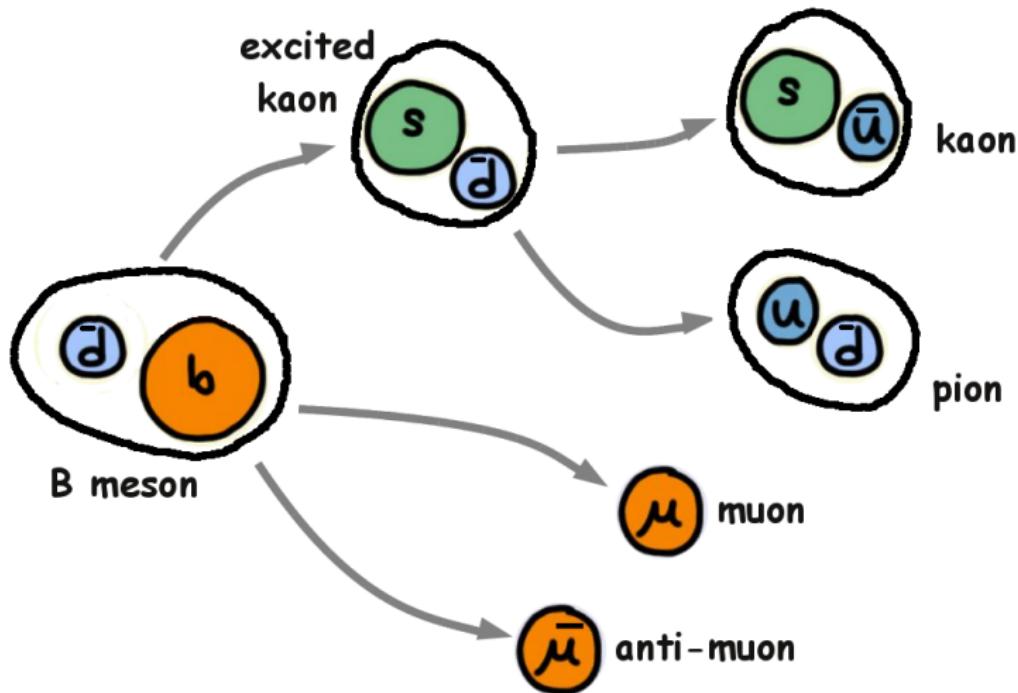
“The R_K Anomaly”

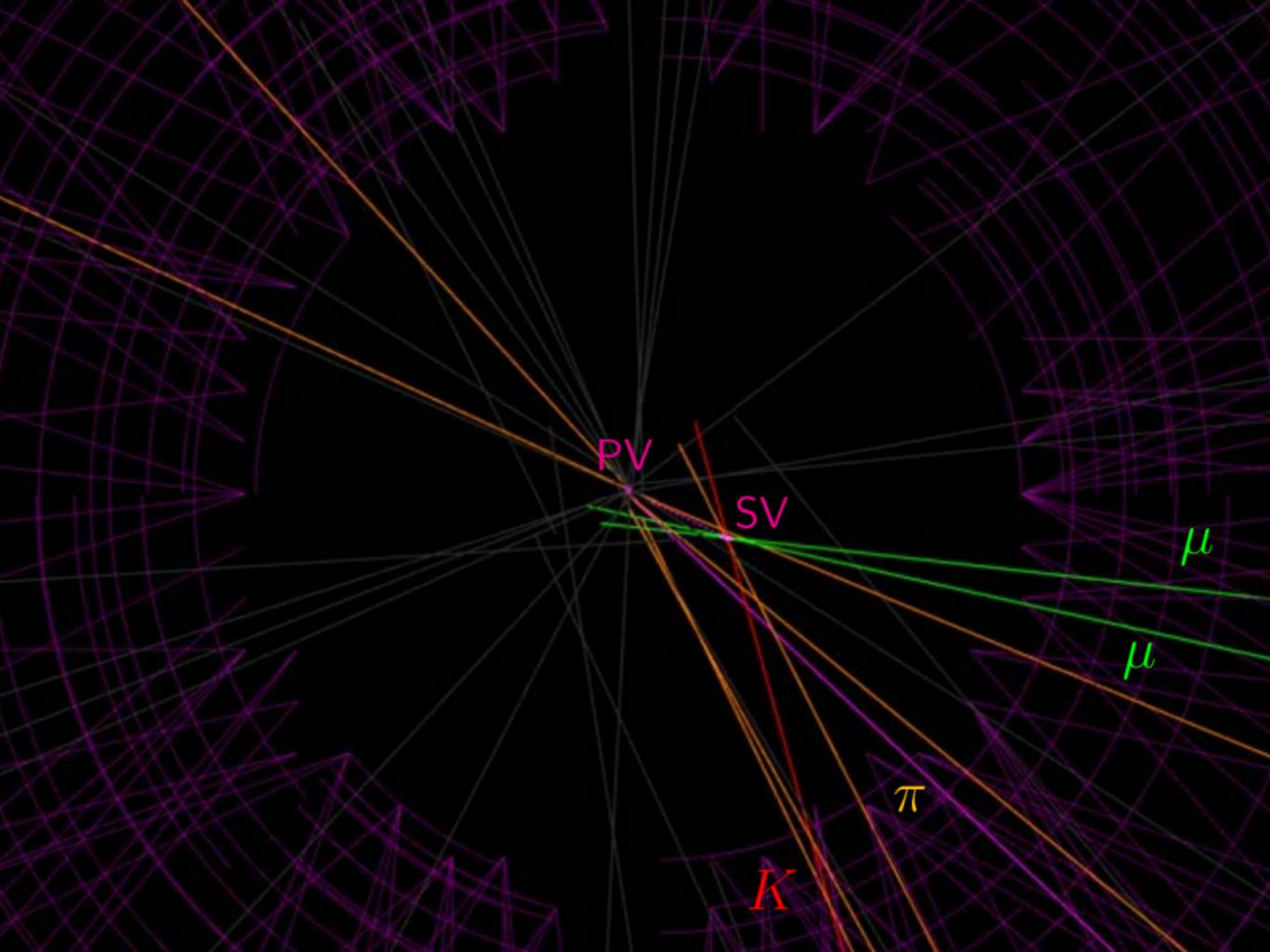


2.6σ hint for violation of lepton flavor universality (LFU)

$$R_K = \frac{\text{BR}(B \rightarrow K \mu^+ \mu^-)_{[1,6]}}{\text{BR}(B \rightarrow K e^+ e^-)_{[1,6]}} = 0.745^{+0.090}_{-0.074} \pm 0.036$$

The $B \rightarrow K^*(\rightarrow K\pi)\mu^+\mu^-$ Decay





PV

SV

π

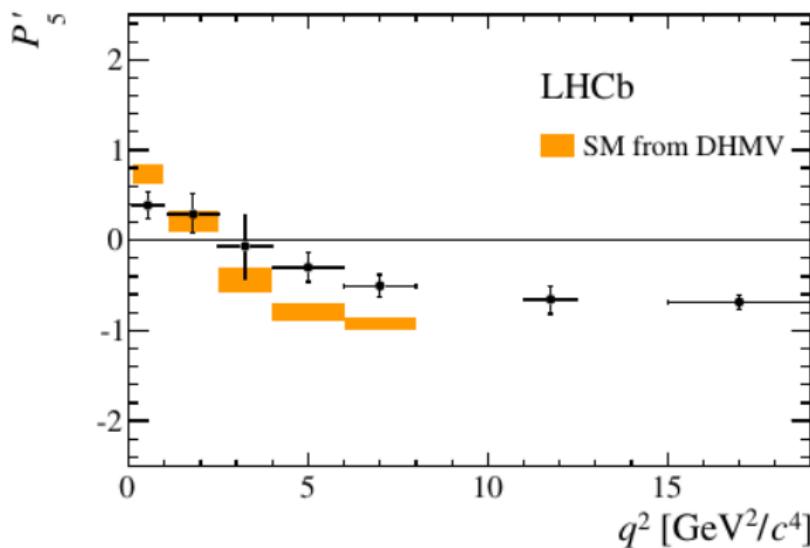
K

μ

μ

"The $B \rightarrow K^* \mu^+ \mu^-$ Anomaly"

LHCb 1512.04442



2.8σ deviation in $[4,6] \text{ GeV}^2$ bin
($+3.0\sigma$ in $[6,8] \text{ GeV}^2$ bin)

P'_5 characterizes the angular distribution of the decay products

WA, Ball, Bharucha,
Buras, Straub, Wick 0811.1214

Bobeth et al. 1212.2321

Descotes-Genon et al.
1207.2753, 1303.5794

...

What Could It Be?

	branching ratios	angular observables	LFU ratios

What Could It Be?

	branching ratios	angular observables	LFU ratios
statistical fluctuations?	✓	✓	✓

What Could It Be?

	branching ratios	angular observables	LFU ratios
statistical fluctuations?	✓	✓	✓
parametric uncertainties?	✓	✗	✗

What Could It Be?

	branching ratios	angular observables	LFU ratios
statistical fluctuations?	✓	✓	✓
parametric uncertainties?	✓	✗	✗
underestimated hadronic effects?	✓	✓	✗

What Could It Be?

	branching ratios	angular observables	LFU ratios
statistical fluctuations?	✓	✓	✓
parametric uncertainties?	✓	✗	✗
underestimated hadronic effects?	✓	✓	✗
New Physics?	✓	✓	✓

Summary of the Second Lecture

- ▶ Low energy flavor observables have indirect sensitivity to very high scales
- ▶ If there is new physics at the TeV scale, why have we not seen it yet in flavor observables?
- ▶ The idea of Minimal Flavor Violation can tame flavor violation in new physics models
- ▶ Few anomalies exist in flavor measurements.
Are they first hints for new physics?