

**Journal club, 12 May 2016**  
**Dark Matter in the Milky Way**  
**MITP, 2-13 May 2016**

1. Huang et al  
“The Milky Way’s rotation curve out to 100 kpc and its constraint on the Galactic mass distribution”  
<http://arxiv.org/abs/1604.01216>
2. Lu et al  
“The connection between the host halo and the satellite galaxies of the Milky Way”  
<https://arxiv.org/abs/1605.02075>
3. Lin & Ishak  
“Ultra faint dwarf galaxies: an arena for testing dark matter versus modified gravity”  
<http://arxiv.org/abs/1604.00950>
4. Nipoti  
“On the origin of Sérsic profiles of galaxies and Einasto profiles of dark-matter halos”  
<https://arxiv.org/abs/1605.00680>
5. Relativistic treatment of galactic rotation curves  
Magalhaes & Cooperstock, <http://arxiv.org/abs/1508.07491>  
Carrick & Cooperstock, <http://arxiv.org/abs/1101.3224>  
Rowland, <http://www.worldscientific.com/doi/abs/10.1142/S0218271815500650>  
Cooperstock, <http://www.worldscientific.com/doi/abs/10.1142/S0217732316500371>  
[Aaron Dutton’s slides attached]

Galactic Mapping with general relativity and  
the observed rotation curves

1508.07491 Magalhaes & Cooperstock

**Metric in cylindrical coordinates, r, z**

$$ds^2 = -e^\nu(dr^2 + dz^2) - (r^2 - N^2)d\phi^2 - 2Ncd\phi dt + c^2 dt^2,$$

**Rotation velocity, V**      $V(r, z) = r\omega(r, z) \approx \frac{cN(r, z)}{r}$ .     **Metric function, N**

**Einstein Eqs.**      $N_{rr} + N_{zz} - \frac{N_r}{r} = 0$ .      $\frac{N_r^2 + N_z^2}{r^2} = \frac{8\pi G\rho}{c^2}$ ,

**New variable**      $\Phi = \int \frac{N}{r} dr$ ,      $V = c \frac{\partial \Phi}{\partial r}$ .

**Poisson Eq.**      $\Delta \Phi = 0$ ,

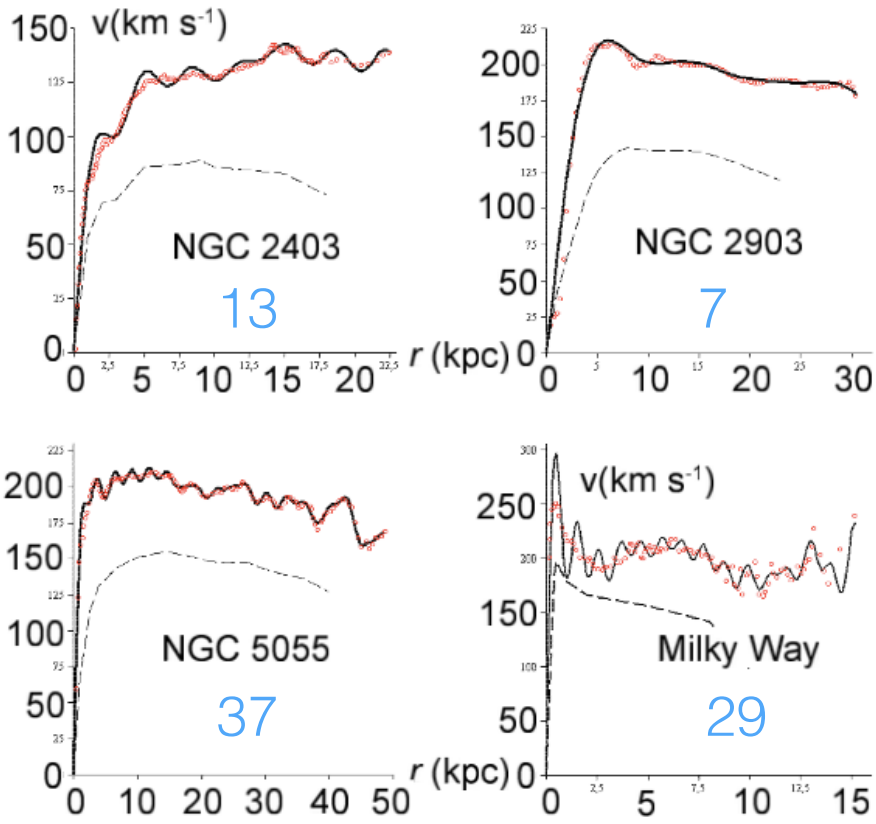
**Solution: sum of  
bessel functions**  
(n is arbitrary)      $\Phi = \sum_n C_n e^{-k_n |z|} J_0(k_n r)$ ,

$$V = -c \sum_n k_n C_n e^{-k_n |z|} J_1(k_n r),$$

**compute  
density**

$$V = -c \sum_n k_n C_n e^{-k_n |z|} J_1(k_n r),$$

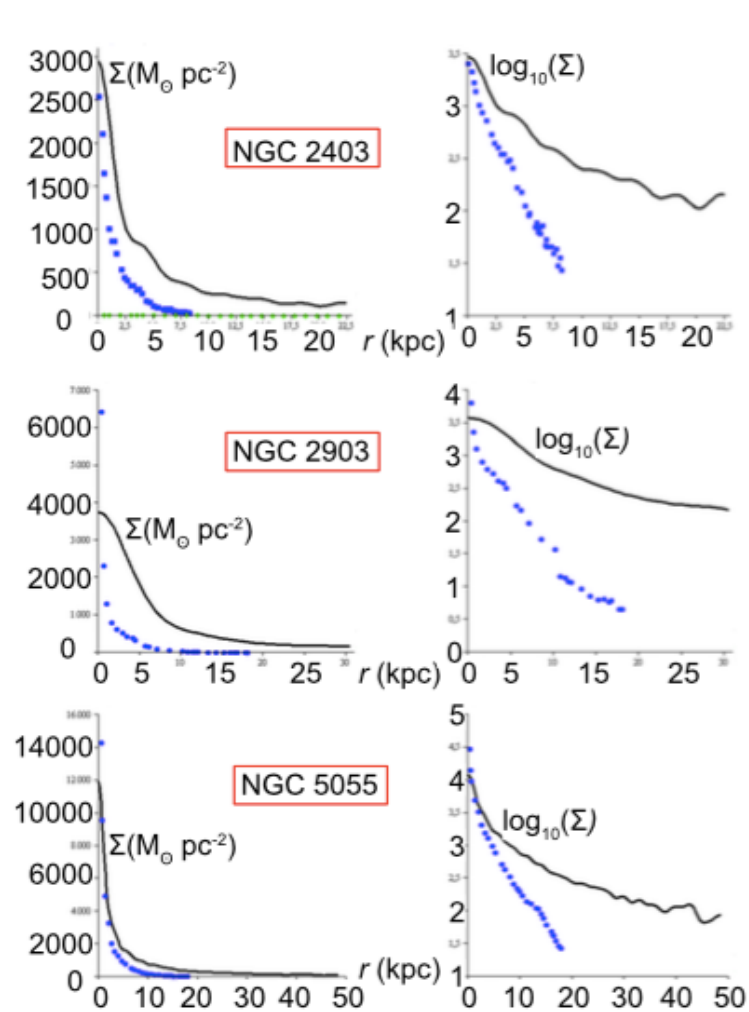
Rotation Velocity [km/s]



- Observations
- GR model
- ..... Newtonian

Radius [kpc]

## Surface Density Profiles



○ Observations

— GR model

GR model has much more (baryonic) mass at large radii than observed