

# CKM fits and kaon decays

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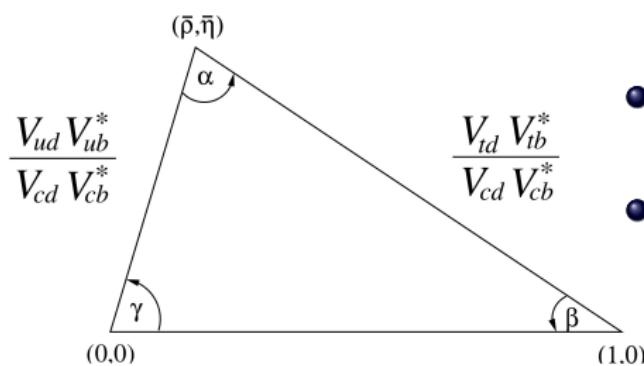


# CKMfitter

# The CKM matrix

In SM, flavour dynamics related to weak charged transitions  
which mix quarks of different generations

Encoded in unitary CKM matrix  $V_{CKM} = \begin{bmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{bmatrix}$

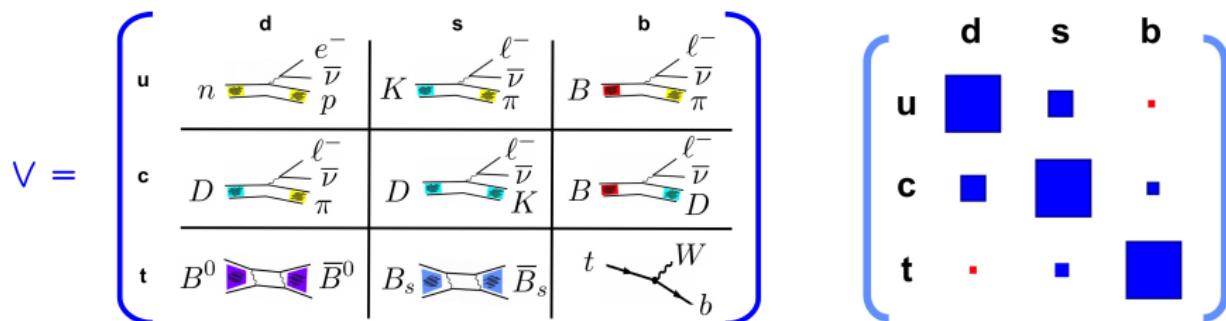


- 3 generations  $\Rightarrow$  1 phase, only source of  $CP$ -violation in SM
- Wolfenstein parametrisation, defined to hold to all orders in  $\lambda$  and rephasing invariant

$$\lambda^2 = \frac{|V_{us}|^2}{|V_{ud}|^2 + |V_{us}|^2} \quad A^2 \lambda^4 = \frac{|V_{cb}|^2}{|V_{ud}|^2 + |V_{us}|^2} \quad \bar{\rho} + i\bar{\eta} = -\frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*}$$

$\Rightarrow$  4 parameters describing the CKM matrix

# Extracting the CKM parameters



- $CP$ -invariance of QCD to build hadronic-indep.  $CP$ -violating asym. or to determine hadronic inputs from data
- Statistical framework to combine data and assess uncertainties

	Exp. uncert.		Theoretical uncertainties
Tree	$B \rightarrow DK$	$\gamma$	$B(b) \rightarrow D(c)\ell\nu$ $ V_{cb} $ vs form factor $F^{B \rightarrow D}$ (OPE)
			$B(b) \rightarrow \pi(u)\ell\nu$ $ V_{ub} $ vs form factor $F^{B \rightarrow \pi}$ (OPE)
			$M \rightarrow \ell\nu, M \rightarrow N\ell\nu$ $ V_{UD} $ vs $f_M$ (decay cst), $F^{M \rightarrow N}$
Loop	$B \rightarrow J/\Psi K_s$	$\beta$	$\epsilon_K$ ( $K$ mix) $(\bar{\rho}, \bar{\eta})$ vs $B_K$ (bag parameter)
	$B \rightarrow \pi\pi, \rho\rho$	$\alpha$	$\Delta m_d, \Delta m_s$ ( $B_d, B_s$ mix) $ V_{tb} V_{tq} $ vs $f_B^2 B_B$ (bag param)

# The inputs

CKM  
fitter

frequentist ( $\simeq \chi^2$  minim.) + Rfit scheme for theory uncert.

data = weak  $\otimes$  QCD  $\implies$  Need for hadronic inputs (mostly lattice)

$ V_{ud} $	superallowed $\beta$ decays	PRC79, 055502 (2009)
$ V_{us} $	$K_{\ell 3}$	$f_+(0) = 0.9645 \pm 0.0015 \pm 0.0045$
	$K \rightarrow \ell\nu, \tau \rightarrow K\nu_\tau$	$f_K = 155.2 \pm 0.2 \pm 0.6 \text{ MeV}$
$ V_{us}/V_{ud} $	$K \rightarrow \ell\nu/\pi \rightarrow \ell\nu, \tau \rightarrow K\nu_\tau/\tau \rightarrow \pi\nu_\tau$	$f_K/f_\pi = 1.1952 \pm 0.0007 \pm 0.0029$
$\epsilon_K$	PDG	$\hat{B}_K = 0.7615 \pm 0.0027 \pm 0.0137$
$ V_{cd} $	$D \rightarrow \mu\nu, D \rightarrow \pi\ell\nu$	$f_{D_s}/f_D = 1.175 \pm 0.001 \pm 0.004, f_+^{D \rightarrow \pi}(0)$
$ V_{cs} $	$D_s \rightarrow \mu\nu, D_s \rightarrow \tau\nu, D \rightarrow \pi\ell\nu$	$f_{D_s} = 248.2 \pm 0.3 \pm 1.9 \text{ MeV}, f_+^{D \rightarrow K}(0)$
$ V_{ub} $	inclusive and exclusive $B$ semileptonic	$ V_{ub}  \cdot 10^3 = 4.01 \pm 0.08 \pm 0.22$
$ V_{cb} $	inclusive and exclusive $B$ semileptonic	$ V_{cb}  \cdot 10^3 = 41.00 \pm 0.33 \pm 0.74$
$B \rightarrow \tau\nu$	$(1.24 \pm 0.22) \cdot 10^{-4}$	$f_{B_s}/f_{B_d} = 1.205 \pm 0.003 \pm 0.006$
		$f_{B_s} = 224.0 \pm 1.0 \pm 2.0 \text{ MeV}$
$ V_{ub}/V_{cb} $	$\Lambda_b$ semileptonic decays	integrals of $\Lambda_b$ form factors
$\Delta m_d$	last WA $B_d$ - $\bar{B}_d$ mixing	$B_{B_s}/B_{B_d} = 1.023 \pm 0.013 \pm 0.014$
$\Delta m_s$	last WA $B_s$ - $\bar{B}_s$ mixing	$B_{B_s} = 1.320 \pm 0.016 \pm 0.030$
$\beta$	last WA $J/\psi K^{(*)}$	isospin
$\alpha$	last WA $\pi\pi, \rho\pi, \rho\rho$	GLW/ADS/GGSZ
$\gamma$	last WA $B \rightarrow D^{(*)} K^{(*)}$	as well as $m_t, m_c, \alpha_s(M_Z)$ !

# Statistical framework

$q = (A, \lambda, \bar{\rho}, \bar{\eta} \dots)$  to be determined

- $\mathcal{O}_{\text{meas}} \pm \sigma_{\mathcal{O}}$  experimental values of observables
- $\mathcal{O}_{\text{th}}(q)$  theoretical description in a given model

In case of statistical uncertainties  $\sigma_{\mathcal{O}}$ , likelihoods and  $\chi^2$

$$\mathcal{L}(q) = \prod_{\mathcal{O}} \mathcal{L}_{\mathcal{O}}(q) \quad \chi^2(q) = -2 \ln \mathcal{L}(q) = \sum_{\mathcal{O}} \left( \frac{\mathcal{O}_{\text{th}}(q) - \mathcal{O}_{\text{meas}}}{\sigma_{\mathcal{O}}} \right)^2$$

- Central value: estimator  $\hat{q}$  **max likelihood**:  $\chi^2(\hat{q}) = \min_q \chi^2(q)$
- Range: **confidence level** for each  $q_0$  ( $p$ -value for  $q = q_0$ ) by:

$$\Delta \chi^2(q_0) = \chi^2(q_0) - \min_q \chi^2(q)$$

assumed to obey  $\chi^2$  law with  $N = \dim(q)$  to yield CIs

- Pull: **comparison of  $\chi^2_{\min}$**  with and without one measurement

$$p_{\mathcal{O}} = \sqrt{\min_q \chi^2_{\text{with meas}}(q) - \min_q \chi^2_{\text{without meas}}(q)}$$

⇒ Specific scheme to treat theoretical uncertain (currently Rfit)

# Averaging lattice results

## Collecting lattice results

- follow FLAG to exclude limited results
- supplement with more recent published results with error budget

## Splitting error estimates into stat and syst

- Stat : essentially related to size of gauge conf
- Syst : fermion action,  $a \rightarrow 0$ ,  $L \rightarrow \infty$ , mass extrapolations...  
added **linearly** using error budget

## “Educated Rfit” used to combine the results

- no correlations assumed
- product of (Gaussian + Rfit) likelihoods for central value
- product of Gaussian (stat) likelihoods for stat uncertainty
- syst uncertainty of the combination = most precise method
  - the present state of art cannot allow us to reach a better theoretical accuracy than the best of all estimates
  - best estimate should not be penalized by less precise methods

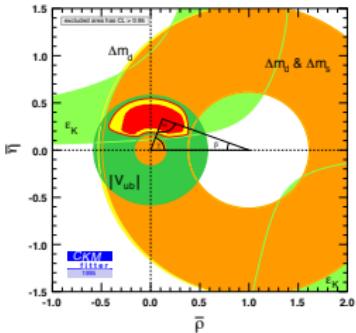
## Illustration for $f_K/f_\pi$

Reference	$N_f$	Mean	Stat	Syst
ETMC09	2	1.210	0.006	0.024
HPQCD/UKQCD07	2+1	1.189	0.002	0.014
MILC10	2+1	1.197	0.002	$+0.003$ $-0.007$
BMW10	2+1	1.192	0.007	0.013
LVdW11	2+1	1.202	0.011	0.024
RBC-UKQCD12	2+1	1.1991	0.0116	0.0185
HPQCD13	2+1+1	1.1938	0.0015	0.0032
FNAL-MILC14	2+1+1	1.1956	0.0010	$+0.0033$ $-0.0024$
ETMC14	2+1+1	1.188	0.011	0.020
Our average		1.1952	0.0007	0.0029

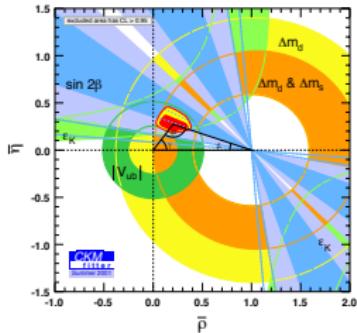
- Other values proposed:  $1.194 \pm 0.005$  ( $N_f = 2$  FLAG),  
 $1.192 \pm 0.005$  ( $N_f = 3$  FLAG)...
- Results for QCD decay constants (further etm corrections in BRs)
- Strange for absolute reference + ratio of non-strange and strange
- Used for decay constants, bag parameters, form factors...

# Two decades of CKM

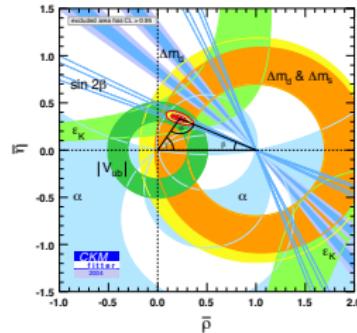
[LEP, KTeV, NA48, Babar, Belle, CDF, DØ, LHCb, CMS...]



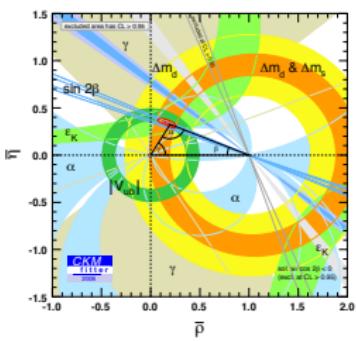
1995



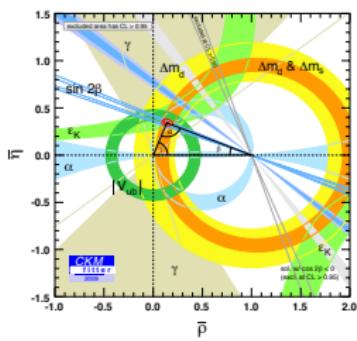
2001



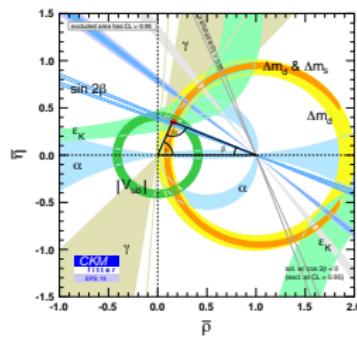
2004



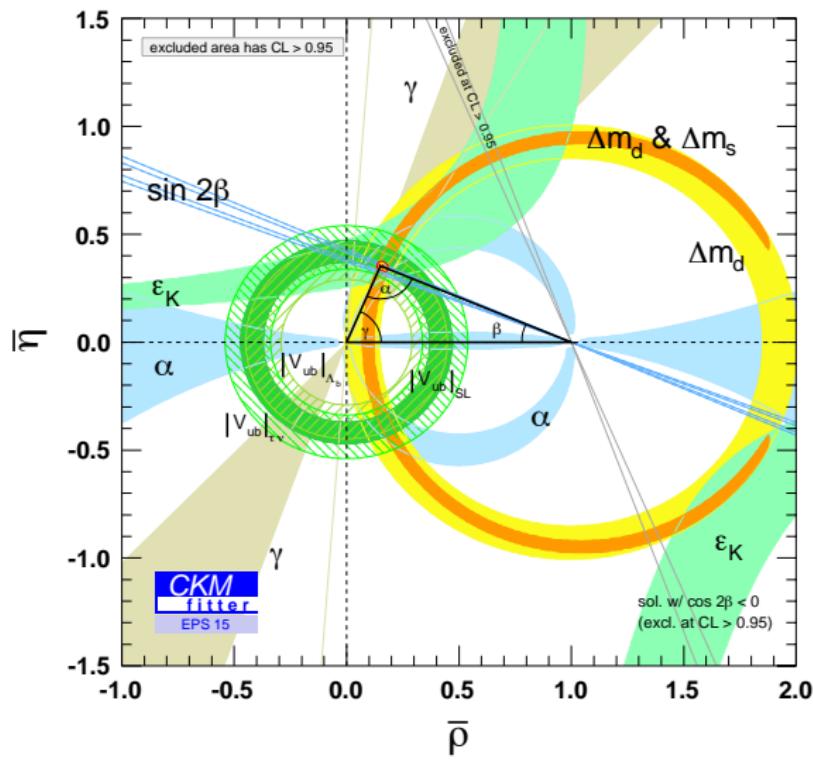
2006



2009



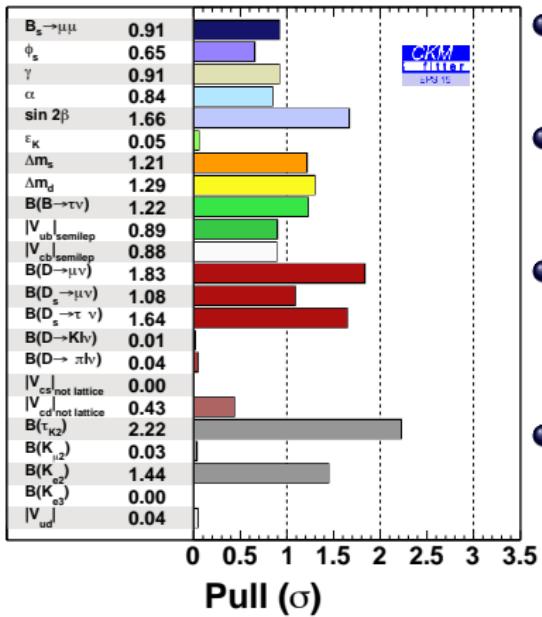
2015



$|V_{ud}|, |V_{us}|$   
 $|V_{cb}|, |V_{ub}|_{SL}$   
 $B \rightarrow \tau\nu$   
 $|V_{ub}/V_{cb}|_{\Lambda_b}$   
 $\Delta m_d, \Delta m_s$   
 $\epsilon_K$   
 $\sin 2\beta$   
 $\alpha$   
 $\gamma$

$$\begin{aligned}
 A &= 0.823^{+0.007}_{-0.014} \\
 \lambda &= 0.2254^{+0.0004}_{-0.0003} \\
 \bar{\rho} &= 0.150^{+0.012}_{-0.006} \\
 \bar{\eta} &= 0.354^{+0.007}_{-0.008} \\
 &\quad (68\% \text{ CL})
 \end{aligned}$$

# Pulls



- Pulls for various observables (included in the fit or not)
- For 1D, pull obs =  $\sqrt{\chi^2_{\text{min; with obs}} - \chi^2_{\text{min; w/o obs}}}$
- If Gaussian errors, uncorrelated, random vars of mean 0 and variance 1
- Here correlations, and some pulls = 0 due to the Rfit model for syst

No indication of significant deviations from CKM picture

# Leptonic and semileptonic decays

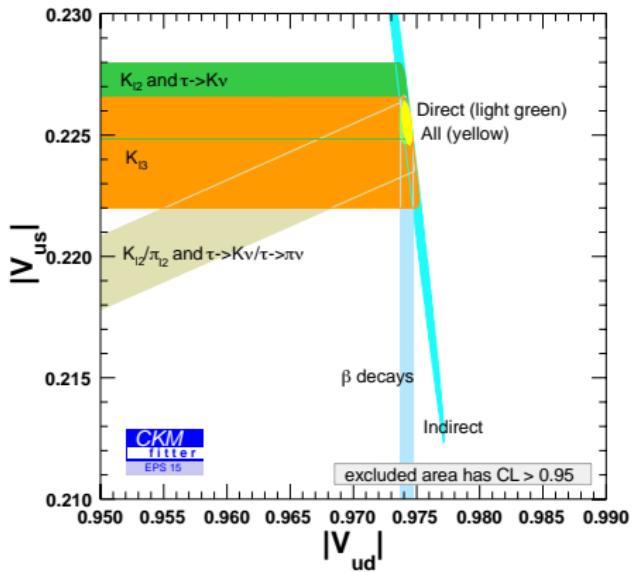
# Leptonic and semileptonic kaon decays

Two type of constraints in the global fit from kaons

- tree-level decays: leptonic and semileptonic decays
- kaon mixing

$ V_{us}  f_+^{K \rightarrow \pi}(0)$	$0.21664 \pm 0.00048$	[PDG]
$Br(K^- \rightarrow e^- \bar{\nu}_e)$	$(1.581 \pm 0.008) \times 10^{-5}$	[PDG]
$Br(K^- \rightarrow \mu^- \bar{\nu}_\mu)$	$0.6355 \pm 0.0011$	[PDG]
$Br(\tau^- \rightarrow K^- \bar{\nu}_\tau)$	$(0.6955 \pm 0.0096) \times 10^{-2}$	[HFAG]
$Br(K^- \rightarrow \mu^- \bar{\nu}_\mu)/Br(\pi^- \rightarrow \mu^- \bar{\nu}_\mu)$	$1.3365 \pm 0.0032$	[PDG]
$Br(\tau^- \rightarrow K^- \bar{\nu}_\tau)/Br(\tau^- \rightarrow \pi^- \bar{\nu}_\tau)$	$(6.43 \pm 0.09) \times 10^{-2}$	[HFAG]
<hr/>		
$f_+^{K \rightarrow \pi}(0)$	$0.9645 \pm 0.0015 \pm 0.0045$	[our average]
$f_K$	$(155.2 \pm 0.2 \pm 0.6) \text{ MeV}$	[our average]
$f_K/f_\pi$	$1.1952 \pm 0.0007 \pm 0.0029$	[our average]

# $|V_{ud}|$ and $|V_{us}|$



- “Direct” (semi- and leptonic) vs “indirect” (other sectors)
- ( $|V_{ud}|$ ,  $|V_{us}|$ ): nuclear  $\beta$  + leptonic  $K$ ,  $\pi$  and  $\tau$  decays
- Same level of accuracy for exp and lattice inputs

	Leptonic	Semilep	
	$ V_{us} $	$ V_{us}/V_{ud} $	$ V_{us} $
Exp	0.1%	0.1%	0.2%
Lattice	0.4%	0.3%	0.5%

- $|V_{ud}|$  from superallowed  $\beta$  decays is 10 times more accurate...

# Radiative corrections for $K \rightarrow e\nu$ , $K \rightarrow \mu\nu$ , $\tau \rightarrow K\nu$

[Marciano-Sirlin, Decker-Finkemeier, Cirigliano-Rosell]

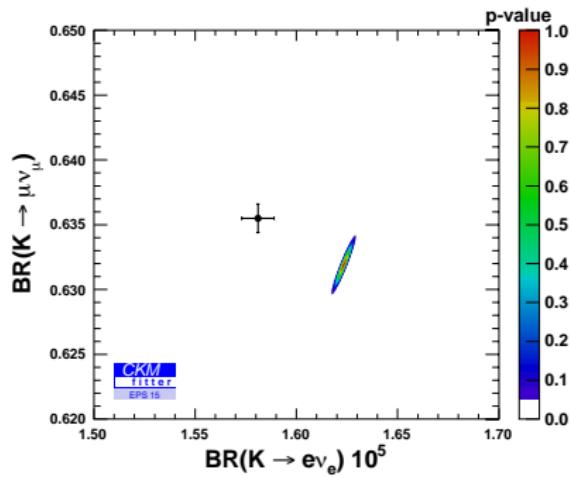
$$B = B_0 \times \text{short - dist. ew corr} \times \text{long - dist. ew corr} \times \text{struct - dep.corr}$$

- Short. dist. expressing  $W$  exchanges in terms of  $G_F$  [universal]
- Long. dist. using a point-like meson [universal]
- Struct. dep. probing the structure of the meson [process-dep.]

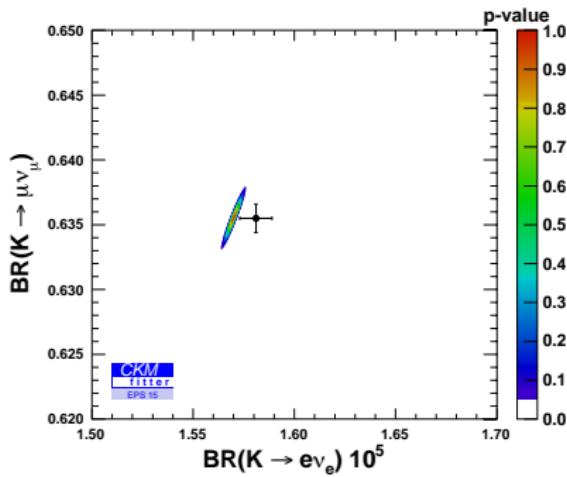
$$\begin{aligned} B(K \rightarrow \ell\nu) &= \frac{G_F^2 |V_{us}|^2}{8\pi} f_K^2 m_K m_\ell^2 \left(1 - \frac{m_\ell^2}{M_K^2}\right)^2 \left(1 + 2\frac{\alpha}{\pi} \log \frac{M_Z}{M_p}\right) \\ &\quad \left(1 + \frac{\alpha}{\pi} F(m_\ell/m_K)\right) (1 + O(\alpha)) \\ B(\tau \rightarrow K\nu_\tau) &= \frac{G_F^2 |V_{us}|^2}{16\pi} f_K^2 m_K m_\ell^2 \left(1 - \frac{m_K^2}{M_\tau^2}\right)^2 \left(1 + 2\frac{\alpha}{\pi} \log \frac{M_Z}{M_\tau}\right) \\ &\quad \left(1 + \frac{\alpha}{\pi} G(m_K/m_\tau)\right) (1 + O(\alpha)) \end{aligned}$$

# The importance of radiative corrections

Comparing the indirect fit results with the measurement for  $Br(K \rightarrow \ell\nu)$   
⇒ Good test of radiative corrections and lattice QCD !



No radiative corrections

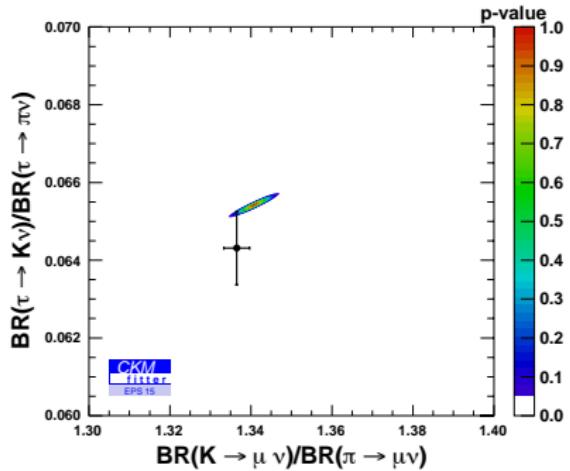


Radiative corrections

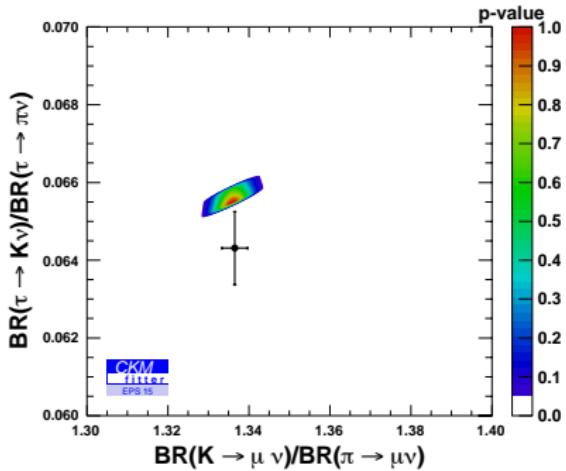
NB: Struct-dep corr not included but much smaller than the two others

# ...but not in all cases

Ratios of  $K$  and  $\pi$  leptonic decays into  $\mu$  or  $\tau$  less sensitivity to the issue (part of radiative corrections cancel + heavy leptons)



No radiative corrections



Radiative corrections

Radiative corrections needed in the global fit to get a decent fit  
 $\chi^2_{\min} = 58$  (naive  $p$ -value 0.002%)  $\rightarrow \chi^2_{\min} = 20$  (naive  $p$ -value 49.3%)

# Kaon mixing

Two type of constraints in the global fit from kaons

- tree-level decays
- kaon mixing:  $\epsilon_K$

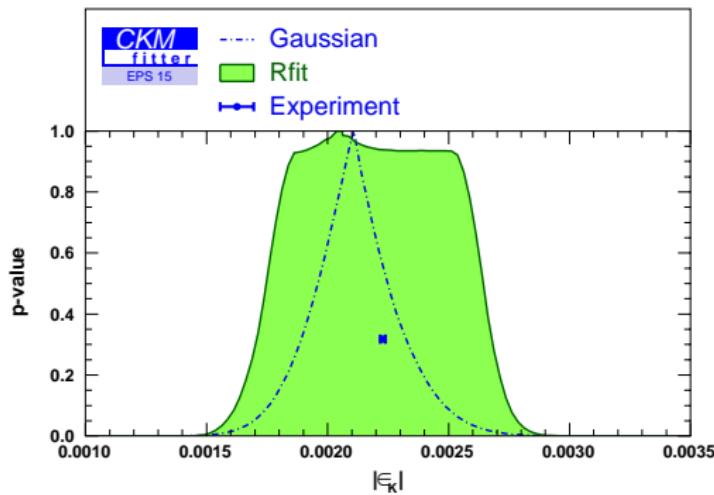
$$|\epsilon_K| = \kappa_\epsilon C_\epsilon \hat{B}_K [\text{Im}[(V_{ts} V_{td}^*)^2] \eta_{tt} S(x_t) + 2\text{Im}[(V_{cs} V_{cd}^* V_{ts} V_{td}^*)] \eta_{ct} S(x_c, x_t) + \text{Im}[(V_{cs} V_{cd}^*)^2] \eta_{cc} S(x_c)]$$

- Inami-Lim  $S_0(x_q = m_X^2/m_W^2)$
- $C_\epsilon$  normalisation
- $\kappa_\epsilon$  correcting factor (determination of  $Q_6$ , higher order OPE)

$ \epsilon_K $	$(2.228 \pm 0.011) \times 10^{-3}$	PDG
$B_K$	$0.7615 \pm 0.0027 \pm 0.0137$	[our average]
$\eta_{cc}$	$1.87 \pm 0 \pm 0.76$	[Brod-Gorbahn]
$\eta_{ct}$	$0.497 \pm 0 \pm 0.047$	[Brod-Gorbahn]
$\eta_{tt}$	$0.5765 \pm 0 \pm 0.0065$	[Nierste]
$\kappa_\epsilon$	$0.940 \pm 0.013 \pm 0.023$	[Buras, Guadagnoli, Isidori]

From time to time, issues with the compatibility of  $\epsilon_K$  with the rest of the fit, related to the fact that  $\epsilon_K$  has a strong dependence on

- $B_K$  : role of theoretical uncertainties
- $|V_{cb}|$ : inclusive, exclusive or average



- Rfit versus Gaussian treatment of theoretical uncertainties
- agreement of prediction with experiment in both cases

# $|V_{cb}|$ from semileptonic $B$ decays

Two ways of getting  $|V_{cb}|$ :

- Inclusive :  $b \rightarrow c\ell\nu + \text{OPE}$  for moments
- Exclusive :  $B \rightarrow D^{(*)}\ell\nu + \text{Form factors}$

[HFAG, Gambino and Schwanda]

[J. A. Bailey et al., Fermilab-MILC]

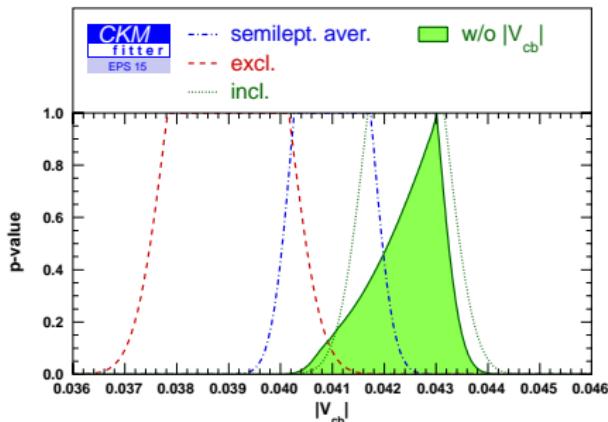
$$|V_{cb}|_{inc} = 42.42 \pm 0.44 \pm 0.74$$

$$|V_{cb}|_{exc} = 38.99 \pm 0.49 \pm 1.17$$

$$|V_{cb}|_{ave} = 41.00 \pm 0.33 \pm 0.74$$

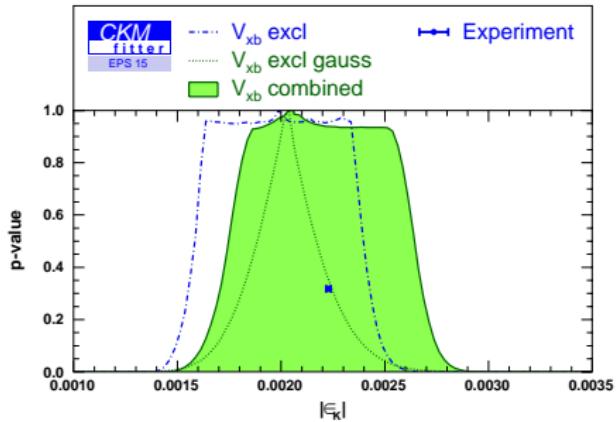
with all values  $\times 10^{-3}$

- HFAG, with theory errors added linearly
- systematics combined using Educated Rfit

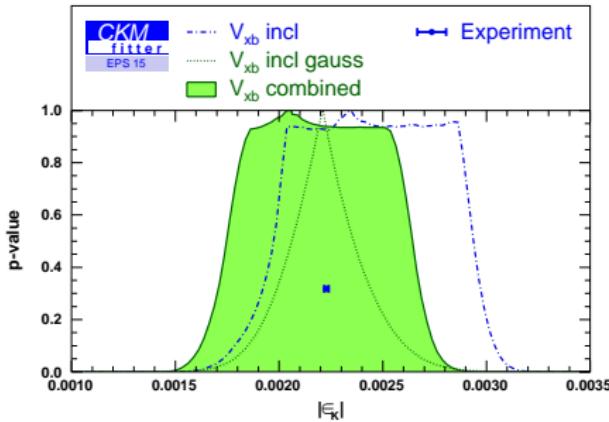


Indirect det. from global fit:  $|V_{cb}|_{fit} = 43.0^{+0.4}_{-1.4}$  (4%)

# Exclusive versus inclusive for $\epsilon_K$



$|V_{xb}|$  exclusive only



$|V_{xb}|$  inclusive only

- Exclusive slightly off compared to inclusive
- But good agreement in all cases

# $\epsilon_K$ at NNLO

QCD short-distance corrections computed up to NNLO

•  $\eta_{tt}$ :  $0.5765 \pm 0.0065 \rightarrow 0.5765 \pm 0.0065$

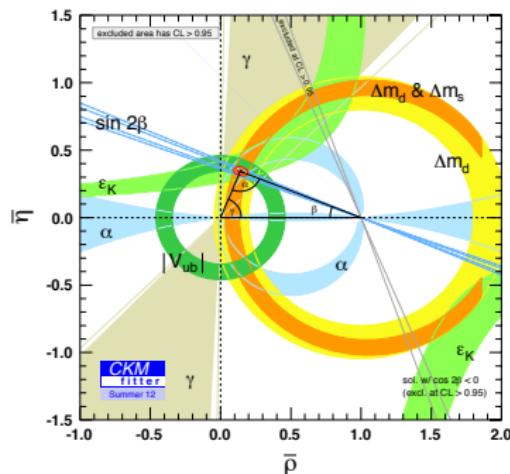
[Buras, Jamin, Weisz]

•  $\eta_{ct}$ :  $0.47 \pm 0.04 \rightarrow 0.496 \pm 0.047$

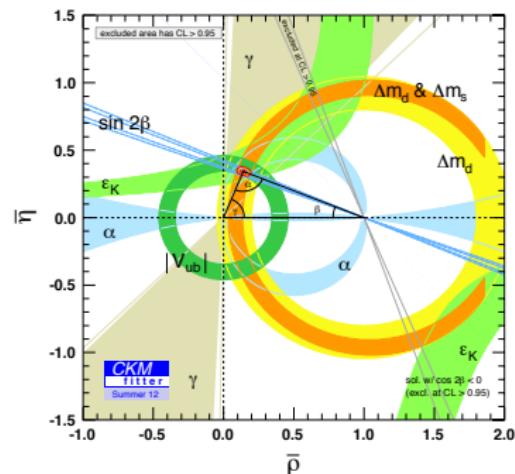
[Brod, Gorbahn]

•  $\eta_{cc}$ :  $(1.46 \pm \delta_{cc}) \left[ 1 - 1.2 \left( \frac{\bar{m}_c}{1.25 \text{ GeV}} \right) \right] \left[ 1 + 52(\alpha_s(M_Z) - 0.118) \right], \delta_{cc} \simeq 0.22$   
 $\rightarrow 1.87 \pm 0.76$

[Brod, Gorbahn]



$\eta$  at NLO (Rfit)



$\eta$  at NNLO (Rfit)

# The role of lattice inputs

- Compare input and fit result (without including the inputs)
- Fit results consistent, but not always competitive in accuracy, with lattice results

	Input		Fit [input not included]	
$f_K$	$155.2 \pm 0.2 \pm 0.6$	(0.4%)	$156.5^{+0.1}_{-0.8}$	(0.3%)
$f_K/f_\pi$	$1.194 \pm 0.001 \pm 0.003$	(0.3%)	$1.191^{+0.006}_{-0.003}$	(0.4%)
$f_+^{K \rightarrow \pi}(0)$	$0.9645 \pm 0.0015 \pm 0.0045$	(0.5%)	$0.9594^{+0.0024}_{-0.0029}$	(0.3%)
$\hat{B}_K$	$0.762 \pm 0.003 \pm 0.014$	(1.9%)	$0.70^{+0.28}_{-0.05}$	(24%)

Similarly for  $\kappa_\epsilon$ , we have

	Input		Fit [input not included]	
$\kappa_\epsilon$	$0.940 \pm 0.013 \pm 0.023$	(2.8%)	$0.875^{+0.317}_{-0.069}$	(22%)

$$K \rightarrow \pi \nu \bar{\nu}$$

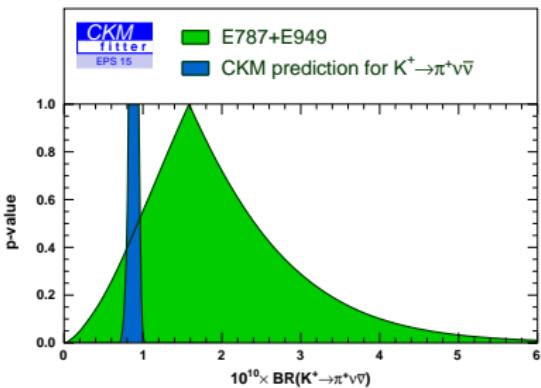
# $K \rightarrow \pi \nu \bar{\nu}$

$$\mathcal{B}[K^+ \rightarrow \pi^+ \nu \bar{\nu}]_{\text{SM}} = \kappa_+ (1 + \Delta_{em}) \left[ \left( \frac{Im \lambda_t}{\lambda^5} X_t \right)^2 + \left( \frac{Re \lambda_c}{\lambda} (P_c + \delta P_{c,u}) + \frac{Re \lambda_t}{\lambda^5} X_t \right)^2 \right]$$

$$\mathcal{B}[K_L \rightarrow \pi^0 \nu \bar{\nu}]_{\text{SM}} = \kappa_L \left( \frac{Im \lambda_t}{\lambda^5} X_t \right)^2,$$

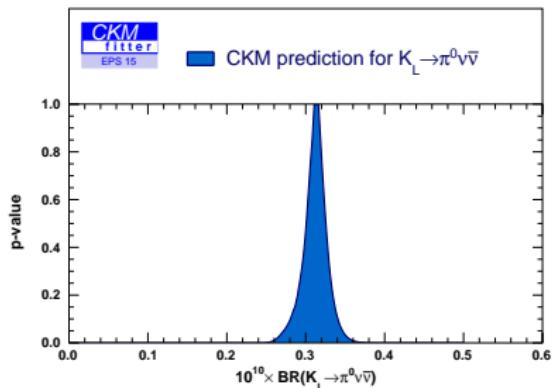
[Buras et al.; Brod, Gorbahn; Mescia, Smith]

- isospin-breaking parameter  $\kappa_{+,L}$  from semileptonic  $K$  decays
- $\Delta_{em}$  electromagnetic correction,
- $X_t$  top-quark contributions,  $P_c$  and  $\delta P_{c,u}$  light-quark contributions



$$Br(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (0.89^{+0.09}_{-0.10}) \times 10^{-10}$$

S. Descotes-Genon (LPT-Orsay)



$$Br(K_L \rightarrow \pi^0 \nu \bar{\nu}) = (0.31^{+0.02}_{-0.02}) \times 10^{-10}$$

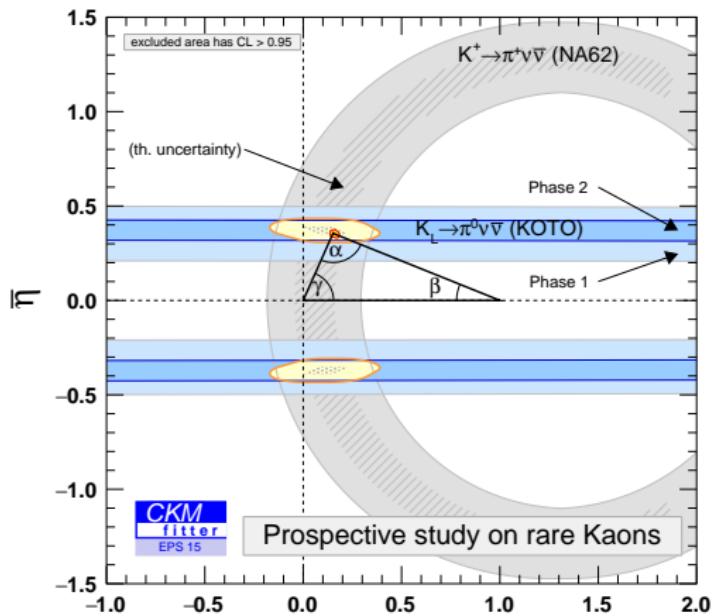
CKMfitter

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# Prospective

- NA62 :  $Br(K^+ \rightarrow \pi^+ \nu \bar{\nu})$  at 10% accuracy
- KOTO : Phase 1  $\sim 3\sigma$  constraint on the branching ratio (SM),  
Phase 2 stage with  $Br(K_L \rightarrow \pi^0 \nu \bar{\nu})$  at 10% accuracy



- NA62: in grey the role played by theoretical uncertainties
- KOTO : phases 1 and 2 indicated

# More information

The screenshot shows the CKMfitter website interface. At the top, there's a navigation bar with links to Home, Plots & Results, Specific Studies, Talks & Writeups, Publications, and CKMfitter Group. Below the navigation bar, a large banner displays the CKMfitter logo. The main content area contains two tables: one titled "CKMfitter global fit results as of Summer 15:" and another titled "UT angles and sides". Both tables provide detailed numerical data with error bars.

Observable	Central $\pm 1\sigma$	$\pm 2\sigma$	$\pm 3\sigma$
A	[0.927 ± 0.0066 ± 0.0136]	[0.823 ± 0.013 -0.027] ± 0.020 -0.036	
$\lambda$	[0.22543 ± 0.00042 ± 0.00031]	[0.22543 ± 0.00075 -0.00064] ± 0.00101 -0.00097	
polar	[0.1504 ± 0.0121 ± 0.0062]	[0.150 ± 0.029 -0.019] ± 0.037 -0.019	
rbar	[0.3540 ± 0.0069 ± 0.0076]	[0.354 ± 0.016 -0.019] ± 0.028 -0.027	
$J [10^{-3}]$	[3.140 ± 0.069 -0.084]	[3.14 ± 0.16 -0.21] ± 0.26 -0.31	

Observable	Central $\pm 1\sigma$	$\pm 2\sigma$	$\pm 3\sigma$
sin 2 $\alpha$	-0.013 ± 0.034 -0.071	-0.013 ± 0.069 -0.168	-0.01 ± 0.11 -0.22
sin 2 $\alpha$ (meas. not in the fit)	-0.024 ± 0.038 -0.134	0.024 ± 0.075 -0.181	-0.02 ± 0.11 -0.23
sin 2 $\beta$	0.710 ± 0.011 -0.011	0.710 ± 0.025 -0.021	0.710 ± 0.039 -0.032
sin 2 $\beta$ (meas. not in the fit)	0.748 ± 0.030 -0.032	0.748 ± 0.056 -0.050	0.748 ± 0.071 -0.065
$\alpha$ [deg]	90.4 ± 2.0 -1.0	90.4 ± 4.8 -2.0	90.4 ± 6.2 -3.1

More on <http://ckmfitter.in2p3.fr>

- J. Charles, Theory  
O. Deschamps, LHCb  
SDG, Theory  
H. Lacker, ATLAS/BaBar  
A. Menzel, ATLAS  
S. Monteil, LHCb  
V. Niess, LHCb  
J. Ocariz, ATLAS/BaBar  
J. Orloff, Theory  
A. Perez, Babar  
W. Qian, LHCb  
V. Tisserand, BaBar/LHCb  
K. Trabelsi, Belle/LHCb  
P. Urquijo, Belle/Belle II  
L. Vale Silva, Theory

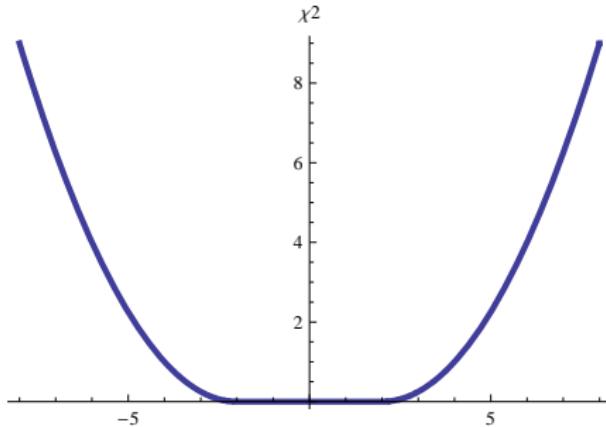
# Spares

# Rfit scheme

CKM  
fitter

: Treatment of systematics within the Rfit scheme

- modify likelihood  $\mathcal{L} = \exp(-\chi^2/2)$  to get a  $\chi^2$  with flat bottom (syst) and parabolic walls (stat)
- all values within range of syst treated on the same footing



# $|V_{ub}|$ from semileptonic $B$ decays

Two ways of getting  $|V_{ub}|$ :

- Inclusive :  $b \rightarrow u\ell\nu$  + Operator Product Expansion [HFAG BLNP]
- Exclusive :  $B \rightarrow \pi\ell\nu$  + Form factors [J. A. Bailey et al., Fermilab-MILC]

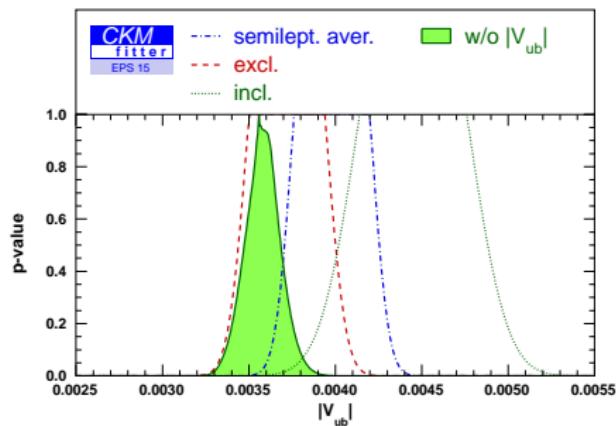
$$|V_{ub}|_{inc} = 4.45 \pm 0.18 \pm 0.31$$

$$|V_{ub}|_{exc} = 3.72 \pm 0.09 \pm 0.22$$

$$|V_{ub}|_{ave} = 4.01 \pm 0.08 \pm 0.22$$

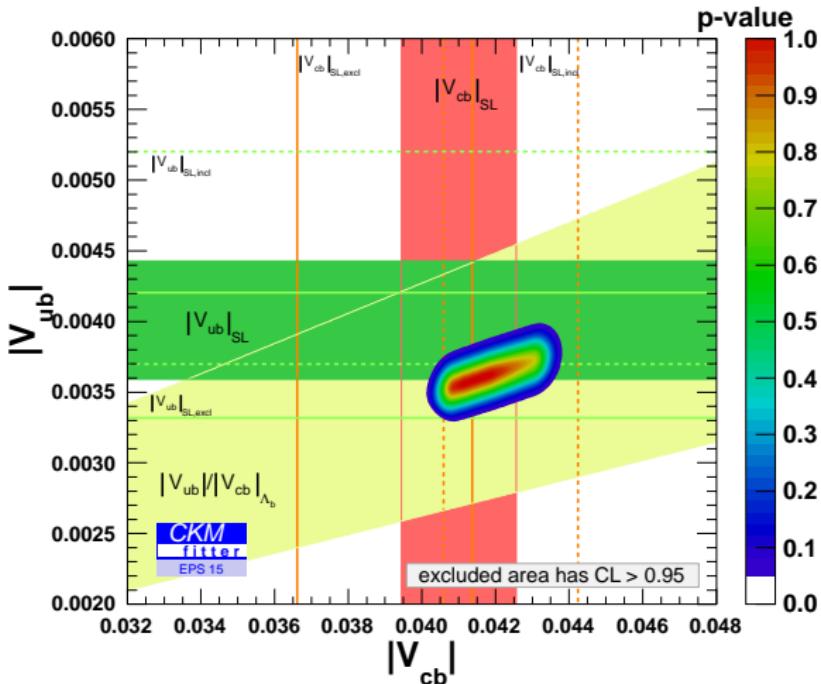
with all values  $\times 10^{-3}$

- HFAG, with theory errors added linearly
- systematics combined using Educated Rfit



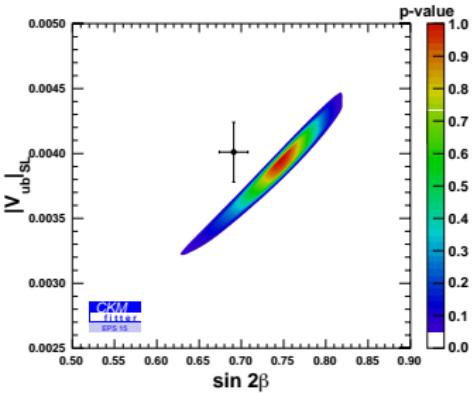
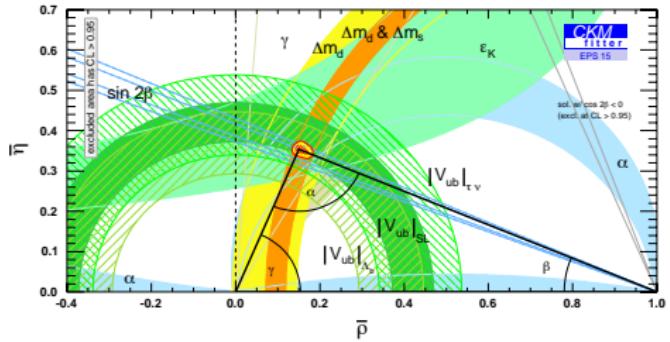
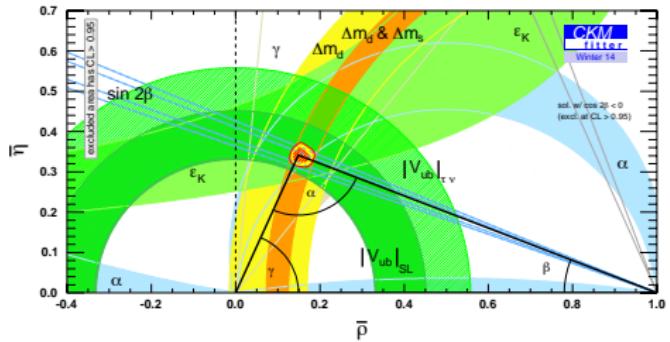
Indirect det. from global fit:  $|V_{ub}|_{fit} = 3.57^{+0.15}_{-0.14}$  (4%)

$|V_{ub}|, |V_{cb}|$



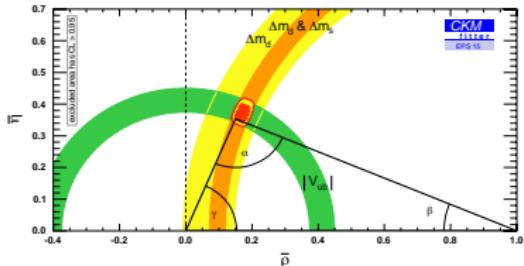
- Information on  $|V_{ub}|$  from  $Br(B \rightarrow \tau\nu)$
- New LHCb result on  $|V_{ub}/V_{cb}|$  from  $\Gamma(\Lambda_b \rightarrow p\mu\nu)/\Gamma(\Lambda_b \rightarrow \Lambda_c\mu\nu)$  at high  $q^2$   
[Detmold, Lehner and Meinel]
- Global fit favours exclusive  $|V_{ub}|_{SL}$  but inclusive  $|V_{cb}|_{SL}$

# From 2014 to 2015

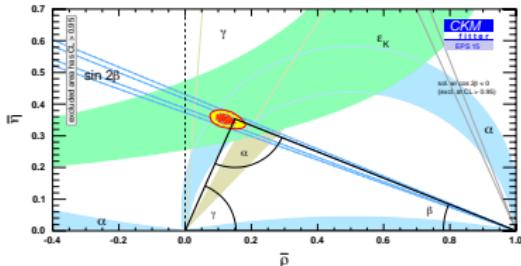


- Increase in the average used as input for  $|V_{ub}|_{SL}$
- slight tension between  $|V_{ub}|_{SL}$  and  $\sin(2\beta)$  ( $1.5 \sigma$  for 2D hyp)
- reducing uncertainty on CKM params (mostly  $\bar{\eta}$ )

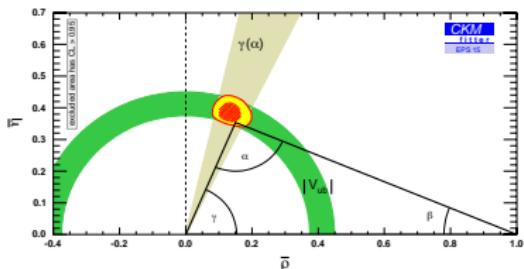
# Consistency of the KM mechanism



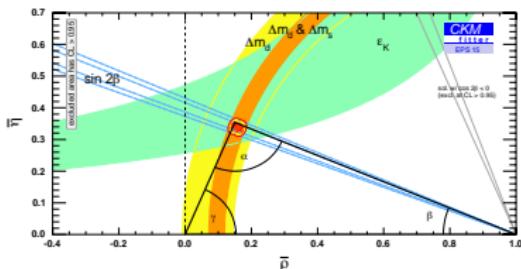
$CP$ -allowed only



$CP$ -violating only



Tree only



Loop only

Validity of Kobayashi-Maskawa picture of  $CP$  violation