



Shaping the Universe:
Framework and Footprints of
Cosmological Phase Transitions
January 27 – 30, 2026

 <https://indico.mitp.uni-mainz.de/event/466/>



Gravitational wave signatures of dark sector portal leptogenesis

Indrajit Saha

Indian Institute of Technology Guwahati, Assam, India

Based on : 2504.14671

In collaboration with D. Borah and D. Mahanta



Outline:

- Motivation
- Scotogenic model (Extended)
- First order Phase Transition (FOPT)
- Leptogenesis
- Stochastic Gravitational Waves (GW)
- Dark matter
- Conclusion

Motivation

- The Observed baryon asymmetry of the Universe as baryon to photon ratio is

$$\eta_B = \frac{n_B - n_{\bar{B}}}{n_\gamma} \simeq 6.2 \times 10^{-10}$$

Planck 2018 data, arXiv:1807.06209

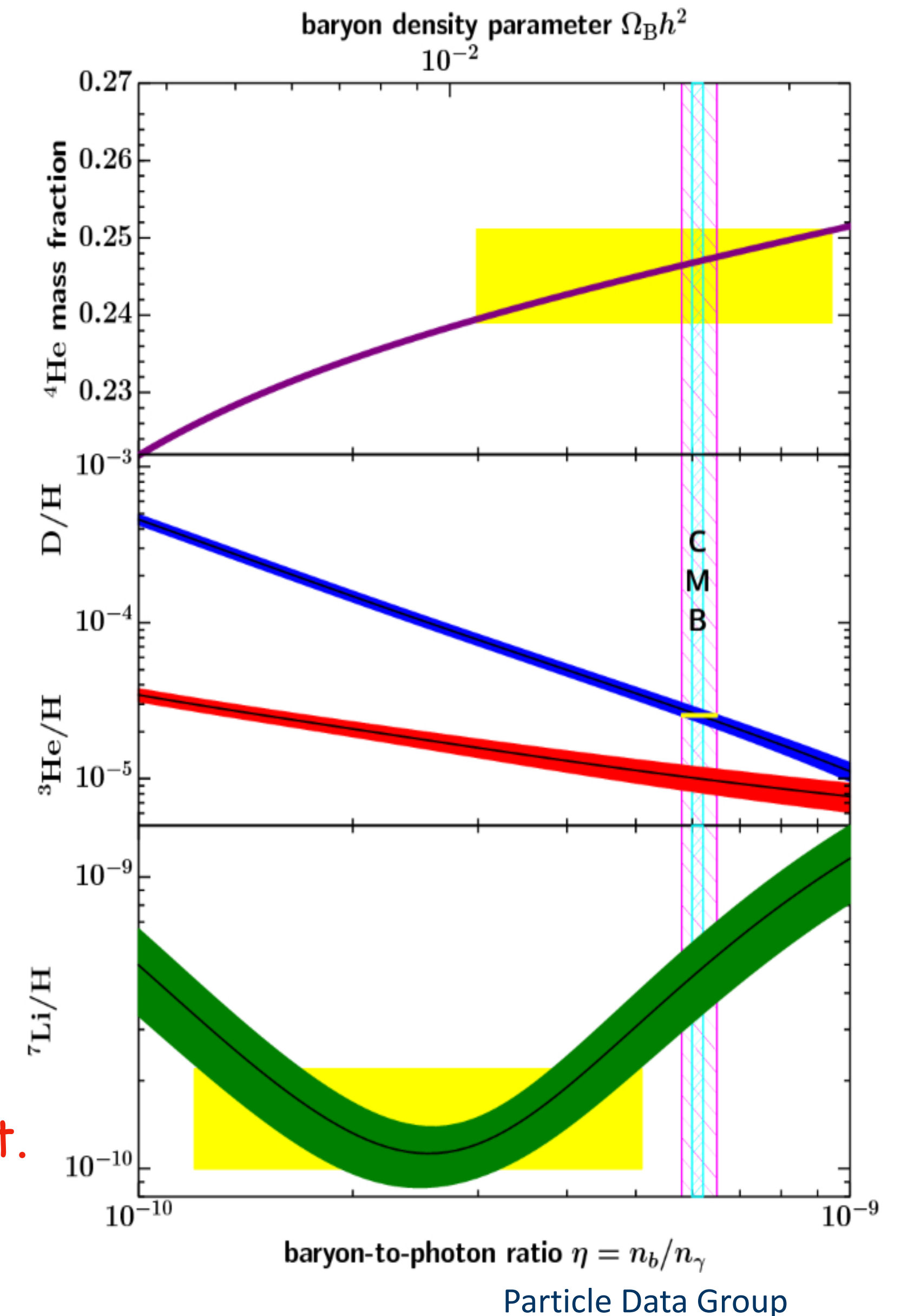
Baryogenesis

Sakharov's
Conditions

Sakharov 1967

- Baryon number violation
- C & CP violation
- Departure from thermal equilibrium

Standard Model unable to satisfy above conditions in required amount.



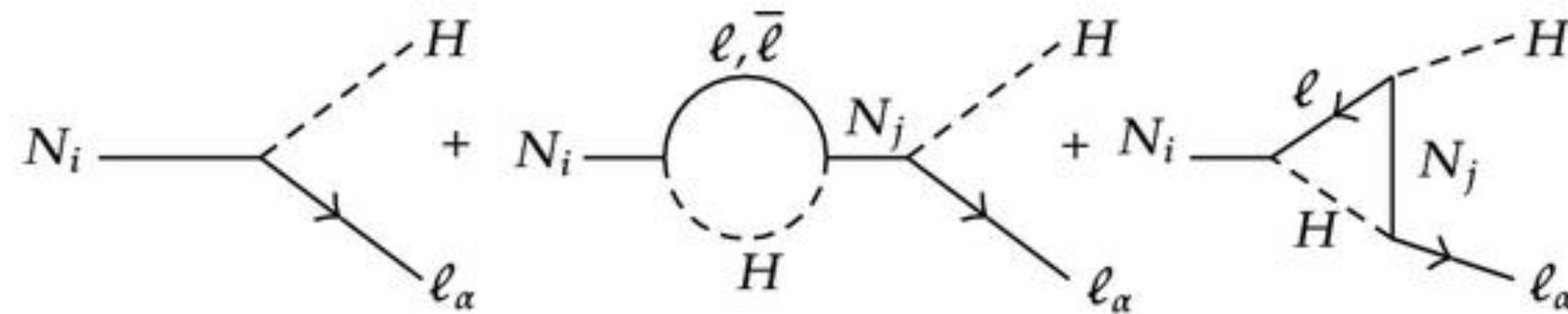
Baryogenesis via Leptogenesis

- ❖ Right-handed neutrino decays out of equilibrium (Fukugita & Yanagida 1986)

$$Y_{ij} \bar{L}_i \tilde{H} N_j + \frac{1}{2} M_{ij} N_i N_j$$

- ❖ CP violation due to phases in Yukawa couplings Y , leads to a lepton asymmetry

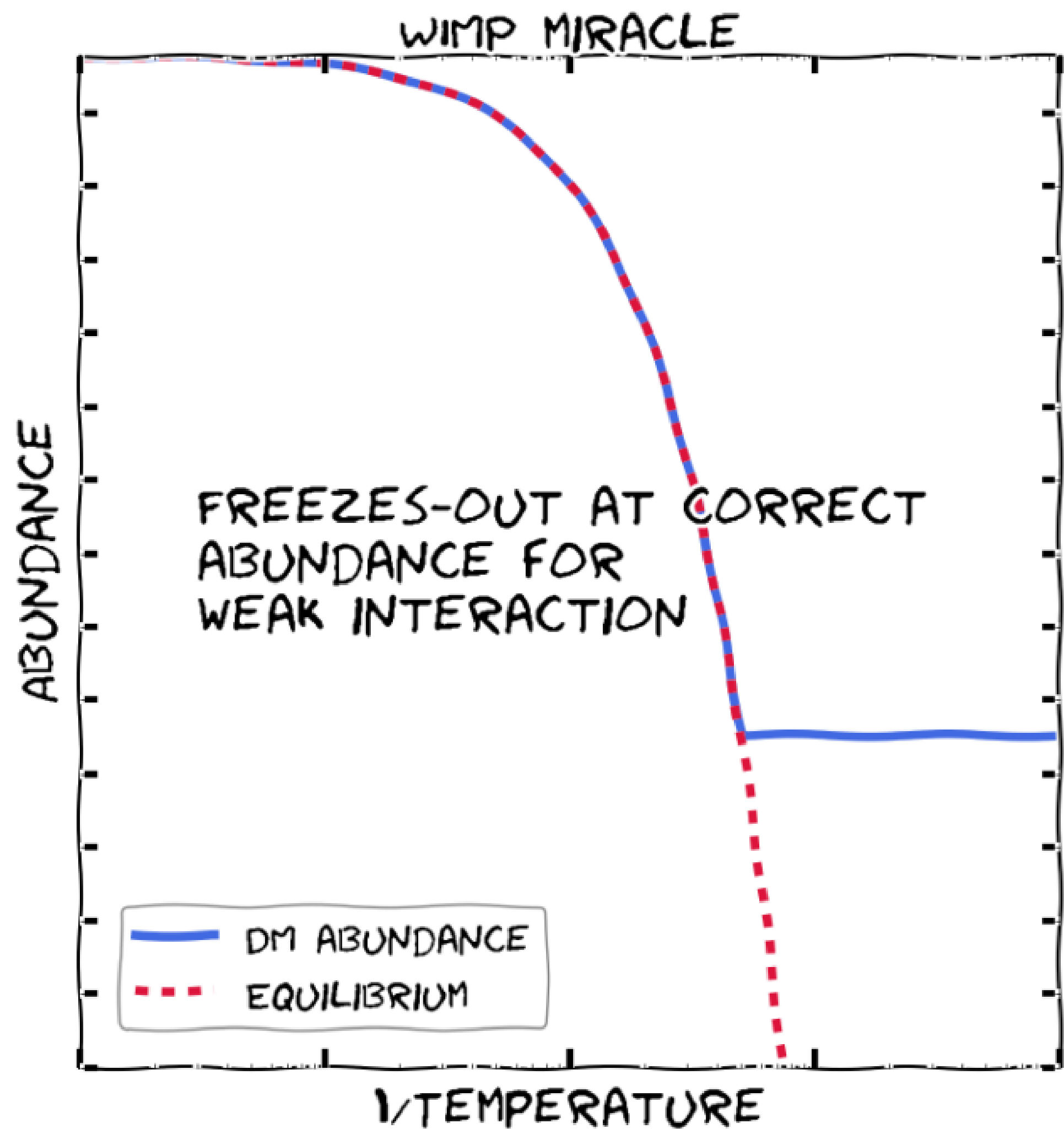
$$\epsilon_{\alpha\alpha} \equiv \frac{\Gamma(N_1 \rightarrow \phi l_\alpha) - \Gamma(N_1 \rightarrow \bar{\phi} \bar{l}_\alpha)}{\Gamma(N_1 \rightarrow \phi l) + \Gamma(N_1 \rightarrow \bar{\phi} \bar{l})}$$



- ❖ The frozen-out lepton asymmetry is converted into baryon asymmetry by electroweak sphalerons

$$\eta_B = \frac{a_{\text{sph}}}{f} \epsilon_1 \kappa$$

We know it exist



https://andrewfowlie.github.io/talks/melbourne_dm.pdf



$$\frac{dn_X}{dt} = -3Hn_X - \langle \sigma_{\text{ann}} v \rangle (n_X^2 - n_{\text{eq}}^2)$$

Baryon-DM coincidence: $\Omega_{DM} \approx 5\Omega_B$

They can have a common origin !

First order Phase transition:

Leptogenesis

Dark Matter

Common origin

First order
Phase
transition

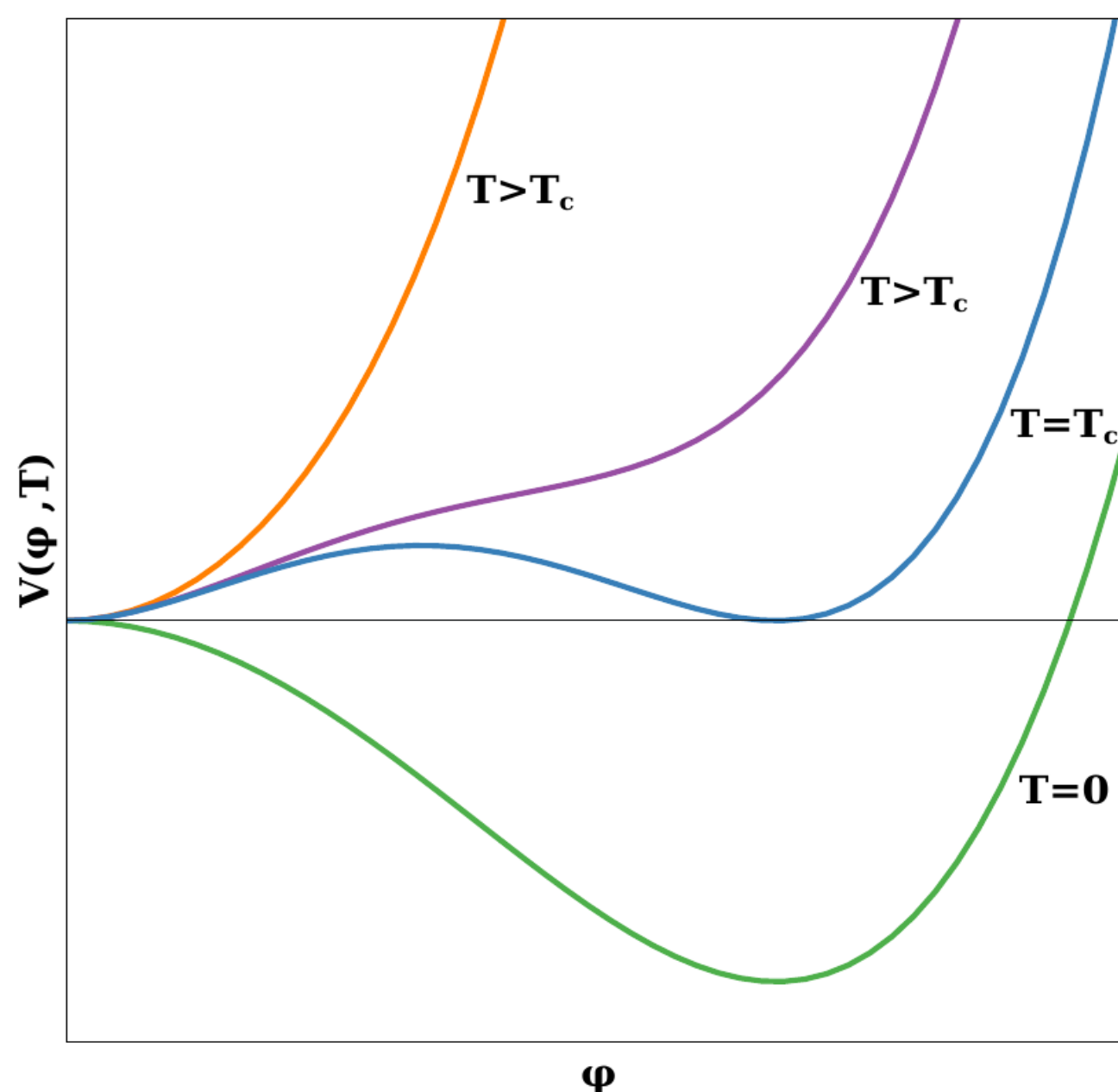
Gravitational waves



LIGO



IPTA



- ⊗ As the Universe cools down, the scalar field went from **symmetric** phase to **broken** phase.
- ⊗ The vacuum expectation value (vev) of the scalar field is the **order parameter**.
- ⊗ In first order phase transition (FOPT), the vev of the scalar field changes **discontinuously**.
- ⊗ The minima become degenerate at **critical temperature**.

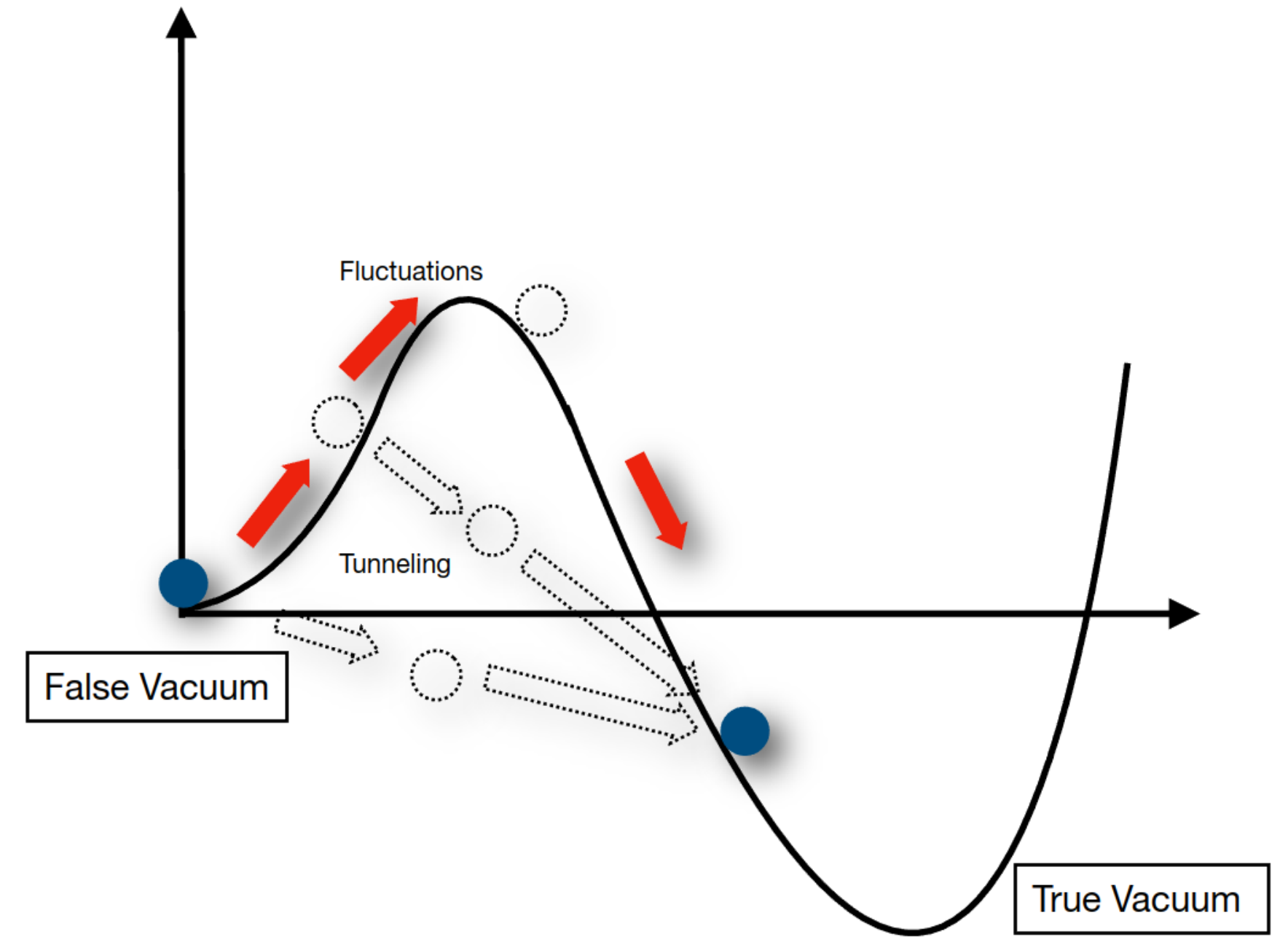
The rate of tunneling per unit volume:

$$\Gamma(T) = \mathcal{A}(T)e^{-S_3(T)/T},$$

$$S_3 = \int_0^\infty dr 4\pi r^2 \left[\frac{1}{2} \left(\frac{d\phi}{dr} \right)^2 + V_{\text{tot}}(\phi, T) \right].$$

$$\Gamma(T_n) = \mathbf{H}^4(T_n).$$

Linde, Phys.Lett.B 100 (1981)



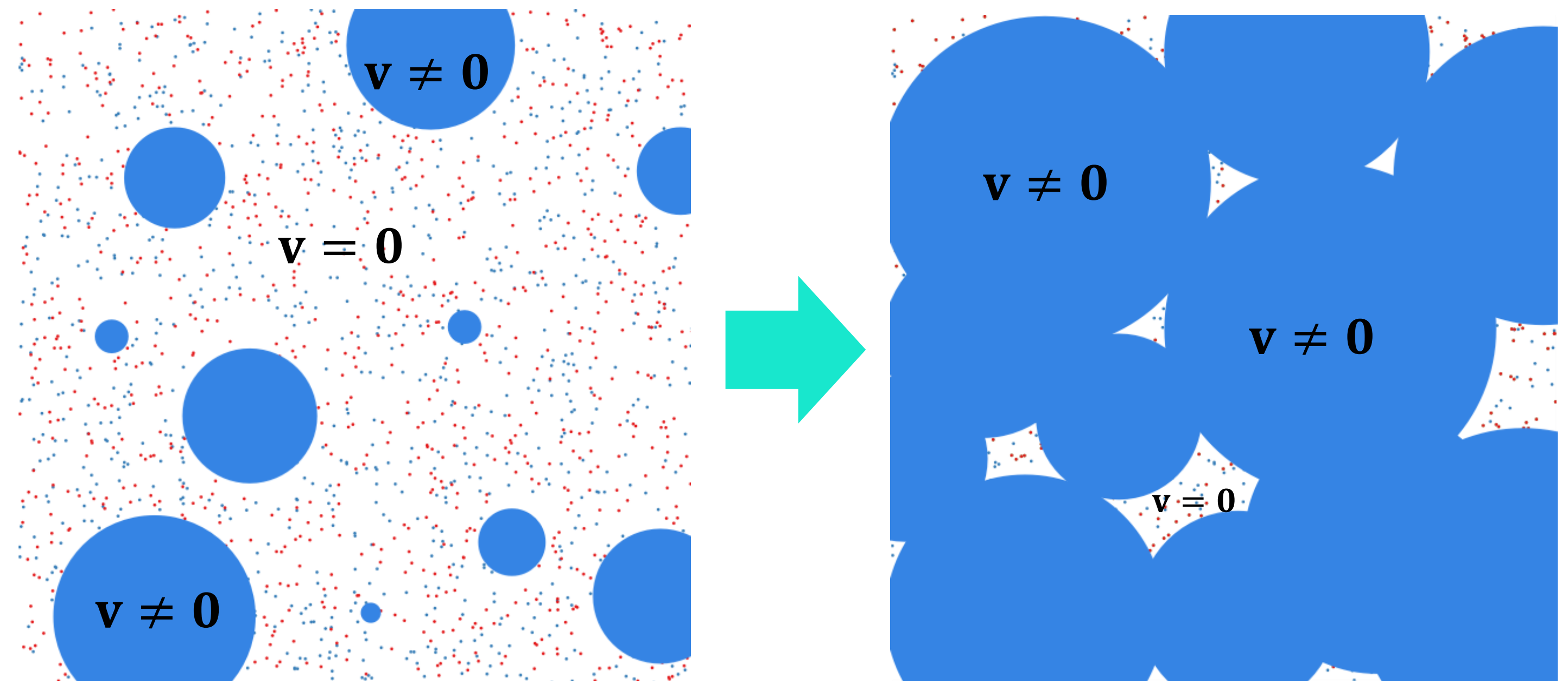
Vacuum energy released

$$\alpha_* = \frac{\epsilon_*}{\rho_{\text{rad}}},$$

$$\epsilon_* = \left[\Delta V_{\text{tot}} - \frac{T}{4} \frac{\partial \Delta V_{\text{tot}}}{\partial T} \right]_{T=T_*},$$

Duration of the FOPT

$$\frac{\beta}{\mathbf{H}(T)} \simeq T \frac{d}{dT} \left(\frac{S_3}{T} \right)$$



Scotogenic Model (Extended):

	L	Φ	N_1	ψ	η	χ
$SU(2)$	2	2	1	1	2	1
$U(1)_Y$	$-\frac{1}{2}$	$\frac{1}{2}$	0	0	$\frac{1}{2}$	0
Z_2	1	1	1	-1	-1	-1

Leptonic Yukawa interaction:

$$-\mathcal{L}_Y \supset y_N \bar{\ell} \tilde{\Phi} N_1 + y_\psi \bar{\ell} \tilde{\eta} \psi + y_1 \bar{N}_1^c \psi \chi + \frac{1}{2} M_{N_1} \bar{N}_1^c N_1 + \frac{1}{2} M_\psi \bar{\psi}^c \psi + \text{h.c.}$$

Scalar Potential:

$$V_{\text{tree}} = \mu_\Phi^2 |\Phi|^2 + \mu_\eta^2 |\eta|^2 + \lambda_1 |\Phi|^4 + \lambda_2 |\eta|^4 + \lambda_3 |\Phi|^2 |\eta|^2 + \lambda_4 |\eta^\dagger \Phi|^2 + \lambda_5 [(\eta^\dagger \Phi)^2 + \text{h.c.}] + \frac{\mu_\chi^2}{2} \chi^2 + \lambda_7 \chi^4 + \lambda_8 \chi^2 |\Phi|^2 + \lambda_9 \chi^2 |\eta|^2 + (\mu_1 \chi \Phi^\dagger \eta + \mu_1^* \chi \eta^\dagger \Phi).$$

Scoto-Seesaw:

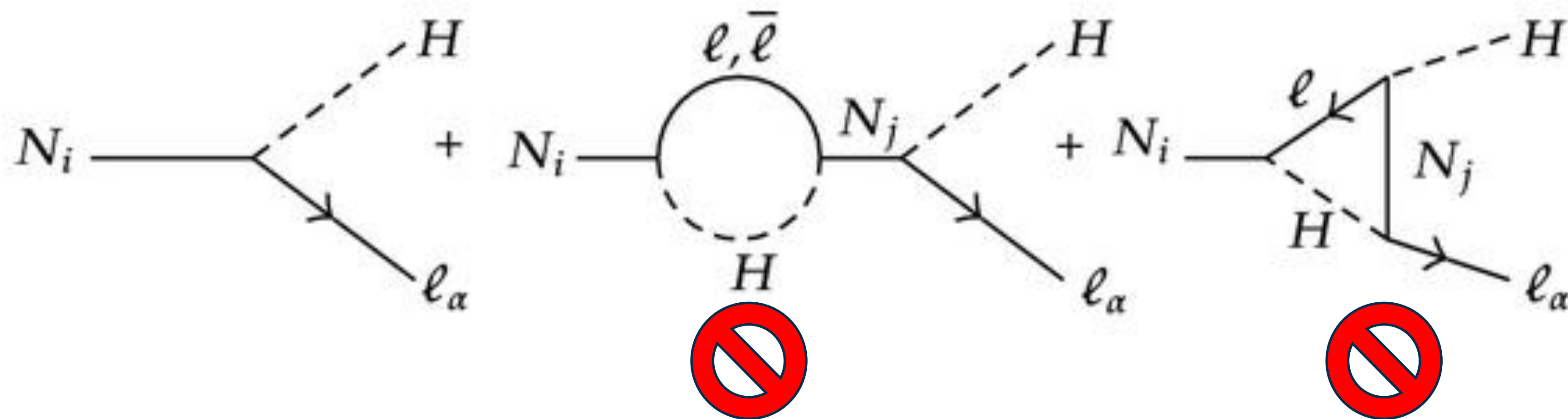
$$\mathcal{Y} = \sqrt{X_M^{-1}} R \sqrt{m_\nu^{\text{diag}}} U^\dagger$$

 Neutrino mass

$$\Phi = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ \phi + v \end{pmatrix}, \eta = \begin{pmatrix} \eta^\pm \\ \frac{(H+iA)}{\sqrt{2}} \end{pmatrix}$$

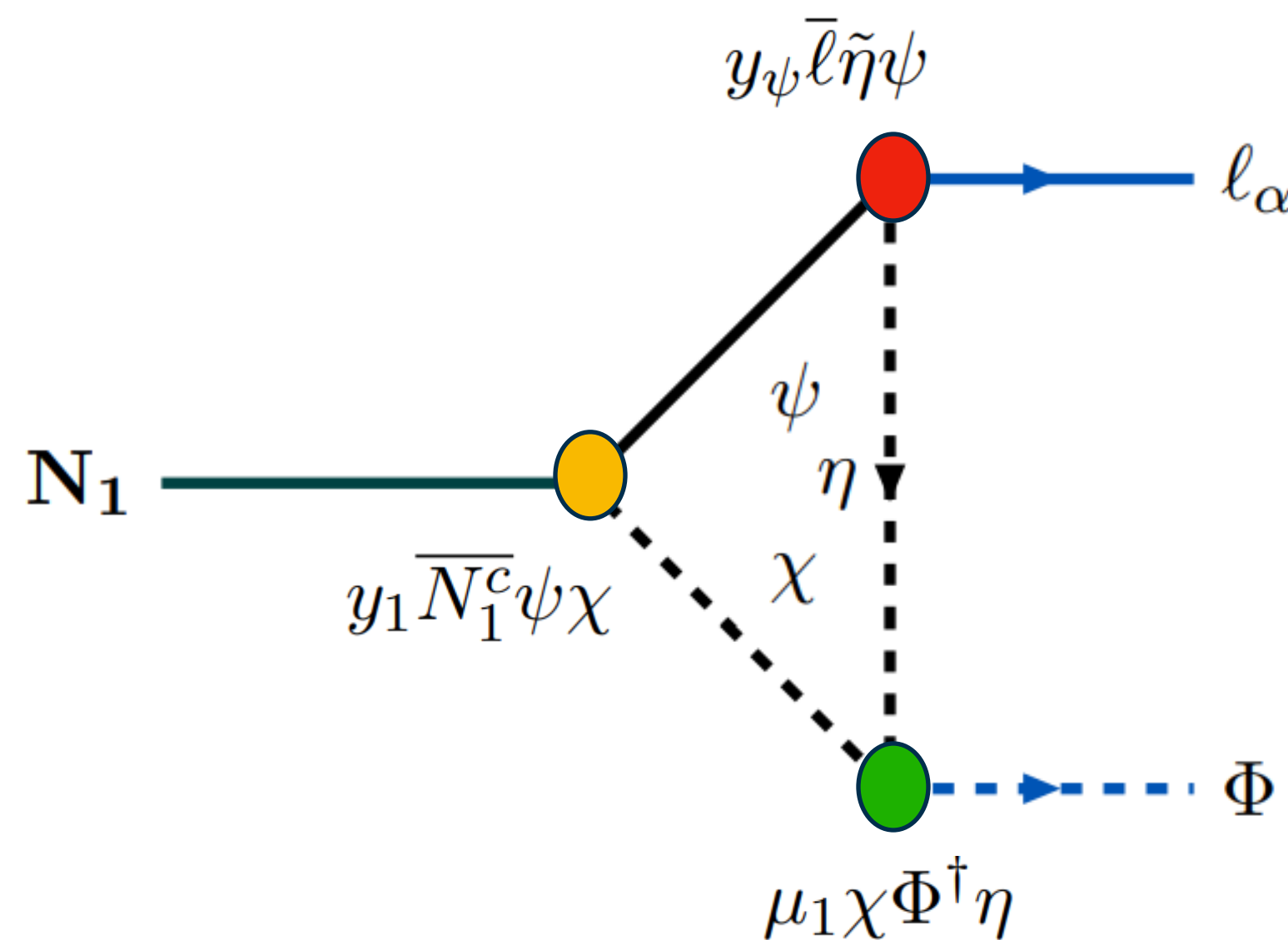
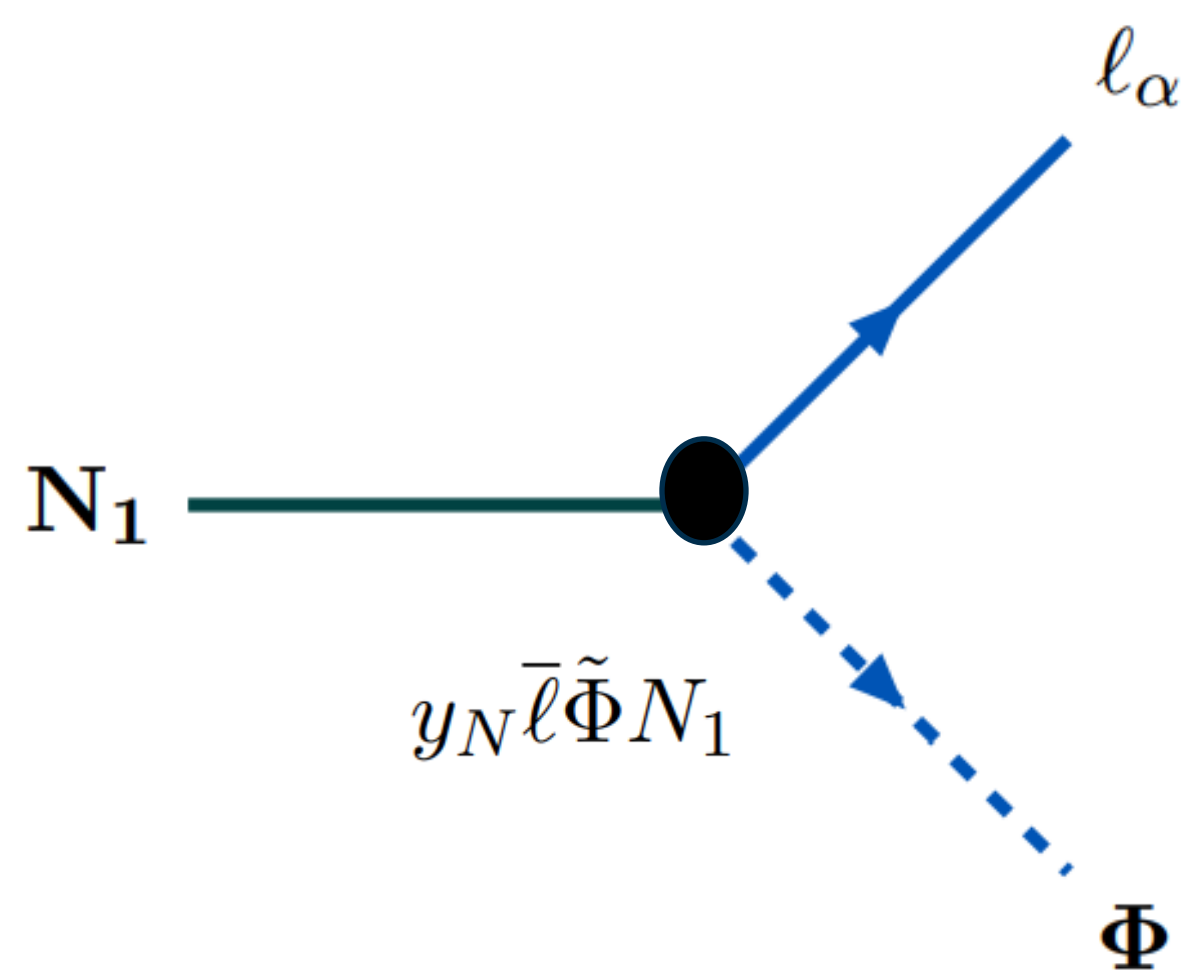
$$X_M = \begin{pmatrix} -X_1 & 0 \\ 0 & X_0 \end{pmatrix}, X_1 = \frac{M_\psi}{32\pi^2} \left(\cos^2 \theta F_1(\eta_1) + \sin^2 \theta F_1(\eta_2) - F_1(A) \right), X_0 = \frac{v^2}{2M_{N_1}}$$

Leptogenesis



No asymmetry

Scalar portal Leptogenesis



Non-Zero asymmetry

H or Φ , Higgs
 N_j or ψ , RHN

First Order Phase Transition:

$$V_{\text{tot}} = V_{\text{tree}} + V_{\text{CW}} + V_{\text{th}},$$

$$V_{\text{CW}} = \sum_i (-)^{n_f} \frac{n_i}{64\pi^2} m_i^4(\phi) \left(\log \left(\frac{m_i^2(\phi)}{\mu^2} \right) - \frac{3}{2} \right),$$

$$V_{\text{th}} = \sum_i \left(\frac{n_{B_i}}{2\pi^2} T^4 J_B \left[\frac{m_{B_i}}{T} \right] - \frac{n_{F_i}}{2\pi^2} T^4 J_F \left[\frac{m_{F_i}}{T} \right] \right),$$

Coleman & Weinberg, PRD 7 (1973), Dolan & Jackiw, PRD 9 (1974)

Field dependent masses: $m_{\eta^\pm}^2(\phi) = \mu_\eta^2 + \frac{\lambda_3}{2}\phi^2$ ($n_{\eta^\pm} = 2, C_{\eta^\pm} = \frac{3}{2}$), $m_A^2(\phi) = \mu_\eta^2 + \frac{\lambda_3 + \lambda_4 - 2\lambda_5}{2}\phi^2$ ($n_A = 1, C_A = \frac{3}{2}$),

$m_W^2(\phi) = \frac{g_2^2}{4}\phi^2$ ($n_W = 6, C_W = \frac{5}{6}$), $m_Z^2(\phi) = \frac{g_1^2 + g_2^2}{4}\phi^2$ ($n_Z = 3, C_Z = \frac{5}{6}$),

$m_t^2(\phi) = \frac{y_t^2}{2}\phi^2$ ($n_t = 12, C_t = \frac{3}{2}$), $m_b^2(\phi) = \frac{y_b^2}{2}\phi^2$ ($n_b = 12, C_b = \frac{3}{2}$),

$m_{\eta_1}^2(\phi) = \frac{1}{2}(\mu_\chi^2 + \mu_\eta^2 + (\lambda_8 + \lambda_H/2)\phi^2 - \sqrt{\{\mu_\chi^2 - \mu_\eta^2 + (\lambda_8 - \lambda_H/2)\phi^2\}^2 + |\mu_1|^2\phi^2})$ ($n_{\eta_1} = 1, C_{\eta_1} = \frac{3}{2}$),

$m_{\eta_2}^2(\phi) = \frac{1}{2}(\mu_\chi^2 + \mu_\eta^2 + (\lambda_8 + \lambda_H/2)\phi^2 + \sqrt{\{\mu_\chi^2 - \mu_\eta^2 + (\lambda_8 - \lambda_H/2)\phi^2\}^2 + |\mu_1|^2\phi^2})$ ($n_{\eta_2} = 1, C_{\eta_2} = \frac{3}{2}$).

$$m_i^2(\phi, T) = m_i^2(\phi) + \Pi_S(T), \quad m_{\eta_2}^2(\phi, T) = m_{\eta_2}^2(\phi) + \Pi_\chi(T)$$

Finite temperature effect on masses:

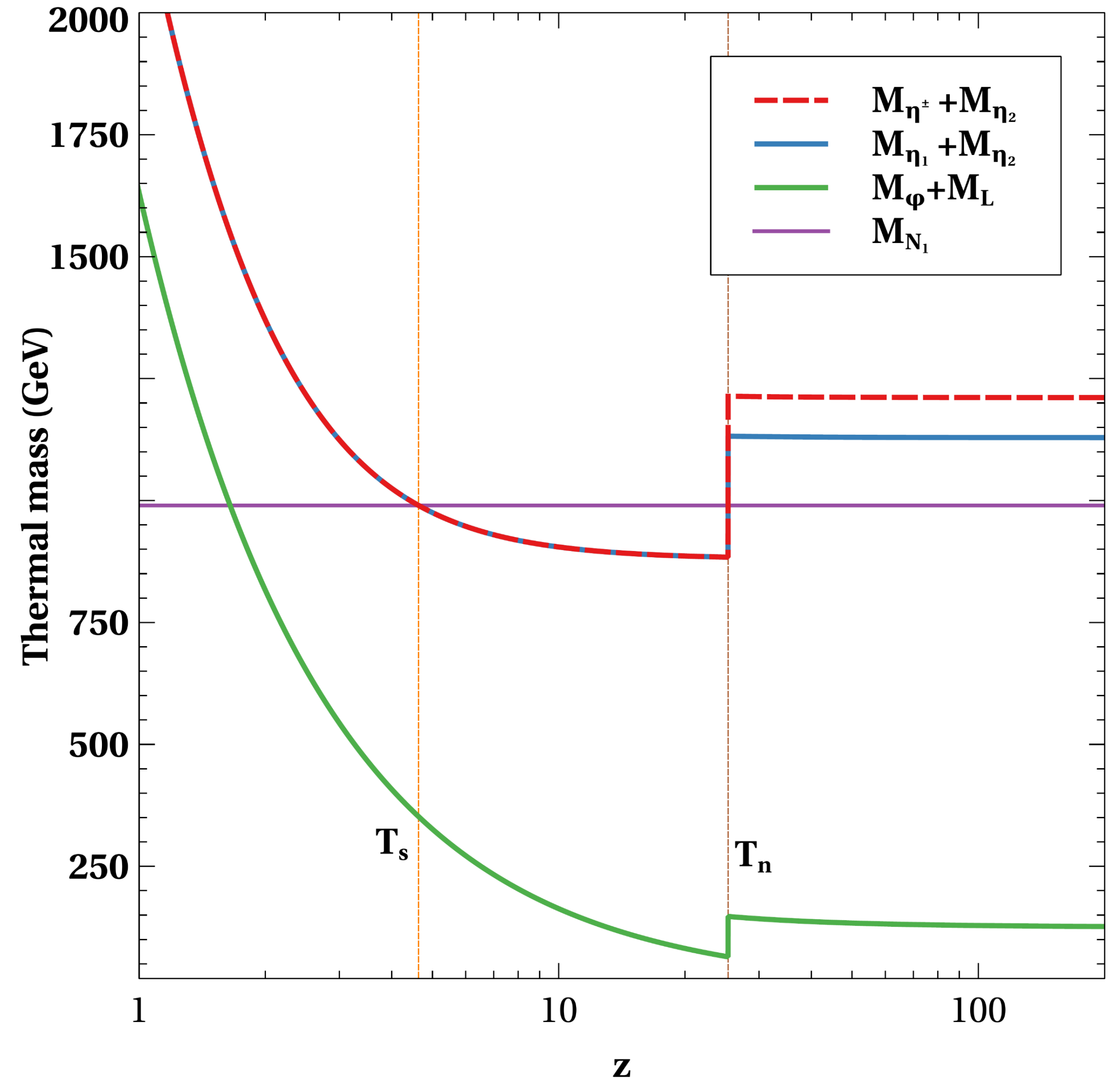
N_1 can decay if

$$M_{\Phi}(T) + M_L(T) < M_{N_1}$$

But, N_1 decay can generate asymmetry if η and χ are on-shell

$$M_{\eta}(T) + M_{\chi}(T) < M_{N_1}$$

Mass of ψ is higher than mass of N_1



Boltzmann equation:

$$\begin{aligned}
\frac{dY_{N_1}}{dz} = & -D_N \left(Y_{N_1} - Y_{N_1}^{\text{eq}} \right) - \frac{s}{H(z)z} \left(Y_{N_1}^2 - \left(Y_{N_1}^{\text{eq}} \right)^2 \right) \left[\langle \sigma v \rangle_{N_1 N_1 \rightarrow \chi \chi} + \langle \sigma v \rangle_{N_1 N_1 \rightarrow \Phi \Phi^\dagger} \right. \\
& \left. + \langle \sigma v \rangle_{N_1 N_1 \rightarrow l_\alpha \bar{l}_\beta} \right] - \frac{s}{H(z)z} \left(Y_{N_1} - Y_{N_1}^{\text{eq}} \right) \left[2Y_l^{\text{eq}} \langle \sigma v \rangle_{\bar{l} N_1 \rightarrow \bar{q} t} + 4Y_t^{\text{eq}} \langle \sigma v \rangle_{N_1 t \rightarrow \bar{l} q} \right. \\
& \left. + 2Y_\chi^{\text{eq}} \langle \sigma v \rangle_{N_1 \chi \rightarrow \bar{l} \eta^\dagger} + 2Y_\Phi^{\text{eq}} \langle \sigma v \rangle_{N_1 \Phi \rightarrow l_\alpha V_\mu} + 2y_\psi^{\text{eq}} \langle \sigma v \rangle_{N_1 \psi \rightarrow \Phi \eta^\dagger} \right], \quad (3.3)
\end{aligned}$$

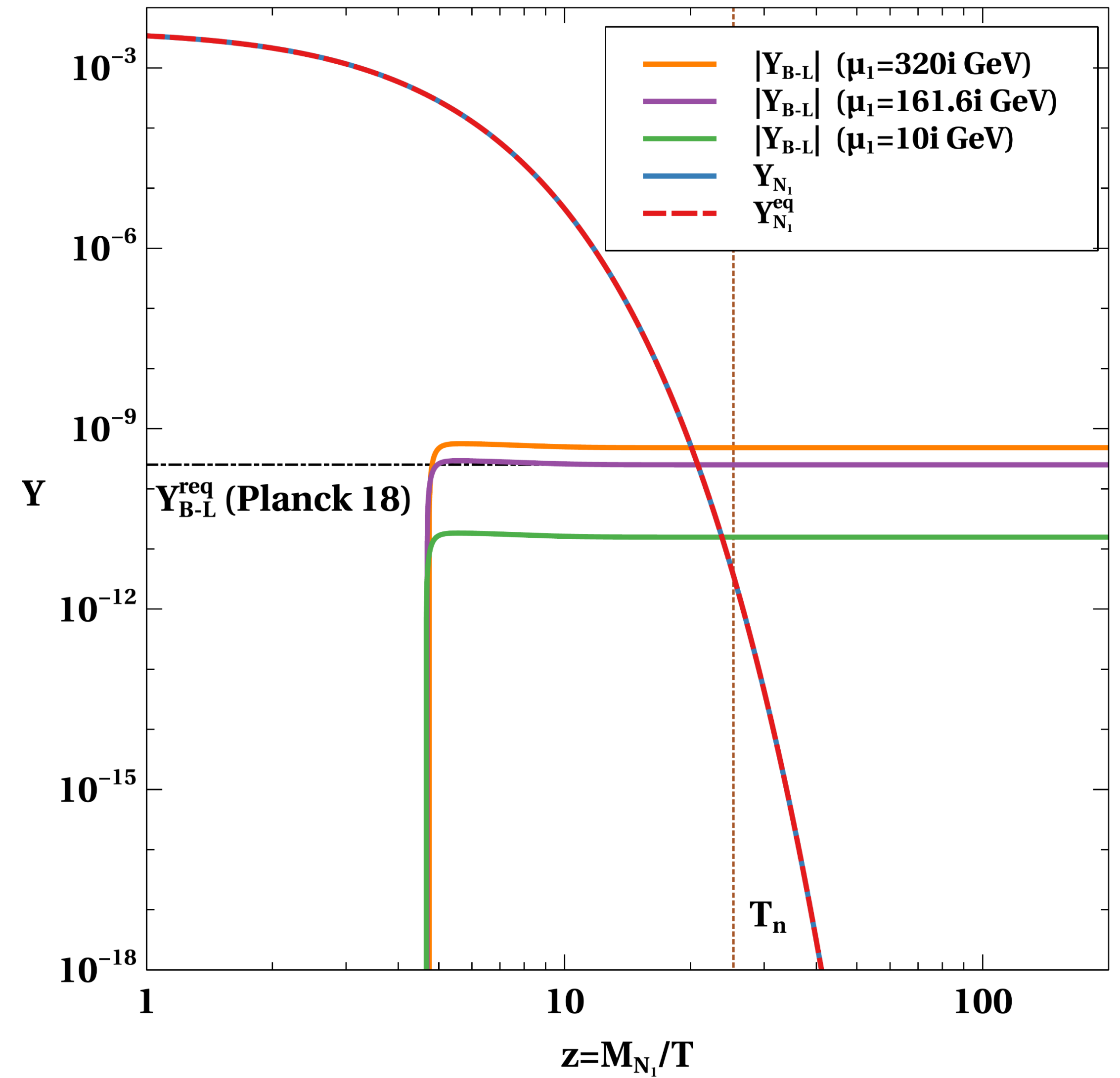
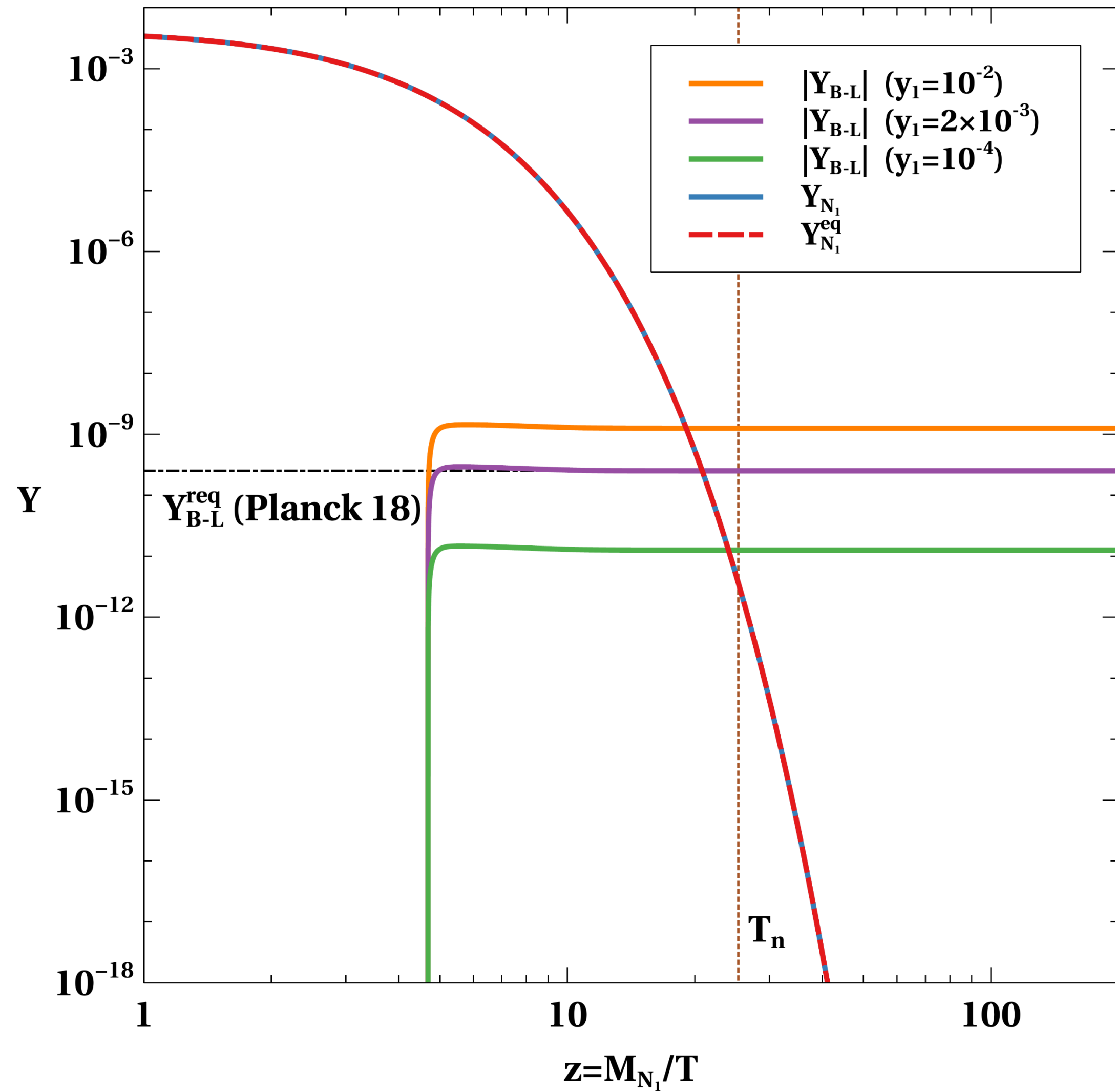
$$\begin{aligned}
\frac{dY_{\text{B-L}}}{dz} = & -\epsilon_1 D_N \left(Y_{N_1} - Y_{N_1}^{\text{eq}} \right) - W_{\text{ID}} Y_{\text{B-L}} - \frac{s}{H(z)z} Y_{\text{B-L}} \left[2Y_\Phi^{\text{eq}} \langle \sigma v \rangle_{l \Phi^\dagger \rightarrow \bar{l} \Phi} + Y_{N_1} \langle \sigma v \rangle_{\bar{l} N_1 \rightarrow \bar{q} t} \right. \\
& \left. + 2Y_q^{\text{eq}} \langle \sigma v \rangle_{\bar{l} q \rightarrow N_1 t} + 2Y_l^{\text{eq}} \langle \sigma v \rangle_{\ell \ell \rightarrow \Phi^\dagger \Phi^\dagger} + Y_\eta^{\text{eq}} \langle \sigma v \rangle_{\bar{l} \eta^\dagger \rightarrow N_1 \chi} + Y_V^{\text{eq}} \langle \sigma v \rangle_{\bar{l} V_\mu \rightarrow \Phi N_1} \right].
\end{aligned}$$

CP asymmetry parameter:

$$\epsilon_1 = \frac{1}{8\pi} \frac{\text{Im}(y_N^\dagger y_\psi y_1 \mu_1)}{(y_N^\dagger y_N) M_{N_1}} \left(1 - 2\sqrt{\sigma} + (\delta - \sqrt{\delta} - \zeta) \ln \left[\frac{\delta - (1 - \sqrt{\sigma})^2}{\delta - \sigma} \right] \right)$$

$$\delta = \frac{M_\psi^2}{M_{N_1}^2}, \quad \zeta = \frac{m_\eta^2}{M_{N_1}^2}, \quad \xi = \frac{m_h^2}{M_{N_1}^2}, \quad \omega = \frac{m_l^2}{M_{N_1}^2} \quad \text{and} \quad \sigma = \frac{m_\chi^2}{M_{N_1}^2}$$

Evolution of comoving number densities:

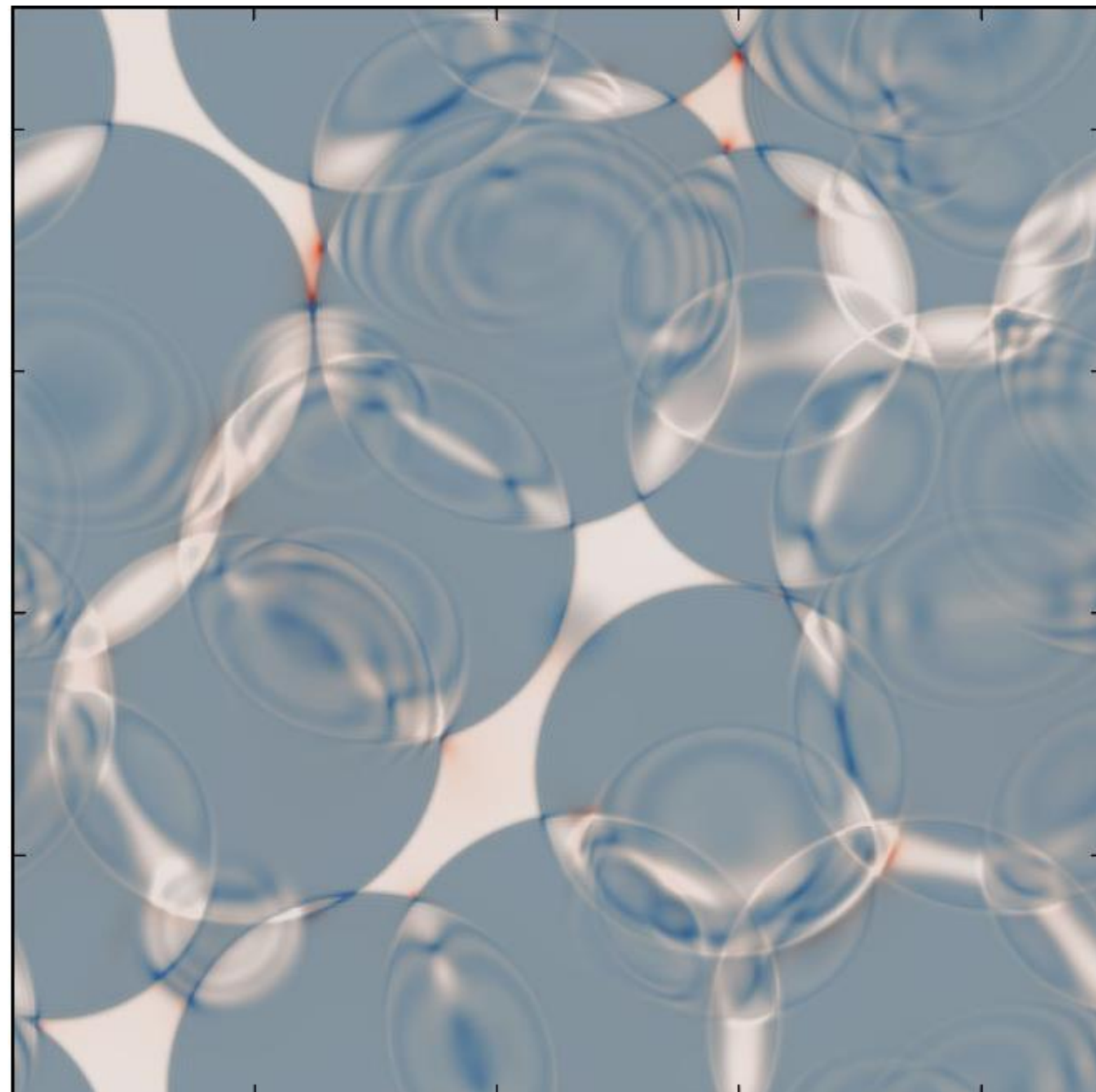


Stochastic Gravitational Waves:

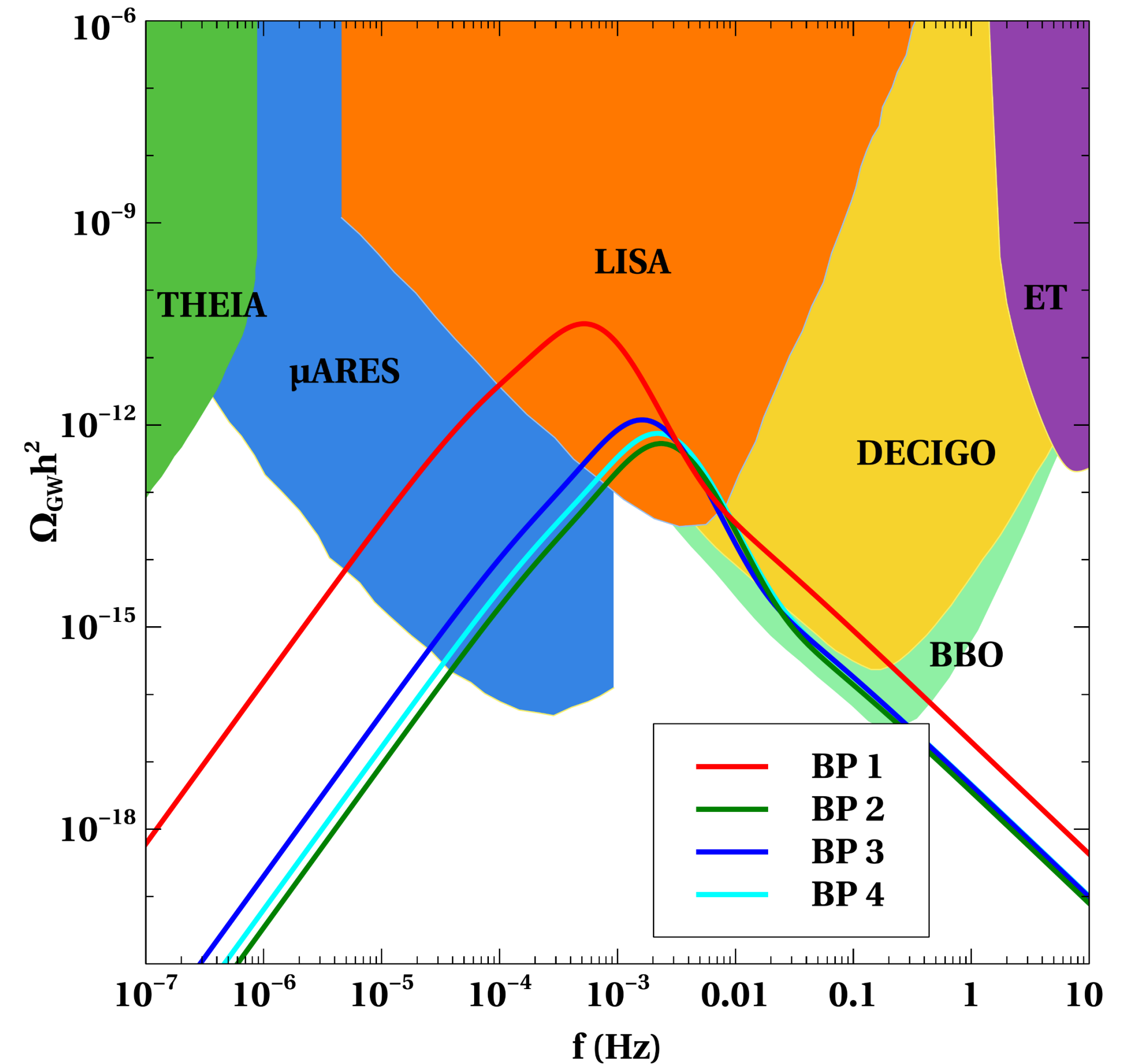
$$\Omega_{\text{GW}}^{\text{PT}}(f) = \Omega_{\phi}(f) + \Omega_{\text{sw}}(f) + \Omega_{\text{turb}}(f),$$


$$h^2\Omega(f) = \mathcal{R}\Delta(v_w) \left(\frac{\kappa\alpha_*}{1+\alpha_*}\right)^p \left(\frac{\mathbf{H}_*}{\beta}\right)^q \mathcal{S}(f/f_{\text{peak}})$$

Caprini et al. JCAP 04 (2016)



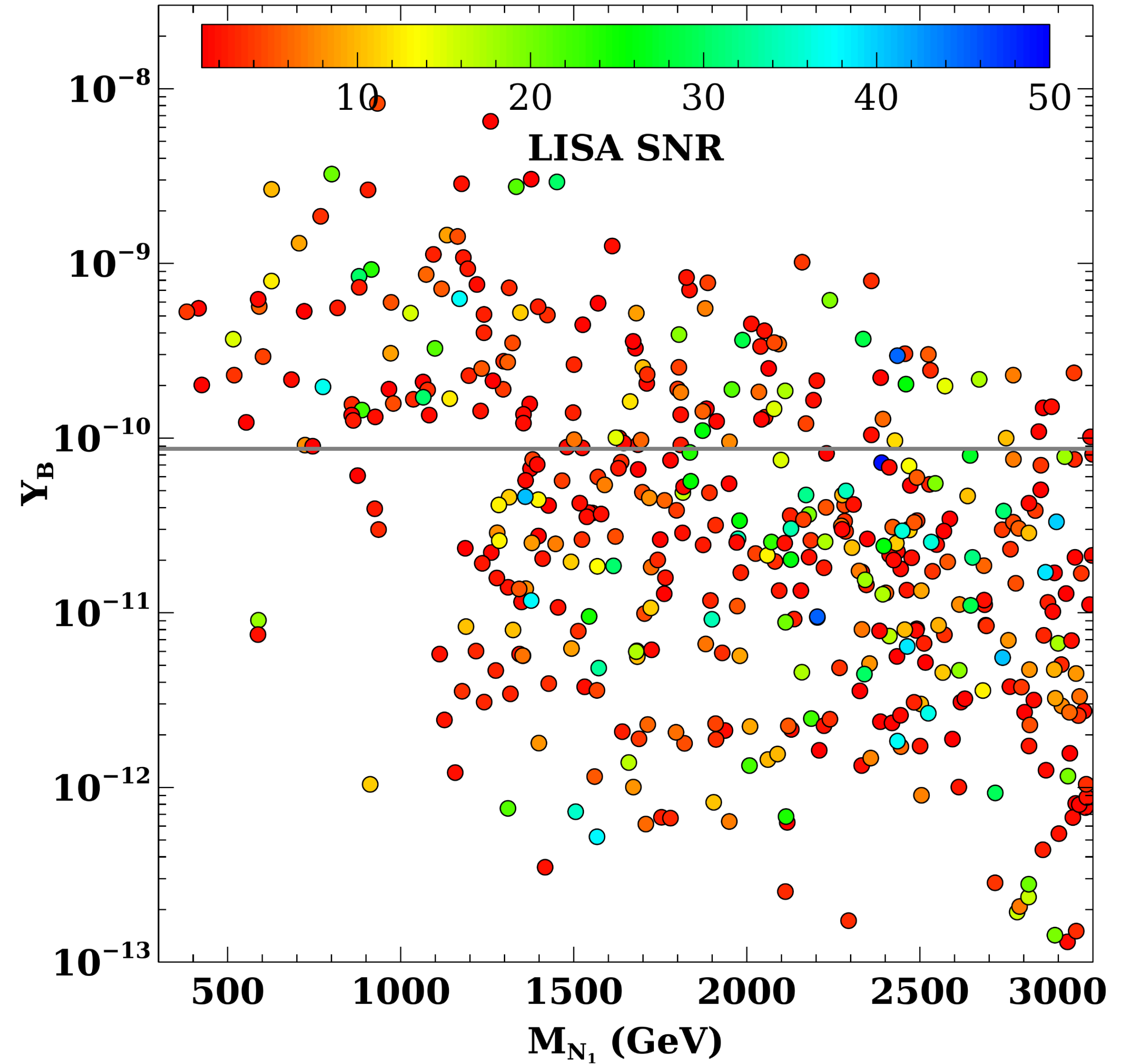
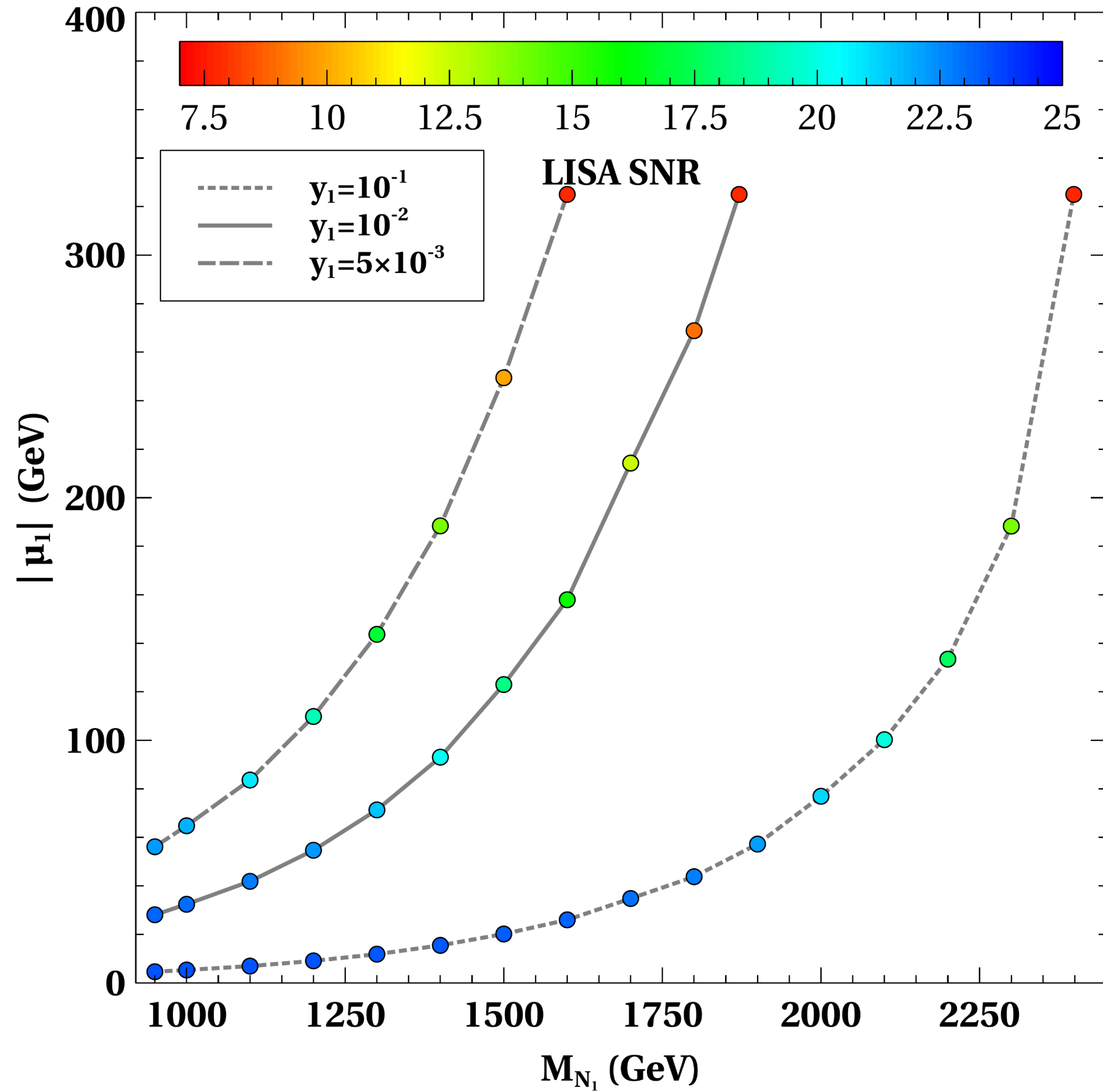
Cutting et al. 97, 123513 (2018)



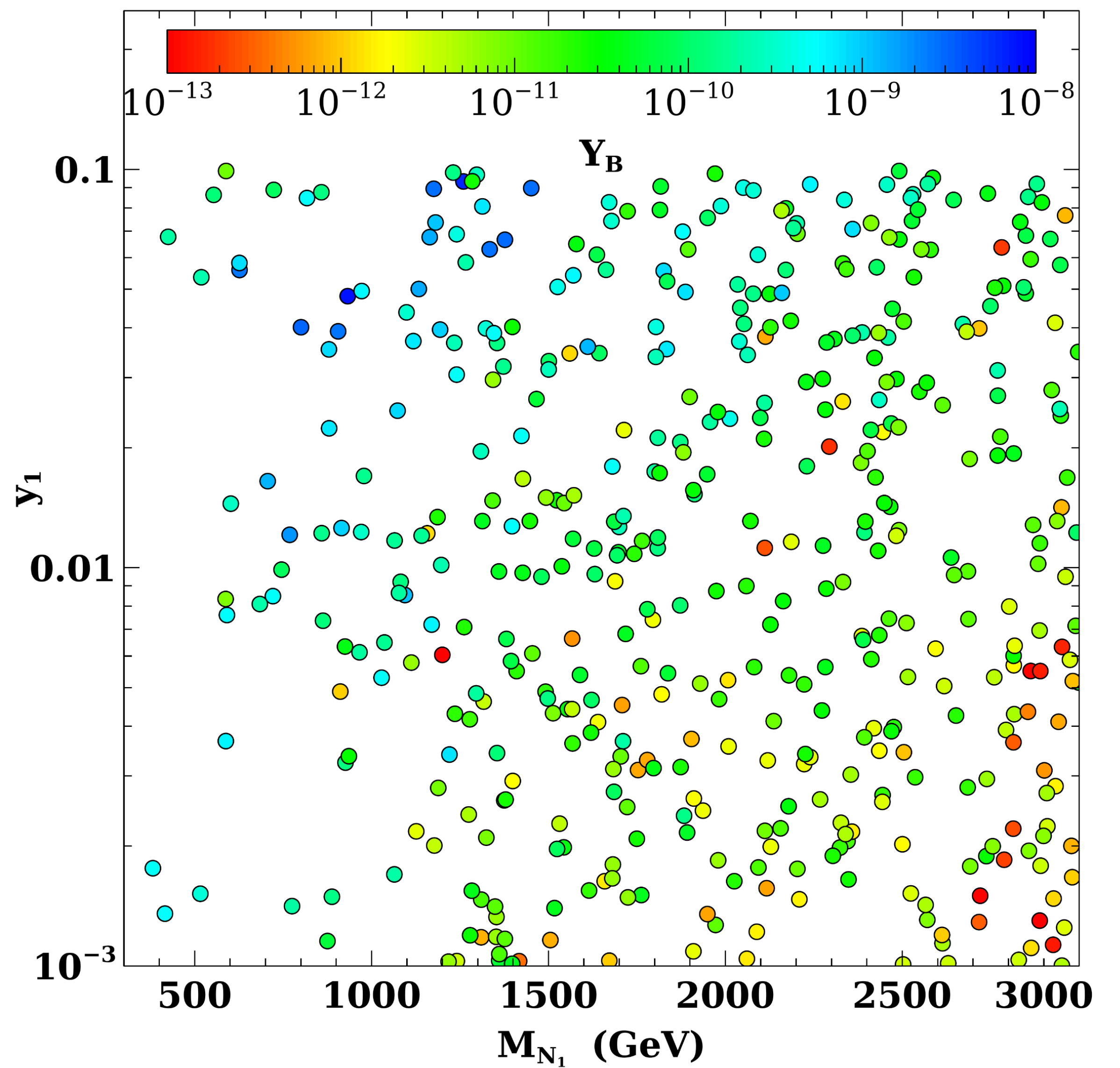
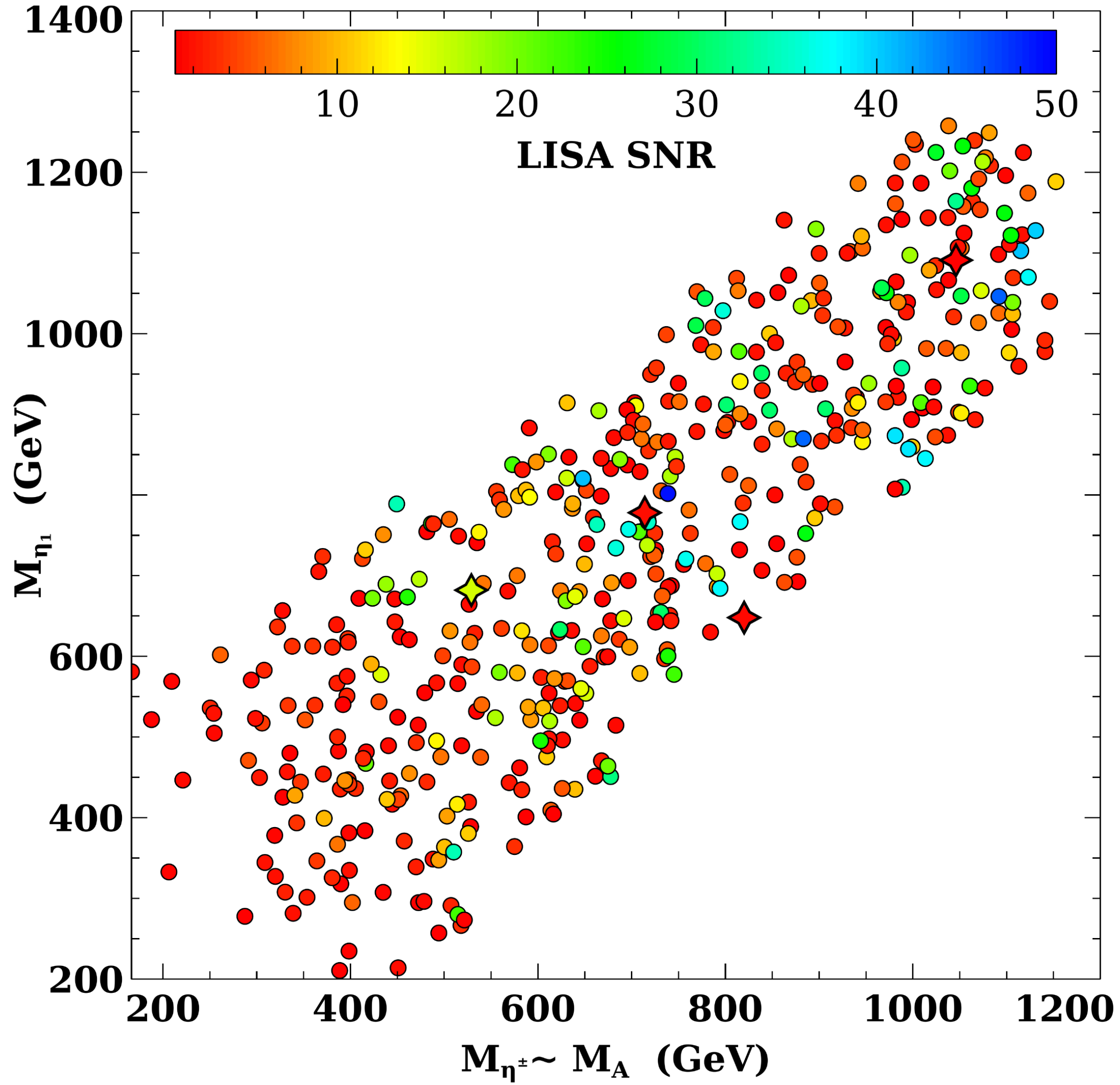
Total contributions from bubble collision, 
sound wave and turbulence in plasma medium

Sound wave in the plasma has dominating contribution

Correlation between Gravitational Waves and Leptogenesis:



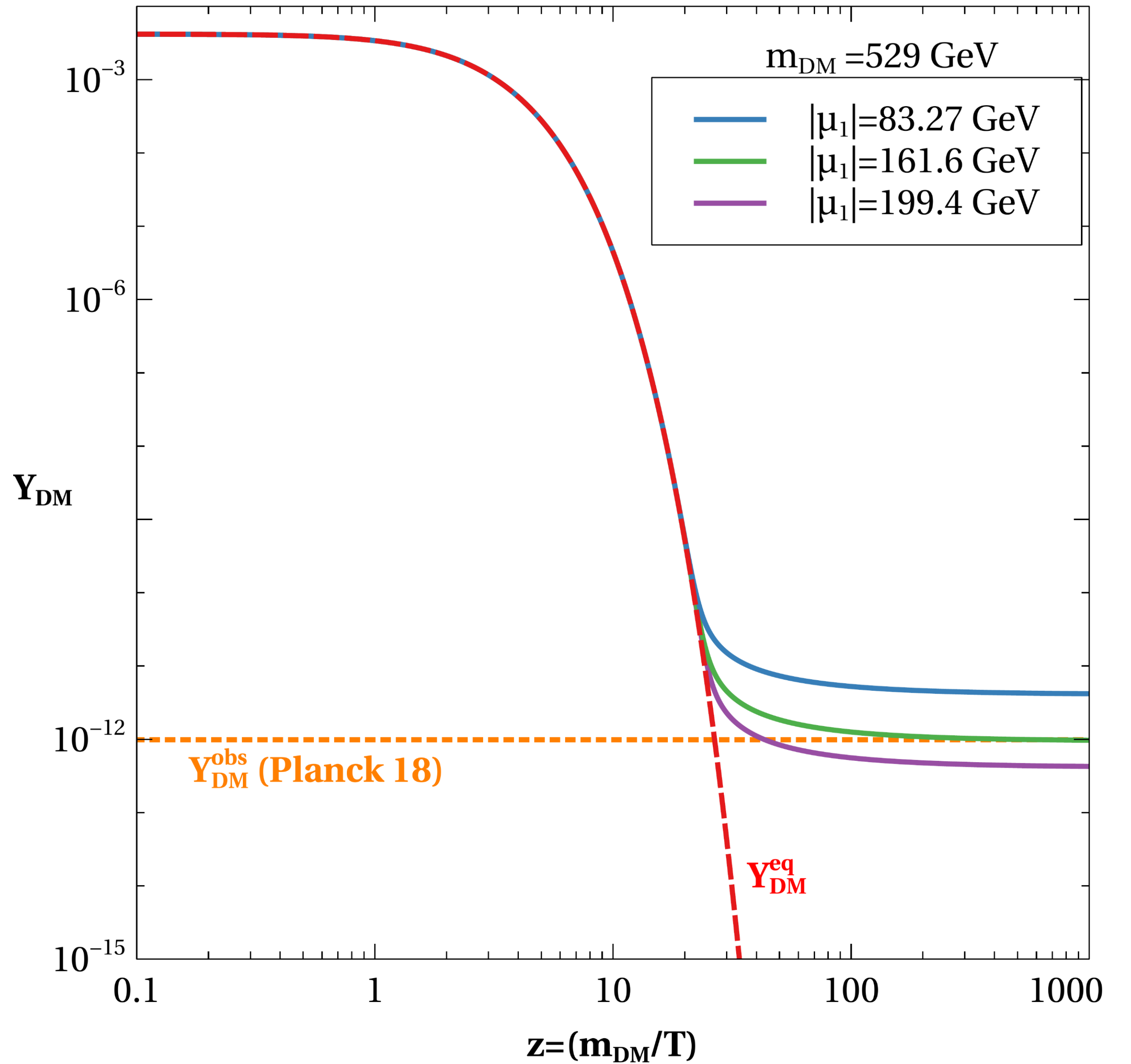
Correlation between Gravitational Waves and Leptogenesis:



Dark Matter:

Dark matter candidates: η_1, η_2, A

$$\frac{dY_{\text{DM}}}{dx} = -\frac{s}{H(x)x} (Y_{\text{DM}}^2 - (Y_{\text{DM}}^{\text{eq}})^2) \langle \sigma v \rangle_{\text{DM DM} \rightarrow \text{SM SM}}$$



Conclusion:

- We have addressed baryon-DM coincidence $\Omega_{DM} \approx 5\Omega_B$.
- We have realized first order Electroweak phase transition with GW within LISA sensitivity.
- The scalar portal is responsible for generation of asymmetry..
- There is a correlation between leptogenesis and signal to noise ratio..

The background of the image is a repeating pattern of overlapping circles. Each circle contains several concentric, thin gray lines, creating a ripple effect. The circles are scattered across the white background, with some overlapping each other. The text 'Thank You' is centered in the middle of the image.

Thank You

	μ_η (GeV)	μ_χ (GeV)	M_{η_1} (GeV)	$M_\eta(M_A)$ (GeV)	M_{η_2} (GeV)	$ \mu_1 $ (GeV)	y_1 (10^{-3})	T_c (GeV)	T_n (GeV)	β/H_*	α_*	M_{N_1} (GeV)
BP1	450	430	529	682	600	161.6	2.00	65.6	39.1	136.0	0.52	989
BP2	938	592	1046	1091	815	733.5	1.10	66.5	48.9	443.6	0.20	1700
BP3	660	220	714	778	598	301.2	1.33	71.6	48.8	308.2	0.21	995
BP4	524	57	820	648	336	461.1	1.62	67.2	47.9	429.4	0.23	935

Table 2. Benchmark points satisfying the requirements of observed baryon asymmetry and dark matter. The mass of Z_2 -odd heavy fermion is kept at $M_\psi \sim 10M_{N_1}$.