



Cluster of Excellence Precision Physics,  
Fundamental Interactions and Structure of Matter



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# Experimental Input to Standard Model Prediction of $(g-2)_\mu$



*March 10, 2016*  
*MITP Mainz, Germany*  
*Determination of Fundamental Parameters in QCD*

# Standard Model Prediction of $(g-2)_\mu$

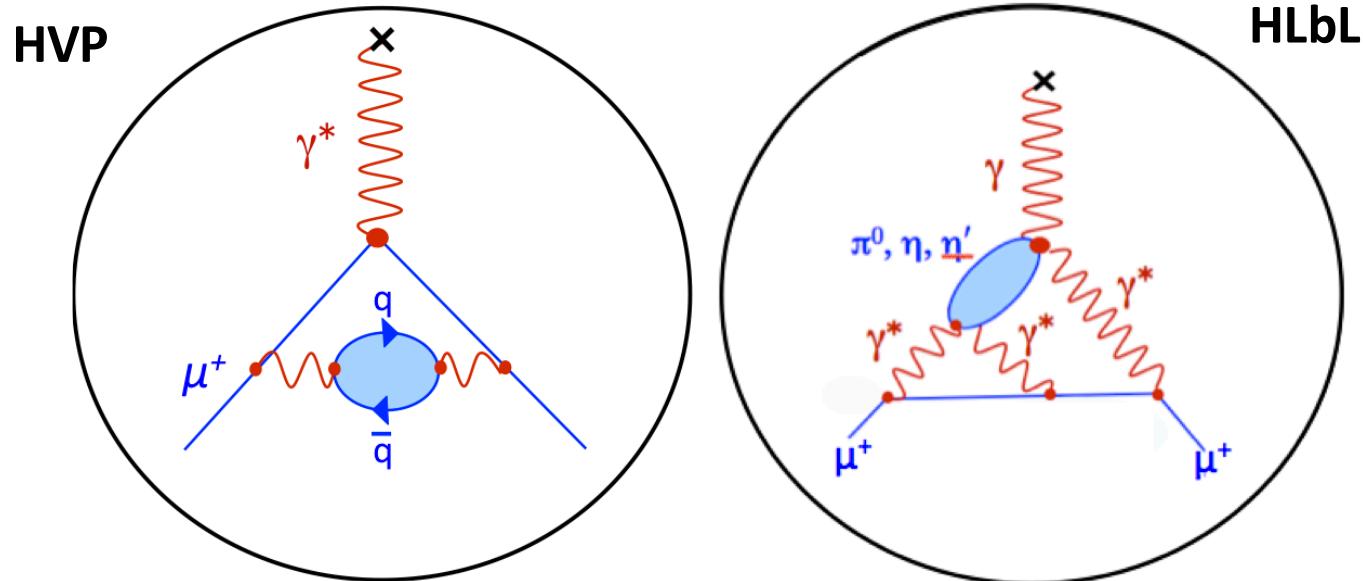
Hadronic contribution **non-perturbative**, the **limiting** contribution

$$a_\mu^{SM} = a_\mu^{\text{QED}} + a_\mu^{\text{weak}} + a_\mu^{\text{had}} = (11\,659\,180.2 \pm 4.9) \cdot 10^{-10}$$

Teubner et al. '11

→ **HVP**: Hadronic Vacuum Polarization  $(692.3 \pm 4.2) \cdot 10^{-10}$   
 NLO  $(-9.8 \pm 0.1) \cdot 10^{-10}$ ; NNLO  $(1.2 \pm 0.01) \cdot 10^{-10}$

→ **HLbL**: Hadronic Light-by-Light  $(10.5 \pm 2.6) \cdot 10^{-10}$



# *Outline*

## **Hadronic Vacuum Polarization <-> Hadronic Cross Section $R_{had}$**

- Overview hadronic cross section measurements
- BES III ISR Program, Status  $e^+e^- \rightarrow \pi^+\pi^-\gamma$  analysis
- $R$  Scan  $> 2$  GeV

## **Hadronic Light-by-Light <-> Transition Form Factors $F(Q_1^2, Q_2^2)$**

- Overview meson transition form factors
- BES III status and expectations

## **Conclusions**

- [ • Dark Photon as a possible solution for  $(g-2)_\mu$  discrepancy ]

# $R_{\text{had}}$

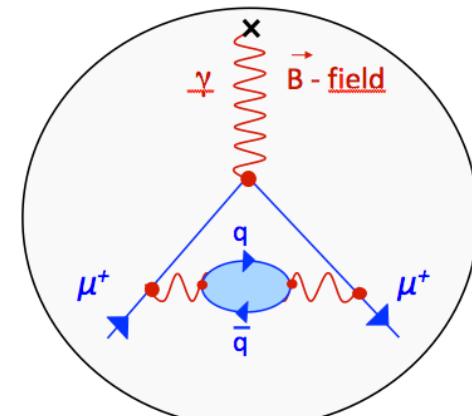
# Hadronic Cross Section $\sigma_{\text{had}}$

Relation to  $(g-2)_\mu$  HVP:

M. Davier et al., Eur. Phys. J. C71 (2011) 1515

F. Jegerlehner, Acta Phys. Pol. B40 (2009) 3097

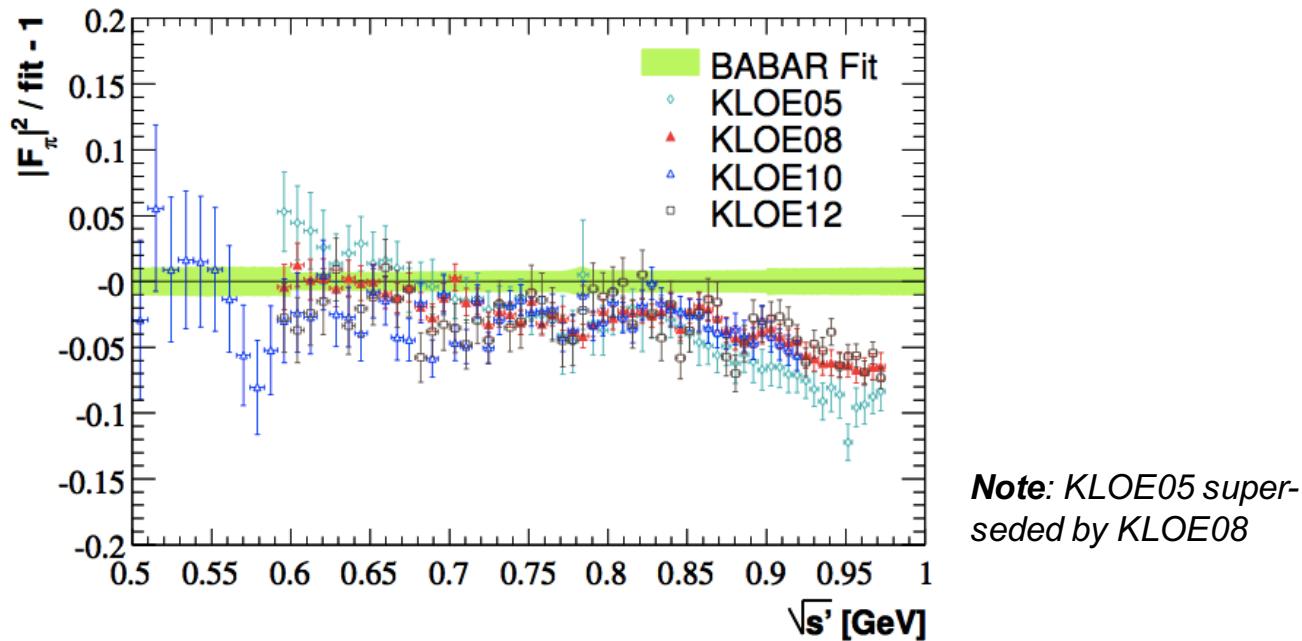
T. Teubner et al., arXiv: 1105.3149



# Most relevant Channel: $e^+e^- \rightarrow \pi^+\pi^-$

$$a_\mu^{HVP} = \frac{1}{4\pi^3} \int_{4m_\pi^2}^\infty ds K(s) \sigma_{had}$$

$\sigma_{had} = \sigma(e^+e^- \rightarrow \text{hadrons})$   
 $\sim 1/s \rightarrow \text{Data below } \sim 3 \text{ GeV needed!}$

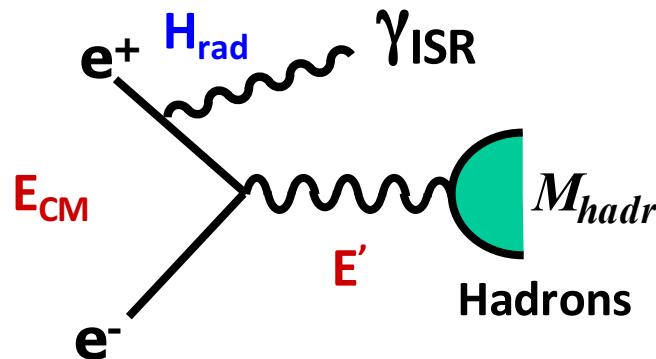


- KLOE and BABAR dominate the world average
- Relatively large systematic differences, esp. above  $\rho$  peak
- Knowledge of  $a_\mu^{\text{had}}$  dramatically limited due to this difference

# Initial State Radiation

Rev. Mod. Phys. 83, 1545–1588 (2011)

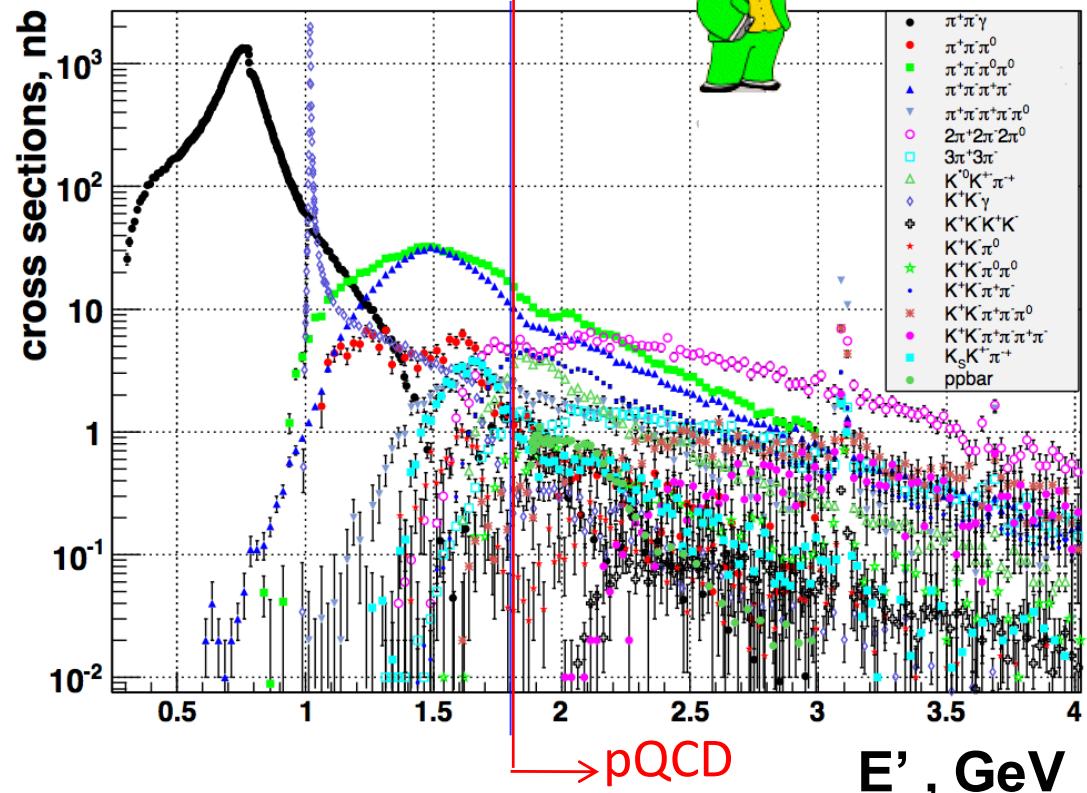
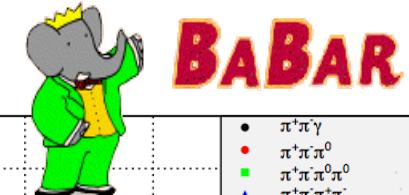
## Initial State Radiation (ISR) aka Radiative Return



- Needs **no** systematic variation of beam energy
- High statistics thanks to high integrated luminosities
- Precise knowledge of radiative corrections mandatory ( $H_{rad}$ )

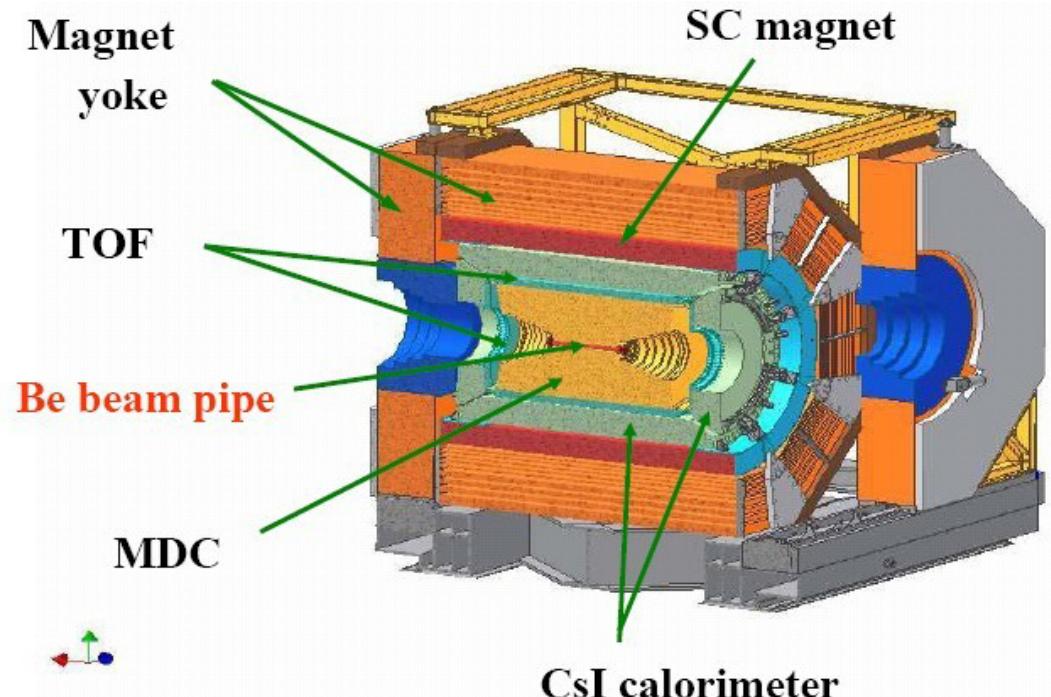
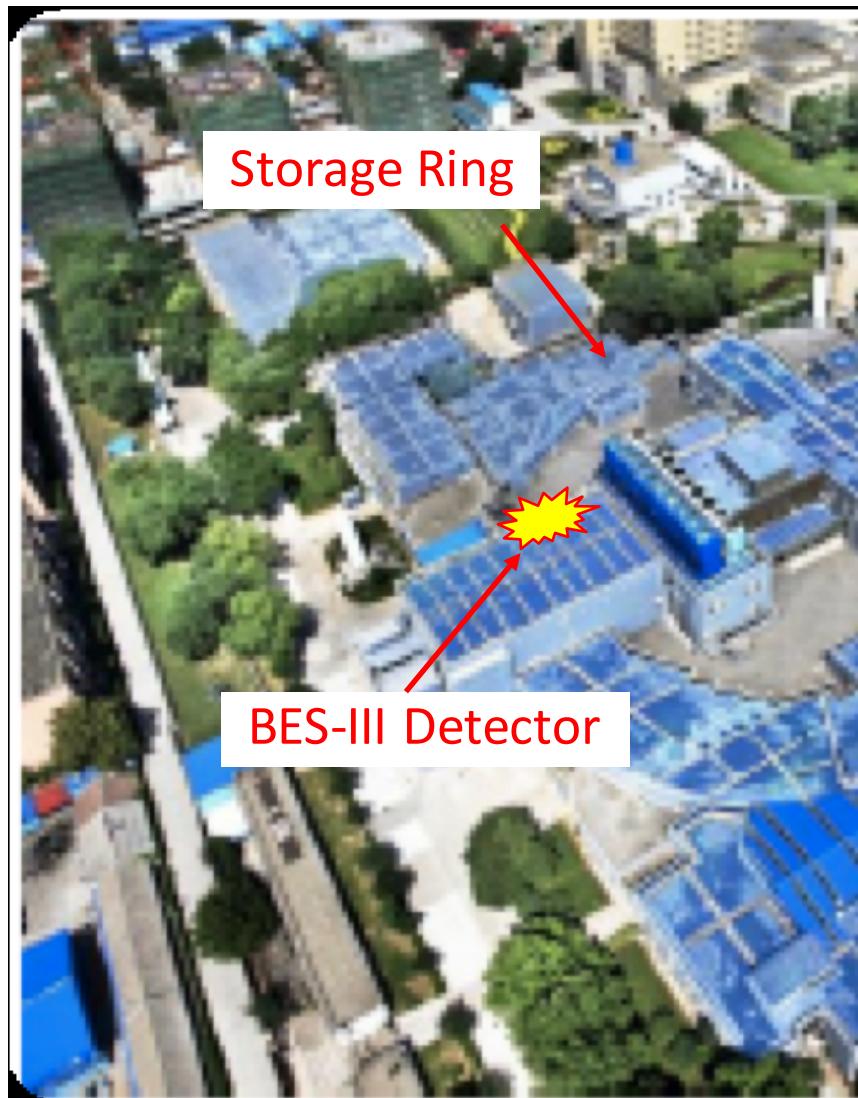
PHOKHARA event generator Czyż, Kühn, et al.

ISR spectra measured by



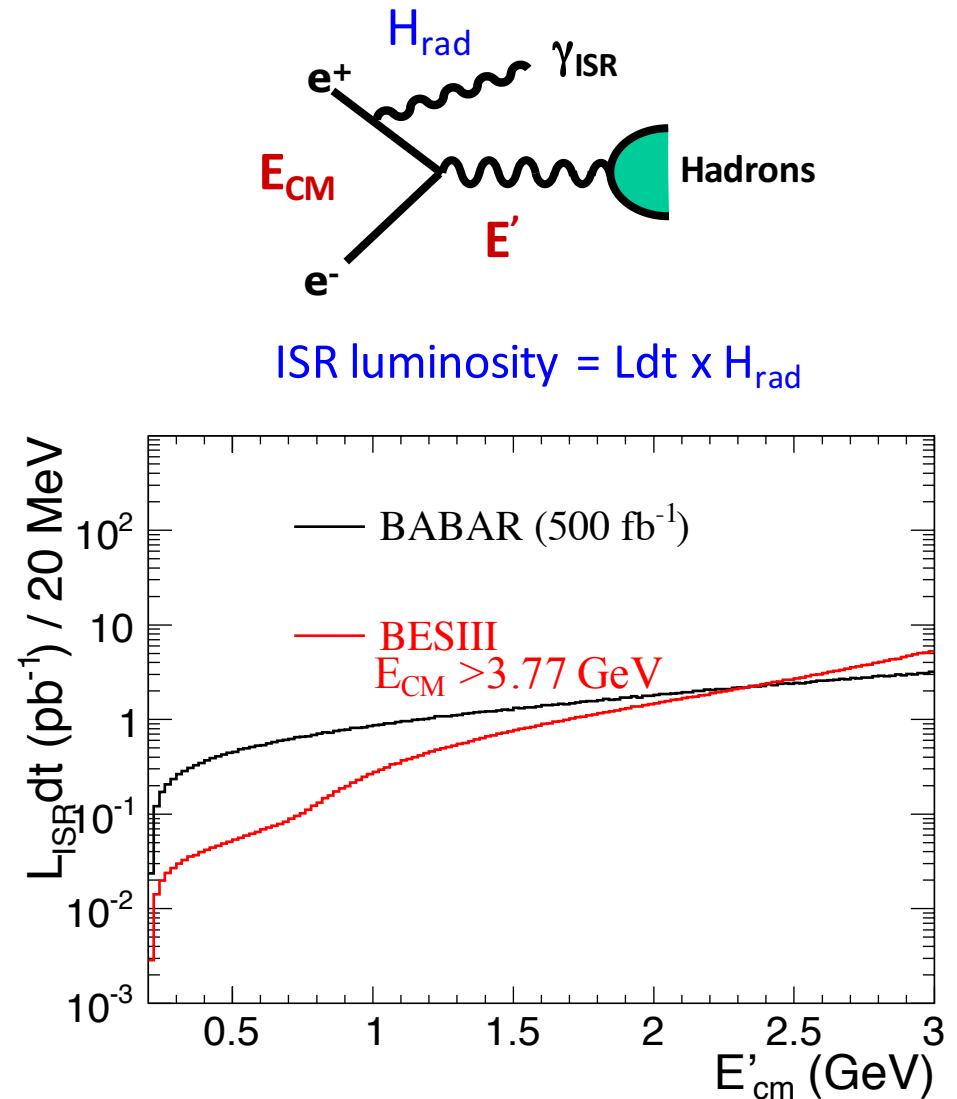
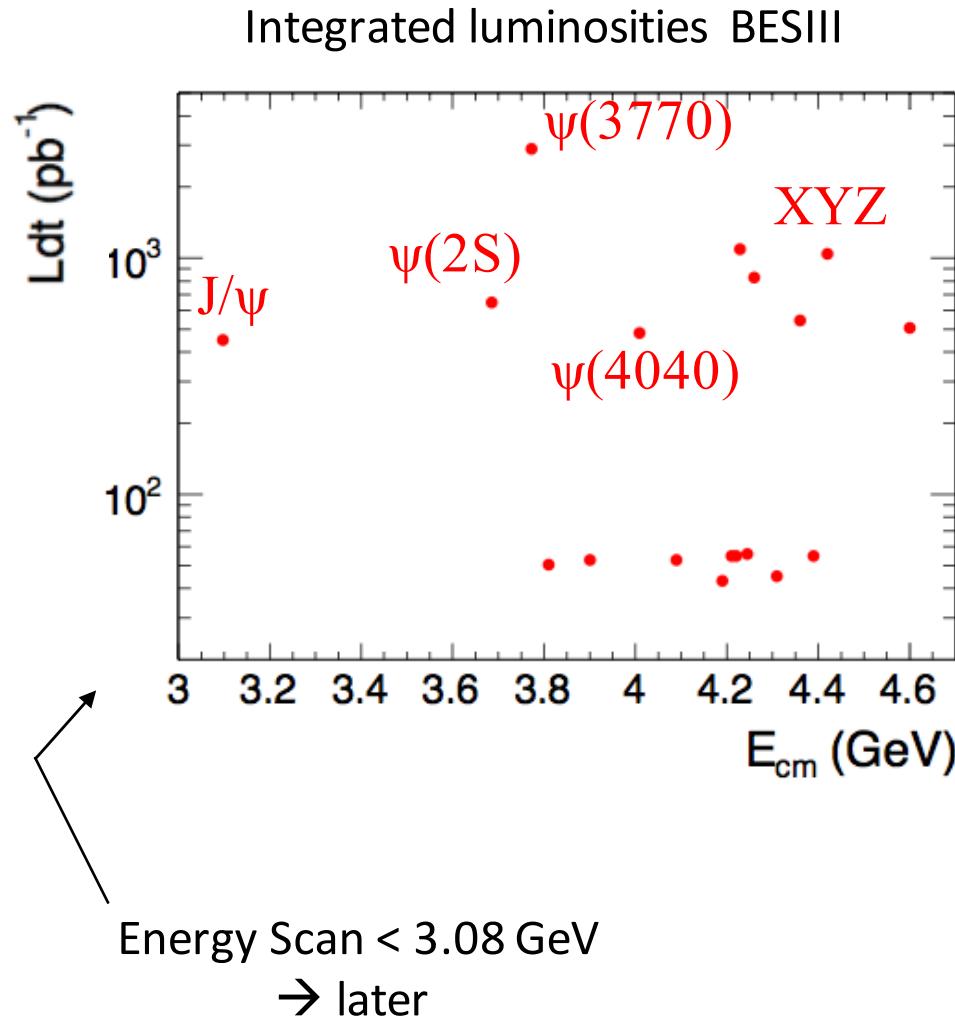
→ Entire  $E$  range  $< E_{CM}$  accessible

# BEPC II Project

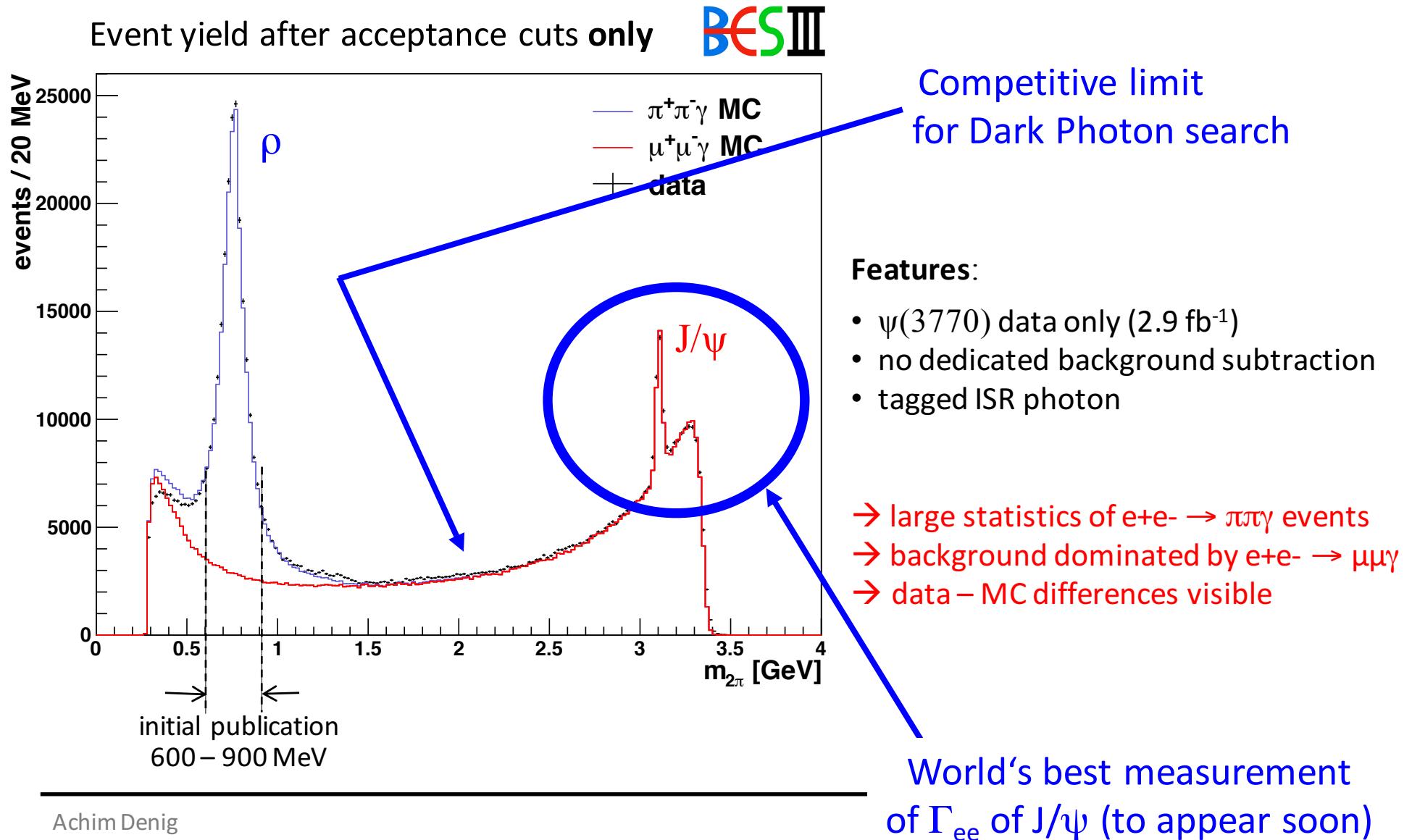


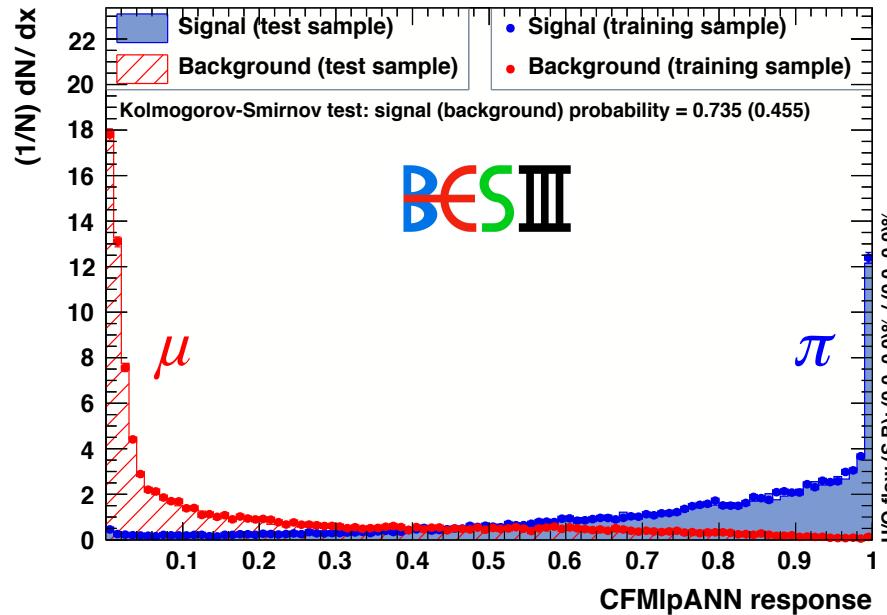
CM Energy 2.0 – 4.6 GeV  
Design Luminosity  $10^{33} \text{ cm}^{-2} \text{ s}^{-1}$   
Achieved Luminosity 70%@ $\psi(3770)$

# Data Samples for ISR Physics

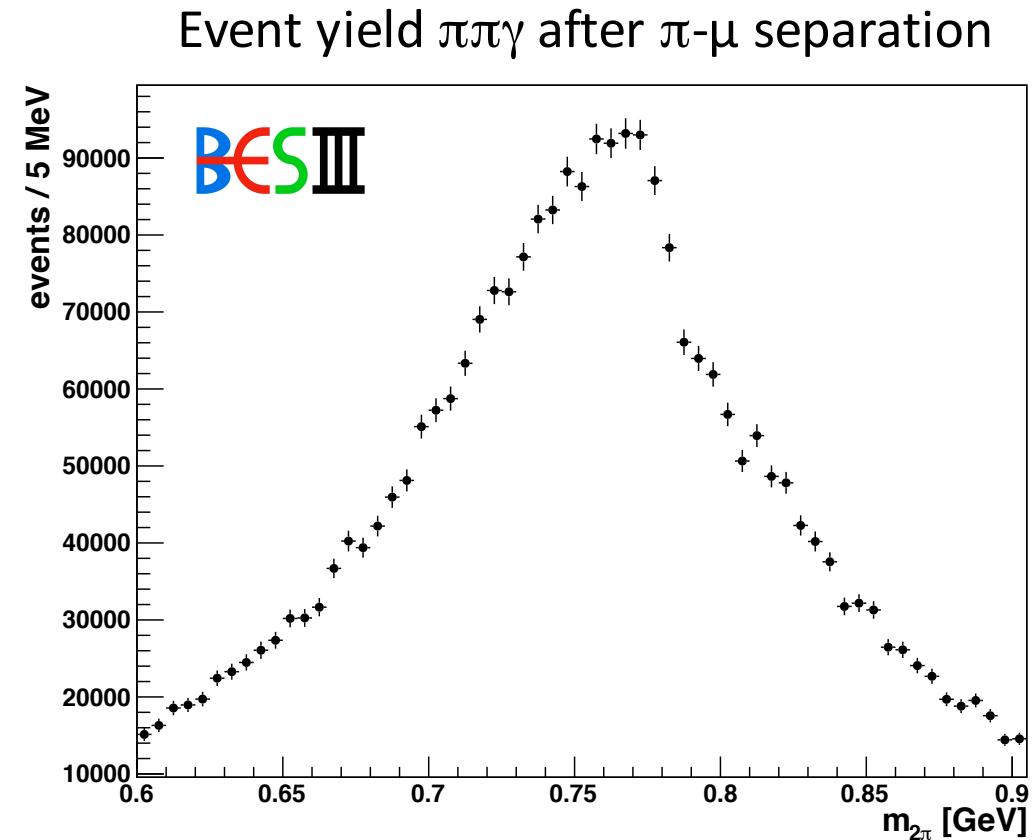


# Flagship ISR Analysis: $e^+e^- \rightarrow \pi^+\pi^-\gamma_{ISR}$



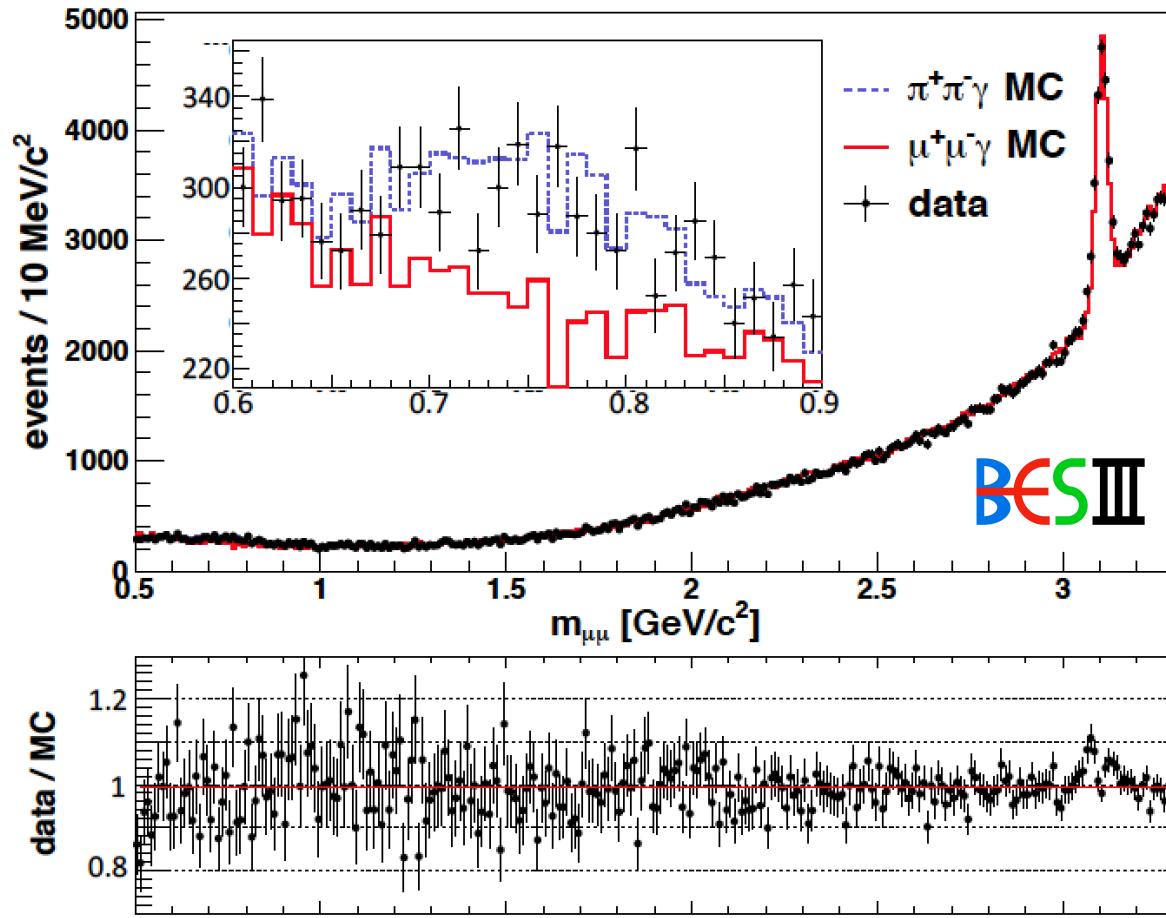
$e^+e^- \rightarrow \pi^+\pi^-\gamma_{ISR}$ :  $\pi - \mu$  Separation

**TMVA method (Neural Network):**

- trained using  $\mu\mu\gamma$  and  $\pi\pi\pi\gamma$  MC events
- information based on track level
- efficiency matrix ( $p, \Theta$ ) for data, MC
- correct for data - MC differences
- cross checked for different TMVA methods



# Measurement of $\mu^+\mu^-\gamma$ : Data vs. QED

Event yield  $\mu\mu\gamma$  after  $\pi$ - $\mu$  separation  
and all efficiency corrections



## Features:

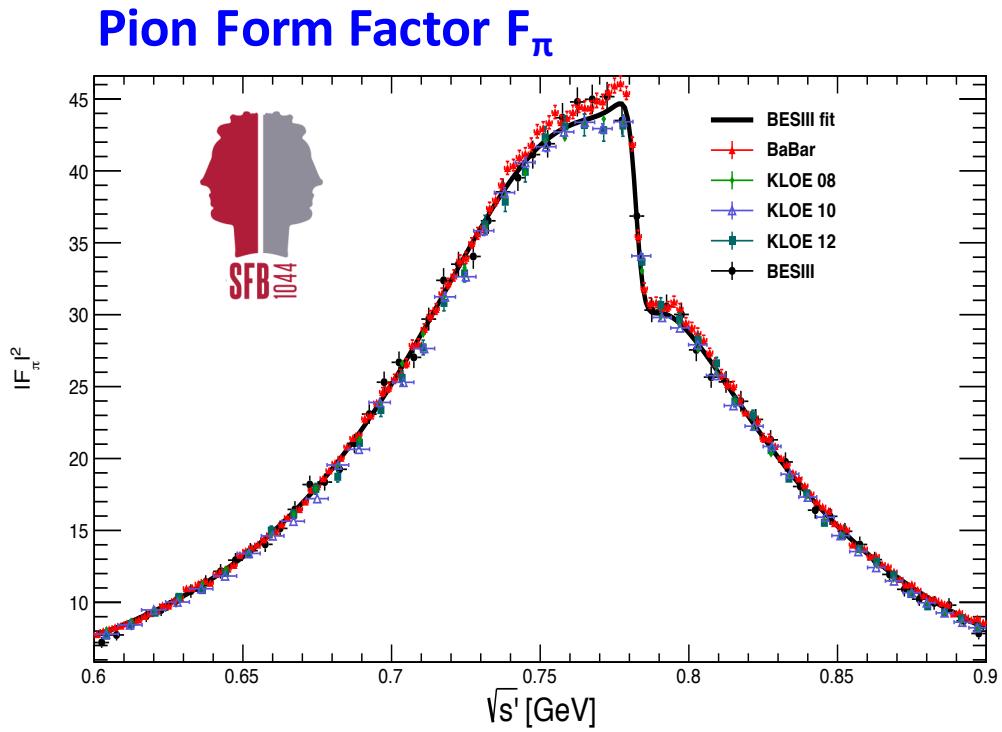
- background from  $\pi\pi\gamma$  very small
- PHOKHARA accuracy <0.5%
- luminosity measurement based on Bhabha ev., 1.0% accuracy

→ excellent agreement with QED

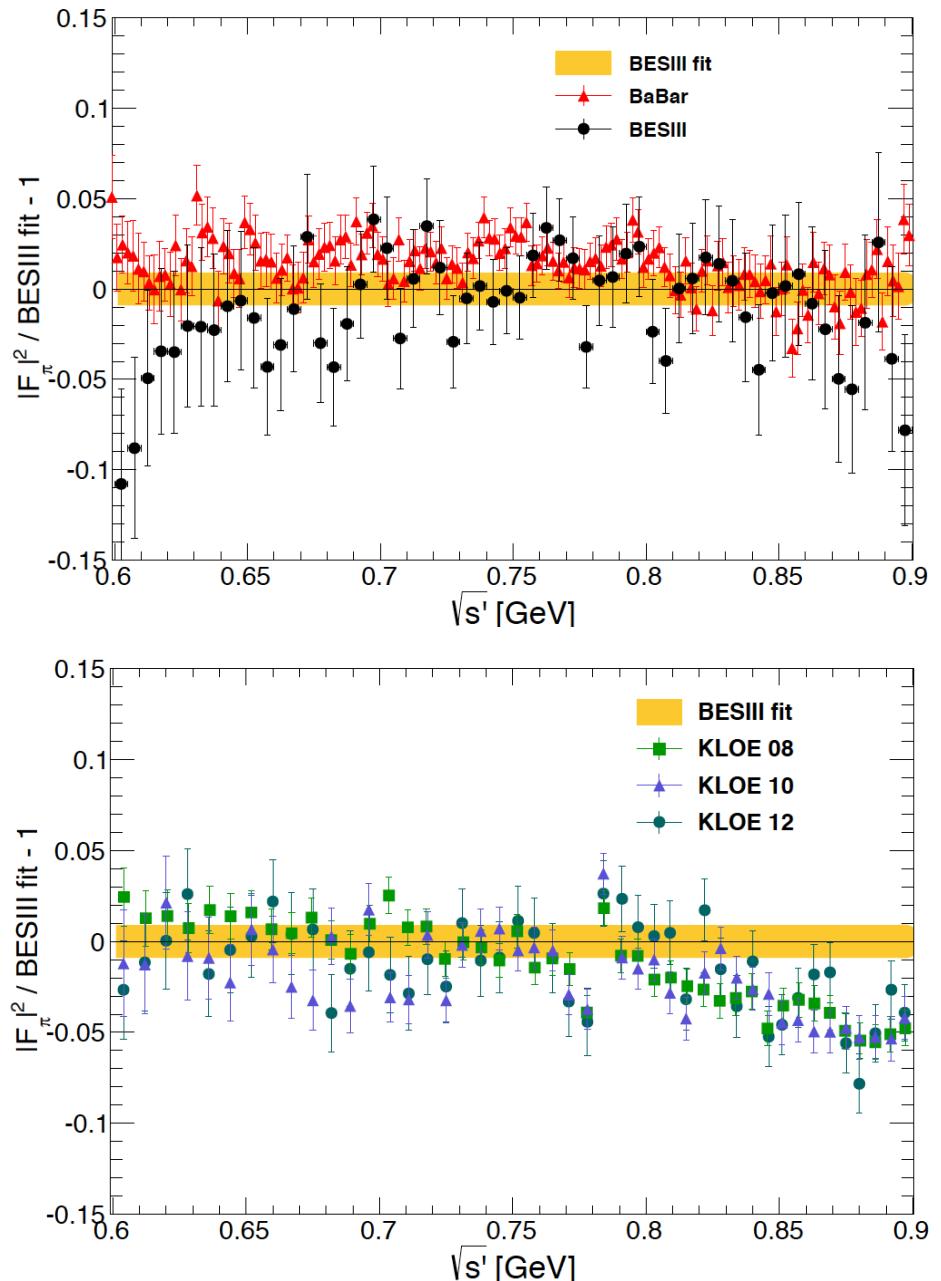
$$\Delta(\text{MC/QED-data}) - 1 = \\ (1.0 \pm 0.3_{\text{stat}} \pm 0.9_{\text{syst}}) \%$$

→ accuracy on 1% level as needed to be competitive !

# Comparison with existing Data

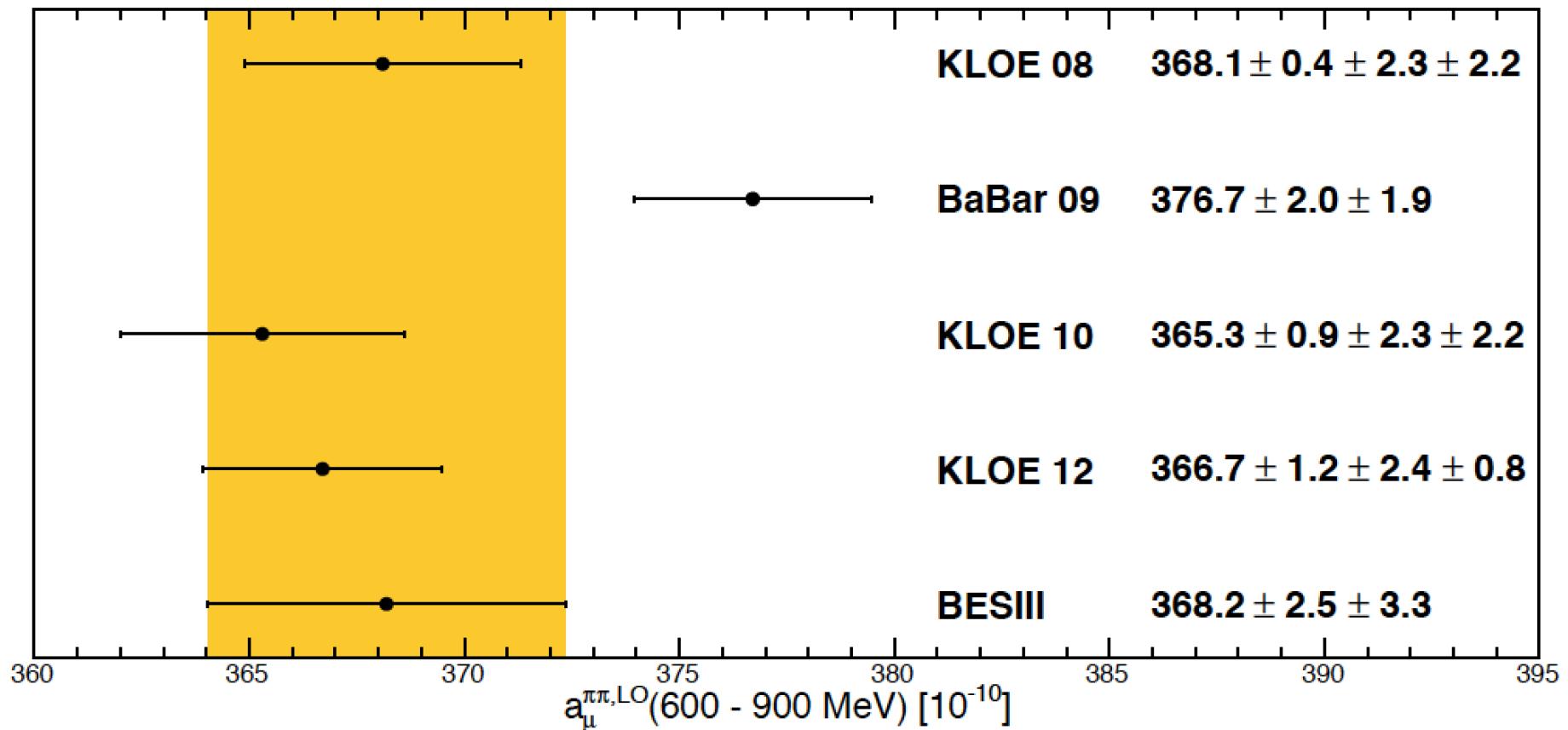


0.9 % accuracy (dominated by theory)  
 Normalization to luminosity / radiator function  
 Cross check with  $R = \pi\pi\gamma/\mu\mu\gamma$  ratio



# *Impact on Hadronic Vacuum Polarization*

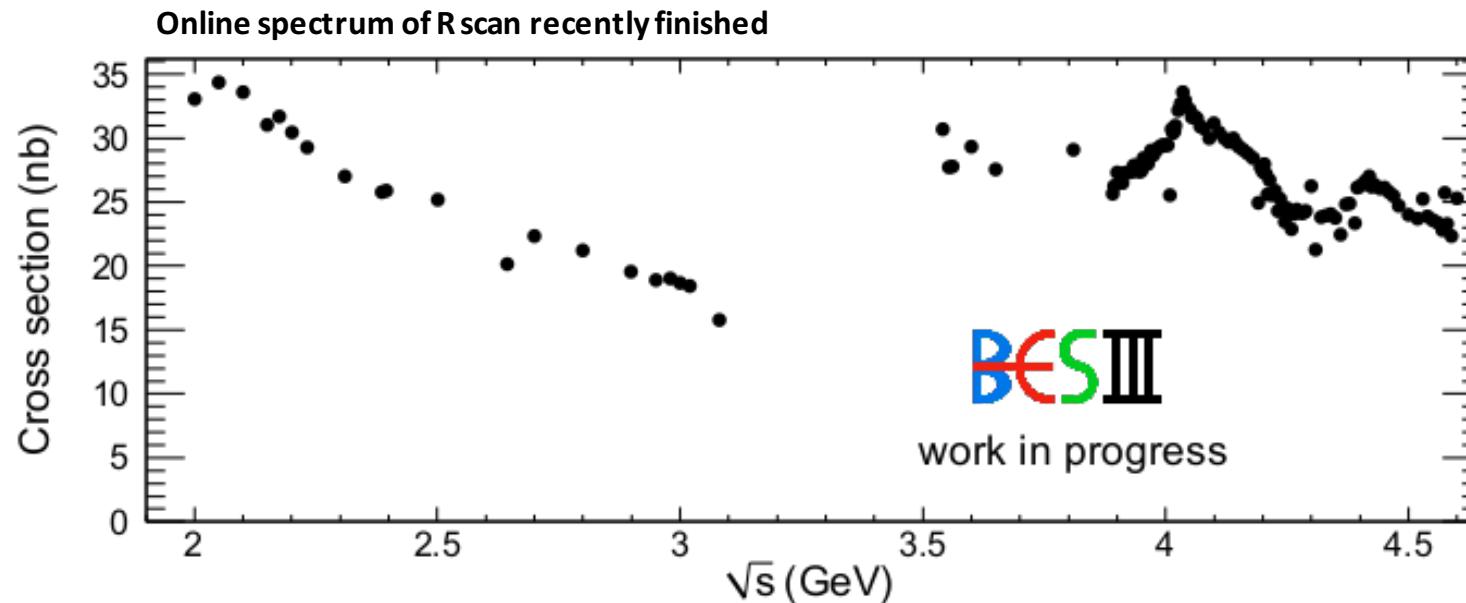
Phys. Lett. B753 (2016) 629



→ BES III confirms ~4 sigma deviation in  $(g-2)_{\mu}$ !  
 → Also  $3\pi$  and  $4\pi$  channels in preparation

# *R Scan 2 – 4.6 GeV recently completed*

Reducing the uncertainty of  $\alpha_{\text{em}}(M_Z^2)$  by a factor of 2  
→ A new quantity of electroweak precision fits



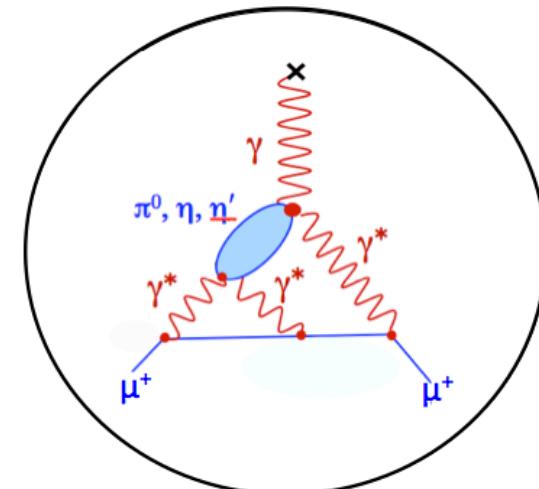
$R_{\text{incl}} = \sigma_{\text{had}}/\sigma_{\mu\mu}$  ratio with targeted 3% systematic accuracy (statistical error <<1%)

- 125 scan points with  $>10^5$  hadronic events each → statistical error negligible
- World's best measurement so far from BES /BESII with 5 ... 8 % total error (with 3 ... 5% statistical error)

# Meson Transition Form Factors

## $F(Q^2)$

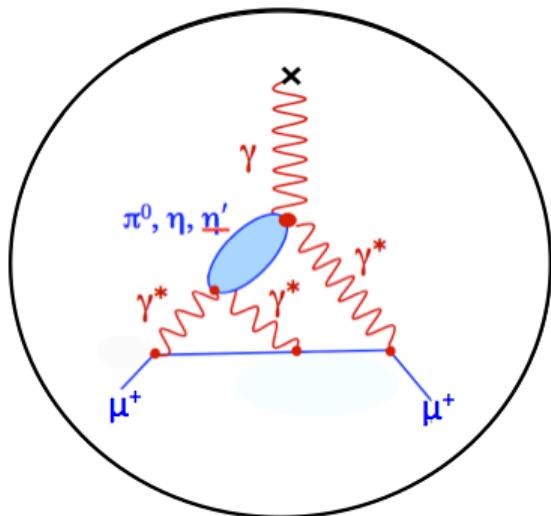
Relation to  $(g-2)_\mu$  HLbL:  
arXiv:1408.2517 (G. Colangelo et al.)  
arXiv:1409.0819 (M. Vanderhaeghen et al.)



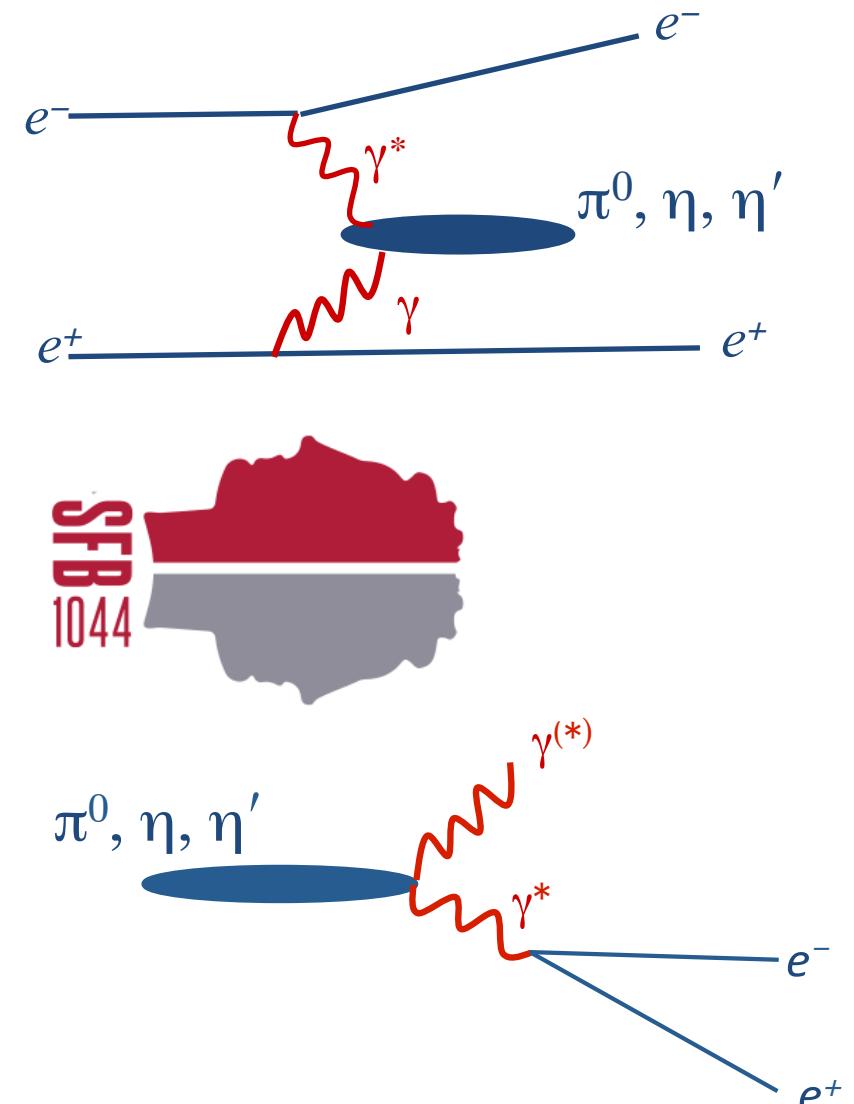
# Hadronic Light-by-Light Scattering

**HLbL:**  $(10.5 \pm 2.6) \cdot 10^{-10}$   
Prades, de Rafael, Vainshtein '09

$(18.8 \pm 0.4_{\text{stat}}) \cdot 10^{-10}$   
Goeke, Fischer, Williams '11



Relation ?  
 $\leftrightarrow$   
**Exp. Input !**  
**Transition**  
**Form Factors**  
 **$F(Q^2)$**



**Future: data-driven approach!**

Dispersion Relations being developed  
using experimental measurements  
of meson transition form factors!

Colangelo et al '14; Pauk, Vanderhaeghen '14

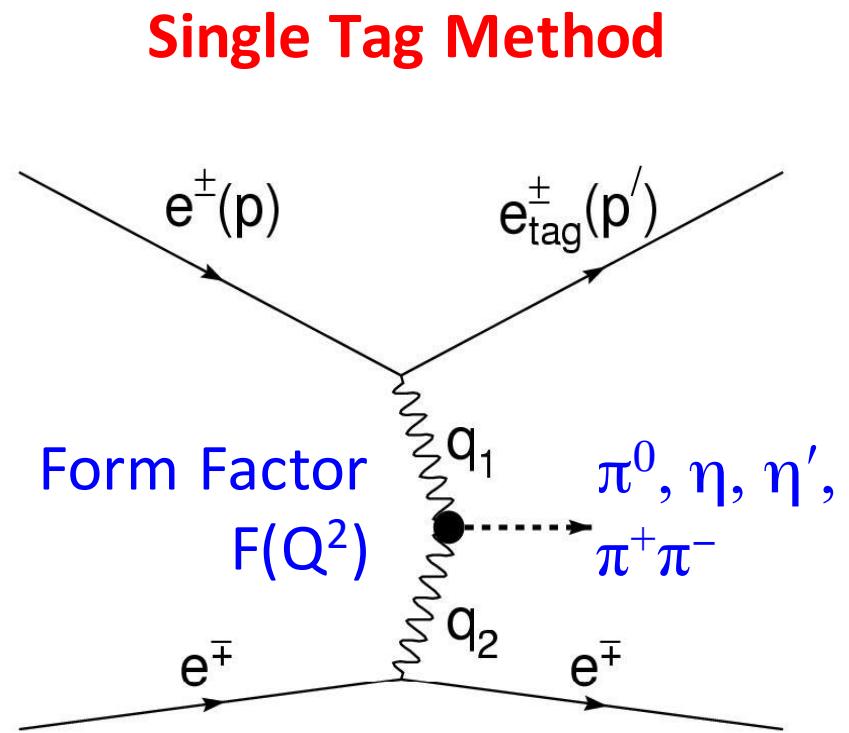
# Spacelike FFs $\gamma\gamma^*\rightarrow P$

## Selection criteria

- 1 electron (positron) detected
  - 1 positron (electron) along beam axis
  - Meson fully reconstructed
- cut on angle of missing momentum

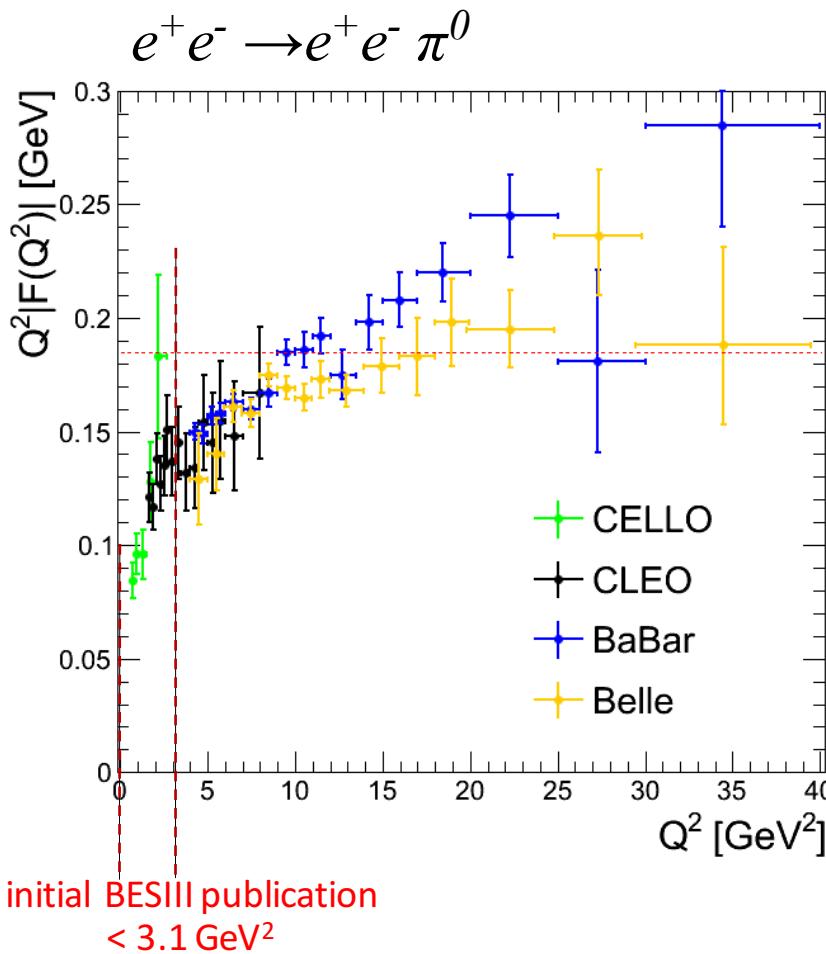
## Momentum transfer

- tagged:  $Q^2 = -q_1^2 = -(p - p')^2$   
→ Highly virtual photon
- untagged:  $q^2 = -q_2^2 \sim 0 \text{ GeV}^2$   
→ Quasi-real photon



EKHARA event generator  
Czyż, Ivashyn

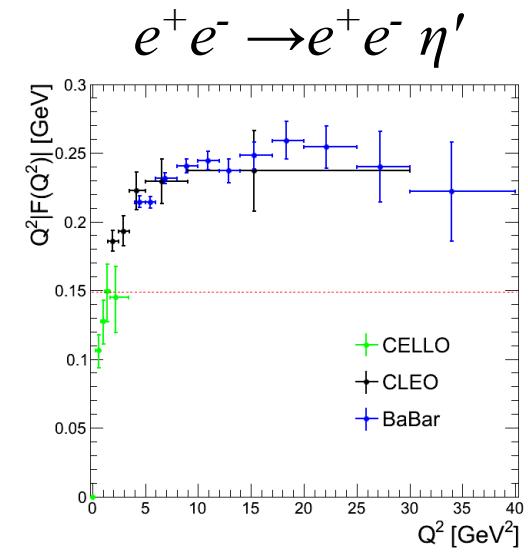
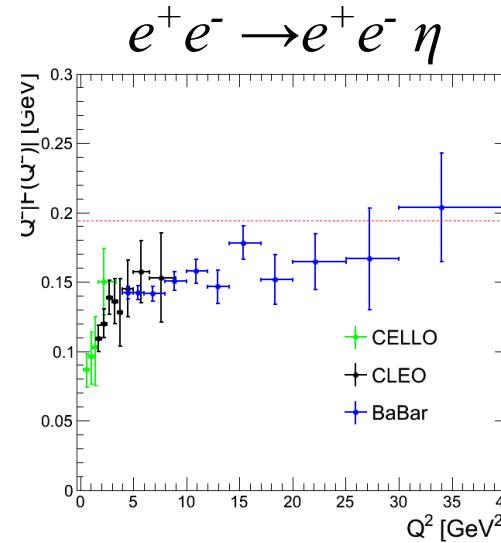
# Existing Data on SL Transition FFs



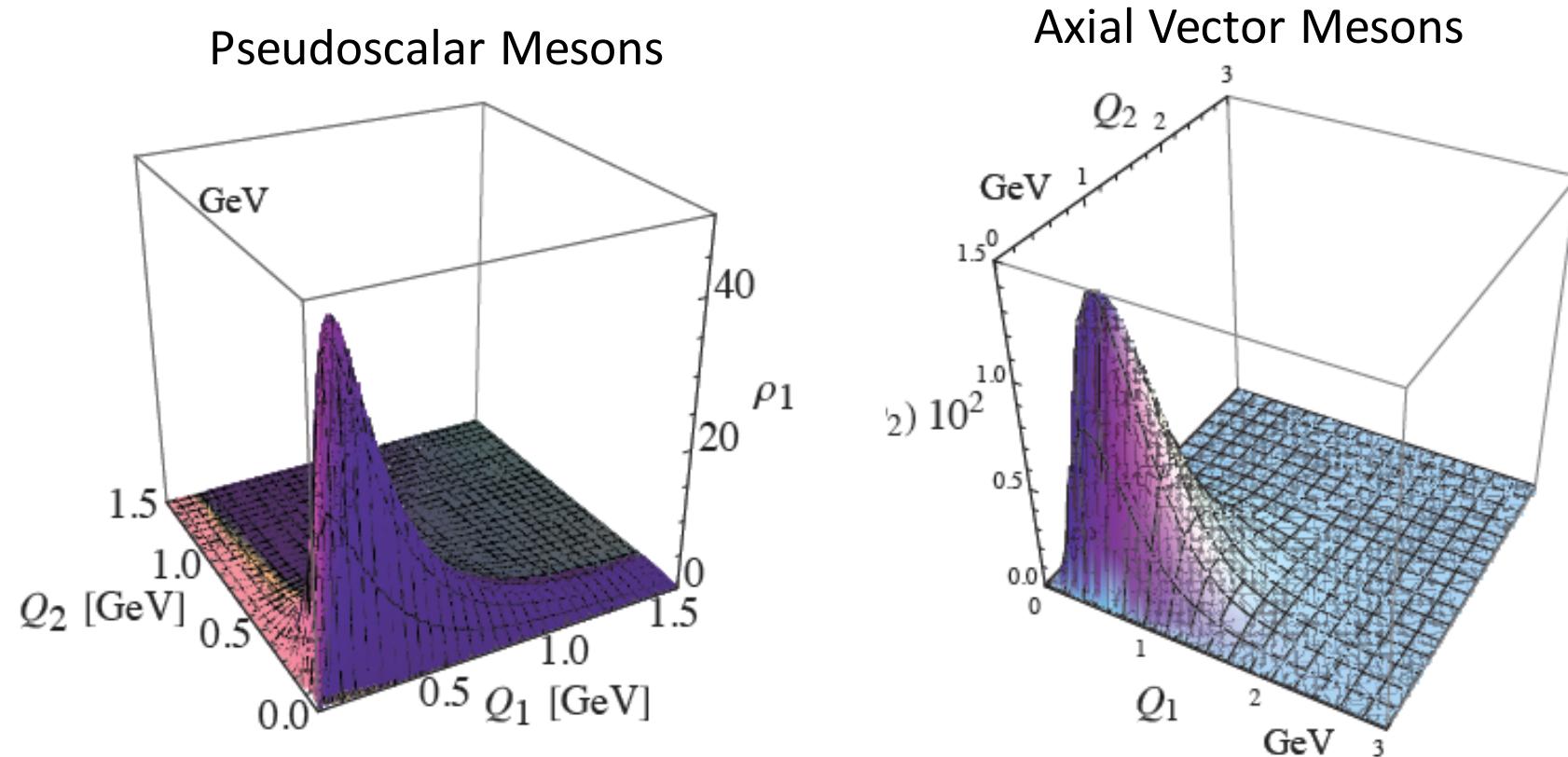
## Features:

- recent high-Q<sup>2</sup> data from BABAR and BELLE Q<sup>2</sup> > 4 GeV<sup>2</sup>
- above 1.5 GeV<sup>2</sup> data from CLEO
- below 1.5 GeV<sup>2</sup> data from CELLO, very poor accuracy

→ low Q<sup>2</sup> range not covered  
most relevant for HLbL contribution to  $(g-2)_\mu$   
→ most relevant channels:  $\pi^0, \eta, \eta', \pi\pi$



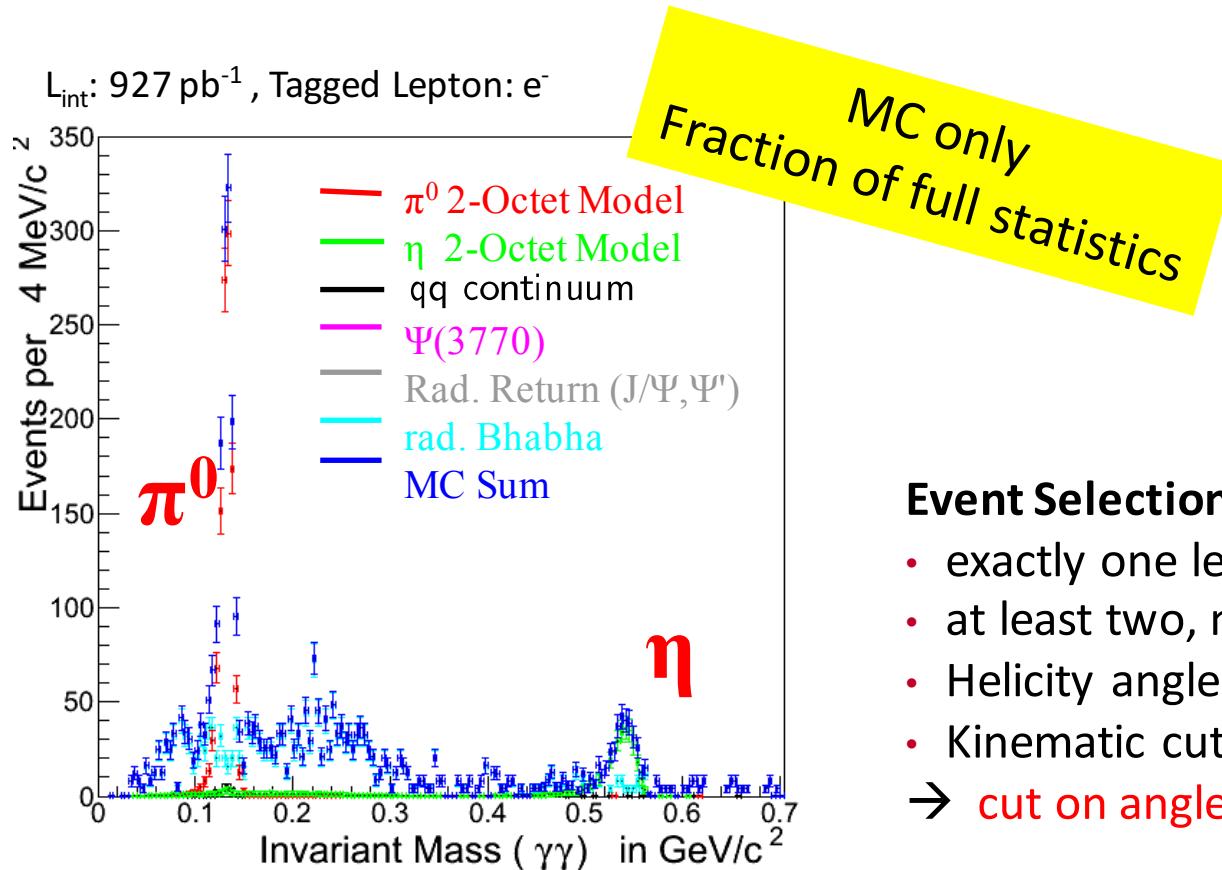
# Relevance for $HLbL$



**Weighting functions dominate at low  $Q < 2$  GeV !**

courtesy: V. Pauk, JLAB

# BES III Analysis: $e^+e^- \rightarrow e^+e^- \pi^0$



### Event Selection:

- exactly one lepton candidate
  - at least two, max four photons
  - Helicity angle  $\cos \Theta_H > 0.8$
  - Kinematic cuts to reject ISR background
- cut on angle of missing momentum

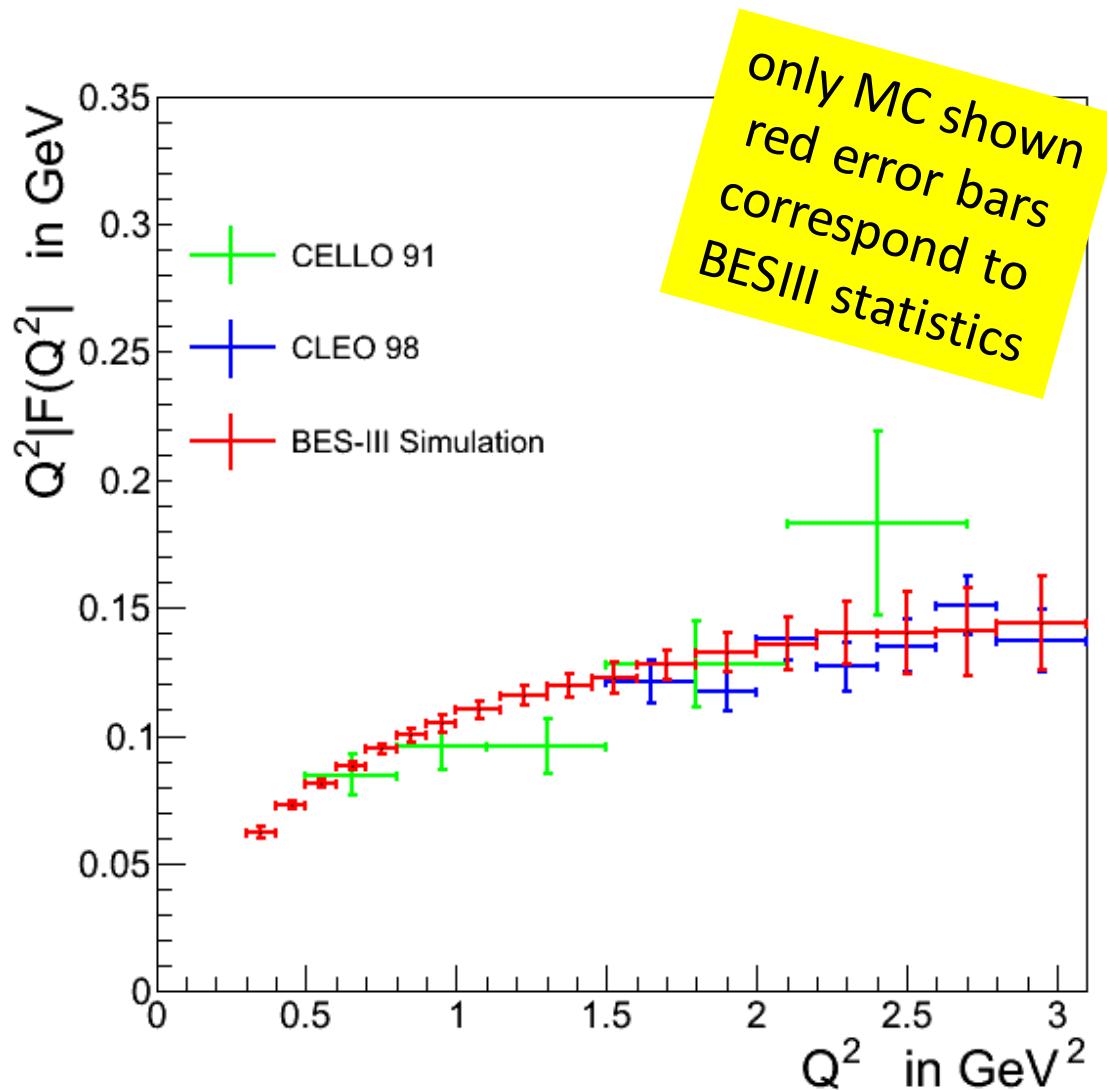
**Strategy:**

Count  
 $\pi^0$  yield in  
bins of  $Q^2$

$d\sigma/dQ^2$

Form factor  
 $F(Q^2)$

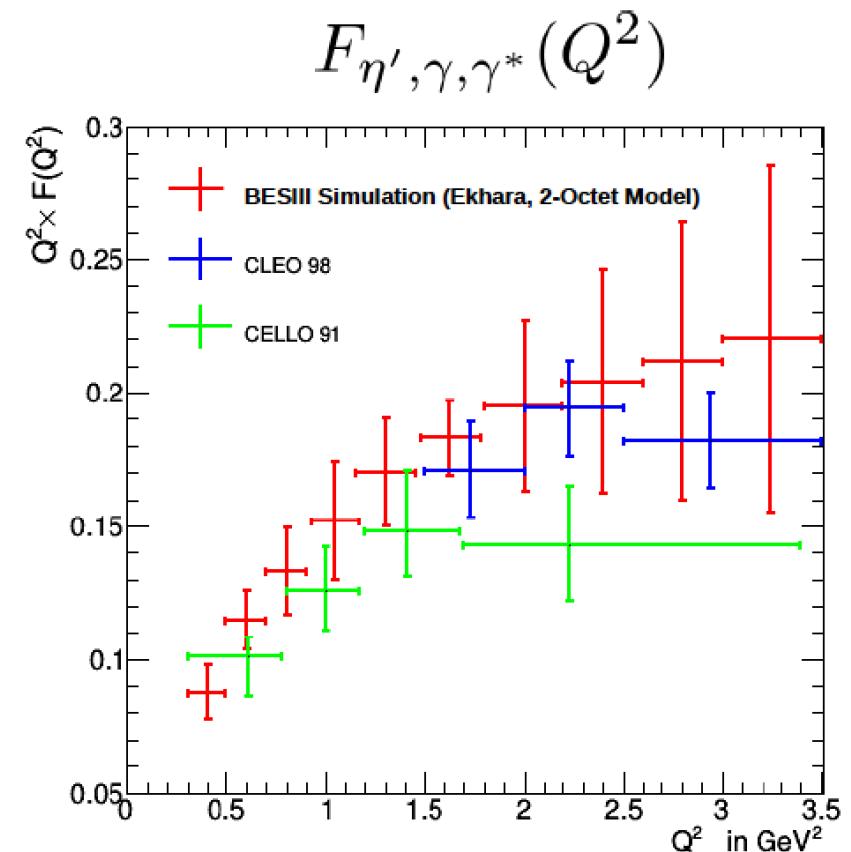
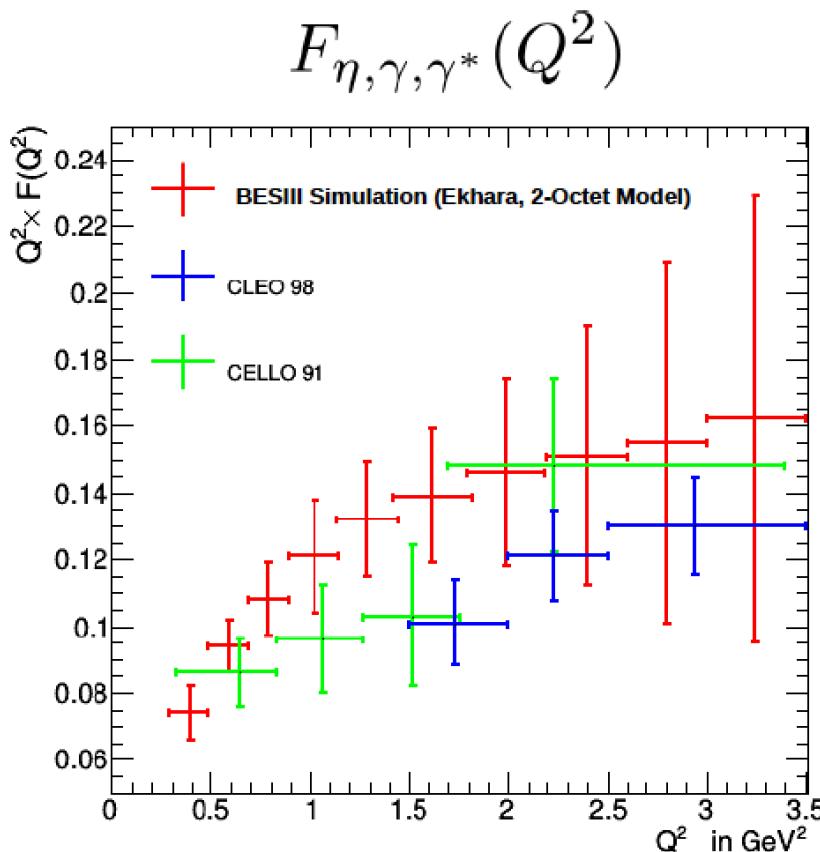
# BES III Analysis: $\gamma \gamma^* \rightarrow \pi^0$



- Full Simulation
  - $L_{int}: 2.92 \text{ fb}^{-1}$
  - Single Tag with both,  $e^\pm$
- Extract TFF for  $0.3 \leq Q^2[\text{GeV}^2] \leq 3.1$

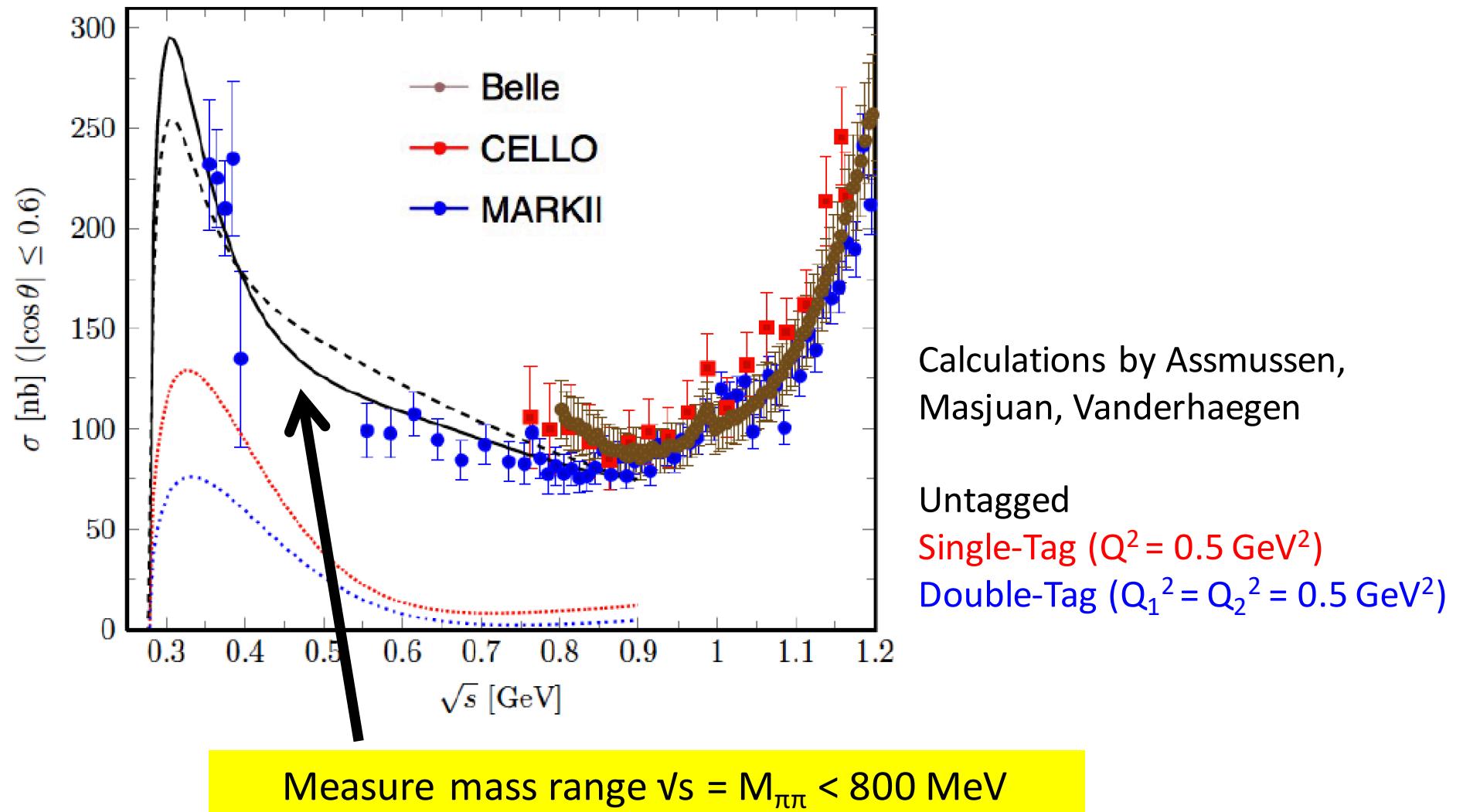
→ Unprecedented  
 $Q^2 < 1.5 \text{ GeV}^2$   
Input for  $(g-2)_\mu$

# BES III Analysis: $\gamma \gamma^* \rightarrow \eta / \eta'$



only MC shown - red error bars correspond to BESIII statistics  
increase statistics by taking into account more decay channels

# BES III Analysis: $\gamma\gamma^* \rightarrow \pi^+\pi^-$



# **Conclusions & Outlook**

# Conclusions and Outlook

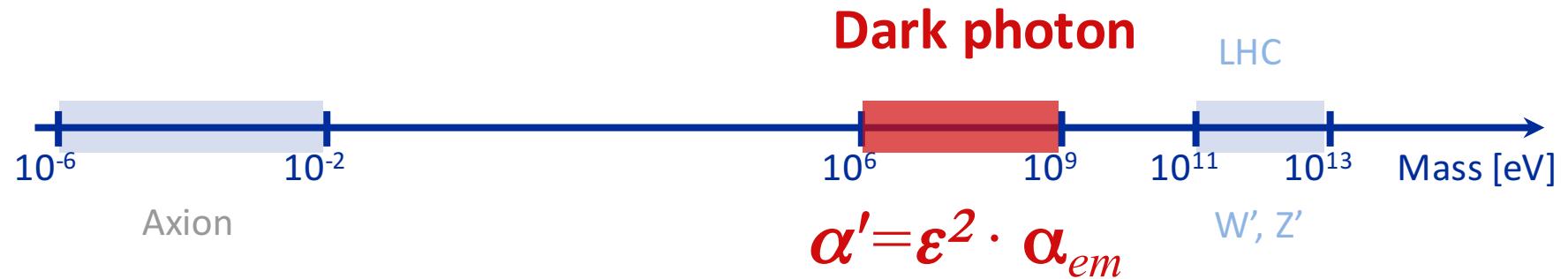
- Important results (to be expected) from BESIII for SM prediction of  $(g-2)_\mu$ 
  - Precision R measurements relevant for HVP contribution
  - Space-like transition form factors of meson(s) relevant for HLbL contribution
- Competing experiments ongoing in Frascati, Novosibirsk, soon BELLE-II (?)

What accuracy can be achieved for  $a_\mu^{\text{had}}$  ?

→ Reduction of factor of 2 of uncertainty of SM prediction in reach



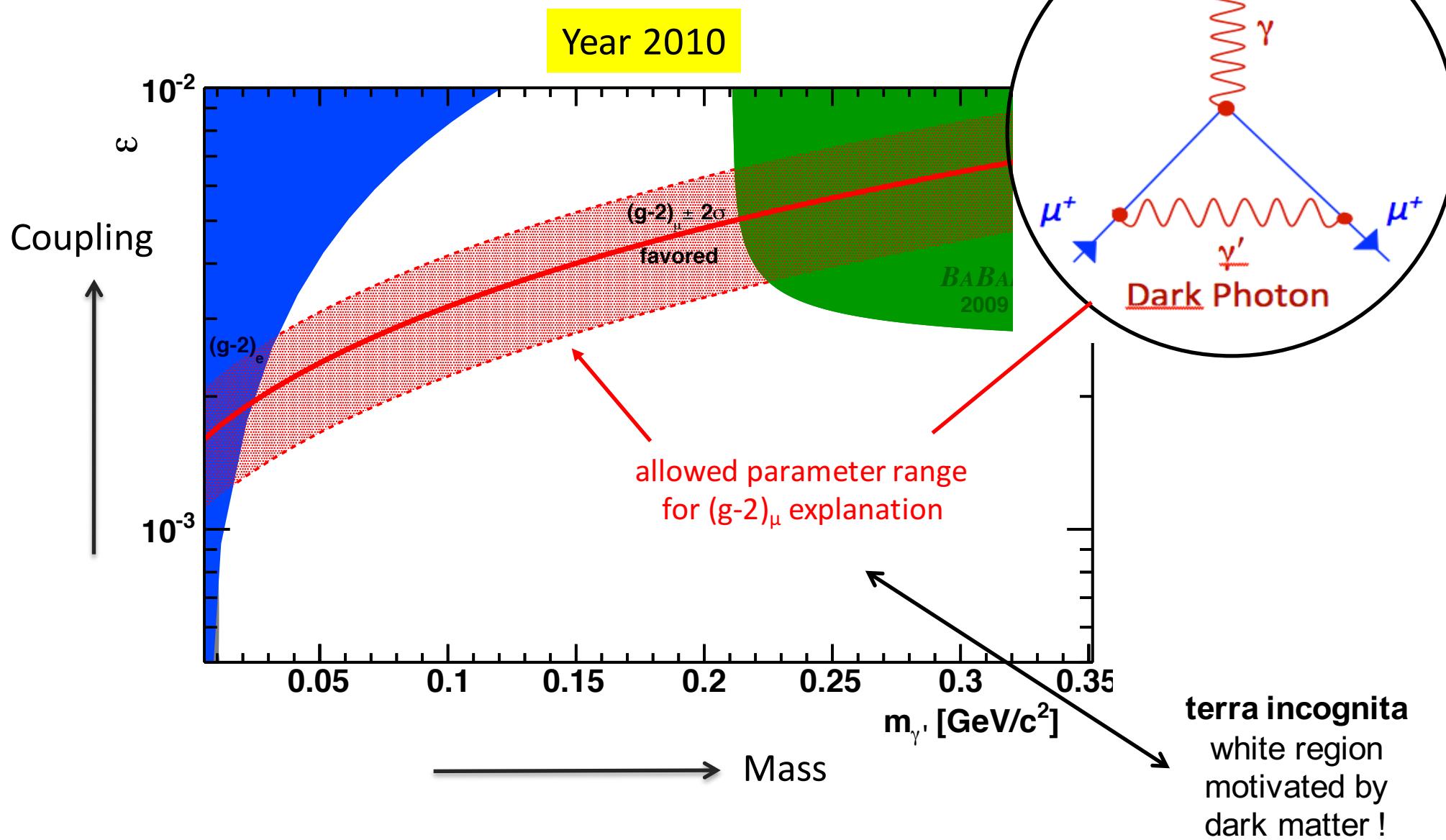
New massive force carrier of extra  $U(1)_d$  gauge group;  
predicted in almost all string compactifications



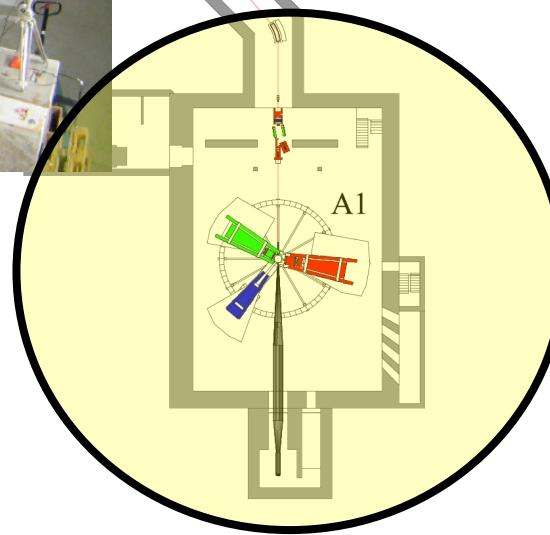
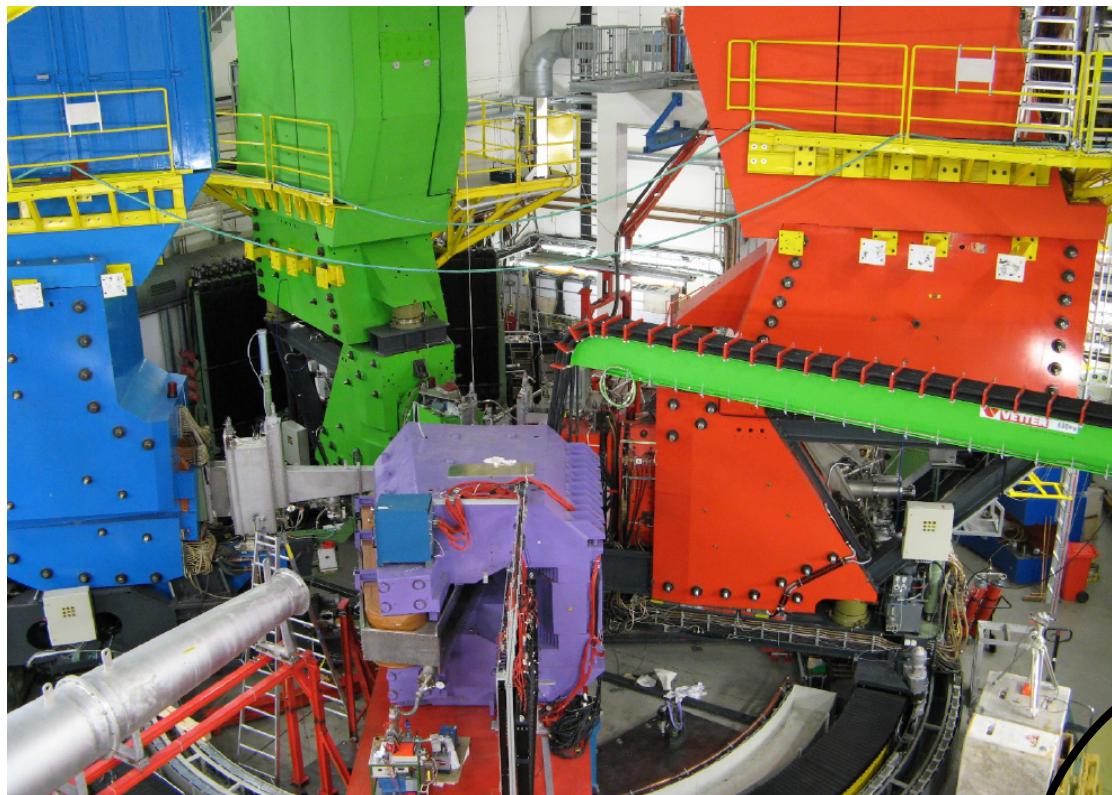
## Search for the $O(\text{GeV}/c^2)$ mass scale in a world-wide effort

- Could explain large number of **astrophysical anomalies**  
 $\text{Arkani-Hamed et al. (2009)}$   
 $\text{Andreas, Ringwald (2010); Andreas, Niebuhr, Ringwald (2012)}$
- Could explain presently seen **deviation of  $3.6\sigma$  between  $(g-2)_\mu$**   
 Standard Model prediction and direct  $(g-2)_\mu$  measurement  
 $\text{Pospelov (2008)}$

# *Dark Photon and $(g-2)_\mu$*



# *Experiment A1: High-Resolution Spectrometers*



## **Experiment A1: Electron Scattering**

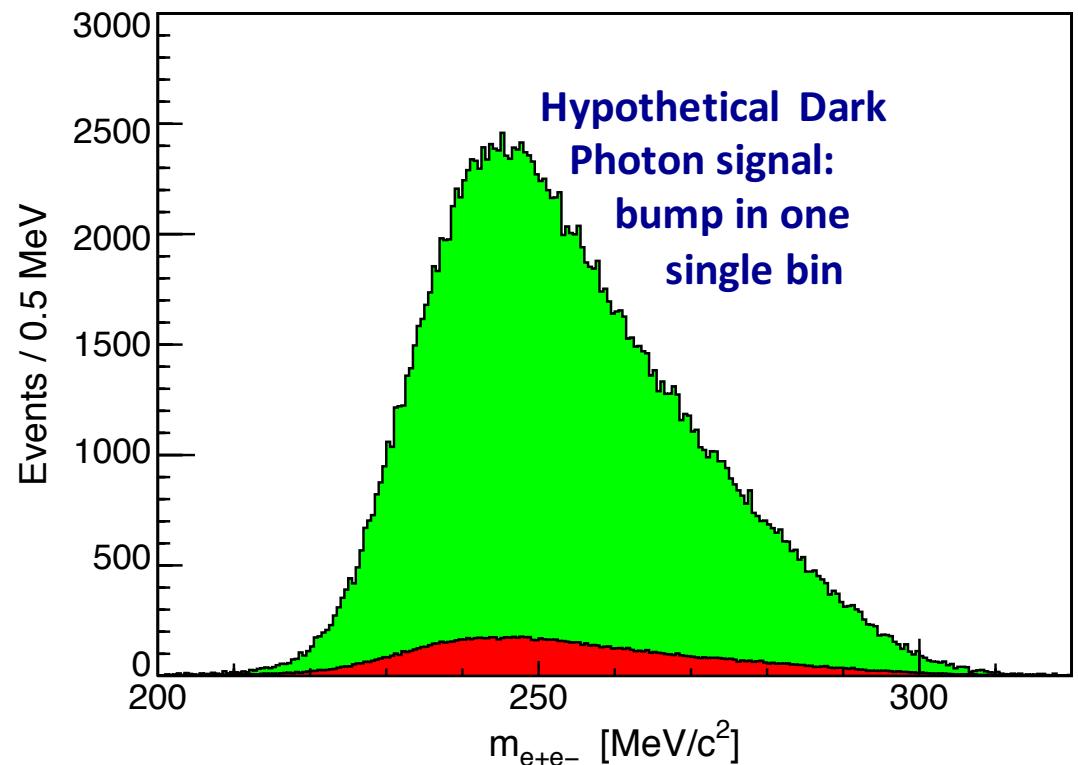
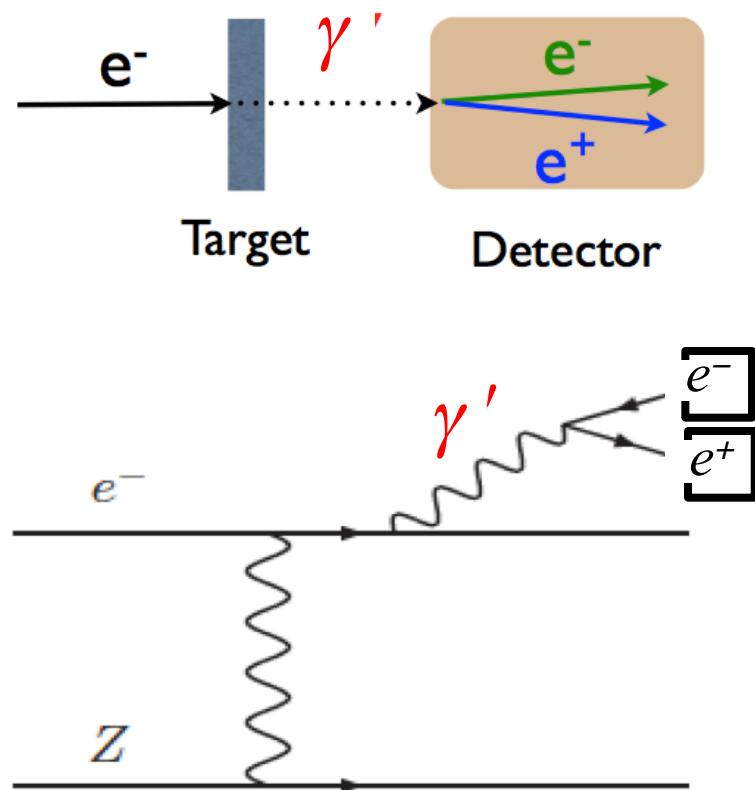
- 4 magnetic focussing spectrometers
- Resolution:  $\delta p/p < 10^{-4}$
- Angular acceptance: <30 mrad

# Results from A1

Low-Energy Electron Accelerators with high Intensity ideally suited for Dark Photon search

Bjorken et al. (2009)

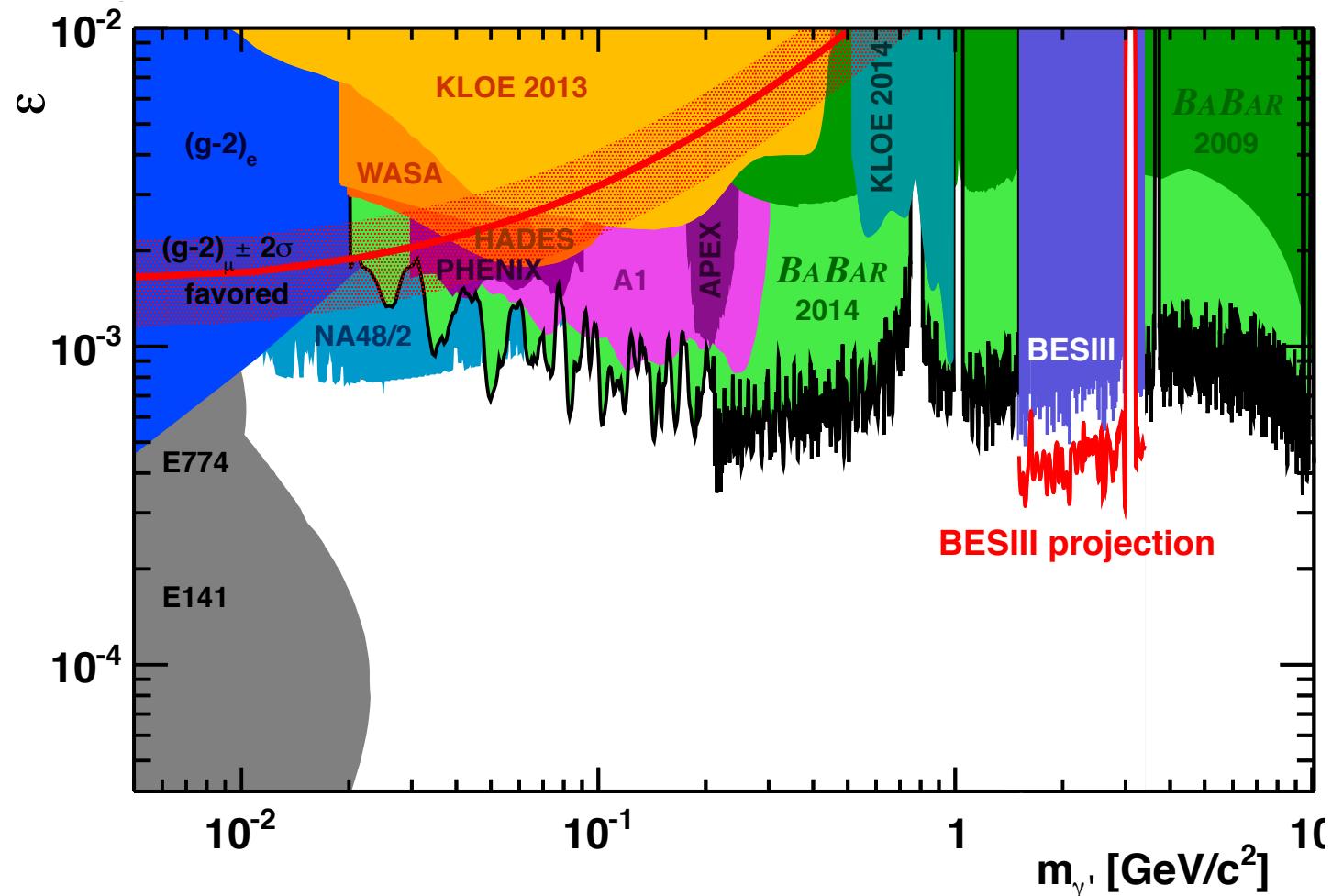
## Signal processes



# Results from A1 @ MAMI

Merkel et al. [A1]  
 PRL '11  
 PRL '14

- $E_{\text{beam}}$  180 - 855 MeV
- 100  $\mu\text{m}$  beam current
- Stack of Ta targets
- 22 kinematic settings
- coincidence between 2 spectrometers for e-, e+

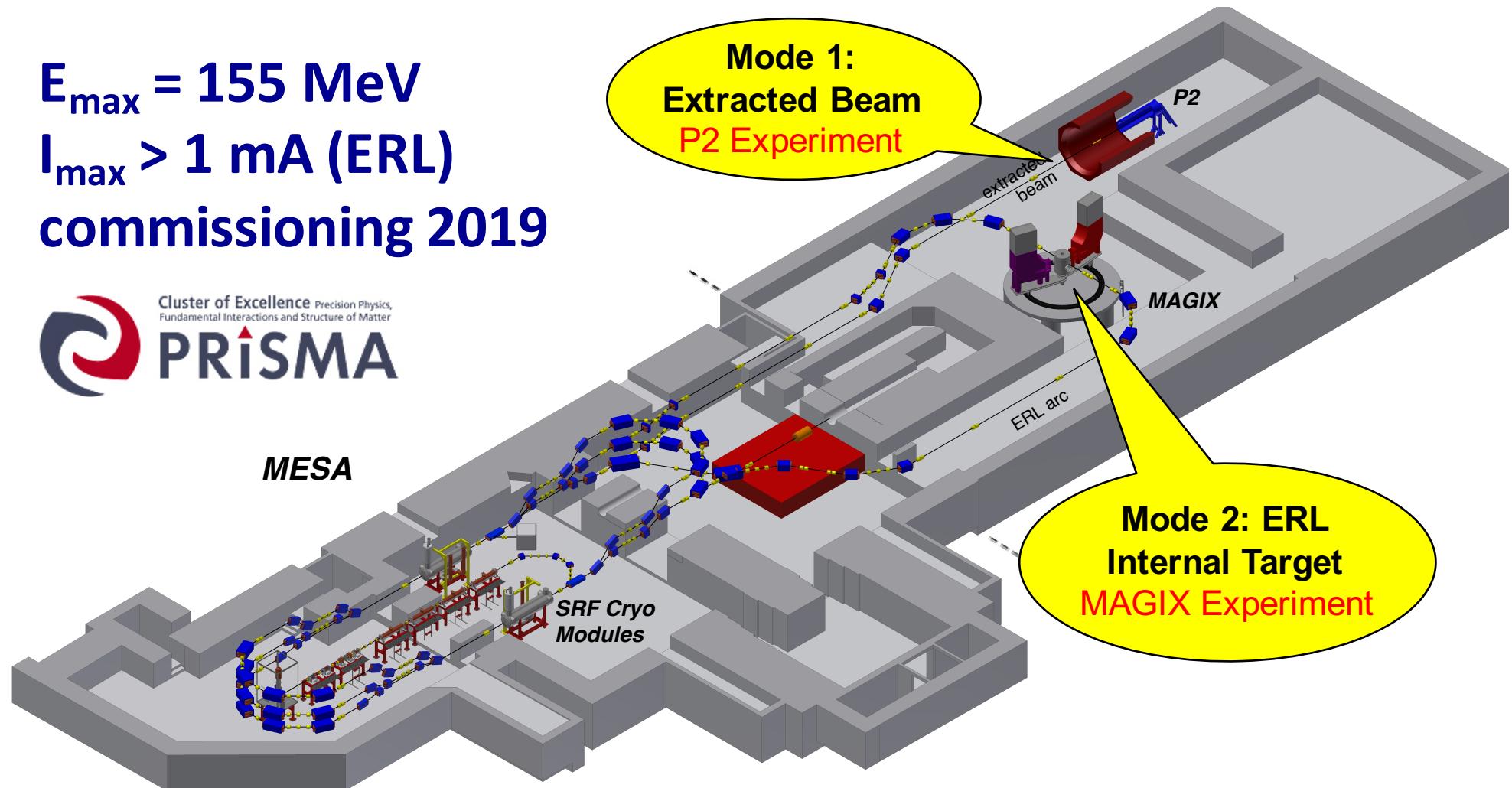


→ at time of publication most stringent  
 limit ruling out major part of the parameter range motivated by  $(g-2)_\mu$

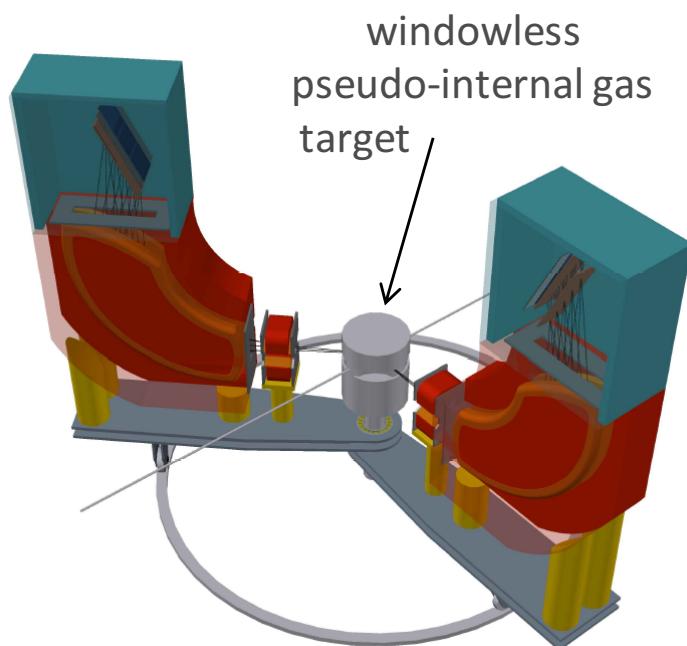
# *Low-Energy Electron Accelerator MESA*

## Mainz Energy-Recovering Superconducting Accelerator

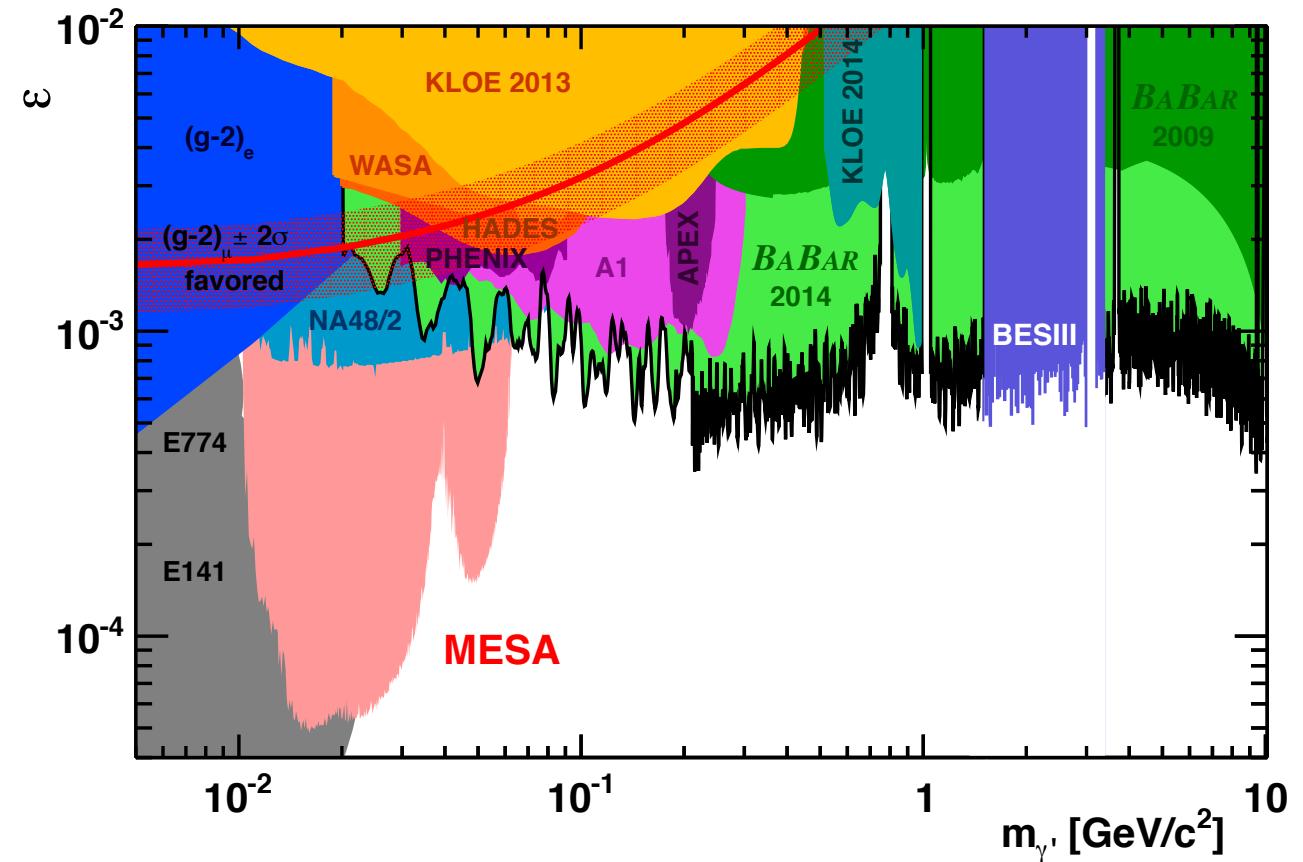
$E_{\max} = 155 \text{ MeV}$   
 $I_{\max} > 1 \text{ mA (ERL)}$   
commissioning 2019



# *Outlook: Dark Photon at MAGIX @ MESA*



**MAGIX / MESA**



**Model 1: Dark Photon coupling to SM particles**

→ parameter range motivated by Dark Photon relation to Dark Matter

**Model 2: Dark Photon not coupling to SM particles**

→ could still explain  $(g-2)_\mu$  discrepancy

→ search possible thanks to excellent momentum resolution of MAGIX spectrometers via missing mass