

QUANTUM SIGNATURES AND DECOHERENCE DURING INFLATION FROM DEEP SUBHORIZON PERTURBATIONS

Arxiv:2503.23150

4 year PHD @ SISSA, Astroparticle group

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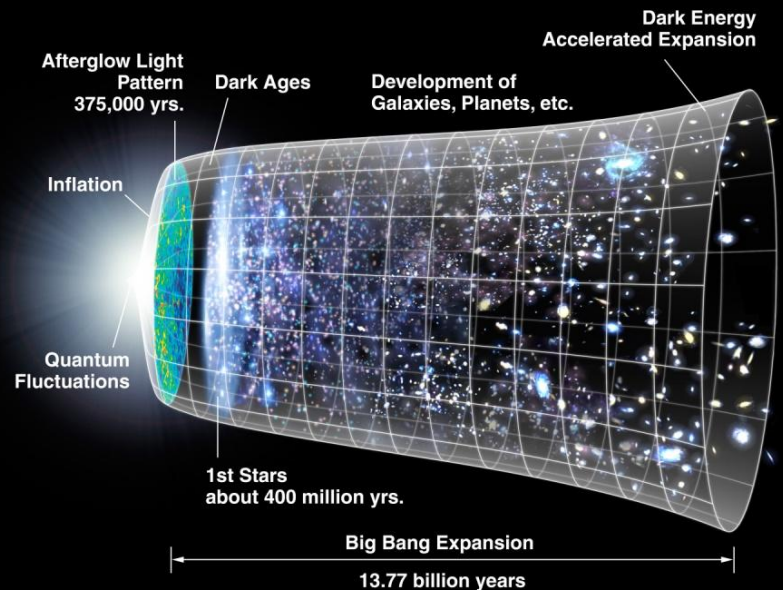
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Mainz, OQS, 22/04/2026

INFLATION AND QUANTUM TO CLASSICAL TRANSITION

- Accelerated expansion driven by one (or more) quantum scalar field(s)
- **Quantum fluctuations** of the scalar field are the **seeds** for the anisotropies we observe in CMB and for the clusters of galaxies (**classical**)



How these **quantum fluctuations** became **classical objects**?



INDEX

- Cosmological perturbations: why we need inflation?
- The problem of the Quantum to classical transition
- Decoherence in single field inflation: state of the art
- Quantum signatures and decoherence during inflation from deep subhorizon perturbations
- Conclusions

HISTORY OF OUR UNIVERSE

- Universe is expanding

$$ds^2 = -dt^2 + a^2(t)dx^2 = a^2(\eta)(-d\eta^2 + dx^2)$$

- Scale factor a

Radiation domination

$$a \propto t^{1/2}$$

Non – Relativistic Matter domination

$$a \propto t^{1/3}$$

proper length $l(t) \propto a(t) x$ comoving length

- Initially whole Universe in thermal equilibrium
- Temperature is decreasing with expansion

$$T \propto 1/a$$

HISTORY OF OUR UNIVERSE: WHAT WE KNOW

- Big Bang Nucleosynthesis (BBN) first direct probe

$$T \simeq O(1) \text{ MeV}$$

To match observed abundance of light elements (H, He) in the Universe must happen in **Radiation Domination**

- Photons γ in equilibrium with electrons, protons until
(after, Compton scattering are inefficient)

$$T \simeq O(1) \text{ eV}$$

- Then photons propagate freely to us: Cosmic Microwave Background that we now observe

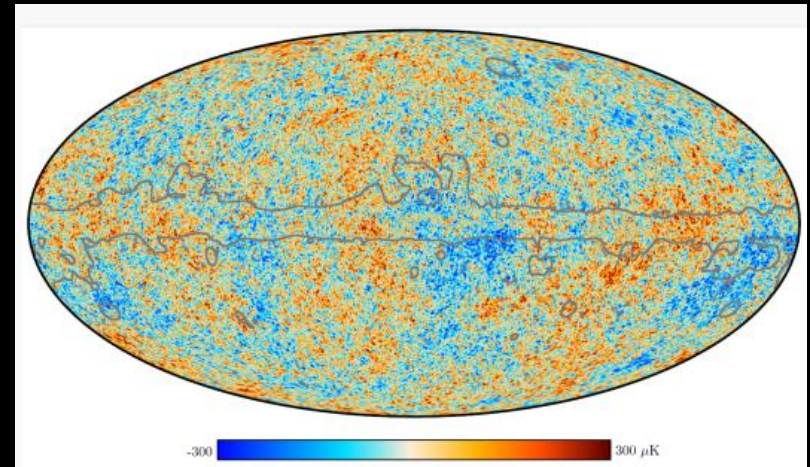
$$T \simeq 10^{-4} \text{ eV} \simeq 2.7 \text{ K}$$

CMB

- Universe is globally isotropic and homogeneous: Very finely tuned!

But small inhomogeneities...

$$\frac{\delta T}{T} \simeq 10^{-5}$$



Planck 2018

Gaussian, stochastic, quasi scale invariant fluctuations; power spectrum (FT 2 point correlation function) against scale k

$$\mathcal{P}(k) = A_s \left(\frac{k}{k_0} \right)^{n_s - 1}$$

- A amplitude 2×10^{-9}
- n_s spectral index 0.9469 ± 0.0042 (Planck 2018)

INFLATION

- Accelerated expansion driven by one (or more) quantum scalar field(s)
- Solves fine tuning problem: homogeneous and isotropic;

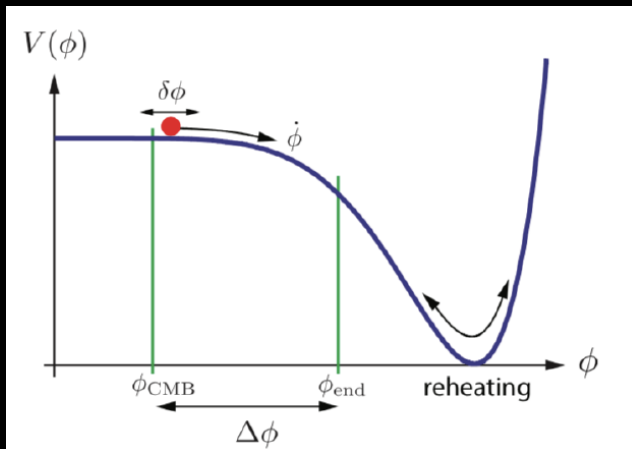
(quasi)de Sitter metric

$$ds^2 = -dt^2 + a^2(t)dx^2 = a^2(\eta)(-d\eta^2 + dx^2)$$

Scale factor:

$$a(t) \simeq e^{Ht} = e^{N_{efolds}} \quad a = -\frac{1}{H\eta}$$

Hubble (energy) scale H : connected to horizon $1/H$ Hubble radius



H almost constant for a long period of time; deviations parametrized by

$$\epsilon = -\frac{\dot{H}}{H^2}$$

THE THEORY OF INFLATION

- Provides a mechanism to explain anisotropies and inhomogeneities from the tiny **quantum fluctuations** of the scalar field

Quantum fluctuations of the scalar field

$$\delta\hat{\phi}$$



$$\hat{v} = a\sqrt{2\epsilon}M_{pl}\hat{\zeta}$$

Scalar (curvature) perturbations ζ , or canonical Sasaki Mukhanov variable v
Region where the universe is **slightly over or underdense**

$$\hat{\zeta}|\zeta\rangle = \zeta|\zeta\rangle$$

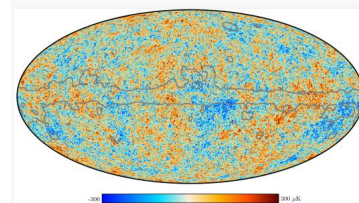
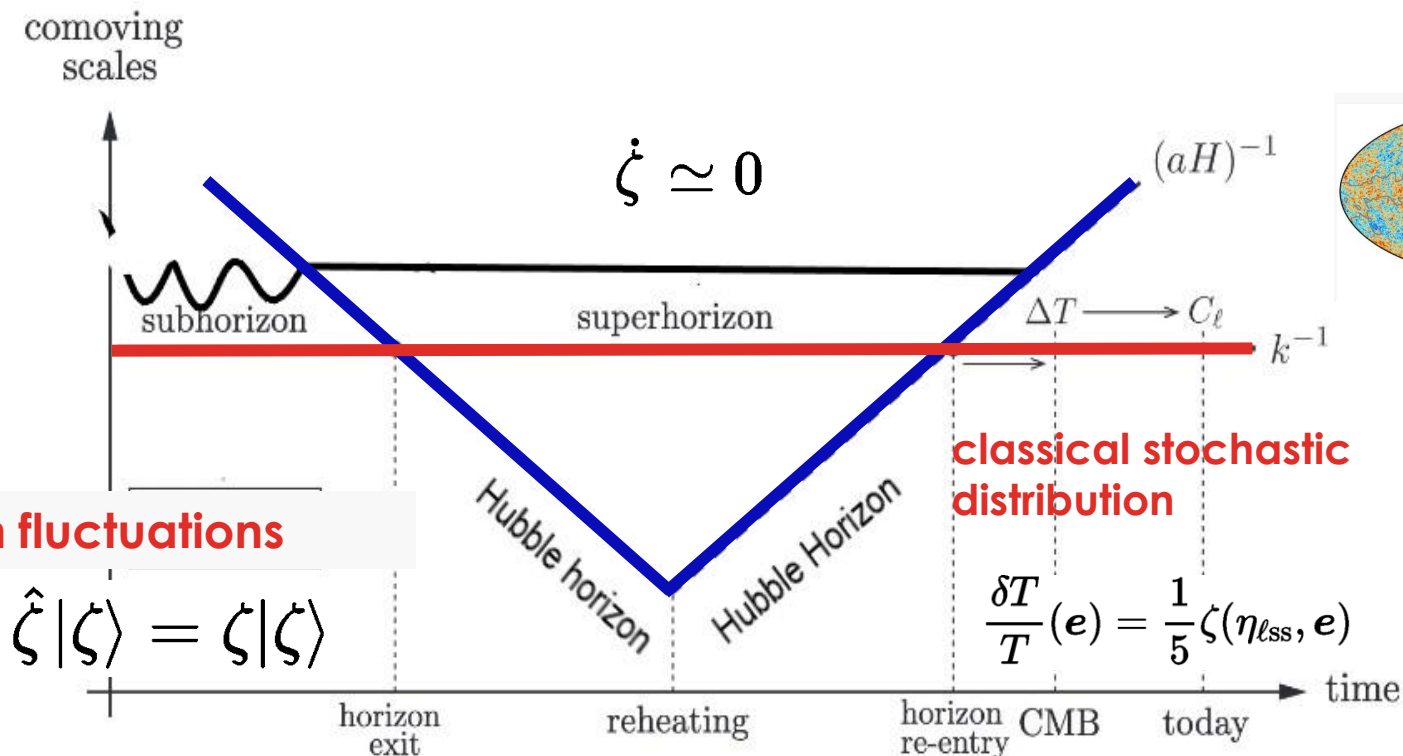
- ζ quantum operator;
- Configuration of perturbations are eigenvectors of ζ

$$g_{ij}(\vec{x}, t) = a^2(t)e^{2\zeta(\vec{x}, t)}(\delta_{ij} + h_{ij}(\vec{x}, t))$$

Tensor perturbation h_{ij} (Stochastic Gravitational Waves Background)

- quantum fluctuations of the scalar field are the **seeds** for the anisotropies we observe in CMB.

Quantum fluctuations



- Credits: Coles and Lucchin, Cosmology, D. Baumann, Lectures on Inflation.

How could quantum fluctuations become classical objects?

How could quantum fluctuations become classical objects?

$$\hat{\zeta} | \text{CMB I} \rangle = \zeta | \text{CMB I} \rangle$$

- ζ quantum operator;
- Configuration of perturbations (~CMB Maps) are eigenvectors of ζ

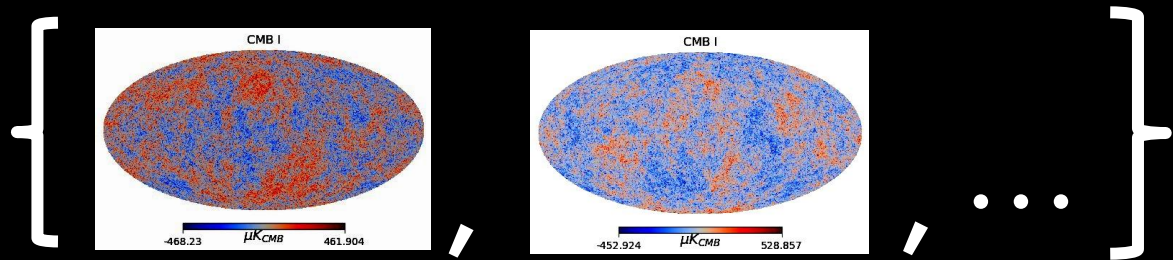
$$|\psi\rangle = | \text{CMB I} \rangle + | \text{CMB I} \rangle + \dots$$

COHERENT **SUPERPOSITION**

Quantum to classical transition!

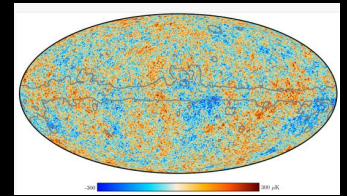


DECOHERENCE!
(after interaction, and entanglement with unobservable environment)



STATISTICAL ENSEMBLE

BUT ONLY ONE REALIZATION!



WHAT DOES DECOHERENCE DO?

Interaction with an unobservable environment: **OPEN QUANTUM SYSTEM**



Entanglement, suppress quantum coherence between different possible outcomes

Interference terms in red

$$\rho_{sys} = \begin{pmatrix} |\zeta_1\rangle\langle\zeta_1| & |\zeta_1\rangle\langle\zeta_2| \\ |\zeta_2\rangle\langle\zeta_1| & |\zeta_2\rangle\langle\zeta_2| \end{pmatrix} \xrightarrow{\text{decoherence}} \rho_{sys} = \text{Tr}_{ENV} \rho_{sys+env} = \begin{pmatrix} |\zeta_1\rangle\langle\zeta_1| & 0 \\ 0 & |\zeta_2\rangle\langle\zeta_2| \end{pmatrix}$$

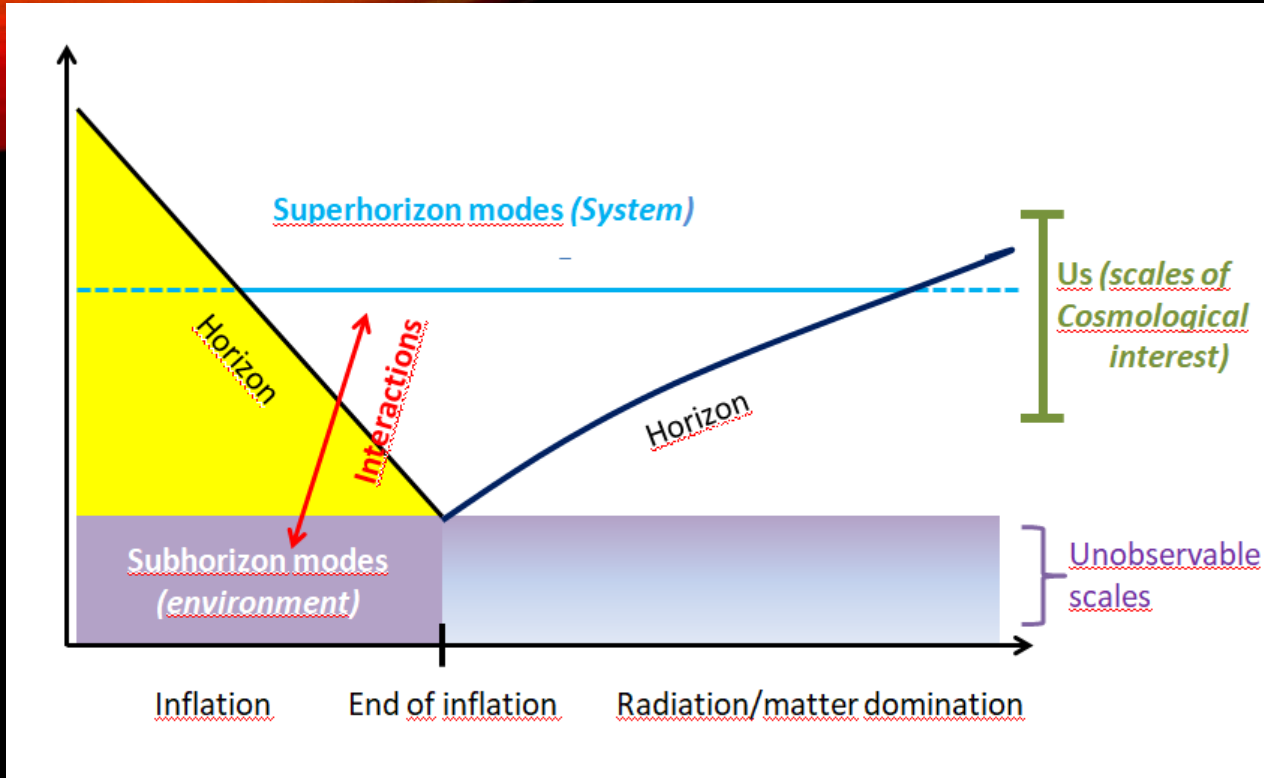
How to quantify? Purity!



Statistical ensemble!

$$\gamma = \text{Tr} \rho^2 = 1 \xrightarrow{\text{decoherence}} \gamma = \text{Tr} \rho_r^2 \rightarrow 0$$

OPEN QUANTUM SYSTEMS



Single field
inflation

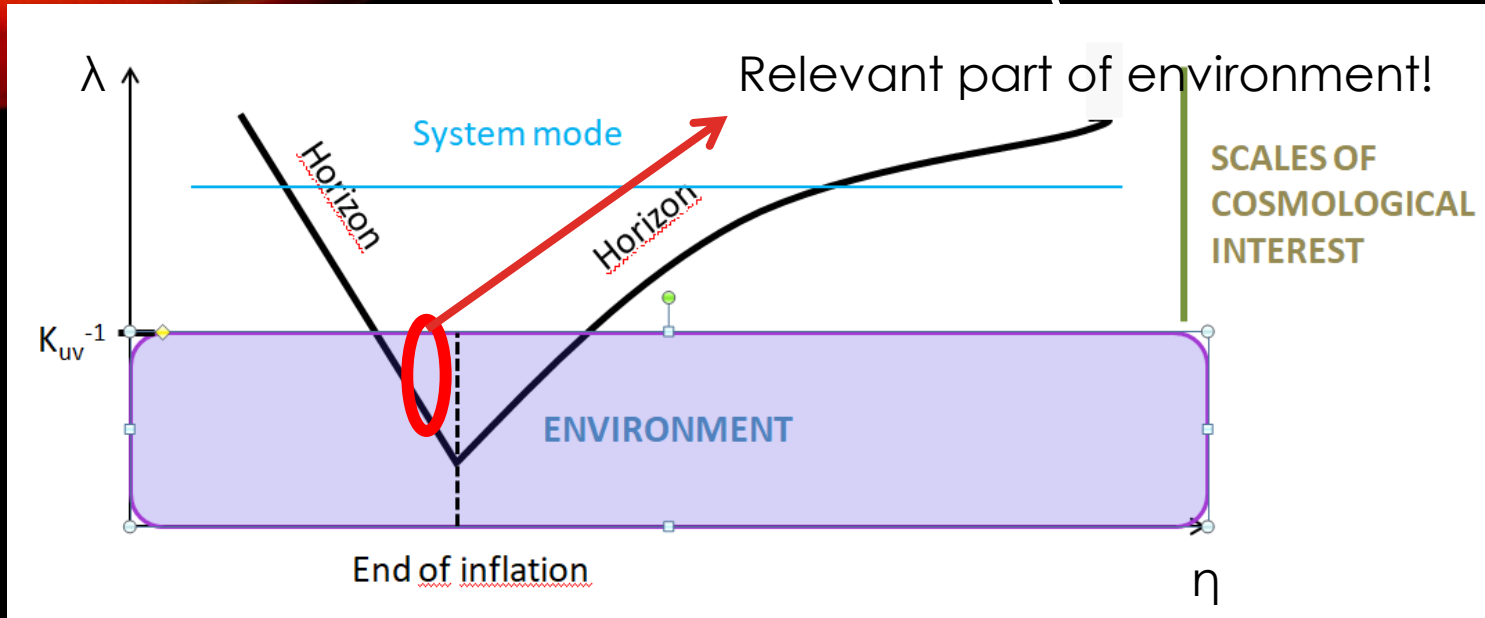
$$\zeta = \zeta_S + \zeta_L$$

(Nonlinear) **gravitational Interaction (GR)**

- **long wavelength system;** ← **Entanglement**
- **short wavelength environment.** →

Decoherence **already during inflation**, after Horizon crossing:
Superhorizon phenomenon.

MINIMAL DECOHERENCE (BURGESS+, 22)



- **Fixed Superhorizon** Environment: $k > 125/\text{Mpc} = k_{uv}$ System: Scalar perturbation, $k < k_{uv}$.

ASSUMPTION: **Superhorizon environment. ONLY in this case** time derivative interactions are suppressed!

- GR nonlinear gravitational interactions (Maldacena, 2003);

$$S = \frac{\epsilon M_{pl}^2}{8} \int dt d^3x \left(a^3 \zeta \dot{h}_{ij} \dot{h}_{ij} + a \zeta \partial_l h_{ij} \partial_l h_{ij} - 2a^3 \dot{h}_{ij} \partial_l h_{ij} \partial_l (\nabla^2)^{-1} \dot{\zeta} \right)$$

- Considered **ONLY** spatial derivatives interactions (circled ones)!

OUR WORK

MAIN ORIGINAL POINTS:

- Consider a time dependent environment of **subhorizon modes**;
- Show that decoherence can be achieved also by **just subhorizon environment: dominant interactions are derivativeless interactions**;
- We consider for the first time **all the interactions**, underlining the importance **of the interplay between mixed couples**.
- **Resummation to some quantum corrections to the v correlators**:
 - Lamb Shift (unitary corrections) for power-spectrum and bispectrum of the Sasaki Mukhanov variable v ;
 - Non unitary corrections to the power spectrum.

IN THE MEANTIME:

- Comment on **Quantum master equation, Markovianity/non-Markovianity**;
- Evaluate effects on the quantum master equation of **time dependent environment**.

OUR WORK

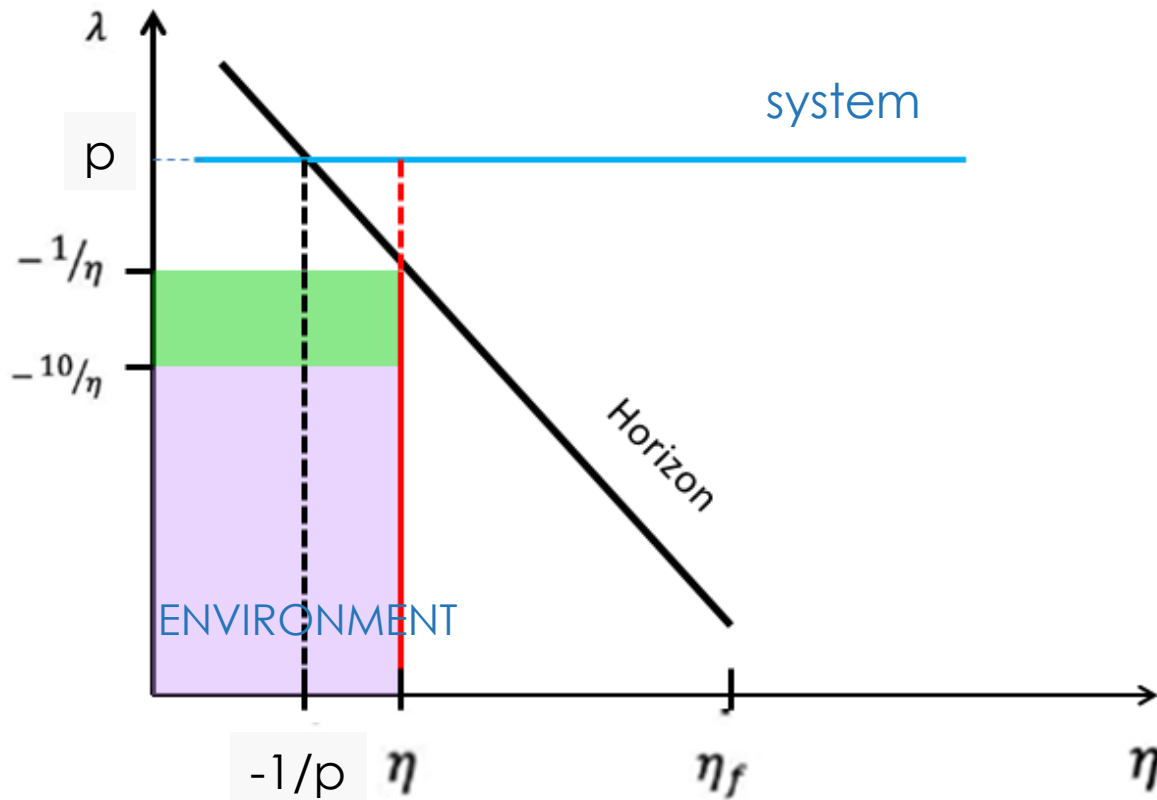
- Environment of subhorizon tensorial modes (i.e. GW, h_{ij});
- System of superhorizon curvature scalar modes, ζ
(canonically norm., \mathbf{v})
- GR non linear gravitational interactions (Gangui+1993, Maldacena 2003)

$$S = \frac{\epsilon M_{pl}^2}{8} \int dt d^3x \left(a^3 \zeta \dot{h}_{ij} \dot{h}_{ij} + a \zeta \partial_l h_{ij} \partial_l h_{ij} - 2a^3 \dot{h}_{ij} \partial_l h_{ij} \partial_l (\nabla^2)^{-1} \dot{\zeta} \right)$$

SUBHORIZON ENVIRONMENT: WE CONSIDER THE INTERPLAY BETWEEN ALL INTERACTIONS!

See also: Burgess et al, Arxiv:2509.07769

OUR MODEL: THE ENVIRONMENT



SYSTEM: **Superhorizon**
Scalar Mode.

↕ **Entanglement**

ENVIRONMENT:
Deep subhorizon modes
Of **Gravitational waves**.

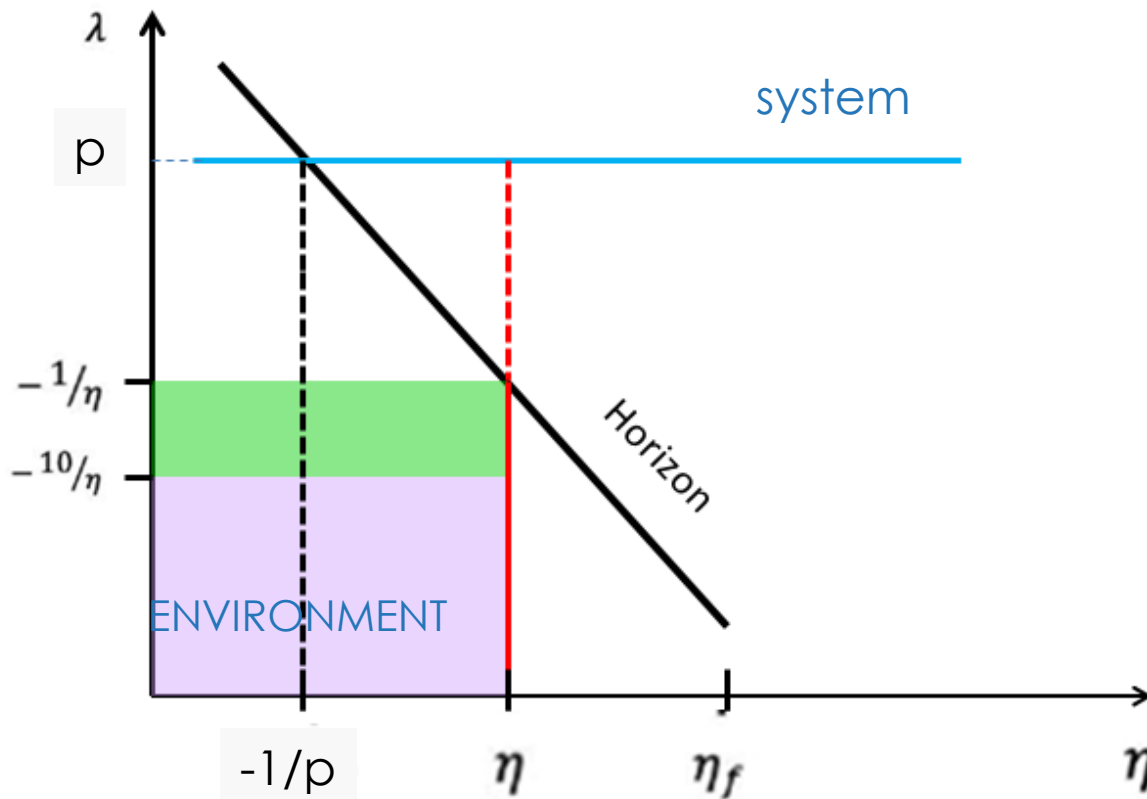
1. Time dependent
environment

2. Short Correlation time!

$$\tau_{env} \ll \tau_{sys}$$

$$\tau_{env} \ll \tau_{int}$$

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QUANTUM MASTER EQUATION

$$\text{Tr}_{\mathcal{E}} \frac{d}{d\eta} \rho(\eta) = \frac{d\rho_r}{d\eta}(\eta) = -g^2 \int_{\eta_{in}}^{\eta} d\eta' \text{Tr}_{\mathcal{E}} [H_{int\ i}(\eta), [H_{int\ j}(\eta'), \rho_r(\eta')]] \quad i, j = 1, 2, 3$$

Convolution!

- BORN-MARKOV APPROXIMATION: density matrix evolves slowly (Interaction picture)

$$\rho_r(\eta') \rightarrow \rho_r(\eta)$$

$$\tau_{env} \ll \tau_{int} \propto 1/g^2$$

Quantum master equation:

$$\rho_r'(\eta) = -g(\eta) \int_{\eta_0}^{\eta} d\eta' g(\eta') \sum_{\mathbf{p}} [v_{\mathbf{p}}(\eta) v_{-\mathbf{p}}(\eta') \rho_r(\eta) K(p, \eta, \eta') + \rho_r(\eta) v_{-\mathbf{p}}(\eta') v_{\mathbf{p}}(\eta) K^*(p, \eta, \eta') - v_{\mathbf{p}}(\eta) \rho_r(\eta) v_{-\mathbf{p}}(\eta') K^*(p, \eta, \eta') - v_{-\mathbf{p}}(\eta') \rho_r(\eta) v_{\mathbf{p}}(\eta) K(p, \eta, \eta')]$$

Memory in:

Interactions

Free system operator!

ENVIRONMENTAL CORRELATION FUNCTIONS (FAST, peaked around $\eta' \sim \eta$)

QUANTUM MASTER EQUATION

- “Equation of motion” for the Density Matrix of the System (canonical form)

$$\frac{d\rho_r}{d\eta} = -i[H + H_{LS}, \rho_r(\eta)] + \sum_p D_{11}(\eta) \left(v_p(\eta)\rho_r(\eta)v_p^\dagger(\eta) - \frac{1}{2}\{v_p^\dagger(\eta)v_p(\eta), \rho_r(\eta)\} \right)$$



Lamb Shift Hamiltonian

-finite renormalization of the Unitary hamiltonian, gives corrections to **spectral index of Power Spectrum**.

Non Unitary part:

- Decoherence;
- non-Unitary correction to observables.

$D_{11}(\eta)$ “canonical decay rate”

$$D_{11}(\eta) = g(\eta) \int_{-1/p}^{\eta} d\eta' g(\eta') 2\Re K(\eta, \eta') A(p, \eta, \eta')$$

System operator memory:

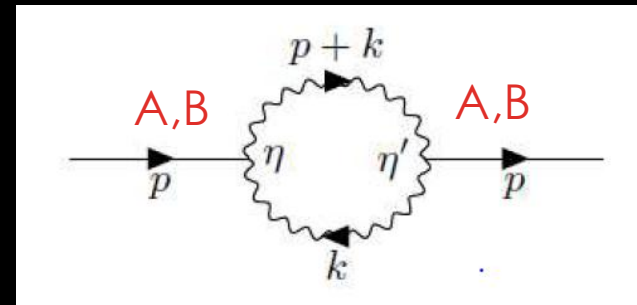
$$v_p(\eta') = v_p(\eta) A(p, \eta, \eta') + \dots$$

SUBHORIZON ENVIRONMENT: WE CONSIDER THE INTERPLAY BETWEEN ALL INTERACTIONS!

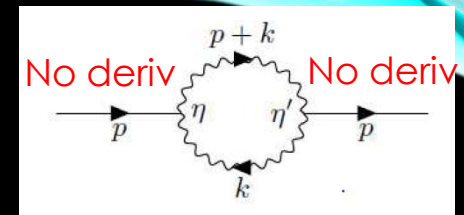
$$S = \frac{\epsilon M_{pl}^2}{8} \int dt d^3x \left(a^3 \zeta \dot{h}_{ij} \dot{h}_{ij} + a \zeta \partial_l h_{ij} \partial_l h_{ij} - 2a^3 \dot{h}_{ij} \partial_l h_{ij} \partial_l (\nabla^2)^{-1} \dot{\zeta} \right)$$

A) DERIVATIVELESS interaction, more important contributions.

B) DERIVATIVE interactions (just like the circled one).



DERIVATIVELESS INTERACTIONS



- $D_{11} > 0$ **positive!**

$$D_{11}^{int11} = \frac{\epsilon H^2}{4\pi^2 M_{pl}^2 \eta^2} \left(\frac{\pi}{2} - 1.52 \right) \simeq \frac{\epsilon H^2}{4\pi^2 M_{pl}^2 \eta^2} 0.05$$

Derivativeless interactions gives **Markovian evolution!**

- We can achieve decoherence by just environment of **subhorizon modes!**

$$\frac{1}{\gamma^2} = 1 + \frac{\epsilon H^2}{\pi^2 M_p^2} 1.25 \times 10^{-3} \left(\frac{aH}{p} \right)^3 \lesssim 10^{-18} e^{3(N_{end} - N_*)}$$

$$\frac{\epsilon H^2}{M_{pl}^2} \lesssim 10^{-13}$$

$$\left(\frac{\lambda_{phys}}{R_H} \right)^3 = e^{3(N_{end} - N_*)}$$

Decoherence happens when system is superhorizon!

If saturating the bounds, then at least: $N_{end} - N_* \simeq 15$ e-folds

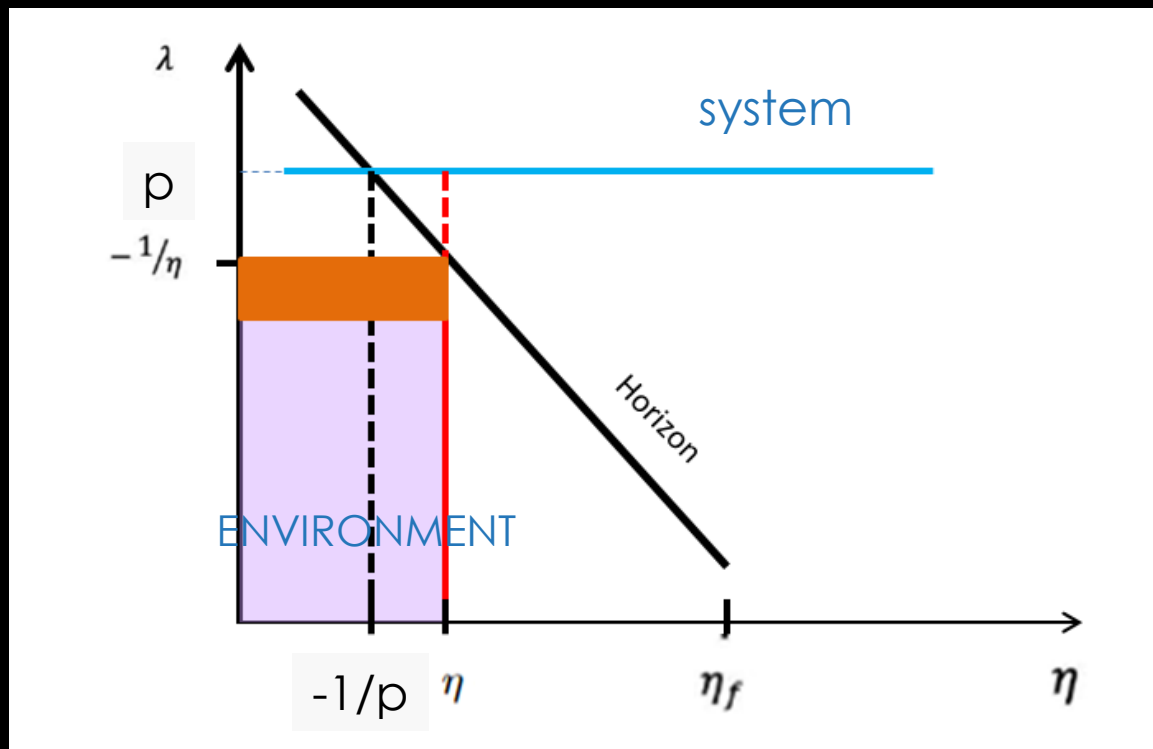
CMB well decohered!!

TIME DEPENDENT ENVIRONMENT

• Also used in: ('19 Gong-Seo, '21-'22 Brahma et al.,....)

'23 Burgess: nobody computed the effect

$$\text{Tr}_{ENV(\eta)} \frac{d}{d\eta} \rho(\eta) \neq \frac{d}{d\eta} \text{Tr}_{ENV(\eta)} \rho(\eta) = \frac{d}{d\eta} \rho_r(\eta)$$



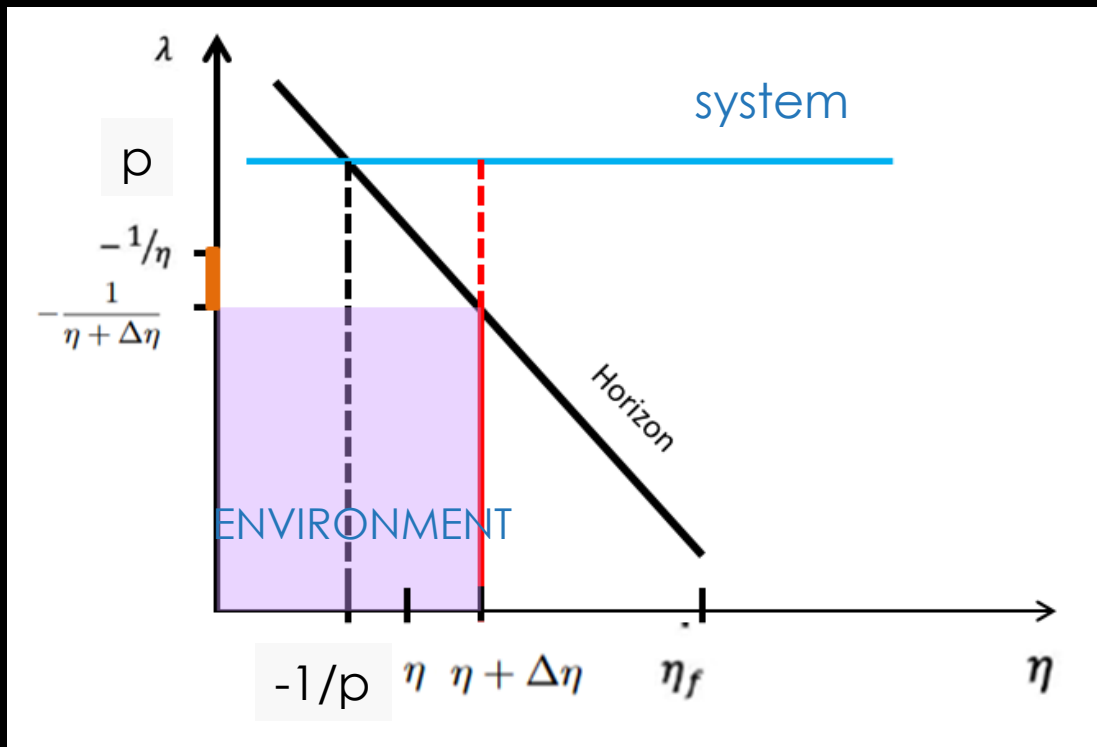
Orange modes:
Crossing the horizon
in $\Delta\eta$

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$$\text{Tr}_{ENV(\eta)} \frac{d}{d\eta} \rho(\eta) \not\approx \frac{d}{d\eta} \text{Tr}_{ENV(\eta)} \rho(\eta) = \frac{d}{d\eta} \rho_r(\eta)$$



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TIME DEPENDENT ENVIRONMENT

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$$\begin{aligned} \rho_{r,I}(\eta + \Delta\eta) - \rho_{r,I}(\eta) &= -\Delta\eta g(\eta) \int_{\eta_0}^{\eta} d\eta_2 g(\eta_2) \text{Tr}_{E(\eta)} [H_{\text{int}}(\eta), [H_{\text{int}}(\eta_2), \rho(\eta_2)]] \\ &- \int_{\eta_0}^{\eta} d\eta_1 g(\eta_1) \int_{\eta_0}^{\eta_1} d\eta_2 g(\eta_2) \text{Tr}_{E(\eta+\Delta\eta)-E(\eta)} [H_{\text{int}}(\eta_1), [H_{\text{int}}(\eta_2), \rho(\eta_2)]] \end{aligned}$$

THE CANONICAL FORM IS RESPECTED!!

• **Just a modification of D_{11}**

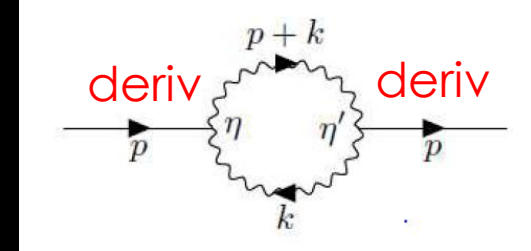
$$\Delta D_{11} \simeq -0.02 \frac{H^2 \epsilon}{8\pi^2 M_{pl}^2}$$

• **Smaller, does not change sign to D_{11}**

INTERPLAY WITH OTHER INTERACTIONS

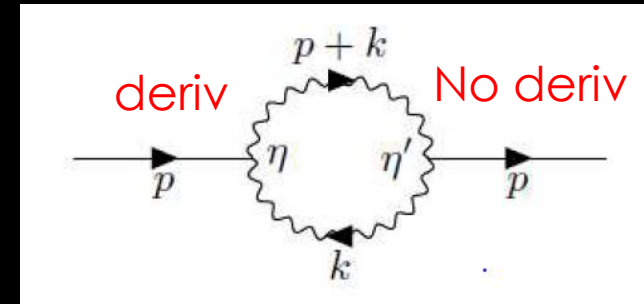
DERIVATIVE INTERACTIONS

- NEGLIGIBLE!! (Just for deep subhorizon modes)



MIXED DERIVATIVE-DERIVATIVELESS INTERACTIONS

- **Mixed terms give NEGATIVE CONTRIBUTIONS**



$$D_{11}^{int1-23} \simeq -\frac{\epsilon H^2}{4M_{pl}^2 \eta^2} 0.11$$

- **More negative** than the previous one! **NON MARKOVIAN!**

$$D_{11}^{TOT} \simeq -\frac{\epsilon H^2}{4M_{pl}^2 \eta^2} 0.06$$

TOT: $D_{11} < 0!$

'22 Burgess+ Minimal decoherence: if $D_{11} < 0$, **Strong Markovian approximation!**

$$\tau_{env} \ll \tau_{int}$$

Markovian approximation: $\rho_r(\eta') \rightarrow \rho_r(\eta)$

System memory

$$D_{11}(\eta) = g(\eta) \int_{-1/p}^{\eta} d\eta' g(\eta') 2\Re K(\eta, \eta') A(p, \eta, \eta')$$

Neglects also **FREE SYSTEM MEMORY!**

$$v_p(\eta') \rightarrow v_p(\eta)$$

$$A(p, \eta, \eta') \rightarrow 1$$

For us **very well justified:**

$$\tau_{env} \simeq \frac{1}{10aH} \ll \tau_{sys} \simeq \frac{1}{aH}$$

The sum is now **positive** again!!

$$D_{11}^{SMAR} = D_{11}^{int11} + D_{11}^{int1-23} \simeq \frac{\epsilon H^2}{4M_{pl}^2 \eta^2} 5 \times 10^{-4}$$

In the end, decoherence is nevertheless effective:

$$N_{end} - N_* \simeq 17 \text{efolds}$$

Still, no definitive proof...

QUANTUM MASTER EQUATION

- “Equation of motion” for the Density Matrix of the System (canonical form)

$$\frac{d\rho_r}{d\eta} = -i[H + H_{LS}, \rho_r(\eta)] + \sum_p D_{11}(\eta) \left(v_p(\eta) \rho_r(\eta) v_p^\dagger(\eta) - \frac{1}{2} \{v_p^\dagger(\eta) v_p(\eta), \rho_r(\eta)\} \right)$$



Lamb Shift Hamiltonian

-finite renormalization of the Unitary hamiltonian, gives corrections to **spectral index of** Power Spectrum.

Non Unitary part:

- Decoherence;
- non-Unitary correction to observables.

LAMB SHIFT

- Compute corrections to Power Spectrum due to **trilinear interactions** at second order: "**loop quantum correction**";
- Method: in-in formalism, just a **unitary** dynamics;
- But...late time secular effects: large logarithms in corrections (Seery'10 for a review)

$$\Delta P_{vv} \propto \log(-k\eta_f), \log^2(-k\eta_f), \dots, \log^n(-k\eta_f) \dots = \log \frac{k}{aH}, \log^2 \frac{k}{aH}, \dots, \log^n \frac{k}{aH} \dots$$

•May break perturbation theory!

- Many methods in the past for resummation.
- By solving QME you automatically resum!

$$\mathcal{P}(k, \eta) \propto e^{\frac{2\epsilon H^2}{4\pi^2 M_{pl}^2} \ln(-k\eta)} + \text{other terms}$$

In general, **not in single field inflation**, where there are also quartic Interactions and backreaction effects that cancel this effect!
But here we are interested in showing the resummation

LAMB SHIFT:UNITARY RENORMALIZATION

- Entanglement with environment “renormalizes” in a finite way energy levels of the system (in this case, mass);

Modifies spectral index in the ν Power Spectrum:

$$\delta n_s \simeq \frac{\epsilon H^2}{4M_{pl}^2 \pi^2} 2.4$$

- Blue Correction to spectral index n_s (bigger power at smaller scales)
- No secular corrections.

$$\mathcal{P}(k) = A_s \left(\frac{k}{k_0} \right)^{n_s - 1}$$

- **NON-Perturbative resummation!!**
- Quantum “loop” corrections, but **“automatically” produce resummation by considering the interaction with an environment for decoherence.**

$$\mathcal{P}(k, \eta) \propto e^{\frac{2\epsilon H^2}{4\pi^2 M_{pl}^2} \ln(-k\eta)} + \text{other terms}$$

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$$\mathcal{P}(k) = A_s \left(\frac{k}{k_0} \right)^{n_s - 1}$$

Corrections from non unitary part:

Same order, different form

$$\frac{\delta A_s}{A_s} = \left(\frac{\pi}{2} - 1.5 \right) \frac{\epsilon H^2}{432 \pi^2 M_{pl}^2}$$

Of course, too little (Gravitational interactions)!

$$\frac{\epsilon H^2}{M_{pl}^2} \lesssim 10^{-13}$$

What about specific models with stronger non Gaussianity?

Lamb Shift for the Bispectrum

Tensorial environment on scalar system

$$\langle v(\vec{k}_1) v(\vec{k}_2) v(\vec{k}_3) \rangle = (2\pi)^3 B(k_1, k_2, k_3) \delta^3(\vec{k}_1 + \vec{k}_2 + \vec{k}_3)$$

FT of the 3-point correlation function

Important for the investigation of non gaussianity

- Dealt with (in a different way) in Daddi Hammou+'22, Martin+'18, A.Salcedo+24
- Three modes k_1, k_2, k_3 superhorizon at the end of inflation

$$B(k_1, k_2, k_3, \eta) = B\left(k_1, k_2, k_3, -\frac{1}{k_1}\right) e^{\frac{3.6\epsilon H^2}{4\pi^2 M_{pl}^2} \ln(-k_1\eta)} + \text{other terms}$$

Again, **NON PERTURBATIVE RESUMMATION!**

CONCLUSIONS

- We computed **decoherence in single field inflation**, in an environment only of subhorizon modes;
- We considered more than just one interaction at a time, but also the interplay between them, underlining the importance **of non-Markovian effects**;
- We elaborated on possible ways to deal with non-Markovianity, and the possible limits of application of the **Strong Markovian approximation**;
- We evaluated the impact of a **time dependent environment** onto the quantum master equations;
- We show the resummation properties of the quantum master equation by applying it to some corrections to the **Power spectrum and Bispectrum**.

TAKE HOME MESSAGE AND FUTURE PROJECTS

- **Non unitary evolution during inflation is needed for explaining quantum to classical transition. Non unitary effects should be there even** in a minimal setting:
- The evolution of perturbations is never closed: in cosmology multiple environments are always present! Open quantum system investigation needed!
- (non-)Markovianity is ubiquitous in inflation! How to deal with it?
- Can we prove, either directly, or indirectly, e.g. through corrections by decoherence, the quantum nature of inflationary perturbations?
- Small-scale modes
 - If modes cross the horizon in the last e-folds of inflation *may not have the time to decohere?*
 - There may be genuine quantum features! Gravitational waves?*

GRAVITATIONAL WAVE-LENSING BEYOND RAYS: A DISORDER SYSTEM APPROACH

Arxiv: 2604.15313

With R. Amoruso (UniPd), G.Braga (GSSI), A.Garoffolo (Upenn),
N.Bartolo (UniPd), S.Matarrese (UniPd)

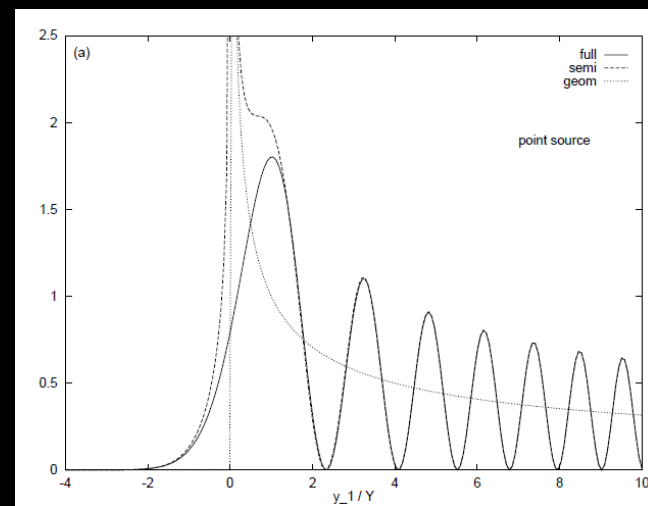
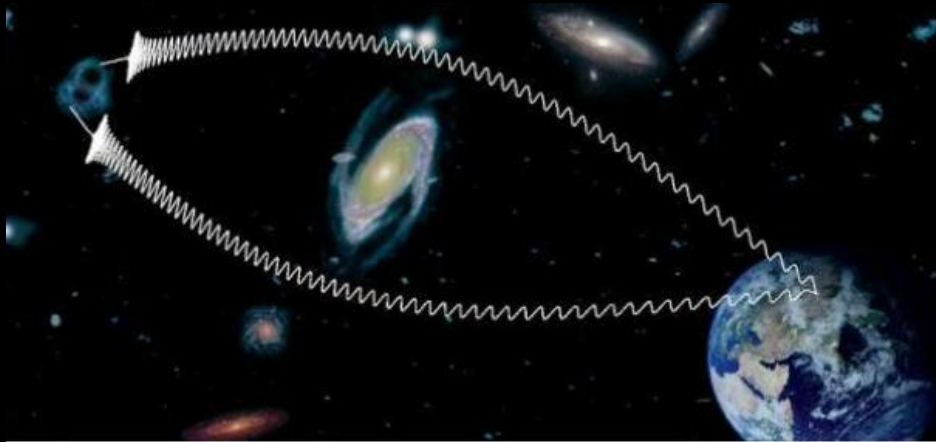


Figure taken from
Nakamura+, 2003

Structures give random phase shifts to the gravitational waves, thus **destroying interference**



THANK YOU FOR YOUR
ATTENTION!