

# Nuclear physics constraints on neutron star physics

William G. Newton

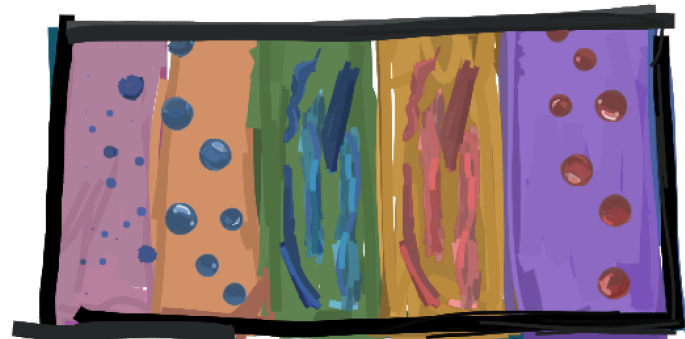
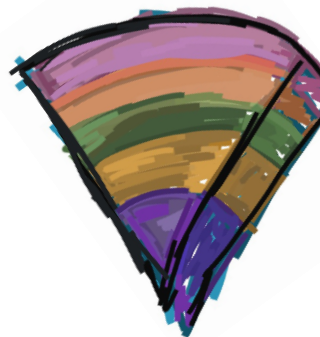
The work presented in this talk would not be possible without an amazing team of undergraduates and Master's students, including

Rebecca Preston, Lauren Balliet, Michael Ross Amber Stinson, August Doss, Gabriel Crocombe, Josh Belieu, Savannah Wright, Parker Reeves

Duncan Neill, David Tsang – University of Bath

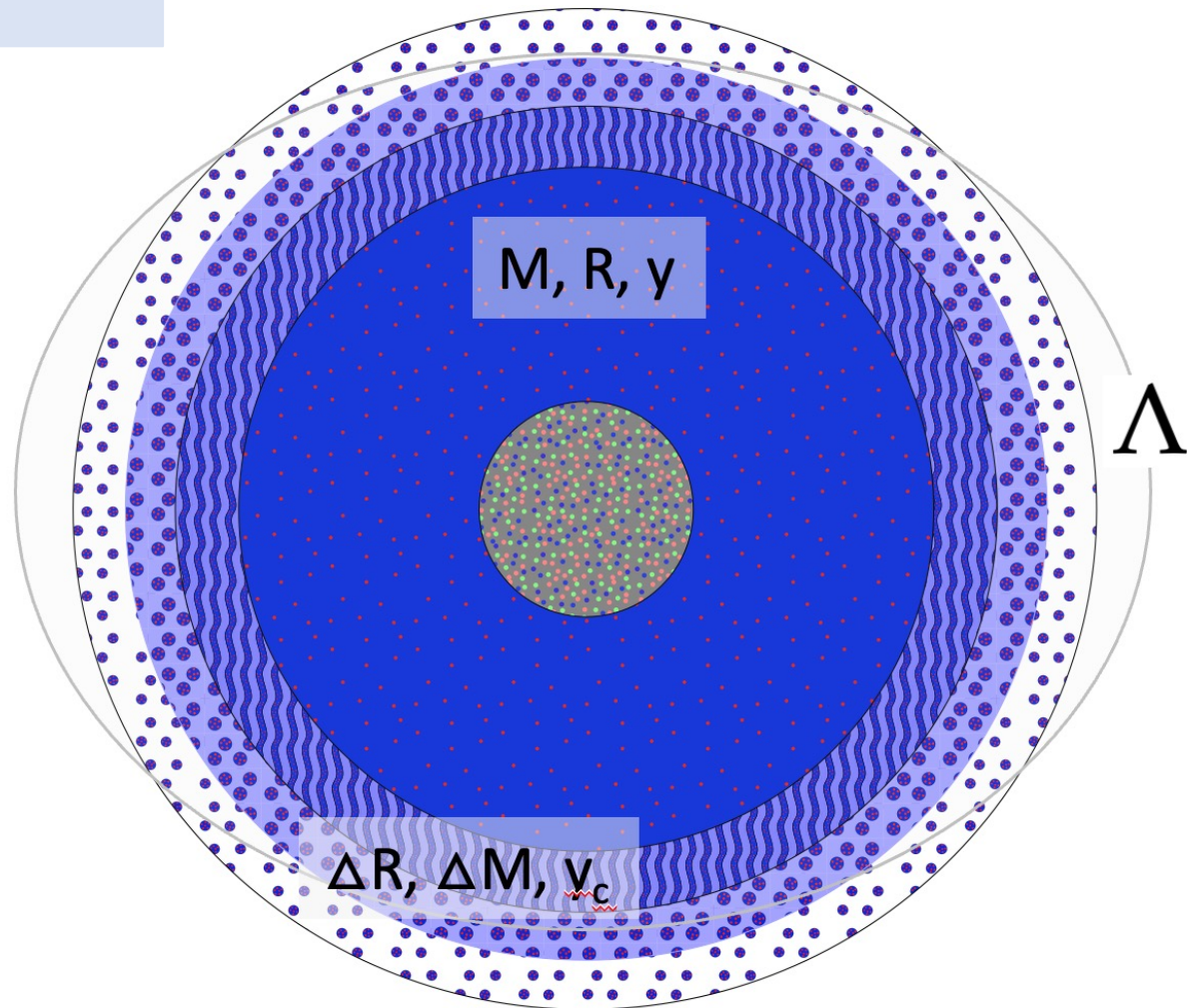
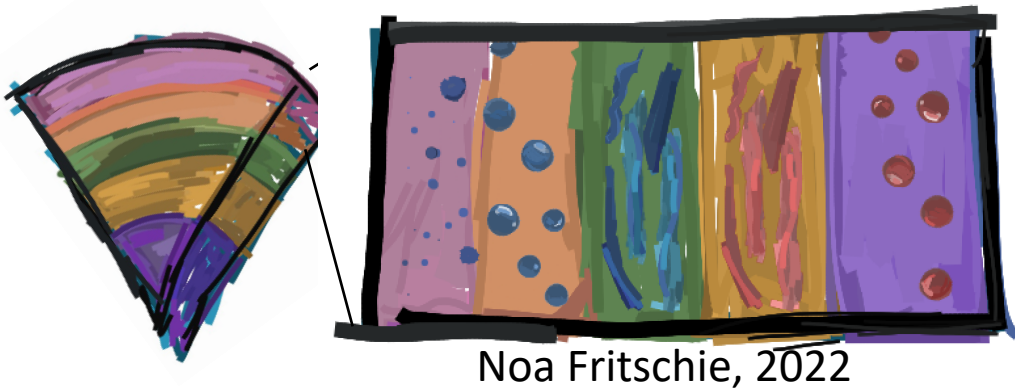


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UNIVERSITY



Noa Fritschie, 2022

# A neutron star's intrinsic structure



Outer crust/ inner crust/ mantle/ outer core/ inner core

$N, e/$

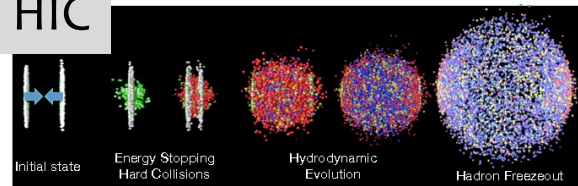
$N, e, n/$

$N^*, e, n(p)/ n, p, e, \mu/$

$\Lambda$  or  $q$  or...

# Nuclear structure/ dynamics

HIC

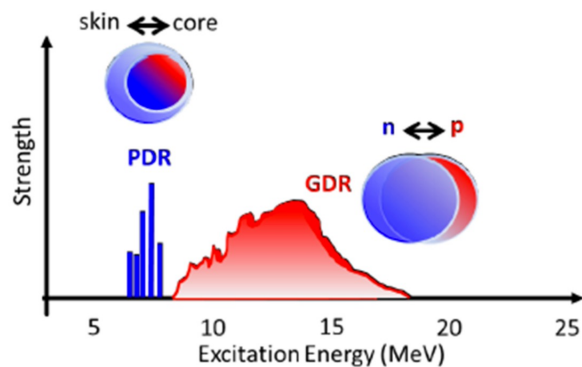


T.K.Nayak, arxiv:1201.4264

neutron skins

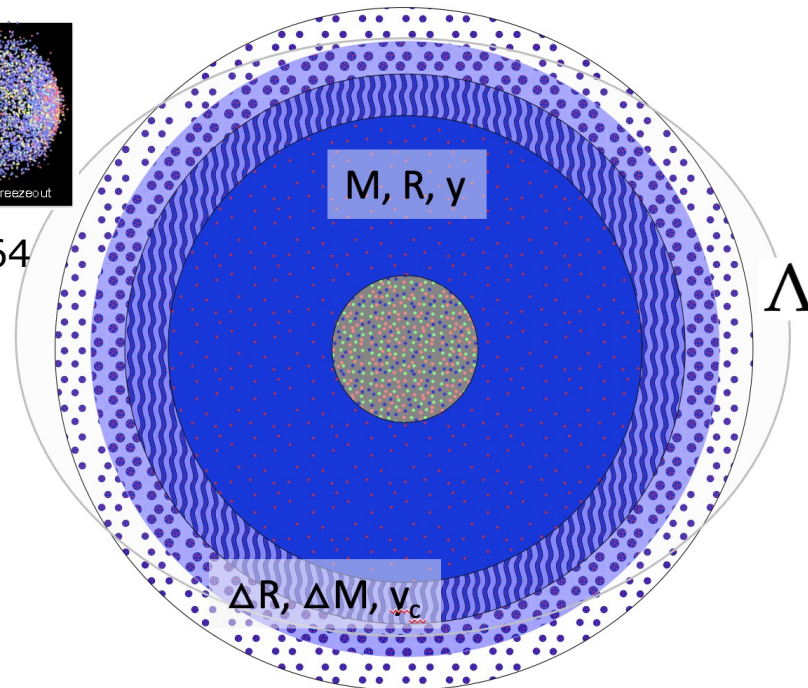


Abrahamyan+,  
PRL 108, 112592 (2012)



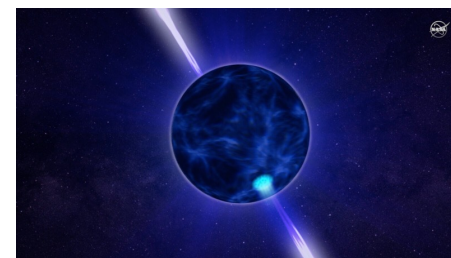
Bracco, Lanza, Tamii,  
PPNP 106, 360 (2019)

# Multi-messenger nuclear astrophysics



# Neutron star structure/ dynamics

Glitches, flares,  
cooling



Hot spots  
Oscillations,  
Crust cooling

Tides, mergers

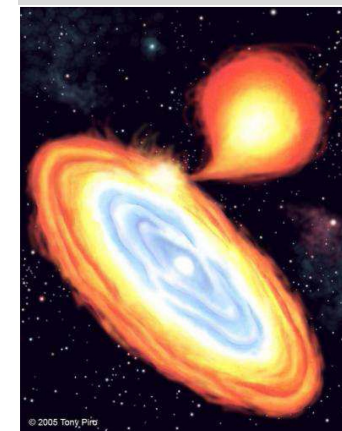
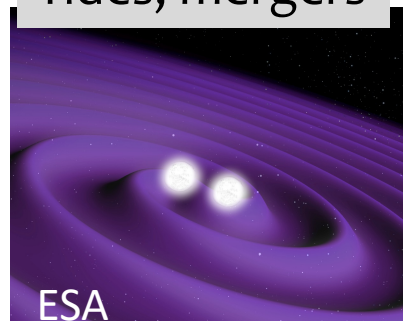
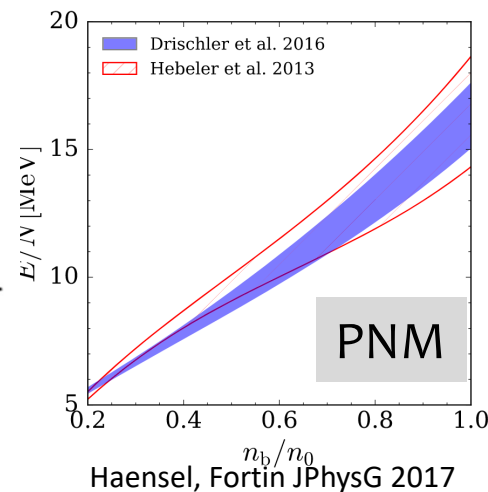
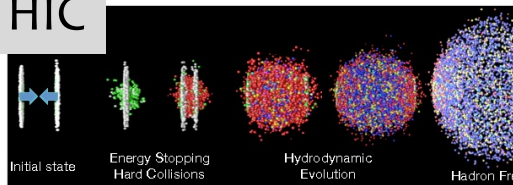


Figure: Artist's impression of a LMXB  
- credit Tony Piro, 2005.



# Nuclear structure/ dynamics

HIC

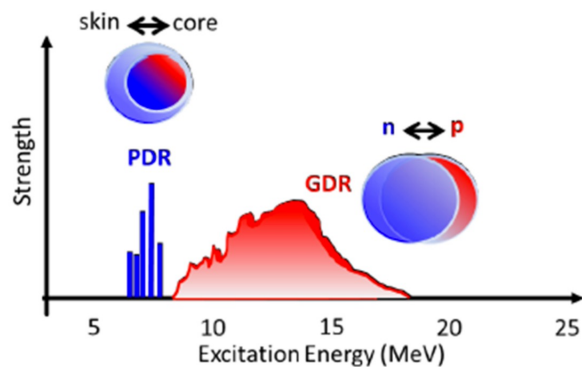


T.K.Nayak, arxiv:1201.426

## neutron skins

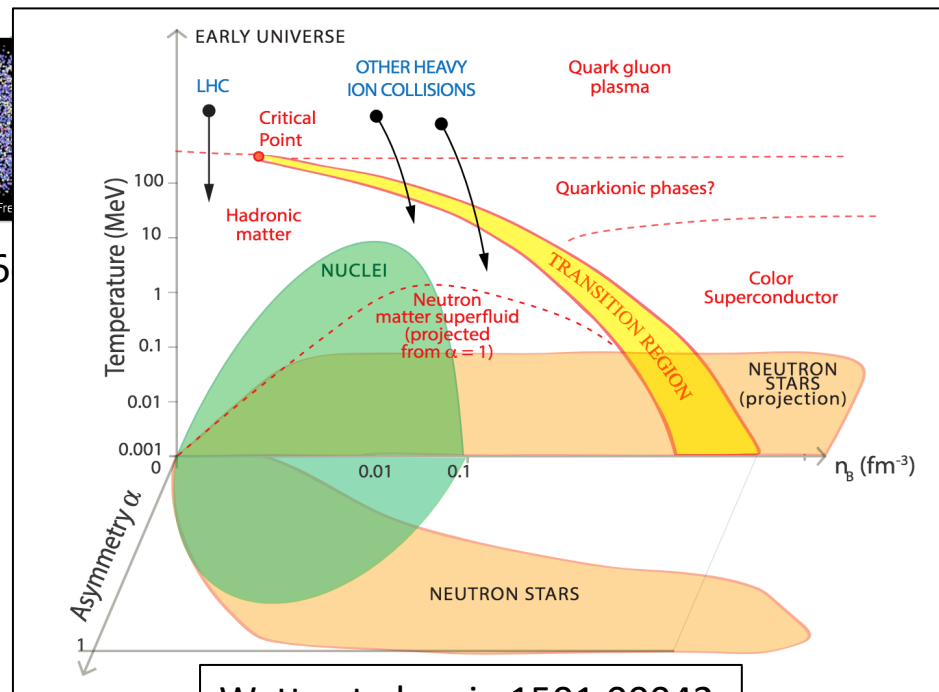


Abrahamyan+,  
PRL 108, 112592 (2012)



Bracco, Lanza, Tamii,  
PPNP 106, 360 (2019)

# Multi-messenger nuclear astrophysics



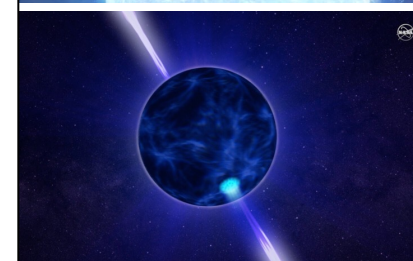
Watts et al arxiv:1501.00042

# Neutron star structure/ dynamics

## Glitches, flares, cooling



NASA /Chris Smith



## Hot spots Oscillations, Crust cooling

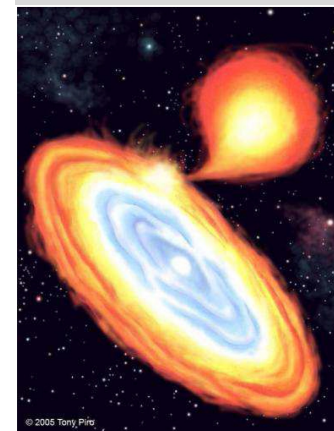
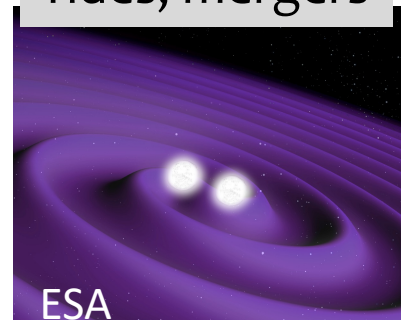
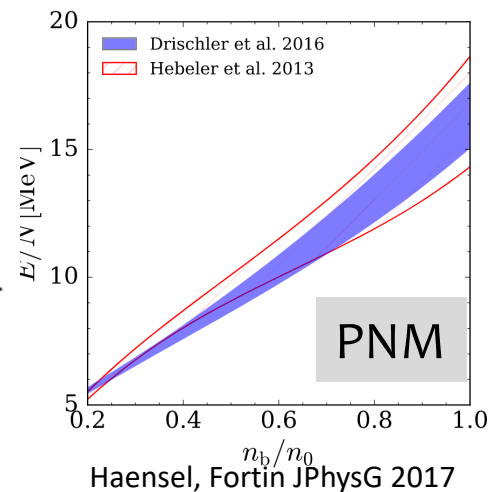


Figure: Artist's impression of a LMXB  
- credit Tony Piro, 2005.

## Tides, mergers



ESA

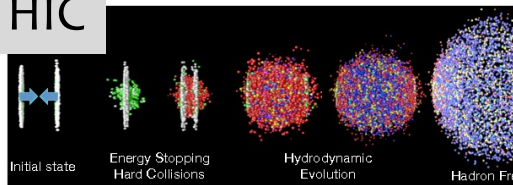


PNM

Haensel, Fortin JPhysG 2017

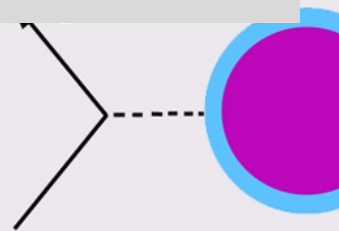
# Nuclear structure/ dynamics

HIC

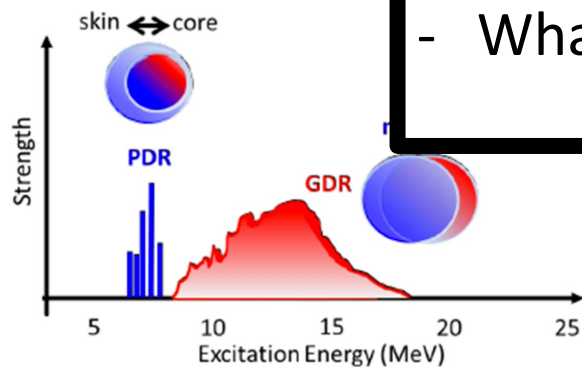


T.K.Nayak, arxiv:1208.4074

neutron skins

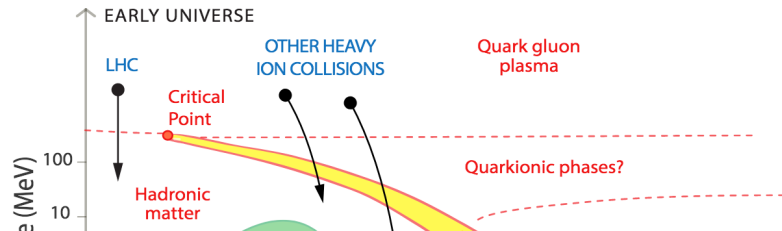


Abrahamyan+,  
PRL 108, 112592 (2012)



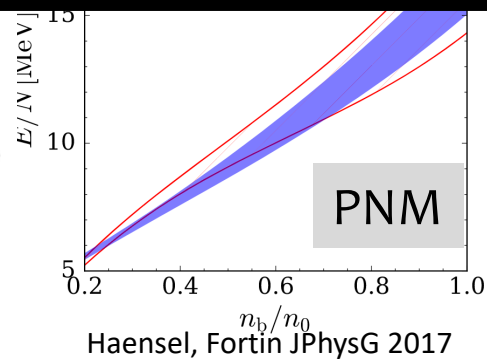
Bracco, Lanza, Tamii,  
PPNP 106, 360 (2019)

# Multi-messenger nuclear astrophysics



Communication between communities:

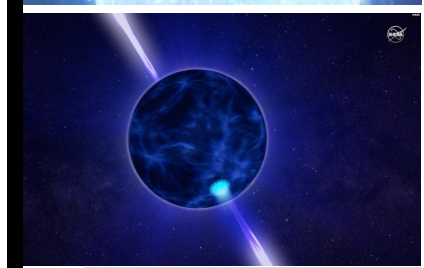
- What are we interested in?
- What do we need?
- How are we defining quantities?
- What are the limits of models?
- How are the uncertainties quantified?
- What are the model dependencies?



Haensel, Fortin JPhysG 2017

# Neutron star structure/ dynamics

Glitches, flares,  
cooling



Hot spots  
Oscillations,  
Crust cooling

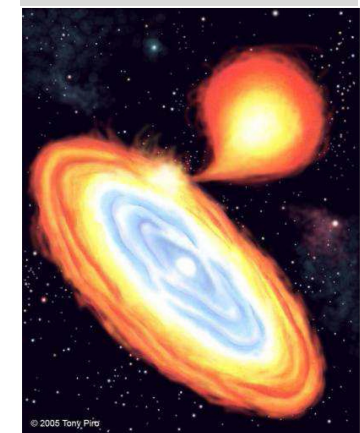
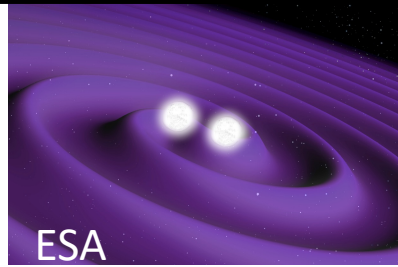
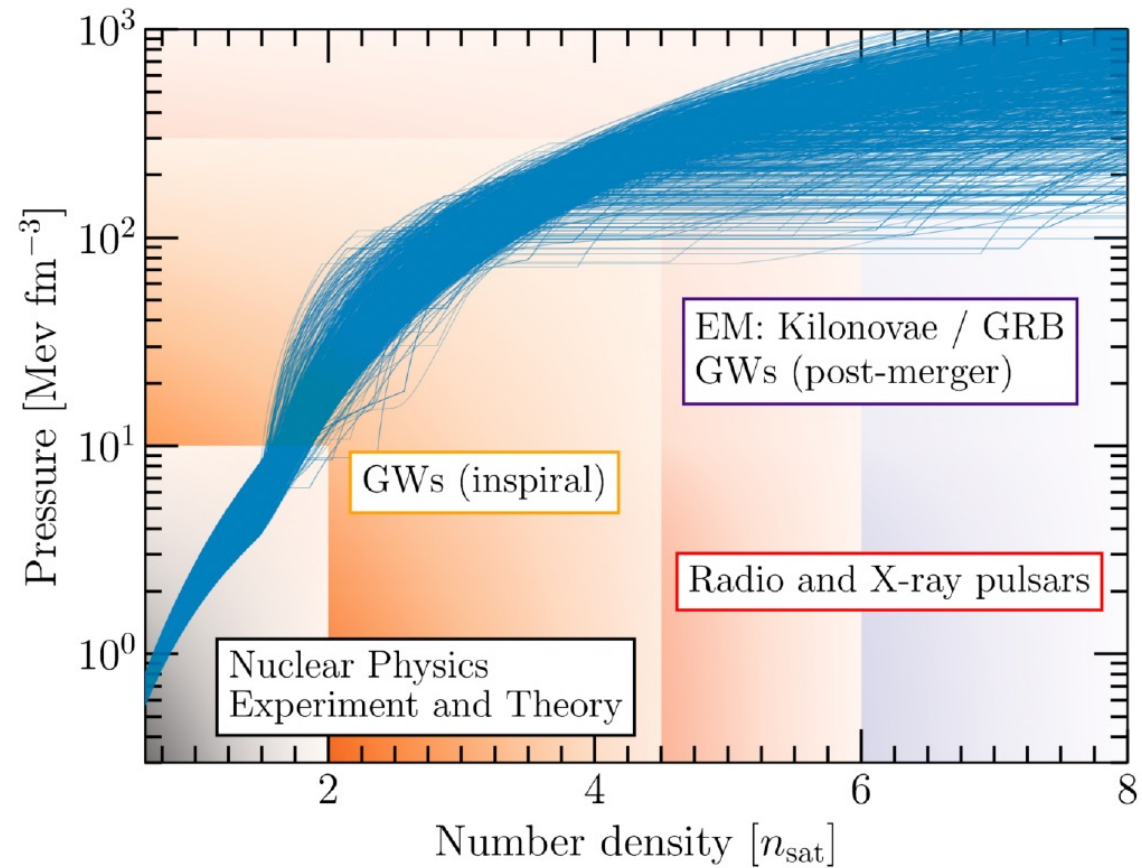


Figure: Artist's impression of a LMXB - credit Tony Piro, 2005.

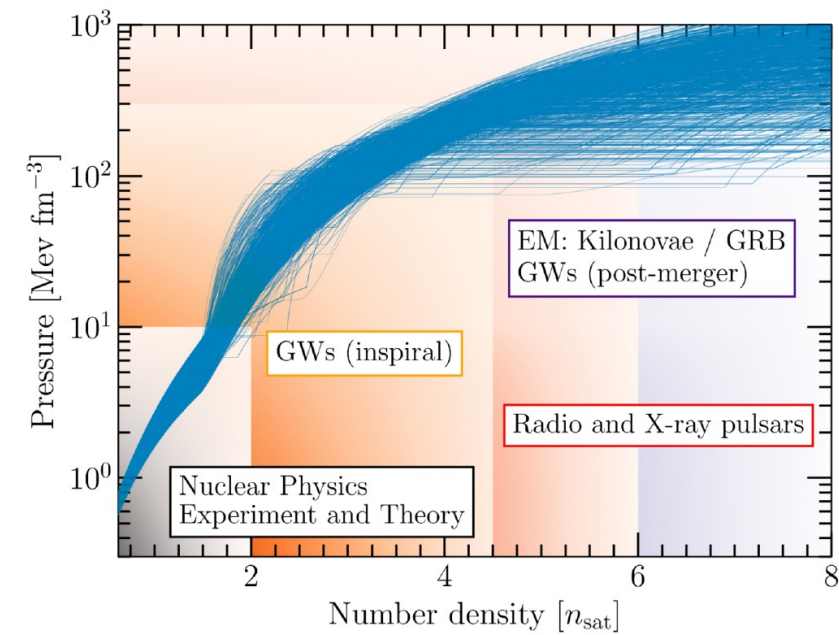


Modern approach: create ensembles of EOSs/neutron star models for statistical inference

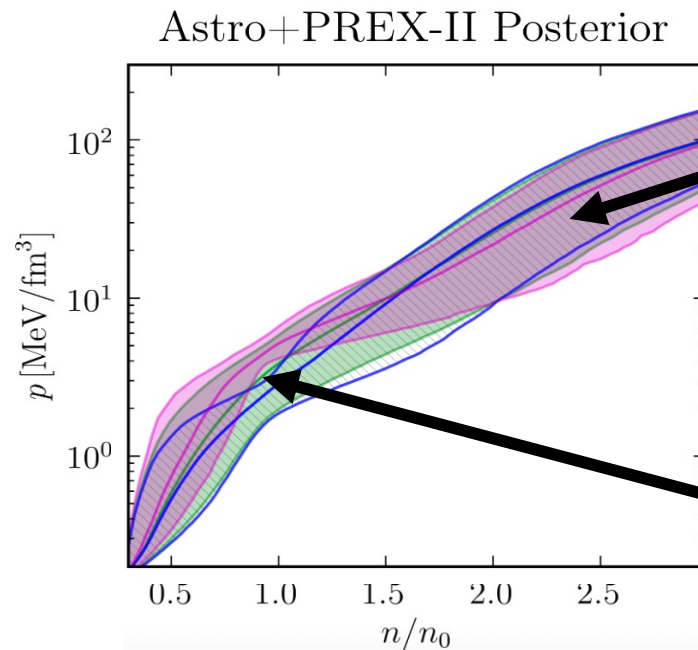


Pang et al, arxiv:2205.08513

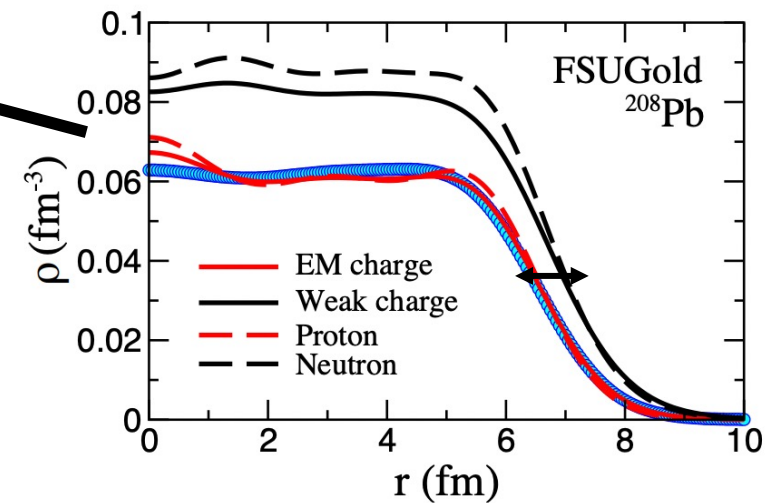
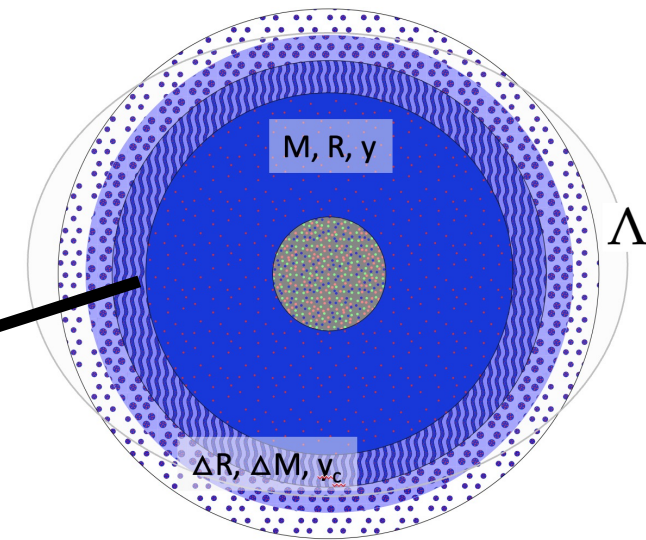
Modern approach: create ensembles of EOSs/neutron star models for statistical inference



Pang et al, arxiv:2205.08513



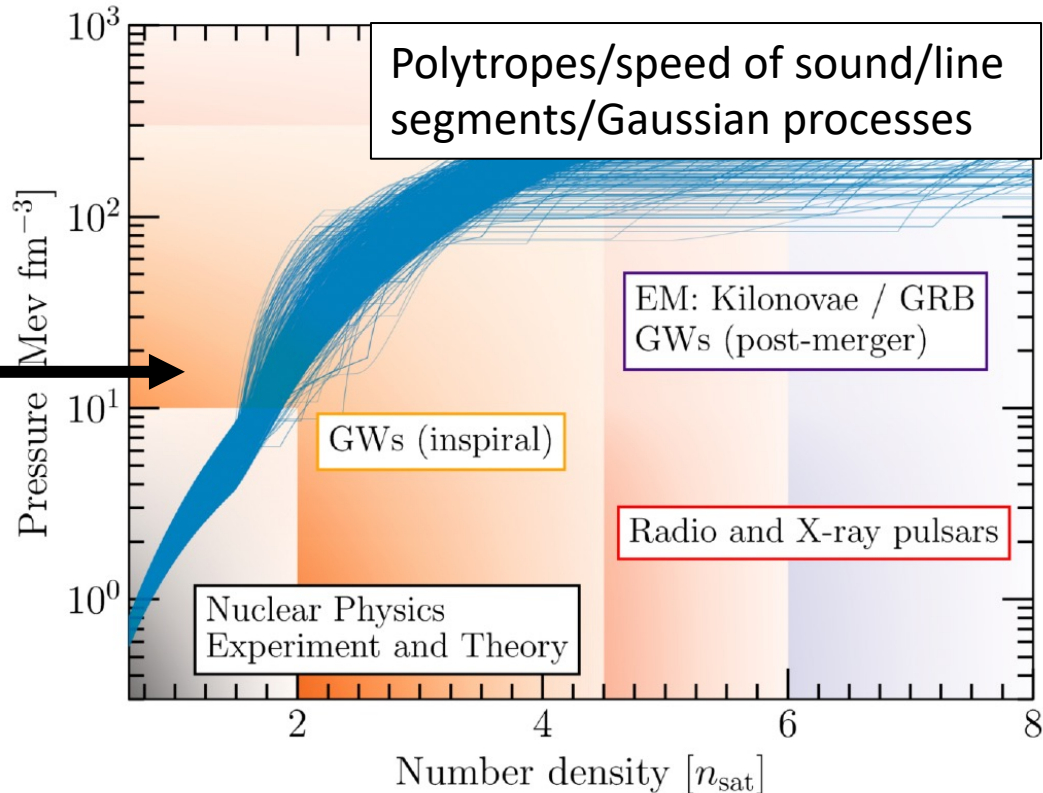
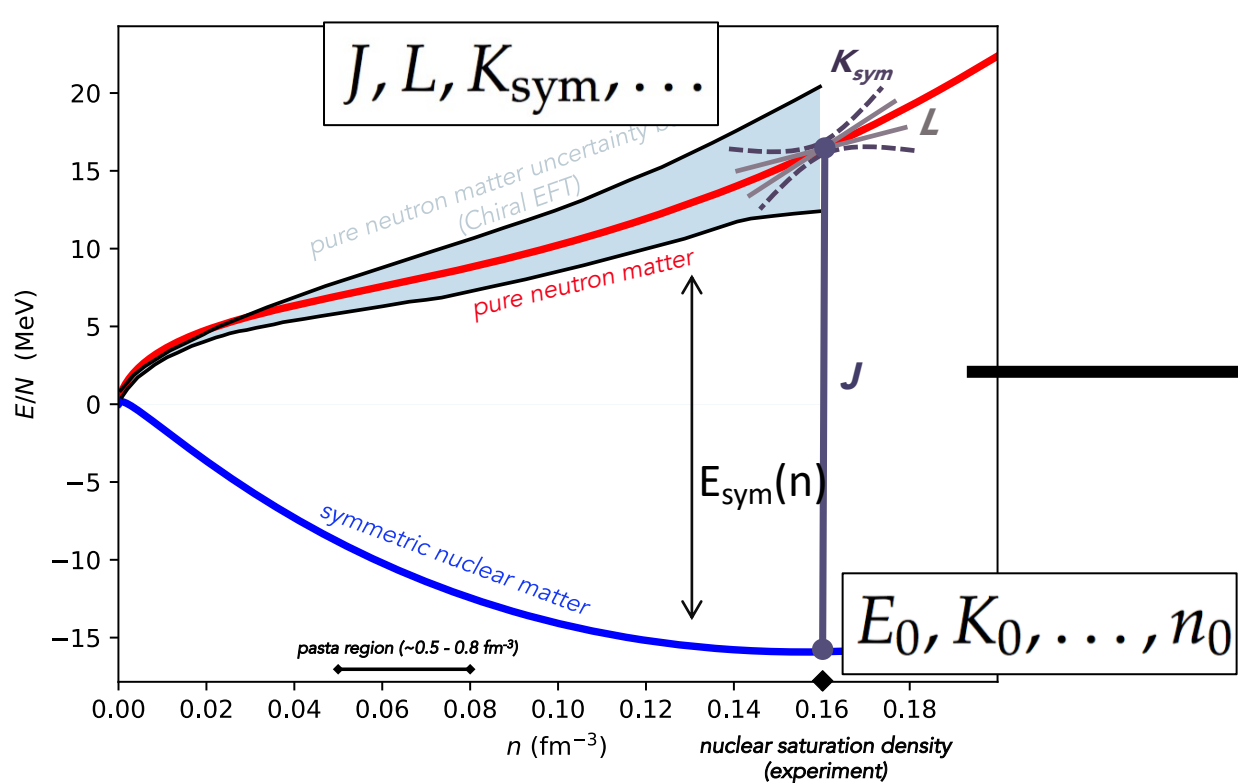
Essick+ arXiv 2102.10074



Thiel+ arXiv:1904.12269

# The Nuclear Matter Equation of State

$$E_{\text{sym}}(\rho) = J + L\left(\frac{\rho - \rho_0}{3\rho_0}\right) + \frac{K_{\text{sym}}}{2}\left(\frac{\rho - \rho_0}{3\rho_0}\right)^2 + \frac{Q_{\text{sym}}}{6}\left(\frac{\rho - \rho_0}{3\rho_0}\right)^3 \dots$$

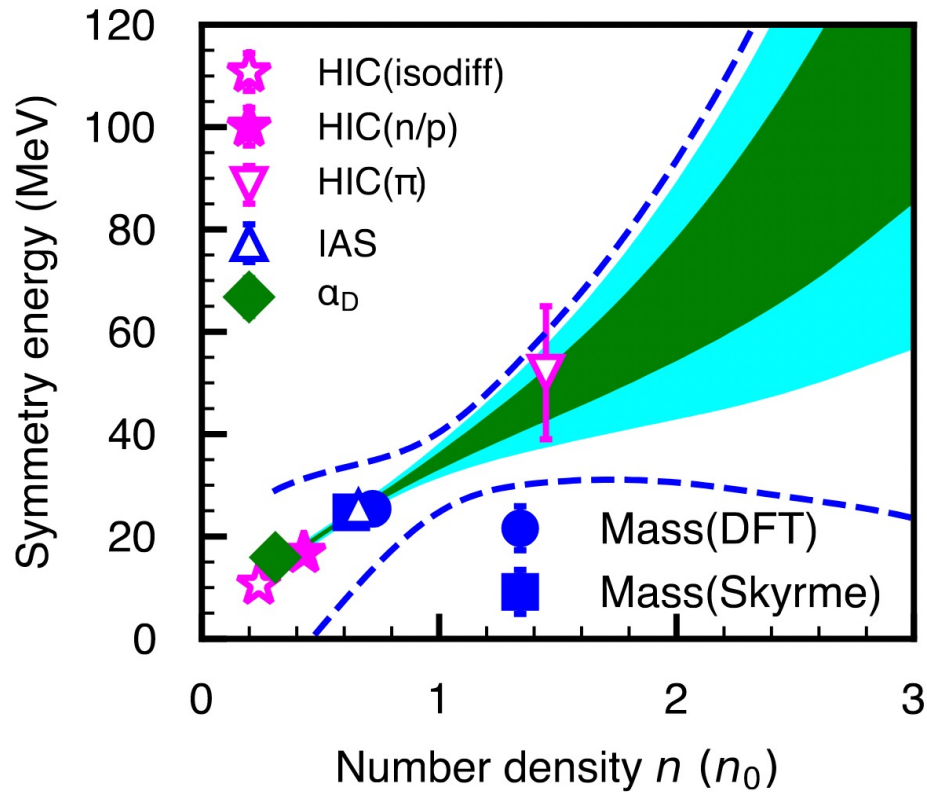


$$E_0(\rho) = E_0(\rho_0) + \frac{K_0}{2}\left(\frac{\rho - \rho_0}{3\rho_0}\right)^2 + \frac{J_0}{6}\left(\frac{\rho - \rho_0}{3\rho_0}\right)^3,$$

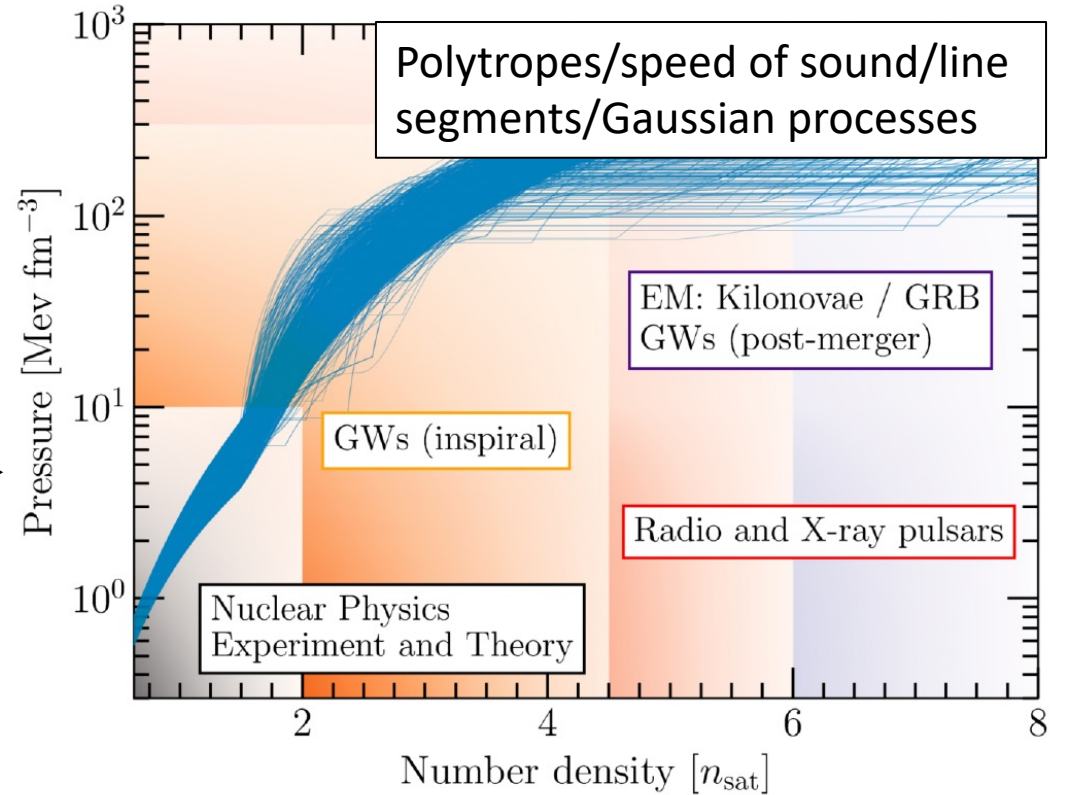
Li, arxiv:2105.04629

# The Nuclear Matter Equation of State

$$E_{\text{sym}}(\rho) = J + L\left(\frac{\rho - \rho_0}{3\rho_0}\right) + \frac{K_{\text{sym}}}{2}\left(\frac{\rho - \rho_0}{3\rho_0}\right)^2 + \frac{Q_{\text{sym}}}{6}\left(\frac{\rho - \rho_0}{3\rho_0}\right)^3 \dots$$



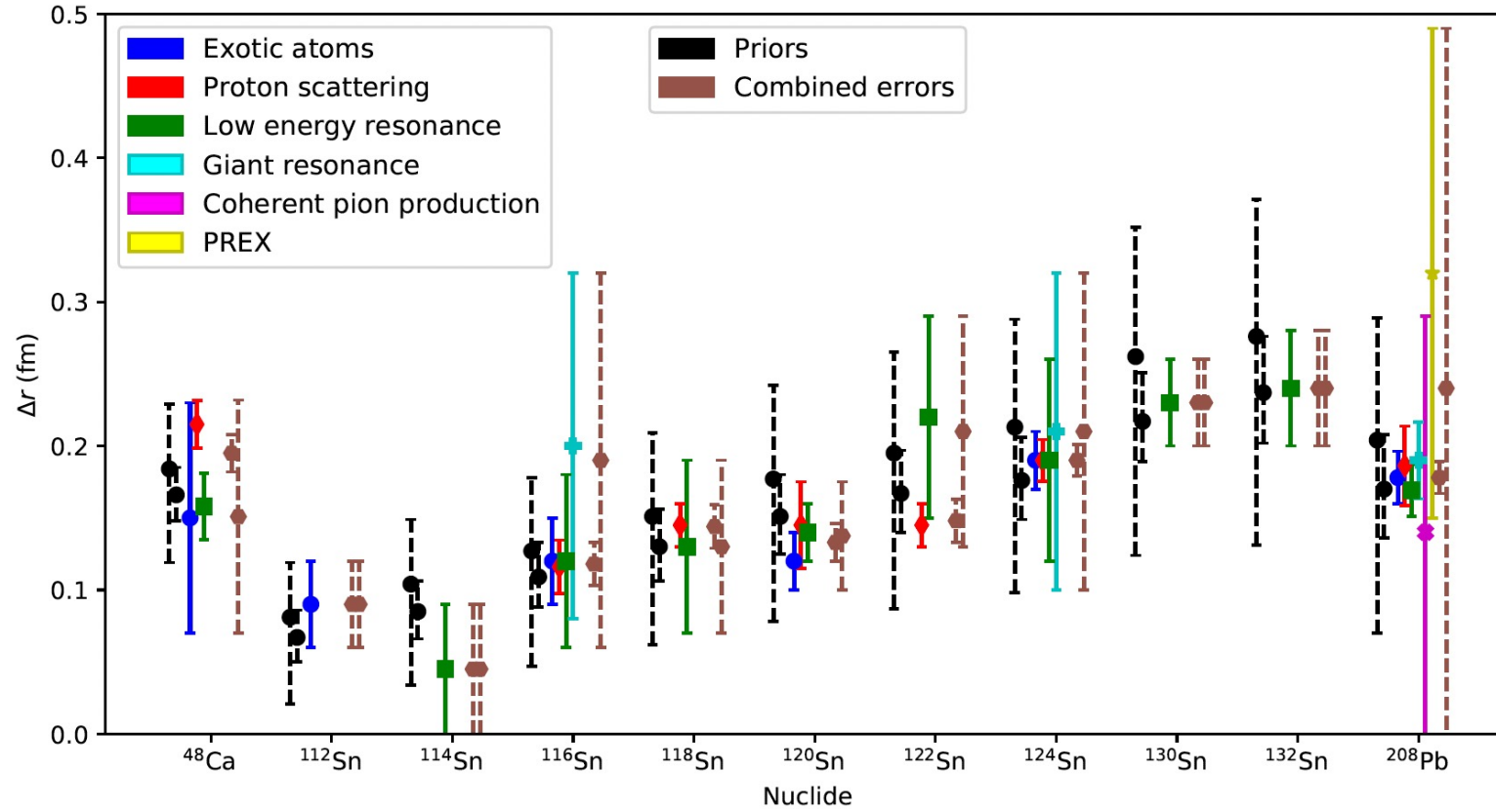
Lynch+, arXiv:2310.11588



Pang et al, arxiv:2205.08513

$$E_0(\rho) = E_0(\rho_0) + \frac{K_0}{2}\left(\frac{\rho - \rho_0}{3\rho_0}\right)^2 + \frac{Q_0}{6}\left(\frac{\rho - \rho_0}{3\rho_0}\right)^3 \dots,$$

# Data: Neutron Skins



Newton, Crocombe arxiv:2008.00042

Lattimer, arXiv:2301.03666

Xu+ arXiv:2007.07669

# Data: Weak form factors

## PREX, CREX

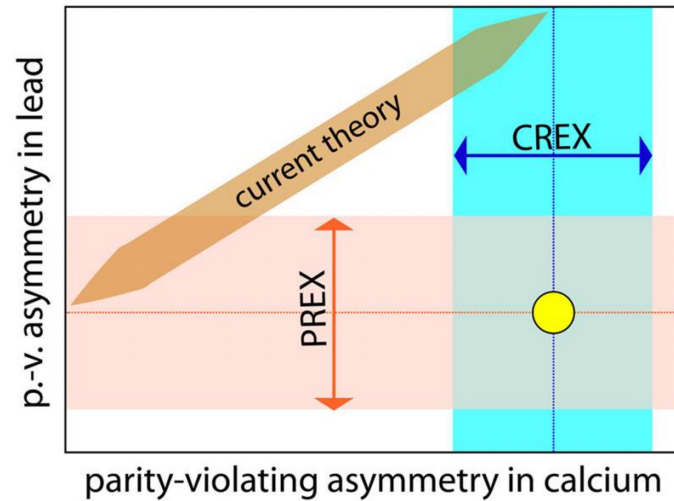
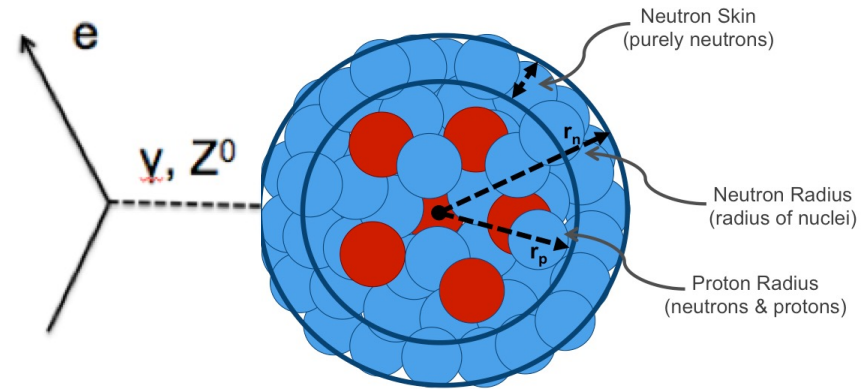
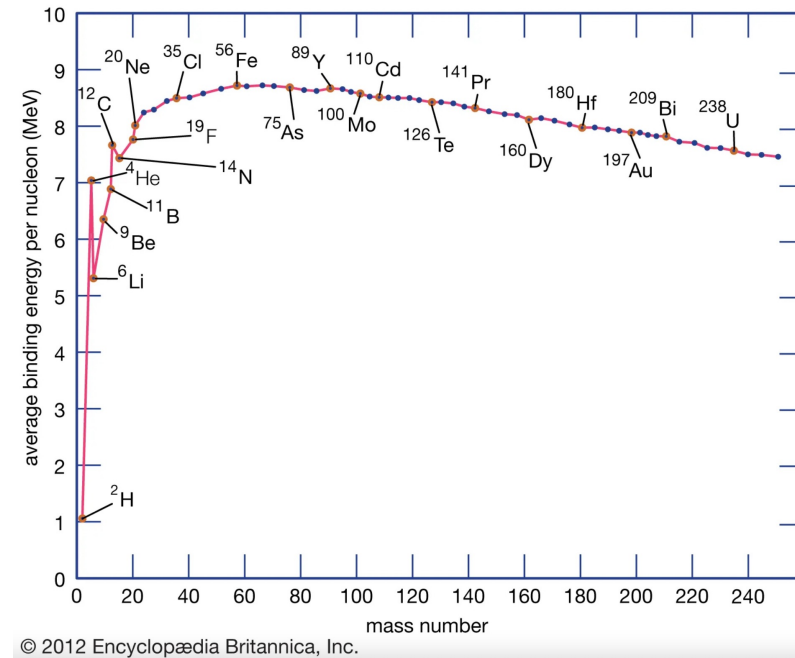
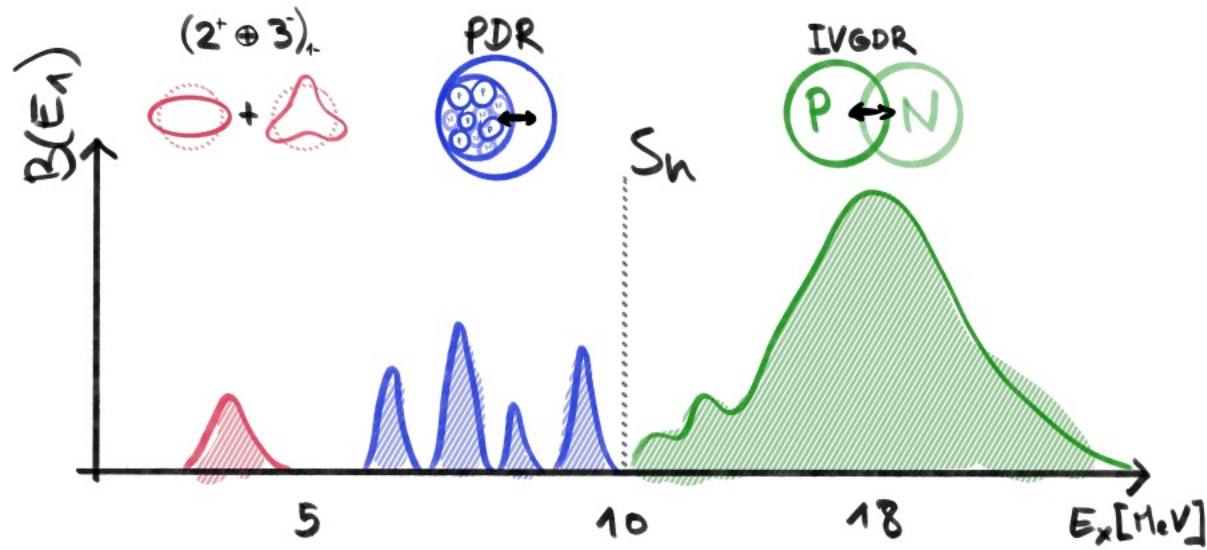


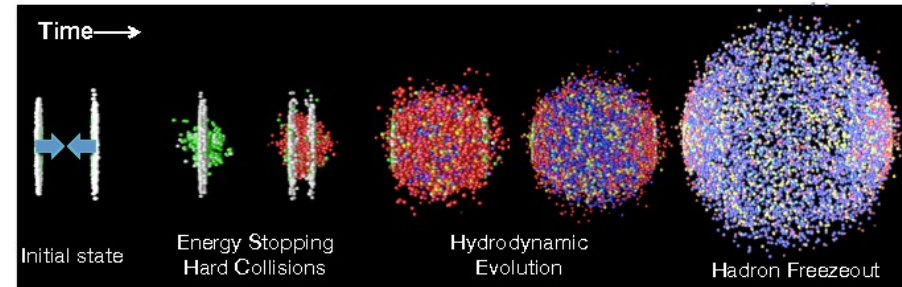
Image: Witold Nazarewicz

# Data: Dipole Polarizability/Giant Resonances, Nuclear Masses, HIC, IAS

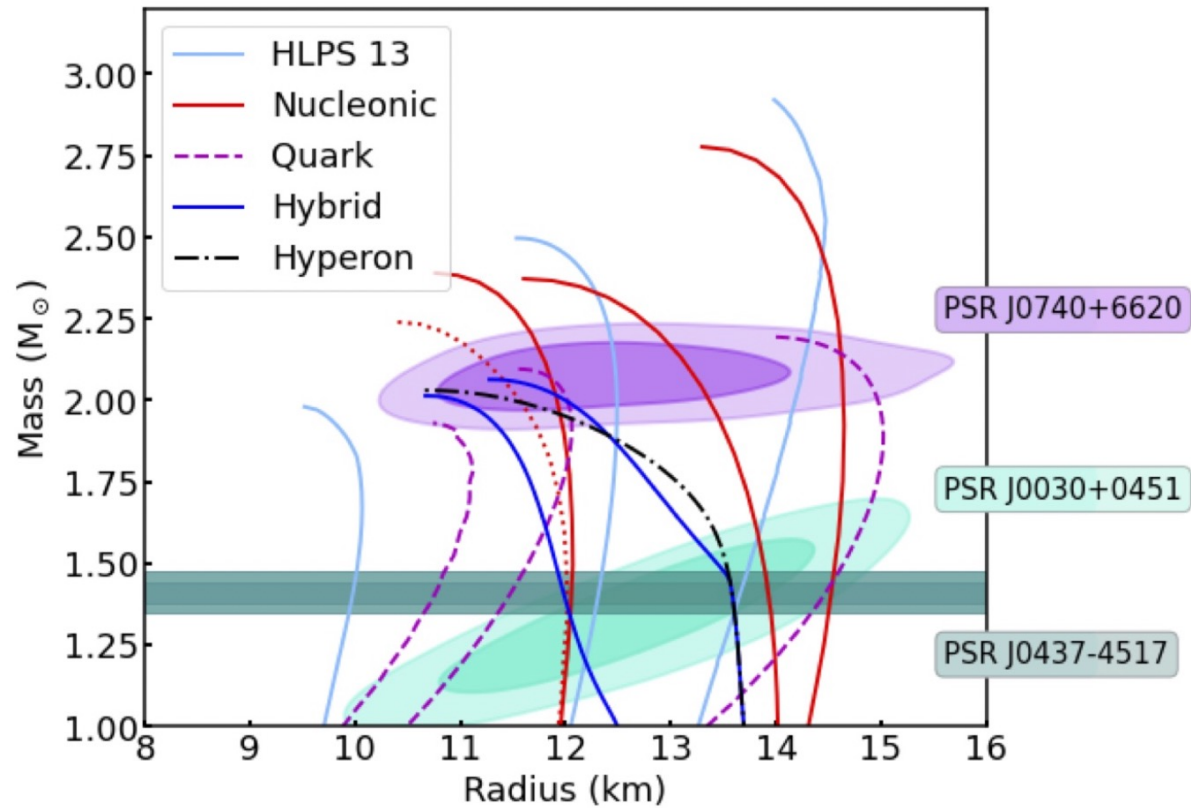


Thiel+ arXiv:1904.12269

Bracco, Lanza, Tamii,  
PPNP 106, 360 (2019)



# Data: Neutron star mass/radii (e.g. NICER)

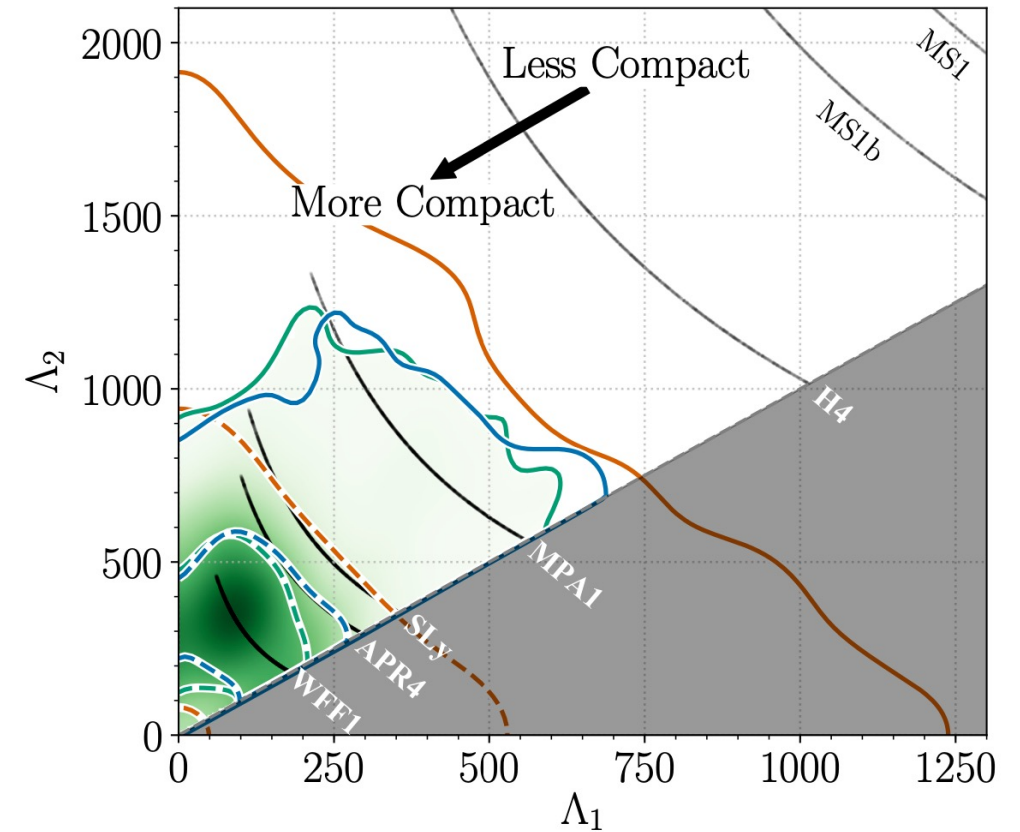


Riley arxiv:1912.05702, arxiv:2105.06980

Miller et al arxiv:2105.06979, arxiv:1912.05705

Raaijmakers et al arxiv: 1912.05703, 2105.06981

# Data: Tidal Deformability



LIGO/Virgo arxiv:1805.11581

# Increasing number of attempts to combine nuclear/Astro observables

	Huth+	Dietrich+	Koehn+	Capano+	Lynch+	Essick+	Greif+
“accepted” $n_0, E_0, K_0$	■	■	■	■	■	■	■
$\alpha_D$			■		■	■	■
Neutron skins (PVES)			■		■	■	■
Neutron skins (other)					■	■	■
Weak form factor (PVES)						■	
Nuclear masses (CSH)			■		■		
Isobaric Analog States					■		
ISGMR/GQR					■		
IVGDR					■		
HIC: n/p ratio	■		■		■		
HIC: isospin diffusion					■		
HIC: $\pi$ spectra					■		
HIC: Elliptic flow	■				■		
Mirror nuclei...							

Huth+ [arxiv:2107.06222](https://arxiv.org/abs/2107.06222)

Dietrich+ [arXiv:2002.11355](https://arxiv.org/abs/2002.11355)

Greif+ [arXiv:2005.14164](https://arxiv.org/abs/2005.14164)

Capano+ [arXiv:1908.10352](https://arxiv.org/abs/1908.10352)

Lynch+ [arXiv:2310.11588](https://arxiv.org/abs/2310.11588)

Koehn+ [arXiv:2402.04172](https://arxiv.org/abs/2402.04172)

Essick+ [arXiv 2102.10074](https://arxiv.org/abs/2102.10074)

# Increasing number of attempts to combine lots of nuclear/Astro observables

	Huth+	Dietrich+	Koehn+	Capano+	Lynch+	Essick+	Greif+
Radii (NICER)	■		■		■	■	■
Radii (other)			■				
GW170817: $\Lambda$	■		■	■	■	■	■
GW170817: collapse		■	■	■			
GW170817-AT2017gfo	■	■	■	■			
Maximum mass	■	■	■			■	■
QPOs			■				
Moment of Inertia							
Binding Energy							
Max rotation rate							
Crust cooling							
Glitches							
Crust oscillations							

Huth+ arxiv:2107.06222

Dietrich+ arXiv:2002.11355

Greif+ arXiv:2005.14164

Capano+ arXiv:1908.10352

Lynch+ arXiv:2310.11588

Koehn+ arXiv:2402.04172

Essick+ arXiv 2102.10074

# Connecting NM params to nuclear observables

Density Functional Theory (e.g. Skyrme-type)

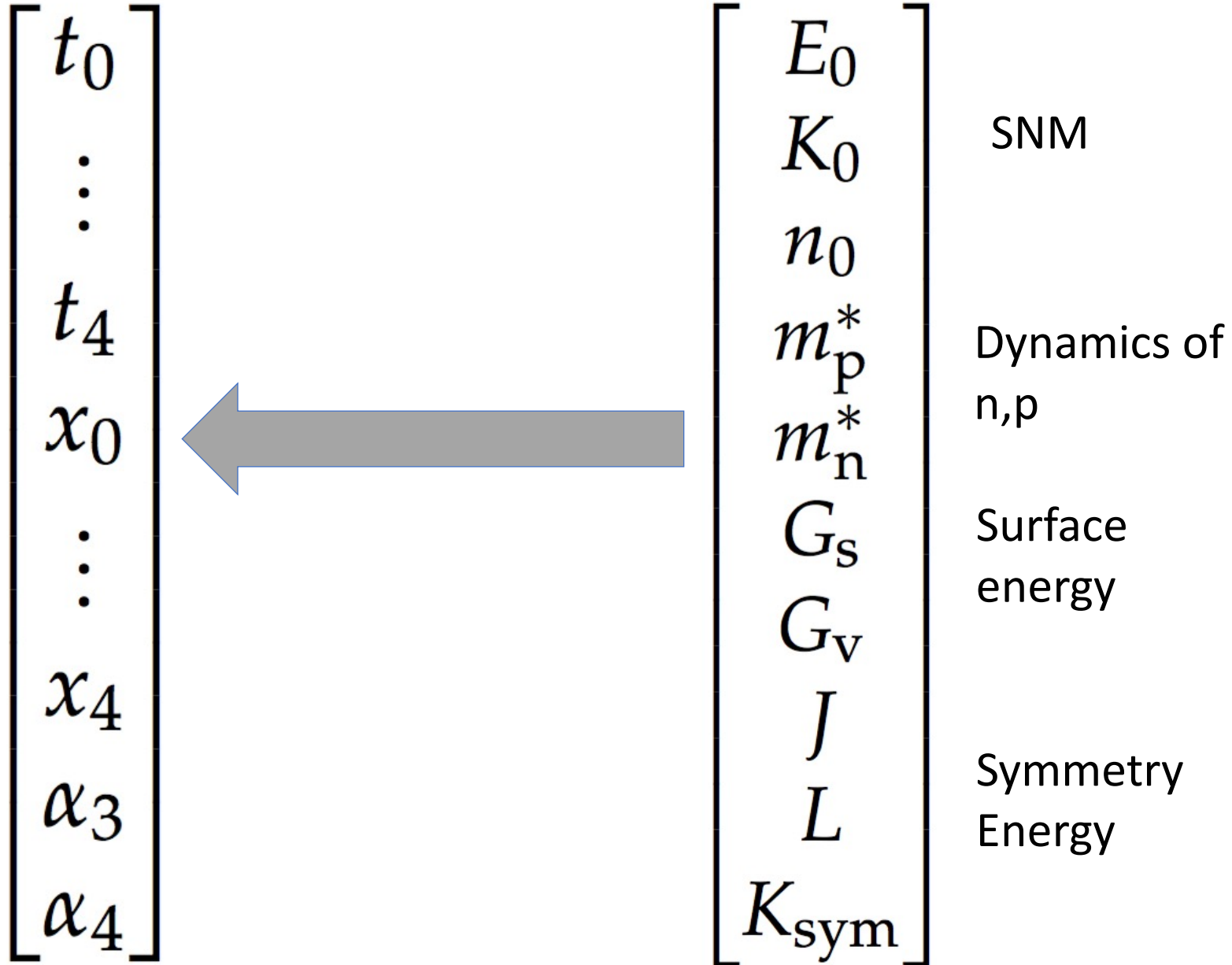
$$\mathcal{H}_\delta = \frac{1}{4}t_0\rho^2[(2 + x_0) - (2x_0 + 1)(y_p^2 + y_n^2)] \quad \text{Local interaction}$$

$$\begin{aligned} \mathcal{H}_\rho &= \frac{1}{4}t_3\rho^{2+\alpha_3}[(2 + x_3) - (2x_3 + 1)(y_p^2 + y_n^2)] \quad \text{Density dependent} \\ &+ \frac{1}{4}t_4\rho^{2+\alpha_4}[(2 + x_4) - (2x_4 + 1)(y_p^2 + y_n^2)] \end{aligned}$$

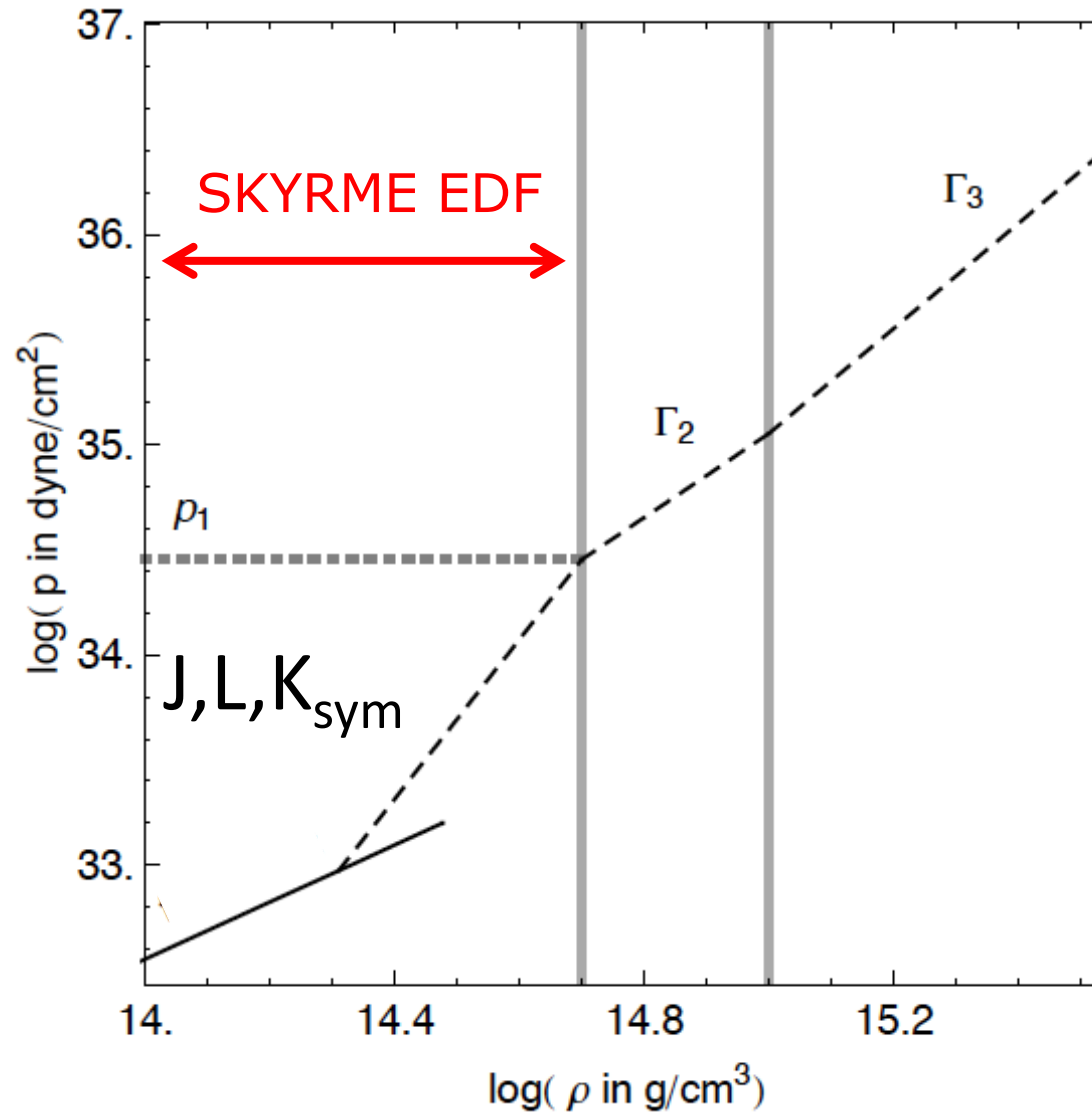
$$\begin{aligned} \mathcal{H}_{\text{eff}} &= \frac{1}{8}\rho[t_1(2 + x_1) + t_2(2 + x_2)]\tau \quad \text{3 body} \\ &+ \frac{1}{8}\rho[t_1(2x_1 + 1) + t_2(2x_2 + 1)](\tau_p y_p + \tau_n y_n) \quad \dots \end{aligned}$$

$$\begin{aligned} \mathcal{H}_{\text{grad}} &= \frac{1}{32}(\nabla\rho)^2[3t_1(2 + x_1) - t_2(2 + x_2)] \quad \text{Gradient...} \\ &- \frac{1}{32}[3t_1(2x_1 + 1) + t_2(2x_2 + 1)][(\nabla\rho_p)^2 + (\nabla\rho_n)^2] \end{aligned}$$

# Map nuclear matter parameters to model parameters and systematically generate models

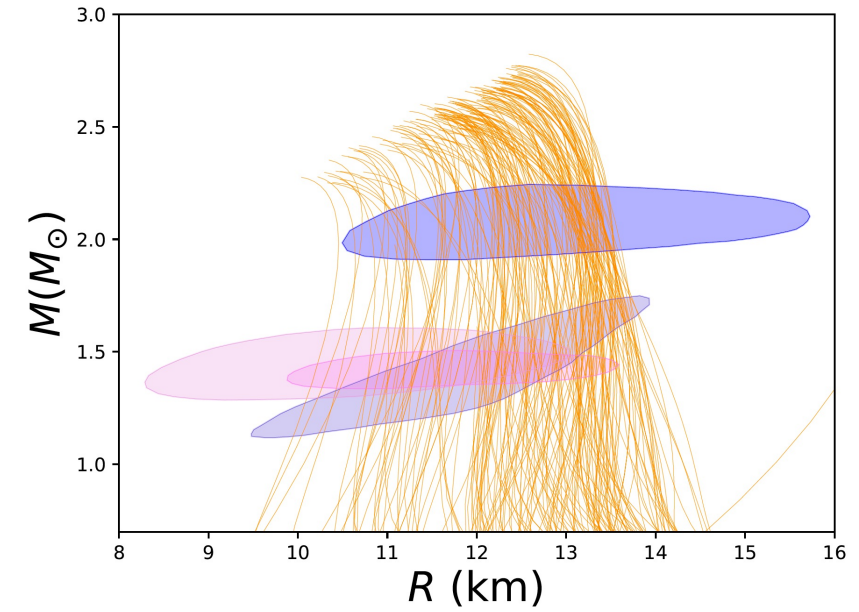
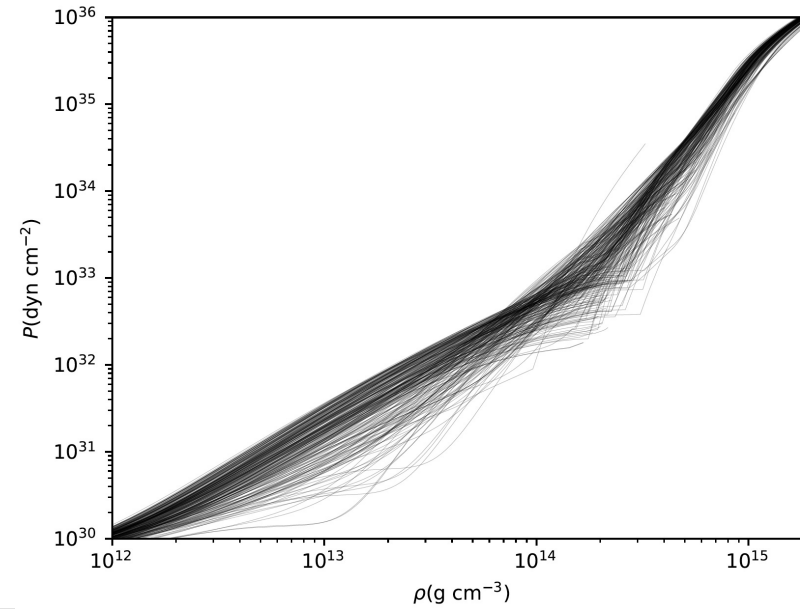
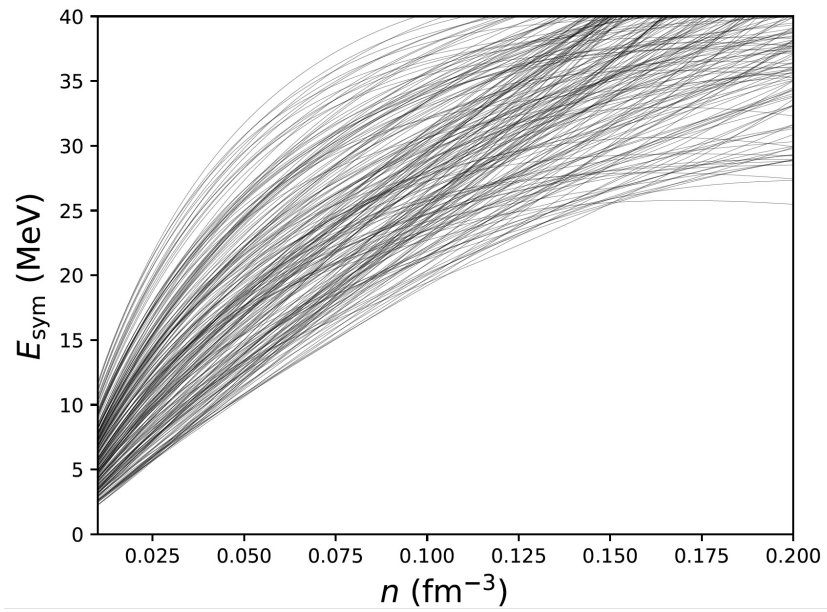


# EOS model: Skyrme EDF + 2 Piecewise Polytrope or speed of sound model

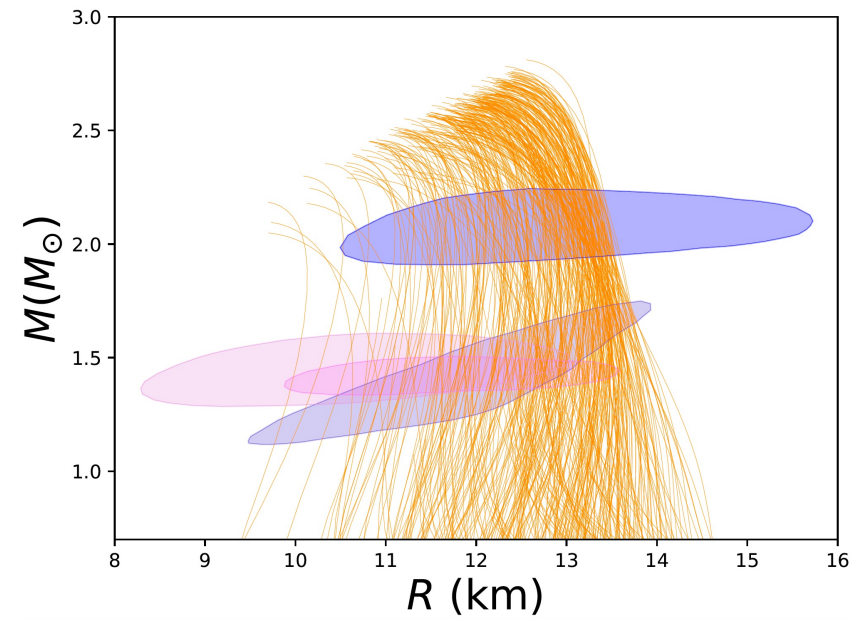
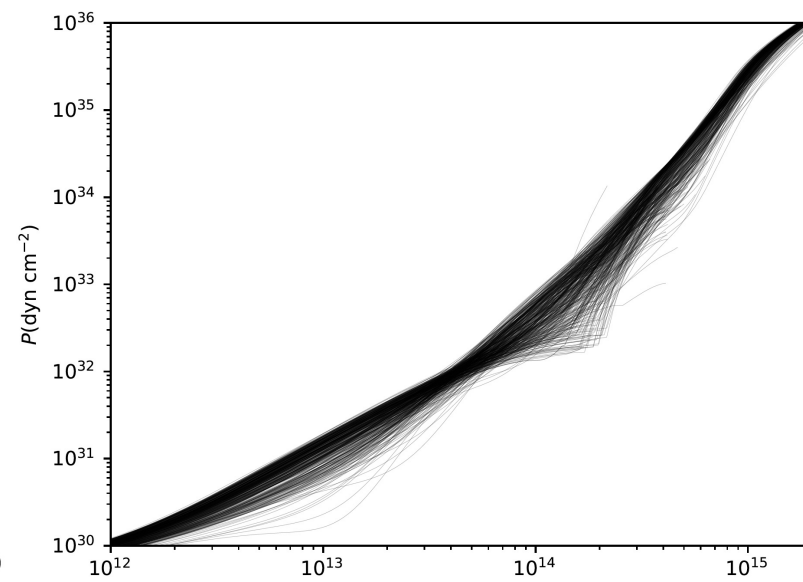
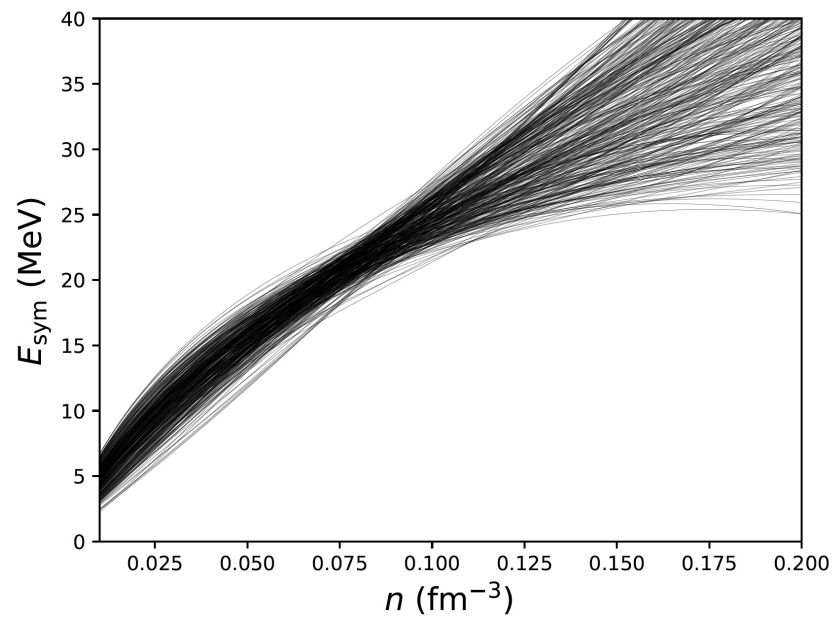


Read+, arxiv:0812.2163; see also works by Steiner, Lattimer, Özel...

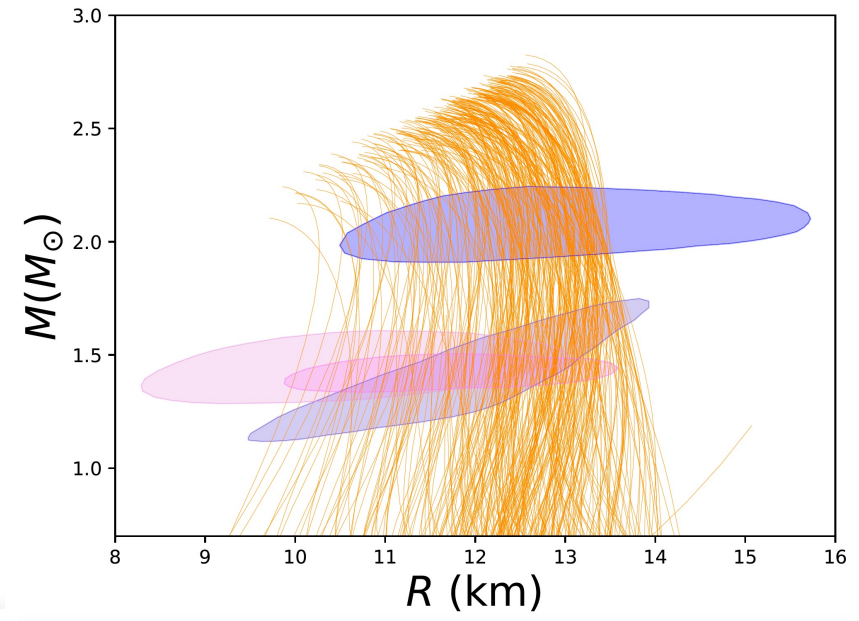
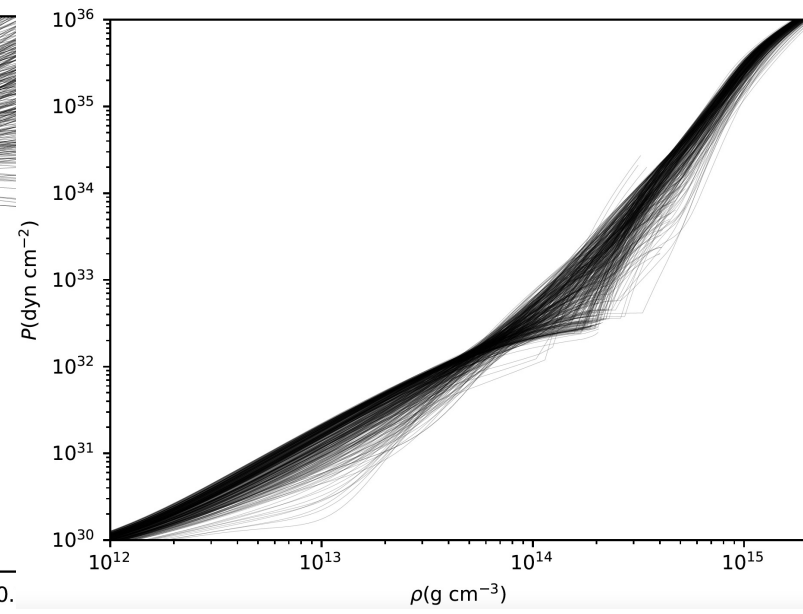
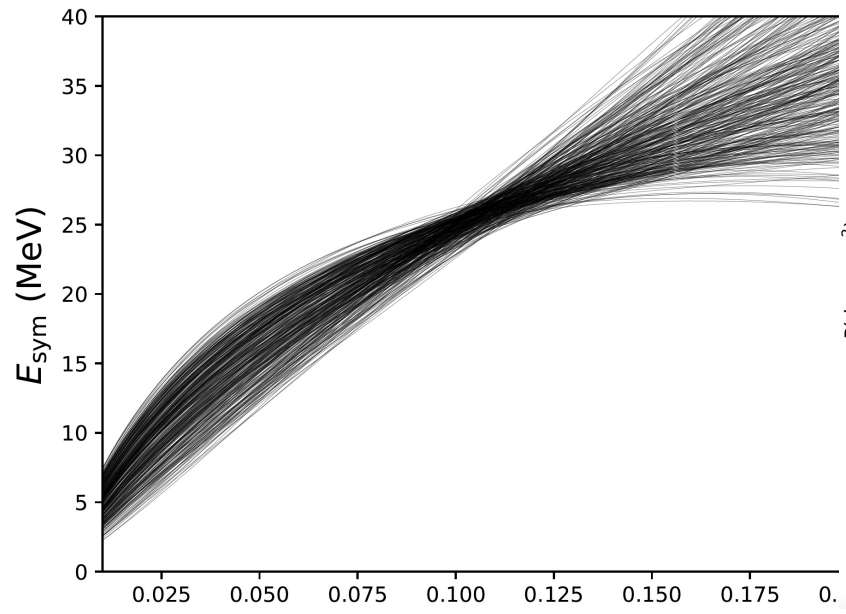
# Prior



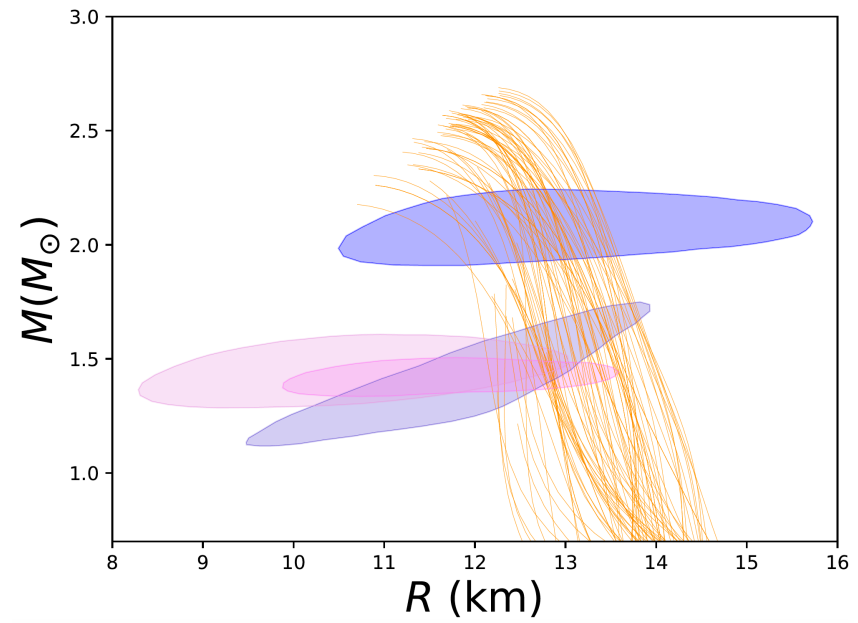
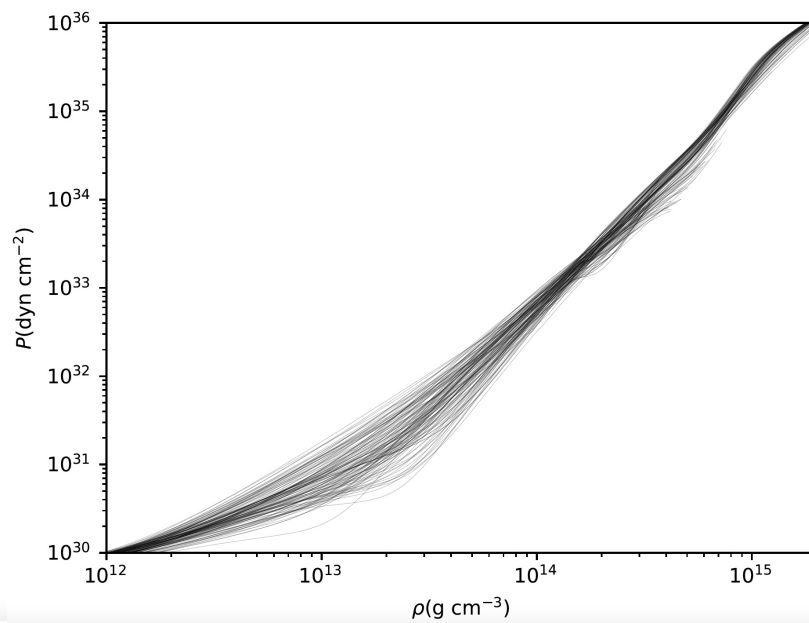
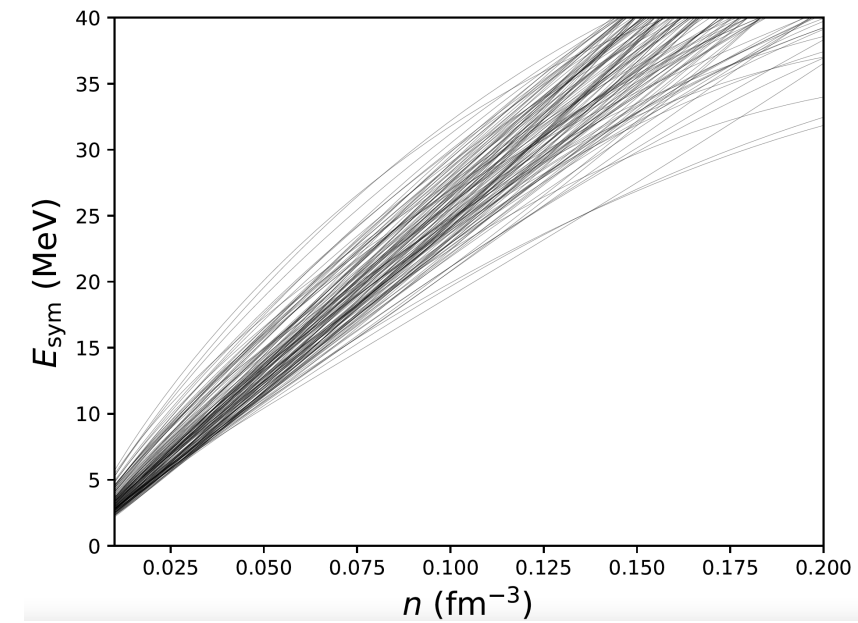
$\alpha_D$



# BE

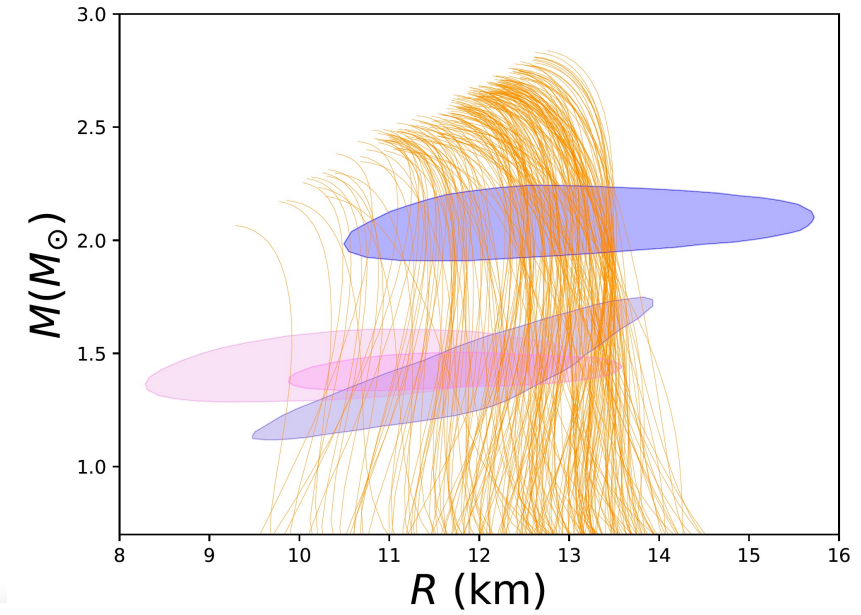
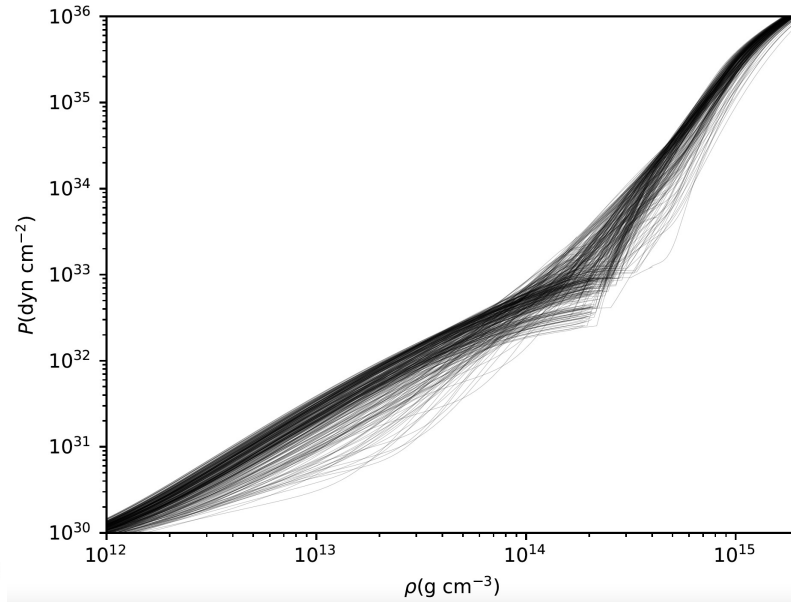
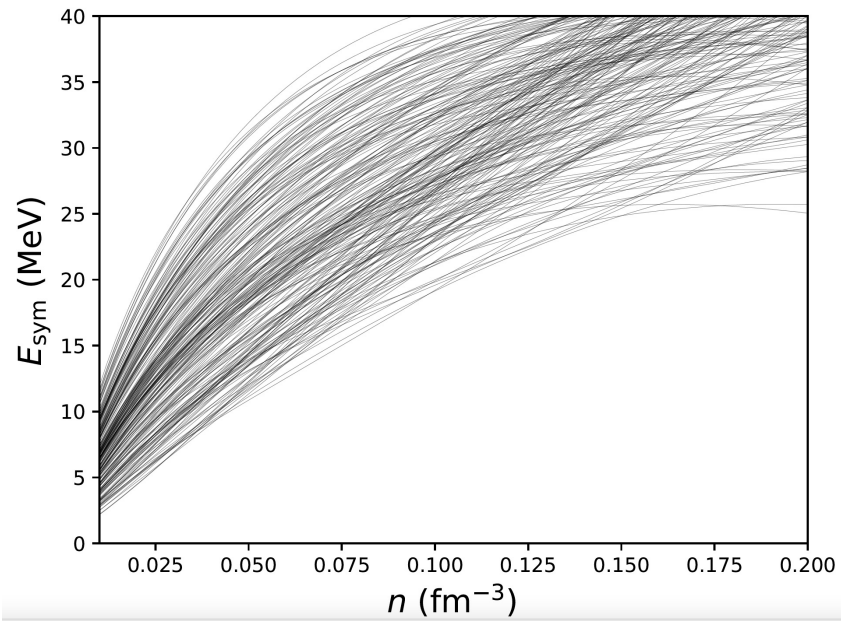


$F_w^{208}$

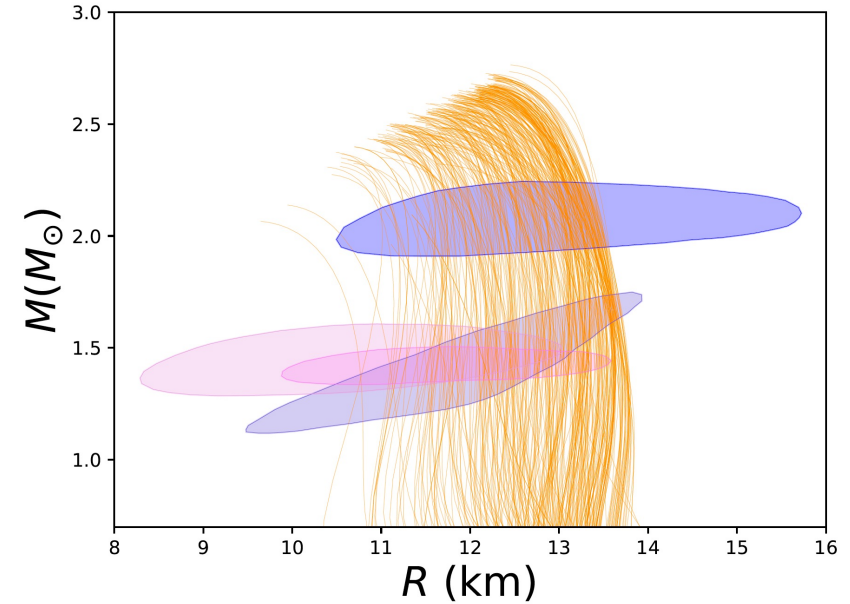
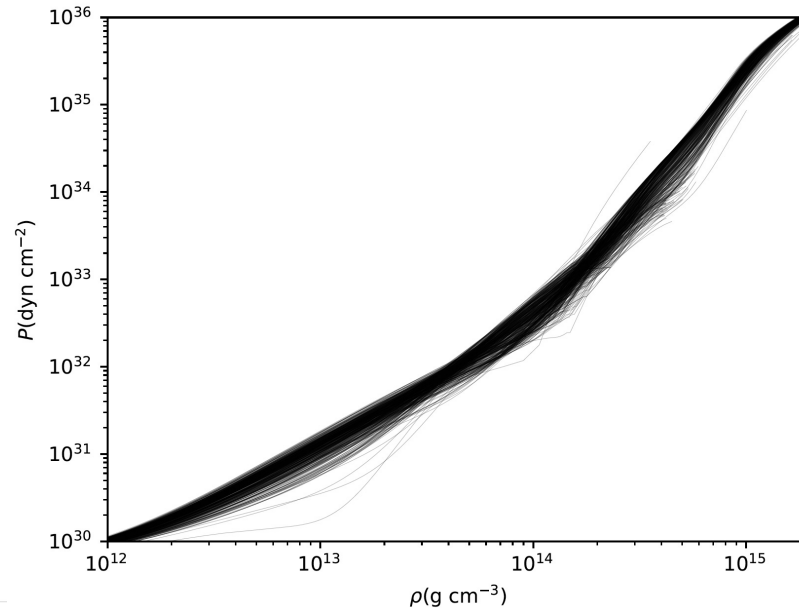
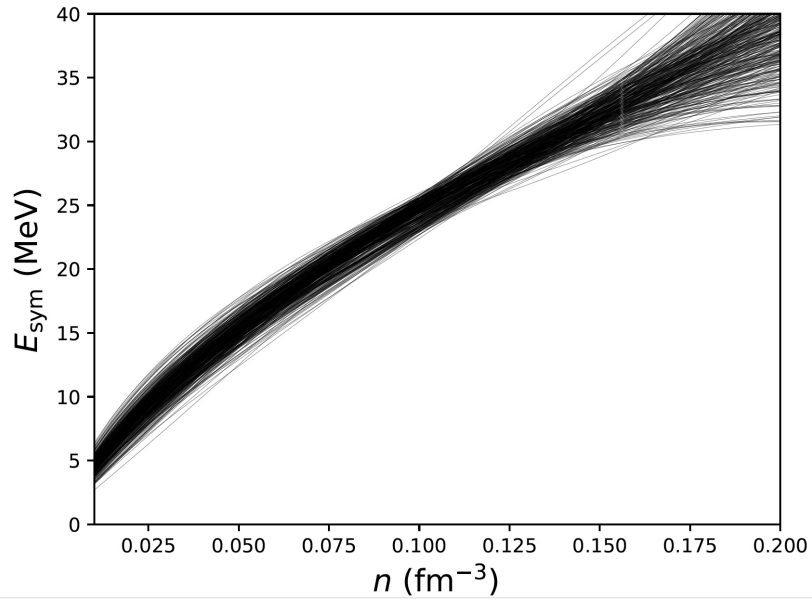


# Pion spectral ratios

(From Lynch+ arXiv:2310.11588; Liu+ arxiv:2006.15861)



Combined – Slight preference for higher radii  
- Nuclear has stuff to say!



# Systematic errors to look out for:

- Choice of model
- Choice of observables to include – and ignore
- Choice of model parameters
- Priors on those parameter
- Difference in definitions of parameters
- Model dependence extrapolating from one density to another
- Using “observables” that have already been inferred using a different model to yours
- Awareness of what is actually being measured
- No neutron star crust! – Systematic error in radius up to 0.5km

## Systematic Errors



**Low Accuracy  
High Precision**

Pic: Aaron Zhu

# Symmetry energy: some communication problems

- Proliferation of nomenclature

$$E_{\text{sym}}, S, J, a_{\text{sym}}, c_{\text{sym}}, \dots$$

- Second order or all orders?

$$E_{\text{sym},2}(\rho) = \left. \frac{1}{2} \frac{\partial^2 E(\rho, \delta)}{\partial \delta^2} \right|_{\delta=0}$$

$$E_{\text{sym}}(\rho) = E(\rho, \delta = 1) - E(\rho, \delta = 0) = E_{\text{PNM}}(\rho) - E_{\text{SNM}}(\rho)$$

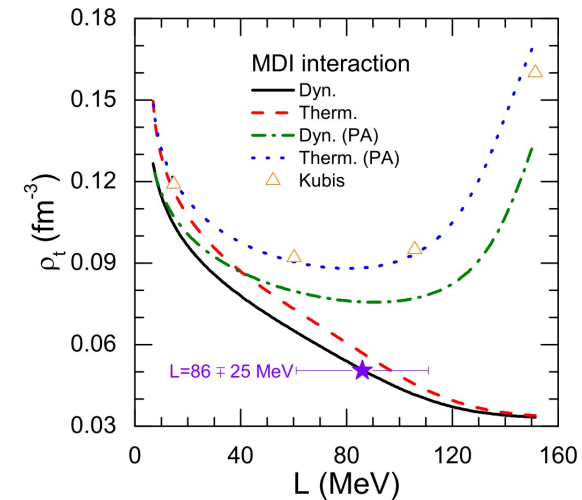
Difference < 3 MeV at saturation density BUT could be larger in RMF models (e.g. Zhao+ arXiv:2406.05267: "CREX1" RMF model:  $J_2=32.9$  MeV,  $J=54.3$  MeV! In neutron-rich matter  $\delta \cong 1$  so higher order terms become important

- Non-analytic terms in  $\delta$  Expansion

$$E_{\text{sym},\log} \delta^4 \log \delta$$

(Somasundaram+ 2009.04737, Kaiser arXiv:1504.00604

Xu et al, arxiv:0807.4477

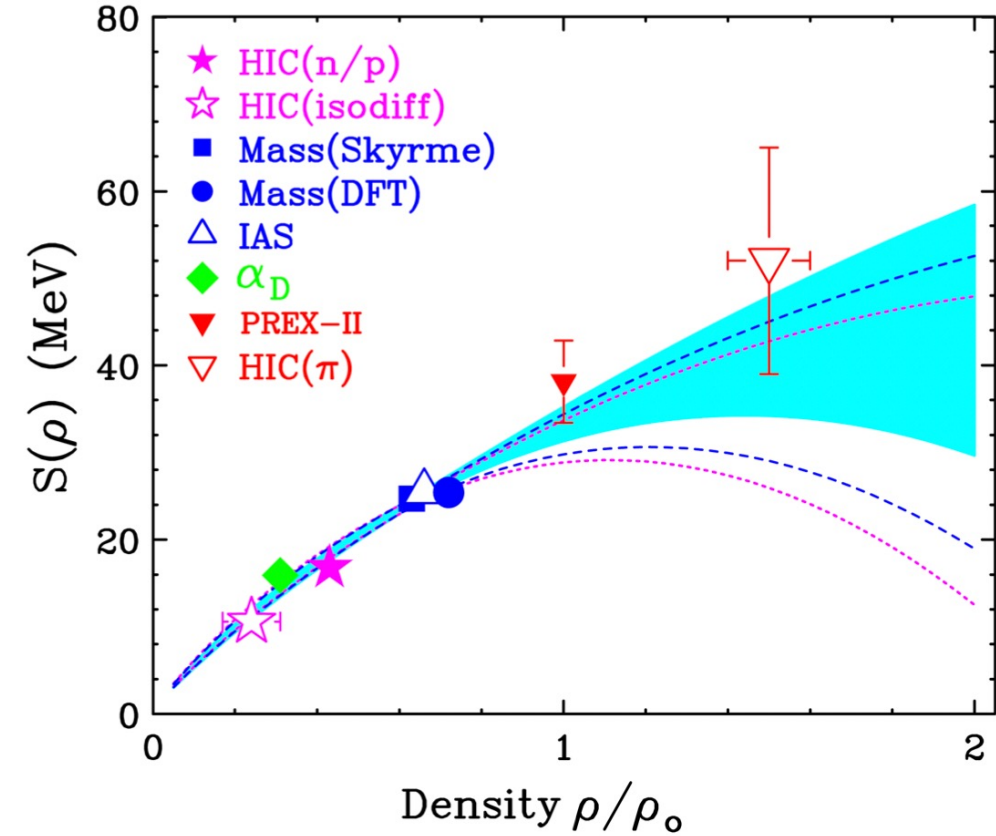


Systematic Errors



Low Accuracy  
High Precision

Different observables  
constrain at different  
densities...



Tsang and Lynch, arxiv:2106.10119

Different observables constrain at different densities...

... so resulting constraints on nuclear matter parameters at saturation density involve model-dependent extrapolation

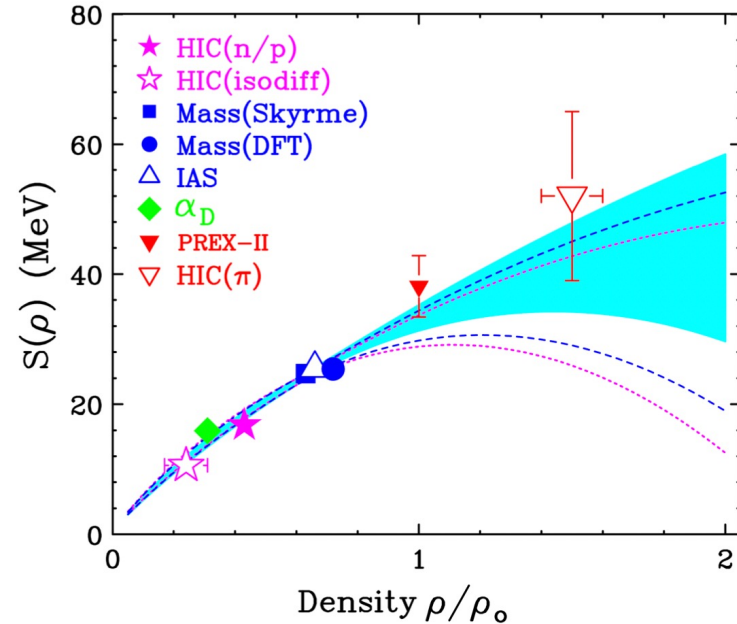
$$E_{\text{sym}}(\rho) = E_{\text{sym}}(\rho_0) + L\left(\frac{\rho - \rho_0}{3\rho_0}\right) + \frac{K_{\text{sym}}}{2}\left(\frac{\rho - \rho_0}{3\rho_0}\right)^2 + \frac{J_{\text{sym}}}{6}\left(\frac{\rho - \rho_0}{3\rho_0}\right)^3$$

$$S_{\text{RMF}}(\rho) = A(\rho)\rho^{2/3} + B(\rho)\rho,$$

$$S_{\text{SHF}}(\rho) = a\rho^{2/3} - b\rho - c\rho^{5/3} - d\rho^{\sigma+1}$$

$$S(\text{SHF, ext}) = a\rho + b\rho^{4/3} + c\rho^{5/3} + d\rho^2 + \dots$$

$$S(n) = E_{\text{kin},0}\left(\frac{n}{n_{\text{sat}}}\right)^{2/3} + E_{\text{pot},0}\left(\frac{n}{n_{\text{sat}}}\right)^{\gamma_{\text{asy}}}.$$

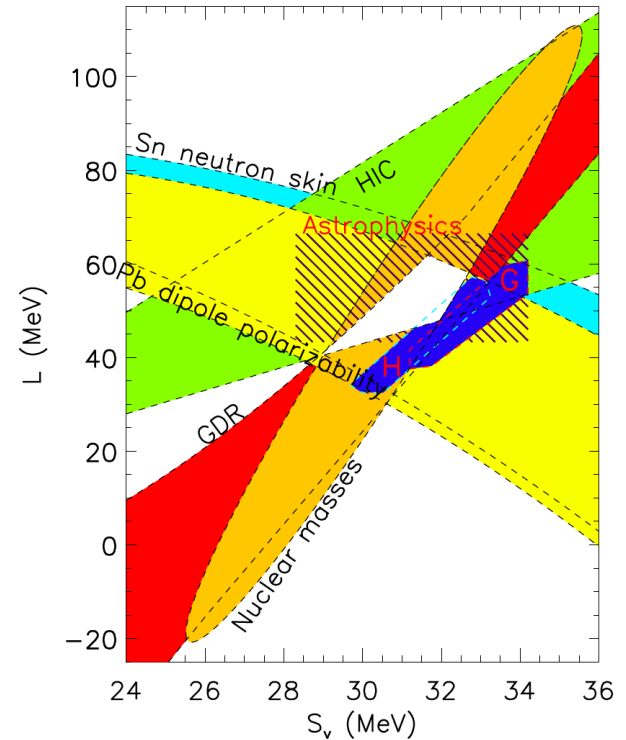


Tsang and Lynch, arxiv:2106.10119

Systematic Errors



Low Accuracy  
High Precision



Lattimer, Lim ApJ771(2013)  
Lattimer, Steiner EPJA50 (2013)

# Why pay attention to model systematics

One can argue they are small compared with uncertainties in measurements  
...until someone checks and finds out they're not...

We don't know how multiple systematics compound

Over next 1-2 decades, much more data at current and proposed facilities:

MREX:  $\Delta F_w$  improved by **factor of 3**

NewAthena/eXTP  $\Delta R \sim \mathbf{0.5km}$  or better, crust cooling, X-ray glitches

Einstein/Cosmic Explorer  $\Delta R \sim \mathbf{0.1km}$  (optimistic estimate! and converted from tidal deformability)

Moment of inertia: **10% by 2030**, increasing in precision thereafter

If a galactic supernova goes off: **Binding energy of NS to 10%**

SkA: Order of magnitude more pulsars

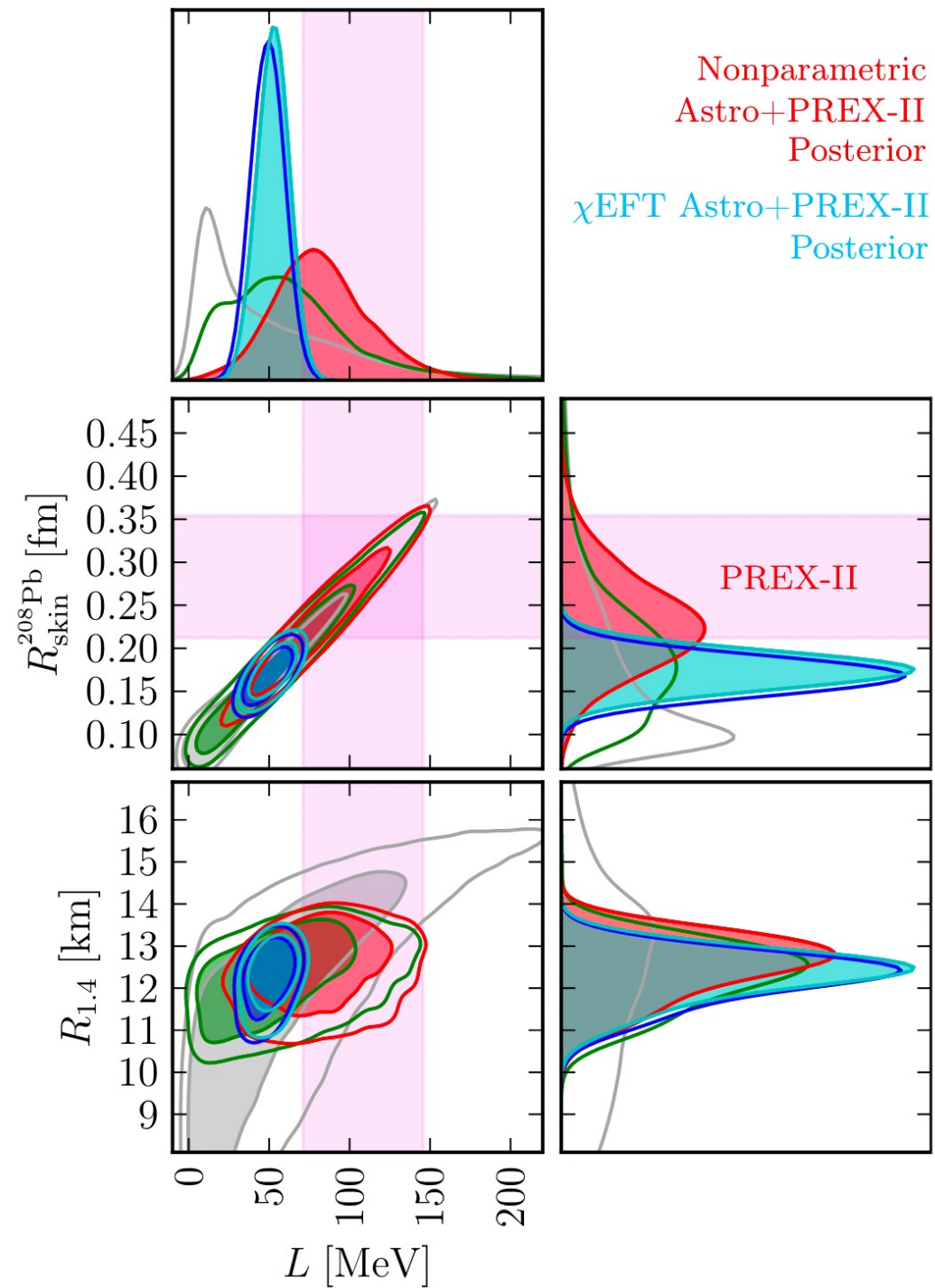
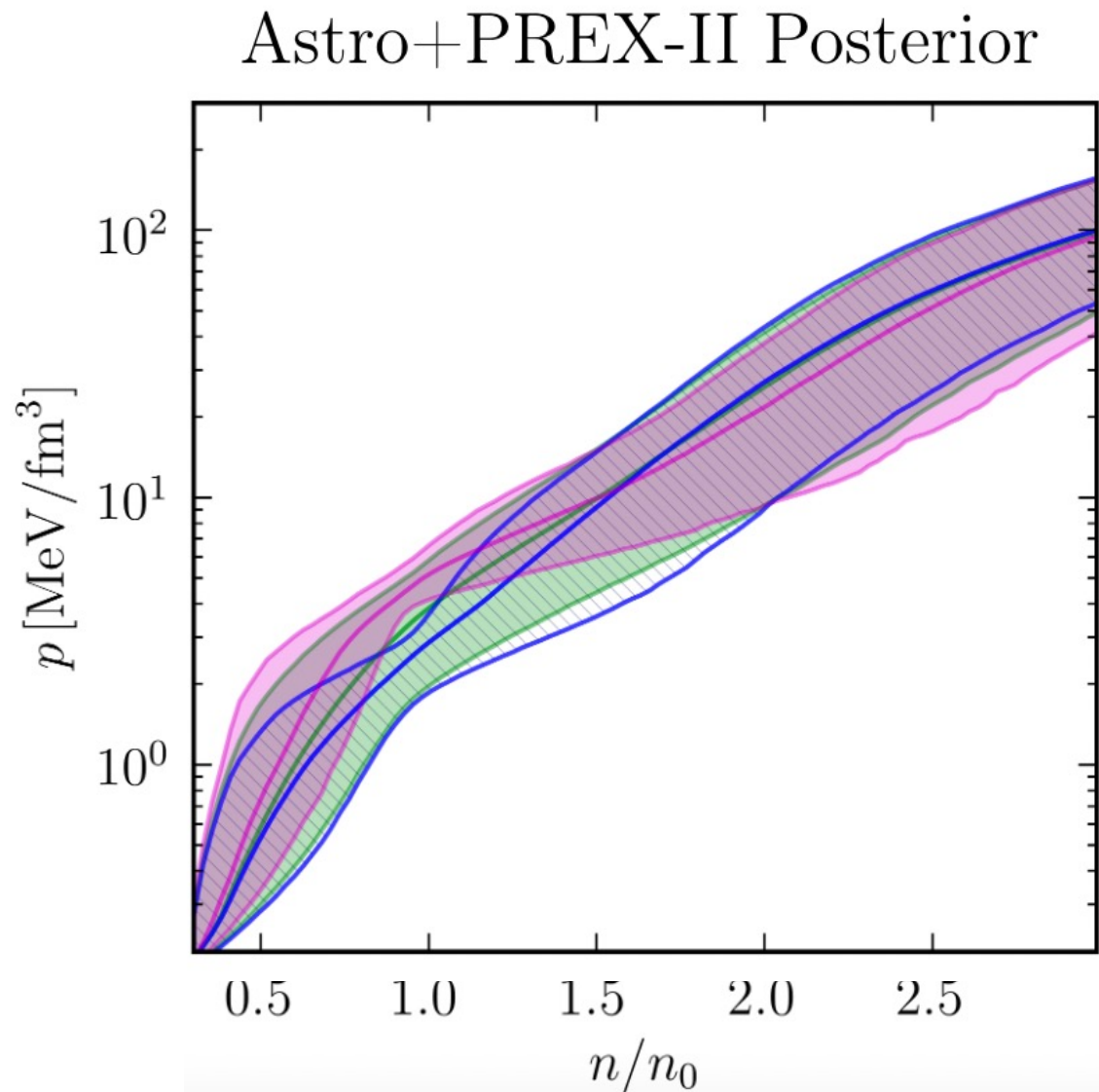
More info across density/temperature space from GSI/FAIR, FRIB, RIKEN, RHIC....

Much more data on crust cooling, pulsar glitches, crust oscillations

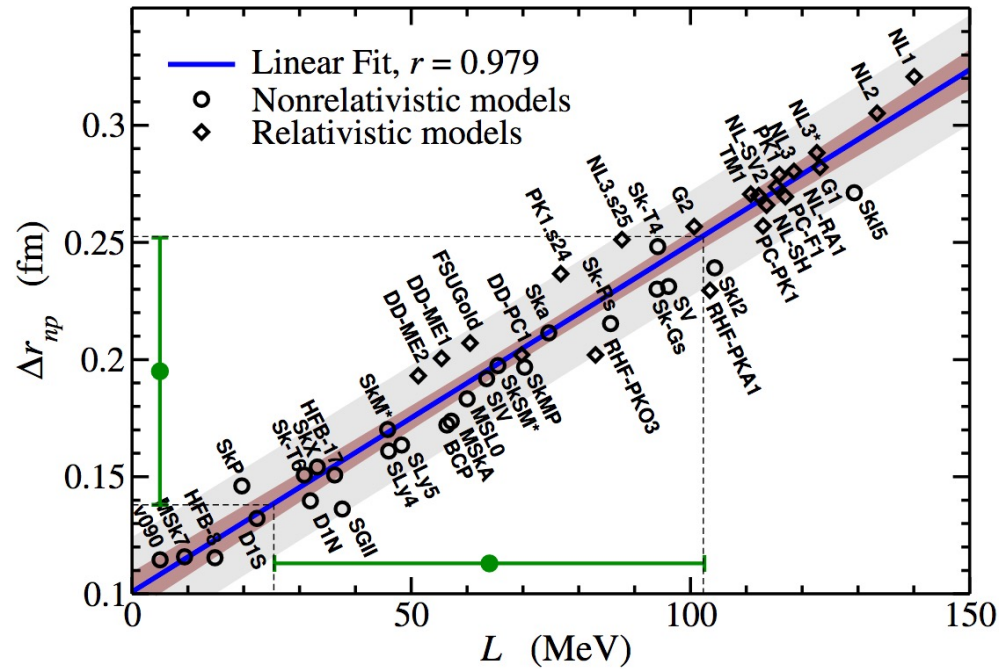
For example, neglecting crust&rotation both lead to systematic errors close to 0.5km

Not overly optimistic to expect significant improvement in precision of measurements over the next 1-2 decades.  
Suddenly “small” systematics are not so small

# Example 1: Essick+ arXiv 2102.10074



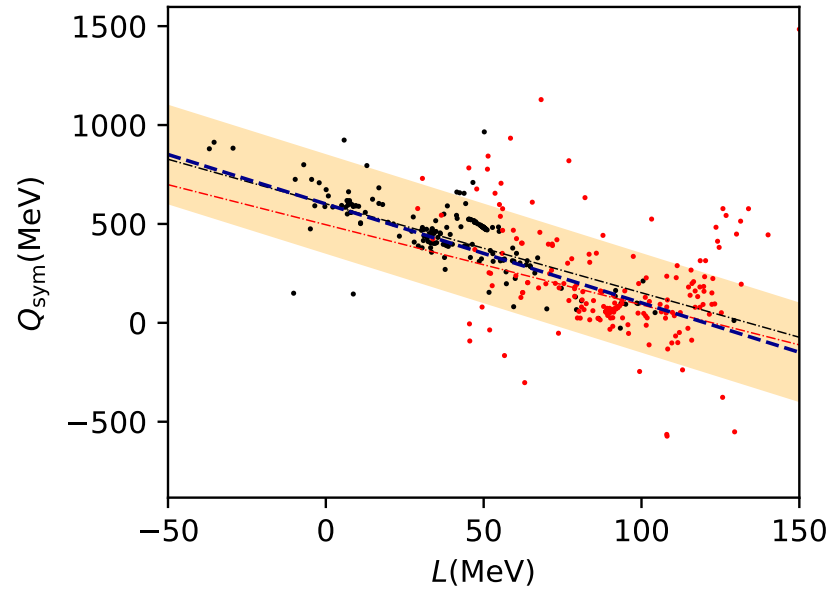
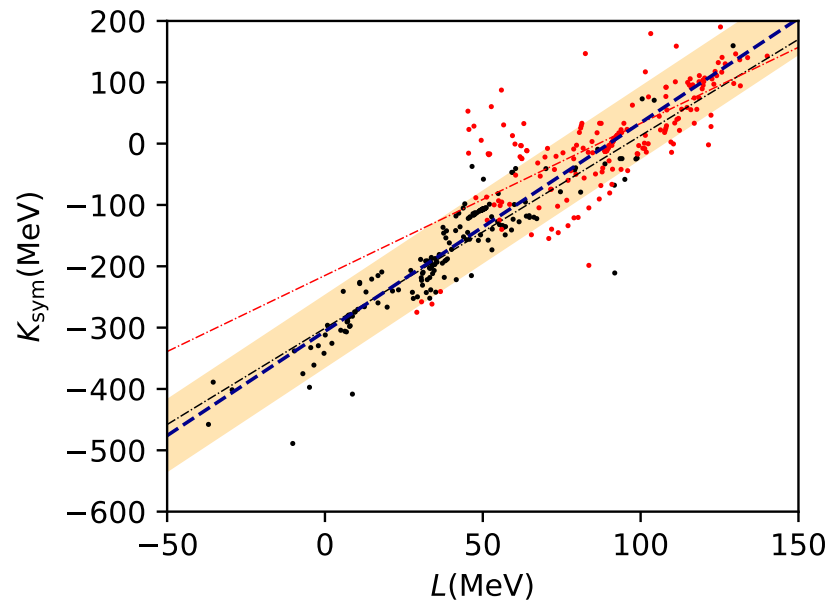
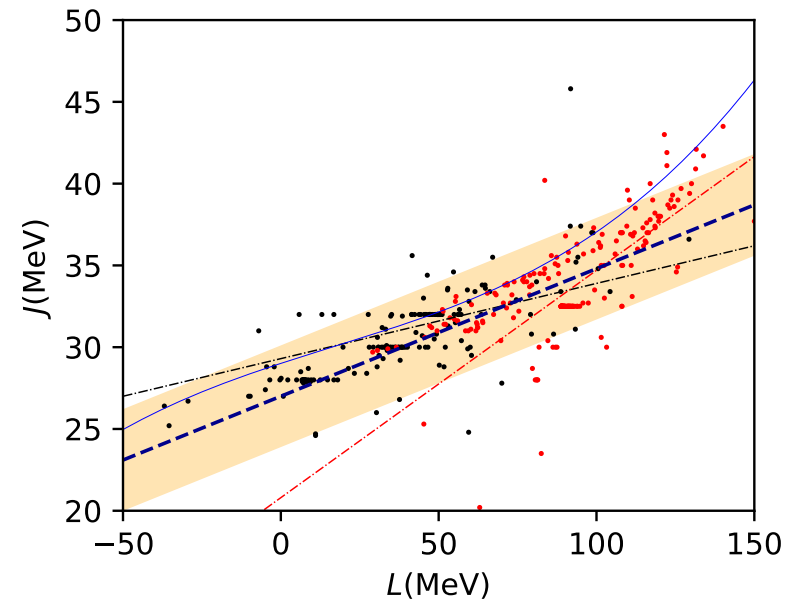
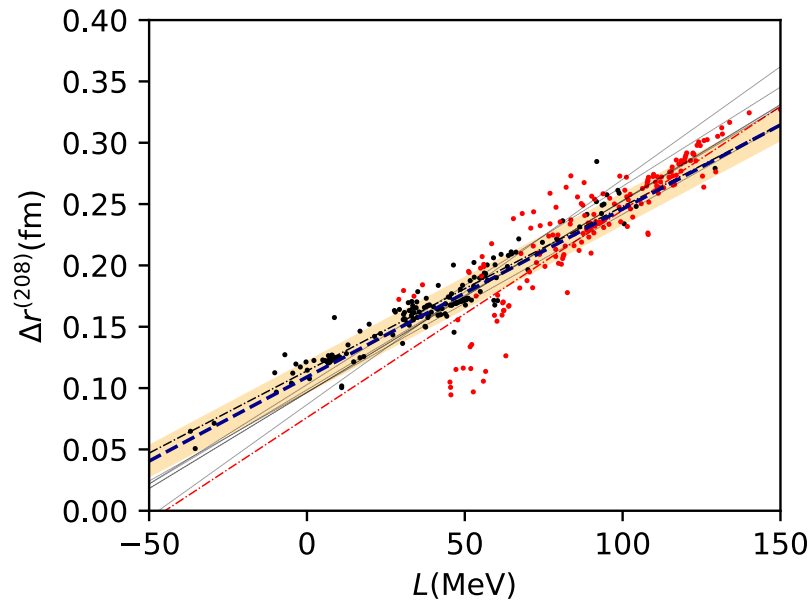
# Connecting L to neutron skin: Existing DFTs predict neutron skin-L relation

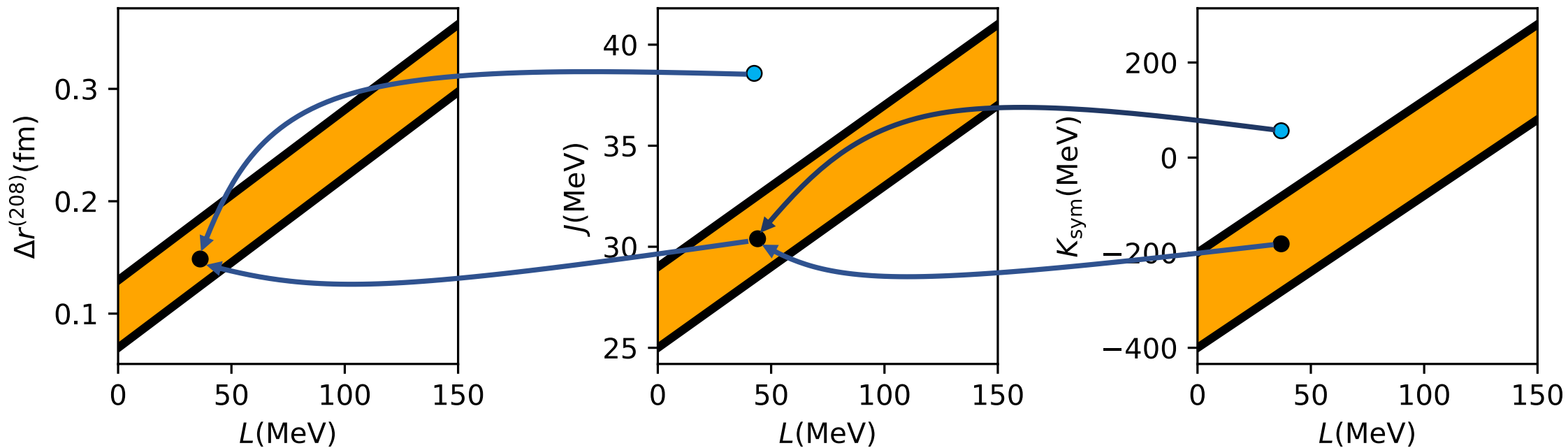


Roca-Maza et al, arxiv:1103.1762

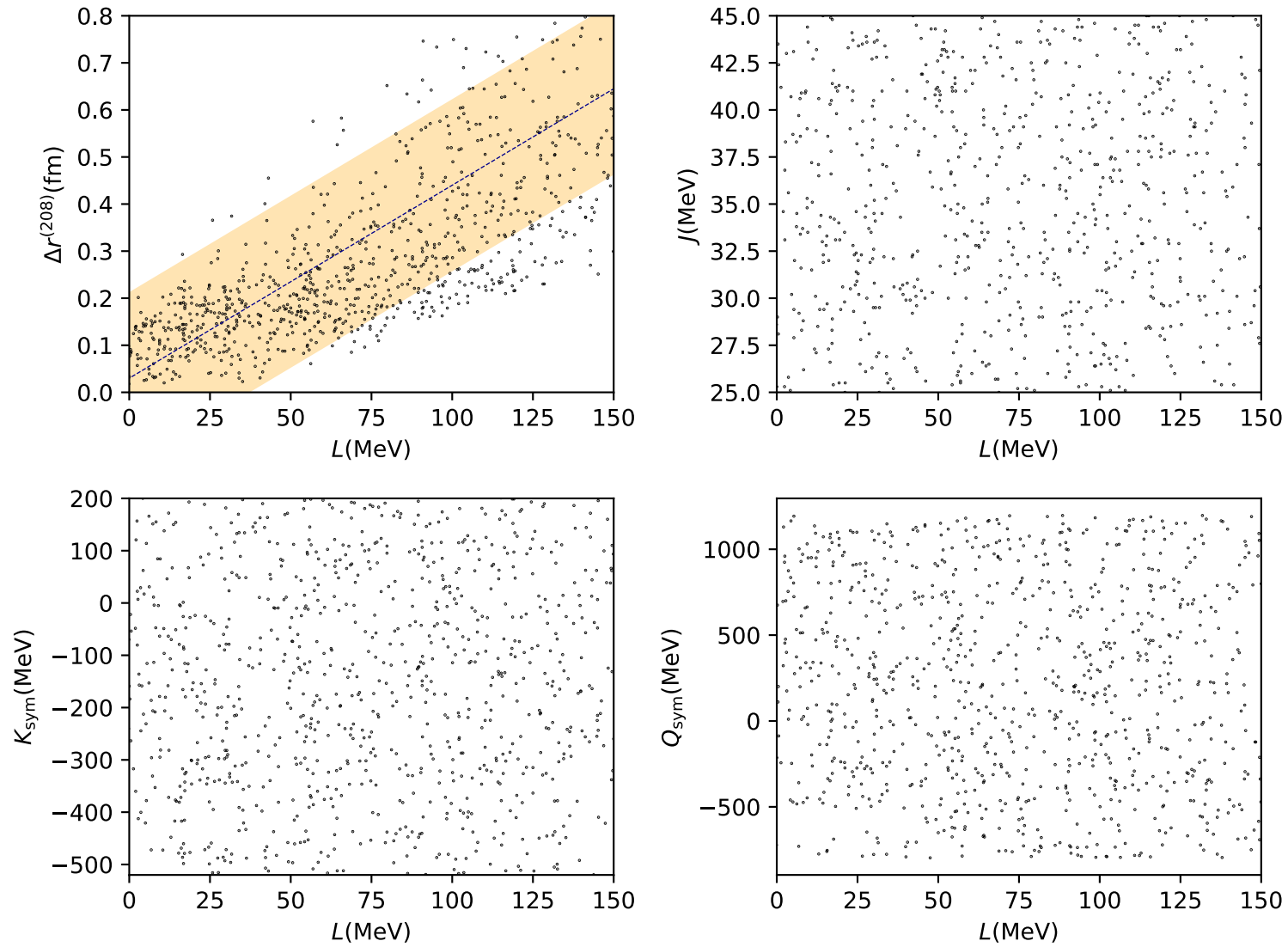
- This relation *includes* the aggregate effects of including the nuclear binding energy data in fitting individual models, not something that is controlled
- This induces correlations between  $J, L, K_{\text{sym}}$

# Using 200+Skyrmes and 100+RMF (Dutra arXiv:1202.3902,1405.3633)

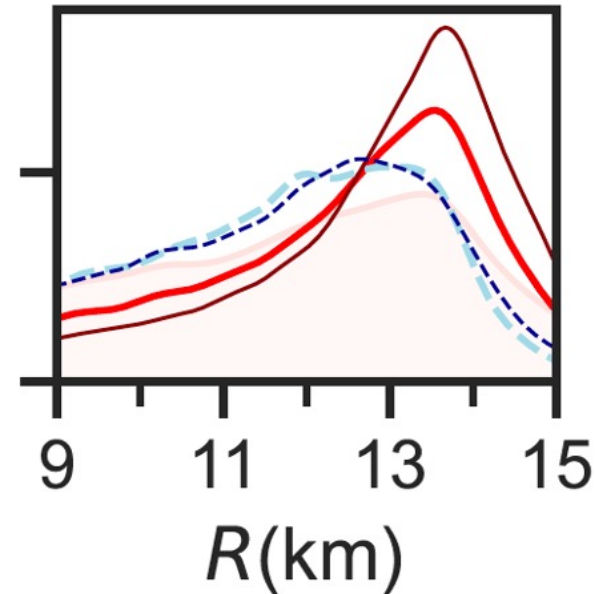
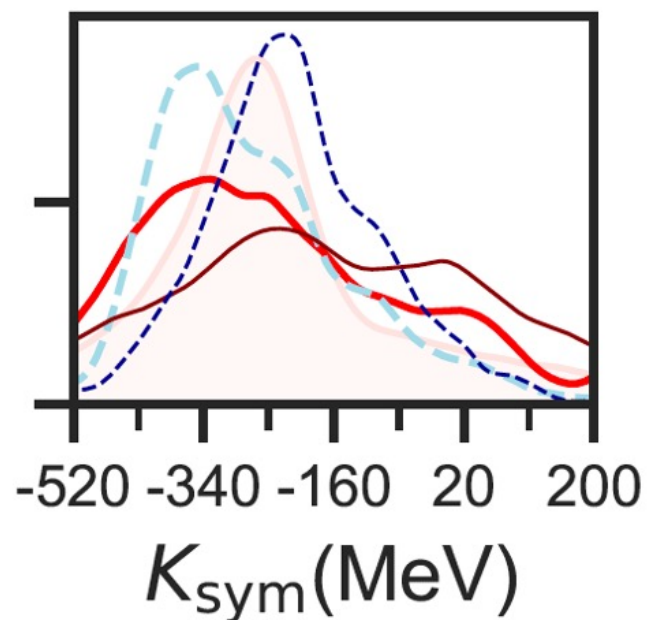
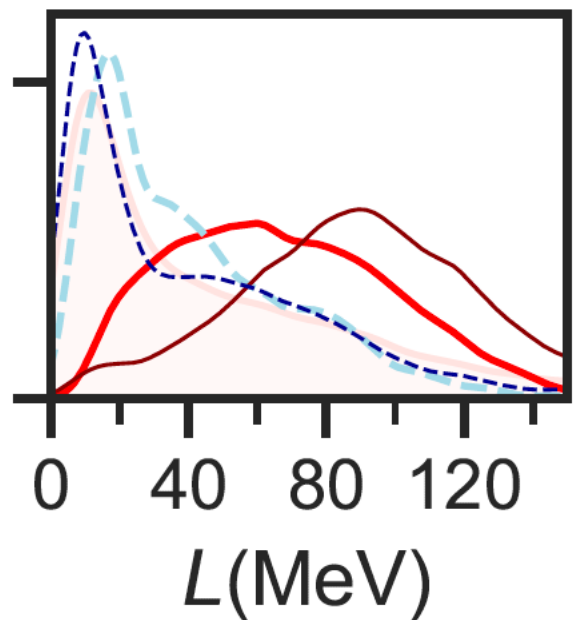




# Skyrme EDF: neutron skin of $^{208}\text{Pb}$ , uniform priors on symmetry energy params $J, L, K_{\text{sym}}, Q_{\text{sym}}$



Using priors from Essick+ arXiv 2102.10074



	Prior	
	PREX	$65.47^{38.33}_{32.05}$
	Dip.Pol.	
	PREX_emp	
	Dip.Pol._emp	$89.41^{34.67}_{35.06}$

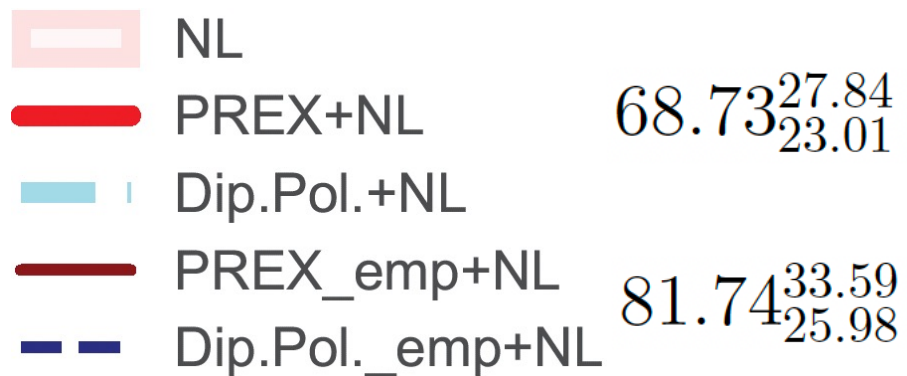
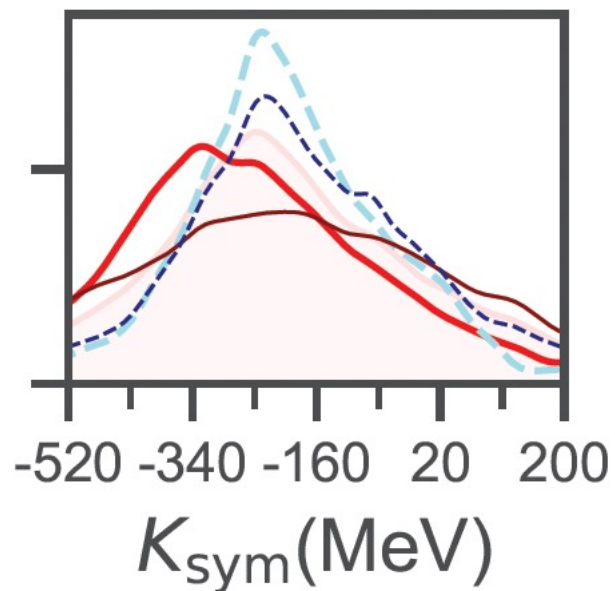
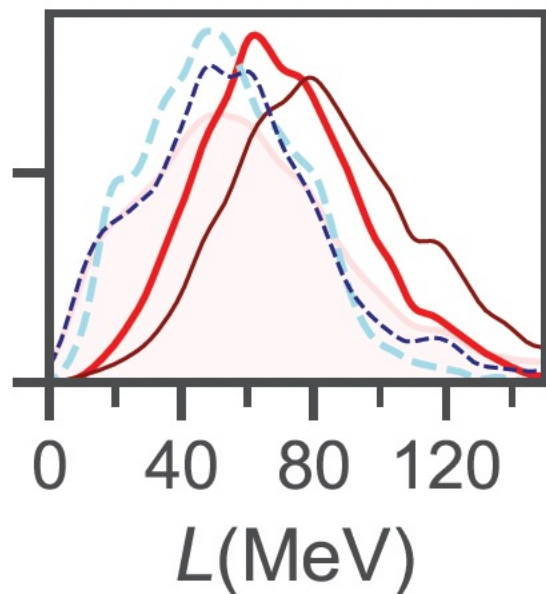
	Prior	
	PREX	$-316.91$
	Dip.Pol.	
	PREX_emp	
	Dip.Pol._emp	$-215.09^{300.40}_{284.37}$

	Prior	
	PREX	$12.86^{1.45}_{2.61}$
	Dip.Pol.	
	PREX_emp	$13.21^{1.08}_{2.23}$
	Dip.Pol._emp	

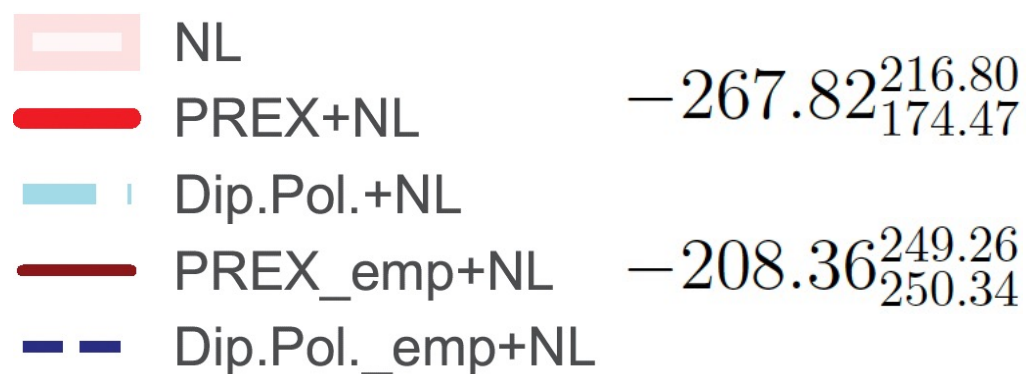
(MeV)

(MeV)

(km)



(MeV)



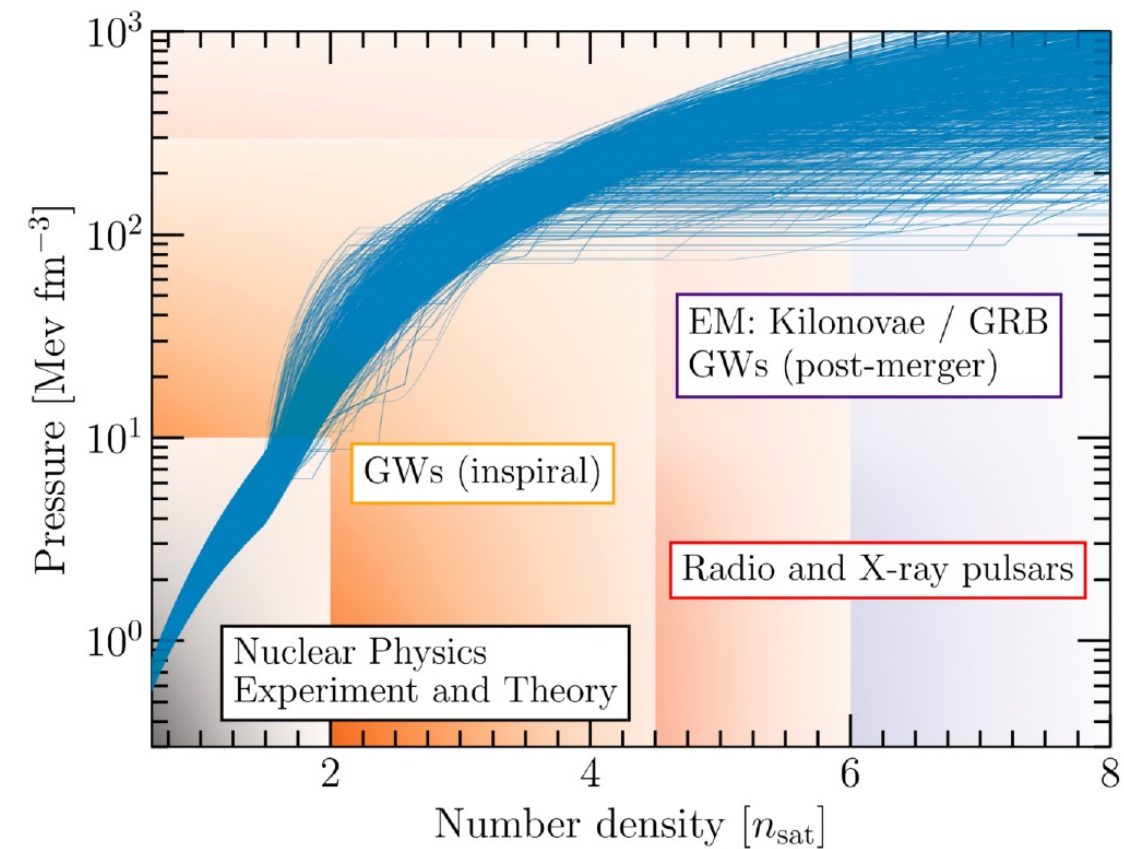
(MeV)

Experiments such as neutron skin and dipole polarizability probes EOS below mostly saturation density, how relevant are those in determine neutron star properties?

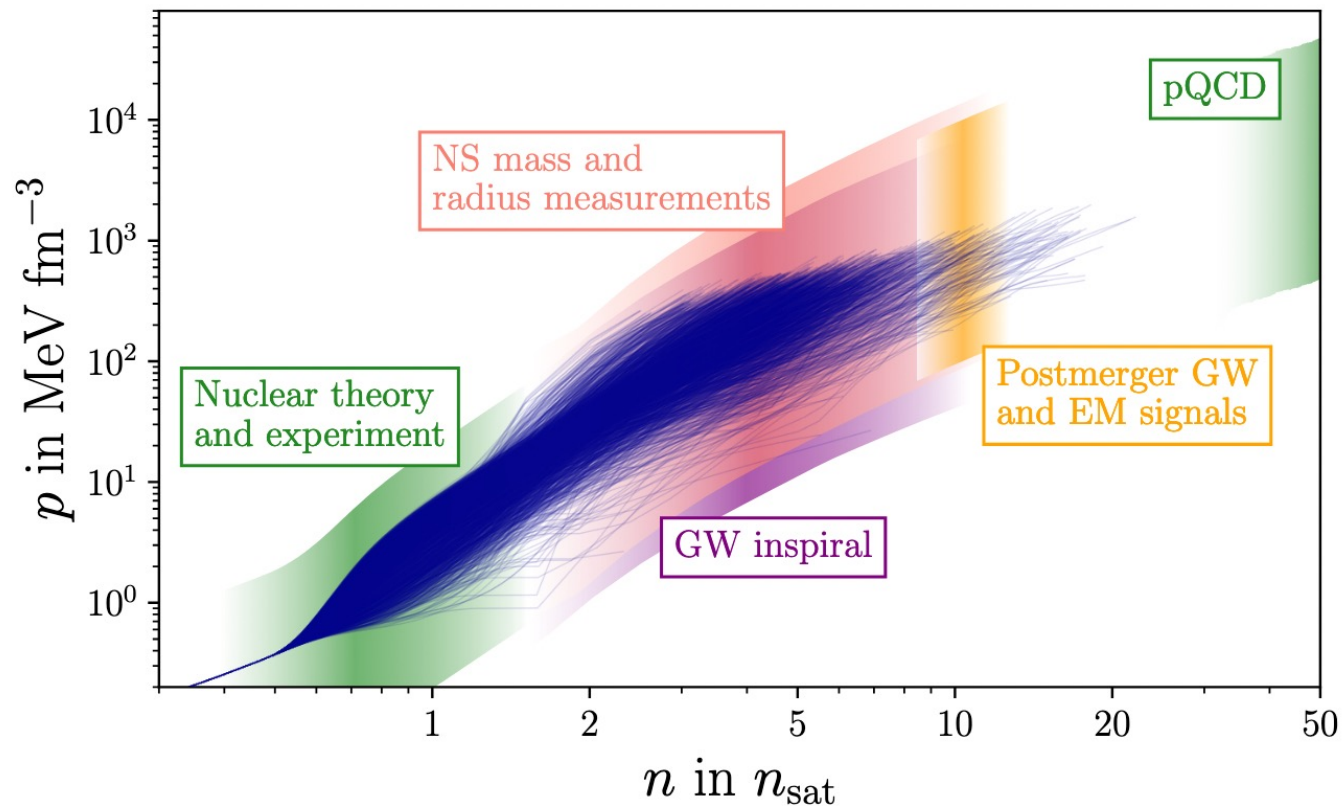


(with apologies to Matt Groening)

# Crust usually de-emphasized in EOS plots

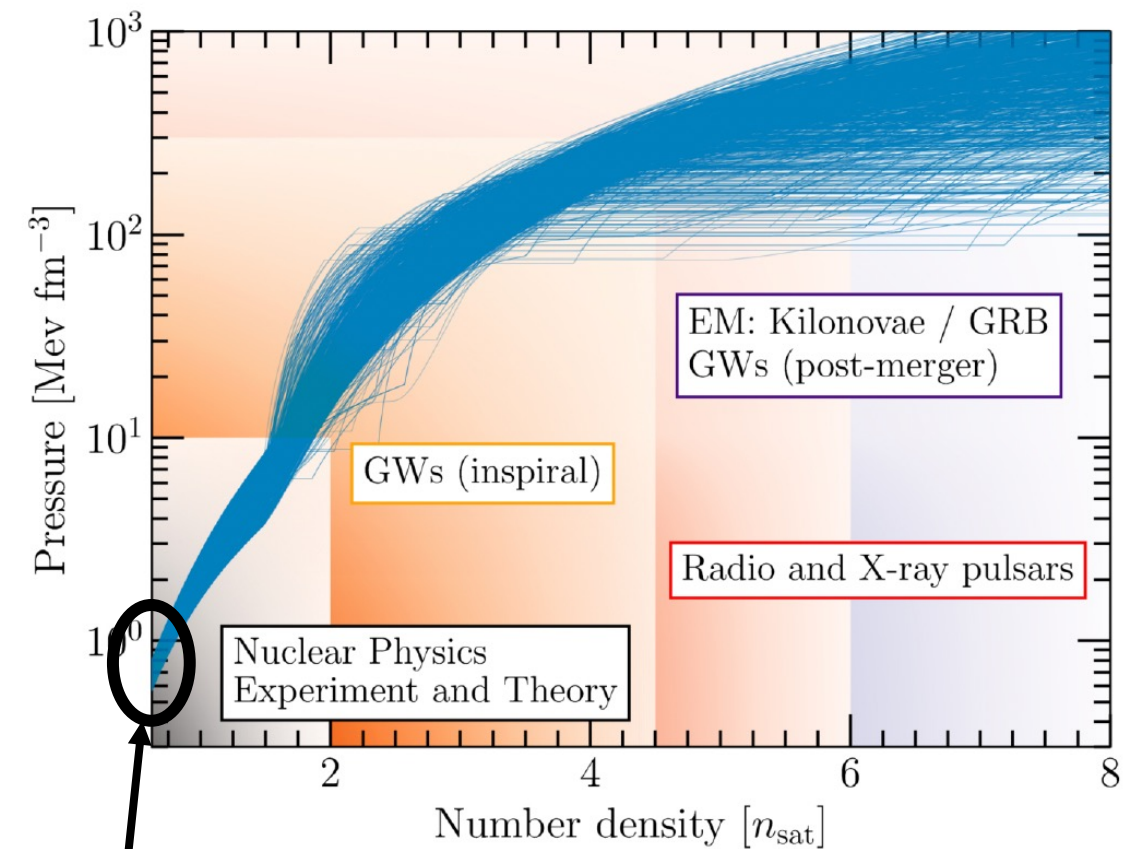


Pang et al, arxiv:2205.08513



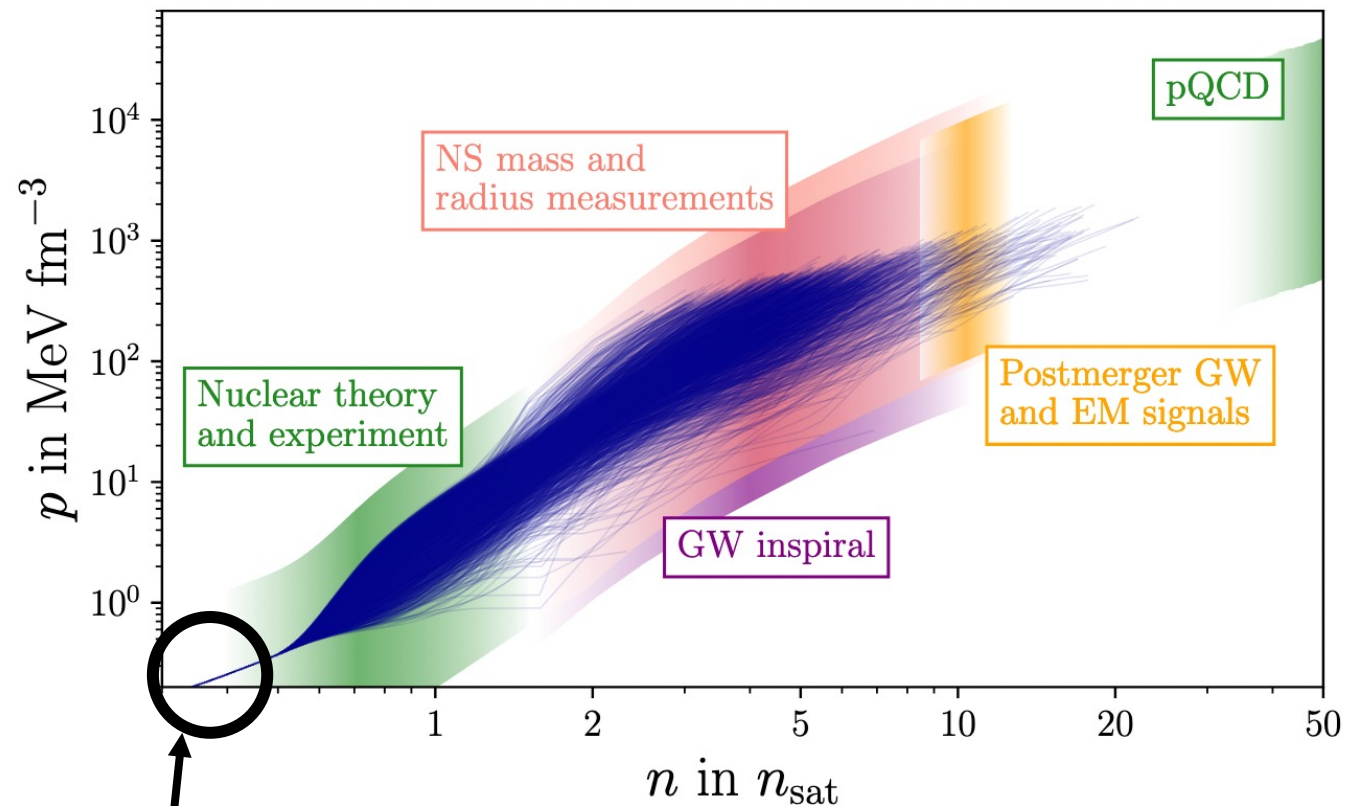
Koehn+ arXiv:2402.04172

# Crust usually de-emphasized in EOS plots



Pang et al, arxiv:2205.08513

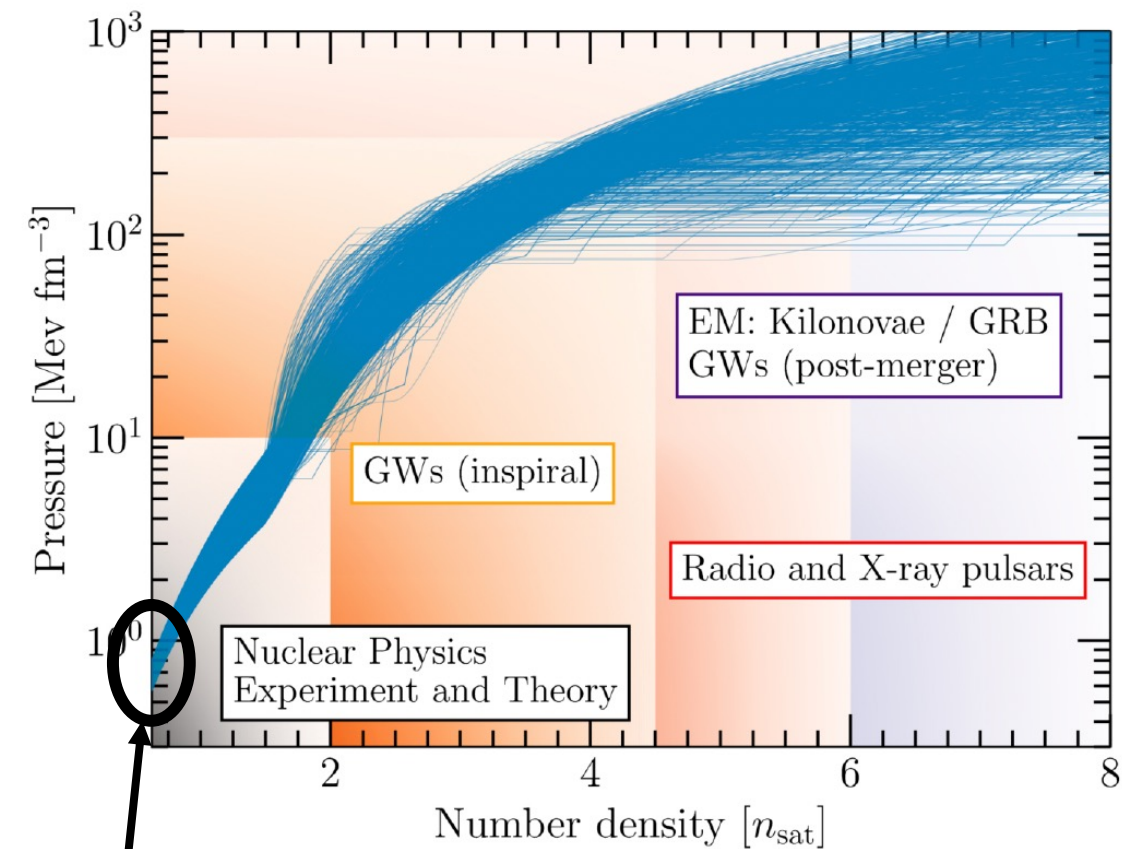
There's the crust!



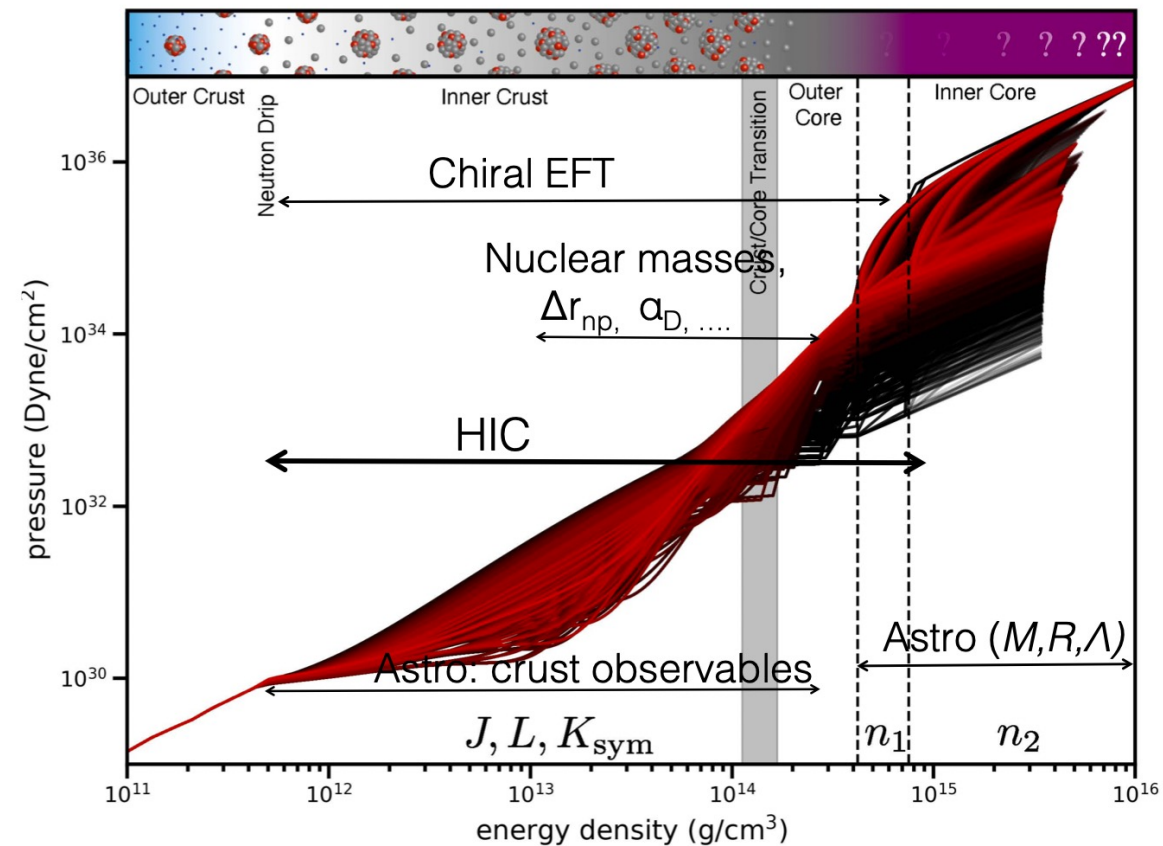
Koehn+ arXiv:2402.04172

Just one crust EOS!

# Crust usually de-emphasized in EOS plots



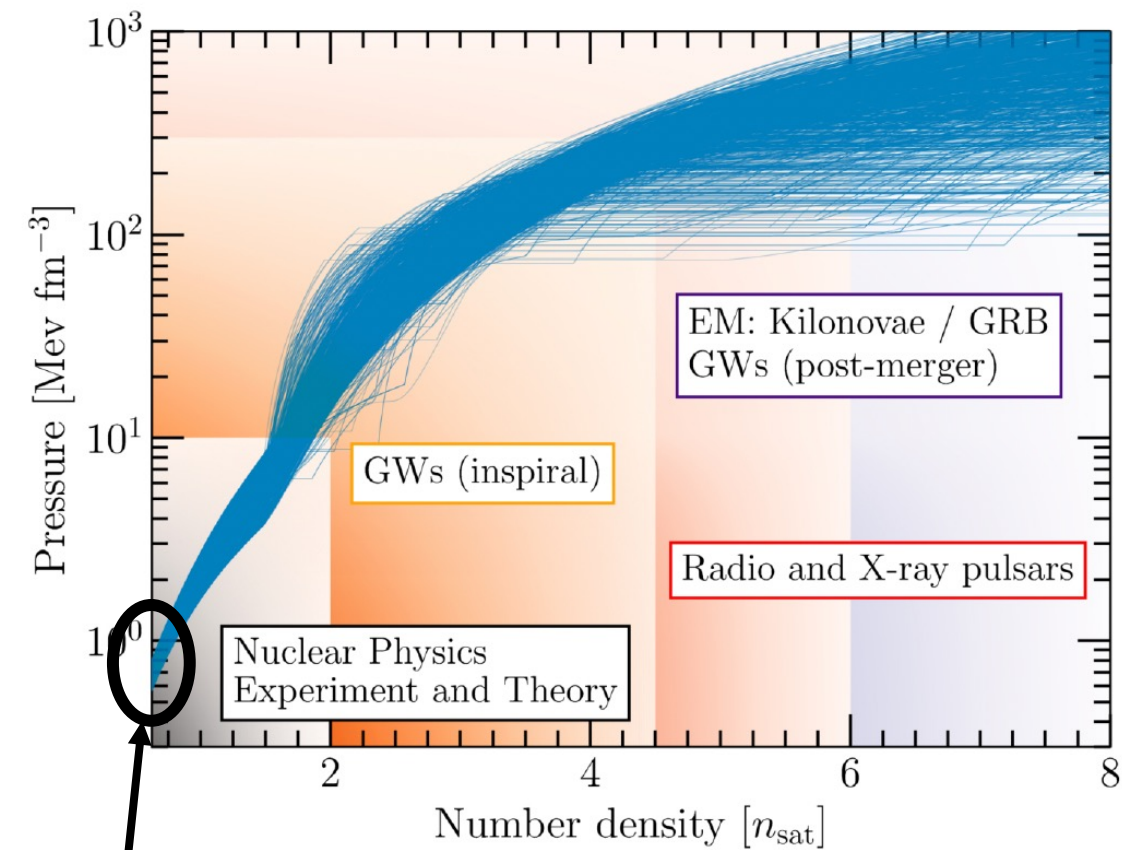
Pang et al, arxiv:2205.08513



Neill+ 2208.00994; Sorenson+ 2301.13253

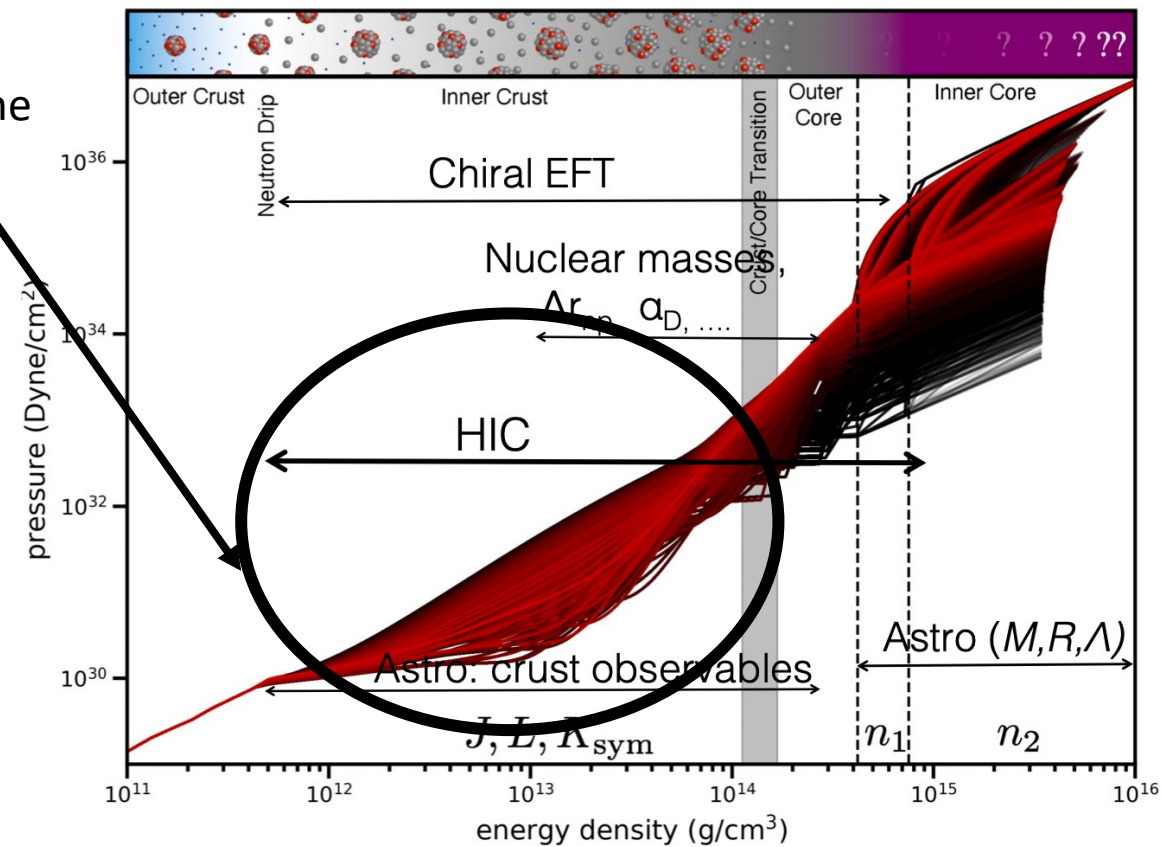
There's the crust!

# Crust usually de-emphasized in EOS plots



Pang et al, arxiv:2205.08513

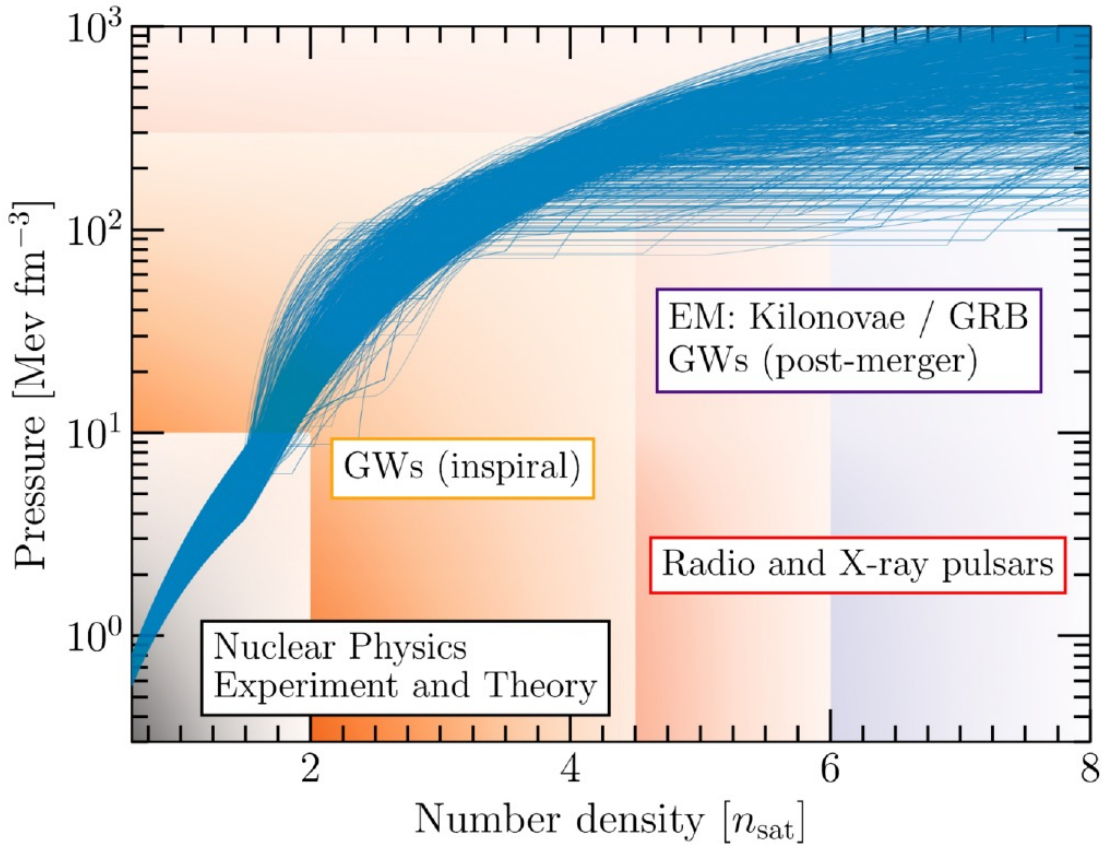
There's the crust!



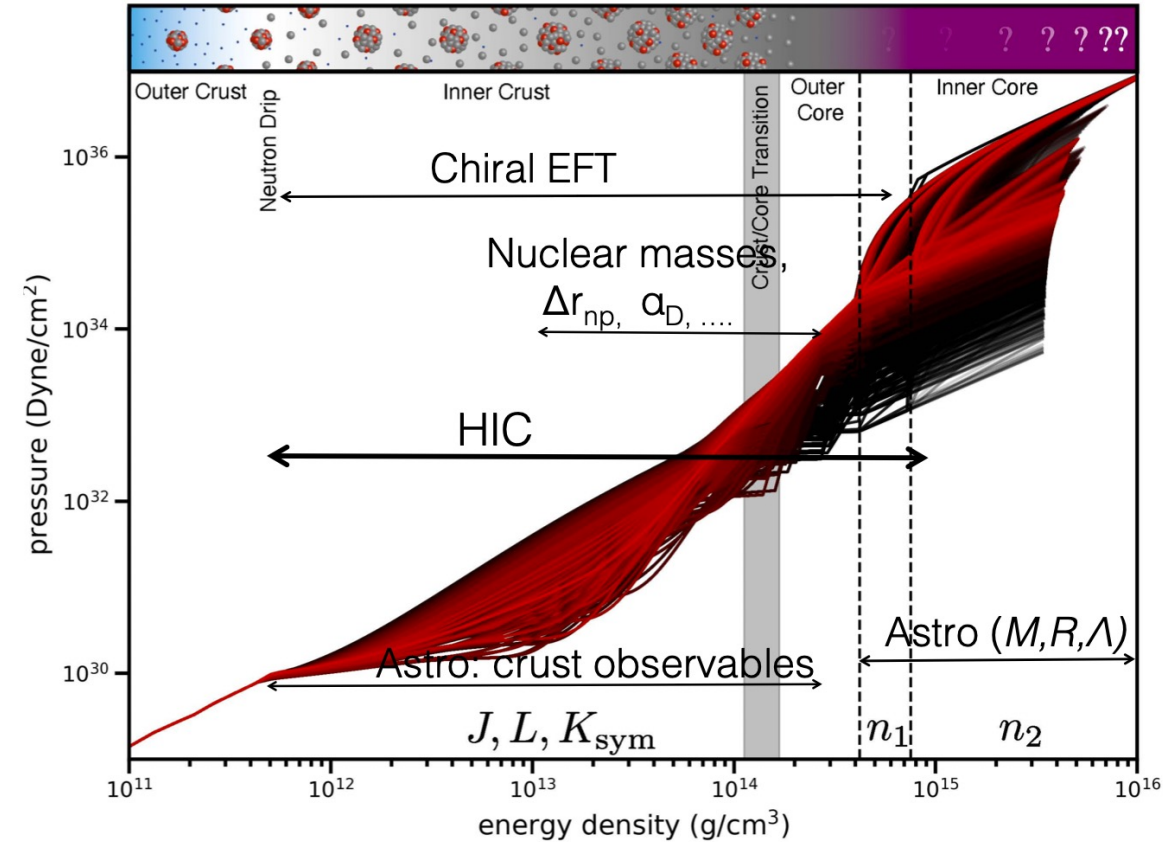
Neill+ 2208.00994; Sorenson+ 2301.13253

There's the crust!

# Core consistent with crust needed for inference of bulk properties



Pang et al, arxiv:2205.08513



Neill+ 2208.00994; Sorenson+ 2301.13253

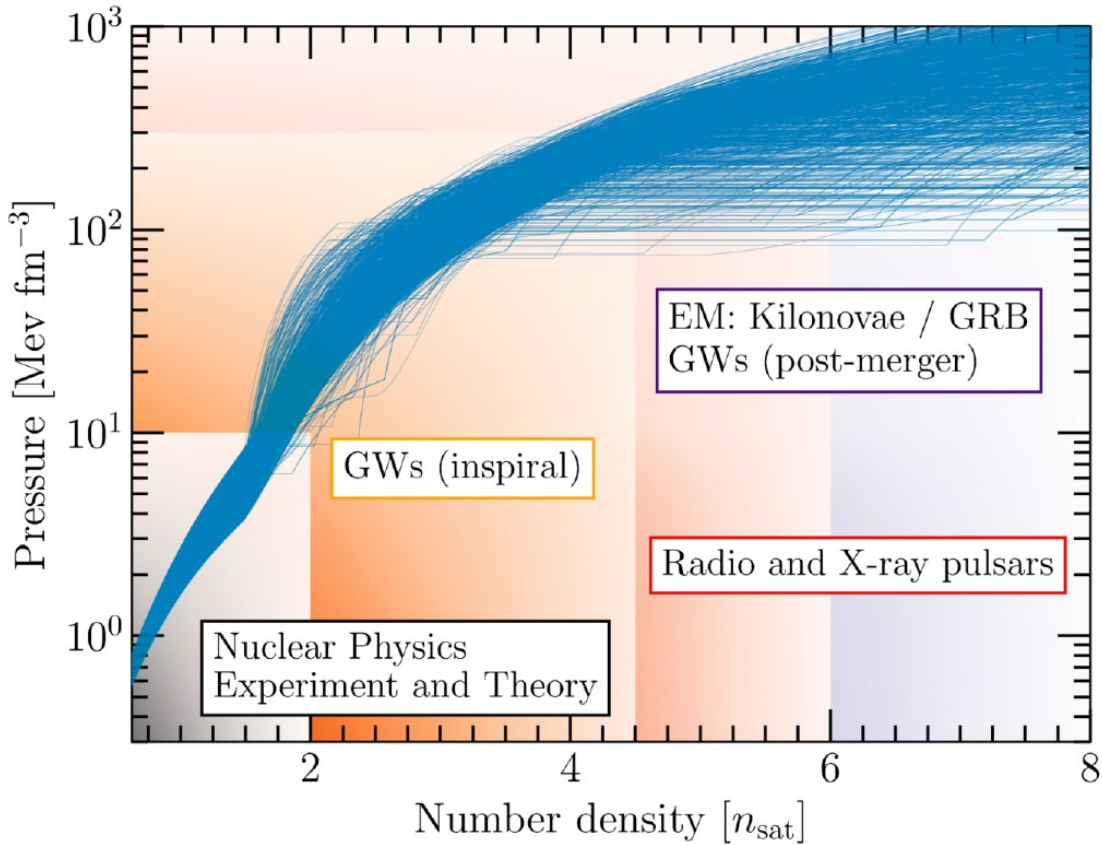
Lami Suleiman + *Phys.Rev.C* 104 (2021) 1, 015801

Crust inconsistent with core EOS leads to errors up to 5% in radius inference – that's 0.5km

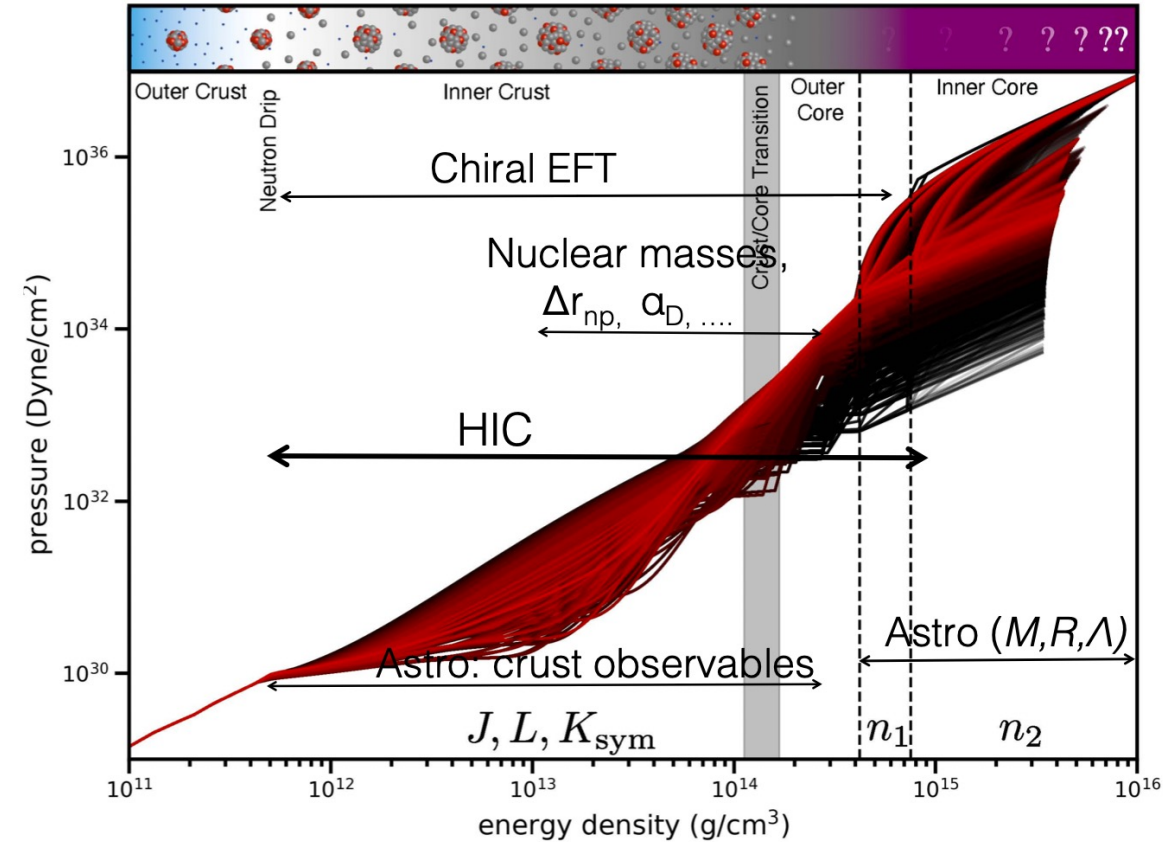
Precision of universal relations underestimated

**NEXT GENERATION X-RAY/GW MEASUREMENTS WILL NEED BETTER CRUST MODELING**

# Core consistent with crust needed for inference of bulk properties



Pang et al, arxiv:2205.08513



Neill+ 2208.00994; Sorenson+ 2301.13253

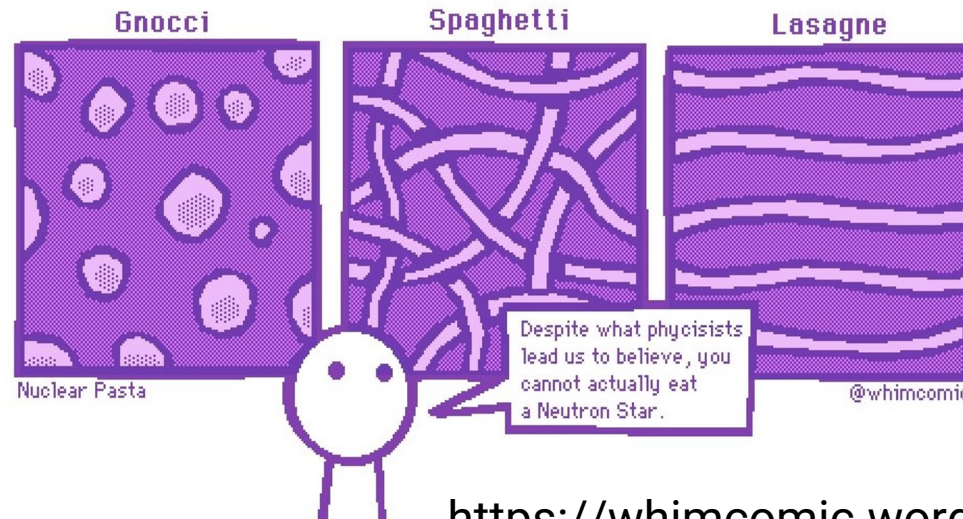
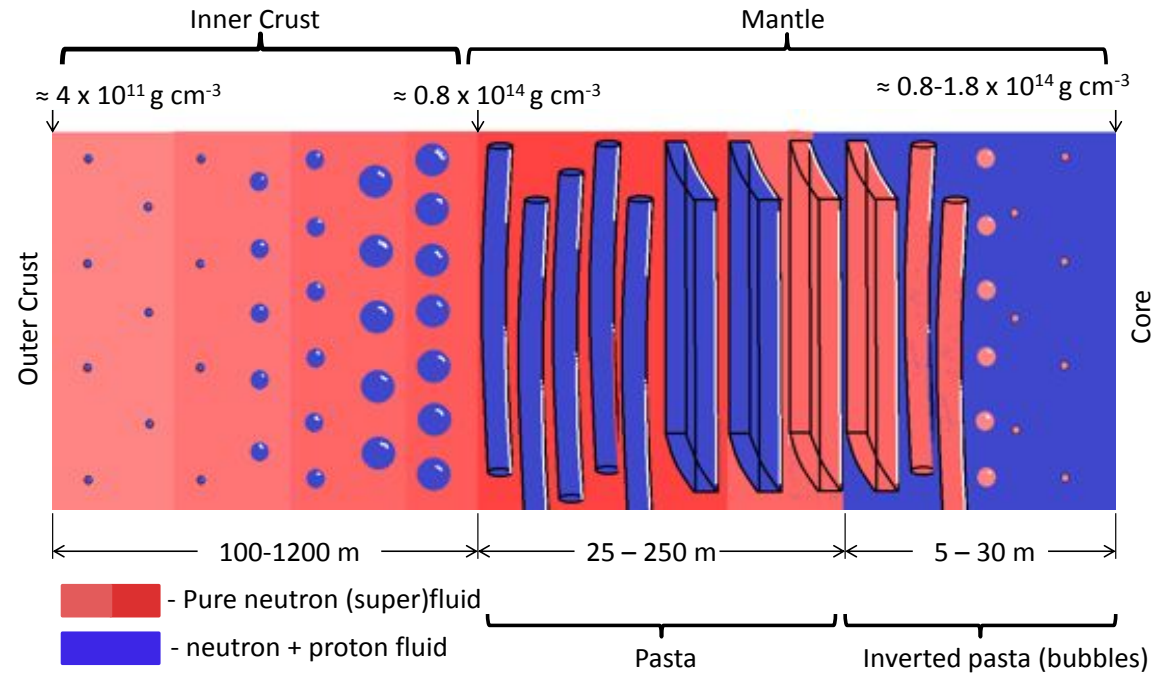
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**NEXT GENERATION X-RAY/GW MEASUREMENTS WILL NEED BETTER CRUST MODELING**

# Modeling the crust



## Structure of Matter below Nuclear Saturation Density

D. G. Ravenhall

*Department of Physics, University of Illinois at Urbana-Champaign, Urbana, Illinois 61801*

and

C. J. Pethick

*Department of Physics, University of Illinois at Urbana-Champaign, Urbana, Illinois 61801,  
and NORDITA, DK-2100 Copenhagen Ø, Denmark*

and

J. R. Wilson

*Lawrence Livermore National Laboratory, Livermore, California 94550*

(Received 5 May 1983)

It will be interesting to explore the consequences of these spaghettilike and lasagnalike phases of dense matter. Their physical properties will have to reflect the great departure from isotropy that these phases possess. Neutrino scattering

properties. After all, the cooking of spaghetti, while it spoils the perfect straightness of the strands, does not destroy the characteristic short-range order.

# Neutron star mantle as a complex nuclear fluid

## DYNAMICAL SIMULATION OF NUCLEAR “PASTA”: SOFT CONDENSED MATTER IN DENSE STARS

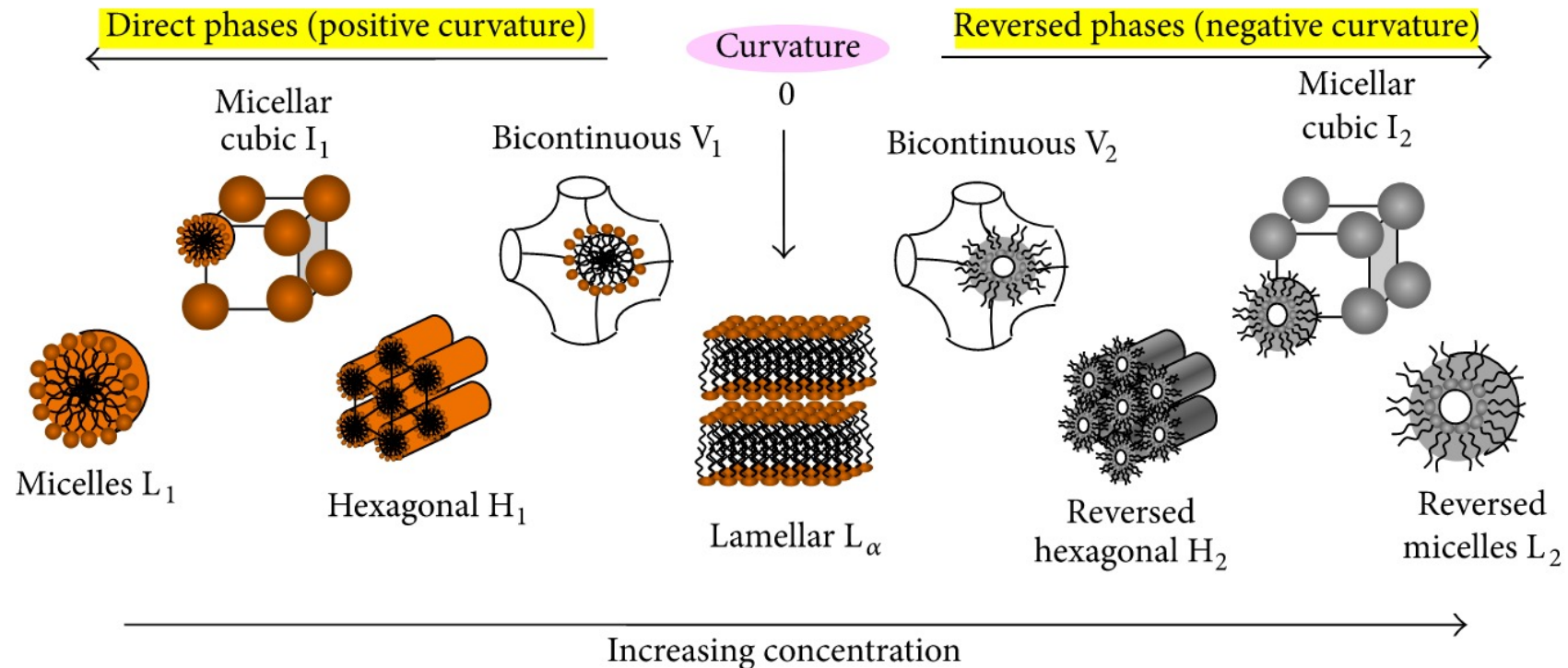
*Gentaro Watanabe<sup>a,b\*</sup> and Hidetaka Sonoda<sup>c,b</sup>*

Arxiv:cond-mat/0502515v2

## Colloquium: Astromaterial science and nuclear pasta

M. E. Caplan and C. J. Horowitz

Rev. Mod. Phys. **89**, 041002 — Published 23 October 2017



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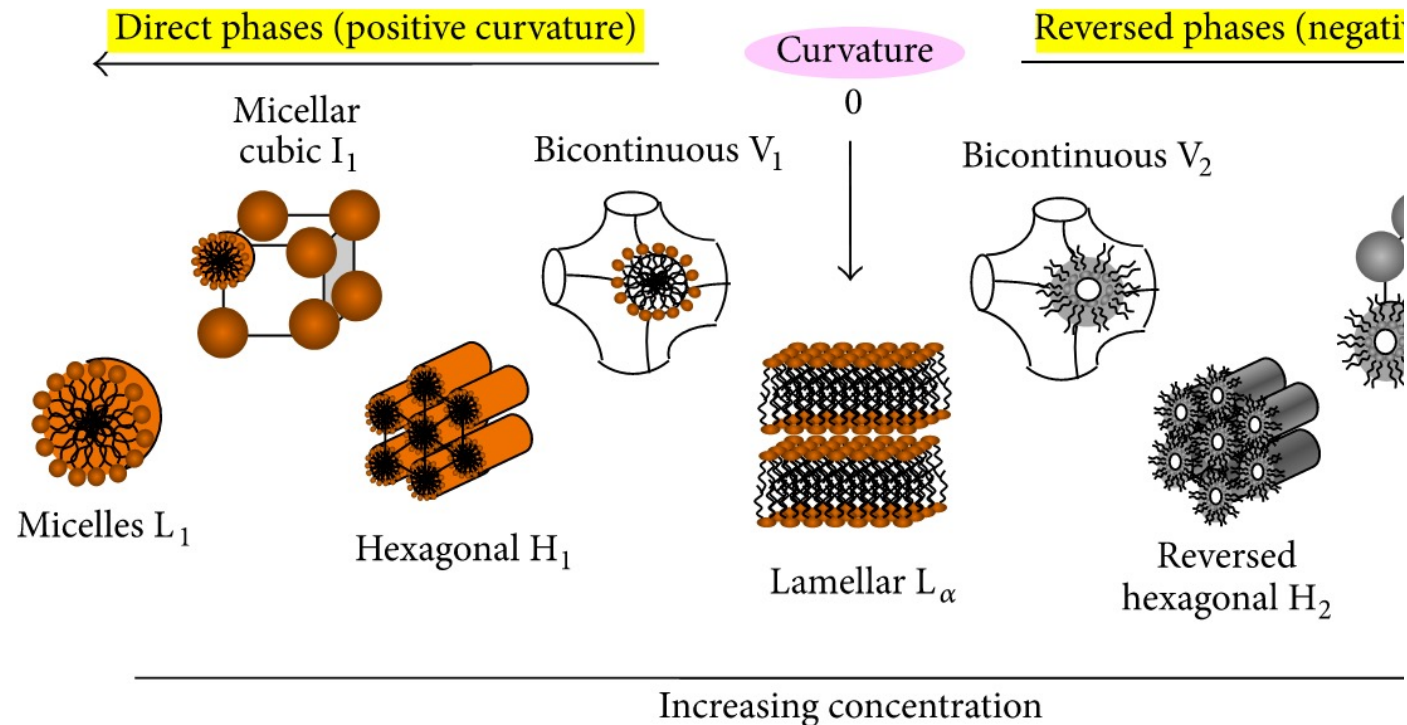
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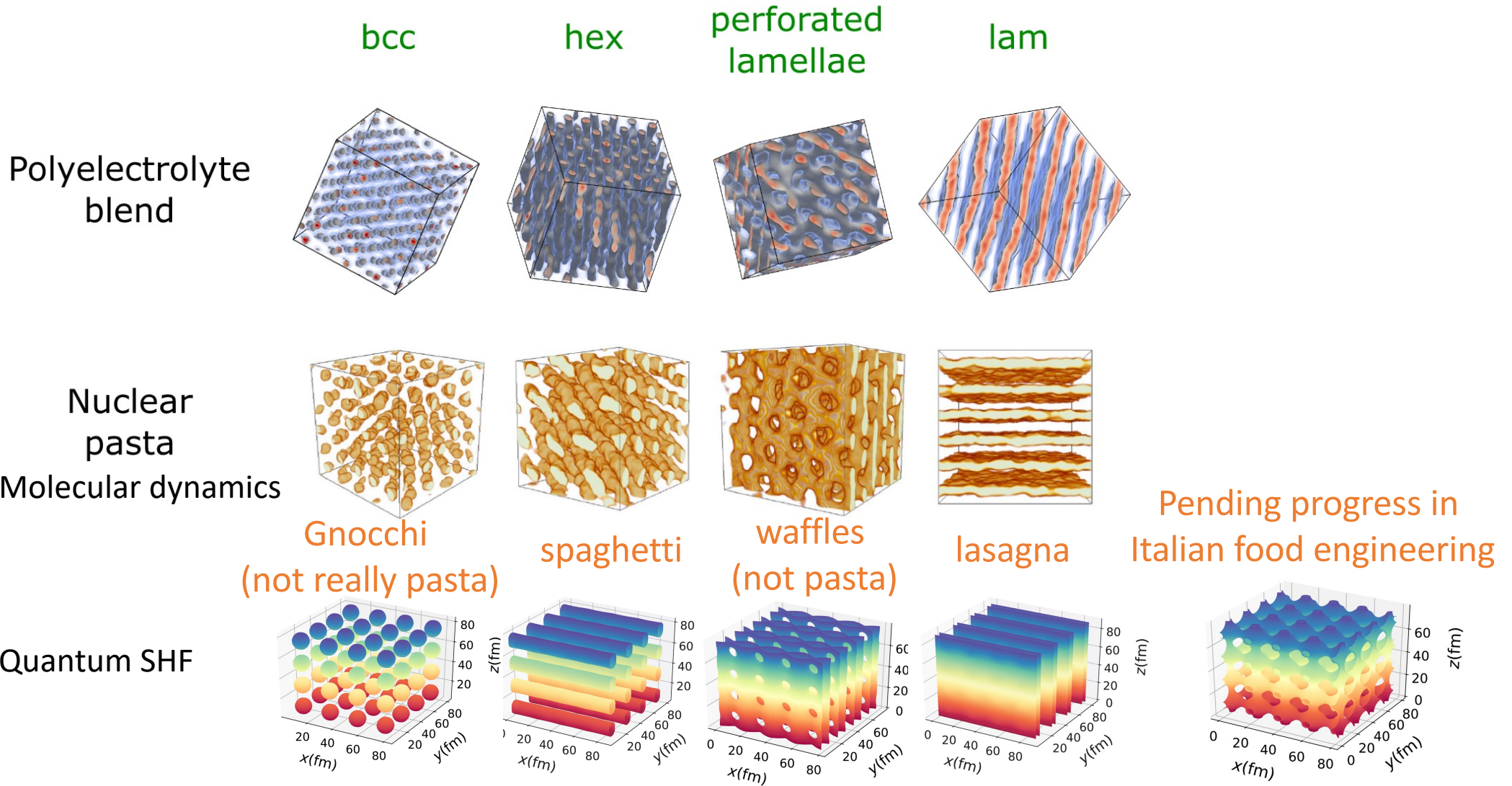
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# Driven by competition between short range attractive and long-range repulsive interactions - a generic feature of soft-condensed matter systems



Rumyantsev, dePablo: *Macromolecules* 53, 2020

Molecular dynamics simulations: Caplan, Horowitz, *Rev. Mod. Phys.* 89, 041002 (2017)

Quantum simulations: Newton et al, arxiv:2104.11835

## Nuclear Waffles

A. S. Schneider,<sup>1,\*</sup> D. K. Berry,<sup>2,†</sup> C. M. Briggs,<sup>1,‡</sup> M. E. Caplan,<sup>1,§</sup> and C. J. Horowitz<sup>1,¶</sup>

<sup>1</sup>*Department of Physics and Nuclear Theory Center,  
Indiana University, Bloomington, IN 47405, USA*

<sup>2</sup>*University Information Technology Services, Indiana University, Bloomington, IN 47408, USA*

(Dated: May 14, 2018)

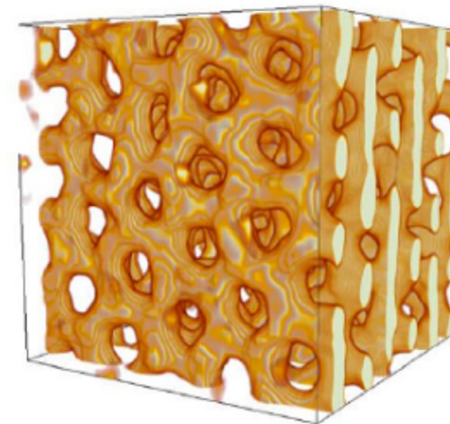
### Elastic properties of phases with nonspherical nuclei in dense matter

C. J. Pethick,<sup>1,2</sup> Zhaowen Zhang,<sup>1</sup> and D. N. Kobyakov<sup>3</sup>

<sup>1</sup>*The Niels Bohr International Academy, The Niels Bohr Institute,  
University of Copenhagen, Blegdamsvej 17, DK-2100 Copenhagen Ø, Denmark*

<sup>2</sup>*NORDITA, KTH Royal Institute of Technology and Stockholm University, Roslagstullsbacken 23, SE-106 91 Stockholm, Sweden*

<sup>3</sup>*Institute of Applied Physics of the Russian Academy of Sciences, 603950 Nizhny Novgorod, Russia*



<sup>3</sup> In Ref. [22] phases with spatially modulated plate-like elements are referred to as “waffles” but, to avoid proliferation of nomenclature, we shall refer to them as “lasagna”.

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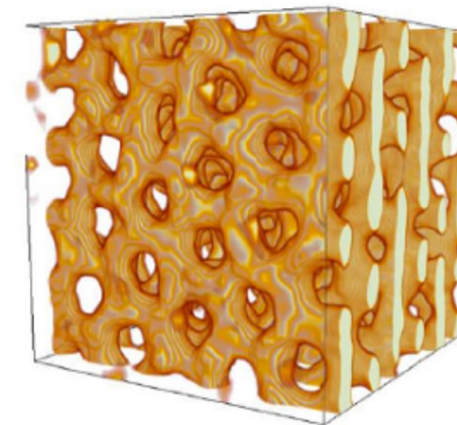
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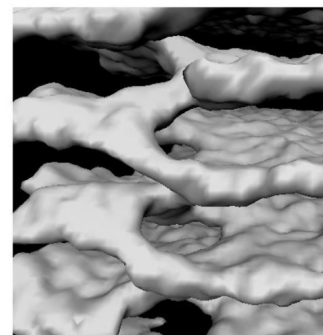
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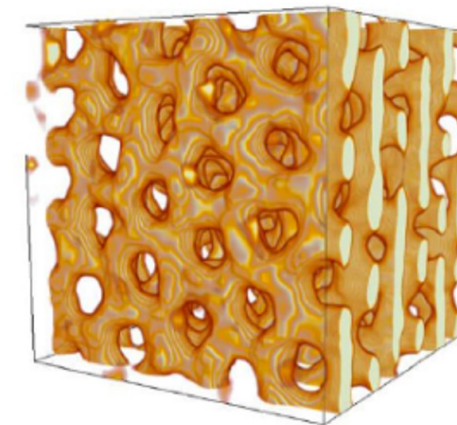
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### Parking-garage structures in astrophysics and biophysics

C. J. Horowitz,<sup>1,\*</sup> D. K. Berry,<sup>1,†</sup> M. E. Caplan,<sup>1,‡</sup> Greg Huber,<sup>2,§</sup> and A. S. Schneider



Horowitz et al, PRL.114.031102 (20



# NUCLEAR PASTA RECIPE: ANGEL HAIR WITH CARROTS

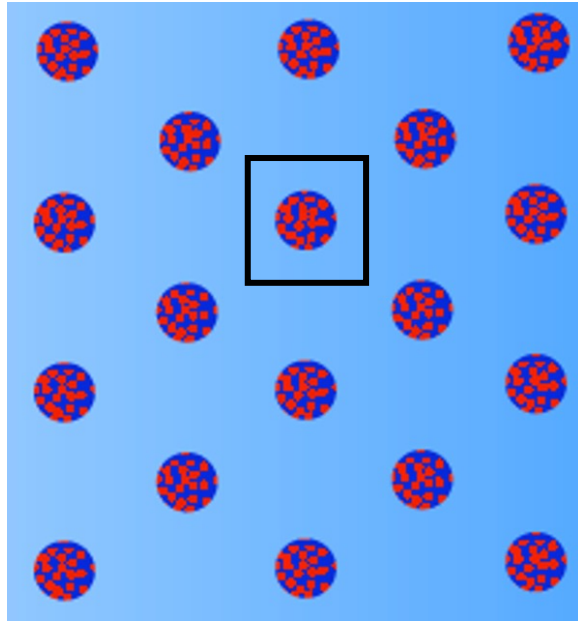


crammed into a 20km-wide sphere... Because of the immense gravity, the outer layers of neutron stars freeze solid to form a crust that surrounds a liquid core. Below the crust, protons and neutrons compete and end up forming long cylindrical shapes or flat planes. These have become known as 'spaghetti' and 'lasagna'—or nuclear pasta."

Given this exciting discovery, Barilla Executive Chef Lorenzo Boni decided to get creative and make his own version of nuclear pasta using Barilla Angel Hair, carrots, red bell peppers and Romano cheese. A few pieces of Barilla Collezione Orecchiette and some sprinkles of Barilla Pastina make the perfect garnish for the plate. Try it for dinner tonight—it's out of this world!

<https://www.barilla.com/en-us/posts/2018/10/22/nuclear-pasta-recipe-angel-hair-with-carrots>

# Modeling the crust with the Compressible liquid drop model



CLDM: Bulk fluid and surface degrees of freedom

$$\mathcal{H}_\delta + \mathcal{H}_\rho + \mathcal{H}_{\text{eff}} \quad \sigma(y_p)$$

Nuclear EDF: Bulk +  
separate surface energy function  
specific model: LLPR 1985

$$\sigma_s(y_p) = \sigma_0 \frac{2^{p+1} + b}{\frac{1}{y_p^p} + b + \frac{1}{(1-y_p)^p}}$$

Newton et al arxiv: 1110.4043

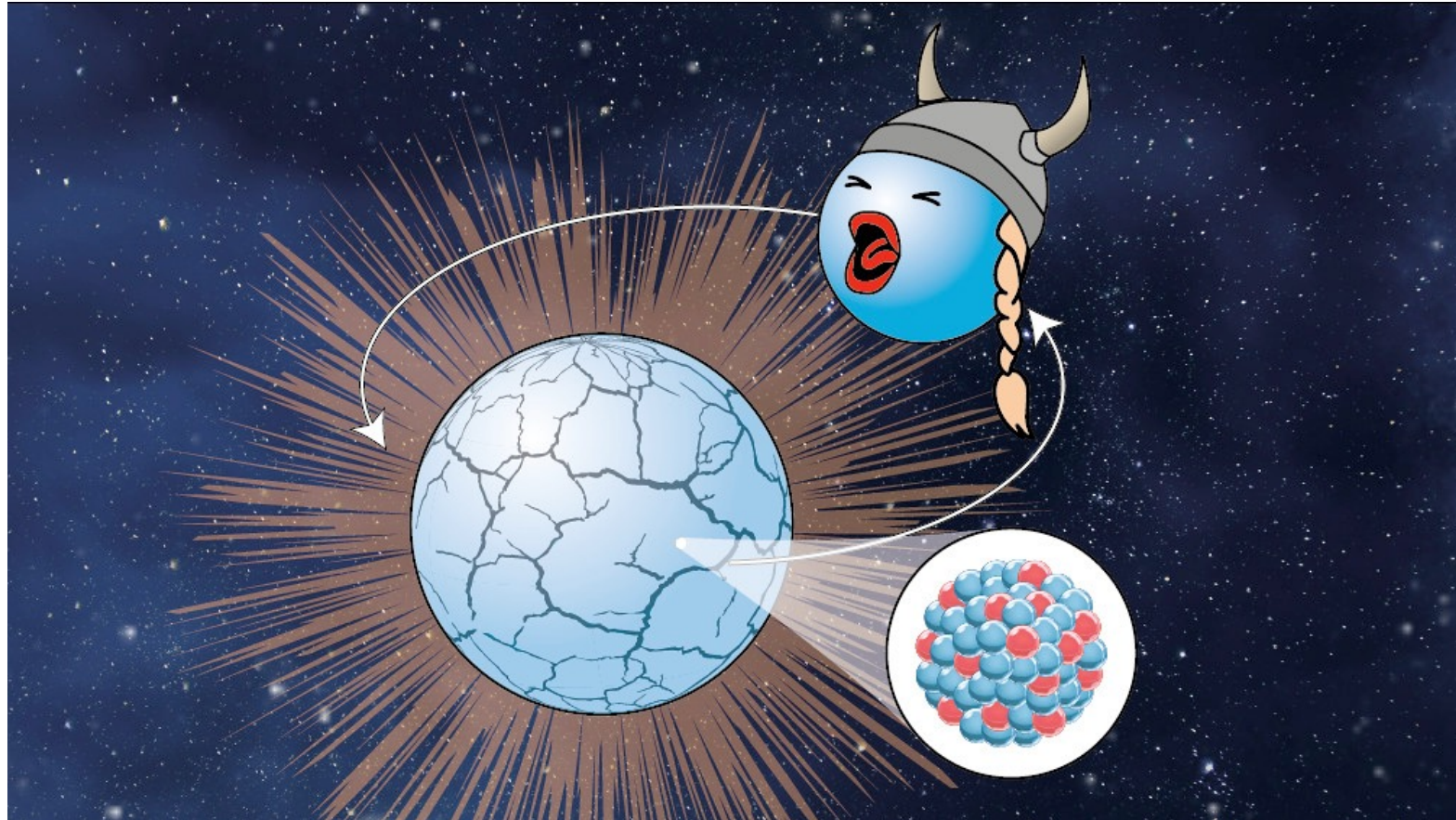
Balliet+; arxiv:2009.07696

# Application: resonant crust-shattering flares

Neill, Newton & Tsang, MNRAS 504, 2021

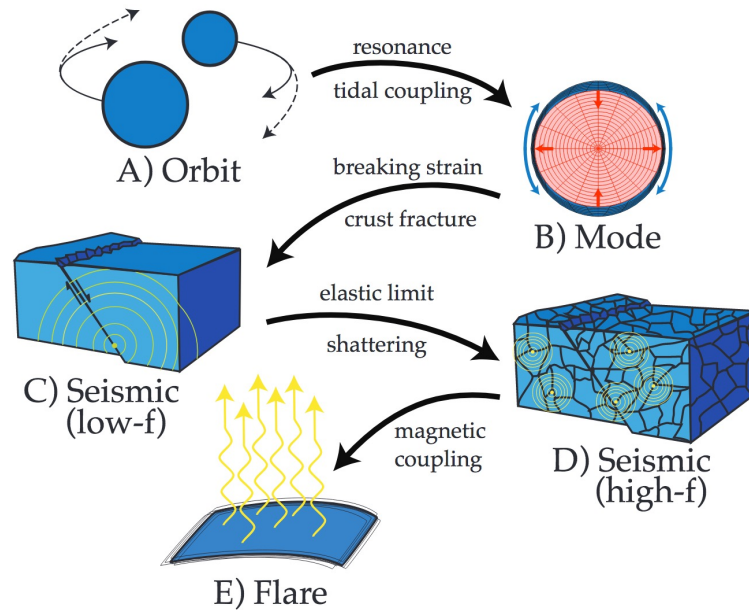
Neill, Preston, Newton, Tsang, PRL130, 2022

Neill, Tsang, Newton, MNRAS 532, 1, 827



Picture: David Tsang

The elastic crust can be made to resonantly vibrate by the tidal field of its companion – something we can potentially measure!

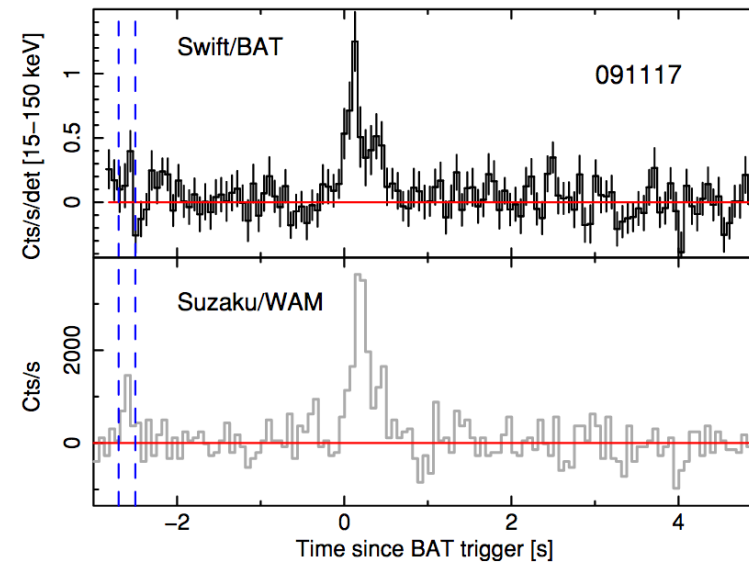
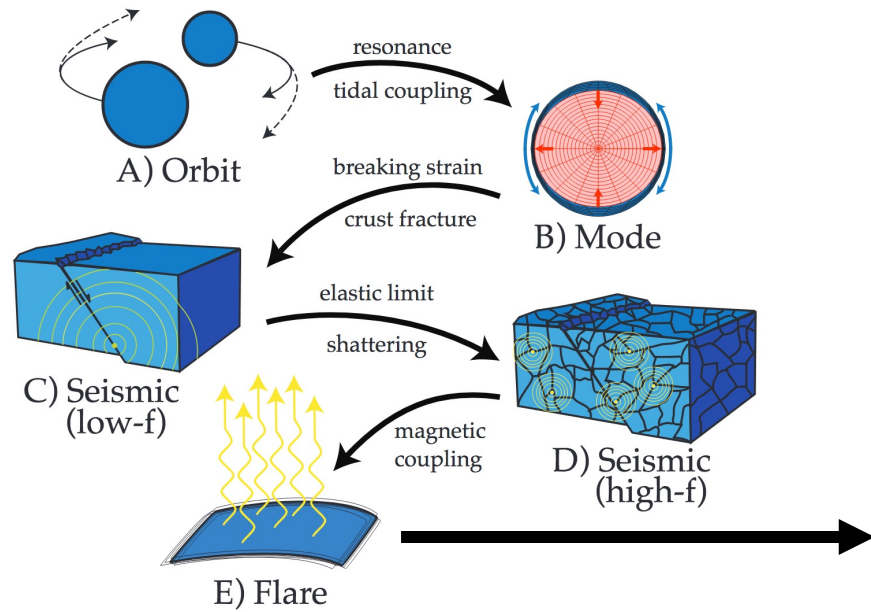


D.Tsang, Apj 777, 2013

Neill, Newton & Tsang, MNRAS 504, 2021

Neill, Preston, Newton, Tsang, PRL130, 2022

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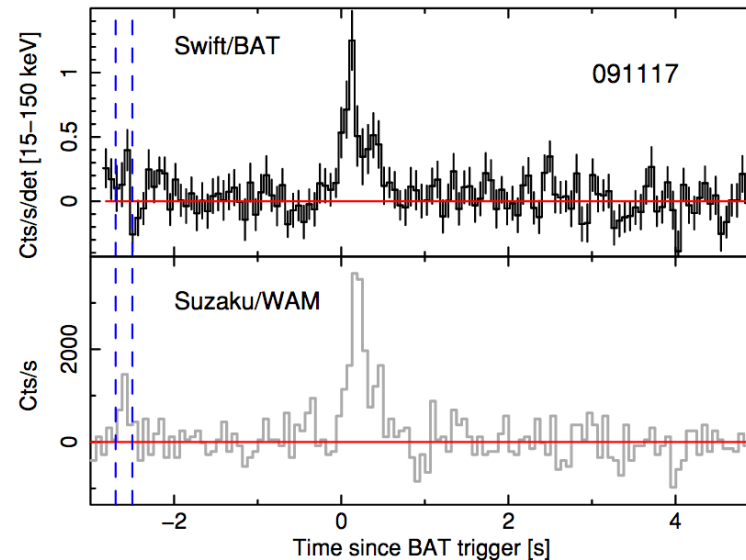
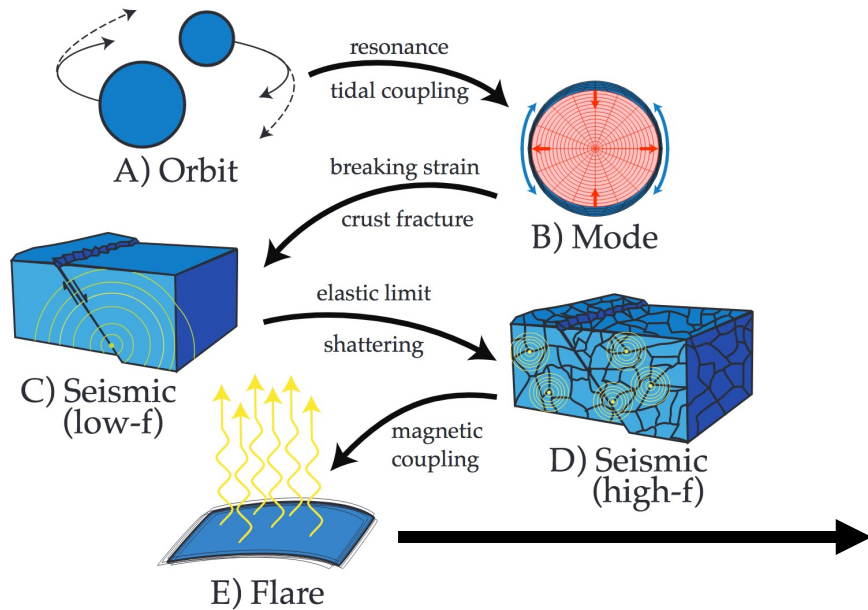
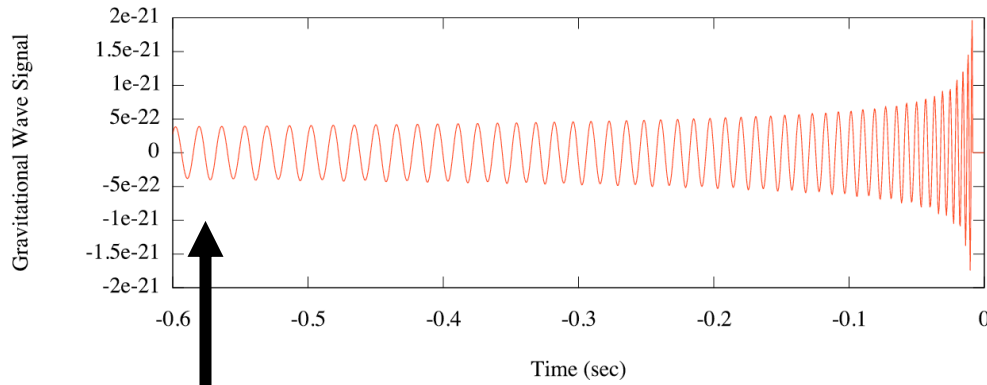


D.Tsang, Apj 777, 2013  
 Neill, Newton & Tsang, MNRAS 504, 2021  
 Neill, Preston, Newton, Tsang, PRL130, 2022

Troja, Rosswog, Gehrels, ApJ723, 2010

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Example Inspiral Gravitational Waves



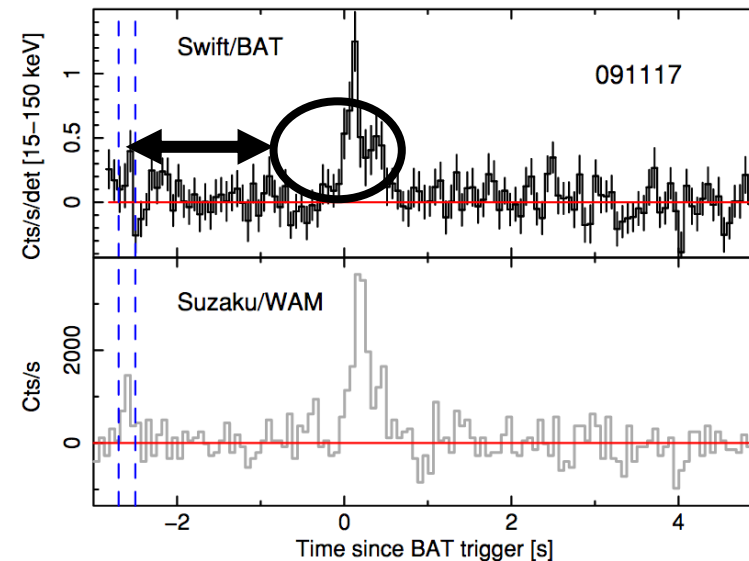
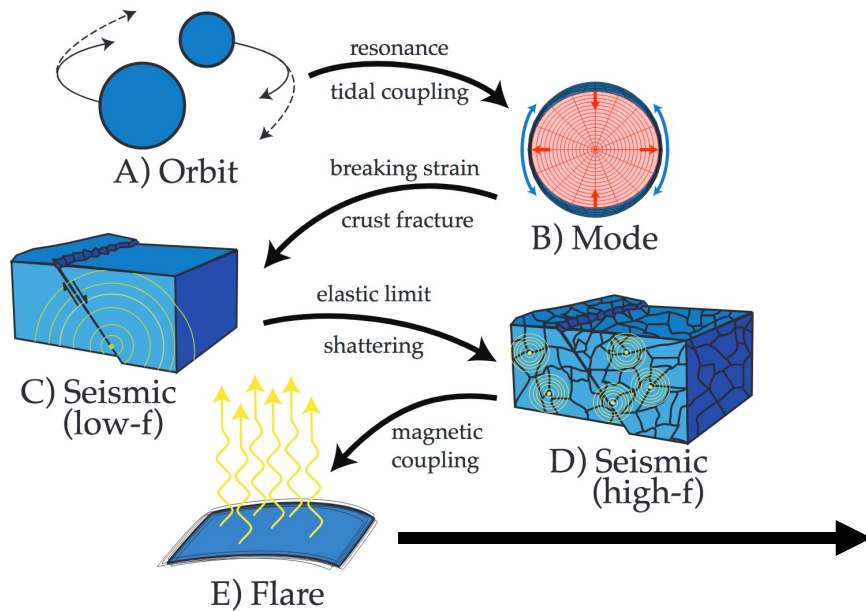
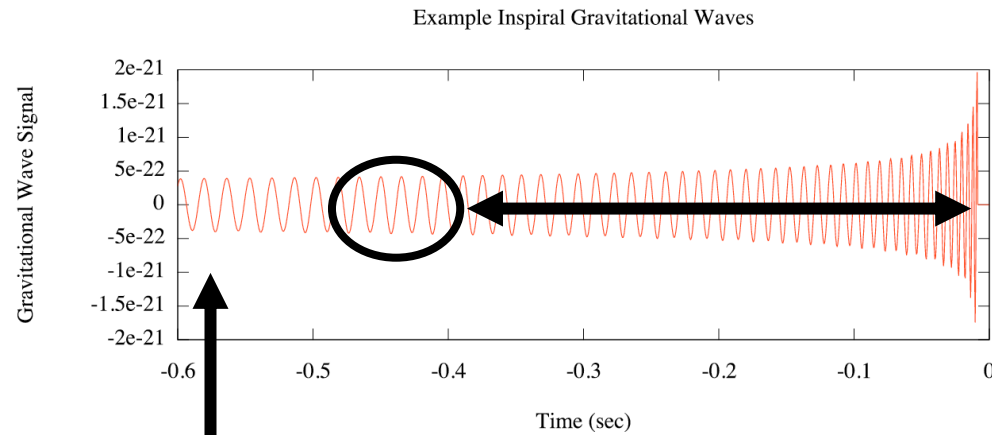
Troja, Rosswog, Gehrels, ApJ723, 2010

D.Tsang, Apj 777, 2013

Neill, Newton & Tsang, MNRAS 504, 2021

Neill, Preston, Newton, Tsang, PRL130, 2022

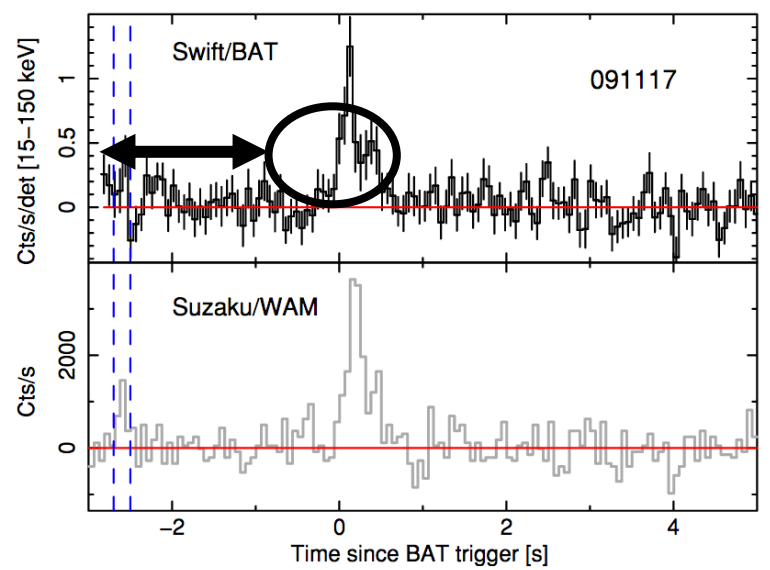
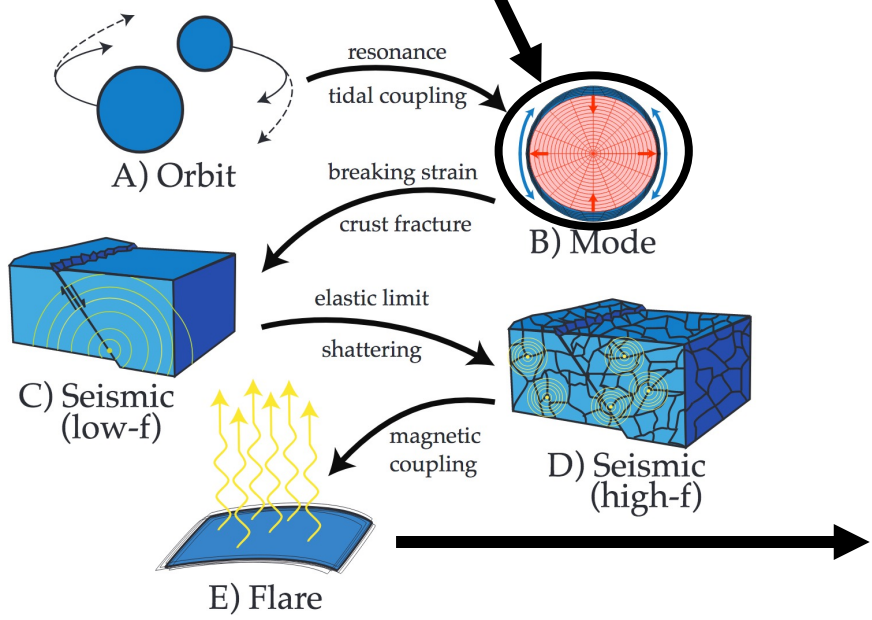
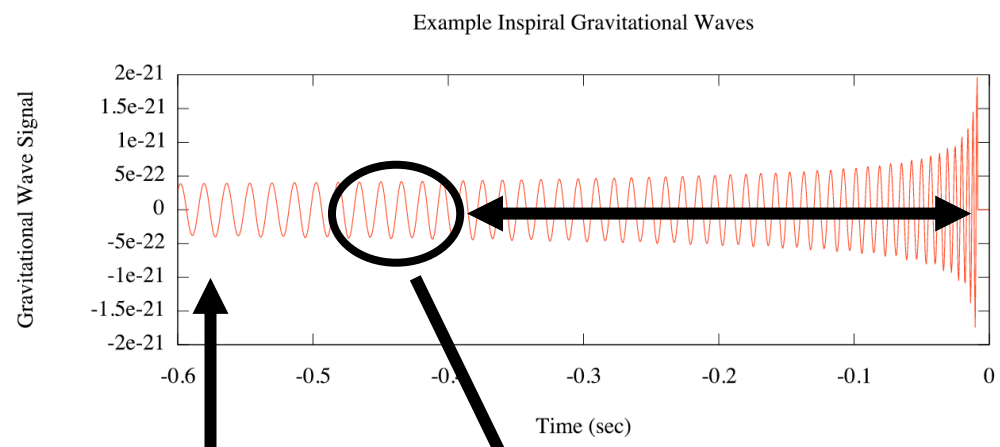
The elastic crust can be made to resonantly vibrate by the tidal field of its companion – something we can potentially measure!



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 Neill, Newton & Tsang, MNRAS 504, 2021  
 Neill, Preston, Newton, Tsang, PRL130, 2022

Troja, Rosswog, Gehrels, ApJ723, 2010

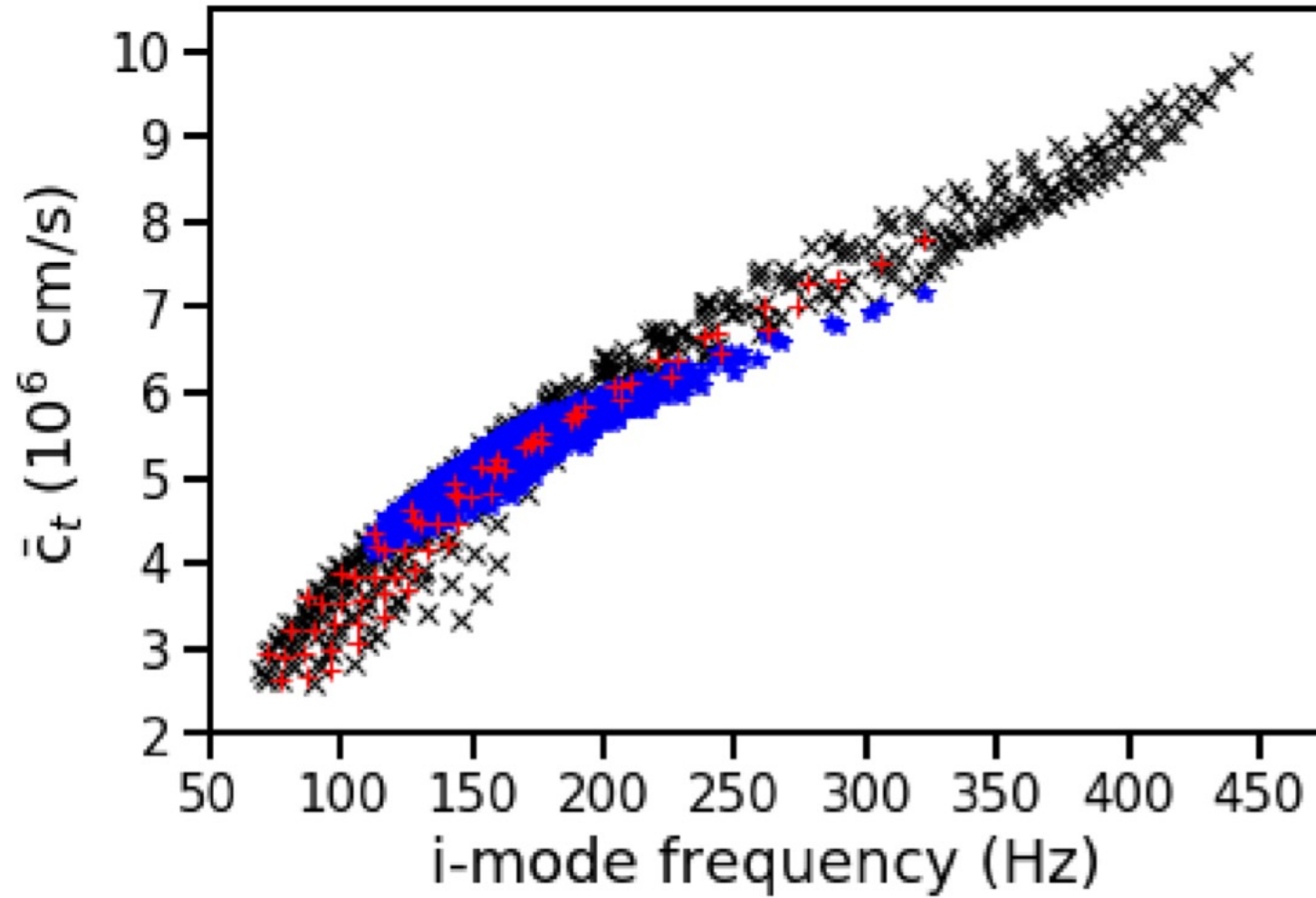
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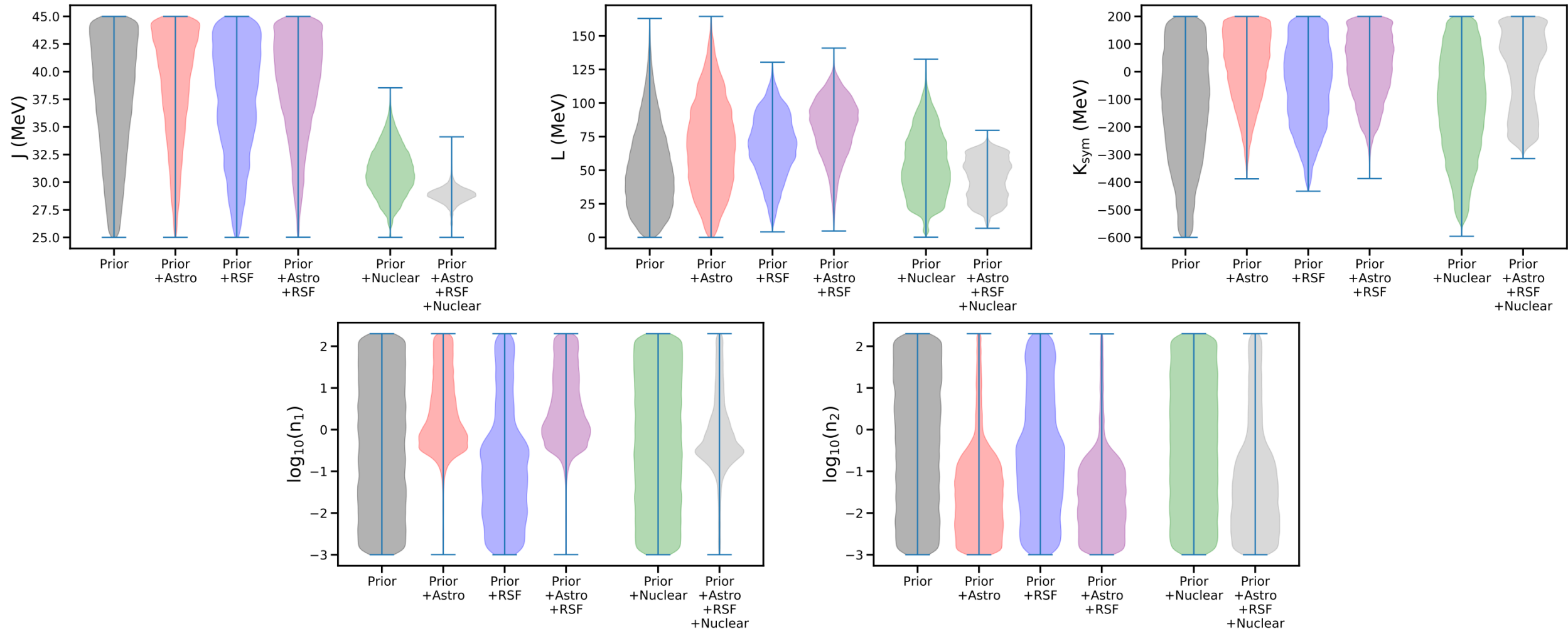
Troja, Rosswog, Gehrels, ApJ723, 2010

Strong correlation between shear speed and *i*-mode frequency



Neill, Newton & Tsang, MNRAS 504, 2021

# Inference using a synthetic detection of an RSF at a frequency of 250 Hz, comparison with Nicer-Ligo and nuclear binding energy data



- $J$  not constrained by astro
- $L$  constrained by nuclear, RSF
- $K_{\text{sym}}$  constrained by RSF/NL
- Polytrope parameters constrained by NL

# Take-aways:

- Many nuclear physics observables have a say on the behavior of the EOS in the crust up to  $2n_{\text{sat}}$
- Communities need to communicate!
- Many systematic errors, good news: some of them aren't *terribly* hard to address
- And we need to address them before next gen experiments/observatories
- Inconsistent neutron star crust!
  - Systematic error in radius up to 0.5km
  - Bring crust observables into play
- $L$ ,  $K_{\text{sym}}$  are sensitive to astrophysical observables from crust to core, even when inner core non-nucleonic
- During a neutron star merger, the stars may resonantly excite each other's solid crust to shattering
- We can harness multi-messenger observations to test this and potentially measure the material properties of neutron star crusts

