

MPA Summer School 2025
Thomas Becher, University of Bern

Precision Physics at Current and Future Colliders



Statistical Precision

How many Z - bosons did the LHC produce so far?

Cross section at 13 TeV

$$\sigma(pp \rightarrow Z + X) \approx 60 \text{ nb}$$

Integrated luminosity

$$L_{\text{int}} \approx 300 \text{ fb}^{-1}$$

Branching ratio to $\ell = e, \mu$

$$\text{Br}(Z \rightarrow \ell^+ \ell^-) = 3.36 \%$$

Statistical Precision

How many Z - bosons did the LHC produce so far?

Cross section at 13 TeV

$$\sigma(pp \rightarrow Z + X) \approx 60 \text{ nb}$$

Integrated luminosity

$$L_{\text{int}} \approx 300 \text{ fb}^{-1}$$

Branching ratio to $\ell = e, \mu$

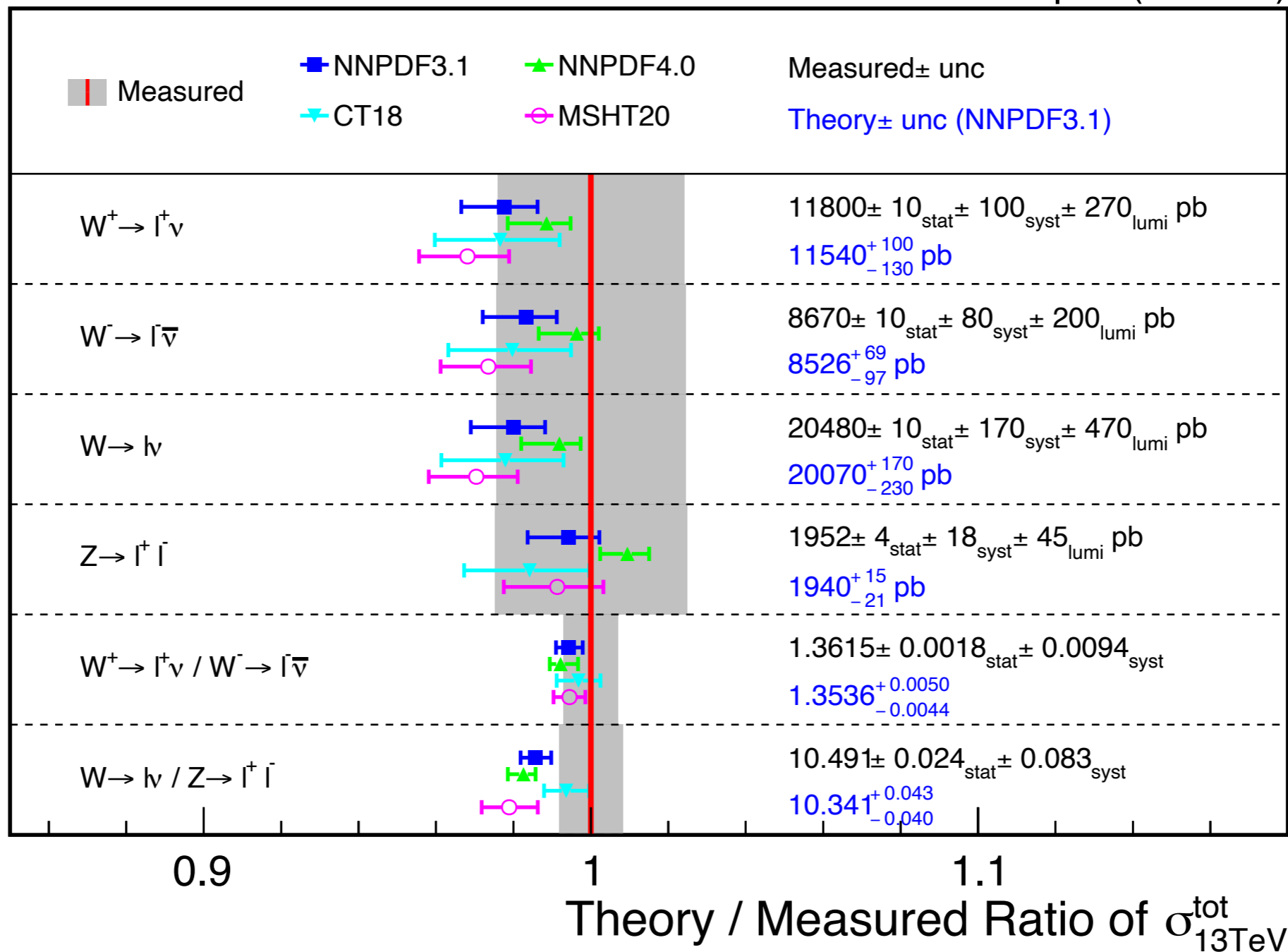
$$\text{Br}(Z \rightarrow \ell^+ \ell^-) = 3.36 \%$$

Amounts to

$\sim 10^9$ lepton pairs from Z decays!

CMS

206 pb⁻¹ (13 TeV)



NNLO Theory uncertainty: scale variation, PDFs, α_s

fcc-ee

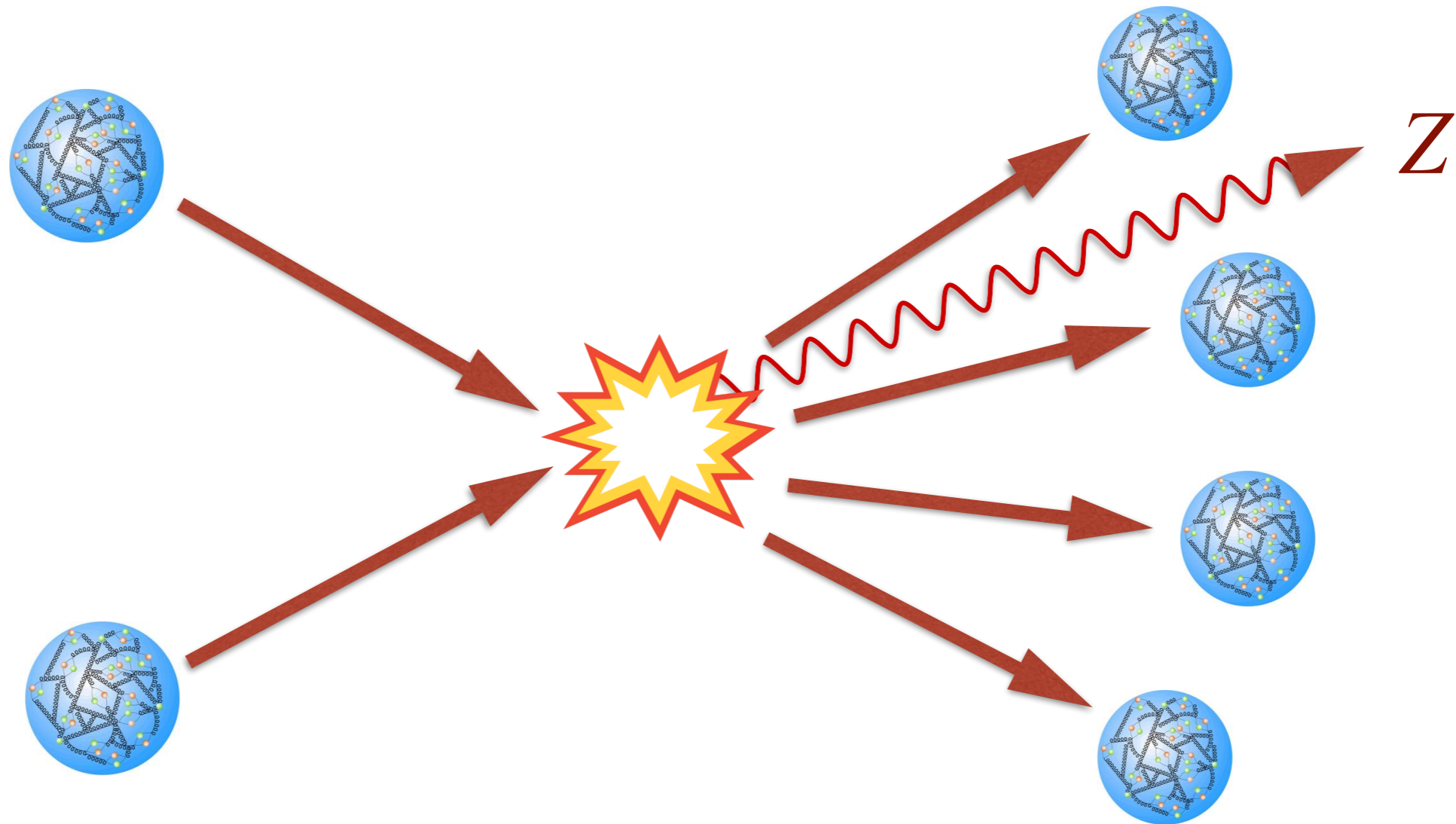
When the fcc-ee will run at the Z -resonance, it should produce

6×10^{12} Z -bosons

one LEP sample every few minutes!

Incredible statistical accuracy (factor 500 smaller stat. uncertainties than LEP!) in a very clean environment!

Huge opportunity and enormous challenge to theoretical predictions!



The LHC collides very energetic **hadrons**, complicated **relativistic bound states of quarks and gluons**, which scatter into a huge number of hadrons + EW particles.



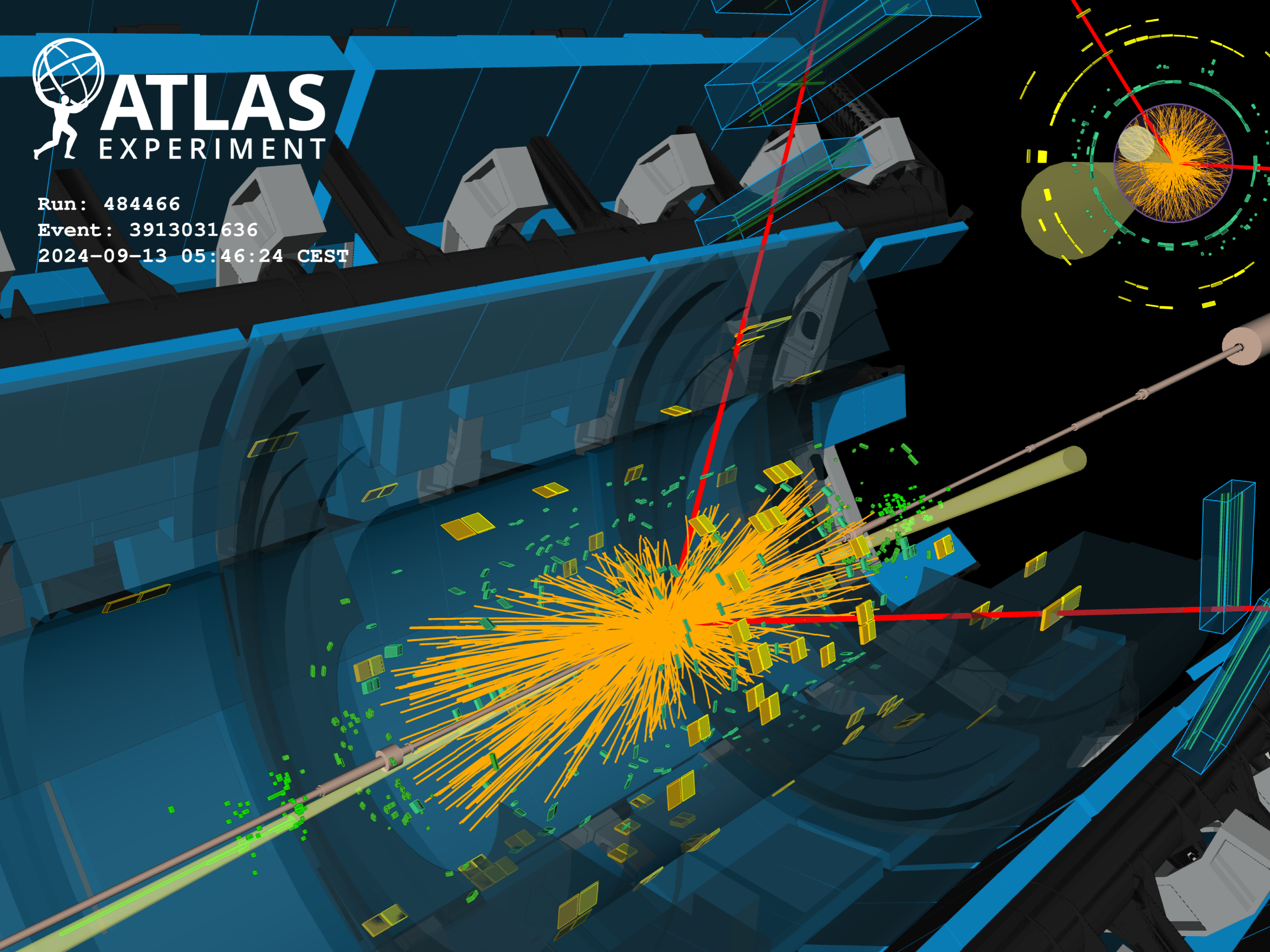
ATLAS

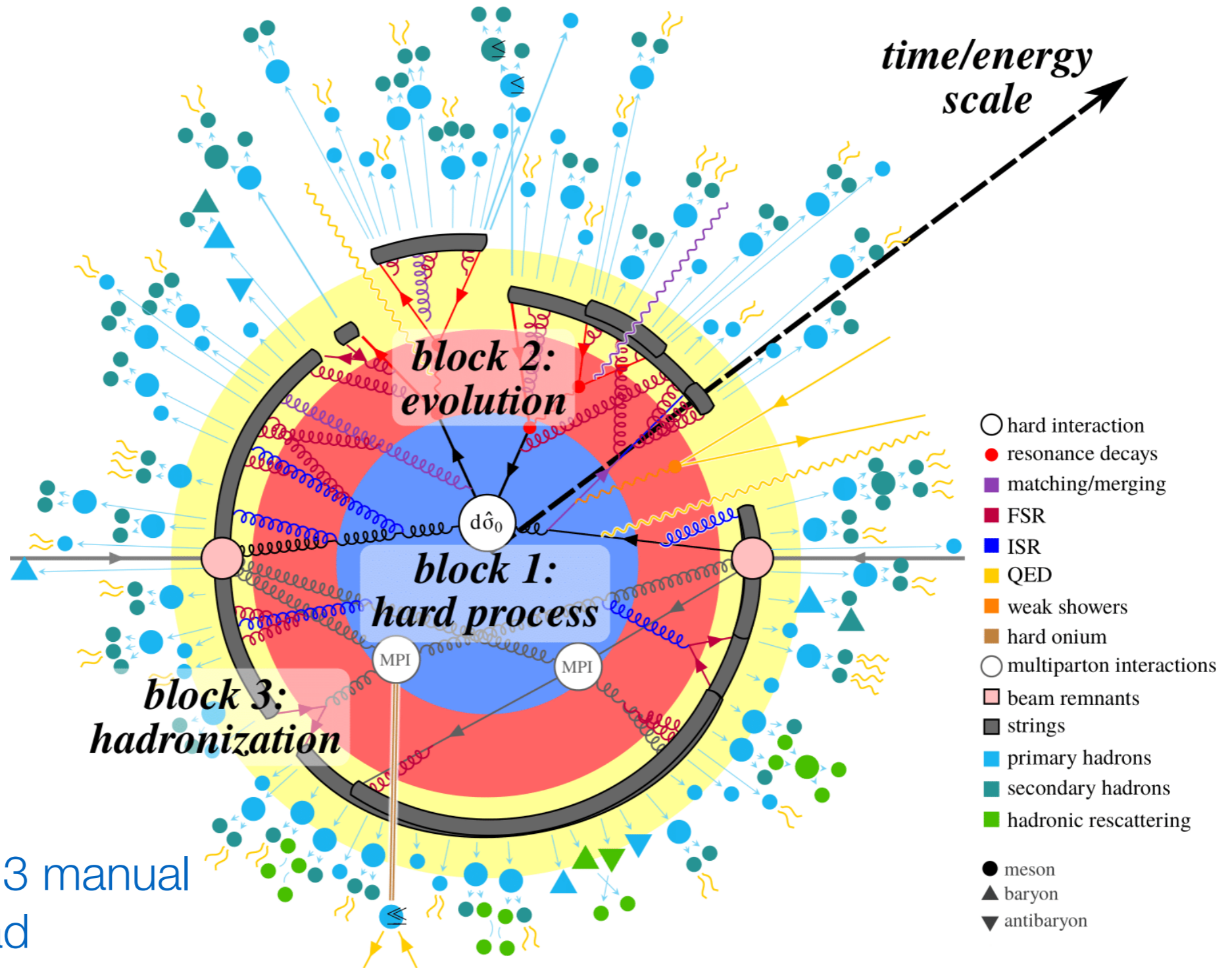
EXPERIMENT

Run : 484466

Event : 3913031636

2024-09-13 05:46:24 CEST





from Pythia 8.3 manual
MLHad

Theoretical predictions are obviously very challenging, mainly due to **QCD (strong interaction)** effects!

Standard Model Production Cross Section Measurements

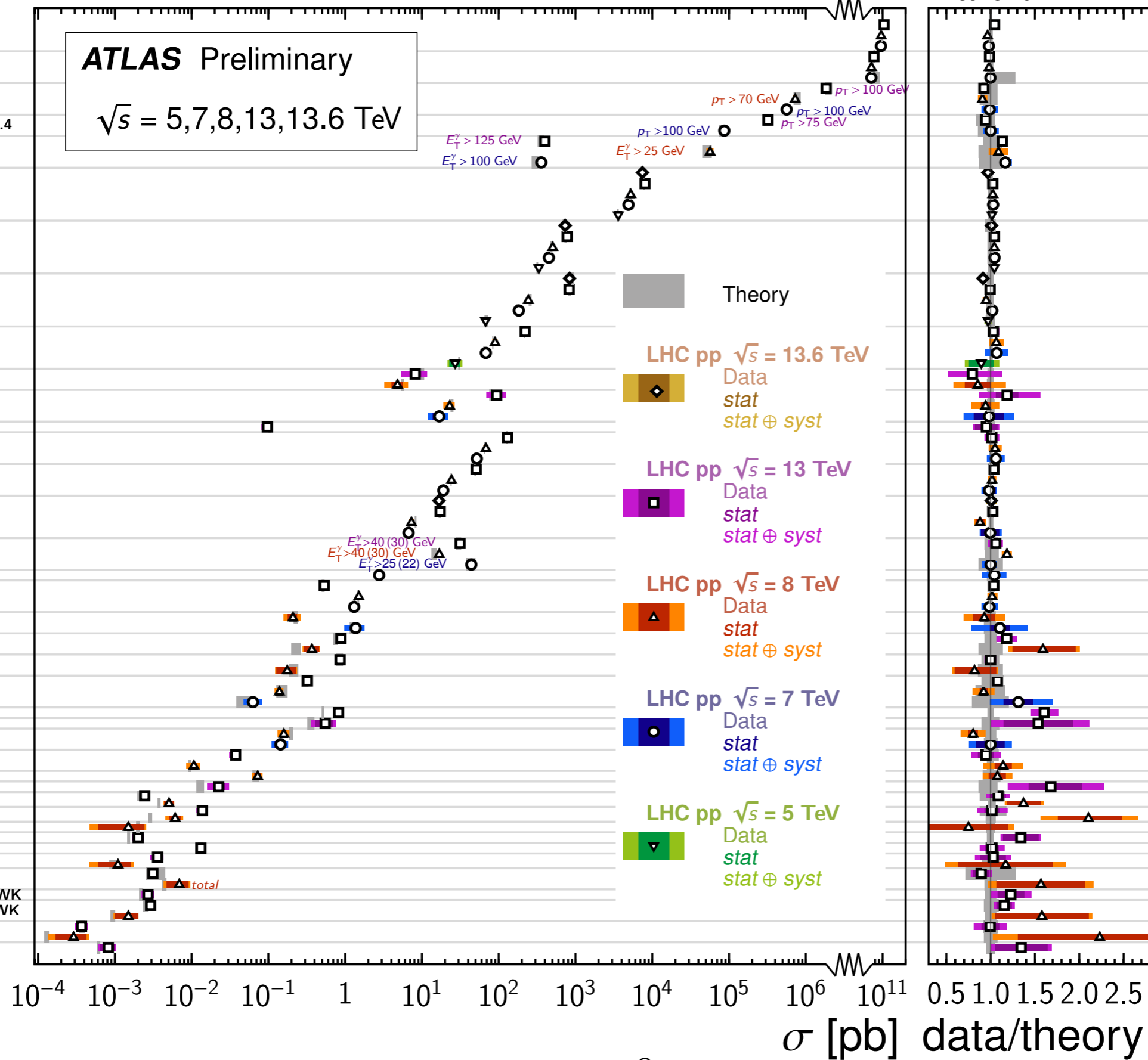
Status:
June 2024

$\int \mathcal{L} dt$
[fb⁻¹]

Reference

- pp
- pp inelastic
- Jets R=0.4
- Dijets R=0.4
- γ
- W
- Z
- $t\bar{t}$
- $t\bar{t}$ -chan
- $\bar{t}s$ -chan
- Wt
- tZj
- WW
- WZ
- ZZ
- $\gamma\gamma$
- W γ
- Z γ
- WV
- $t\bar{t}W$
- $t\bar{t}Z$
- $t\bar{t}\gamma$
- WWW
- WWZ
- Wjj EWK
- Zjj EWK
- $\gamma\gamma\gamma$
- ttt
- Z $\gamma\gamma$
- W $\gamma\gamma$
- WW γ
- WZ γ
- W γ jj EWK
- Z γ jj EWK
- $\gamma\gamma \rightarrow WW$
- W⁺W⁻jj EWK
- W[±]W[±]jj EWK
- WZjj EWK
- ZZjj EWK

ATLAS Preliminary
 $\sqrt{s} = 5, 7, 8, 13, 13.6$ TeV



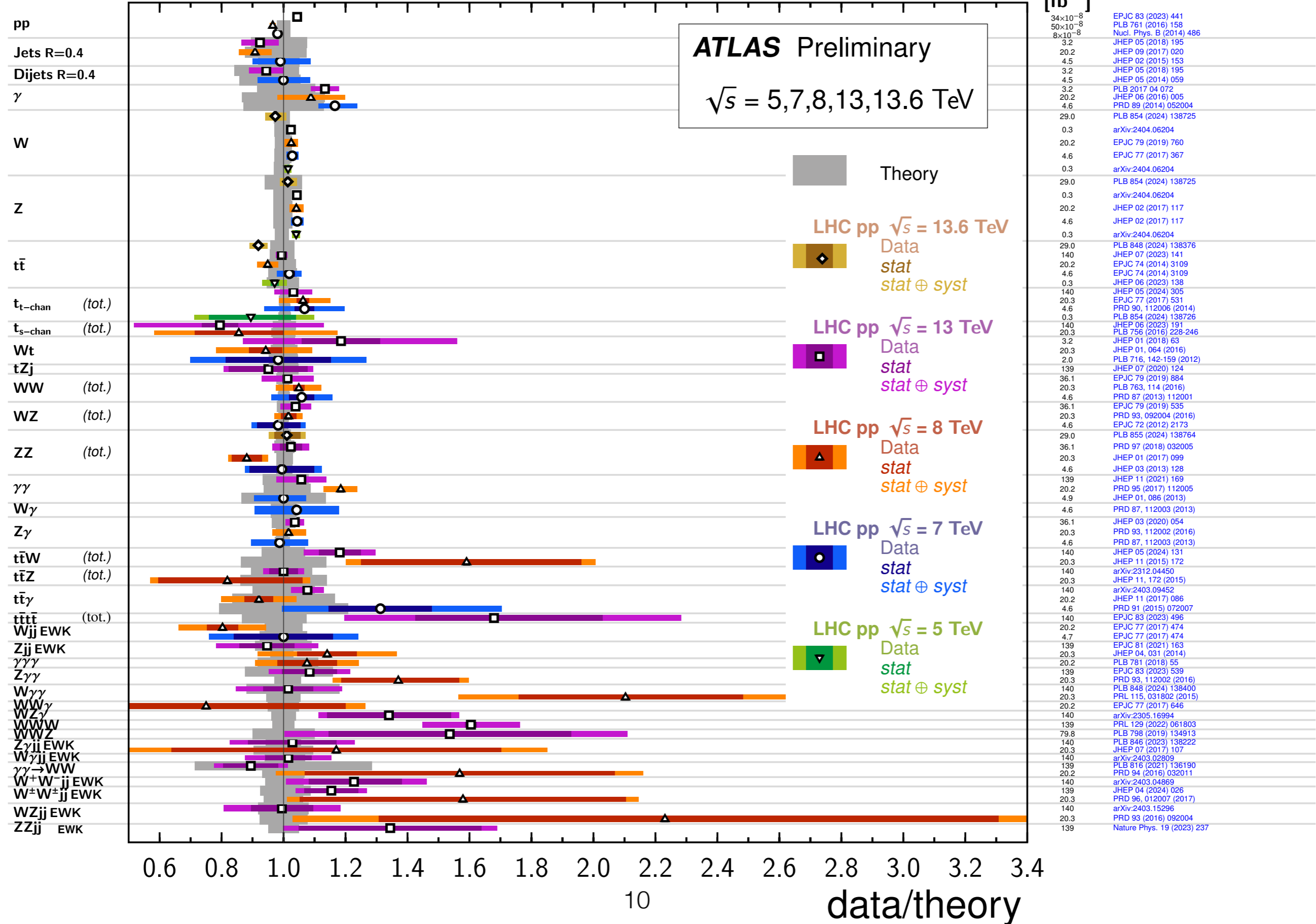
- EPJC 83 (2023) 441
- PLB 761 (2016) 158
- Nucl. Phys. B (2014) 486
- EPJC 83 (2023) 441
- PLB 761 (2016) 158
- Nucl. Phys. B (2014) 486
- JHEP 05 (2018) 195
- JHEP 09 (2017) 020
- JHEP 02 (2015) 153
- JHEP 05 (2018) 195
- JHEP 05 (2014) 059
- PLB 2017 04 072
- JHEP 06 (2016) 005
- PRD 89 (2014) 052004
- PLB 854 (2024) 138725
- arXiv:2404.06204
- EPJC 79 (2019) 760
- EPJC 77 (2017) 367
- arXiv:2404.06204
- PLB 854 (2024) 138725
- arXiv:2404.06204
- JHEP 02 (2017) 117
- JHEP 02 (2017) 117
- arXiv:2404.06204
- PLB 848 (2024) 138376
- JHEP 07 (2023) 141
- EPJC 74 (2014) 3109
- EPJC 74 (2014) 3109
- JHEP 06 (2023) 138
- JHEP 05 (2024) 305
- EPJC 77 (2017) 531
- PRD 90, 112006 (2014)
- PLB 854 (2024) 138726
- JHEP 06 (2023) 191
- PLB 756 (2016) 228-246
- JHEP 01 (2018) 63
- JHEP 01, 064 (2016)
- PLB 716, 142-159 (2012)
- JHEP 07 (2020) 124
- EPJC 79 (2019) 884
- PLB 763, 114 (2016)
- PRD 87 (2013) 112001
- EPJC 79 (2019) 535
- PRD 93, 092004 (2016)
- EPJC 72 (2012) 2173
- PLB 855 (2024) 138764
- PRD 97 (2018) 032005
- JHEP 01 (2017) 099
- JHEP 03 (2013) 128
- JHEP 11 (2021) 169
- PRD 95 (2017) 112005
- JHEP 01, 086 (2013)
- PRD 87, 112003 (2013)
- JHEP 03 (2020) 054
- PRD 93, 112002 (2016)
- PRD 87, 112003 (2013)
- EPJC 77 (2017) 563
- JHEP 01 (2015) 049
- JHEP 05 (2024) 131
- JHEP 11 (2015) 172
- arXiv:2312.04450
- JHEP 11, 172 (2015)
- arXiv:2403.09452
- JHEP 11 (2017) 086
- PRD 91 (2015) 072007
- PRL 129 (2022) 061803
- PLB 798 (2019) 134913
- EPJC 77 (2017) 474
- EPJC 77 (2017) 474
- EPJC 81 (2021) 163
- JHEP 04, 031 (2014)
- PLB 781 (2018) 55
- EPJC 83 (2023) 496
- EPJC 83 (2023) 539
- PRD 93, 112002 (2016)
- PLB 846 (2023) 138222
- PRL 115, 031802 (2015)
- EPJC 77 (2017) 646
- arXiv:2305.16994
- arXiv:2403.02809
- PLB 846 (2023) 138222
- JHEP 07 (2017) 107
- PLB 816 (2021) 136190
- PRD 94 (2016) 032011
- arXiv:2403.04869
- JHEP 04 (2024) 026
- PRD 96, 012007 (2017)
- arXiv:2403.15296
- PRD 93 (2016) 092004
- Nature Phys. 19 (2023) 237

Standard Model Production Cross Section Measurements

Status:
June 2024

$\int \mathcal{L} dt$
[fb⁻¹]

Reference



Despite these challenges, some observables at the LHC can be precisely predicted (and measured!).

Key ingredients

- **Factorization** and **asymptotic freedom**. Short-distance QCD effects can be computed in perturbation theory
- **Infrared safety**: sufficiently inclusive observables are insensitive to long-distance hadronization effects.
- Modeling: **parton shower Monte Carlo** event generators do a great job at simulating realistic events, including hadronization.

Outline of the lectures

1. (Non-)perturbative QCD

- Feynman rules and perturbation theory
- Asymptotic freedom
- R -ratio and hadronization effects
- Higher-order corrections and IR divergences

2. - 4. Hadronic collisions (Maria Ubiali)

- Factorization of hadron-collider cross sections
- Parton Distribution functions
- DIS and Drell Yan process

Outline (...)

5. IR safe observables

- IR safety
- Event shapes, jets, EECs
- Soft and collinear factorization, SCET
- Resummation

6. Fixed-order results and parton showers

- Monte Carlo techniques
- Fixed-order results up to N³LO
- Parton showers
- Modeling (Recoil, UE, hadronization, ...)

*It is better to uncover a little
than to cover a lot.*

Victor Weisskopf

Please stop me at any point during
the lectures if you have questions!

QFT textbooks

- An Introduction to Quantum Field Theory, G. Serman '93
- An Introduction to Quantum Field Theory, M. Peskin and D. Schroeder '95
- Quantum Field Theory and Standard Model, M. Schwartz '13
- ...

Collider QCD

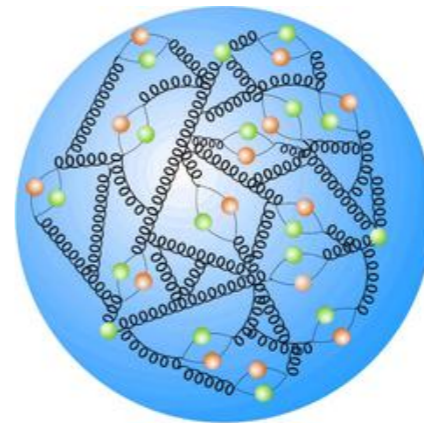
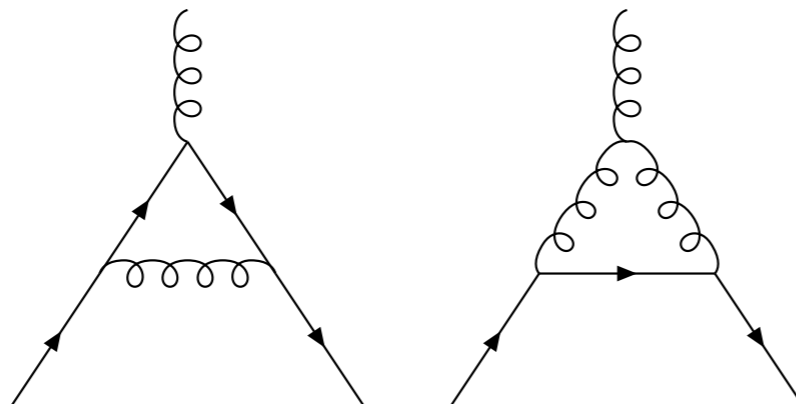
- QCD and Collider Physics, R. K. Ellis, W. J. Stirling, B. R. Webber '96
- The Black Book of Quantum Chromodynamics, J. Campbell, J. Huston, F. Krauss '17
- Quantum Chromodynamics, Huston, Rabbertz, Zanderighi, review by the Particle Data Group '25

Special topics

- Pythia 6.4 Physics and Manual, [Sjostrand](#), [Mrenna](#), [Skands '06](#) + manuals for later versions
- Towards Jetography, [G. Salam '09](#)
- Introduction to Soft-Collinear Effective Theory, [T. Becher](#) , [A. Broggio](#) , [A. Ferroglia '15](#)
- Jet Substructure at the LHC: A Review of Recent Advances in Theory and Machine Learning, [A. Larkoski](#), [I. Mout](#), [B. Nachman '17](#)
- Energy Correlators: A Journey From Theory to Experiment, [I. Mout](#) and [H.X. Zhu '25](#)

Part I

(Non-)perturbative QCD



- Lagrangian and Feynman rules
- Feynman rules and perturbation theory
- Asymptotic freedom
- R -ratio and hadronization effects

Gauge invariance

Quark fields in QCD are invariant under

$$\psi(x) = \begin{pmatrix} \psi_1(x) \\ \psi_2(x) \\ \psi_3(x) \end{pmatrix} \rightarrow \psi'(x) = \mathbf{V}(x) \psi(x)$$

$N_c = 3$ "colors" of quarks

with local transformation

$$\mathbf{V}(x) = e^{i \omega^a(x) \mathbf{T}^a} \in SU(3)$$

group generators, 3×3 matrices

repeated indices summed!
sum over $a = 1, \dots, 8$

QCD Lagrangian

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu}^a F^{a\mu\nu} + \sum_q \bar{\psi}_q \left(\gamma^\mu i \mathbf{D}_\mu - m_q \mathbf{1} \right) \psi_q$$

with

$$F_{\mu\nu}^a = \partial_\mu A_\nu^a - \partial_\nu A_\mu^a + g f^{abc} A_\mu^b A_\nu^c$$

$$i \mathbf{D}_\mu = i \partial_\mu \mathbf{1} + g \mathbf{T}^a A_\mu^a$$

8 gluon fields A_μ^a with $a = 1 \dots 8$.

Structure constants $[\mathbf{T}^a, \mathbf{T}^b] \equiv i f^{abc} \mathbf{T}^c$

Side-remarks: θ -term

Lagrangian on previous slide contains all terms up to operator dimension $d = 4$, with one exception

$$\mathcal{L}_\theta = \theta \frac{g_s^2}{64\pi^2} \epsilon^{\mu\nu\rho\sigma} F_{\mu\nu}^a F_{\rho\sigma}^a = \theta \frac{g_s^2}{32\pi^2} F_{\mu\nu}^a \tilde{F}^{\mu\nu a}$$

where $\epsilon^{\mu\nu\rho\sigma}$ is the totally antisymmetric tensor and θ is a free parameter. This term

- is a total derivative, not visible in PT
- violates P, T, CP

In QCD, term would induce e.g. an electric dipole moment neutron. Experimentally $\theta < 10^{-10}$.

Side-remarks: $d > 4$ terms

Can write down gauge invariant terms with higher dimension, for example [$\mathbf{F}_{\mu\nu} = F_{\mu\nu}^a \mathbf{t}^a$]

$$\Delta \mathcal{L} = \frac{1}{\Lambda^2} \text{tr} \left(\mathbf{F}_{\nu}^{\mu} \mathbf{F}_{\rho}^{\nu} \mathbf{F}_{\mu}^{\rho} \right) \quad (d = 6)$$

Higher-dimensional operators are suppressed by powers of scale Λ

- New heavy particles with masses $M \sim \Lambda$ induce such operators at low energies through virtual effects
- Precision measurements probe such operators!
- Systematic framework: SMEFT (see Ulrich's lecture)

Side-remarks: Gauge fixing

Due to the gauge symmetry many field configurations are equivalent. Drop out when computing expectation values, but cause problems in path integral

$$Z = \int \mathcal{D}\mathbf{A}_\mu \exp\left(iS[\mathbf{A}_\mu]\right)$$

Solution by [Faddeev-Popov '67](#) is to factor out integration over gauge-related configurations, leaving behind a gauge-fixed action.

Gauge fixing introduces extra terms into the action and auxiliary “ghost” fields. Depending on gauge fixing, ghost fields enter higher-order computations.

Ghost fields will not be needed for this lecture, see QFT textbooks for more information.

Gauge interactions

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + i\bar{\psi} \not{D} \psi$$

$$+ \sum_i \psi_i^\dagger y_{ij} \psi_j \phi + \text{h.c.} + |D_\mu \phi|^2 - V(\phi)$$

Yukawa interactions

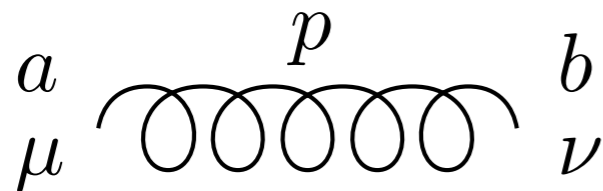
Note: no mass terms! Masses are generated through vacuum expectation value of Higgs field ϕ .

	Gauge group	Charged fermions	Gauge bosons	Coupling	Low- E
Strong interaction (QCD)	SU(3)	quarks u, d, c, s, t, b in $N_c = 3$ colors	$N_c^2 - 1 = 8$ gluons	$\alpha_s = \frac{g_s^2}{4\pi}$	Confinement
Electroweak	SU(2) x U(1)	all fermions different charges for ψ_L and ψ_R	W^\pm, Z, γ	$\alpha = \frac{e^2}{4\pi}$ G_F	Higgs mechanism, screening

Feynman rules for QCD

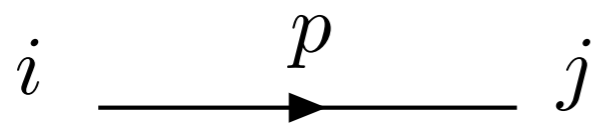
By expanding the action in the fields and Fourier transforming, one obtains Feynman rules in momentum space.

Bilinear terms in action give propagators



Gluon: $-i \delta_{ab} g_{\mu\nu} / p^2$ $a, b = 1, 2, \dots, N_c^2 - 1$

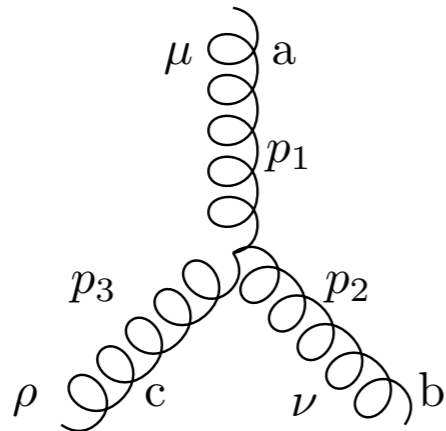
Feynman gauge. Different form for other gauge fixing



Fermion: $i \delta_{ij} (\gamma^\mu p_\mu + m) / (p^2 - m^2)$

$i, j = 1, \dots, N_c$

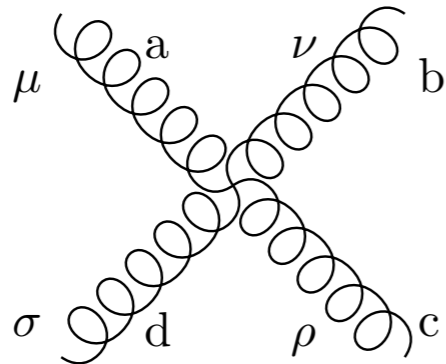
Interaction vertices



Lagrangian: $-g f^{abc} (\partial_\mu A_\nu^a) A_\mu^b A_\nu^c$

$$g_s f^{abc} \left(g_{\mu\nu} (p_1 - p_2)_\rho + g_{\nu\rho} (p_2 - p_3)_\mu + g_{\rho\mu} (p_3 - p_1)_\nu \right)$$

3! = 6 terms from symmetrization in gluon fields



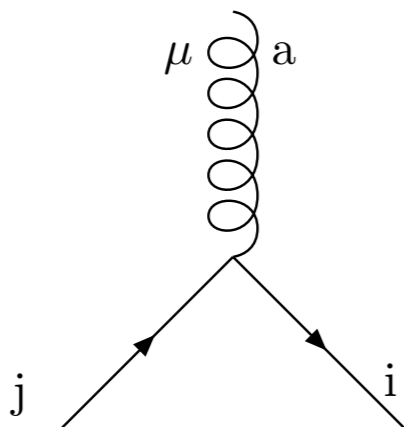
$$-i g_s^2 f^{eab} f^{ecd} (g_{\mu\rho} g_{\nu\sigma} - g_{\mu\sigma} g_{\nu\rho})$$

$$-i g_s^2 f^{eac} f^{ebd} (g_{\mu\nu} g_{\rho\sigma} - g_{\mu\sigma} g_{\nu\rho})$$

$$-i g_s^2 f^{ead} f^{ebc} (g_{\mu\nu} g_{\rho\sigma} - g_{\mu\rho} g_{\nu\sigma})$$

$$\frac{1}{4} g_s^2 f^{abc} f^{ade} A_\mu^b A_\nu^c A_\mu^d A_\nu^e$$

4! = 24 terms, 4 identical

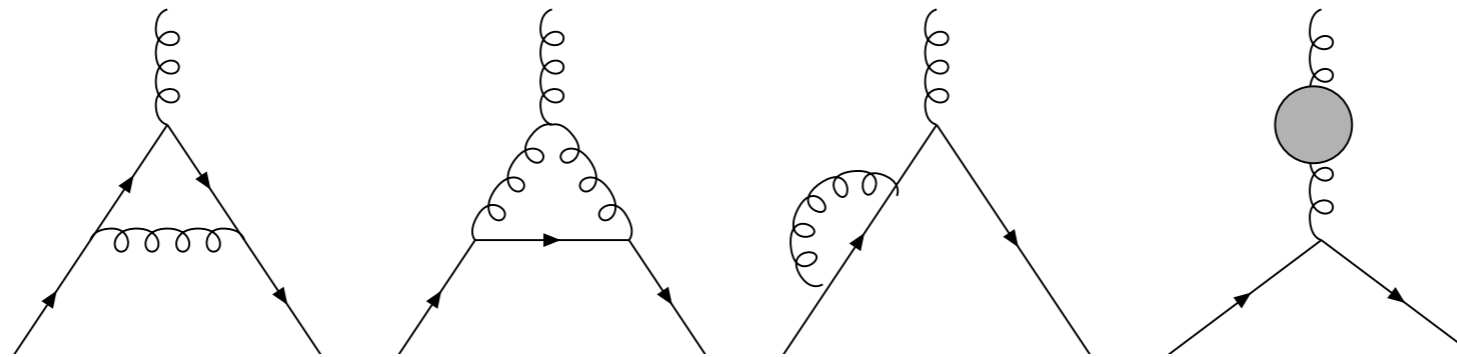


$$i g_s \gamma^\mu (T^a)_{ij}$$

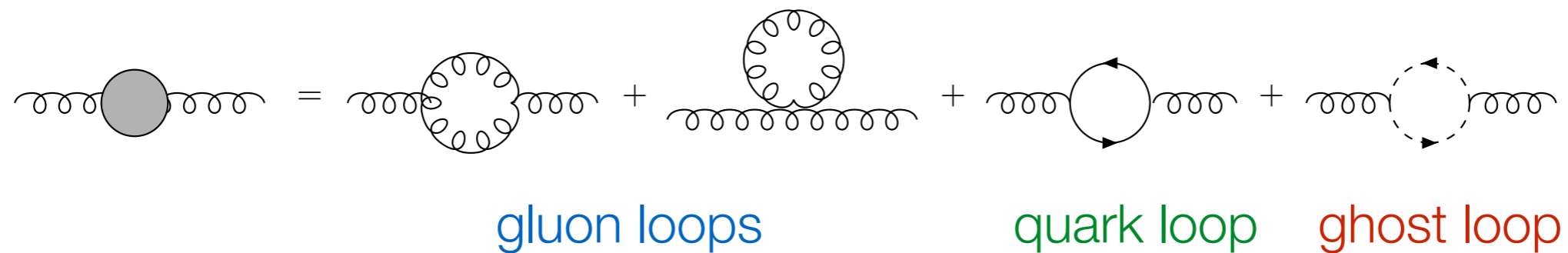
$$g_s \bar{\Psi}_i \gamma^\mu A_\mu^a (T^a)_{ij} \Psi_j$$

Loop corrections

Compute higher-order corrections to the quark-gluon coupling



with



Renormalization

Loop corrections suffer from UV divergences

- **Regularize** integrals (UV cutoff, dimensional regularization, ...) to make divergences explicit
- **Renormalization**: Subtract divergent pieces and absorb them into parameters of theory, e.g.

$$\alpha_s^0 \rightarrow \alpha_s(\mu)$$

bare coupling, absorbs divergences

renormalized coupling, finite

subtraction scale *aka* renormalization scale

Running coupling

Behavior of the coupling when the scale μ is changed is governed by renormalization group equation

$$\mu \frac{\partial \alpha_s(\mu)}{\partial \mu} = \frac{\partial \alpha_s(\mu)}{\partial \ln \mu} = \beta(\alpha_s(\mu))$$

driven by the β -function

$$\beta(\alpha_s) = -2\alpha_s \left[\beta_0 \alpha_s + \beta_1 \alpha_s^2 + \mathcal{O}(\alpha_s^3) \right]$$

from one-loop diagrams

from two-loop diagrams

Solution at one loop

$$\alpha_s(\mu) = \frac{\alpha_s(\mu_0) \text{ value at reference scale } \mu_0}{1 + \alpha_s(\mu_0) \beta_0 \ln(\mu^2/\mu_0^2)}$$

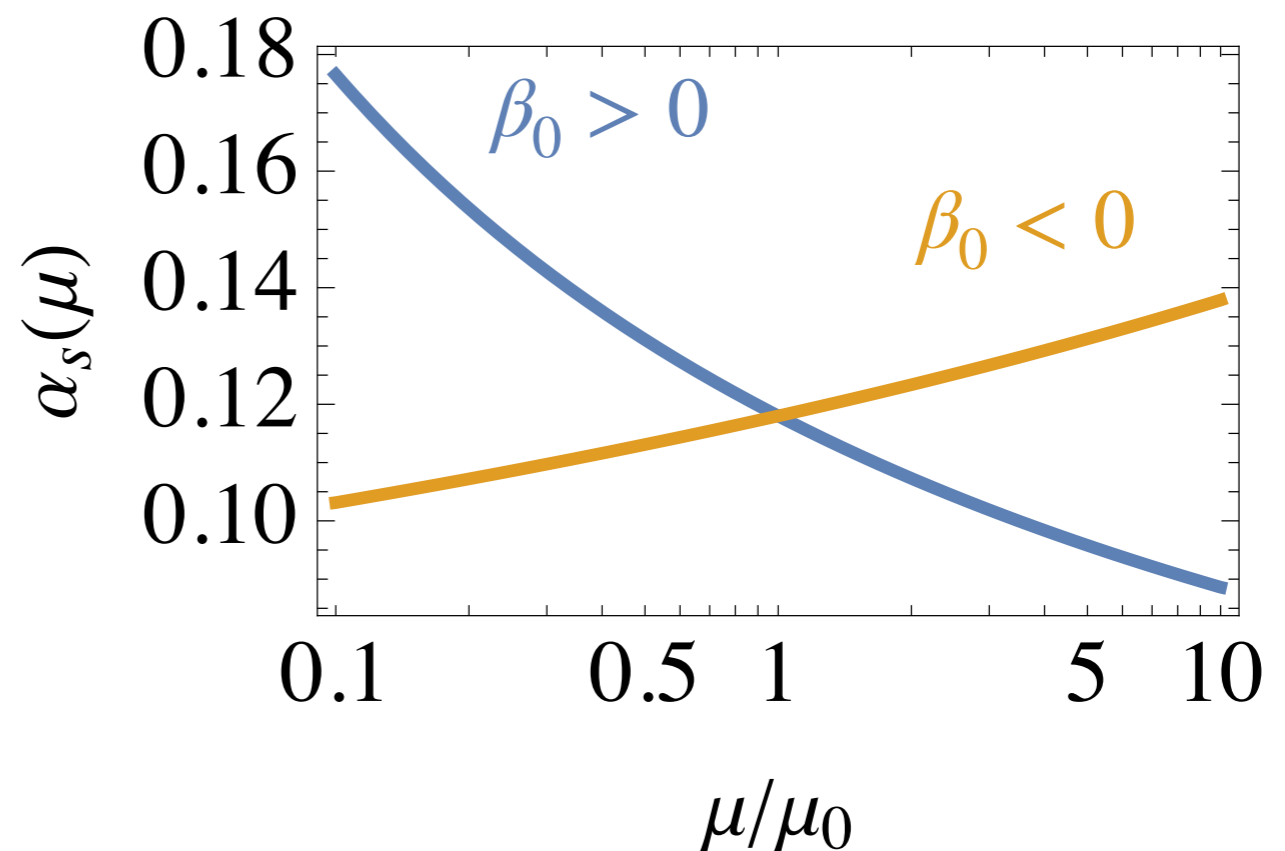
In QCD one obtains

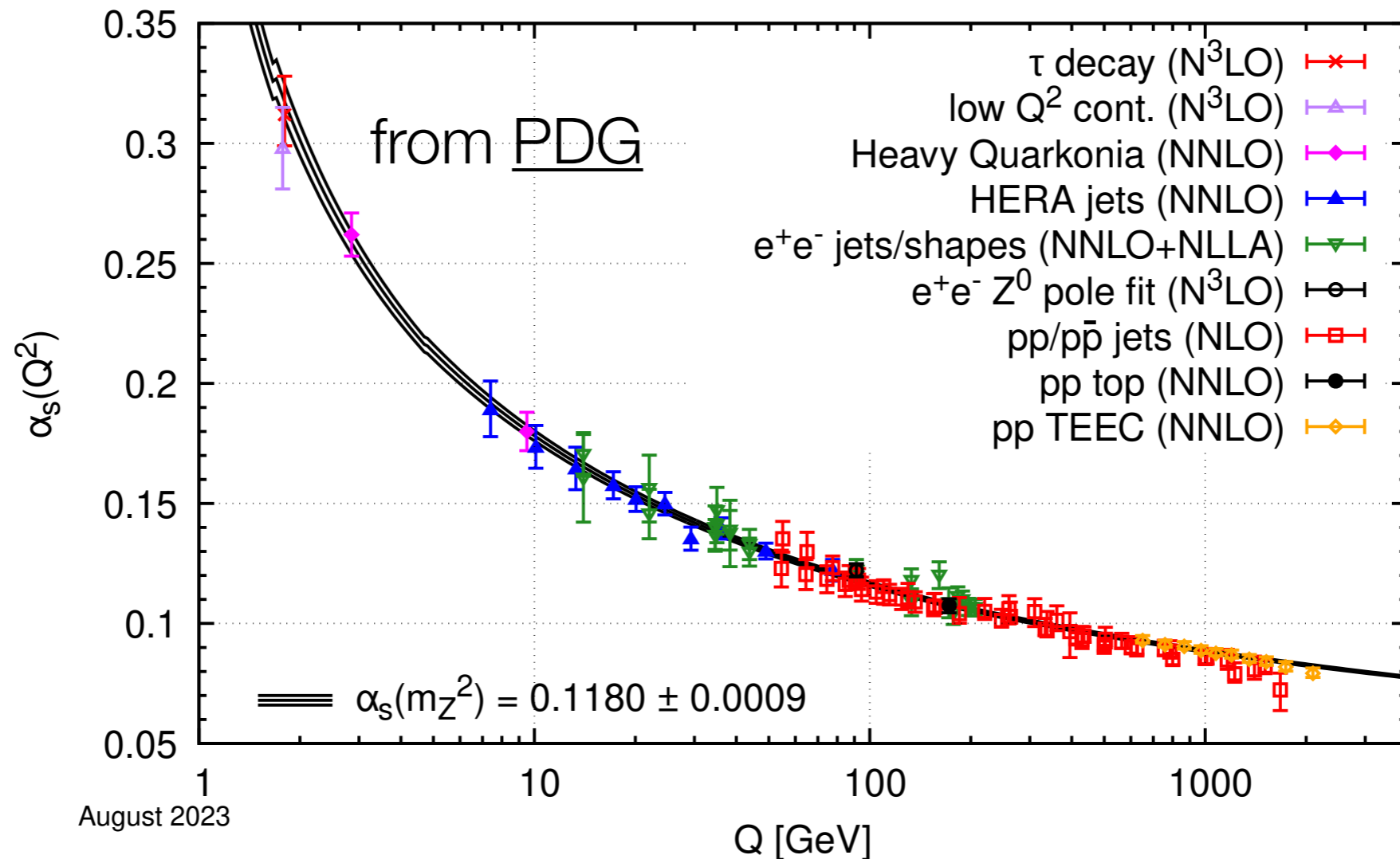
$$\beta_0 = \frac{1}{12\pi} (11 N_c - 2n_f) > 0$$

weak coupling at very high energies:

asymptotic freedom!

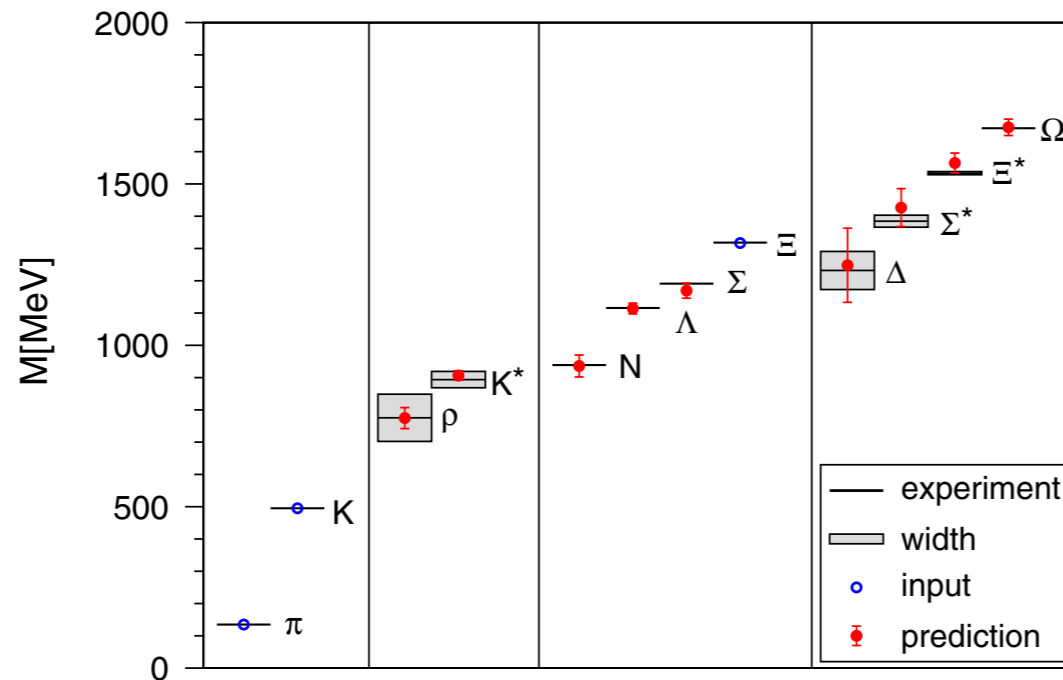
Nobel Prize '04
for Gross, Politzer, Wilczek





- Running of coupling confirmed by experimental measurements at different energies with $\mu = Q$
- Coupling $\alpha_s(\mu) \rightarrow \infty$ at low $\mu = \Lambda_{QCD} \sim 200 \text{ MeV}$
- Note: β -function has been computed to 5 loops! Implemented in code RunDec.

Low energy: non-perturbative QCD



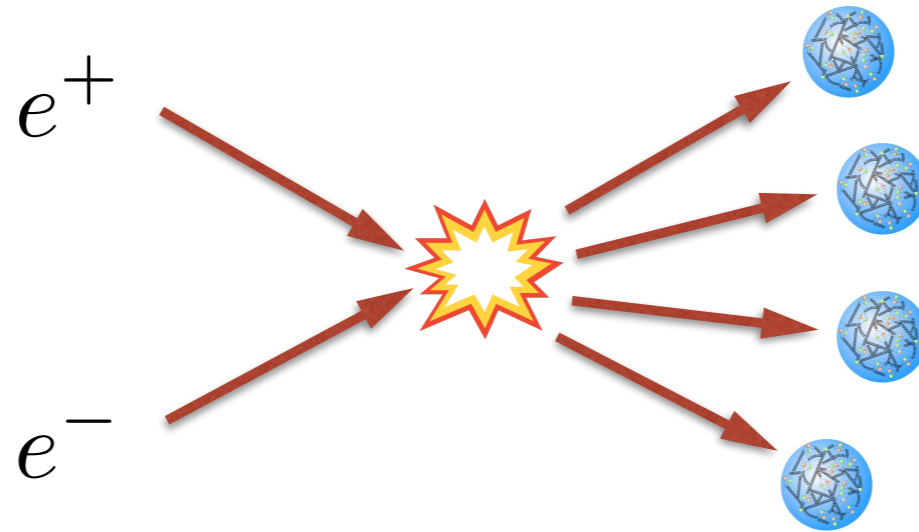
Dürr et al. '08
BMW Collaboration

Numerical solution of QCD path integral with **lattice QCD** successfully determines simple (“Euclidean”) low-energy quantities

- hadron masses, hadron form factors, ...

Side remark: Proton and neutron masses almost entirely due to non-perturbative QCD dynamics, quark mass contribution (due to Higgs VEV) very small.

Perturbative QCD?



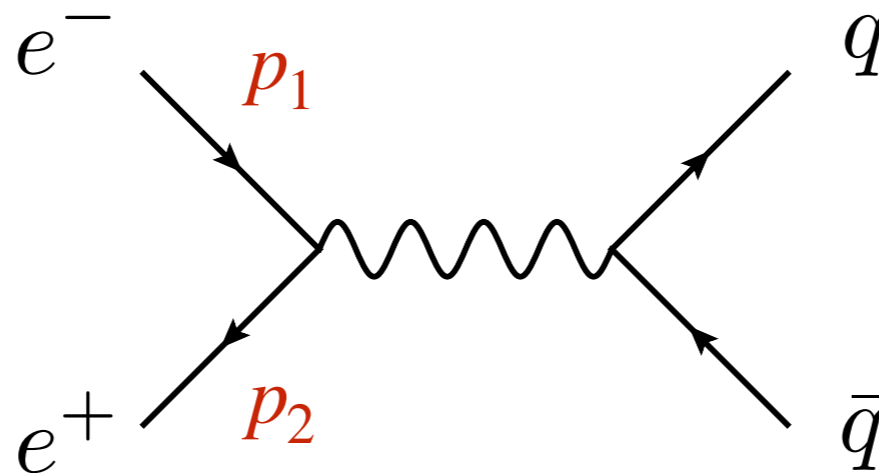
Let us now compute the inclusive cross section

$$\sigma(e^+e^- \rightarrow \text{hadrons})$$

in perturbation theory, by boldly replacing the final state with quarks and gluons.

R -ratio

Lowest order diagram



has the same form as $e^+e^- \rightarrow \mu^+\mu^-$. Define the ratio $[s = (p_1 + p_2)^2]$

$$R(s) = \frac{\sigma(e^+e^- \rightarrow q\bar{q})}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)}$$

Theoretical prediction

If we neglect quark and muon masses, numerator and denominator are identical up to charge factors.

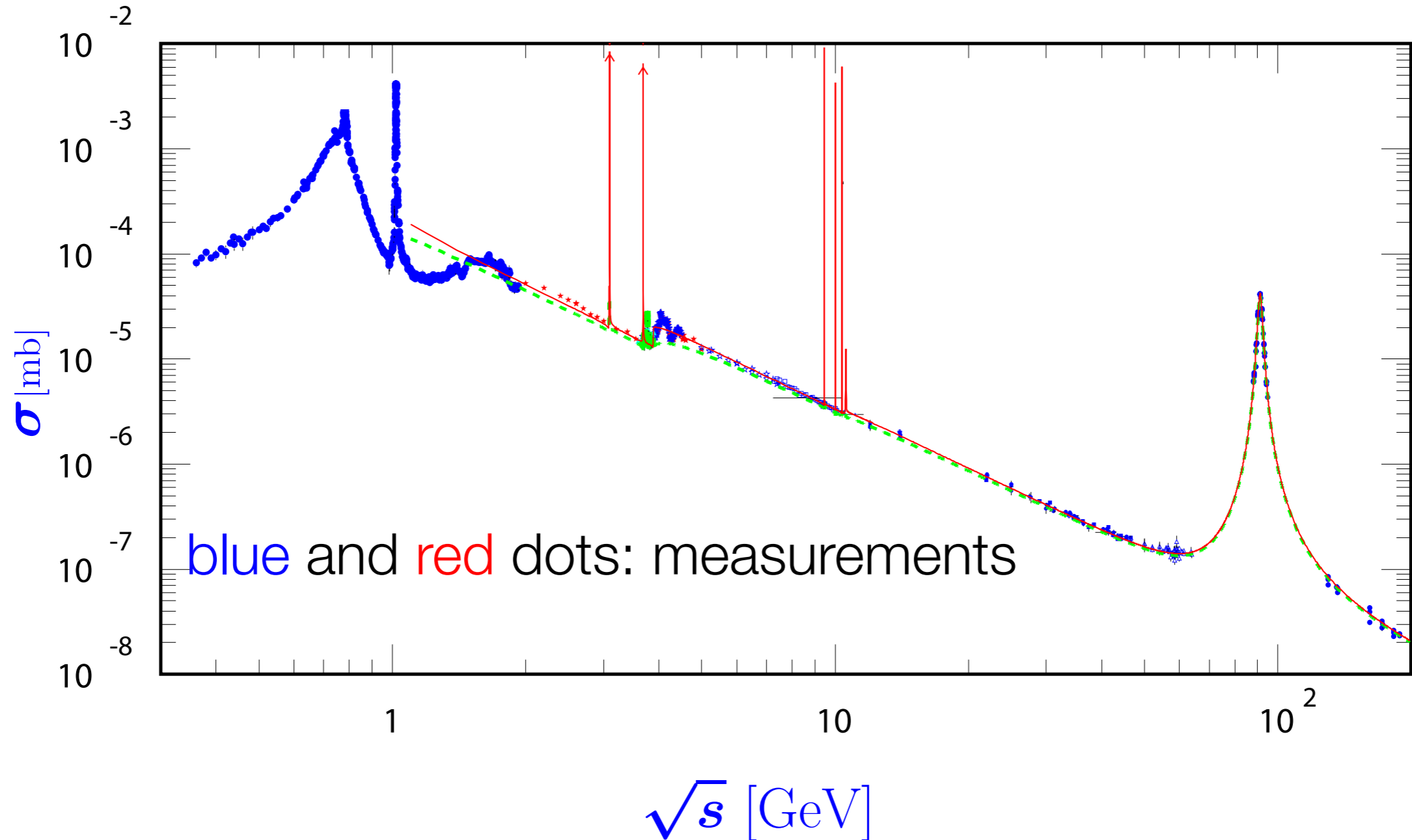
$$R(s) = N_c \sum_f Q_f^2$$

$N_c = 3$ quarks per flavor

$Q_f = +2/3$ for u, c, t
 $Q_f = -1/3$ for d, s, b

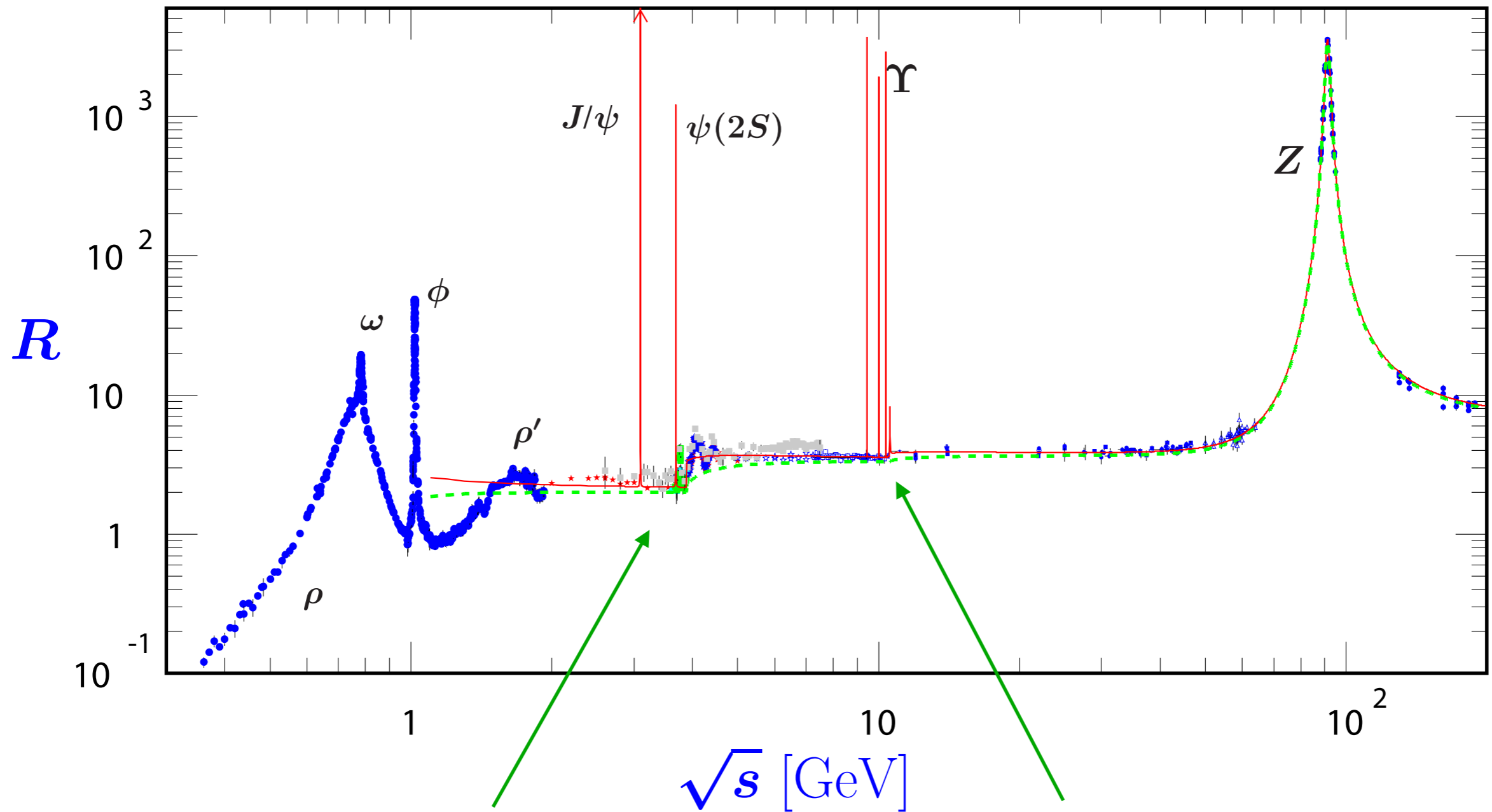
sum over all quark flavors f
accessible at center-of-mass energy s

$e^+e^- \rightarrow$ hadrons: cross section



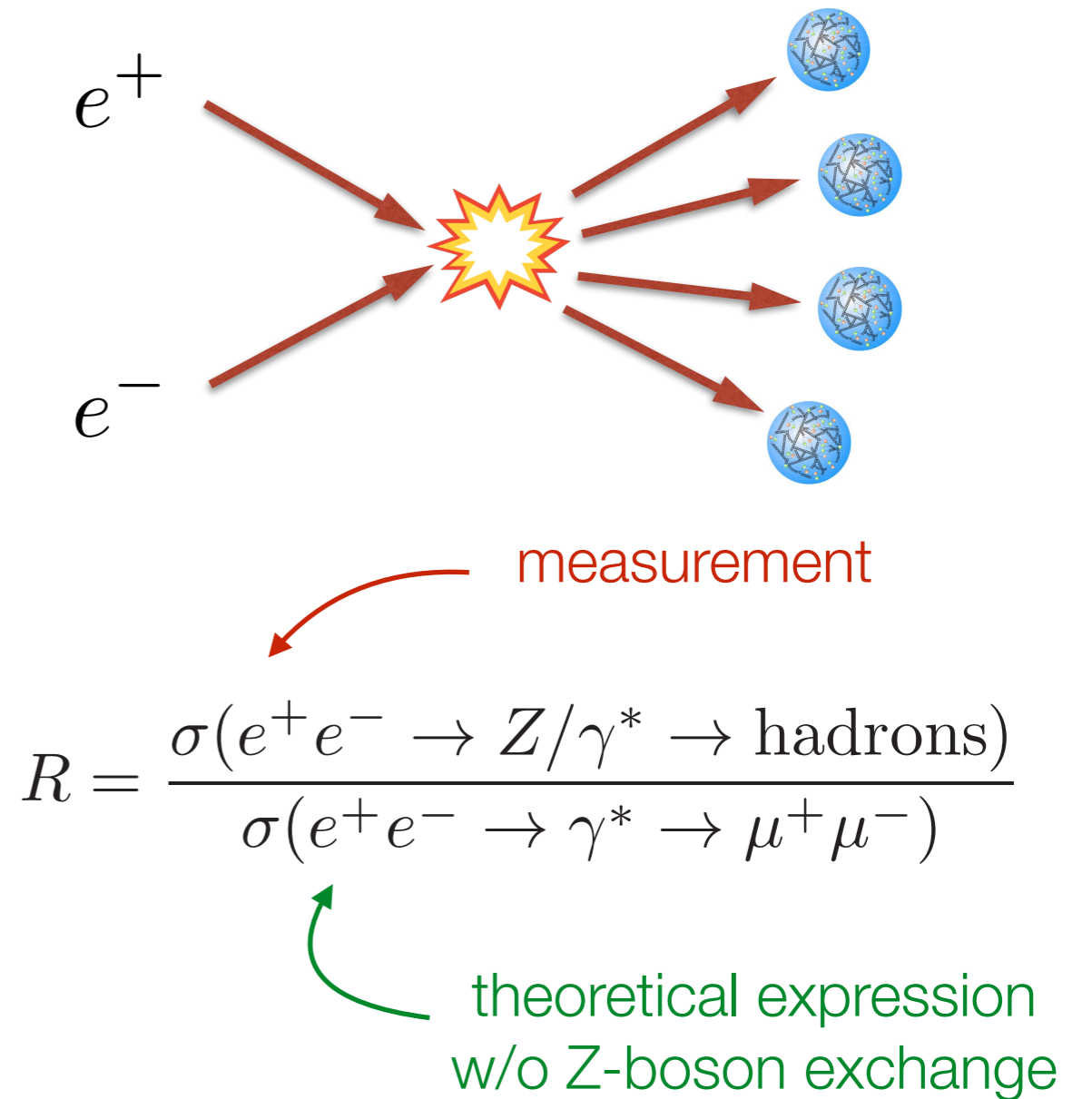
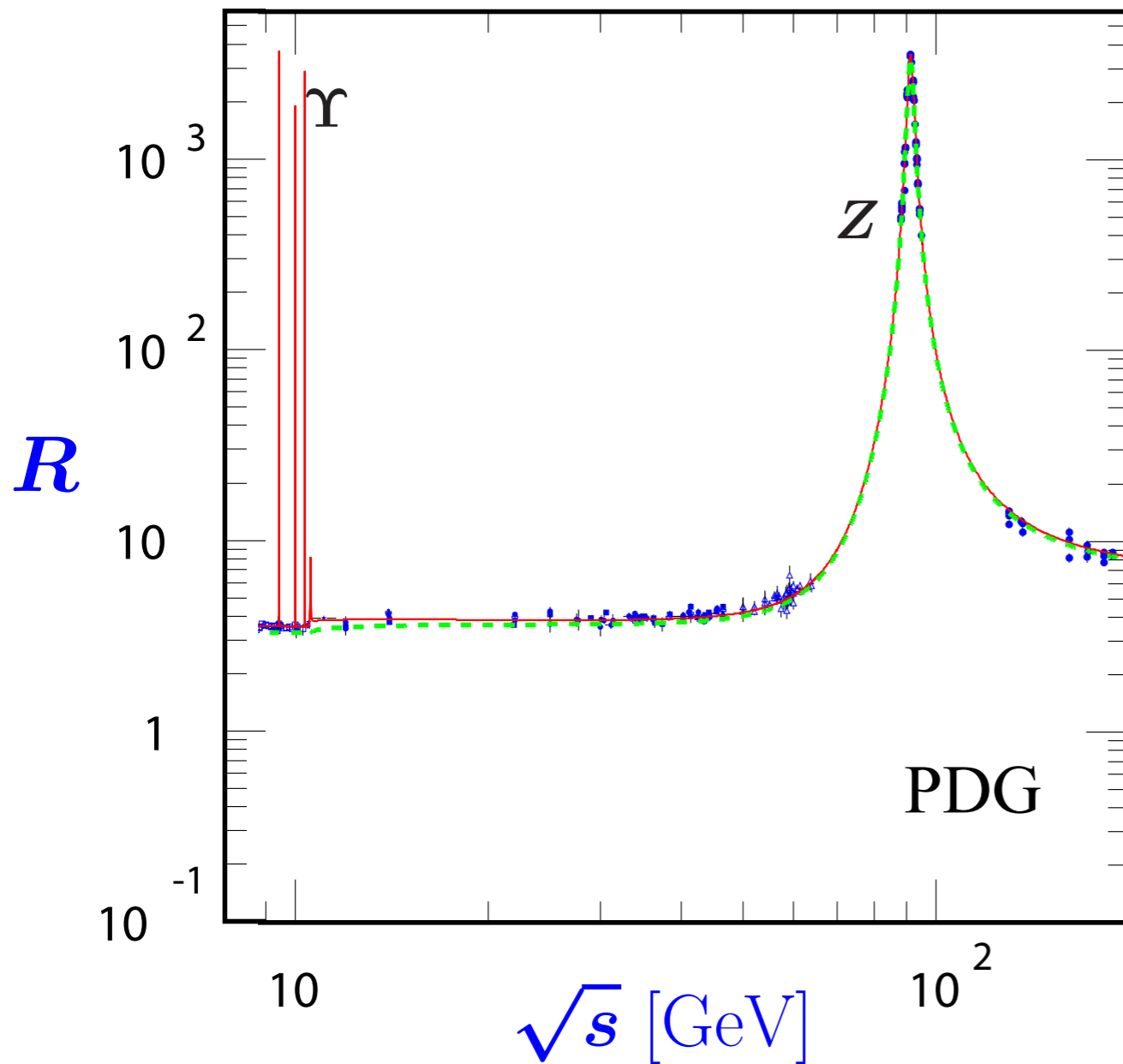
compiled by the Particle Data Group

R -ratio



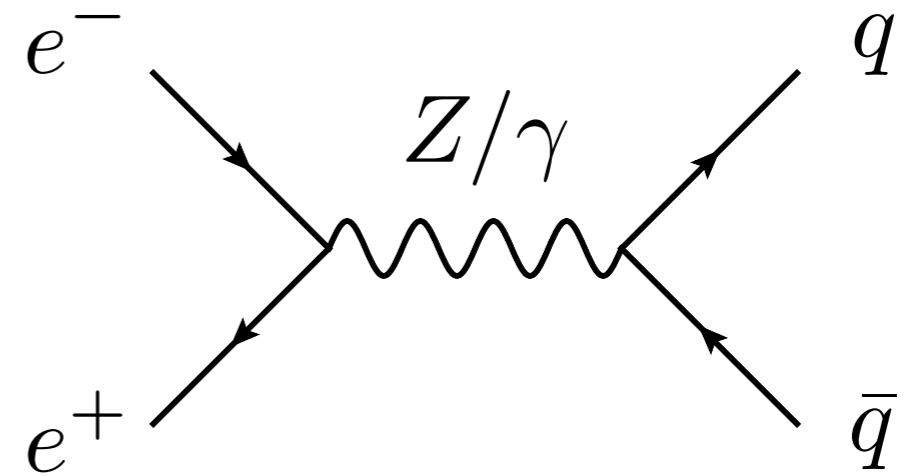
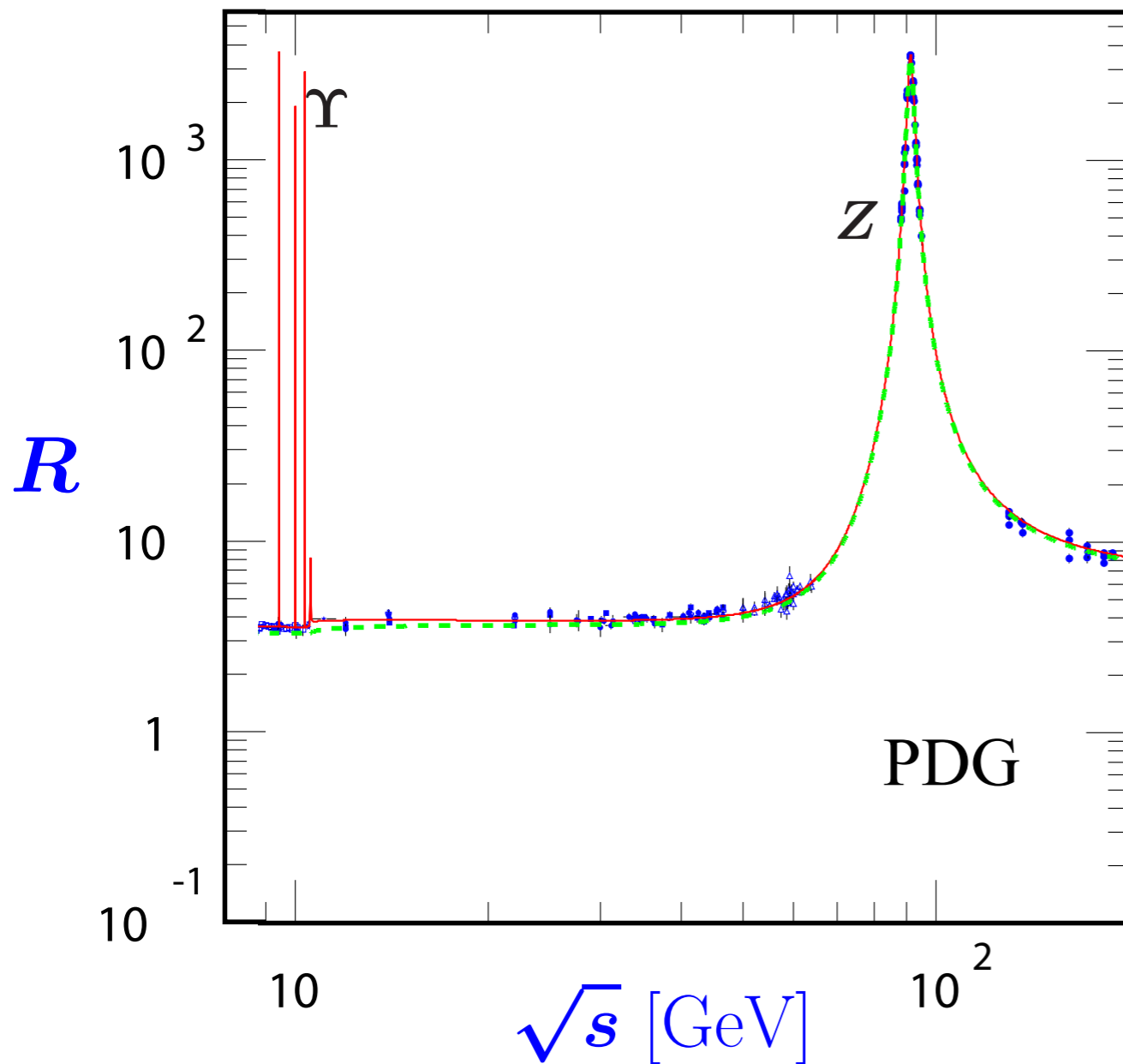
$c\bar{c}$ resonances
 $m_c \approx 1.3 \text{ GeV}$

$b\bar{b}$ resonances
 $m_b \approx 4.2 \text{ GeV}$



Blue: experimental measurements

Green and red lines theoretical predictions



sum over colors and flavors of quarks

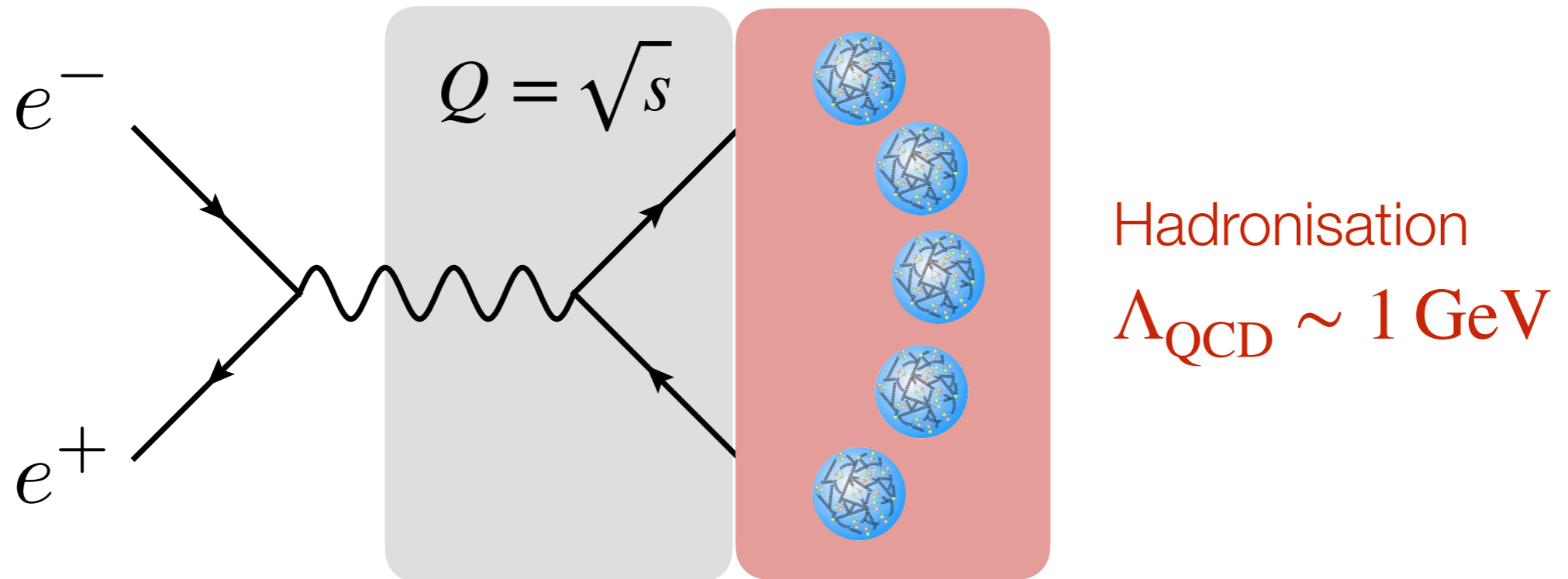
$$R_{\text{pert}} = \frac{\sigma(e^+e^- \rightarrow Z/\gamma^* \rightarrow q\bar{q})}{\sigma(e^+e^- \rightarrow \gamma^* \rightarrow \mu^+\mu^-)}$$

Dashed green: LO perturbation theory

Solid red: N³LO perturbation theory

Remarkable agreement with data: **asymptotic freedom**

Intuitive explanation:



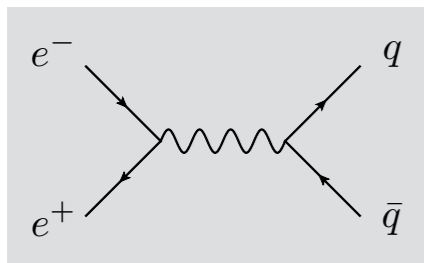
Large **scale separation** $Q \gg \Lambda_{\text{QCD}}$.

- Two step process: 1.) $q\bar{q}$ production 2.) rearrangement into hadrons
- For σ_{total} , small sensitivity to step 2.)

Formal explanation: the Operator Product Expansion (OPE)^{*} factorizes low and high energy contributions

$$R(s) = C_1(s) \underbrace{\langle 0 | 1 | 0 \rangle}_{= 1} + C_{q\bar{q}}(s) \underbrace{\langle 0 | m_q \bar{q}q | 0 \rangle}_{\sim m_q \Lambda_{\text{QCD}}^3} + C_{GG}(s) \underbrace{\langle 0 | G^2 | 0 \rangle}_{\sim \Lambda_{\text{QCD}}^4} + \dots$$

$\sim 1/s^2$



Wilson coefficients:
high-energy physics
independent of states

Matrix elements:
non-perturbative,
hadronisation effects

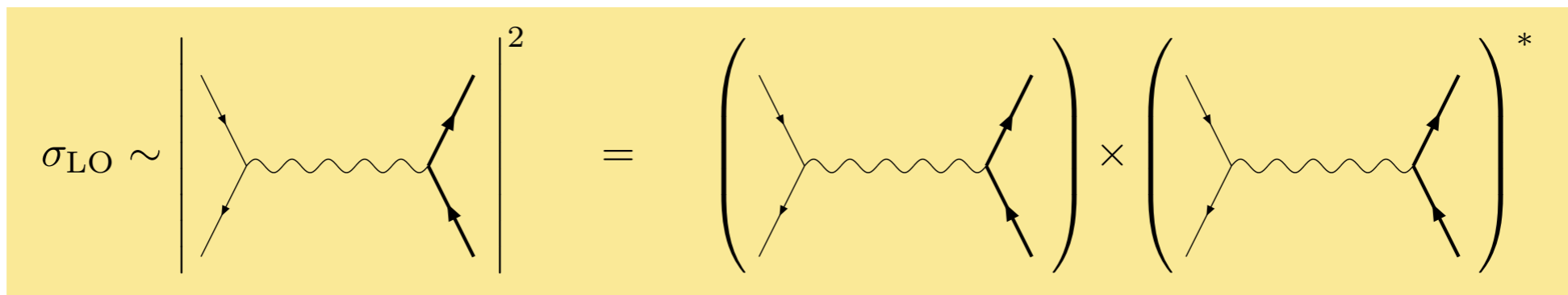
The successful prediction of the R -ratio in perturbation theory leads to the following questions

1. Can one improve the prediction by going to **higher orders** in perturbation theory?
2. Are there other, **less inclusive cross sections**, which are **insensitive to hadronisation** effects?

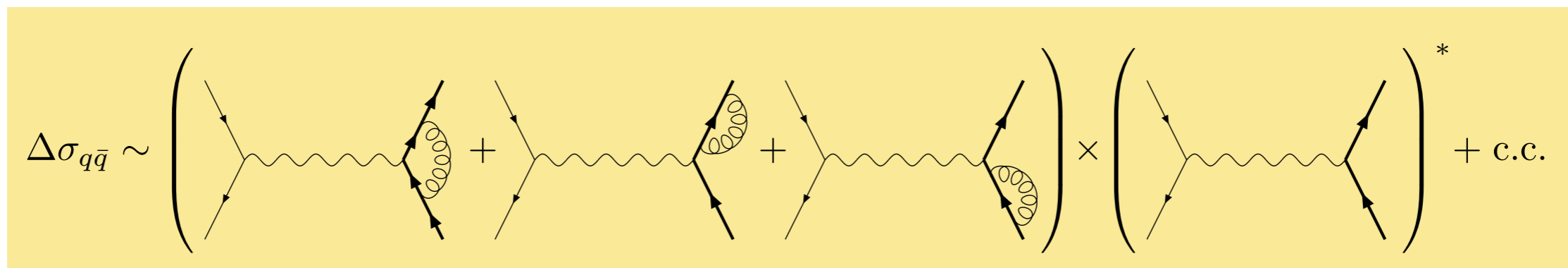
Interestingly, answer to 1.) informs 2.). Will first study the structure of perturbative corrections, then introduce classes of observables which are insensitive to hadronisation.

Perturbative corrections

Before, we computed the leading order (LO) R -ratio

$$\sigma_{\text{LO}} \sim \left| \text{diagram} \right|^2 = \left(\text{diagram} \right) \times \left(\text{diagram} \right)^*$$
The diagram shows the leading order cross-section σ_{LO} as the squared magnitude of a tree-level Feynman diagram. This is equivalent to the product of the diagram and its complex conjugate. The tree-level diagram consists of two incoming fermion lines (left) and two outgoing fermion lines (right), connected by a wavy photon line.

The loop corrections are

$$\Delta\sigma_{q\bar{q}} \sim \left(\text{diagram}_1 + \text{diagram}_2 + \text{diagram}_3 \right) \times \left(\text{diagram} \right)^* + \text{c.c.}$$
The diagram shows the loop correction $\Delta\sigma_{q\bar{q}}$ as the sum of three one-loop diagrams multiplied by the complex conjugate of the tree-level diagram, plus the complex conjugate of the sum. The three loop diagrams are: a self-energy loop on the incoming fermion line, a self-energy loop on the outgoing fermion line, and a vertex correction loop on the photon-fermion vertex.

Loop integrals suffer from divergences.
Regularize them by computing in $d = 4 - 2\varepsilon$
(dimensional regularization).

Result ($Q^2 = s$)

$$\Delta\sigma_{q\bar{q}} = \sigma_{\text{LO}} \frac{\alpha_s}{3\pi} \left(\frac{\bar{\mu}^2}{Q^2} \right)^\varepsilon \left(-\frac{4}{\varepsilon^2} - \frac{6}{\varepsilon} - 16 + \frac{7}{3}\pi^2 + \mathcal{O}(\varepsilon) \right)$$

$$[\bar{\mu}^2 = 4\pi e^{\gamma_E} \mu^2]$$

diverges for $\varepsilon \rightarrow 0$!

These are not ultraviolet divergences!

Repeat the computation with massive quarks and gluons.

Result for small masses is finite (source: ChatGPT)

$$\Delta\sigma_{q\bar{q}} = \sigma_{\text{LO}} \frac{\alpha_s}{3\pi} \left[-2 \ln^2 \left(\frac{Q^2}{m_q^2} \right) + 6 \ln \left(\frac{Q^2}{m_q^2} \right) - 2 \ln \left(\frac{Q^2}{m_g^2} \right) + \text{constants} \right]$$

but depends on small quark masses and unphysical gluon mass.

Here masses act as infrared regulator: divergences come back as we switch off the masses!

Divergences arose because we computed the unphysical **exclusive** cross section $\sigma_{q\bar{q}}$.

In theories with massless particles (QED, QCD, ...) fully exclusive cross sections do not make sense! For massless particles cannot distinguish

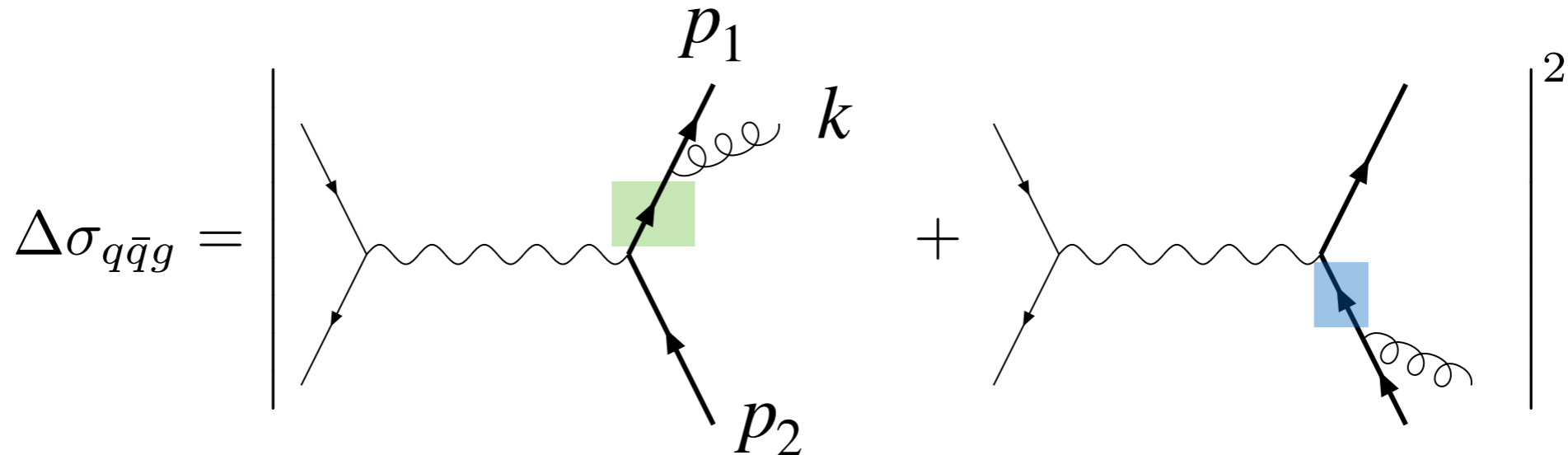


if emission is **soft** ($E \rightarrow 0$) or **collinear** ($\theta \rightarrow 0$) !

Bloch and Nordsieck '37

Kinoshita '62 Lee, Nauenberg '64

Need to include real emission corrections!



$$\frac{1}{4} \sum_{\text{spins}} |\mathcal{M}_{q\bar{q}g}|^2 = \sigma_{\text{LO}} \frac{16\pi}{Q^2} C_F g_s^2 \frac{(p_1 \cdot k)^2 + (p_2 \cdot k)^2 + Q^2 p_1 \cdot p_2}{p_1 \cdot k p_2 \cdot k}$$

diverges for $k \rightarrow 0$ and for $k \parallel p_1$ or $k \parallel p_2$.

Phase space integral does not exist, regularize in $d = 4 - 2\varepsilon$.

Aside: phase-space in d -dimensions

Massless toy example, $k \equiv E_k = |\vec{k}|$

$$I = \int \frac{d^{d-1}k}{2E_k} \frac{1}{E_k^2} \theta(Q - E_k) = \int_0^Q dk k^{d-2} \int d\Omega_{d-1} \frac{1}{2E_k^3}$$

set $d = 4 - 2\varepsilon$

spherical coordinates

$$I = \frac{1}{2} \int_0^Q dk k^{-1-2\varepsilon} \Omega_{d-1} = -\frac{Q^{-2\varepsilon}}{4\varepsilon} \Omega_{3-2\varepsilon}$$

surface of $d-1$ dimensional unit sphere, see QFT books!

IR divergence

Rewrite kinematics in terms of variables y_i

$$2p_1 \cdot p_2 = y_3 Q^2$$

$$2p_1 \cdot p_k = y_2 Q^2$$

$$2p_2 \cdot p_k = y_1 Q^2$$

In CMS system

$$q^\mu = p_1^\mu + p_2^\mu + k^\mu = (Q, 0, 0, 0)$$

and

$$y_i = 1 - \frac{2E_i}{Q} > 0 \quad \text{with} \quad y_1 + y_2 + y_3 = 1$$

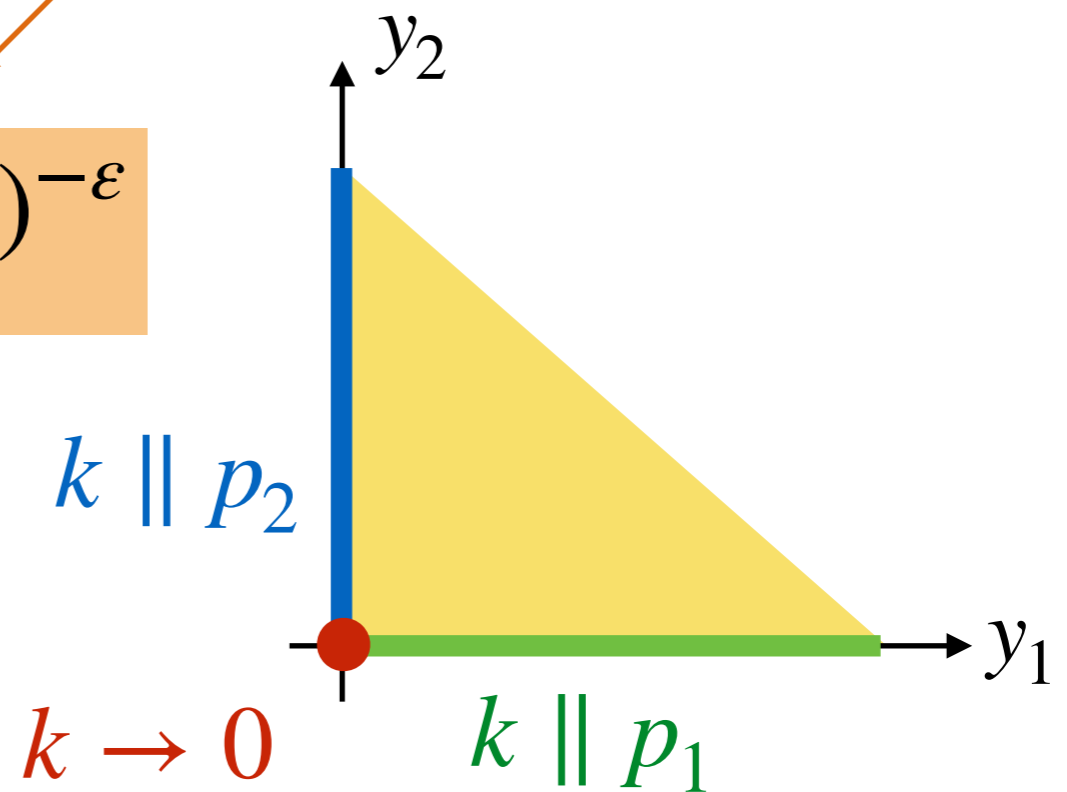
In terms of new variables (with $y_3 = 1 - y_1 - y_2$)

$$\frac{1}{4} \sum_{\text{spins}} |\mathcal{M}_{q\bar{q}g}|^2 = \sigma_{\text{LO}} \frac{16\pi}{Q^2} C_F g_s^2 \frac{y_1^2 + y_2^2 + 2y_3}{y_1 y_2} + O(\varepsilon)$$

Phase-space integral

$$PS_3 \propto \int_0^1 dy_1 \int_0^{y_1} dy_2 (y_1 y_2 y_3)^{-\varepsilon}$$

regularized if $\varepsilon < 0$



With the regularization in place, we can compute the total cross section

$$\sigma_{\text{tot}} = \sigma(e^+e^- \rightarrow X) = \sigma_{q\bar{q}} + \sigma_{q\bar{q}g} + \mathcal{O}(\alpha_s^2)$$

and obtain

$$\sigma_{\text{tot}} = \sigma_{LO} \left(1 + \frac{\alpha_s}{3\pi} \left[\begin{array}{c} \text{virtual corrections} \\ -\frac{4}{\varepsilon^2} - \frac{6}{\varepsilon} - 16 + \frac{7\pi^2}{3} \end{array} \right] + \frac{\alpha_s}{3\pi} \left[\begin{array}{c} \text{real emission} \\ \frac{4}{\varepsilon^2} + \frac{6}{\varepsilon} + 19 - \frac{7\pi^2}{3} \end{array} \right] \right)$$

With the regularization in place, we can compute the total cross section

$$\sigma_{\text{tot}} = \sigma(e^+e^- \rightarrow X) = \sigma_{q\bar{q}} + \sigma_{q\bar{q}g} + \mathcal{O}(\alpha_s^2)$$

and obtain

$$\sigma_{\text{tot}} = \sigma_{\text{LO}} \left(1 + \overset{\text{few \%}}{\frac{\alpha_s(\mu)}{\pi}} \right)$$

Finite! Small correction, insensitive to low-energy scales such as quark masses.

And excellent agreement with data far away from resonance regions!

Scale (in-)dependence

Perturbative result for the R-ratio

$$\sigma_{\text{tot}} = \sigma_{\text{LO}} \left(1 + \frac{\alpha_s(\mu)}{\pi} \right)$$

seems to depend on renormalization scale μ !

But σ_{tot} is a physical cross section, cannot depend on unphysical scale μ !

- change in μ is higher-order effect, compensated by perturbative corrections!

NNLO result for the R -ratio

$$\sigma_{\text{tot}} = \sigma_{\text{LO}} \left(1 + \frac{\alpha_s(\mu)}{\pi} + \left(\frac{\alpha_s(\mu)}{\pi} \right)^2 \left(\pi \beta_0 \ln \frac{\mu^2}{Q^2} - 11\zeta_3 + \frac{365}{24} \right) + \left(\frac{2\zeta_3}{3} - \frac{11}{12} \right) n_f \right)$$

- β_0 -terms compensate scale dependence of NLO coefficient
- Residual scale dependence is N³LO effect
- Must choose $\mu \sim Q$ to avoid large logarithm in perturbative corrections

Since scale dependence is a higher-order effect, variation $Q/2 < \mu < 2Q$ is used to estimate perturbative uncertainty

Infrared Safe Observables Factorization and Resummation

- IR safety
- Event shapes, jets, EECs
- Soft-collinear factorization
- SCET and resummation

IR finiteness

What other observables \mathcal{O} , defined in terms of the particle momenta $\{p_1, p_2, \dots, p_n\}$ can be computed in perturbation theory? Observable must be

A. insensitive to soft radiation

$$\lim_{k \rightarrow 0} \mathcal{O}_{n+1}(p_1, p_2, \dots, p_n, k) = \mathcal{O}_n(p_1, p_2, \dots, p_n)$$

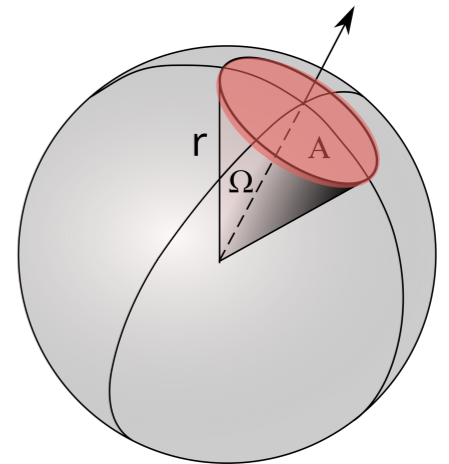
B. collinear safe for $p_1 \parallel p_2$

$$\mathcal{O}_{n+1}(p_1, p_2, \dots, p_{n+1}) = \mathcal{O}_n(p_1 + p_2, \dots, p_n)$$

If A.) and B.) hold, then IR divergent parts are always treated inclusively, so that cancellation of divergences occurs.

IR safe or not?

- Total cross section $\mathcal{O}_n = 1$
- Number of particles $\mathcal{O}_n = n$
- Maximum energy of particle
- Energy flow into particular angular area A of the detector
- Jet cross sections



IR safe or not?

- Total cross section $\mathcal{O}_n = 1$



- Number of particles $\mathcal{O}_n = n$

✗ soft & collinear unsafe

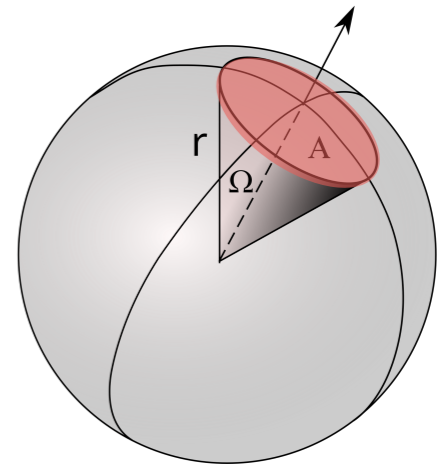
- Maximum energy of particle

✗ collinear unsafe

- Energy flow into particular angular area A of the detector



- Jet cross sections  *if* properly defined!



Observables

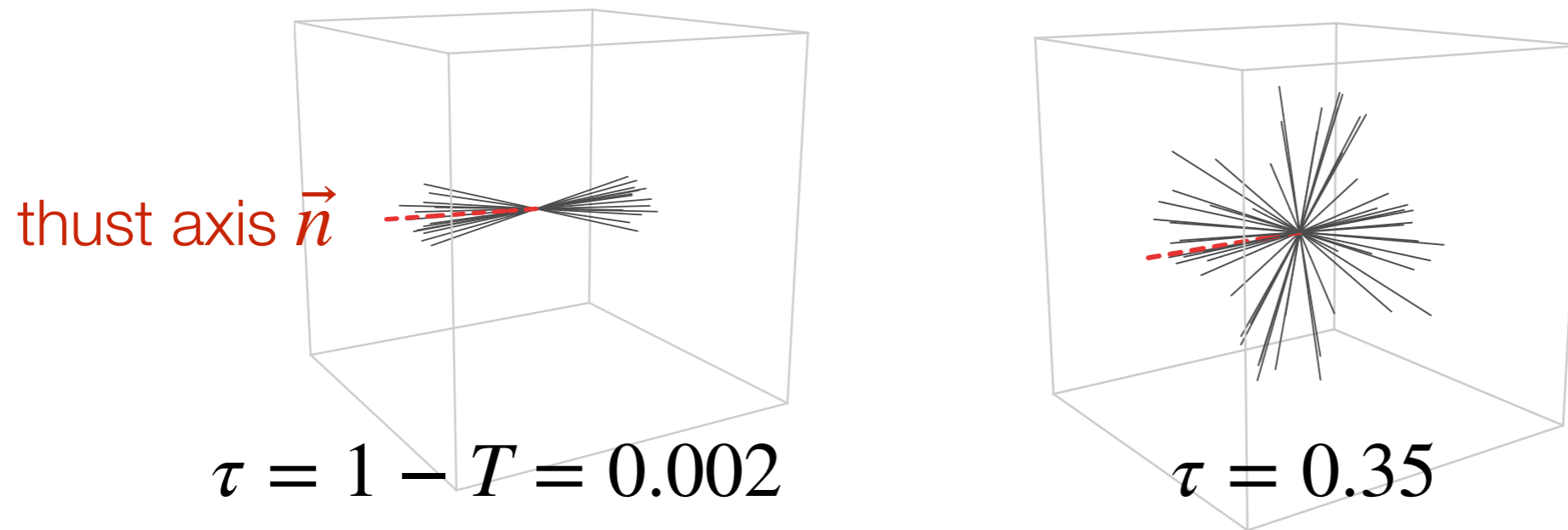
Collider observables should

- A. not be sensitive to non-perturbative low-energy QCD
- B. provide detailed information about short-distance physics

Will now discuss several classes of observables introduced to fulfill these requirements

- Jets, event shapes, energy correlators

Event shapes: e.g. thrust T



Event shape variables parameterize geometric properties of energy and momentum flow.

$$T = \frac{1}{Q} \max_{\vec{n}} \sum_i |\vec{n} \cdot \vec{p}_i|$$

Farhi '77

Generalization to multiple directions and hadronic collisions: *N-jettiness* Stewart, Tackmann, Waalewijn '10

The thrust distribution at LO has the form

$$\frac{1}{\sigma_0} \frac{d\sigma}{d\tau} = \frac{2\alpha_s}{3\pi} \left[-\frac{3}{\tau} + 6 + 9\tau + \frac{(6\tau^2 - 6\tau + 4)}{(1-\tau)\tau} \ln \frac{1-2\tau}{\tau} \right]$$

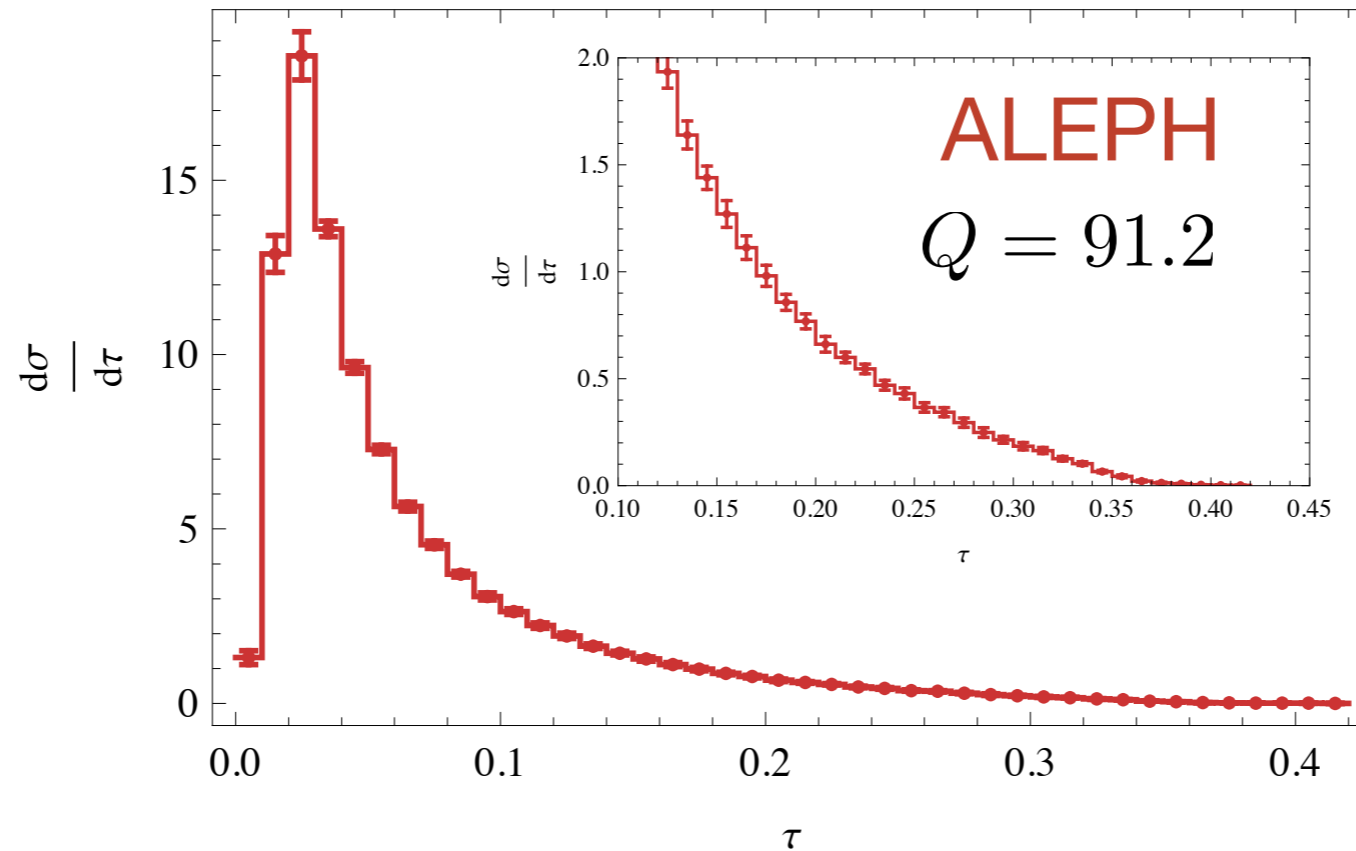
$$= \frac{2\alpha_s}{3\pi} \left[\frac{-4 \ln \tau - 3}{\tau} + d_{\text{regular}}(\tau) \right]$$

singular terms

Sudakov double logarithm

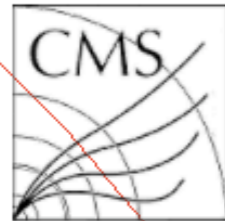
$$R(\tau) = \int_0^\tau d\tau' \frac{1}{\sigma_0} \frac{d\sigma}{d\tau'} = \frac{2\alpha_s}{3\pi} \left[-2 \ln^2 \tau - 3 \ln \tau + \dots \right]$$

At small τ the perturbative corrections are enhanced!
 Fixed-order expansion in α_s breaks down.

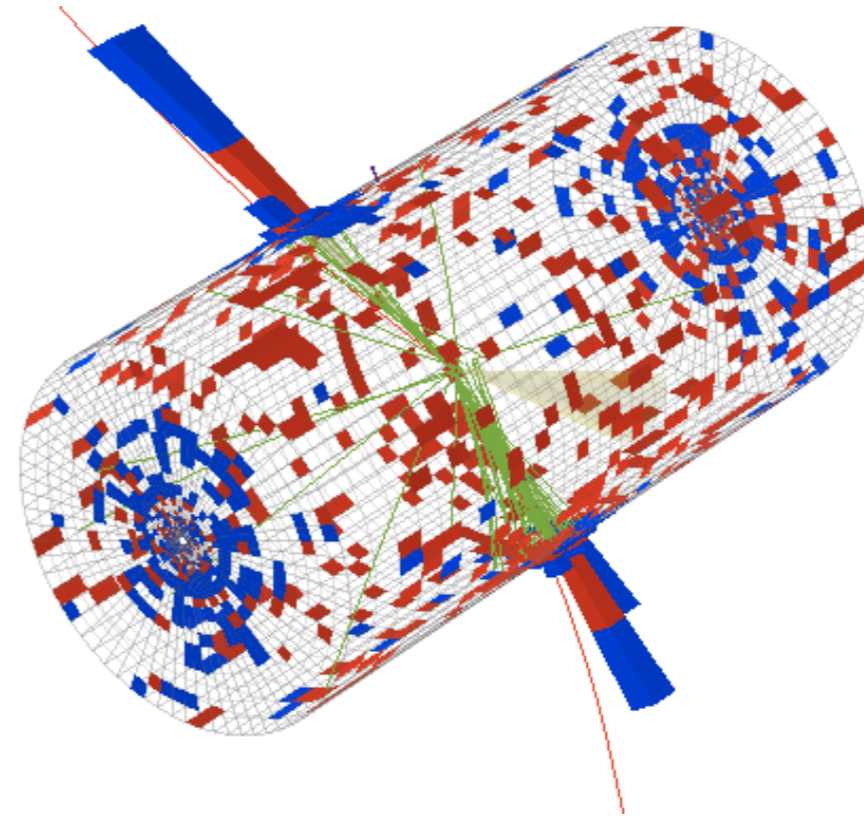


- Precise measurements of thrust and other event shapes at e^+e^- colliders; comparison to theoretical prediction used to extract α_s
- To describe peak region, one needs **resummation** of logarithmically enhanced terms and include **non-perturbative effects**
- Sensitivity to soft radiation is **problematic at hadron colliders**.
Solution: Shapes defined with jets, grooming, or soft-insensitive observables such as EEC.

Jet cross sections

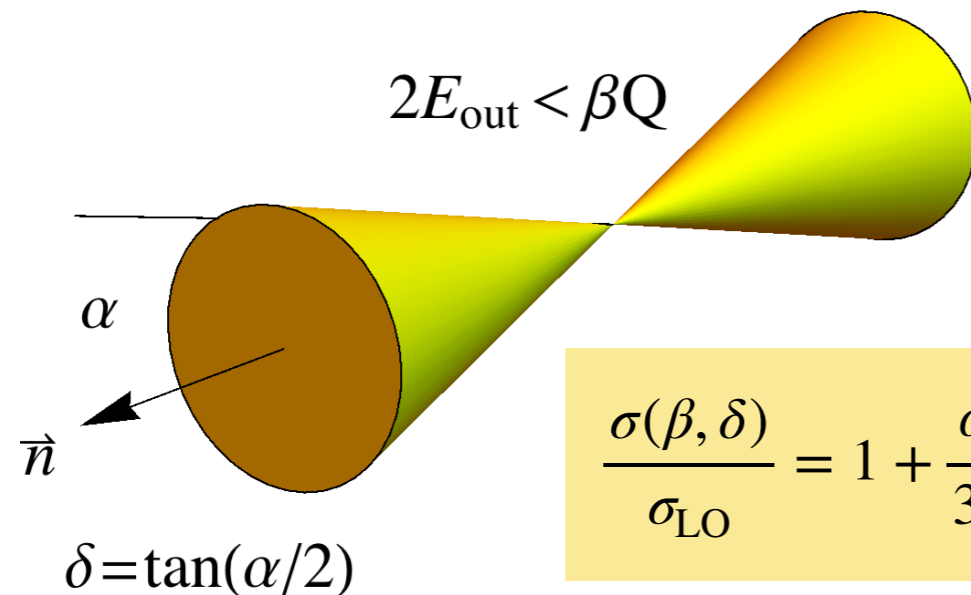


CMS Experiment at LHC, CERN
Data recorded: Fri Oct 5 12:29:33 2012 CEST
Run/Event: 204541 / 52508234
Lumi section: 32



Idea: define a cross section which reflects underlying hard partonic process, but includes soft and collinear radiation to be infrared safe.

Sterman-Weinberg '77 jets



$$\frac{\sigma(\beta, \delta)}{\sigma_{\text{LO}}} = 1 + \frac{\alpha_s}{3\pi} \left(-16 \ln \beta \ln \delta - 12 \ln \delta + 10 - \frac{4\pi^2}{3} \right) + \mathcal{O}(\beta, \delta)$$

Original definition of a two-jet cross section in e^+e^- collisions.
Two parameters

- Cone angle δ , energy fraction β outside cone

Infrared safe, but perturbative corrections are enhanced by $\ln \delta$ and $\ln \beta$. Also, careful analysis shows that lowest scale is $\Lambda = \beta \delta Q$, must ensure $\Lambda \gg \Lambda_{\text{QCD}}$.

Cone jets

To define multijet cone-jet cross sections, one needs **IR safe** prescriptions to

- choose cone directions
- to treat overlapping cones (split/merge)

Cone algorithms used at the Tevatron relied on seeds and were IR unsafe!

SISCone Salam, Soyez '08 is modern, seedless cone algorithm suited for hadron colliders.

Sequential recombination jets

Alternative definition of a jet is to sequentially combine particles into jets.

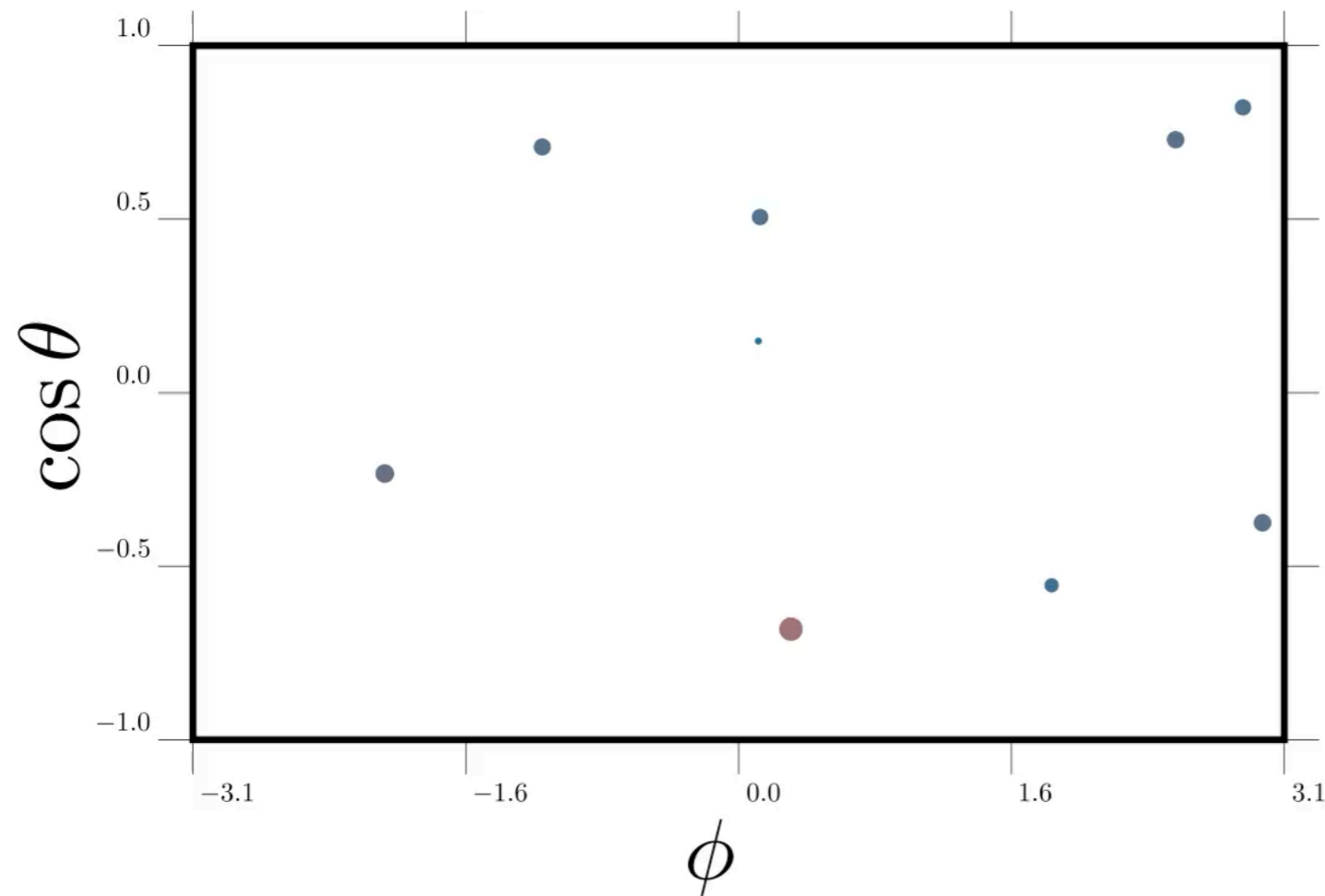
Simplest prescription for e^+e^- is JADE algorithm

1. For all pairs of particles ij , compute

$$d_{ij} = 2E_i E_j (1 - \cos \theta_{ij}) / Q^2$$

2. Find pair ij with minimum value $y_{\min} = d_{ij}$.
3. If $y_{\min} < y_{\text{cut}}$ combine pair ij into new particle, go to step 1.)
4. Otherwise declare all remaining particles jets.

Sequential clustering^{*}



1. Find minimum d_{ij}
 $\min(d_{ij}) = ?$
2. Combine i and j into a new jet
3. Stop if $\min(d_{ij})$ is larger than y_{cut}

^{*} clustering is for k_T algorithm (see next slides), not JADE

For massless particles $d_{ij} = (p_i + p_j)^2 / Q^2$.

- The JADE algorithm is **infrared safe**, since soft and collinear particles are immediately combined.

However, jets are quite irregular

- Soft particles moving in opposite directions can end up in same jet
- perturbation theory: **$\ln(y_{\text{cut}})$** terms with very complicated higher-order structure

k_T algorithm in e^+e^-

Catani et al. '91

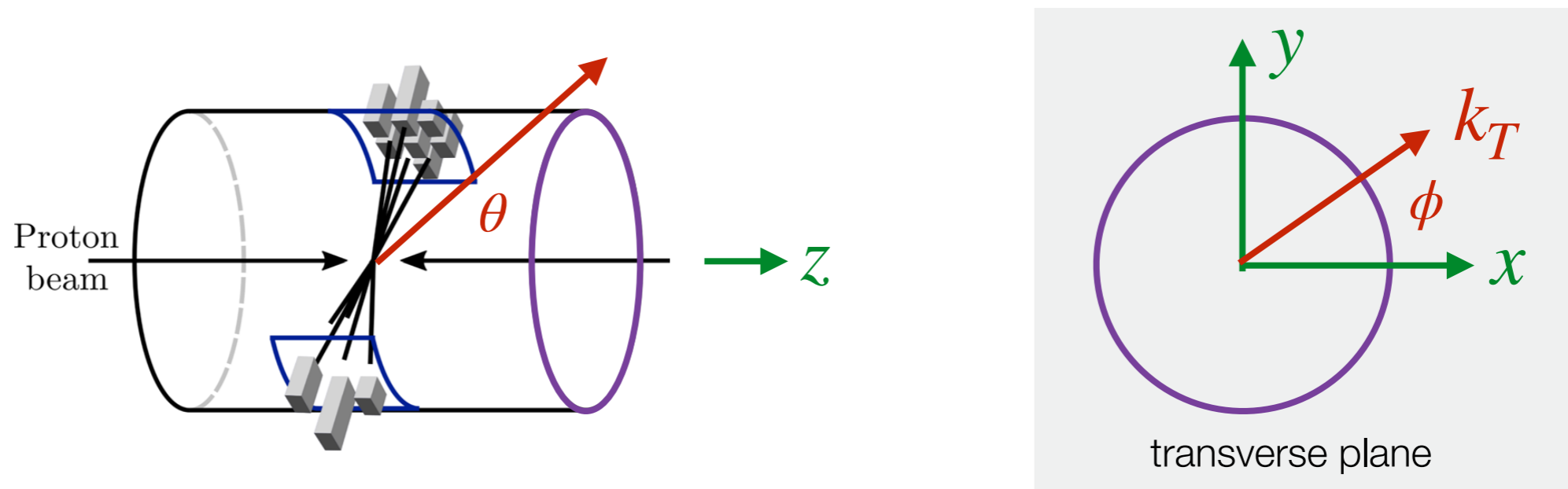
Improved version of the JADE algorithm with distance measure

$$d_{ij} = 2 \min(E_i^2, E_j^2) (1 - \cos \theta_{ij}) / Q^2$$

Modification

- ensures that soft partons are clustered with nearby partons
- if i is softer parton then $d_{ij} \approx E_i^2 \theta_{ij}^2$,
transverse momentum of i relative to particle j

Hadron collider kinematics



Partons (quarks and gluons) of the protons collide with different energies. Lab frame \neq partonic center of mass frame. Use variables invariant under boosts along beam axis:

- Momentum transverse to the beam k_T , azimuthal angle ϕ and rapidity differences Δy

Rapidity

$$y = \frac{1}{2} \ln \left(\frac{E + p_z}{E - p_z} \right)$$

Pseudo-rapidity

$$\eta = \frac{1}{2} \ln \left(\frac{1 + \cos \theta}{1 - \cos \theta} \right)$$

massless particles:
 $y = \eta$

k_T algorithm for hadron colliders

Catani et al. '93; Ellis and Soper '93

Distance measure

$$d_{ij} = \min(k_{Ti}^{2p}, k_{Tj}^{2p}) \frac{\Delta R_{ij}^2}{R^2}$$

$$d_{iB} = k_{Ti}^{2p}$$

distance to beam

with angular distance

$$\Delta R_{ij}^2 = (y_i - y_j)^2 + (\phi_i - \phi_j)^2$$

- Parameter R is the “jet radius”
- k_T algorithm: $p = 1$; C/A algorithm: $p = 0$

cluster soft into nearby

“Cambridge/Aachen” cluster solely based on angle

Clustering sequence for hadron collider algorithms

1. Compute beam distance d_{iB} and distance d_{ij} for all pairs
2. If minimum is d_{ij} then recombine, go to step 1
3. If minimum is d_{iB} then i declare i a jet and remove it from list

Inclusive algorithm: all particles are clustered into jets and many jets have very low k_T

- Hard jets selected by imposing minimum k_T^{\min} on jets
- Exclusive n -jet samples by vetoing additional jets above k_T^{\min}

anti- k_T algorithm

Cacciari, Salam, Soyez '08; > 11'000 citations

Experimentally, k_T and C/A jets were unpopular, because the jets had irregular shapes.

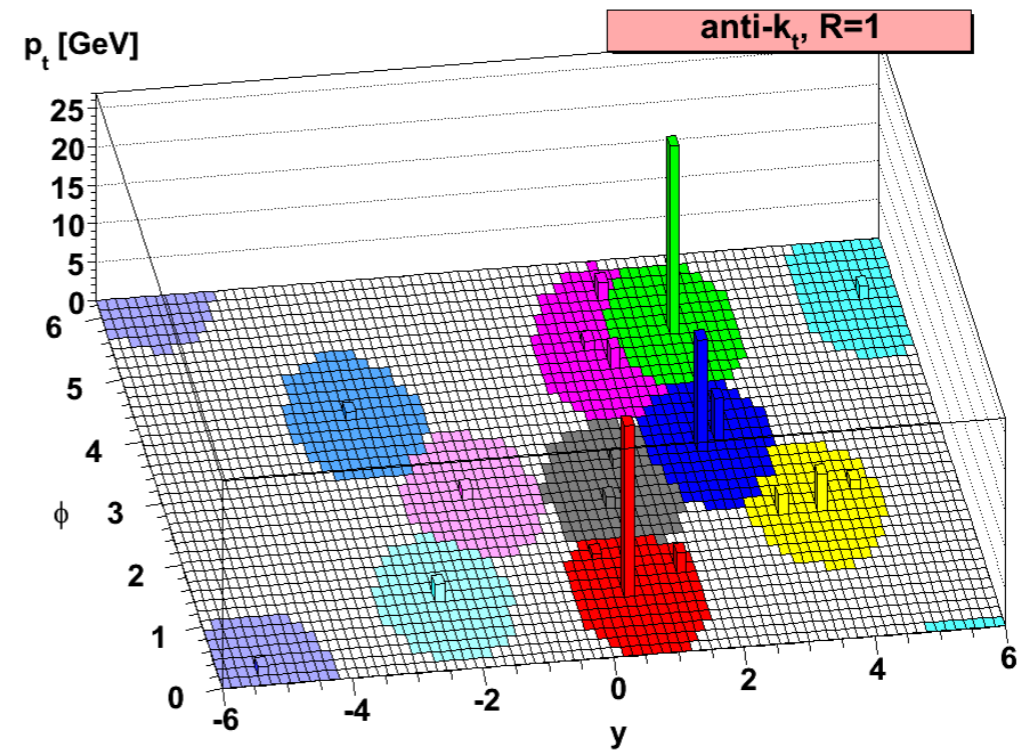
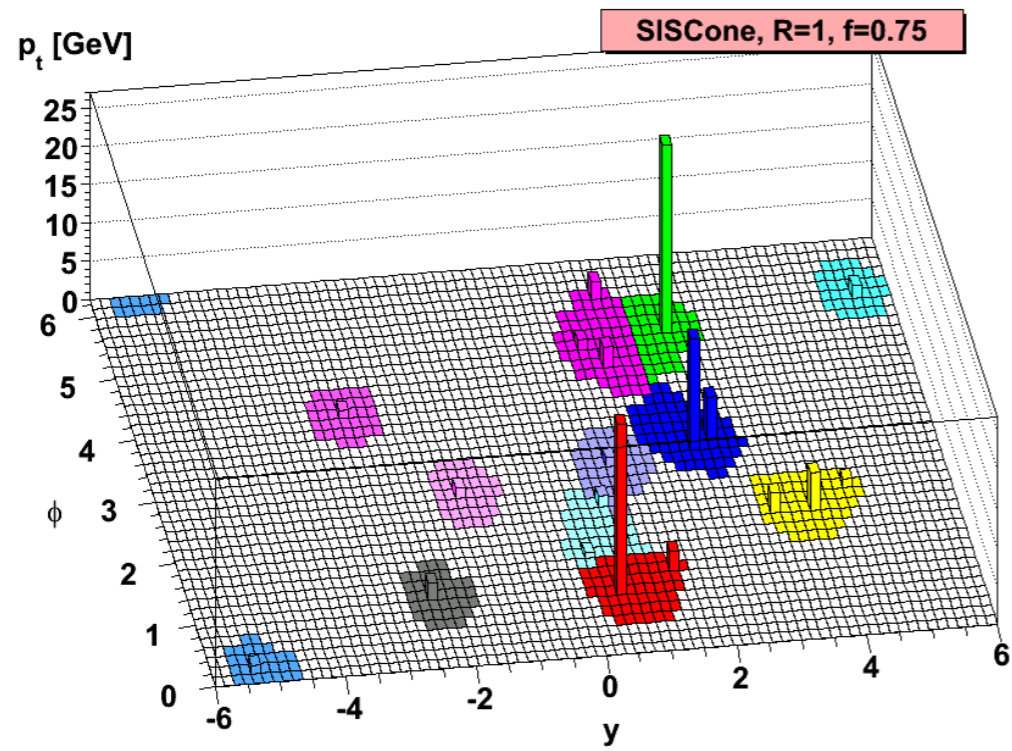
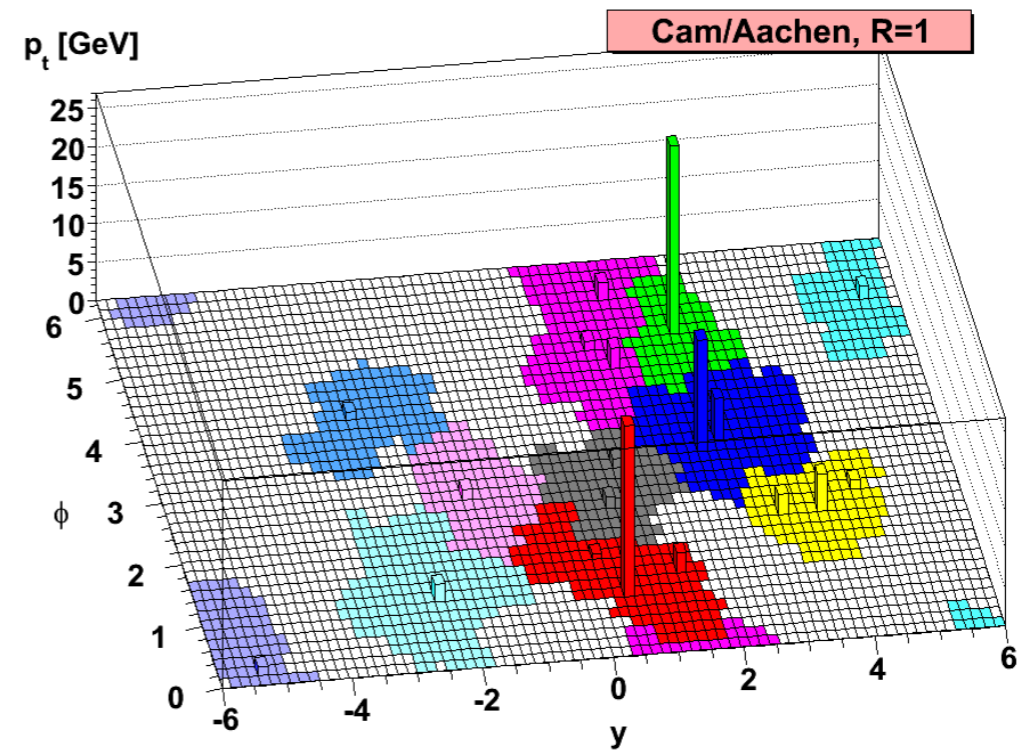
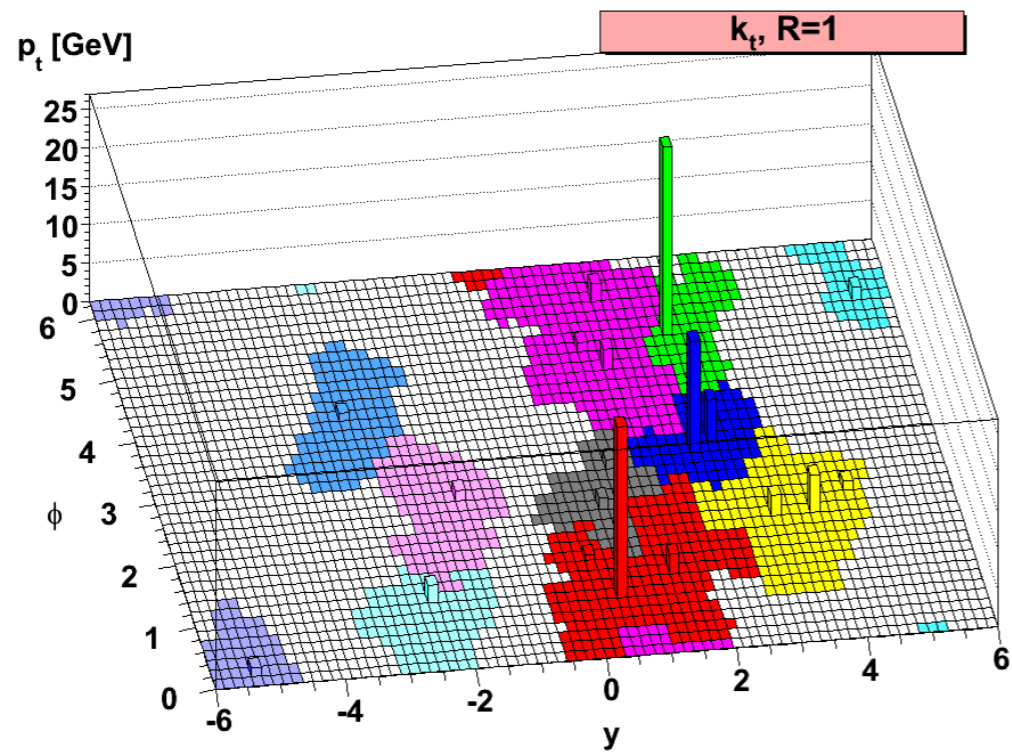
Problem is solved by setting $p = -1$ (anti- k_T algorithm)

$$d_{ij} = \min(k_{Ti}^{-2}, k_{Tj}^{-2}) \frac{\Delta R_{ij}^2}{R^2} \quad \text{and} \quad d_{iB} = k_{Ti}^{-2}$$

Reverses clustering sequence:

- start with hardest parton, cluster nearby softer particles into it

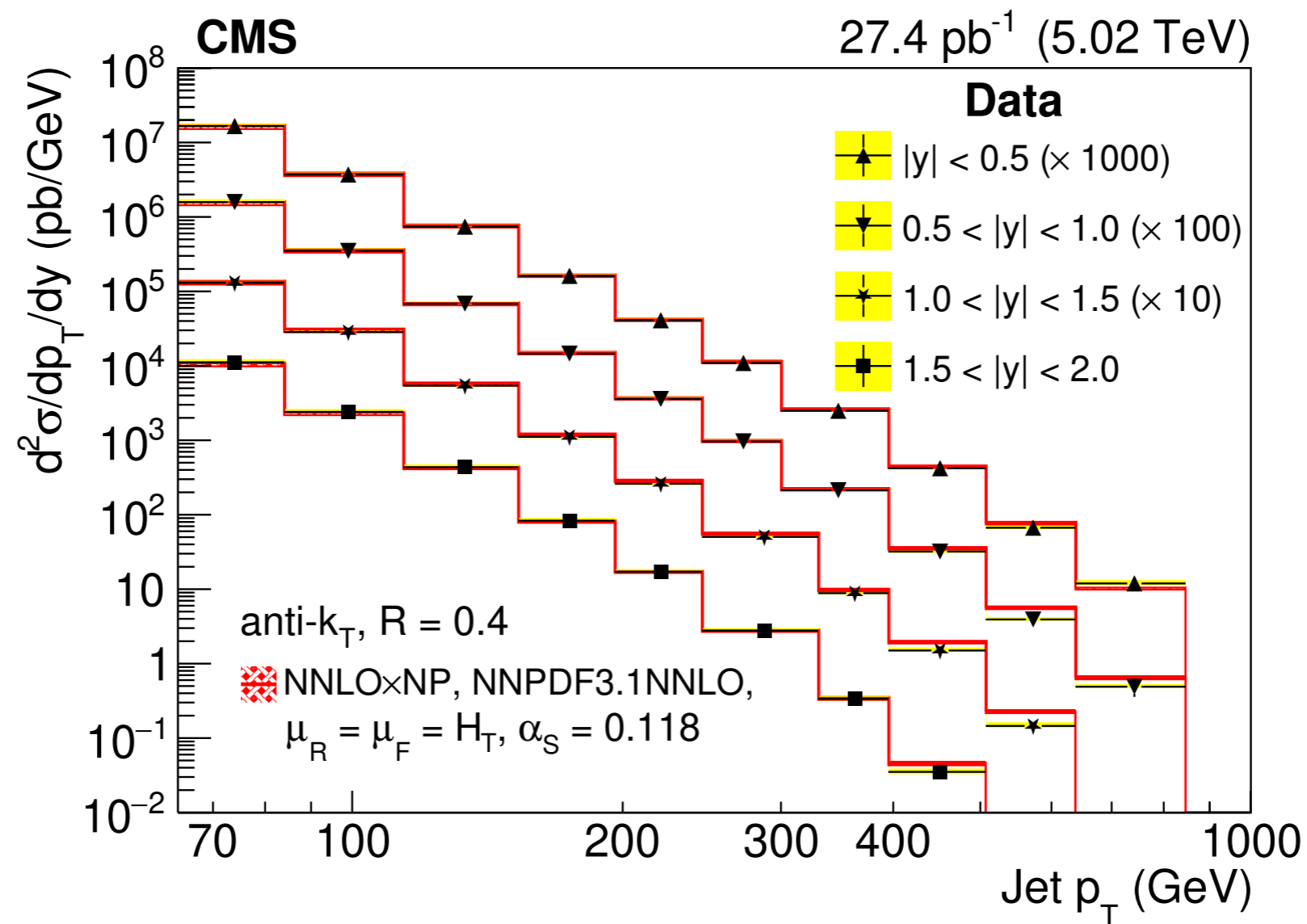
and leads to very cone-like jets! **Default LHC algorithm.**



parton shower event + many additional very soft partons

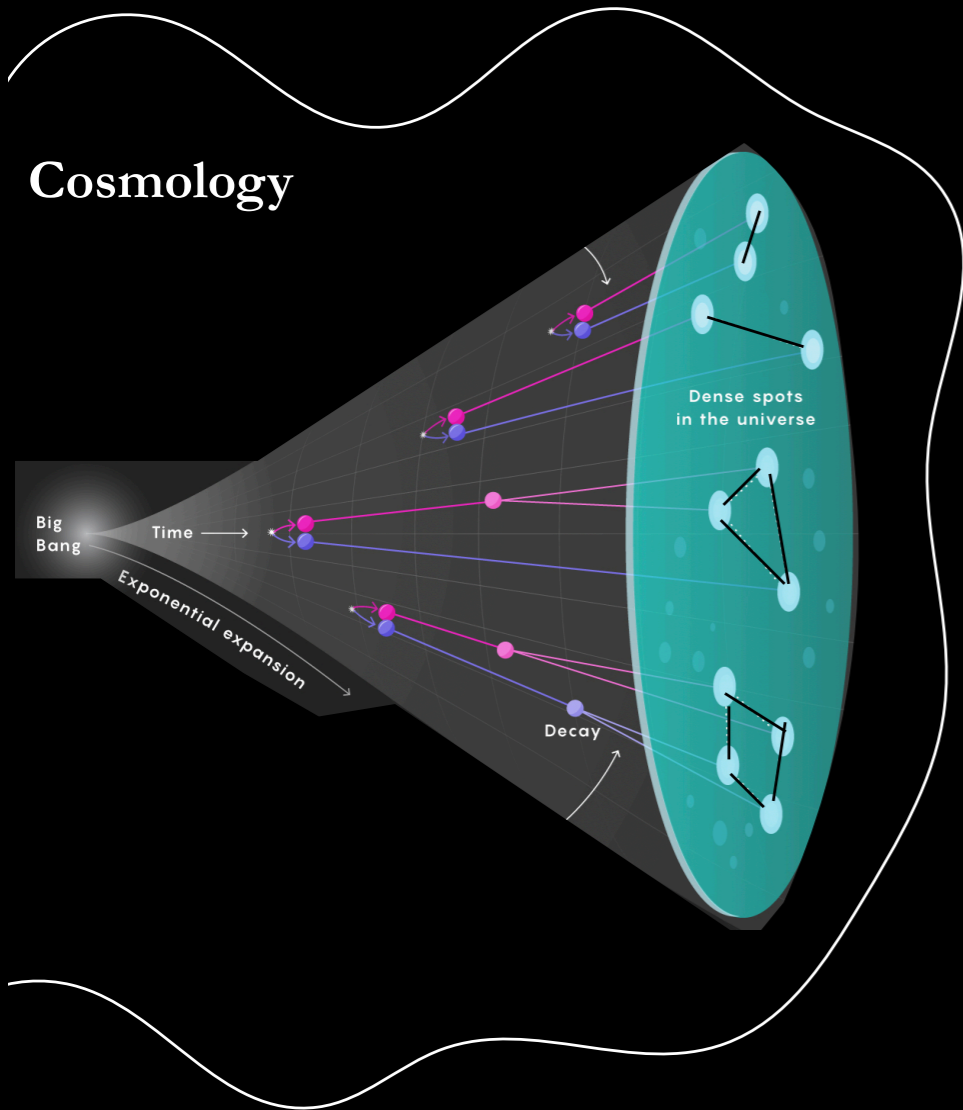
Cacciari, Salam, Soyez '08

Inclusive jet cross section $pp \rightarrow \text{jet} + X$



- Plot shows p_T and rapidity y of leading jet.
- NNLO theory prediction needs PDFs (see next lecture), nonperturbative (NP) effects estimated by parton shower

Cosmology



High Energy Collider

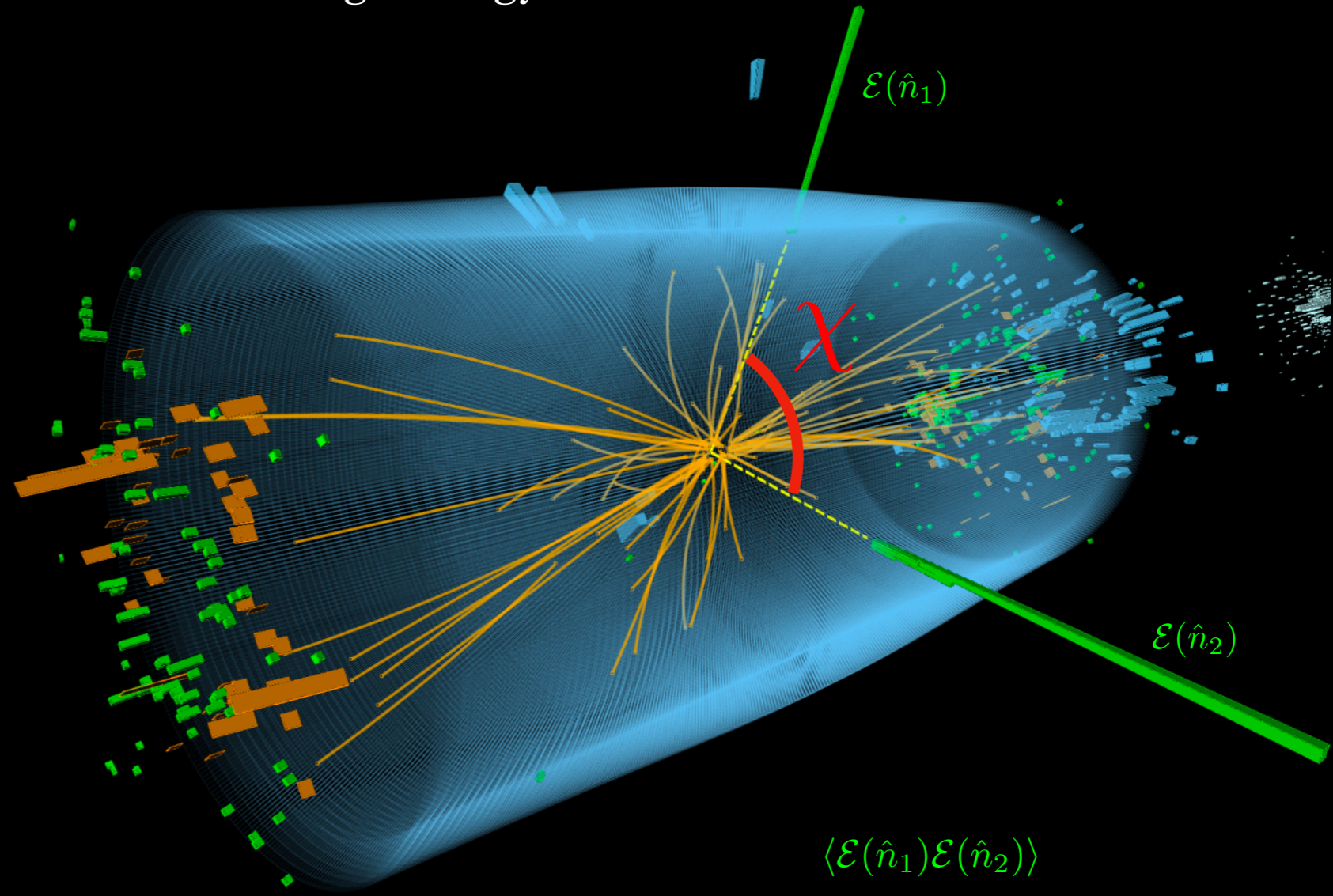
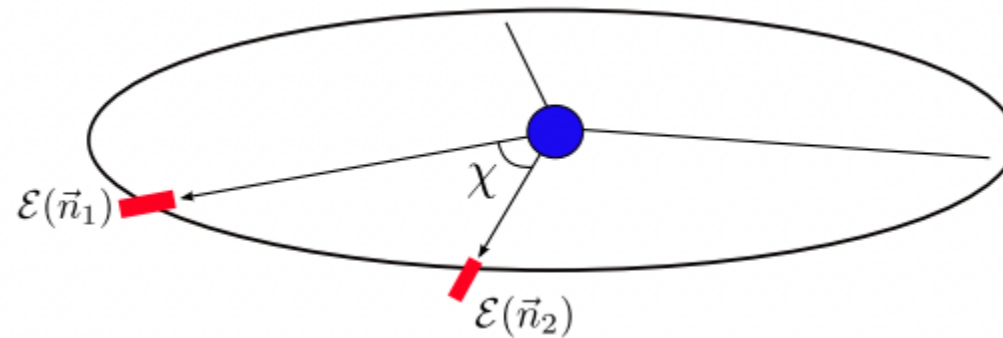


illustration from Kyle Lee

Energy-Energy Correlators (EECs)



Matrix elements

Energy-flow operator

$$\langle \Psi | \mathcal{E}(\hat{n}_1) \cdots \mathcal{E}(\hat{n}_k) | \Psi \rangle \quad \text{with} \quad \mathcal{E}(\hat{n}) = \int_0^\infty dt \lim_{r \rightarrow \infty} r^2 n^i T_{0i}(t, r\hat{n})$$

Sveshnikov, Tkachov '95

characterize **energy flow into the detector**

A lot of new interesting developments in using these energy-energy correlators to study jet substructure, determine α_s and m_t , ...

Correlators have many good properties

- weighted by energy: insensitive to soft radiation:
- factorization, light-ray OPE, CFT techniques Hofman, Maldacena '08

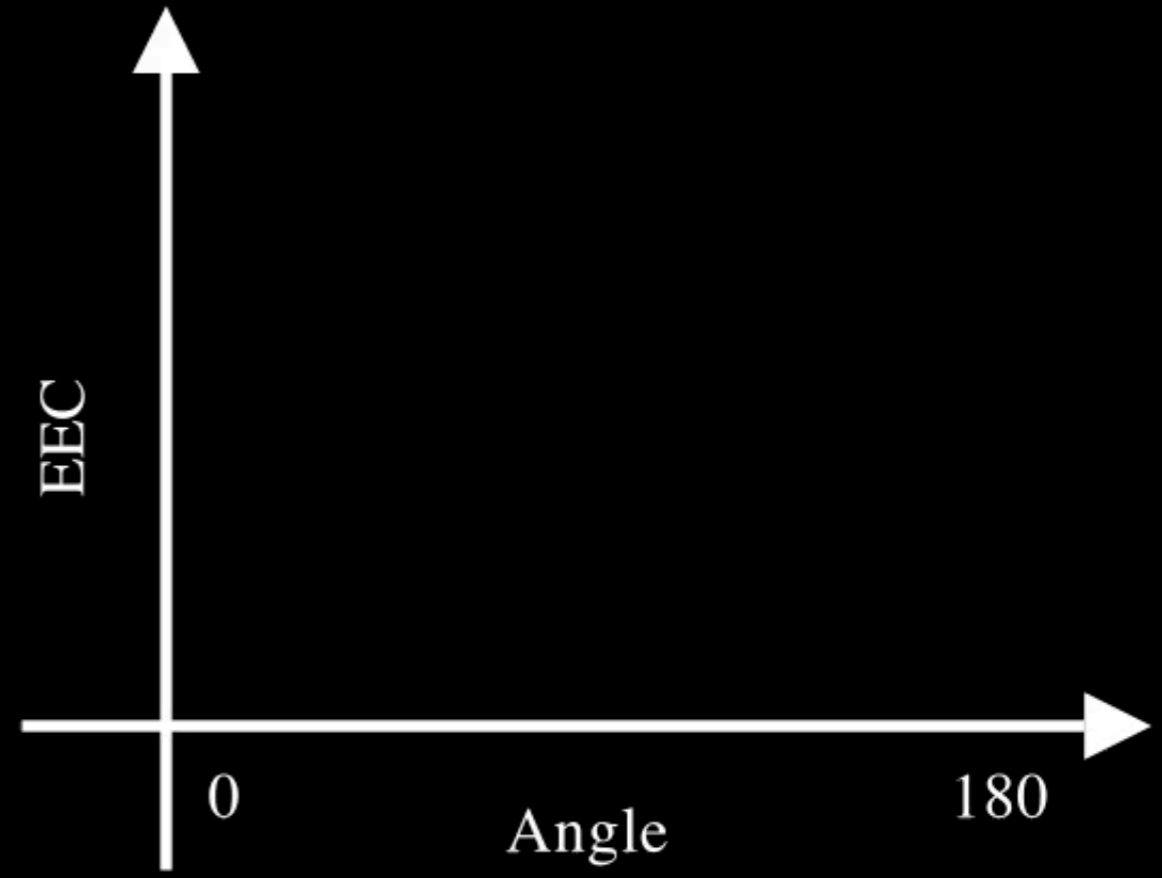
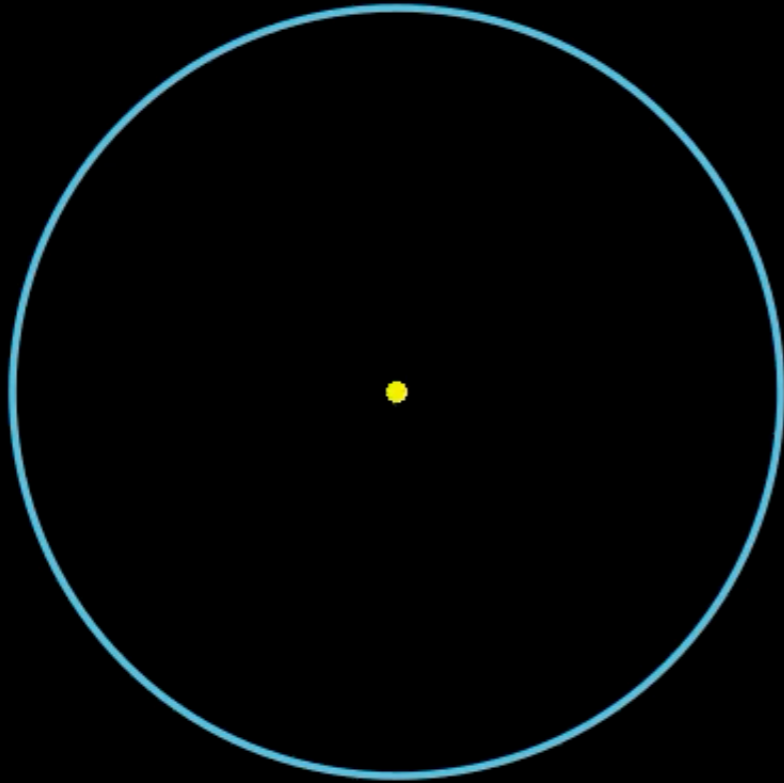
2-point EEC

Simplest correlator is two-point function

$$\text{EEC}(\chi) = \sum_{a,b} \int d\sigma_{e^+e^- \rightarrow a+b+X} \frac{E_a E_b}{Q^2} \delta(\cos \chi_{ab} - \cos \chi)$$

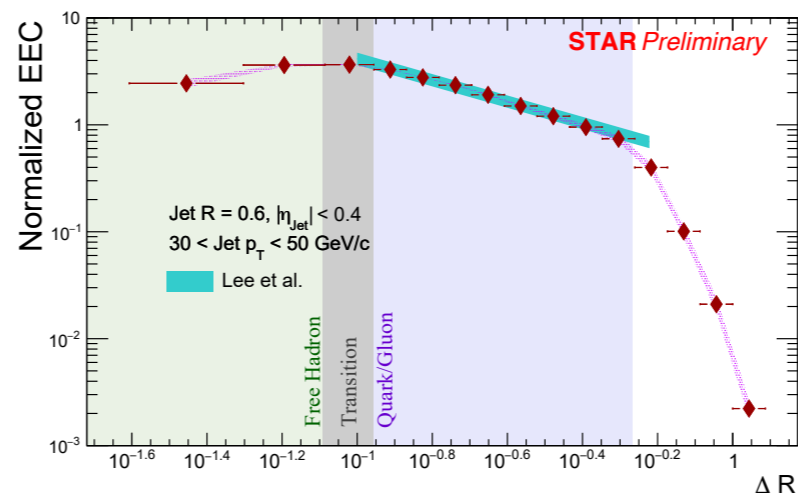
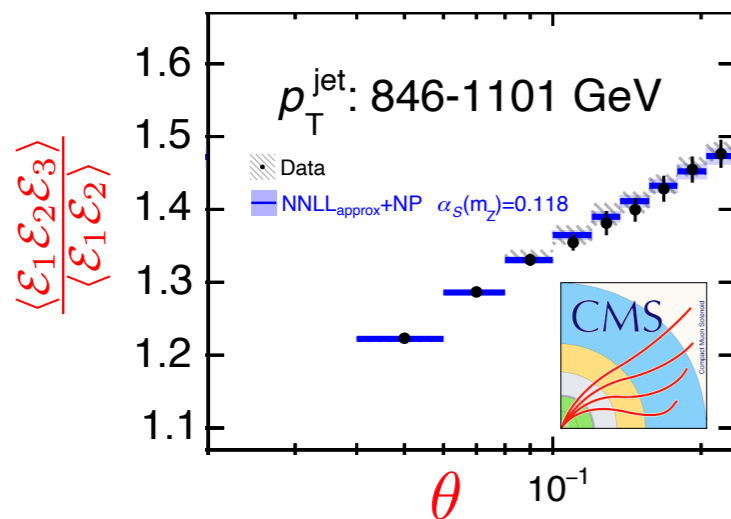
Basham, Brown, Ellis, Love '78

- Record intermediate angle χ between pairs of particles a and b , and put product $E_a E_b$ of their energies into χ histogram.
- In contrast to event-shapes and jets, each event has multiple entries into histogram!

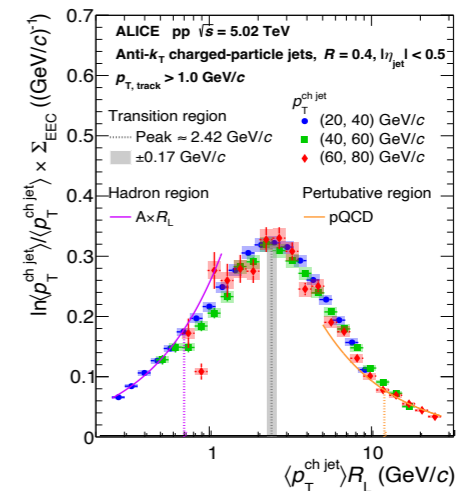


Credit: Hua Xing Zhu

EEC measurements at LHC



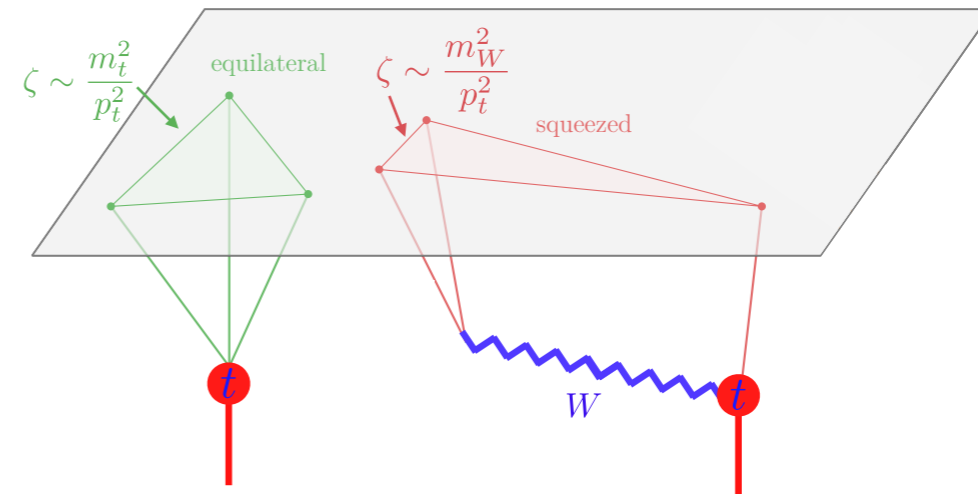
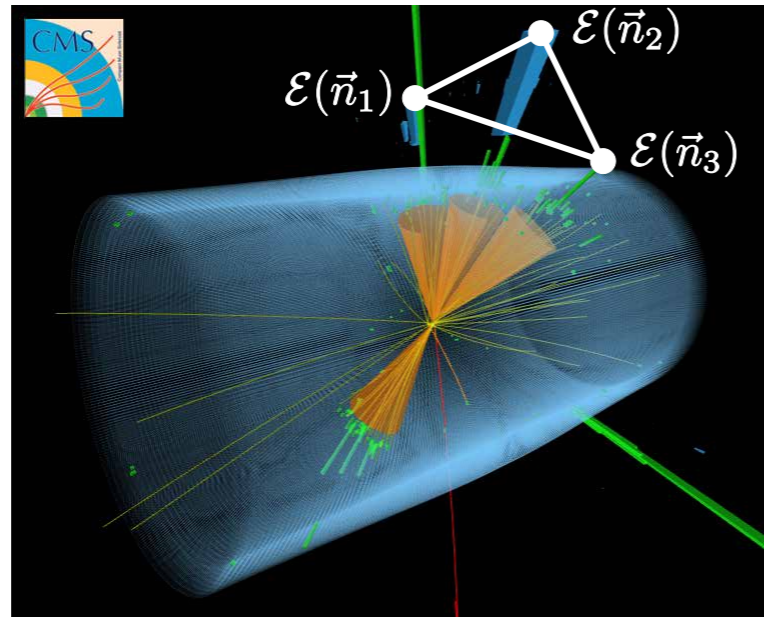
NLL: Lee, Mecaj, Mout '22



- Now many measurements of **transverse EECs** within jets at hadron colliders (ALICE, ATLAS, CMS, STAR).
- Large angles: perturbative. Very small angles: hadronisation
- CMS α_s determination based prediction with resummation [Chen, Gao, Li, Xu, Zhang, Zhu '23](#)

$$\alpha_s(M_Z) = 0.1229^{+0.0014}_{-0.0012} \text{ (stat)}^{+0.0030}_{-0.0033} \text{ (theo)}^{+0.0023}_{-0.0036} \text{ (exp)}$$

Jet substructure from EECs



Top quark jets have substructure from top decay

$$t \rightarrow W^+ + b \quad \text{and} \quad W^- \rightarrow u\bar{d}$$

Proposals to extract ratio m_t/m_W from 3-point correlator in top decays [Holguin, Moulton, Pathak, Procura, Schöfbeck, Schwarz '23, '24](#); [Xiao, Ye, Zhu '24](#)

QCD made simple(r)

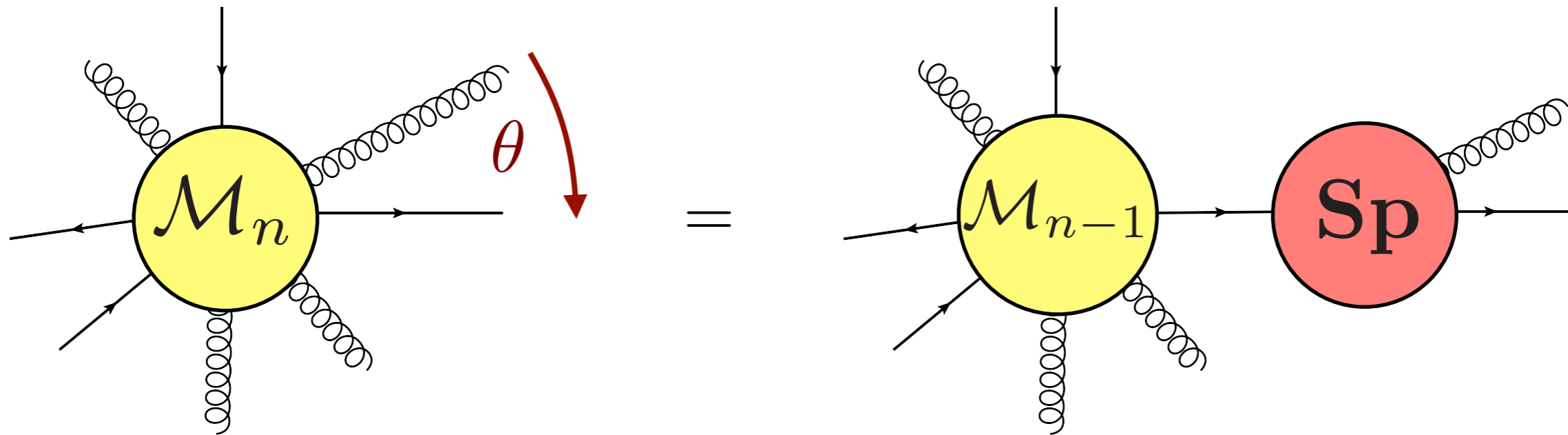
The perturbative expressions for the scattering of quarks and gluons simplify considerably in the

- **Collinear limit**, where multiple particles move in a similar direction.
- **Soft limit**, in which particles with small energy and momentum are emitted.

Cross sections are enhanced

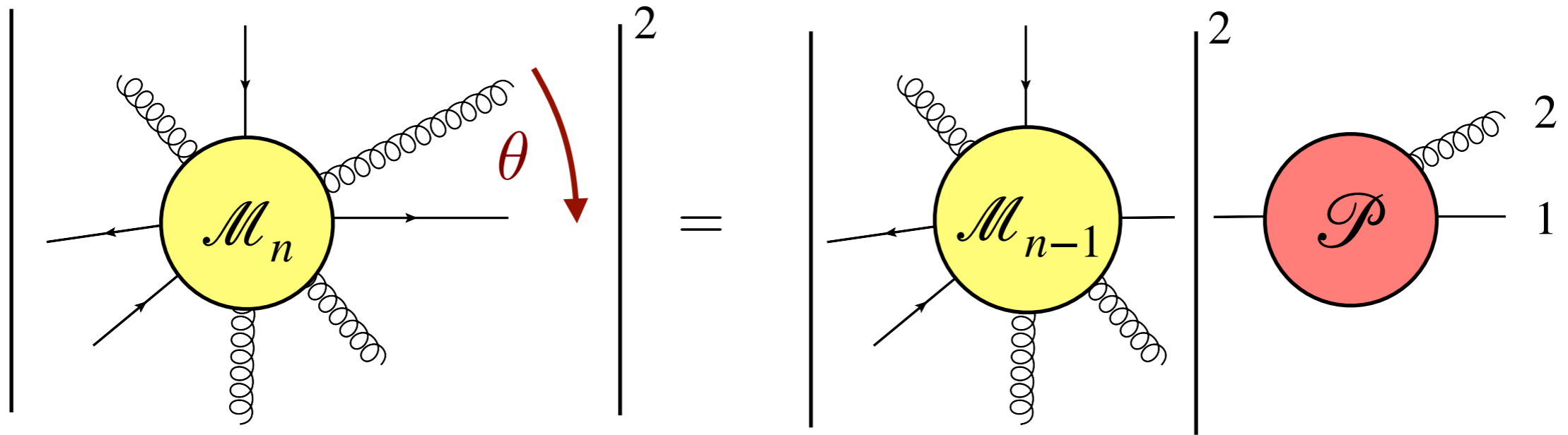
- **IR singularities** cancel for IR safe observables, but
- induce **large logarithms** (see e.g. thrust, SW-jets) which should be resummed to all orders.

Collinear limit



In the limit $\theta \rightarrow 0$, where the partons become collinear, the n -parton amplitude factorizes into a product of an $(n - 1)$ -parton amplitude times a splitting amplitude **Sp**.

Collinear limit



Factorization is particularly simple, if we square the amplitude and sum over spins

$$|\mathcal{M}_n(p_1, p_2, \dots, p_n)|^2 = \frac{g_s^2}{p_1 \cdot p_2} \mathcal{P}_{P \rightarrow 1+2}(z) |\mathcal{M}_{n-1}(P, \dots, p_n)|^2$$

splitting functions

Collinear kinematics: $p_1 \approx zP$ and $p_2 \approx (1-z)P$
with momentum fraction $0 < z < 1$

The splitting functions

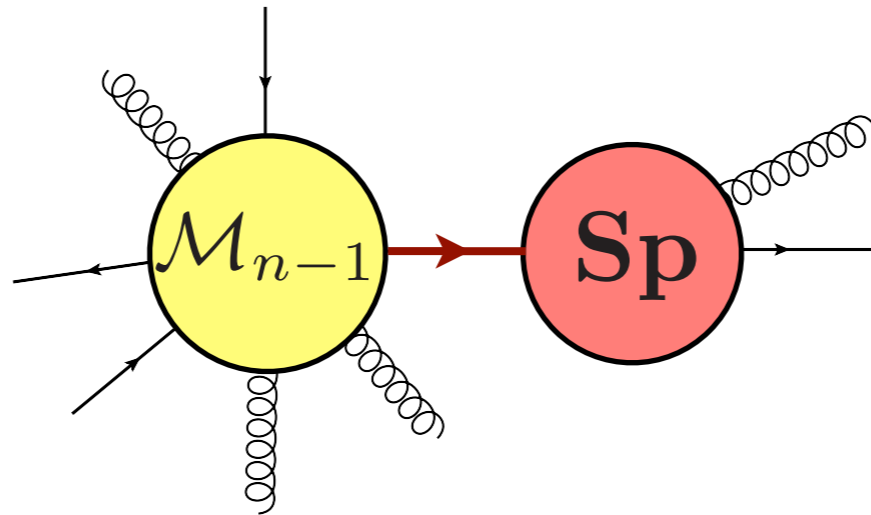
$$\mathcal{P}_{q \rightarrow q+g}(z) = C_F \left[\frac{1+z^2}{1-z} \right]$$

$$\mathcal{P}_{g \rightarrow \bar{q}+q}(z) = T_F \left[1 - 2z(1-z) \right]$$

$$\mathcal{P}_{g \rightarrow g+g}(z) = 2C_A \left[\frac{z}{1-z} + \frac{1-z}{z} + z(1-z) \right]$$

play an important role in QCD, e.g. in PDF evolution and in parton showers (next lecture). Short-hand notation

$$\mathcal{P}_{a \rightarrow b}(z) \quad \text{for} \quad \mathcal{P}_{a \rightarrow b+c}(z)$$



The splitting amplitude diverges as $\theta \rightarrow 0$ and the factorization holds up to regular terms

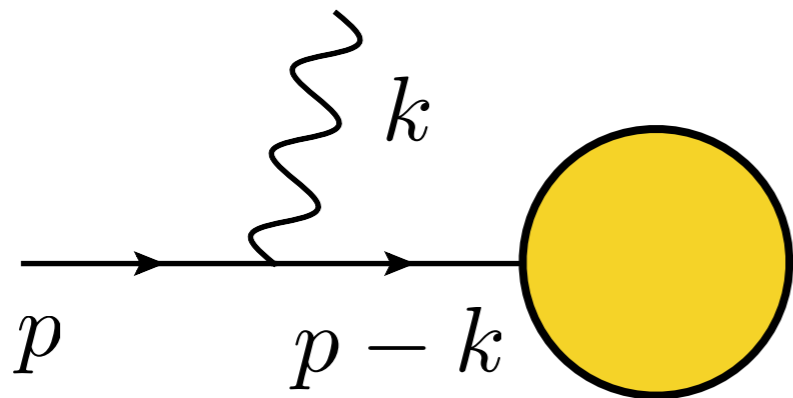
For the cross section, one finds

$$d\sigma_n \sim d\sigma_{n-1} \frac{d\theta}{\theta} \frac{dE_g}{E_g} d\phi$$

Logarithmic enhancements at **small angle**, and also at **small gluon energy**. No interference!

Soft limit

Also when particles with small energy and momentum are emitted, the amplitudes simplify:



$$\dots \frac{\not{p} - \not{k} + m}{(p - k)^2 - m^2} \gamma_\mu u(p)$$
$$\approx \dots u(p) \frac{p_\mu}{p \cdot k}$$

Soft emission factors from the rest of the amplitude.

$p \cdot k = E \omega (1 - \cos \theta)$ in denominator leads to logarithmic enhancements at small energy and small angle.

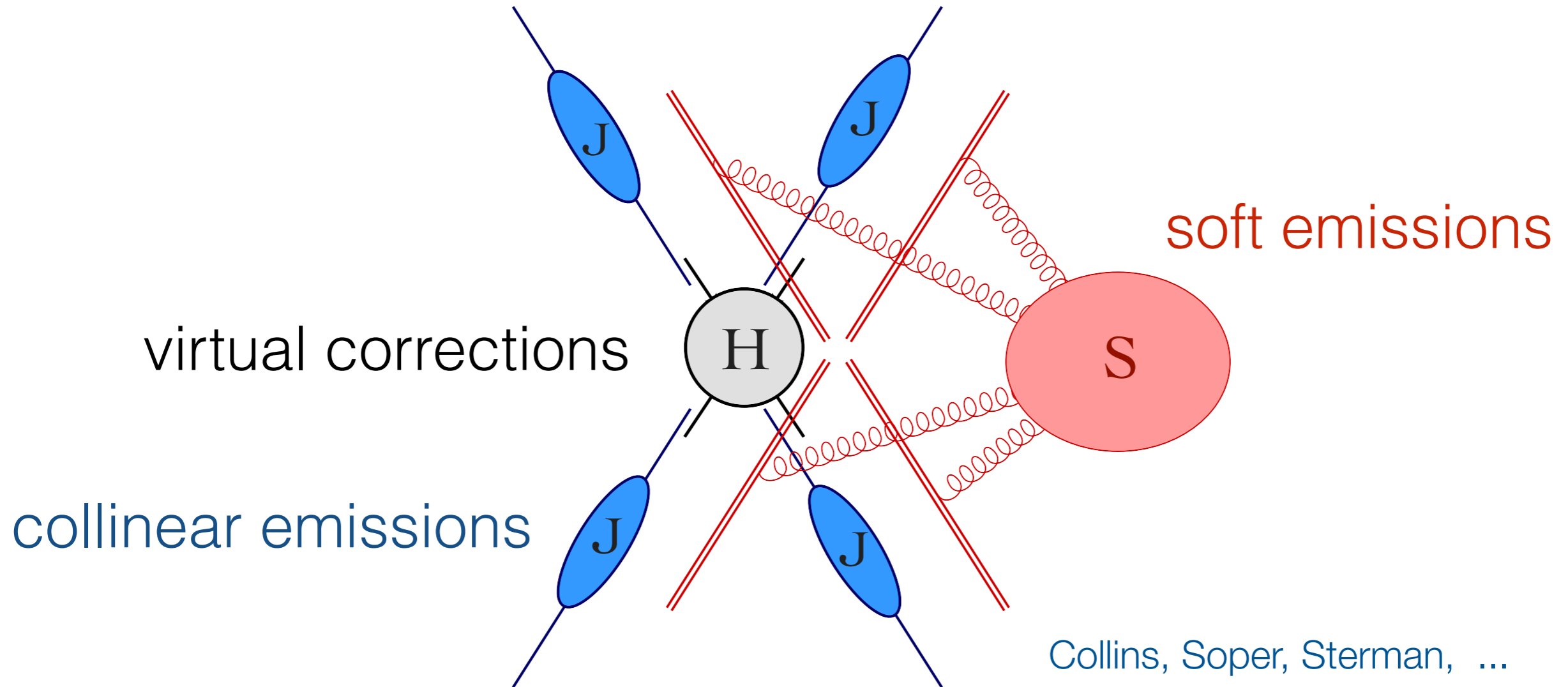
The cross section for the emission of one gluon is

$$d\sigma_{n+1}^{\text{soft}} = \frac{\alpha_s}{2\pi} \frac{d\omega}{\omega} \frac{d\Omega}{2\pi} \sigma_n \sum_{i,j=1}^n C_{ij} \frac{\omega^2 p_i \cdot p_j}{p_i \cdot k p_j \cdot k}$$

color factor $\sim \mathbf{T}_i \cdot \mathbf{T}_j$

So for massless particles soft emission is a *pure interference effect*, in marked contrast to collinear emissions!

Soft-collinear factorization



Basis for higher-log resummation. More complicated than structure than what's implemented in a parton shower:

- Interference, color structure, spin, loop corrections.

Soft-Collinear Effective Theory (SCET)

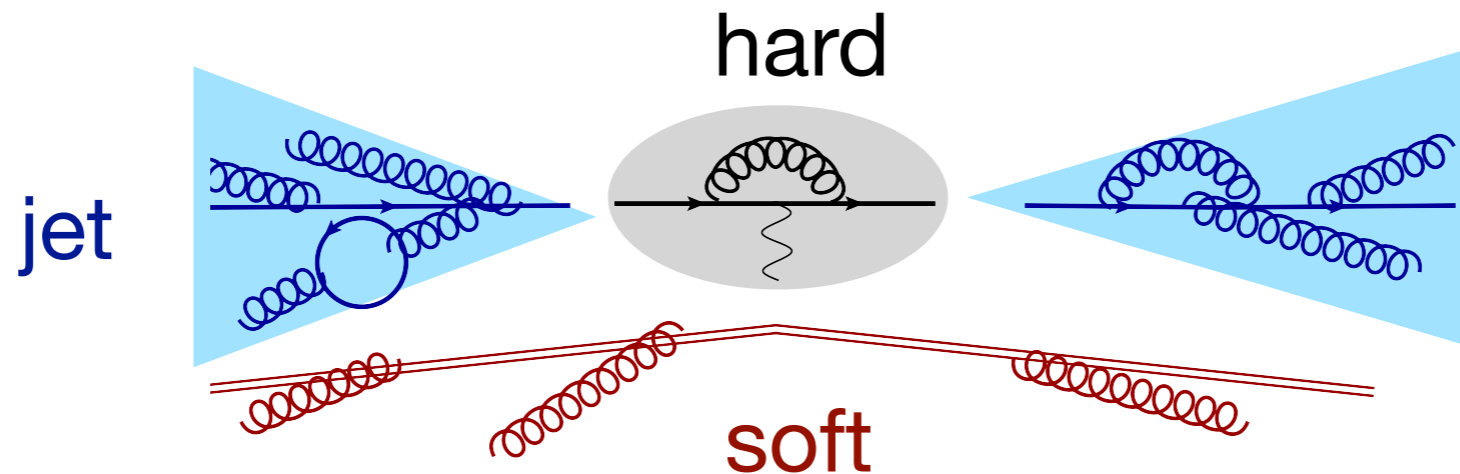
Bauer, Pirjol, Stewart et al. 2001, 2002; Beneke, Diehl et al. 2002; ...

Implements interplay between soft and energetic collinear particles into effective field theory

Hard } high-energy

Collinear *fields* } low-energy part

Soft *fields*



Allows one to analyze **factorization** of cross sections and perform **resummations** of large Sudakov logarithms.

Diagrammatic Factorization

The simple structure of soft and collinear emissions forms the basis of the classic factorization proofs, which were obtained by analyzing Feynman diagrams.

Collins, Soper, Sterman 80's ...

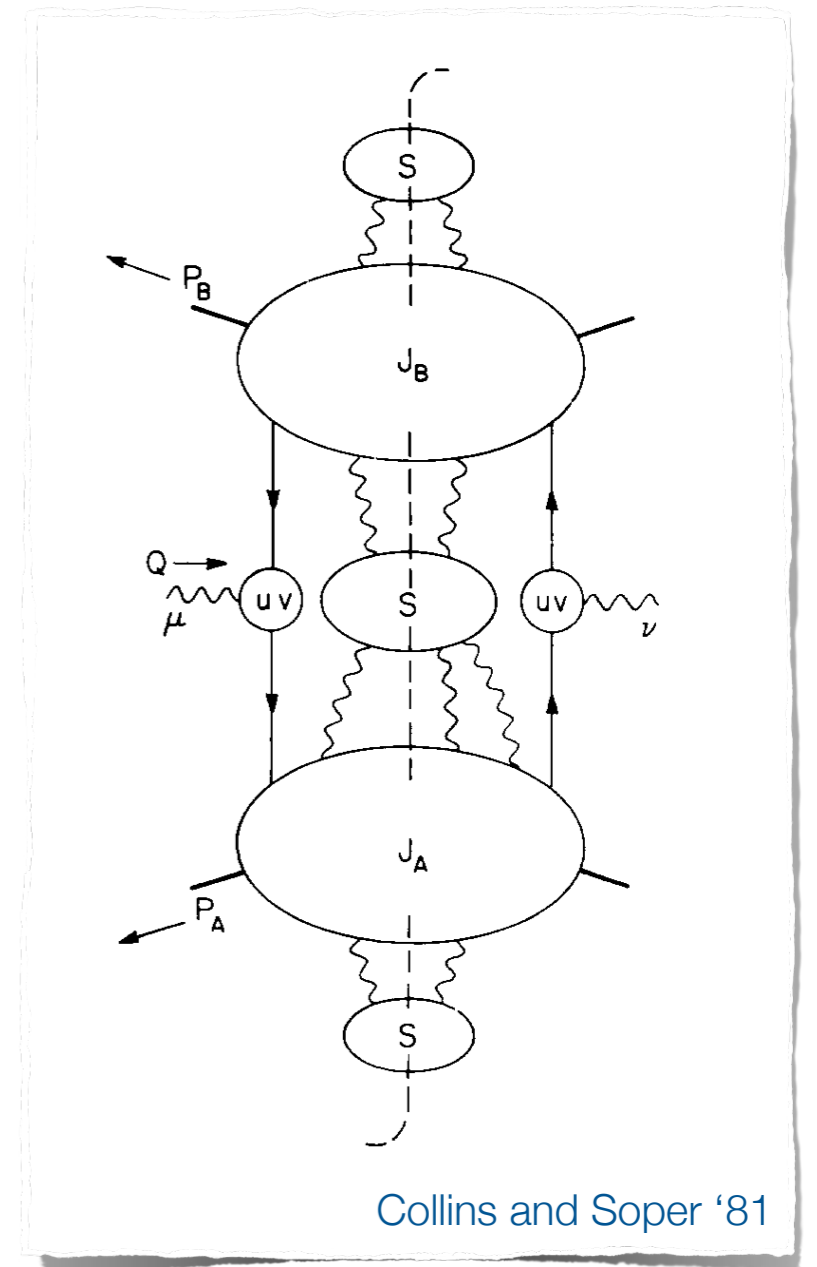
Advantages of the the SCET approach:

Simpler to exploit **gauge invariance** on the Lagrangian level

Operator definitions for the soft and collinear contributions

Resummation with **renormalization group**

Can include **power corrections**



Lecture Notes in Physics 896

Thomas Becher
Alessandro Broggio
Andrea Ferroglia

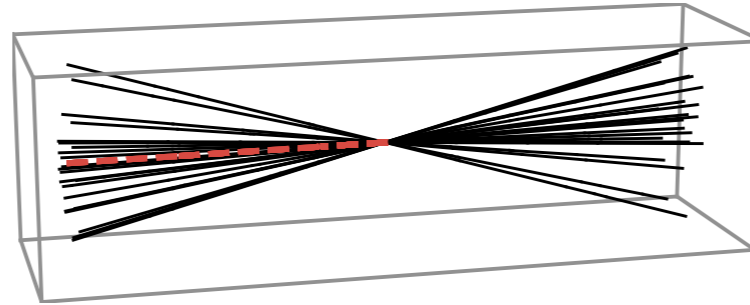
Introduction to Soft-Collinear Effective Theory

 Springer

arXiv:1410.1892

Example: factorization for Thrust

$$T = \max_{\mathbf{n}} \frac{\sum_i |\mathbf{p}_i \cdot \mathbf{n}|}{\sum_i |\mathbf{p}_i|}$$



$$1 - T \approx \frac{M_1^2 + M_2^2}{Q^2}$$

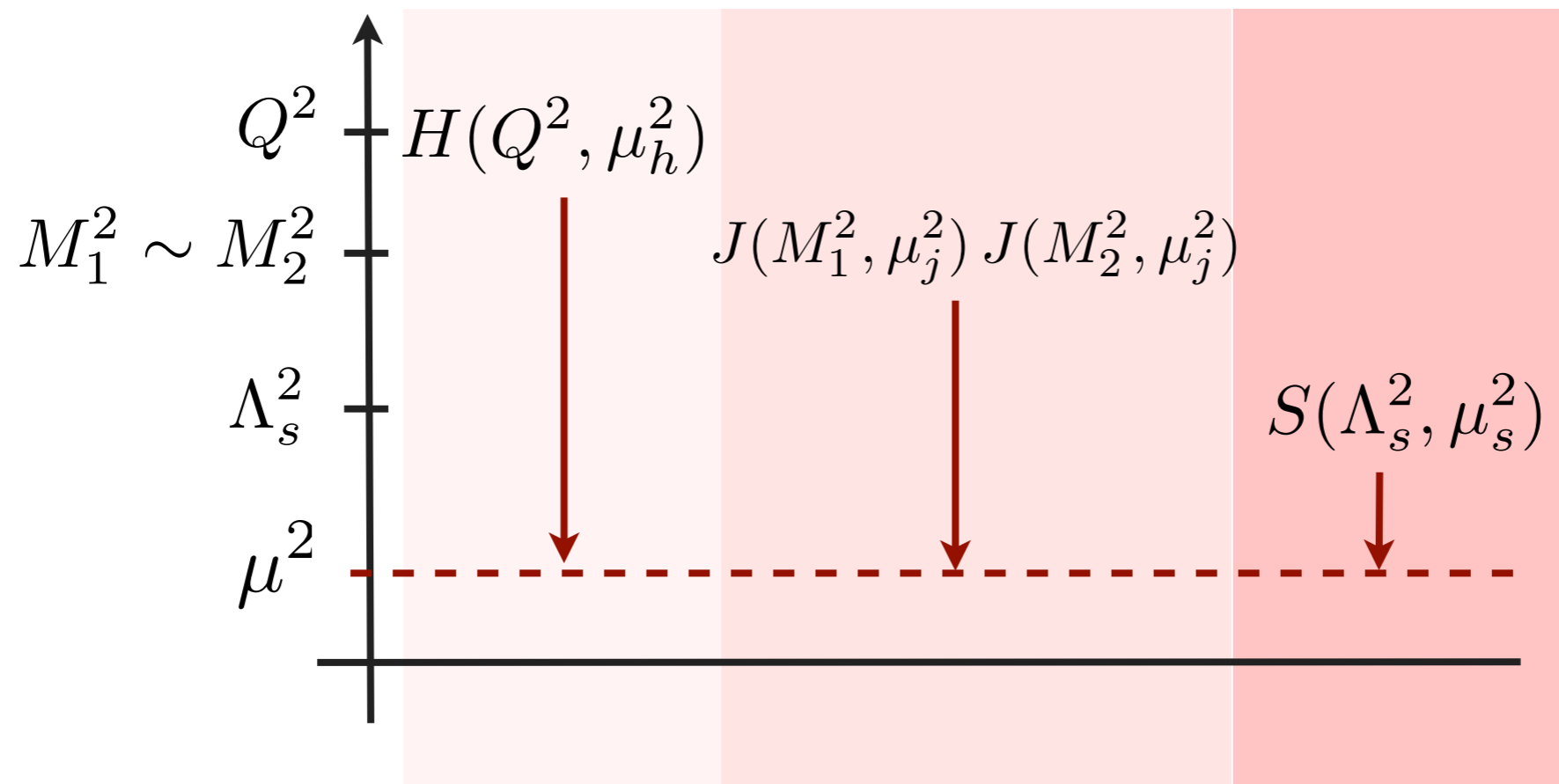
- The perturbative result for the thrust distribution contains logarithms $\alpha_s^2 \ln^{2n}(\tau)$, where $\tau = 1 - T$.
- Near the end-point $\tau \rightarrow 0$ the logarithmic terms dominate.
- Using SCET one can derive a factorization theorem

$$\frac{1}{\sigma_0} \frac{d\sigma}{d\tau} = H(Q^2, \mu) \int dM_1^2 \int dM_2^2 J(M_1^2, \mu) J(M_2^2, \mu) S_T\left(\tau Q - \frac{M_1^2 + M_2^2}{Q}, \mu\right)$$

Scales: Q^2 \gg $M^2 \sim \tau Q^2$ \gg τQ
 hard collinear soft

Resummation by RG evolution

Evaluate each part at its characteristic scale, evolve to common reference scale μ



Each contribution is evaluated at its natural scale. No large perturbative logarithms.

RG-improved perturbation theory

Aside: counting of logarithms

The integrated cross section

$$\Sigma(\tau) = \frac{1}{\sigma} \int_0^\tau d\tau' \frac{d\sigma}{d\tau'}$$

has for low τ an expansion of the form ($L = \ln \tau$)

$$\Sigma(\tau) = 1 + \alpha_s (c_2 L^2 + c_1 L + c_0) + \alpha_s^2 (c_4 L^4 + c_3 L^3 + \dots) + \alpha_s^3 (c_6 L^6 + \dots) + \dots$$

leading logarithms

next-to-leading logarithms

Exponentiation

The resummed cross section has the form

$$\Sigma(\tau) = \exp \left(L g_1(\alpha_s L) + g_2(\alpha_s L) + \alpha_s g_3(\alpha_s L) + \alpha_s^2 g_4(\alpha_s L) + \dots \right)$$

Nontrivial, crucial feature: **only one L per order**

Accuracy:

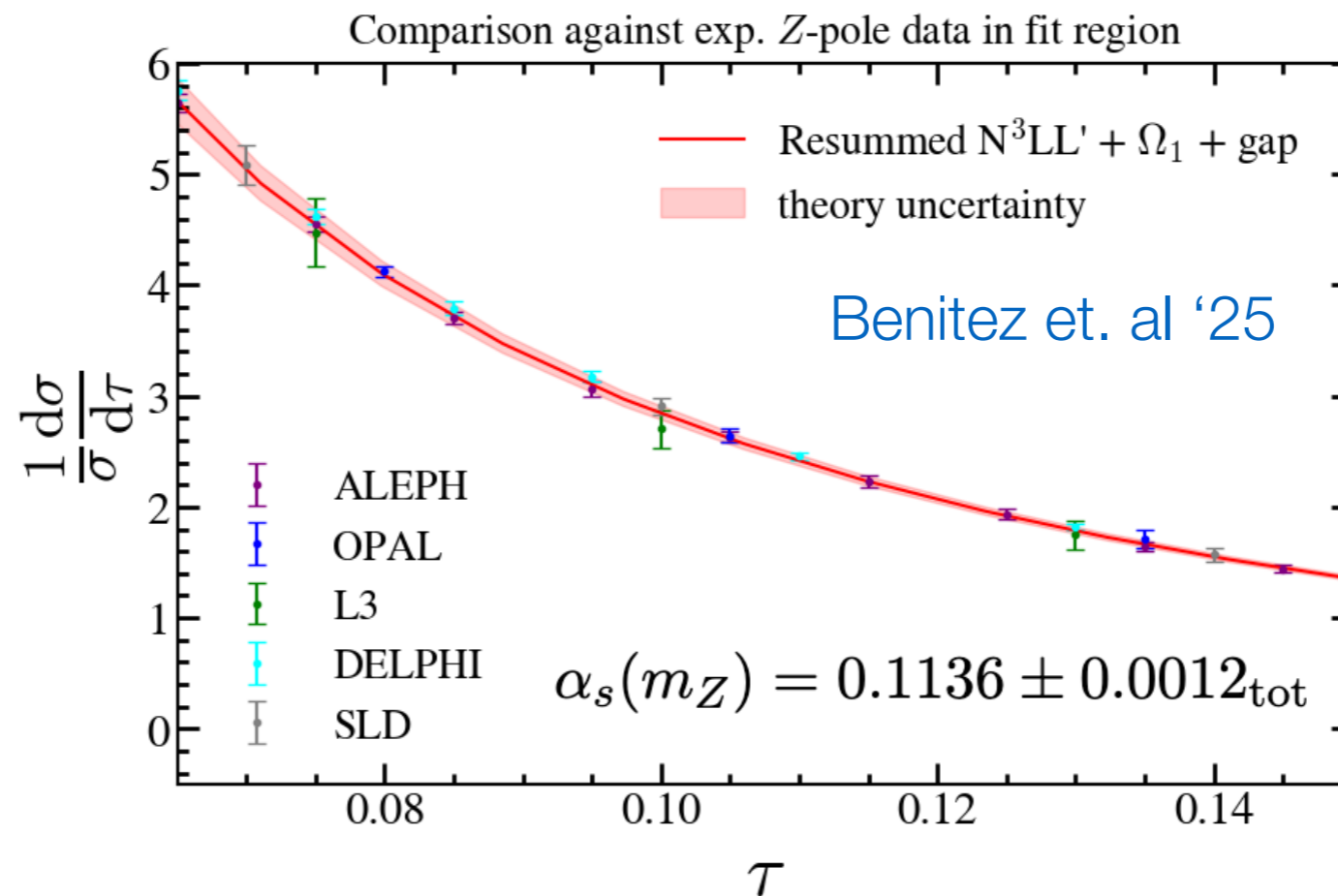
- **LL**: g_1 ; **NLL**: g_1, g_2 ; **NNLL**: g_1, g_2, g_3

Systematics: expand in α_s but count $\alpha_s L$ as $O(1)$

Matching:

N³LL + **NNLO**

logarithms at small τ + fixed order at larger τ

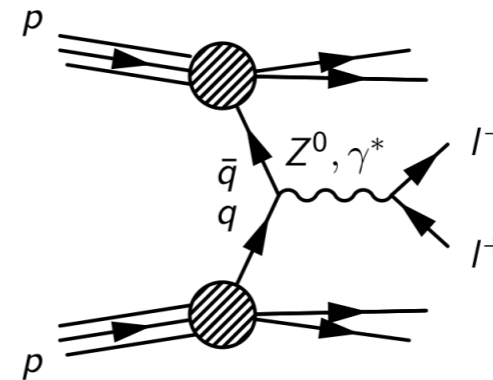
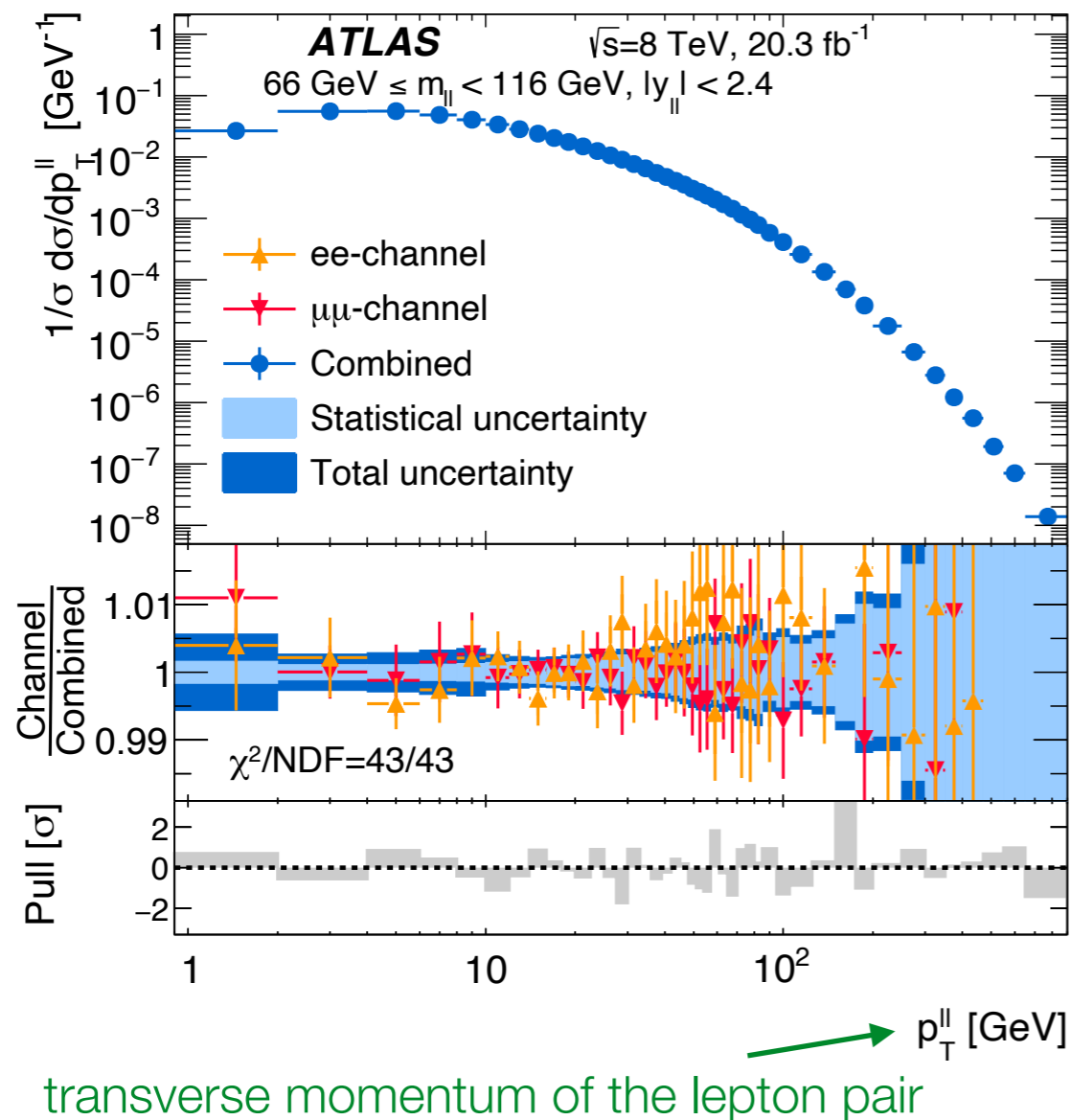


State of the art theoretical predictions for thrust include

- NNLO fixed order + resummation up to N^3LL + fit for hadronisation effects (parameter Ω_1)
- Fit to data gives low α_s in strong tension with world average

Ongoing discussions (see e.g. talks by [Benitez](#), [Ferrera](#) and [Nason](#) at [PSR2025](#) conference) how this can be resolved.

Transverse momentum spectrum in DY

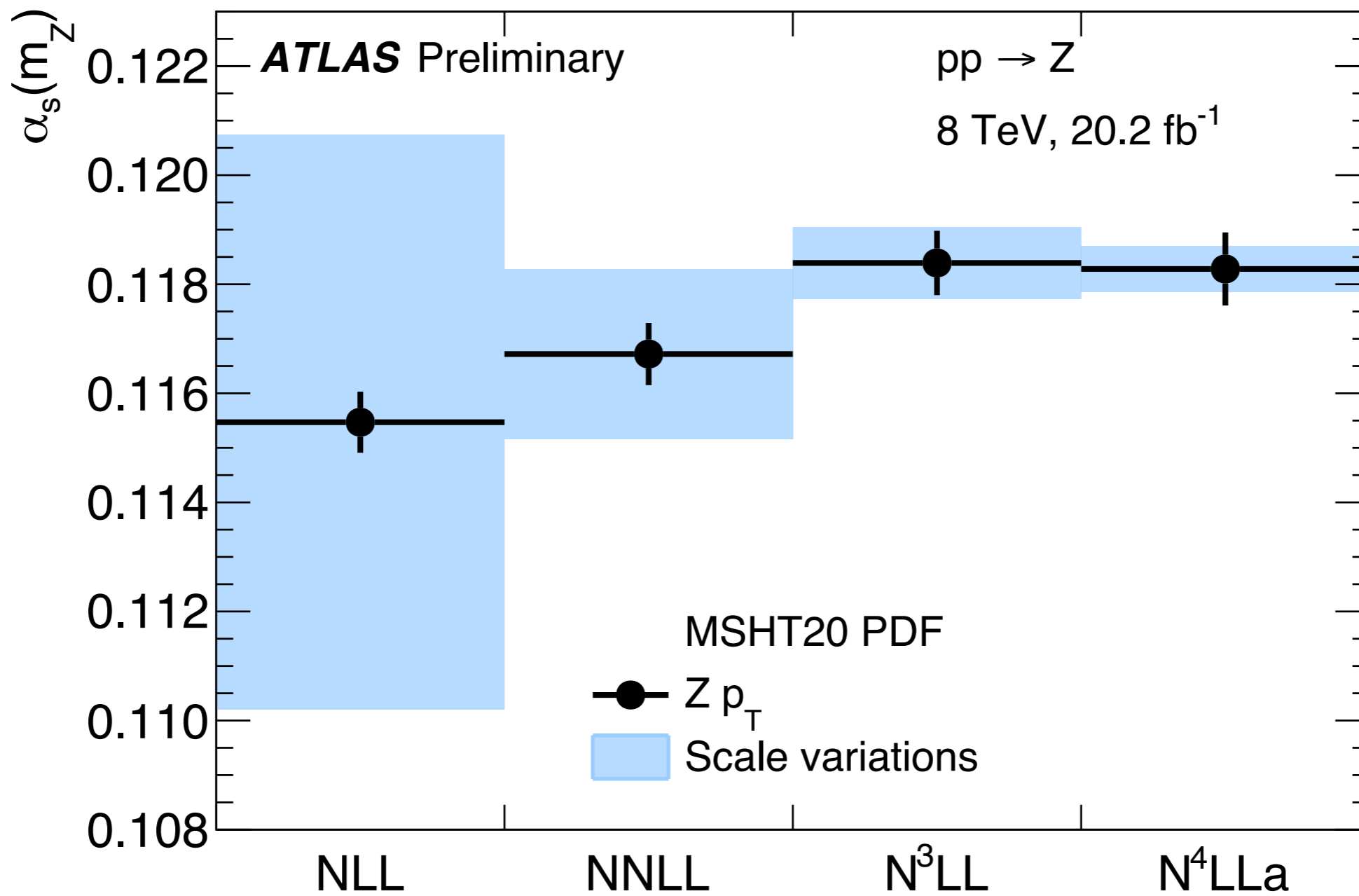


ATLAS 2309.12986 has extracted α_s from a fit to the spectrum. Use

- N³LO fixed order +
- aN⁴LL resummation
- fit for NP effects

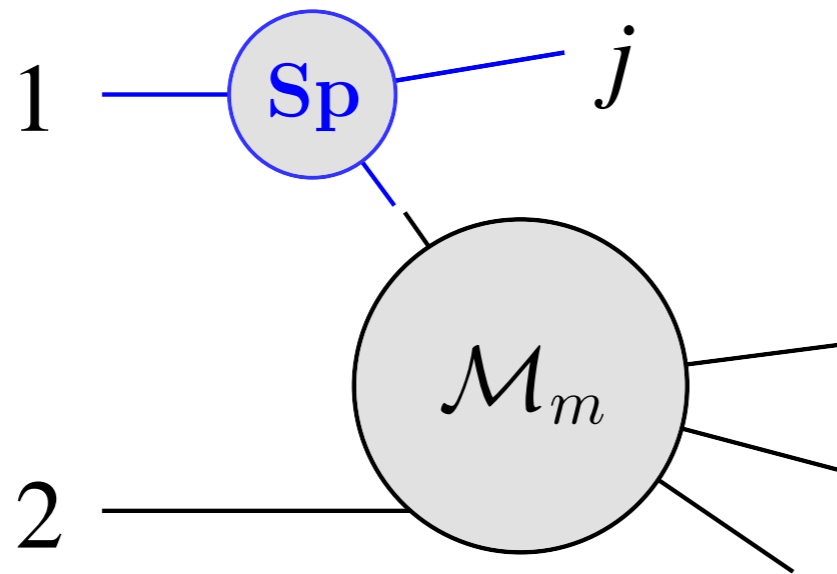
$$\alpha_s(M_Z) = 0.1183 \pm 0.0009$$

Most precise experimental determination of α_s . Agrees well with world average.



Collinear Factorization Violation

Catani, de Florian, Rodrigo '11; Forshaw, Seymour, Siodmok '12



New results for \mathbf{Sp}
Henn, Ma, Xu, Yan, Zhang, Zhu '24
Guan, Herzog, Ma, Mistlberger,
Suresh '24

For space-like collinear limit $1 \parallel j$ the **splitting amplitude \mathbf{Sp}** depends on the colors and directions of the partons not involved in the splitting!

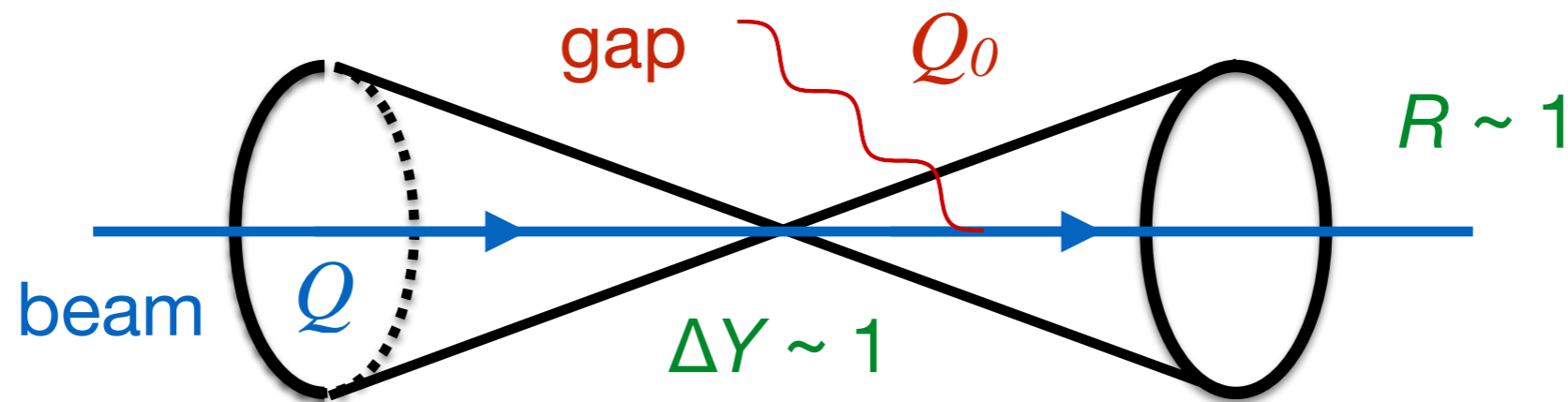
- Related to non-cancellation due to soft phases

Implications for PDF factorization?

Super-Leading Logs (SLLs)

Forshaw, Kyrieleis, Seymour '06 '08

Factorization breaking leads to an interesting effect in gap between jet cross sections



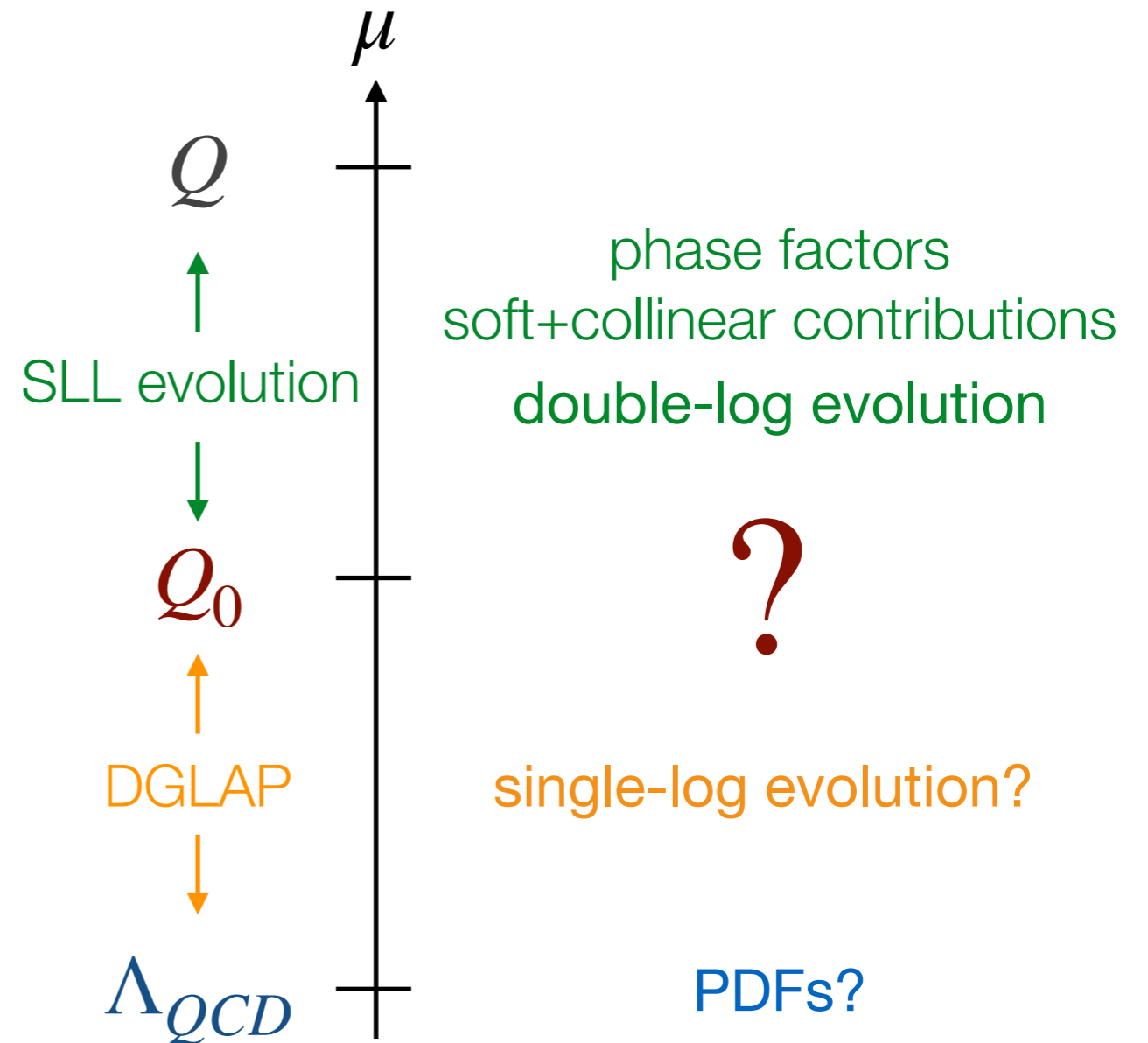
Large logarithms $\alpha_s^n L^m$ with $L = \ln(Q/Q_0)$

- e^+e^- : $m \leq n$, leading logs $m = n$
- pp : $\alpha_s L, \alpha_s^2 L^2, \alpha_s^3 L^3, \alpha_s^4 L^5 \dots, \alpha_s^{3+n} L^{3+2n}$

Resummation can be achieved by solving **double-logarithmic evolution equation**, see Romy's talk!

SLLs vs DGLAP

- Double-logarithmic SLLs directly related to collinear factorization breaking
- SLLs generated from double logarithmic running
- If PDF factorization holds, something interesting must happen at scale Q_0 which converts between the two evolutions



Detailed analysis of SCET low-energy matrix elements at three-loop level reveals **soft-collinear interactions due to Glauber modes** (described by Glauber-SCET Lagrangian Rothstein, Stewart '16).

Collinear factorization
breaking at $\mu = Q$

X

soft-collinear factorization
breaking by Glauber modes
at $\mu = Q_0$

=

PDF factorization
for $\mu < Q_0$

TB, Hager, Jaskiewicz, Neubert, Schwienbacher '24; 2509.07082

Resolves tension between collinear factorization breaking and PDF factorization. **Strong argument that PDF factorization also holds for jet processes**, not only for the DY process as established in the original proof [Collins, Soper and Sterman '85](#).

Fixed-Order Results and Parton Showers

- Monte Carlo techniques
- Fixed-order MCs
- Parton showers

Monte-Carlo integration

Basic principle is to evaluate integrals by random sampling

$$I = \int_0^1 dx f(x) \rightarrow I_N = \frac{1}{N} \sum_{i=1}^N f(z_i)$$

where $z_i \in [0,1]$ are random numbers with flat distribution.

Uncertainty estimate from variance

$$I = I_N \pm \frac{\sigma}{\sqrt{N}} \quad \text{with} \quad \sigma^2 \approx \sigma_N^2 = \frac{1}{N} \sum_{i=1}^N f(z_i)^2 - I_N^2$$

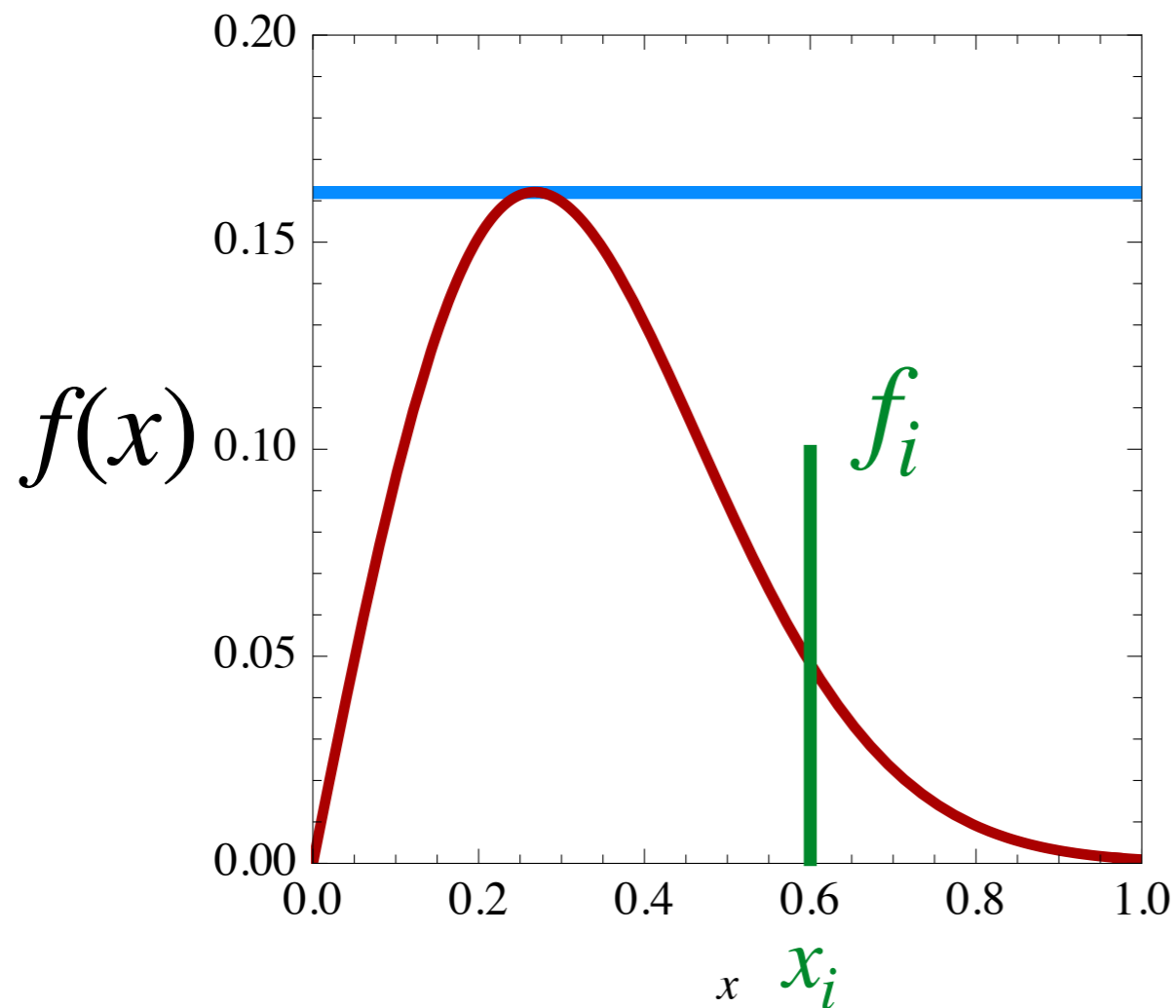
- Scales as $1/\sqrt{N}$; **independent of dimension** of integral
- Minimize variance (variable change) for accurate results
(Exercise: try MC integration for $f(x) = 1/\sqrt{x}$)

Event generator

- MC method is used for phase-space integration. Dimension of integrals is $3n-4$ for n particles
- MC sample point $f(z_i)$ can be viewed a (collider) event with “weight” $w_i = f(z_i)$
- In nature, events have $w_i = 1$. Instead of a large function value $f(z_i)$, we get more events when the cross section is large, fewer when it is small
- Convenient to have a $w_i = 1$ event sample, then event generator behaves like a virtual collider

Unweighting

For a bounded function $0 \leq f(x) \leq f_{\max}$ we can obtain $w_i = 1$ events as follows



1. choose random $x_i \in [0, 1]$
2. choose random $f_i \in [0, f_{\max}]$
3. if $f_i < f(x_i)$ accept event

Fixed-order MC codes

- With appropriate cuts, differential tree-level cross sections are positive and bounded
 - Tree level $w = 1$ event generators
 - $w = 1$ parton showers
- Higher-order partonic cross sections are unbounded and do not have definite sign (negative virtual corrections)
 - Higher-order fixed-order MC codes can not provide $w = 1$ events
 - Only suitable integrals are IR finite and meaningful

Real emission IR singularities

Result for the $q\bar{q}g$ real emission phase space in $d = 4 - 2\varepsilon$ has the form

$$\sigma_{q\bar{q}g} = \int_0^1 dy_1 \int_0^{y_1} dy_2 y_1^{-1-\varepsilon} y_2^{-1-\varepsilon} f(y_1, y_2, \varepsilon) \mathcal{O}(y_1, y_2)$$

where $f(y_1, y_2)$ is regular. For IR safe $\mathcal{O}(y_1, y_2)$, poles in ε in $\sigma_{q\bar{q}g}$ cancel against those in loop corrections to $\sigma_{q\bar{q}}$.

Result in $d = 4 - 2\varepsilon$ is **unsuitable for MC integration!**

Solution:

- Extract IR singularities, combine with virtual.
- MC integral for finite remainder.

Toy integral

Virtual and real correction

$$V = \left(-\frac{1}{\varepsilon} + 2 \right) f(0) \quad \text{and} \quad R = \int_0^1 dx \frac{1}{x^{1-\varepsilon}} f(x)$$

IR safety: $\lim_{x \rightarrow 0} f(x) = f(0)$

Methods to isolate divergences:

- subtraction
- slicing

Subtraction method

Subtract singular limit in integrand in

$$\bar{R} = R - S = \int_0^1 dx \frac{1}{x^{1-\epsilon}} [f(x) - f(0)]$$

Subtraction term is evaluated analytically

$$S = f(0) \int_0^1 \frac{1}{x^{1-\epsilon}} = f(0) \frac{1}{\epsilon}$$

and added to virtual correction

$$\sigma_f^{\text{NLO}} = R + V = (R - S) + (V + S) = \bar{R} + \bar{V}$$

- Both \bar{R} and \bar{V} are finite for $\epsilon = 0$.
- Real emission \bar{R} can be evaluated with MC integration.

Slicing method

Isolate singular piece by splitting integration

$$R_\delta = \int_\delta^1 dx \frac{1}{x^{1-\varepsilon}} f(x)$$

Integrand is regular, bounded, positive, can set $\varepsilon = 0$ and use MC. In remainder, approximate $f(x) = f(0) + \mathcal{O}(x)$

$$S_\delta = f(0) \int_0^\delta \frac{1}{x^{1-\varepsilon}} + \mathcal{O}(\delta) = f(0) \left(\frac{1}{\varepsilon} + \ln \delta \right) + \mathcal{O}(\delta)$$

and add to virtual correction

$$\sigma_f^{\text{NLO}} = R_\delta + (S_\delta + V) + \mathcal{O}(\delta) = \sigma(x > \delta) + \sigma(x < \delta)$$

The two parts are physical cross sections!

Slicing

In contrast to subtraction, slicing involves an expansion in slicing parameter δ .

- Important that is δ small enough that power corrections in δ are negligible!
- Small δ is numerically difficult. Large cancellations between R_δ and $\sigma(x < \delta)$

Advantage of slicing is that it is done on the level of cross sections, which can be computed independently

$$\sigma = \sigma(x > \delta) + \sigma(x < \delta)$$

For NLO: tree-level cross section;
compute with tree-level generator

expanded in δ and observable independent;
compute using factorization theorem at small δ

NLO subtraction methods

Realistic NLO computation for n -jet cross section involves

- n -parton phase space for virtual corrections
- $(n+1)$ -parton real emissions corrections
- Singularities when 2 partons become collinear, or 1 parton becomes soft

There are general algorithms for the subtraction terms, **based on universal soft and collinear factorization**

- **FKS subtraction** Frixione, Kunszt, Signer '95
- **Dipole subtraction** Catani Seymour '98

Both schemes have been automated and implemented into numerical codes.

One-loop amplitudes

Passarino and Veltman '79 showed that all loop integrals can be decomposed in a **small set of known scalar integrals**

$$\begin{aligned}
 \mathcal{M}^{1\text{-loop}} = & \sum_{i_0 < i_1 < i_2 < i_3} d_{i_0 i_1 i_2 i_3} \text{Box}_{i_0 i_1 i_2 i_3} & D_i &= (l + p_i)^2 - m_i^2 \\
 & + \sum_{i_0 < i_1 < i_2} c_{i_0 i_1 i_2} \text{Triangle}_{i_0 i_1 i_2} & \text{Tadpole}_{i_0} &= \int d^d l \frac{1}{D_{i_0}} \\
 & + \sum_{i_0 < i_1} b_{i_0 i_1} \text{Bubble}_{i_0 i_1} & \text{Bubble}_{i_0 i_1} &= \int d^d l \frac{1}{D_{i_0} D_{i_1}} \\
 & + \sum_{i_0} a_{i_0} \text{Tadpole}_{i_0} & \text{Triangle}_{i_0 i_1 i_2} &= \int d^d l \frac{1}{D_{i_0} D_{i_1} D_{i_2}} \\
 & + R + \mathcal{O}(\epsilon) & \text{Box}_{i_0 i_1 i_2 i_3} &= \int d^d l \frac{1}{D_{i_0} D_{i_1} D_{i_2} D_{i_3}}
 \end{aligned}$$

However, original integral reduction method leads to numerical instabilities and is unsuitable for complicated processes.

Integral reduction

This problem has been solved. We now have automated methods to reliably compute also fairly complicated loop amplitudes

- Unitarity and on-shell methods [Ossola, Papadopoulos, Pittau '07](#); [Ellis, Giele, Kunszt '07](#) with fully numerical evaluation based on reduction at the integrand level
- Improvements on “traditional” reduction technique [Denner, Dittmaier '06, '11](#)

NLO: one-loop amplitudes

Main **one-loop** amplitude providers:

- ▶ **BlackHat**(<https://blackhat.hepforge.org/>)
 - ▶ **Collier** (<https://collier.hepforge.org>)
 - ▶ **GoSam** (<https://gosam.hepforge.org>)
 - ▶ **Golem95** (<https://golem.hepforge.org/>)
 - ▶ **Helac-NLO/Helac-1Loop** (<https://helac-phegas.web.cern.ch>)
 - ▶ **Ninja** (<https://ninja.hepforge.org/>)
 - ▶ **Njet** (<https://www.physik.hu-berlin.de/de/pep/tools/njet>)
 - ▶ **NLOX** (<http://www.hep.fsu.edu/~nlox/>)
 - ▶ **OpenLoops** (<https://openloops.hepforge.org>)
 - ▶ **Recola/Recola2** (<https://recola.hepforge.org>)
- ✓ Fast, automated generation and numerical evaluation of one-loop amplitudes
 - ✓ Easy interface with Sherpa, Herwig, POWHEG, and others
 - ✓ QCD only, or full SM (QCD+EW)

from Giulia Zanderighi's talk at Planck2025

NLO: general purpose tools

1. MadGraph5_aMC@NLO (<https://launchpad.net/mg5amcnlo>)

- Full automation of NLO QCD and EW
- Process generation via FeynRules/UFO. Supports parton showers via aMC@NLO

2. Sherpa+OpenLoops (<https://sherpa.hepforge.org>, <https://openloops.hepforge.org>)

- SHERPA handles phase space, subtraction, matching, and showering
- OpenLoops provides fast NLO matrix elements. Efficient for multi-leg processes

3. Herwig+Matchbox (<https://herwig.hepforge.org>)

- Herwig's Matchbox module enables automated NLO QCD corrections and matching
- Works with external amplitude providers (OpenLoops, MadGraph, etc.)

4. POWHEG-BOX (<http://powhegbox.mib.infn.it>)

- NLO with matching to parton showers (POWHEG method)
- Semi-automated; requires user input for new processes

5. MCFM (<https://mcfm.fnal.gov>)

- Parton-level code for NLO calculations (less automated)
- Mostly SM processes. Mostly based on analytic calculations, very stable and fast

...

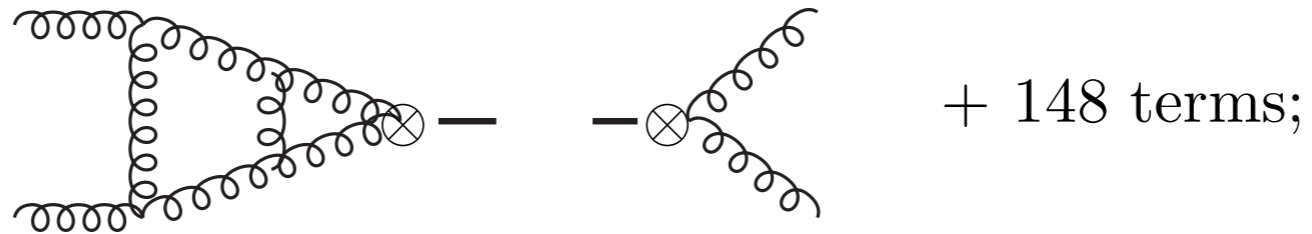
from Giulia Zanderighi's talk at Planck2025

Process		Syntax	Cross section (pb)					
Single Higgs production			LO 13 TeV			NLO 13 TeV		
g.1	$pp \rightarrow H$ (HEFT)	p p > h	$1.593 \pm 0.003 \cdot 10^1$	+34.8%	+1.2%	$3.261 \pm 0.010 \cdot 10^1$	+20.2%	+1.1%
				-26.0%	-1.7%		-17.9%	-1.6%
g.2	$pp \rightarrow H j$ (HEFT)	p p > h j	$8.367 \pm 0.003 \cdot 10^0$	+39.4%	+1.2%	$1.422 \pm 0.006 \cdot 10^1$	+18.5%	+1.1%
				-26.4%	-1.4%		-16.6%	-1.4%
g.3	$pp \rightarrow H j j$ (HEFT)	p p > h j j	$3.020 \pm 0.002 \cdot 10^0$	+59.1%	+1.4%	$5.124 \pm 0.020 \cdot 10^0$	+20.7%	+1.3%
				-34.7%	-1.7%		-21.0%	-1.5%
g.4	$pp \rightarrow H j j$ (VBF)	p p > h j j \$\$ w+ w- z	$1.987 \pm 0.002 \cdot 10^0$	+1.7%	+1.9%	$1.900 \pm 0.006 \cdot 10^0$	+0.8%	+2.0%
				-2.0%	-1.4%		-0.9%	-1.5%
g.5	$pp \rightarrow H j j j$ (VBF)	p p > h j j j \$\$ w+ w- z	$2.824 \pm 0.005 \cdot 10^{-1}$	+15.7%	+1.5%	$3.085 \pm 0.010 \cdot 10^{-1}$	+2.0%	+1.5%
				-12.7%	-1.0%		-3.0%	-1.1%
g.6	$pp \rightarrow HW^\pm$	p p > h wpm	$1.195 \pm 0.002 \cdot 10^0$	+3.5%	+1.9%	$1.419 \pm 0.005 \cdot 10^0$	+2.1%	+1.9%
				-4.5%	-1.5%		-2.6%	-1.4%
g.7	$pp \rightarrow HW^\pm j$	p p > h wpm j	$4.018 \pm 0.003 \cdot 10^{-1}$	+10.7%	+1.2%	$4.842 \pm 0.017 \cdot 10^{-1}$	+3.6%	+1.2%
				-9.3%	-0.9%		-3.7%	-1.0%
g.8*	$pp \rightarrow HW^\pm j j$	p p > h wpm j j	$1.198 \pm 0.016 \cdot 10^{-1}$	+26.1%	+0.8%	$1.574 \pm 0.014 \cdot 10^{-1}$	+5.0%	+0.9%
				-19.4%	-0.6%		-6.5%	-0.6%
g.9	$pp \rightarrow H Z$	p p > h z	$6.468 \pm 0.008 \cdot 10^{-1}$	+3.5%	+1.9%	$7.674 \pm 0.027 \cdot 10^{-1}$	+2.0%	+1.9%
				-4.5%	-1.4%		-2.5%	-1.4%
g.10	$pp \rightarrow H Z j$	p p > h z j	$2.225 \pm 0.001 \cdot 10^{-1}$	+10.6%	+1.1%	$2.667 \pm 0.010 \cdot 10^{-1}$	+3.5%	+1.1%
				-9.2%	-0.8%		-3.6%	-0.9%
g.11*	$pp \rightarrow H Z j j$	p p > h z j j	$7.262 \pm 0.012 \cdot 10^{-2}$	+26.2%	+0.7%	$8.753 \pm 0.037 \cdot 10^{-2}$	+4.8%	+0.7%
				-19.4%	-0.6%		-6.3%	-0.6%
g.12*	$pp \rightarrow HW^+W^-$ (4f)	p p > h w+ w-	$8.325 \pm 0.139 \cdot 10^{-3}$	+0.0%	+2.0%	$1.065 \pm 0.003 \cdot 10^{-2}$	+2.5%	+2.0%
				-0.3%	-1.6%		-1.9%	-1.5%
g.13*	$pp \rightarrow HW^\pm \gamma$	p p > h wpm a	$2.518 \pm 0.006 \cdot 10^{-3}$	+0.7%	+1.9%	$3.309 \pm 0.011 \cdot 10^{-3}$	+2.7%	+1.7%
				-1.4%	-1.5%		-2.0%	-1.4%
g.14*	$pp \rightarrow H Z W^\pm$	p p > h z wpm	$3.763 \pm 0.007 \cdot 10^{-3}$	+1.1%	+2.0%	$5.292 \pm 0.015 \cdot 10^{-3}$	+3.9%	+1.8%
				-1.5%	-1.6%		-3.1%	-1.4%
g.15*	$pp \rightarrow H Z Z$	p p > h z z	$2.093 \pm 0.003 \cdot 10^{-3}$	+0.1%	+1.9%	$2.538 \pm 0.007 \cdot 10^{-3}$	+1.9%	+2.0%
				-0.6%	-1.5%		-1.4%	-1.5%
g.16	$pp \rightarrow H t \bar{t}$	p p > h t t~	$3.579 \pm 0.003 \cdot 10^{-1}$	+30.0%	+1.7%	$4.608 \pm 0.016 \cdot 10^{-1}$	+5.7%	+2.0%
				-21.5%	-2.0%		-9.0%	-2.3%
g.17	$pp \rightarrow H t j$	p p > h t t j	$4.994 \pm 0.005 \cdot 10^{-2}$	+2.4%	+1.2%	$6.328 \pm 0.022 \cdot 10^{-2}$	+2.9%	+1.5%
				-4.2%	-1.3%		-1.8%	-1.6%
g.18	$pp \rightarrow H b \bar{b}$ (4f)	p p > h b b~	$4.983 \pm 0.002 \cdot 10^{-1}$	+28.1%	+1.5%	$6.085 \pm 0.026 \cdot 10^{-1}$	+7.3%	+1.6%
				-21.0%	-1.8%		-9.6%	-2.0%
g.19	$pp \rightarrow H t \bar{t} j$	p p > h t t~ j	$2.674 \pm 0.041 \cdot 10^{-1}$	+45.6%	+2.6%	$3.244 \pm 0.025 \cdot 10^{-1}$	+3.5%	+2.5%
				-29.2%	-2.9%		-8.7%	-2.9%
g.20*	$pp \rightarrow H b \bar{b} j$ (4f)	p p > h b b~ j	$7.367 \pm 0.002 \cdot 10^{-2}$	+45.6%	+1.8%	$9.034 \pm 0.032 \cdot 10^{-2}$	+7.9%	+1.8%
				-29.1%	-2.1%		-11.0%	-2.2%

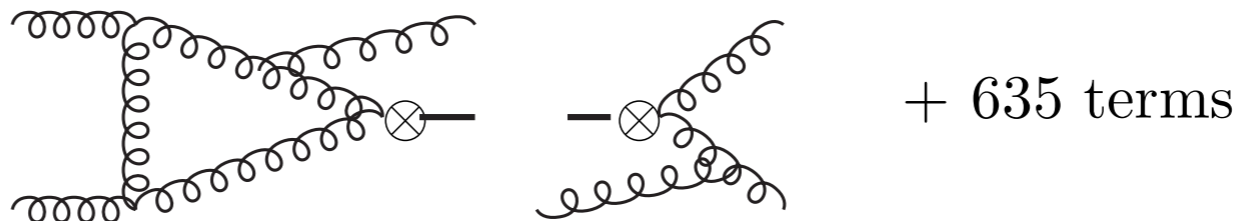
sample results from **MadGraph5_aMC@NLO** Alwall et al. '14
(paper now has >9700 citations)

NNLO ingredients

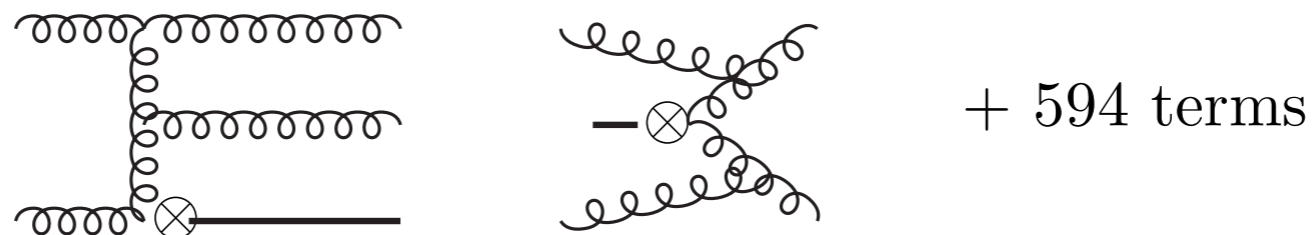
- Two-loop virtual



- Real-virtual



- Double-real



(NNLO Higgs production [Anastasiou and Melnikov '02](#))

NNLO subtraction

Challenging structure of IR singularities at NNLO

- Double-soft, triple-collinear, soft-collinear, ...
- Difficult to find have subtraction terms covering all limits that can be integrated analytically.

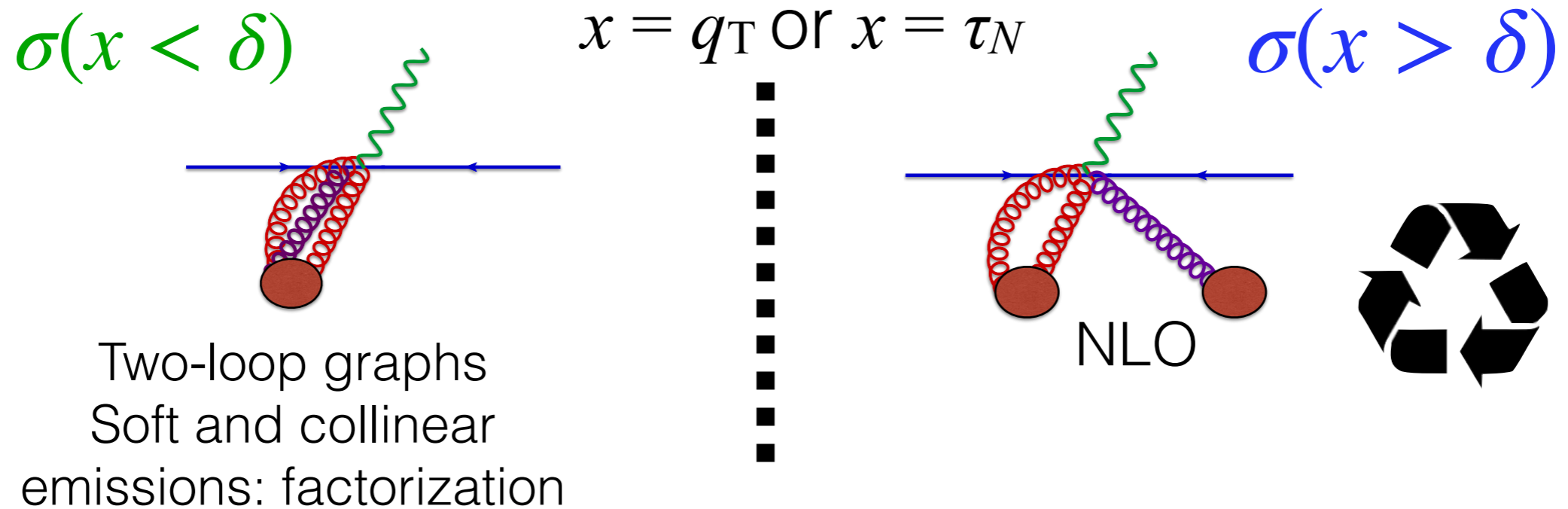
Many methods, all used in particular NNLO computations

- Antenna subtraction, sector improved residue subtraction, nested soft-collinear subtraction, local analytic subtraction, ColourFull subtraction, projection to Born, ...

Still a very active area of research.

NNLO slicing

Catani, Grazzini '07, Boughezal, Liu, Petreillo 15, Gaunt, Stahlhofen, Tackmann Walsh 15



Use transverse momentum q_T or event shape τ_N (N -jettiness) to separate out most singular region of NNLO computation

- Factorization theorems to compute $\sigma(x < \delta)$ in singular region
- Existing NLO codes away from end-point for $\sigma(x > \delta)$

Used widely, especially for electroweak boson production processes (also at N³LO!) and for boson + jet processes.

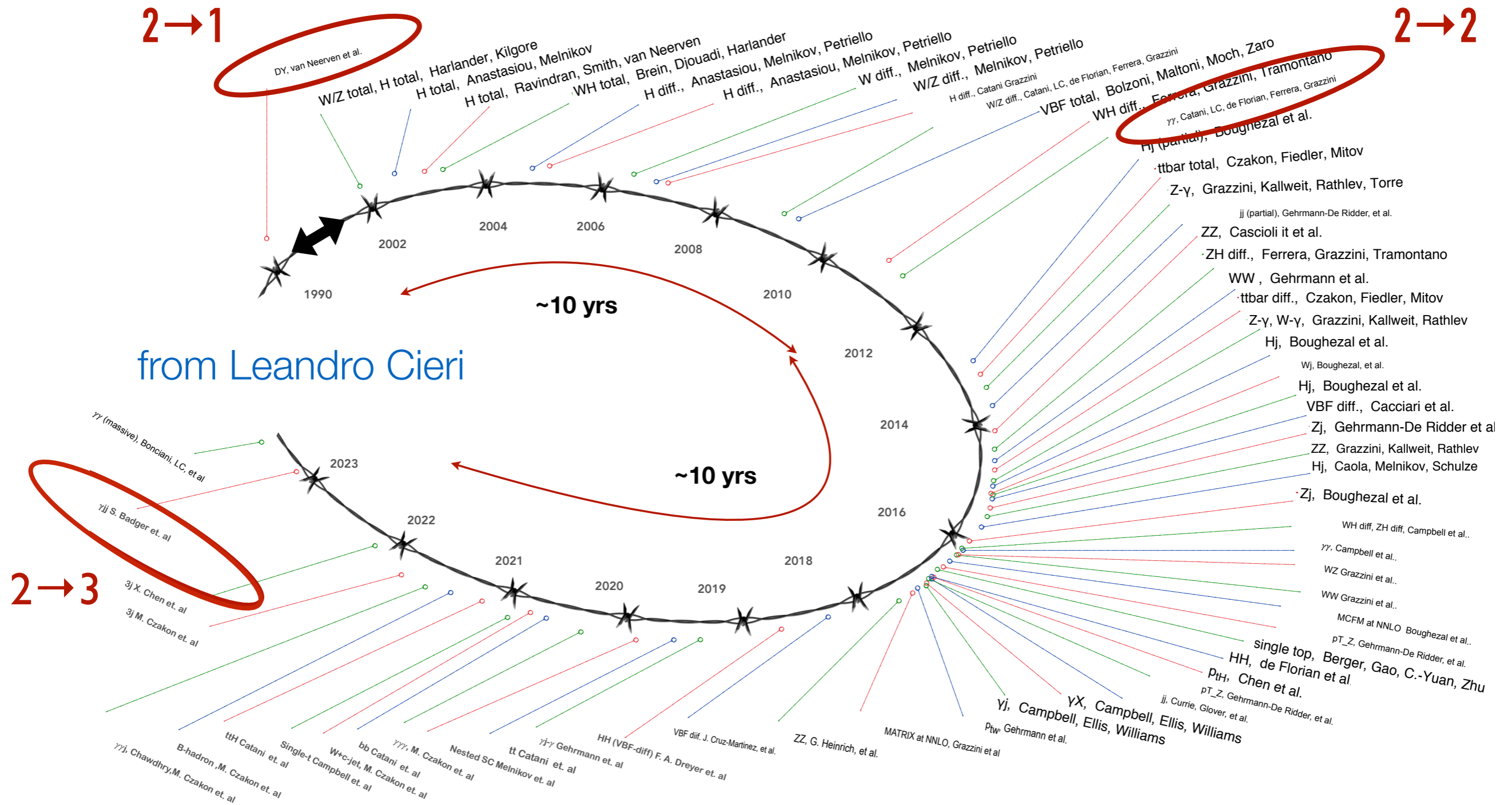
Two loop amplitudes

Big challenge at NNLO is the computation of two-loop integrals. Main strategy is

- reduction of loop integrals for a given process to a small set of master integrals using IBP identities
- analytic evaluation of the master integrals using **differential equations**, difference equations, **Mellin–Barnes representations**, Method of Regions expansions, **iterated integrals**...
- or numerical methods such as **sector decomposition** or **auxiliary mass flow**

Many new developments. Current **frontier is $2 \rightarrow 2$ with masses/off-shell legs**, **massless $2 \rightarrow 3$** .

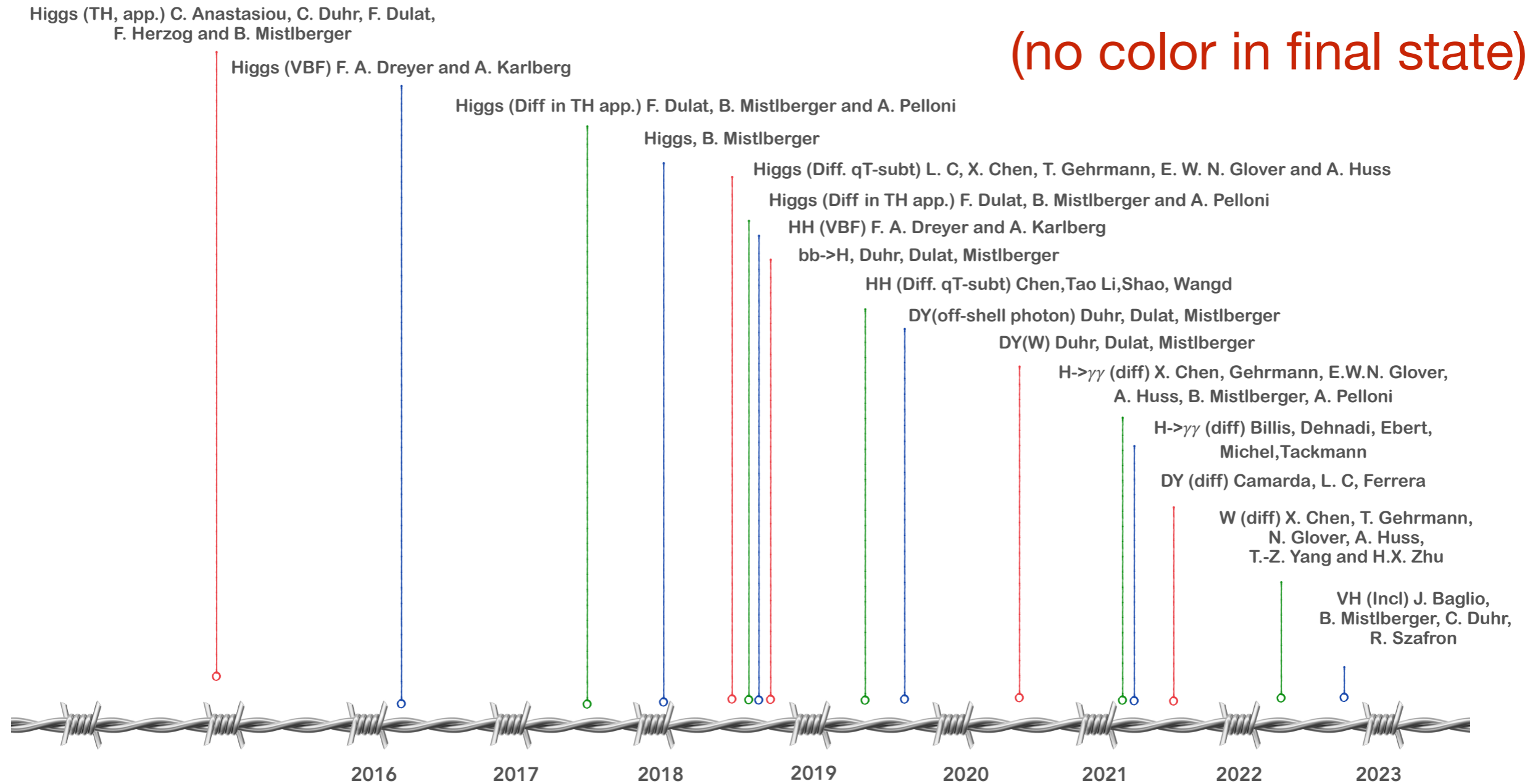
NNLO results



10 years / additional leg. No full automation yet!

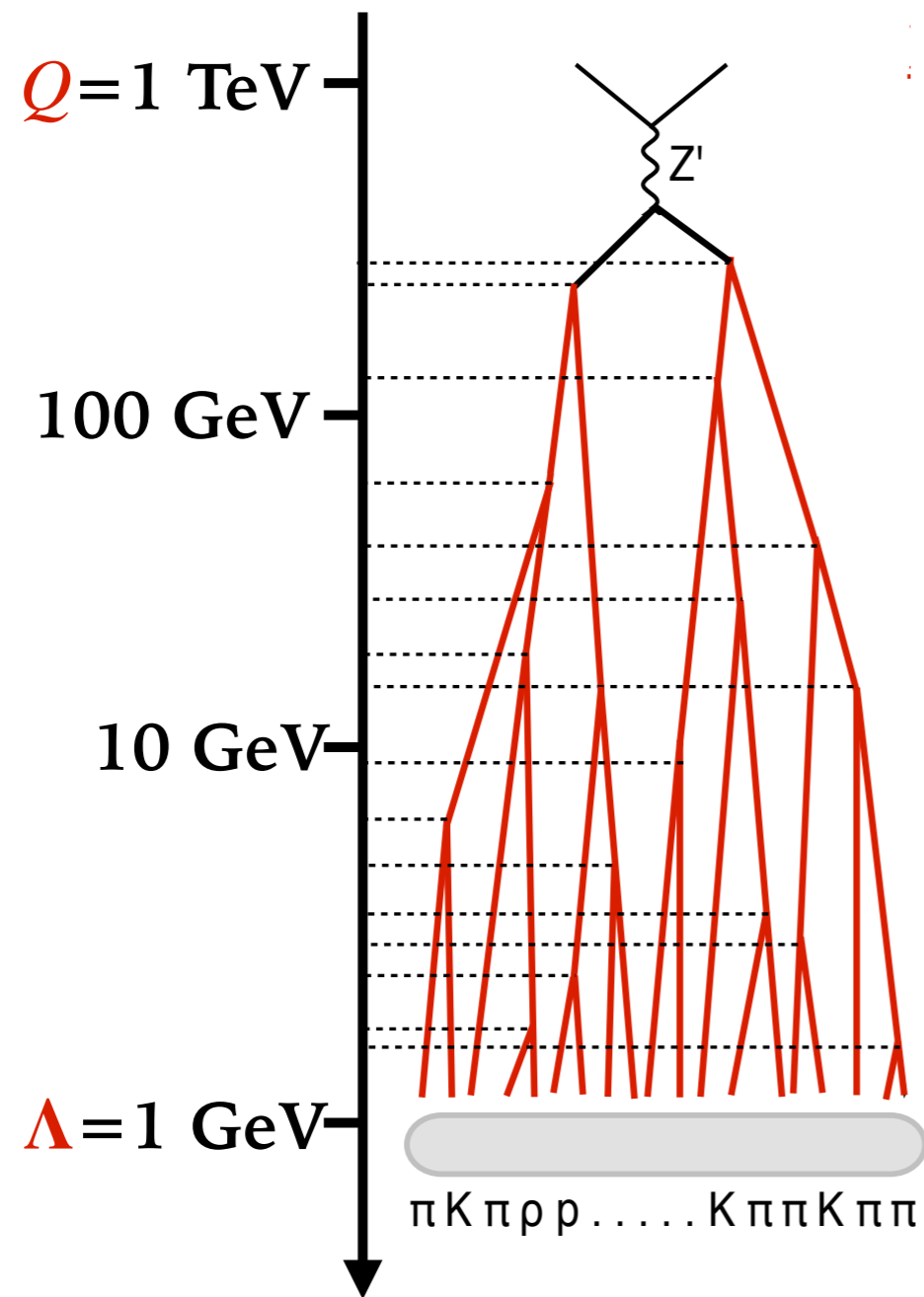
Status at N³LO

Drell-Yan like $2 \rightarrow 1$
(no color in final state)



from Leandro Cieri

Parton shower MCs



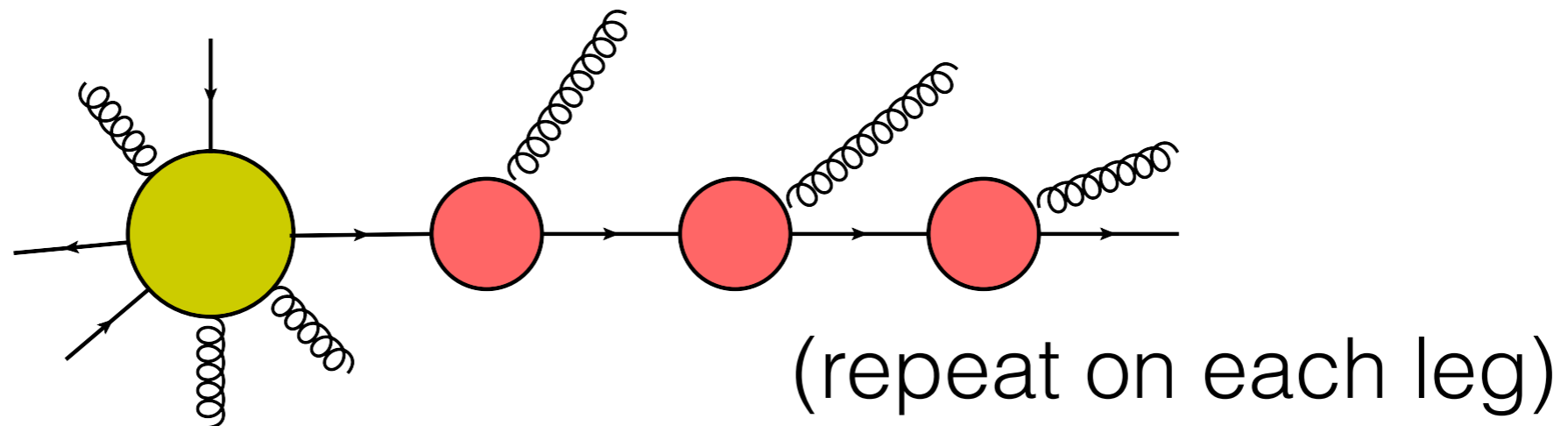
from Silvia Ferrario Ravasio

A crucial tool that can produce realistic collider events. Two main elements

- **cascade of quark and gluon emissions** down to low scale, approximate cross sections, based on **collinear and soft factorization**
- hadronisation model at the low scale
- + many additional ingredients. Hadron decays, MPI, QED, ...

Two basic types

- A. $1 \rightarrow 2$ branchings. Independent emissions from each leg

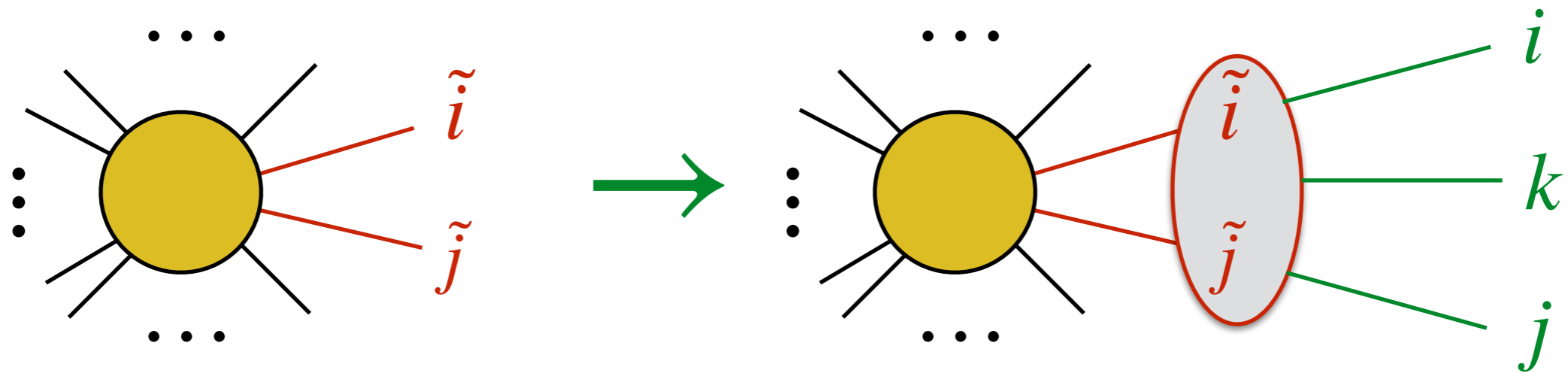


based on collinear factorization. Use **angular ordering** [Marchesini, Webber '88](#) to get correct soft radiation pattern for simple observables.

Implemented in [Herwig](#) parton shower.

Two basic types

B. Dipole showers based on $2 \rightarrow 3$ branchings.



LO soft emission is sum of dipoles!

Dipoles/antennas capture both soft and collinear limit at LO and produce both types of enhancements:
NLL accuracy is possible!

Well suited for matching to fixed order. Basis of most modern showers.

Recoil scheme

Soft and collinear factorization is based on expansions in these limits, e.g.

$$p_1 + \dots + p_n + k_{\text{soft}} \approx p_1 + \dots + p_n$$

Parton showers instead distribute recoil to have **exact momentum conservation** in each emission.

Two classes of prescriptions

- **Local recoil:** distribute recoil inside dipole. Modify $\tilde{p}_i \rightarrow p_i$ and $\tilde{p}_j \rightarrow p_j$ to ensure

$$\tilde{p}_i + \tilde{p}_j = p_i + p_j + k$$

- **Global recoil:** absorb k_T into all partons, also those not involved in the splitting.

Recoil and logarithmic accuracy

The recoil prescription can violate the scale separation underlying soft-collinear factorization.

For this reason **parton showers such as Pythia, Herwig and Sherpa do not achieve full NLL accuracy.**

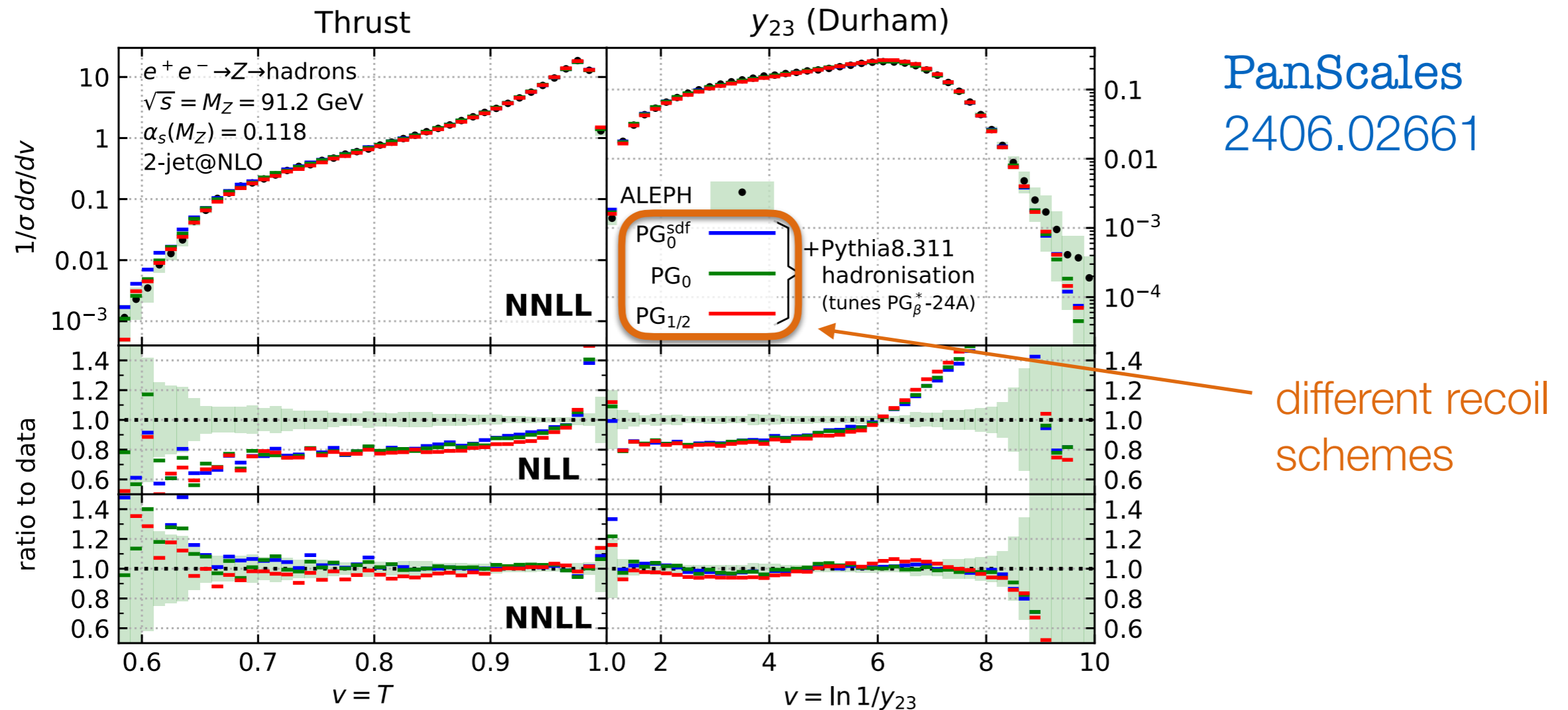
A new generation of parton showers is currently being developed which correctly resum **NLL logarithms**

- **ALARIC, Deductor, PanScales, Herwig⁷, ...**

The **PanScales** collaboration has even presented results for some observables at **NNLL accuracy.**

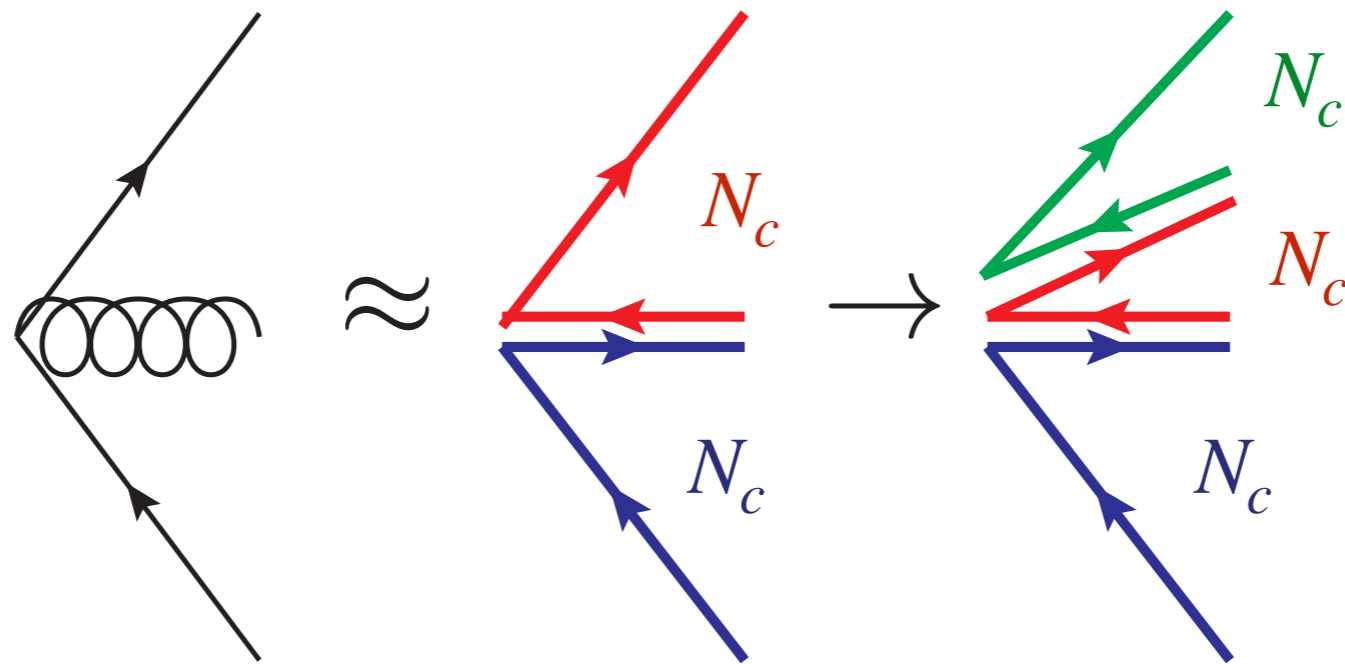
Exciting and important new development!

NNLL results for e^+e^- collisions



- Detailed numerical checks against “analytical” resummations to verify NNLL accuracy.
- NNLL achieves marked improvement over NLL!

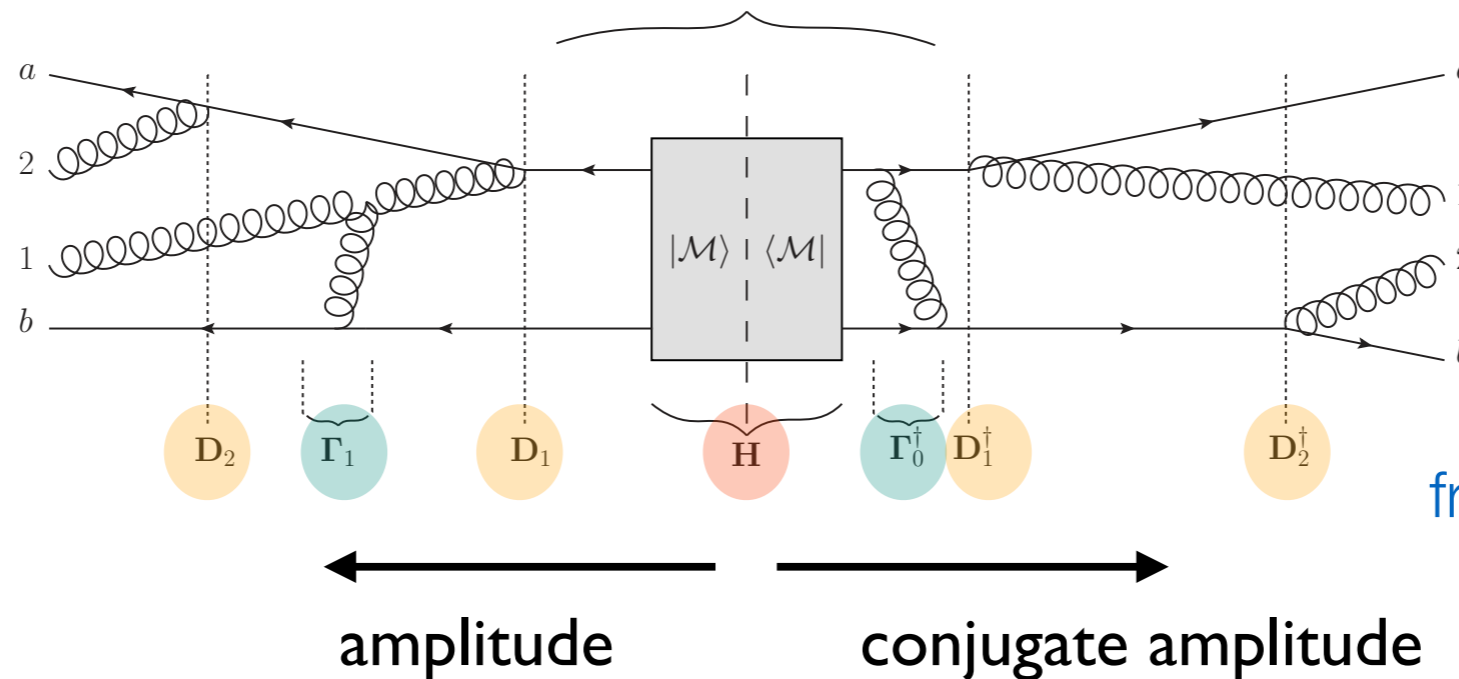
Large- N_c limit



Traditionally, parton showers work in the large- N_c limit

- huge simplification of color structure, everything is described in terms of **color dipoles**
- no interference, **shower can be formulated on the level level of cross section**

Amplitude-level evolution



from Simon Plätzer

Ongoing work on **full color parton shower**

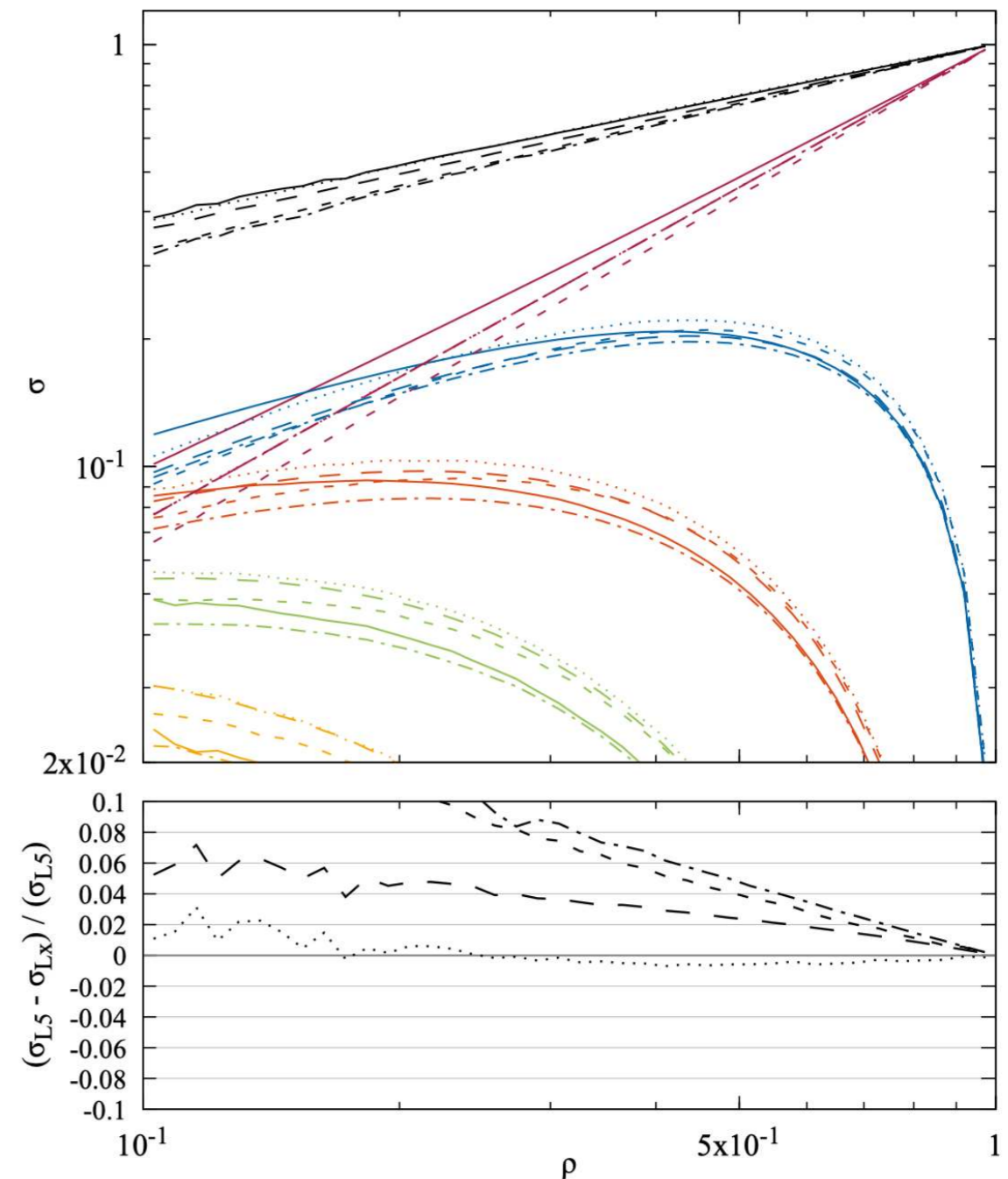
- Needs separate evolution for amplitude and its conjugate!
- Must efficiently sample the huge color space of the partons!
- Interference: no probabilistic event interpretation

Approximate treatment in **Deductor**, full color sampling in **CVolver**

CVolver results for $q\bar{q} \rightarrow q\bar{q}$

2505.13183

- Cross section with central jet veto $\rho = E_{\text{veto}}/Q$
- Partonic result only, fixed kinematics
- Plot compares full color (solid line) to strict large- N_c (short dashed) and various other approximations
- Black is full result, colors individual emissions (1 to 5)
- Agreement with results of [Hatta and Ueda](#) using Langevin method

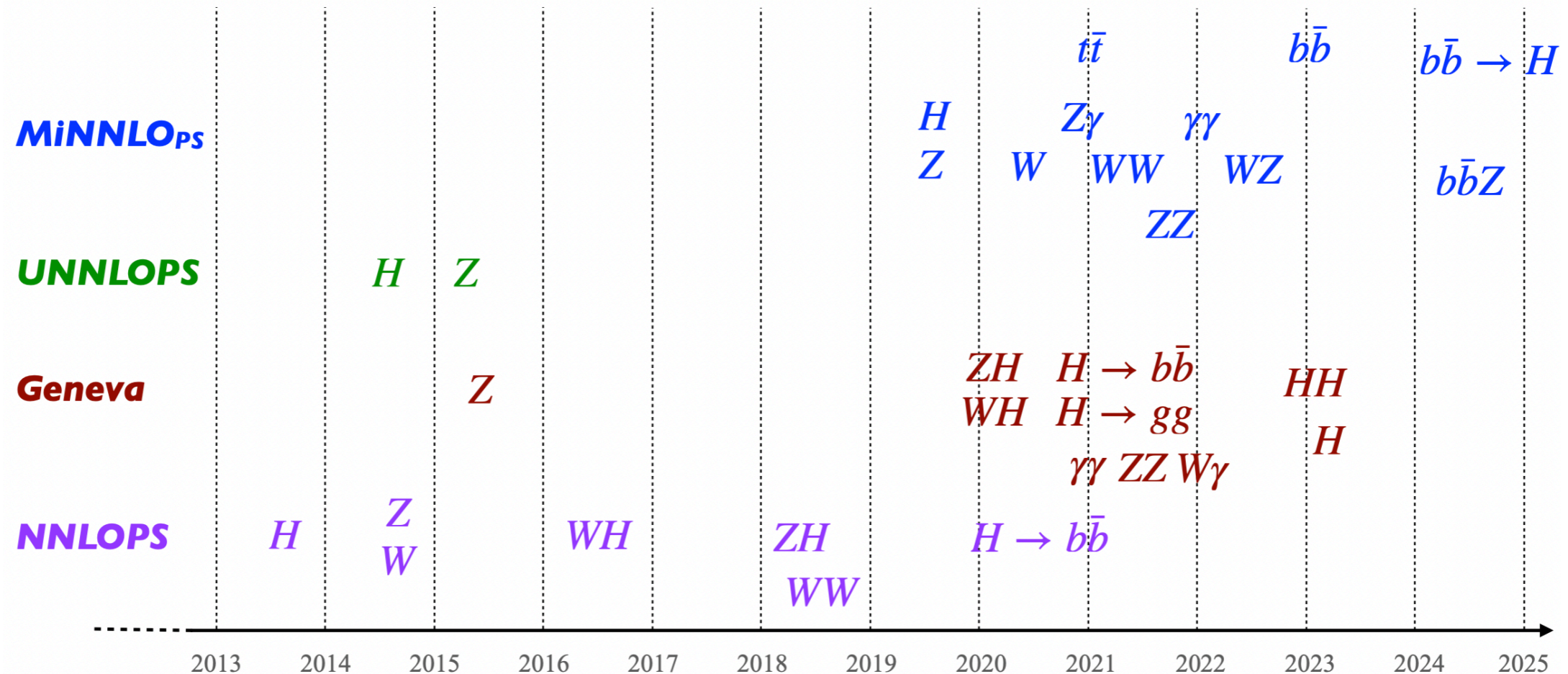


Matching to fixed order

- Shower generates emissions using approximate amplitudes (soft and collinear limits)
- Important to combine shower and fixed-order computations, so that at least the first emissions are exact
- Important to **avoid double counting** emissions!
- Different schemes available
 - LO (+merging): **CKKW, MLM, ...**
 - NLO: **MC@NLO, POWHEG, ...**
 - NNLO: **MiNNLO_{PS}, UNNLOPS, Geneva, NNLOPS,**

Parton shower matching

Different methods developed. NNLOPS with leading logarithmic accuracy in the shower well understood

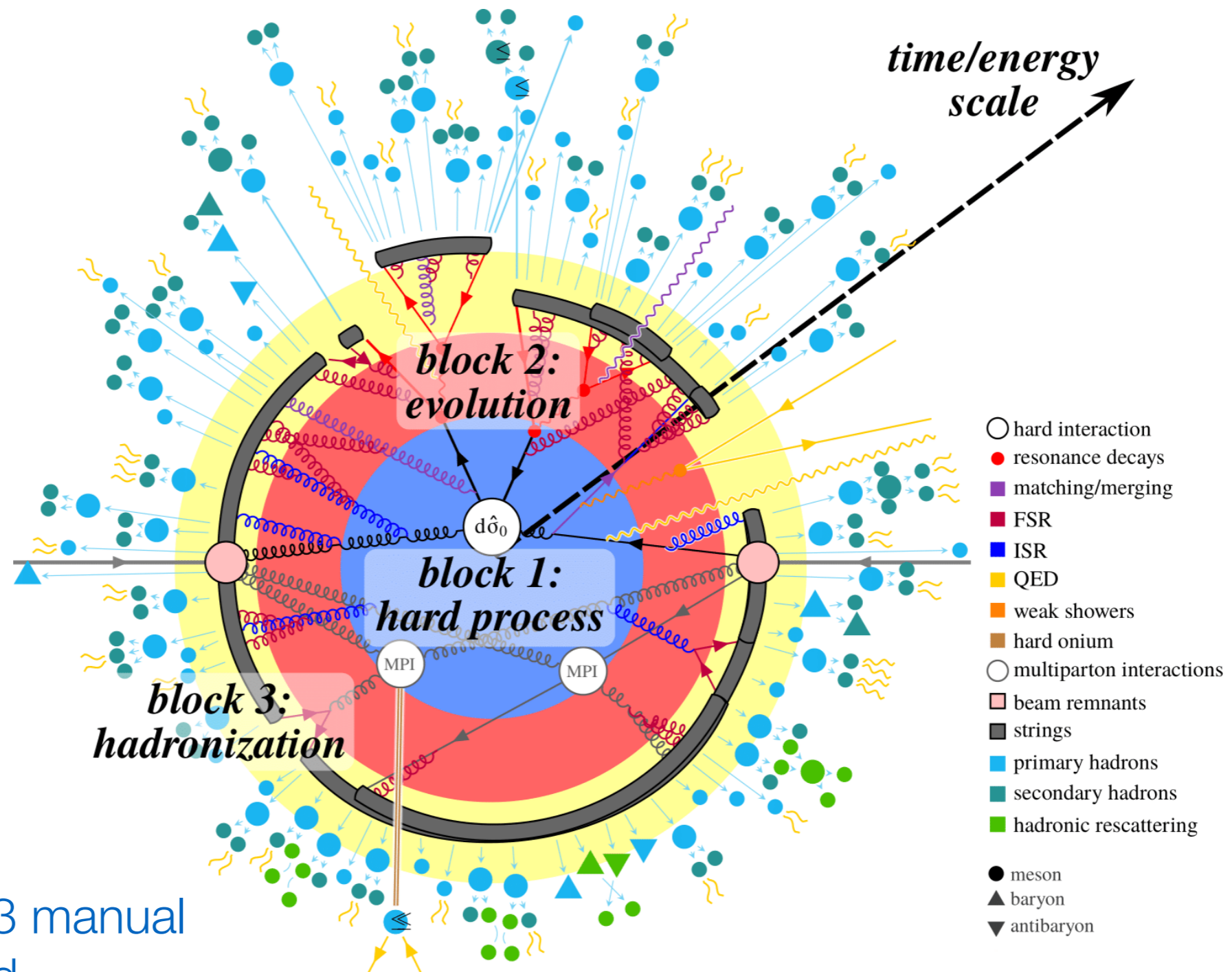


Not yet clear how to preserve accuracy of more accurate showers in the matching



from Giulia Zanderighi's talk at Planck2025

The final frontier: hadronisation



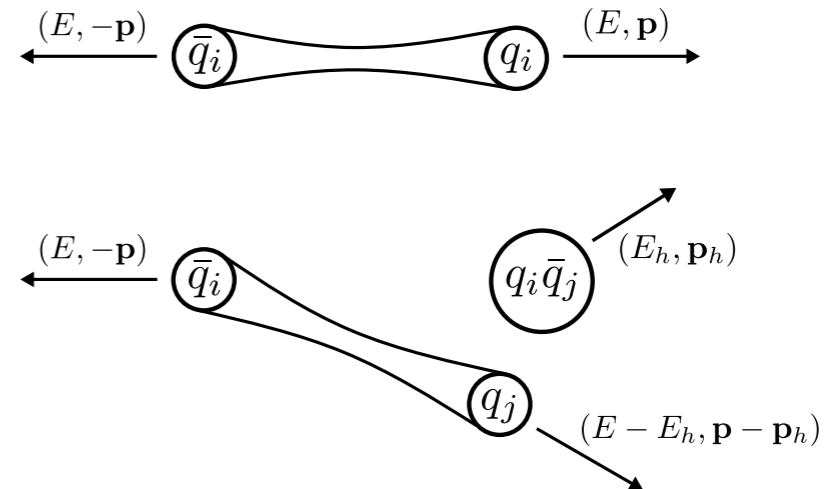
from Pythia 8.3 manual
MLHad

Hadronization models

A. Lund string model (**Pythia**)

Each dipole has a connecting string, hadrons through string breaking.

O(20) model parameters



B. Cluster fragmentation (**Herwig**)

Idea: fragmentation involves partons which are nearby in phase space.

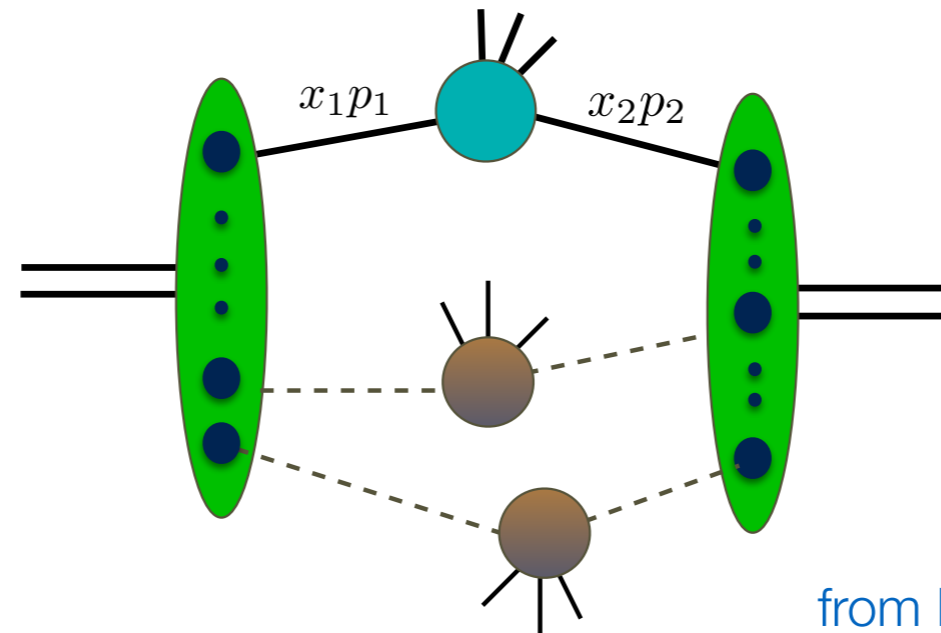
- After shower stops, **form color singlet clusters** of particles (“pre-confinement”). [Gluons are split into quarks.]
- Decay clusters into hadrons according to certain weights.

O(10) model parameters

Hadronisation: new developments

- [HadML](#) and [MLHad](#): machine learning techniques to parameterize and learn hadronisation from data, estimate hadronization uncertainties
- Consistency studies with NLL showers, varying shower cutoff scale; effect on top mass? [Hoang, Jin, Plätzer, Samitz](#)
- New studies within [Dokshitzer, Webber '95 model](#) of hadronisation. [Dasgupta, Hounat '24](#); [Bafi and Farren-Colloty, Helliwell, Patel, Salam](#) within [PanScales](#)
- Effects of color on hadronisation, within the context of amplitude showers? [Plätzer, Forshaw, ...](#)
- Quantum information and hadronisation [von Kuk, Lee, Michel, Sun '25](#)

Multi-parton interactions (MPI)



Showering and hadronizing the hard partons does not give a satisfactory description of hadron collider data.

- Shower MCs model additional collisions induced from proton remnants: MPI. “Underlying event”
- Also include “color reconnections” with partons from hard shower.

Conclusion

QCD is the essence of collider physics!

- Understanding of QCD effects is essential for LHC precision physics program...
- ... but also fascinating QFT!

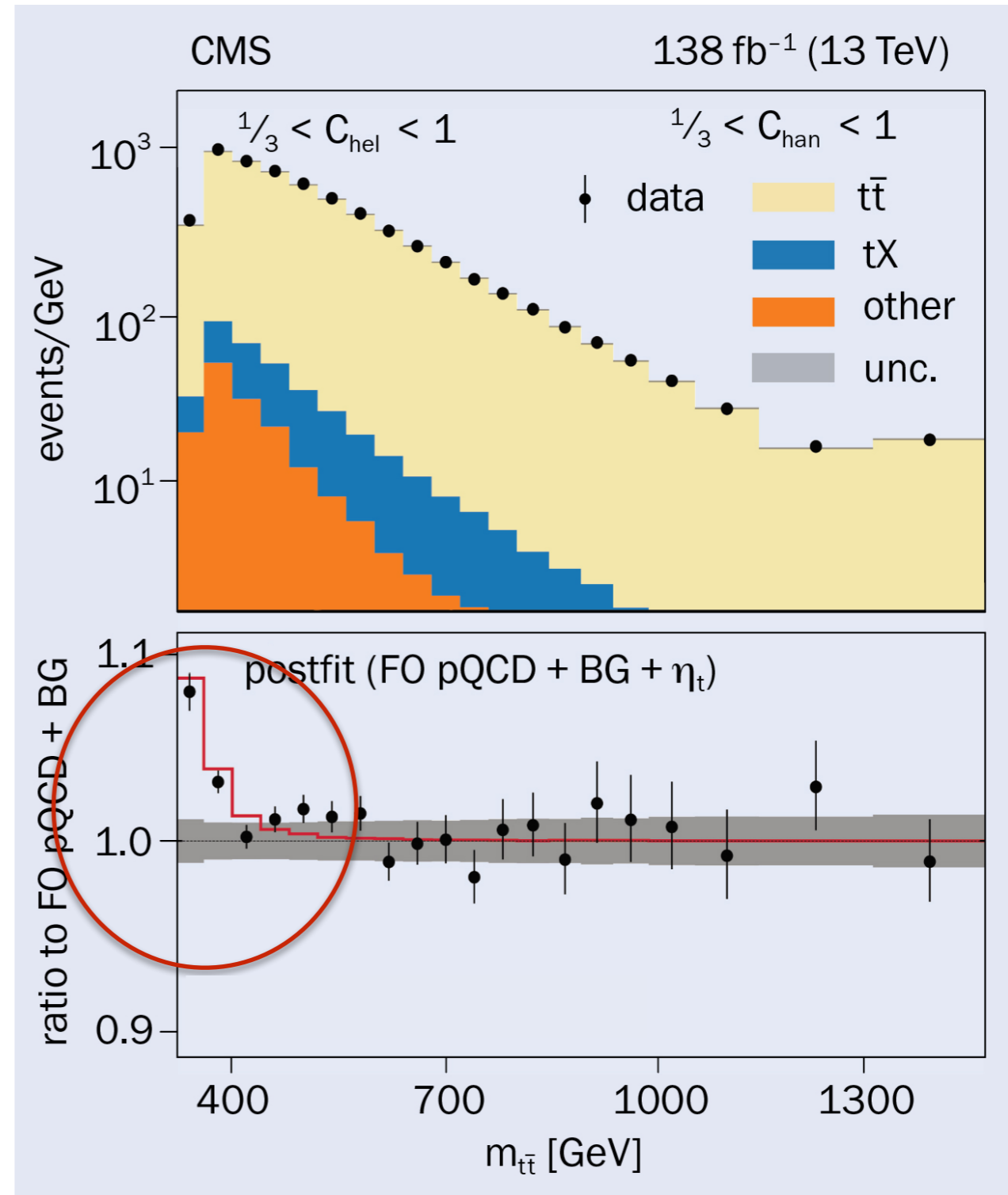
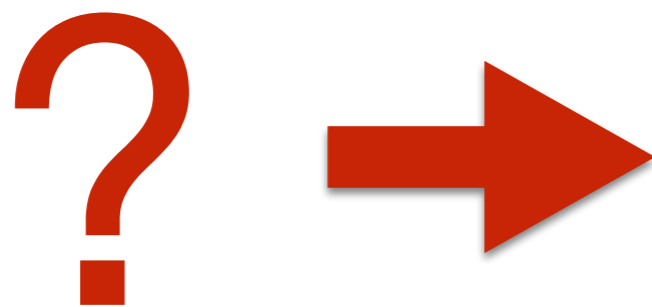
QCD recently celebrated its 50th anniversary

- Mature and well developed...
- ... but also many new ideas, breakthroughs (and open problems)!

One last example to close...

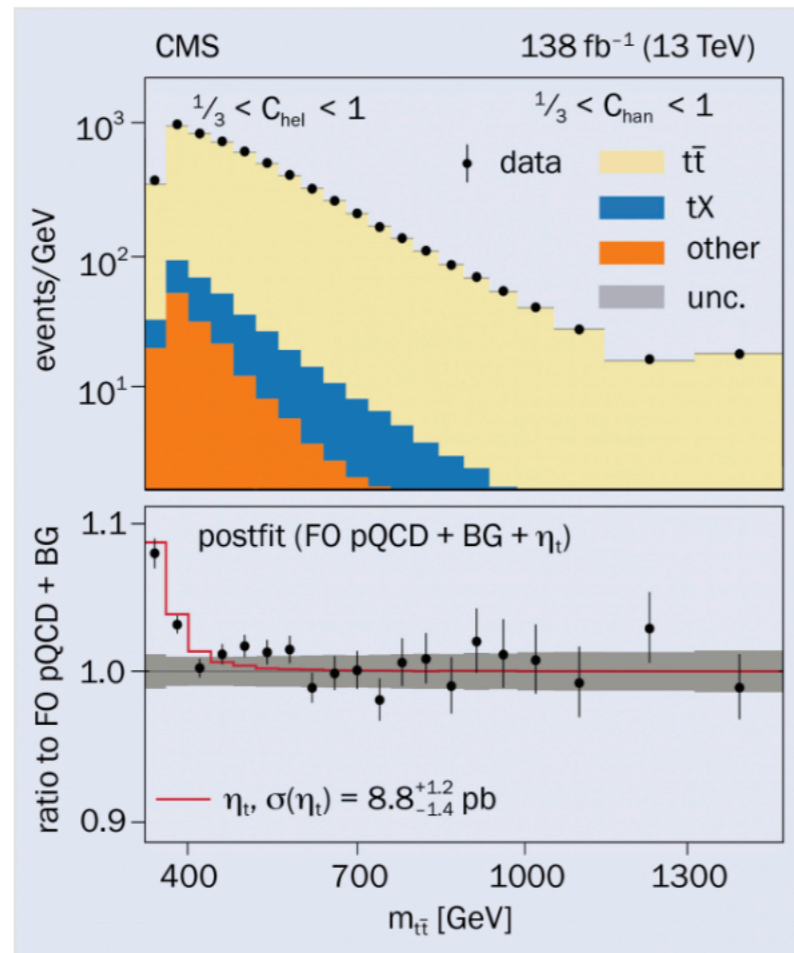
CMS [2503.22382](#)

Measurement of spin correlations in $t\bar{t}$ production



CMS observes top–antitop excess

2 April 2025



Threshold excess The invariant mass spectrum of top quark–antiquark pairs observed by the CMS experiment in certain domains of the reconstructed spin-correlation observables C_{hel} and C_{han} (top panel) and the signal-to-background ratio (bottom panel). Excess events at threshold can be modelled by including a new top–antitop bound state in the background model (red line). Credit: CMS Collab. 2025 arXiv:2503.22382.

CERN’s Large Hadron Collider continues to deliver surprises. While searching for additional Higgs bosons, the CMS collaboration may have instead uncovered evidence for the smallest composite particle yet observed in nature – a “quasi-bound” hadron made up of the most massive and shortest-lived fundamental particle known to science and its antimatter counterpart. The findings, which do not yet constitute a discovery claim and could also be susceptible to other explanations, were reported this week at the Rencontres de Moriond conference in the Italian Alps.

Almost all of the Standard Model’s shortcomings motivate the search for additional Higgs bosons. Their properties are usually assumed to be simple. the 125 GeV Higgs boson discovered