

Gravitational Sensing of Ultralight Dark Matter

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Quantum Sensing for Fundamental Physics

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**What do we know about
Dark Matter Density
around the solar system?**

$$\rho \stackrel{?}{=} 0.4 \text{ GeV}/\text{cm}^3$$

only over ***kpc-scale***

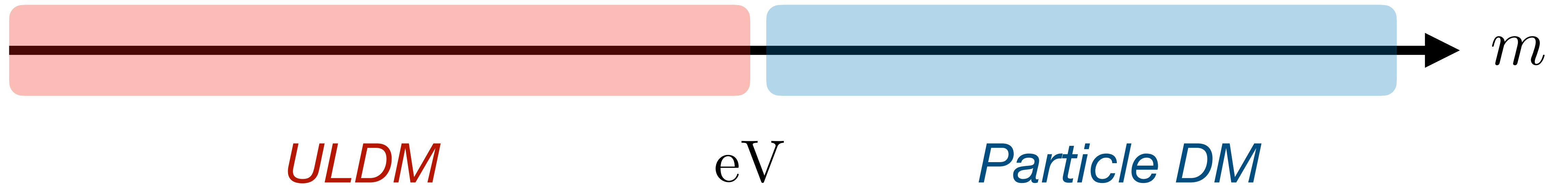
near the solar system

$$\rho \lesssim \mathcal{O}(1) \times 10^4 \text{ GeV}/\text{cm}^3$$

Probing ultralight DM with GW detectors

Ultralight Dark Matter

we define *ultralight dark matter (ULDM)*
as *bosonic DM candidates with* $m < \text{eV}$

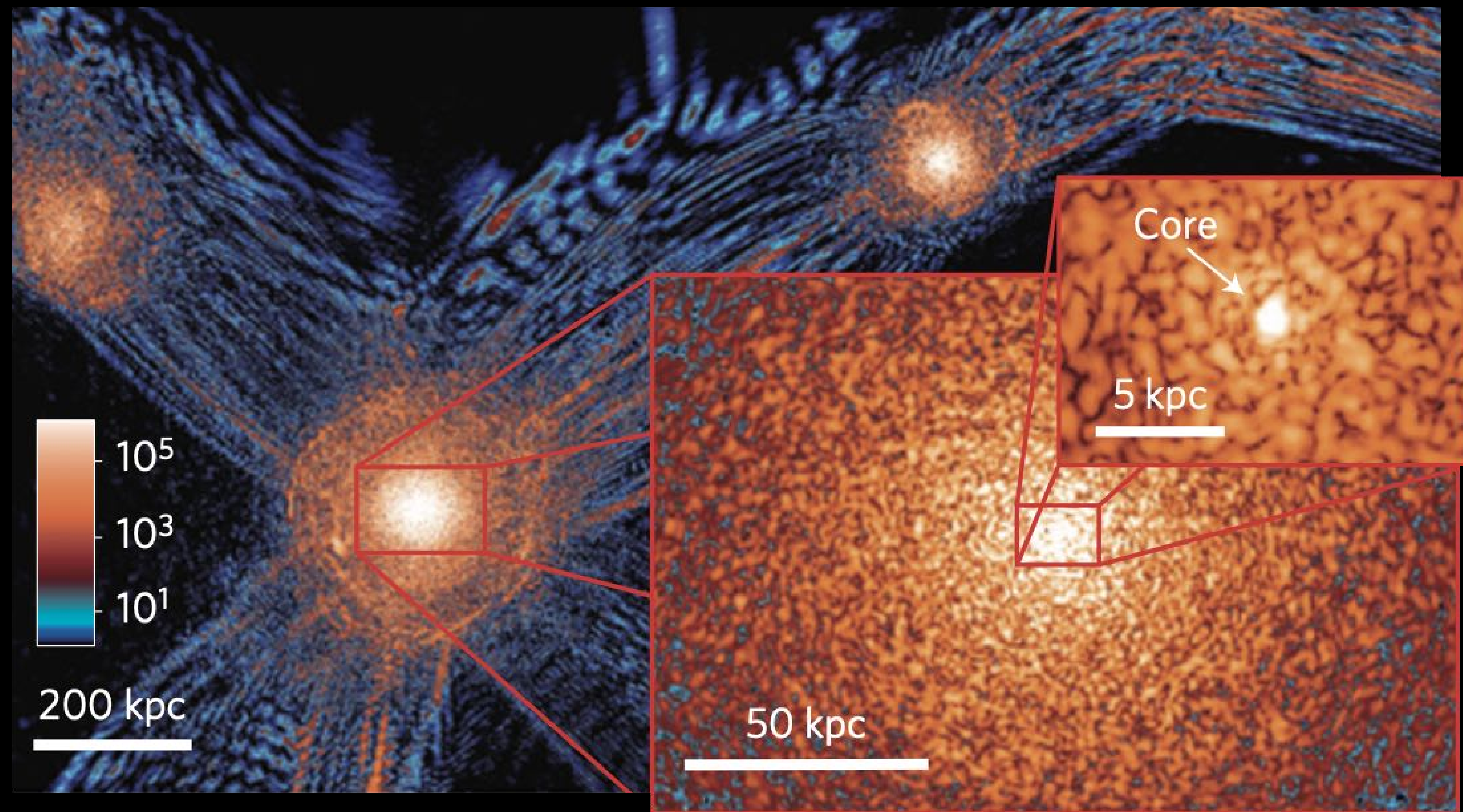


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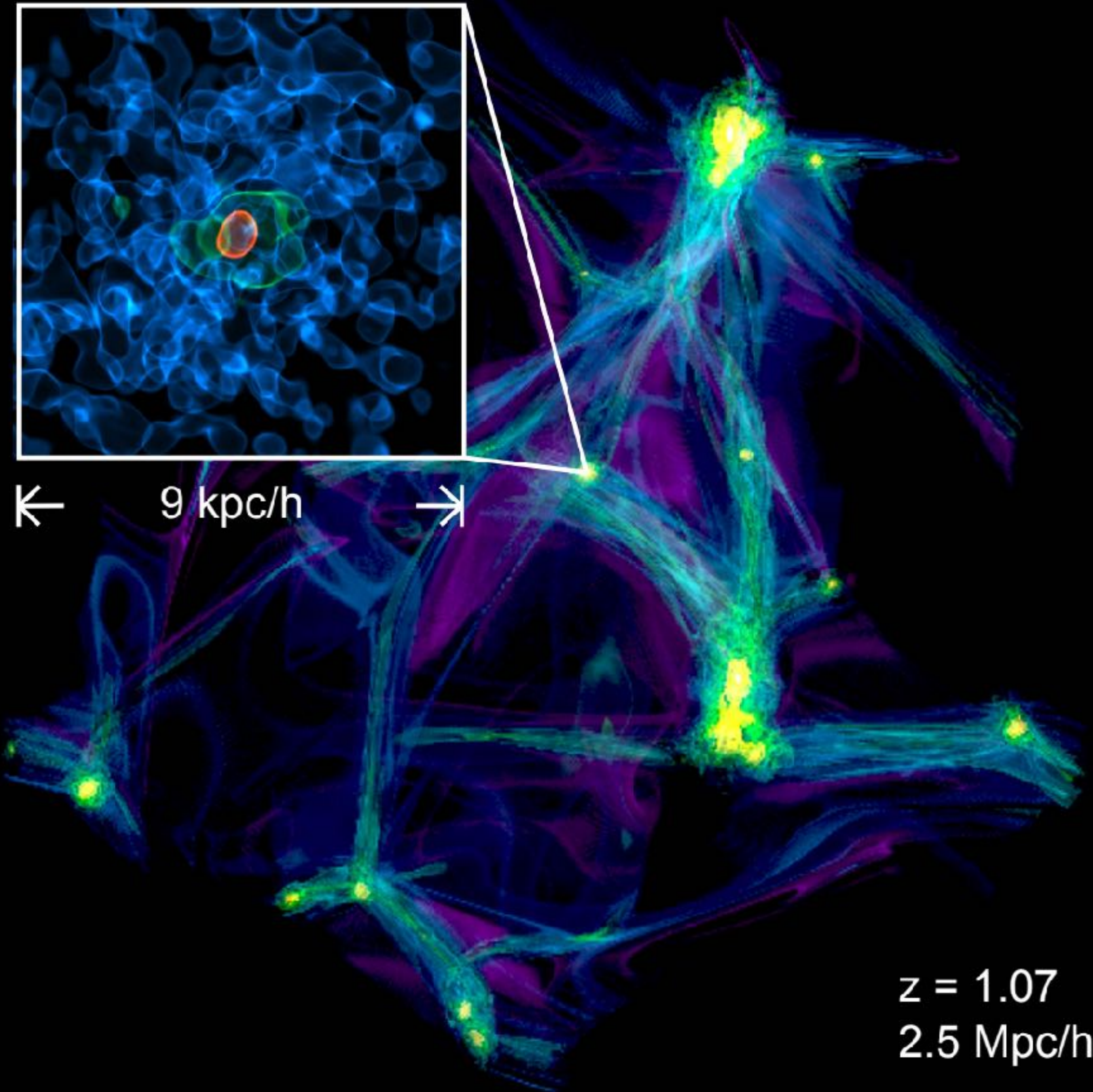
$$m \lesssim 10 \text{ eV}$$

$$N_{\text{occ}} \sim n_{\text{dm}} \lambda^3 \sim \left(\frac{10 \text{ eV}}{m} \right)^4$$

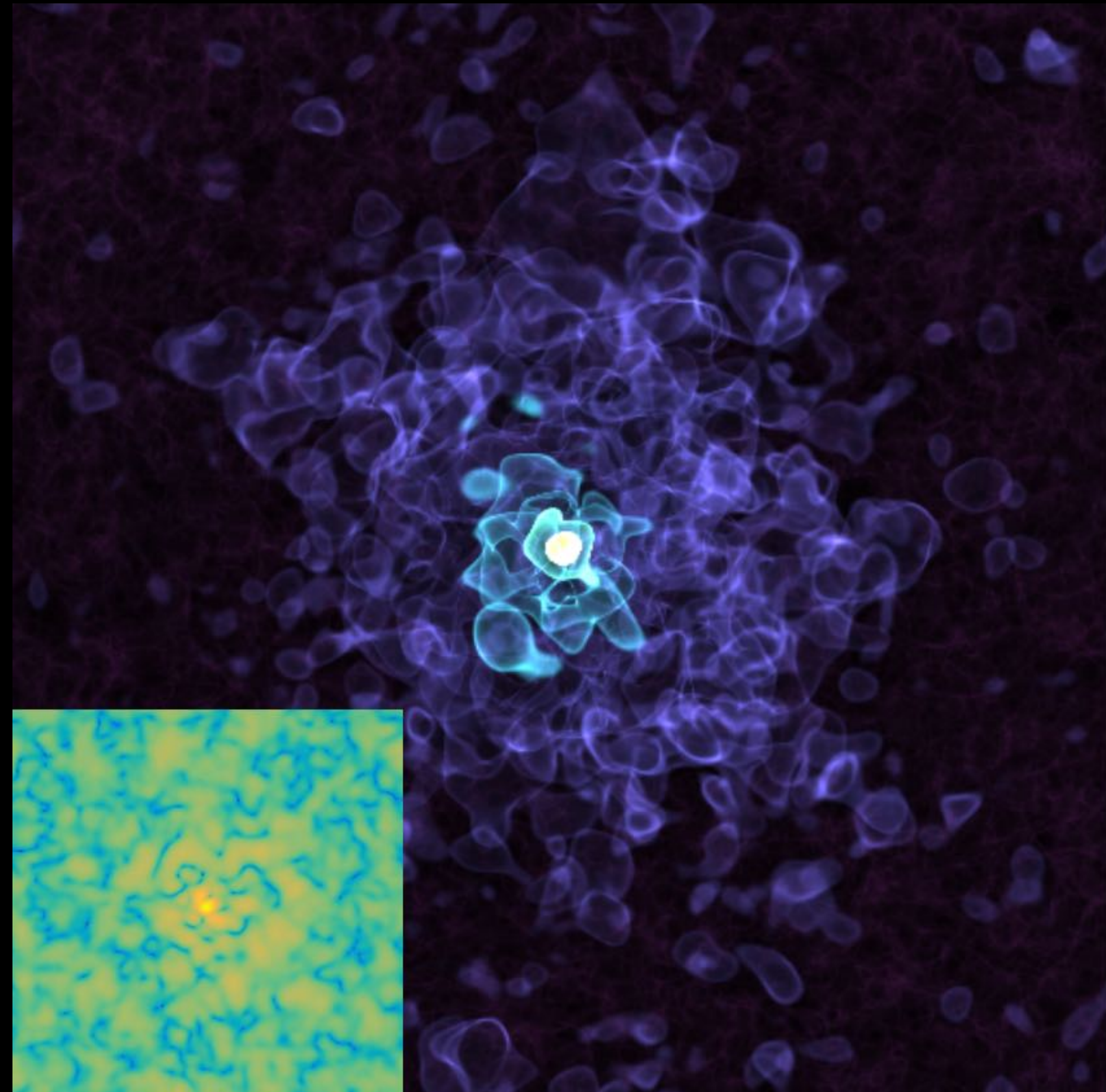




Mocz et al (17)



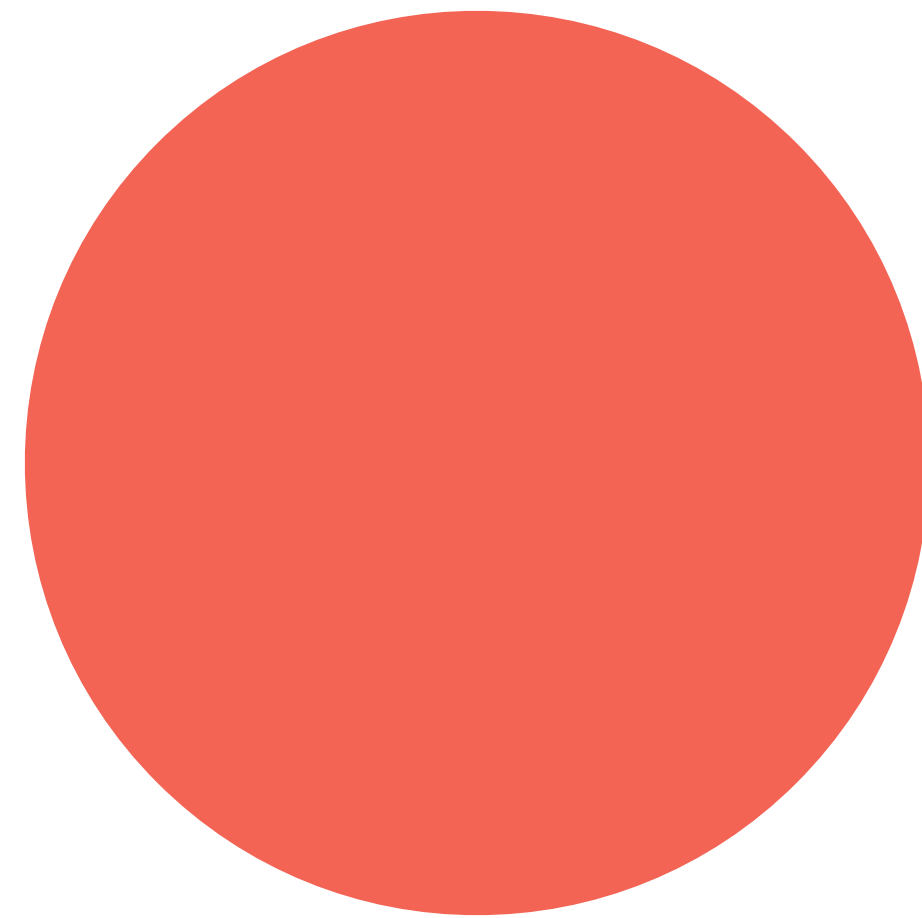
Veltmaat, Niemeyer, Schwabe (18)



An intuitive understanding of the granule structure:

Quasiparticle

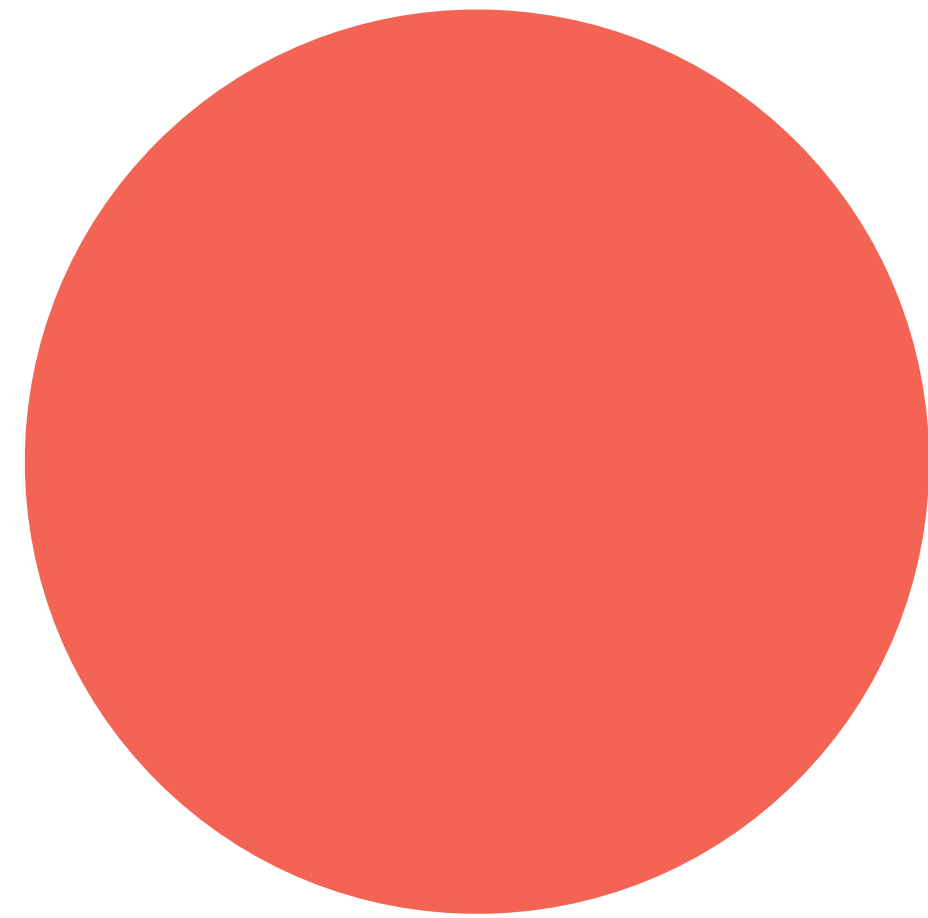
[Hui et al 17]



$$\ell \sim \lambda = \frac{1}{mv}$$

$$m_{\text{eff}} \sim \rho_{\text{DM}} \ell^3$$

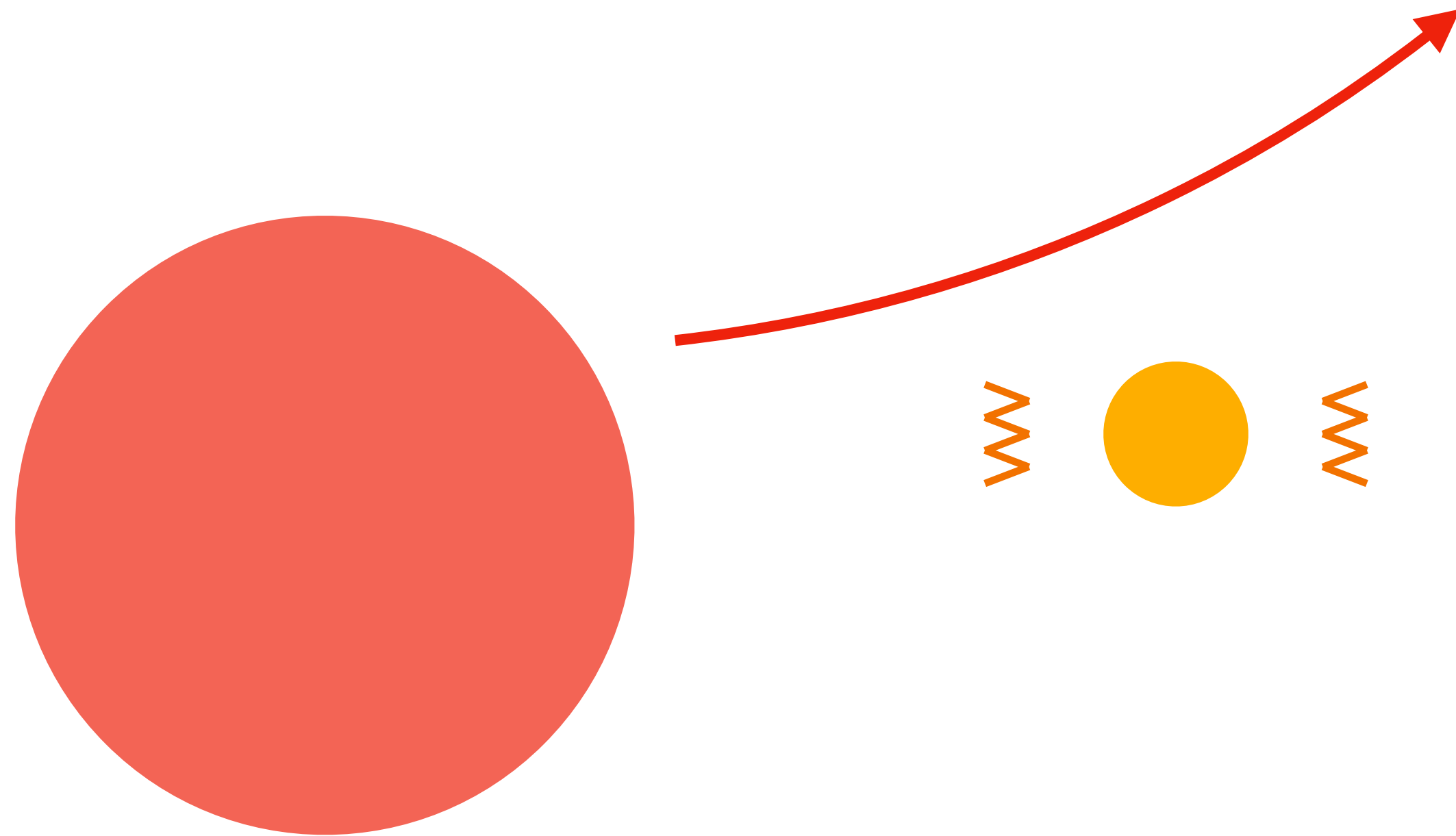
the size and mass of them could be astronomical



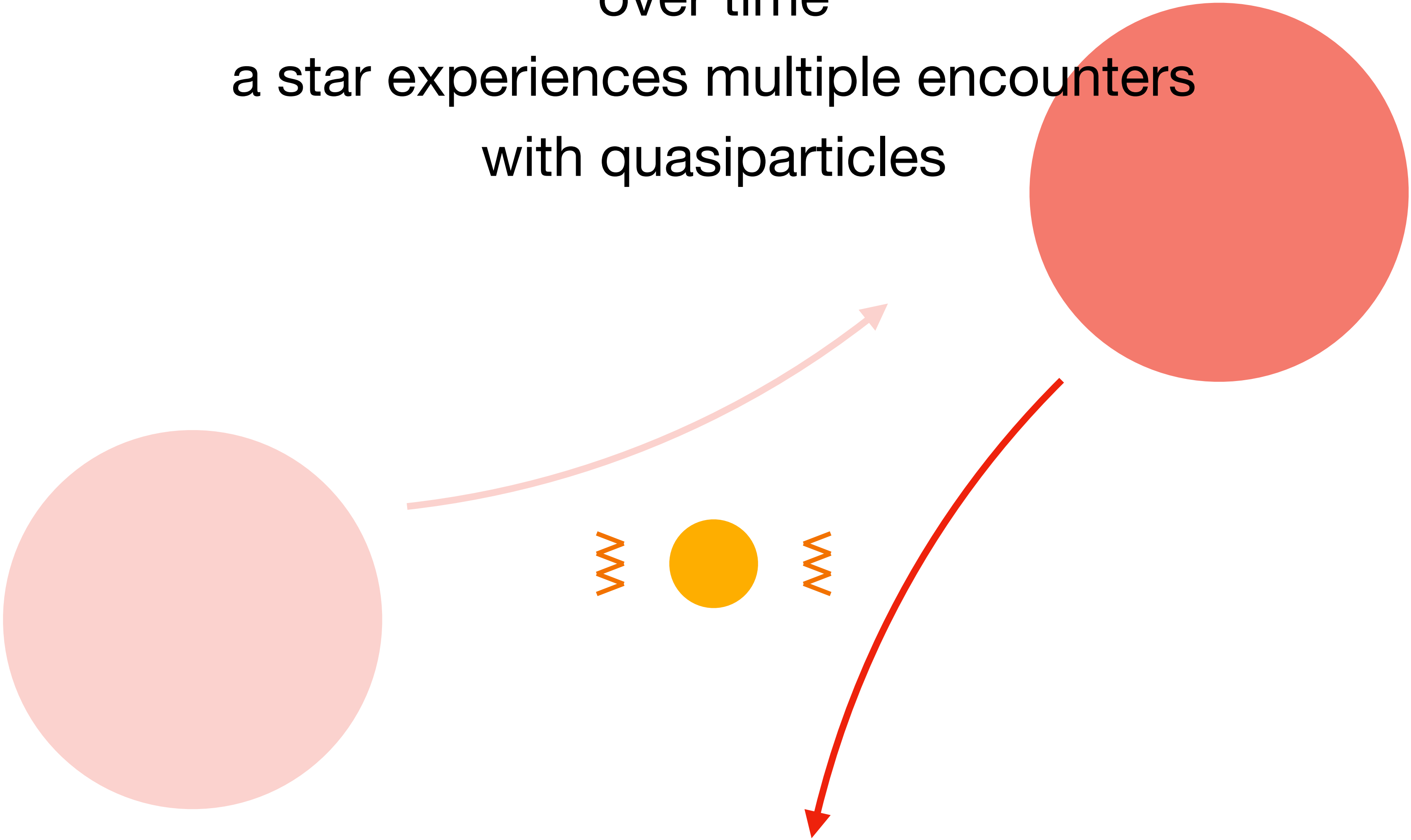
$$\ell \sim \lambda = \frac{1}{mv} \sim 10 \text{ AU} \times \left(\frac{10^{-16} \text{ eV}}{m} \right)$$

$$m_{\text{eff}} \sim \rho_{\text{DM}} \ell^3 \sim 10^{15} \text{ kg} \times \left(\frac{10^{-16} \text{ eV}}{m} \right)^3$$

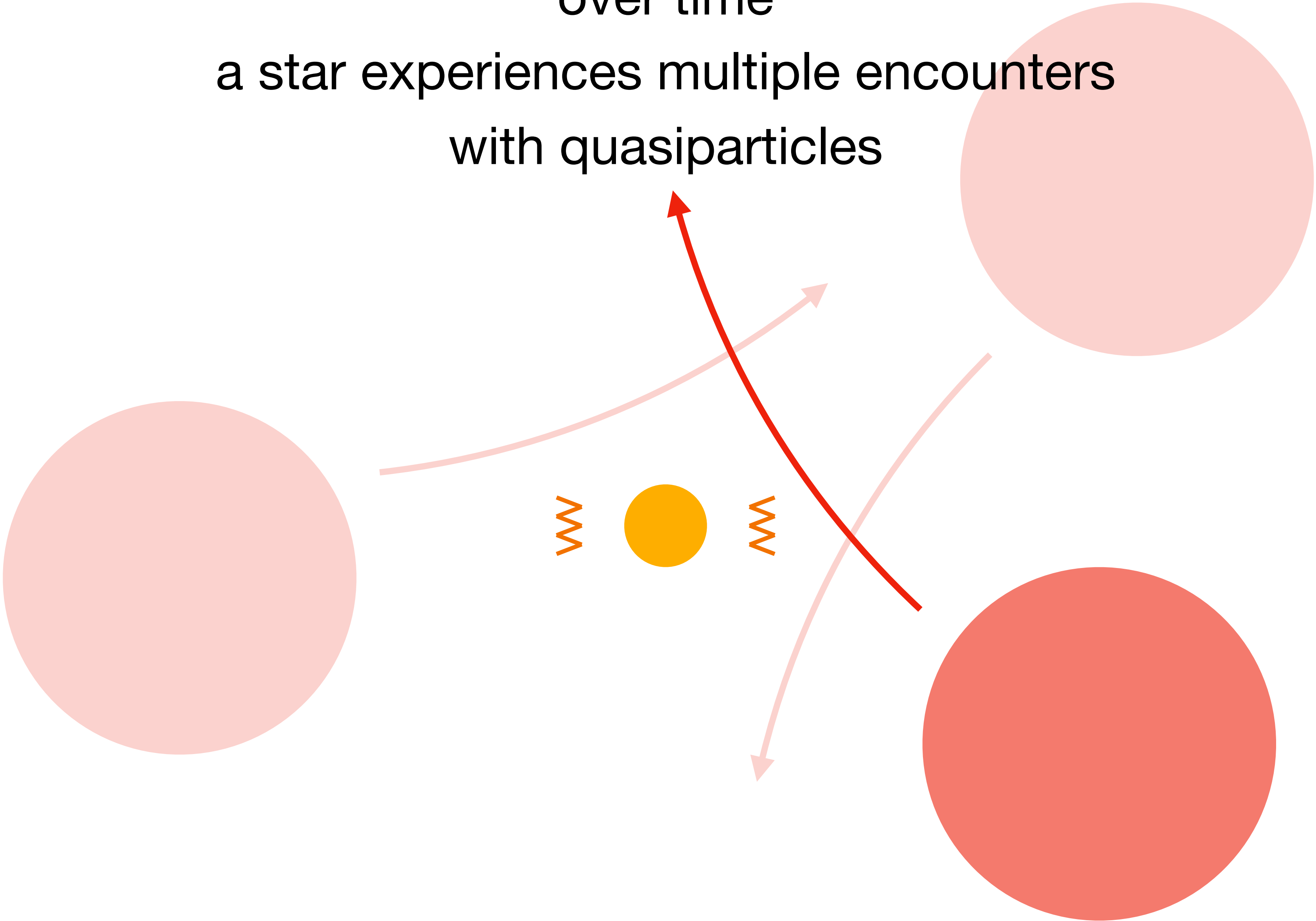
being that massive
it may engage in interaction with stars
and significantly perturb the motion of them



over time
a star experiences multiple encounters
with quasiparticles



over time
a star experiences multiple encounters
with quasiparticles



so what?

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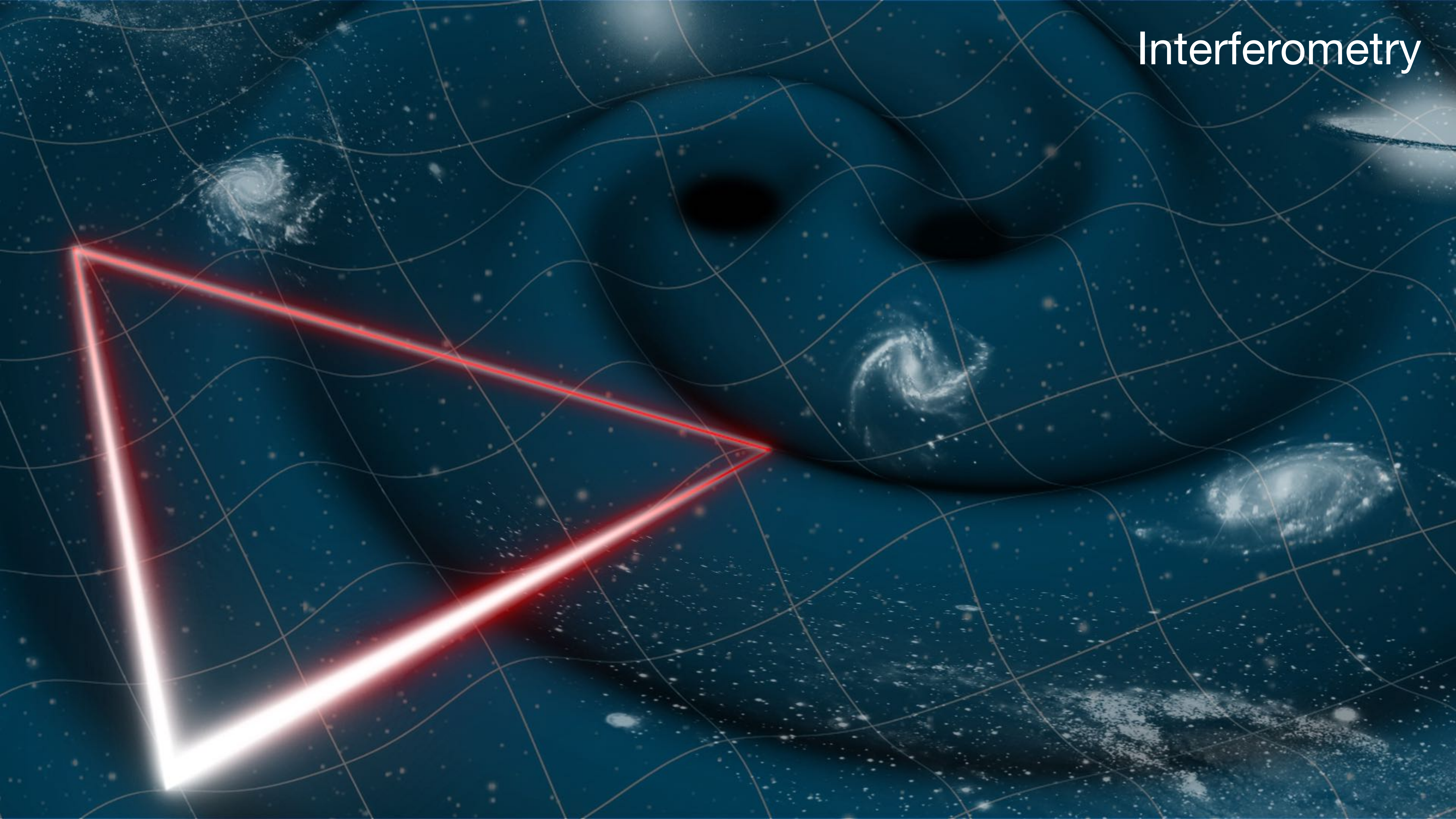
quasiparticles *bombards* normal matters,
leaving *distinctive stochastic signals* in *GW detectors*



so what?

quasiparticles *bombards* normal matters,
leaving *distinctive stochastic signals* in *GW detectors*

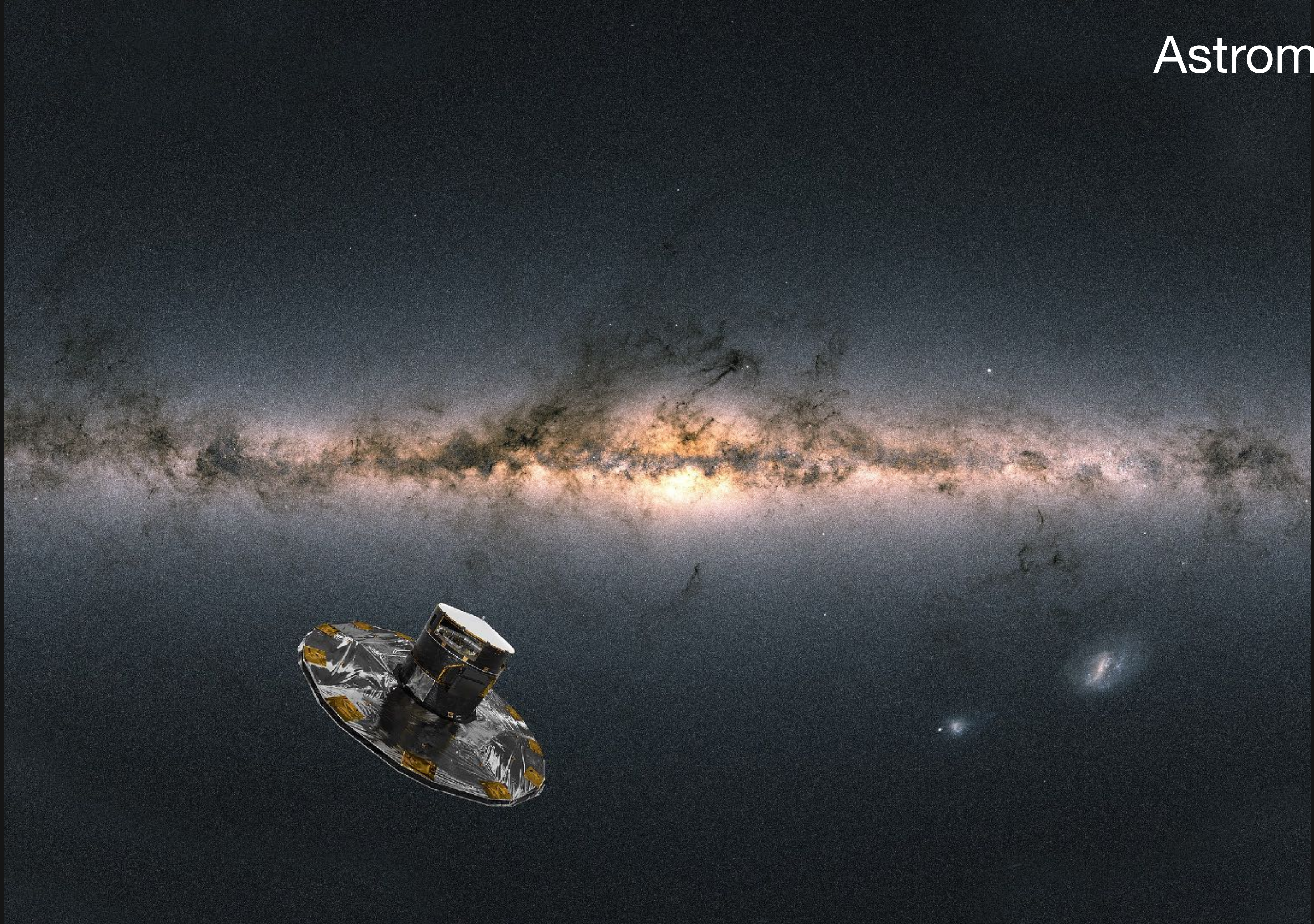
Interferometry

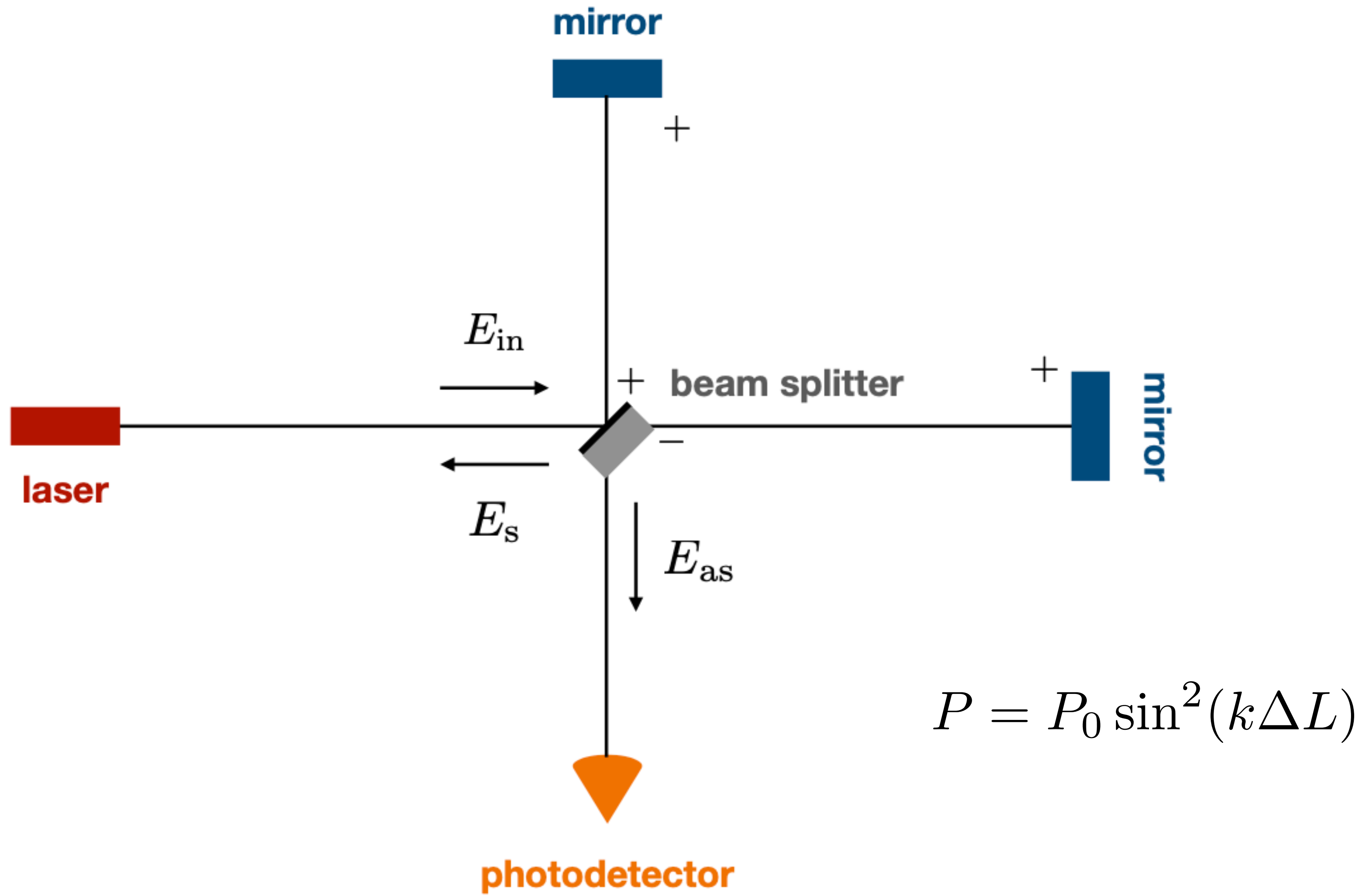


Pulsar Timing Array



Astrometry

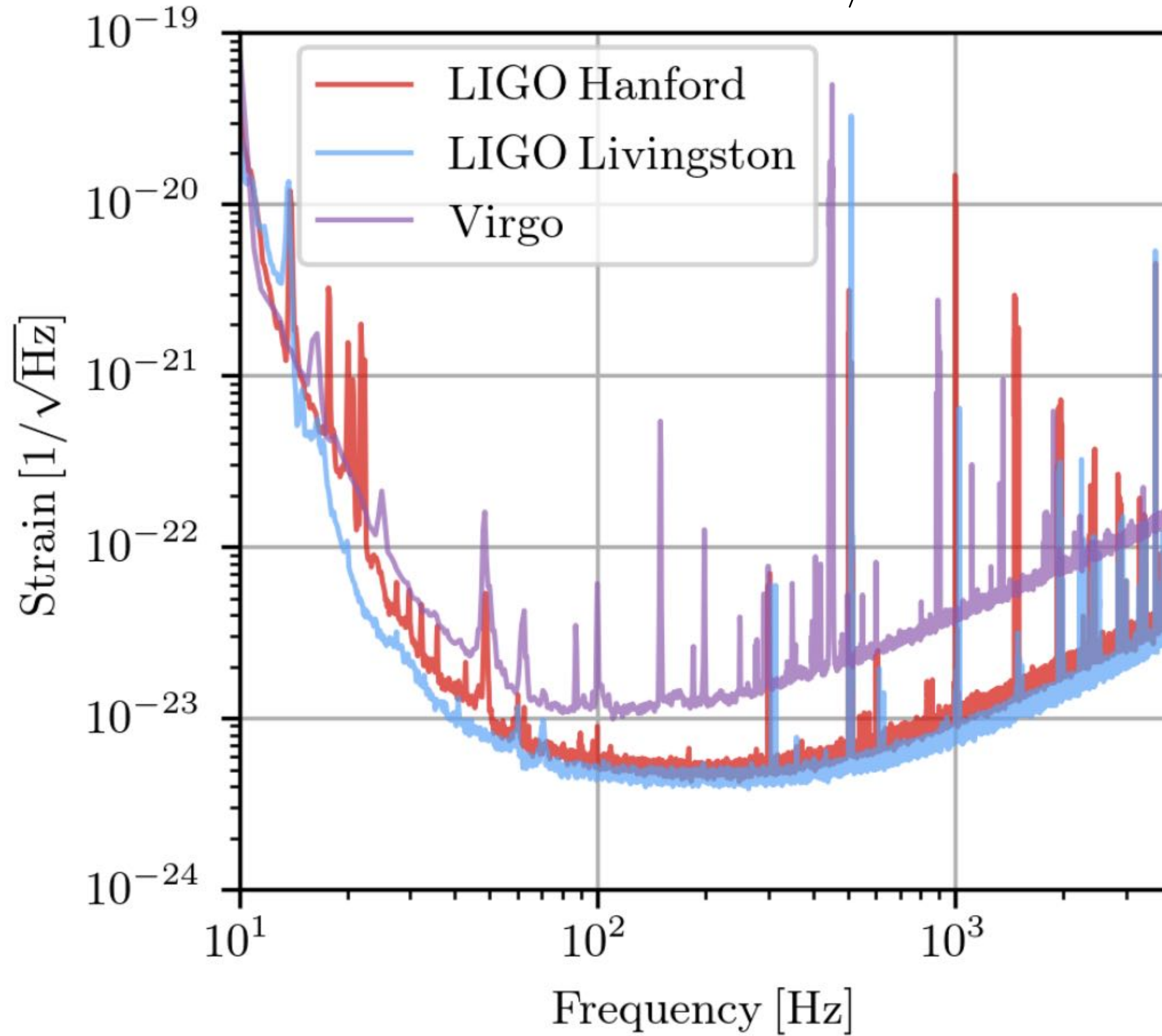


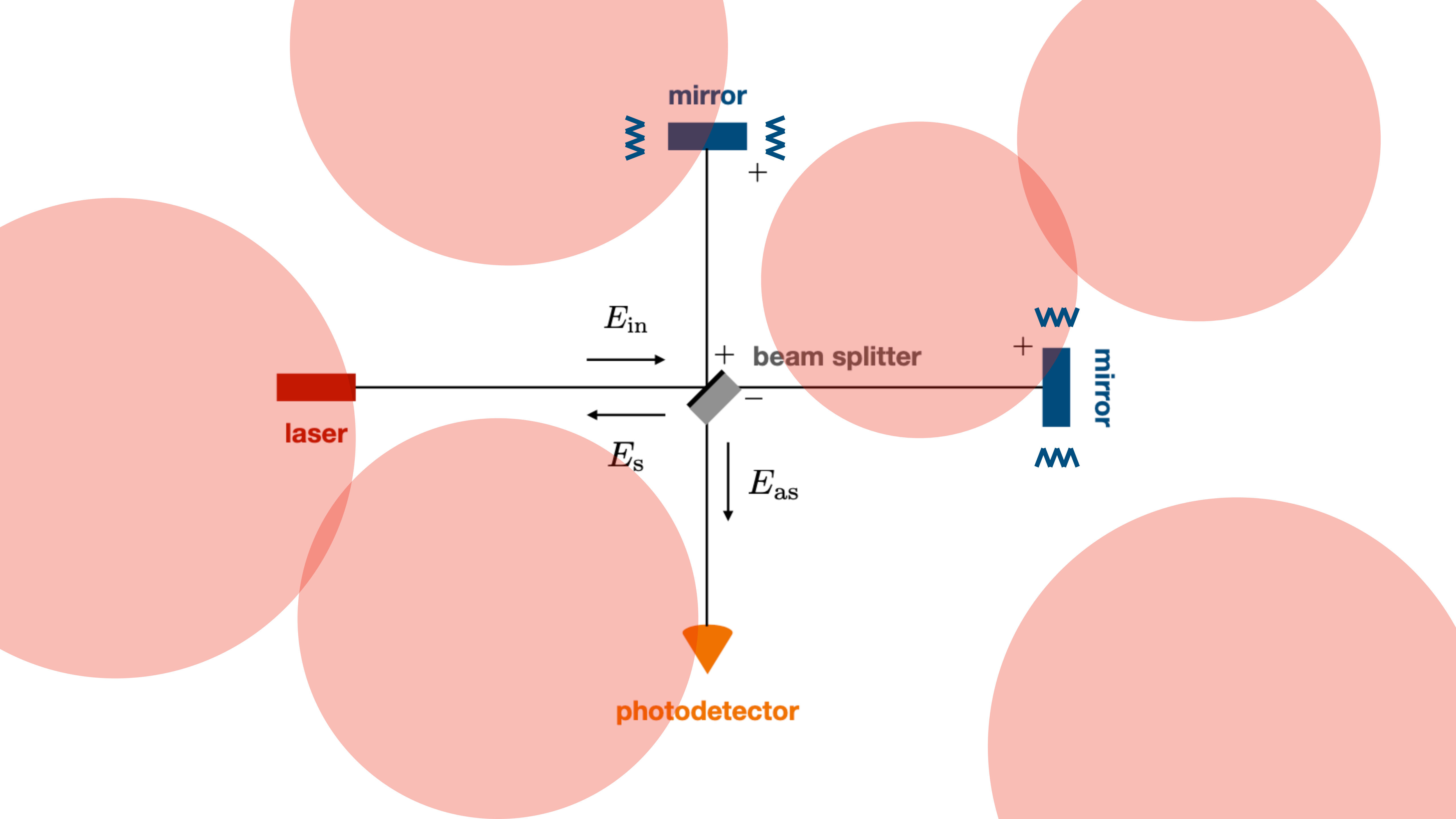




$$S_n^{1/2}(f) \sim S_{\Delta L/L}^{1/2}(f)$$

$$\langle x^2 \rangle = \int df S_x(f)$$





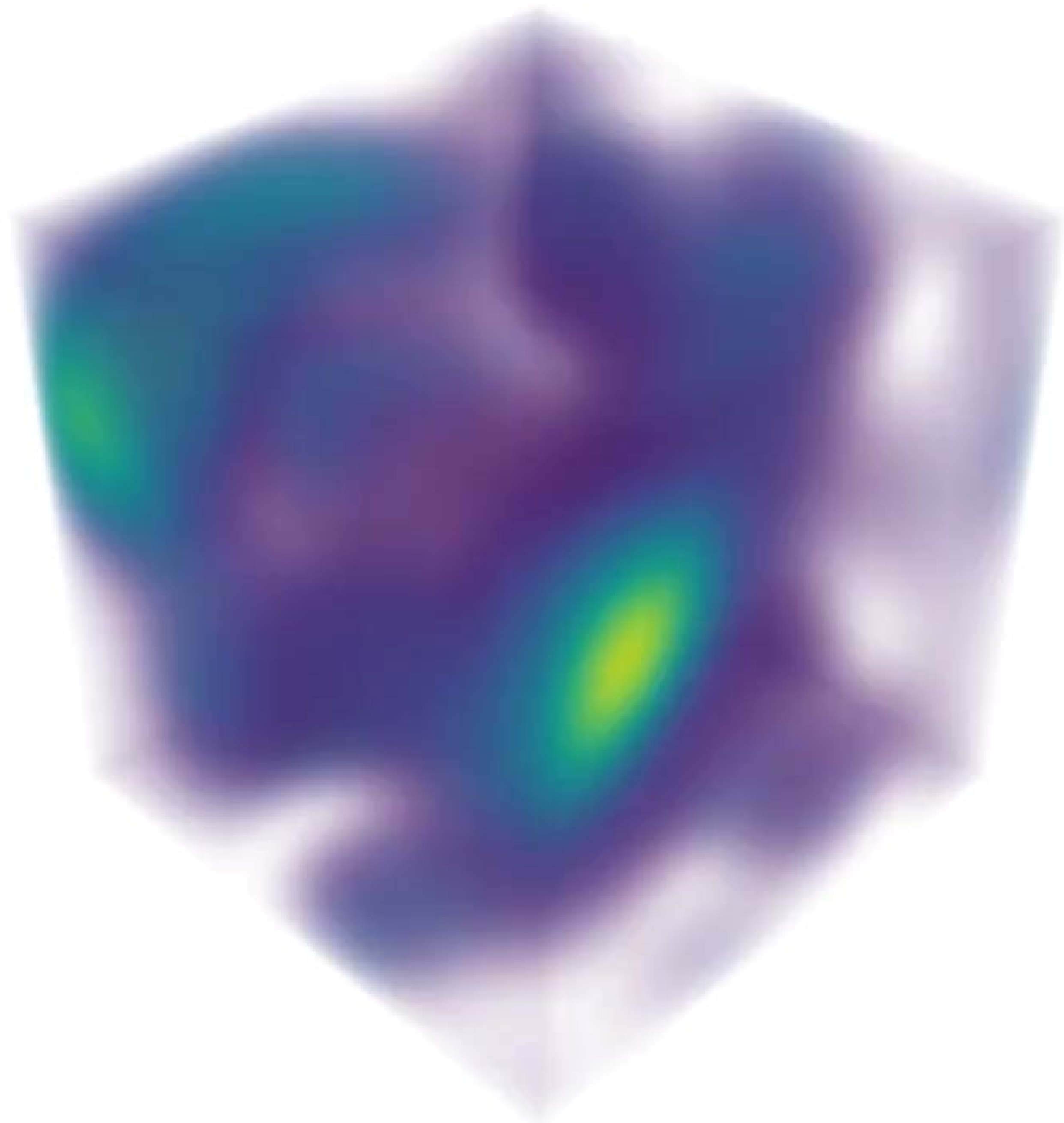
can we actually measure
ULDM signals with GW interferometers?

$$\ddot{x} = -\nabla\Phi$$

$$\nabla^2\Phi = 4\pi G\rho$$

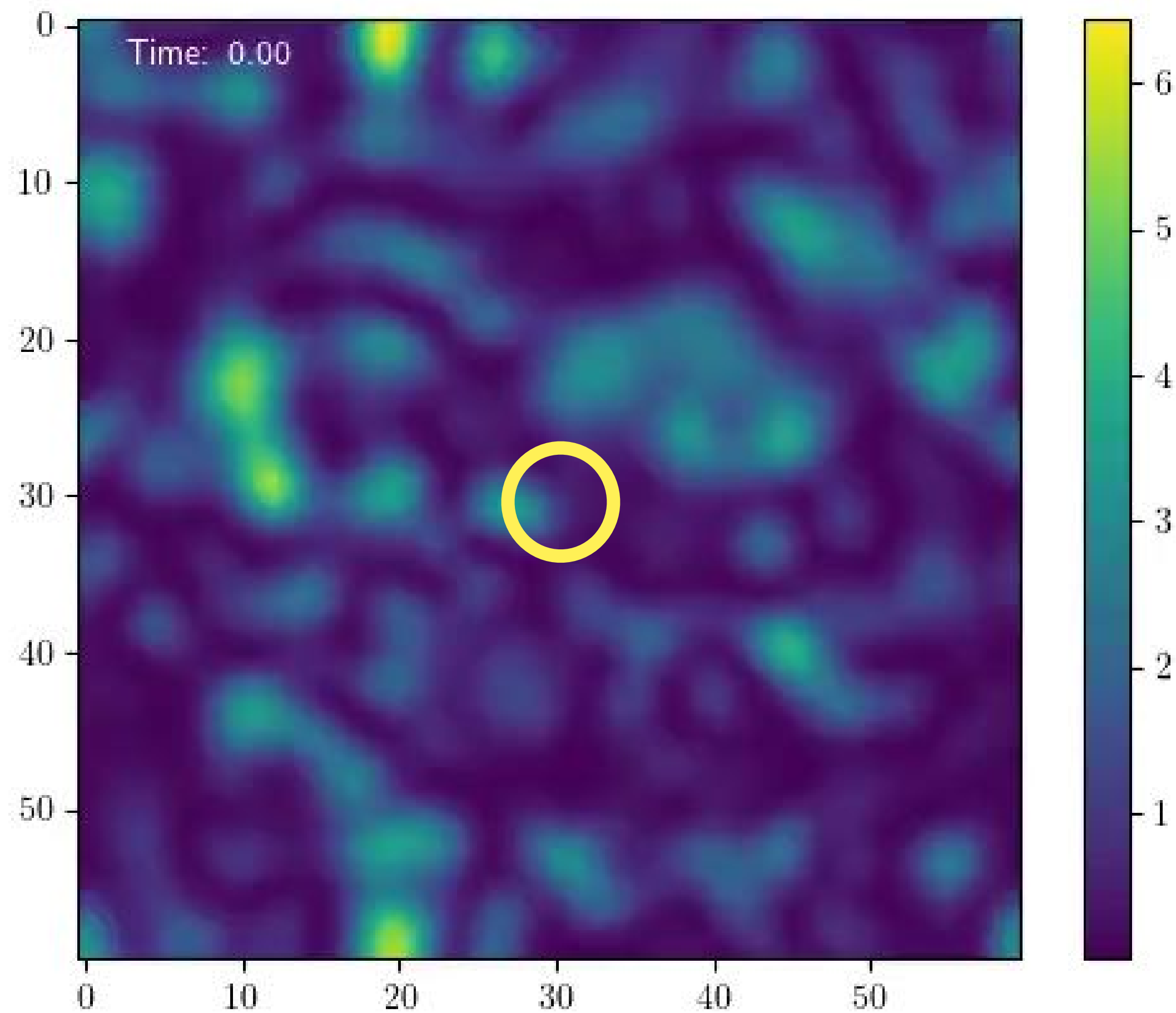
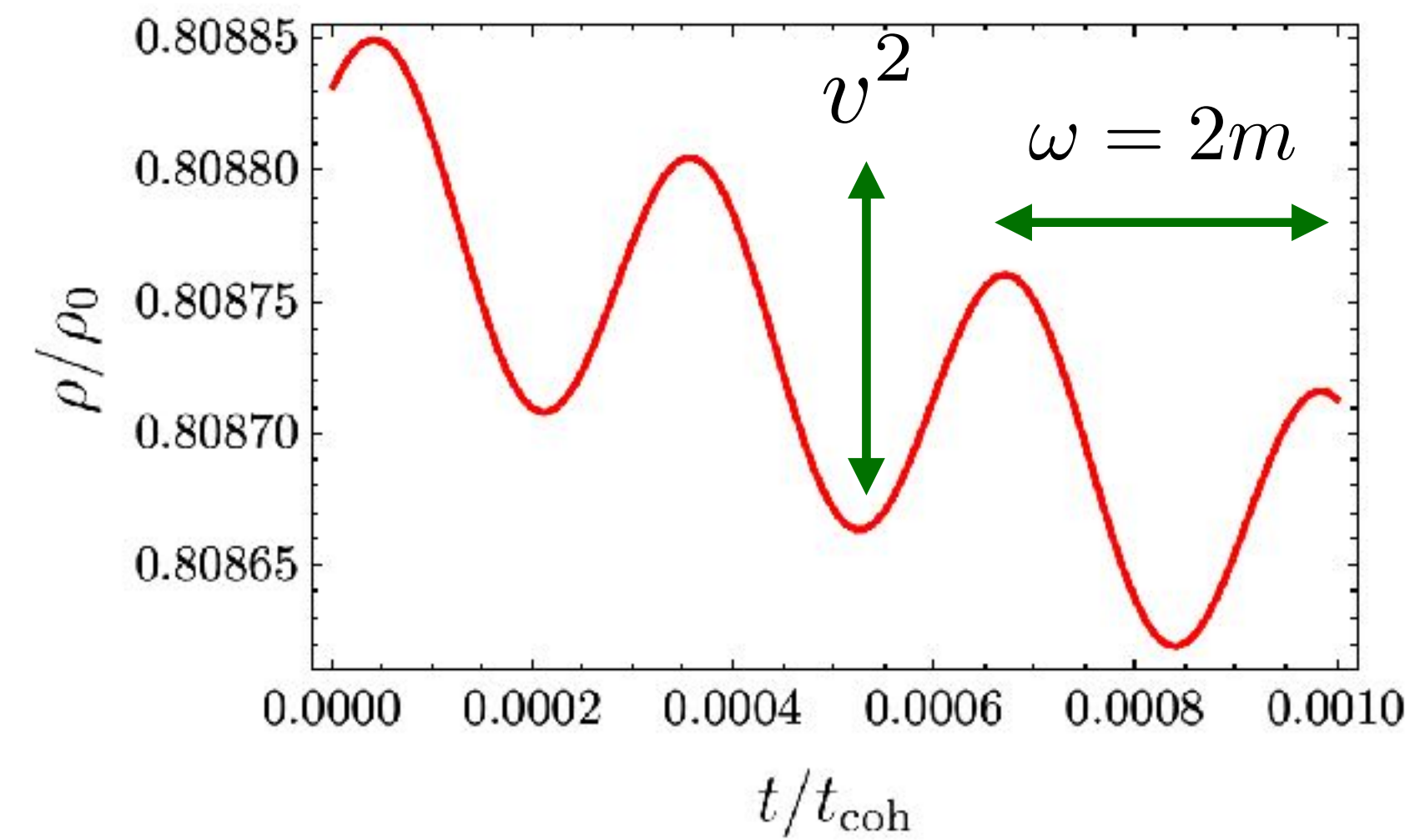


what is reflected in *detector observables*
is the *statistical properties of density fluctuations of ULDM*

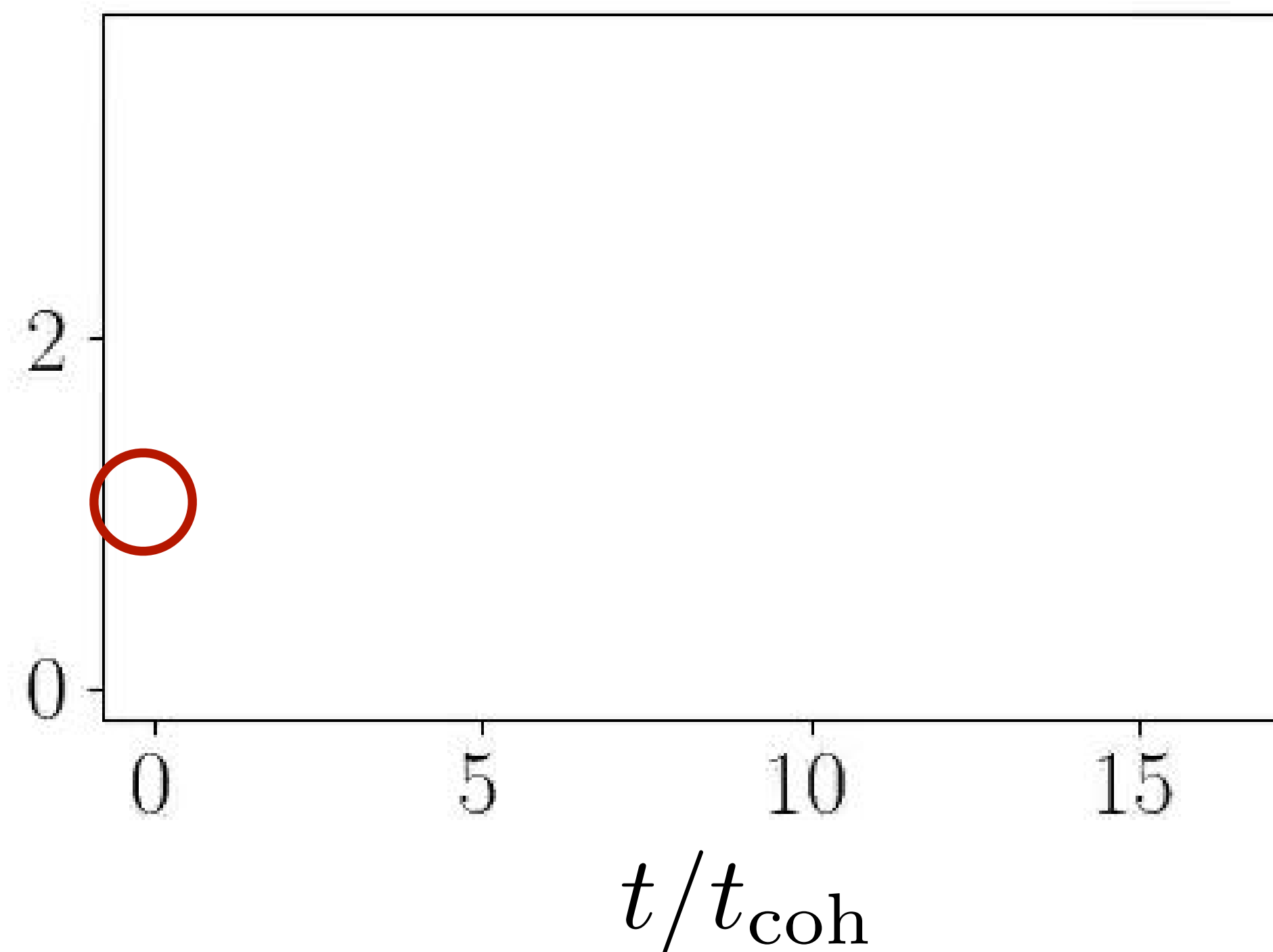


the density-density correlator at the same position is

$$\langle \delta(x)\delta(x) \rangle = \int \frac{d\omega}{2\pi} S_\delta(\omega)$$



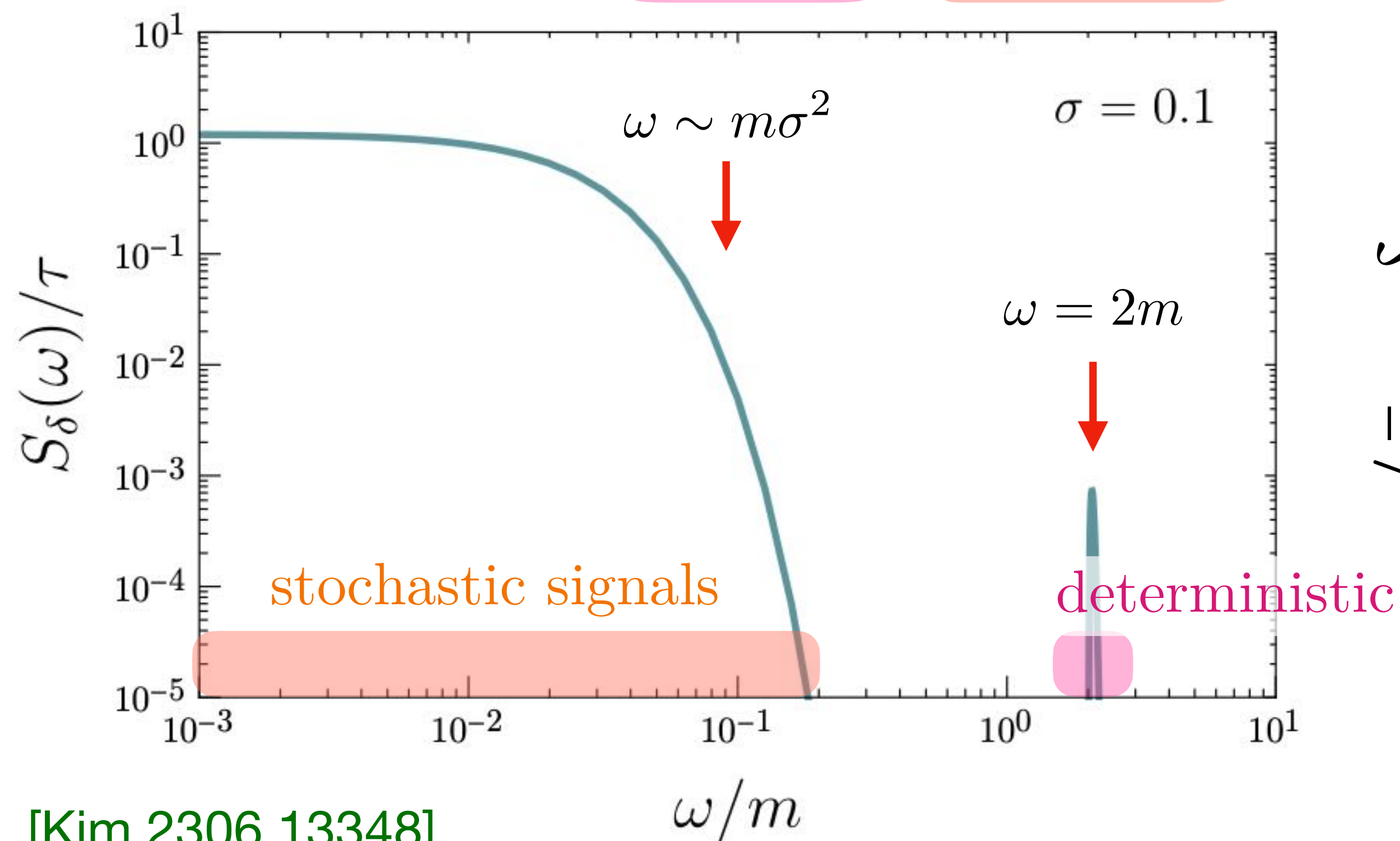
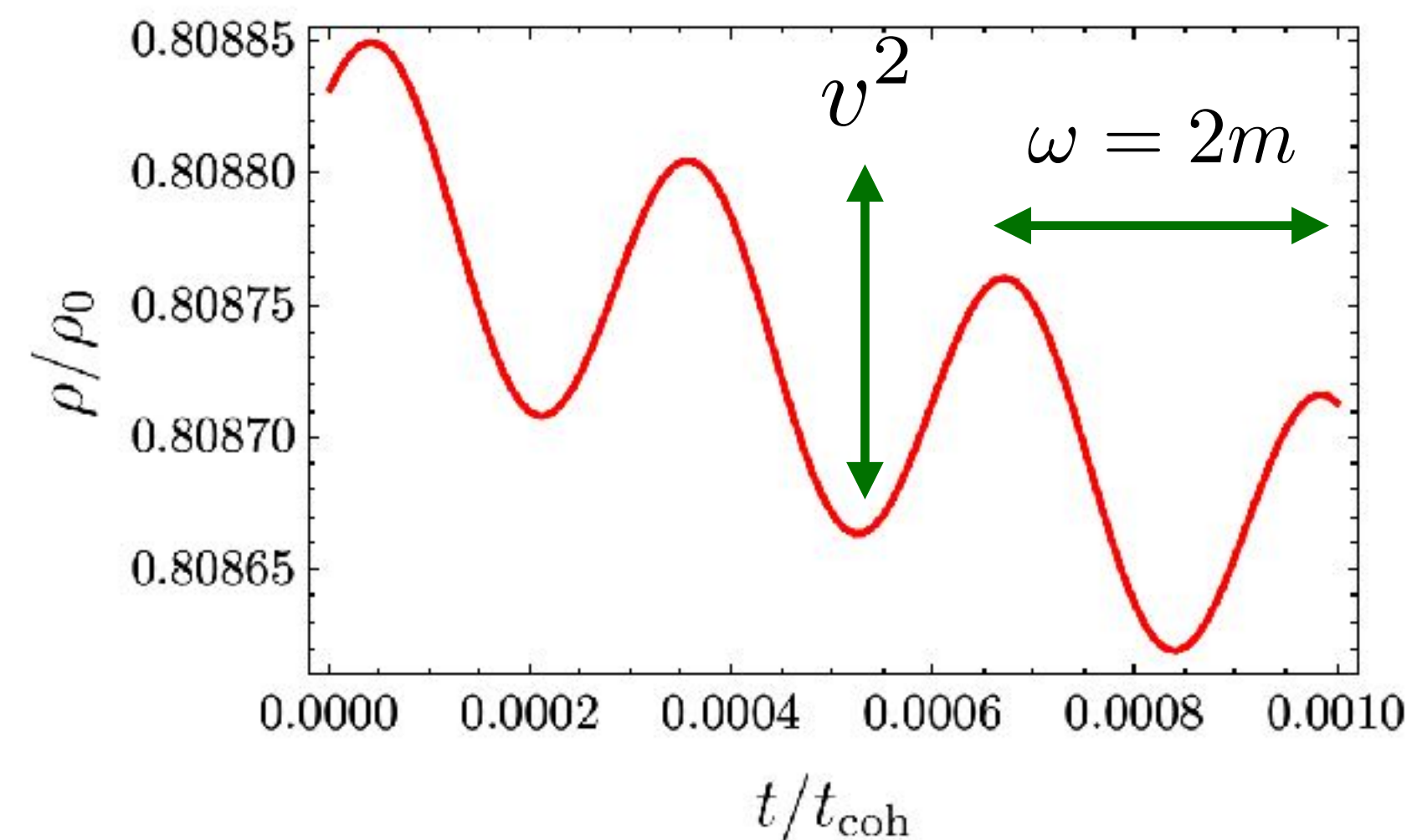
$$\rho/\bar{\rho} = \delta$$



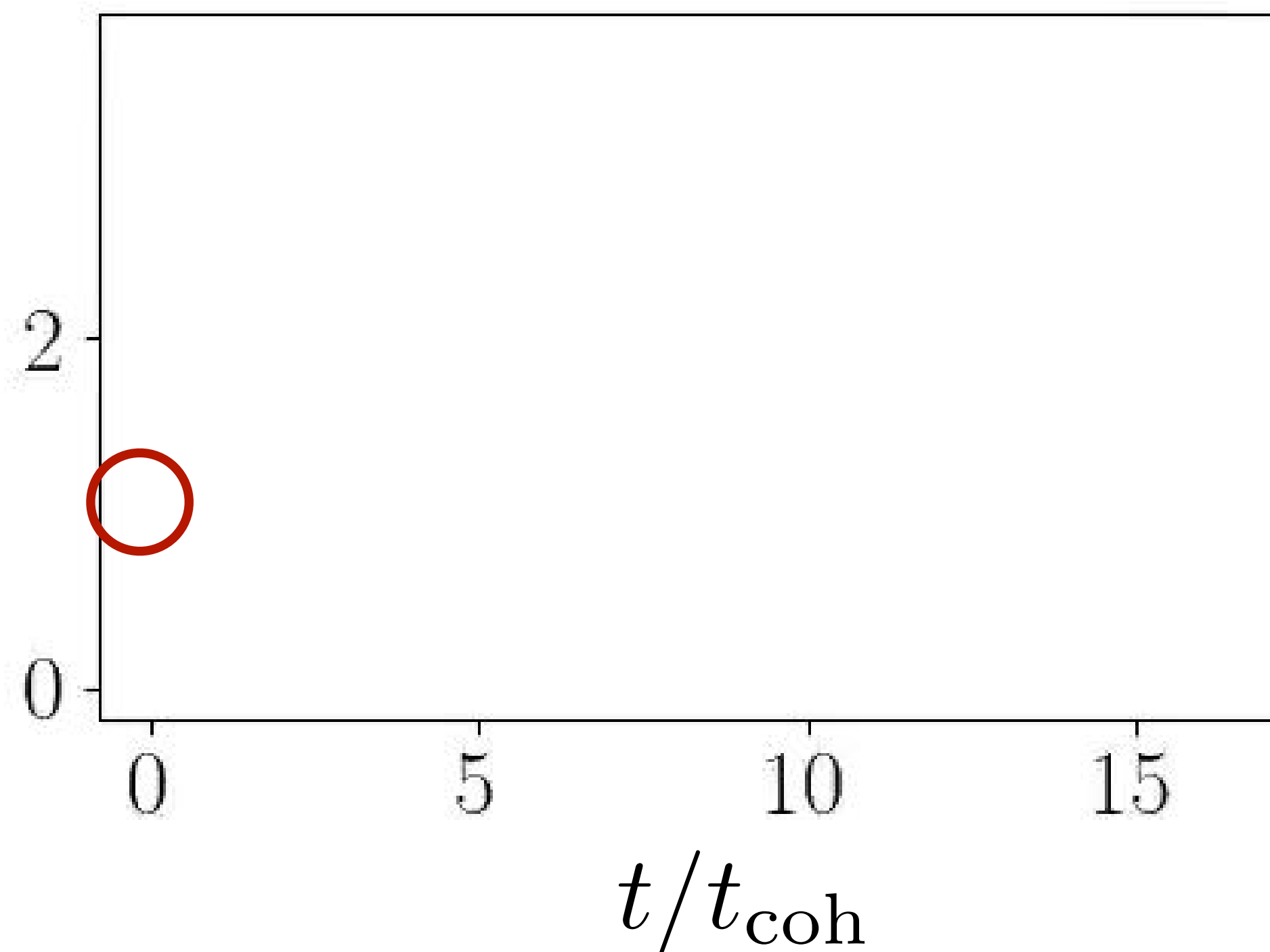
the density-density correlator at the same position is

$$\langle \delta(x)\delta(x) \rangle = \int \frac{d\omega}{2\pi} S_\delta(\omega)$$

$$S_\delta(\omega) = \tau [\sigma^4 A_\delta(\omega) + B_\delta(\omega)]$$

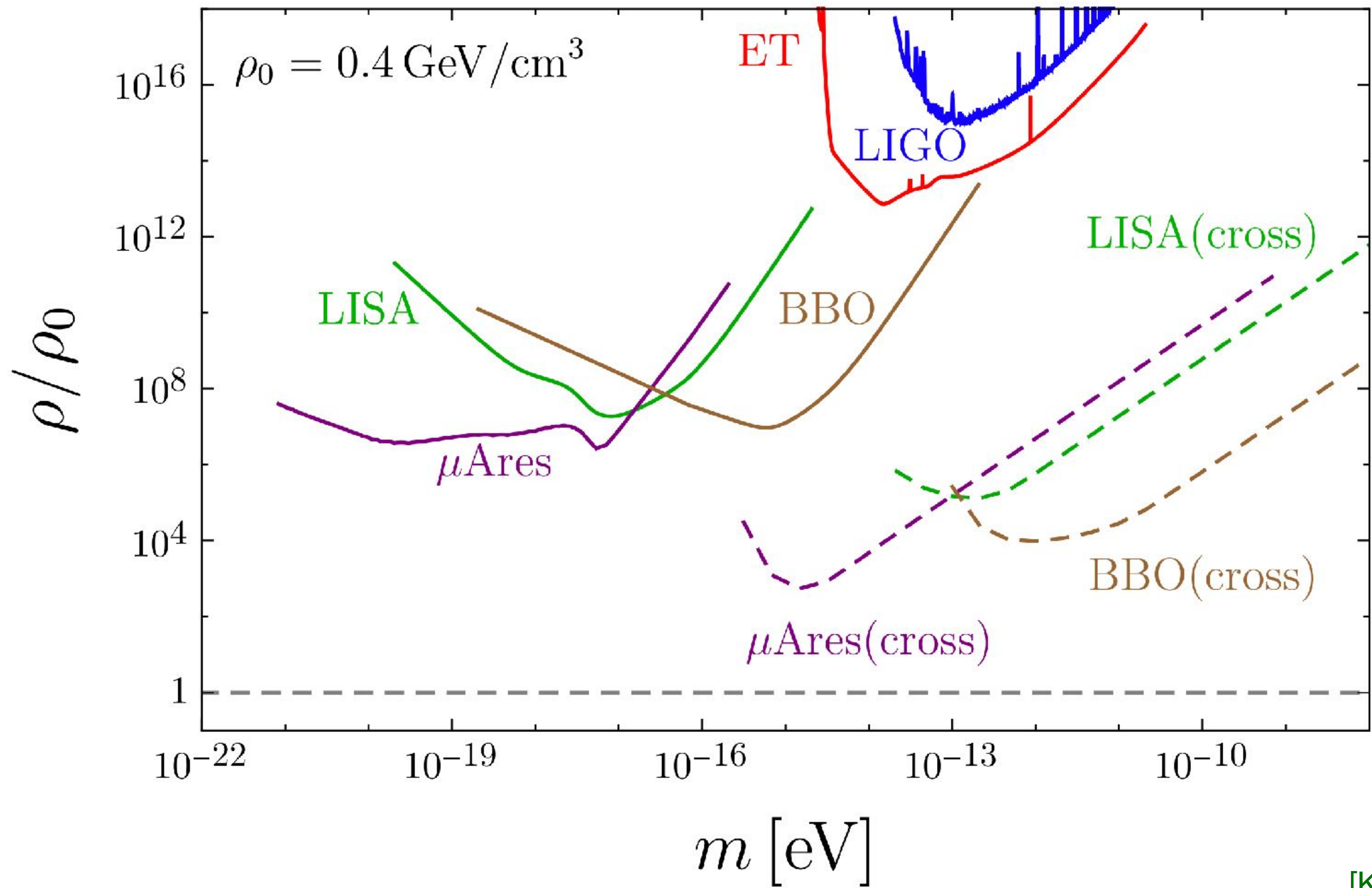


$$\rho/\bar{\rho} = \delta$$



[Kim 2306.13348]

[Kim, Lenoci, Perez, Ratzinger, 2307.14962]

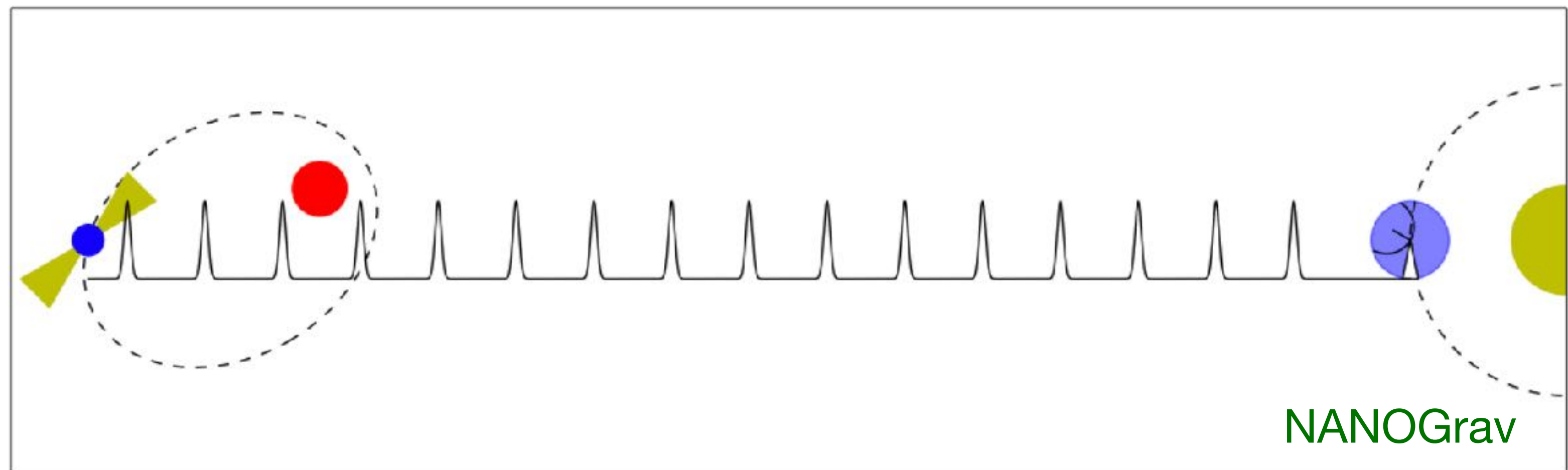


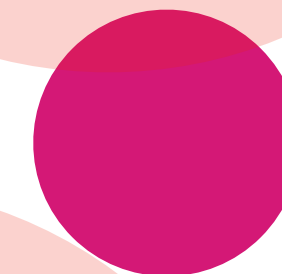
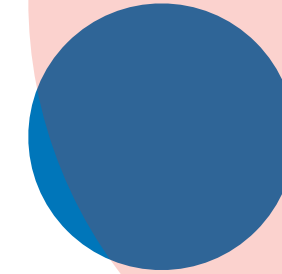
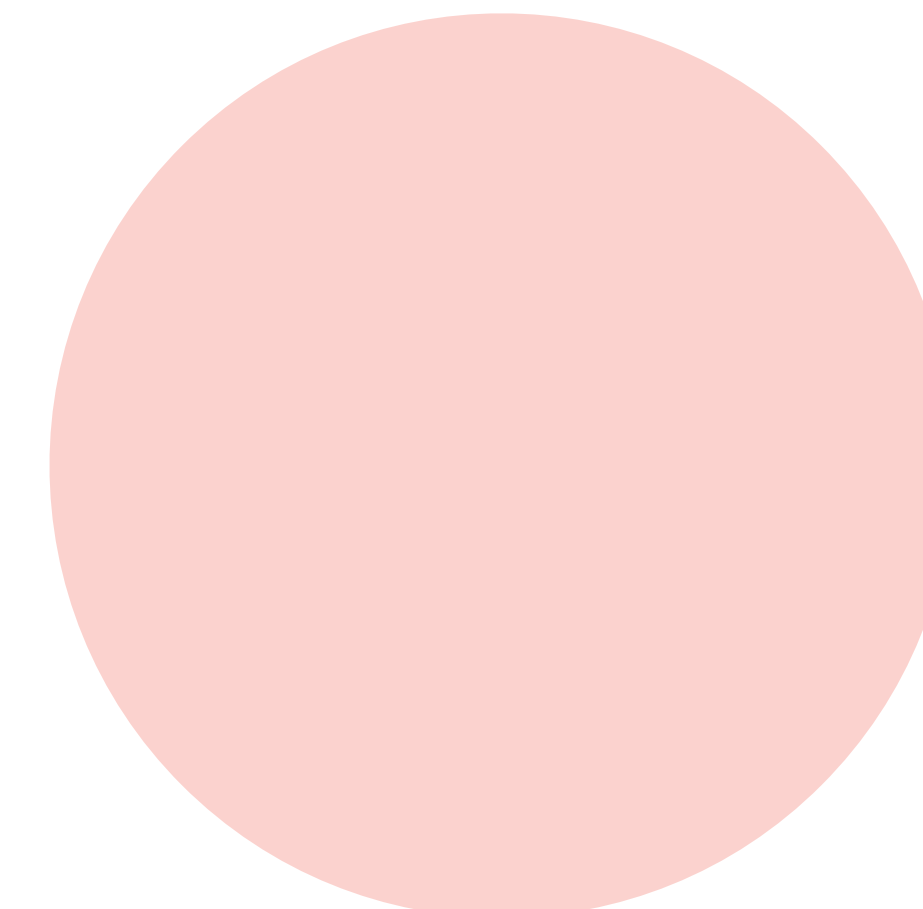
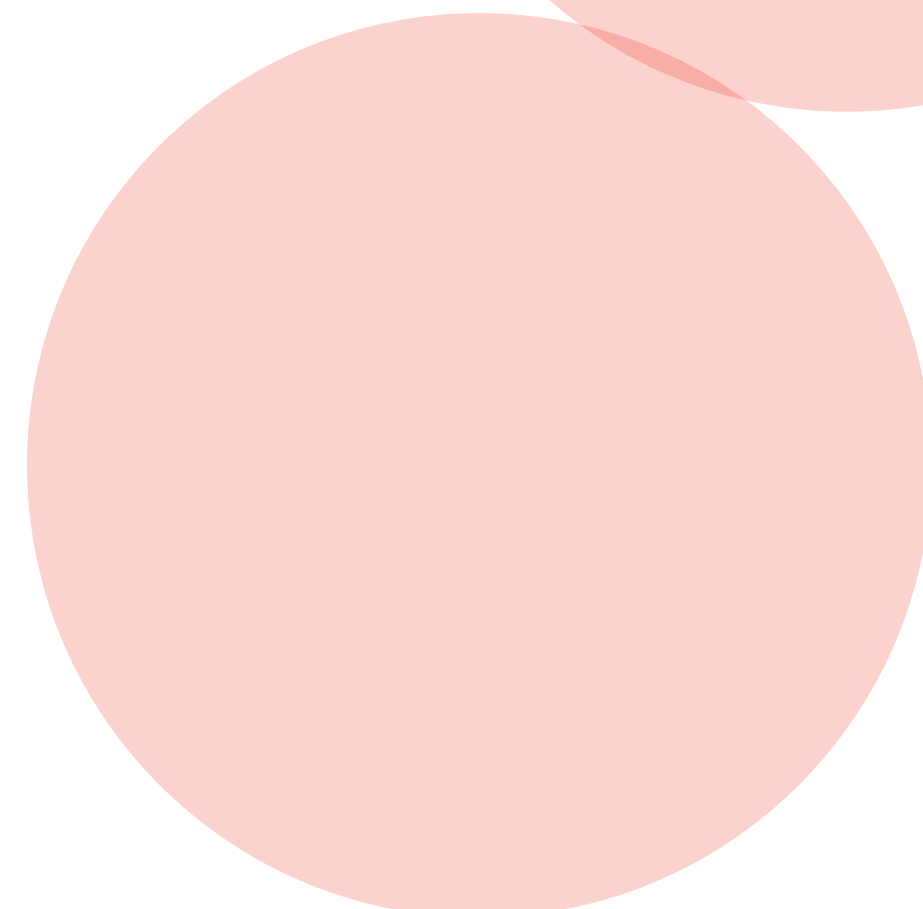
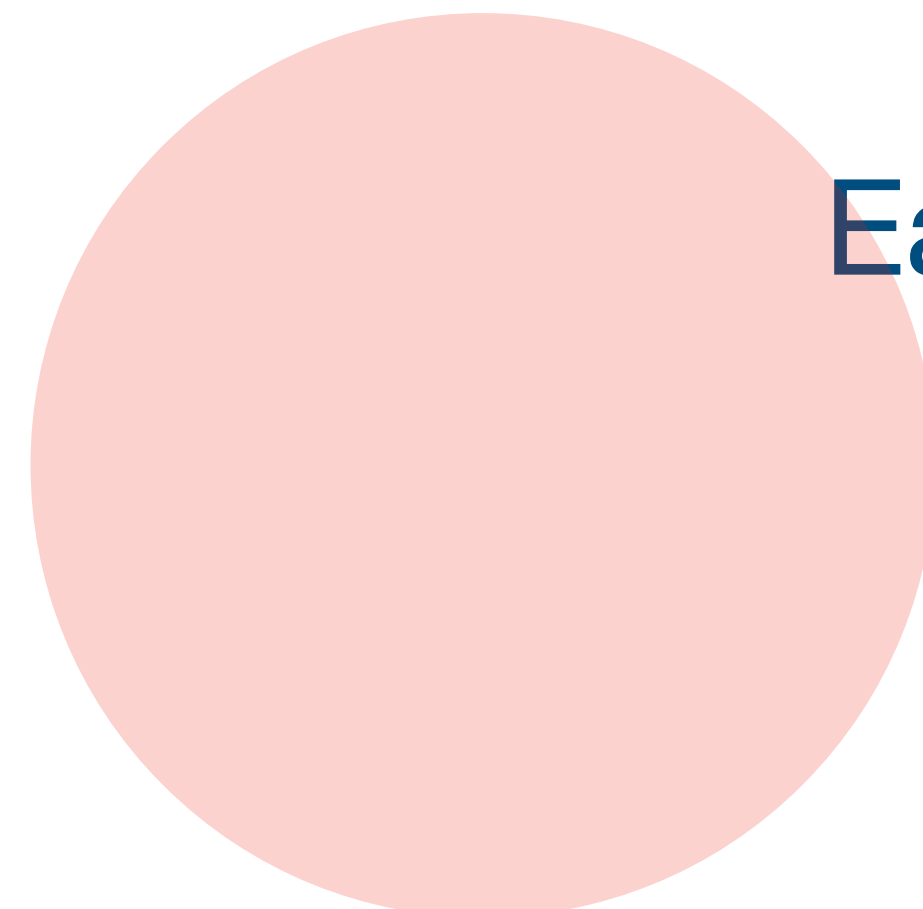
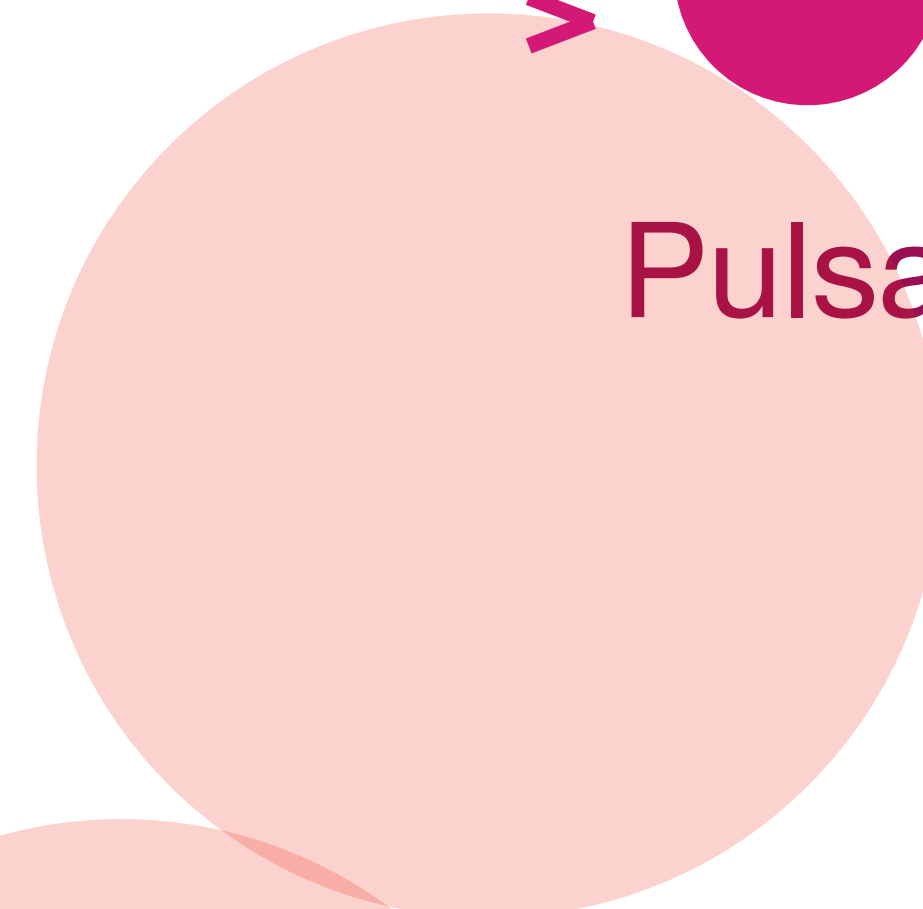
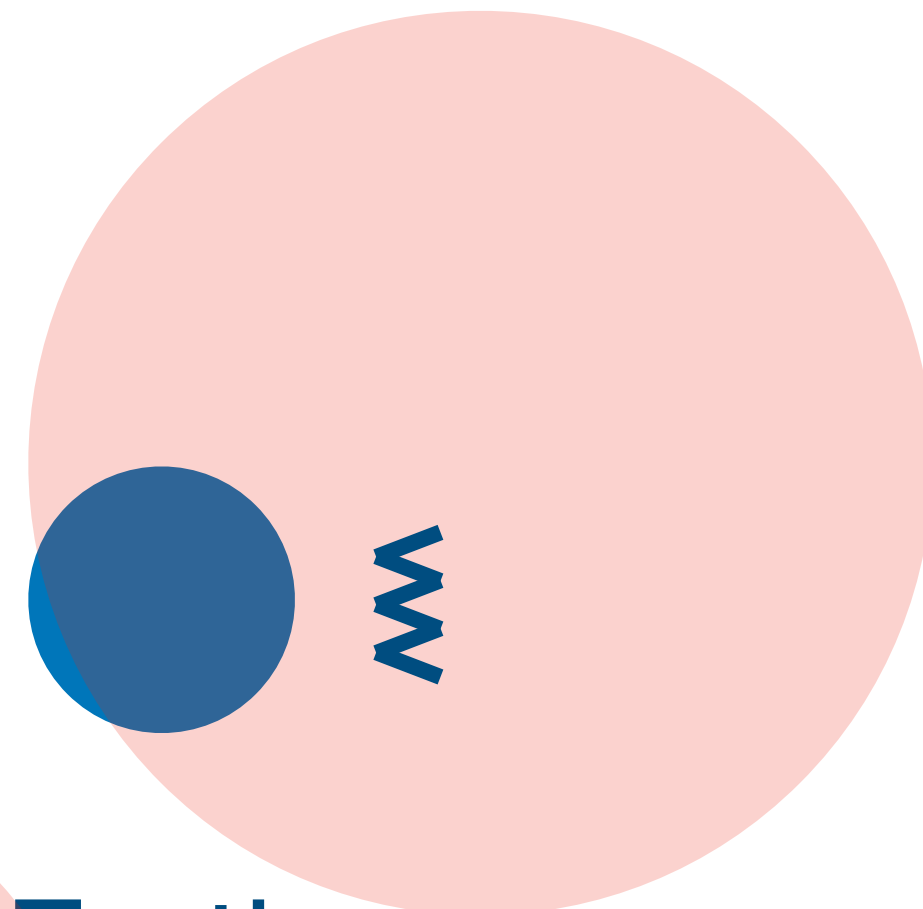
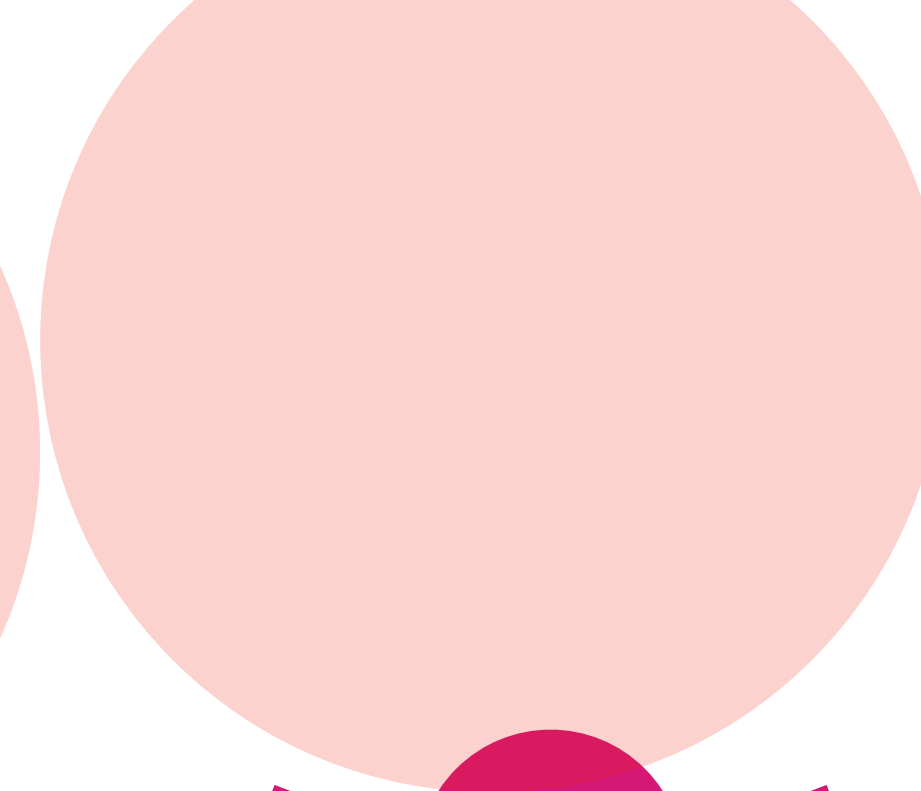
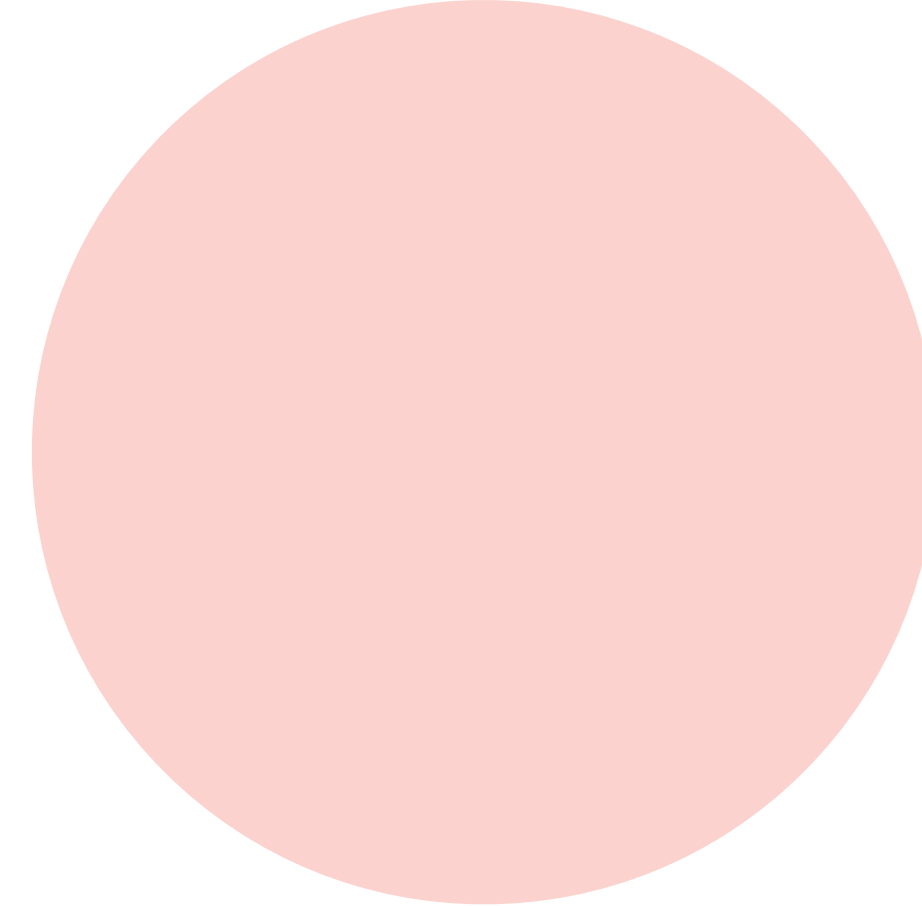
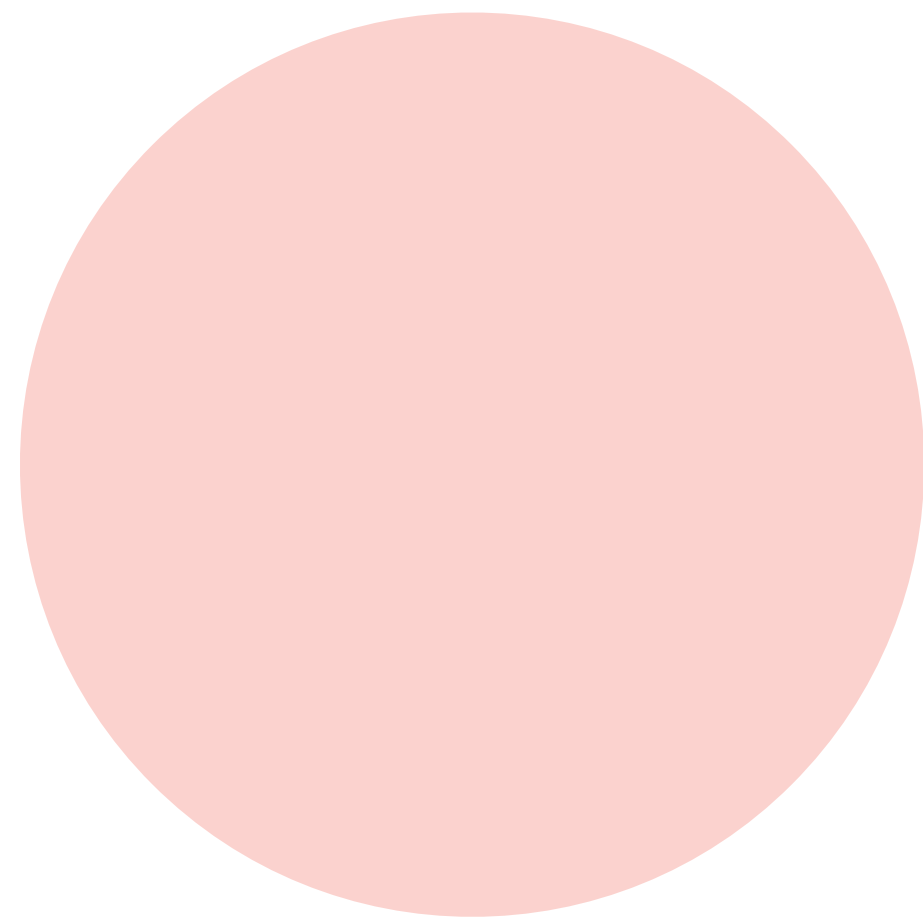
another example:

Pulsar Timing Array

Earth

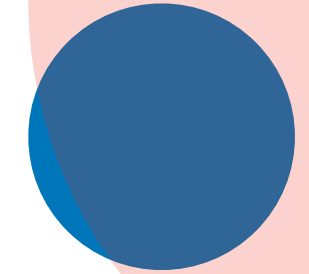
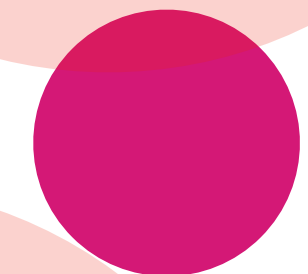
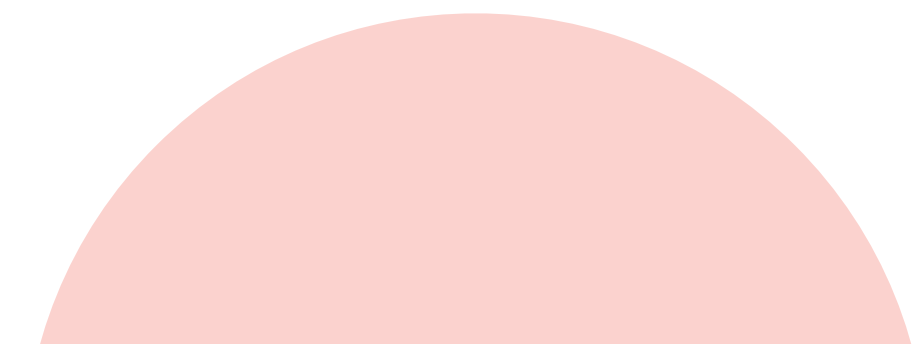
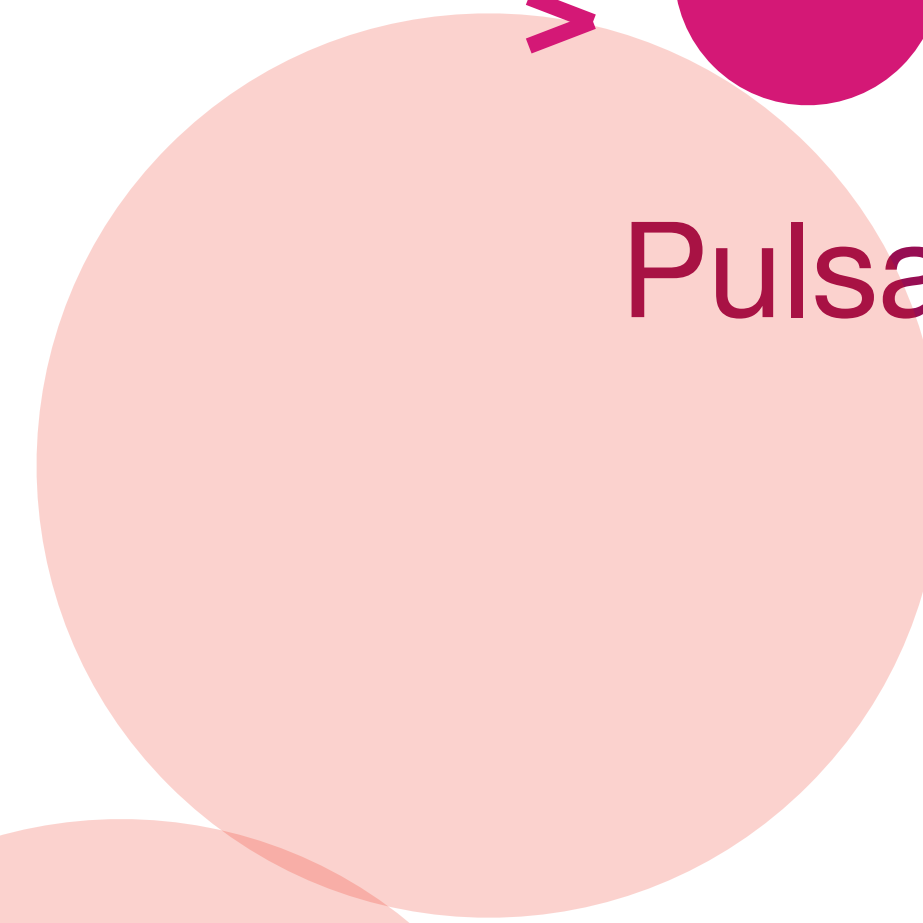
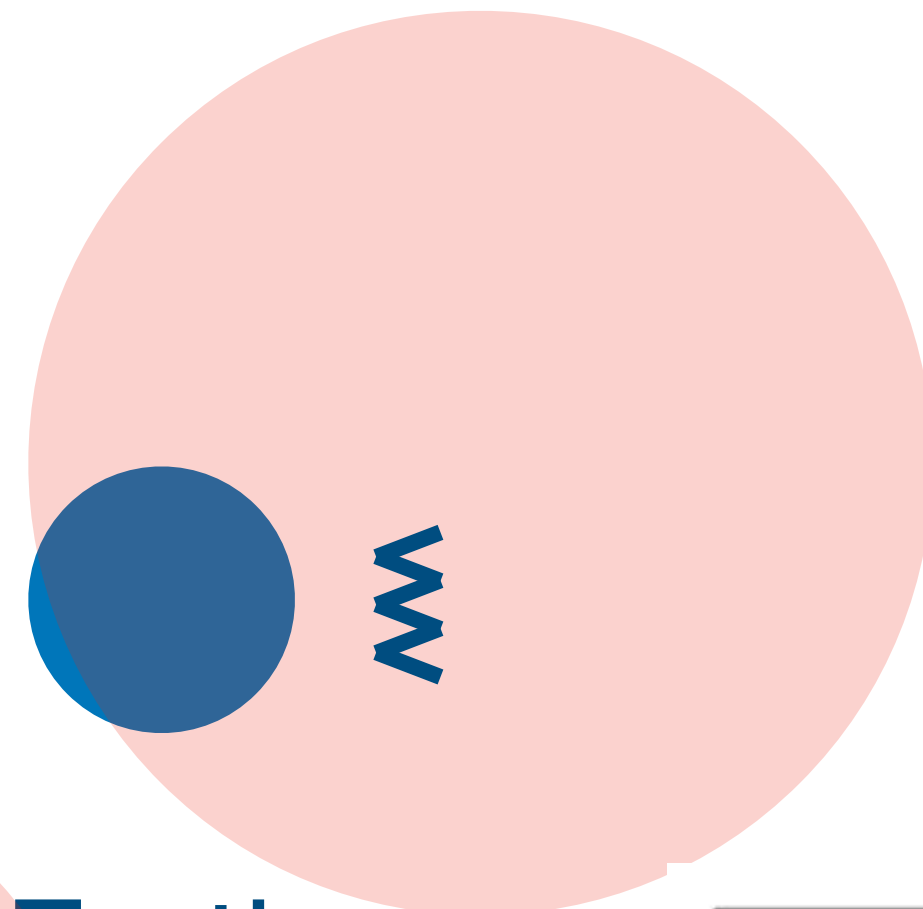
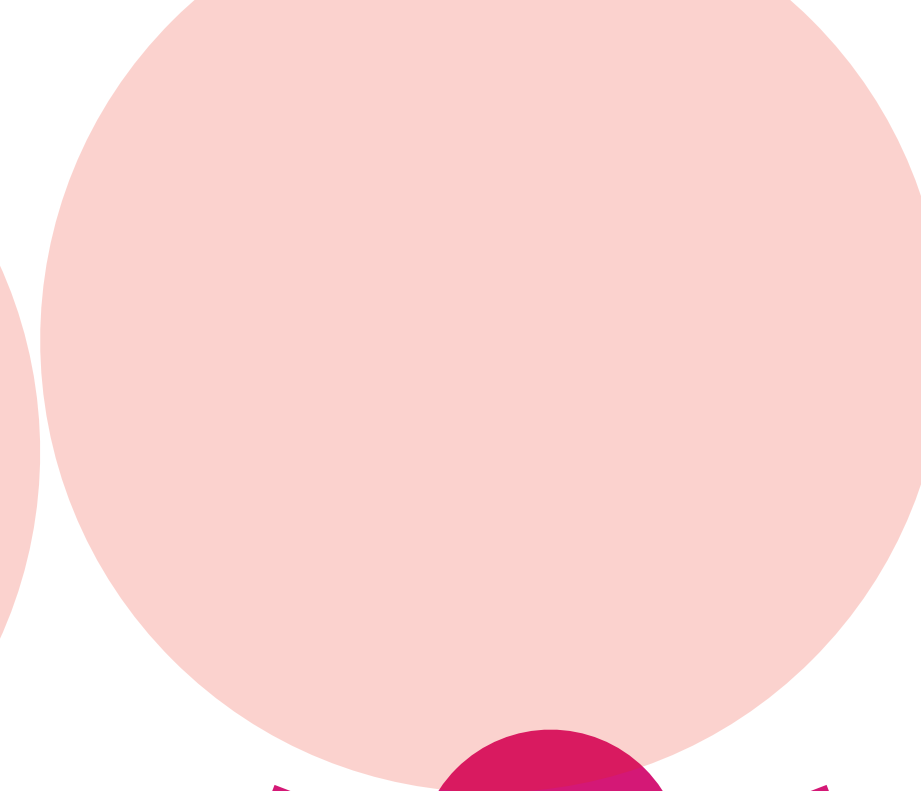
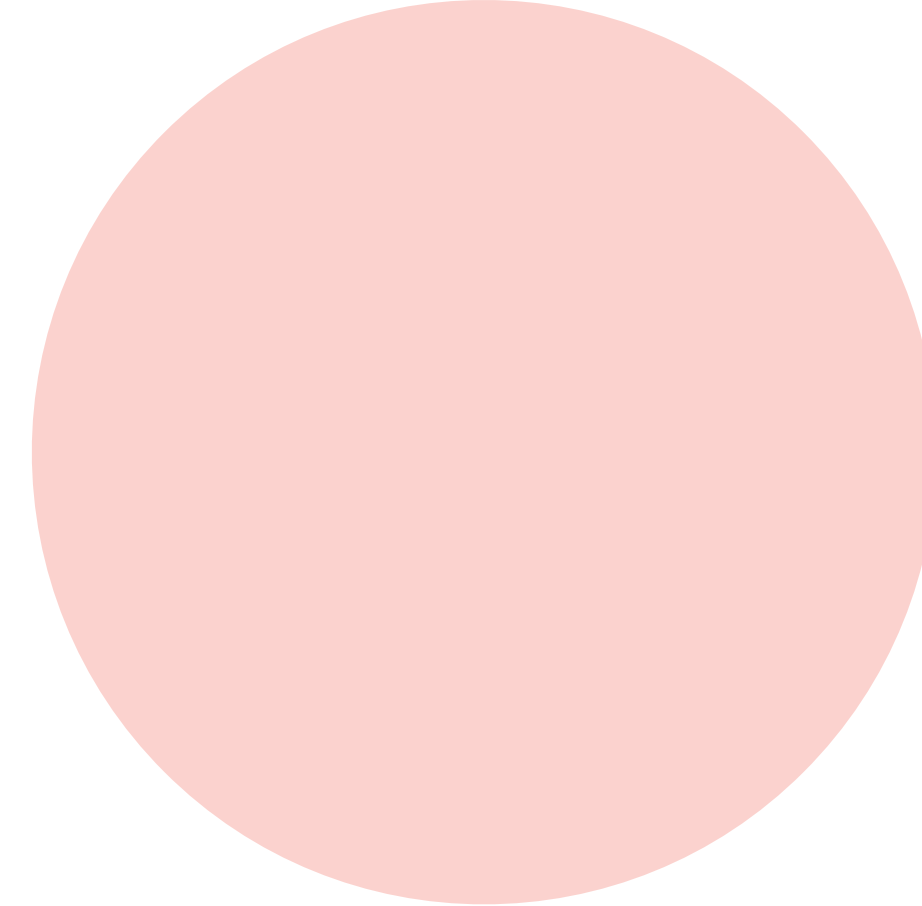
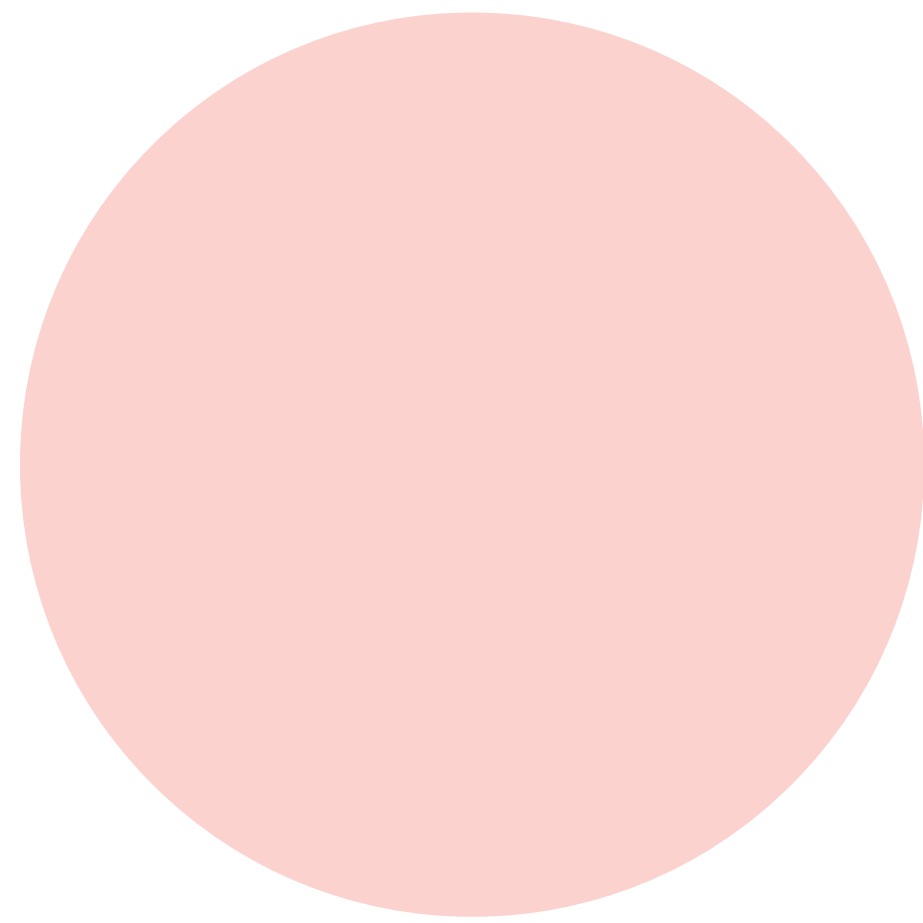
Pulsar





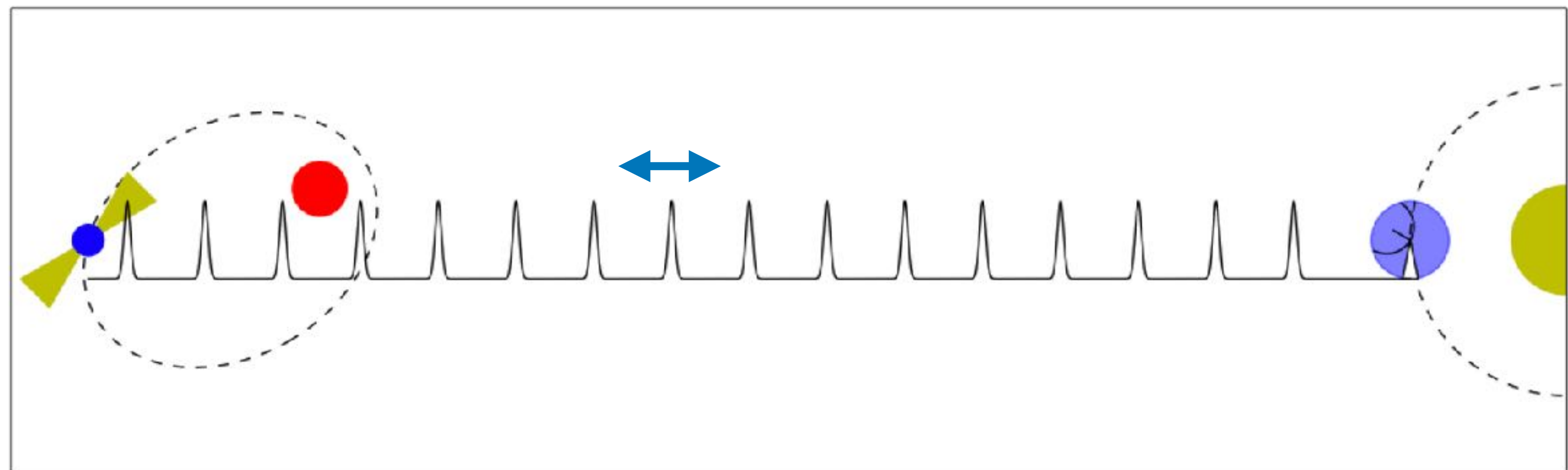
Earth

Pulsar



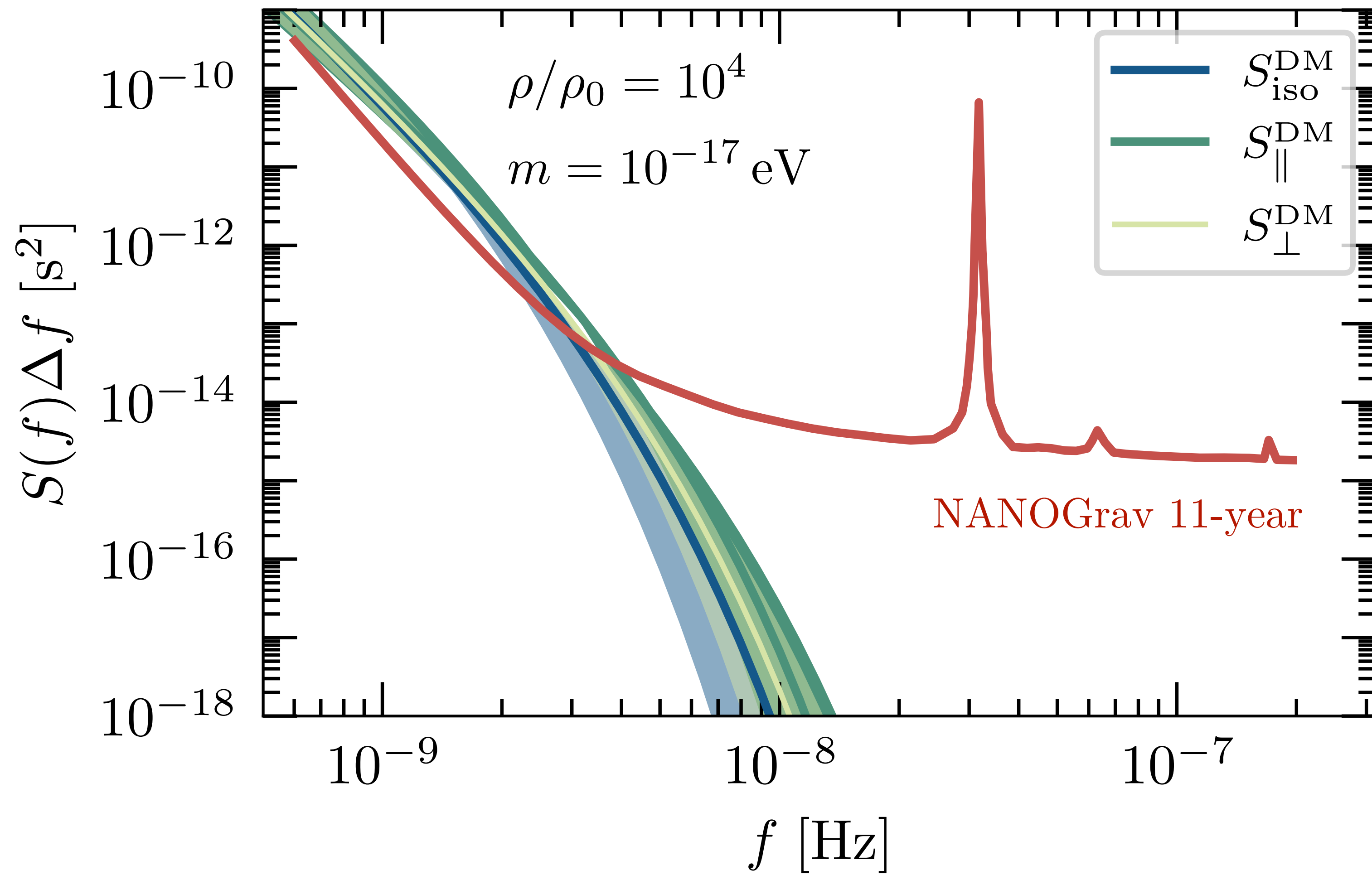
Pulsar

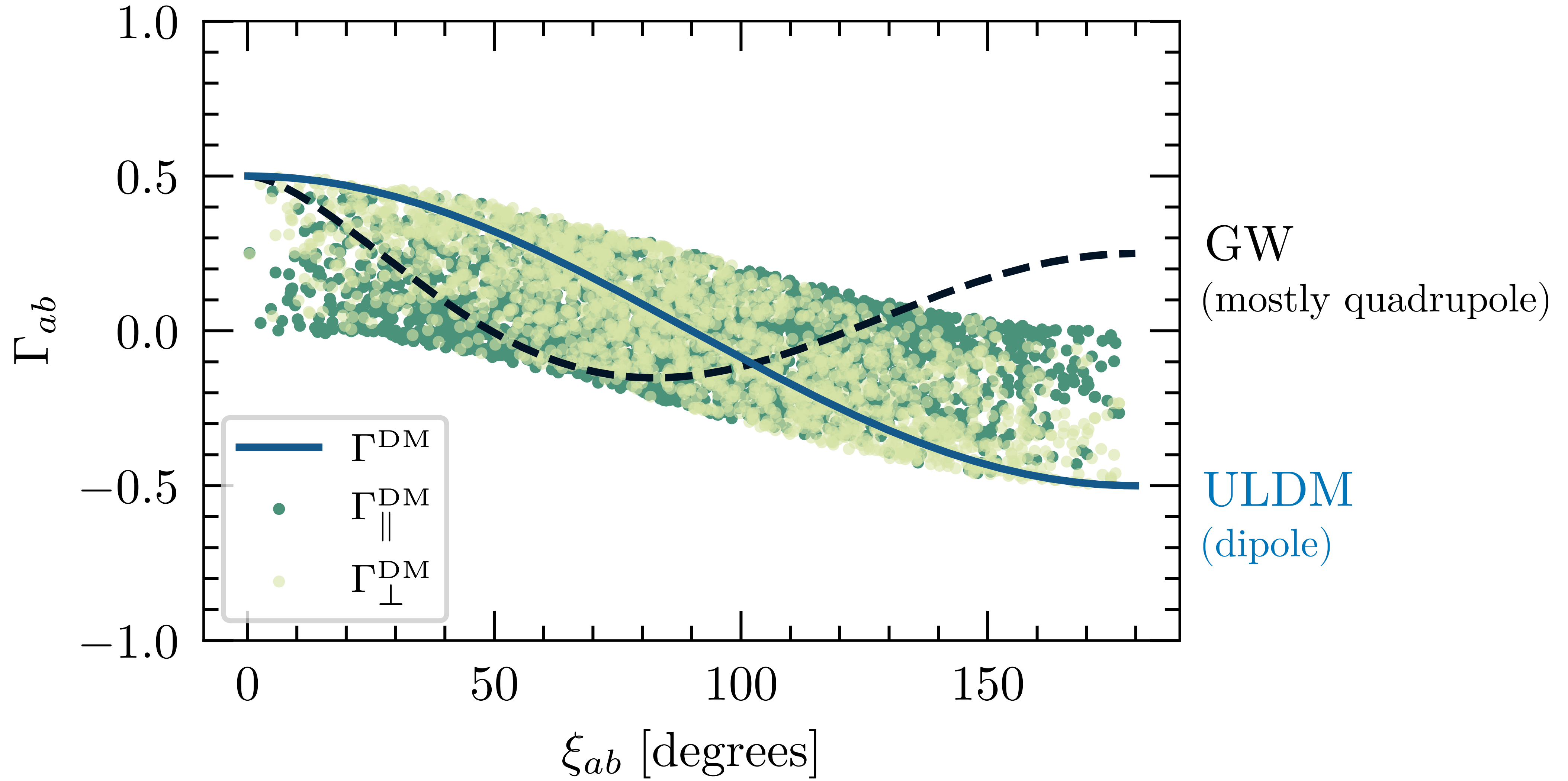
Earth

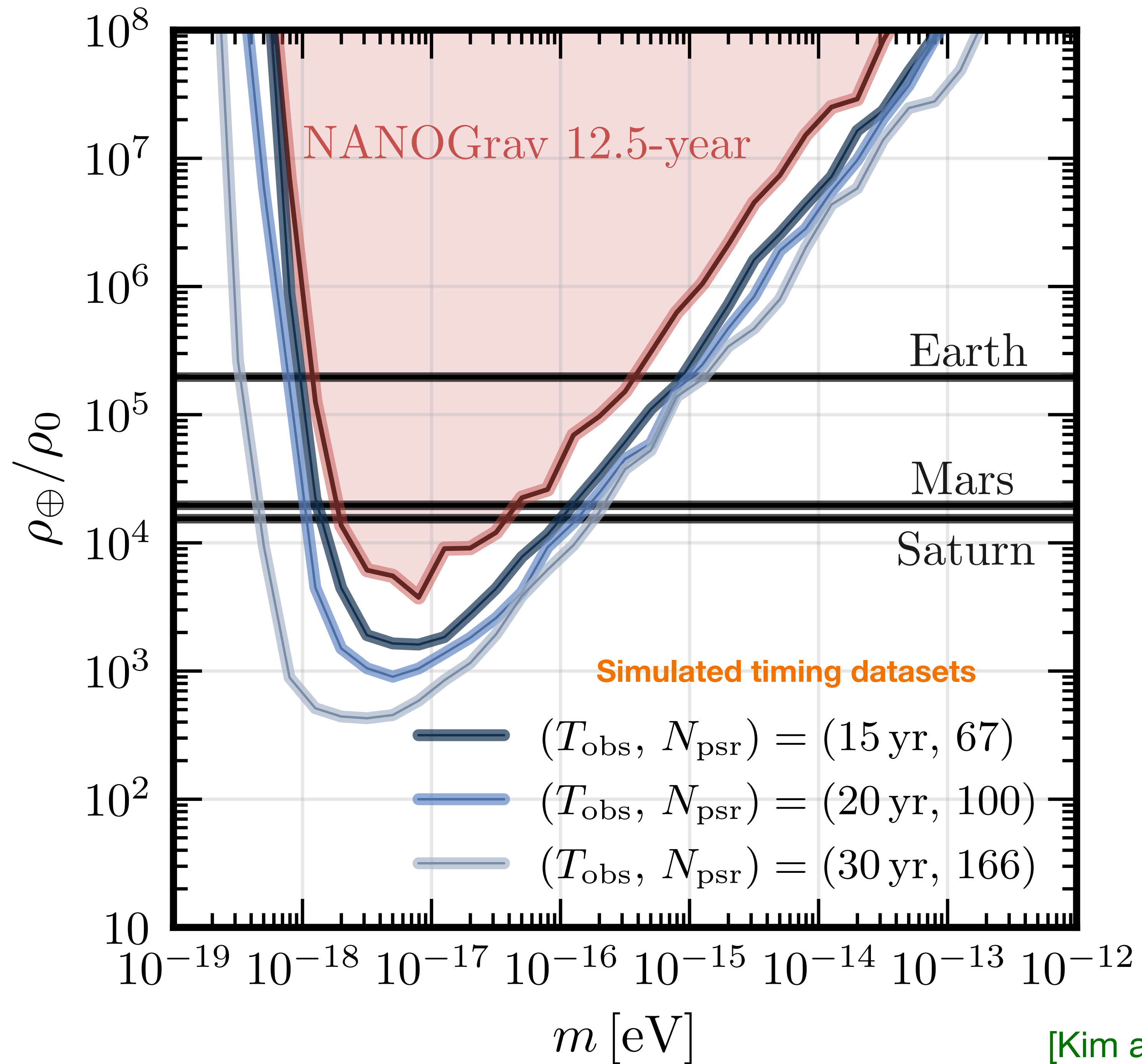


ultralight dark matter signal is characterised by
spectrum and *correlation*

$$\langle \delta t_a \delta t_b \rangle = \int df \Gamma_{ab}^{\text{ULDM}} S_{\delta t}^{\text{ULDM}}(f)$$







one last example:

Astrometry

astrometry involves
precision measurements of
positions / velocities of stars

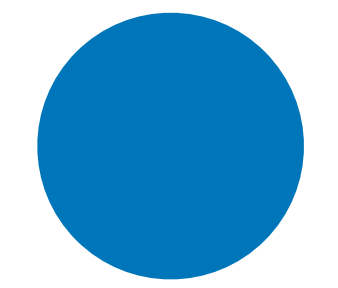
current/future astrometry missions measure

$$N_{\star} = 10^8 - 10^9$$

at the precision of

$$\Delta\theta \sim \mathcal{O}(10^2) \mu\text{as}$$

$$\mu\text{as} = 5 \times 10^{-12} \text{ rad}$$

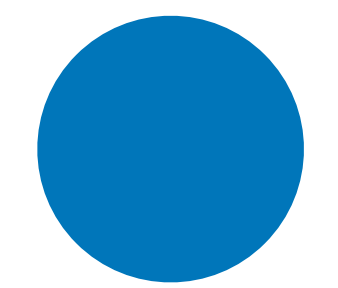


Earth



star



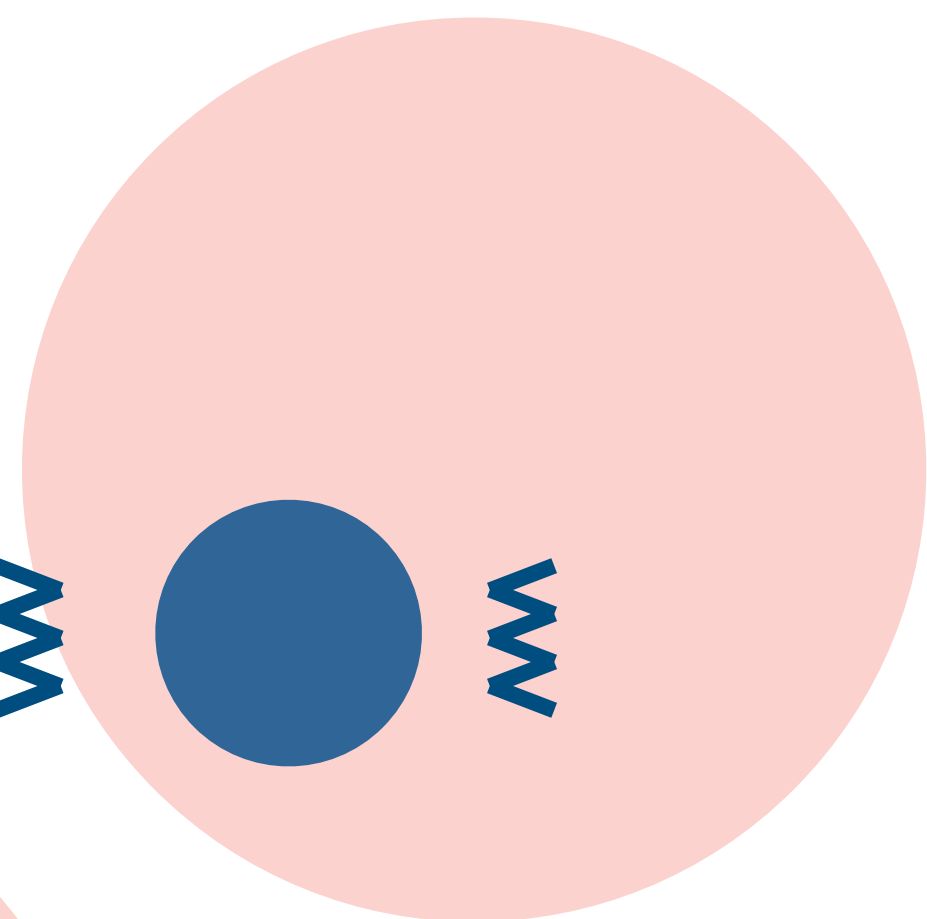
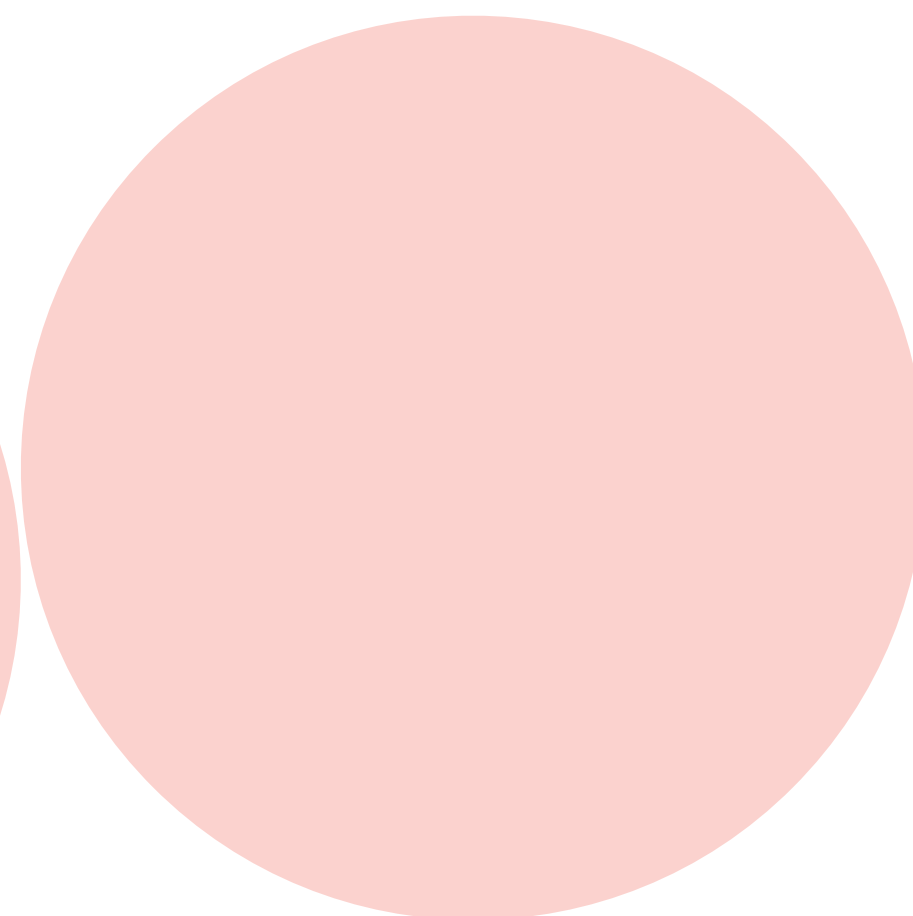
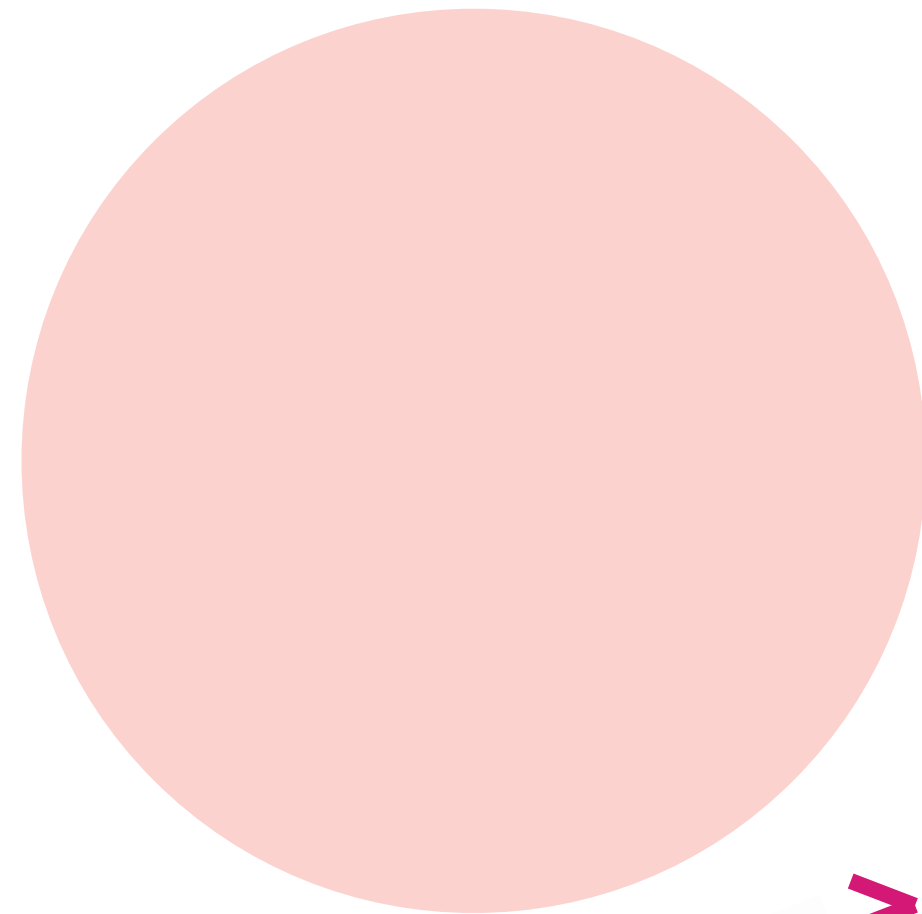
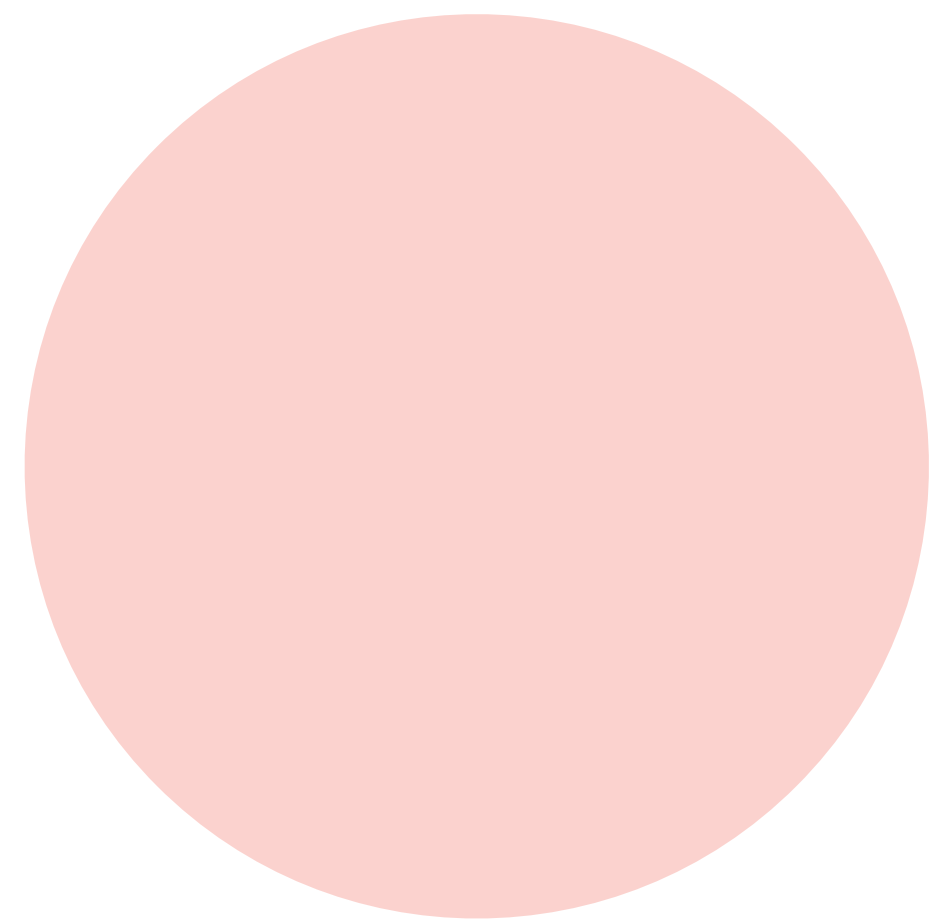


Earth

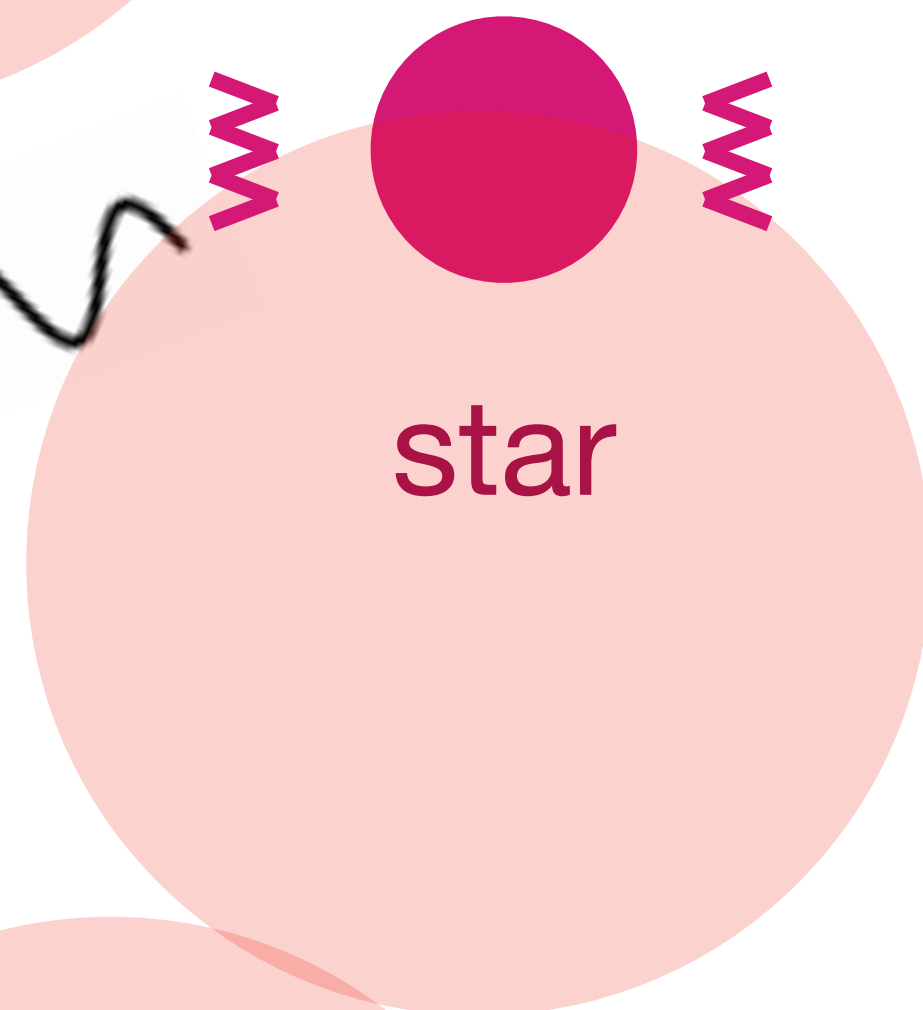


star

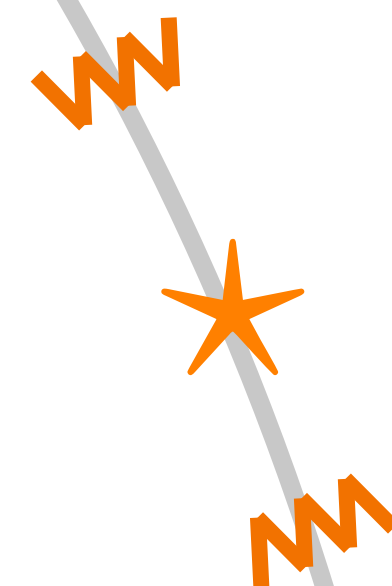




Earth



star

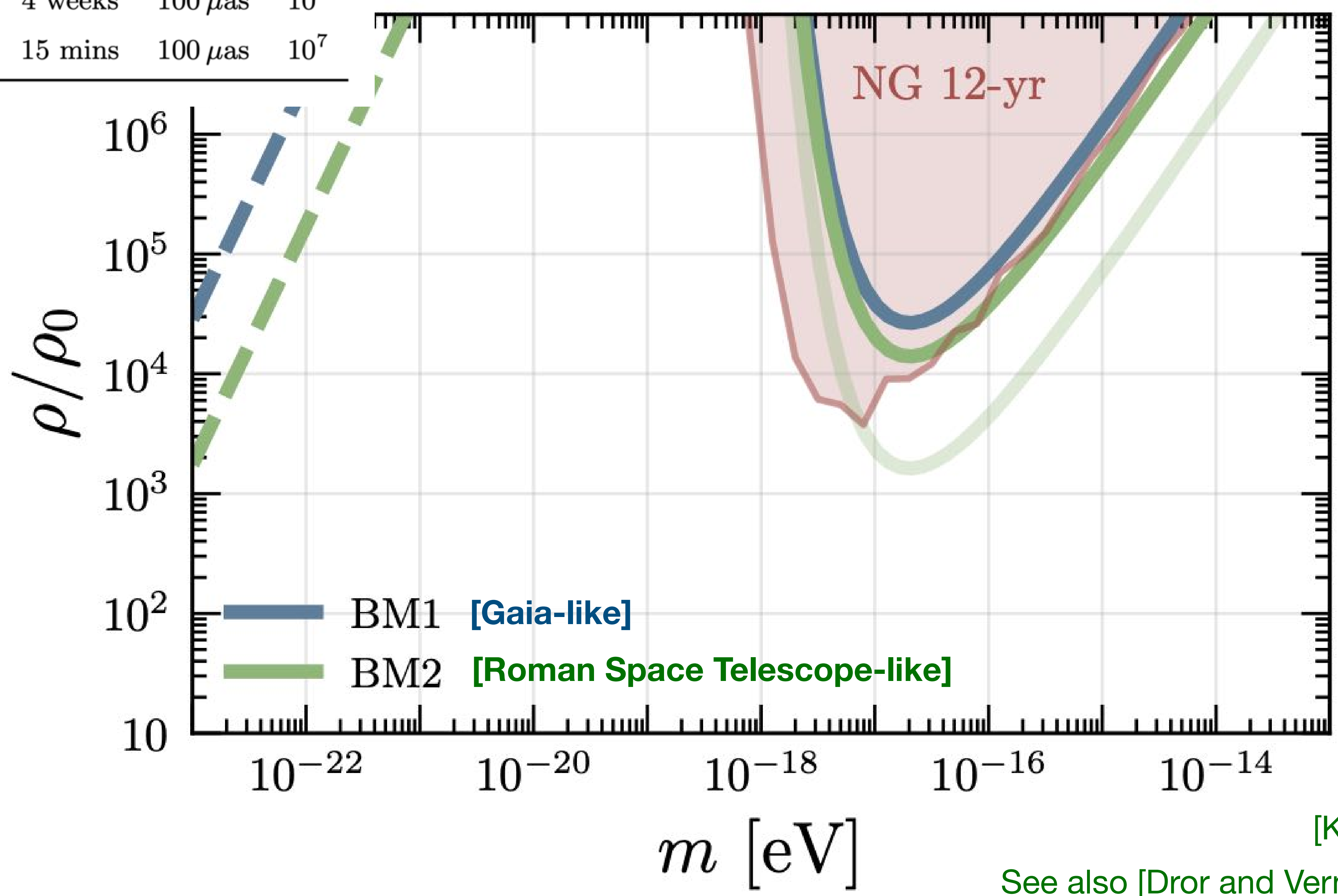


similarly

the signal is characterised by **spectrum** and **correlation**

$$\langle \delta n_a^i(t) \delta n_b^j(t') \rangle = \int df \Gamma_{ab}^{ij} S(f) \cos[2\pi f(t - t')]$$

	T	Δt	σ_r	N_\star
BM1	10-yr	4 weeks	100 μas	10^8
BM2	10-yr	15 mins	100 μas	10^7



[Kim 2406.03539]

See also [Dror and Verner 2406.03526]

Remark I

all of the results shown here are sensitive to
ULDM density around/within the solar system

local dark matter density is often derived over kpc scales



$$\rho_0 = 0.4 \text{ GeV}/\text{cm}^3$$

is an ***average density over the volume of kpc***

what we are probing is
(or what matters for all terrestrial DM detector is)



• $\sim (100\text{AU})^3 = 10^{-19} \text{kpc}^3$

currently no measurement on this scale exists

only constraints exist

$$\rho/\rho_0 \lesssim 10^{11}$$

From geodetic satellite and LLR
[Adler (08)]

$$\rho/\rho_0 \lesssim 6 \times 10^6$$

From asteroids in the solar system
[Tsai, Eby et al (22)]

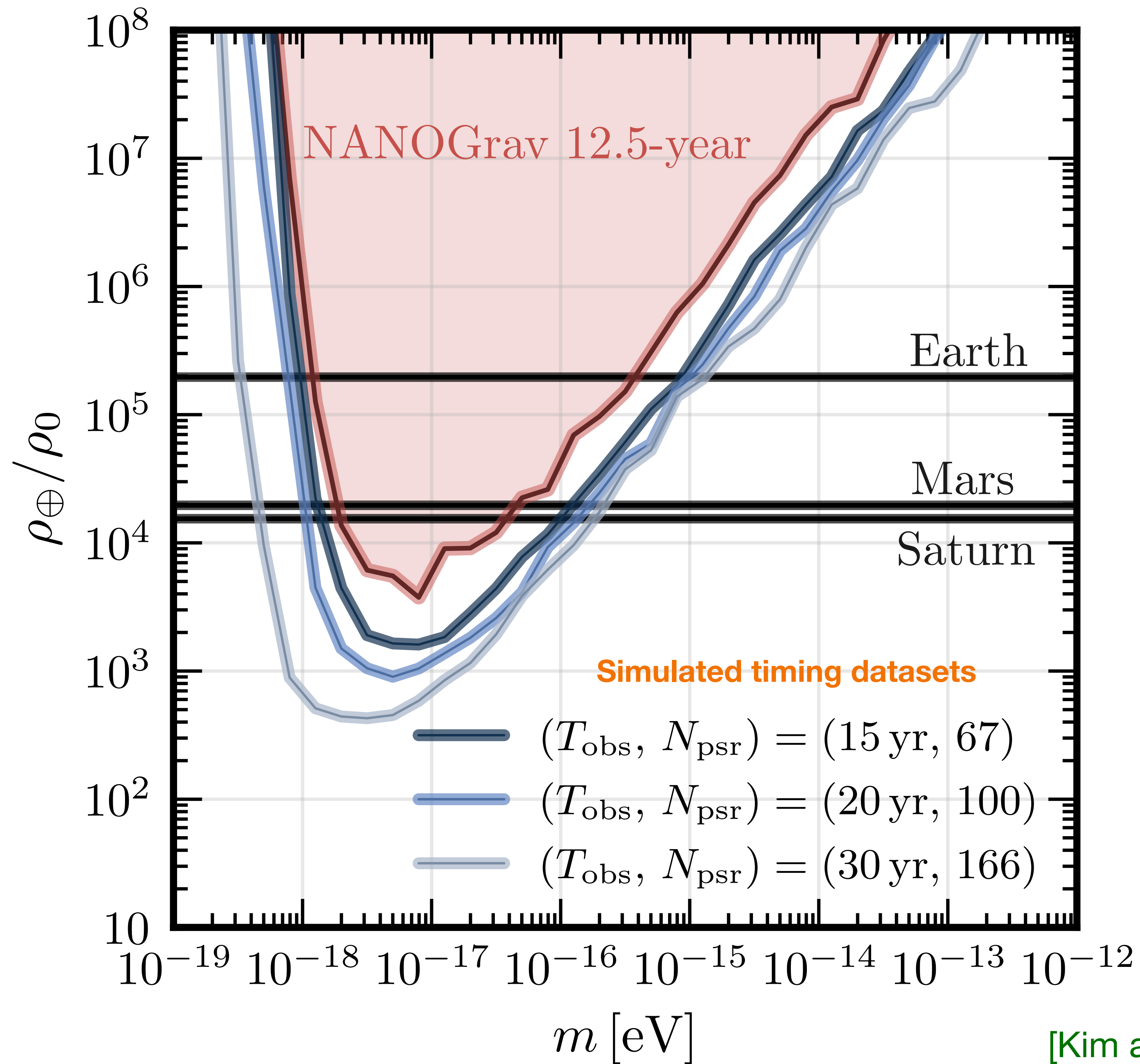
$$\rho/\rho_0 \lesssim 2 \times 10^4$$

From solar system ephemerides
[Pitjev, Pitjeva (13)]

GW detectors will provide
one of the strongest probes of ULDM density
within/around the solar system

Remark II

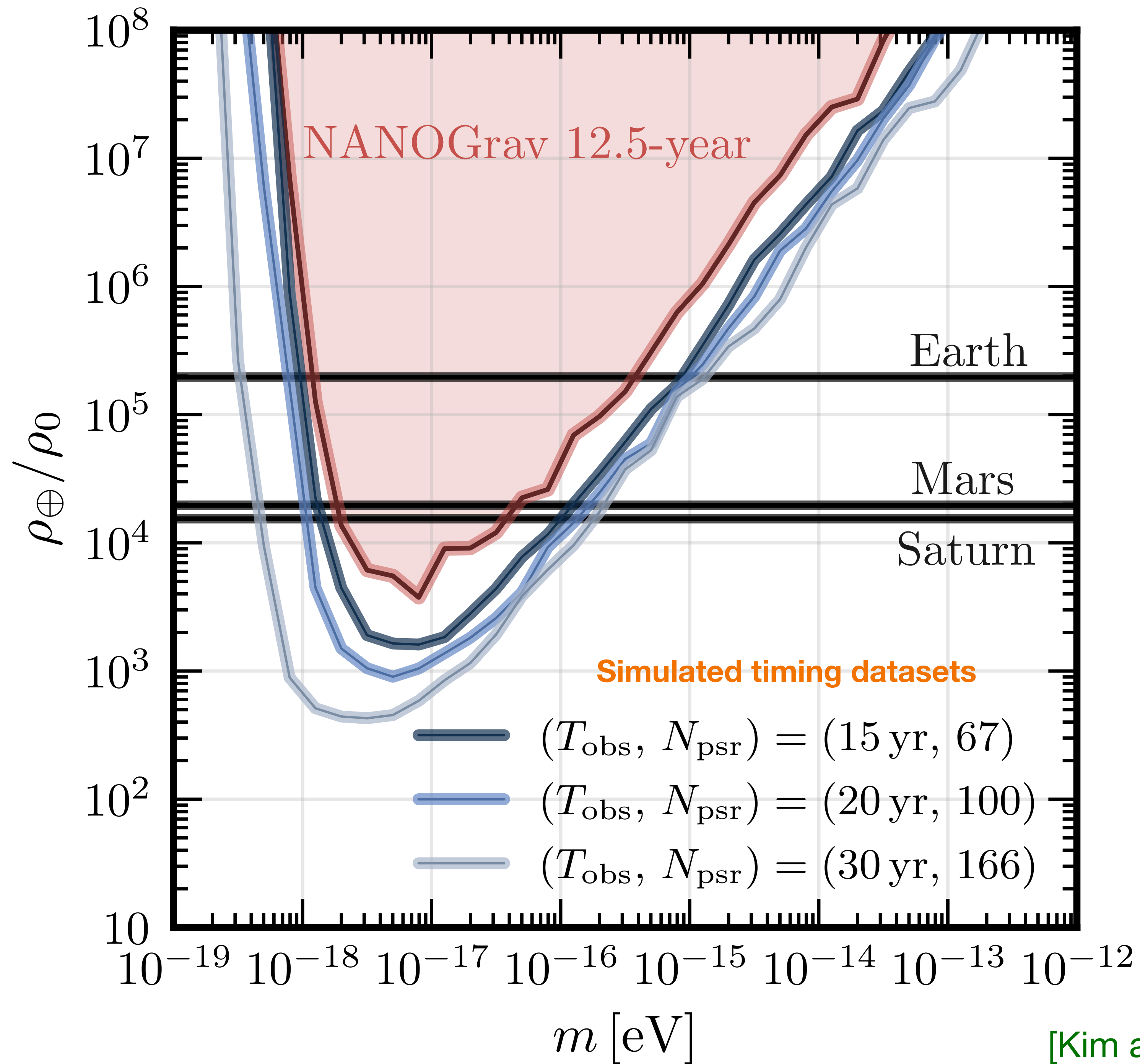
prospects of pulsar timing array



Next International Pulsar Timing Array (IPTA) data release
is expected to include

$$N_{\text{psr}} \sim 100$$

$$T_{\text{obs}} = 20^+ \text{ yr}$$



with next-gen radio telescope (e.g. Square Kilometer Array)
an order of magnitude or more improvement might be feasible

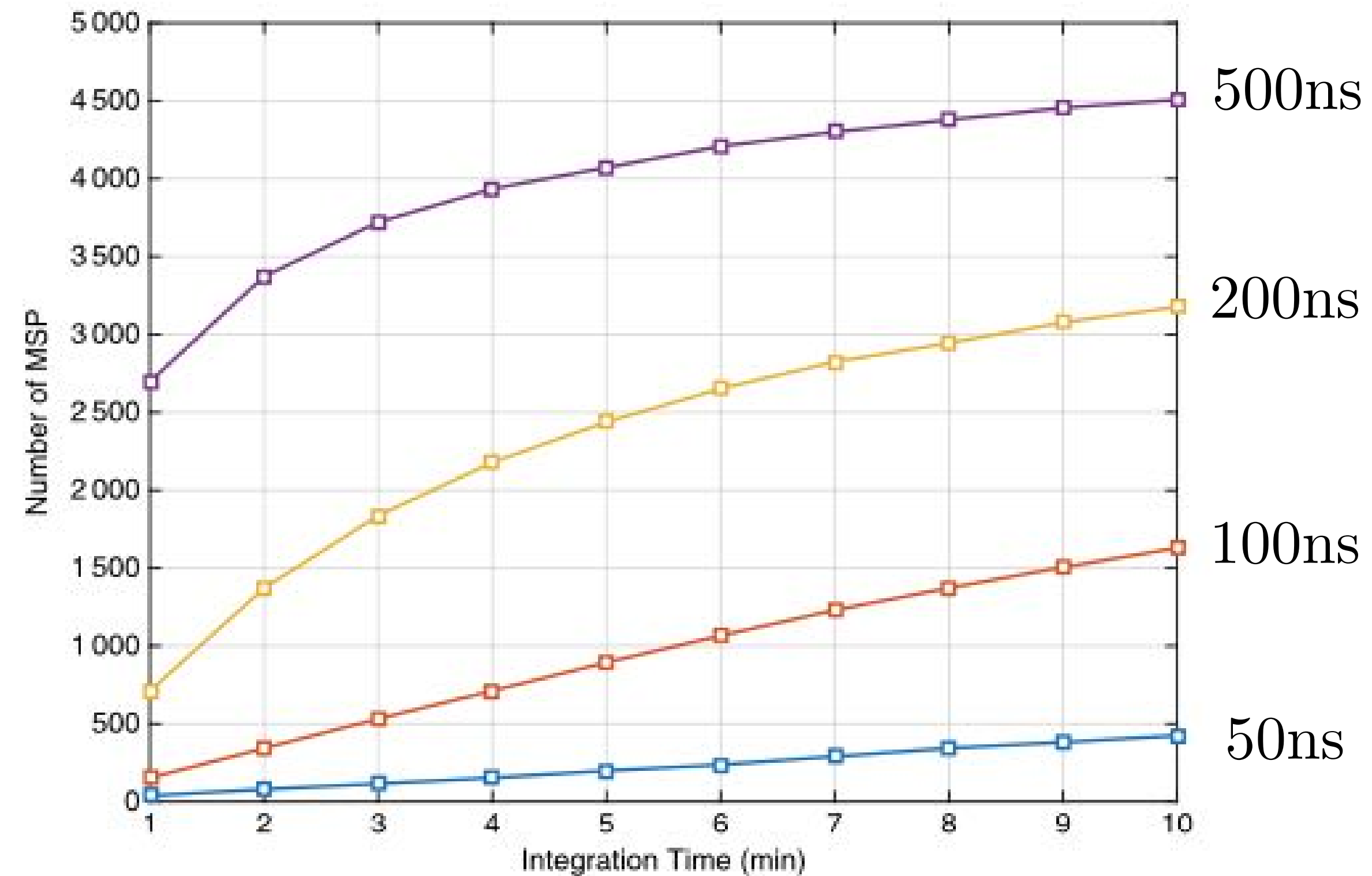


Figure 10. Numbers of MSPs that can archive a certain RMS noise level (or better) with varying integration time. Colour lines indicate different RMS noise levels (from bottom to top): 50 ns (blue), 100 ns (red), 200 ns (yellow), and 500 ns (purple).

