

# Axion dark matter detection with exotic phases of matter

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YOUNGST@RS - Quantum Sensing for Fundamental Physics



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# Axion dark matter

Basic Properties:

- Bosonic, high occupation number, behave like a classical field
- Velocity  $\sim 100$  km/sec

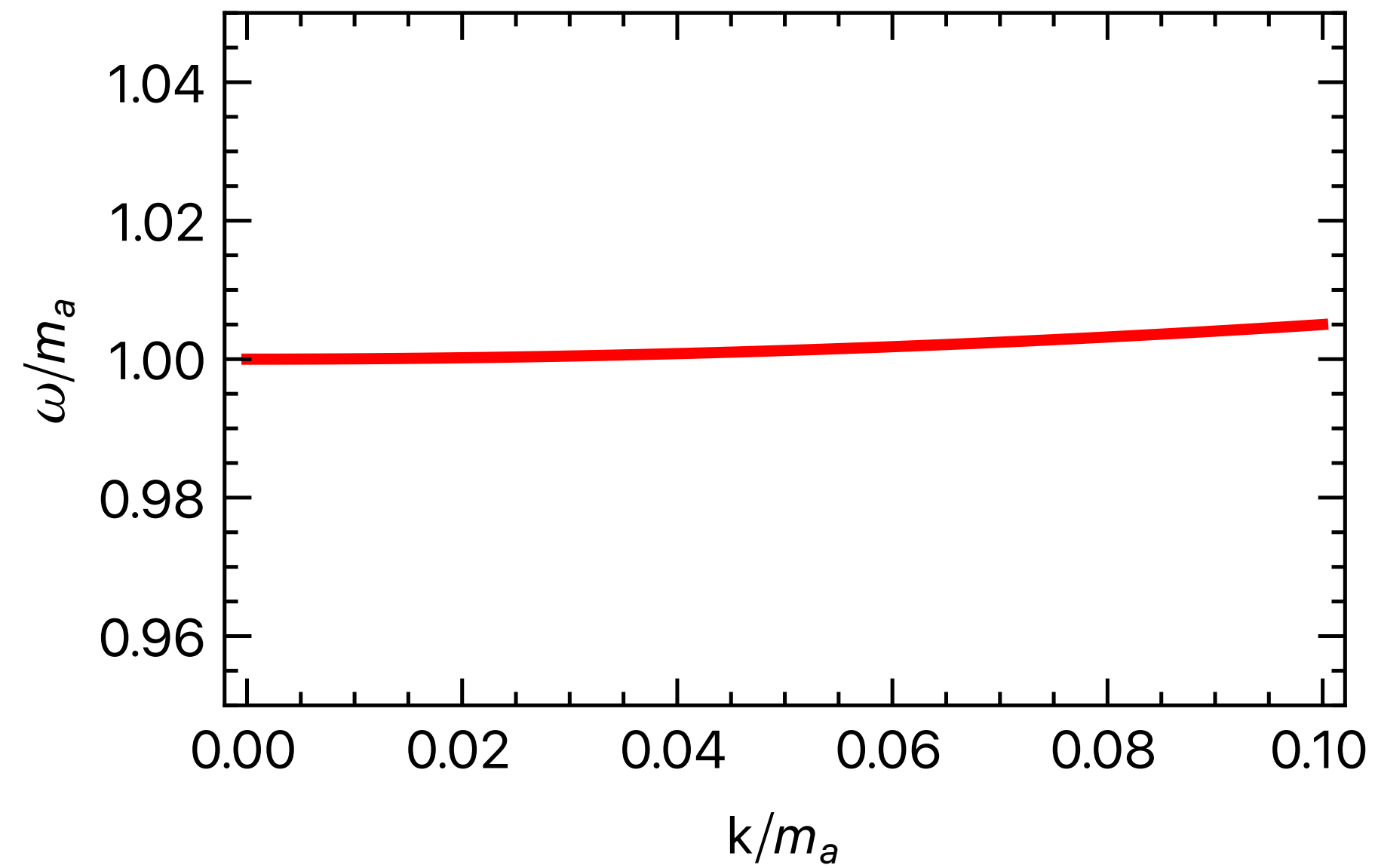
$$a_{\text{DM}}(t) \sim A \cos(\omega t - \mathbf{k} \cdot \mathbf{x}) \sim A \cos(m_a t)$$

$\frac{\sqrt{\rho_{\text{DM}}}}{m_a}$        $m_a + \frac{1}{2}m_a v^2$        $m_a \mathbf{v}$

# Axion dark matter

Dispersion relation

$$\frac{\omega}{m_a} = 1 + \frac{1}{2} \left( \frac{k}{m_a} \right)^2$$



$$a_{\text{DM}}(t) \sim A \cos(\omega t - \mathbf{k} \cdot \mathbf{x}) \sim A \cos(m_a t)$$

$$\frac{\sqrt{\rho_{\text{DM}}}}{m_a} \quad m_a + \frac{1}{2} m_a v^2 \quad m_a \mathbf{v}$$

Arrows indicate the mapping from the terms in the equation above to the corresponding terms in the dispersion relation below.

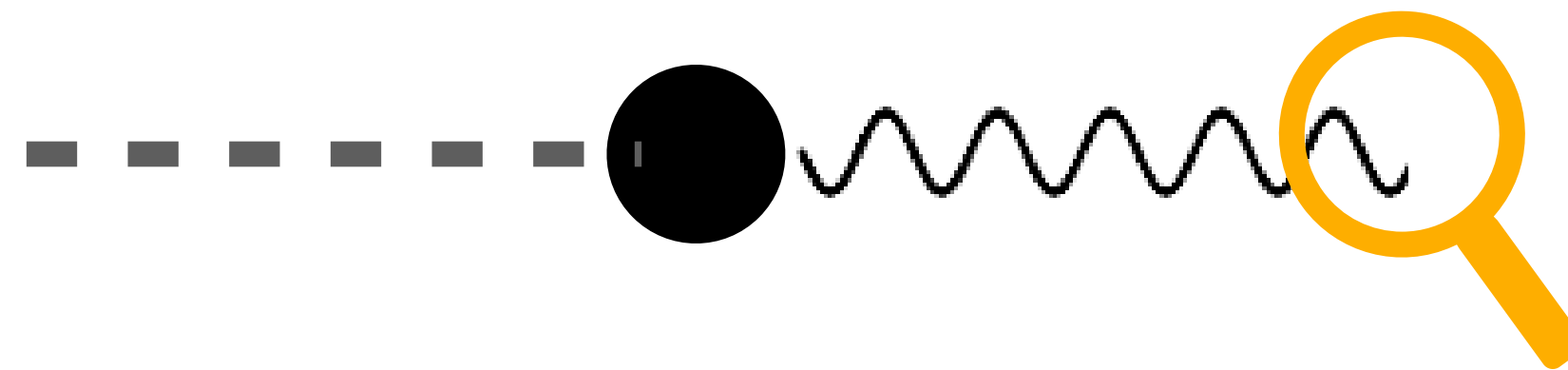
# Outline

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- Examples of axion absorption
- NMR with helium-3B, an example of forward scattering
- An example with scattering

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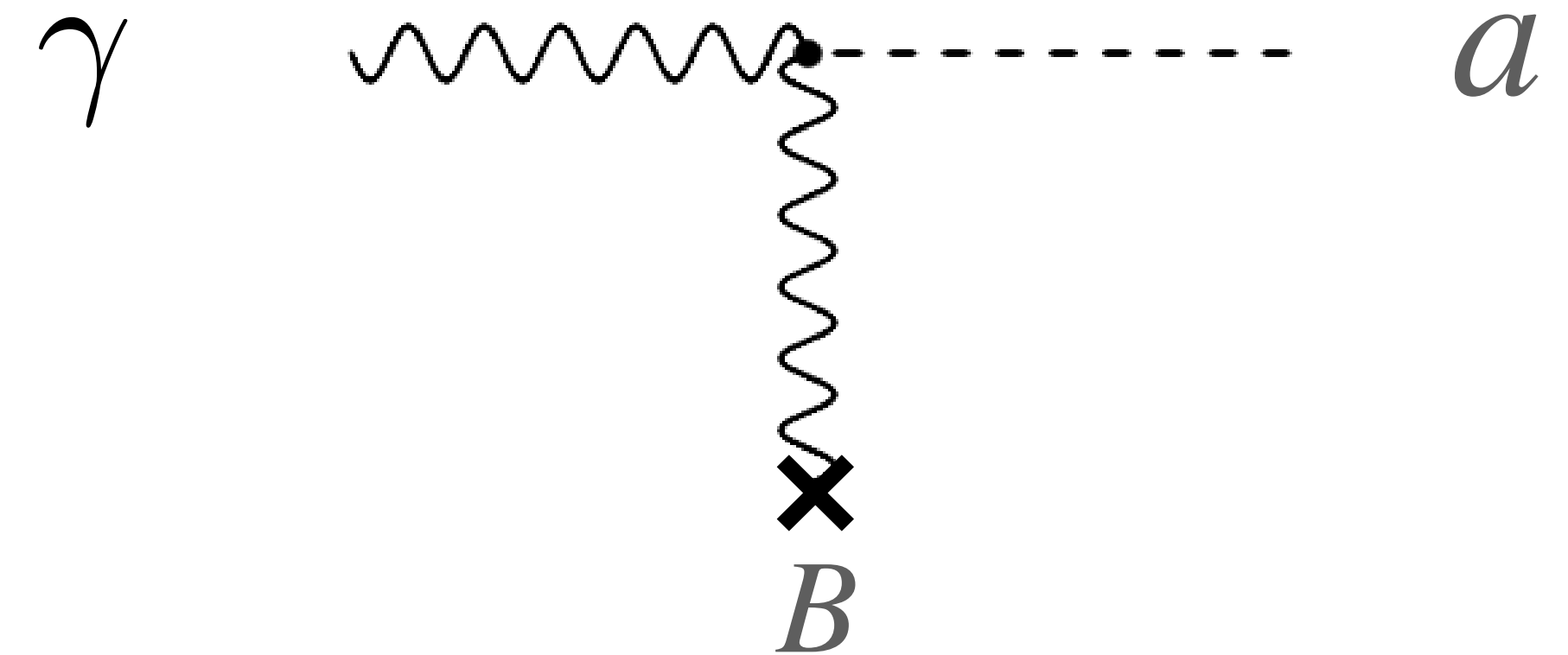
## Detection via absorption



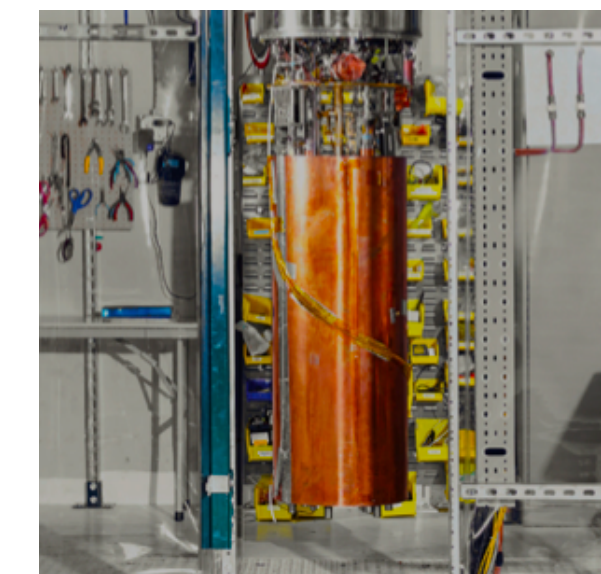
# Axions can interact with photons

$$\tilde{F}^{\mu\nu} = \frac{1}{2} \epsilon^{\mu\nu\rho\sigma} F_{\rho\sigma}$$

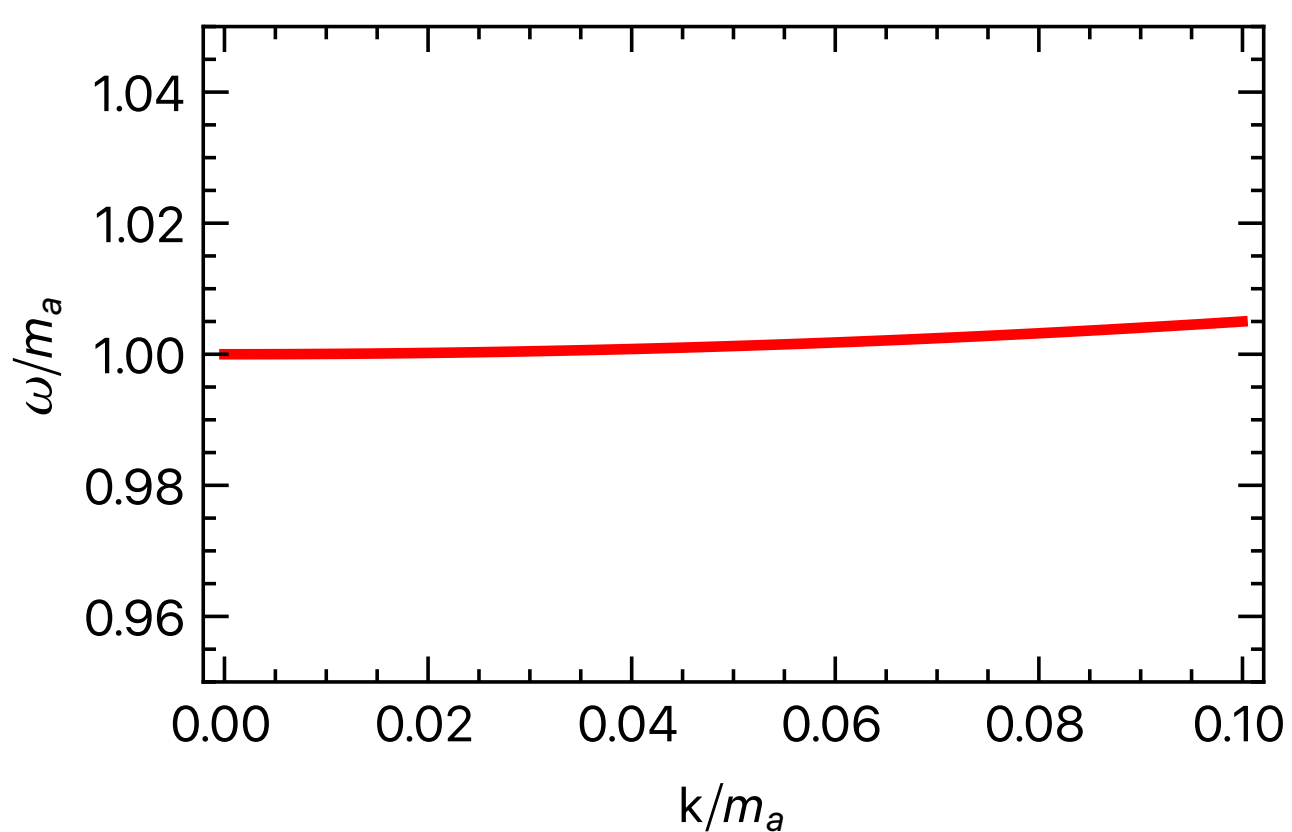
$$\begin{aligned} \mathcal{L}_{\text{int}} &\supset -\frac{g_{a\gamma}}{4} a F_{\mu\nu} \tilde{F}^{\mu\nu} \\ &= g_{a\gamma} a \mathbf{E} \cdot \mathbf{B} \end{aligned}$$



- Axions can convert to photons in a background magnetic field
- Better conversion efficiency if photon's dispersion is similar to axion's, e.g. cavity photon

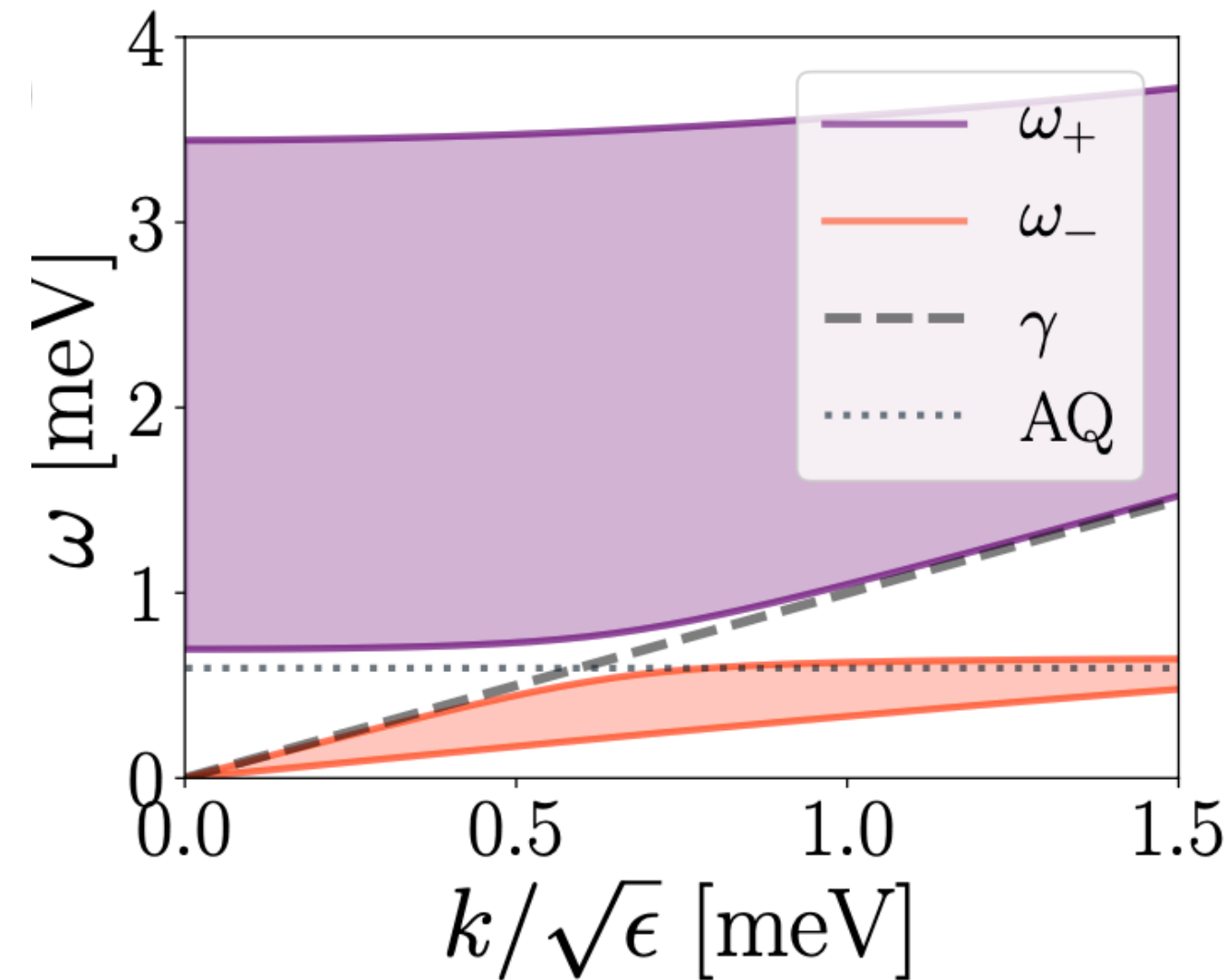


ADMX @ GHz



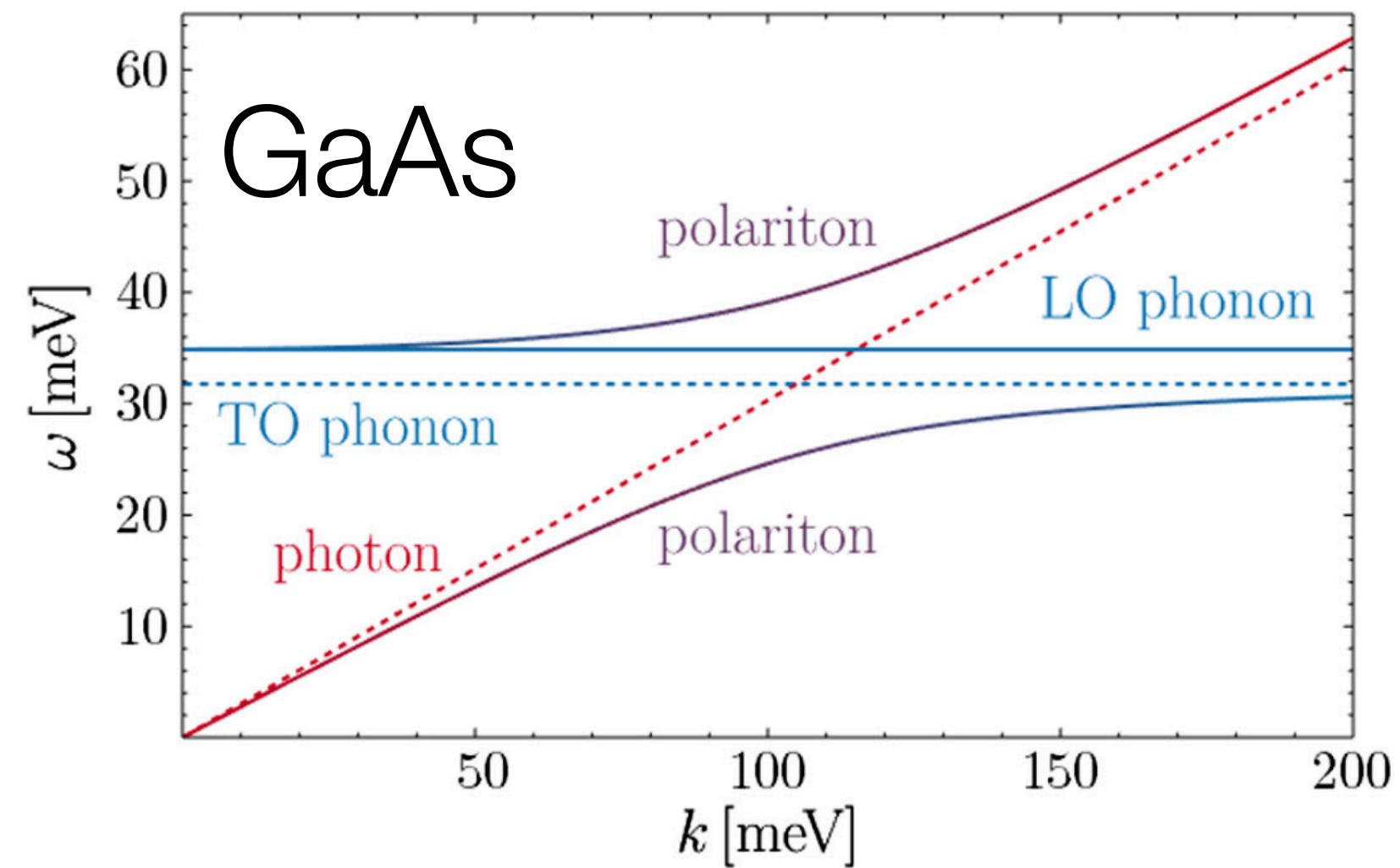
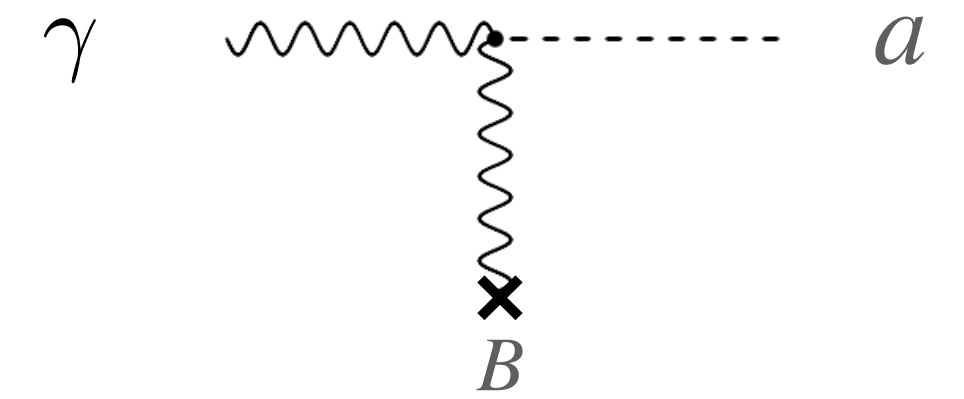
# Light in special materials

Antiferromagnetically doped topological insulators



MARSH, FONG, LENTZ, SMEJKAL and ALI (2019)

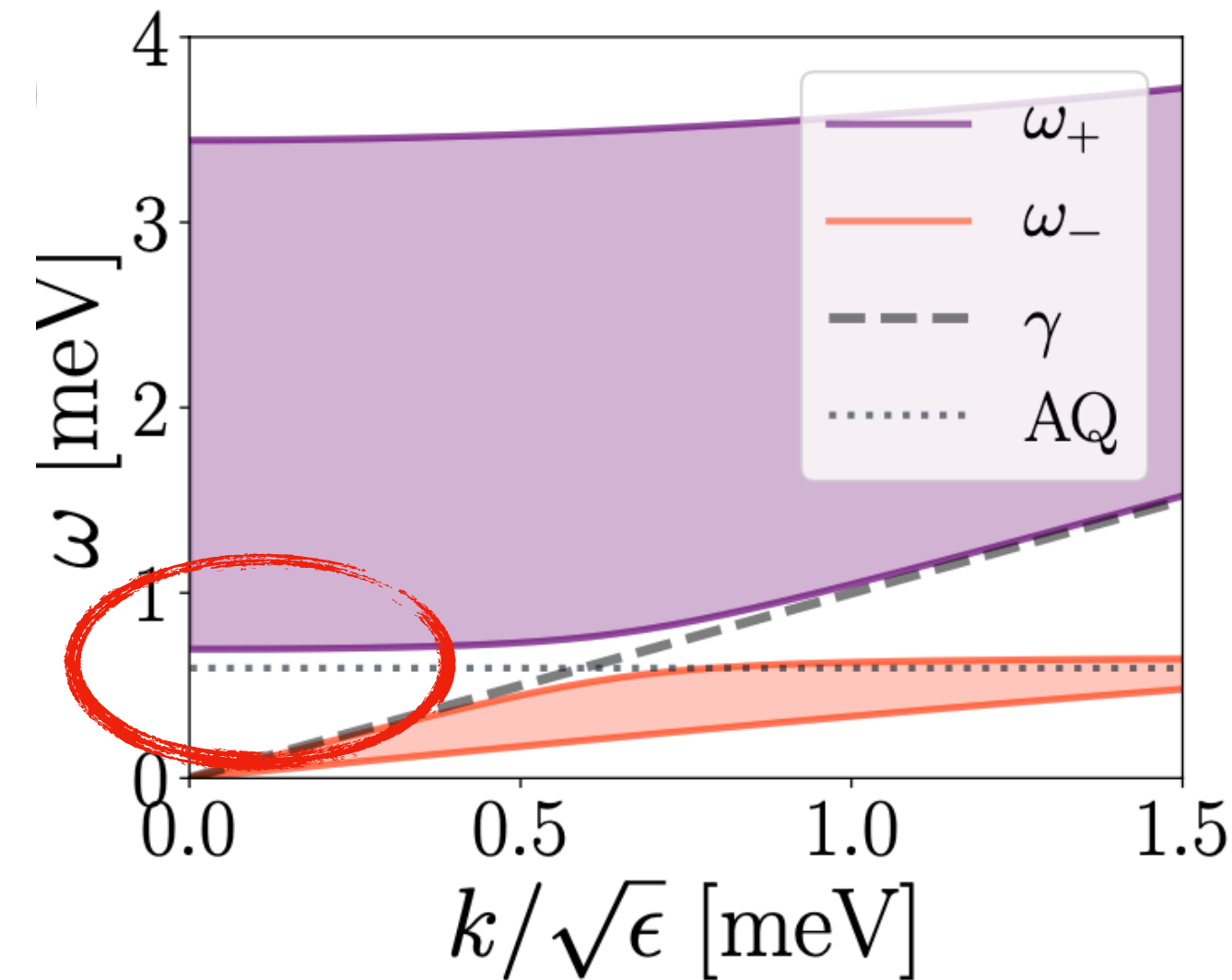
Polar crystals



MITRIDATE, TRICKLE, ZHANG, and ZUREK (2020)

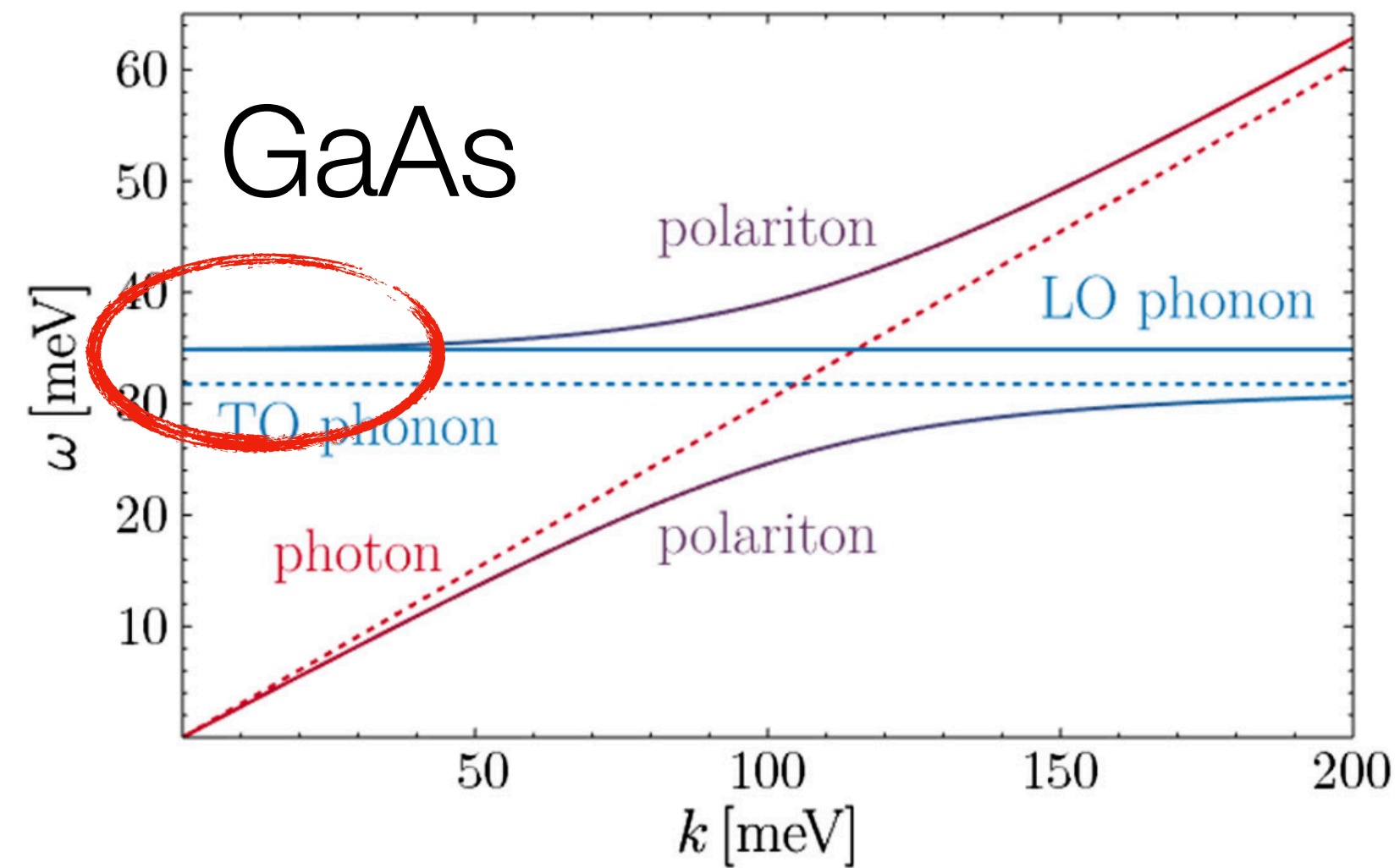
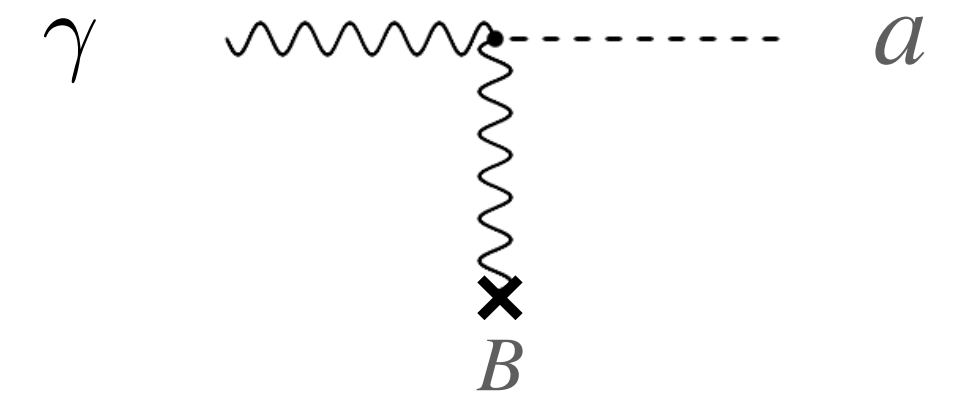
# Light in special materials

Antiferromagnetically doped topological insulators

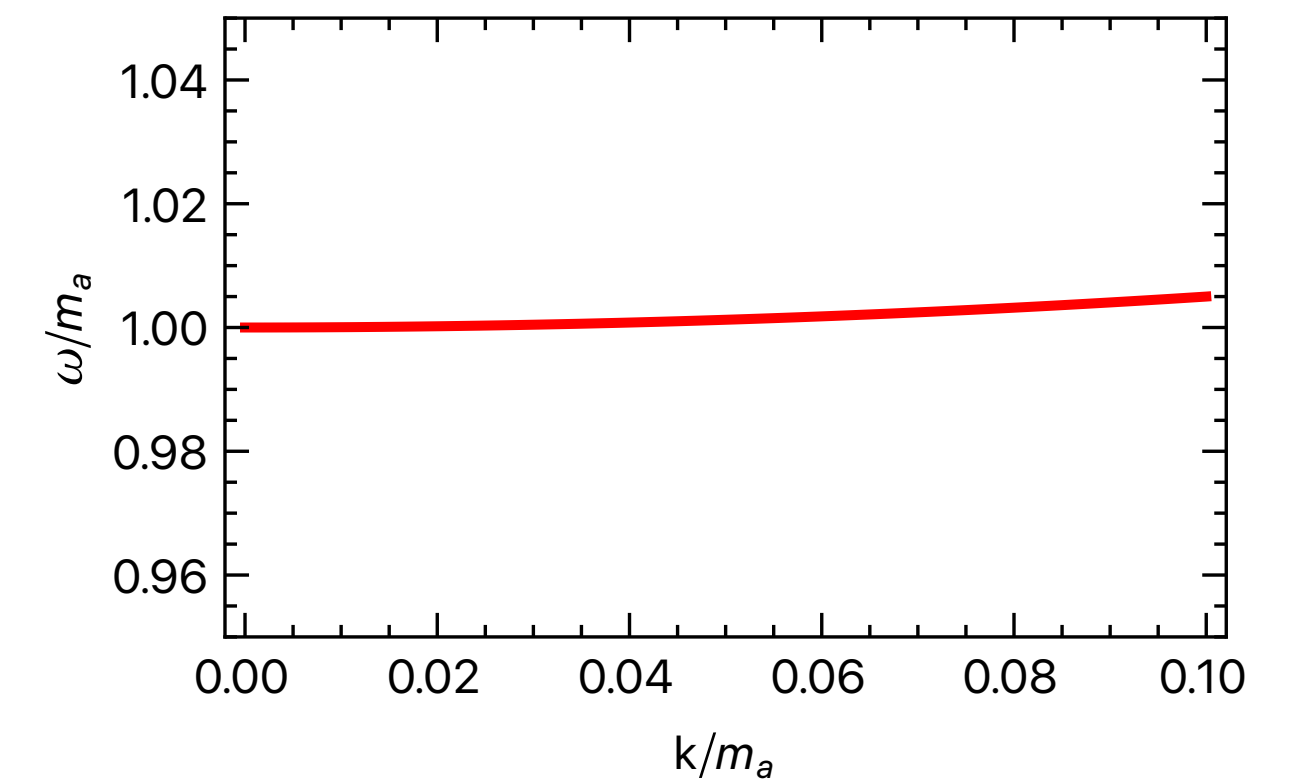


MARSH, FONG, LENTZ, SMEJKAL and ALI (2019)

Polar crystals



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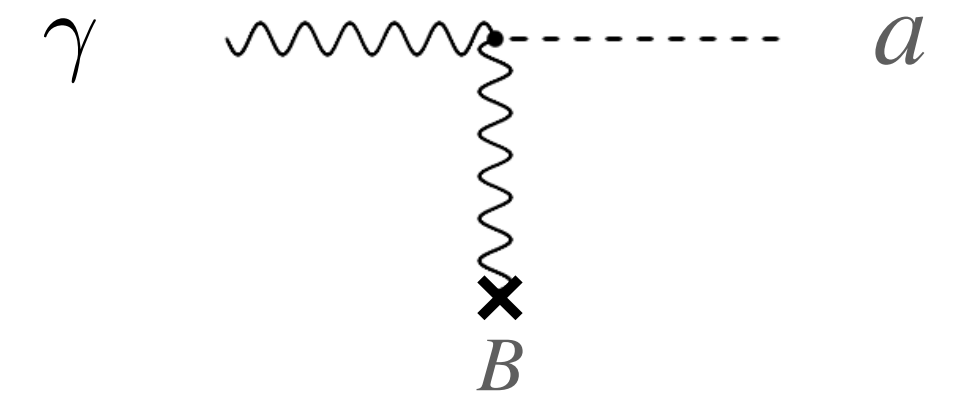




# Light in special materials

Antiferromagnetically  
doped  
topological insulators

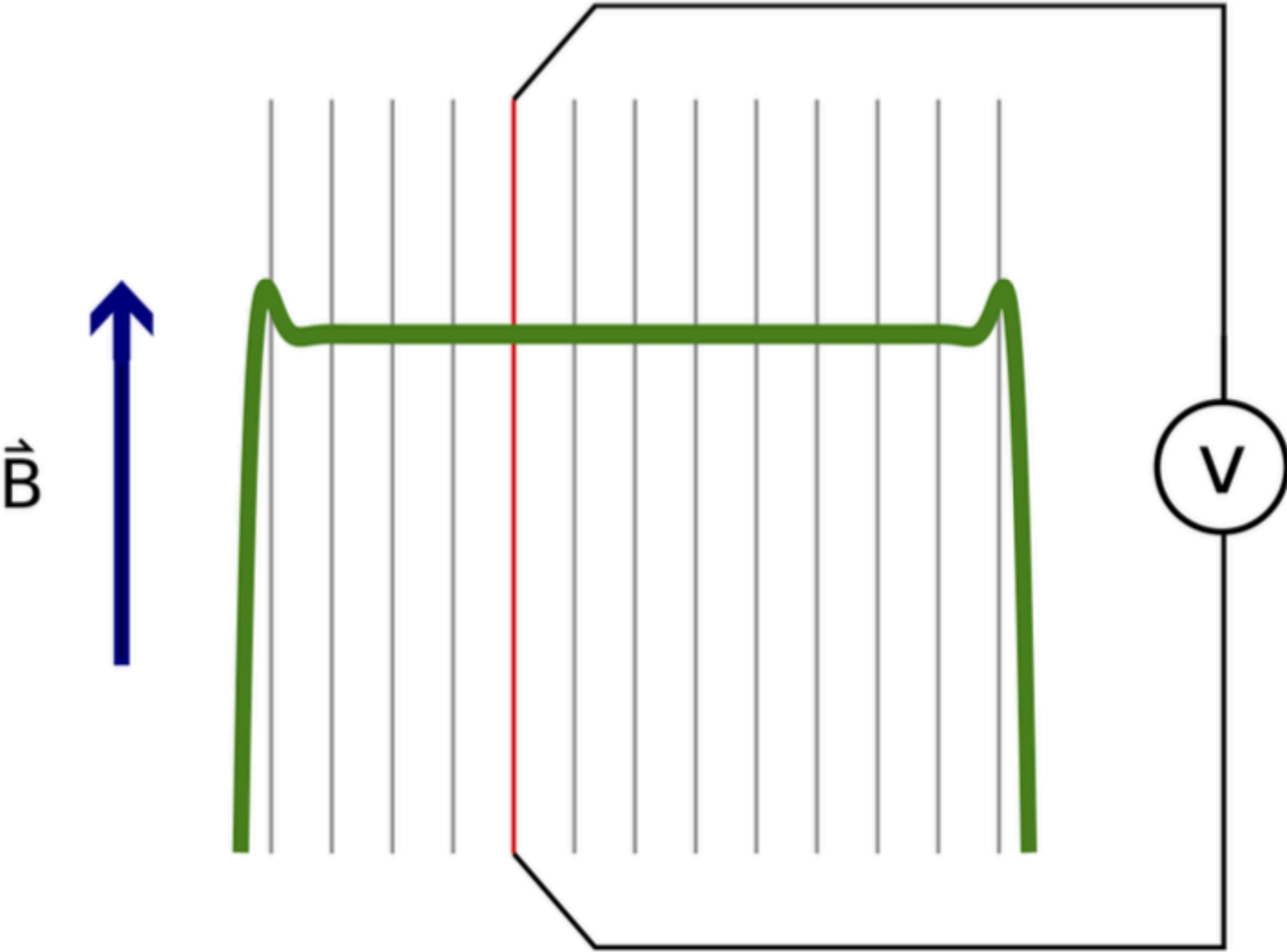
Polar crystals



- Axions can convert to quasiparticles, such as phonons and magnons.
- Target frequency: meV and above.
- Detection of axion via detection of quasiparticles, itself challenging.
- Quasiparticles must have high Q, or very little loss.

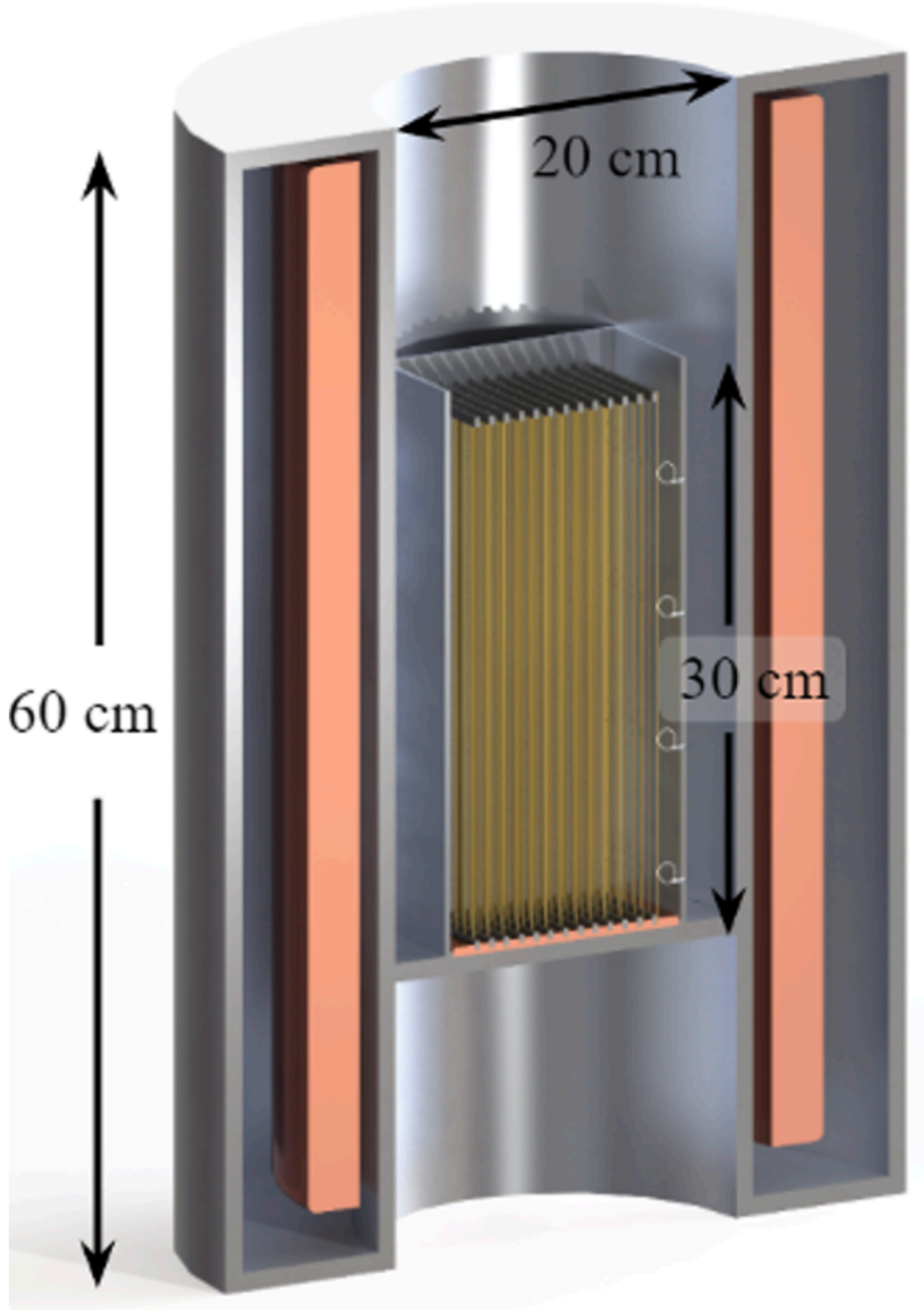
# Light in meta-materials

Array of wires, targeting  $10^{-4}$  eV



LAWSON, MILLAR, PANCALDI, VITAGLIANO AND WILCZEK (2019)

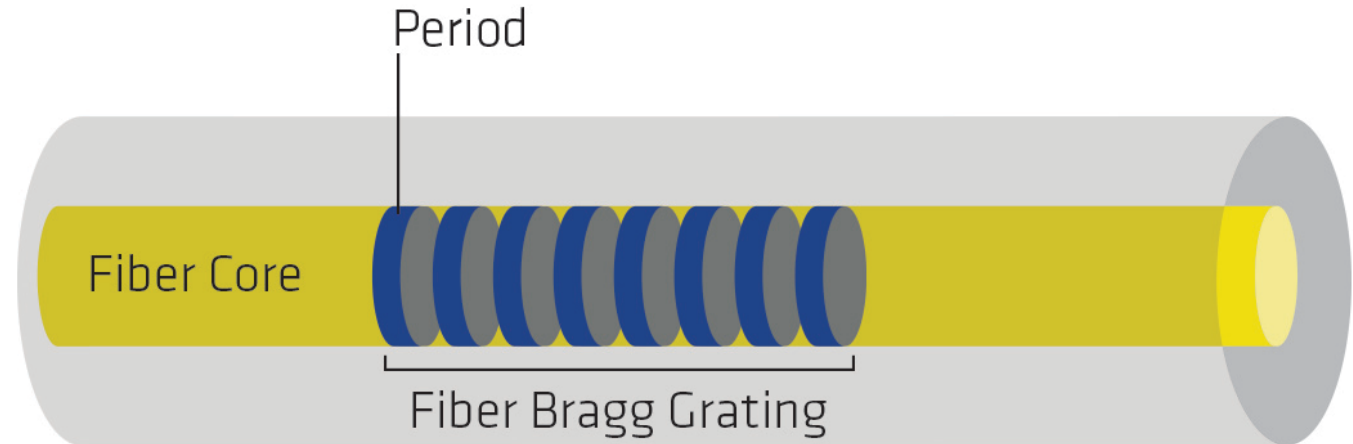
  
alpha



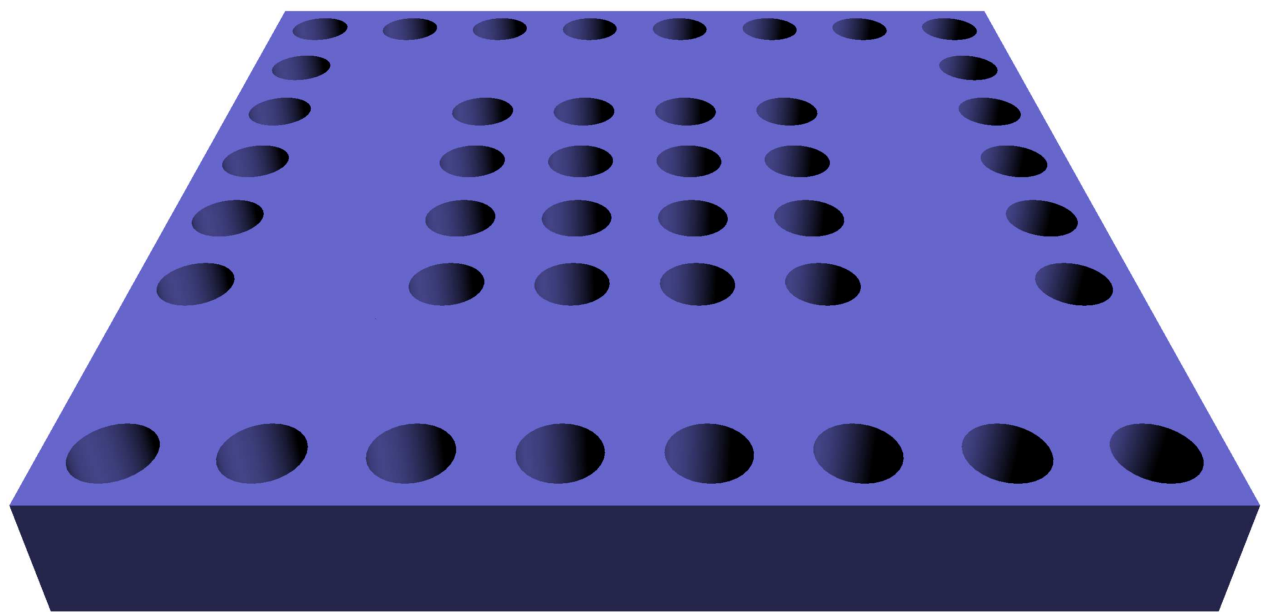
# Light in meta-materials

*Nature Reviews Materials*  
volume  
1, Article number: 16048 (2016)

## Photonic crystals, targeting eV

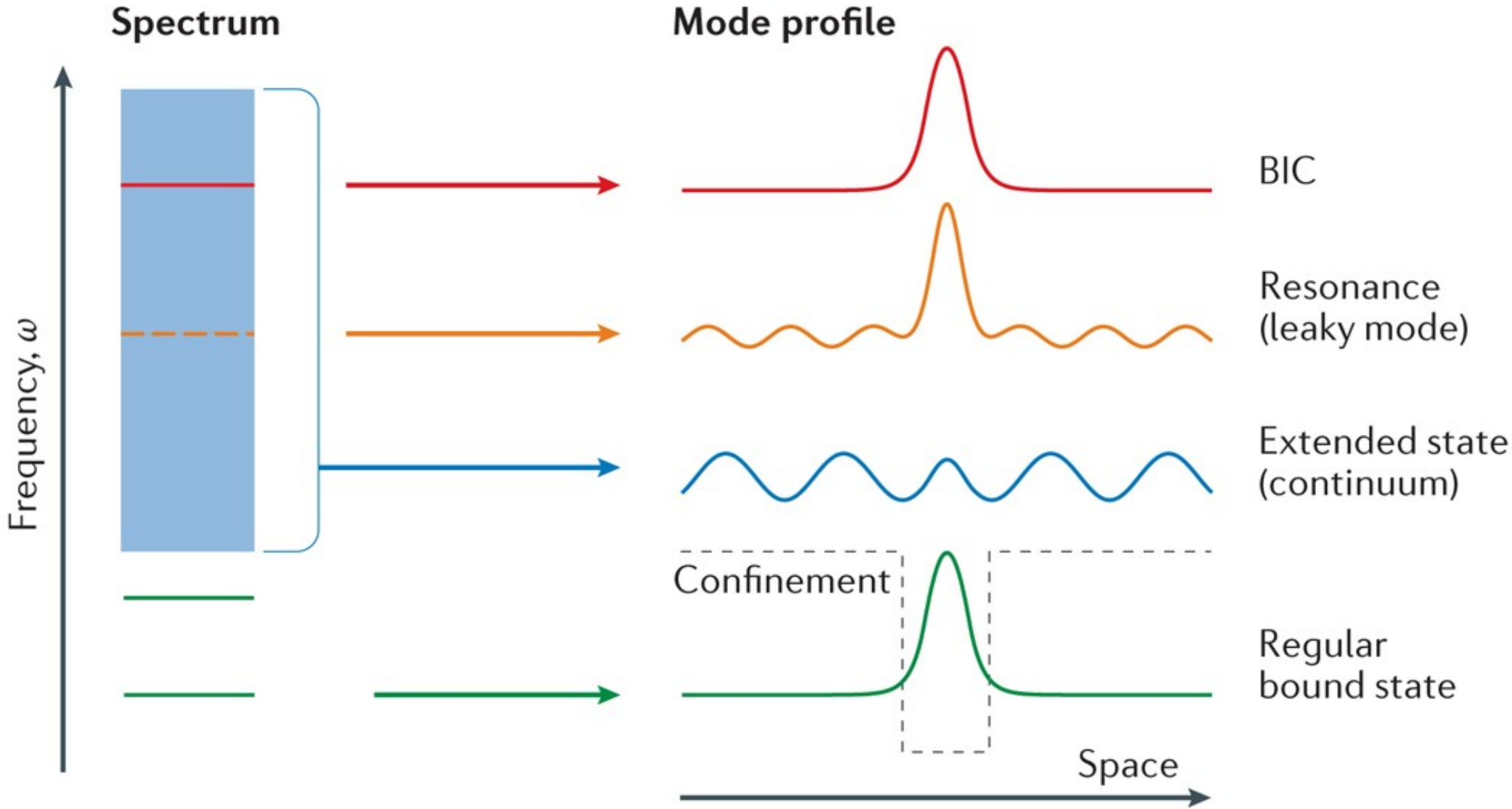


<https://www.teraxion.com/en/company/fiberbragggrating/>



BLINOV, GAO, HARNIK, JANISH and SINCLAIR  
(2024)

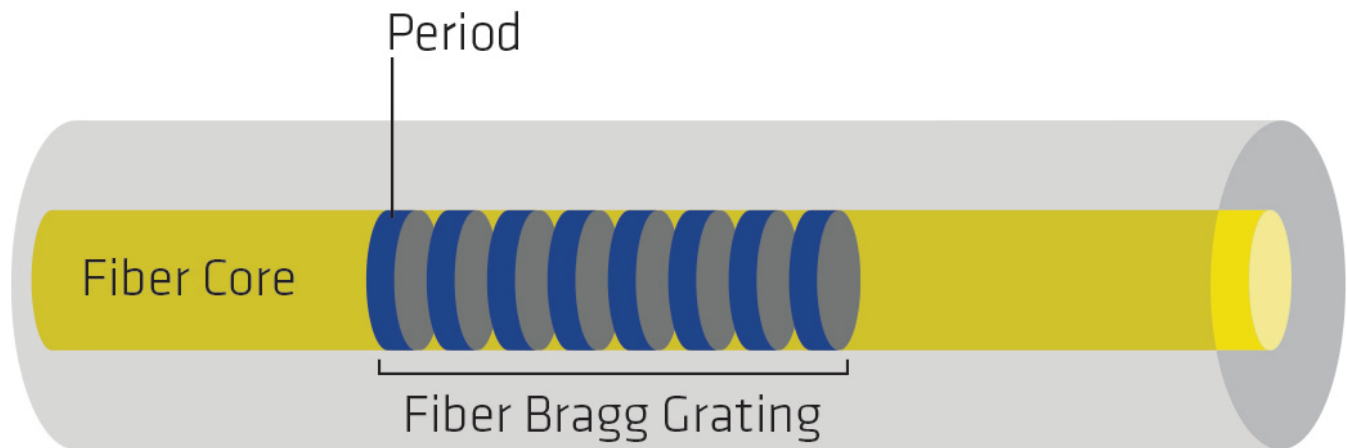
## Bound States in Continuum



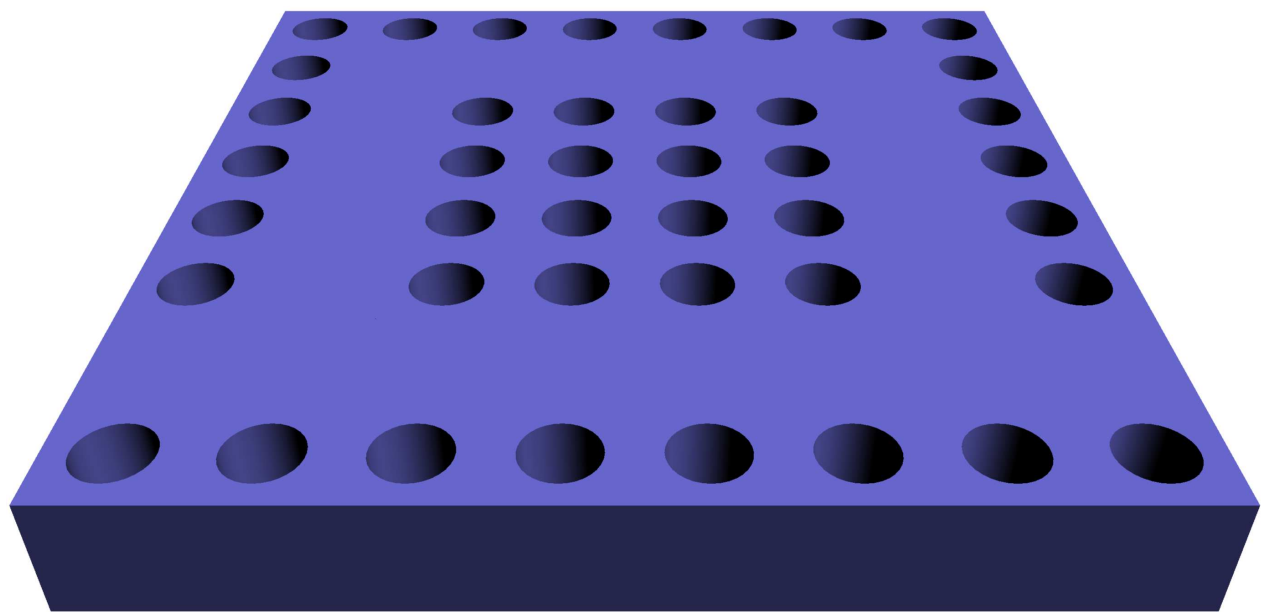
Nature Reviews | [Materials](#)

# Light in meta-materials

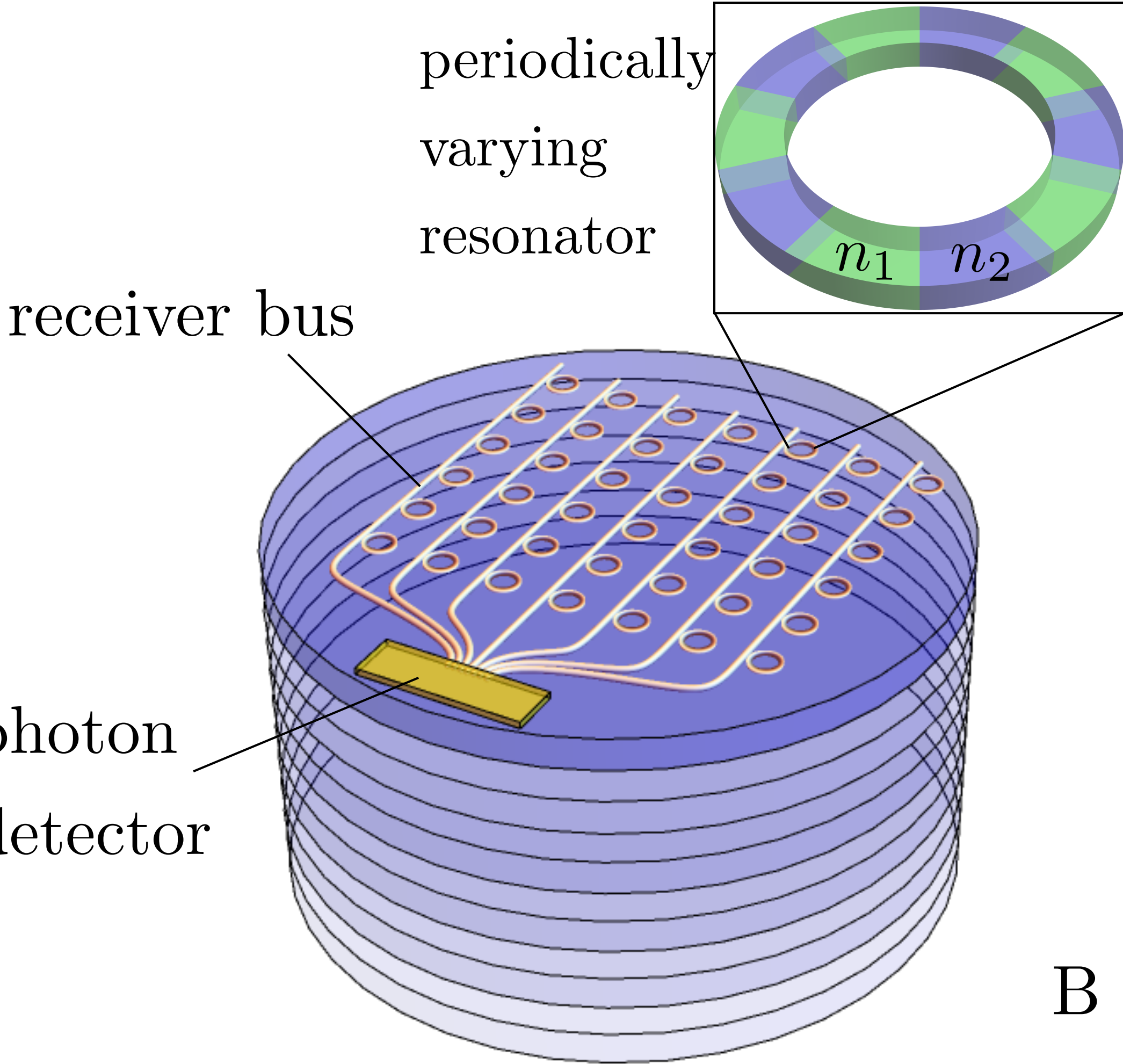
Photonic crystals, targeting eV



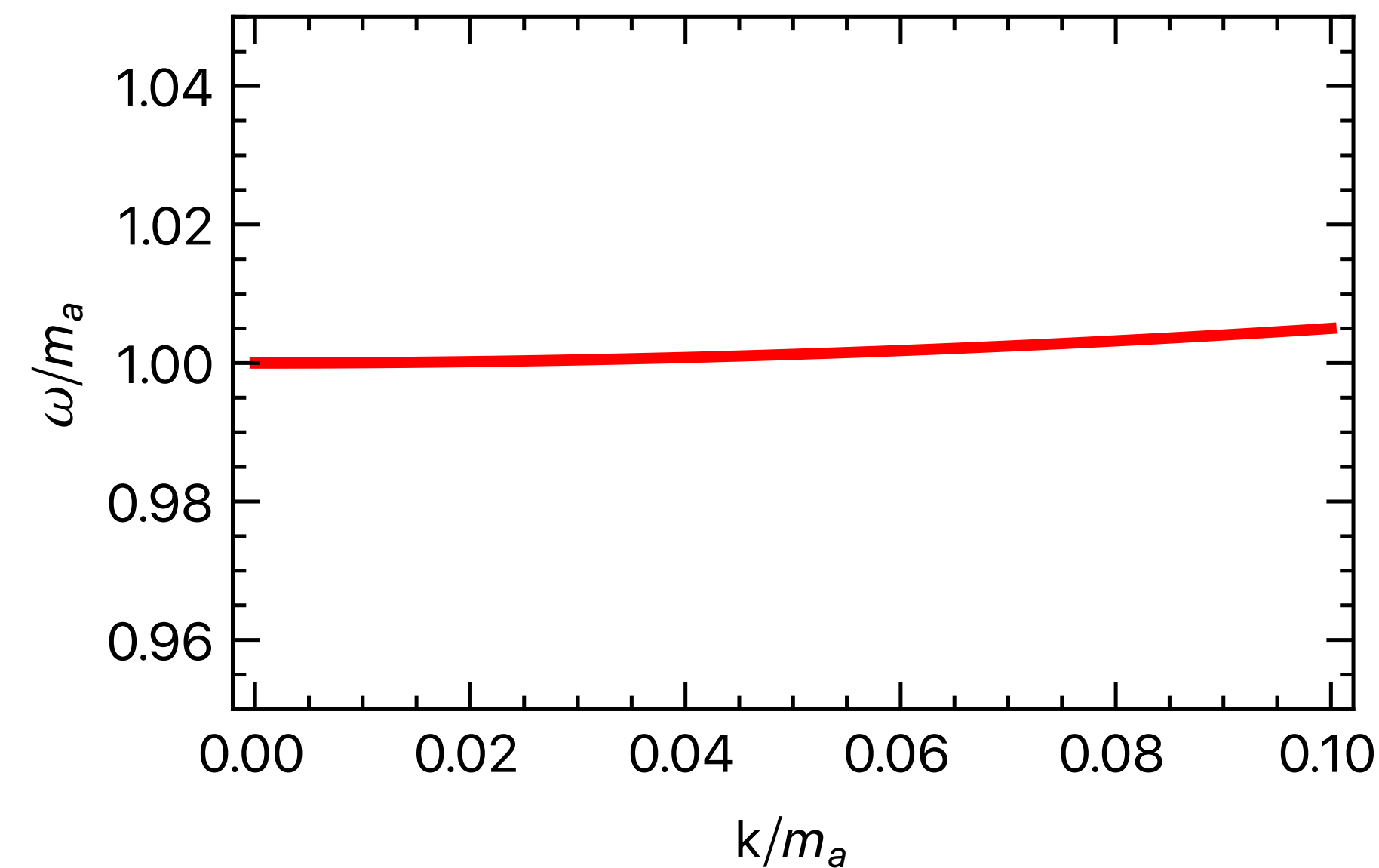
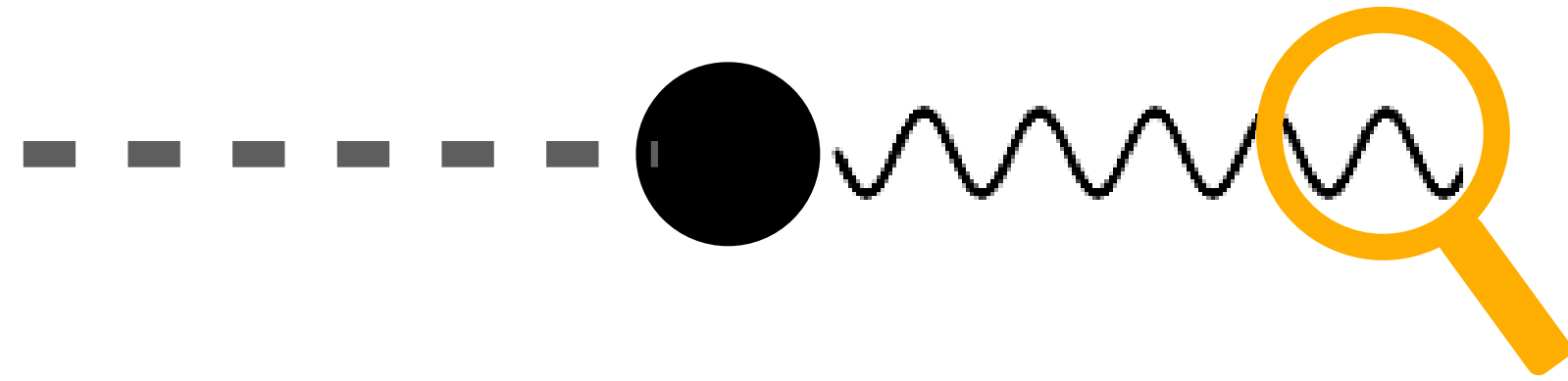
<https://www.teraxion.com/en/company/fiberbragggrating/>



BLINOV, GAO, HARNIK, JANISH and SINCLAIR  
(2024)



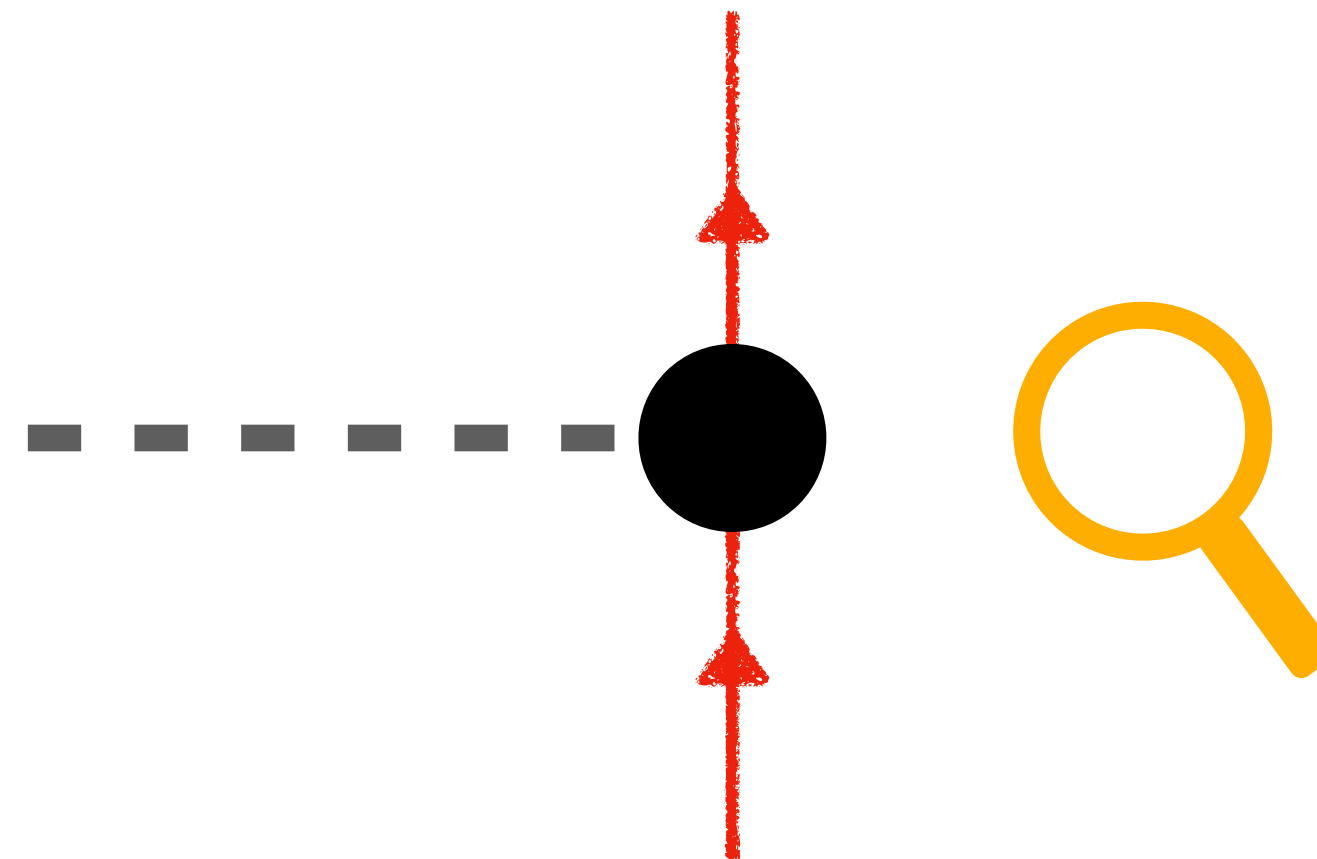
# Summary of detection via absorption



- Used axion-photon coupling as an example
- Want photons with a gapped “flat” dispersion
- Can exist in the form of polaritons in certain special materials, or in the form of “slow” light in meta-materials
- Axion-electron coupling can also allow conversion into gapped magnon

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## Forward scattering (NMR)



# Axions can couple to spins of fermions

$$\mathcal{L}_{\text{int}} \supset g_{af} \partial_\mu a \bar{f} \gamma^\mu \gamma^5 f \quad g_{af} \sim \frac{1}{f_a}$$

NR fermions  $V(\mathbf{x}) = i \frac{\dot{a}^{\text{cl}}}{f_a} \frac{\mathbf{p}' + \mathbf{p}}{m} \cdot \mathbf{S} - i \frac{2 \nabla a^{\text{cl}} \cdot \mathbf{S}}{f_a}$

Compared with  $\gamma_f \mathbf{S} \cdot \mathbf{B}$

$$B_a \sim g_{af} \frac{\nabla a}{\gamma_f}$$

gyromagnetic ratio

$$\gamma_n = \frac{e\hbar}{2m_p} g_n \quad \gamma_e = \frac{e\hbar}{2m_e} g_e$$

# Axions can couple to nuclear spins

$$\mathcal{L}_{\text{int}} \supset g_{aN} \partial_\mu a \bar{N} \gamma^\mu \gamma^5 N$$

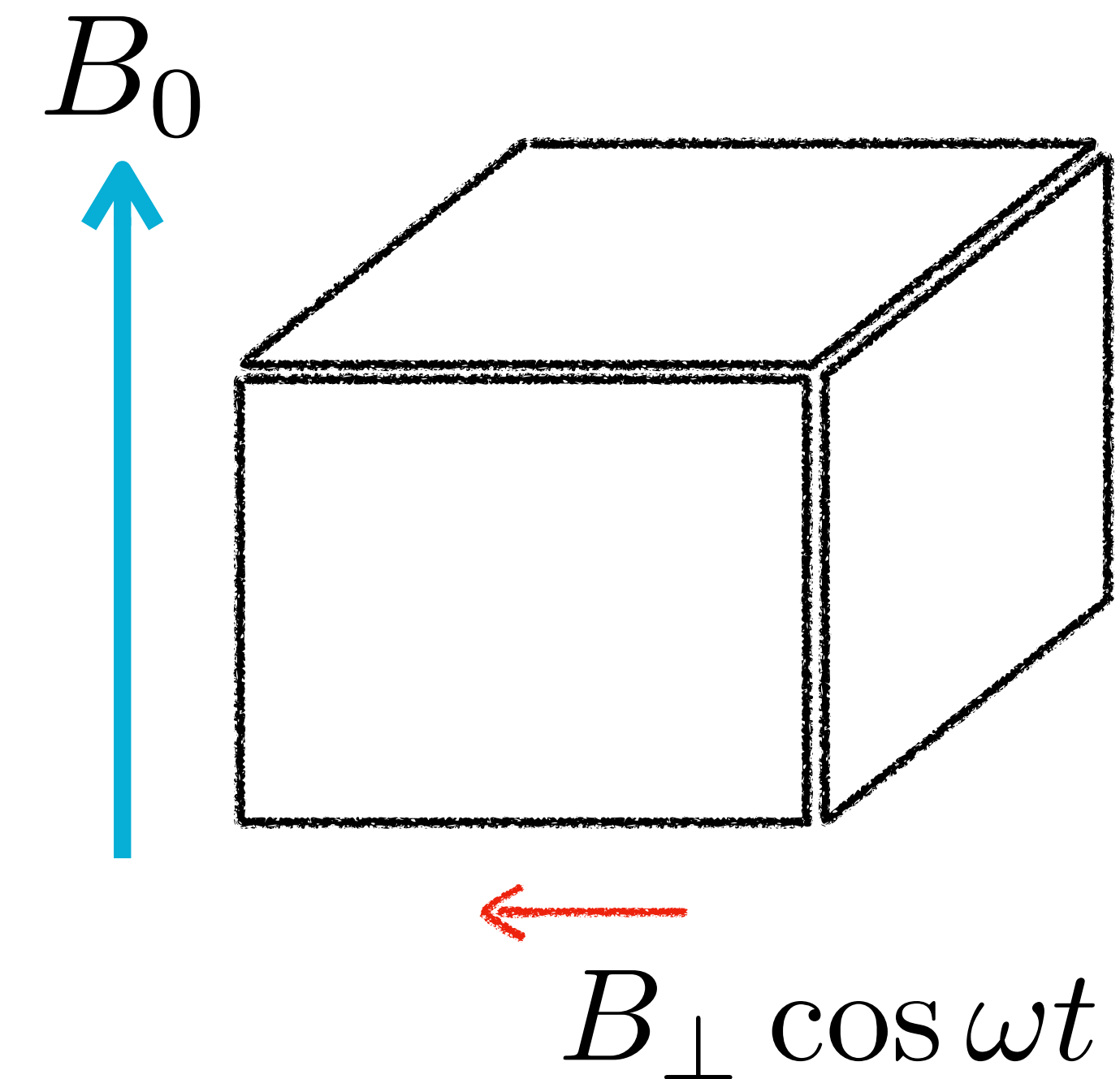
$g_{aN}$  allows us to search for axion DM using Nuclear Magnetic Resonance (NMR).

$$H_{\text{eff}} \supset \langle \vec{\mu}_n \rangle \cdot \underbrace{g_{aN} \frac{\vec{\nabla} a}{\gamma_n}}_{\vec{B}_{a_{\text{DM}}} \sim 10^{-16} \text{T} \left( \frac{g_{aN}}{10^{-10} \text{GeV}^{-1}} \right)}$$



# Nuclear magnetic resonance

- Resonance condition:  $\omega = \omega_L = \gamma B_0$

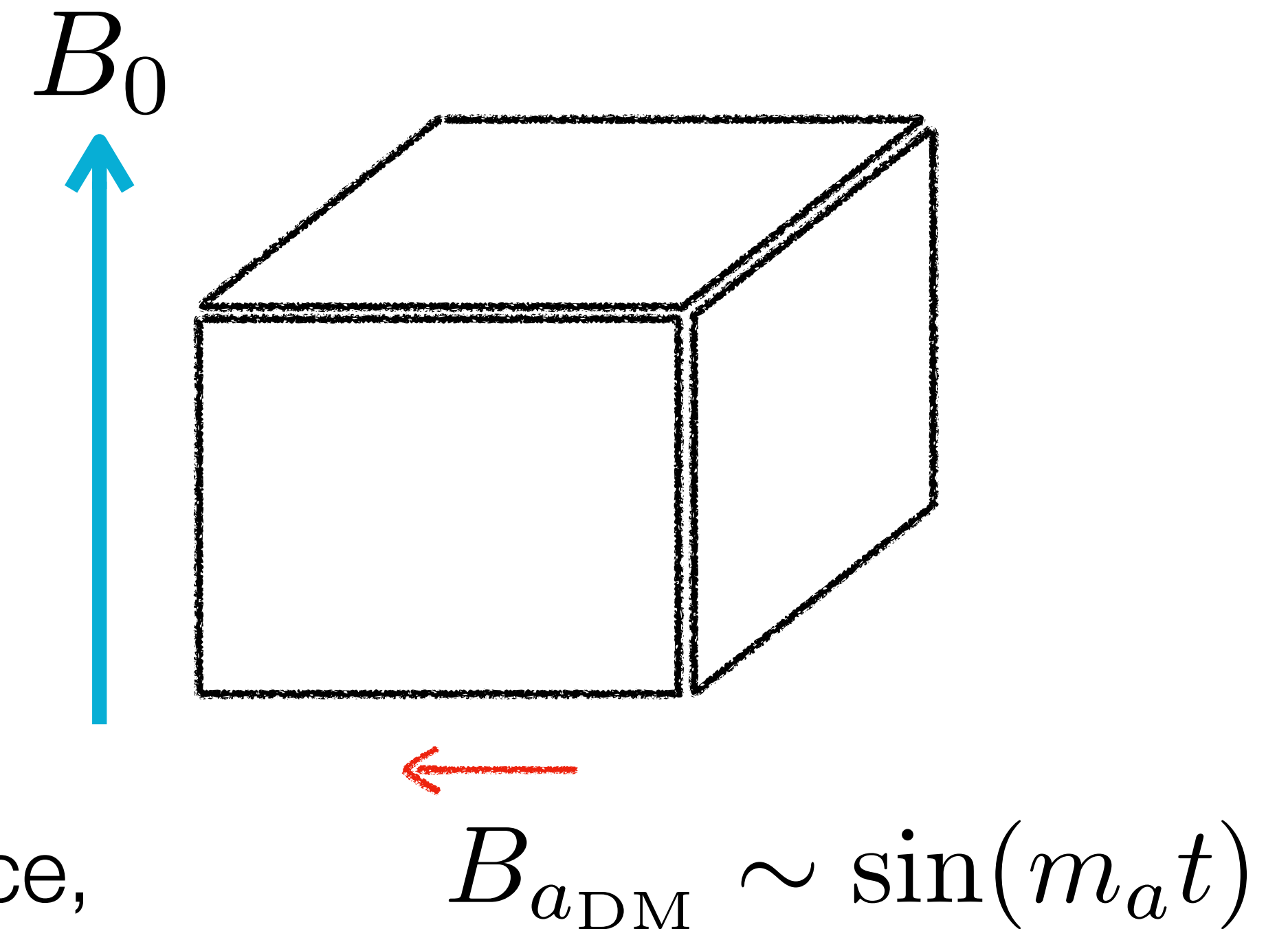


# Nuclear magnetic resonance

- Resonance condition:  $\omega = \omega_L = \gamma B_0$
- Tune  $B_0$  to match axion mass with Larmor frequency  $\omega_L$

Graham and Rajendran (2013)

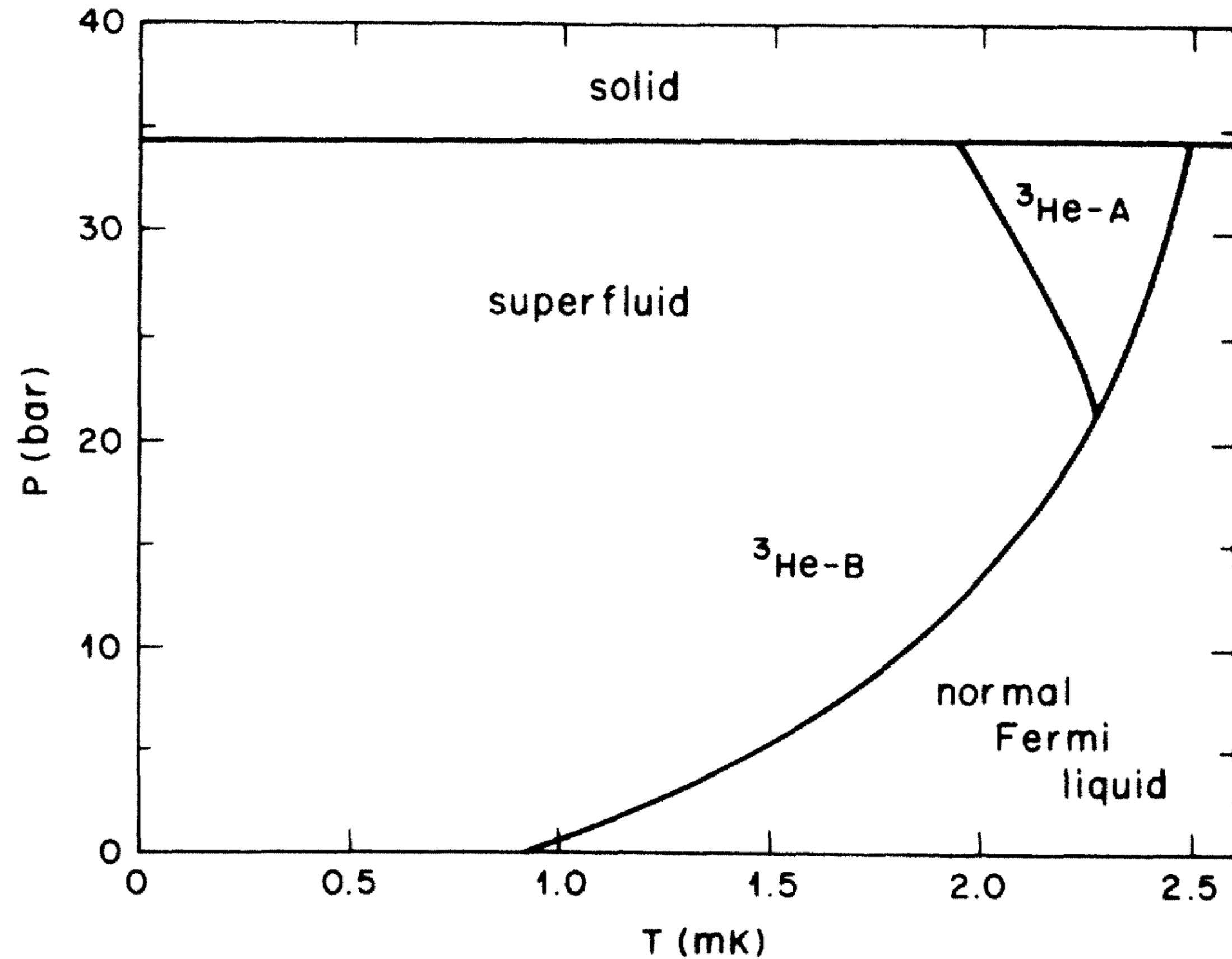
- Signal to noise is limited by decoherence of nuclear spins
- Special phases of helium-3 have large coherence, can be a good NMR material



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# Helium 3 B, homogeneous precession domain

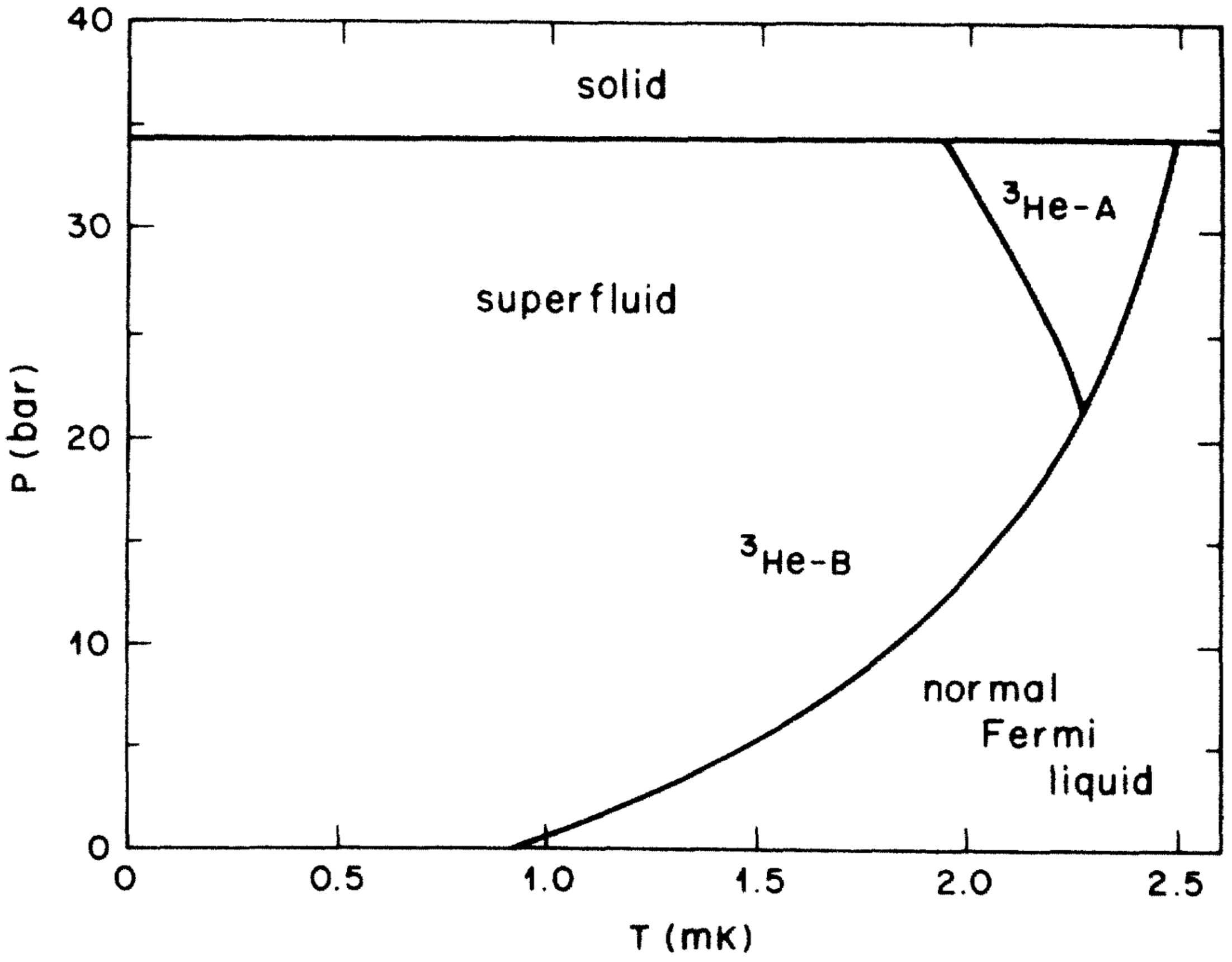
# Properties of $^3\text{He}$



- $T < \sim 1\text{K}$ , Fermi liquid, He-3 quasiparticles

Phys. Rev. B 33, 7520 (1986)

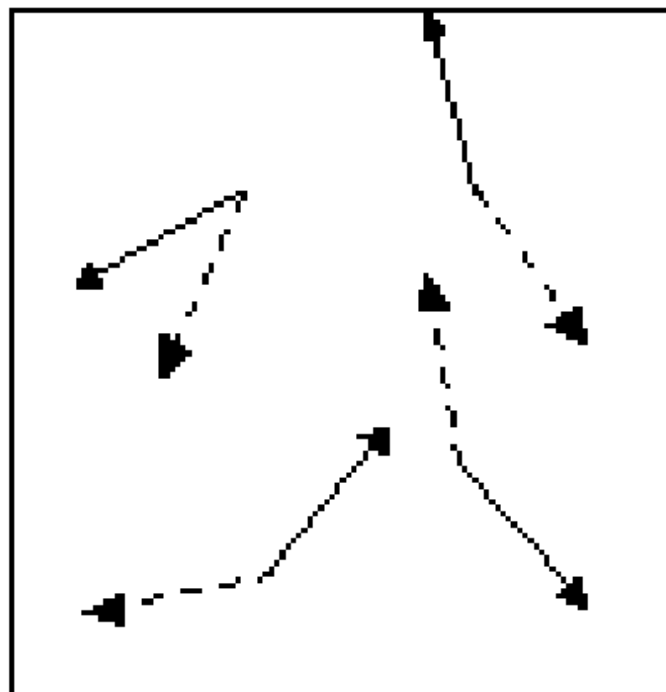
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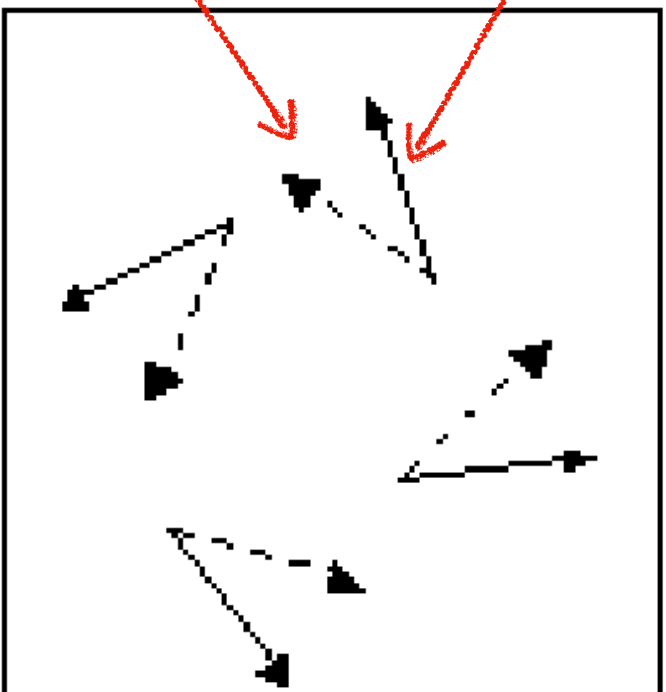
Phys. Rev. B 33, 7520 (1986)

- $T < \sim \text{mK}$ , superfluid phase ( $\sim$  BEC of Cooper pairs of He-3 quasiparticles)

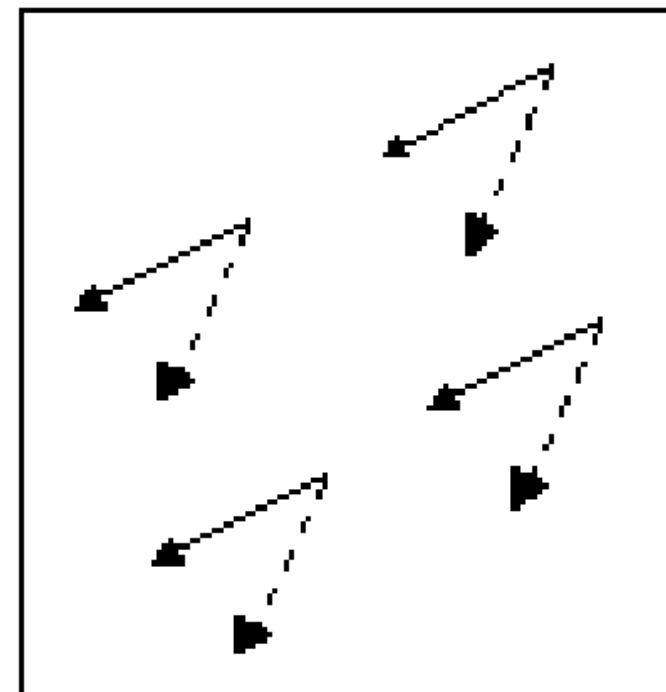
$$L = 1 \quad S = 1$$



Unbroken phase



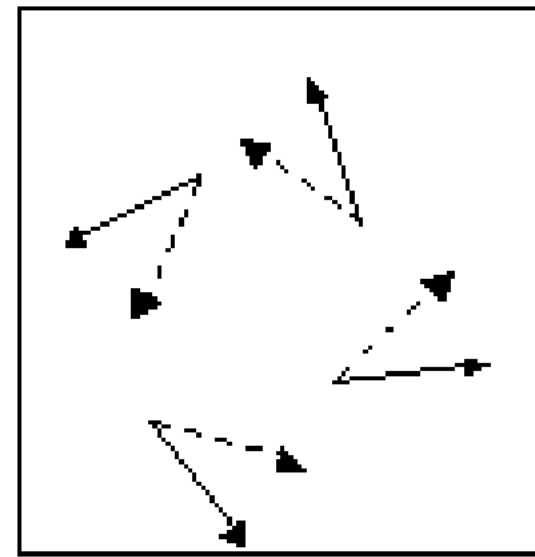
B-phase



A-phase

# ${}^3\text{He} - \text{B}$

## B-phase

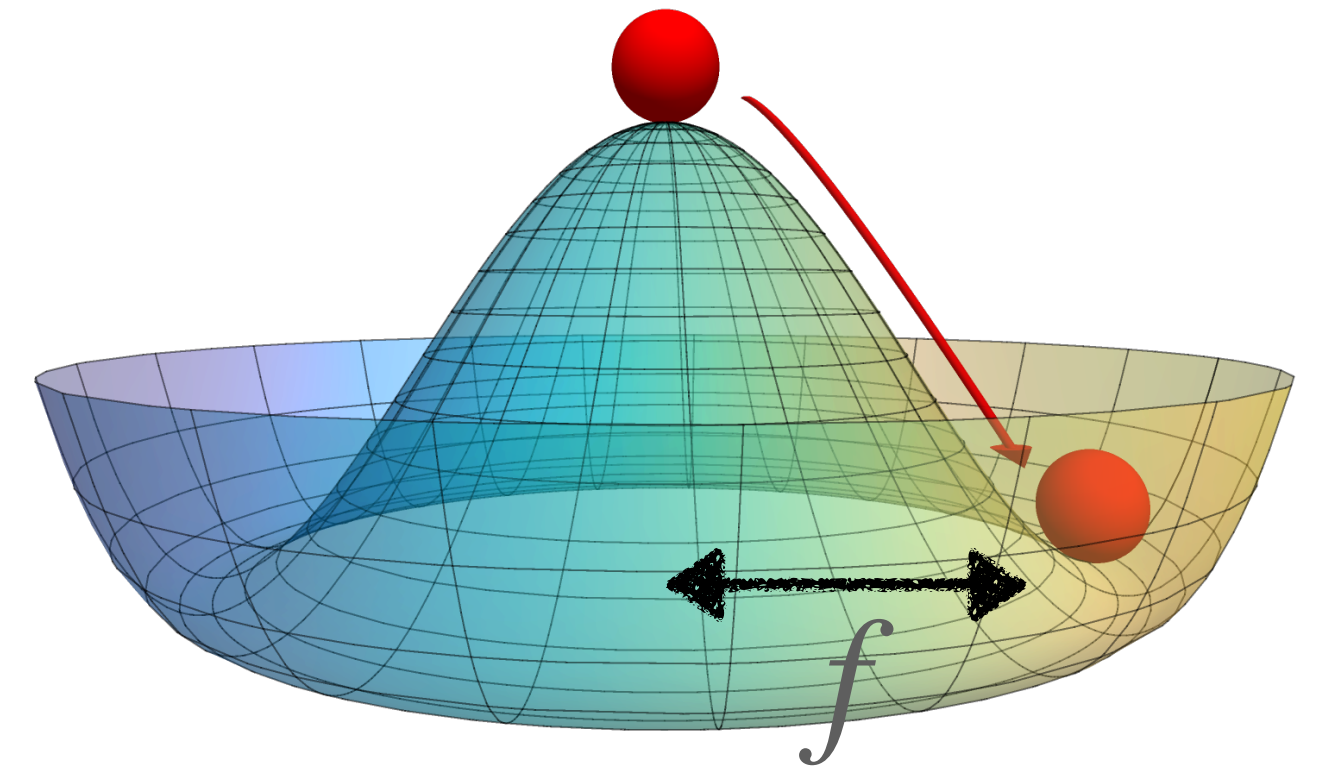


spontaneously broken spin orbit symmetry

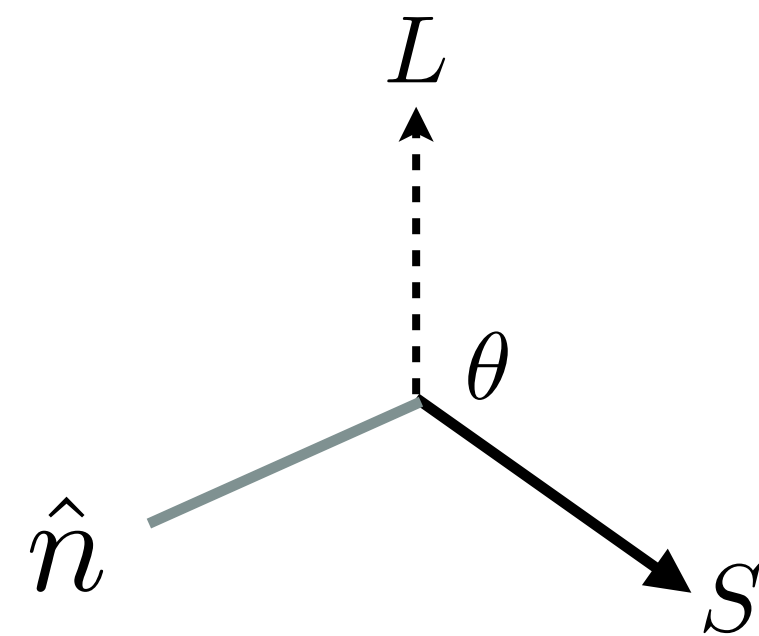
$$SO(3)_S \times SO(3)_L \times U(1)_\phi \rightarrow SO(3)_{L+S}$$

$$e^{i\phi} R_{\mu j}(\hat{n}, \theta)$$

Leggett Rev. Mod. Phys. 47, 331 (1975)

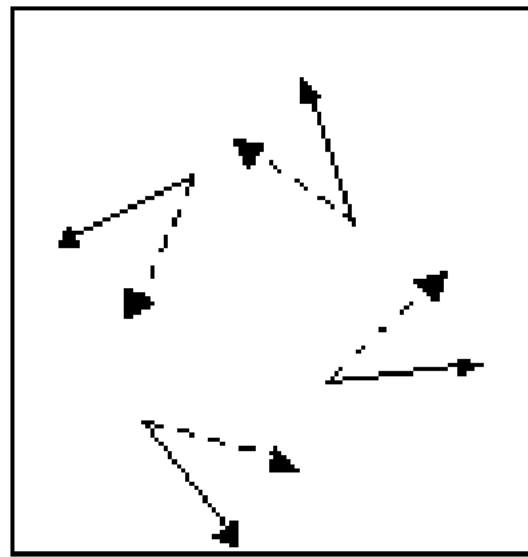


But, a lot of degenerate ground states



# ${}^3\text{He} - \text{B}$

## B-phase

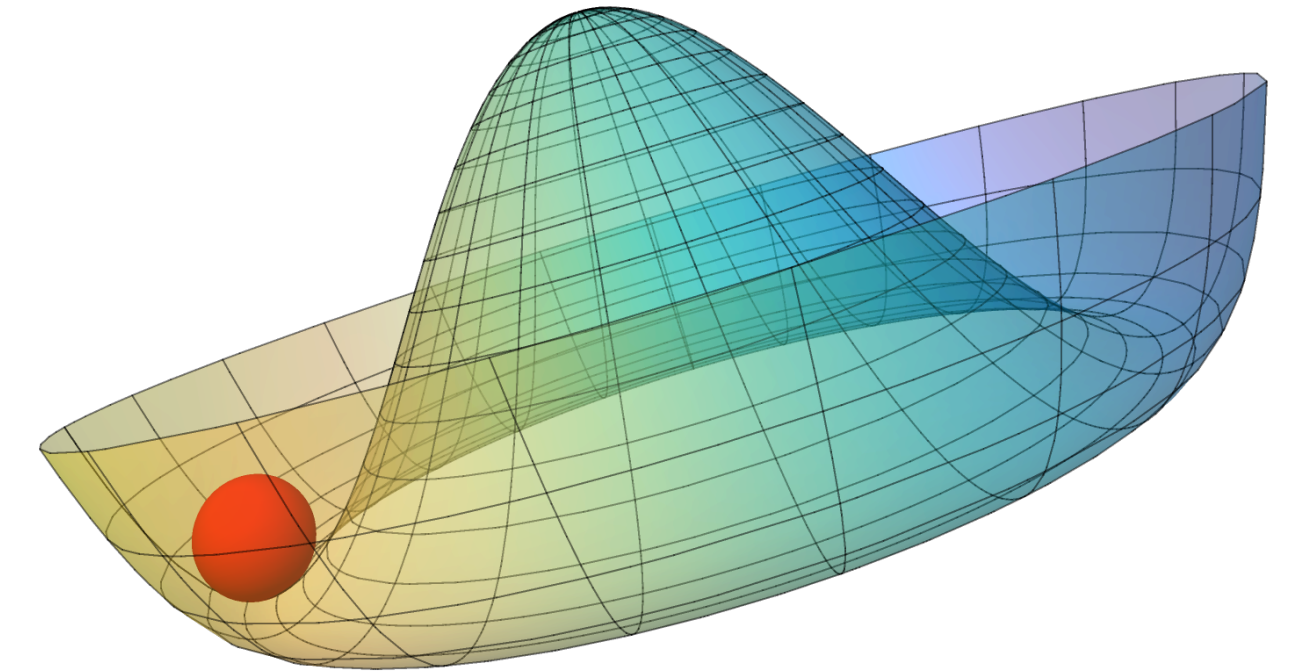


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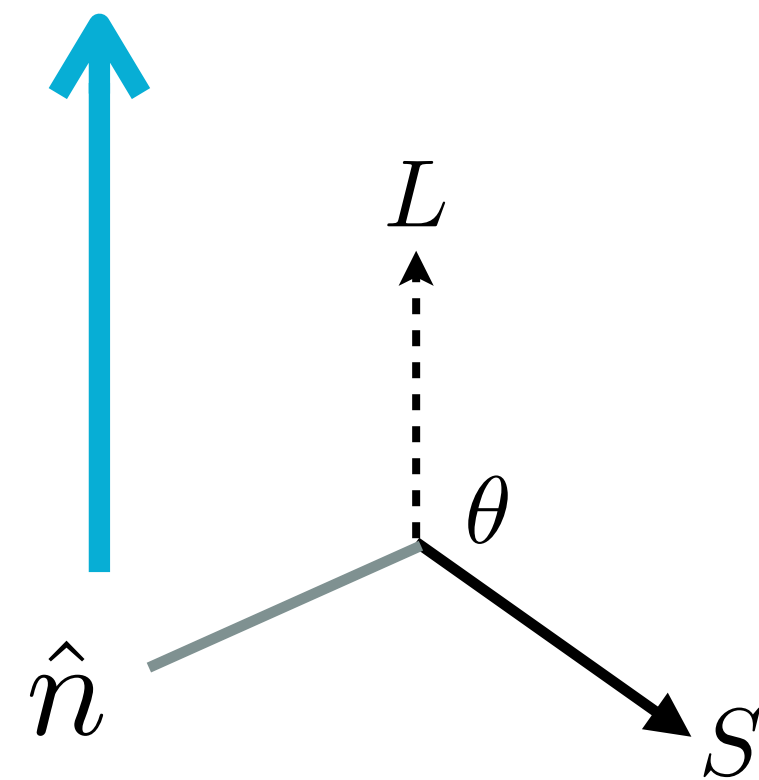
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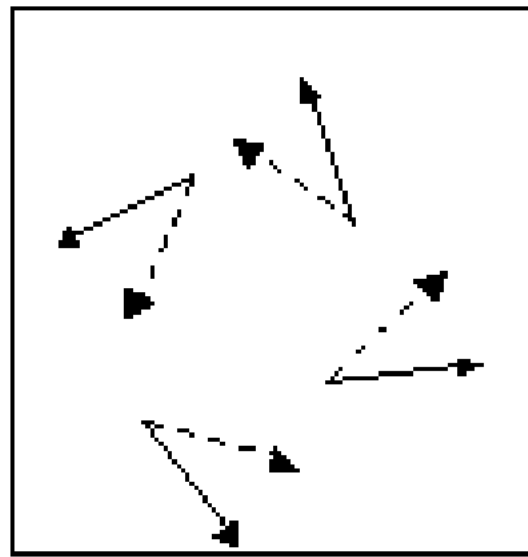
$H \hat{z}$



External magnetic field:  $H \hat{z}$

# ${}^3\text{He} - \text{B}$

## B-phase

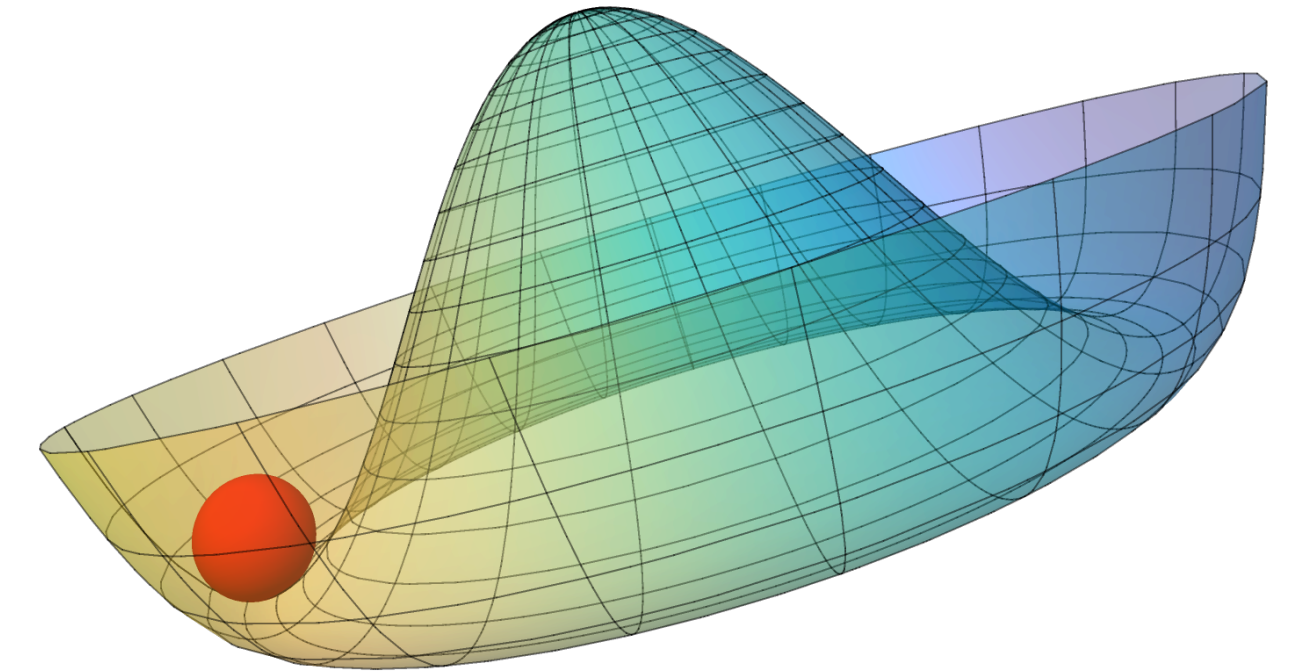


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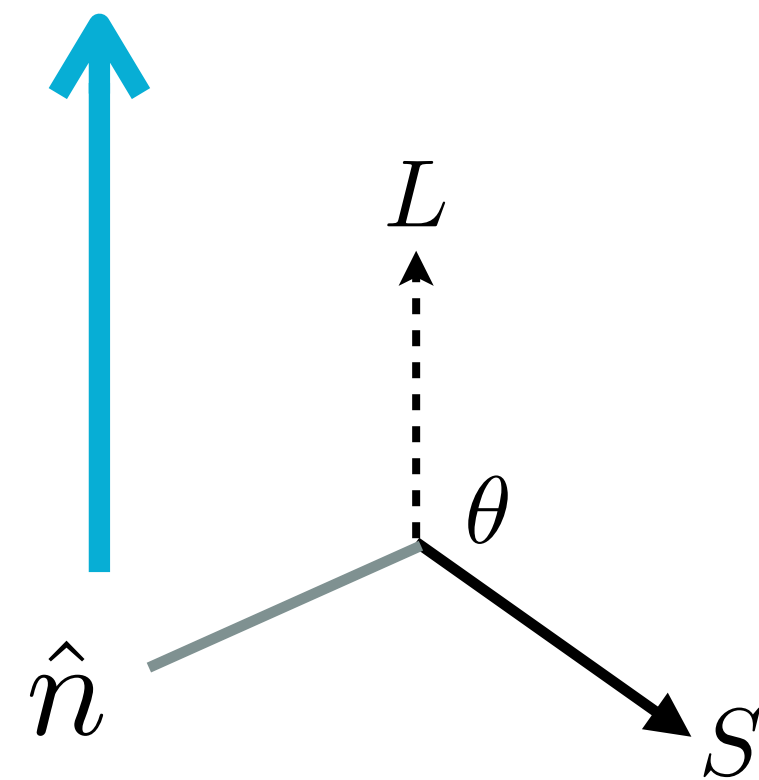
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$H \hat{z}$



External magnetic field:  $H \hat{z}$

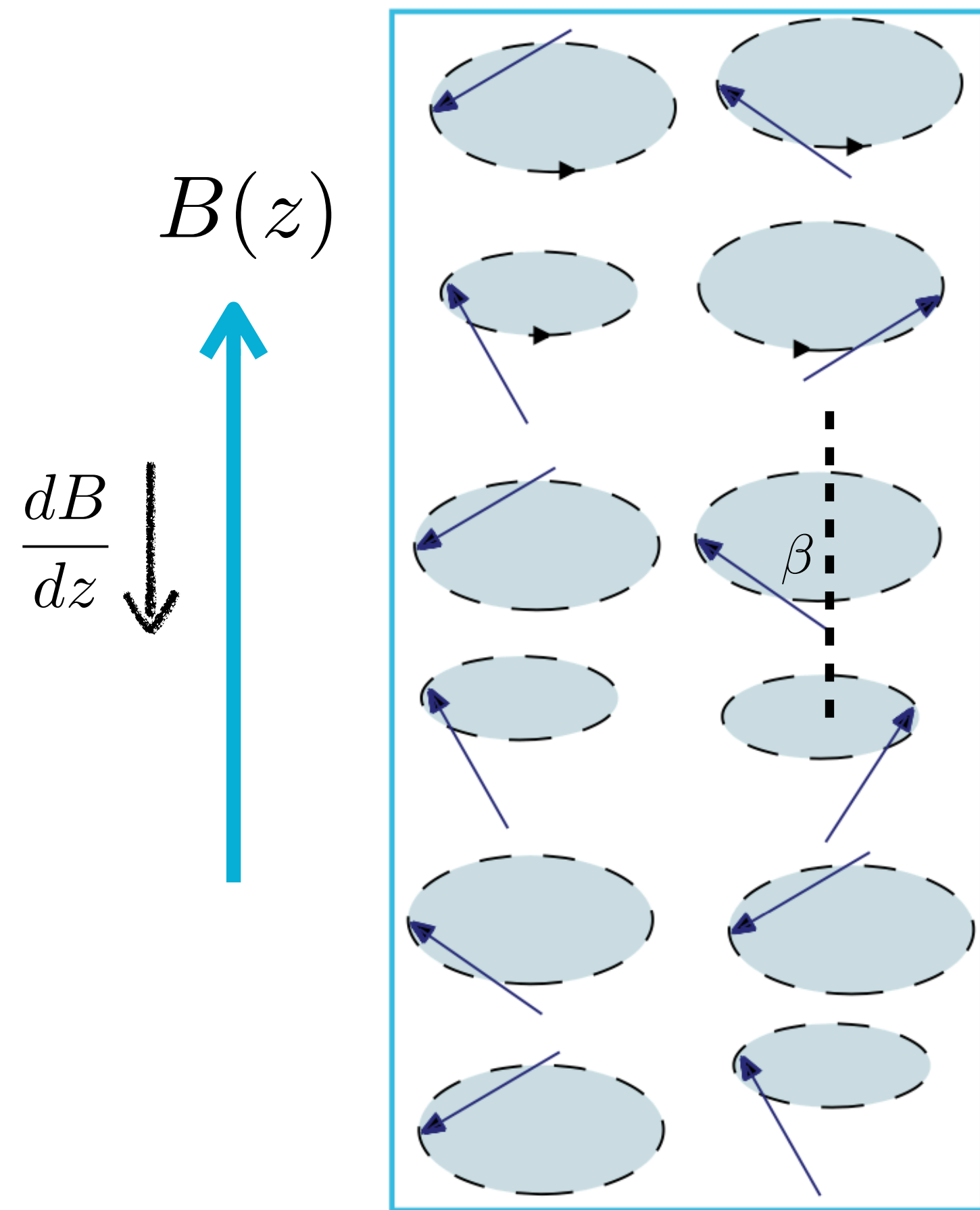
Dipole interaction:  $\cos \theta = -\frac{1}{4}$



# Pulsed NMR with $^3\text{He} - \text{B}$

[Bunkov and Volovik, 0904.3889 and 1003.4889]

Fomin Sov. Phys. JETP 61, 1207 (1985)



Spins tipped by a tip angle  $\beta$  immediately after the pulse

Characteristic time scale with superfluid  $\hbar/\Delta(T)$

$$\Delta(T) \sim 10^2 (1 - T/T_c)^{1/2} \text{MHz}$$

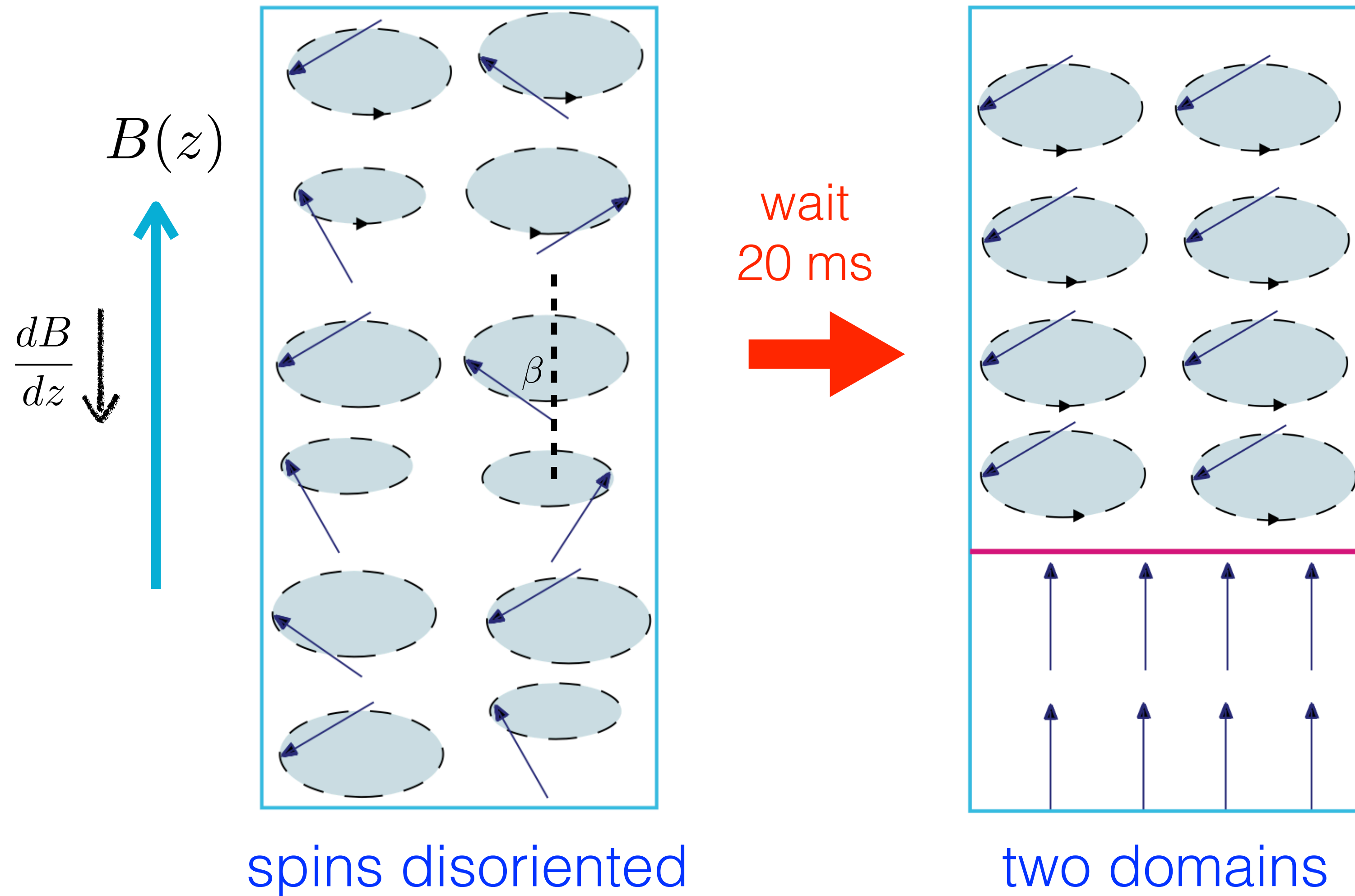
spins disoriented

# Pulsed NMR with $^3\text{He} - \text{B}$

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## BEC of N Magnons

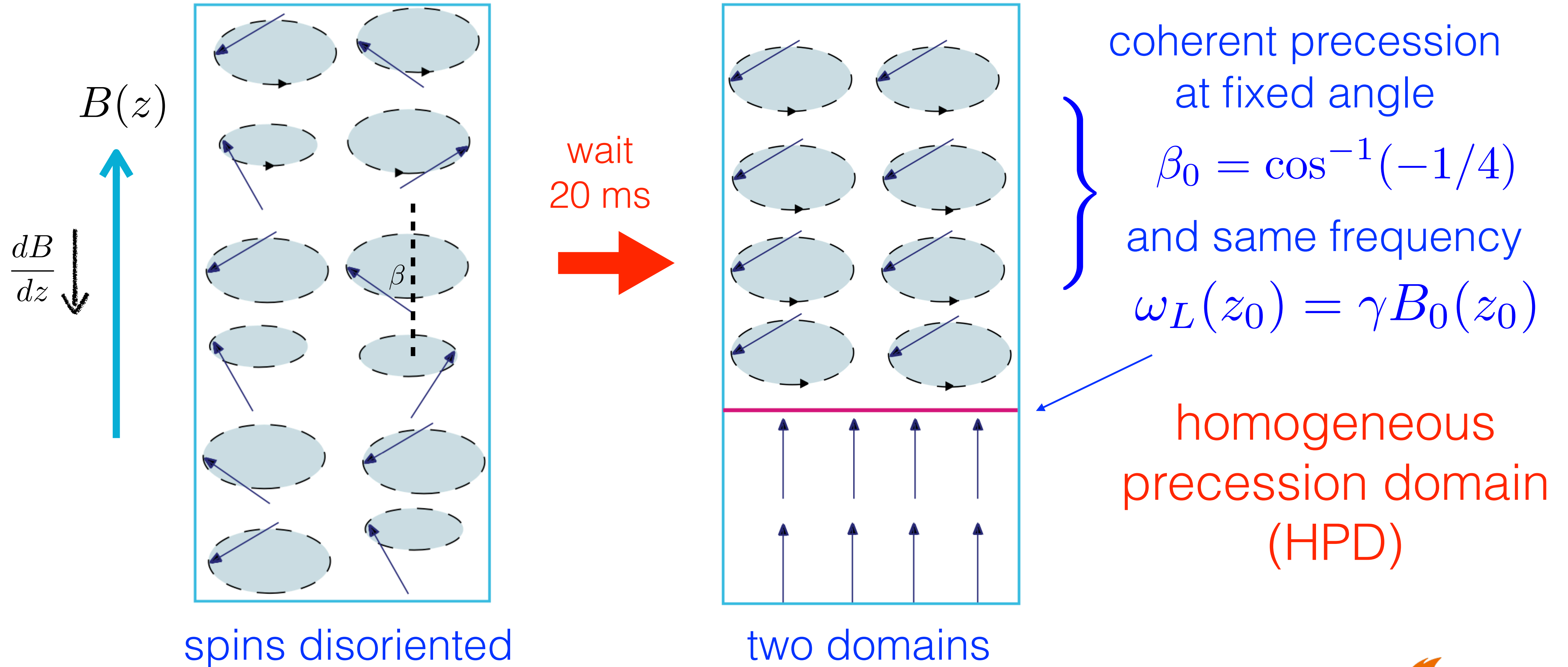


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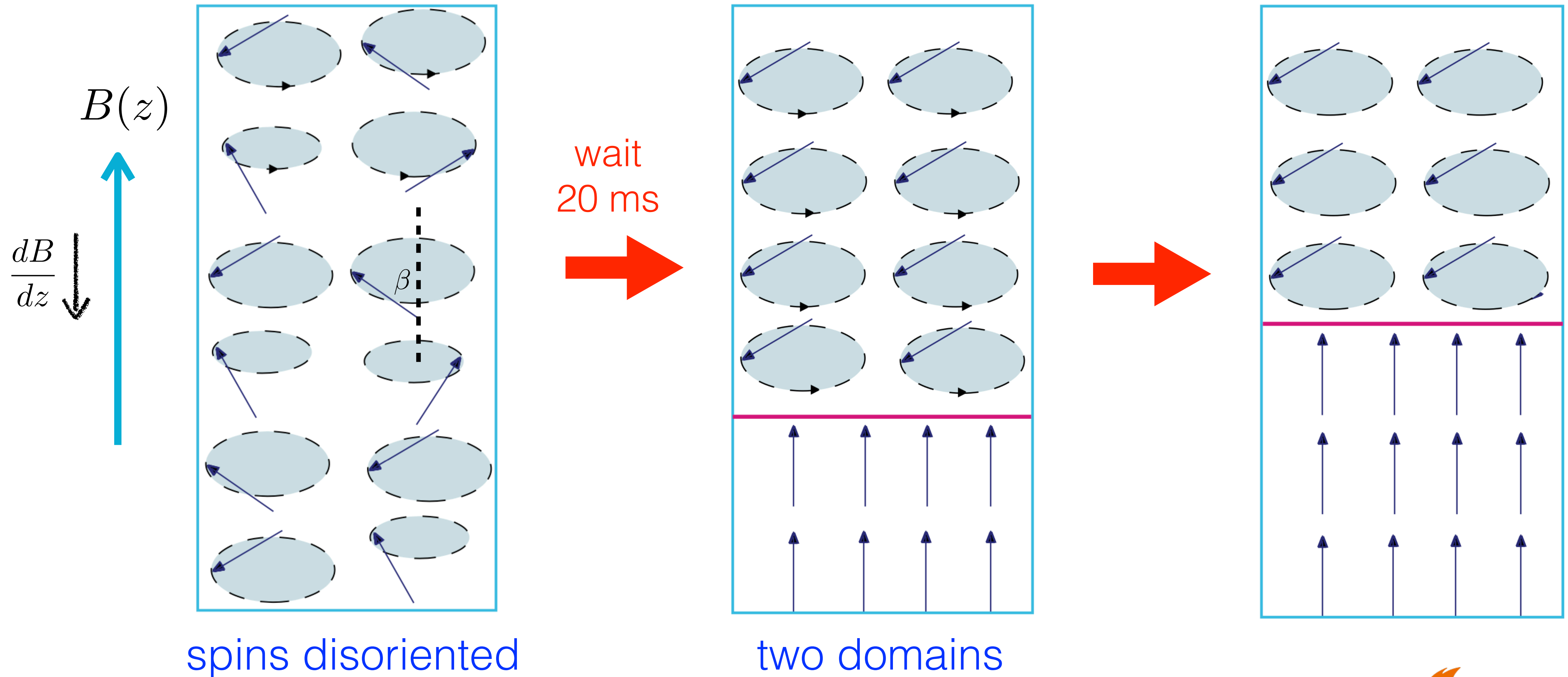
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BEC of N Magnons

Coherent decay of magnons  $N \sim 1/T_1$



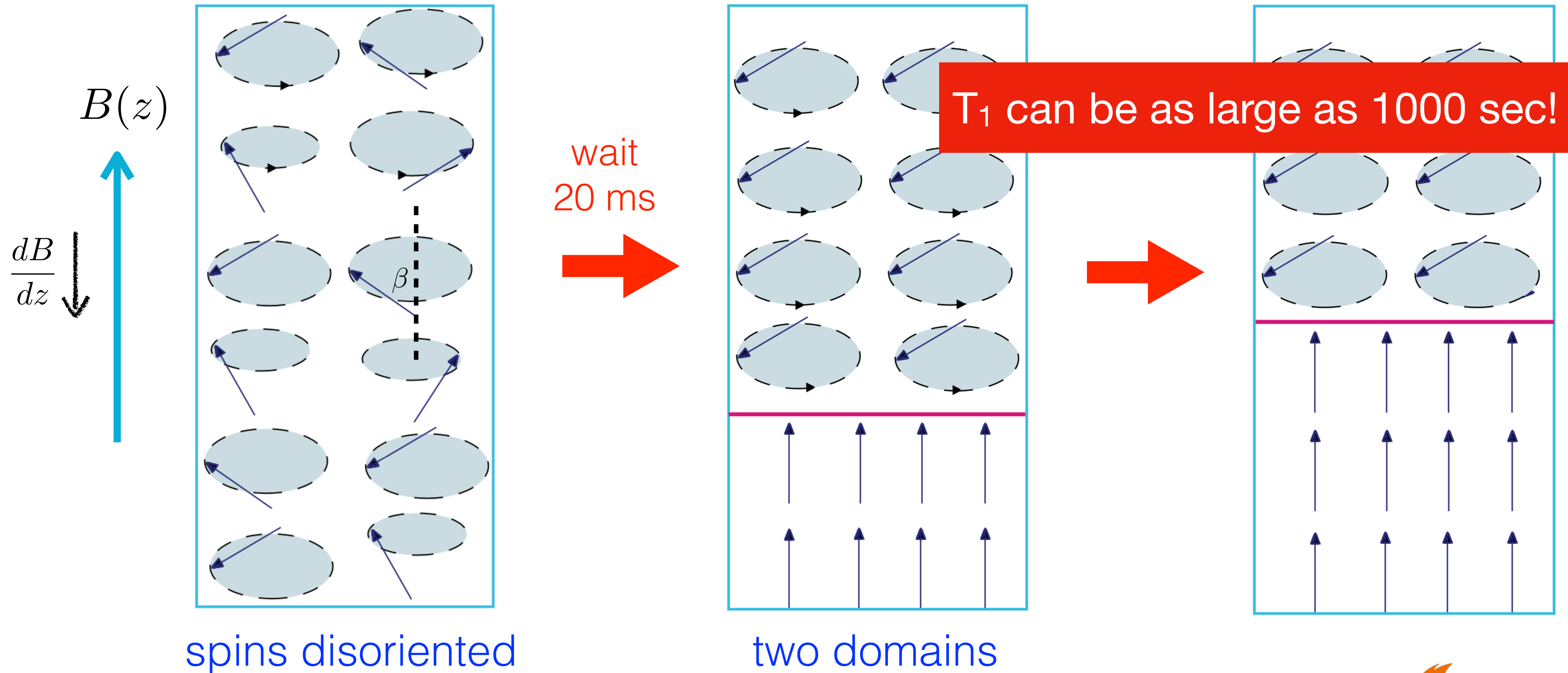
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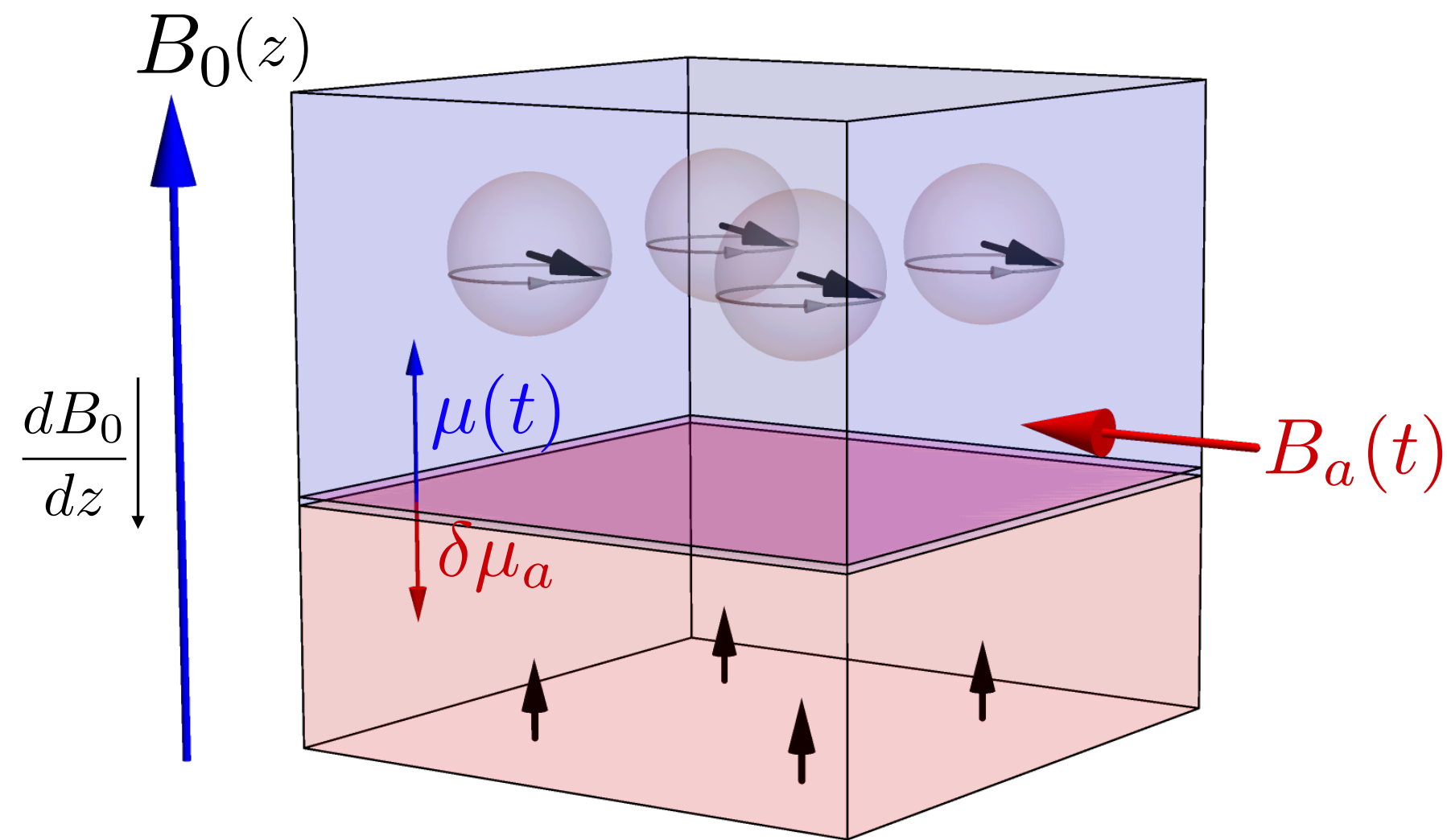
Fomin Sov. Phys. JETP 61, 1207 (1985)

BEC of N Magnons

Coherent decay of magnons  $N \sim 1/T_1$



# Axion wind detection using the HPD of He-3



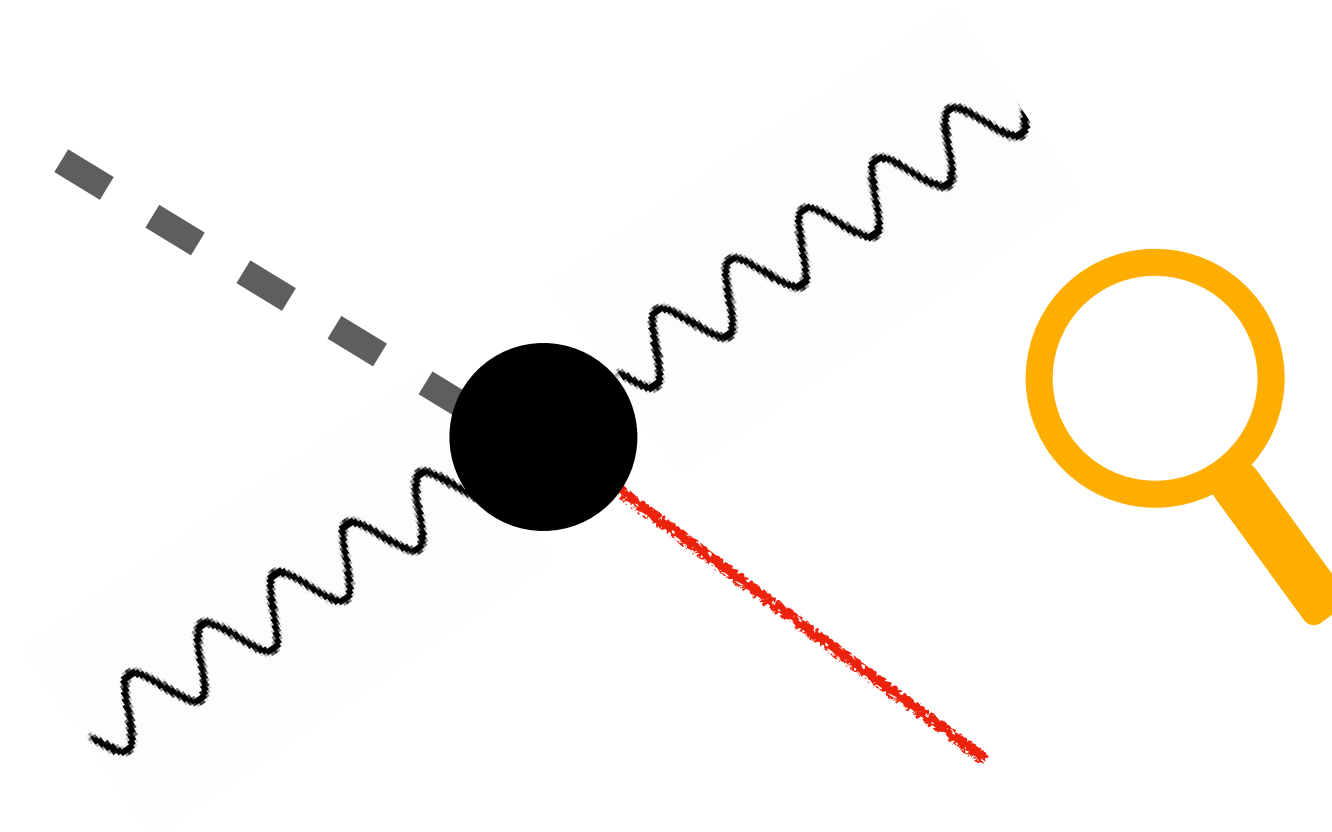
- Rely on axion-nucleon coupling
- Target frequency: 10neV range
- Scan axion masses naturally during decay of the HPD
- Challenging to read out the signal, see Yoni's talk

GAO, HALPERIN, KAHN, NGUYEN, Schütte-Engel and SCOTT (2022)

FOSTER, GAO, HALPERIN, KAHN, MANDE, NGUYEN, Schütte-Engel and SCOTT (2023)

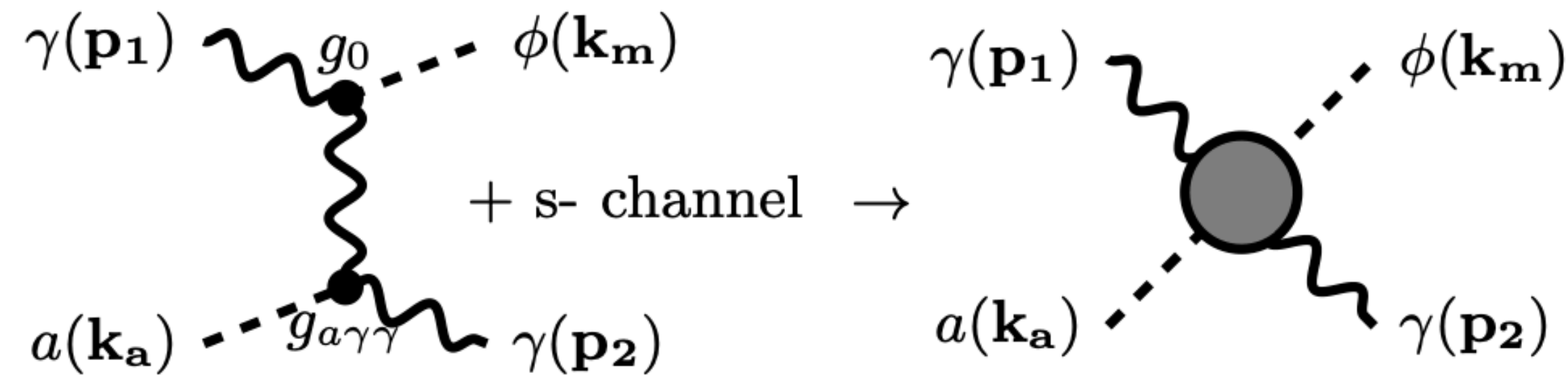
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## An example of 2-2 scattering



# Optomechanical cavity filled with Superfluid He-4

MURGUI, WANG and ZUREK (2023)



Momentum conservation

$$\mathbf{p}_1 + \mathbf{k}_a = \mathbf{p}_2 + \mathbf{k}_m$$

Energy conservation

$$|\mathbf{p}_1| + m_a \simeq |\mathbf{p}_2| + c_s |\mathbf{k}_m|$$

- Works because of phonon's dispersion:  $c_s \ll 1$
- Target frequency:  $\mu\text{eV} \sim \text{meV}$



# Conclusion

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- The landscape of axion dark matter is extremely broad, covering many orders of magnitude in mass range. Discovering different possibilities requires a varied set of experimental techniques.
- Special materials /exotic matter can be advantageous in terms of better phase matching between axion and signal photon, unique target frequencies due to the quasiparticle dispersion, as well as lower noise in some cases.
- In the future, more investigations, such as background noise characterization, signal readout optimization, for each proposed setup, are required.

Thank you for your attention!