

The SM as an Effective Field Theory: an overview

Ilaria Brivio



Physics across energy scales



All Theories are Effective

an **Effective Theory** is obtained from a more fundamental one taking a kinematic or parametric limit \rightarrow typically ET = the LO in an **expansion**

- ET typically **simpler** than the full theory in the pertinent regime
- one doesn't need to know the full theory to calculate! the ET is enough

separation of scales/decoupling

Newtonian gravity can be formulated w/o general relativity nuclear physics can be formulate w/o QCD chemistry can be formulated w/o SM...



→ we expect any theory to be replaced by another one going to higher energies (until the ultimate Theory of Everything)

Effective Field Theories



Effective Field Theories

Fermi Theory of β decay

Bottom-up paradigm



measuring EFT parameters **reveals properties** of full theory \rightarrow complement direct searches, reach into higher energies

 ${\bf EFT}$ fully specified by fields+symmetries at ${\bf E}=\mu$

- \rightarrow no reference to underlying model
- \rightarrow free couplings that can be measured!
- \rightarrow higher-*d* terms \Rightarrow limited UV validity, due to *E* growth

The Standard Model Effective Field Theory – SMEFT

promoting the Standard Model to an EFT

add **higher-dimensional** terms made of SM **fields** and respecting the SM **symmetries**

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda} \mathcal{L}_5 + \frac{1}{\Lambda^2} \mathcal{L}_6 + \frac{1}{\Lambda^3} \mathcal{L}_7 + \frac{1}{\Lambda^4} \mathcal{L}_8 + \dots \qquad \qquad \mathcal{L}_d = \sum_i C_i \mathcal{O}_i^{(d)}$$

 $C_i =$ Wilson coefficients

 $\mathcal{O}_i^{(d)} =$ gauge-invariant operators forming a <u>basis</u>: a complete, non-redundant set

- describes any beyond-SM theory, provided it lives at $\Lambda \gg v$
- ▶ a complete catalogue of all allowed beyond-SM effects, organized by expected size
- > not experiment-specific! can be used as a common framework for LHC and other experiments
- ▶ a proper QFT! renormalizable order-by-order, systematically improvable in loops

SMEFT at d = 6: the Warsaw basis

X ³		φ^6 and $\varphi^4 D^2$		$\psi^2 \varphi^3$		
Q_G	$f^{ABC}G^{A\nu}_{\mu}G^{B\rho}_{\nu}G^{C\mu}_{\rho}$	Q_{arphi}	$(arphi^\dagger arphi)^3$	$Q_{e\varphi}$	$(arphi^{\dagger}arphi)(ar{l}_{p}e_{r}arphi)$	
$Q_{\widetilde{G}}$	$f^{ABC} \widetilde{G}^{A\nu}_{\mu} G^{B\rho}_{\nu} G^{C\mu}_{\rho}$	$Q_{\varphi \Box}$	$(arphi^\daggerarphi) \Box (arphi^\daggerarphi)$	$Q_{u\varphi}$	$(arphi^\dagger arphi) (ar q_p u_r \widetilde arphi)$	
Q_W	$\varepsilon^{IJK}W^{I\nu}_{\mu}W^{J\rho}_{\nu}W^{K\mu}_{\rho}$	$Q_{\varphi D}$	$\left(arphi^{\dagger} D^{\mu} arphi ight)^{\star} \left(arphi^{\dagger} D_{\mu} arphi ight)$	$Q_{d\varphi}$	$(arphi^\dagger arphi) (ar q_p d_r arphi)$	
$Q_{\widetilde{W}}$	$\varepsilon^{IJK}\widetilde{W}^{I\nu}_{\mu}W^{J\rho}_{\nu}W^{K\mu}_{\rho}$] 4
$X^2 \varphi^2$		$\psi^2 X \varphi$		$\psi^2 arphi^2 D$		
$Q_{\varphi G}$	$\varphi^{\dagger}\varphiG^{A}_{\mu u}G^{A\mu u}$	Q_{eW}	$(\bar{l}_p \sigma^{\mu u} e_r) \tau^I \varphi W^I_{\mu u}$	$Q_{\varphi l}^{(1)}$	$(\varphi^{\dagger}i\overleftrightarrow{D}_{\mu}\varphi)(\overline{l}_{p}\gamma^{\mu}l_{r})$	-
$Q_{\varphi \widetilde{G}}$	$arphi^\dagger arphi \widetilde{G}^A_{\mu u} G^{A\mu u}$	Q_{eB}	$(\bar{l}_p \sigma^{\mu u} e_r) \varphi B_{\mu u}$	$Q^{(3)}_{arphi l}$	$(\varphi^\dagger i \overleftrightarrow{D}^I_\mu \varphi) (\bar{l}_p \tau^I \gamma^\mu l_r)$	
$Q_{\varphi W}$	$arphi^\dagger arphi W^I_{\mu u} W^{I\mu u}$	Q_{uG}	$(\bar{q}_p \sigma^{\mu u} T^A u_r) \widetilde{\varphi} G^A_{\mu u}$	$Q_{arphi e}$	$(\varphi^{\dagger}i\overleftrightarrow{D}_{\mu}\varphi)(\bar{e}_{p}\gamma^{\mu}e_{r})$	Fa
$Q_{\varphi \widetilde{W}}$	$arphi^\dagger arphi \widetilde{W}^I_{\mu u} W^{I\mu u}$	Q_{uW}	$(ar{q}_p \sigma^{\mu u} u_r) au^I \widetilde{arphi} W^I_{\mu u}$	$Q^{(1)}_{arphi q}$	$(arphi^\dagger i \overleftrightarrow{D}_\mu arphi) (ar{q}_p \gamma^\mu q_r)$	IB
$Q_{\varphi B}$	$\varphi^{\dagger}\varphiB_{\mu u}B^{\mu u}$	Q_{uB}	$(\bar{q}_p \sigma^{\mu u} u_r) \widetilde{\varphi} B_{\mu u}$	$Q^{(3)}_{arphi q}$	$(\varphi^{\dagger}i\overleftrightarrow{D}^{I}_{\mu}\varphi)(\bar{q}_{p}\tau^{I}\gamma^{\mu}q_{r})$	
$Q_{\varphi \widetilde{B}}$	$arphi^\dagger arphi \widetilde{B}_{\mu u} B^{\mu u}$	Q_{dG}	$(\bar{q}_p \sigma^{\mu u} T^A d_r) \varphi G^A_{\mu u}$	$Q_{\varphi u}$	$(\varphi^{\dagger}i\overleftrightarrow{D}_{\mu}\varphi)(\bar{u}_{p}\gamma^{\mu}u_{r})$	
$Q_{\varphi WB}$	$arphi^\dagger au^I arphi W^I_{\mu u} B^{\mu u}$	Q_{dW}	$(\bar{q}_p \sigma^{\mu u} d_r) \tau^I \varphi W^I_{\mu u}$	$Q_{arphi d}$	$(\varphi^{\dagger}i\overleftrightarrow{D}_{\mu}\varphi)(\bar{d}_{p}\gamma^{\mu}d_{r})$	
$Q_{\varphi \widetilde{W}B}$	$arphi^\dagger au^I arphi \widetilde{W}^I_{\mu u} B^{\mu u}$	Q_{dB}	$(\bar{q}_p \sigma^{\mu u} d_r) \varphi B_{\mu u}$	$Q_{\varphi ud}$	$i(\widetilde{arphi}^{\dagger}D_{\mu}arphi)(ar{u}_{p}\gamma^{\mu}d_{r})$	



go down to O(100) imposing flavor symmetries, CP Faroughy et al 2005.05366 Greljo et al 2203.09561 IB 2012.11343

> they are \sim never all relevant at the same time

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3 rzadkowski, Iskrzynski, Misiak, Rosiek 1008.4884

SMEFT at d = 6: the Warsaw basis

$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$		
Q_{ll}	$(ar{l}_p \gamma_\mu l_r) (ar{l}_s \gamma^\mu l_t)$	Q_{ee}	$(ar{e}_p \gamma_\mu e_r) (ar{e}_s \gamma^\mu e_t)$	Q_{le}	$(ar{l}_p \gamma_\mu l_r) (ar{e}_s \gamma^\mu e_t)$	
$Q_{qq}^{(1)}$	$(ar{q}_p \gamma_\mu q_r) (ar{q}_s \gamma^\mu q_t)$	Q_{uu}	$(ar{u}_p \gamma_\mu u_r)(ar{u}_s \gamma^\mu u_t)$	Q_{lu}	$(ar{l}_p \gamma_\mu l_r) (ar{u}_s \gamma^\mu u_t)$	
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r) (\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{dd}	$(ar{d}_p\gamma_\mu d_r)(ar{d}_s\gamma^\mu d_t)$	Q_{ld}	$(ar{l}_p \gamma_\mu l_r) (ar{d}_s \gamma^\mu d_t)$	
$Q_{lq}^{(1)}$	$(ar{l}_p \gamma_\mu l_r) (ar{q}_s \gamma^\mu q_t)$	Q_{eu}	$(ar{e}_p \gamma_\mu e_r) (ar{u}_s \gamma^\mu u_t)$	Q_{qe}	$(ar{q}_p \gamma_\mu q_r) (ar{e}_s \gamma^\mu e_t)$	
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r) (\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{ed}	$(ar{e}_p \gamma_\mu e_r) (ar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(ar{q}_p \gamma_\mu q_r) (ar{u}_s \gamma^\mu u_t)$	
		$Q_{ud}^{(1)}$	$(ar{u}_p \gamma_\mu u_r) (ar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r) (\bar{u}_s \gamma^\mu T^A u_t)$	
		$Q_{ud}^{(8)}$	$(ar{u}_p \gamma_\mu T^A u_r) (ar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(ar{q}_p \gamma_\mu q_r) (ar{d}_s \gamma^\mu d_t)$	
				$Q_{qd}^{(8)}$	$(ar{q}_p \gamma_\mu T^A q_r) (ar{d}_s \gamma^\mu T^A d_t)$	
$(\bar{L}R)$	$(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$	B-violating				
Q_{ledq}	$(ar{l}_p^j e_r) (ar{d}_s q_t^j)$	Q_{duq}	$\varepsilon^{\alpha\beta\gamma}\varepsilon_{jk}\left[(d_p^{\alpha})^TCu_r^{\beta}\right]\left[(q_s^{\gamma j})^TCl_t^k\right]$			
$Q_{quqd}^{(1)}$	$(ar{q}_p^j u_r) arepsilon_{jk} (ar{q}_s^k d_t)$	Q_{qqu}	$\varepsilon^{\alpha\beta\gamma}\varepsilon_{jk}\left[(q_p^{\alpha j})^T C q_r^{\beta k}\right]\left[(u_s^{\gamma})^T C e_t\right]$			
$Q_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \varepsilon_{jk} (\bar{q}_s^k T^A d_t)$	Q_{qqq}	$\varepsilon^{\alpha\beta\gamma}\varepsilon_{jk}\varepsilon_{mn}\left[(q_p^{\alpha j})^T C q_r^{\beta k}\right]\left[(q_s^{\gamma m})^T C l_t^n\right]$			
$Q_{lequ}^{(1)}$	$(ar{l}_p^j e_r) arepsilon_{jk} (ar{q}_s^k u_t)$	Q_{duu}	$arepsilon^{lphaeta\gamma}\left[(d_p^lpha)^TCu_r^eta ight]\left[(u_s^\gamma)^TCe_t ight]$			
$Q_{leav}^{(3)}$	$(\bar{l}_{r}^{j}\sigma_{\mu\nu}e_{r})\varepsilon_{jk}(\bar{q}_{s}^{k}\sigma^{\mu\nu}u_{t})$					



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3rzadkowski, Iskrzynski, Misiak, Rosiek 1008.4884

A fast growing series

parameters computed with Hilbert series and automated. flavor plays a major role.

Henning,Lu,Melia,Murayama 1512.03433



bases available up to dimension 12

- d = 5 Weinberg PRL43(1979)1566
- $\mathbf{d} = \mathbf{6}$ Grzadkowski et al 1008.4884 ...
- **d** = 7 Lehman 1410.4193, Henning et al 1512.0343
- **d** = 8 Li et al 2005.00008, Murphy 2005.00059
- ${f d}$ = 9 Li et al 2007.07899, Liao,Ma 2007.08125
- **d** = 10,11,12 Harlander,Kempksens,Schaaf 2305.06832

In SMEFT, operators of odd dimension violate the conservation of B and/or L Kobach 1604.05726

Renormalization Group evolution

when going to 1-loop divergences appear, reabsorbed by counterterms of the same dimension

 \rightarrow SMEFT operators **run and mix** with each other, order by order in A



fully computed at 1 loop for dim-6, automated in DsixTools, wilson

Alonso, Jenkins, Manohar, Trott 1308.2627, 1310.4838, 1312.2014 Celis, Fuentes-Martin, Ruiz-Femenia, Vicente, Virto 1704.04504, 2010.16341, Aebischer, Kumar, Straub 1804.05033

partial results for dim6-2loops and dim8-1loop \rightsquigarrow Luigi, Stefano

Elias-Miro' et al 2005.06983,2112.12131, Bern, Parra-Martinez 2005.12917, Jin, Ren, Yang 2011.02494, Fuentes-Martin et al 2311.13630,2410.07320 Bresciani, Levati, Mastrolia, Paradisi 2312.05026, Chala et al 2106.05291,2205.03301,2309.16611,2409.15408, Boughezal et al 2408.15378...

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Below m_W : the Low Energy EFT (LEFT) or Weak EFT (WET)

at energies $\lesssim m_W$, the heaviest SM particles effectively decouple, and another EFT is more appropriate

fields: SM w/o H, W, Z, t symmetries: $U(1)_{em} \times SU(3)_c$

$$\mathscr{L}_{LEFT} = \mathscr{L}_{QED+QCD} + \frac{v}{v}\mathscr{L}_3 + \frac{1}{v}\mathscr{L}_5 + \frac{1}{v^2}\mathscr{L}_6 + \dots$$

$$\begin{split} \mathscr{L}_{\mathsf{QED}+\mathsf{QCD}} &= -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \frac{1}{4} G^{A}_{\mu\nu} G^{A\mu\nu} + \sum_{\psi} \bar{\psi} i \not{D} \psi - \sum_{\psi} \left[\bar{\psi}_{\mathsf{R}} \mathsf{M}_{\psi} \psi_{\mathsf{L}} + \mathsf{h.c.} \right] \\ &+ \theta_{\mathsf{QED}} \frac{e^2}{32\pi^2} F_{\mu\nu} \tilde{F}^{\mu\nu} + \theta_{\mathsf{QCD}} \frac{g_s^2}{32\pi^2} G_{\mu\nu} \tilde{G}^{A\mu\nu} \end{split}$$

c employed extensively in **flavor physics**. at even lower energies $\leq \Lambda_{QCD}$: chiral perturbation theory

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LEFT operators



bases available up to d = 9 Liao, Manohar, Stoffer 1709.04486, Aebischer, Fael, Greub, Virto 1704.06639 Liao, Ma, Wang 2005.08013, Murphy 2012.13291, Li, Ren, Xiao, Yu, Zheng 2012.09188

matching to SMEFT and RG running \leadsto Ben

Aebischer, Crivellin, Fael, Greub 1512.02830, Jenkins, Manohar, Stoffer 1709.04486, 1711.05270

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The bigger picture – a blooming research field!



SMEFT @LHC: two main challenges

1. being sensitive to indirect BSM effects \rightarrow needs uncertainty reduction

in bulk
$$\sim \frac{v^2}{\Lambda^2} = \frac{v^2 g_{UV}}{M^2}$$
. $g_{UV} \simeq 1, \quad M \simeq 2 \text{ TeV} \rightarrow 1.5\%$
on tails $\sim \frac{E^2}{\Lambda^2} \simeq \frac{E^2 g_{UV}}{M^2}$ $E \simeq 1 \text{ TeV}, \quad M \simeq 3 \text{ TeV} \rightarrow 10\%$

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2. making sure that, if we observe a deviation, we interpret it correctly

- minimizing bias by retaining all relevant contributions
- correct understanding of uncertainties and correlations
- systematic mapping to BSM models
 tree-level dictionary: de Blas et al 1711.10391
 1-loop dictionary: Guedes et al 2303.16965

Example: SMEFT in Higgs physics



Marginalized fit results

ATLAS 2402.05742

all Warsaw basis considered, only 19 combinations meaningfully constrained

selected with Principal Component Analysis:

diagonalize Fisher information matrix

$$\mathcal{I}_{ij} = -rac{\partial^2 \log \mathcal{L}}{\partial C_i \partial C_j}$$



Marginalized fit results





 \sqrt{s} =13 TeV, 139 fb⁻¹ m = 125.09 GeV

ATLAS

SMEFT $\Lambda = 1$ TeV



Correlations

ATLAS 2402.05742



ATLAS 2402.05742





Open challenges and active lines of development

Q improve **predictions** to higher perturbative orders

improve **matching and running** to higher perturbative and EFT orders

flavor measurements with **flavor** measurements with **flavor** measurements

improve statistical analyses with likelihoods, optimal observables...

explore interplay of SMEFT constraints with direct searches

truncation uncertainties and impact of dim-8

☑ move (partially) to HEFT ?

Origin of SMEFT truncation uncertainties / EFT validity concern

- Λ is unknown
- LHC measurements often reach into high energies $(m, p_T, m_T \dots)$
- often measurement precision is not sufficient to guarantee that deviations from SM are small

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is $(E, v) \ll \Lambda$ a valid assumption?

are $d \ge 8$ terms always negligible?

can there be UV scenarios for which SMEFT does not describe the low-E limit?

Poor SMEFT convergence

EFT obtained from matching to full model



Poor SMEFT convergence



♥ top-down: truncated EFT does not reproduce full model at high-E

 $\mathbf{\nabla}$ **bottom-up**: fit to data finds wrong values of C_i

$$\rightarrow$$
 several studies of $d = 8$ impact

Exploring the impact of dim-8 terms

- hard to establish true relevance when left free (eg in a fit)
- checking impact when matched to specific models helps accounting for natural size



The Higgs Effective Field Theory – HEFT

rather than H doublet: singlet h + Goldstones **U** Feruglio 9301281, Grinstein,Trott 0704.1505, Buchalla,Catà 1203.6510, Alonso et al 1212.3305, IB et al 1311.1823,1604.06801, Buchalla et al 1307.5017,1511.00988...

$$H \mapsto rac{v+h}{\sqrt{2}} \mathbf{U} \begin{pmatrix} 0\\ 1 \end{pmatrix}, \qquad \mathbf{U} = \exp\left(rac{iec{\sigma} \cdot ec{\pi}}{v}
ight)$$

SMEFT expands around EW-symmetric point, HEFT expands around EW vacuum

Alonso, Jenkins, Manohar 1511.00724, 1605.03602



• more complicated power counting, mix of χ PT and canonical dimensions

Gavela, Jenkins, Manohar, Merlo 1601.07551 Buchalla, Catà, (Celis), Krause 1312.5624, 1603.03062

orders are defined as $\mathscr{L}_{HEFT} = \mathscr{L}_0 + \frac{\mathscr{L}_1}{\mathscr{L}_1} + \mathscr{L}_2 + \dots$

 \mathscr{L}_1 = leading deviations from SM = "4 derivatives" = NLO

- order-by-order, more operators than SMEFT: for 3 flavors, L, B conserving: L: 6573, L: 10⁶ + Hilbert series counting is available Gráf, Henning, Lu, Melia, Murayama 2211.06725
 complete bases available up to L2 Buchalla, Catà, Krause 1307.5017, IB et al 1604.06801 Sun, Xiao, Yu 2210.14939, Sun, Wang, Yu 2211.11598
- ▶ looking at the bosonic sector, \mathscr{L}_1 contains 39 operators \rightarrow better than dim-8!

15 in dim-6 Warsaw basis < **39** < 89 in dim-8 Murphy basis

Main HEFT features

- ▶ more general than SMEFT, because implements weaker symmetry requirement
 - \rightarrow \exists UV scenarios that can be matched to HEFT but <u>not</u> SMEFT Cohen et al 2008.0597, Banta et al 2110.02967

$\textbf{HEFT} \ \supset \ \textbf{SMEFT} \ \supset \ \textbf{SM}$

▶ in general more convergent than SMEFT: takes fewer orders to reproduce well UV model $\rightarrow \mathcal{F}(h)$ resums series in $(H^{\dagger}H)^n \sim \text{geoSMEFT: Helset, Martin, Trott 2001.01453}$

 \rightarrow classic example: composite Higgs for largish ξ



 \otimes spectacularly large deviations in Higgs couplings to V, f mostly excluded: bounds at $\sim 10\%$



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- Higgs self-couplings leave more freedom

 \rightsquigarrow Anisha



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- $\textcircled{\sc opt}$ some models that cannot match onto SMEFT (loryons) are still allowed, despite requiring $\Lambda \lesssim 3 \, {\rm TeV}$ for unitarity arguments



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- \otimes spectacularly large deviations in Higgs couplings to V, f mostly excluded: bounds at $\sim 10\%$
- Higgs self-couplings leave more freedom
- $\textcircled{\sc opt}$ some models that cannot match onto SMEFT (loryons) are still allowed, despite requiring $\Lambda \lesssim 3 \, {\rm TeV}$ for unitarity arguments
- in models that *can* match onto SMEFT, but for which SMEFT is **poorly convergent**, HEFT should be at least as relevant as dim-8 corrections
 - \rightarrow HEFT as an alternative to dim-8?

Wrapping up

- ▶ Effective Field Theories are a powerful theoretical concept, long used to investigate nature
- **SMEFT** has become a very popular tool for BSM searches
 - \rightarrow enable **model-independent** "agnostic" searches
 - \rightarrow allow joining information from LHC searches and measurements at other experiments
- the SMEFT program for LHC is blooming.
 → massive developments in several directions, theoretical, experimental, technical...
 → sensitivity already in the interesting region for many operator classes
- ► HEFT is an alternative formulation that has been recently resurfacing
 → particularly intersesting for multi-Higgs measurements
 → could help describe cases where SMEFT convergence is not so good

