



UNIVERSITÀ
DEGLI STUDI
DI PADOVA



Istituto Nazionale di Fisica Nucleare
Sezione di Padova

Neutrino Phenomenology from Flavour Deconstruction

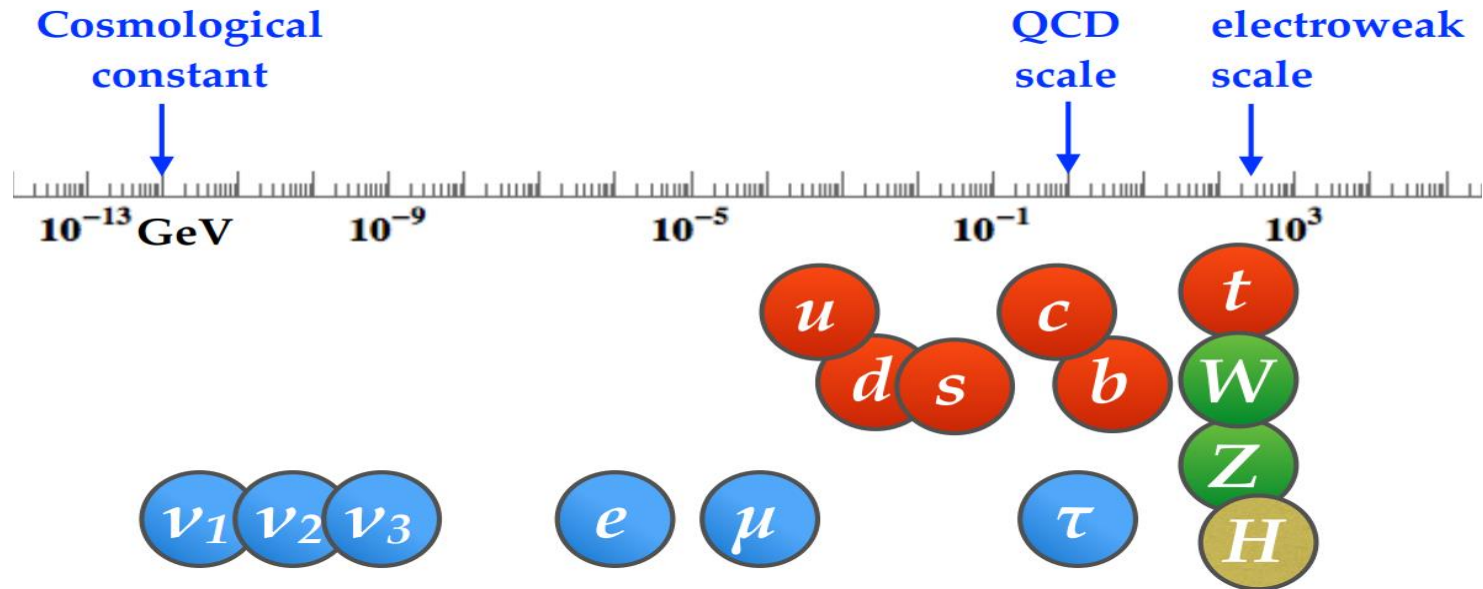
Andrea Sainaghi

In collaboration with Gino Isidori, Paride Paradisi and Nudžeim Selimović



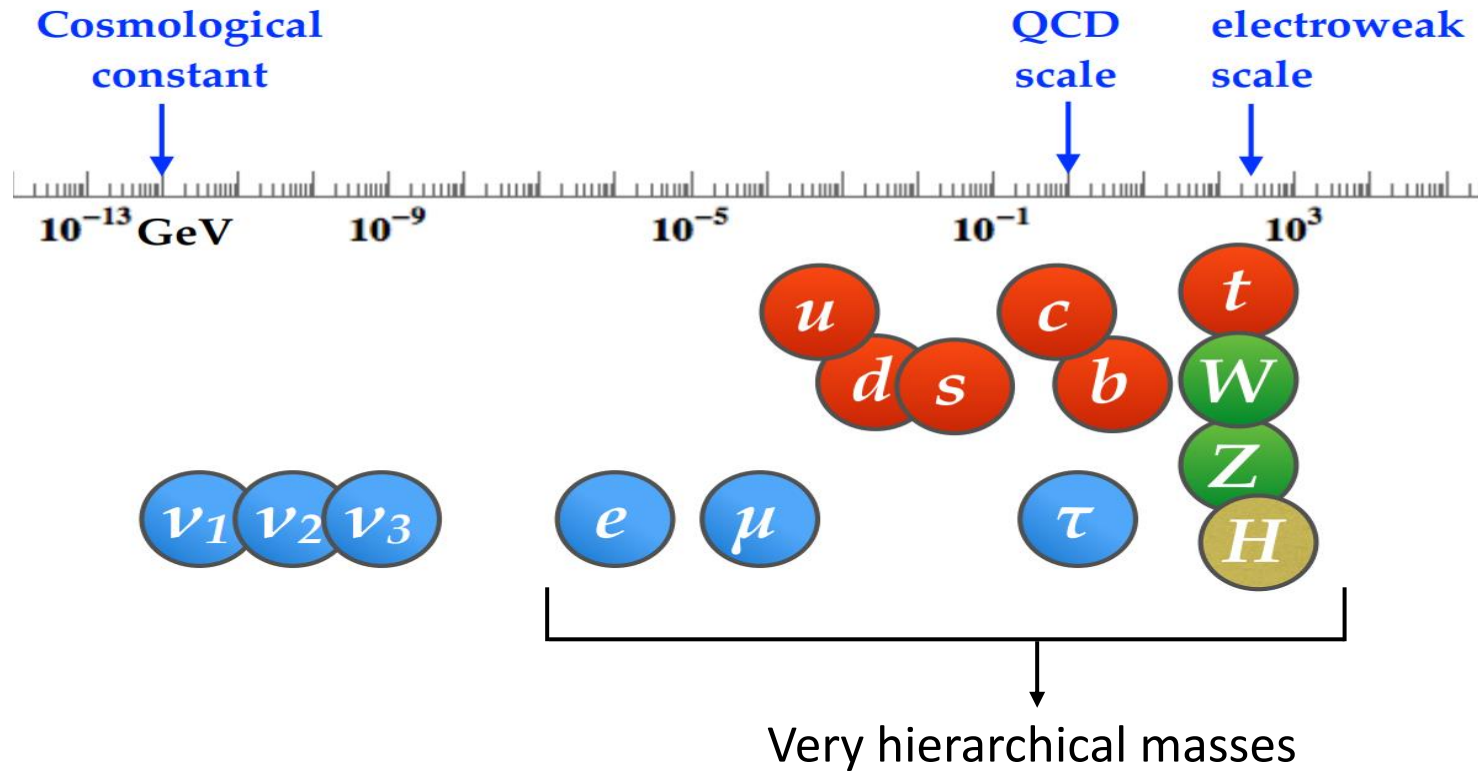
The Flavour Puzzle

Why are the SM-fermion masses so different?

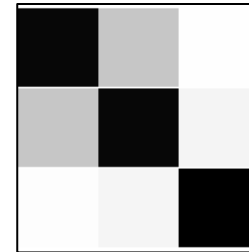


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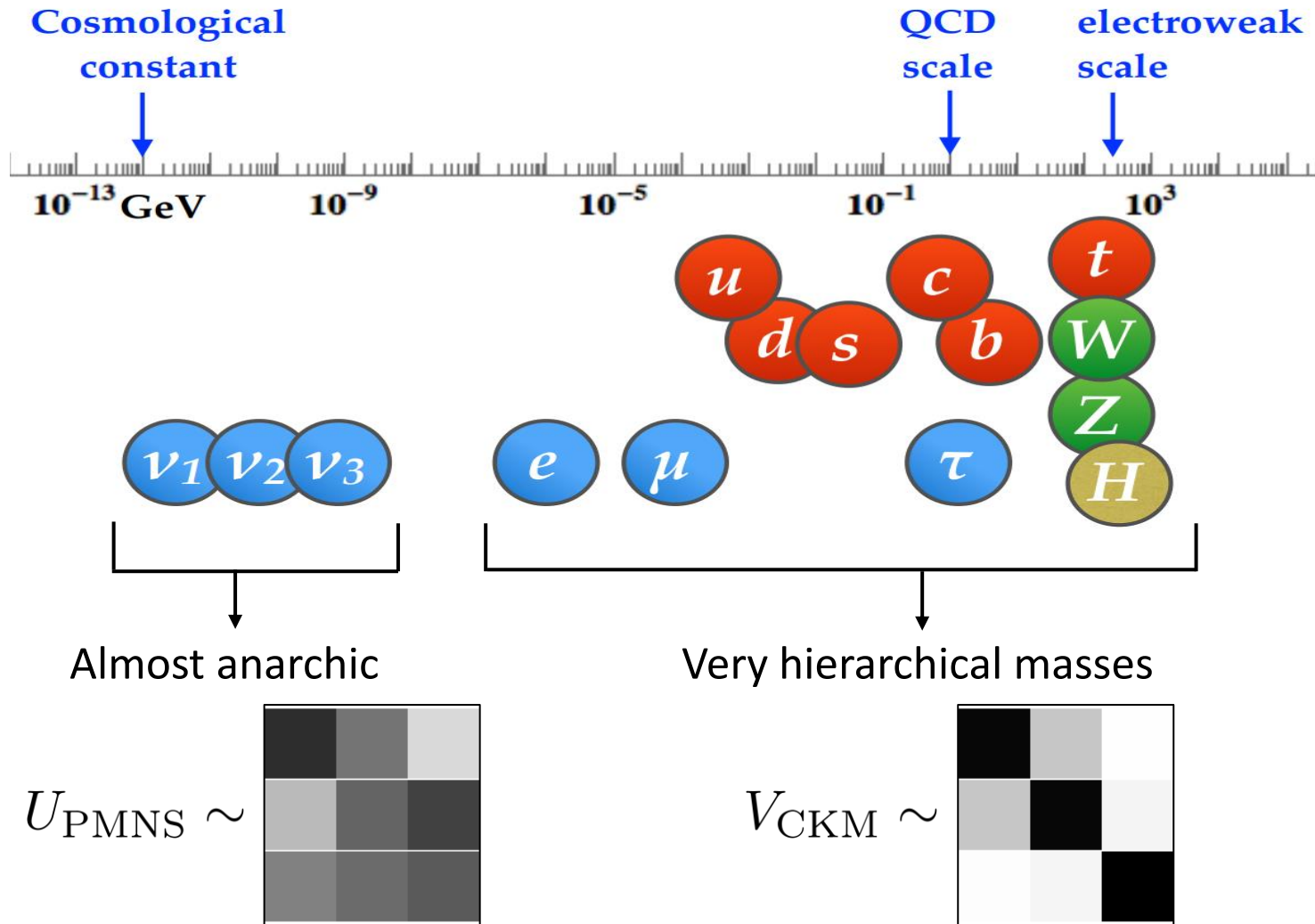


$$V_{\text{CKM}} \sim$$



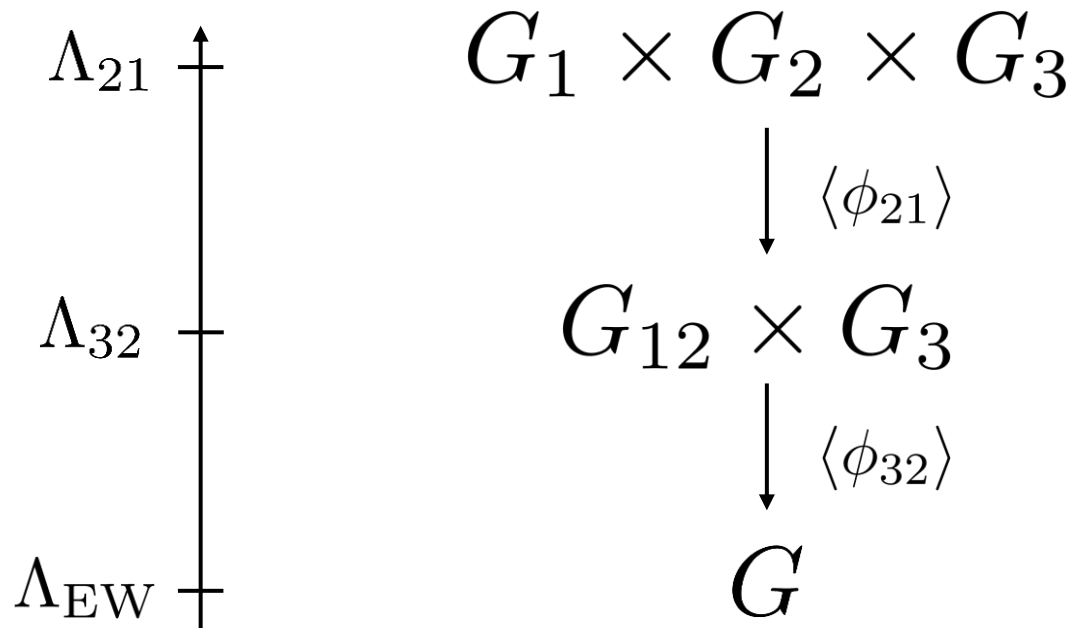
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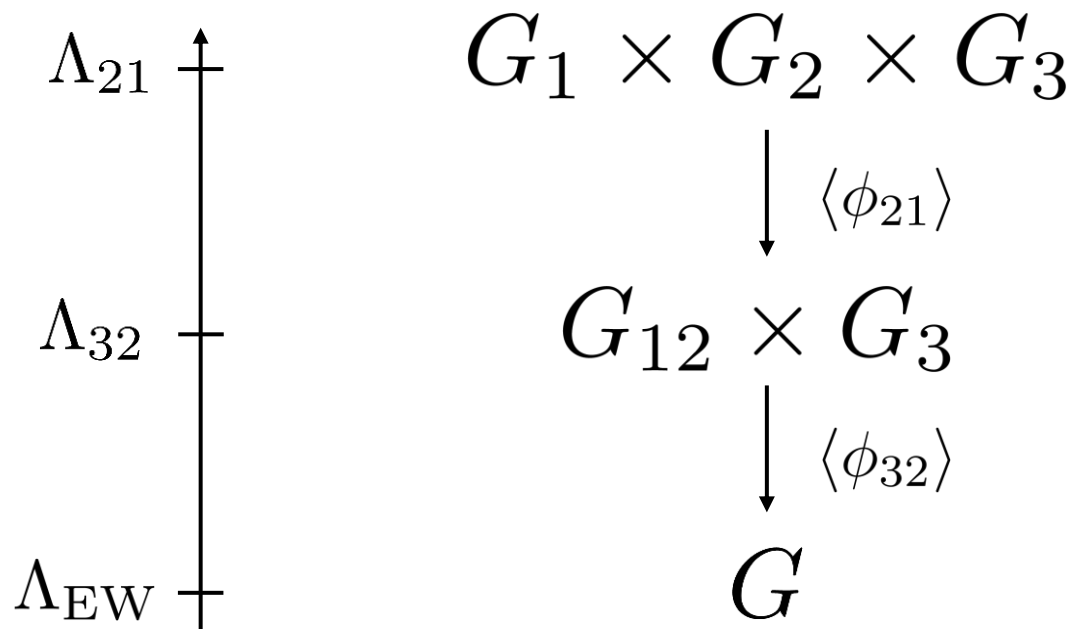
The Flavour Puzzle

Flavour deconstruction refers to a framework wherein the SM gauge group G is extended in the UV to G^3 , one for each fermion generation



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The hierarchies in the charged fermion masses are reproduced as long as

$$\langle \phi_{32} \rangle / \Lambda_{32} \ll 1 \quad \langle \phi_{21} \rangle / \Lambda_{21} \ll 1$$

However, it fails in explaining the anarchic neutrino sector

Theory Setup

Recently, [Greljo, Isidori, 2024] showed how to generate neutrino masses in a given flavour-deconstructed model using an Inverse Seesaw mechanism

$$-\mathcal{L} \supset \bar{\ell}_i Y_\nu^{ij} \tilde{H} \nu_j + \bar{s}_i M_R^{ij} \nu_j + \frac{1}{2} \bar{s}_i \mu^{ij} s_j^c + \text{h.c.}$$

Y_ν , M_R , μ are 3x3 matrices with $M_R \gg v Y_\nu \gg \mu$ $v \equiv \langle H \rangle$

$$Y_\nu \sim \begin{pmatrix} \varepsilon_1 \varepsilon_2 & & \\ & \varepsilon_1 & \\ & & 1 \end{pmatrix} \quad M_R \sim \Lambda \begin{pmatrix} \eta_1 \eta_2 & \eta_1 & 1 \\ \eta_1 \eta_2 & \eta_1 & 1 \\ \eta_1 \eta_2 & \eta_1 & 1 \end{pmatrix}$$

$\mu \longrightarrow$ Anarchic

$\Lambda \equiv \langle \chi \rangle$, where χ is a scalar which is charged under the flavour gauge sector G_3

The flavour non-universal gauge group ensures the hierarchies $\varepsilon_{2,1}, \eta_{2,1} \ll 1$

Mass Spectrum

Below the EW scale we have as mass eigenstates:

- 3 light active neutrinos with Majorana masses ν_L^i

$$m_\nu \approx A \mu A^T$$

- 3 heavy neutral leptons (HNLs) with hierarchical and (almost) Dirac masses n^i

$$M_n \approx \begin{pmatrix} 0 & M_R \\ M_R^T & \mu \end{pmatrix}$$

The anarchy in the active neutrino mass matrix is guaranteed since there is a (even partial) cancellation in the hierarchies as

$$A \equiv v Y_\nu M_R^{-1} \sim \frac{v}{\Lambda} \begin{pmatrix} \Delta_1 \Delta_2 & \Delta_1 \Delta_2 & \Delta_1 \Delta_2 \\ \Delta_1 & \Delta_1 & \Delta_1 \\ 1 & 1 & 1 \end{pmatrix} \quad \Delta_i \equiv \frac{\varepsilon_i}{\eta_i}$$

SM Interactions

The HNLs interact weakly with the SM

$$\mathcal{L} \supset \frac{g}{\sqrt{2}} \bar{e}_L W^- \textcolor{blue}{U} \nu_L + \frac{g}{\sqrt{2}} \bar{e}_L W^- \textcolor{violet}{V} n_L + \text{h.c.} + \mathcal{L}_Z$$

We exploit the following parameterization for the mixing matrices

$$\textcolor{blue}{U} = \mathcal{N} \left(1 - \frac{1}{2} \textcolor{green}{W} \textcolor{green}{W}^\dagger \right) \quad \textcolor{violet}{V} = \mathcal{N} \textcolor{green}{W} \quad \textcolor{green}{W} = \mathcal{U}^\dagger \hat{\textcolor{green}{A}} U_S^\dagger$$

Where \mathcal{N} is the PMNS matrix of the SM and \mathcal{U} , U_S are 3x3 unitary matrices while $\hat{\textcolor{green}{A}} = \frac{y_\nu v}{\Lambda} \text{diag}(\Delta_1 \Delta_2, \Delta_1, 1)$

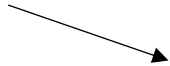
Parameters

There are 12 parameters relevant for the phenomenology:

Λ



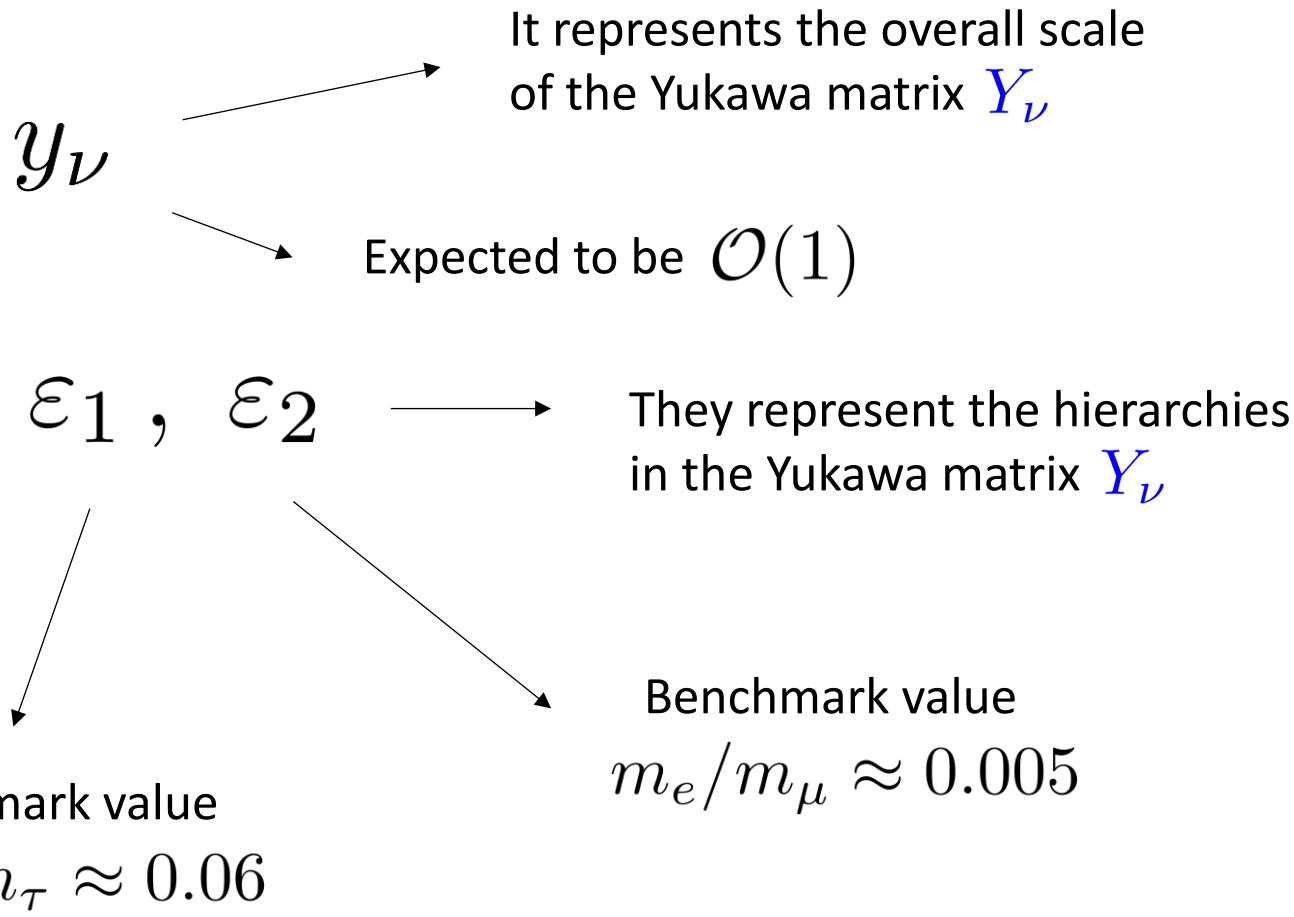
New-Physics (NP) scale



Hopefully around few TeV


Parameters

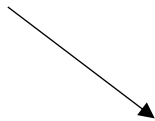
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Parameters

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$\alpha_1, \alpha_2, \alpha_3$  Three angles that parameterize the 3x3 unitary matrix \mathcal{U}



If the leptonic Yukawa matrices are diagonalized on the left by matrices close to the identity, then

$$\alpha_i \approx \theta_i \quad (\theta_i \text{ are the PMNS mixing angles})$$

$$\mathcal{L} \supset \frac{g}{\sqrt{2}} \bar{e}_L W^- U \nu_L + \frac{g}{\sqrt{2}} \bar{e}_L W^- V n_L + \text{h.c.} + \mathcal{L}_Z$$

$$U = \mathcal{N} \left(1 - \frac{1}{2} W W^\dagger \right) \quad V = \mathcal{N} W \quad W = \mathcal{U}^\dagger \hat{A} U_S^\dagger \quad \alpha_i \text{ here}$$

Parameters

There are 12 parameters relevant for the phenomenology:

$$\beta_1, \beta_2, \beta_3$$

Three angles that parameterize
the 3x3 unitary matrix U_S

In principle, they can range in
 $[0, 2\pi]$

They are related to the singlets of the Inverse
Seesaw only, so there is no way to constrain them

$$\mathcal{L} \supset \frac{g}{\sqrt{2}} \bar{e}_L W^- U \nu_L + \frac{g}{\sqrt{2}} \bar{e}_L W^- V n_L + \text{h.c.} + \mathcal{L}_Z$$

$$U = \mathcal{N} \left(1 - \frac{1}{2} W W^\dagger \right) \quad V = \mathcal{N} W \quad W = \mathcal{U}^\dagger \hat{A} U_S^\dagger$$

$\nearrow \beta_i \text{ here}$

Parameters

There are 12 parameters relevant for the phenomenology:

$$\Delta_1, \Delta_2$$

They effectively represent the hierarchies in the Heavy mass matrix M_R

$$\left[\text{Traded for } \eta_1, \eta_2 \rightarrow \Delta_i \equiv \frac{\varepsilon_i}{\eta_i} \right]$$

If they departure too much from 1, the model fails in reproducing the PMNS matrix as μ is assumed anarchic

Expected to be anarchic $\leftarrow \mu = W^{-1} \hat{m}_\nu (W^{-1})^T$

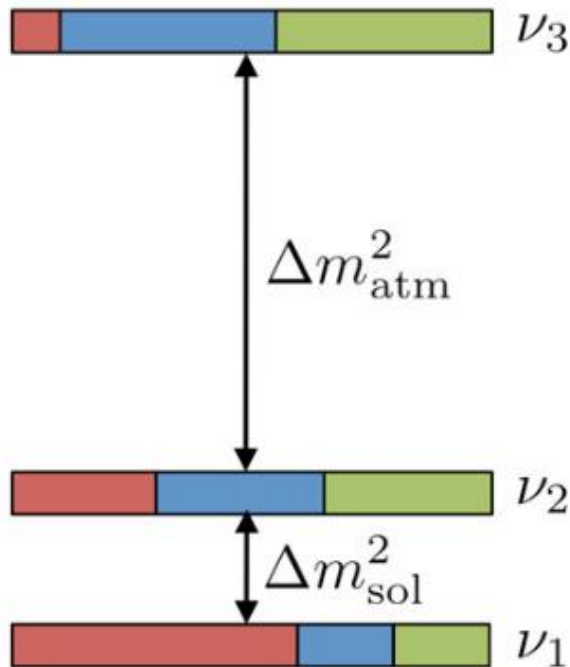
Δ_i here

Range?

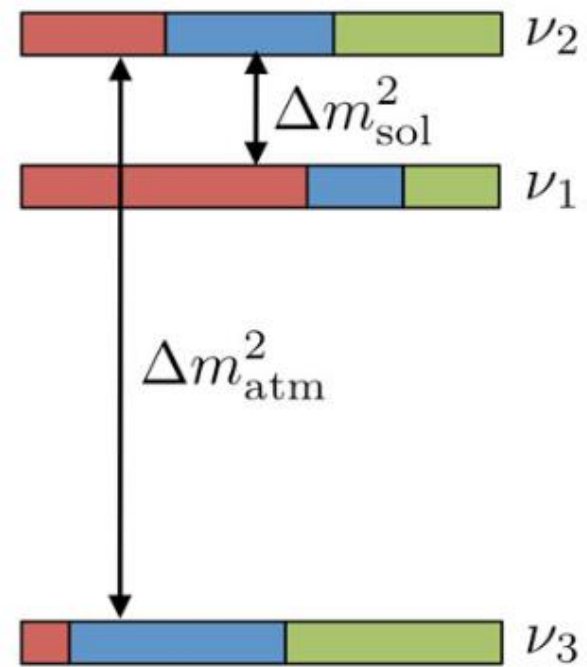
Neutrino Masses

The absolute scale of SM neutrino masses is still unknown

Normal Hierarchy (NH):



Inverted Hierarchy (IH):



$$\Delta m_{\text{atm}}^2 = 2.56 \cdot 10^{-3} \text{ eV}^2$$

$$\Delta m_{\text{sol}}^2 = 7.36 \cdot 10^{-5} \text{ eV}^2$$

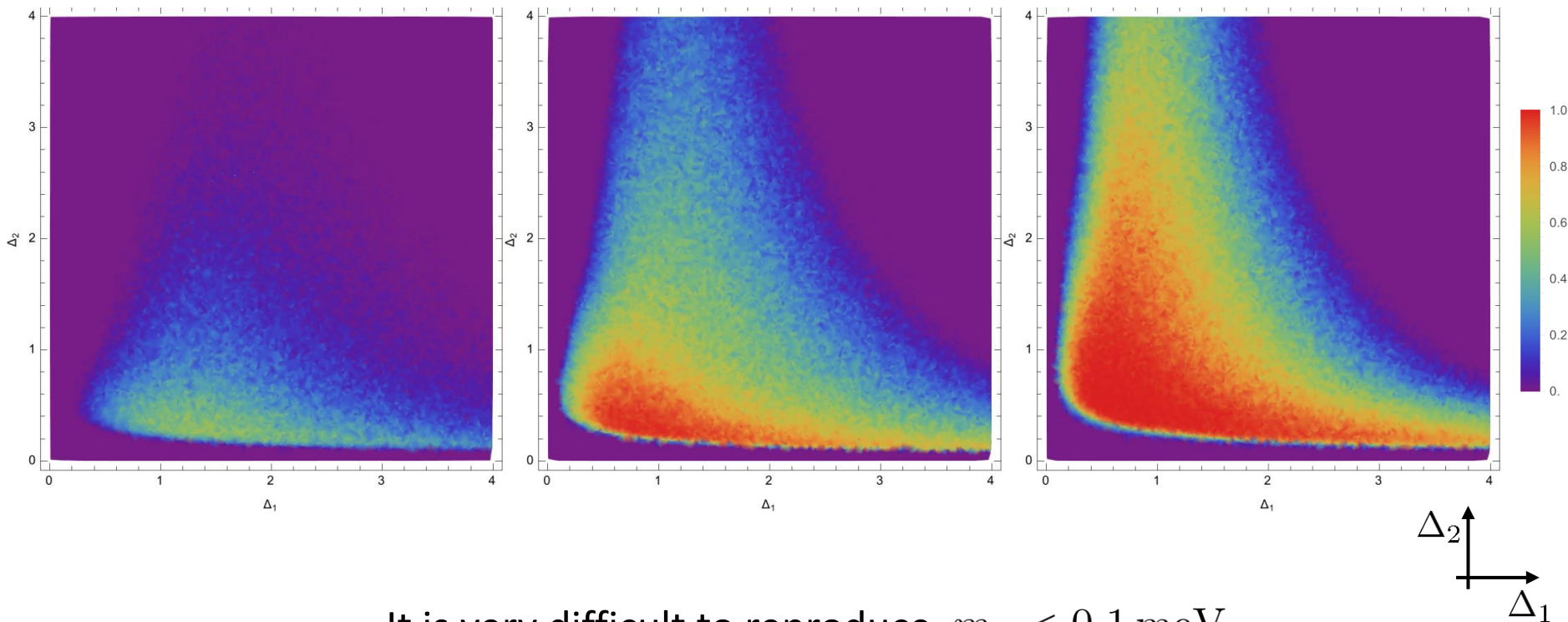
Range of Δ

Normal Hierarchy:

$0.1 < m_1 \text{ (meV)} < 1$

$1 < m_1 \text{ (meV)} < 10$

$10 < m_1 \text{ (meV)} < 50$



It is very difficult to reproduce $m_1 < 0.1$ meV

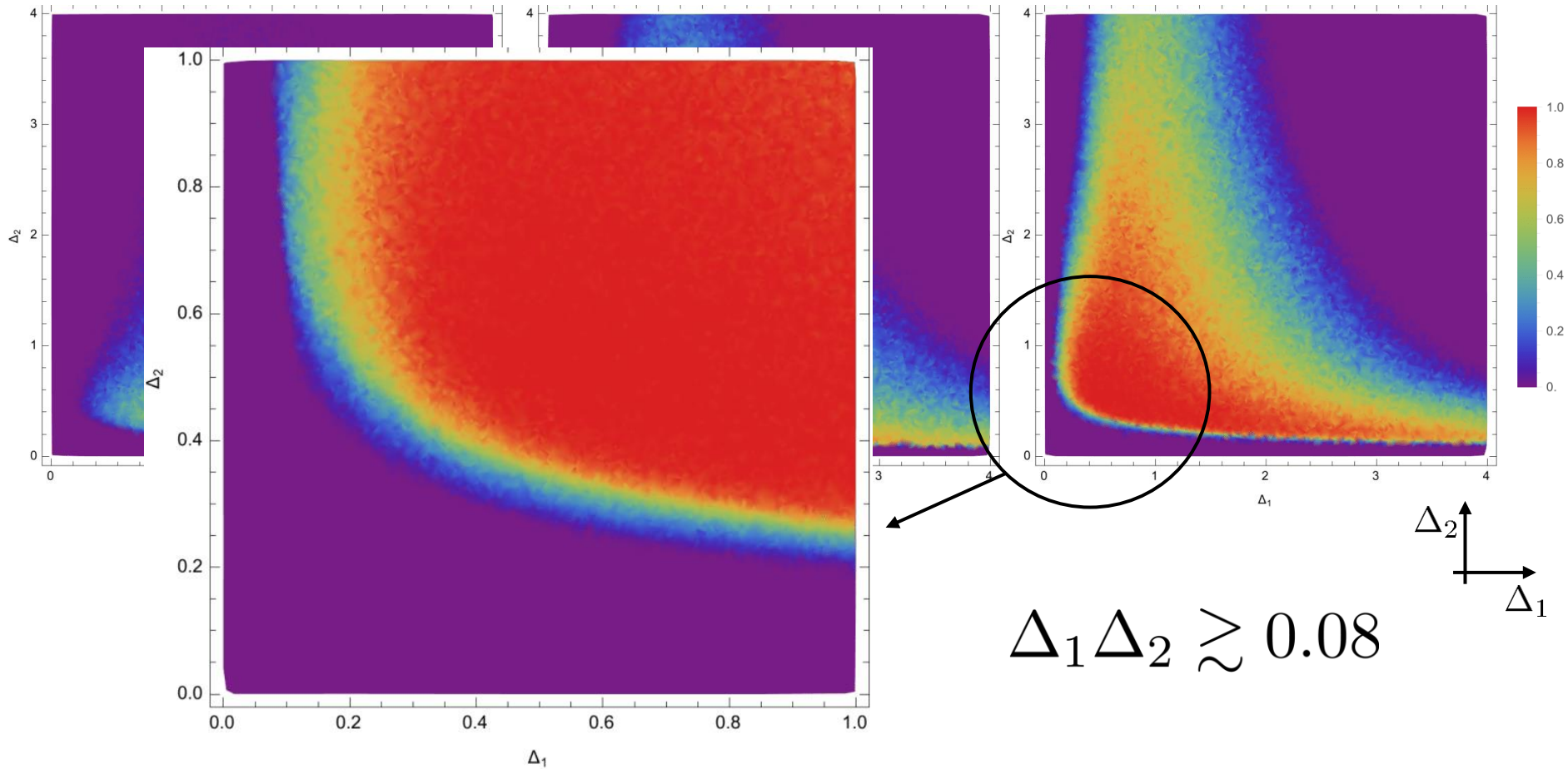
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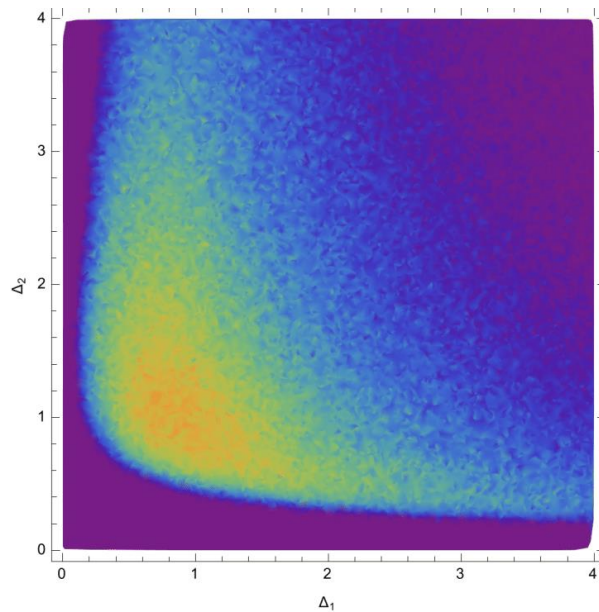
$$10 < m_1 \text{ (meV)} < 50$$



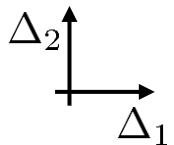
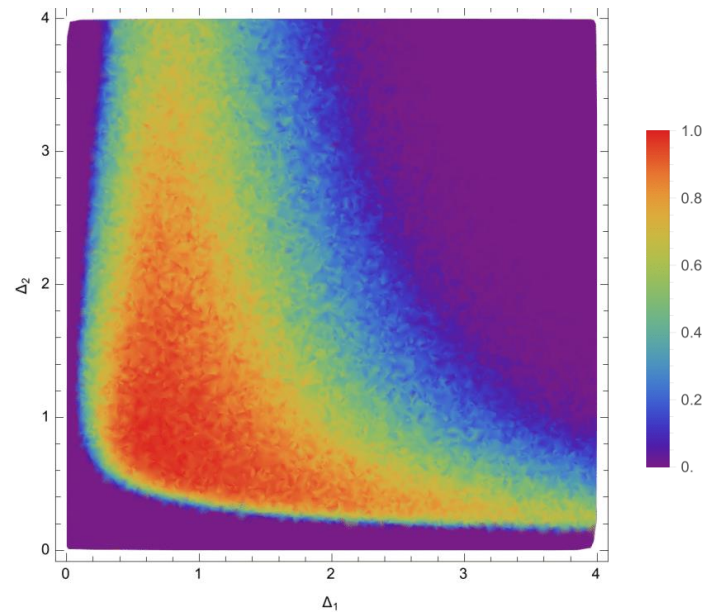
Range of Δ

Inverted Hierarchy:

$$1 < m_3 \text{ (meV)} < 10$$



$$10 < m_3 \text{ (meV)} < 50$$



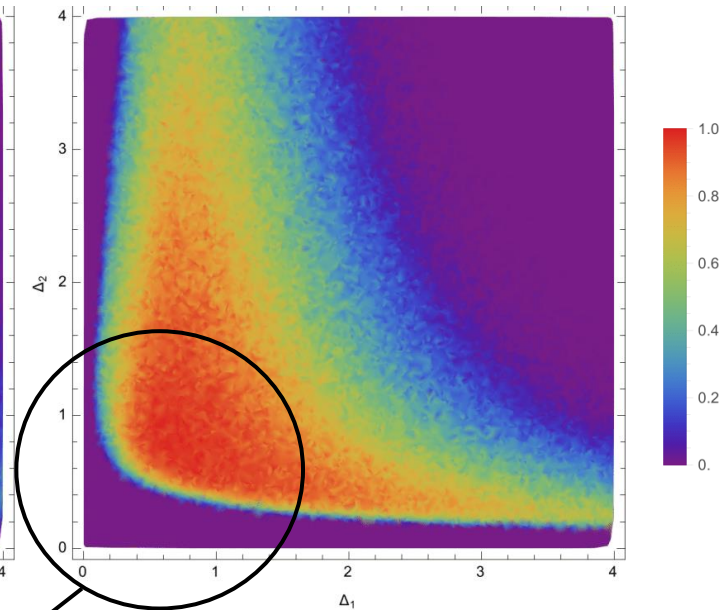
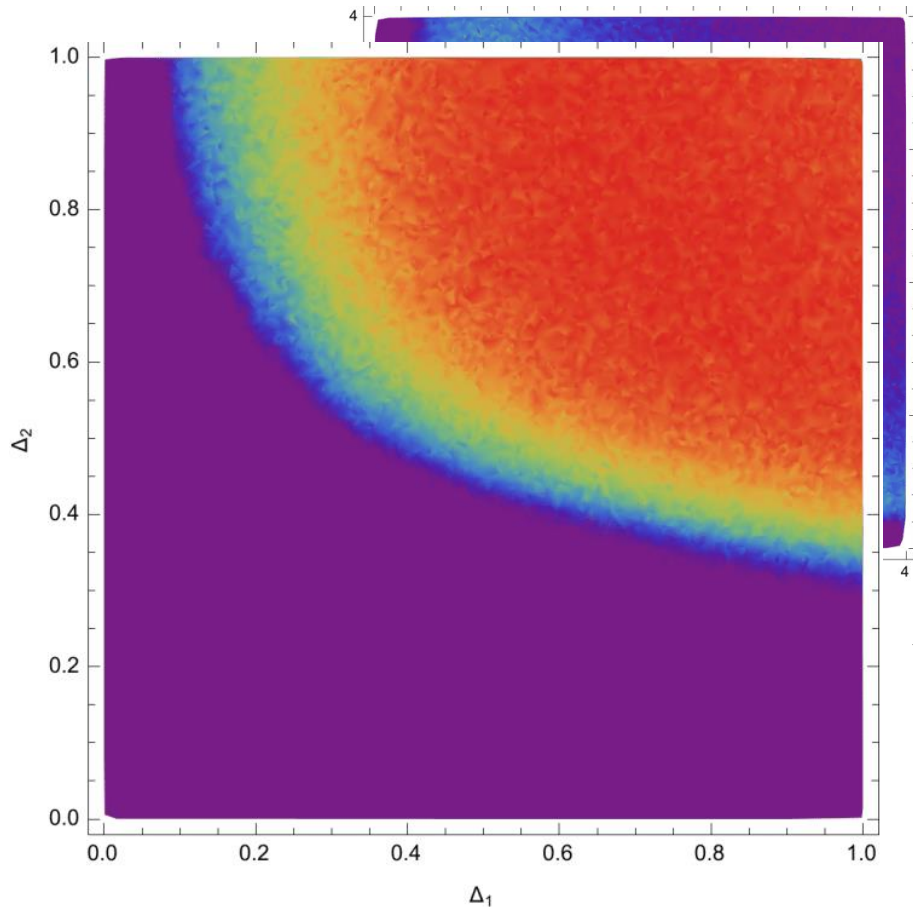
It is very difficult to reproduce $m_3 < 1$ meV

Range of Δ

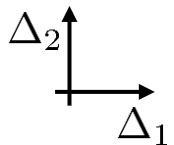
Inverted Hierarchy:

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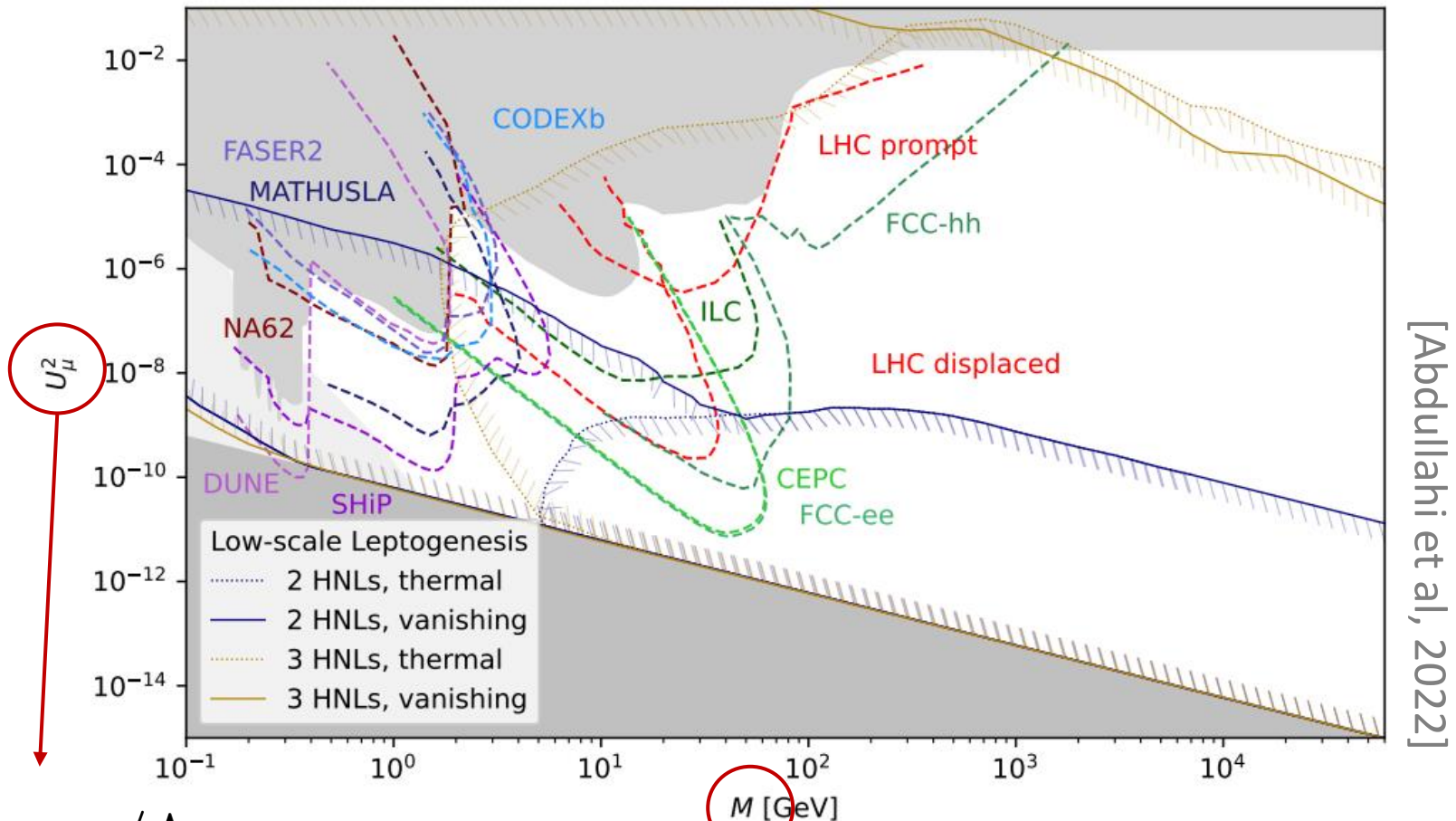


$$\Delta_1 \Delta_2 \gtrsim 0.15$$



Direct Searches

The HNLs have hierarchical masses and interact with the charged leptons



$$V_{\ell N} \sim v/\Lambda \quad M_1 = \Lambda \frac{\varepsilon_1}{\Delta_1} \frac{\varepsilon_2}{\Delta_2} \quad M_2 = \Lambda \frac{\varepsilon_1}{\Delta_1} \quad M_3 = \Lambda$$

Direct Searches

If the lightest HNL is lighter than Z and W bosons, it can be produced on-shell at colliders

$$M_1 < M_{W,Z}$$

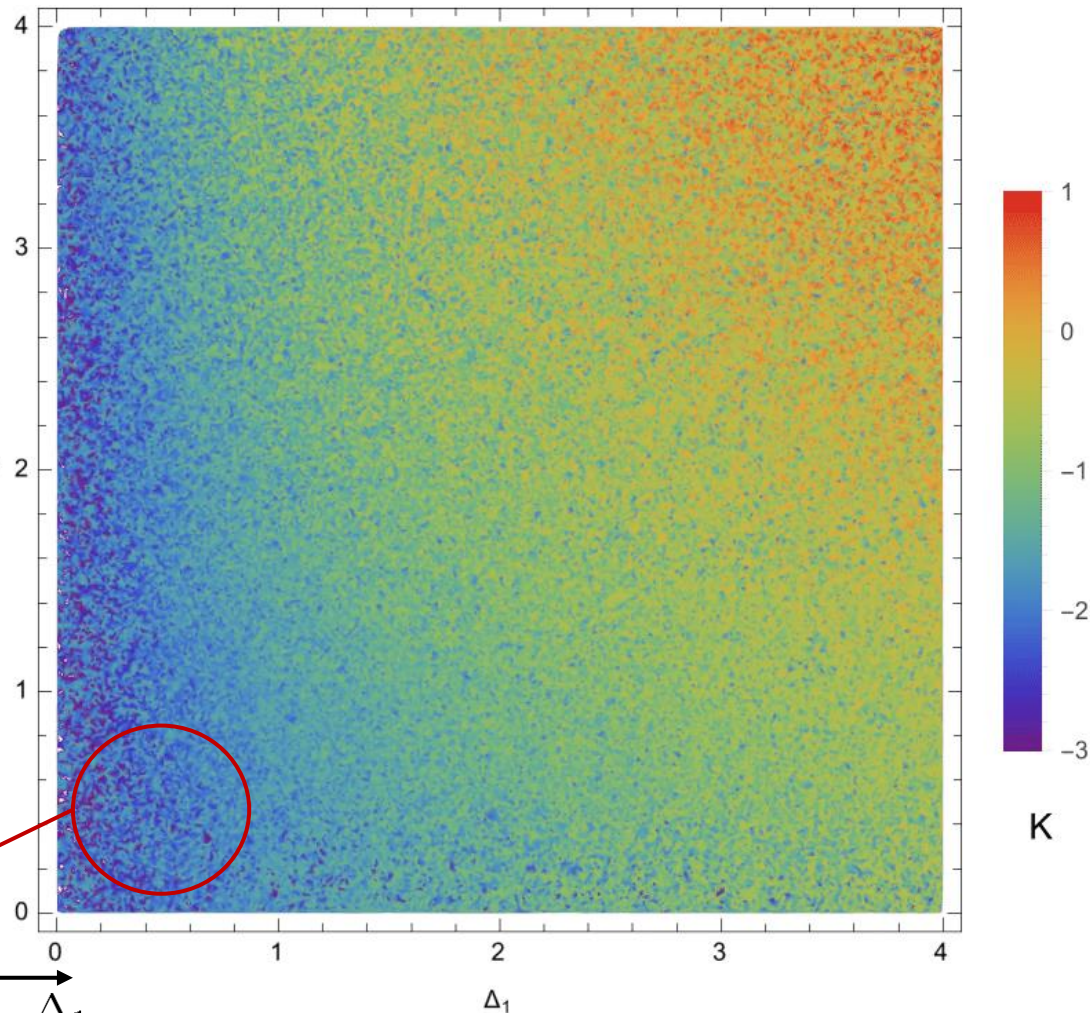
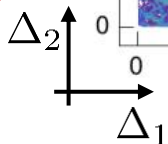


$$\Lambda \gtrsim y_\nu 10^{(K+5)/2} \text{ TeV}$$

From the current bound on

$$|V_{\ell N}|^2 < 10^{-5}$$

$$\Lambda \gtrsim 20 \text{ TeV}$$



Direct Searches

$$M_1 < M_{W,Z} \quad \longrightarrow \quad \Lambda \gtrsim 20 \text{ TeV}$$

Otherwise, by imposing $M_1 > M_{W,Z}$



$$\Lambda \gtrsim 40 \left(\frac{\Delta_1 \Delta_2}{0.13} \right) \left(\frac{m_\mu / m_\tau}{\varepsilon_1} \right) \left(\frac{m_e / m_\mu}{\varepsilon_2} \right) \text{ TeV}$$

Compatible with NP at TeV scale!

$$\Lambda \gtrsim \text{few TeV}$$

Recall that

$$\text{NH: } \Delta_1 \Delta_2 \gtrsim 0.08$$

$$\text{IH: } \Delta_1 \Delta_2 \gtrsim 0.15$$

LFV Processes

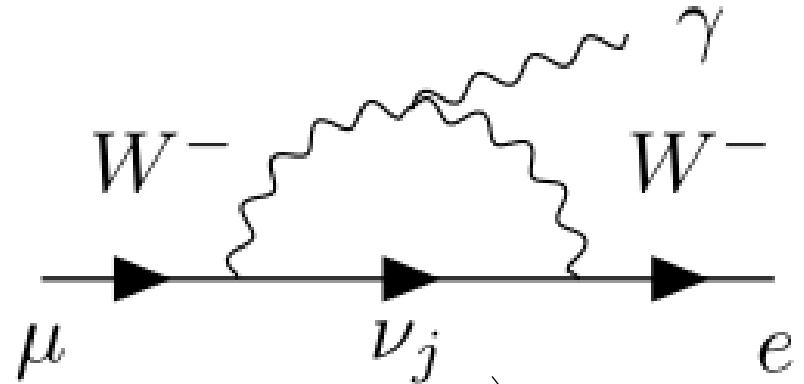
Currently, $\mu \rightarrow e\gamma$ is the most constraining LFV process

$$\text{Br}(\mu \rightarrow e\gamma) = \frac{3\alpha}{2\pi} |\delta_\nu|^2$$

$$\delta_\nu = \sum_k V_{ek} V_{\mu k}^* G_\gamma \left(\frac{M_k^2}{M_W^2} \right)$$

$$\approx \frac{v^2}{\Lambda^2} \Delta_1^2 \Delta_2 \sum_k (U_S)_{ek} (U_S^*)_{\mu k} G_\gamma \left(\frac{M_k^2}{M_W^2} \right)$$

β_i inside here



Both light and heavy states

LFV Processes

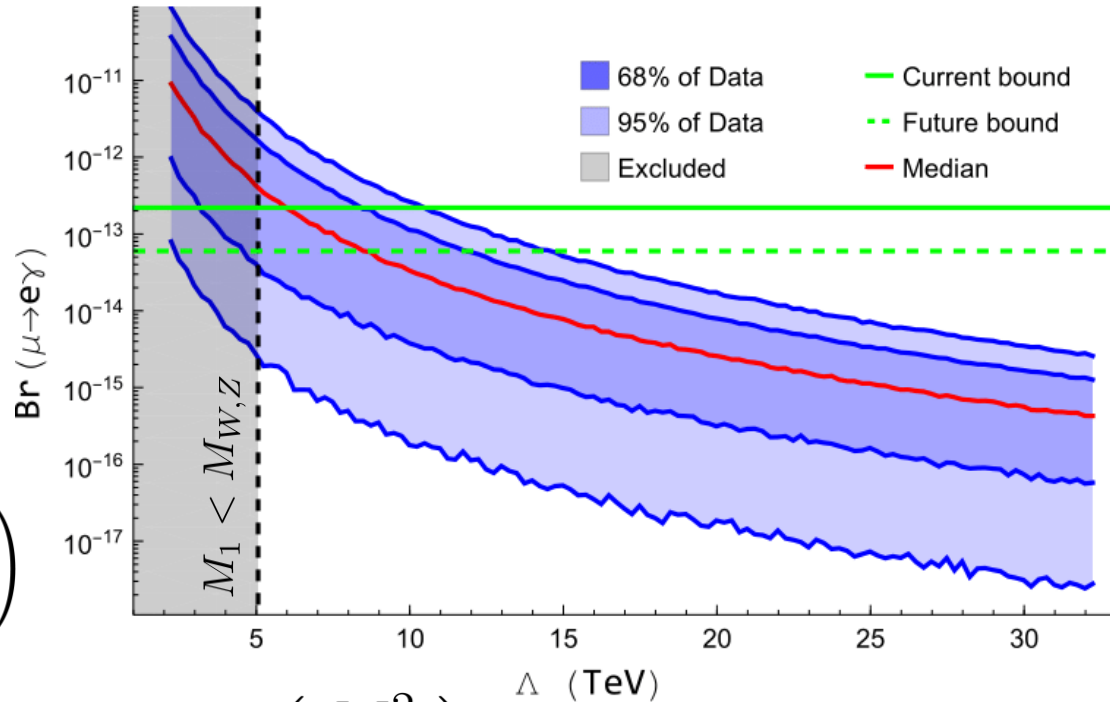
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$$\approx \frac{v^2}{\Lambda^2} \underbrace{\Delta_1^2 \Delta_2}_{\text{Normal Hierarchy}} \sum_k \underbrace{(U_S)_{ek} (U_S^*)_{\mu k}}_{\beta_i \text{ inside here}} G_\gamma \left(\frac{M_k^2}{M_W^2} \right)$$

Normal Hierarchy allows for Λ to be around few TeV



Plot of $\text{Br}(\mu \rightarrow e\gamma)$ with

$$\Delta_1 = 0.45 \quad \Delta_2 = 0.3$$

$$\varepsilon_1 = 0.06 \quad \varepsilon_2 = 0.04$$

$$y_\nu = 1$$

LFV Processes

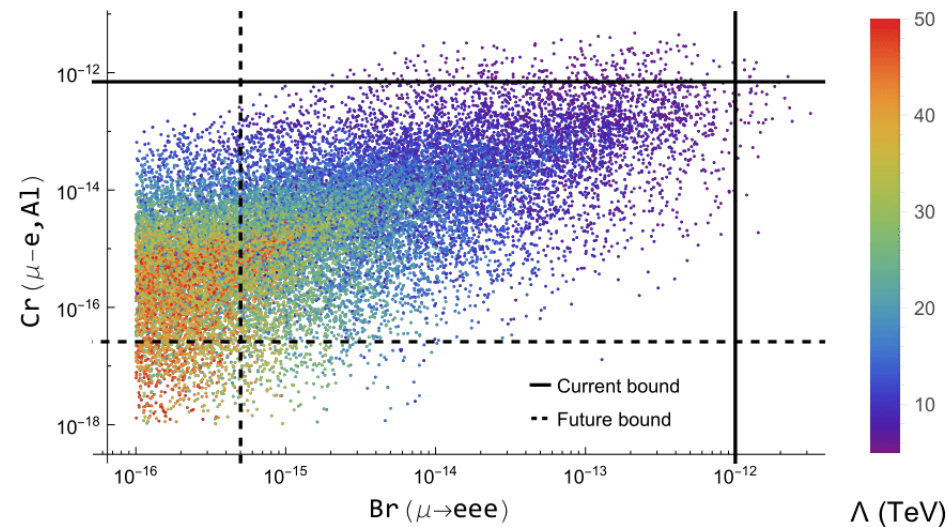
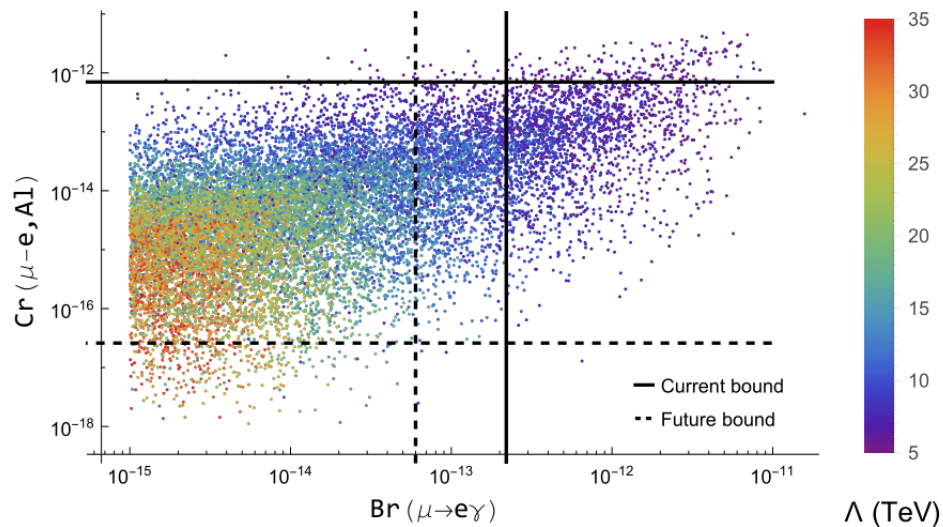
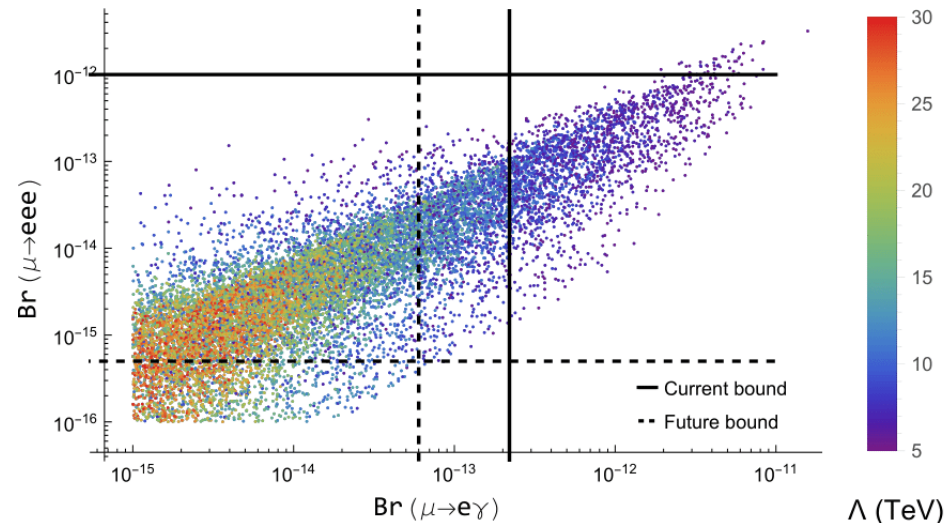
Correlation plots between
the main LFV processes

$$\text{Br}(\mu \rightarrow e\gamma) \quad \text{Br}(\mu \rightarrow eee)$$

$$\text{Cr}(\mu - e, \text{Al})$$

$$\Delta_1 = 0.5 \quad \Delta_2 = 0.5$$

$$\varepsilon_1 = 0.06 \quad \varepsilon_2 = 0.02 \quad y_\nu = 1$$



LFV Processes

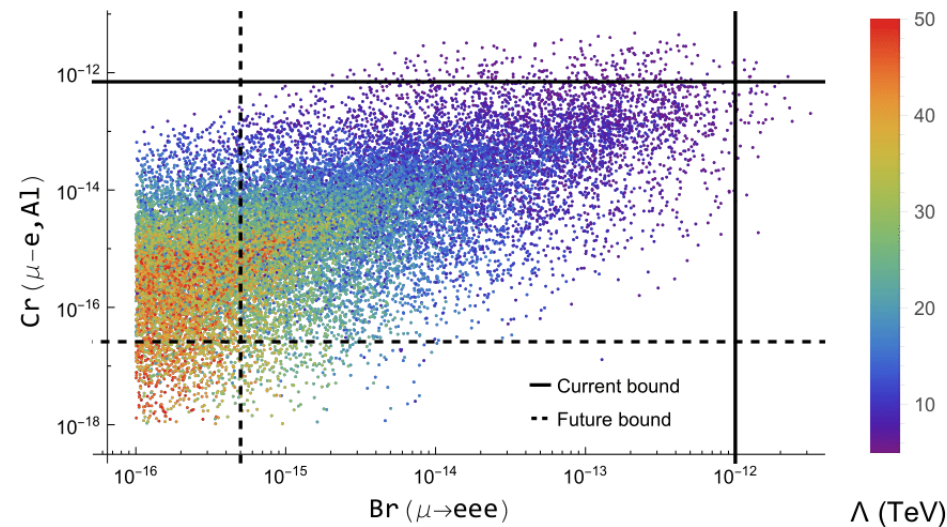
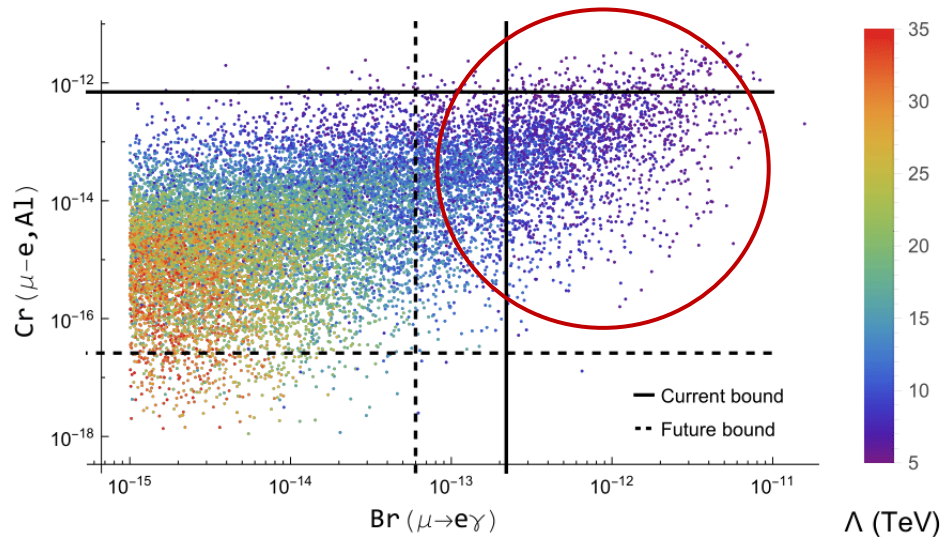
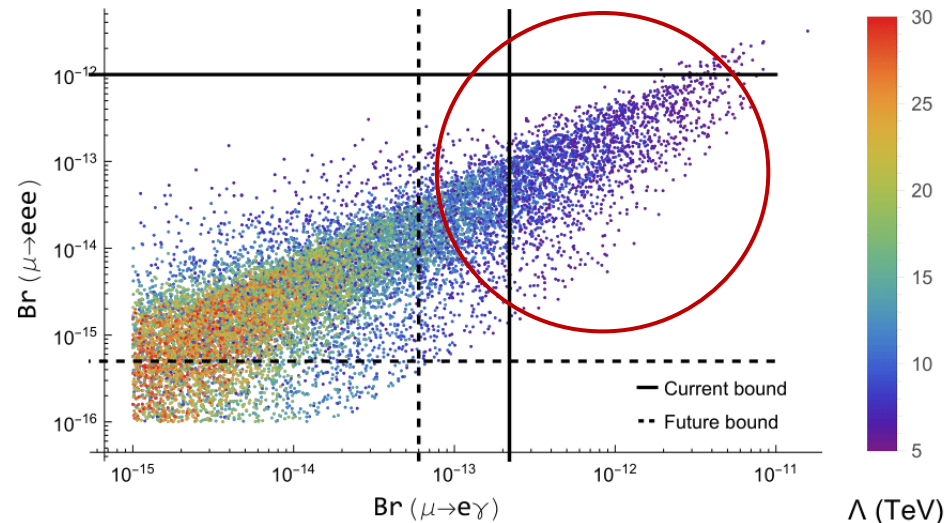
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LFV Processes

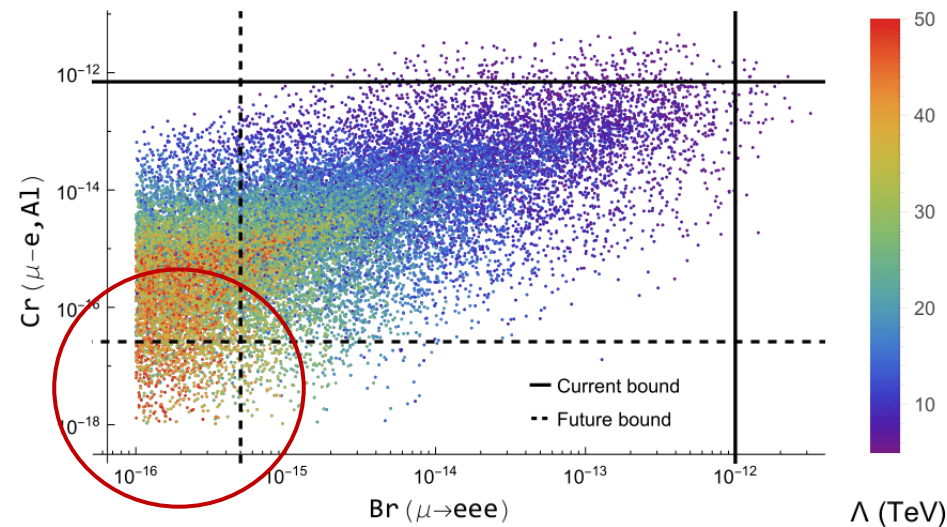
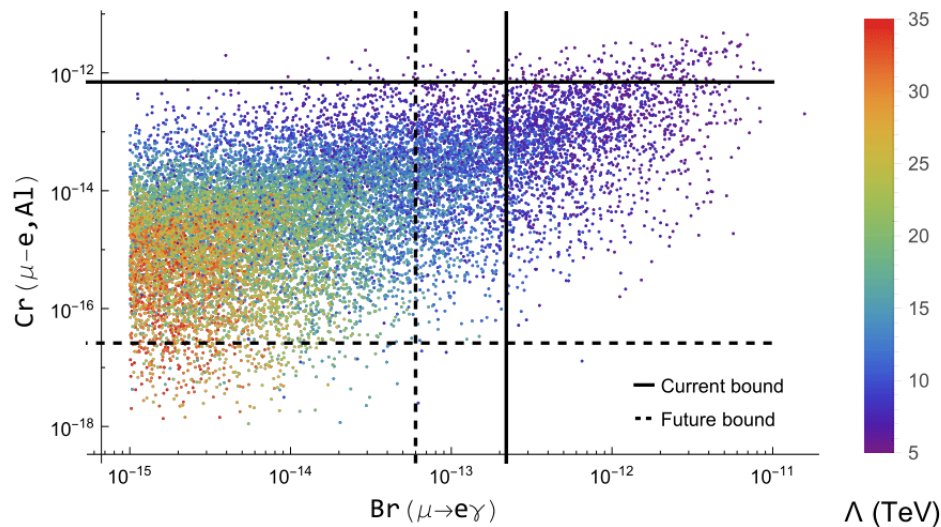
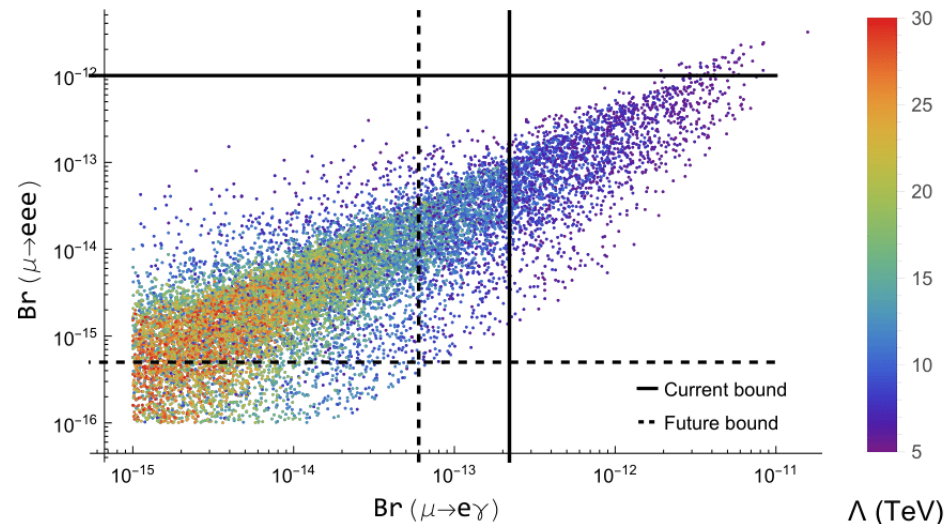
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$$\Delta_1 = 0.5 \quad \Delta_2 = 0.5$$

$$\varepsilon_1 = 0.06 \quad \varepsilon_2 = 0.02 \quad y_\nu = 1$$



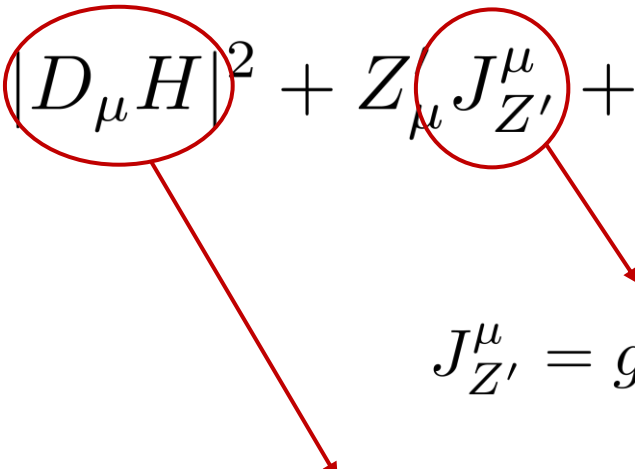
LFV from Gauge and Yukawa Sectors

Flavour-deconstructed models predict LFV processes even without including neutrinos

$$\mathcal{L} \supset |D_\mu H|^2 + Z'_\mu J^\mu_{Z'} + \frac{1}{2} M_{Z'}^2 Z'_\mu Z'^\mu + \mathcal{L}_Y$$

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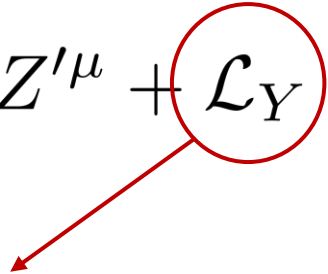
$$J_{Z'}^\mu = g_{\text{NP}} \sum_{\psi} \bar{\psi} \gamma^\mu \psi Q_{Z'}(\psi)$$


$$D_\mu H \supset \partial_\mu H - \frac{ig}{c_W} (T_3 - s_W^2 Q) Z_\mu H - ig_{\text{NP}} Q_{Z'}(H) Z'_\mu H$$

Z' \longrightarrow It is a neutral heavy gauge boson that couples non-universally with all the fermions in the theory

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$$\mathcal{L}_Y \sim y_{33} \bar{\ell}_3 H e_3 + \sum_{j=1,2} \sum_{\alpha=\text{heavy}} Y_{j\alpha} \bar{\ell}_j H E_\alpha$$
$$+ \left[\sum_{\alpha=\text{heavy}} Y'_{\alpha i} \bar{E}_\alpha \phi_{32} e_2 + \sum_{\alpha=\text{heavy}} M_\alpha \bar{E}_\alpha E_\alpha + 1^{\text{st}} \text{ generation} \right]$$


$E_\alpha \longrightarrow$ Heavy NP fermions

$$\Lambda_{32} \sim M_\alpha$$

LFV from Gauge and Yukawa Sectors

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$$+ \left[\sum_{\alpha=\text{heavy}} Y'_{\alpha i} \bar{E}_\alpha \phi_{32} e_2 + \sum_{\alpha=\text{heavy}} M_\alpha \bar{E}_\alpha E_\alpha + 1^{\text{st}} \text{ generation} \right]$$

It generates a mass-mixing matrix between light and heavy fermions

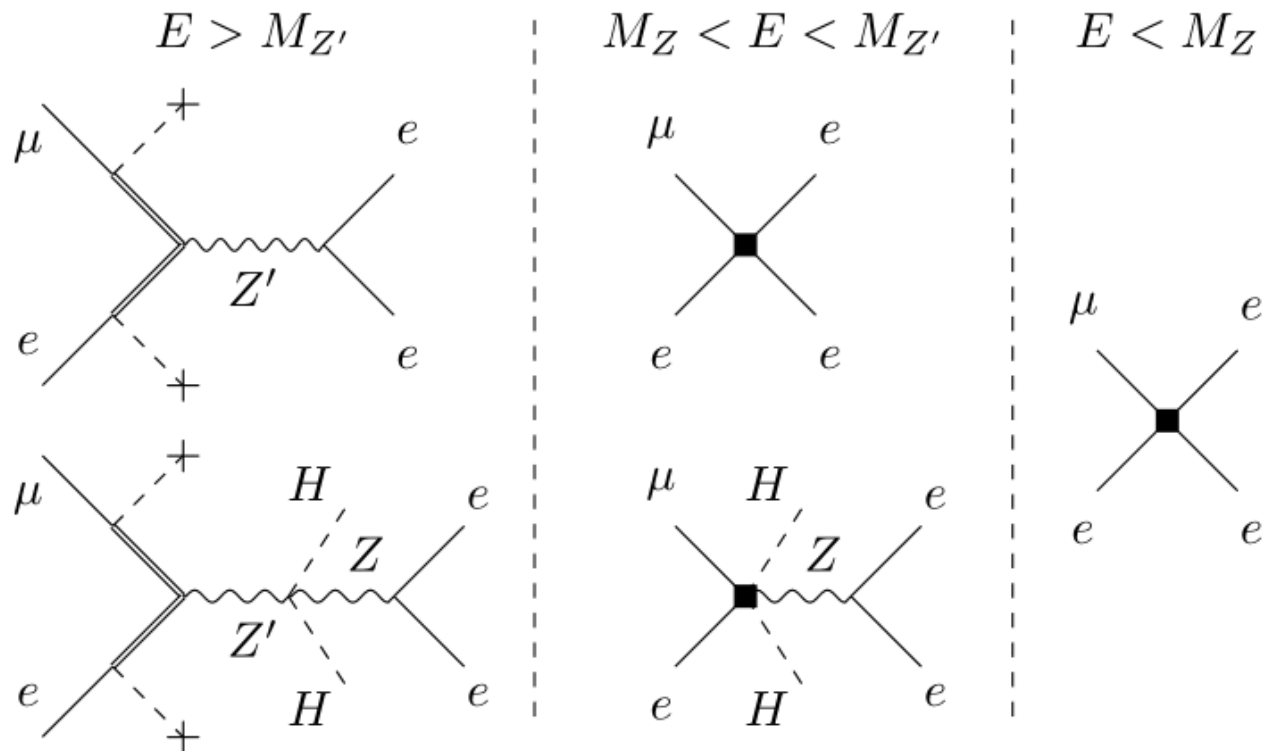
$$U_{\text{mix}} = \begin{pmatrix} \mathbb{I} - \frac{1}{2} \mathcal{E}^\dagger \mathcal{E} & \mathcal{E}^\dagger \\ -\mathcal{E} & \mathbb{I} - \frac{1}{2} \mathcal{E} \mathcal{E}^\dagger \end{pmatrix}$$

$$\mathcal{E} \sim \langle \phi_{32} \rangle / \Lambda_{32}$$

LFV from Gauge and Yukawa Sectors

Flavour-deconstructed models predict LFV processes even without including neutrinos

$$\mathcal{L} \supset |D_\mu H|^2 + Z'_\mu J^\mu_{Z'} + \frac{1}{2} M_{Z'}^2 Z'_\mu Z'^\mu + \mathcal{L}_Y$$



LFV from Gauge and Yukawa Sectors

Flavour-deconstructed models predict LFV processes even without including neutrinos

$$\mathcal{L} \supset |D_\mu H|^2 + Z'_\mu J^\mu_{Z'} + \frac{1}{2} M_{Z'}^2 Z'_\mu Z'^\mu + \mathcal{L}_Y$$

$$\frac{\text{Br}(\mu \rightarrow eee)|_{Z'}}{\text{Br}(\mu \rightarrow eee)|_\nu} \approx (10^{-1} \div 10) \times \left(\frac{1}{y_\nu}\right)^4 \left(\frac{0.5^3}{\Delta_1^2 \Delta_2}\right)^2 \left(\frac{\varepsilon_e \varepsilon_\mu}{0.05^2}\right)^2 \left(\frac{\alpha_{\text{NP}}}{\alpha}\right)^2 \left(\frac{\Lambda}{M_{Z'}}\right)^4$$

$$\frac{\text{Cr}(\mu - e, Al)|_{Z'}}{\text{Cr}(\mu - e, Al)|_\nu} \approx (10^{-1} \div 10) \times \left(\frac{1}{y_\nu}\right)^4 \left(\frac{0.5^3}{\Delta_1^2 \Delta_2}\right)^2 \left(\frac{\varepsilon_e \varepsilon_\mu}{0.05^2}\right)^2 \left(\frac{\alpha_{\text{NP}}}{\alpha}\right)^2 \left(\frac{\Lambda}{M_{Z'}}\right)^4$$

This range is only due to β_i

Mixing between third
and light generations

Neutrino sector could dominate for $\Lambda \lesssim M_{Z'}$

Explicit Model

This model-independent study can be easily matched to any given flavour-deconstructed model of interest

As example, we refer to Model B discussed in [Greljo, Isidori, 2024]

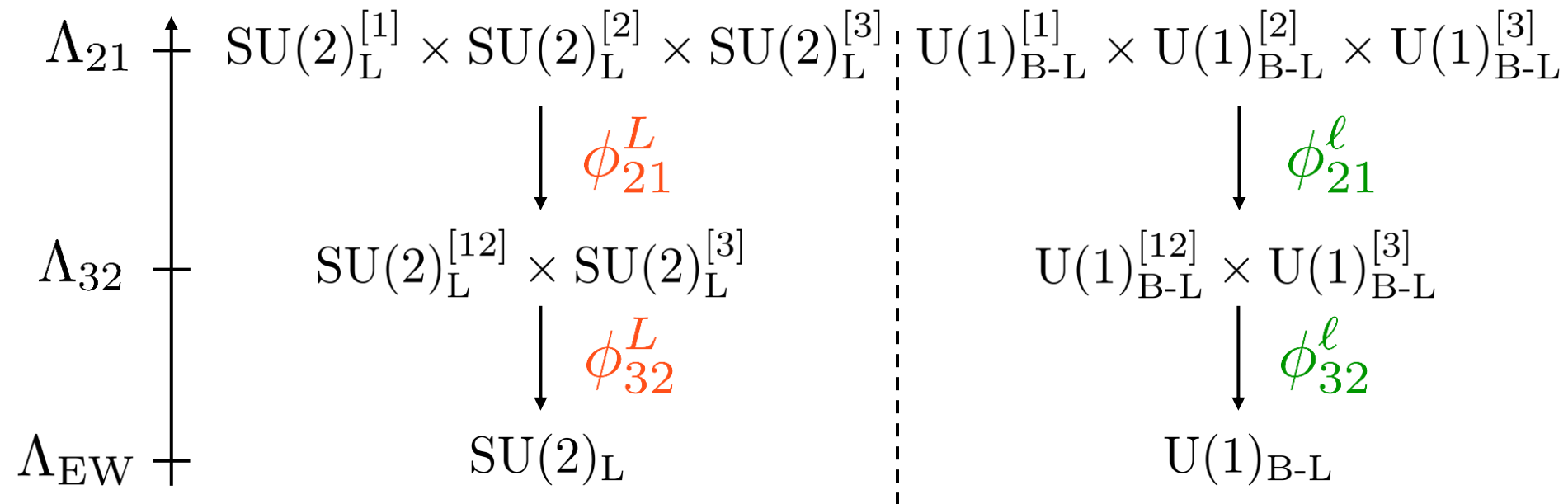
Explicit Model

This model-independent study can be easily matched to any given flavour-deconstructed model of interest

Gauge group: $SU(3)_C \times SU(2)_L^3 \times U(1)_R \times U(1)_{B-L}^3$

↙ Flavour-deconstructed ↘

To break the symmetry down to the SM gauge group we need some scalar fields



Explicit Model

This model-independent study can be easily matched to any given flavour-deconstructed model of interest

Gauge group: $SU(3)_C \times SU(2)_L^3 \times U(1)_R \times U(1)_{B-L}^3$

The Lagrangian contains all the possible EFT operators allowed by the full symmetry

$$\mathcal{L}_Y = y_{33} \bar{\ell}_3 \tilde{H} \nu_3 + \frac{c_{32}}{\Lambda_{32}} \bar{\ell}_3 \tilde{H} \phi_{32}^\ell \nu_2 + \frac{c_{23}}{\Lambda_{32}^2} \bar{\ell}_2 \tilde{H} \phi_{32}^L \phi_{32}^\ell \nu_3 + 1\text{-st generation} \quad \left. \vphantom{\mathcal{L}_Y} \right\} \rightarrow Y_\nu$$

$$\mathcal{L}_R = \tilde{c}_{i3} \bar{s}_i \chi \nu_3 + \frac{\tilde{c}_{i2}}{\Lambda_{32}} \bar{s}_i \chi \phi_{32}^\ell \nu_2 + 1\text{st generation} \quad \left. \vphantom{\mathcal{L}_R} \right\} \rightarrow M_R$$

\swarrow
 $\langle \chi \rangle \sim \Lambda$

Explicit Model

This model-independent study can be easily matched to any given flavour-deconstructed model of interest

$$\text{Gauge group: } \text{SU}(3)_C \times \text{SU}(2)_L^3 \times \text{U}(1)_R \times \text{U}(1)_{B-L}^3$$

The Lagrangian leads to the following hierarchical matrices

$$Y_\nu \sim \begin{pmatrix} \varepsilon_1 \varepsilon_2 & \varepsilon_1 \varepsilon_2 \eta_2 & \varepsilon_1 \varepsilon_2 \eta_1 \eta_2 \\ \varepsilon_1 \eta_2 & \varepsilon_1 & \varepsilon_1 \eta_1 \\ \eta_1 \eta_2 & \eta_1 & 1 \end{pmatrix} \quad M_R \sim \Lambda \begin{pmatrix} \eta_1 \eta_2 & \eta_1 & 1 \\ \eta_1 \eta_2 & \eta_1 & 1 \\ \eta_1 \eta_2 & \eta_1 & 1 \end{pmatrix}$$

$$\varepsilon_1 = \langle \phi_{32}^L \rangle / \Lambda_{32}$$

$$\varepsilon_2 = \langle \phi_{21}^L \rangle / \Lambda_{21}$$

$$\eta_1 = \langle \phi_{32}^\ell \rangle / \Lambda_{32}$$

$$\eta_2 = \langle \phi_{21}^\ell \rangle / \Lambda_{21}$$

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$$\eta_2 = \langle \phi_{21}^\ell \rangle / \Lambda_{21}$$

We have the freedom to
require Normal Hierarchy

$$\Delta_1 \lesssim 1 \quad \Delta_2 \lesssim 1$$

$$\implies \Lambda \gtrsim \text{few TeV}$$

Conclusions

In this work we have considered the leading phenomenological implications of neutrino anarchy in flavour deconstruction [Greljo, Isidori, 2024]

- We have computed which is the expected absolute neutrino mass scale predicted by any given flavour-deconstructed model
- We have shown that Normal Hierarchy allows for the NP scale Λ to be lower with respect to Inverted Hierarchy
- The contribution to LFV processes coming from the neutrino sector can be dominant over the Gauge and Yukawa sectors
- In some cases, the NP scale Λ can be as low as few TeV and can be probed by near future experiments, such as Mu3e and COMET