

Semileptonic B decays

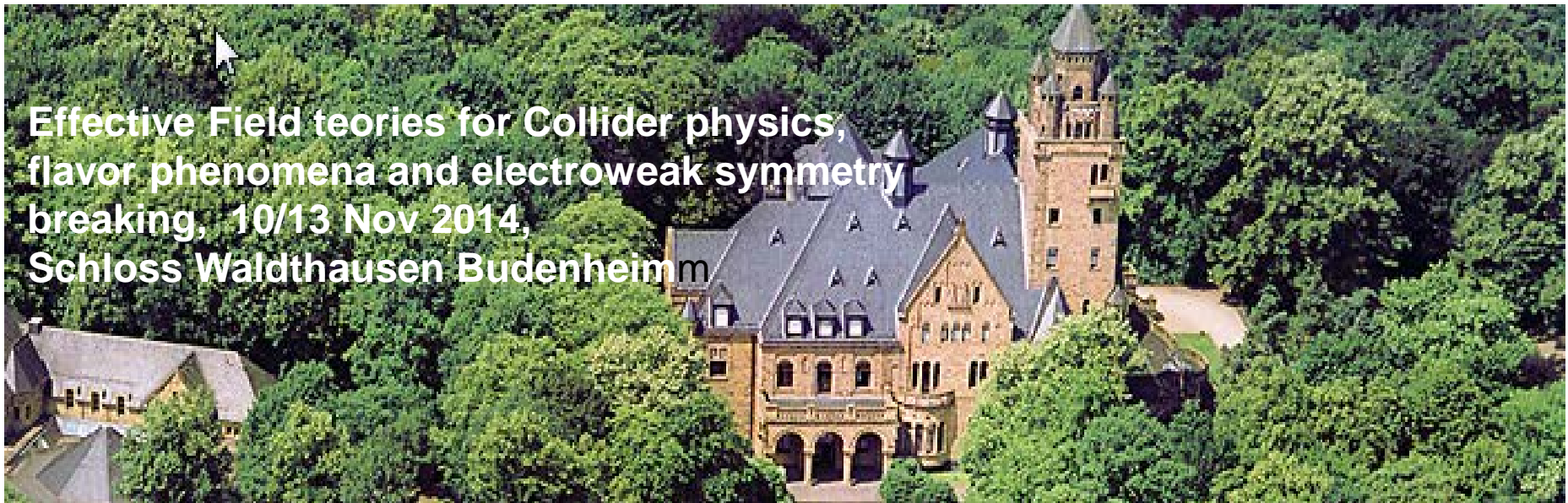
Giulia Ricciardi

Università di Napoli "Federico II"

Italy



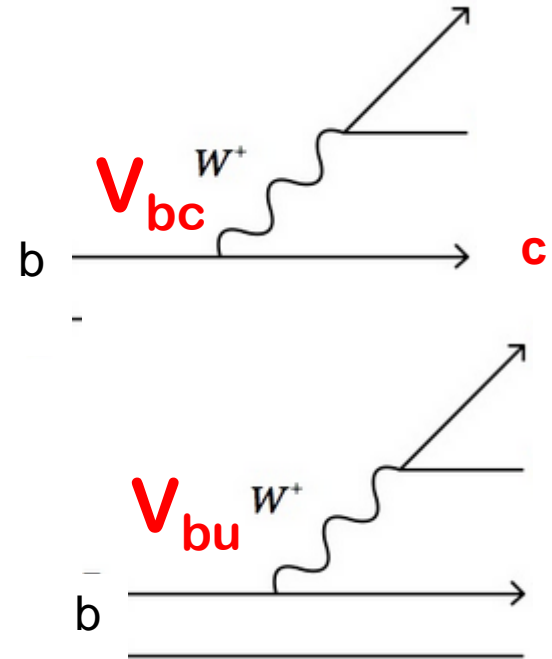
Effective Field theories for Collider physics,
flavor phenomena and electroweak symmetry
breaking, 10/13 Nov 2014,
Schloss Waldthausen Budenheim



Overview

- $b \rightarrow c \ell \nu$
- Exclusive $B \rightarrow D^{(*)} \ell \nu$,
 - Inclusive $B \rightarrow X_c \ell \nu$

- $b \rightarrow u \ell \nu$
- Exclusive $B \rightarrow \pi (\dots) \ell \nu$,
 - Inclusive $B \rightarrow X_u \ell \nu$



Most precise determination of $|V_{ub}|$ $|V_{cb}|$

See talk of Buras for motivations

- Tension between inclusive and exclusive determinations
- Low mass open charm spectrum
- BSM when $\ell \rightarrow \tau$

Exclusive decays $B \rightarrow D^{(*)} \ell \nu$

$$\frac{d\Gamma}{d\omega} (B \rightarrow D^* (D)) \propto |V_{cb}|^2 (\omega^2 - 1)^{1/2 (3/2)} \mathcal{F}(\omega)^2 (G(\omega)^2)$$

$$\omega = \frac{p_{D^{(*)}} \cdot p_B}{m_B m_{D^{(*)}}}$$

Standard Step by Step

Comparison with data at a kinematically not suppressed point $\mathcal{F}(\omega)^2 |V_{cb}|^2$

Extrapolation at zero-recoil point $\omega=1$



dependence on
parameterization

Perturbative and non-perturbative $1/m_{c,b}^n$
corrections to unity form factors (in HF limit)

↑ perturbative order:
complete α_s^2 at zero
recoil

$|V_{cb}|$ extraction

Czarnecki, Melnikov 1996-99

B → D*ℓν

Generally Preferred

- ✓ less suppressed at zero recoil: $(\omega^2-1)^{1/2}$ (rather than $(\omega^2-1)^{3/2}$)
- ✓ vanishing corrections order $1/m$ (Luke's theorem)

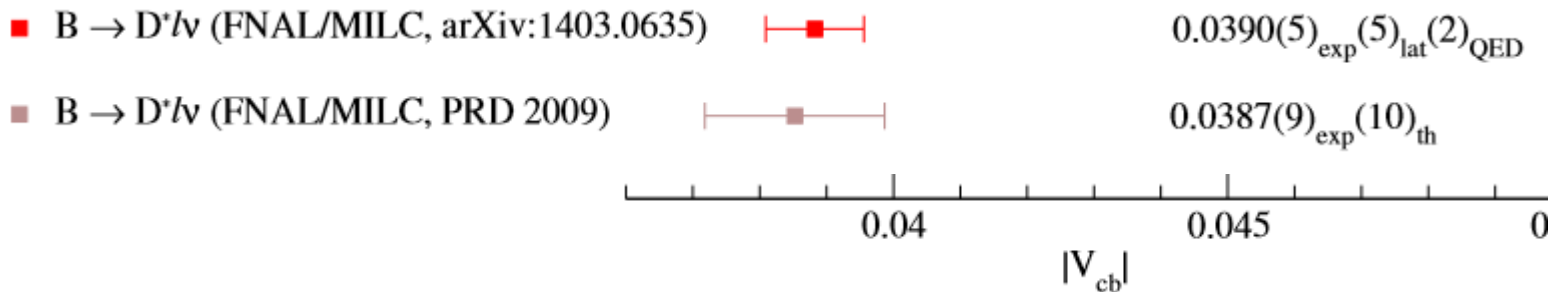
✓ Latest from Lattice

-first unquenched calculation

includes loops of sea quarks, up, down, strange $N_f=2+1$

$$\mathcal{F}(1) = 0.906 \pm 0.004 \pm 0.012$$

Bailey et al. Fermilab/MILC 1403.0635



Bailey,
lattice 14

Uncertainty	$ V_{cb} $
QCD	1.4%
QED	0.5%
Expt	1.3%

Largest error from discretization,
Estimated taking the difference between
HQET description of LGT and QCD

-Preliminary results ETM Nf=2 (realistic charm finite mass) in agreement
 Atoui 1305.0462

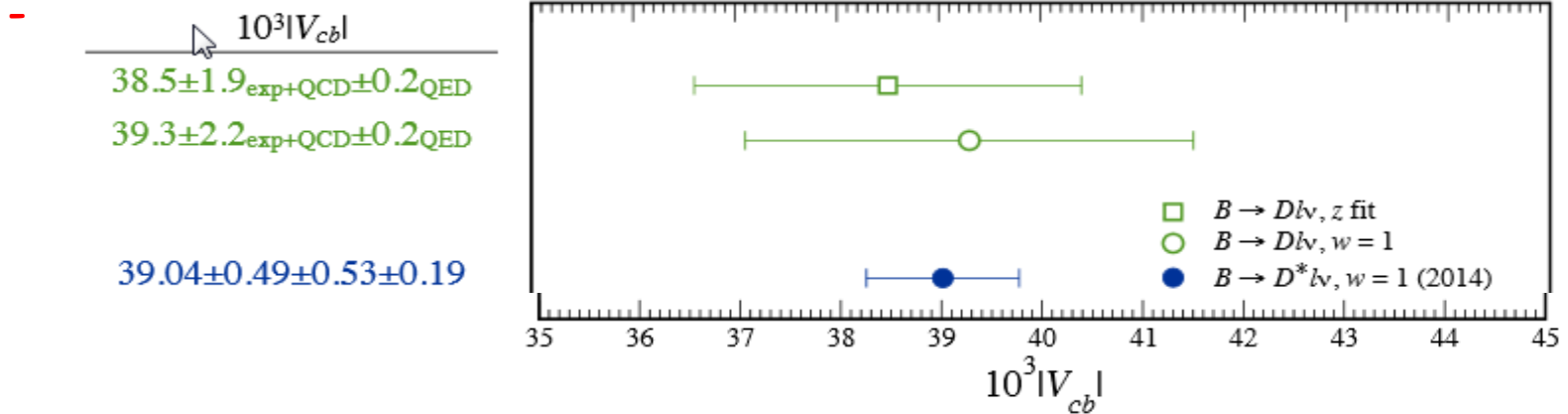
-only quenched results at the non-recoil point
 («step scaling» method, alternative to HQET)

de Divitiis et al 0707.0582

$$B \rightarrow D \ell \nu$$

✓ unquenched calculations at non-zero recoil full kinematic range

Qiu et al Fermilab/MILC 1312.0155



-Heavy-quark discretization errors largest source of uncertainty
 work in progress to reduce it

Jang et al SWME, MILC, and Fermilab 1311.5029

LCSR (see Mannel's talk)

□ $B \rightarrow D^* \ell \nu$

- ✓ Recent calculations incorporates higher order effects and estimates inelastic corrections

$$\mathcal{F}(1) = 0.86 \pm 0.02$$

Gambino, Mannel, Uraltsev, 1206.2296+HFAG 12
Gambino Schwanda 1307.4551

-Much larger th error (More than twice on $|V_{cb}|$)

-OPE power corrections $1/m^{4,5}$ matrix elements estimated by ground state saturation

Mannel, Turczyk, Uraltsev 2010, Heinonen, Mannel 2014

□ $B \rightarrow D \ell \nu$

- ✓ heavy quark expansion (+ BPS limit, where HF symmetries hold all orders)

Uraltsev 04

- ✓ +PDG 0312001

$$\mathcal{G}(1) = 1.04 \pm 0.02$$

-Exp+th on $|V_{cb}|$ uncertainty comparable with LQCD

Consistently lower than LQCD (higher $|V_{cb}|$)

Exclusive summary

<i>Exclusive decay</i>	$ V_{cb} \times 10^3$
<i>$B \rightarrow D^* l \bar{\nu}$</i>	
FNAL/MILC (Lattice unquenched 2014)	$39.04 \pm 0.49_{\text{exp}} \pm 0.53_{\text{QCD}} \pm 0.19_{\text{QED}}$
HFAG (Lattice unquenched 2012)	$39.54 \pm 0.50_{\text{exp}} \pm 0.74_{\text{th}}$
Rome (Lattice quenched $\omega \neq 1$ 2008)	$37.4 \pm 0.5_{\text{exp}} \pm 0.8_{\text{th}}$
HFAG (Sum Rules 2012)	$41.6 \pm 0.6_{\text{exp}} \pm 1.9_{\text{th}}$
<i>$\bar{B} \rightarrow D l \bar{\nu}$</i>	
FNAL/MILC (Lattice unquenched $\omega \neq 1$ 2013)	$38.50 \pm 1.9_{\text{exp+lat}} \pm 0.2_{\text{QED}}$
PDG (HQE + BPS 2012)	$40.6 \pm 1.5_{\text{exp}} \pm 0.8_{\text{th}}$
Rome (Lattice quenched $\omega \neq 1$ 2009)	$41.6 \pm 1.8 \pm 1.4 \pm 0.7_{FF}$

Prospects

✓ Experimental progress

- high statistics at LHCb for $B \rightarrow D^{(*)} \ell \nu$; however, at B factories fully reconstruction of B (or conjugate) helps measurements in presence of missing neutral particle (ν)

- Belle II estimated error on $|V_{cb}|$ at 75 ab^{-1} is about 1%

✓ $B_s \rightarrow D_s \ell \nu$

- More affordable on lattice: light spectator fixed to its known mass (m_s) and no extrapolation in the light quark mass needed

- Modification of step scaling method

Blossier et al(ETM Collab). 0909.3187

- Agreement with SR data

$$\mathcal{G}(1) = 1.052(46)$$

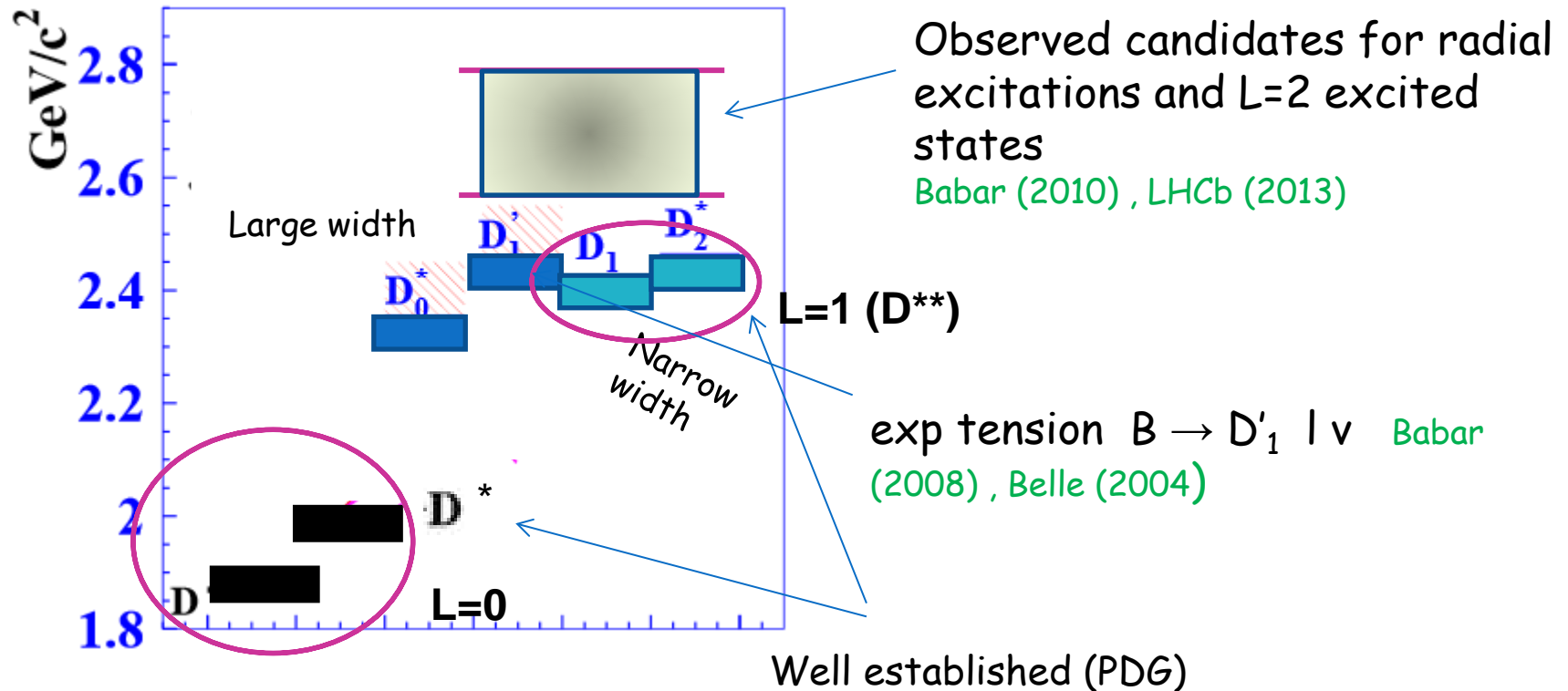
Atoui et al 1310.5238

✓ Extraction from baryonic decays at hadronic machines, (exp hard)

$$\Lambda_b^0 \rightarrow \Lambda_c^+ \ell^- \bar{\nu}$$

Stone and Zhang 1402.4205

Low mass open charm spectrum



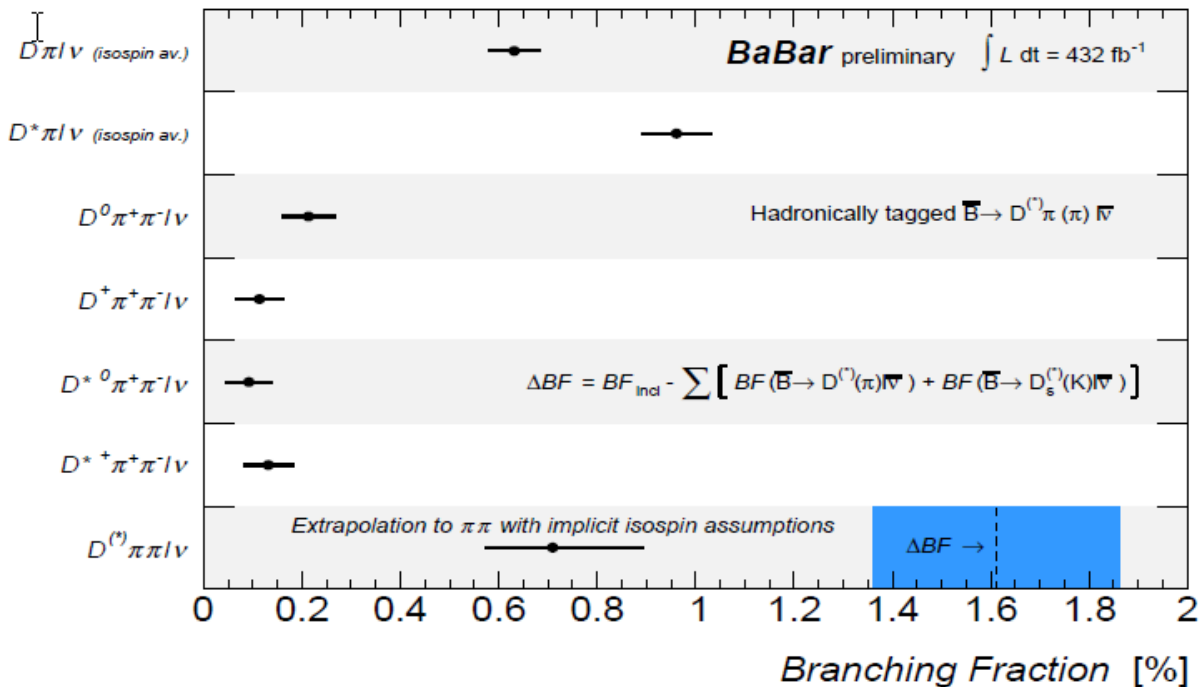
higher mass charm states background events to $B \rightarrow D^{(*)} | \nu$
(e.g. via $B \rightarrow D^{**} | \nu$)

Theoretical puzzles

1) BR for inclusive $B \rightarrow X_c \ell \nu$ not saturated by sum of exclusive BR (gap puzzle)

- Decays into $D^{(*)}$ make up $\sim 70\%$ of total inclusive $B \rightarrow X_c \ell \nu$ rate
- Decays into $D^{(*)} \pi$ make up $\sim 15\%$ of total inclusive $B \rightarrow X_c \ell \nu$ rate

Leaves a gap of about 15%



Closing the gap experimentally?

assigning about 0.7% to $B \rightarrow D^{(*)} \pi \pi \ell \nu$ production, significance reduced from 7σ to 3σ .

In the HQ limit $j_l = L \otimes s_l$

P-wave mesons can be grouped into two doublets:

$j_l=1/2$

strongly decays only through S-waves \rightarrow broad states

$j_l=3/2$

strongly decays only through D-waves \rightarrow narrow states

2) narrow width dominates over large width states (sum rules + HQ, quark models)

Le Yaouanc et al 96, Uraltsev 2001, Morenas et al. 1997, Ebert et al. 1998, Leibovich et al. 2007, Bigi et al. 2007....)

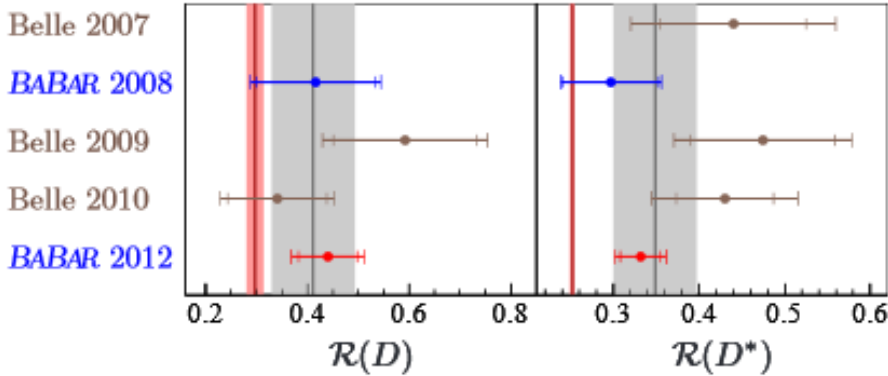
not confirmed by data (1/2 vs 3/2 puzzle)

Belle, Babar 06

- ✓ Relevance of the infinite mass limit approach in $b \rightarrow c$ decay
- ✓ Background for $|V_{ub}|$

B \rightarrow D^(*) τ ν_τ

B factories



$$\mathcal{R}_{\tau/l}^* \equiv \frac{\mathcal{B}(B \rightarrow D^* \tau \nu)}{\mathcal{B}(B \rightarrow D^* l \nu)} = 0.332 \pm 0.024 \pm 0.018$$

$$\mathcal{R}_{\tau/l} \equiv \frac{\mathcal{B}(B \rightarrow D \tau \nu)}{\mathcal{B}(B \rightarrow D l \nu)} = 0.440 \pm 0.058 \pm 0.018$$

Babar 2012 1205.5442

$$\mathcal{R}_{\tau/l}(SM) = 0.297 \pm 0.017 \quad \mathbf{2.0\sigma}$$

also Becirevic et al 1206.4977

$$\mathcal{R}_{\tau/l}^*(SM) = 0.252 \pm 0.003 \quad \mathbf{2.7\sigma}$$

Combined **3.4 σ**

✓ Agreement with Belle sample 657×10^6 B pair events

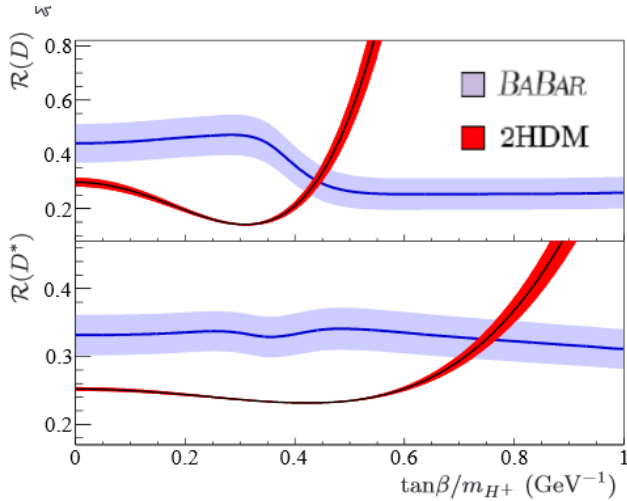
Belle 0910.4301.

✓ NP breaking of lepton-flavour universality?

an additional tensor operator in the effective Hamiltonian?

F. De Fazio, CKM 14

Awaiting for Belle update with full data set (772×10^6 B pairs)

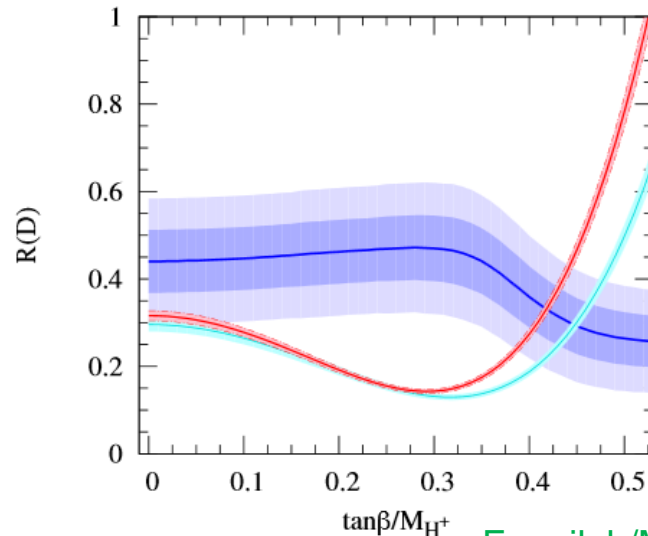


Babar 2012 1205.5442

- ✓ Excludes type II 2HDM charged Higgs boson with 99.8% CL ($m_{H^+} > 10$ GeV)
(Region with $m_{H^+} < 10$ GeV already excluded by $B \rightarrow Xs \gamma$ measurements) Misiak 0609232

Using estimates of FF from HQET and quenched QCD

by using unquenched lattice for R tension lessens a bit **1.7 σ**



Fermilab/MILC 1206.4992

Inclusive decays $B \rightarrow X_c \ell \nu$

$$\Gamma(B \rightarrow X_q \ell \nu) = \frac{G_F^2 m_b^5}{192\pi^3} |V_{qb}|^2 \left[c_3 \langle O_3 \rangle + c_5 \frac{\langle O_5 \rangle}{m_b^2} + c_6 \frac{\langle O_6 \rangle}{m_b^3} + O\left(\frac{1}{m_b^4}\right) \right]$$

✓ Scheme dependence (quark mass definition: 1S, kinetic, etc.)

✓ Kinetic scheme

- Complete $O(\alpha_s^2)$ corrections to leading term (parton model)+BLM terms $\alpha_s^{n+1} \beta_0^n$
[Melnikov, Czarnecki, Pak, Biswas, Gambino, ...]
- Complete $\alpha_s \frac{\Lambda^2}{mb^2}$ [Mannel, Pivovarov, Becher, Boos, Lunghi, Alberti, Ewerth, Gambino, Nandi, ...]
(see Mannel's talk)
- $O(1/mb^{2,3})$ known, $O(\Lambda/m_b^{4,5})$ estimated
[Gremm, Kapustin, Dassinger, Turczyk, Mannel, Gambino, Bigi, Uraltsev, Zwicky ...]
- $\log mc, 1/mc^2$... intrinsic charm estimates
[Breidenbach, Feldmann, Mannel, Turczyk, Bigi, Mannel, Uraltsev, ...]
- Threshold resummation (double Sudakov-like logs) not relevant (cut off by the mc mass)
Di Giustino, GR, Trentadue 11, ...

• $B \rightarrow X_c \tau \nu$ studied at order $\alpha_s \frac{\Lambda^2}{mb^2}$

Global fit results

width + hadron, lepton momenta: about 70 measurements available (80% from B factories)

Additional constraint to increase precision estimate in m_b
photon energy moments in $B \rightarrow X_s \gamma$, or a precise constraint on m_c

Constraint	$ V_{cb} $ (10^{-3})
$B \rightarrow X_s \gamma$	$41.94 \pm 0.43_{\text{fit}} \pm 0.59_{\text{th}}$
$m_c^{\overline{\text{MS}}}(3 \text{ GeV})$	$41.88 \pm 0.44_{\text{fit}} \pm 0.59_{\text{th}}$

kinetic scheme **HFAG 12** $\frac{\delta V_{cb}}{V_{cb}} < 2\%$

to compare with excl $\sim 2\%$

Latest global fits in kinetic scheme (mc constraint)

$$|V_{cb}| = (42.42 \pm 0.86) \times 10^{-3}$$

Gambino Schwanda 2014

Including α_s/m_b^2 : error decreases

$$|V_{cb}|_{\text{inc}} = (42.42 \pm 0.81) \times 10^{-3}$$

Healey ICHEP 2014

Incorporating α_s/m_b^3 in progress

$|V_{cb}|$ summary

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<i>Inclusive decays</i>	
HFAG ($B_s \rightarrow X_s \gamma$ constraint)	$41.94 \pm 0.43_{\text{fit}} \pm 0.59_{\text{th}}$
HFAG (m_c constraint)	$41.88 \pm 0.44_{\text{fit}} \pm 0.59_{\text{th}}$
Gambino, Schwanda 2014	42.42 ± 0.86

3 σ disagreement

Future:

- ❑ CLEO \rightarrow \approx 50-70 more stat B factories \rightarrow \approx 50 more stat Belle II
- ❑ LHCb: about 5 million $B \rightarrow D^* \mu \nu$ decay no prospects for $|V_{cb}|$ measurement

$|V_{ub}|$ exclusive determination

- Traditionally extracted by the decay $B \rightarrow \pi \ell \nu$
(only a single form factor in massless limit)

$$\frac{d\Gamma(\bar{B}^0 \rightarrow \pi^+ \ell \bar{\nu})}{dq^2} = \frac{G_F^2 |\vec{p}_\pi|^3}{24\pi^3} |V_{ub}|^2 |f_+(q^2)|^2 \quad \langle \pi^+(p) | \bar{u} \gamma_\mu b | \bar{B}^0(p+q) \rangle = f_+(q^2) (2p_\mu + q_\mu)$$

Non-pert th predictions for f_+ usually confined to regions of q^2

Complementarity

- ✓ Light Cone Sum Rules LCSR **low q^2 regions $\sim < 16 \text{ GeV}$**
(OPE near the light-cone)

LCSR Khodjamirian et al 11, BGL: Boyd, Grinstein, Lebed, ...

- ✓ Lattice **large $q^2 \sim > 16 \text{ GeV}$** (to avoid large discretization errors)

Better fit with data

[Unquenched HPQCD 07, FNAL/MILC 09, ma preliminary from ALPHA, HPQCD, FNAL/MILC, RBC/UKQCD 2012]

$|V_{ub}|$ HFAG exclusive determination

Also HFAG simultaneous fit of the BCL parameterization to data and LQCD calculations (all q^2 range)

$$|V_{ub}| = (3.28 \pm 0.29) \times 10^{-3}$$

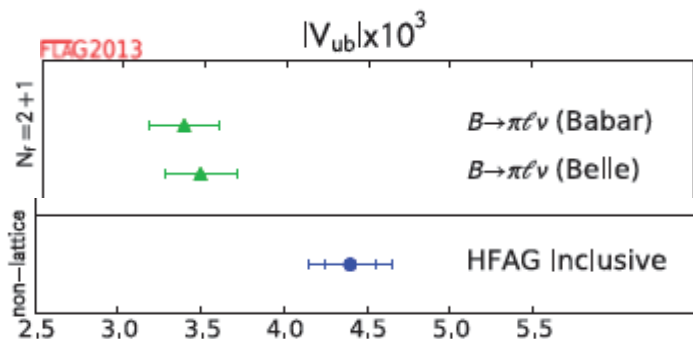
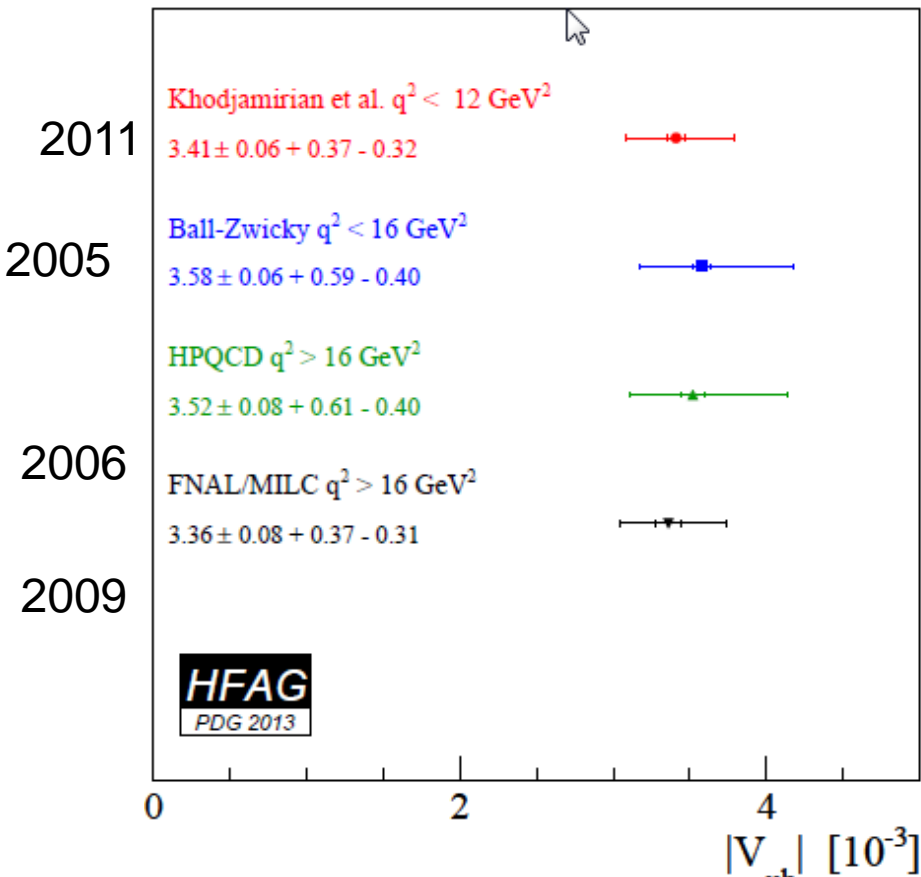
additional recent LCSR calculations + Babar, Belle data

$$|V_{ub}| = (3.32^{+0.26}_{-0.22}) \cdot 10^{-3}$$

Imson, Khodjamirian, Mannel, van Dyk 14097816

3 σ tension between exclusive and inclusive determinations

EI-Khadra ICHEP 2014



new players

X_u	Theory	q^2 GeV/ c^2	$ V_{ub} $ 10^{-3}
π^0	LCSR [33]	< 12	$3.35 \pm 0.23 \pm 0.09^{+0.36}_{-0.31}$
	LCSR [34]	< 16	$3.63 \pm 0.20 \pm 0.10^{+0.60}_{-0.40}$
	HPQCD [35]	> 16	$3.44 \pm 0.31 \pm 0.09^{+0.59}_{-0.39}$
	FNAL [36]	> 16	$3.29 \pm 0.30 \pm 0.09^{+0.37}_{-0.30}$
π^+	LCSR [33]	< 12	$3.40 \pm 0.13 \pm 0.09^{+0.37}_{-0.32}$
	LCSR [34]	< 16	$3.58 \pm 0.12 \pm 0.09^{+0.59}_{-0.39}$
	HPQCD [35]	> 16	$3.81 \pm 0.22 \pm 0.10^{+0.66}_{-0.43}$
	FNAL [36]	> 16	$3.64 \pm 0.21 \pm 0.09^{+0.40}_{-0.33}$
ρ^0	LCSR [24]	< 16	$3.56 \pm 0.11 \pm 0.09^{+0.54}_{-0.37}$
	BM [37]		$3.76 \pm 0.11 \pm 0.10^{+0.31}_{-0.25}$
	UKQCD [38]	full range	$3.68 \pm 0.10 \pm 0.10^{+0.29}_{-0.34}$
	ISGW2 [25]		$3.98 \pm 0.11 \pm 0.10$
ρ^+	LCSR [24]	< 16	$3.51 \pm 0.16 \pm 0.13^{+0.53}_{-0.36}$
	BM [37]		$3.66 \pm 0.15 \pm 0.14^{+0.30}_{-0.24}$
	UKQCD [38]	full range	$3.59 \pm 0.15 \pm 0.13^{+0.28}_{-0.33}$
	ISGW2 [25]		$3.87 \pm 0.16 \pm 0.15$
ω	LCSR [24]	< 12	$3.08 \pm 0.29 \pm 0.11^{+0.44}_{-0.31}$
	ISGW2 [25]	full range	$3.03 \pm 0.23 \pm 0.11$

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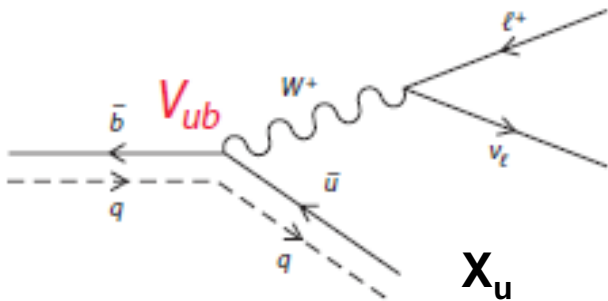
Belle 1306.2781

Babar PRD88 (2013) 032005

High statistic $B \rightarrow pl \nu$ studies may be sensitive to small right-handed admixture to SM weak currents

Bernlochner, Ligeti, Turczyk 1408.2616

Inclusive $|V_{ub}|$



large $b \rightarrow c$ background ($|V_{cb}/V_{ub}|^2 \approx 100$)

Need experimental phase space cuts to reduce background;
in general

$$m_X \ll E_X$$

Phase space regions where OPE fails become dominant; new
unwelcome effects (with respect to semileptonic $b \rightarrow c$):

- Final gluon radiation strongly inhibited: soft and collinear singularities
- perturbative expansion of spectra affected by large logarithms

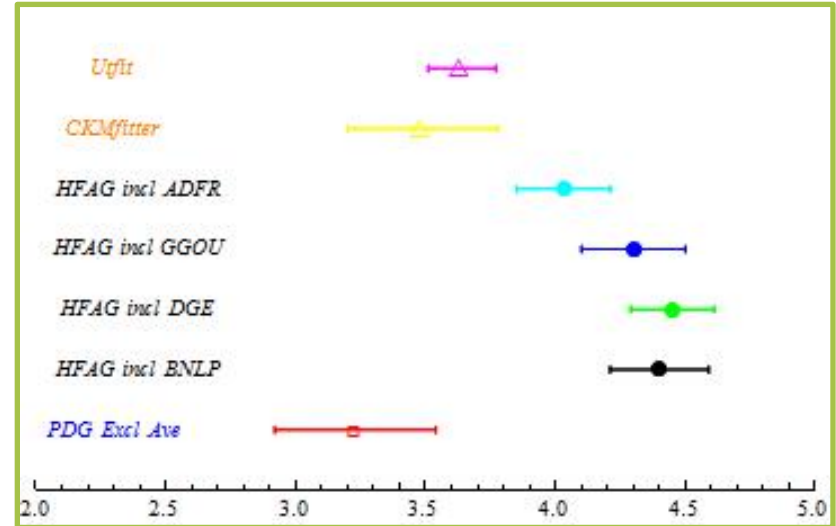
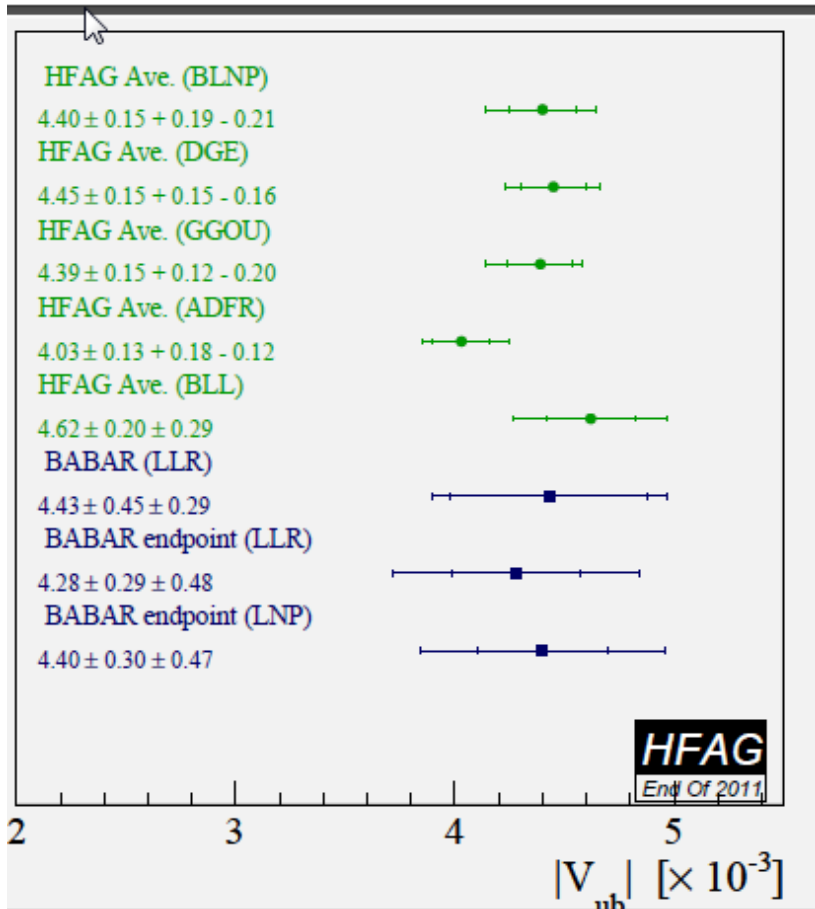
$$\alpha_s^n \log^{2n}(2 E_X/m_X)$$

to be resummed at all orders in PT

- non-perturbative effects related to a small vibration of the b quark in the B meson (Fermi motion) enhanced

Results averages: Long lasting puzzle

Inclusive



Strong statement
 (not yet contrasted in literature):
 No NP allowed by present constraints
 Pokorski Crivellin 1407.1320

At SuperFlavour factories (75 ab^{-1}) errors expected to reduce to 3% (excl) 2% (incl)

Conclusions

recent progress and future prospects

- Significant advances in experiment (phase space in inclusive decays, $B \rightarrow D^{(*)} \pi \pi | \nu$ decays, decays into τ ...)
more expected: LHCb now and Belle II from 2016
- Significant reduction of LQCD errors & new non recoil calculations
other lattice groups and methods overcoming preliminary stage
- LCSR $|V_{ub}|$ «ultimate» errors critical method analysis (correlation between normalization and shape, z-parameterization,...) + new goal in inclusive $|V_{cb}|$ (higher orders...)

NP always more constrained; each novelty aligns to SM

but $|V_{ub}| |V_{cb}|$ discrepancy between exclusive, inclusive still alive ,
with different levels of vitality...