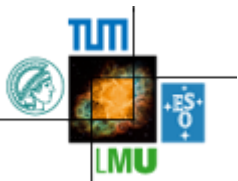


Flavour Expedition to the Zeptouniverse

Andrzej J. Buras
(Technical University Munich, TUM-IAS)



ERC Workshop
Mainz, November 2014



A Journey to the Very Short Distance Scales:

1676 - 2046

Microuniverse

10^{-6}m

**Bacteriology
Microbiology**

Nanouniverse

10^{-9}m

Nanoscience

Femtouniverse

10^{-15}m

**Nuclear Physics
Low Energy Elementary
Particle Physics**

Attouniverse

10^{-18}m

**High Energy Particle
Physics (present)**

**High Energy Proton-Proton
Collisions at the LHC**

$5 \cdot 10^{-20}\text{m}$

**Frontiers of Elementary
Particle Physics in 2010's**

**High Precision Measurements
of Rare Processes (Europe,
Japan, USA)**

10^{-21}m

Zeptouniverse



**New Physics beyond the SM
must exist !!!**



**It is our duty to find it.
If not at the LHC then through
high precision experiments.**



**Quark Flavour Physics
Lepton Flavour Violation
EDMs + $(g-2)_{\mu,e}$**

**In our search for a more
fundamental theory we need
to improve our understanding
of **Flavour****

1.
$$\frac{\text{Br}(B_d \rightarrow \mu^+ \mu^-)}{\text{Br}(B_s \rightarrow \mu^+ \mu^-)} \approx (4.3 \pm 1.8) \left[\frac{\text{Br}(B_d \rightarrow \mu^+ \mu^-)}{\text{Br}(B_s \rightarrow \mu^+ \mu^-)} \right]_{\text{SM CMFV}}$$

(LHCb, CMS)

2. Anomalies in angular observables in $B_d \rightarrow K^* \mu^+ \mu^-$ (LHCb)



3. $B \rightarrow D^* \tau \nu, B \rightarrow D \tau \nu$ (2-3 σ) (BaBar)
(4 σ) (+ Belle)

4. Breakdown of Lepton-Universality in $B^+ \rightarrow K^+ l^+ l^-$

5. Some Tensions in UT-fits (present already since 2008)

2015-2025 : Expedition
Attouniverse → Zeptouniverse
 $10^{-18}\text{m} \rightarrow 10^{-21}\text{m}$

Quark
Flavour =
Physics

**2015-2025 : Expedition
Attouniverse → Zeptouniverse
 $10^{-18}\text{m} \rightarrow 10^{-21}\text{m}$**

**Quark
Flavour
Physics =**



Searching for New Physics on the Way to Zeptoniverse

Searching for New Physics on the Way to Zeptouniverse

21st Century



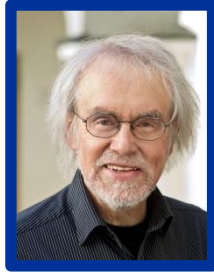
Advanced ERC Grant at the TUM Institute for Advanced Study Zeptouniverse Base Camp



**HEADQUARTERS
ERC-Flavour**



Present ERC Flavour Team



AJB



J.Girrbach-Noe



G.Isidori



S.Pokorski



F. De Fazio



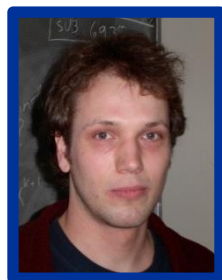
D.Buttazzo



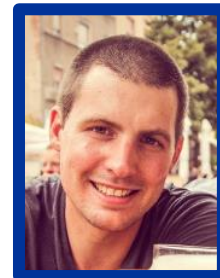
G.Buchalla



A.Ibarra



C.Bobeth



R.Kneijens



M.Ratz



O.Cata

Basic Questions for Next 28min

- 1.** Can Quark Flavour Physics give us insight into the dynamics at very SD scales if no direct clear signal of NP will be seen at the LHC? No new particles below 6 TeV.
- 2.** Can we reach Zeptouniverse 10^{-21}m (~ 200 TeV) by means of Quark Flavour Physics?
- 3.** Which Processes could give us the best resolution of SD scales?

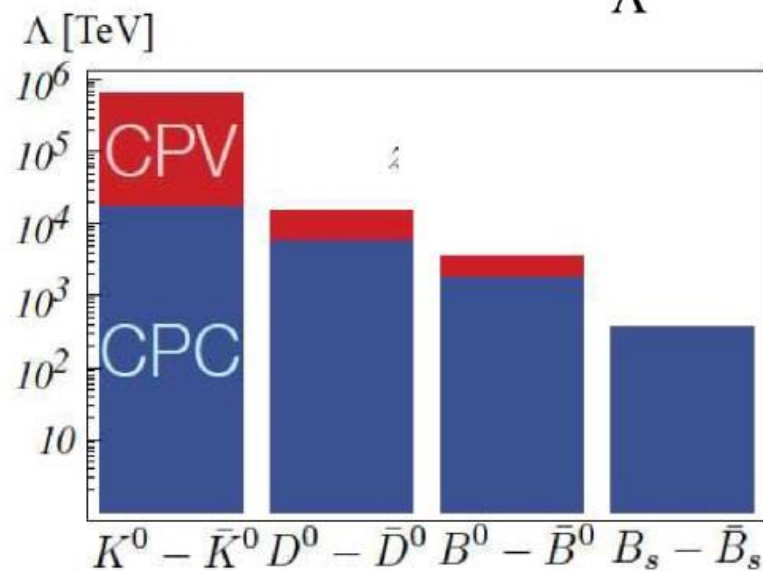
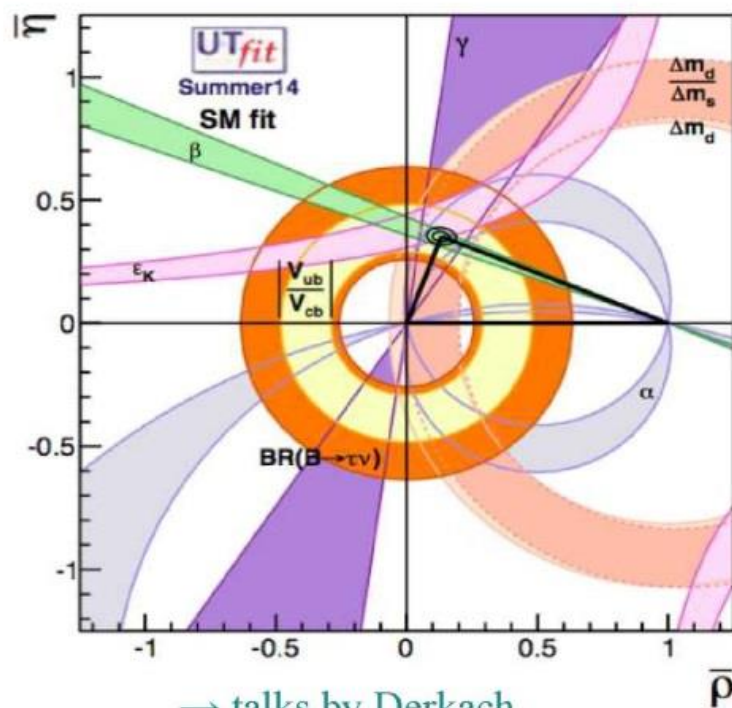
See also Charles et al.
(1309.2293)

- Are there other sources of flavor symmetry breaking (beside the SM Yukawa couplings)?

- What determines the observed pattern of quark & lepton mass matrices?

That's the question addressed by precision measurements (& searches) of flavor-changing processes of quarks & charged-leptons → So far everything seems to fit well with the SM → Strong limits on NP

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda^2} \mathcal{O}_{\Delta F=2}$$



Kamenik '13, G.I. '13, ...
[wide literature]

The sensitivity of $\Delta F=2$ processes to scales $\Lambda_{\text{NP}} > 1000 \text{ TeV}$ is impressive !!!

Yet

Three points to be made in this talk

1

New Physics at these scales cannot be measured in K, B_s, B_d, D rare decays (NP effects negligible)



2

We cannot learn much about the nature of this physics through $\Delta F=2$ processes and Effective Theory approach except when flavour symmetries $U(3)^3$ (MFV), $U(2)^3$ are involved.

3

We need badly rare decays to learn about physics beyond the LHC.

?

What are the maximal scales at which NP can be seen in rare K, B_s, B_d, D decays?

Three Basic Requirements

1 Precise CKM parameters from tree level decays (negligible NP contributions)

Main Targets : $|V_{ub}|, |V_{cb}|, \gamma$

2 Precise Lattice QCD Calculations

Main Targets : $F_{B_s}, F_{B_d}, \hat{B}_{B_d}, \hat{B}_{B_s}, B_8^{(2/3)}, B_6^{(1/2)}$
+ formfactors ($B \rightarrow K^*, K$)

Significant progress in the last years (dynamical fermions) but higher precision needed in order to see small NP effects.

Determination of $|V_{ub}|$ and $|V_{cb}|$ Crucial for Identification of New Physics

AJB + Girrbach-Noe, 1306.3755 \Leftrightarrow (Dependently on $|V_{ub}|$ and $|V_{cb}|$ different NP is required to fit the data)

Crivellin + Pokorski; 1407.1320
(NP explanation in the difference between exclusive and inclusive determinations currently ruled out)

Scenarios

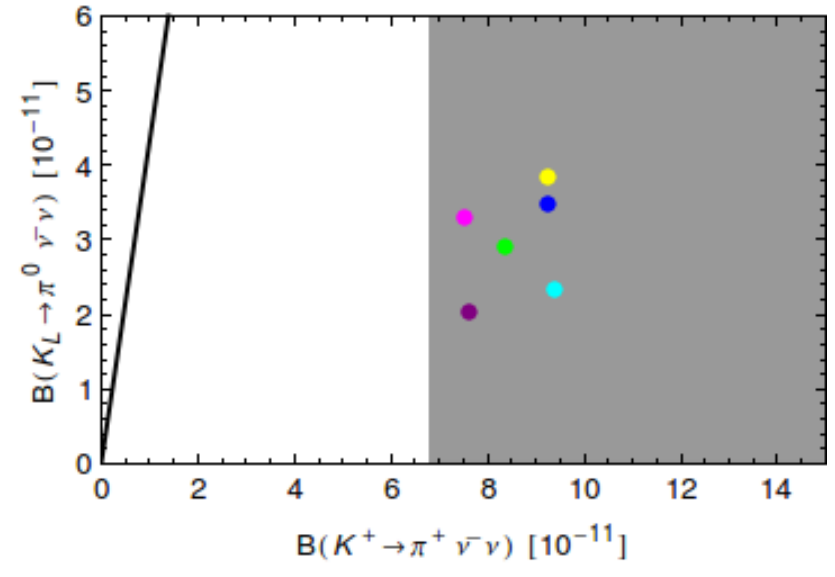
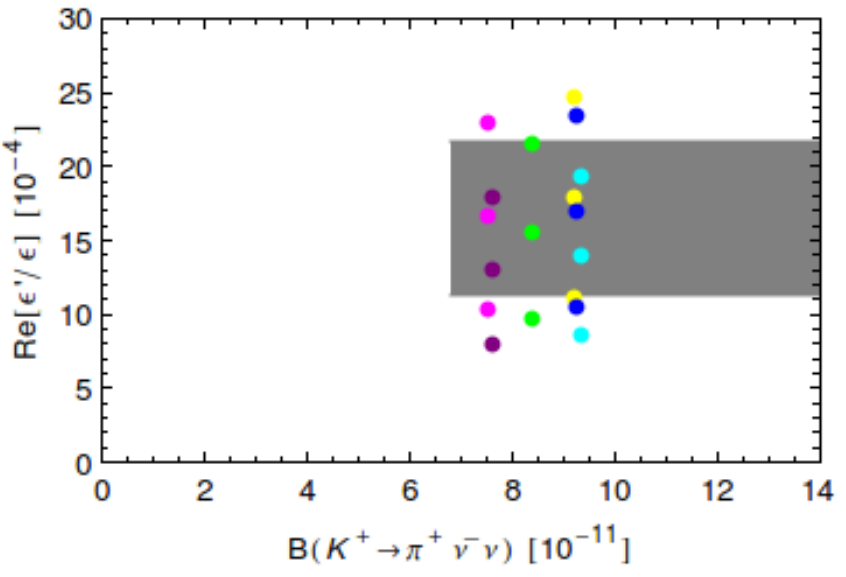
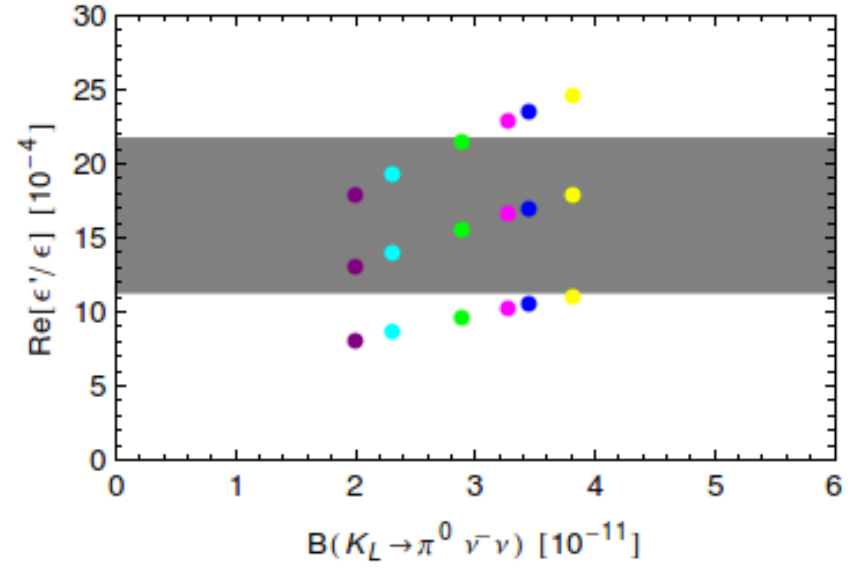
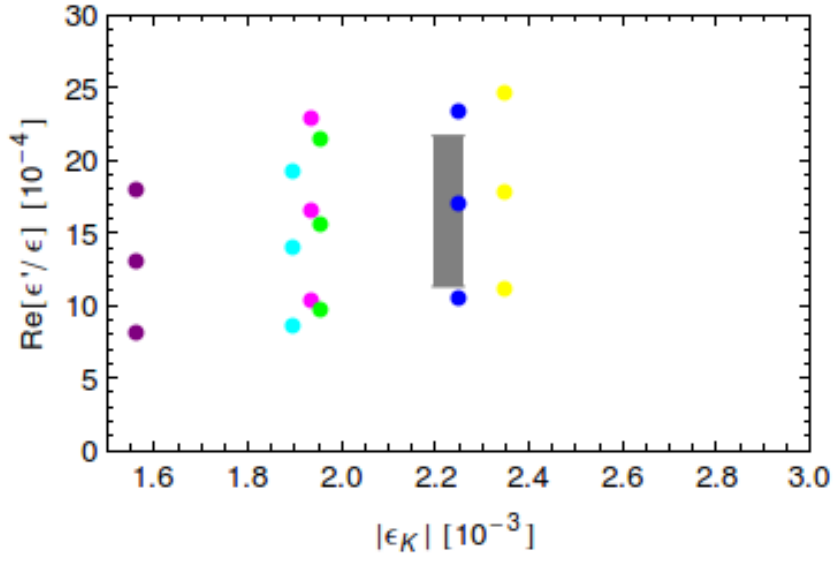
$ V_{ub} \cdot 10^{-3}$	$ V_{cb} \cdot 10^{-3}$
3.2	39.0
3.2	42.0
4.1	39.0
4.1	42.0
3.7	40.5
3.9	42.0

10^3	$ V_{ub} _{exc}$	$\approx 3.4 \pm 0.3$
10^3	$ V_{ub} _{inc}$	$\approx 4.3 \pm 0.3$
10^3	$ V_{cb} _{exc}$	$\approx 39 \pm 1.0$
10^3	$ V_{cb} _{inc}$	$\approx 42 \pm 1.0$

Data

AJB, De Fazio, Girrbach-Noe, 1404.3824

SM Predictions for different $|V_{ub}|, |V_{cb}|$



3

NLO + NNLO QCD Corrections and NLO Electroweak Corrections to Wilson Coefficients

1988 - 2014

Task completed !!

26 Years !

AJB: 1102.5650 (Update, Sept. 2014)

Most recent

NLO Electroweak to $B_{s,d} \rightarrow \mu^+ \mu^-$
NNLO QCD to $B_{s,d} \rightarrow \mu^+ \mu^-$

Bobeth, Gorbahn,
Stamou

Hermann, Misiak,
Steinhauser

Status of $B_{s,d} \rightarrow \mu^+ \mu^-$

The first
NLO QCD
Calculation
of $B_{s,d} \rightarrow \mu^+ \mu^-$

Buchalla + AJB (Nucl. Phys. B400 (1993) 225)

- Reduction of μ_t dependence in $m_t(\mu_t)$
- Finding missing factor of two in branching ratios.



Values of $\text{Br}(B_s \rightarrow \mu^+ \mu^-)_{\text{SM}} \sim 3 - 4 \cdot 10^{-9}$ were
 $\text{Br}(B_d \rightarrow \mu^+ \mu^-)_{\text{SM}} \sim 1 \cdot 10^{-10}$ with us
for last
15 years

Theoretical Improvements
over years

: Buchalla, AJB; Misiak, Urban (~1998)

September
2013

Recently: full NLO Electroweak, NNLO QCD

Bobeth, Gorbahn, Hermann, Misiak, Stamou, Steinhauser

Data (LHCb+CMS)

$$\bar{\text{Br}}(B_s \rightarrow \mu^+ \mu^-)_{\text{SM}} = (3.65 \pm 0.23) \cdot 10^{-9}$$

$$\text{Br}(B_d \rightarrow \mu^+ \mu^-)_{\text{SM}} = (1.06 \pm 0.09) \cdot 10^{-10}$$

$$(2.8 \pm 0.7) \cdot 10^{-9}$$

$$(3.6^{+1.6}_{-1.4}) \cdot 10^{-10}$$

Warning: $|V_{cb}|$ ($|V_{ts}|$) Dependence

BGHMSS

use

$$|V_{cb}|_{\text{incl}} \approx 42 \cdot 10^{-3}$$

$$\Rightarrow \bar{\text{Br}}(B_s \rightarrow \mu\bar{\mu})_{\text{SM}} = (3.65 \pm 0.23) \cdot 10^{-9} \\ (2.8 \pm 0.7) \cdot 10^{-9} \\ \text{(LHCb+CMS)}$$

But
for

$$|V_{cb}|_{\text{excl}} \approx 39 \cdot 10^{-3} \Rightarrow \bar{\text{Br}}(B_s \rightarrow \mu\bar{\mu})_{\text{SM}} \approx (3.1 \pm 0.2) \cdot 10^{-9}$$

Different
Route

(AJB 2003)
(Knegjens 2014)

$$\bar{\text{Br}}(B_s \rightarrow \mu\bar{\mu})_{\text{SM}} = (3.5 \pm 0.2) \cdot 10^{-9} \left[\frac{(\Delta M_s)^{\text{SM}}}{(\Delta M_s)^{\text{Data}}} \right] \left[\frac{1.33}{\hat{B}_s} \right]$$

(No V_{cb} , F_{B_s} dependence)

↑
Lattice

In Order to identify New Physics through Flavour Physics

We need

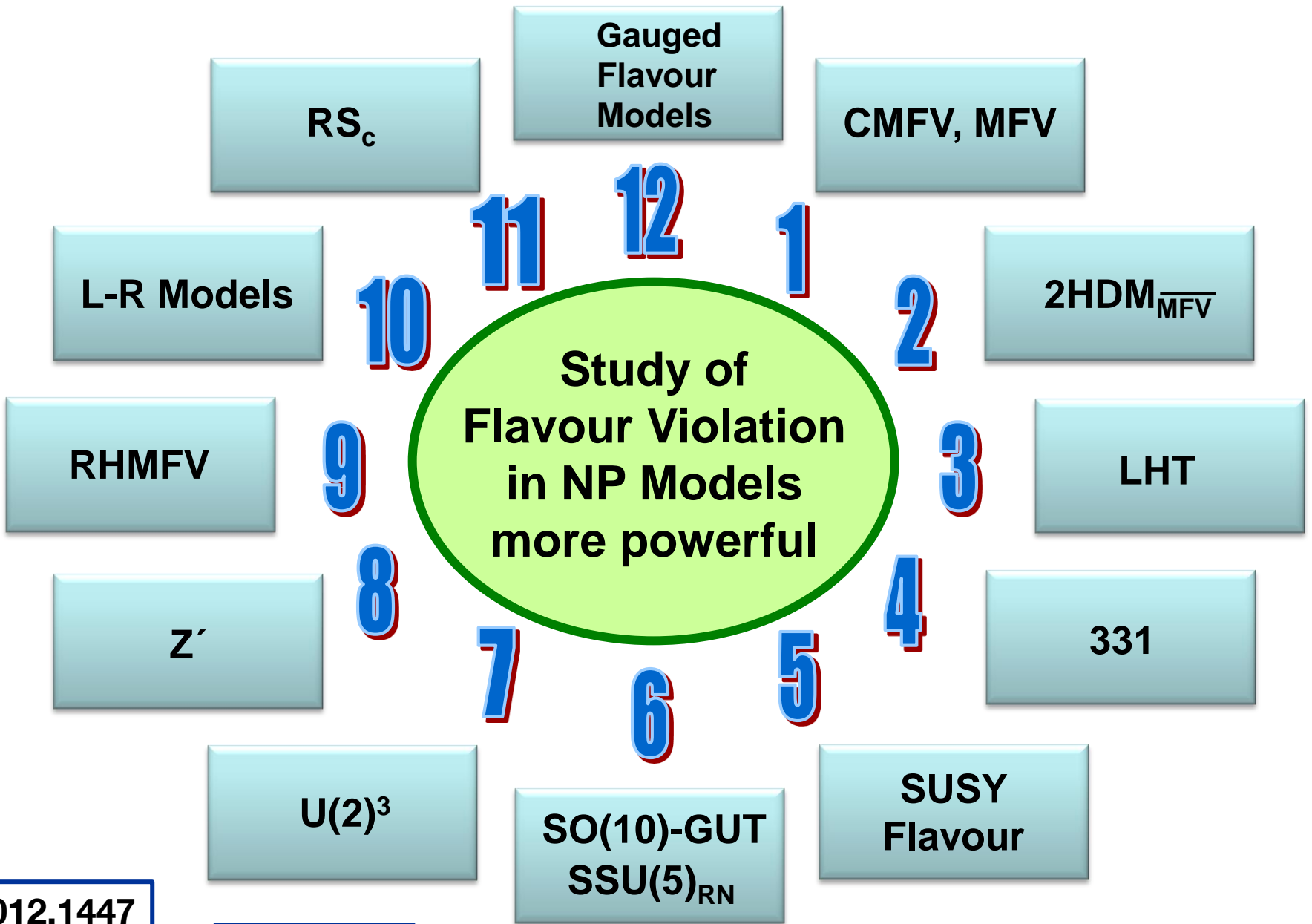
- 1. Many precision measurements of many observables and precise theory.**
- 2. Study Patterns on Flavour Violation in various New Physics models (correlations between many flavour observables).**

...and

3.

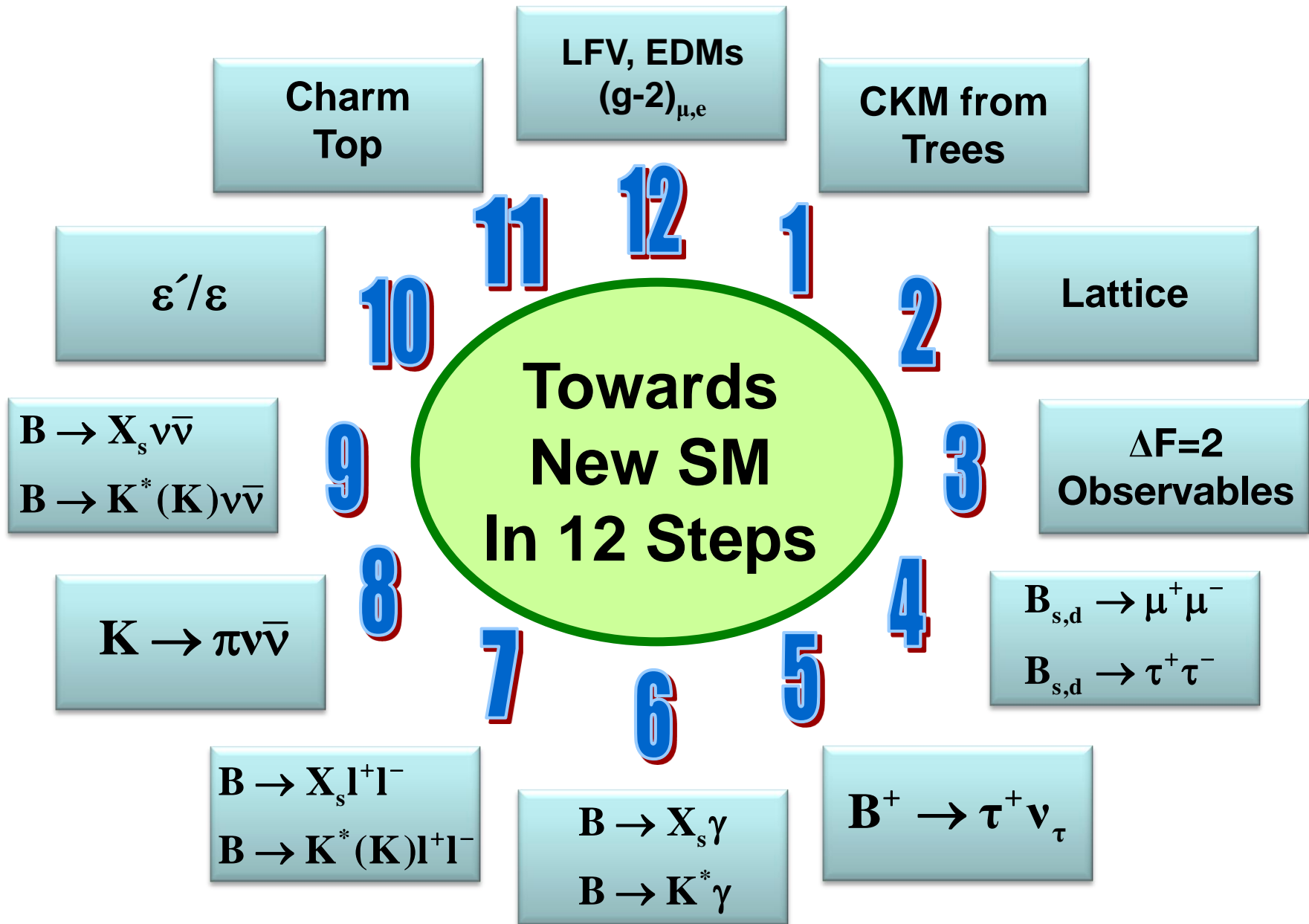
**Correlations between low energy
flavour observables and
Collider Physics (LHC, Tevatron)**

**Here top-down approach more
powerful in flavour physics**



1012.1447
1204.5065

1306.3755



Superstars and Stars of Quark Flavour Physics

Superstars

$\varepsilon_K, \Delta M_s, \Delta M_d, S_{\psi K_s}$	(TH)
$B_s \rightarrow \mu^+ \mu^-, B_d \rightarrow \mu^+ \mu^-, S_{\psi\phi}(\phi_s)$	(LHCb, CMS, ATLAS)
$B \rightarrow K \nu \bar{\nu}, B \rightarrow K^* \nu \bar{\nu}, B \rightarrow X_s \nu \bar{\nu}$	(Belle II)
$K^+ \rightarrow \pi^+ \nu \bar{\nu}, K_L \rightarrow \pi^0 \nu \bar{\nu}$	(NA62, J-Parc)

Stars

$B \rightarrow K^* \mu^+ \mu^-$	$B \rightarrow K \mu^+ \mu^-$
$B \rightarrow D^* \tau \nu_\tau$	$B \rightarrow D \tau \nu_\tau$

Old Superstar

ε'/ε will strike back
provided B_6 (QCD Penguins)
will be precisely known.

B_8 (EW Penguins)
 $\approx 0.65 \pm 0.05$
(UK-QCD)

The Power of Correlations between Flavour Observables (Correlation Primer)

**Crucial Tool for exploring
Attouniverse → Zeptouniverse**

Important Messages

1.

Correlations between decays of a given meson test the Dirac structure of couplings.

2.

Correlations between decays of different mesons test the flavour structure of couplings (flavour symmetries).

Stressed by Monika Blanke (CKM 2014)

Two Simplest General Frameworks

MFV (CMFV) $U(3)^3$

(symmetry between 3 generations)

Stringent Correlations between
 K, B_s, B_d

No new sources of flavour
and CP violation

$$S_{\psi K_s} = \sin 2\beta, \quad S_{\psi\phi} = S_{\psi\phi}^{\text{SM}} = \text{small}$$

No Right-handed currents

$U(2)^3$ Flavour Symmetry

(symmetry between two light
generations)

Stringent Correlations between
 B_s and B_d

Correlations $K \leftrightarrow B_{s,d}$ absent

New sources of CP violation
in B_s, B_d but

$S_{\psi K_s} \leftrightarrow S_{\psi\phi}$
anticorrelated

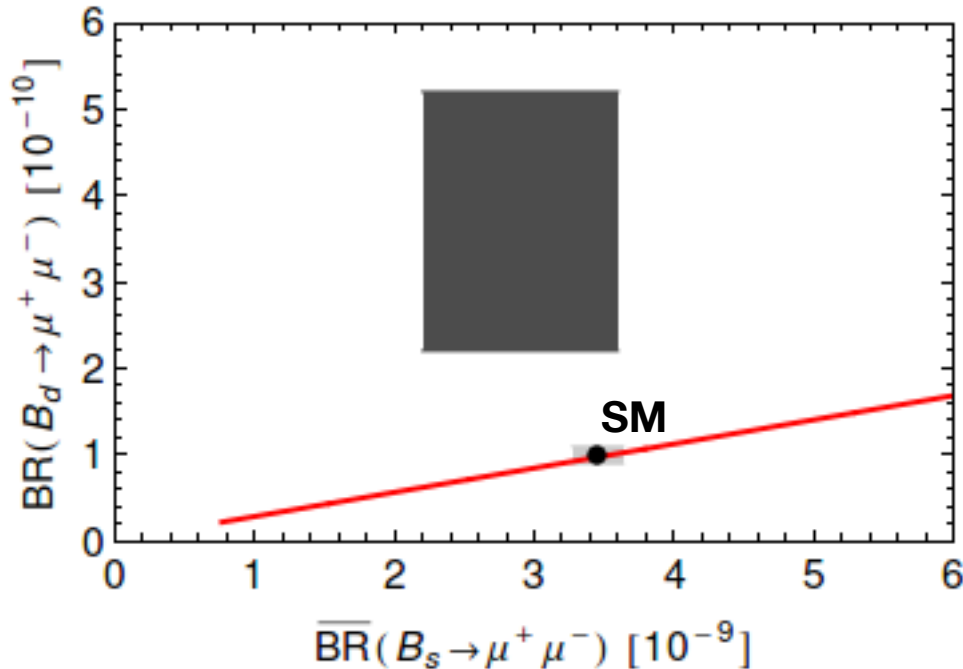
Right-handed currents
strongly suppressed

Constrained Minimal Flavour Violation

$[U(3)]^3$
flavour
symmetry

Valid also
in $U(2)^3$

AJB
Hurth, Isidori, Kamenik, Mescia



Golden Relation

$$\frac{\text{Br}(B_s \rightarrow \mu^+ \mu^-)}{\text{Br}(B_d \rightarrow \mu^+ \mu^-)} = \frac{\hat{B}_d \tau(B_s) \Delta M_s}{\hat{B}_s \tau(B_d) \Delta M_d}$$

AJB 2003

$$\hat{B}_d / \hat{B}_s \simeq 0.99 \pm 0.02 \quad (\text{tmQCD})$$

No CKM

No weak decay constants

$$\overline{\text{Br}}(B_s \rightarrow \mu^+ \mu^-) = (2.8 \pm 0.7) \cdot 10^{-9}$$

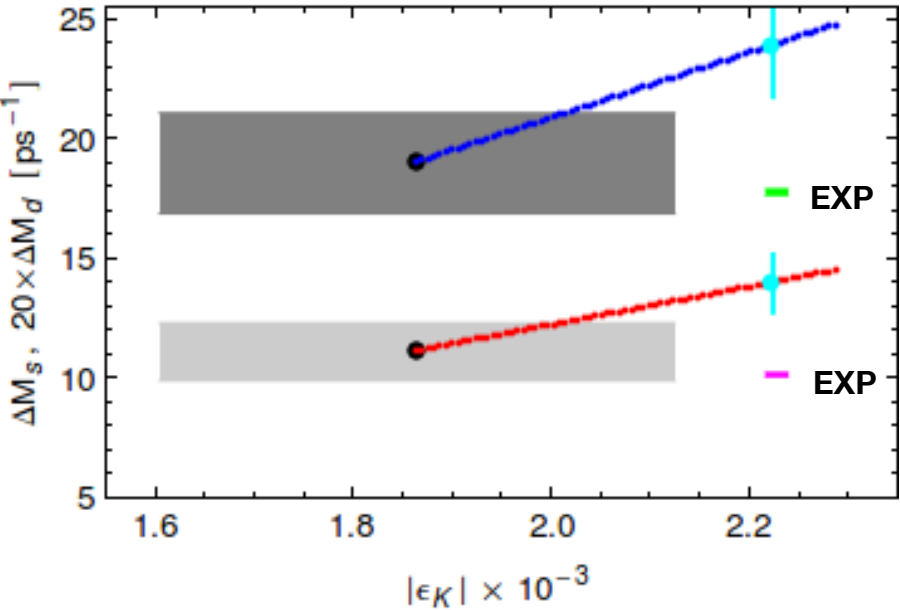
$$\text{Br}(B_d \rightarrow \mu^+ \mu^-) = \left(3.6^{+1.6}_{-1.4} \right) \cdot 10^{-10}$$

(LHCb + CMS)

2 Tensions in $\Delta F=2$ within MFV

$$\epsilon_K \leftrightarrow \Delta M_{s,d}$$

$$\epsilon_K \leftrightarrow S_{\psi K_s}$$



$$\left\{ |V_{ub}|_{\text{excl}} \right\} \Rightarrow \left\{ \begin{array}{l} \epsilon_K^{\text{SM}} < \epsilon_K^{\text{exp}} \\ S_{\psi K_s}^{\text{SM}} \approx S_{\psi K_s}^{\text{exp}} \end{array} \right\}^* \quad (2\sigma)$$

$$\left\{ |V_{ub}|_{\text{incl}} \right\} \Rightarrow \left\{ \begin{array}{l} \epsilon_K^{\text{SM}} \approx \epsilon_K^{\text{exp}} \\ S_{\psi K_s}^{\text{SM}} > S_{\psi K_s}^{\text{Data}} \end{array} \right\} \quad (3\sigma)$$

AJB + Girrbach 1306.3755

Similar tension in
Gauged Flavour Models:
AJB, Merlo, Stamou (2011)

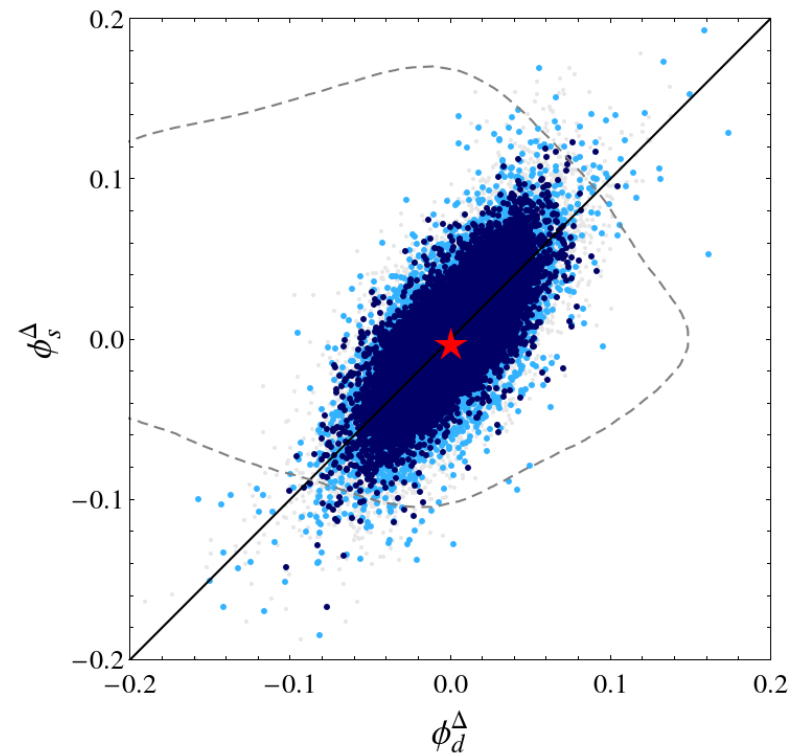
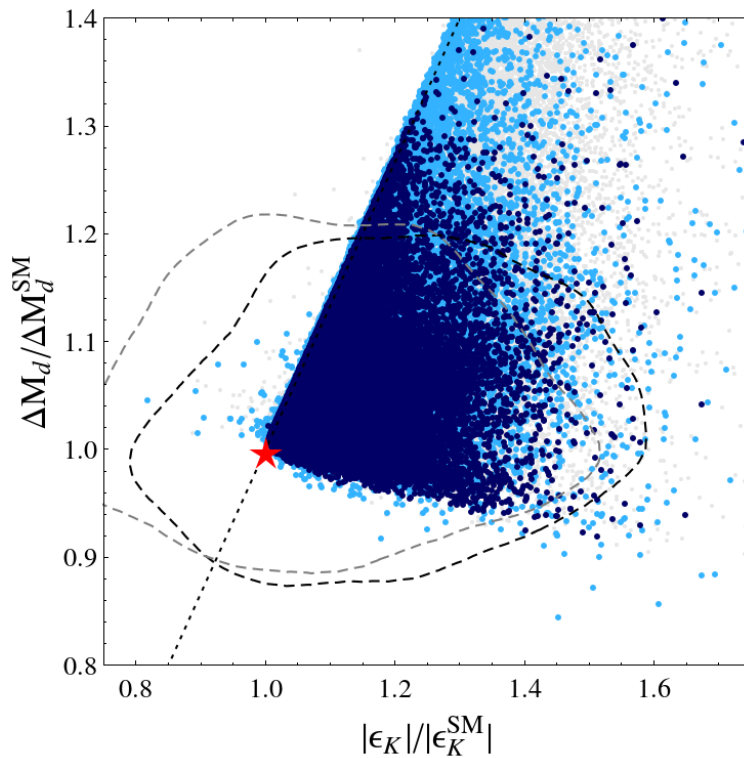
Lunghi + Soni (2008)
AJB + Guadagnoli (2008)

*) Can still work within MFV
($\Delta\epsilon_K > 0$ in MFV) Blanke + AJB
(2006)

Both tensions can only be clarified through improved $|V_{ub}|, |V_{cb}|$ + Lattice Input and improved measurement of $S_{\psi K_s}$

$\Delta F=2$ Observables in Split-Family or "Natural" SUSY with $U(2)^3$ Flavour Symmetry

Barbieri, Buttazzo, Sala, Straub (2014)



$$\epsilon_K \leftrightarrow S_{\psi K_s}$$

$$\epsilon_K \leftrightarrow \Delta M_{s,d}$$

Tensions removed

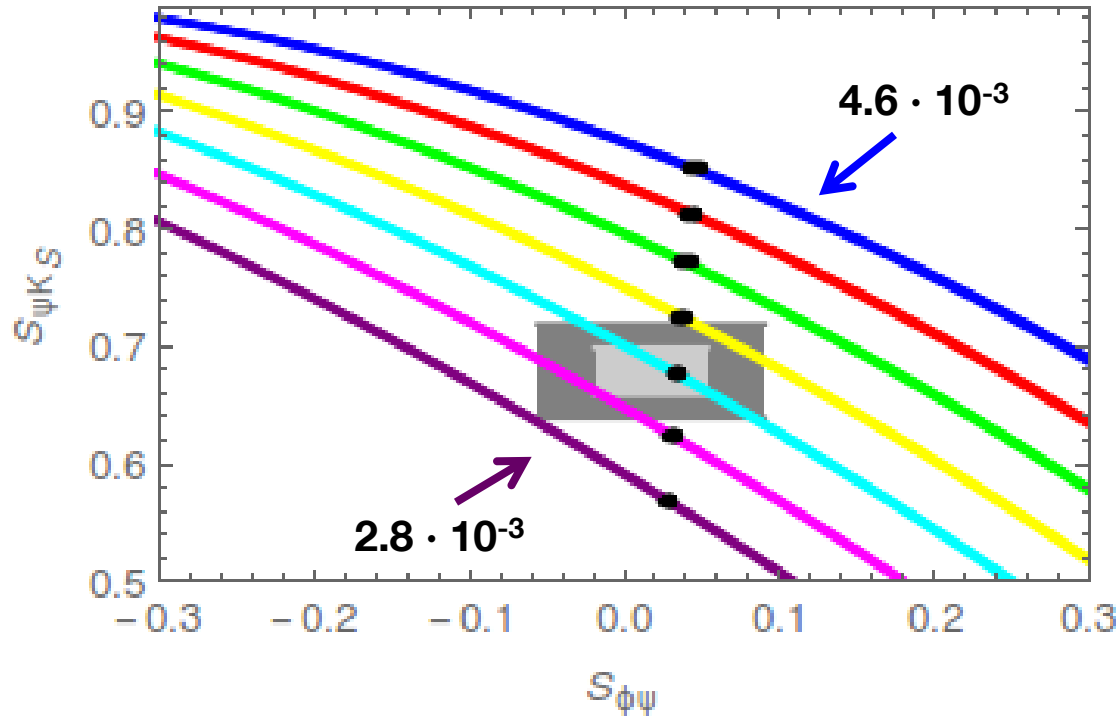
$$S_{\psi K_s} = \sin(2\beta + \phi_d^\Delta)$$

$$S_{\psi\phi} = \sin(2|\beta_s| - \phi_s^\Delta)$$

$$\phi_d^\Delta = \phi_s^\Delta$$

$S_{\psi K_S} - S_{\psi\phi} - |V_{ub}|$ Correlation in $U(2)^3$

Important test of $U(2)^3$ Models



Assuming absence of RH currents

In the $U(2)^3$ Symmetric World we could determine $|V_{ub}|$ without significant hadronic uncertainties (QCD penguins)

L and R Quark Couplings in Tree Level FCNCs

$\Delta F=2$

Cannot distinguish between L and R

(square)

$$\varepsilon_K, \Delta M_{s,d} \sim a g_L^2 + a g_R^2 + c g_L g_R$$

$|c| \gg |a|$
Hadronic matrix elements + RG

K: $c \sim 150 a$ **$B_{s,d}$:** $c \sim 7 a$

$\Delta F=1$

Can distinguish between L and R

L \rightarrow R

A

Decays governed by V-quark couplings (γ_μ)

: $K^+ \rightarrow \pi^+ \nu \bar{\nu}, K_L \rightarrow \pi^0 \nu \bar{\nu}, B \rightarrow K \nu \bar{\nu}$

No sign flip in NP contribution

B

Decays governed by A-quark couplings ($\gamma_\mu \gamma_5$)

: $K_L \rightarrow \mu^+ \mu^-, B_{s,d} \rightarrow \mu^+ \mu^-, B \rightarrow K^* \nu \bar{\nu}$

Sign flip in NP contribution

L \rightarrow R



Correlations A \leftrightarrow B
change to Anticorrelations A \leftrightarrow B

DNA - Charts

1306.3755

AJB + Girrbach



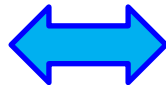
- **SM-like**



- **suppression relative to SM**



- **enhancement relative to SM**



correlation



anti-correlation

DNA - Charts

1306.3755

AJB + Girrbach



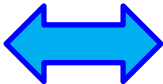
- SM-like



- suppression relative to SM



- enhancement relative to SM



correlation



anti-correlation



Searching for New Physics on the Way to Zeptouniverse

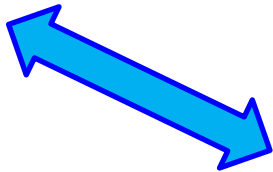
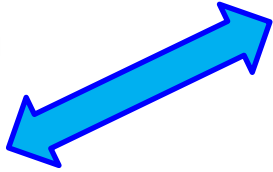


CMFV

ϵ_K

ΔM_s

ΔM_d



$S_{\psi\phi}$

$S_{\psi K_S}$

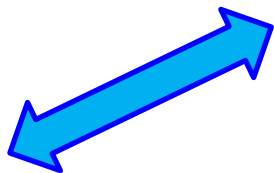
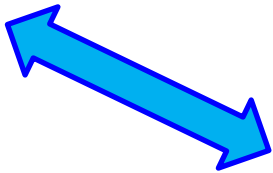
$B_s \rightarrow \mu\bar{\mu}$

$B_d \rightarrow \mu\bar{\mu}$



$K^+ \rightarrow \pi^+ \nu\bar{\nu}$

$K_L \rightarrow \pi^0 \nu\bar{\nu}$



$B \rightarrow K^{(*)} \nu\bar{\nu}$

$U(2)^3$

ϵ_K

ΔM_s



ΔM_d

$S_{\psi\phi}$



$S_{\psi K_s}$

$B_s \rightarrow \mu\bar{\mu}$



$B_d \rightarrow \mu\bar{\mu}$

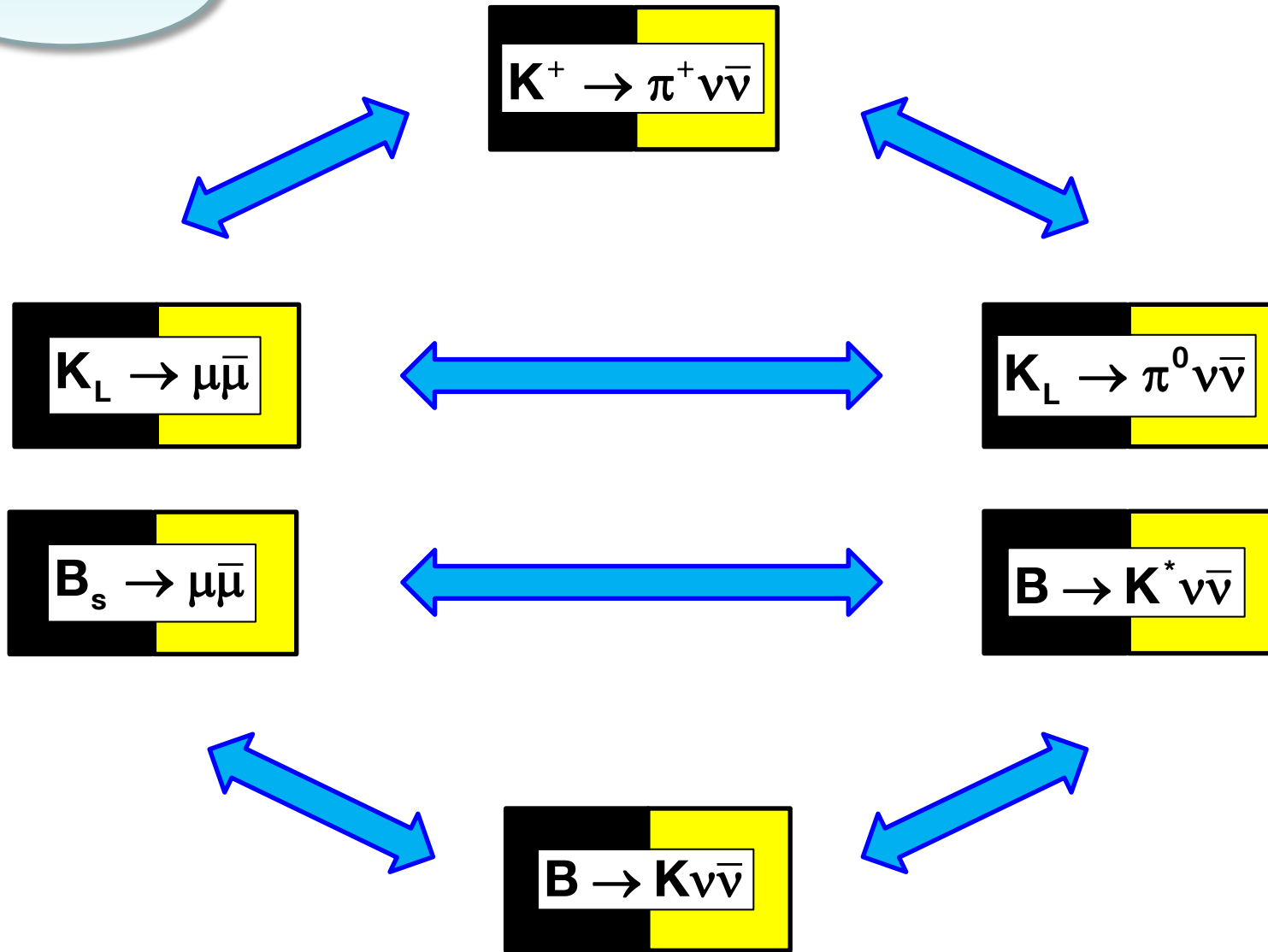
$K^+ \rightarrow \pi^+ \nu\bar{\nu}$



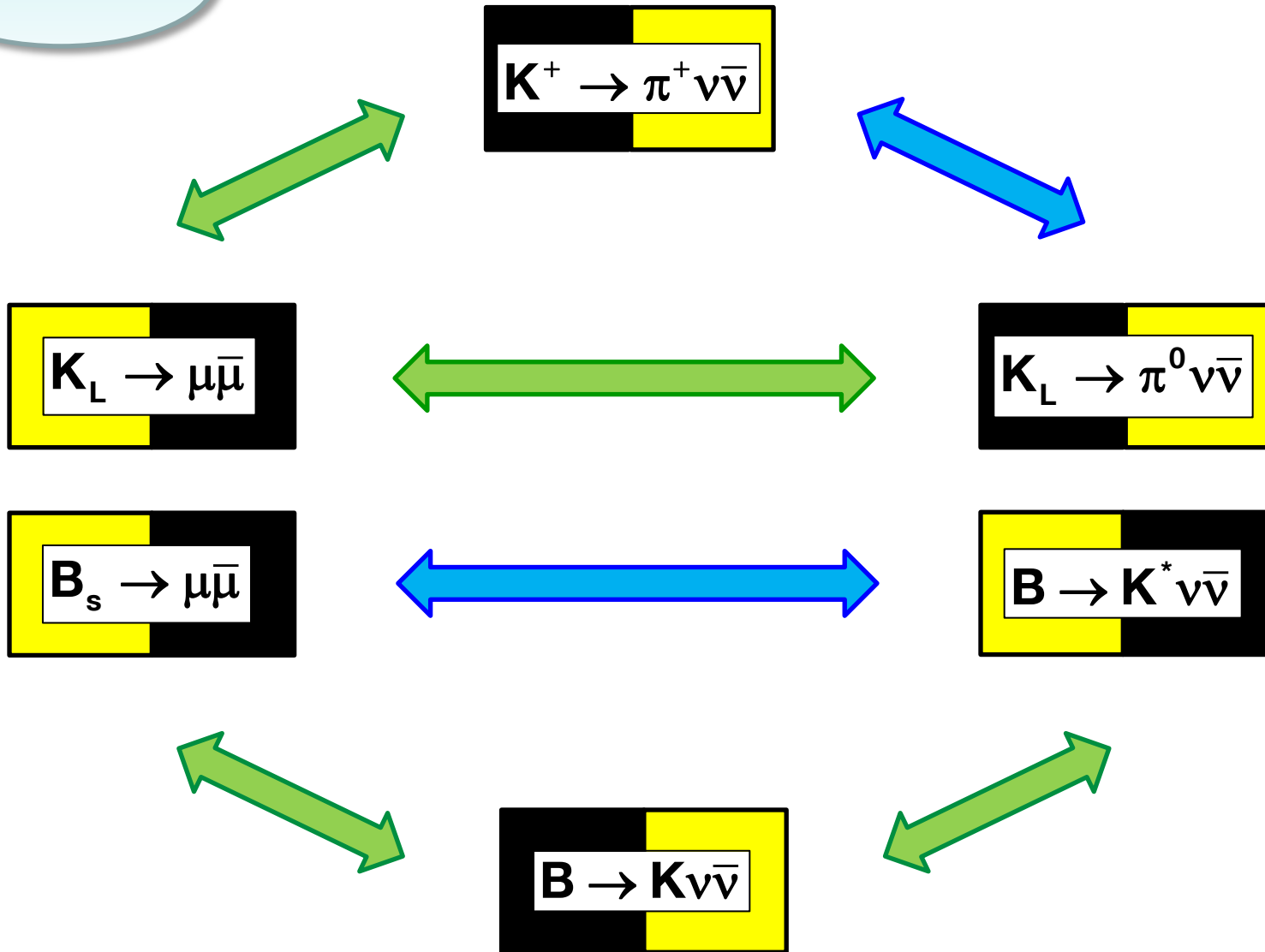
$K_L \rightarrow \pi^0 \nu\bar{\nu}$

$B \rightarrow K^{(*)} \nu\bar{\nu}$

Z'/Z LHS



Z'/Z RHS



3 Correlated Anomalies

(LHCb)

Matias et al
 Altmannshofer+Straub,
 Jäger et al
 Bobeth et al
 Hiller+Schmaltz
 Hurth et al

$$R_{K\mu\mu} = \frac{\text{Br}(B^+ \rightarrow K^+ \mu^+ \mu^-)^{[15,22]}}{\text{Br}(B^+ \rightarrow K^+ \mu^+ \mu^-)_{SM}^{[15,22]}} < 1$$

$$R_{K^*\mu\mu} = \frac{\text{Br}(B^0 \rightarrow K^{*0} \mu^+ \mu^-)^{[15,22]}}{\text{Br}(B^0 \rightarrow K^{*0} \mu^+ \mu^-)_{SM}^{[15,22]}} < 1$$

$$R_{\mu\mu} = \frac{\text{Br}(B_s \rightarrow \mu^+ \mu^-)}{\text{Br}(B_s \rightarrow \mu^+ \mu^-)_{SM}} < 1$$

Can be reproduced by Z or Z' with left-handed FCNC couplings.

$$C_9^{NP} \approx -C_{10}^{NP}$$

(V) (A) $\mu^+ \mu^-$

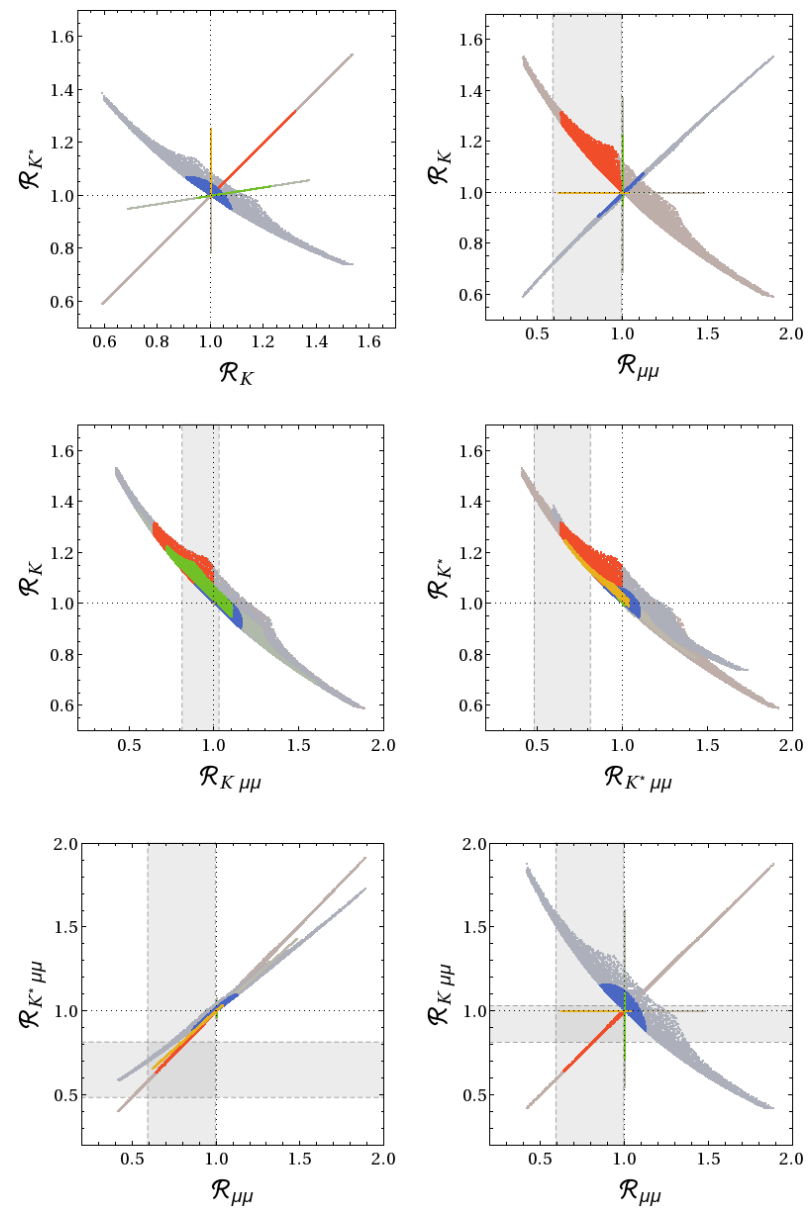
$$R_{K^*(K)} \equiv R_{K^*(K)\nu\bar{\nu}}$$

can distinguish between
 Z and Z' solution

$B \rightarrow K(K^*)\nu\bar{\nu}, B \rightarrow \mu^+\mu^-, B \rightarrow K(K^*)l^+l^-$

AJB
Girrbach-Noe
Niehoff
Straub

1409.4557

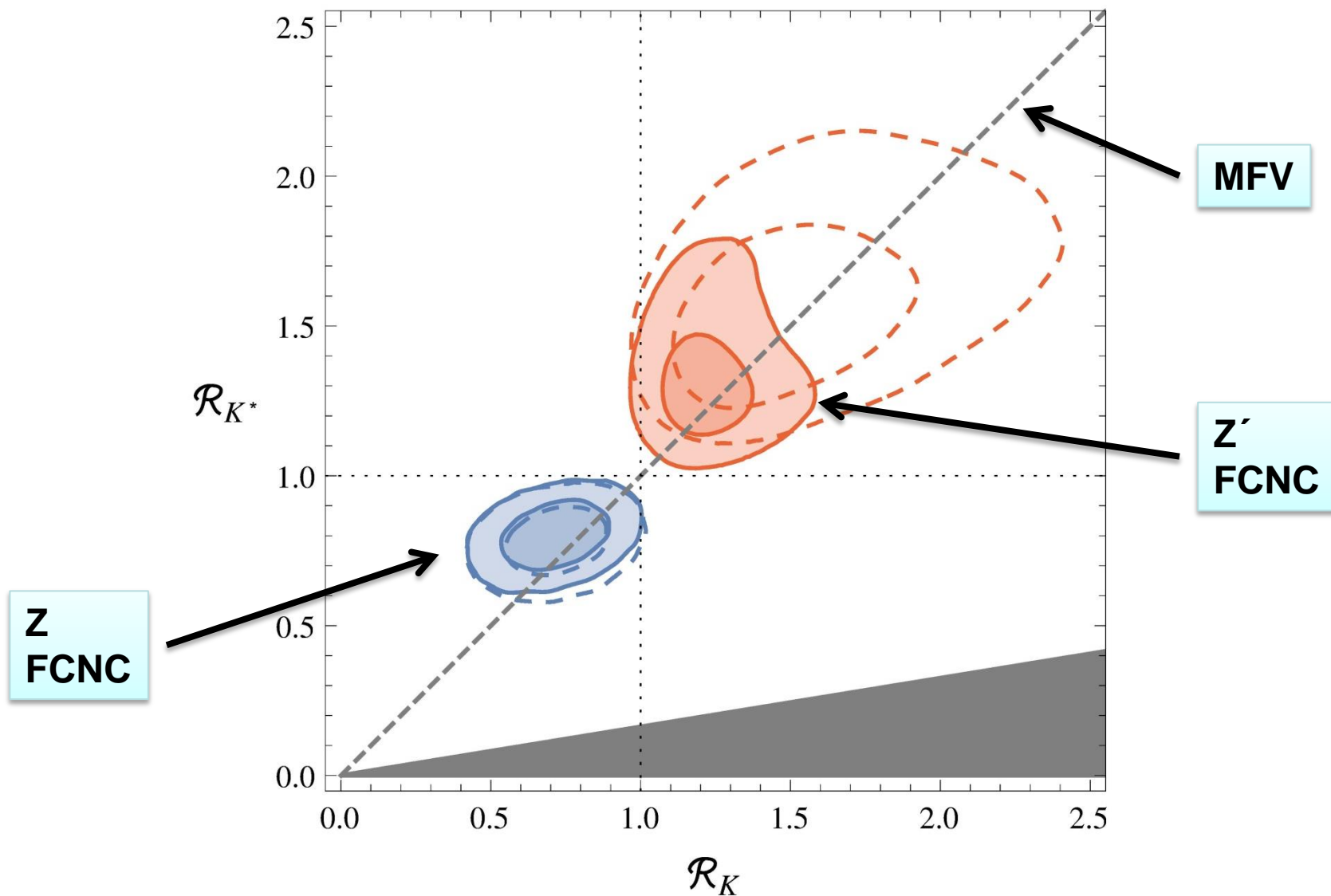


Z'

- LHS
- RHS
- LRS
- ALRS

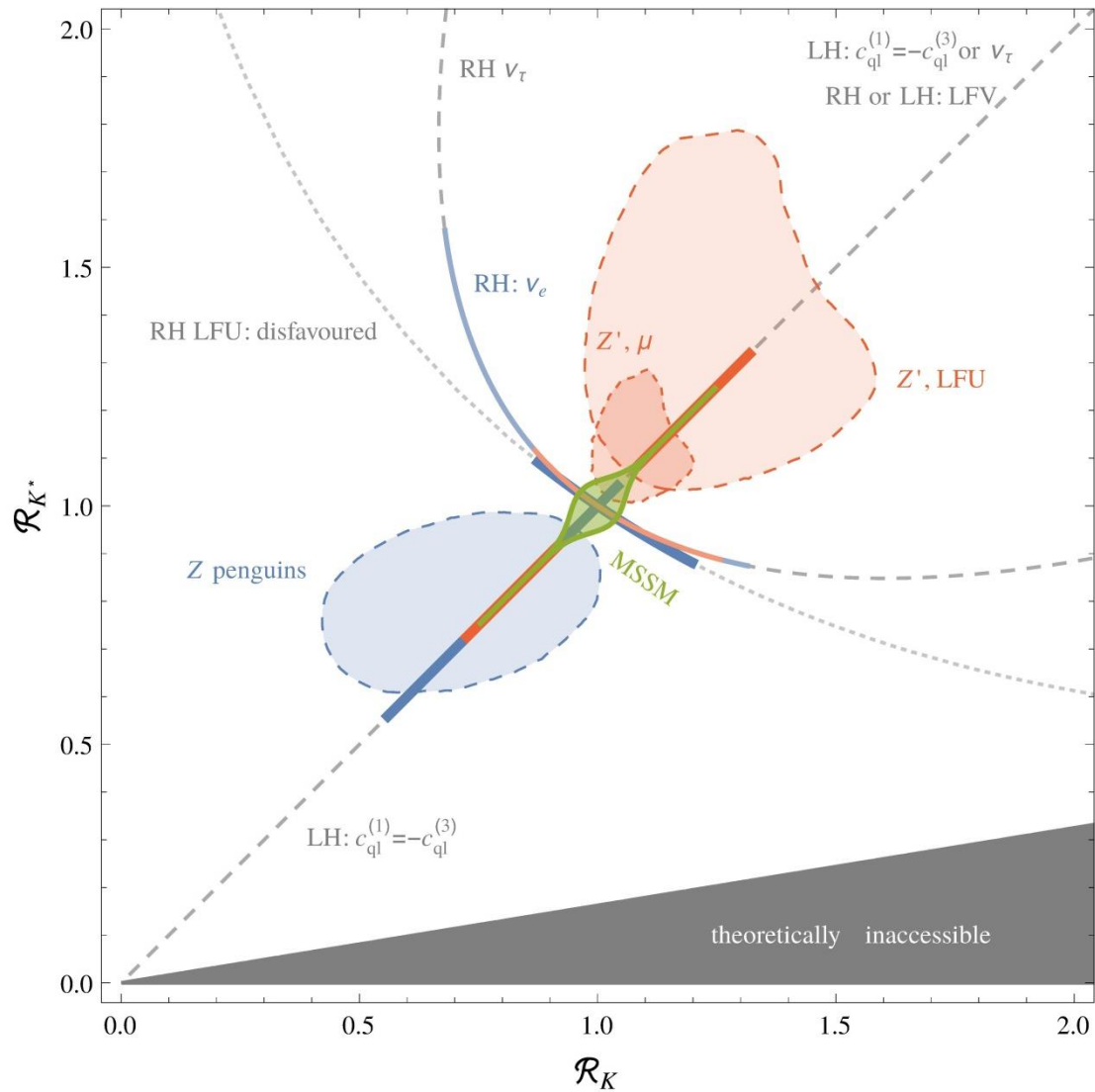
$$B \rightarrow K(K^*)\nu\bar{\nu}$$

BGNS 1409.4557



$B \rightarrow K(K^*)\nu\bar{\nu}$

BGNS 1409.4557



Can we reach Zeptouniverse through Quark Flavour Physics ?

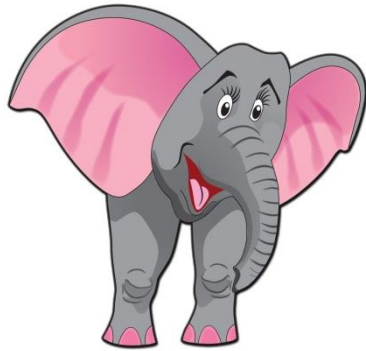
AJB, Buttazzo, Girrbach-Noe, Kneijens, 1407.0728

Due to limits of theory and experiment the answer depends on whether Zeptouniverse is “populated” by

Can we reach Zeptouniverse through Quark Flavour Physics ?

AJB, Buttazzo, Girrbach-Noe, Kneijens, 1407.0728

Due to limits of theory and experiment the answer depends on whether Zeptouniverse is “populated” by



In QFT :

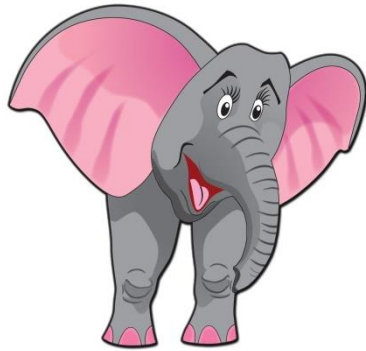
**Large
couplings**

**(still consistent
with perturbativity)**

Can we reach Zeptouniverse through Quark Flavour Physics ?

AJB, Buttazzo, Girrbach-Noe, Kneijens, 1407.0728

Due to limits of theory and experiment the answer depends on whether Zeptouniverse is “populated” by



In QFT :

**Large
couplings**

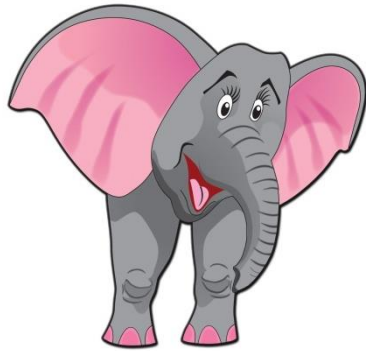
**Moderate
couplings**

**(still consistent
with perturbativity)**

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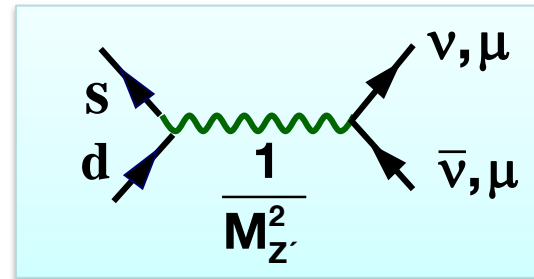
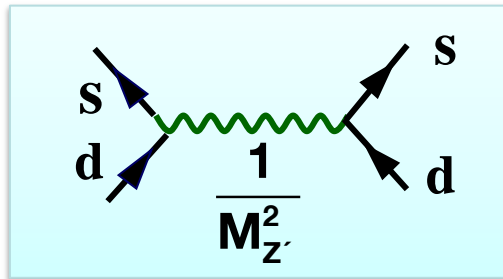
**Moderate
couplings**

**Small
couplings**

**(still consistent
with perturbativity)**

Answer within Z' -Models

(Stringent correlations between $\Delta F=2$ and $\Delta F=1$)



Similar
for B_s, B_d, D, \dots

For fixed lepton couplings, after $\Delta F=2$ constraints, NP effects in rare decays decrease as $1/M_{Z'}$.



Strategy:

Assume largest g_{ij} and $g_{\nu\nu}, g_{\mu\mu}$ couplings subject to $\Delta F=2$ constraints on g_{sd}, g_{sb}, g_{db}

$g_{ij} \approx 3$ still allowed by perturbativity
but often not by $\Delta F=2$ constraints.

NP effects should still be sufficiently large
to be able to see correlations.

Main Messages from this Study

(Maximal Resolution of Short Distance Scales)

1

If only g_L or g_R flavour changing Z' couplings to quarks present and $\Delta F=2$ constraints taken into account:

$K \rightarrow \pi \nu \bar{\nu} \sim 200 \text{ TeV}$

B_d physics: $\sim 15 \text{ TeV}$

B_s physics: $\sim 15 \text{ TeV}$

Maximal scales that can be explored

2

If $g_L = \pm g_R$ the scales are lower:
LR operator in $\Delta F=2$ enhanced through
RG + chiral enhancement in $\Delta M_K, \epsilon_K$



Smaller couplings



Lower scales at which NP dynamics can be tested

3

In order to probe scales above 50 TeV even with B_s, B_d physics we need either left-handed or right-handed elephants:

but

$g_L \neq g_R$ $g_R \neq 0$ $g_L \neq 0$
 $g_L \gg g_R$ or $g_R \gg g_L$

Cannot be distinguished through $\Delta F=2$ observables

Allows us to obtain significant NP effects in rare K, $B_{s,d}$ decays while satisfying $\Delta F=2$ constraints



(Help from LR operators with some tuning)

Important:

But:

Can be distinguished through correlations in rare K and B decays

(See DNA Charts)

Can we reach Zeptouniverse through Quark Flavour Physics ?

(Z)

AJB, Buttazzo, Girrbach-Noe, Kneegjens, 1407.0728

If only left-handed
or only right-handed
couplings present in NP

:

Only with K rare Decays
 $B_s \sim 15 \text{ TeV}$, $B_d \sim 15 \text{ TeV}$

If both LH and RH
present but
 $g_L^{ij} \ll g_R^{ij}$ or $g_L^{ij} \gg g_R^{ij}$

:

$K \rightarrow \pi \nu \bar{\nu}$: $\Lambda_{\text{NP}}^{\text{max}} \simeq 2000 \text{ TeV}$
 B_d : $\Lambda_{\text{NP}}^{\text{max}} \simeq 160 \text{ TeV}$
 B_s : $\Lambda_{\text{NP}}^{\text{max}} \simeq 160 \text{ TeV}$

Can we reach Zeptouniverse through Quark Flavour Physics ?

(Z)

AJB, Buttazzo, Girrbach-Noe, Kneegjens, 1407.0728

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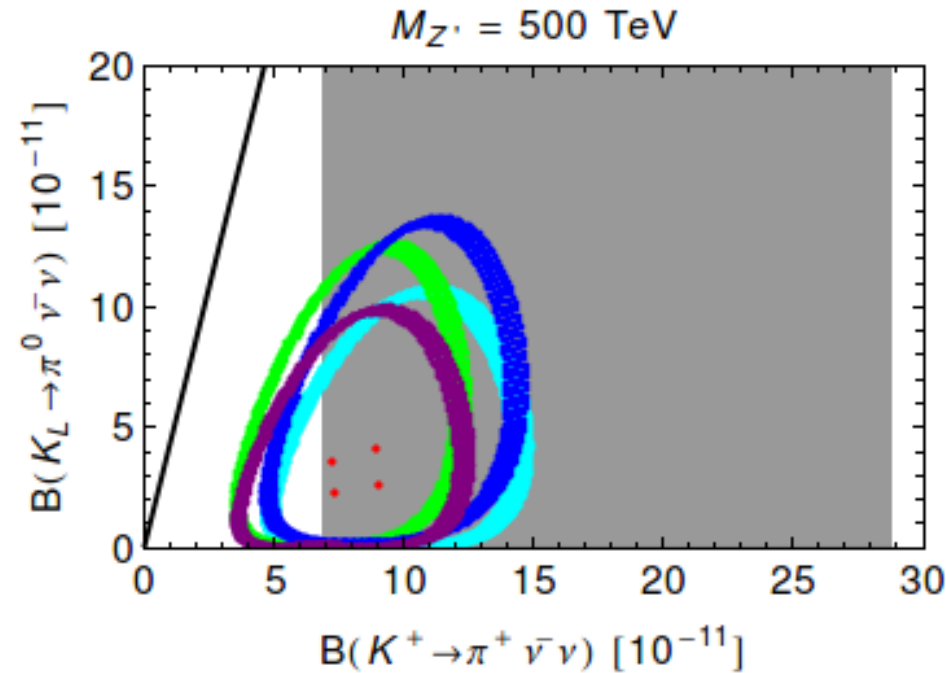
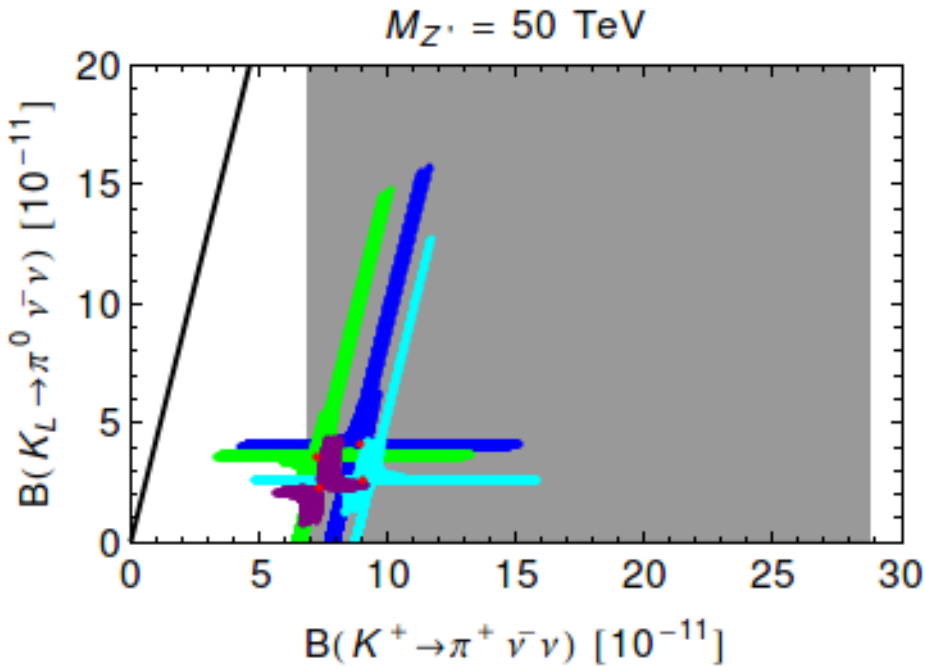
:

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 B_d : $\Lambda_{\text{NP}}^{\text{max}} \simeq 160 \text{ TeV}$
 B_s : $\Lambda_{\text{NP}}^{\text{max}} \simeq 160 \text{ TeV}$

Yes we can !!

Heavy Z' at Work

AJB, Buttazzo, Girschbach-Noe, Kneijens, 1407.0728

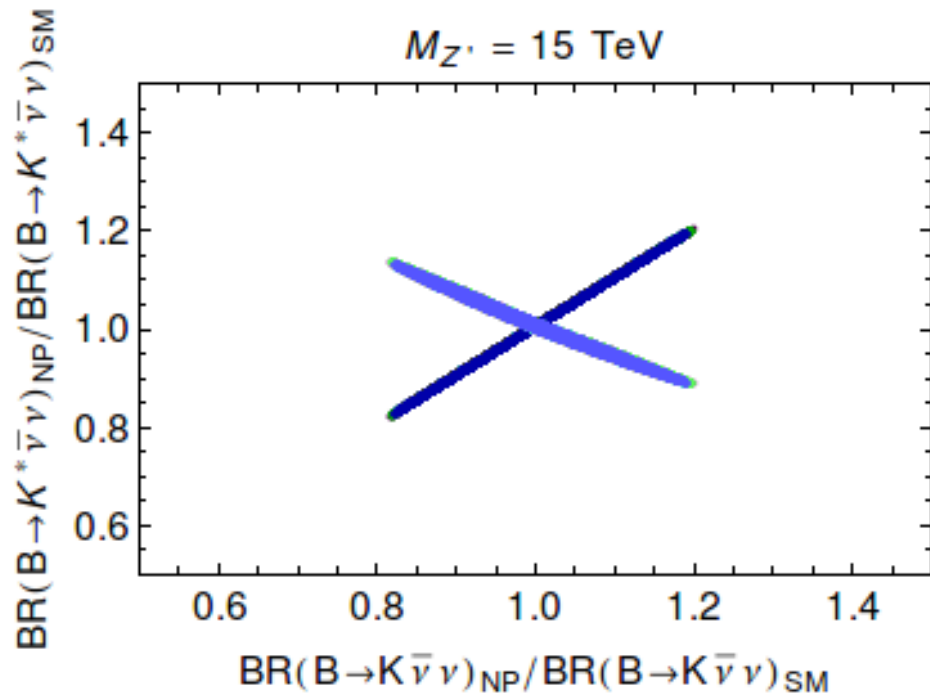


ϵ_K constraint

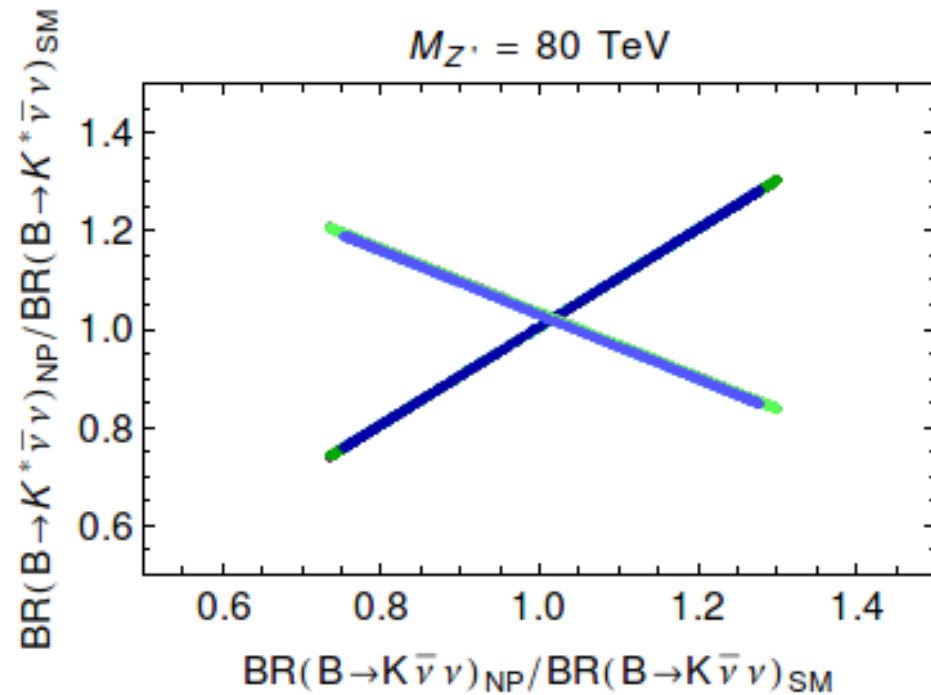
General discussion:
Blanke 0904.2528

No ϵ_K constraint

Heavy Z' at Work

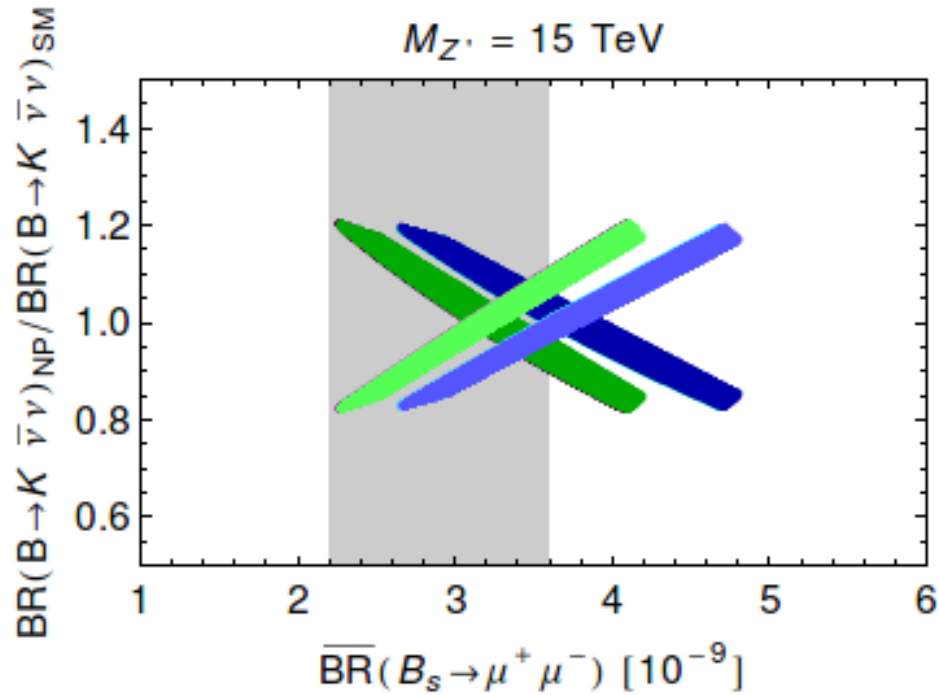


$\Delta F=2$ constraint

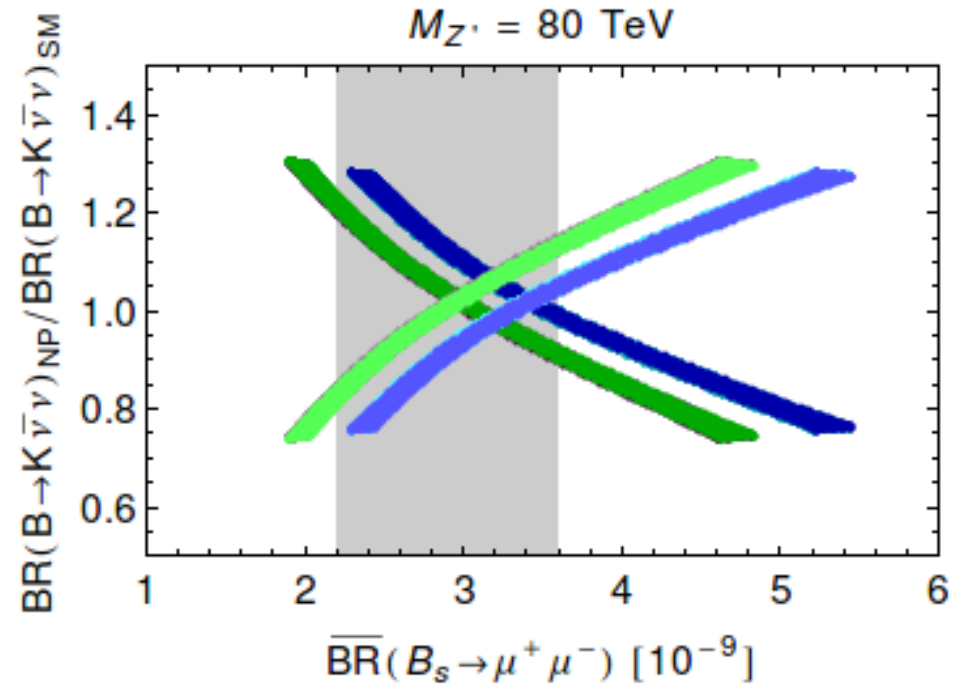


No $\Delta F=2$ constraint

Heavy Z' at Work



$\Delta F=2$ constraint



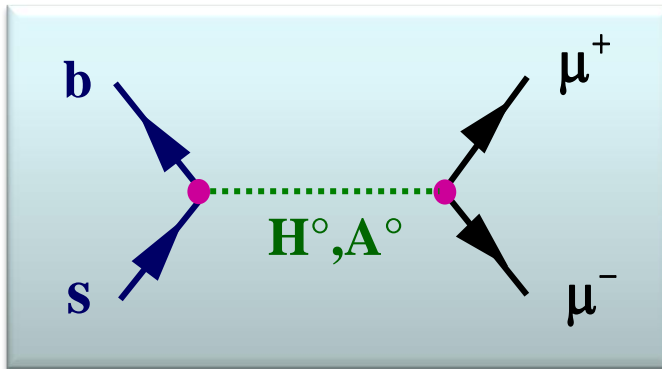
No $\Delta F=2$ constraint

Can we reach Zeptouniverse through S and P

AJB, Buttazzo, Girrbach-Noe, Kneijens, 1407.0728

Yes :

$$B_{s,d} \rightarrow \mu^+ \mu^-$$



S : ≈ 350 TeV

P : ≈ 700 TeV

Pseudoscalars more powerful than scalars because of the interference with SM contribution

Similar to $K \rightarrow \pi \nu \bar{\nu}$ (Z): No tuning necessary to reach Zeptouniverse

S= H^0

P= A^0

Finale: Vivace !

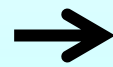
Finale: Vivace !

**We are approaching the
Happy End !!**

Main Message

Rare K, B_s, B_d Decays will play crucial role in identifying New Physics hopefully present on the route

Attouniverse



Zeptouniverse

Coming Years

: Flavour Precision Era

**LHC
Upgrade
E = 14 TeV
(CERN)**

**Precision
B_{d,s} – Meson
Decays
LHC
KEK (Japan)**

**$K^+ \rightarrow \pi^+ \nu \bar{\nu}$ ($\sim 10^{-10}$) (CERN)
 $K_L \rightarrow \pi^0 \nu \tilde{\nu}$ ($\sim 3 \cdot 10^{-11}$) J-PARC
(Japan)**

**Lepton Flavour
Violation**

$\mu \rightarrow e \gamma$
 $\mu \rightarrow e e e$

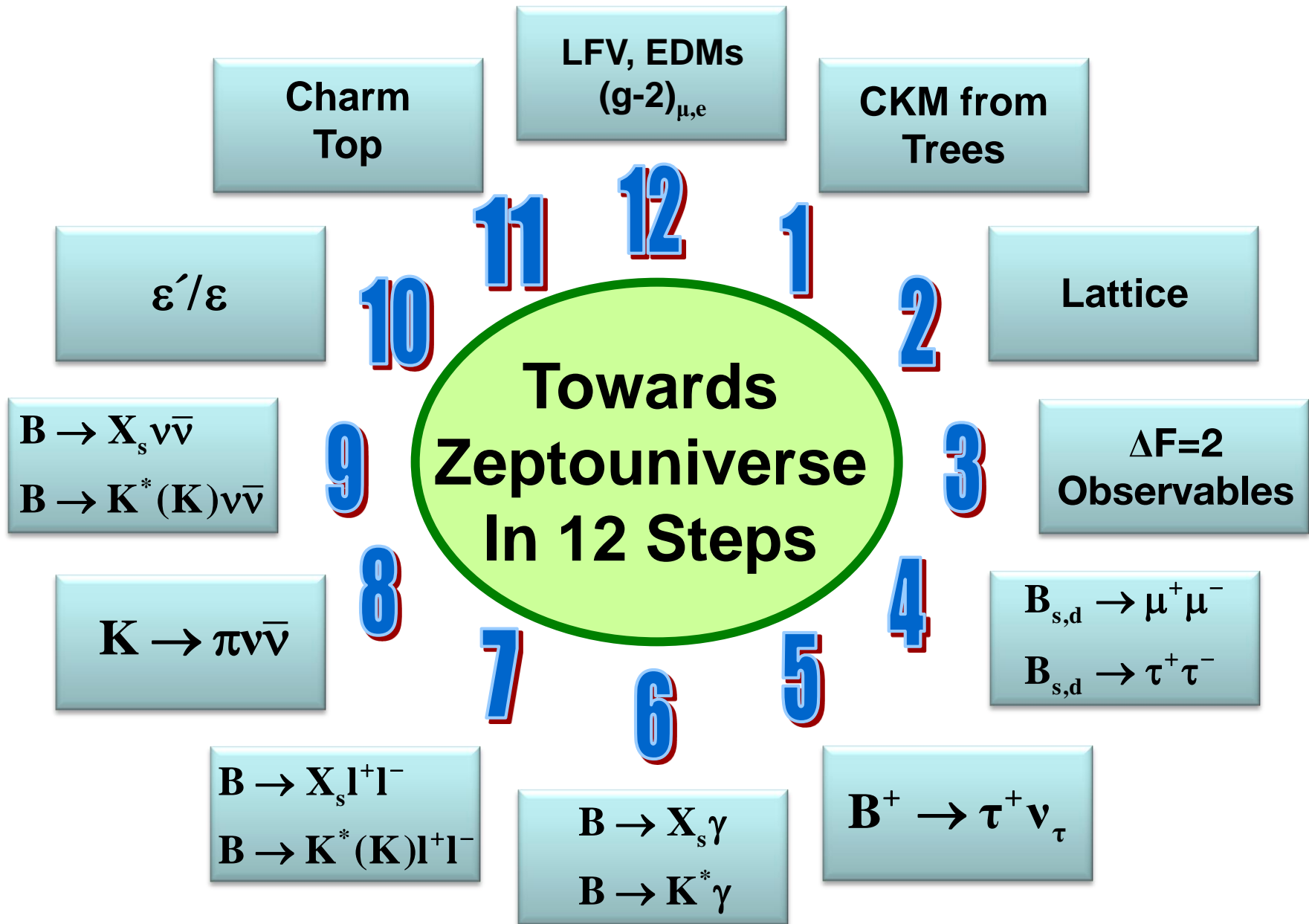
**Electric
Dipole
Moments**

$(g-2)_\mu$

**Improved
Lattice
Gauge Theory
Calculations**

Neutrinos

**Exciting Times are just
ahead of us !!!**



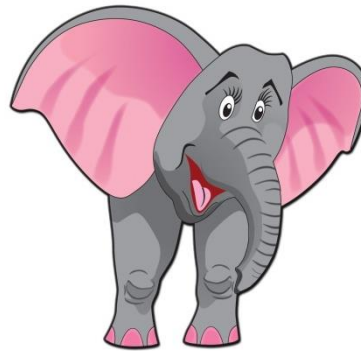
A Zeptouniverse Vision



Seen only in

$$K \rightarrow \pi \nu \bar{\nu}$$

$$B_{d,s} \rightarrow \mu^+ \mu^-$$

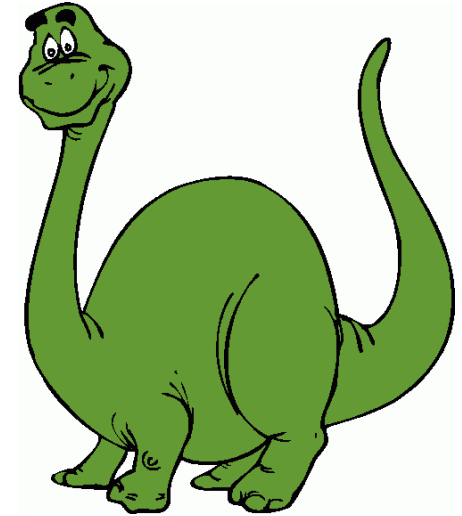


Seen in

$$\text{Rare } B_d$$

$$K \rightarrow \pi \nu \bar{\nu}$$

$$B_{d,s} \rightarrow \mu^+ \mu^-$$



Seen in

$$\text{Rare } B_s$$

$$\text{Rare } B_d$$

$$K \rightarrow \pi \nu \bar{\nu}$$

$$B_{d,s} \rightarrow \mu^+ \mu^-$$

Final Message

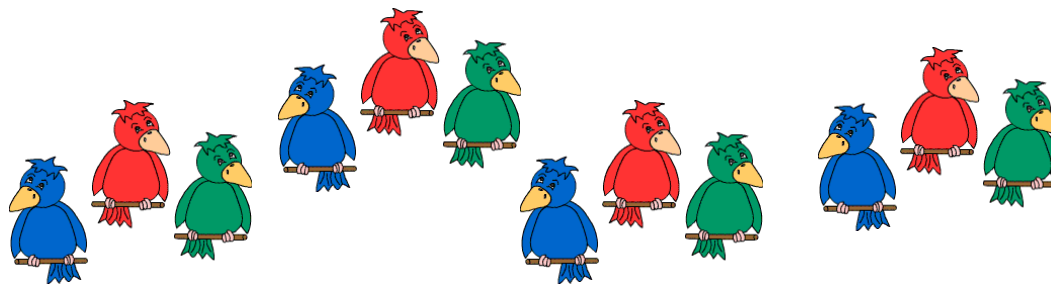
**Great hopes to
see many oases
on the way**

Attouniverse → Zeptouniverse

Final Message

**Great hopes to
see many oases
on the way**

**Attouniverse → Zeptouniverse
and**



at the LHC

Backup

Warning: $|V_{cb}|$ ($|V_{ts}|$) Dependence

BGHMSS

use

$$|V_{cb}|_{\text{incl}} \approx 42 \cdot 10^{-3}$$

$$\Rightarrow \bar{\text{Br}}(B_s \rightarrow \mu\bar{\mu})_{\text{SM}} = (3.65 \pm 0.23) \cdot 10^{-9} \\ (2.9 \pm 0.7) \cdot 10^{-9} \\ \text{(LHCb+CMS)}$$

But
for

$$|V_{cb}|_{\text{excl}} \approx 39 \cdot 10^{-3} \Rightarrow \bar{\text{Br}}(B_s \rightarrow \mu\bar{\mu})_{\text{SM}} \approx (3.1 \pm 0.2) \cdot 10^{-9}$$

Different
Route

(AJB 2003)
(Knegjens 2014)

$$\bar{\text{Br}}(B_s \rightarrow \mu\bar{\mu})_{\text{SM}} = (3.5 \pm 0.2) \cdot 10^{-9} \left[\frac{(\Delta M_s)^{\text{SM}}}{(\Delta M_s)^{\text{Data}}} \right] \left[\frac{1.33}{\hat{B}_s} \right]$$

(No V_{cb} , F_{B_s} dependence)

↑
Lattice

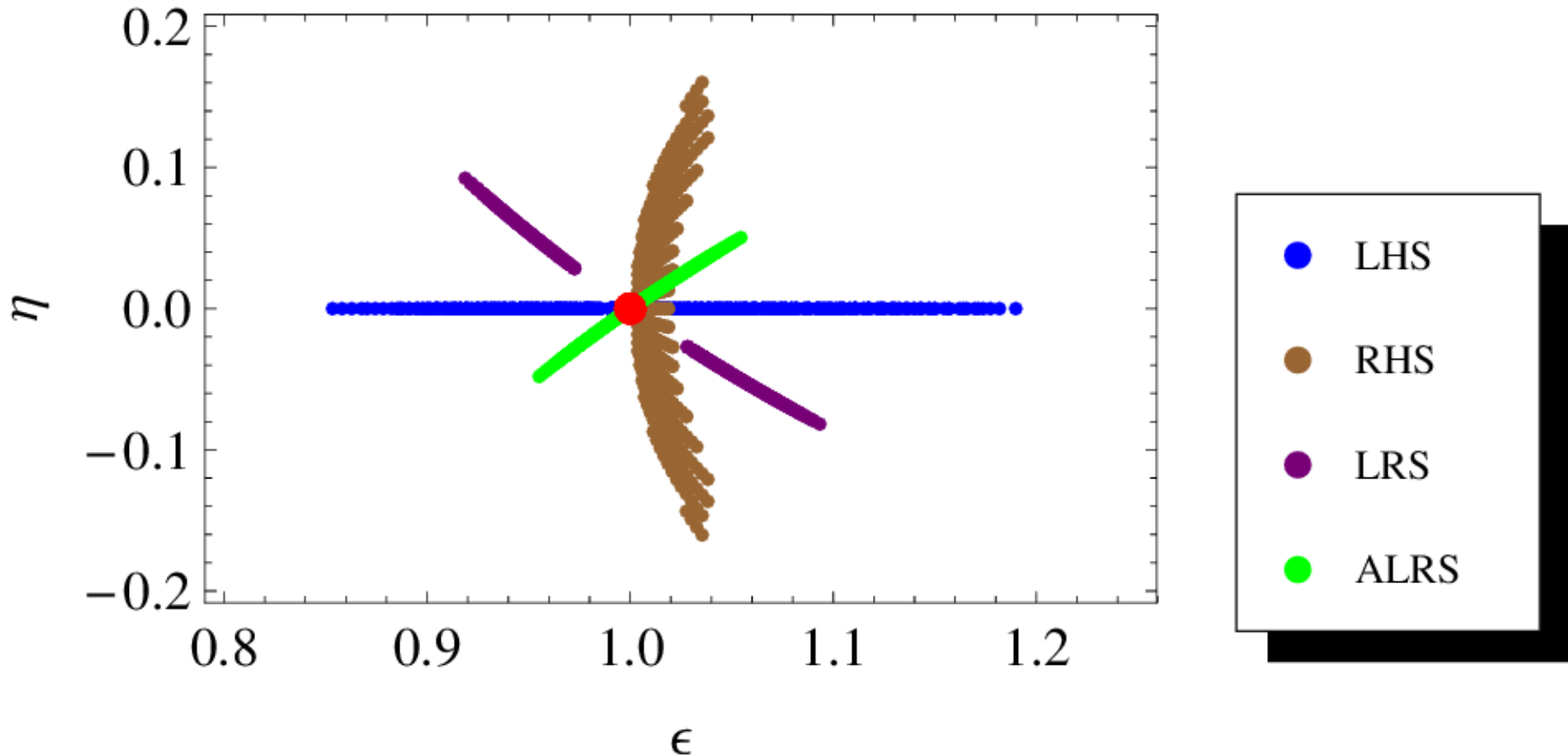
(ϵ, η) : Parameters for $b \rightarrow sv\bar{\nu}$ Transitions

$B \rightarrow K^* v\bar{\nu}$

$B \rightarrow K v\bar{\nu}$

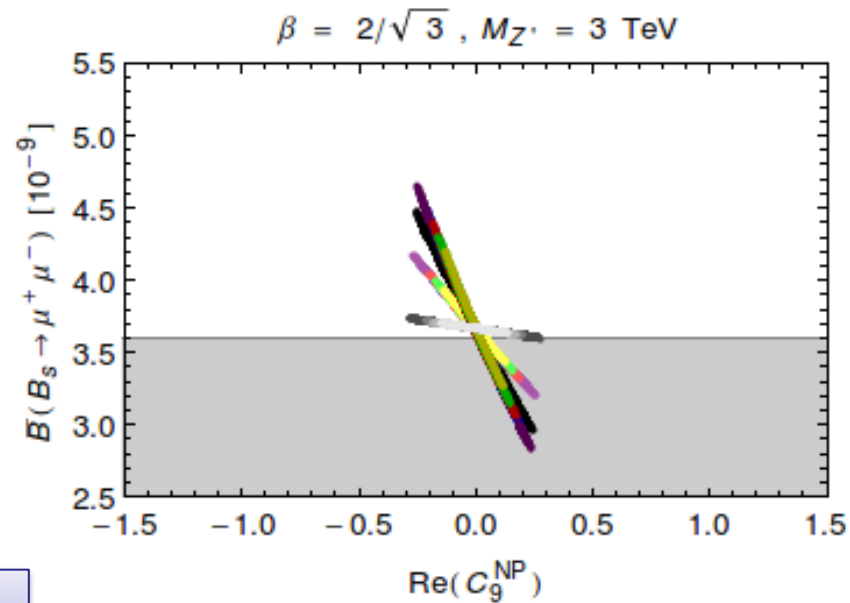
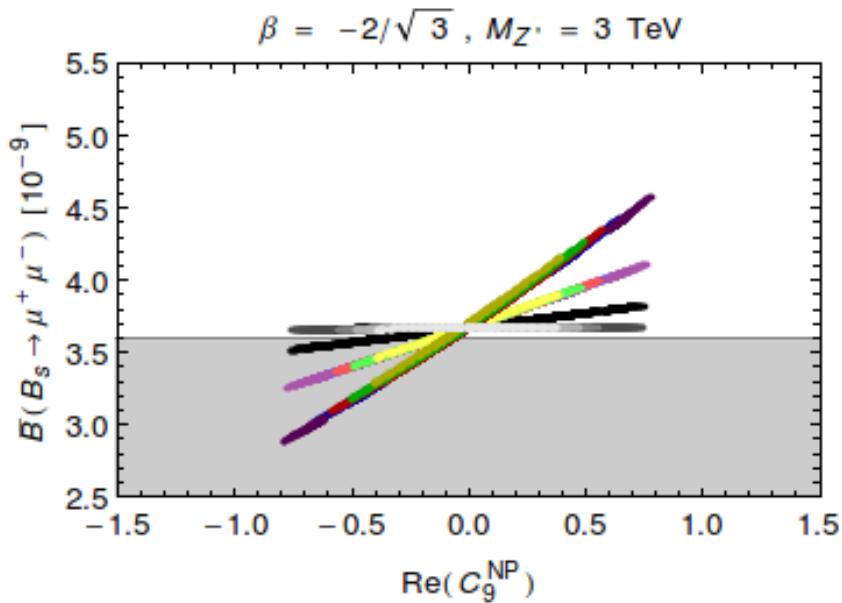
$B \rightarrow X_s v\bar{\nu}$

1211.1896

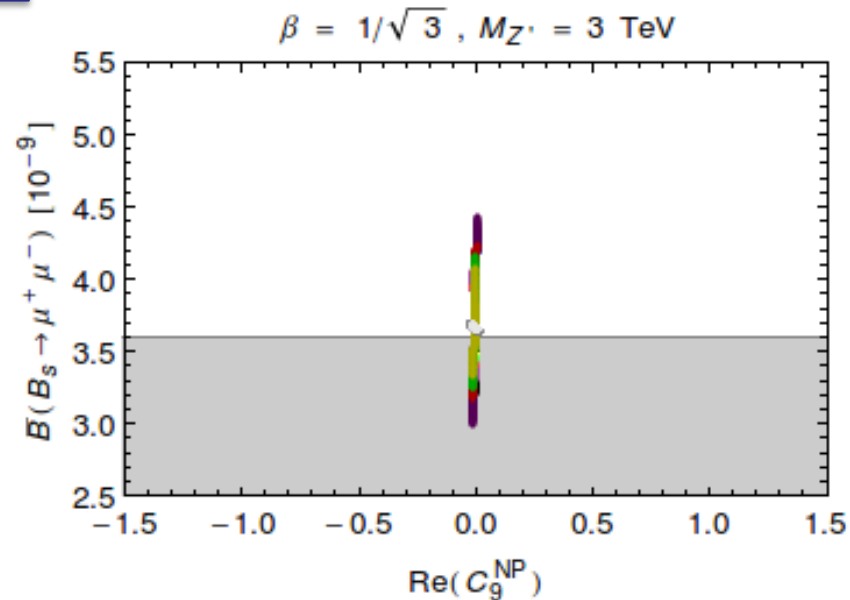
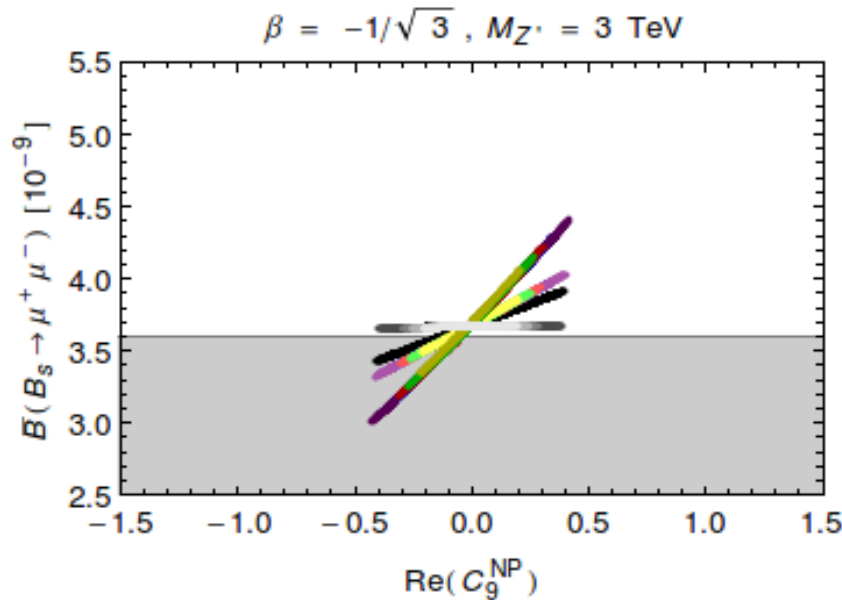


Powerful tests of
right-handed currents

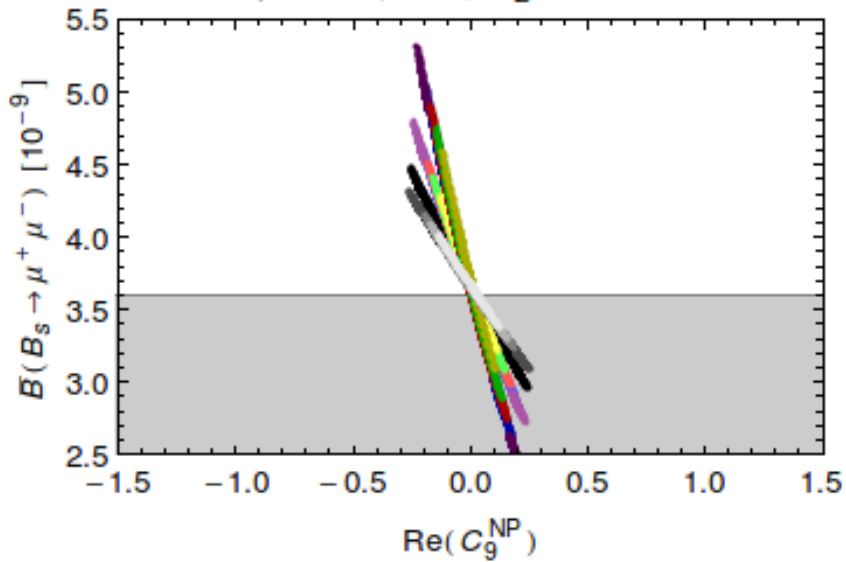
Altmannshofer, AJB, Straub, Wick
0902.0160



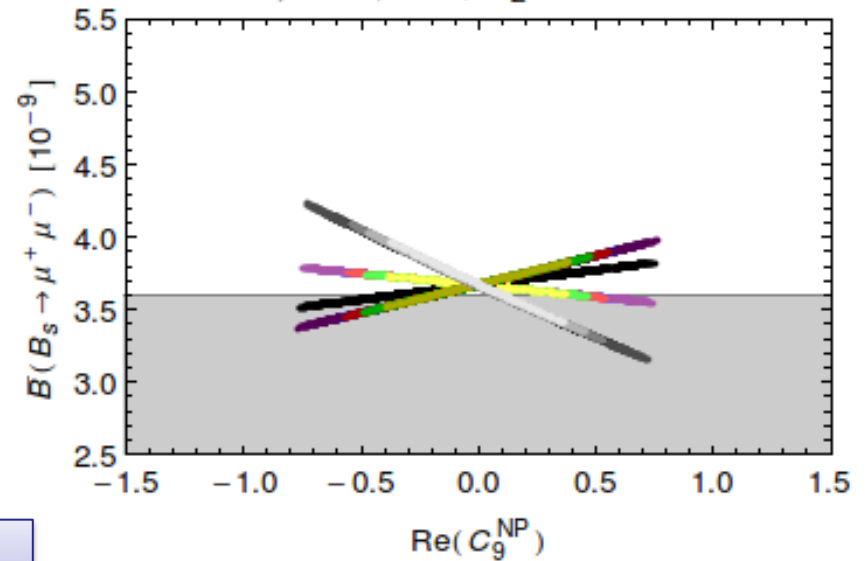
F₁



$\beta = -2/\sqrt{3}, M_{Z'} = 3 \text{ TeV}$

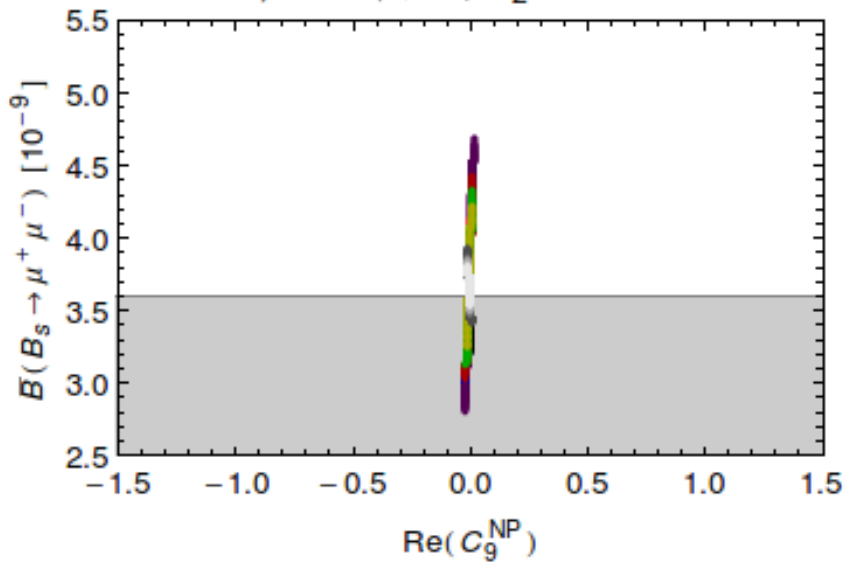


$\beta = 2/\sqrt{3}, M_{Z'} = 3 \text{ TeV}$

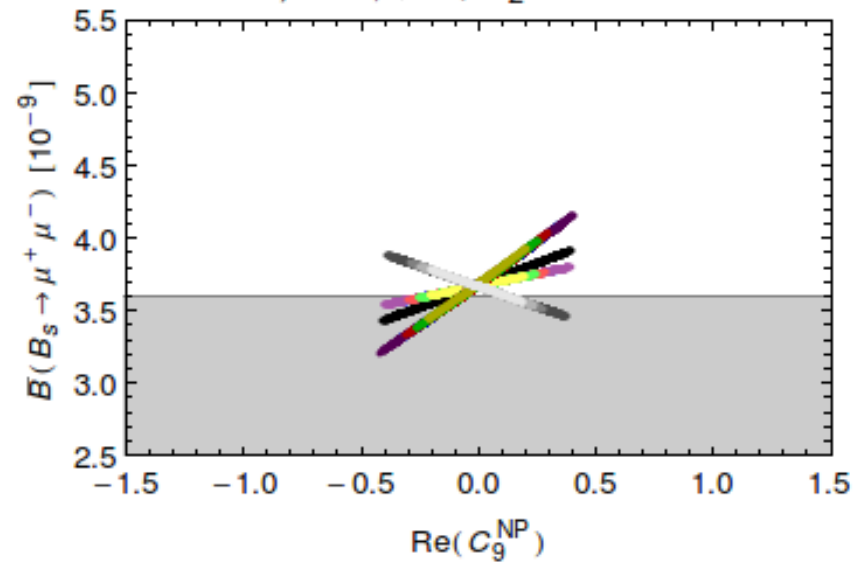


F₂

$\beta = -1/\sqrt{3}, M_{Z'} = 3 \text{ TeV}$



$\beta = 1/\sqrt{3}, M_{Z'} = 3 \text{ TeV}$



Effective Theory Approach

($\Delta F=2$)

$$H_{\text{eff}}(\Delta F = 2) = \underbrace{H_{\text{eff}}^{\text{SM}}(\Delta F = 2)}_{\text{Must be precisely known to identify NP}} + H_{\text{eff}}^{\text{NP}}(\Delta F = 2)$$

$$H_{\text{eff}}^{\text{NP}}(\Delta F = 2) = \sum_{ij} \frac{c_{ij}}{\Lambda_{\text{NP}}^2} \underbrace{Q_{ij}(\Delta F = 2)}_{\text{4-quark operators}}$$

Utfitters
Isidori, Nir, Perez

For $c_{ij} = 0(1)$ sensitivity to physics $\Lambda_{\text{NP}} > 1000 \text{ TeV}$ (LR operators)
($\varepsilon_K, \Delta M_K$)

But with the help of $\Delta F=2$ only it is not possible to learn with ET about the nature of the dynamics at Λ_{NP}

We need

$\Delta F=1$ transitions : Rare K, $B_{s,d}$, D decays



Effective Theory Approach

($\Delta F=1$)

$$H_{\text{eff}}(\Delta F = 1) = H_{\text{eff}}^{\text{SM}}(\Delta F = 1) + H_{\text{eff}}^{\text{NP}}(\Delta F = 1)$$

$$H_{\text{eff}}^{\text{NP}}(\Delta F = 1) = \sum_{ij} \frac{d_{ij}}{\Lambda_{\text{NP}}^2} Q_{ij}(\Delta F = 1)$$

Limitations
of ET :

- a) ET does not provide concrete relations between the c_{ij} ($\Delta F=2$) and d_{ij} ($\Delta F=1$) present in concrete models.

Impossible
to incorporate

Impact of $\Delta F=2$ transitions on
rare $K, B_{s,d}$ decays

Beyond
ET :

- b) ET does not provide relations between different coefficients in concrete models:

Example

331 Models

In models with Z' and Z FCNCs their contribution can interfere constructively and destructively implying very different results

AJB
De Fazio
Girrbach-Noe
1405.3850

R measurement

SM expectations: (S.Fajfer, J.Kamenik, I.Nisandzic, PRD 85, 094025 (2012))

$$R(D) = 0.297 \pm 0.017, R(D^*) = 0.252 \pm 0.003$$

BABAR SM deviations

- $R(\bar{D}^*)$ 2.7σ
- $R(\bar{D})$ 2.0σ
- $R(\bar{D}^{(*)})$ 3.4σ

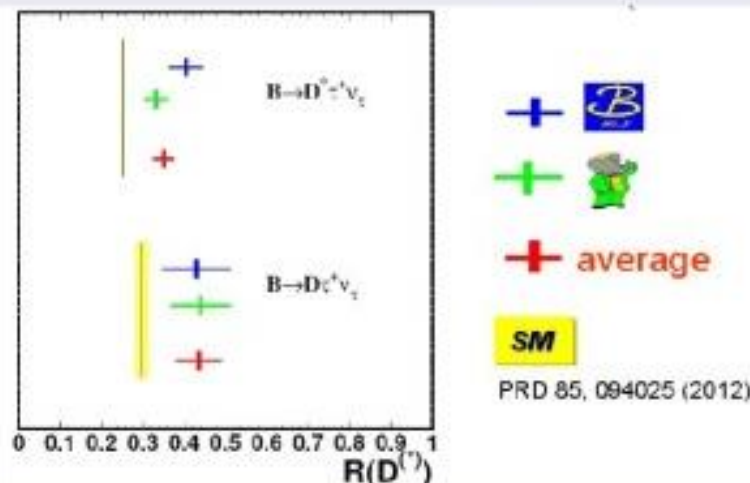
Belle average SM deviations

- $R(\bar{D}^*)$ 3.0σ
- $R(\bar{D})$ 1.4σ
- $R(\bar{D}^{(*)})$ 3.3σ

Observed deviations between observable and SM expectations for $R_{D^{(*)}}$ are not only due to improvement of experimental results but also reduction theoretical uncertainties.

LQCD expectations : A. Bailey, et al., Phys. Rev. Lett. 109, 071802, (2012), arXiv:1206.4992 [hep-ph].

$$R(D) = 0.316 \pm 0.012 \pm 0.007$$



Belle and BABAR average deviation from SM

- $R(\bar{D}^*)$ 3.8σ
- $R(\bar{D})$ 2.4σ
- $R(\bar{D}^{(*)})$ 4.8σ

Simple Tests in the Coming Years



Sign of $S_{\psi\phi}$



$$\frac{\text{Br}(\mathbf{B}_d \rightarrow \mu^+ \mu^-)}{\text{Br}(\mathbf{B}_s \rightarrow \mu^+ \mu^-)} = \frac{\tau(\mathbf{B}_d) m_{\mathbf{B}_d} F_{\mathbf{B}_d}^2}{\tau(\mathbf{B}_s) m_{\mathbf{B}_s} F_{\mathbf{B}_s}^2} \left| \frac{\mathbf{V}_{td}}{\mathbf{V}_{ts}} \right|^2$$



$$\frac{\text{Br}(\mathbf{B}_s \rightarrow \mu^+ \mu^-)}{\text{Br}(\mathbf{B}_d \rightarrow \mu^+ \mu^-)} = \frac{\hat{\mathbf{B}}_d \tau(\mathbf{B}_s) \Delta M_s}{\hat{\mathbf{B}}_s \tau(\mathbf{B}_d) \Delta M_d}$$



$$\text{Br}(\mathbf{K}^+ \rightarrow \pi^+ \nu \bar{\nu}); \quad \text{Br}(\mathbf{K}_L \rightarrow \pi^0 \nu \bar{\nu})$$



Lepton Flavour Violation

$$\mu \rightarrow e\gamma, \quad \mu \rightarrow 3e, \quad \tau \rightarrow 3\mu$$

$$\tau \rightarrow e\gamma, \quad \tau \rightarrow 3e$$

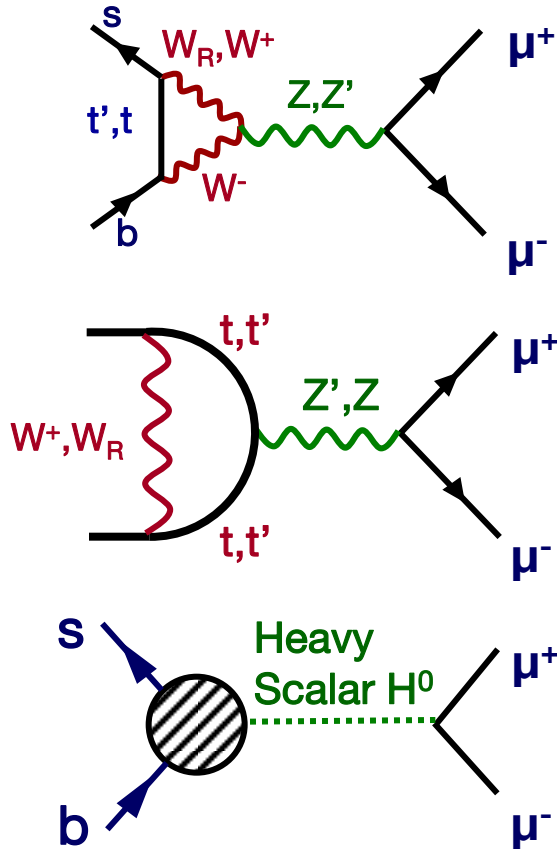
$$\tau \rightarrow \mu\gamma$$



ε'/ε provided QCD Penguin hadronic matrix under control

Standard
Candles
of
Flavour
Physics

$B_s \rightarrow \mu^+ \mu^-$ Beyond the Standard Model



Other Z-Penguins
and Boxes

$$\text{SM: } (3.2 \pm 0.2) \cdot 10^{-9}$$

Model Independent
Limit (95% C.L.)

$$\text{Br}(B_s \rightarrow \mu^+ \mu^-) < 5.6 \cdot 10^{-9}$$

Altmannshofer, Paradisi,
Straub 1111.1257

$$\frac{(\tan \beta)^6}{M_H^4}$$

in SUSY

$$\text{Br}(B_s \rightarrow \mu^+ \mu^-) < 11 \cdot 10^{-9}$$

In the case of

$$\text{Br}(B_s \rightarrow \mu^+ \mu^-) > 6 \cdot 10^{-9}$$

distinction between Z, Z' and H^0
possible

Minimal Effective Model with Right-Handed Currents

AJB, Gemmler, Isidori (1007.1993)

- Explains the difference $|V_{ub}|_{\text{excl}} \neq |V_{ub}|_{\text{incl}}$
- Softens $B^+ \rightarrow \tau^+ \nu_\tau$ problem (large V_{ub})

But with large $S_{\psi\phi}$ predicted: (2010)

Large $\text{Br}(B_s \rightarrow \mu^+ \mu^-)$, SM-like $\text{Br}(B_d \rightarrow \mu^+ \mu^-)$, too large $S_{\psi K_s}$

Impact of small $S_{\psi\phi}$ from LHCb (2012) (Relief !!)

SM-like $\text{Br}(B_s \rightarrow \mu^+ \mu^-)$, $\text{Br}(B_d \rightarrow \mu^+ \mu^-)$, $S_{\psi K_s}$ ok
can be large

$$\mathbf{K}^+ \rightarrow \pi^+ \nu \bar{\nu} \text{ and } \mathbf{K}_L \rightarrow \pi^0 \nu \bar{\nu} \quad (\mathbf{Z}^0\text{-penguins})$$

(TH cleanest FCNC decays in Quark Sector)

Extensive
TH efforts
over
20 years

- Buchalla, AJB; Misiak, Urban (NLO QCD)
- AJB, Gorbahn, Haisch, Nierste (NNLO QCD)
- Brod, Gorbahn, Stamou (QED, EW two loop)
- Isidori, Mescia, Smith (several LD analyses)
- Buchalla, Isidori (LD in $\mathbf{K}_L \rightarrow \pi^0 \nu \bar{\nu}$)

$$\frac{\text{Br}(\mathbf{K}^+ \rightarrow \pi^+ \nu \bar{\nu})}{\text{Br}(\mathbf{K}_L \rightarrow \pi^0 \nu \bar{\nu})} = 3.2 \pm 0.2$$

SM : $\text{Br}(\mathbf{K}^+ \rightarrow \pi^+ \nu \bar{\nu}) = (8.4 \pm 0.7) \cdot 10^{-11}$

$\text{Br}(\mathbf{K}_L \rightarrow \pi^0 \nu \bar{\nu}) = (2.6 \pm 0.4) \cdot 10^{-11}$

Exp : $\text{Br}(\mathbf{K}^+ \rightarrow \pi^+ \nu \bar{\nu}) = \left(17^{+11}_{-10} \right) \cdot 10^{-11}$

$\text{Br}(\mathbf{K}_L \rightarrow \pi^0 \nu \bar{\nu}) \leq 6.8 \cdot 10^{-8}$

(E787, E949 Brookhaven)

(E391a, KEK)

Future :

NA62
ORCA (FNAL)

Both very
sensitive to
New Physics

J-PARC KOTO

CP-conserving
TH uncertainty 2-3%

CP-Violation in Decay
TH uncertainty 1-2%

LHT after LHCb Data

**Our 2006
Predictions**
(Blanke et al.)

$\text{Br}(B_{s,d} \rightarrow \mu^+ \mu^-)$ within 40% from SM

$$|S_{\psi\phi}| \leq 0.25$$

$\{S_{\psi\phi} > 0.20\} \Rightarrow \left\{ \begin{array}{l} \text{No New Physics Effects} \\ \text{in } K^+ \rightarrow \pi^+ \nu \bar{\nu}, K_L \rightarrow \pi^0 \nu \bar{\nu} \end{array} \right\}$

**Concerning
B-Physics**

LHCb Data = Relief for LHT model *)

**Concerning
K-Physics**

**LHCb opened the road to large NP effects
in rare K-decays within LHT model** *)

*)

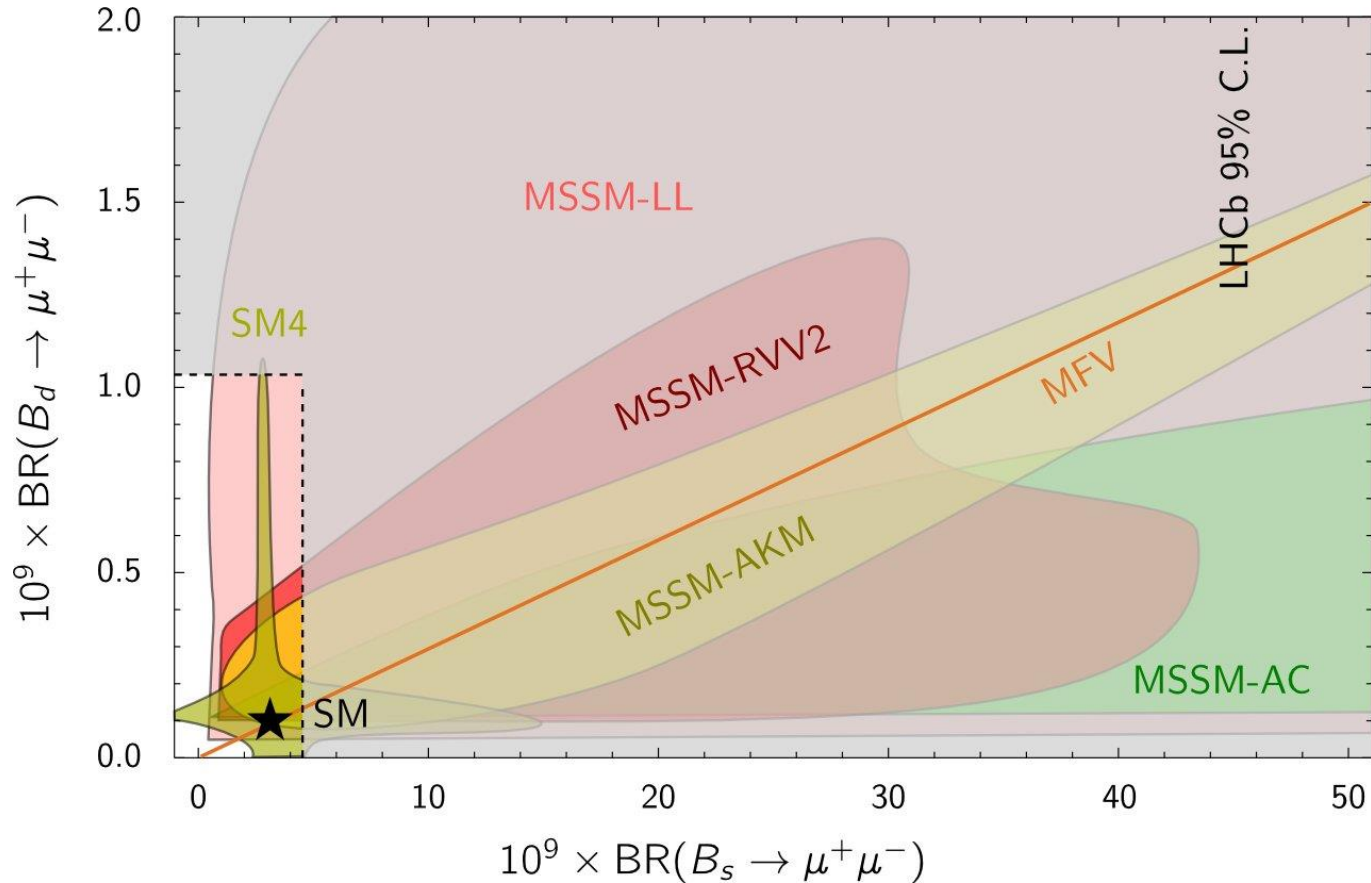
**The same impact of LHCb on Rare B
and K decays within RS_c model**

**Effects in
 $B_{s,d} \rightarrow \mu^+ \mu^-$
even smaller**

Supersymmetric Models Facing LHCb Data

ABGPS

Straub 1012.3893



Models with new left-handed currents favoured

Can $|V_{ub}|_{\text{excl}} \neq |V_{ub}|_{\text{incl}}$ be explained through right-handed currents?

Crivellin; Chen + Nam; Feger, Mannel et al.; AJB, Gemmler, Isidori

RHMFV

Works better with small $S_{\psi\phi}$

$$|V_{ub}|_{\text{excl}} = 3.12 (26) \cdot 10^{-3}$$

$$|V_{ub}|_{\text{incl}} = 4.27 (38) \cdot 10^{-3}$$

$$\varepsilon \approx \frac{v_L}{v_R}$$

$$|V_{ub}|_{\text{excl}} = |V_{ub}^L + a\varepsilon^2 V_{ub}^R|$$

$$|V_{ub}|_{\text{incl}} \approx |V_{ub}^L|$$

Generally: in principle yes

But a very detailed analysis of $SU(2)_L \otimes SU(2)_R \otimes U(1)_{B-L}$ with $g_L \neq g_R$; $V_L \neq V_R$ (mixing) including FCNC constraints + EWP constraints shows that in this concrete model the effect of RH currents too small !!

Blanke
AJB
Gemmler
Heidsieck
(1111.5014)

Comparison of Simplest Models

	$\Delta \varepsilon_K $	ΔM_d	ΔM_s	$\Delta S_{\psi K_s}$	$\Delta S_{\psi\phi}$	Favoured $ V_{ub} $
CMFV	+	+	+	0	0	exclusive
2HDM_{MFV}	0	\pm	\pm	-	+	inclusive
U(2)³	+	\pm	\pm	- 0 +	+ 0 -	inclusive exclusive

$$\left(\frac{\Delta M_s}{\Delta M_d}\right)_{\text{CMFV}} = \left(\frac{\Delta M_s}{\Delta M_d}\right)_{\text{MU(2)^3}} = \left(\frac{\Delta M_s}{\Delta M_d}\right)_{\text{SM}}$$

$$S_{\psi K_s} = \sin(2\beta + 2\varphi_{\text{new}})$$

$$S_{\psi\phi} = \sin(2|\beta_s| - 2\varphi_{\text{new}})$$

(the same relation for $B_{s,d} \rightarrow \mu^+\mu^-$)

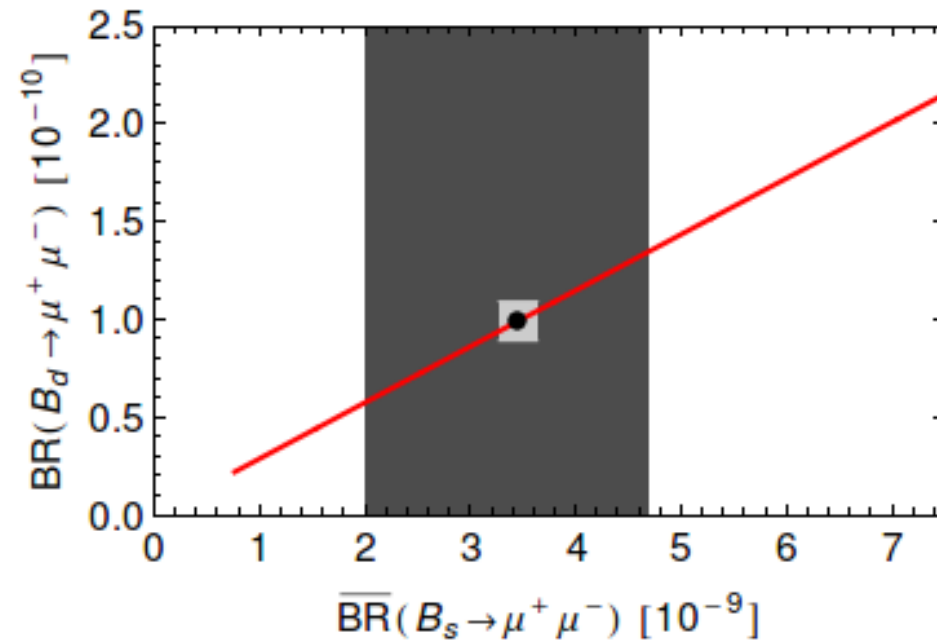
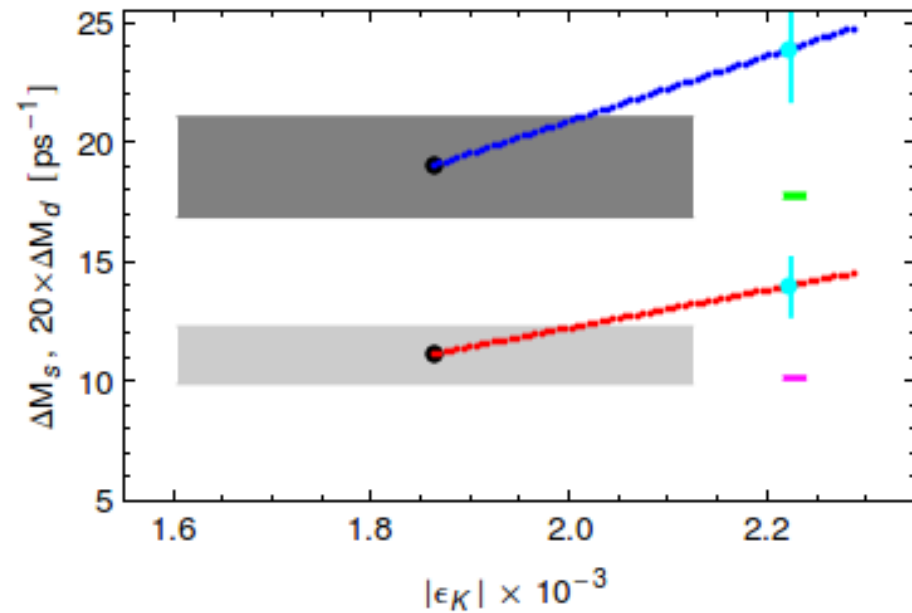
$$\beta = F(|V_{ub}|, \gamma)$$

(weak)

Constrained Minimal Flavour Violation

AJB + J. Girrbach (2012)

0007085
0310208
0604057



Tension within CMFV

EXP

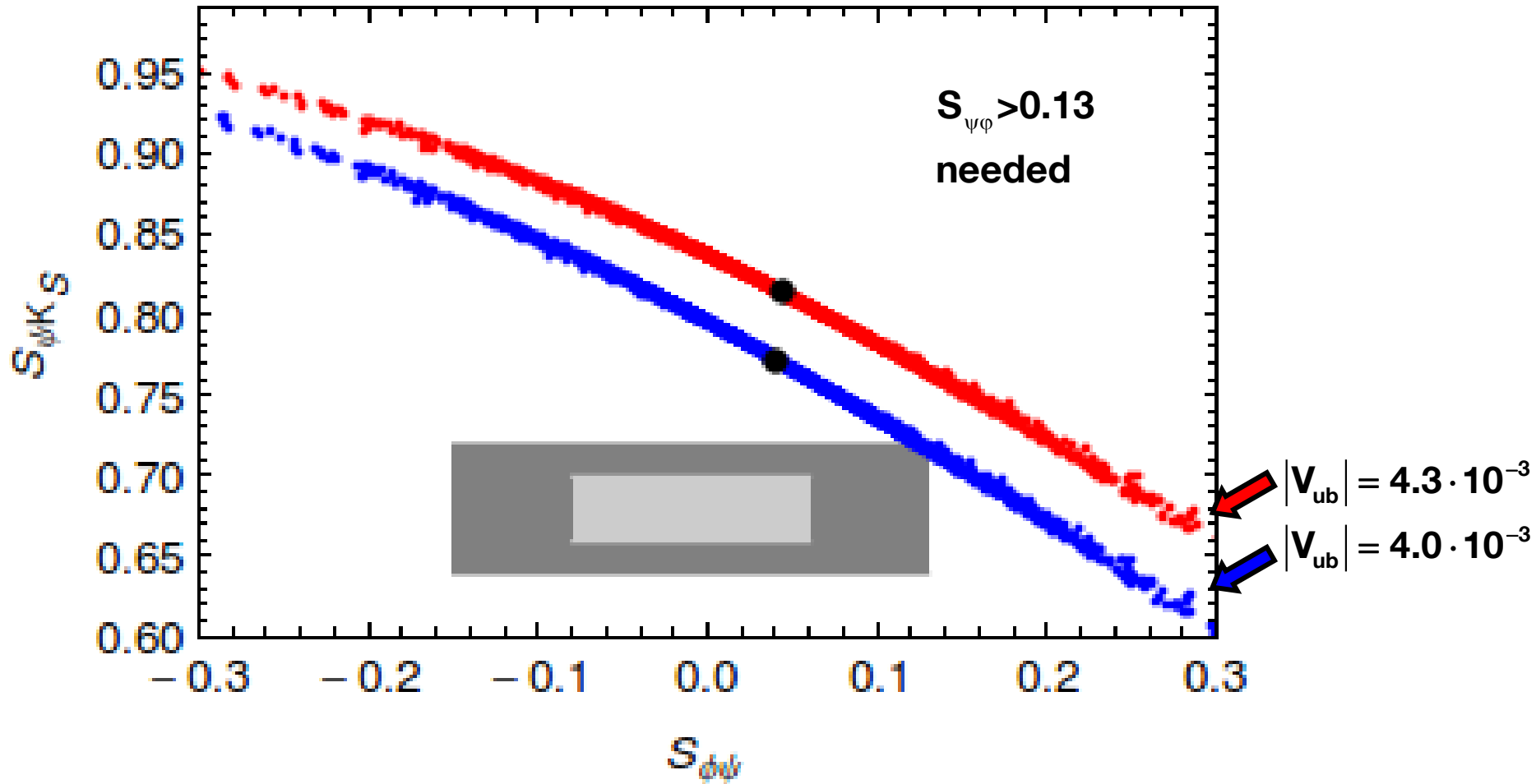
Similar tension in
Gauged Flavour Models:
AJB, Merlo, Stamou (2011)

EXP

$$\overline{Br}(B_s \rightarrow \mu^+ \mu^-) = \left(3.2^{+1.5}_{-1.2} \right) \cdot 10^{-9}$$

2HDM_{MFV} Facing LHCb Data

AJB, Girschbach, Nagai (2013)

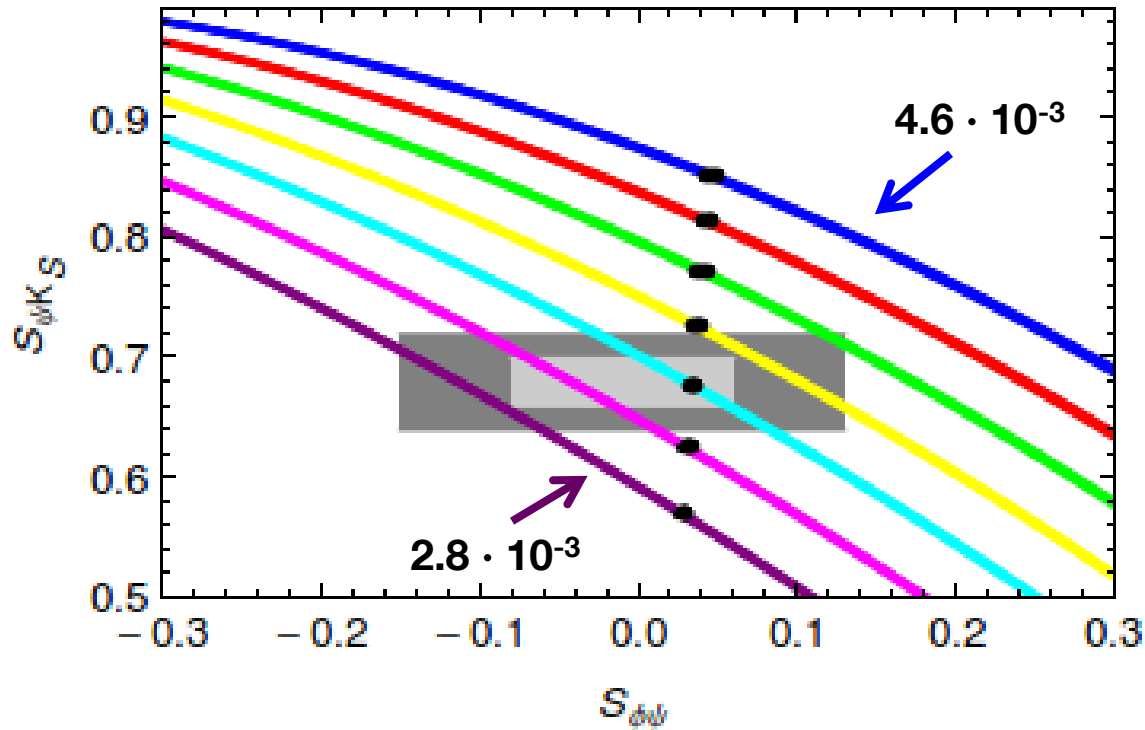


AJB, Carlucci, Gori, Isidori; 1005.5310

AJB, Isidori, Paradisi; 1007.5291

$S_{\psi K_S} - S_{\psi\phi} - |V_{ub}|$ Correlation in $U(2)^3$

Important test of $U(2)^3$ Models

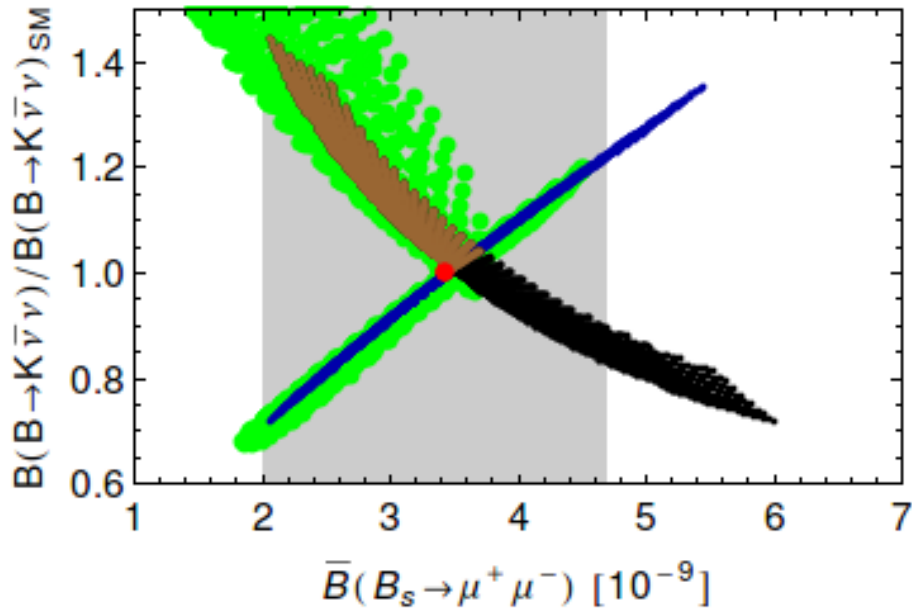


$\gamma = 68^\circ$

In the $U(2)^3$ Symmetric World we could determine $|V_{ub}|$ without significant hadronic uncertainties (QCD penguins)

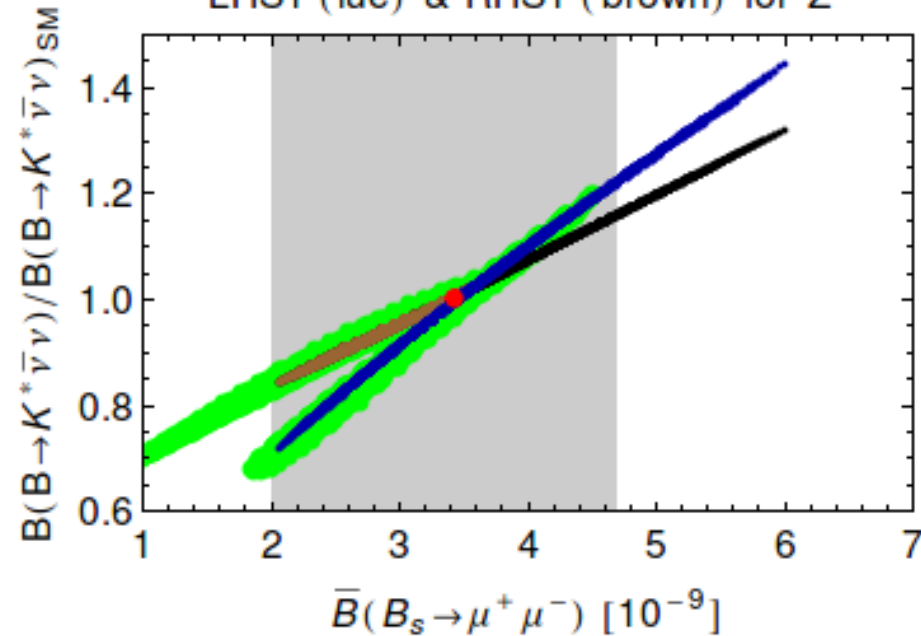
Distinguishing Left-Handed Currents from Right-Handed Currents

LHS1 (blue) & RHS1 (brown) for Z'



AJB, De Fazio, Girrbach
1211.1896

LHS1 (blue) & RHS1 (brown) for Z'



Altmannshofer et al.
0902.0160

■ : forbidden by
 $b \rightarrow sll$

■ : allowed by
 $b \rightarrow sll$

Z'-Couplings

$\bar{\Delta}_L^{sb}(\mathbf{Z}')$
complex

$\bar{\Delta}_A^{\mu\bar{\mu}}(\mathbf{Z}')$ $\bar{\Delta}_V^{\mu\bar{\mu}}(\mathbf{Z}')$
real

$\bar{\Delta}_L^{db}(\mathbf{Z}')$
complex

$\Delta M_s, S_{\psi\phi}$

×

$B_d \rightarrow K^* \mu^+ \mu^-$

×

×

×

$B_s \rightarrow \mu^+ \mu^-$

×

×

$B_d \rightarrow \mu^+ \mu^-$

×

×

$\Delta M_d, S_{\psi\phi}$

×

coupling

$$\bar{\Delta}_i = \frac{\Delta_i}{M_{Z'}}$$

reduced coupling

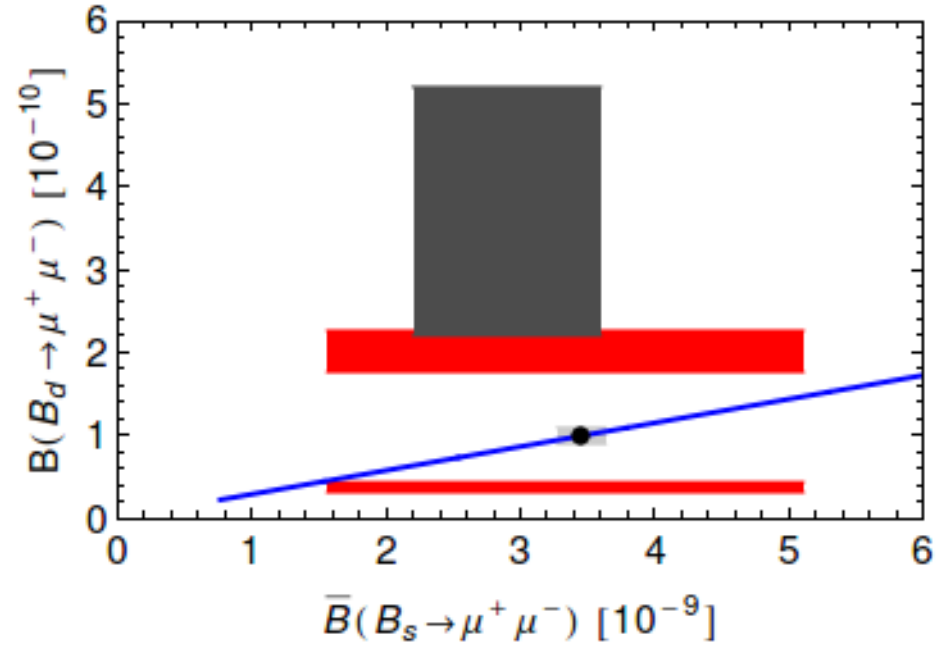
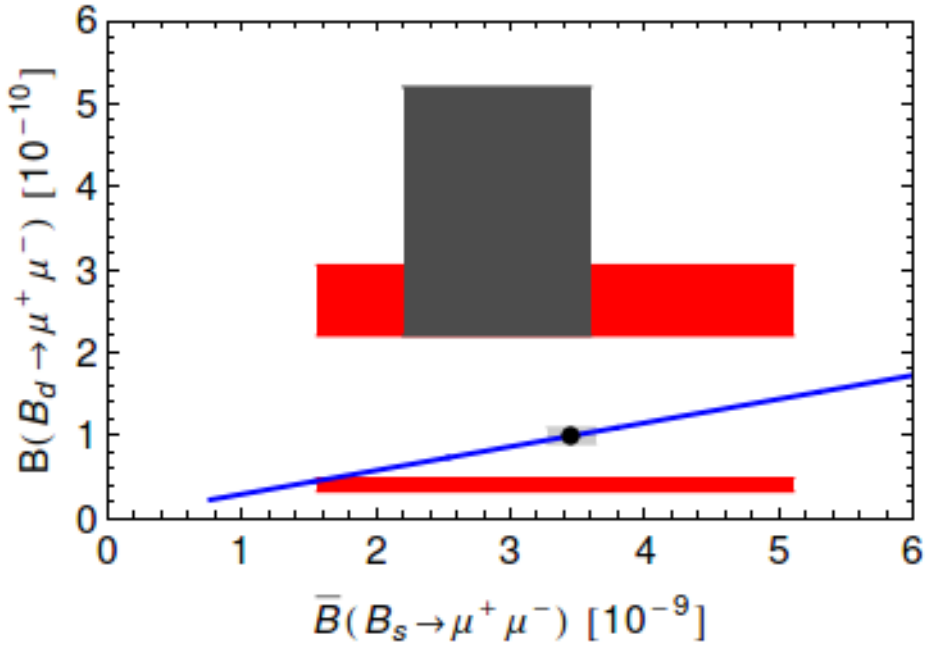
Z-Couplings $\Delta_{A,V}^{\mu\bar{\mu}}$ fixed

$$SU(2)_L : \Delta_L^{vv}(\mathbf{Z}') = \frac{\Delta_V^{\mu\bar{\mu}}(\mathbf{Z}') - \Delta_A^{\mu\bar{\mu}}(\mathbf{Z}')}{2} \rightarrow b \rightarrow sv\bar{v}$$

Violation of CMFV (Z)

High V_{ub}

Low V_{ub}



CMS + LHCb

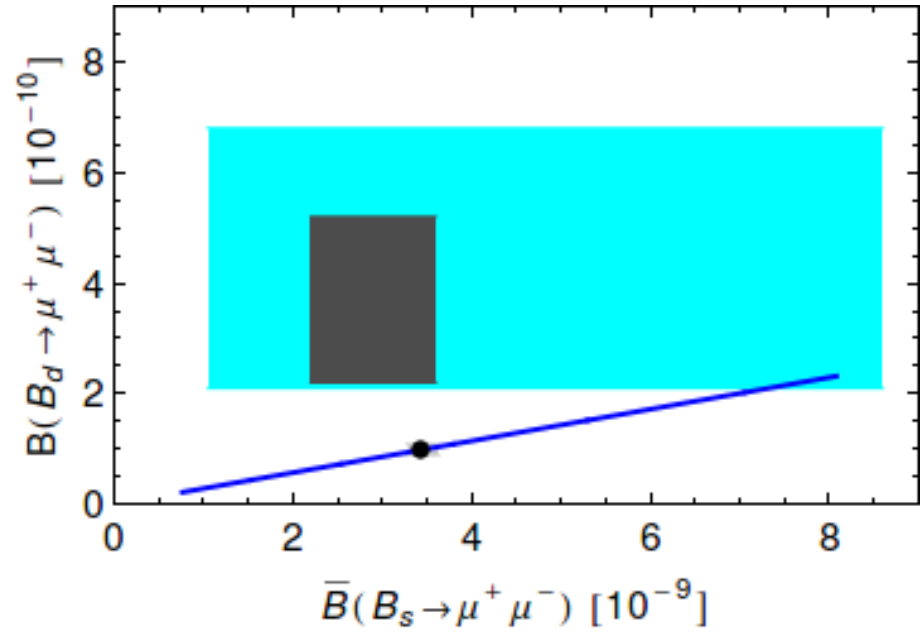
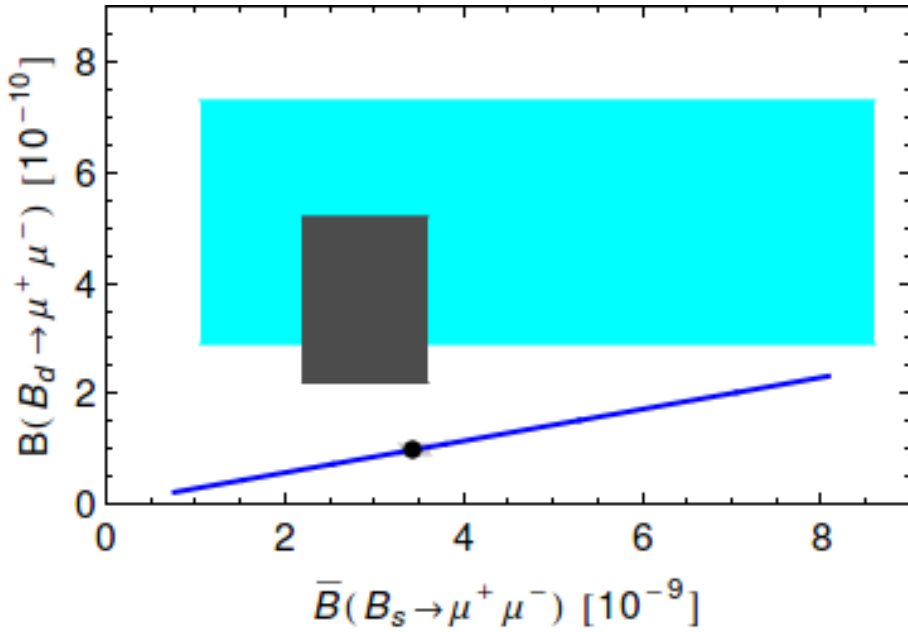


SM

Violation of CMFV (Z)

High V_{ub}

Low V_{ub}



CMS + LHCb



SM

Anomalies in $B_d \rightarrow K^* \mu^+ \mu^-$

(24 angular observables. Good agreement with SM but three deviations)

LHCb

SM

(Altmannshofer + Straub)

$$\langle \mathbf{F}_L \rangle_{[1.6]} = 0.66 \pm 0.07$$

$$0.77 \pm 0.04$$

$$\langle \mathbf{S}_5 \rangle_{[1.6]} = 0.10 \pm 0.10$$

$$-0.14 \pm 0.02$$

$$\langle \mathbf{S}_4 \rangle_{[14,16]} = -0.07 \pm 0.11$$

$$0.29 \pm 0.07$$

(Not understood in any model)

Extensive Analyses:

Descotes-Genon, Matias, Virto (1307.5683)

Altmannshofer + Straub (1308.1501)



DMV
AS

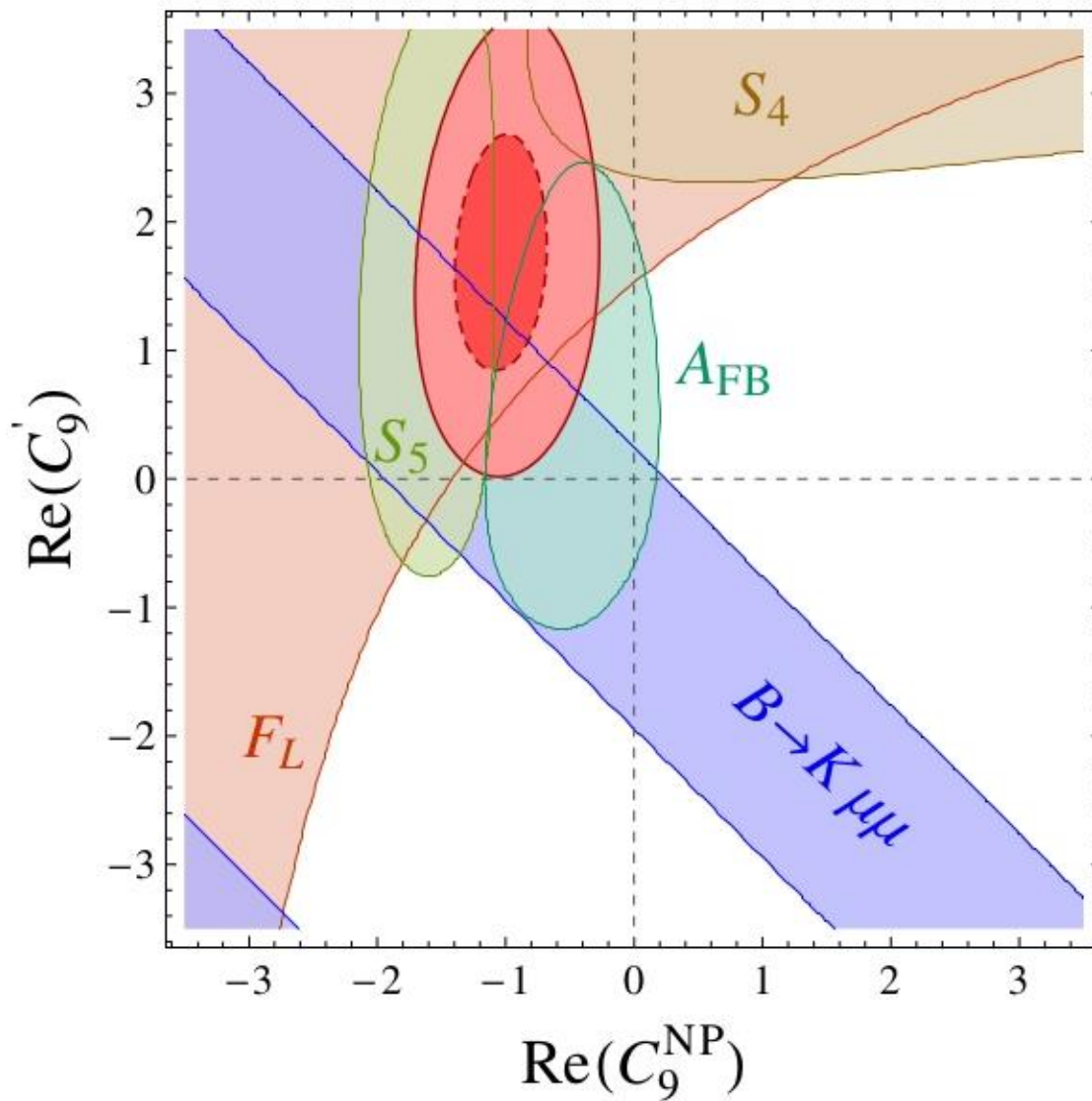
$$C_{7\gamma}^{\text{NP}} < 0, C_9^{\text{NP}} < 0$$

or

AS

$$C_9^{\text{NP}} < 0, C_9' \approx -C_9^{\text{NP}}$$

right-handed



**Altmannshofer
 Straub
 (1308.1501)**

Left-handed Z' and Z FCNC Couplings Facing $B_d \rightarrow K^* \mu^+ \mu^-$ Anomalies

(AJB + Girrbach, 1309.2466)

Z

fails because of small vector coupling to muons when $\Delta M_{s,d}$ constraints taken into account.

Z'

Suggested by Descotes-Genon, Matias, Virto (1307.5683)

Softens $\langle F_L \rangle$, $\langle S_5 \rangle$ anomalies

provided $C_9^{NP} \approx -1.5$ in a correlated manner

See also Altmannshofer Straub (1308.1501)

Note: In Z' models $C_{7\gamma}^{NP} = 0$ (1211.1896)



Optimal solutions to $\langle F_L \rangle$, $\langle S_5 \rangle$ (1309.2466)

Fails for $\langle S_4 \rangle$ must be SM-like

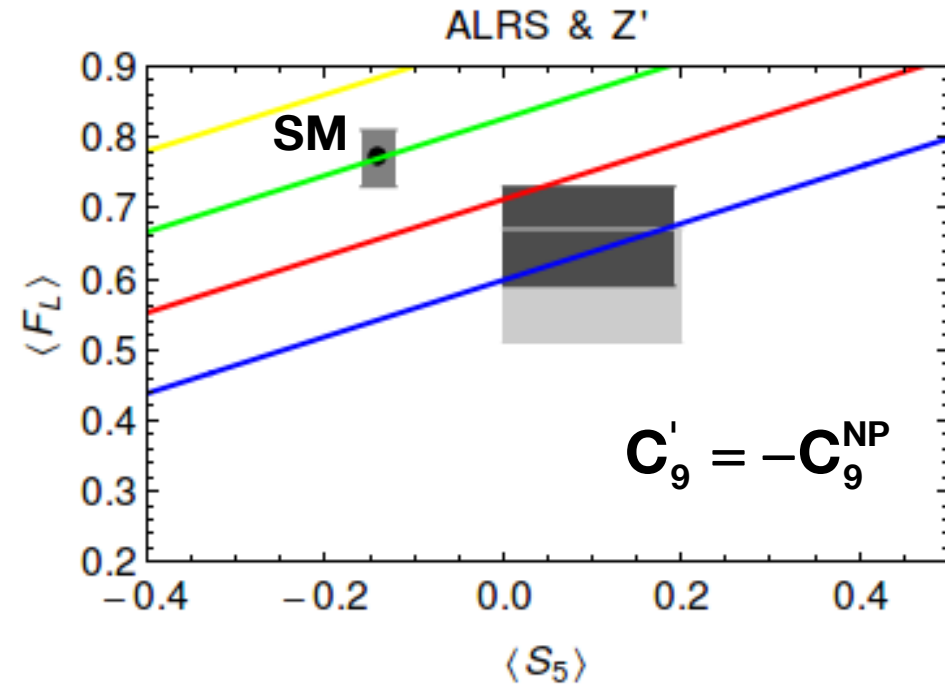
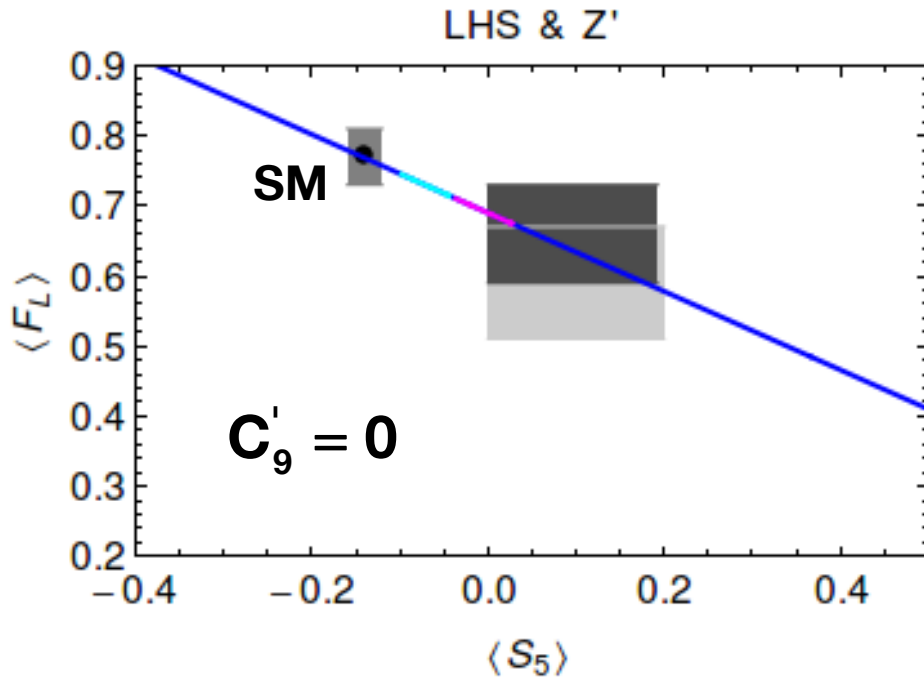
$$C_9^{NP} \neq 0, C_9' = 0 \quad (\text{LHS})$$

$$C_9^{NP} \neq 0, C_9' \approx -C_9^{NP} \quad (\text{ALRS})$$

New Correlations

(General Z')

(AJB + Girrbach, 1309.2466)



— $C_9^{NP} = -(0.8 \pm 0.3)$

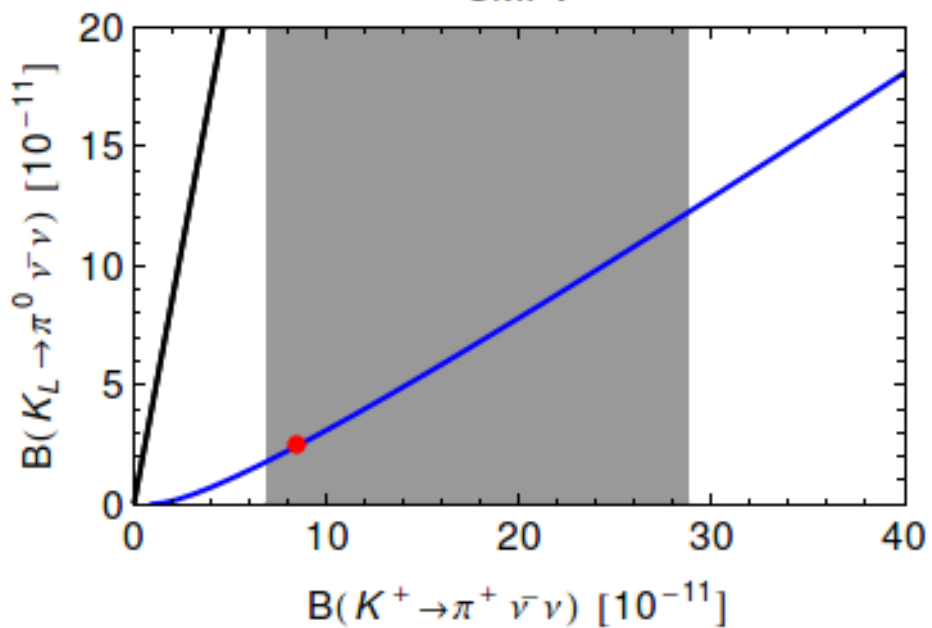
— $C_9^{NP} = -(1.6 \pm 0.3)$

— $C_9^{NP} = -1.0$

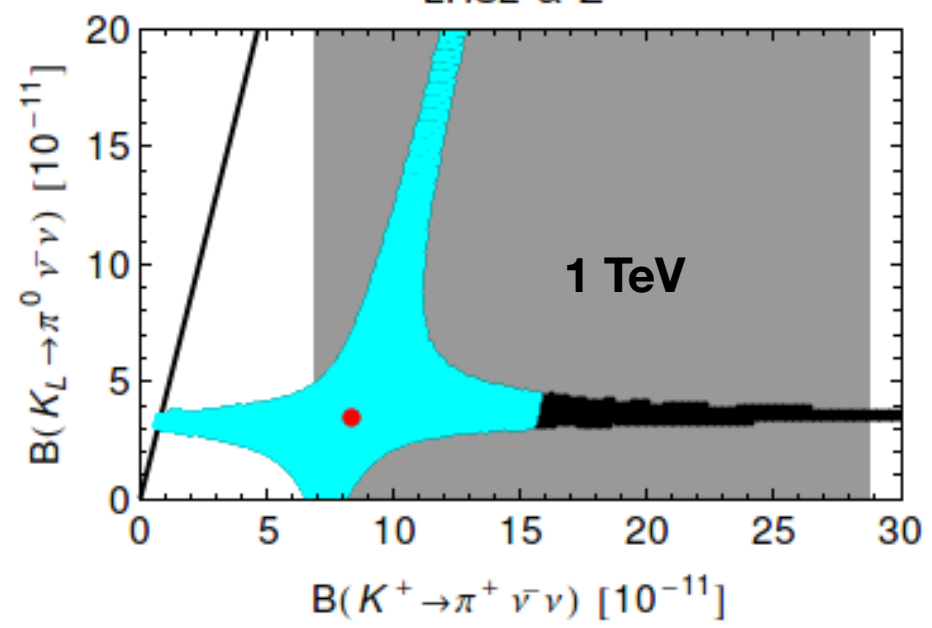
— $C_9^{NP} = -2.0$

— $C_9^{NP} = 0$

CMFV



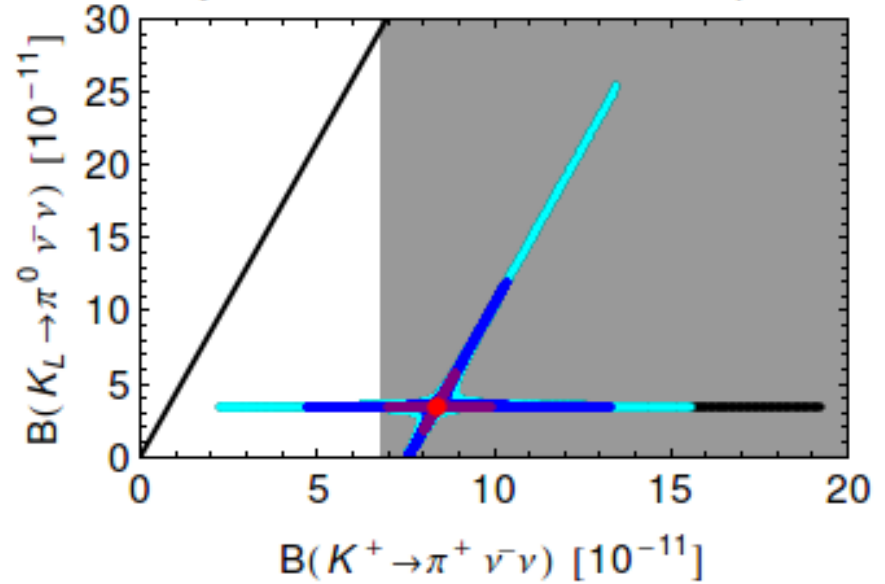
LHS2 & Z'



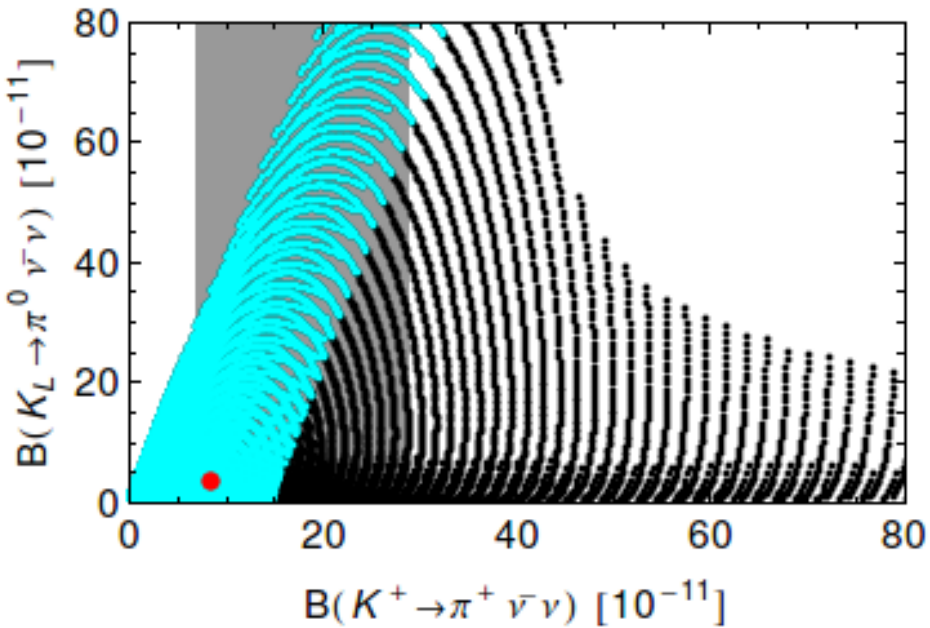
Sensitivity to $M_{Z'}$ beyond the LHC

■ : forbidden by $K_L \rightarrow \mu^+ \mu^-$

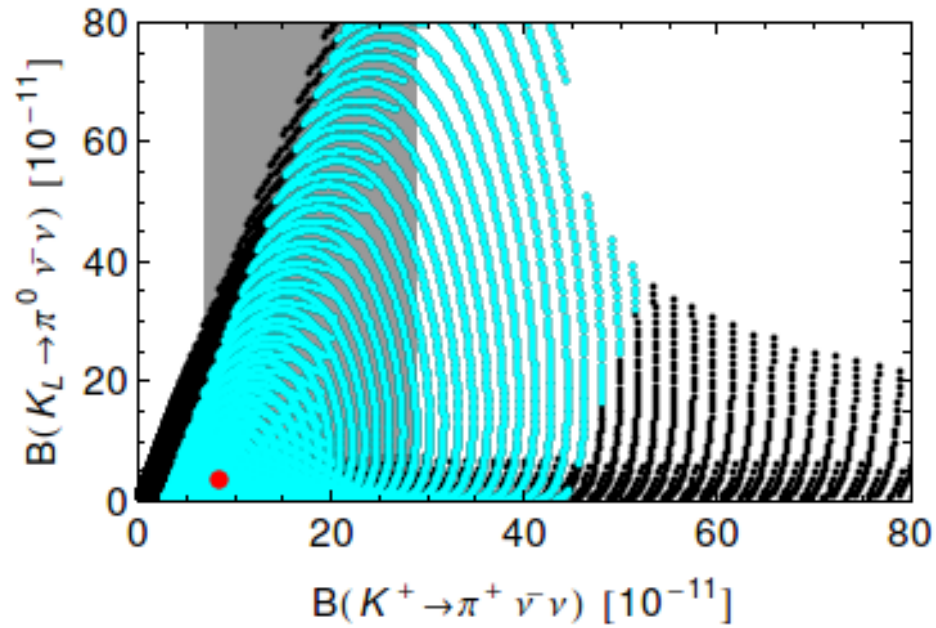
LHS2, Cyan: 5TeV, Blue: 10TeV, Purple: 30TeV



LHS2 & Z



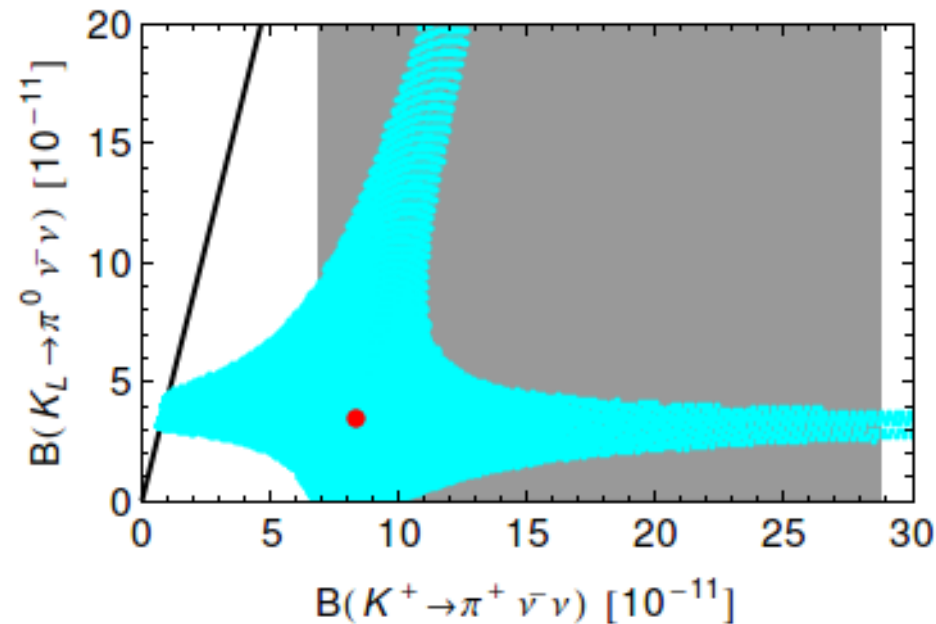
RHS2 & Z



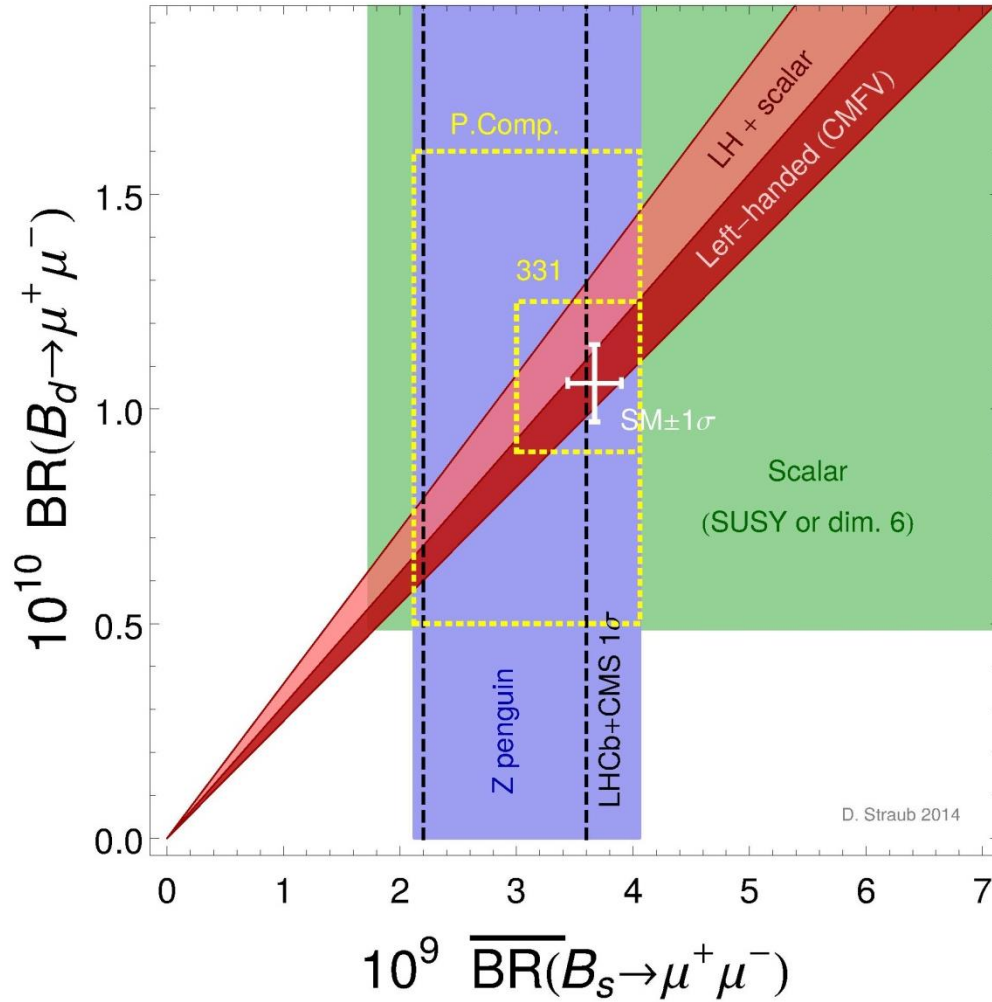
■ : forbidden by
 $K_L \rightarrow \mu^+ \mu^-$

LHS, RHS
 LRHS

LRS2 & Z



Straub's Plot 2014



Two Versions of Effective Theories

1.

$$L_{\text{eff}} = L_{\text{SM}} + \sum_i \frac{c_i}{\Lambda_i^2} Q_i$$

Wilson Coefficients

Local operators

which results from integrating out heavy fields (c_i, Λ_i depend on parameters of a given theory)
Very powerful framework in flavour physics, RG, etc.

2.

The coefficients c_i, Λ_i are free parameters.
Completion unknown. Very limited framework in flavour physics except for cases when flavour symmetries and their breakdown are assumed:
MFV $(U(3))^3, U(2)^3, \dots$

ET \equiv