

# Higgs-boson pair production in the D=6 extension of the Standard Model

*ERC workshop*

*“Effective Field Theories for Collider Physics,  
Flavor Phenomena and Electroweak Symmetry Breaking”*

Mainz, 10.11.2014

**Florian Goertz**



arXiv: 1410.3471

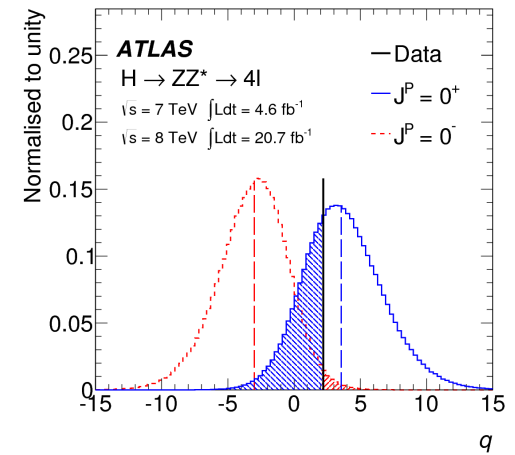
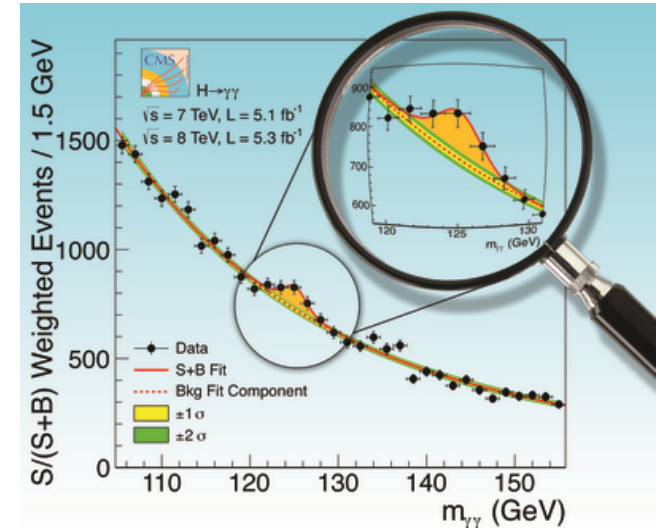
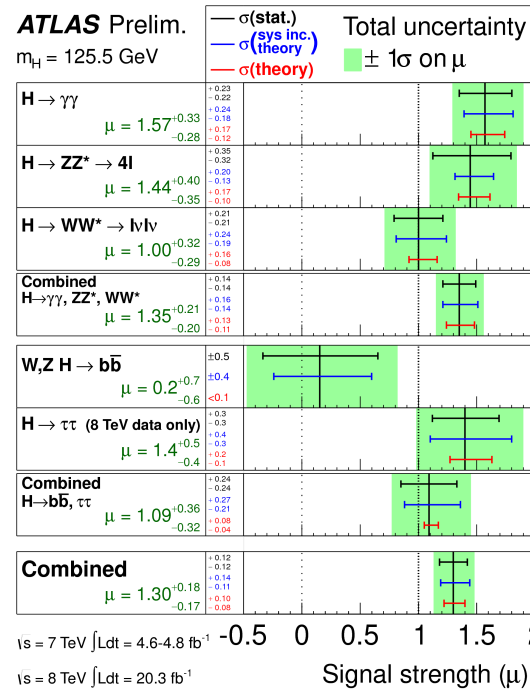
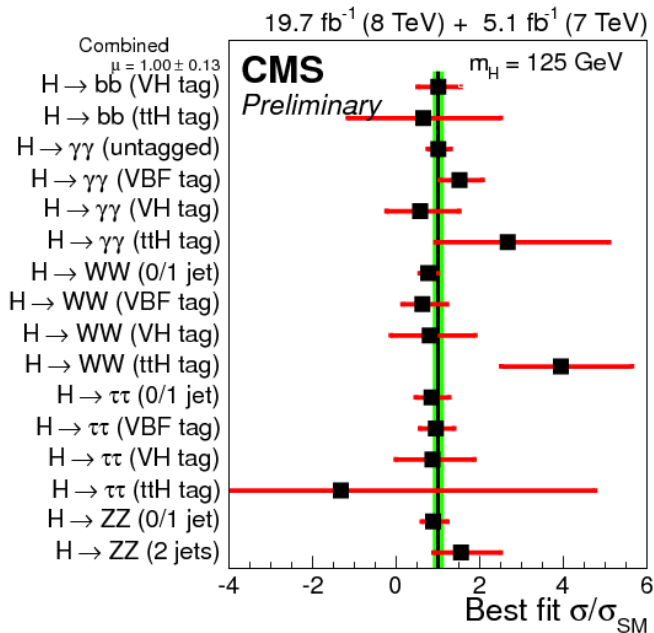
FG, Papaefstathiou, Yang, Zurita



# Introduction

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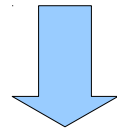
Is it the SM-Higgs Boson?  
Scale of New Physics?



# Introduction

Very important test:

Higgs potential



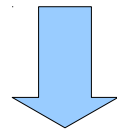
self couplings

$$V(h) = \frac{1}{2} m_h^2 h^2 + \lambda_{hhh} v h^3 + \frac{1}{4} \lambda_{hhhh} h^4 \quad (D \leq 4)$$

# Introduction

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self couplings

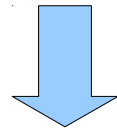
$$V(h) = \frac{1}{2} m_h^2 h^2 + \lambda_{hhh} v h^3 + \frac{1}{4} \lambda_{hhhh} h^4$$

- In the SM:  $\lambda_{hhh}^{SM} = \lambda_{hhhh}^{SM} = \frac{m_h^2}{2v^2} \approx 0.13$

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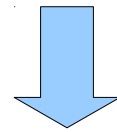
$m_h \simeq 125 \text{ GeV}$  established @LHC



# Introduction

Very important test:

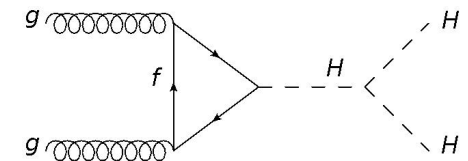
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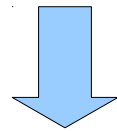
$\lambda_{hhh}$  can be measured in  
*Higgs-pair production*



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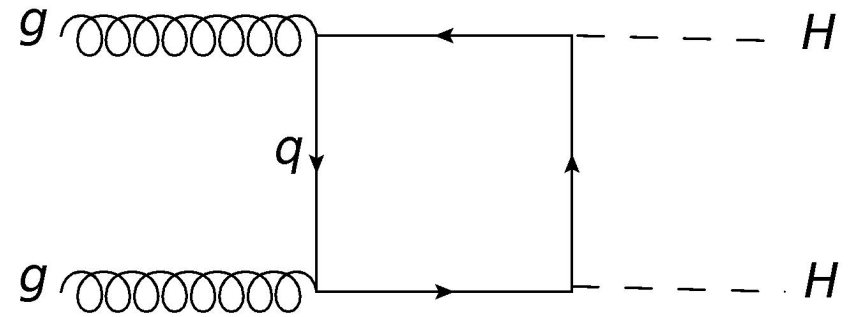
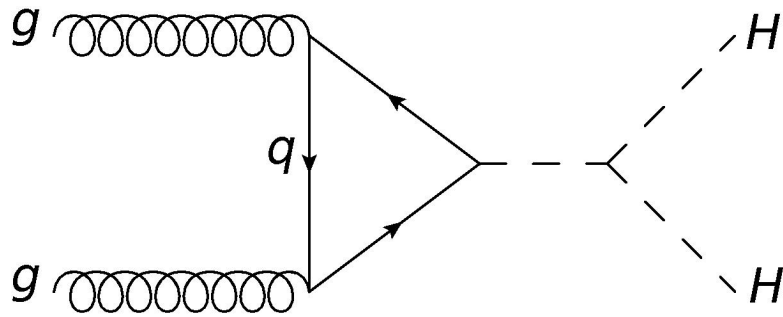
Triple Higgs production: extremely challenging @ (V)LHC  
0.06 fb @ LHC14; 9.45 fb @ VLHC (200 TeV)

Plehn, Rauch, [ph/0507321](https://arxiv.org/abs/1505.07321)



# HH Production @ LHC

- Most important mechanism:  $gg \rightarrow hh$



Eboli, Marques, Novaes, Natale, PLB 197(1987)269

Glover, van der Bij, NPB 309(1988)282

Dawson, Dittmaier, Spira, PRD 58(1998)115012

Grigo, Hoff, Melnikov, Steinhauser, 1305.7340

de Florian, Mazzitelli, 1305.5206, 1309.6594

see also Maltoni, Vryonidou, Zaro, 1408.6542

$$\sigma(gg \rightarrow hh)_{\text{LO}} \sim 17 \text{ fb}$$

$$\sigma(gg \rightarrow hh)_{\text{NLO}} \sim 33 \text{ fb}$$

$$\sigma(gg \rightarrow hh)_{\text{NNLO}} \sim 40 \text{ fb}$$

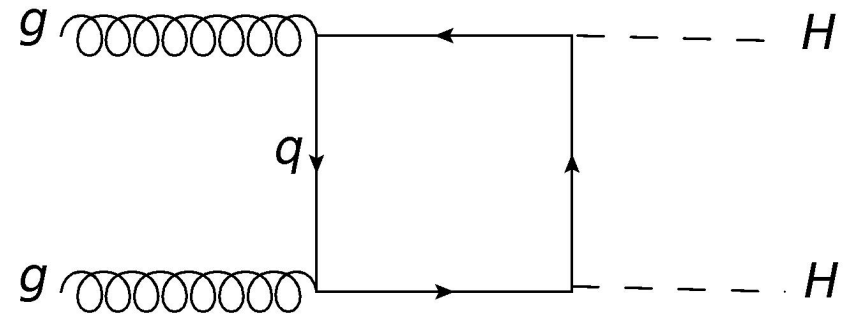
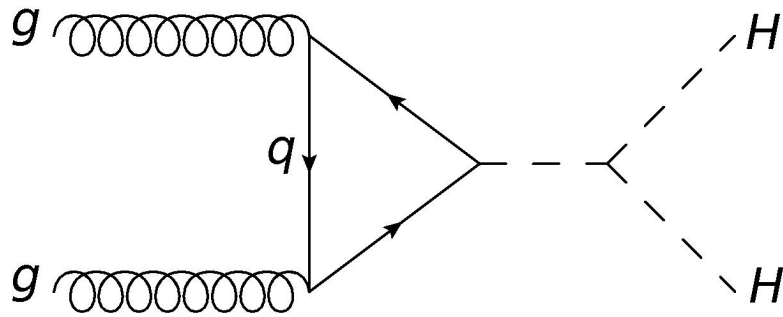
Theoretical error (NNLO):  $f_{th} \sim 10\% (\text{scale}) + 10\% (\text{pdf} + \alpha_s) + 10\% (m_t^{-1})$

LHC@14TeV

$m_h \sim 125 \text{ GeV}$

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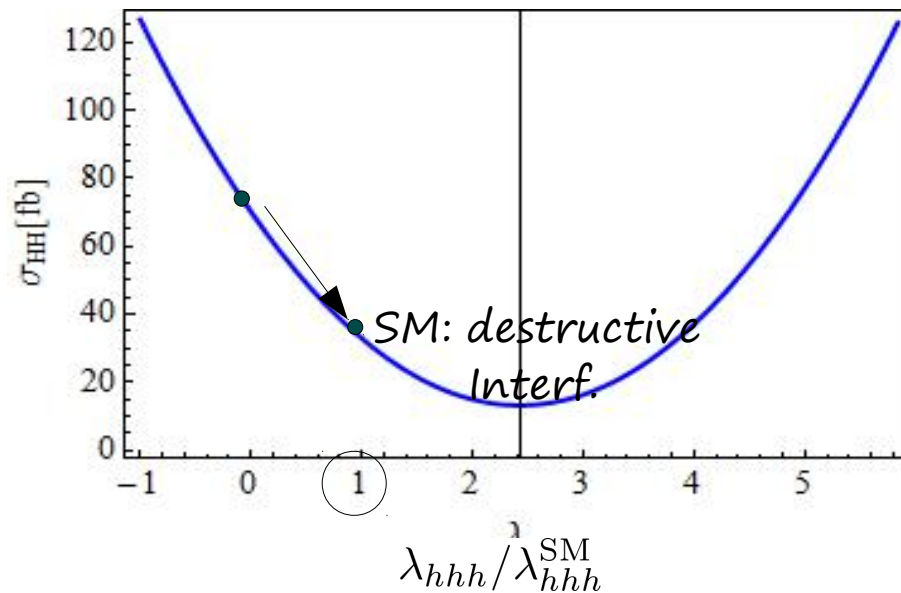
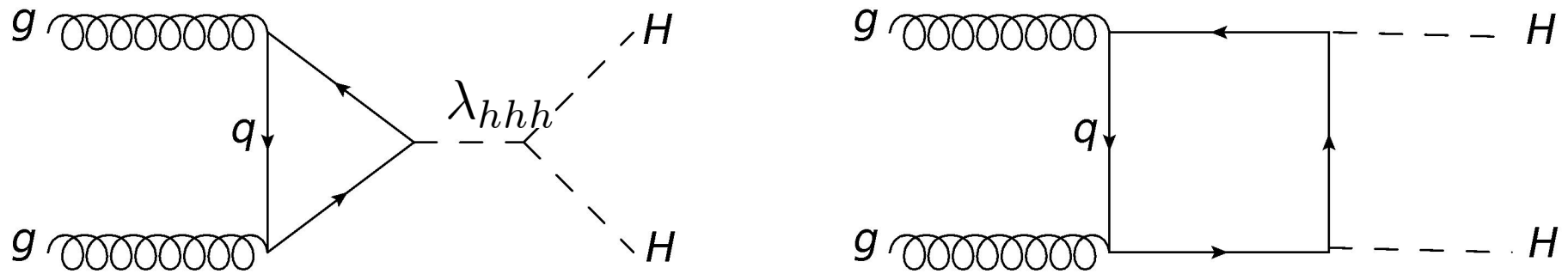
Conservative assumption for analysis:  $f_{th} = 30\%$

LHC@14TeV

$m_h \sim 125 \text{ GeV}$

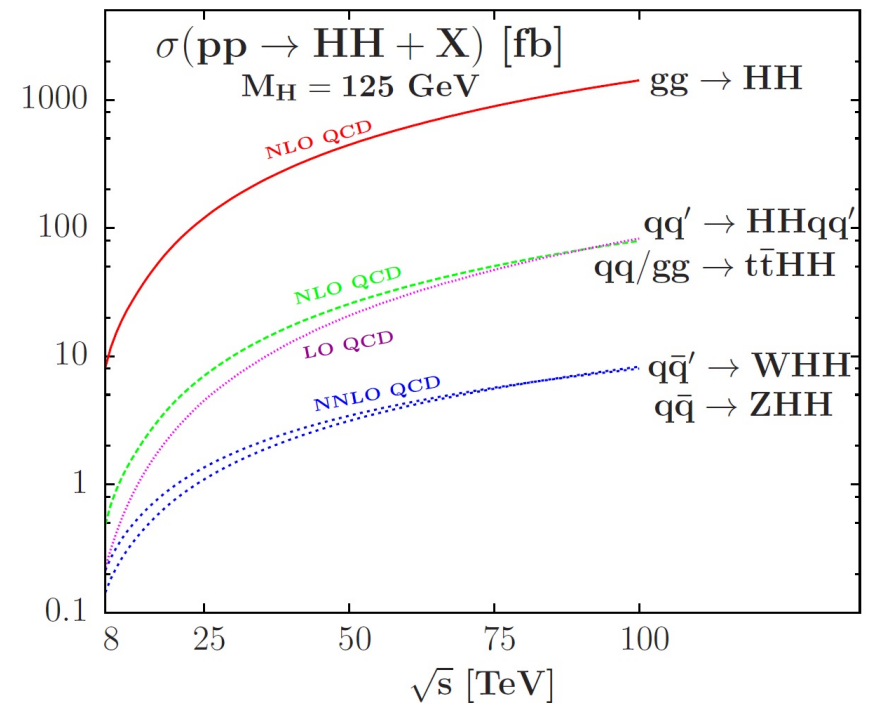
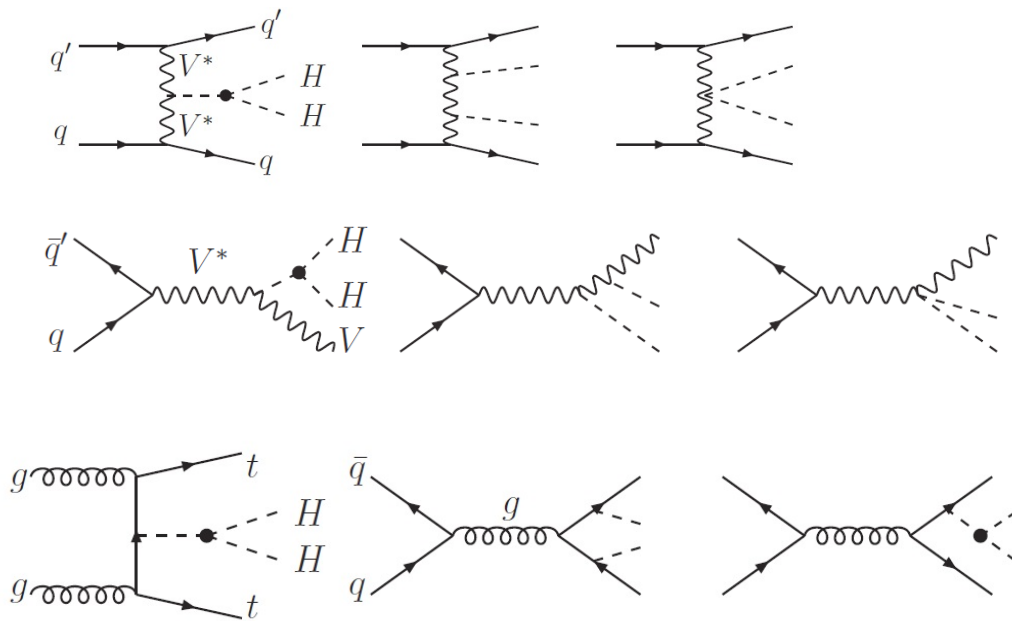
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# HH Production @ LHC

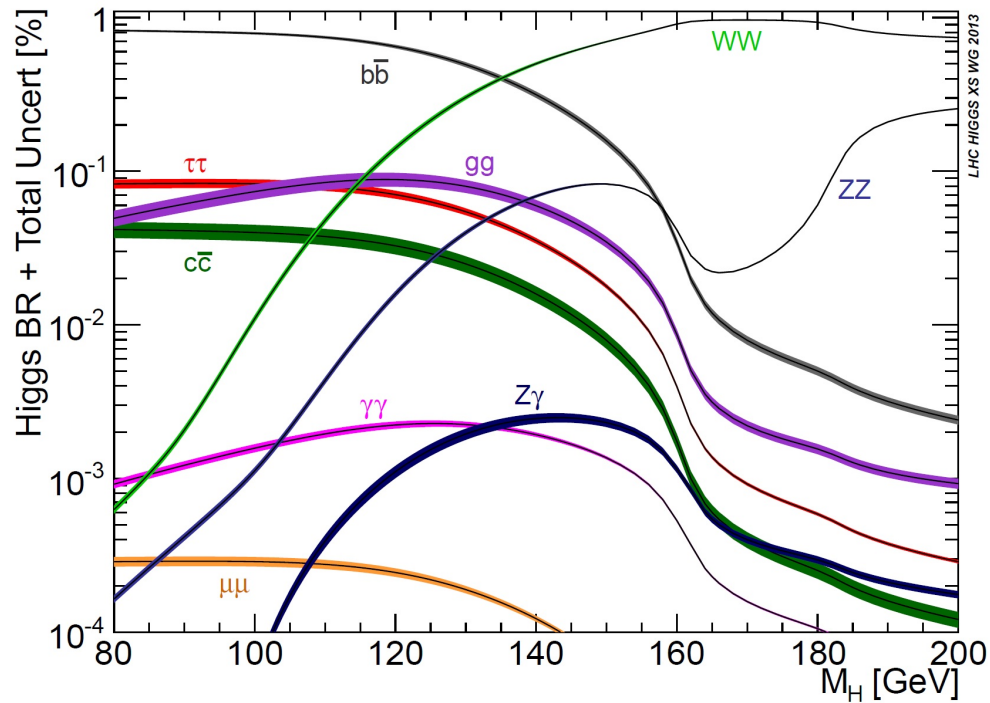
- Other production channels  $qq' \rightarrow hhqq', Vhh, t\bar{t}hh$   
 $\sim 10-30$  times smaller (neglect in the following)



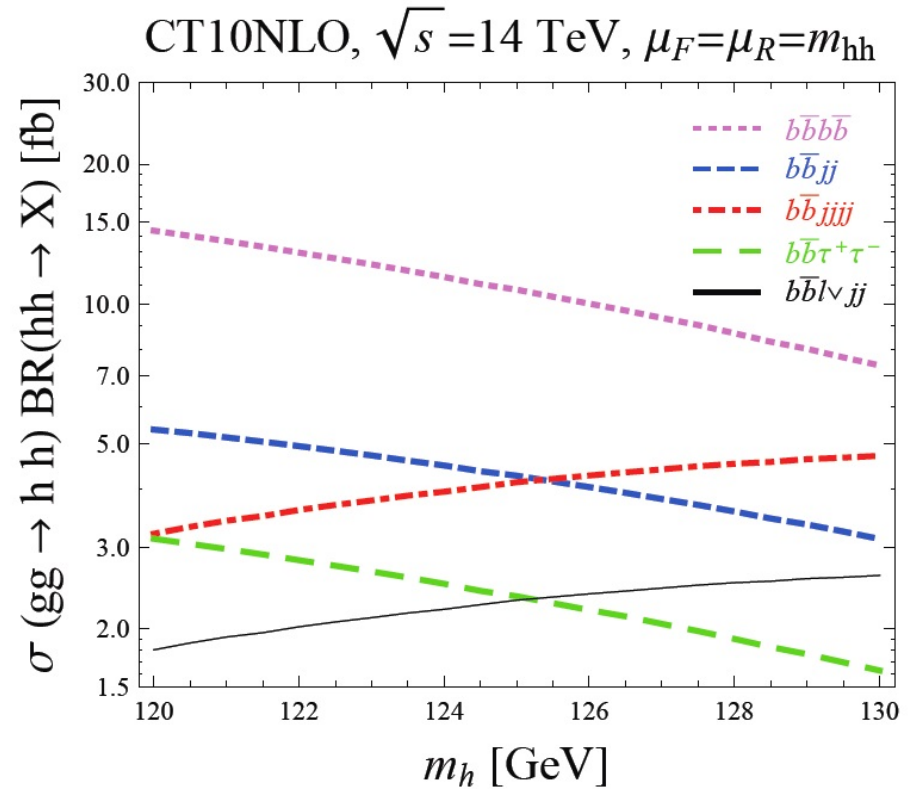
See [e.g.] Baglio, Djouadi, Grober, Muhlleitner, Quevillon, Spira, 1212.5581, and refs. therein

# Decay Channels

- Discovery potential at LHC studied in different channels



Baur, Plehn, Rainwater, hep-ph/0310056



Papaefstathiou, Yang, Zurita, 1209.1489

hadronic modes dominate

# Decay Channels

$$hh \rightarrow b\bar{b}\gamma\gamma$$

Baur, Plehn, Rainwater, hep-ph/0310056

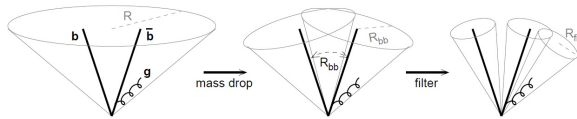
Significance @  $600 \text{ fb}^{-1}$

$$\lesssim 2\sigma \quad (S/B=6/12)$$

$$hh \rightarrow b\bar{b}\tau^+\tau^-$$

Dolan, Englert, Spannowsky, 1206.5001

$$\sim 4.5\sigma \quad (S/B=57/119)$$



Butterworth, Davison,  
Rubin, Salam, 0802.2470

$$hh \rightarrow b\bar{b}W^+W^-$$

Papaefstathiou, Yang, Zurita, 1209.1489

$$\sim 3\sigma \quad (S/B=12/8)$$

Theorists' analyses!

# Decay Channels

$$hh \rightarrow b\bar{b}\gamma\gamma$$

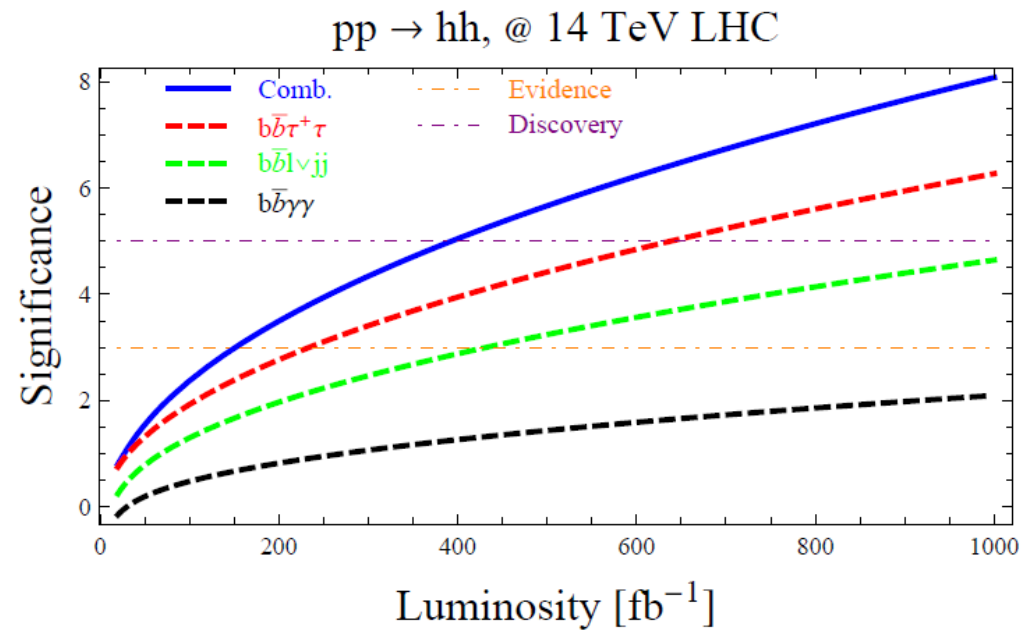
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Papaefstathiou, Yang, Zurita, 1209.1489



FG, Papaefstathiou, Yang, Zurita, 1309.3805



# Measuring $\lambda_{hhh}$

- Expected constraints on  $\lambda \equiv \lambda_{hhh}/\lambda_{hhh}^{\text{SM}}$  @LHC

from FG, Papaefstathiou, Yang, Zurita, 1301.3492

Process	600 fb <sup>-1</sup> (2 $\sigma$ )	600 fb <sup>-1</sup> (1 $\sigma$ )	3000 fb <sup>-1</sup> (2 $\sigma$ )	3000 fb <sup>-1</sup> (1 $\sigma$ )
$b\bar{b}\tau^+\tau^-$	(0.22, 4.70)	(0.57, 1.64)	(0.42, 2.13)	(0.69, 1.40)
$b\bar{b}W^+W^-$	(0.04, 4.88)	(0.46, 1.95)	(0.36, 4.56)	(0.65, 1.46)
$b\bar{b}\gamma\gamma$	(-0.56, 5.48)	(0.09, 4.83)	(0.08, 4.84)	(0.48, 1.87)

- Add single D=6 coefficient / consistency test of SM
- Assumed  $\lambda_{\text{true}} = 1$
- Reduce error by employing ratio  $C_{hh} = \frac{\sigma(gg \rightarrow hh)}{\sigma(gg \rightarrow h)} \equiv \frac{\sigma_{hh}}{\sigma_h}$   
→ reduction of scale uncertainty + cancellation of common systematics (to some extent)

Combination yields  $\sim 30\%$  accuracy with 3000 fb<sup>-1</sup>



# Full Analysis of SM + D=6

# Higgs Boson EFT

- Assume (unspecified) New Physics at a scale  $\Lambda \gg v$   
 $\rightarrow$  leading effects:  $D=6$  operators built of SM content

Buchmuller, Wyler, NPB 268(1986)621–653

Grzadkowski, Iskrzynski, Misiak, Rosiek, 1008.4884

Here:

$$\begin{aligned}
 \mathcal{L} = & \mathcal{L}_{\text{SM}} + \frac{c_H}{2\Lambda^2} (\partial^\mu |H|^2)^2 - \frac{c_6}{\Lambda^2} \lambda |H|^6 \\
 & - \left( \frac{c_t}{\Lambda^2} y_t |H|^2 \bar{Q}_L H^c t_R + \frac{c_b}{\Lambda^2} y_b |H|^2 \bar{Q}_L H b_R + \frac{c_\tau}{\Lambda^2} y_\tau |H|^2 \bar{L}_L H \tau_R + \text{h.c.} \right) \\
 & + \frac{\alpha_s c_g}{4\pi\Lambda^2} |H|^2 G_{\mu\nu}^a G_a^{\mu\nu} + \frac{\alpha' c_\gamma}{4\pi\Lambda^2} |H|^2 B_{\mu\nu} B^{\mu\nu} \\
 & + \frac{ig c_{HW}}{16\pi^2 \Lambda^2} (D^\mu H)^\dagger \sigma_k (D^\nu H) W_{\mu\nu}^k + \frac{ig' c_{HB}}{16\pi^2 \Lambda^2} (D^\mu H)^\dagger (D^\nu H) B_{\mu\nu} \\
 & + \frac{ig c_W}{2\Lambda^2} (H^\dagger \sigma_k \overleftrightarrow{D}^\mu H) D^\nu W_{\mu\nu}^k + \frac{ig' c_B}{2\Lambda^2} (H^\dagger \overleftrightarrow{D}^\mu H) \partial^\nu B_{\mu\nu} \quad (+\mathcal{L}_{\text{CP}} + \mathcal{L}_{4\text{f}})
 \end{aligned}$$

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 &+ \frac{ig c_W}{2\Lambda^2} (H^\dagger \sigma_k \overleftrightarrow{D}^\mu H) D^\nu W_{\mu\nu}^k + \frac{ig' c_B}{2\Lambda^2} (H^\dagger \overleftrightarrow{D}^\mu H) \partial^\nu B_{\mu\nu} \quad (+\mathcal{L}_{\text{CP}} + \mathcal{L}_{4f})
 \end{aligned}$$

Loop induced ←  
see e.g.  
Einhorn, Wudka,  
1307.0478

For non-linear realization, see e.g. Grinstein, Trott 0704.1505;  
Contino, Grojean, Moretti, Piccinini, Rattazzi 1002.1011

# Higgs Boson EFT

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 \end{aligned}$$

- Neglected operators that are strongly constrained from precision tests

See e.g.: Elias-Miro, Espinosa, Masso, Pomarol, 1308.1879; Pomarol, Riva, 1308.2803;

Corbett, Eboli, Gonzalez-Fraile, Gonzalez-Garcia 1207.1344, 1211.4580, 1304.1151;

Falkowski, Riva, Urbano, 1303.1812; Contino, Ghezzi, Grojean, Muhlleitner, Spira, 1303.3876;

Dumont, Fichet, von Gersdorff 1304.3369; Falkowski, Riva, 1411.0669

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 \end{aligned}$$

- Precision tests also lead to the approximate relation (EOM consistent)

$$c_W = -c_B = -\frac{c_{HW}}{16\pi^2} = \frac{c_{HB}}{16\pi^2}$$

*Elias-Miro, Espinosa, Masso, Pomarol, 1308.1879*

*Trott 1409.7605*



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 \mathcal{L} = \mathcal{L}_{\text{SM}} &+ \frac{c_H}{2\Lambda^2} (\partial^\mu |H|^2)^2 - \frac{c_6}{\Lambda^2} \lambda |H|^6 \quad \text{Pure Higgs} \\
 &- \left( \frac{c_t}{\Lambda^2} y_t |H|^2 \bar{Q}_L H^c t_R + \frac{c_b}{\Lambda^2} y_b |H|^2 \bar{Q}_L H b_R + \frac{c_\tau}{\Lambda^2} y_\tau |H|^2 \bar{L}_L H \tau_R + \text{h.c.} \right) \quad \text{Yukawa type} \\
 &+ \frac{\alpha_s c_g}{4\pi\Lambda^2} |H|^2 G_{\mu\nu}^a G_a^{\mu\nu} + \frac{\alpha' c_\gamma}{4\pi\Lambda^2} |H|^2 B_{\mu\nu} B^{\mu\nu} \quad \text{---} \\
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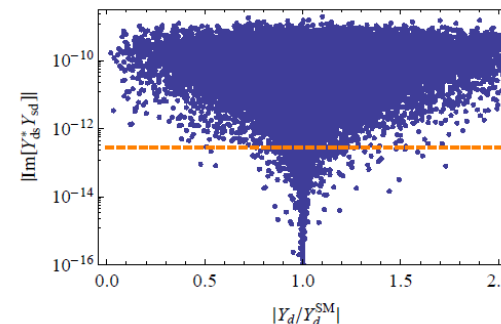
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 &+ \frac{ig c_{HW}}{16\pi^2\Lambda^2} (D^\mu H)^\dagger \sigma_k (D^\nu H) W_{\mu\nu}^k + \frac{ig' c_{HB}}{16\pi^2\Lambda^2} (D^\mu H)^\dagger (D^\nu H) B_{\mu\nu} \\
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 \end{aligned}$$

- What about light-quark Yukawas  
 → can assume MFV, but even should be negligible on more general grounds: FCNCs

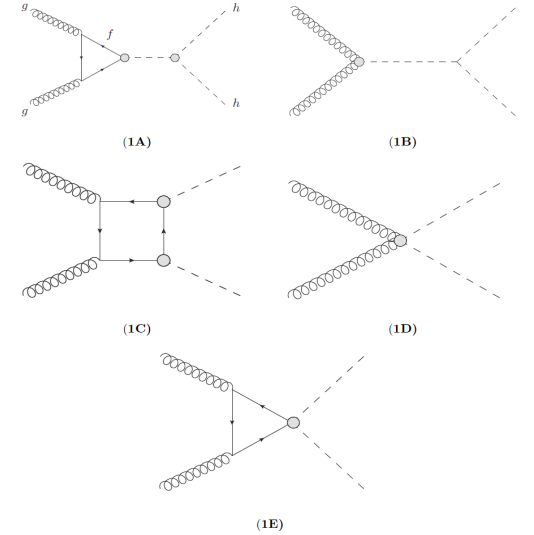


FG, 1406.0102

# $gg \rightarrow hh$

Relevant Terms:

$$\begin{aligned}
 \mathcal{L}_{hh} = & -\frac{m_h^2}{2v} \left( 1 - \frac{3}{2}c_H + c_6 \right) h^3 \\
 & + \frac{\alpha_s c_g}{4\pi} \left( \frac{h}{v} + \frac{h^2}{2v^2} \right) G_{\mu\nu}^a G_a^{\mu\nu} \\
 & - \left[ \frac{m_t}{v} \left( 1 - \frac{c_H}{2} + c_t \right) \bar{t}_L t_R h + \frac{m_b}{v} \left( 1 - \frac{c_H}{2} + c_b \right) \bar{b}_L b_R h + \text{h.c.} \right] \\
 & - \left[ \frac{m_t}{v^2} \left( \frac{3c_t}{2} - \frac{c_H}{2} \right) \bar{t}_L t_R h^2 + \frac{m_b}{v^2} \left( \frac{3c_b}{2} - \frac{c_H}{2} \right) \bar{b}_L b_R h^2 + \text{h.c.} \right]
 \end{aligned}$$

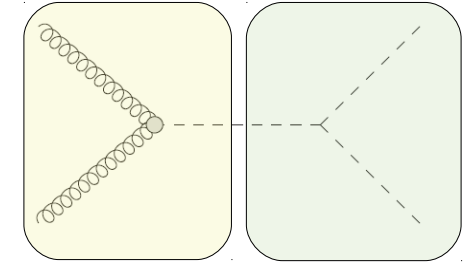
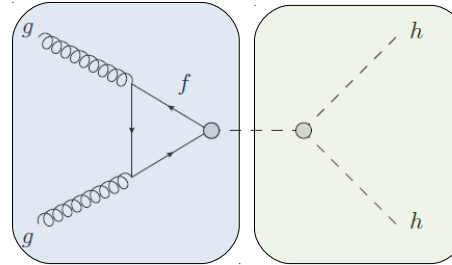


$$c_i \rightarrow c_i \Lambda^2 / v^2, \quad H = \exp \left( -i \frac{T \cdot \xi}{v} \right) \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v + h \end{pmatrix}, \quad h \rightarrow \left( 1 - \frac{c_H v^2}{2\Lambda^2} \right) h - \frac{c_H v}{2\Lambda^2} h^2 - \frac{c_H}{6\Lambda^2} h^3$$

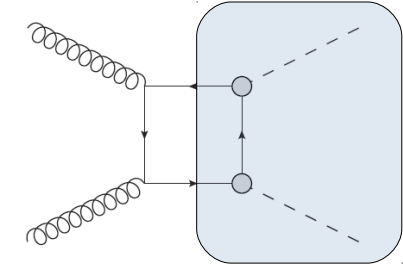
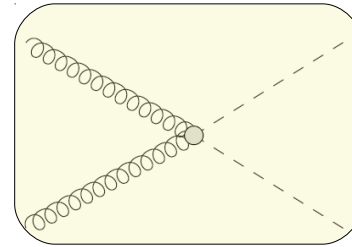
non-linear redefinition:  
removes momentum-dependent interactions

# $gg \rightarrow hh$

$$\mathcal{L}_{hh} = - \frac{m_h^2}{2v} \left( 1 - \frac{3}{2}c_H + c_6 \right) h^3$$

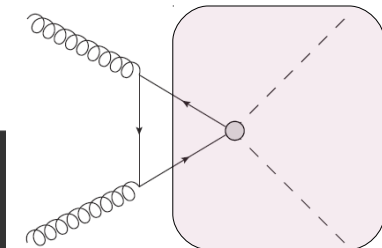


$$+ \frac{\alpha_s c_g}{4\pi} \left( \frac{h}{v} + \frac{h^2}{2v^2} \right) G_{\mu\nu}^a G_a^{\mu\nu}$$



$$- \left[ \frac{m_t}{v} \left( 1 - \frac{c_H}{2} + c_t \right) \bar{t}_L t_R h + \frac{m_b}{v} \left( 1 - \frac{c_H}{2} + c_b \right) \bar{b}_L b_R h + \text{h.c.} \right]$$

$$- \left[ \frac{m_t}{v^2} \left( \frac{3c_t}{2} - \frac{c_H}{2} \right) \bar{t}_L t_R h^2 + \frac{m_b}{v^2} \left( \frac{3c_b}{2} - \frac{c_H}{2} \right) \bar{b}_L b_R h^2 + \text{h.c.} \right]$$



# $\lambda_{hhhh}$ vs $\hat{\lambda}_{hhhh}$

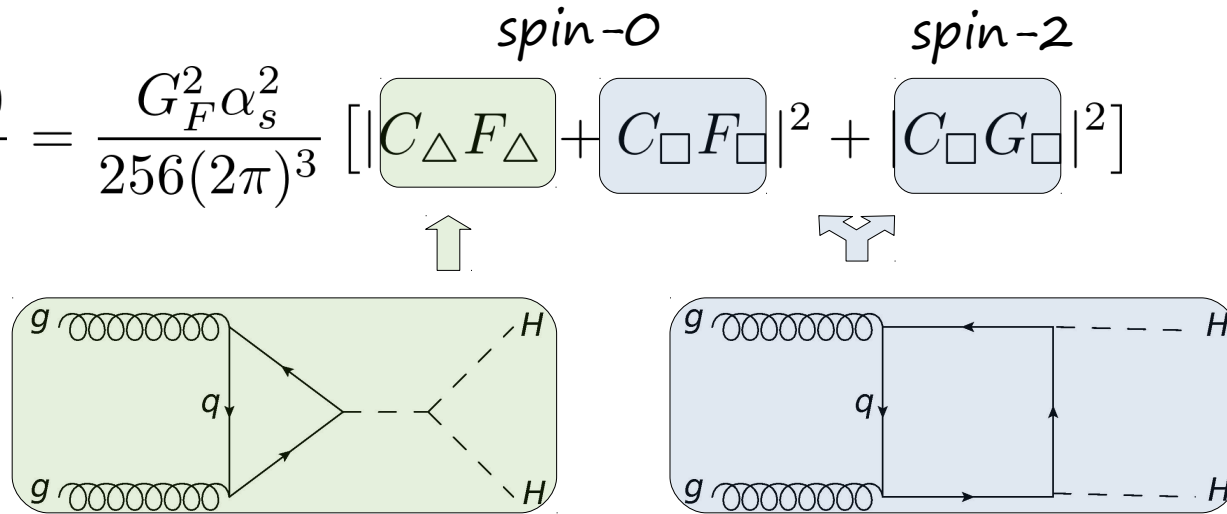
$$\mathcal{L} \supset -\frac{m_h^2}{2v} \left(1 - \frac{3}{2}c_H + c_6\right) h^3 - \frac{m_h^2}{8v^2} \left(1 - \frac{25}{3}c_H + 6c_6\right) h^4$$

$$\lambda_{hhhh} = \frac{m_h^2}{2v^2} (1 + \Delta) \neq \hat{\lambda}_{hhhh} = \frac{m_h^2}{2v^2} \left(1 + 6\Delta + \frac{2}{3}c_H\right)$$

$$\Delta = c_6 - 3c_H/2$$

# Cross Section in SM (LO)

$$\frac{d\hat{\sigma}(gg \rightarrow hh)}{d\hat{t}} = \frac{G_F^2 \alpha_s^2}{256(2\pi)^3} \left[ |C_\Delta F_\Delta + C_\square F_\square|^2 + |C_\square G_\square|^2 \right]$$



$$C_\Delta = \frac{3m_h^2}{\hat{s} - m_h^2},$$

$$C_\square = 1$$

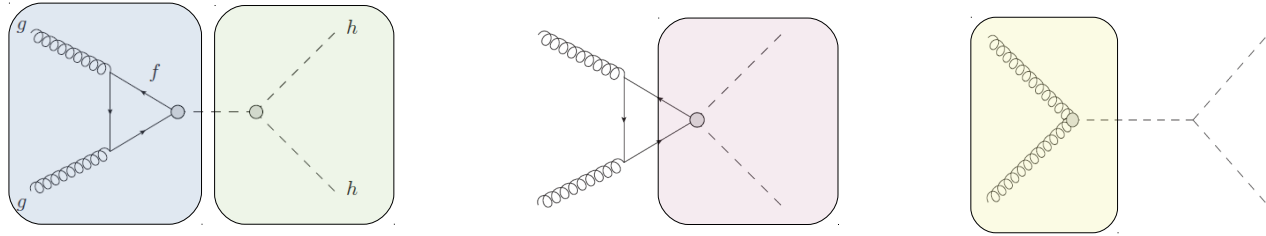
$$F_\Delta = \frac{2}{3} + \mathcal{O}(\hat{s}/m_Q^2),$$

$$F_\square = -\frac{2}{3} + \mathcal{O}(\hat{s}/m_Q^2),$$

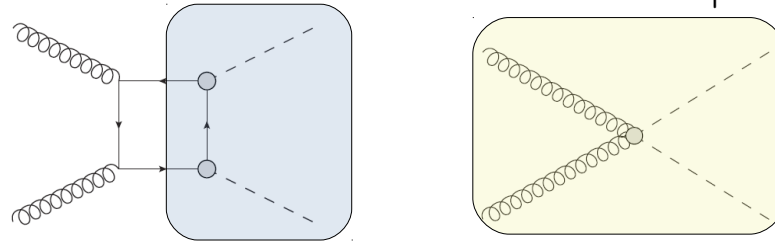
$$G_\square = \mathcal{O}(\hat{s}/m_Q^2)$$

See Plehn, Spira, Zerwas [ph/9603205](https://arxiv.org/abs/hep-ph/9603205)

# Cross Section in D=6 EFT



$$\left. \frac{d\hat{\sigma}(gg \rightarrow hh)}{d\hat{t}} \right|_{\text{EFT}} = \frac{G_F^2 \alpha_s^2}{256(2\pi)^3} \left\{ \left| C_\Delta F_\Delta (1 - 2c_H + c_t + c_6) + 3F_\Delta (3c_t - c_H) + 2c_g C_\Delta \right. \right. \\ \left. \left. + C_\square F_\square (1 - c_H + 2c_t) + 2c_g C_\square \right|^2 + \left| C_\square G_\square \right|^2 \right\}$$



$$C_\Delta = \frac{3m_h^2}{\hat{s} - m_h^2}, \quad C_\square = 1 \\ F_\Delta = \frac{2}{3} + \mathcal{O}(\hat{s}/m_Q^2), \quad F_\square = -\frac{2}{3} + \mathcal{O}(\hat{s}/m_Q^2), \\ G_\square = \mathcal{O}(\hat{s}/m_Q^2)$$



Implemented in MC generator Herwig++

Normalize to NNLO: de Florian, Mazzitelli, 1309.6594

See Plehn, Spira, Zerwas ph/9603205

# Higgs Decays in $D=6$ EFT

Mode	tree	1 loop QCD	1 loop
$h \rightarrow bb$	$c_H, c_b$	$c_H, c_b$	$c_H, c_b, c_t, c_6, c_W$
$h \rightarrow \tau\tau$	$c_H, c_\tau$	-	$c_H, c_\tau, c_6, c_W$
$h \rightarrow \gamma\gamma$	$c_\gamma$	-	$c_H, c_b, c_t, c_\tau, c_W$
$h \rightarrow WW$	$c_H, c_{HW}, c_W$	-	$c_H, c_W, c_b, c_t, c_\tau, c_6$
$gg \rightarrow hh$	$c_g$	$c_t, c_b$	$c_t, c_b, c_H, c_6$
$gg \rightarrow h$	$c_g$	$c_t, c_b, c_H$	$c_t, c_b, c_H$

**Table 1:** Operators that modify the various decays of the Higgs boson at the tree level (second column), at the one-loop level, considering only QCD corrections (third column), as well as at the full one-loop level (fourth column). For completeness, we also include the operators entering  $gg \rightarrow h$  and  $gg \rightarrow hh$ . The operators that are highlighted in bold text are included in the treatment of the present paper in the corresponding topology.



# Higgs Decays in $D=6$ EFT

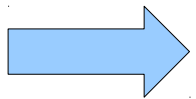
Mode	tree	1 loop QCD	1 loop
$h \rightarrow bb$	$c_H, c_b$	<del><math>c_H, c_b</math></del>	$c_H, c_b, c_t, c_6, c_W$
$h \rightarrow \tau\tau$	$c_H, c_\tau$	-	$c_H, c_\tau, c_6, c_W$
$h \rightarrow \gamma\gamma$	$c_\gamma$	-	$c_H, c_b, c_t, c_\tau, c_W$
$h \rightarrow WW$	$c_H, c_{HW}, c_W$	-	$c_H, c_W, c_b, c_t, c_\tau, c_6$
$gg \rightarrow hh$	$c_g$	$c_t, c_b$	$c_t, c_b, c_H, c_6$
$gg \rightarrow h$	$c_g$	$c_t, c_b, c_H$	$c_t, c_b, c_H$

Loop +  $\Lambda^2$  suppressed wrt SM

Included via eHDECAY:

Contino, Ghezzi, Grojean, Muhlleitner, Spira, 1403.3381

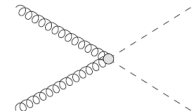
$$c_W = -c_B = -\frac{c_{HW}}{16\pi^2} = \frac{c_{HB}}{16\pi^2}$$

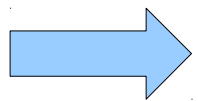


6 Parameters:  $\{c_6, c_H, c_t, c_b = c_\tau, c_g, c_\gamma\}$

Unique accessibility in hh production!

# HH in D=6 EFT

$$\begin{aligned}
 \mathcal{L} = \mathcal{L}_{\text{SM}} &+ \frac{c_H}{2\Lambda^2} (\partial^\mu |H|^2)^2 - \frac{c_6}{\Lambda^2} \lambda |H|^6 \quad \text{Pure Higgs} \\
 &- \left( \frac{c_t}{\Lambda^2} y_t |H|^2 \bar{Q}_L H^c t_R + \frac{c_b}{\Lambda^2} y_b |H|^2 \bar{Q}_L H b_R + \frac{c_\tau}{\Lambda^2} y_\tau |H|^2 \bar{L}_L H \tau_R + \text{h.c.} \right) \quad \text{Yukawa type} \\
 &+ \frac{\alpha_s c_g}{4\pi\Lambda^2} |H|^2 G_{\mu\nu}^a G_a^{\mu\nu} + \frac{\alpha' c_\gamma}{4\pi\Lambda^2} |H|^2 B_{\mu\nu} B^{\mu\nu}
 \end{aligned}$$




6 Parameters:  $\{c_6, c_H, c_t, c_b = c_\tau, c_g, c_\gamma\}$

Unique accessibility in hh production!

# Analysis

- Focus on  $hh \rightarrow b\bar{b}\tau^+\tau^-$   
@LHC14

Dolan, Englert, Spannowsky, 1206.5001

Baglio, Djouadi, Grober, Muhlleitner, Quevillon; 1212.5581

Barr, Dolan, Englert, Spannowsky, 1309.6318

Maierhoefer, Papaefstathiou, 1401.0007

- Main backgrounds:
  - $pp \rightarrow t\bar{t} \rightarrow b\bar{b}\tau^+\tau^- (+E_{\text{mis}})$

Generated with **aMC@NLO**  
(+HERWIG++)

Frixione et. al., 1010.0568

Frederix et. al., 1104.5613

Alwall et. al., 1405.0301

- $pp \rightarrow ZZ \rightarrow b\bar{b}\tau^+\tau^-$

- $pp \rightarrow hZ \rightarrow b\bar{b}\tau^+\tau^-$

# Analysis: $hh \rightarrow b\bar{b}\tau^+\tau^-$

- Main backgrounds:
  - $pp \rightarrow t\bar{t} \rightarrow b\bar{b}\tau^+\tau^- (+E_{\text{mis}})$
  - $pp \rightarrow ZZ \rightarrow b\bar{b}\tau^+\tau^-$
  - $pp \rightarrow hZ \rightarrow b\bar{b}\tau^+\tau^-$

Generated with **aMC@NLO**  
(+HERWIG++)

*Frixione et. al., 1010.0568*

*Frederix et. al., 1104.5613*

*Alwall et. al., 1405.0301*

## ↳ Cuts:

- Two  $\tau$ -tagged jets with  $p_{\perp} > 20$  GeV
- one fat jet with  $R = 1.4$  (CA), two hardest sub-jets  $b$ -tagged ( $|\eta| < 2.5$ )  
*Butterworth, Davison, Rubin, Salam, 0802.2470*
- $m_{\tau^+\tau^-}, m_{\text{fat}} \in [m_h - 25 \text{ GeV}, m_h + 25 \text{ GeV}]$
- $p_{\perp}^{\text{fat}}, p_{\perp}^{\tau\tau} > 100$  GeV,  $\Delta R(h, h) > 2.8$ ,  $p_{\perp}^{hh} < 80$  GeV

$b, \tau$ -tagging efficiencies: 70 %

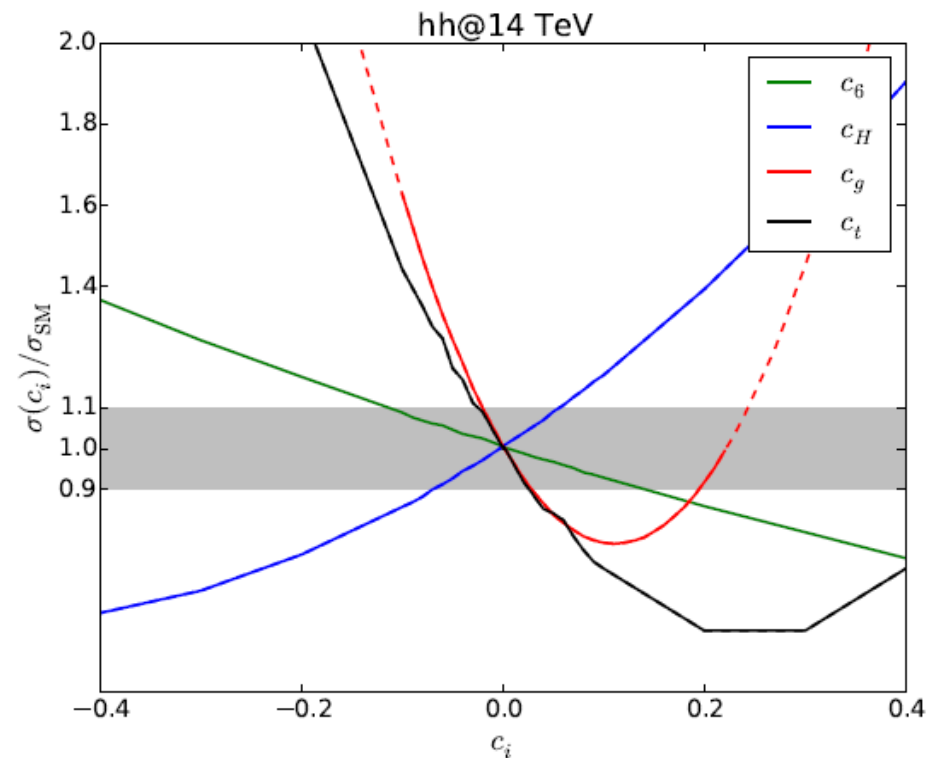
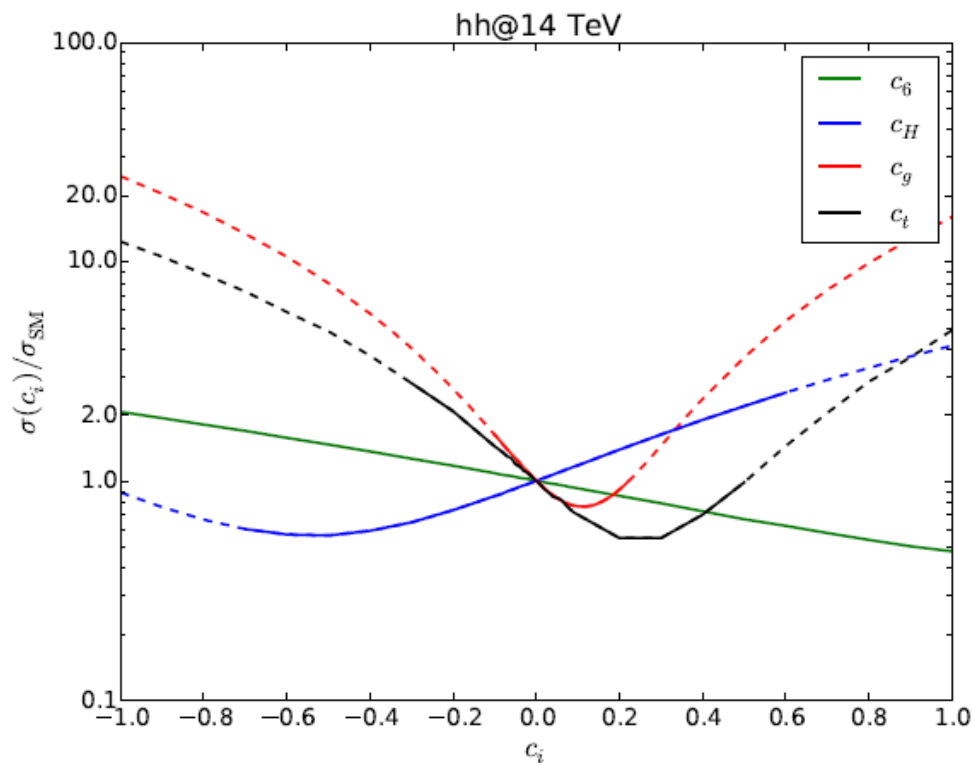
*see: Dolan, Englert, Spannowsky, 1206.5001;*

*Maierhoefer, Papaefstathiou, 1401.0007*



# Results

# $gg \rightarrow hh$ Cross Section

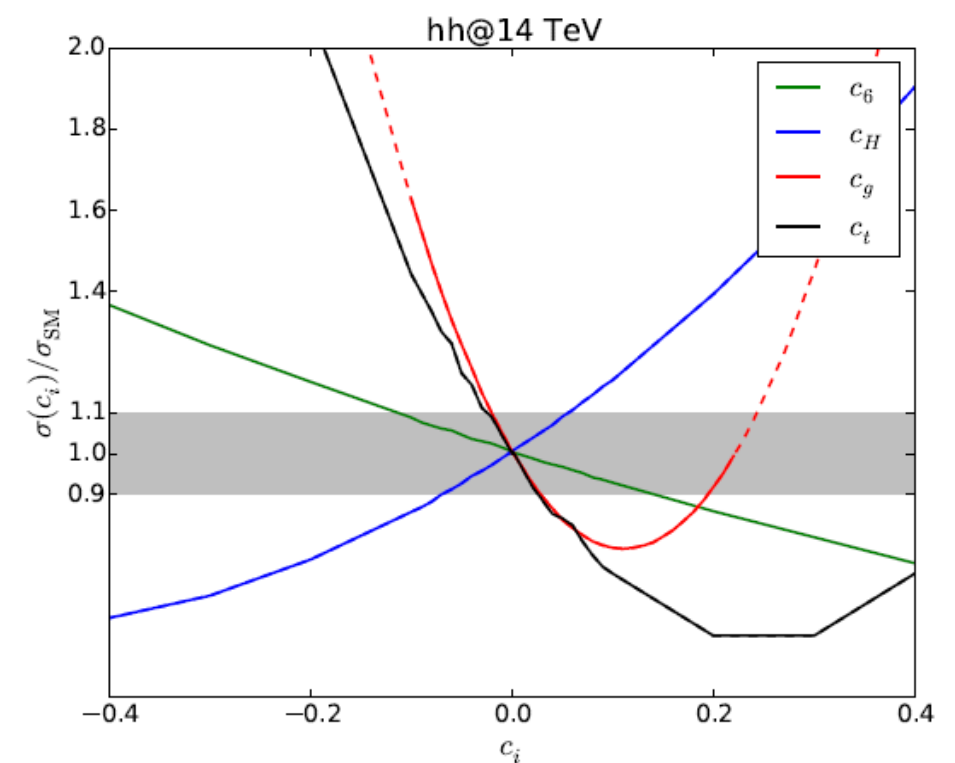
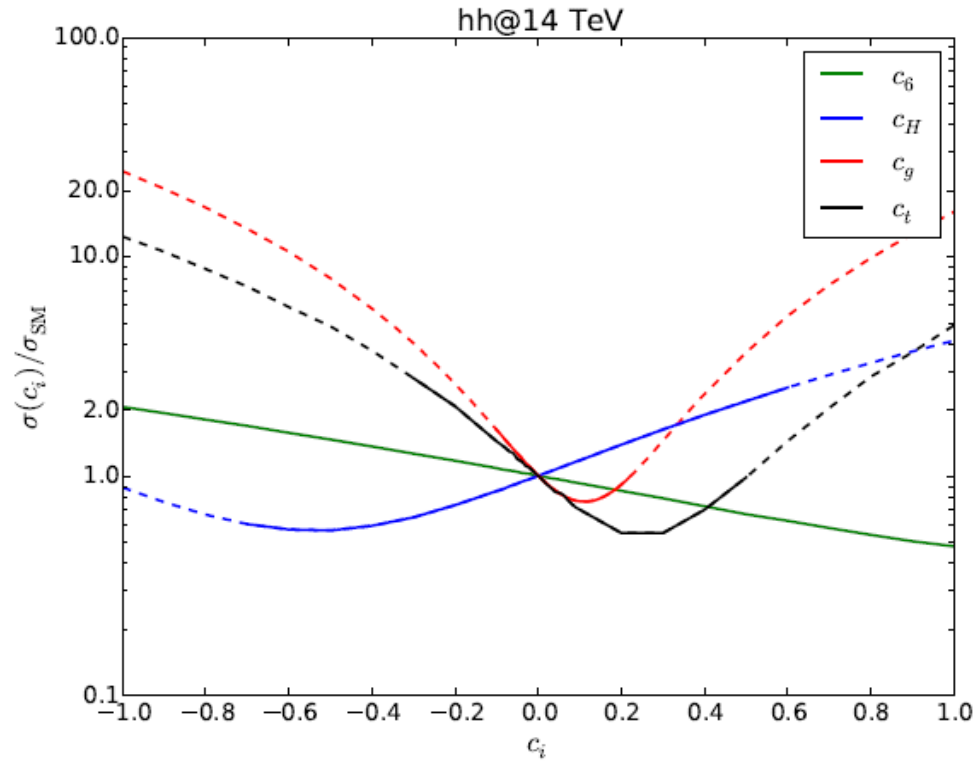


MSTW2008nlo\_nf4 PDF

- Effect of varying individual Wilson coefficients
- Dashed: parameter-range excluded from  $h$  data at the LHC  
 → used HiggsBounds, HiggsSignals on cross sections calculated via eHDECAY

Bechtle et.al., 1311.0055, 1305.1933

# $gg \rightarrow hh$ Cross Section



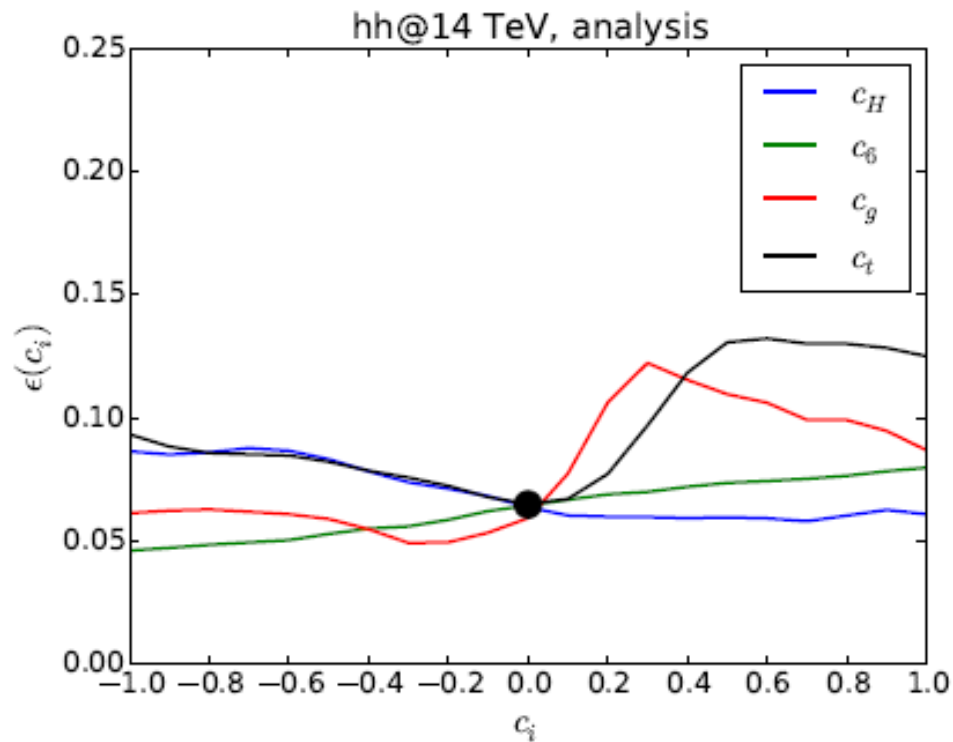
MSTW2008nlo\_nf4 PDF

$$\frac{d\hat{\sigma}(gg \rightarrow hh)}{d\hat{t}} \Big|_{\text{EFT}} = \frac{G_F^2 \alpha_s^2}{256(2\pi)^3} \left\{ \left| C_\Delta F_\Delta (1 - 2c_H + c_t + c_6) + 3F_\Delta (3c_t - c_H) + 2c_g C_\Delta \right. \right. \\ \left. \left. + C_\square F_\square (1 - c_H + 2c_t) + 2c_g C_\square \right|^2 + \left| C_\square G_\square \right|^2 \right\}$$

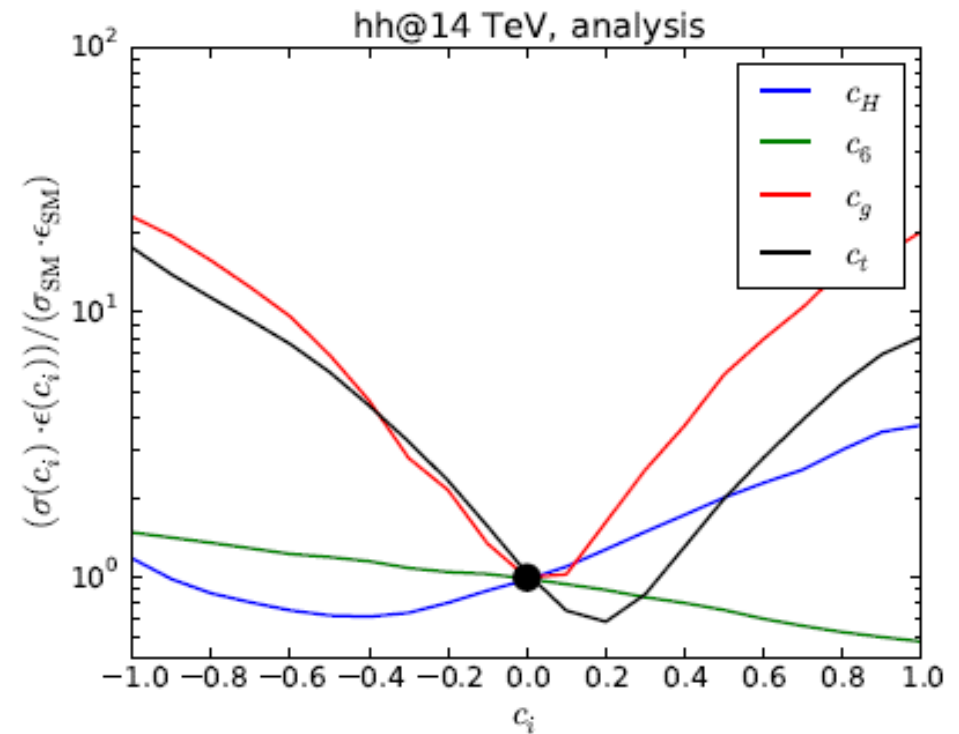


# $gg \rightarrow hh$ after cuts

Efficiency



Cross Section



MC generator important for analysis

→ describe distributions, which determine efficiencies  $\epsilon(c_i)$

# Full Analysis

- Start with model where only  $c_6 \neq 0$  (unconstrained from single  $h$ )
  - ↳ Vary only  $\lambda$  as done in previous studies ( $\rightarrow$  BRs unchanged)
    - $S(c_6)$  signal +  $B$  background events @ given  $L_{\text{int}}$
    - $N(c_6) = S(c_6) + B$ ,  $\delta N^2 = \delta S^2 + \delta B^2$

# Full Analysis

- Start with model where only  $c_6 \neq 0$  (unconstrained from single  $h$ )

↳ Vary only  $\lambda$  as done in previous studies ( $\rightarrow$  BRs unchanged)

- $S(c_6)$  signal +  $B$  background events @ given  $L_{\text{int}}$
- $N(c_6) = S(c_6) + B$ ,  $\delta N^2 = \delta S^2 + \delta B^2 + S^2 f_{\text{th}}^2$

$$\delta N^2 = N + S^2 f_{\text{th}}^2$$

# Full Analysis

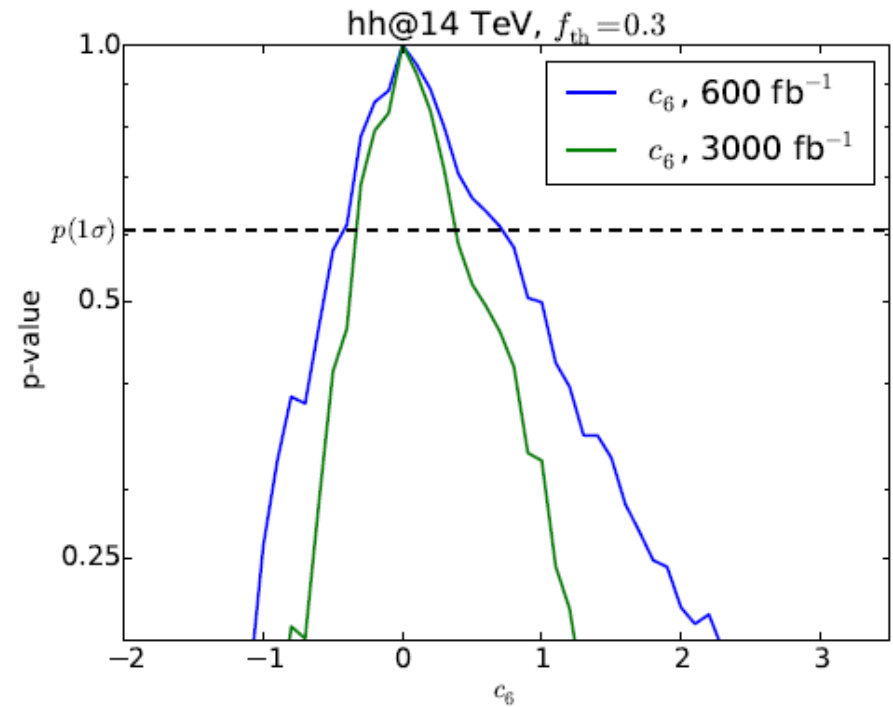
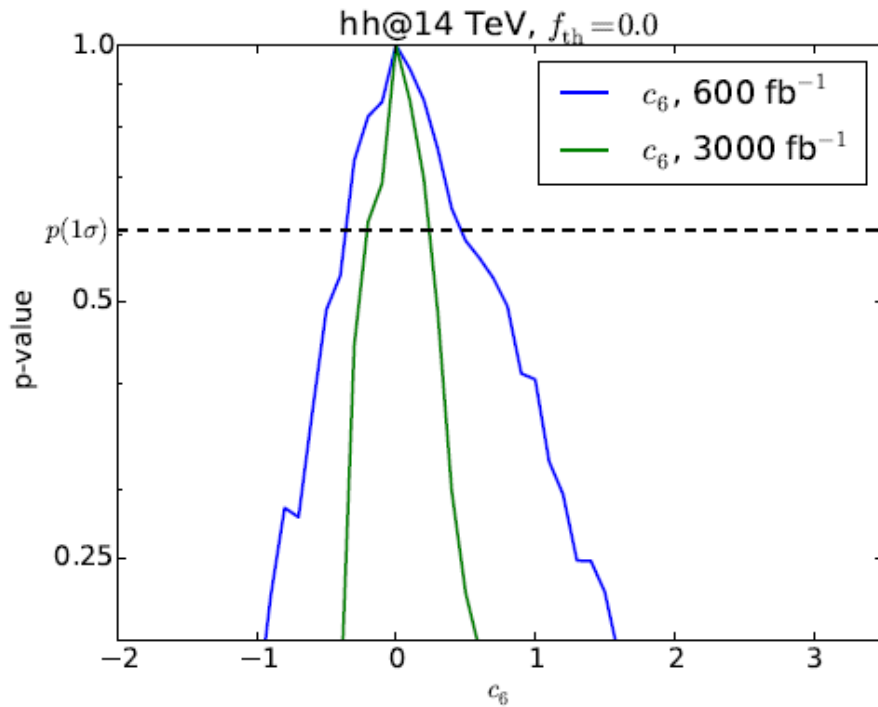
- Start with model where only  $c_6 \neq 0$  (unconstrained from single  $h$ )  
↳ Vary only  $\lambda$  as done in previous studies ( $\rightarrow$  BRs unchanged)

$$\delta N^2 = N + S^2 f_{\text{th}}^2$$

- Expected constraint on  $c_6$ , assuming the SM to be true ( $c_6=0$ ):

Compute how many standard deviations  $\delta N(c_6)$  away a given  $N(c_6)$ , as predicted from theory, is from  $N(c_6 = 0)$ .

# Full Analysis



$$c_6^{1\sigma}(600 \text{ fb}^{-1}) \in (-0.4, 0.5), \quad c_6^{1\sigma}(3000 \text{ fb}^{-1}) \in (-0.3, 0.3), \quad f_{th} = 0$$

$$c_6^{1\sigma}(600 \text{ fb}^{-1}) \in (-0.5, 0.8), \quad c_6^{1\sigma}(3000 \text{ fb}^{-1}) \in (-0.4, 0.4), \quad f_{th} = 0.3$$

$(c_6 > 0)$ —region more challenging as cross section reduced  $\rightarrow$  larger uncertainty

# Full $D=6$ Theory

- Similar as before, assume SM ( $c_i=0$ ) to be true and calculate distance of predicted  $N(c_6, \dots, c_b)$  from  $N(c_6 = 0, \dots, c_b = 0)$  in units of  $\delta N(c_6, \dots, c_b)$ .
- Show results in 2D grids  $(c_6, c_i)$ ,  $i=H,g,\gamma,t,b$
- Marginalize over other directions, varying the coefficients in the 95% CL allowed regions, obtained from HiggsBounds/Signals (with a Gaussian weight)

# Scan of the Parameter Space

- Show results in 2D grids  $(c_6, c_i)$ ,  $i=H,g,\gamma,t,b$
- Marginalize over other directions, varying the coefficients in the 95% CL allowed regions, obtained from HiggsBounds/Signals (with a Gaussian weight)

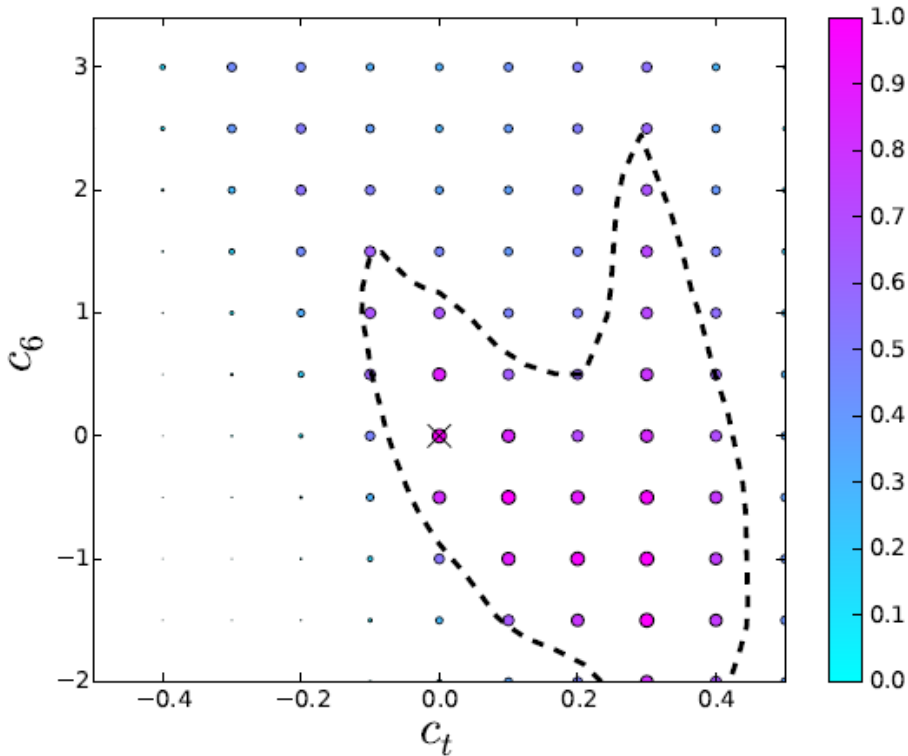
$$p(c_i, c_6) = \frac{\bar{p}(c_i, c_6)}{\max(\bar{p}(c_i, c_6))}, \quad \bar{p}(c_i, c_6) = \sum_{\{c_f\}} p(c_6, c_i, \{c_f\}) \times p_{\text{Gauss.}}(\{c_f\})$$

$$p_{\text{Gauss.}}(\{c_f\}) = \prod_f \frac{1}{\sigma_f \sqrt{2\pi}} \exp \left\{ -\frac{(x_f - \mu_f)^2}{2\sigma_f^2} \right\}$$

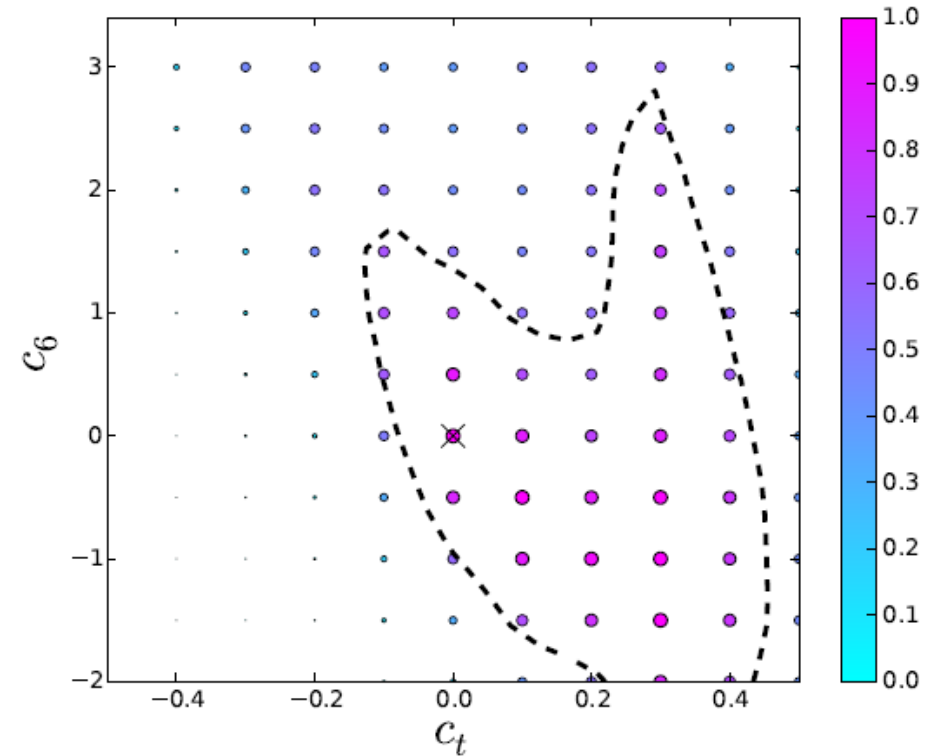
- Draw iso-contours corresponding to probability-drop of  $1\sigma$

# Results: $c_t - c_6$

hh@14 TeV,  $L = 600\text{fb}^{-1}$ ,  $f_{\text{th}}=0.0$ , gaussian



hh@14 TeV,  $L = 600\text{fb}^{-1}$ ,  $f_{\text{th}}=0.3$ , gaussian

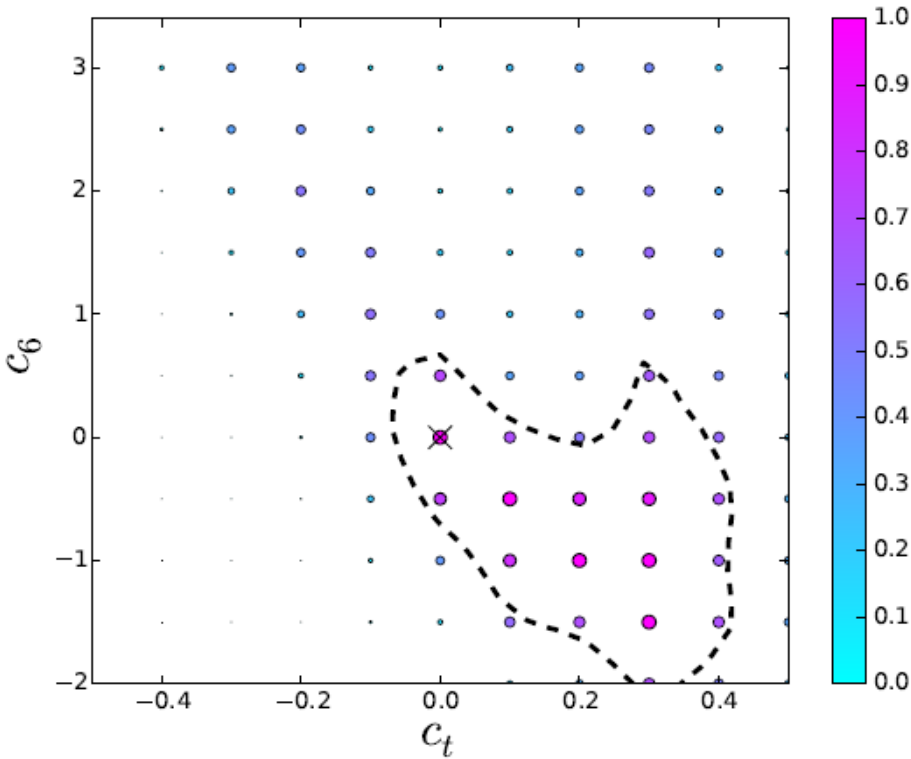


- *Clear correlation visible: Enhanced hh cross section due to negative  $c_t$  can be compensated by reduction due to positive  $c_6$*

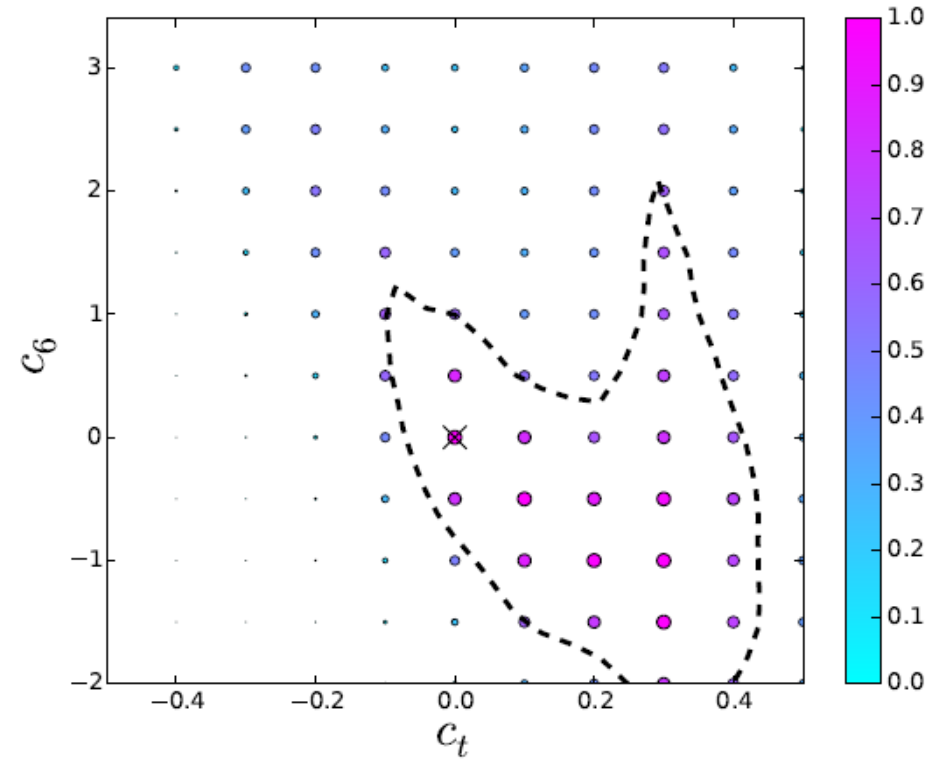


# $c_t - c_6$

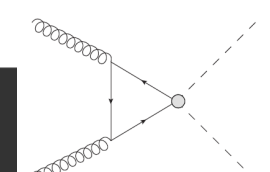
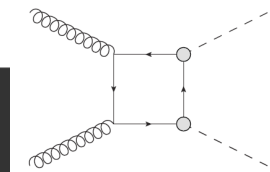
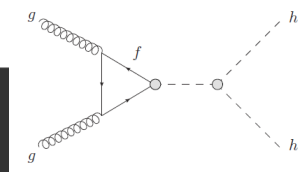
hh@14 TeV,  $L = 3000\text{fb}^{-1}$ ,  $f_{\text{th}}=0.0$ , gaussian



hh@14 TeV,  $L = 3000\text{fb}^{-1}$ ,  $f_{\text{th}}=0.3$ , gaussian

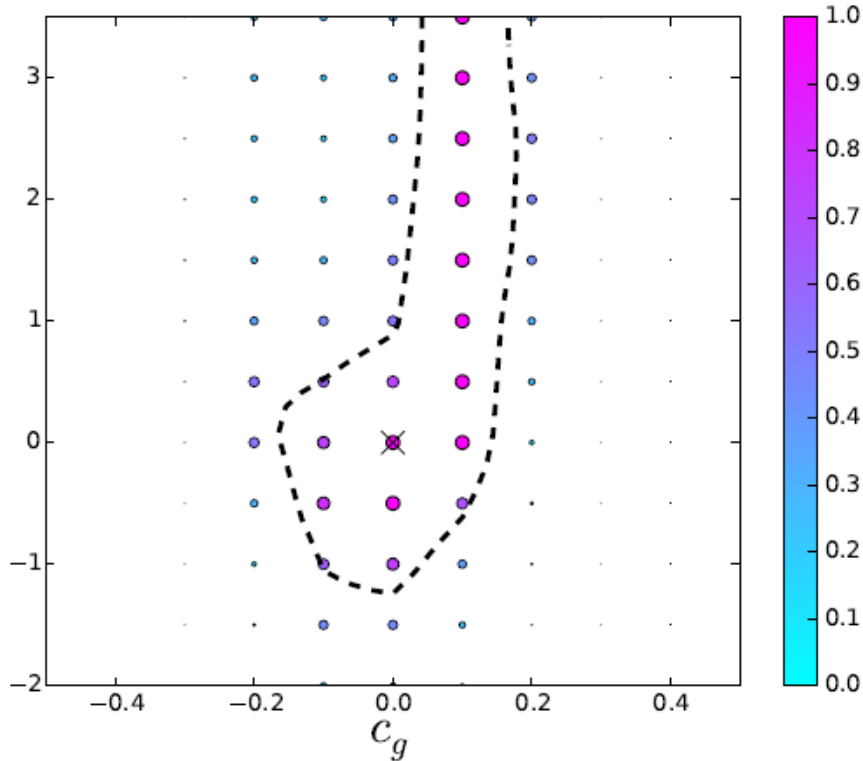


- Better knowledge on 'top Yukawa'  $c_t$  helpful to improve the range for  $c_6$
- On the other hand, could also obtain meaningful information on  $c_t$  in hh

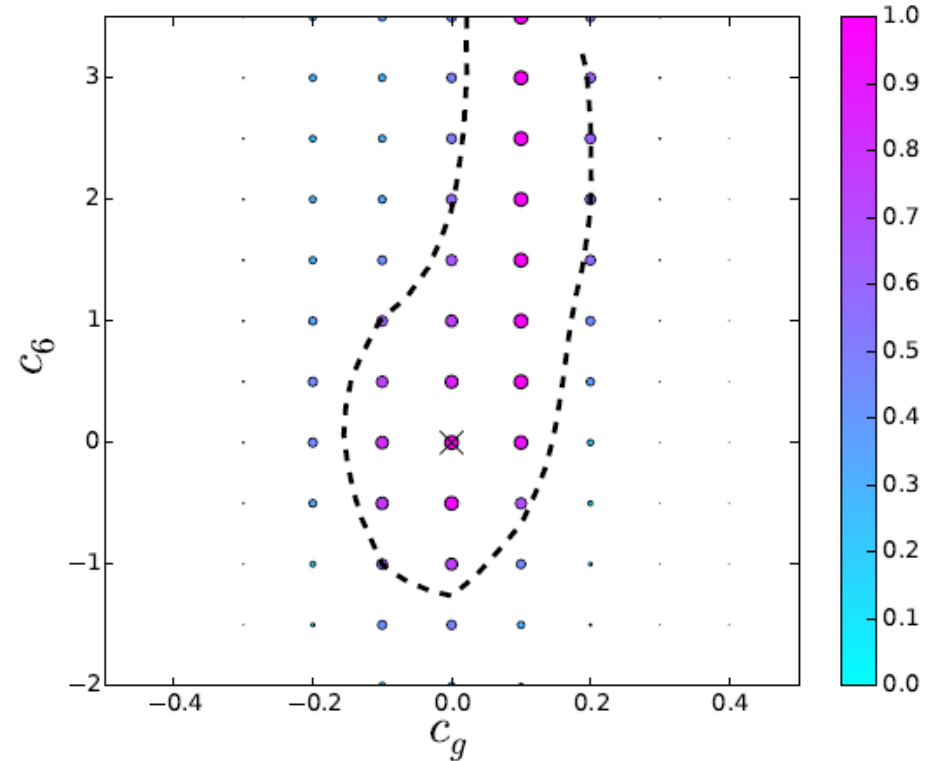


$$c_9 - c_6$$

hh@14 TeV,  $L = 3000\text{fb}^{-1}$ ,  $f_{\text{th}}=0.0$ , gaussian



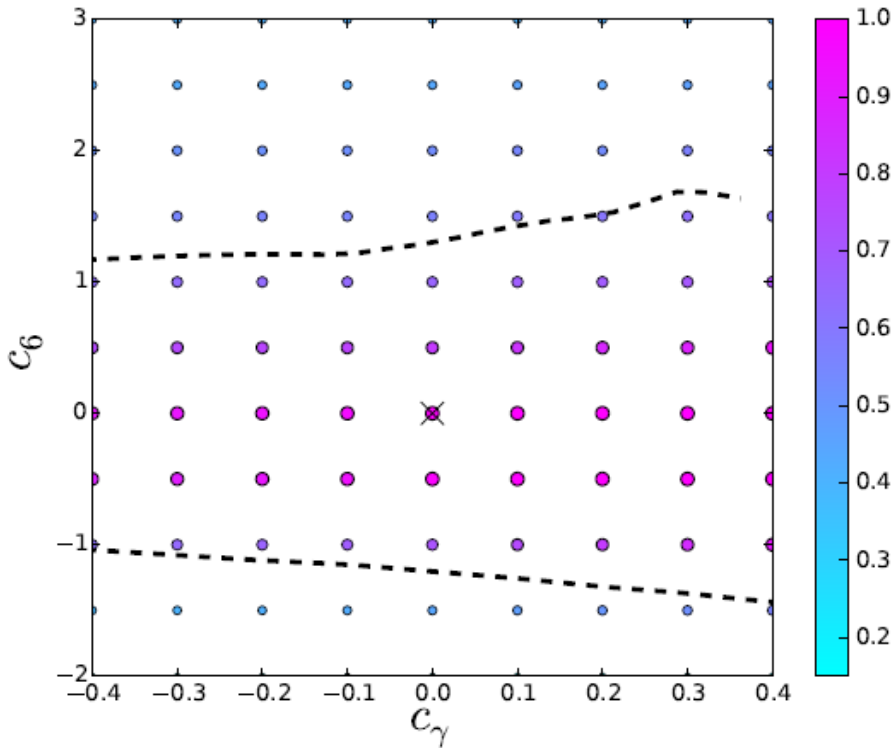
hh@14 TeV,  $L = 3000\text{fb}^{-1}$ ,  $f_{\text{th}}=0.3$ , gaussian



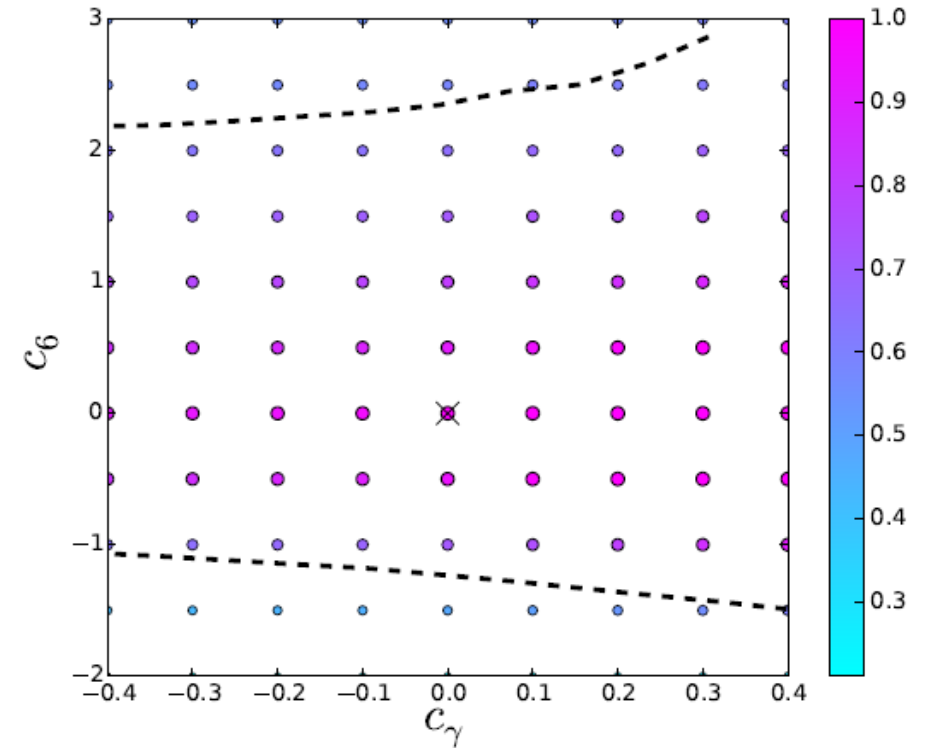
- Again compensation of effects from different operators possible  
 → range for  $c_6$  depends significantly on other coefficients

# $c_\gamma - c_6$

hh@14 TeV,  $L = 3000\text{fb}^{-1}$ ,  $f_{\text{th}}=0.0$ , gaussian

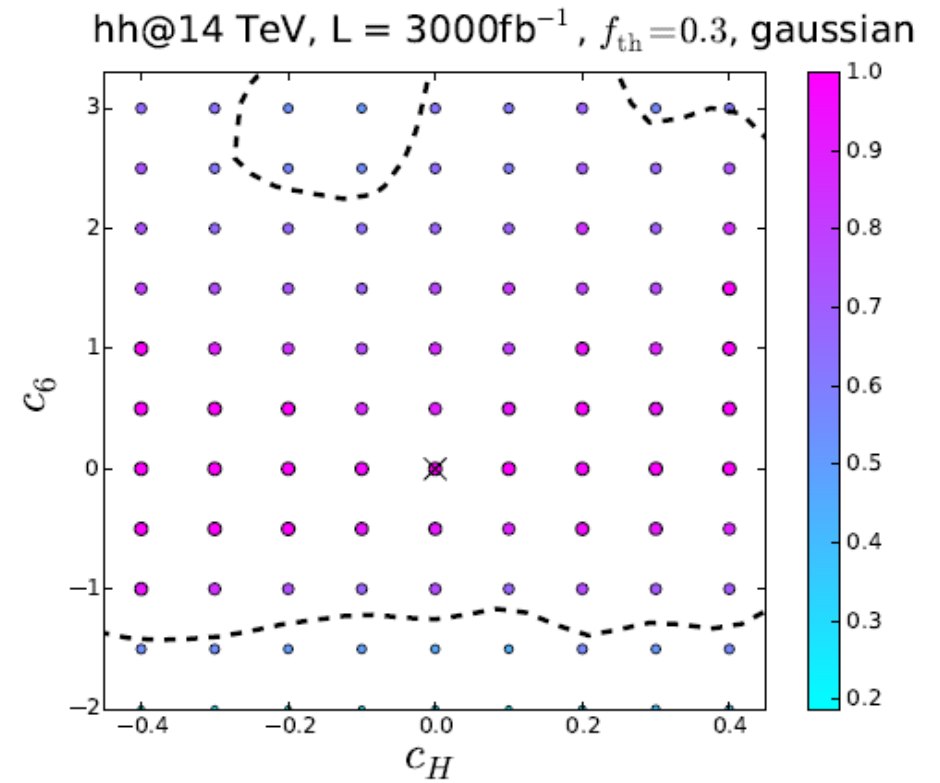
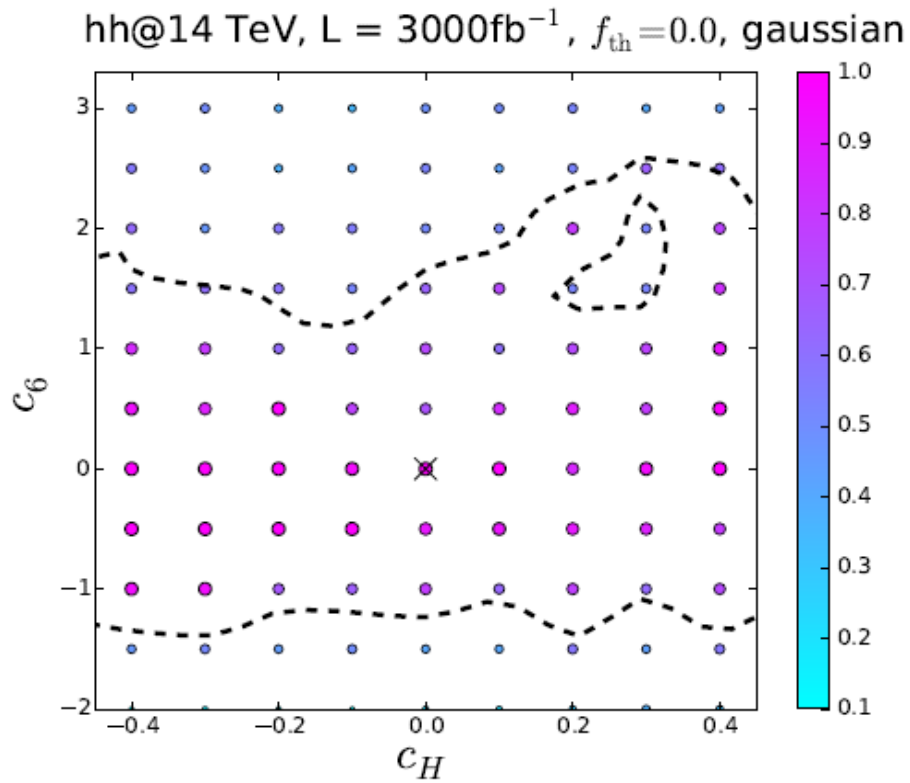


hh@14 TeV,  $L = 3000\text{fb}^{-1}$ ,  $f_{\text{th}}=0.3$ , gaussian



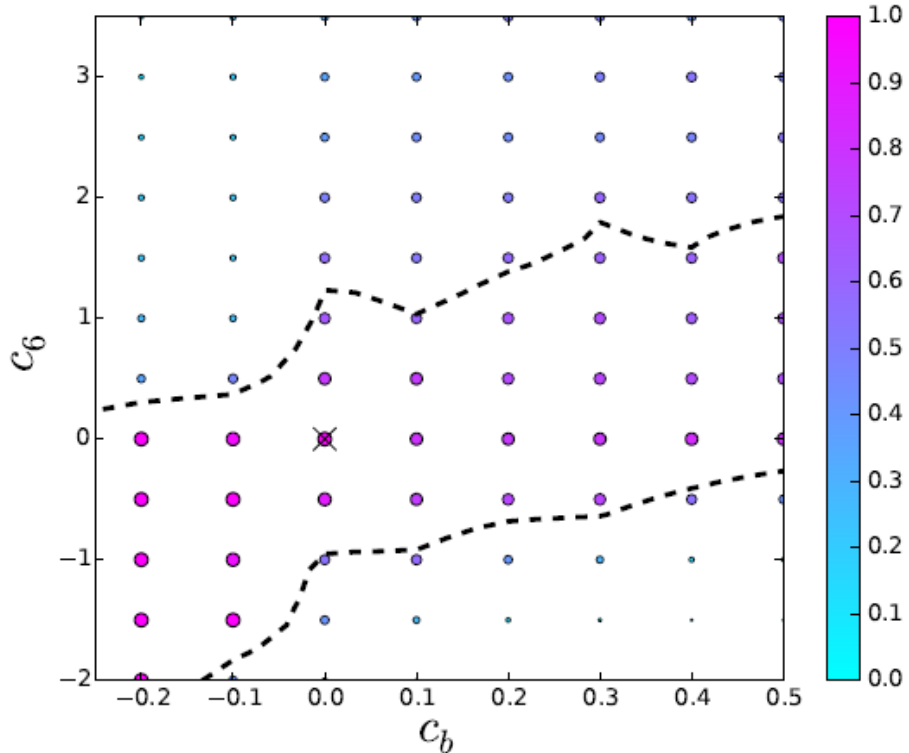
- As expected very weak correlation: only indirectly through dependence of allowed range in  $c_g$  on value of  $c_\gamma$

# $c_H^{-1} c_6$

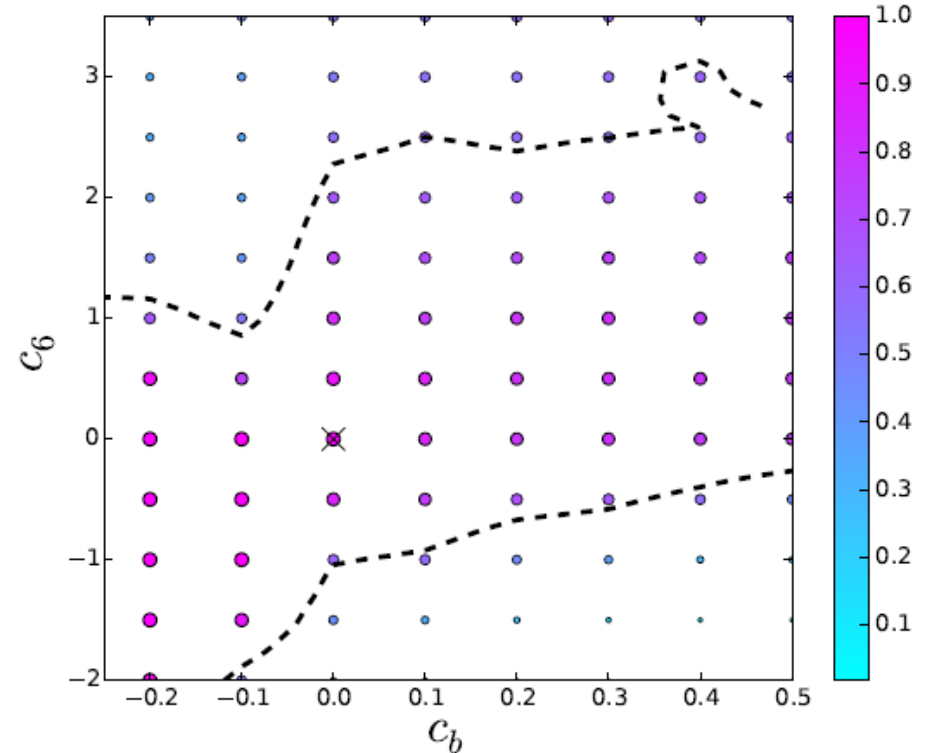


$$(c_b = c_\tau) - c_6$$

hh@14 TeV,  $L = 3000\text{fb}^{-1}$ ,  $f_{\text{th}} = 0.0$ , gaussian

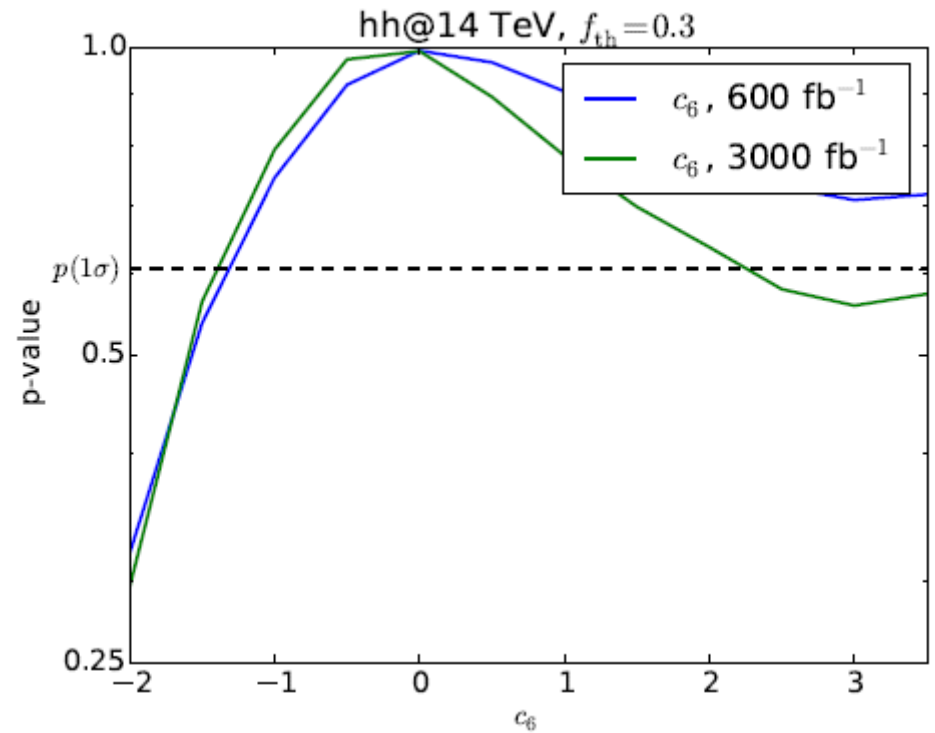
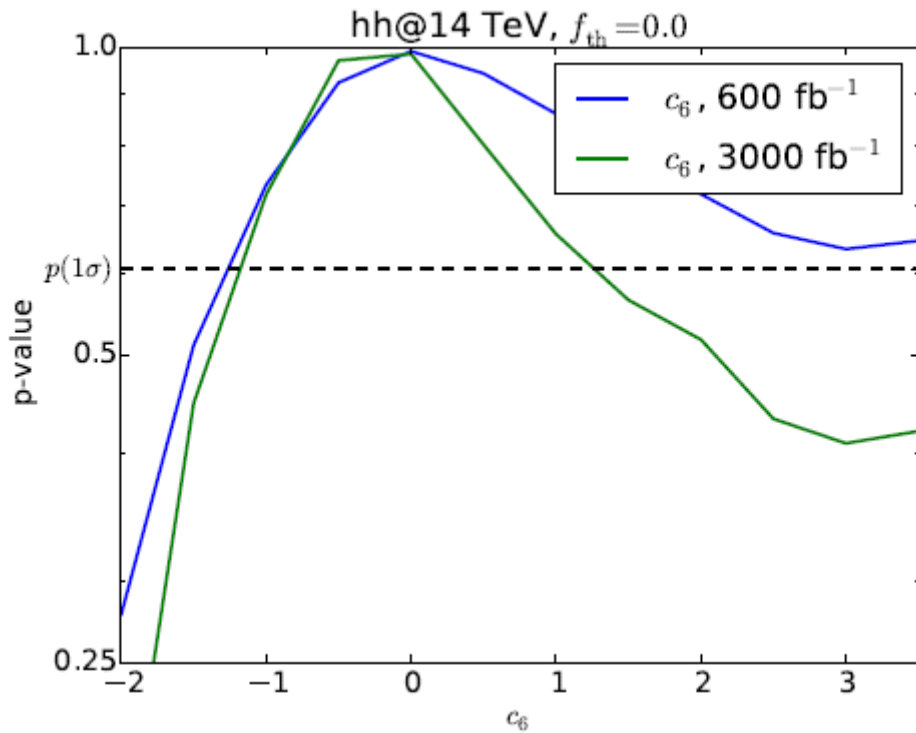


hh@14 TeV,  $L = 3000\text{fb}^{-1}$ ,  $f_{\text{th}} = 0.3$ , gaussian



- Reduced BR due  $(c_b = c_\tau) < 0$  to can be compensated by enhanced production cross section due to negative  $c_6$  and vice versa

# Full Marginalization $\rightarrow c_6$



# Final Results

Expected  $1\sigma$  constraints at the 14 TeV LHC, assuming  $f_{th} = 30\%$

model	$L = 600 \text{ fb}^{-1}$	$L = 3000 \text{ fb}^{-1}$
$c_6$ -only	$c_6 \in (-0.5, 0.8)$	$c_6 \in (-0.4, 0.4)$
full	$c_6 \gtrsim -1.3$	$c_6 \in (-1.2, 2.4)$

# Conclusions and Outlook

Analysis of hh productions can offer viable additional information on the  $D=6$  extension of the SM

## Some Future Directions:

- Optimize analysis for different regions of parameter space
- Break degeneracy  $c_b=c_\tau$ /consider different projections
- Include other decay channels
- Consider distributions to improve bounds



# Backup: Hbounds/Signals Ranges

coefficient	$\mu_f$	$\sigma_f$
$c_H$	-0.035	0.225
$c_t$	-0.04	0.17
$c_b$	0.0	0.18
$c_g$	-0.01	0.06
$c_\gamma$	-0.25	0.62