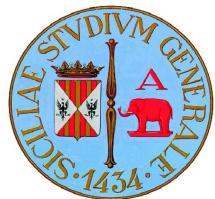


Heavy Flavor Dynamics in Hot QCD matter



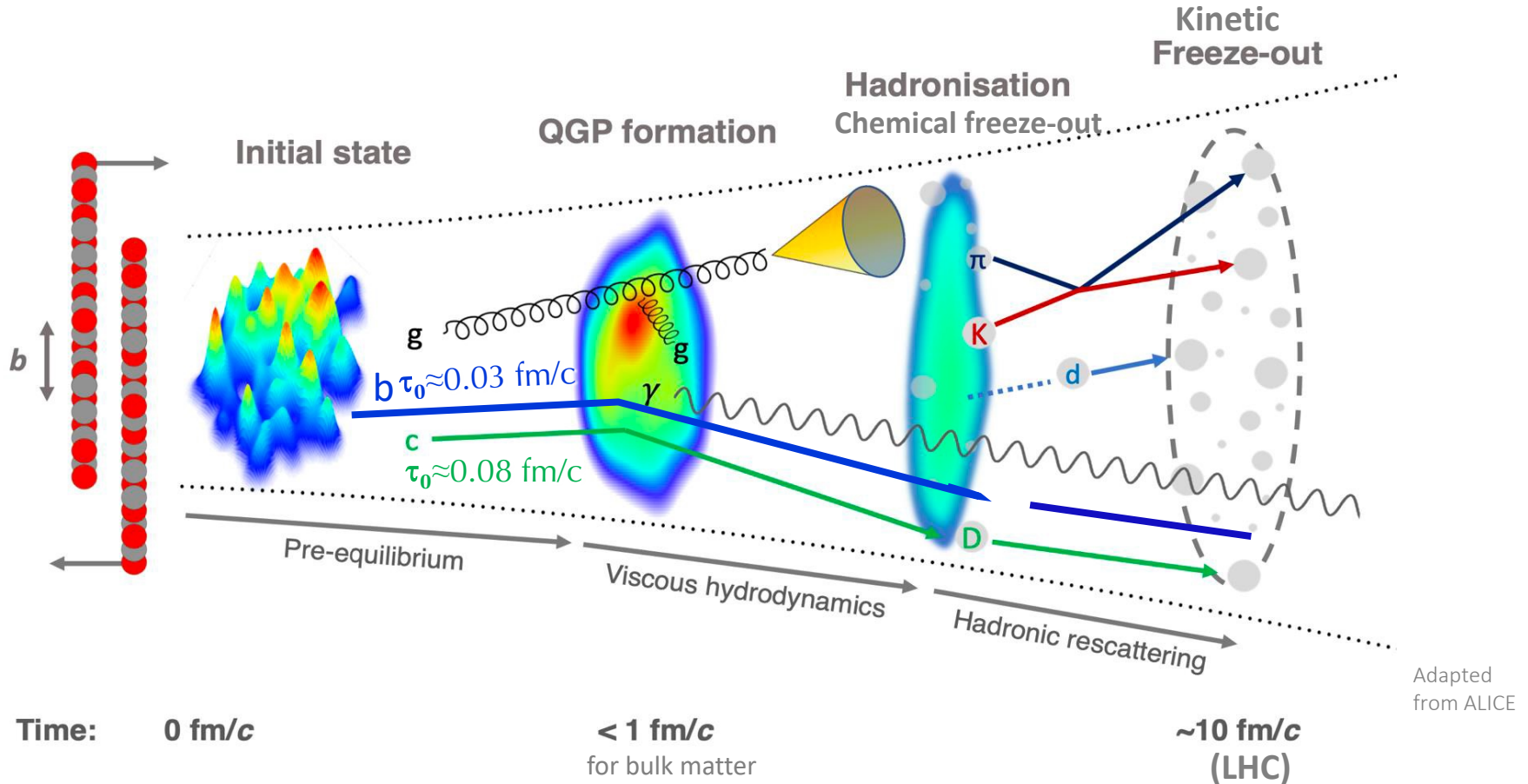
Vincenzo Greco –
University of Catania/INFN-LNS



Collaborators:

- V. Minissale, L. Oliva, S. Plumari, M. Ruggieri, M.L. Sambaturo
- S.K. Das (Ghoa)
- D. Avramescu, T. Lappi (Jyvaskyla)

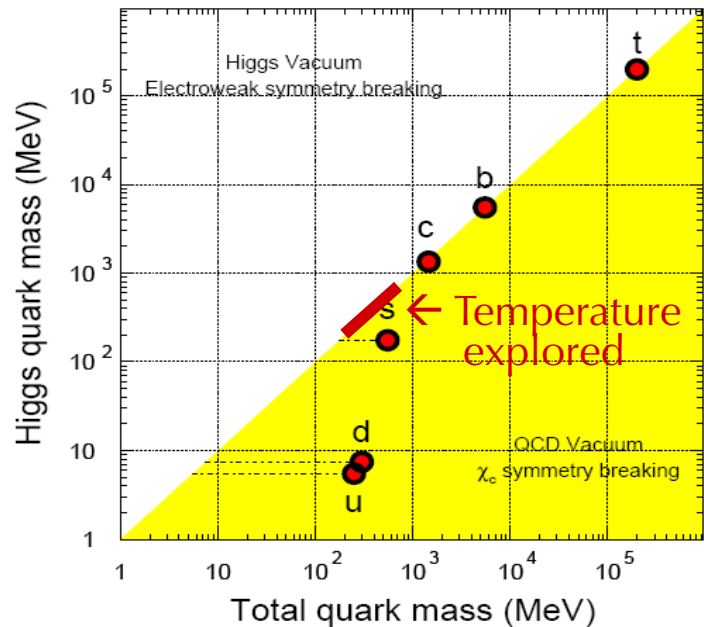
Sketch of Time evolution of uRHICs



Outline

- ✧ **Basic concepts & motivation for HQ physics in uRHICs**
- ✧ **Results from the first & second stage:**
 - strong non-perturbative HQ dynamics [agreement to LQCD?!, close to AdS/CFT limit?]
 - non-universal hadronization in AA $\neq$ e^+e^- seems so already for pp@TeV
- ✧ **Next steps:** low p_T , extension to b & access to new observables
- ✧ **HQ as probe of Glasma early stage phase**

Basic Scales and specific of HQ



Why Heavy?

- *PARTICLE Physics*: $m_{c,b} \gg \Lambda_{\text{QCD}}$ pQCD initial production
- *PLASMA Physics*:
 - $m_{c,b} \gg T_{\text{RHIC,LHC}}$ no thermal production
 - $m_{c,b} \gg gT_{\text{RHIC,LHC}}$ soft scatterings → Brownian motion

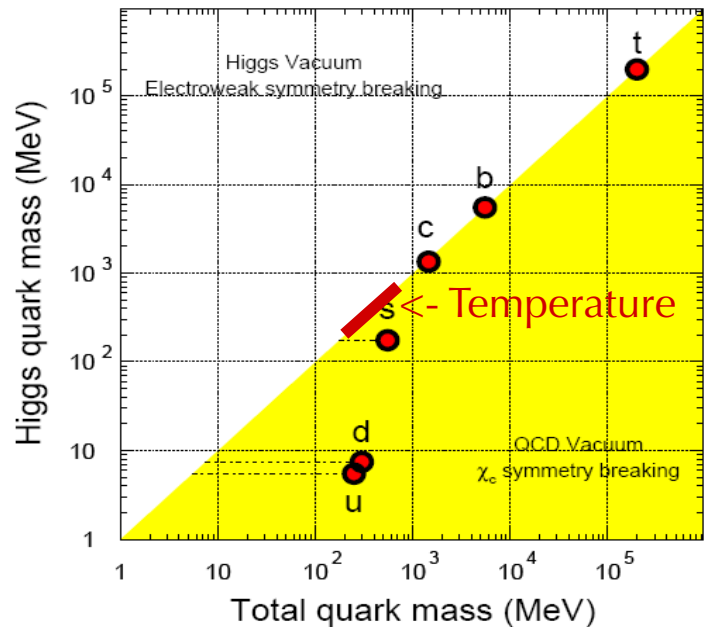
Specific Features:

- $\tau_0 \approx 1/2m_Q$ ($< 0.1 \text{ fm}/c$) $\ll \tau_{\text{QGP}}$ witness of all QGP evolution
- $\tau_{\text{th}} \approx \tau_{\text{QGP}} \gg \tau_{q,g}$ carry more information of their evolution

Reviews:

- F. Prino and R. Rapp, JPG (2019)
- X. Dong and VG, Prog.Part.Nucl.Phys. (2019)
- Jiaxing Zhao et al., Prog.Part.Nucl.Phys. (2020)

Basic Scales and specific of HQ



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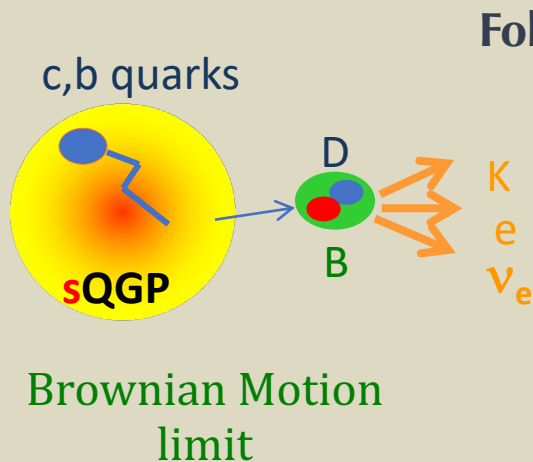
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* For HQ we know initial p_T distribution at variance with light quark & gluons

* HQ not created at hadronization by string breaking + const. quarks close to energy conservation

Standard Dynamics of Heavy Quarks in the QGP



Fokker-Planck approach ($T \ll m_Q$)
in Hydro/transport bulk

$$\frac{\partial f_{c,b}}{\partial t} = \gamma_{\text{drag}} \frac{\partial (p f_{c,b})}{\partial p} + D_p \frac{\partial^2 f_{c,b}}{\partial p^2}$$

$$\langle p \rangle = p_0 e^{-\gamma t}$$

$$\langle \Delta p^2 \rangle = 3D_p / \gamma(1 - e^{-2\gamma t})$$

$$D_p = ET\gamma - \text{Fluct. Diss. Theor.}$$

Space diffusion
coefficient

$$D_s = \frac{T}{M\gamma} = \frac{T^2}{D_p} = \frac{T}{M} \tau_{th}$$

$$\gamma = \int d^3k |M(k, p)|^2 p$$

$$D = \frac{1}{2} \int d^3k |M(k, p)|^2 p^2$$

$|M|^2$ scatt. matrix from:
HTL, pQCD coll., rad., T-matrix,
QPM, NREFT, AdS/CFT...

- ✧ This is the main set up at least at $p_T < 6-8$ GeV
- ✧ Brownian motion challenged for charm ($M_c \sim 3 T \sim gT$) $\rightarrow$ Relativistic Boltzmann dynamics
- ✧ At $p_T > 10$ GeV radiative E_{loss} , q_{had} , jet physics

HQ link to Lattice QCD at finite T

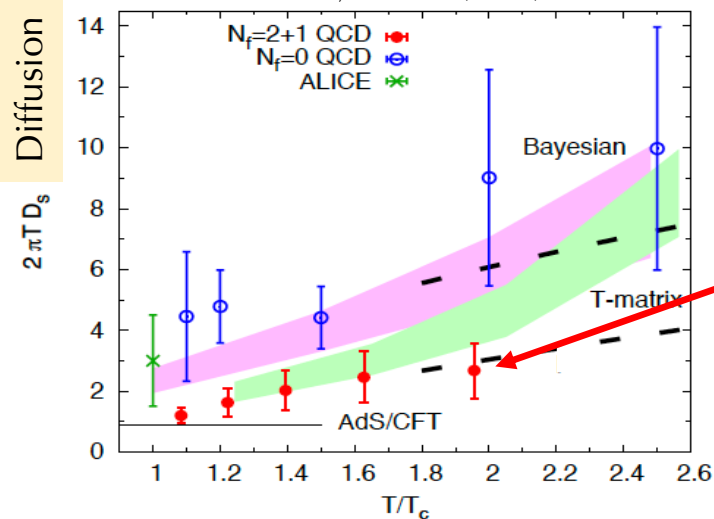
❖ Ab-initio Diffusion Transport Coefficient

Spectral function ρ_E extracted from euclidean color-electric correlator $D_E(\tau) \rightarrow$

Kubo formula diffusion in the $p \rightarrow 0$ limit:

$$\frac{D_p}{T^3} = \lim_{\omega \rightarrow 0} \frac{T \rho_E(\omega)}{\omega} \rightarrow D_s = \frac{T^2}{D_p} = \frac{T}{M_Q \gamma} = \frac{T}{M_Q} \tau_{th}$$

L. Altenkort et al., PRL131 (2024)

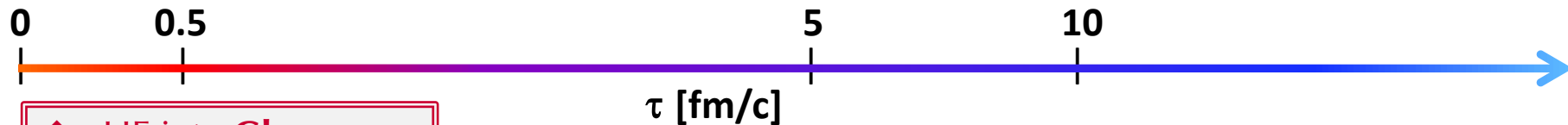


Approximations/limitations:

- Extraction of $\rho_E(\omega)$ from $D_E(\tau)$ is not a well posed problem with a finite limited # of points
- infinite HQ mass vs. charm quark, continuum extrapolation...
- quenched $N_f=0 \rightarrow$ to non quenched QCD (2023-24)

HQ allow for developing a NRQCD EFT at finite T
& many-body T-matrix from $V(r,T)$ by LQCD

Studying the HF in uRHIC



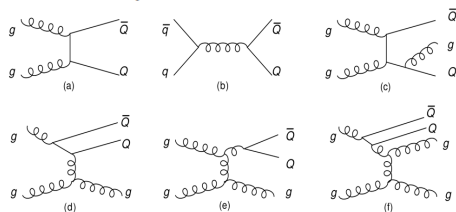
- ❖ HF into **Glasma**
- ❖ HF under **e.m. field**
- ❖ HF under vorticity

$\tau_0 < 0.1$ fm/c

• initial production

- pQCD-NLO
- MC-NLO, POHWEG
- CNM effect [pp,pA exp.]

$$d\sigma^{Q+X} \simeq \sum_{i,j} f_i^A \otimes f_j^B \otimes d\tilde{\sigma}_{ij \rightarrow Q+X}$$



• Dynamics of HF in QGP

- Thermalization
- Transp. Coeff. of QCD matter $D_s(T)$
- Radiative E_{loss} & Jet Quenching

B, D, Λ_c

b, c

$\underline{b}, \underline{c}$

$\underline{B}, \underline{D}, \underline{\Lambda}_c$

Adapted from
Rapp & Greco

• Hadronization

- coalescence and/or fragm.
- large Λ_c/D in pp,pA,AA
→ affects observables

How HQ interact with the medium [low-medium p_T]

❖ 3 kinds of approaches:

a) pQCD inspired + HTL

[Nantes(+rad.) ... Torino, LBL-Duke]

LO diagrams, propagator with reduced IR regulator

$(q^2 - \kappa m_d^2(T))^{-1}$ match **soft scale** resummed in **HTL**

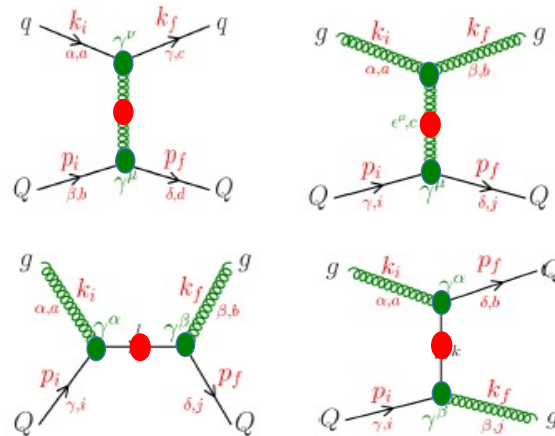
b) Quasi Particle Model + tree level diagrams

[Catania, Frankfurt-PHSD, QLBT o CoLBT,...]

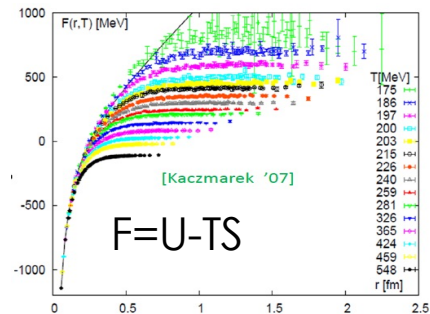
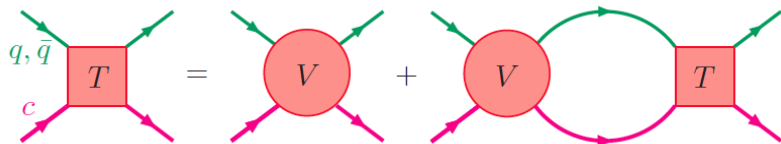
$g(T)$ from a fit to lQCD-EoS

screened propagators with $m_D \sim gT$

Tree-level with vertex $g(T)$
& propagators renormalized



c) T-matrix: scattering under $V(r,T)$ deduced from lQCD (TAMU)

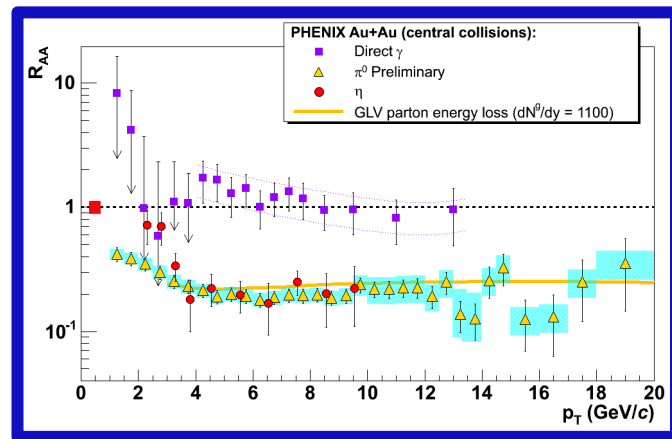


Two Main Observables in HIC

❖ Nuclear Modification factor

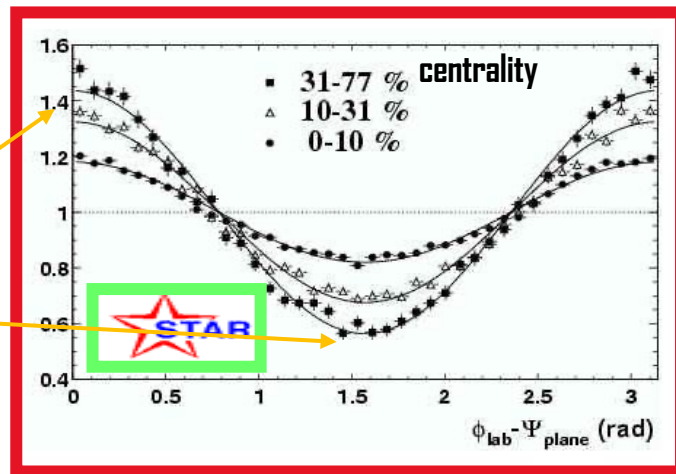
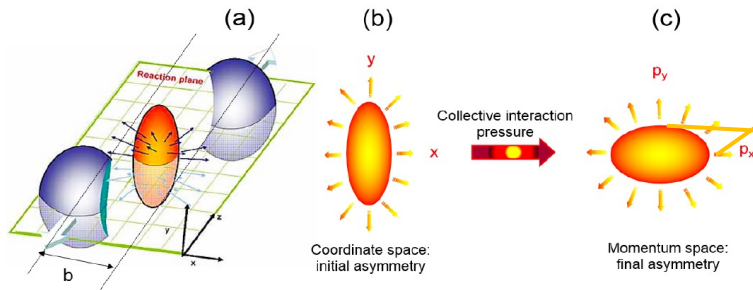
$$R_{AA}(p_T) = \frac{d^2 N^{AA} / dp_T d\eta}{N_{coll} d^2 N^{NN} / dp_T d\eta}$$

- Modification respect to pp
- Decrease with increasing partonic interaction



❖ Anisotropy p-space: Elliptic Flow v_2

$$\frac{dN}{p_T dp_T d\phi} = \frac{dN}{2\pi p_T dp_T} [1 + 2v_2 \cos(2\phi) + \dots]$$

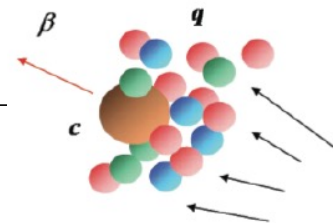


What was the expectation for charm?

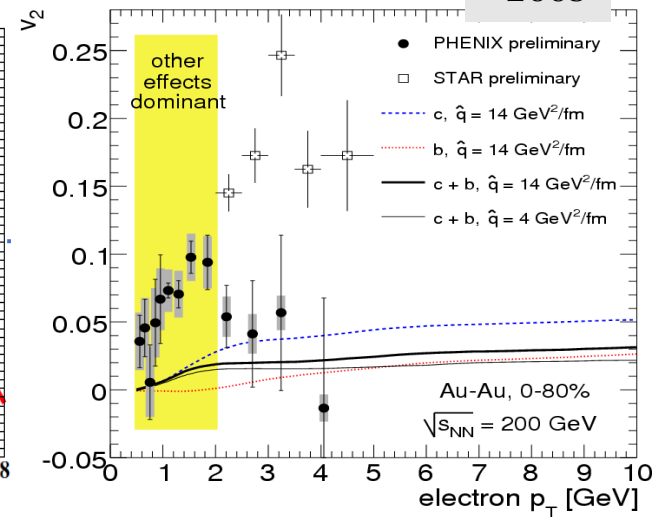
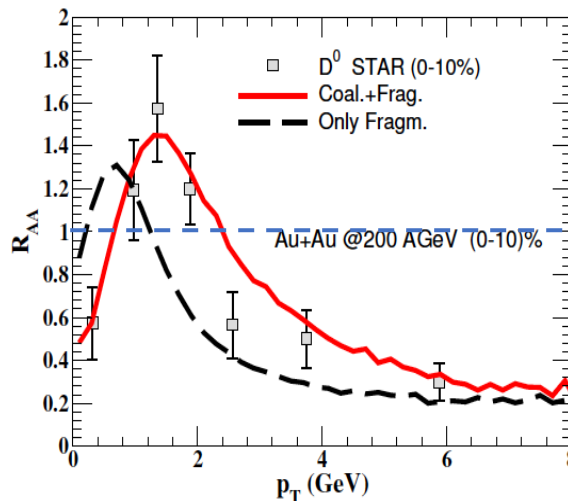
QGP created is made by 99% of $q=u,d,s$, + Charm Quarks $<1\%$

$m_q \approx 0.01 \text{ GeV}$ & $M_c \approx 1.3 \text{ GeV} \rightarrow$ poorly dragged & long thermalization time :

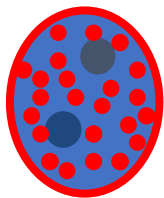
In LO-pQCD $\tau_{c,therm} \approx 20 \text{ fm/c} \gg \tau_{QGP} \gg \tau_{q,therm} \approx O(1) \text{ fm/c} \rightarrow R_{AA} \sim 1$ and $v_2 \sim 0$



For plasma conditions realistically obtainable in the nuclear collisions ($T \sim 250 \text{ MeV}$, $g=2$) $\rightarrow$ *effective masses* $m_{q,g}^* \sim gT \sim 500 \text{ MeV}$



R_{AA} & v_2 with upscaled pQCD cross section



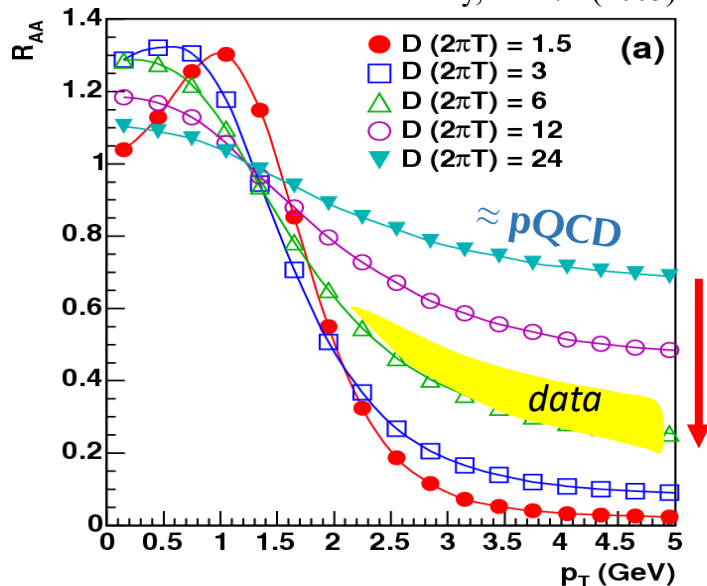
Fokker-Plank for charm
interaction in a hydro bulk

Diffusion coefficient

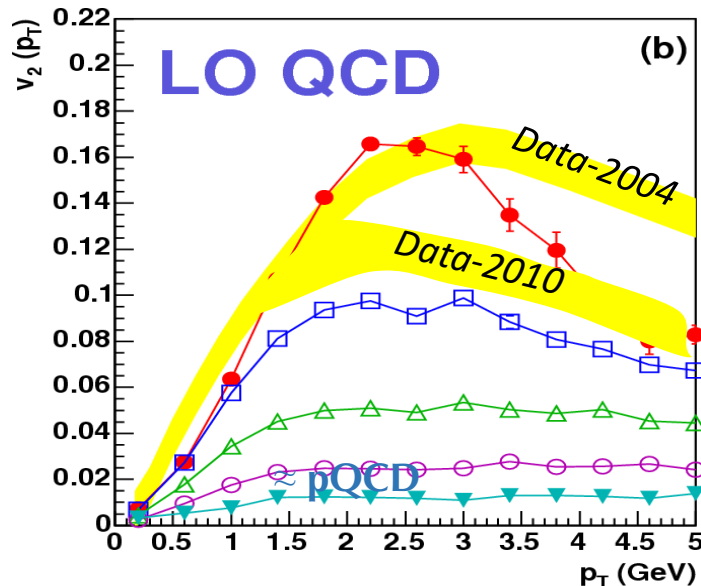
$$D_p \propto \int d^3k \left| M_{g(q)c \rightarrow g(q)c}(k, p) \right|^2 k^2$$

scattering matrix

Moore & Teaney, PRC71 (2005)



Multiplying by
a K-factor pQCD

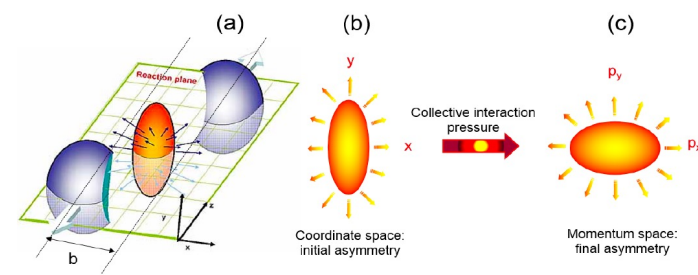


It's not just a matter of pumping up pQCD elastic cross section:
too low R_{AA} or too low v_2

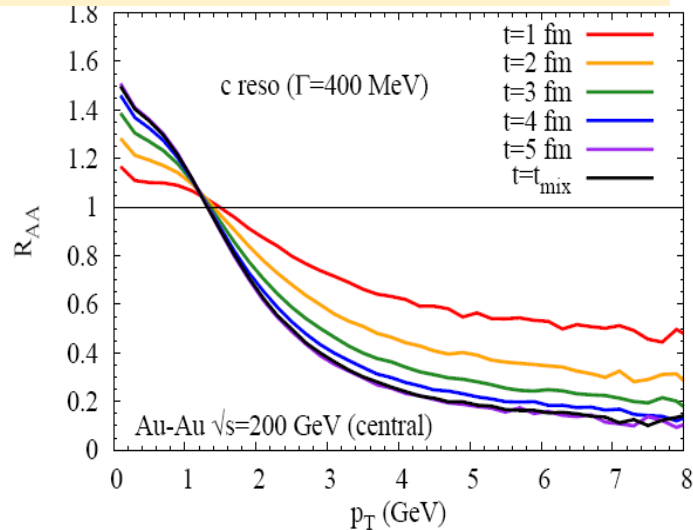
R_{AA} and v_2 evolution & correlation

No interaction means $R_{AA}=1$ and $v_2=0$.
more interaction decrease R_{AA} and increase v_2

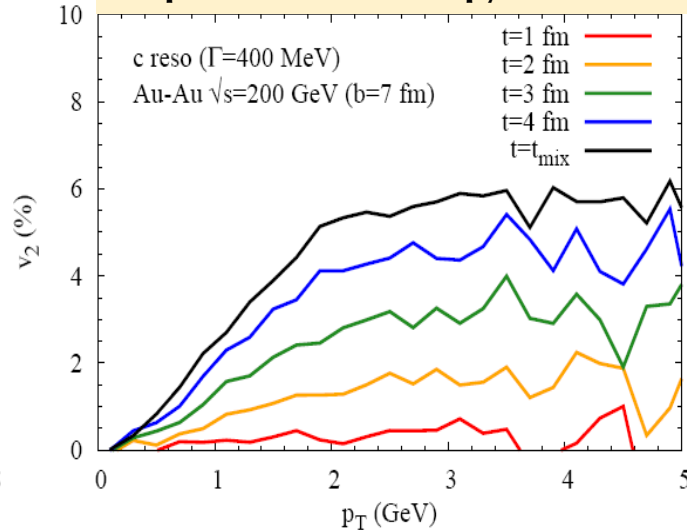
R_{AA} is “generated” faster than v_2



R_{AA} Ratio normalized p_T spectra pp/AA



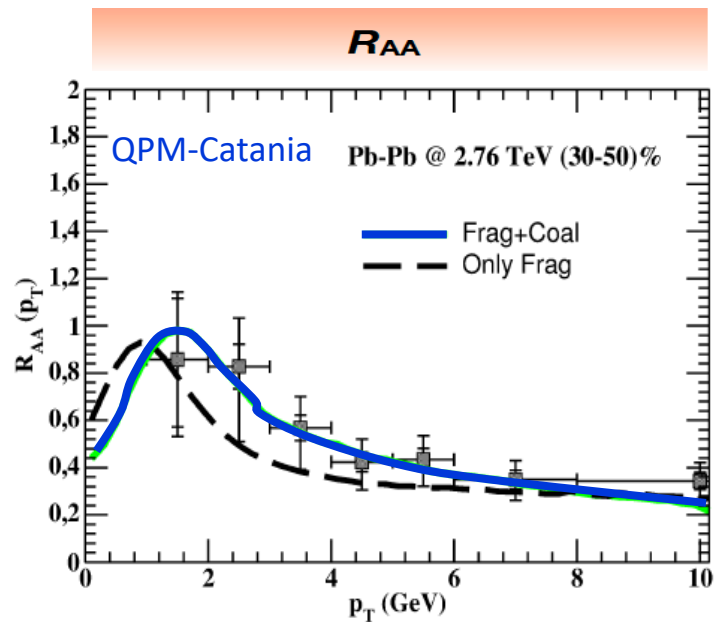
Elliptic Flow: Anisotropy Azimuthal emission



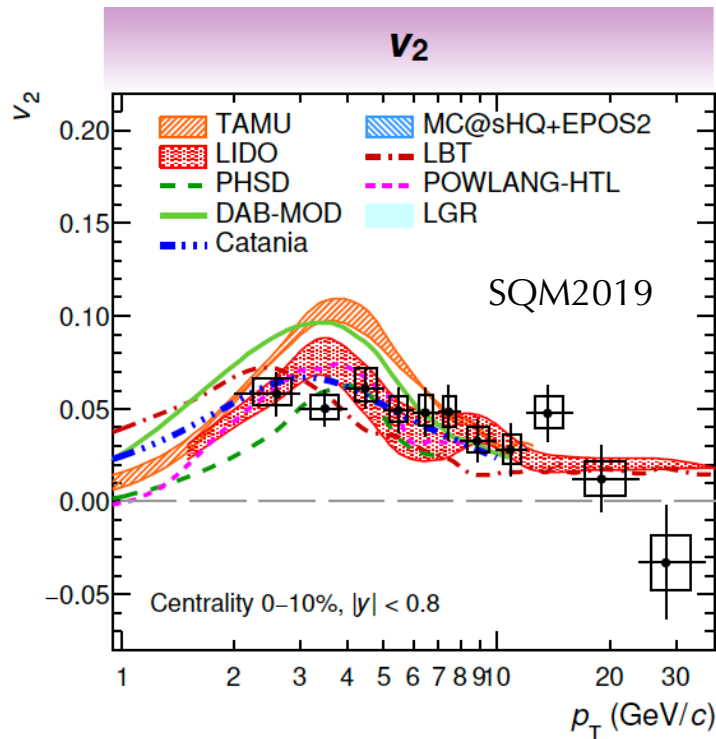
v_2 formation time $t \sim R$
+
for HQ come from
The drag of QGP fluid

The relation between R_{AA} and time is not trivial and is driven by the time (temperature) dependence of the interaction.

Studying charm in uRHICs – after Run 2



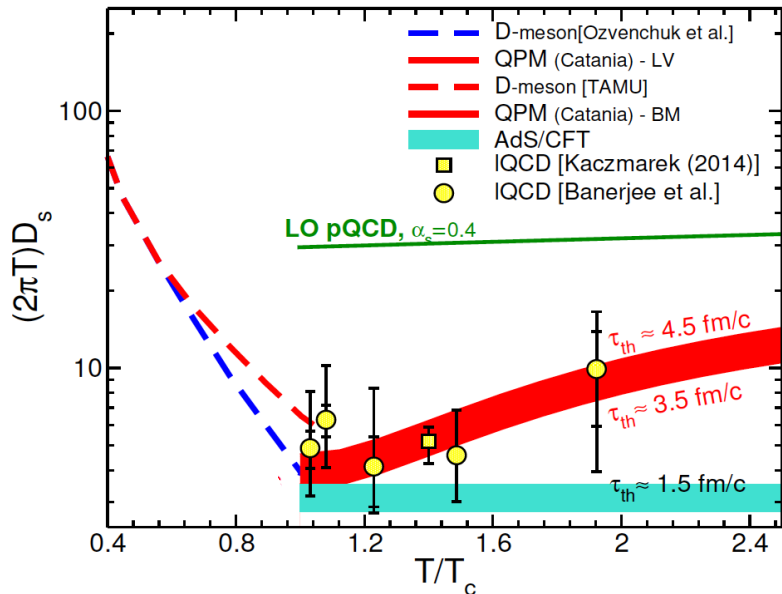
Scardina et al., PRC96(2017)



Note: early data $p_T > 1.5$ -2 GeV with significant error bars

Diffusion Coefficient of Charm Quark: first stage

uRHIC created matter is the **Hot QCD matter not in perturbative regime!**



X. Dong and VG, Prog.Part.Nucl.Phys. (2019)

- ❖ Largely non-perturbative D_s (close AdS/CFT) even if $M_Q \gg \Lambda_{\text{QCD}}$, m_q (bare)
 $\tau_{\text{th}}(\text{charm}, p \rightarrow 0) < 5 \text{ fm/c}$

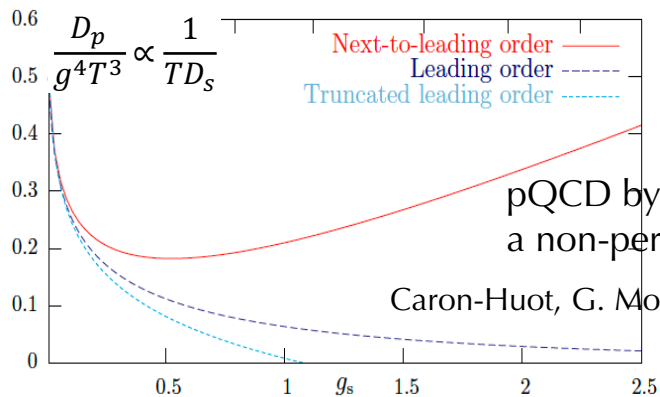
$$\tau_{th} = \frac{M}{2\pi T^2} (2\pi T D_s) \cong 1.8 \frac{2\pi T D_s}{(T/T_c)^2} \text{ fm/c}$$

pQCD, Asymptotic free regime

Not a model fit to IQCD data!

Phenomenology R_{AA} & $v_2 \approx$ Lattice QCD

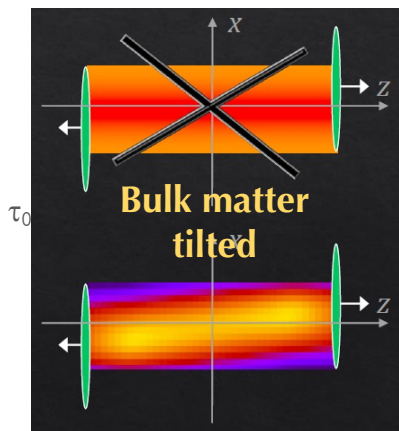
Infinite Strong Coupling (AdS/CFT)



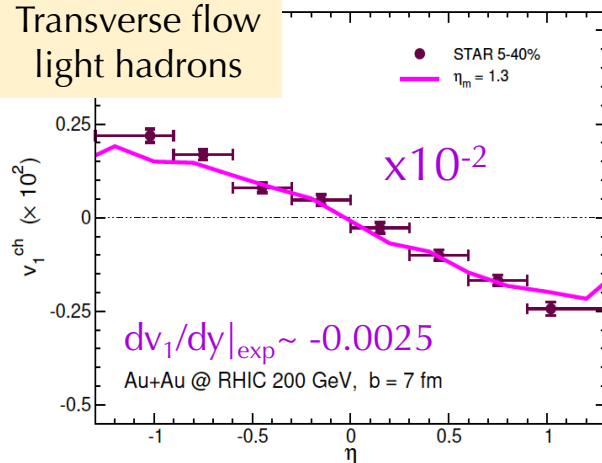
pQCD by itself indicates a non-pert. behavior

Caron-Huot, G. Moore, JHEP(2008)

HQ Surprise also in the transverse flow $v_1 = \langle p_x / p_T \rangle$



Transverse flow
light hadrons

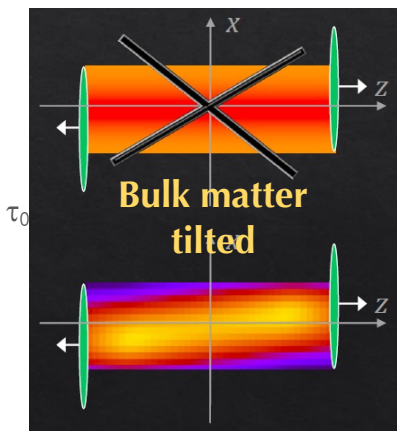


Would you expect charm quark to have a smaller v_2 ? Or a smaller one due to its mass?

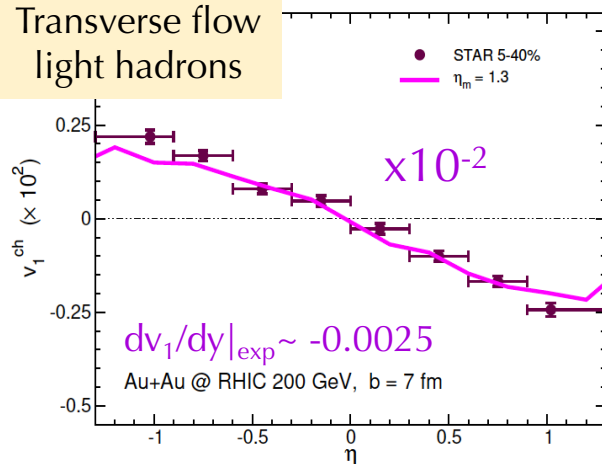
Very surprising!

v_1 (HQ) $\sim$ 30 times v_1 light hadrons ($\pi, K, \dots$)

HQ Surprise also in the transverse flow $v_1 = \langle p_x / p_T \rangle$



Transverse flow
light hadrons

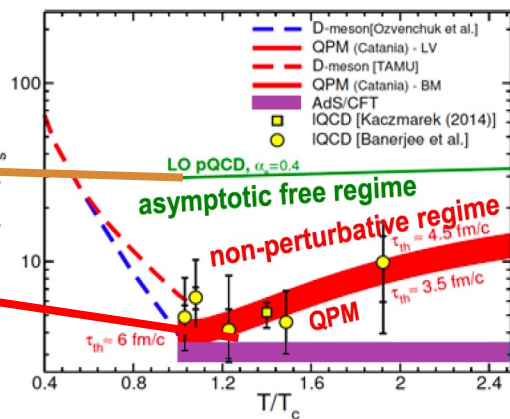
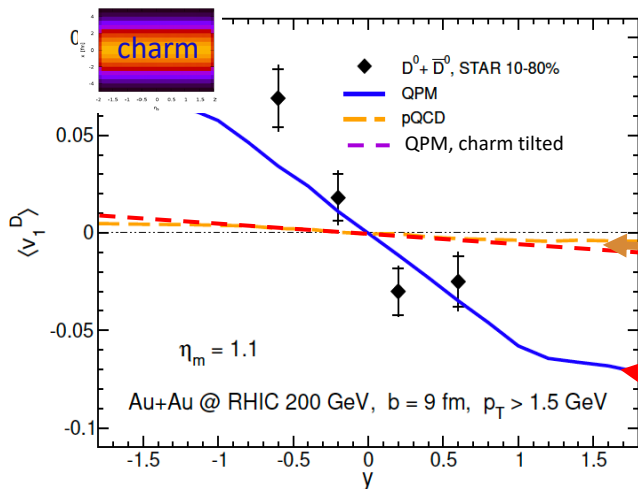


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Very surprising!

v_1 (HQ) ~ 30 times v_1 light hadrons ($\pi, K, \dots$)

$$dv_1/dy = -0.080 \pm 0.017(\text{stat}) \pm 0.016(\text{syst})$$



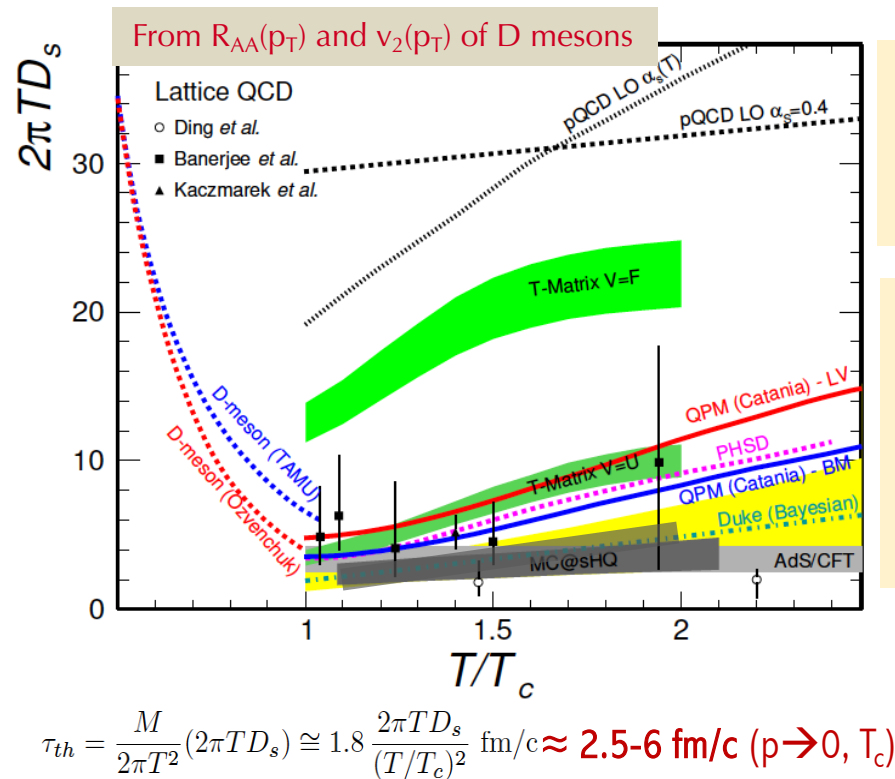
❖ **Needed non-perturbative HQ interaction close to AdS/CFT**

❖ **Needed also initial “tilt” of bulk & none for HQ**

L. Oliva et al., JHEP 05 (2021)

Diffusion of Charm Quark: first stage

X. Dong & VG, Prog.Part.Nucl.Phys. (2019)



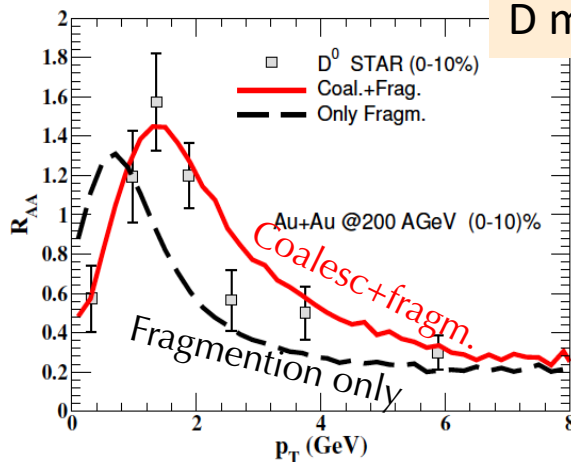
*Main differences in comparing to LQCD-AdS/CFT:

- quenched QCD (Yang-Mills) + $M_Q \rightarrow \infty$
- phenomenology at intermediate p_T – LQCD(AdS/CFT) at $p \rightarrow 0$

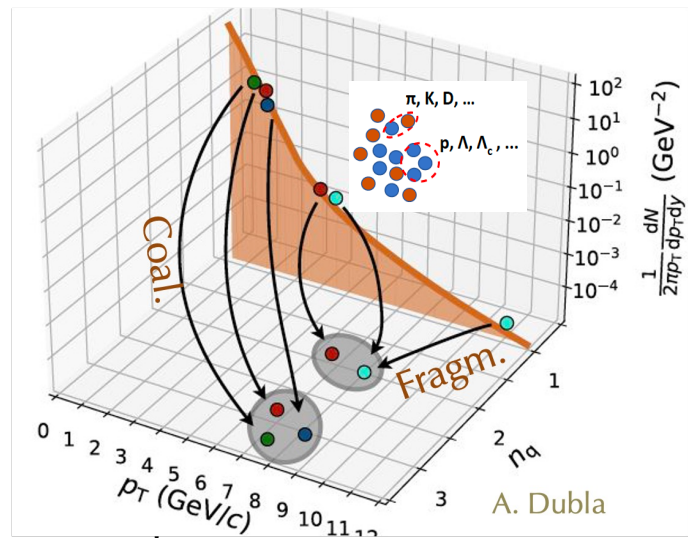
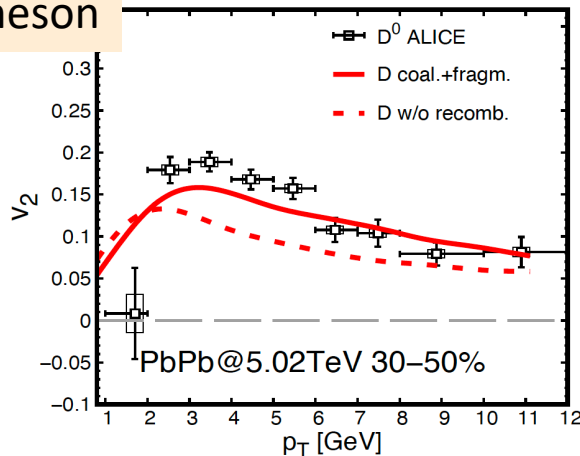
*Main sources of differences in models:

- impact of hadronization («unexpected» large baryon production)
- momentum dependence of matrix elements
- data not enough precise/observable not enough constraining (especially for $p_T \rightarrow 0$)

Impact of HF in-medium Hadronization



D meson



- Opposite to in-medium scattering Coalescence **brings up both** R_{AA} and v_2
 → toward experimental data

Phase-space coalescence: quark recombination

$$f_M(P_H = p_1 + p_2) \approx f_q(p_1) \otimes f_{\bar{q}}(p_2) \otimes \Phi_M(\Delta x, \Delta p)$$

Independent Fragmentation

$$f_H(P_H = zp_T) = f_{q,g}(p_T) \otimes D_{q,g \rightarrow H}(z) \quad , z < 1$$

→ Add momenta: P_T^H from low p_T quark

→ Enhance elliptic flow v_2 adding flows:

$$v_{2D}(p_T) \cong v_{2c} \left(\frac{m_c}{m_D} p_T \right) + v_{2q} \left(\frac{m_q}{m_D} p_T \right)$$

HF Baryon enhancement wrt e^+e^- even in AA& pp@TeV

Phase-space coalescence

Parton Distrib. Funct.

Hadron Wigner function

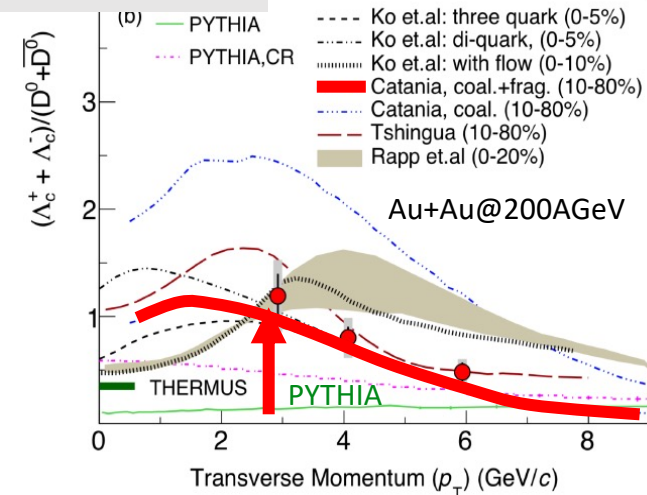
$$\frac{dN_{Hadron}}{d^2 p_T} = g_H \int \prod_{i=1}^n p_i \cdot d\sigma_i \frac{d^3 p_i}{(2\pi)^3} f_q(x_i, p_i) f_w(x_1, \dots, x_n; p_1, \dots, p_n) \delta(p_T - \sum_i p_{iT})$$

Fragmentation

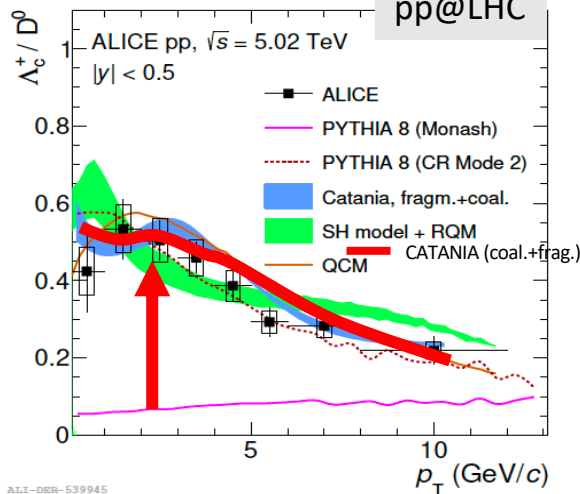
$$\frac{dN_h}{d^2 p_h} = \sum_f \int dz \frac{dN_f}{d^2 p_f} D_{f \rightarrow h}(z)$$

AA@RHIC-STAR

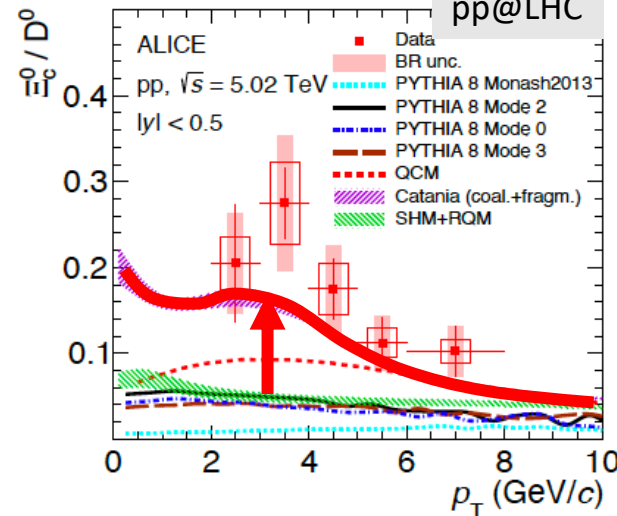
STAR, Phys.Rev.Lett. 124 (2020)



pp@LHC



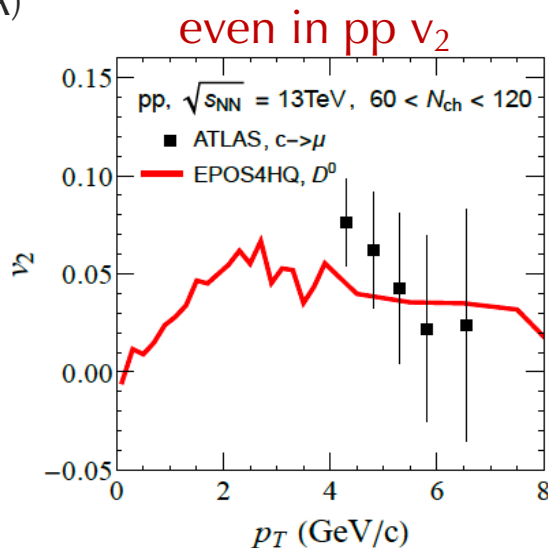
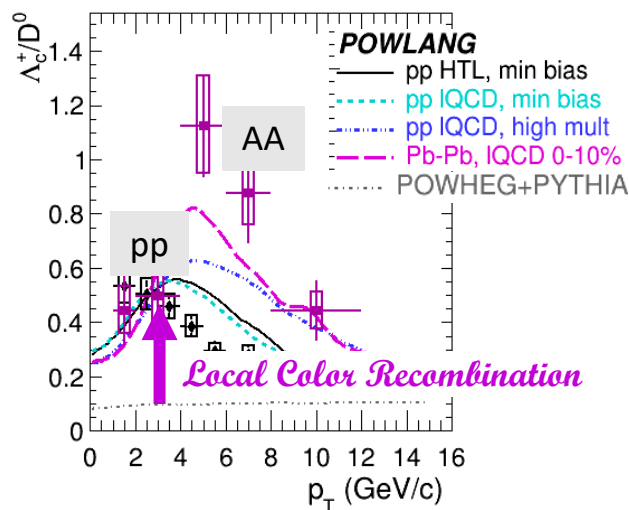
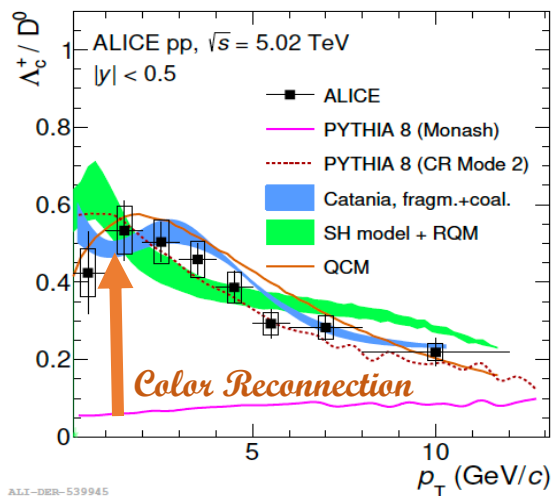
pp@LHC



- I^0 prediction in coalescence [Ko PRC(2009)] of very large $\Lambda_c/D^0 \gg$ SHM[PDG] $\gg$ e^+e^- (~PYTHIA)
- Breaking of Universal Fragmentation Function already in pp in HF sector

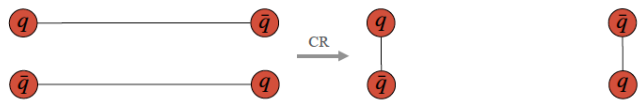
HF hadronization has stimulated several developments

- **PYHTIA** beyond Leading Color (LC) → Color Reconnection (CR) in pp
- Coalescence+Fragmentation approach applied to pp
- Local Color Recombination: **POWLANG** in AA and in pp
- Inclusion of HF Coalescence+ Fragmentation in **EPOS** (pp & AA)

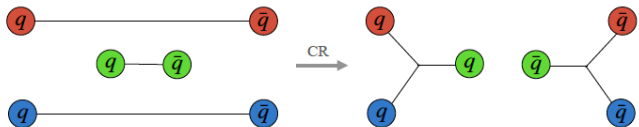


- Yields modified from e^+e^- (e^-p) to pp, then from pp to AA mostly coupling to flowing QGP medium modifies p_T shape of the ratio Λ_c/D ?

PYTHIA Color Reconnection/ Local Color neutralization



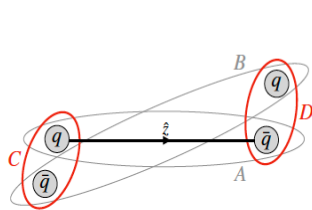
(a) Dipole-type reconnection.



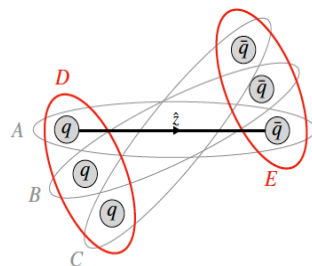
Baryonic reconnection

Leading Color ($N_c \rightarrow \infty$): Prob. of Local Color neutralization $\rightarrow 0$

- When string color reconnection is switched-on in pp
 - $\rightarrow$ Very large baryon Λ_c , Σ_c enhancement
 - $\rightarrow$ not so relevant for D, like coalescence+fragmentation



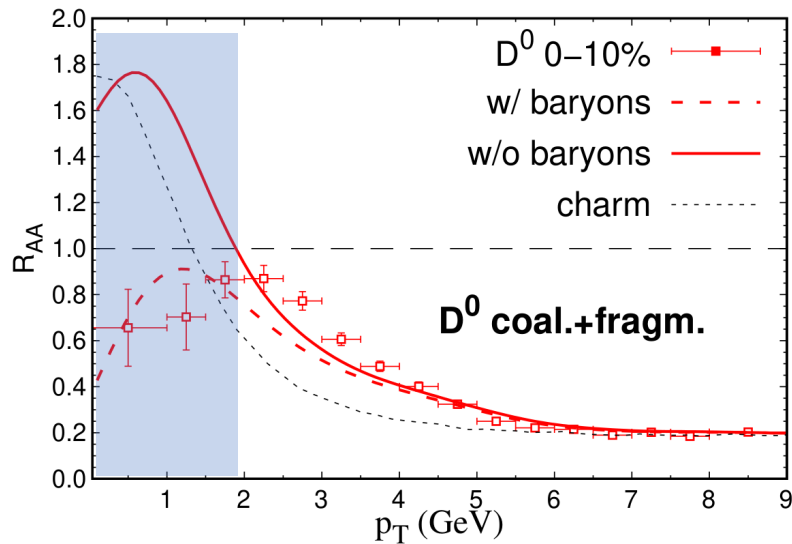
(a) Mesonic reconnection.



(b) Baryonic reconnection.

- Not independent strings - **Local reconnection $\rightarrow$ string energy minimization $\rightarrow$ smaller invariant mass close to D meson states (like in coalescence)**

HF Baryon enhancement: impact on R_{AA}



Till 2019-20 the baryon production ($\Lambda_c, \dots$)
was discarded by theoretical approaches
But data at $p_T > 2$ GeV nearly blind to it

Λ_c baryon production was mostly neglected in most studies of R_{AA} , but:

- Strong impact on R_{AA} low-intermediate $p_T \rightarrow$ affect estimates of D_s

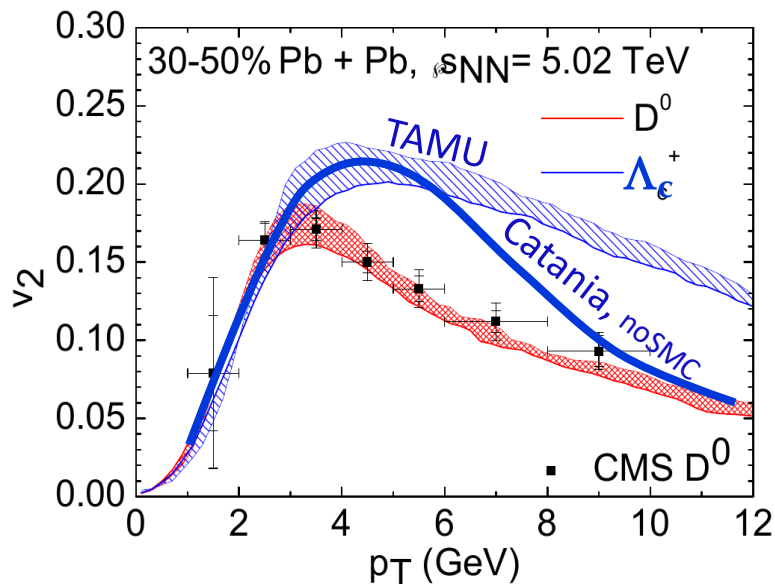
“See” Hadronization mechanism through elliptic flow

If Λ_c enhancement of the yield comes from quark coalescence it should be associated to

→ Large v_2 of $\Lambda_c \sim v_{2c} \left(\frac{m_c}{m_\Lambda} p_T \right) + 2 v_{2q} \left(\frac{m_q}{m_\Lambda} p_T \right)$

→ Effect to be measured in AA; will it be seen also in pp?

[for Run3-4]



✓ Λ_c dominated by coalescence:
 p_T range? self-consistent with Λ_c/D ratio?

➤ Would PYHTIA-CR predict finite v_2 of D , Λ_c in pp?
by String shoving? Can it predict D , Λ_c systematic
for v_2 ?

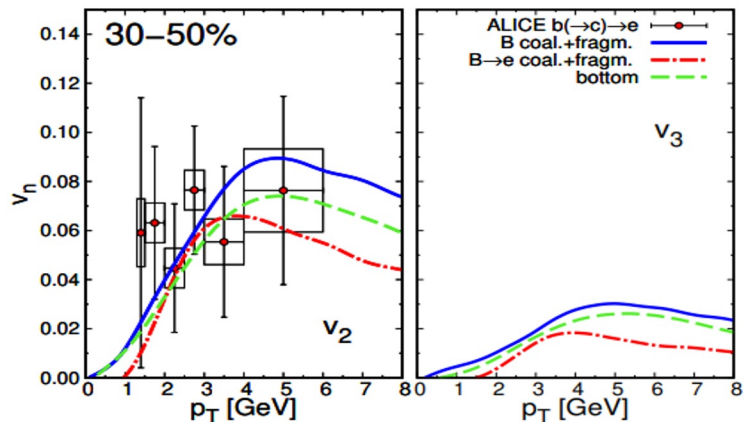
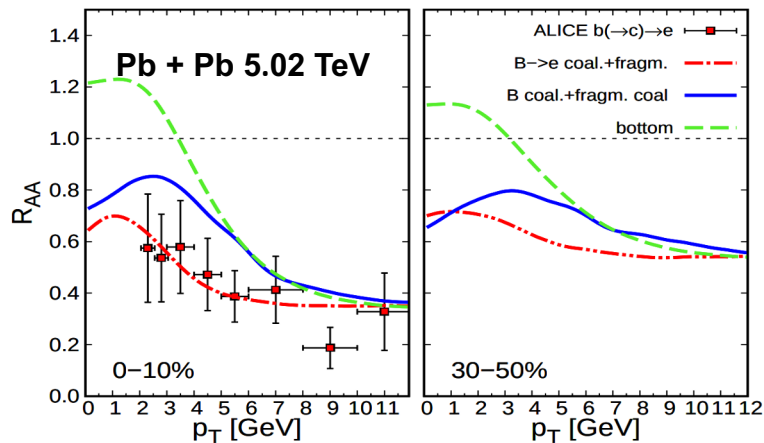
Methods/tools of AA allow better insight
into hadronization in pp!?

Is charm quark really “heavy”?

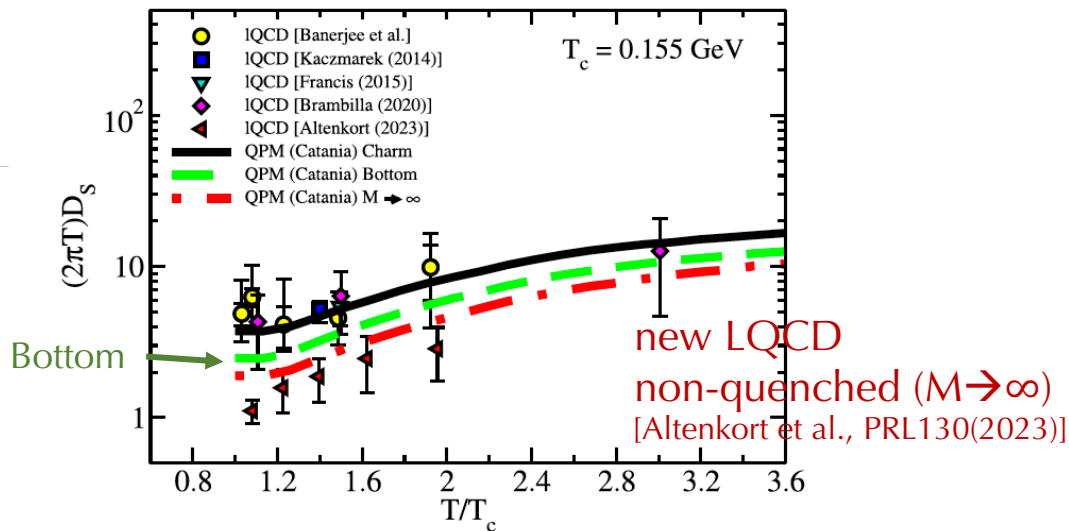


A very solid comparison to LQCD, to the development of NRQCD-EFT, to quantify interaction only by space-diffusion D_s (full Brownian motion) requires a “full” HQ, but $M_c \sim q^2 \sim gT$, $\langle p \rangle \sim 3T$ at $T \sim 300\text{-}500$ MeV
→ full Heavy is the Bottom

Extension to bottom dynamics: R_{AA} v_2, v_3



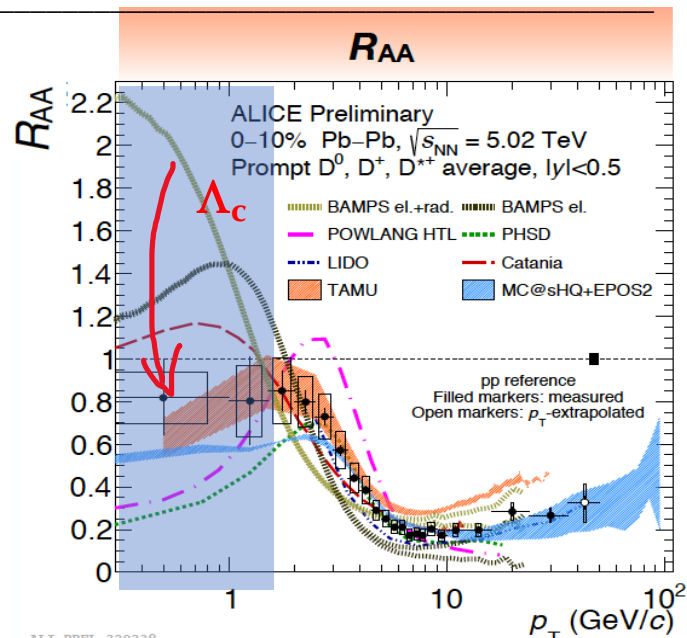
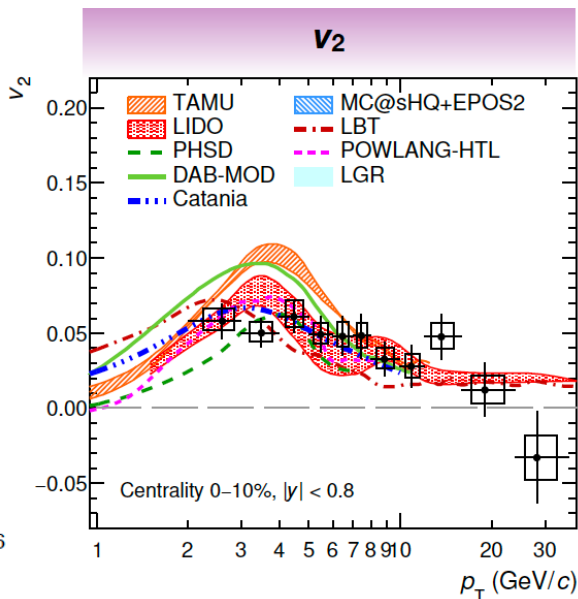
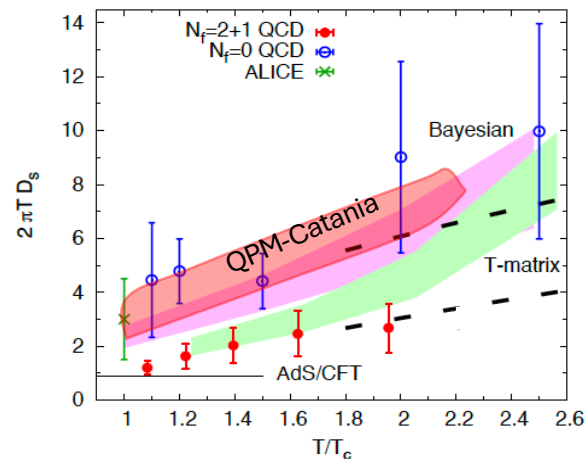
- No parameters changed wrt charm (only M_b)
- Agreement within still large uncertainty
- QPM implies a mass dependence of $D_s(T)$, not seen in LQCD/NRQCD



M.L. Sambataro et al., *PLB* 849(2024)

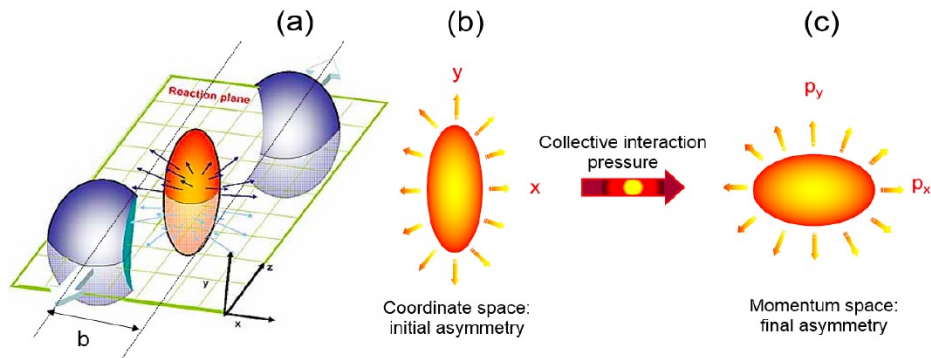
Phase of Transition

$D_s(T, p \rightarrow 0)$ lattice QCD

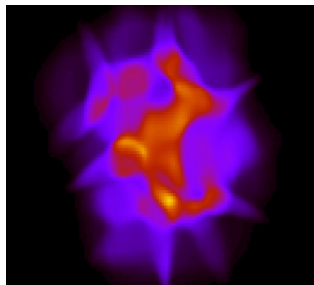


- Very small new LQCD- $D_s(T)$ [$\tau_{th}(\text{charm}, p \rightarrow 0) \sim 1-2 \text{ fm/c}$]: mass independent? down to charm mass?
- Most studies at $p_T > 1.5-2 \text{ GeV}$ [mainly not including impact of Λ_c], need **new wave of prediction**:
 - compare to LQCD **need data $p_T \rightarrow 0$**
 - need precision data at low p_T not only for D but also for Λ_c
 - add more exclusive observables: $v_n(\text{soft})-v_n(\text{hard})$, angular $D\bar{D}$ correlation,...

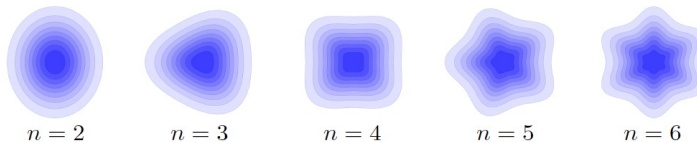
Going deeply into Hot QCD matter created in uRHICs



event-by-event



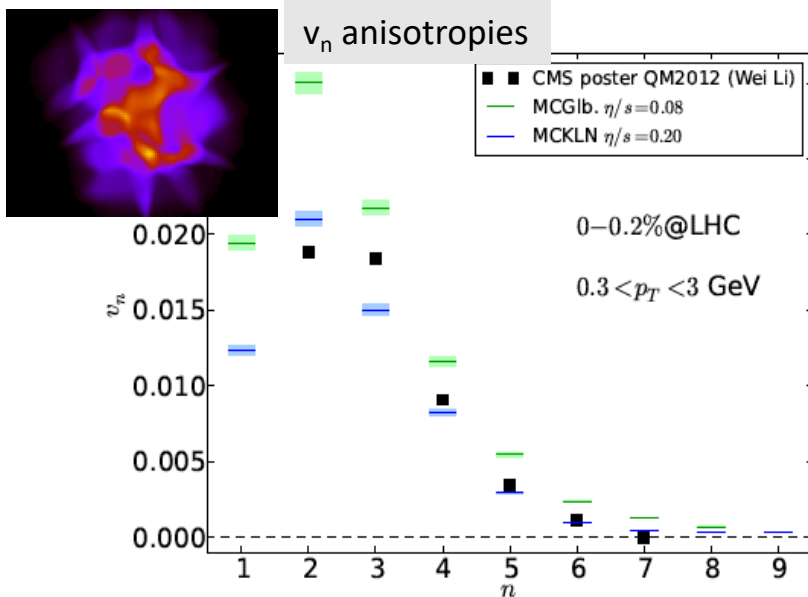
When including fluctuations, all moments appear:



All harmonics appearing
with different weights.

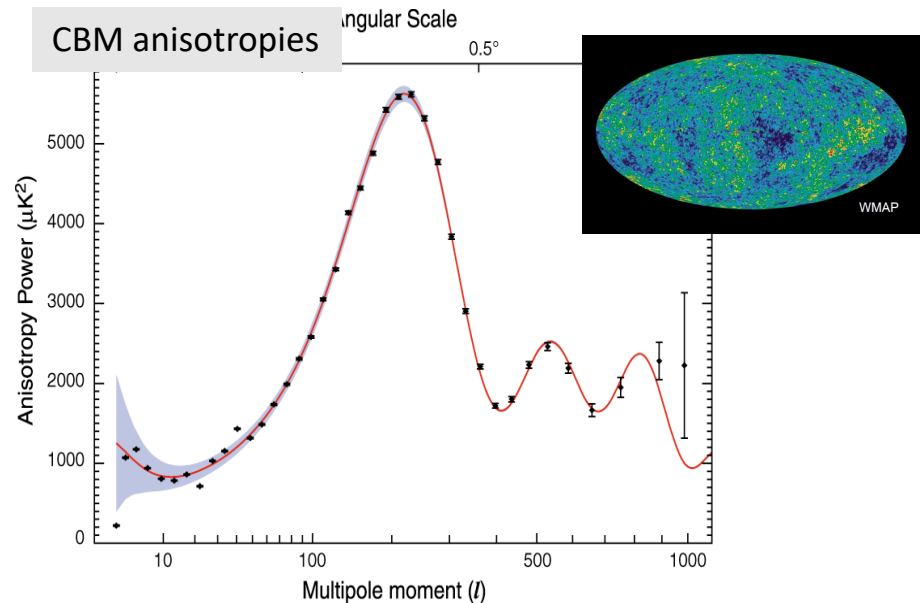
$$v_n = \langle \cos(n\varphi) \rangle$$

Going deeply into Hot QCD matter



- Initial QCD quantum fluctuations
- T dependence of η/s and $D_s(T)$
- Equation of State
- Freeze-out dynamics

Keeping size and time of QGP



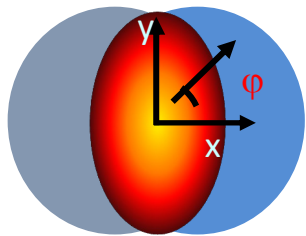
- Spectral Index
- Standard Model Matter
- Cold Dark Matter
- Dark Energy
- Hubble Constant

Keeping Age and Flatness of the Universe

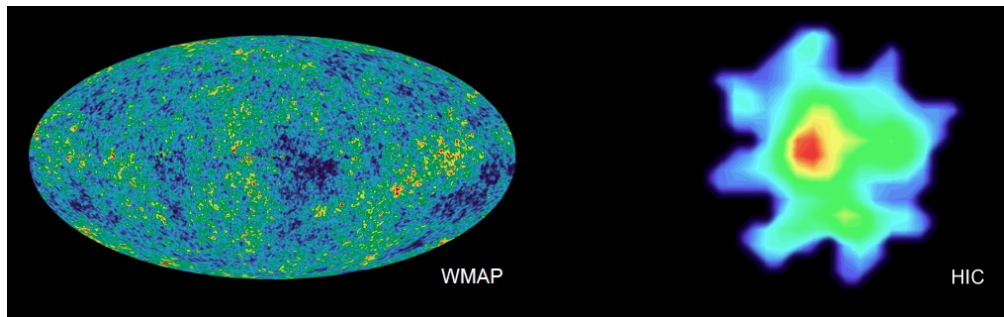
Go to WMAP website and play Build a Universe...

Able to «see» even the local Temperature fluctuations of the QGP

Transverse view

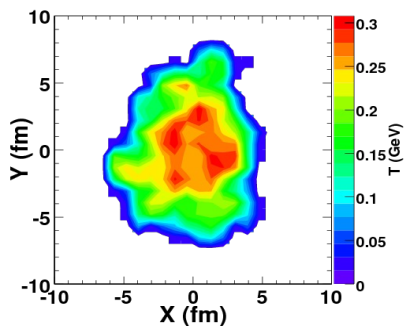


Relativistic HIC
in '90s, '00 till about 2005
Anisotropies only with
even parity due to symmetry
→ v_2 elliptic flow



$v_n(\text{light})$ vs $v_n(\text{charm})$ - ebe

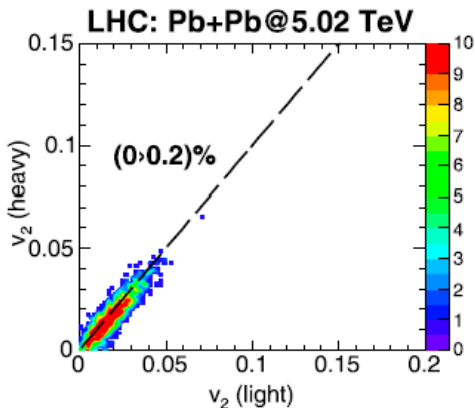
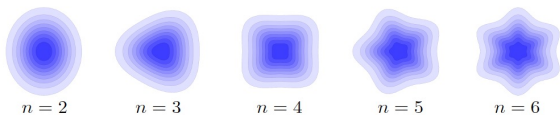
Transverse view of HIC, nowdays



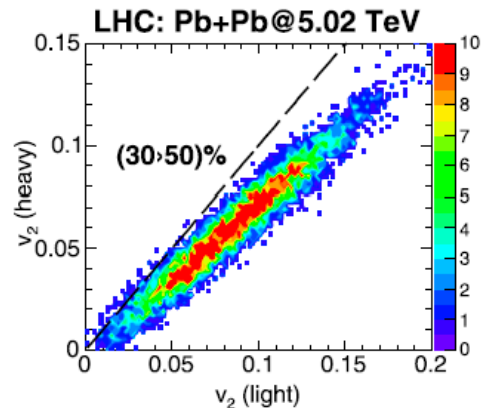
All harmonics appearing
with different weights.

$$v_n = \langle \cos(n\phi) \rangle$$

When including fluctuations, all moments appear:



ultra-central

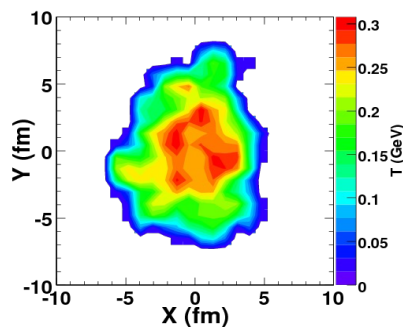
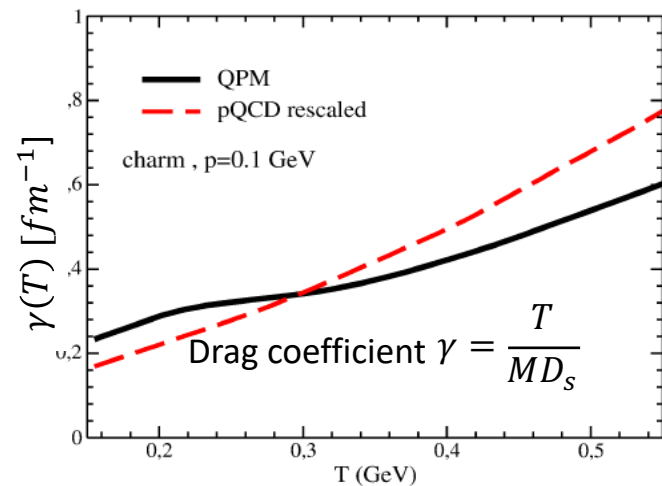


semi-central

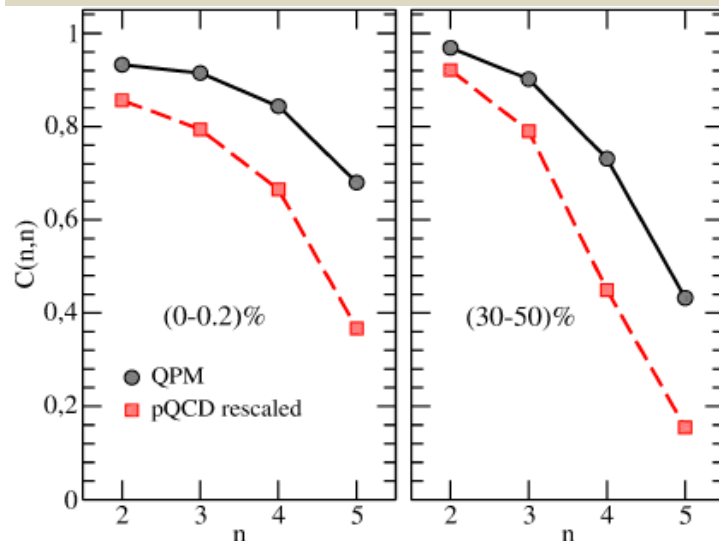
HL-LHC allows to access v_n light-HQ correlation

Event-by-event coupling of the anisotropy of the bulk (light) and the charm (heavy) one
 → Much more precise determination of the strength interaction: drag $\gamma \sim 1/D_s$

$$C(v_n^{light}, v_m^{heavy}) = \left\langle \frac{(v_n^{light} - \langle v_n^{light} \rangle)(v_m^{heavy} - \langle v_m^{heavy} \rangle)}{\sigma_{v_n^{light}} \sigma_{v_m^{heavy}}} \right\rangle$$



Very large sensitivity to T dep. of D_s

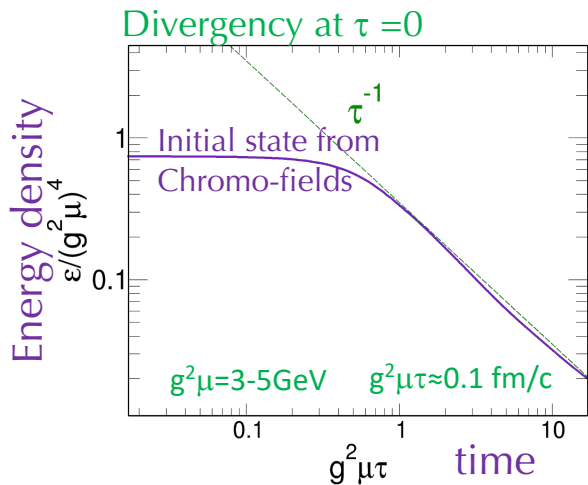
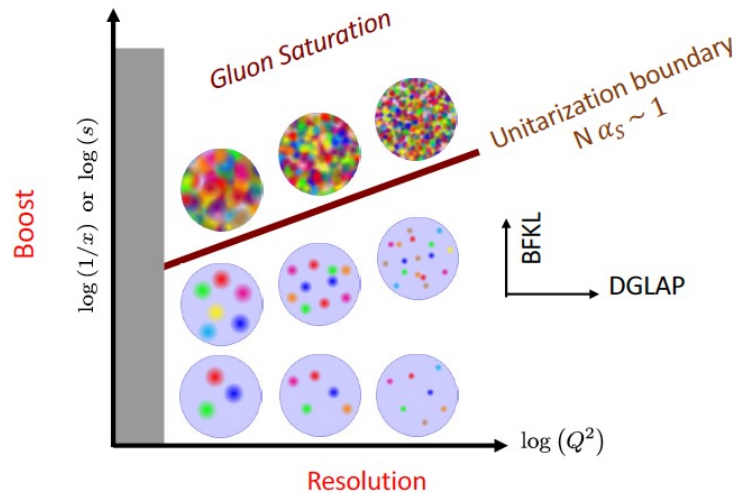
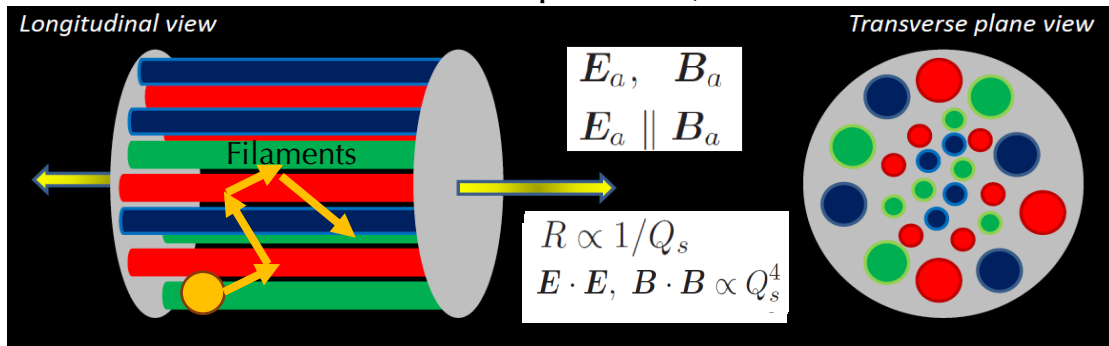


S. Plumari et al., Phys.Lett.B 805 (2020)

All at fixed $R_{AA}(p_T)$

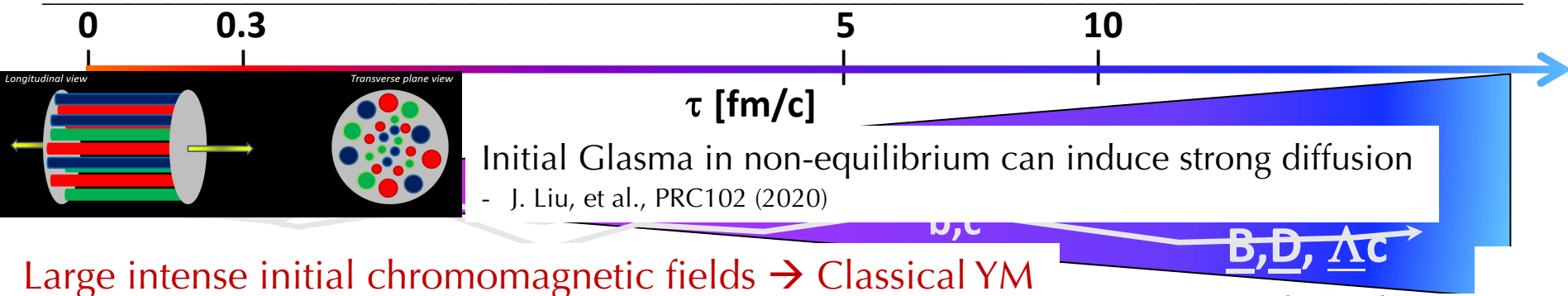
HQ probe of CGC/Glasma phase $0^+ < t < 0.3 \text{ fm/c}$

Color Glass Condensate (CGC) as high-energy limit of QCD (non-linear evolution at low x) in the BFKL direction in the plane $[Q^2, x]$?



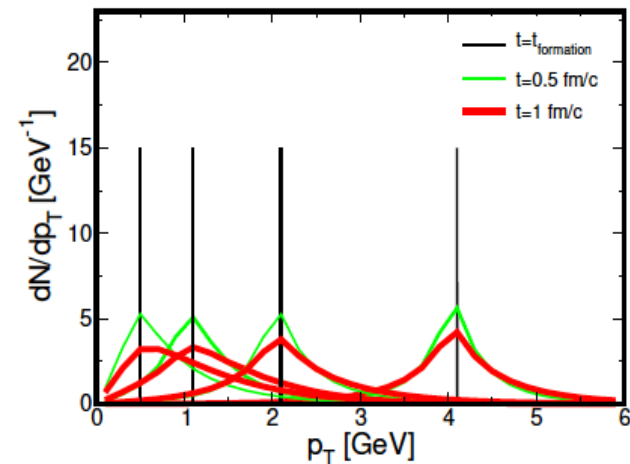
- Solving the $t=0$ divergency $\epsilon \sim \frac{1}{\tau}$ ($\approx$ initio of the Collision Universe)
- The unknown very early stage would not destroy our current picture, but we look for signatures to spot from this phase [$\sim$ Early Universe]

Impact of Glasma phase



Large intense initial chromomagnetic fields $\rightarrow$ Classical YM

Static box- SU(2)



Solving classical Yang-Mills

$$\frac{dA_i^a(x)}{dt} = E_i^a(x),$$

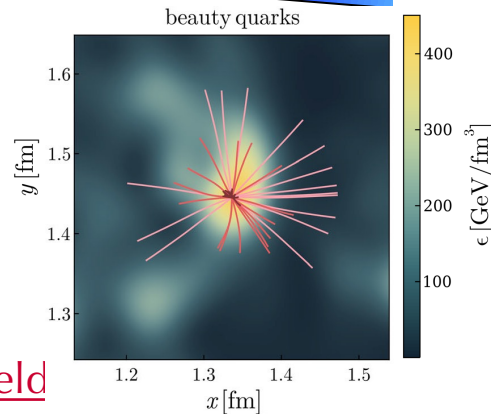
$$\frac{dE_i^a(x)}{dt} = \sum_j \partial_j F_{ji}^a(x) + \sum_{b,c,j} f^{abc} A_j^b(x) F_{ji}^c(x).$$

Heavy quark in the chromo magnetic field

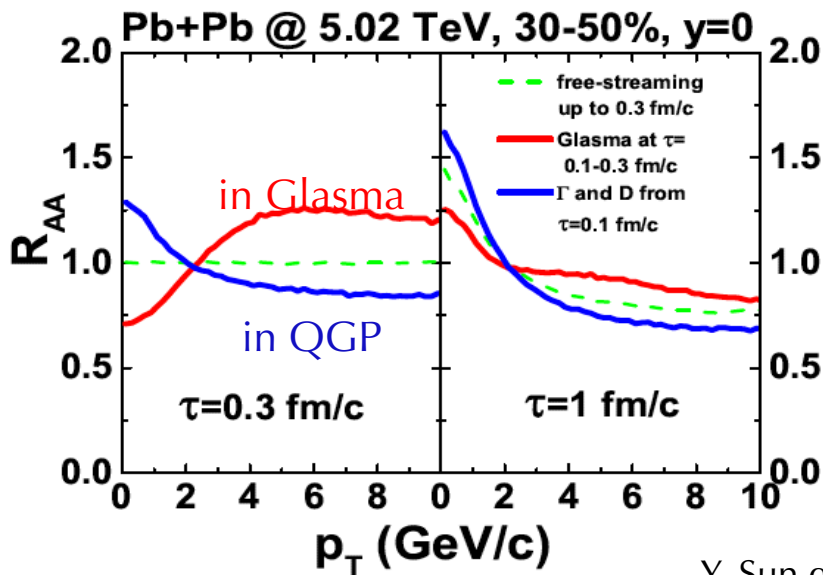
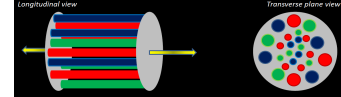
$$\frac{dx_i}{dt} = \frac{p_i}{E},$$

$$E \frac{dp_i}{dt} = Q_a F_{iv}^a p^\nu,$$

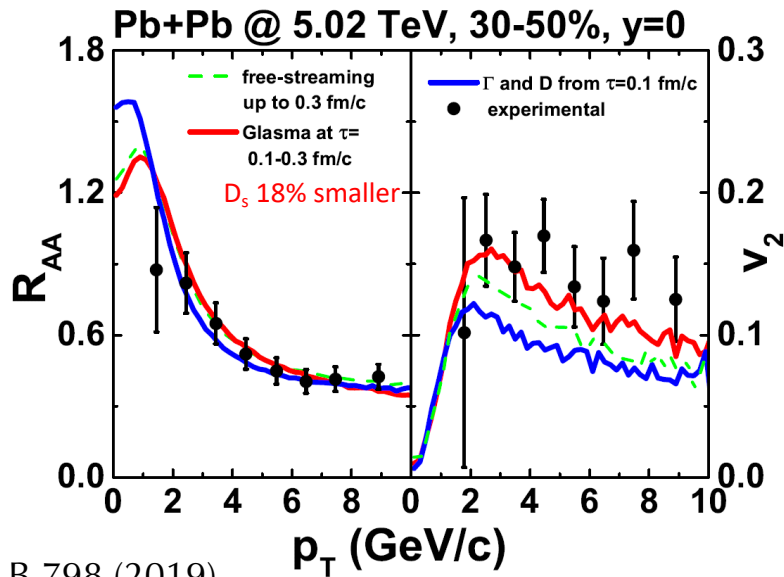
$$E \frac{dQ_a}{dt} = -Q_c \epsilon^{cba} A_b \cdot p,$$



Potential impact on AA observables (starting at $\tau=\tau_{\text{form}}$ -SU(2))

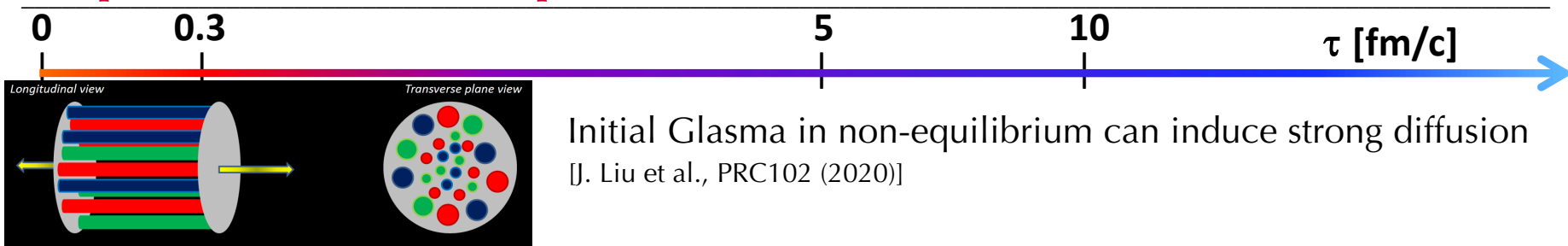


Y. Sun et al., PLB 798 (2019)



- ❖ **Opposite to HQ in QGP:** Dominance of diffusion-like $\rightarrow$ initial **enhancement of $R_{AA}(p_T)$!!!**
- ❖ **Gain in v_2 :** larger interaction in QGP stage needed to have same $R_{AA}(p_T)$ [18% smaller D_s]

Impact of Glasma phase

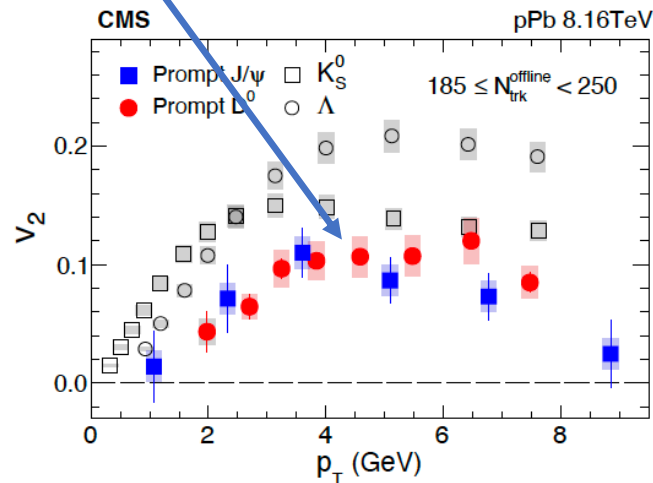
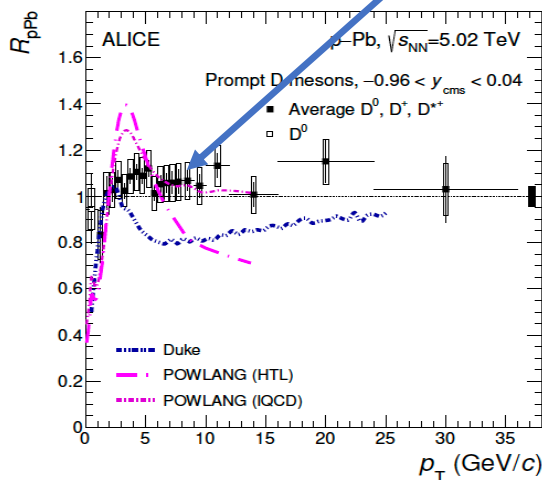
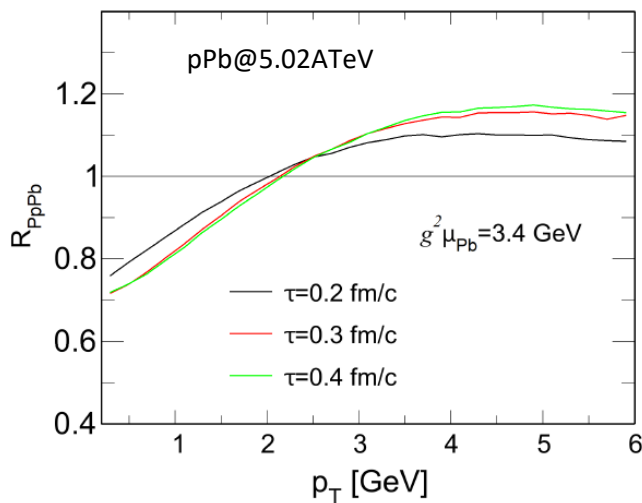


Initial Glasma in non-equilibrium can induce strong diffusion
[J. Liu et al., PRC102 (2020)]

In pA collision it could solve the “puzzle”:

$$R_{pA} \sim 1 \text{ and large } v_2 \text{ of D meson}$$

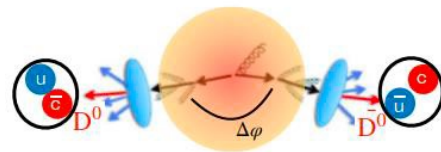
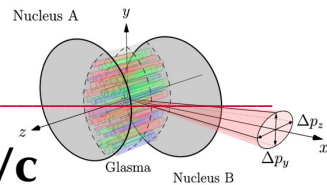
Phenomenological impact



Glasma impact on angular $Q\bar{Q}$

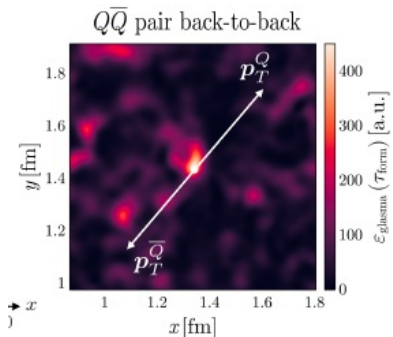
First study of azimuthal $Q\bar{Q}$ correlation: large decorrelation **in only 0.2 fm/c**

Significant effect of glasma on HQ!

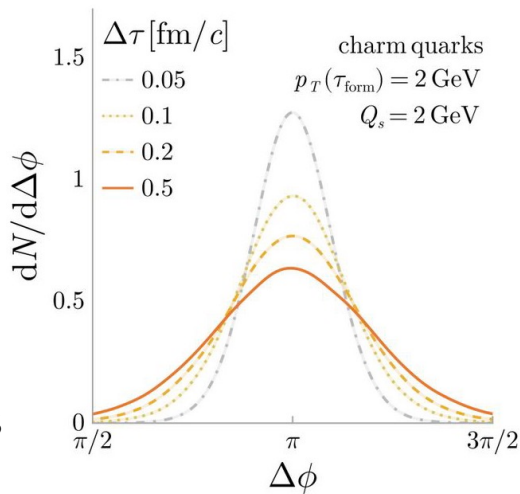


pA collision should keep memory of it especially correlating it to R_{AA} , v_n :

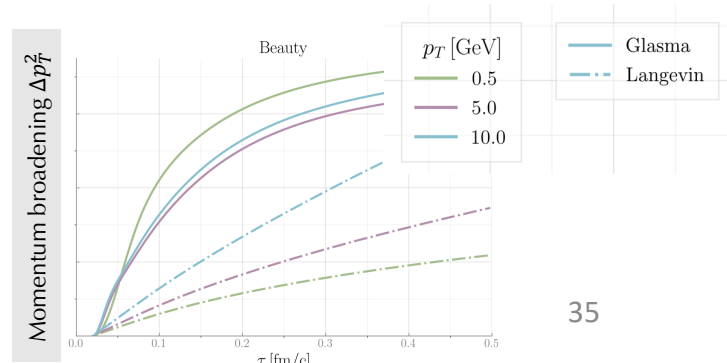
- identify Glasma phase
- solve the puzzle of $R_{pA} \sim 1$ and v_2 large



Nearly **identical** for **bottom** despite mass [smaller τ_{form}]



Calculation in $SU(3)$ +longitudinal expansion



Summary & Perspectives

- ❖ Open HF set up a strong connection among LQCD, NREFT/phenomenology/exp. observables:
 - large non-perturbative interaction: $D_s(T)$:
agreement of phenomenology to LQCD?! close to AdS/CFT? validity of NREFT/ QCD at finite T?!
 - hadronization reveals pp@TeV much closer to AA than e^+e^- or e^-p !?
- ❖ **It is a Phase of Transition to a new PROGRESS:**
 - new LQCD results for $D_s(T)$ $\rightarrow$ smaller than previous average estimate ($\tau_{th}(\text{charm}) \sim 1\text{-}2 \text{ fm}/c$)
 - better identify impact of baryon HF hadronization (large Λ_c/D) on estimate of $D_s(T)$
 - Precision data @low pT | new observables: $R_{AA}(\Lambda_c)$, $v_2(\Lambda_c)$, light-HF v_n correl., $D\bar{D}$ angular corr.
| extension to bottom | **multicharm** production (ALICE3) $\rightarrow$ breakthrough
- ❖ Open HF can have a relevant interplay with developments of Glasma studies [especially for pA]

Back-up Slide

Relativistic Boltzmann equation at finite η/s

Bulk evolution

$$p^\mu \partial_\mu f_q(x, p) + m(x) \partial_\mu^x m(x) \partial_p^\mu f_q(x, p) = C[f_q, f_g]$$

$$p^\mu \partial_\mu f_g(x, p) + m(x) \partial_\mu^x m(x) \partial_p^\mu f_g(x, p) = C[f_q, f_g]$$

Free-streaming

Field interaction

$$\varepsilon - 3p \neq 0$$

Collision term

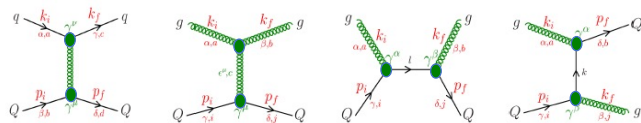
gauged to some $\eta/s \neq 0$

Equivalent to viscous hydro

at $\eta/s \approx 0.1$

HQ evolution

$$p^\mu \partial_\mu f_Q(x, p) = C[f_q, f_g, f_Q](x, p)$$



$$\begin{aligned} C[f_Q] = & \frac{1}{2E_1} \int \frac{d^3 p_2}{2E_2 (2\pi)^3} \int \frac{d^3 p'_1}{2E_1 (2\pi)^3} \\ & \times [f_Q(p'_1) f_{q,g}(p'_2) - f_Q(p_1) f_{q,g}(p_2)] \\ & \times |\mathcal{M}_{(q,g)+Q}(p_1 p_2 \rightarrow p'_1 p'_2)|^2 \\ & \times (2\pi)^4 \delta^4(p_1 + p_2 - p'_1 - p'_2), \end{aligned}$$

Non perturbative dynamics $\rightarrow$ M scattering matrices ($q, g \rightarrow Q$)
evaluated by Quasi-Particle Model fit to **IQCD thermodynamics**

$$m_g^2(T) = \frac{2N_c}{N_c^2 - 1} g^2(T) T^2$$

$$m_q^2(T) = \frac{1}{N_c} g^2(T) T^2$$

$$g^2(T) = \frac{48\pi^2}{(11N_c - 2N_f) \ln \left[\lambda \left(\frac{T}{T_c} - \frac{T_s}{T_c} \right) \right]^2}$$

Impact of off-shell dynamics:

M.L. Sambataro et al., *Eur.Phys.J.C* 80 (2020) 12, 1140

Multicharm production + PbPb $\rightarrow$ OO

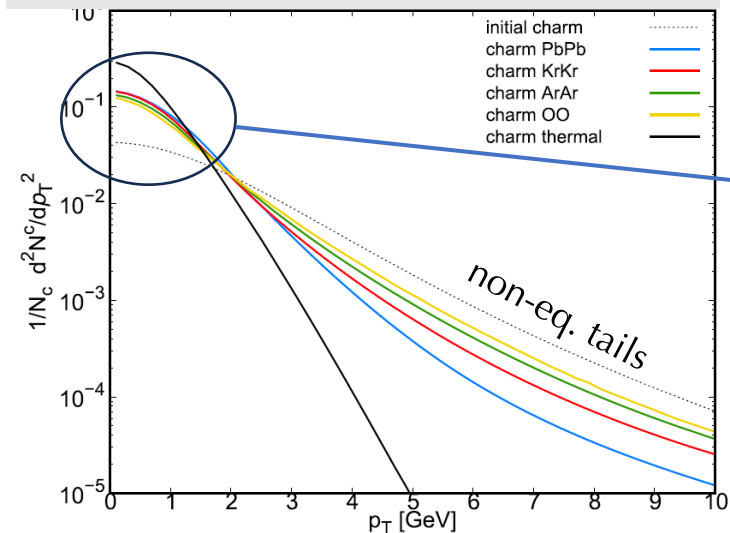
$$\Xi_{cc}^{+,++}, \Omega_{scc}, \Omega_{ccc}$$

Baryon		
$\Xi_{cc}^{+,++} = dec, ucc$	3621	$\frac{1}{2}(\frac{1}{2})$
$\Omega_{scc}^{+} = scc$	3679	$0(\frac{1}{2})$
$\Omega_{ccc}^{++} = ccc$	4761	$0(\frac{3}{2})$

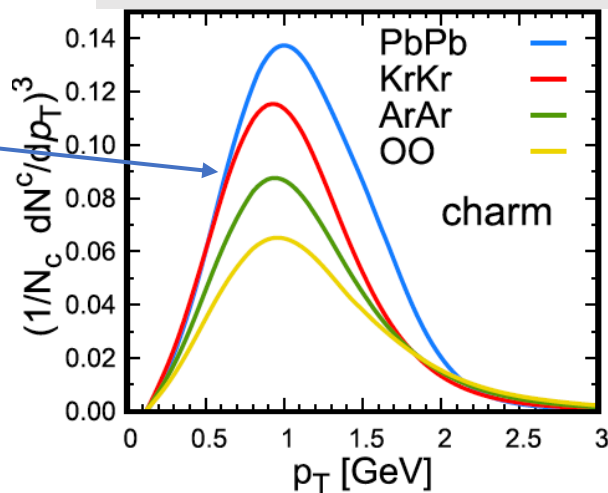
- Understand HQ in medium hadronization:
[pure recombination, no fragmentation at low p_T at least]
- Ω_{ccc} very sensitive (to cubic power) to $(dN_{charm}/dp_T)^3$

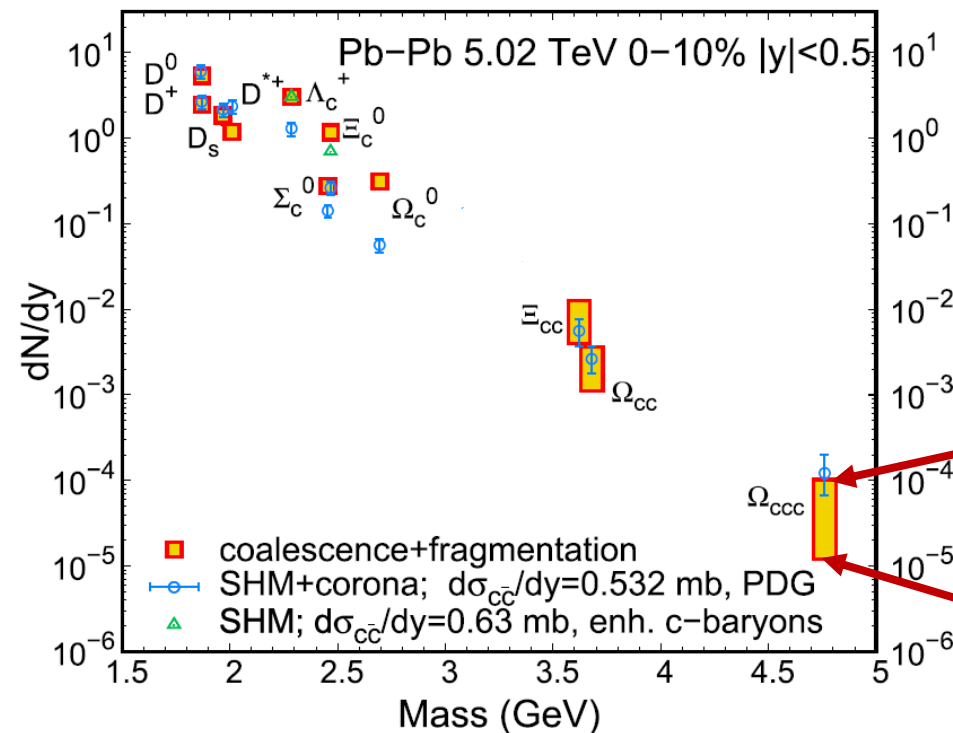
A system size scanning is like looking to see ΔE versus $L \rightarrow dE/dx$

Evolution of p_T charm vs system size



cubic of renormalized charm p_T distrib.





- Both Statistical model (SHM) & a naïve coalescence should lead to a scaling with $V \left(\frac{N_c}{V} \right)^c = N_c \left(\frac{N_c}{V} \right)^{c-1}$ $c = \text{\# of charm in Hadron}$
- Ω_{ccc} yield depends on $\left(\frac{dN_c}{dp_T} \right)^3$

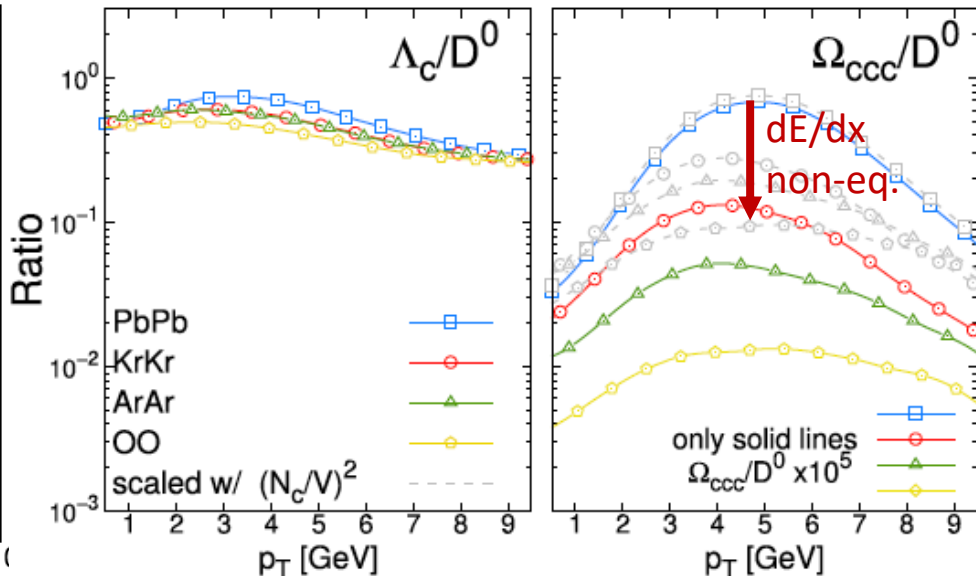
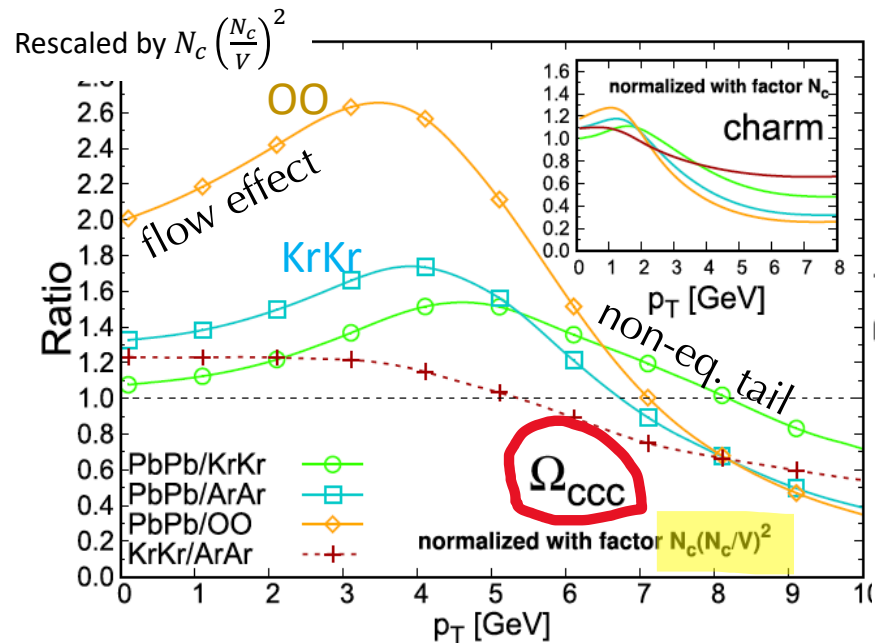
thermal full $dN_{charm}/dp_T \sim SHM$

realistic dN_{charm}/dp_T from $D_s(T)$

- ❖ Makes a 1 order of magnitude difference depending on degree of equilibrium, while very small effect on $D, \Lambda_c \sim (dN_{charm}/dp_T)$, also due to charm # conservation & confinement

$\Omega_{ccc} p_T$ evolution from PbPb to OO

Minissale et al., EPJC84(2024)

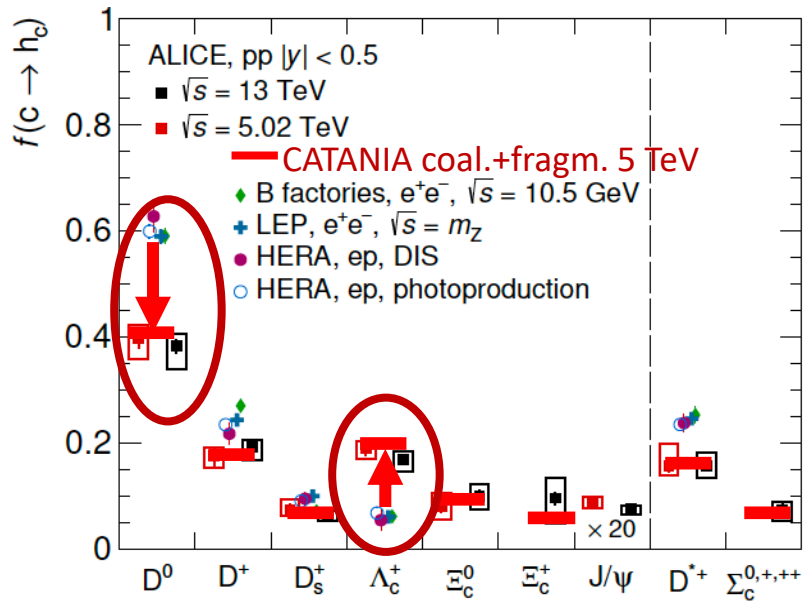


Deviation from scaling $N_c \left(\frac{N_c}{V}\right)^2$ due to different final p_T -charm distribution wrt PbPb

$\Omega_{ccc} p_T$ spectrum evolution with system size unveil direct information of charm dN_c/dp_T with much larger sensitivity w.r.t. D^0 or $\Lambda_c \rightarrow$ precise info on interaction $D_s(T)$

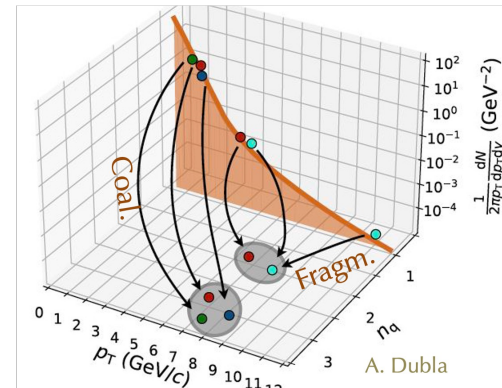
ALICE3

“Fragmentation” Fractions in pp Catania Coalescence



- Evidence of different “Fragmentation” Fractions in pp at LHC wrt e^+e^- & e^-p but similar to AA
- Coalesc.+Fragm. very close to pp FF
- OK SHM-RQM for Λ_c and D’s
- Large Ξ_c , Ω_c only in coalescence, lack of yield in PYTHIA, SHM-RQM,... large error bars

Seems only hadronization models treating pp as a small QGP fireball or allowing local reconnection-recombination get close to data..



QPM ($N_f=2+1$) extension to QPMp ($N_f=2+1+1$)

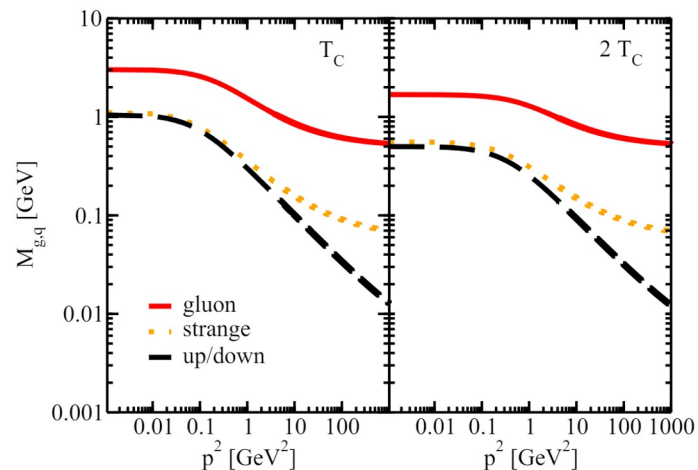
From Dyson-Schwinger ($\sim$ PHSD group in $N_f=2+1$)

$$M_g(T, \mu_q, p) = \left(\frac{3}{2} \right) \left(\frac{g^2(T^*/T_c(\mu_q))}{6} \left[\left(N_c + \frac{1}{2} N_f \right) T^2 + \frac{N_c}{2} \sum_q \frac{\mu_q^2}{\pi^2} \right] \left[\frac{1}{1 + \Lambda_g(T_c(\mu_q)/T^*) p^2} \right] \right)^{1/2} + m_{\chi_8}$$

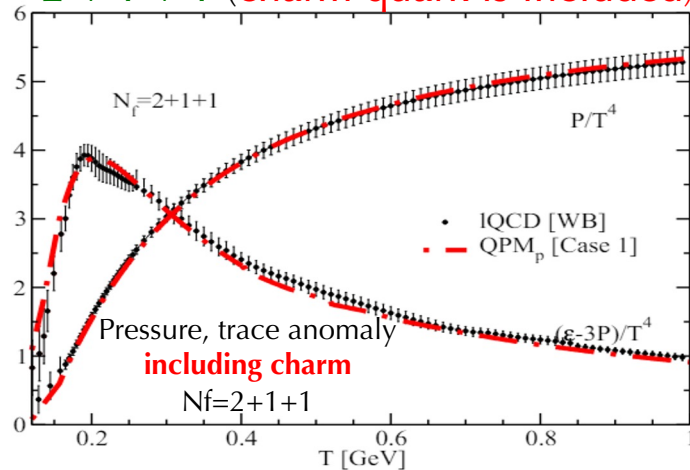
$$M_{q,\bar{q}}(T, \mu_q, p) = \left(\frac{N_c^2 - 1}{8 N_c} g^2(T^*/T_c(\mu_q)) \left[T^2 + \frac{\mu_q^2}{\pi^2} \right] \left[\frac{1}{1 + \Lambda_q(T_c(\mu_q)/T^*) p^2} \right] \right)^{1/2} + m_{\chi_4}$$

C. S. Fischer, J. Phys. G, R253 (2006)
H. Berrehrah, W. et al., PRC 93(2016)
M.L. Sambataro et al. e-Print: 2404.17459

Momentum dependent masses
 $p \gg \Lambda_{\text{QCD}} \rightarrow$ current masses



QPM extended from $N_f = 2+1$
to $N_f = 2 + 1 + 1$ (charm quark is included)

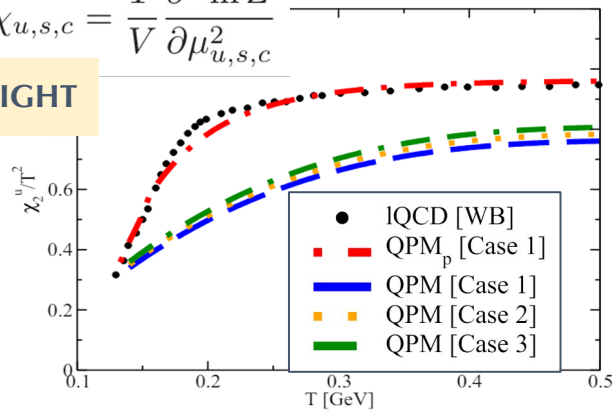


$m_{u,d,s}(p)$ expected but solves also a know issue...

Quark susceptibility from QPM to QPMp

$$\chi_{u,s,c} = \frac{T}{V} \frac{\partial^2 \ln Z}{\partial \mu_{u,s,c}^2}$$

LIGHT



Case 1: $m_c = 1.5 \text{ GeV}$

Case 2: $m_c^2 = m_{c0}^2 + 1/3 g^2 T^2$ with $m_{c0} = 1.3 \text{ GeV}$

Case 3: $m_c(T)$ fixed by charm χ_2^c

$$\chi_2^c = \frac{T}{V} \frac{\partial^2 \ln Z}{\partial \mu_i^2}$$

Quite different quark susceptibility χ_2^q even if correspond to same $\epsilon_{\text{IQCD}}(T)$?!

For $m(p) = \text{const.}$

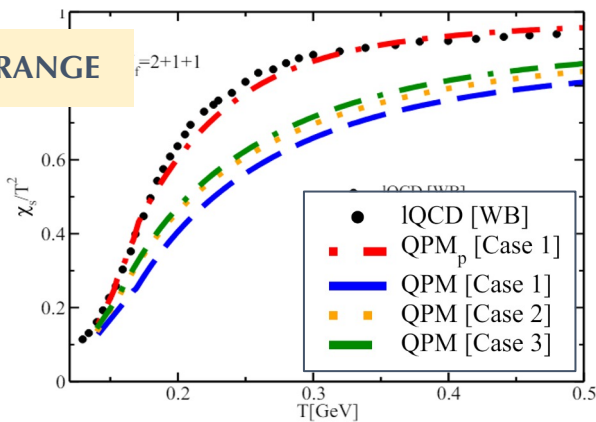
$$\frac{\epsilon}{T^4} \sim \left(\frac{m}{T}\right)^3 K_1\left(\frac{m}{T}\right) + 3 \left(\frac{m}{T}\right)^2 K_2\left(\frac{m}{T}\right)$$

$$\chi_2^q \sim \left(\frac{m}{T}\right)^2 K_2\left(\frac{m}{T}\right)$$

χ_2^q weights higher p of the $f(p)$ wrt ϵ

with $m(p)$ one can have $\epsilon(T)$ like that of a massive gas
with χ_2^q of a lighter mass gas

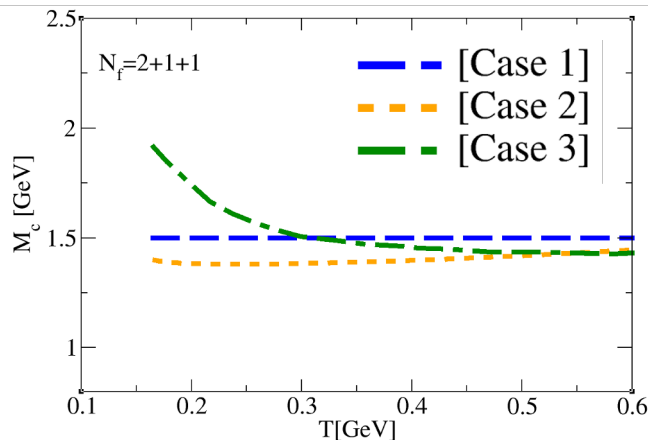
STRANGE



Citare non diagonali Articolo 23 + talk sessione

QPM ($N_f=2+1$) extension to QPMp ($N_f=2+1+1$)

Extending QPM from $N_f = 2+1$
to $N_f = 2 + 1 + 1$ **charm included**



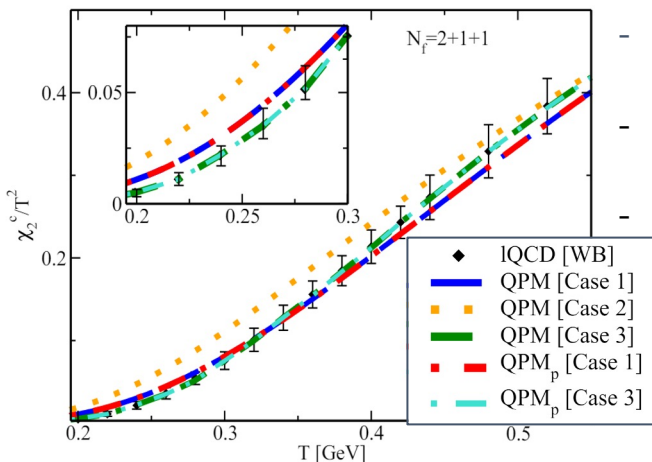
Case 1: $m_c = 1.5 \text{ GeV}$

Case 2: $m_c^2 = m_{c0}^2 + 1/3 g^2 T^2$ [$m_{c0} = 1.3 \text{ GeV}$]

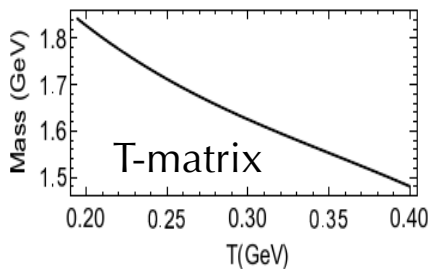
Case 3: $m_c(T)$ fixed by charm $\chi_2^c(T)$

CHARM QUARK SUSCEPTIBILITIES

$$\chi_2^c = \frac{T}{V} \frac{\partial^2 \ln Z}{\partial \mu_i^2}$$



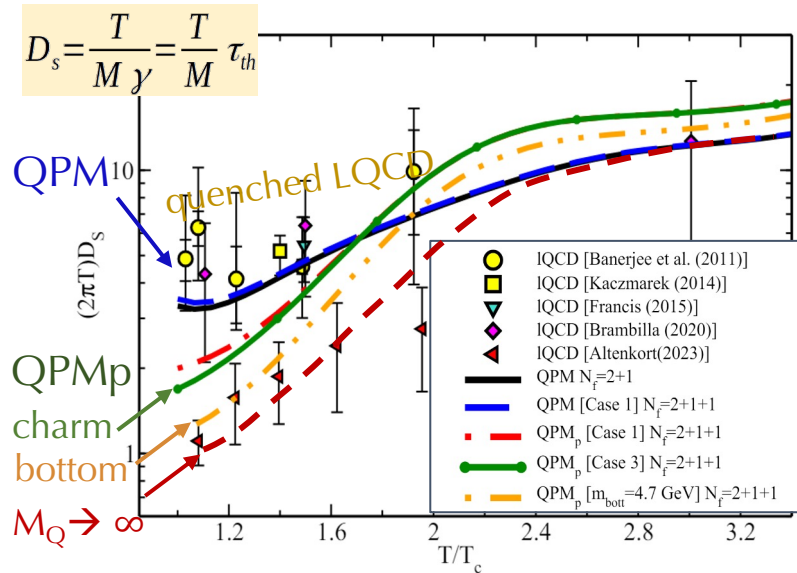
- **Disfavored:** increasing $m_c(T)$ and m_c smaller than 1.5 GeV
- m_c (standard value) not bad!
- IQCD data overestimated for $T \approx 0.2-0.3 \text{ GeV}$ with constant m_c



- Susceptibility seems to imply a decreasing $m_c(T)$ from 1.9 GeV at T_C down to 1.5 GeV at $2T_C$: **similar to T-matrix (TAMU)**

Diffusion $D_s(T)$ from QPM to QPMp

M.L. Sambataro et al. e-Print: 2404.17459

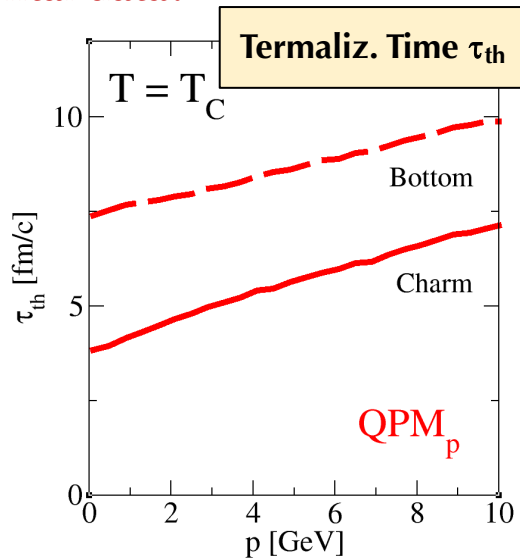


- **QPMp** describes $\epsilon, P, \chi_q, \chi_s$ of LQCD and is **closer than QPM** to D_s to LQCD(new) with dynamical fermions
- Still a significant mass dependence from charm to bottom not seen in LQCD + Non Rel. EFT
- **Can this new $D_s(T)$ generate predictions for R_{AA}, v_2, v_3 in agreement with experimental data?**

- **For observables is relevant the p-dependence:**

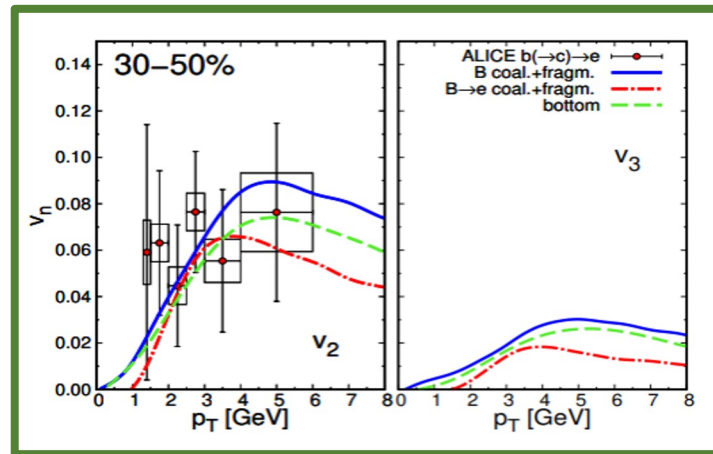
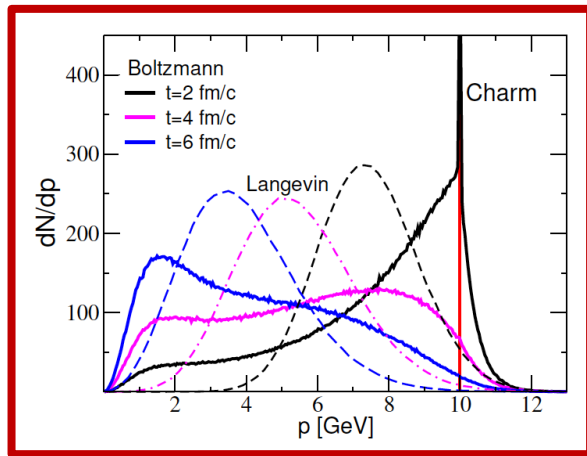
$T=T_c \rightarrow$ 40 % larger τ_{th} (smaller D_s) at $p \sim 5$ GeV, but could be larger: to be done a comparison among different approaches [QPMp p-dependence within the Bayesian analysis of Duke group]

- At T_c seems LQCD+NERFT could lead to a gap wrt D_s calculation from the hadronic part. [Das, Torres-Rincon, 2406.13286[hep-ph]]



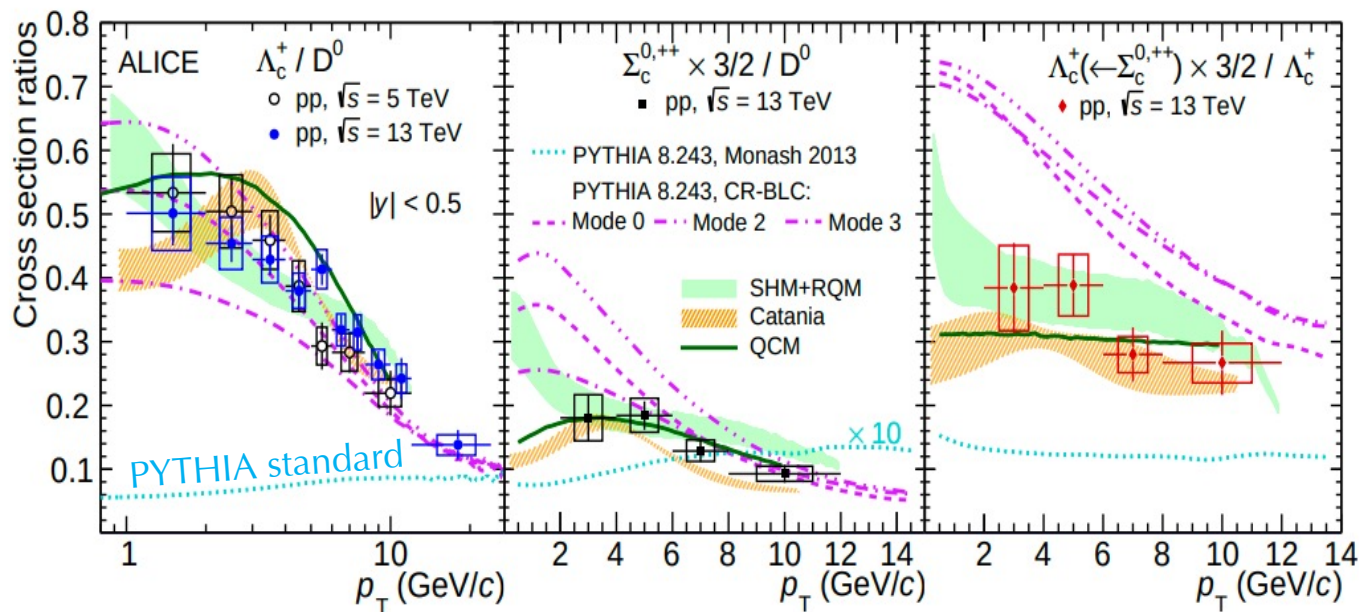
Relevance of direct Bottom measurements

- Quite close to $M \rightarrow \infty$ & **Non Relativistic** limit
 - more solid comparison to LQCD/NRQCD for $D_s(T)$
- $M_Q(T) \gg T$, gT full **Brownian motion**, satisfy fluctuations dissipation theorem
 - damps uncertainties in transport evolution (Langevin, Boltzmann, Kadanoff-Baym...)
- Impact of **hadronization** on R_{AA} & v_n moderate & less different wrt fragmentation
- Larger $\tau_{th}^b \sim M/T$ τ_{th}^c more sensitive to dynamical evolution: carry more info



Going deeper into Λ_c enhancement

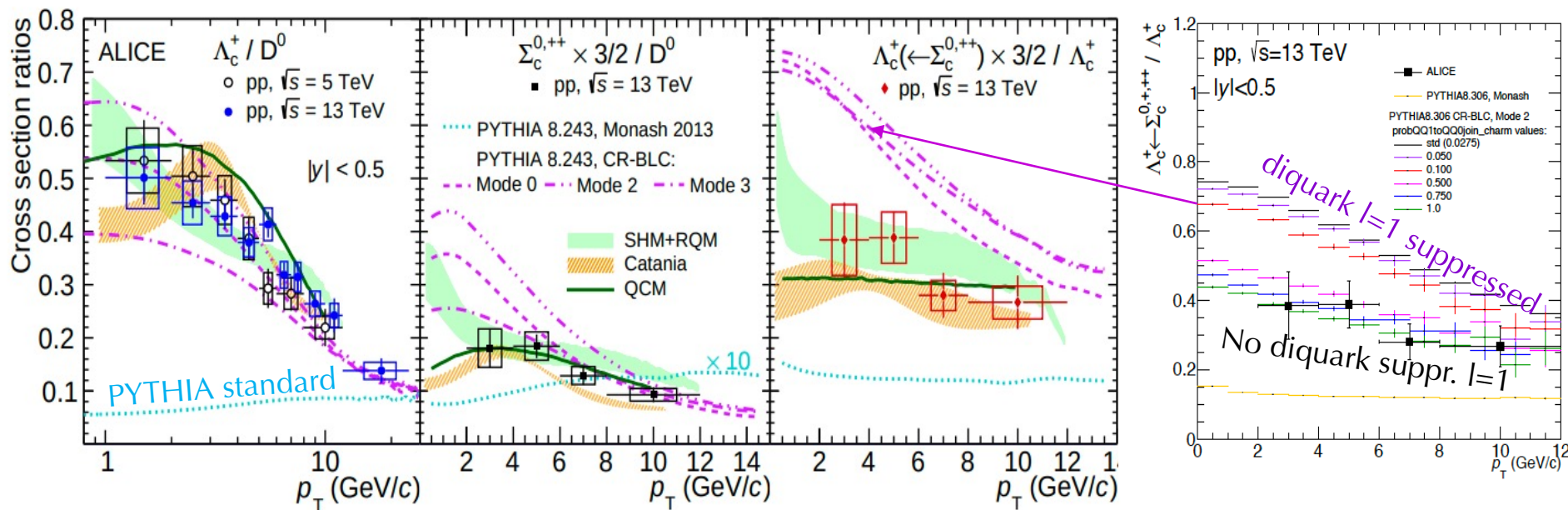
Altmann et al., arXiv 2405.19137



- Catania-coal & SHM-RQM/QCM natural good description of Σ_c/D^0 and $\Lambda_c \leftarrow \Sigma_c$
- PYTHIA-CR too many $\Sigma_c \rightarrow \Lambda_c/D^0$

Going deeper into Λ_c enhancement

Altmann et al., arXiv 2405.19137

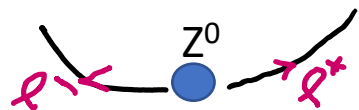


- Catania-coal & SHM-RQM/QCM natural good description of Σ_c/D^0 and $\Lambda_c \leftarrow \Sigma_c$
- PYTHIA-CR too many $\Sigma_c \rightarrow \Lambda_c/D^0$; associated to a suppression of junction **diquark $l=1$** (set $\sim e^+e^-$ for string di-quark). Removing it $\rightarrow$ Agreement to data of $\Lambda_c \leftarrow \Sigma_c$

It goes in the direction of simply recombine according to SU(3) $\sim$ simple coalescence

Magnetic field modifies Z^0 $l^\pm$ invariant mass and width in AA

Y.Sun, V. Greco, X.N. Wang, PLB827 (2022)



$\tau_{\text{decay}}(Z^0) = \tau_{\text{form}}(\text{charm}) = 0.08 \text{ fm/c}$
 $\rightarrow$ Probe same magnetic field!

Acquire $\Delta \mathbf{p}$ by e.m field
 $\rightarrow$ modify invariant mass

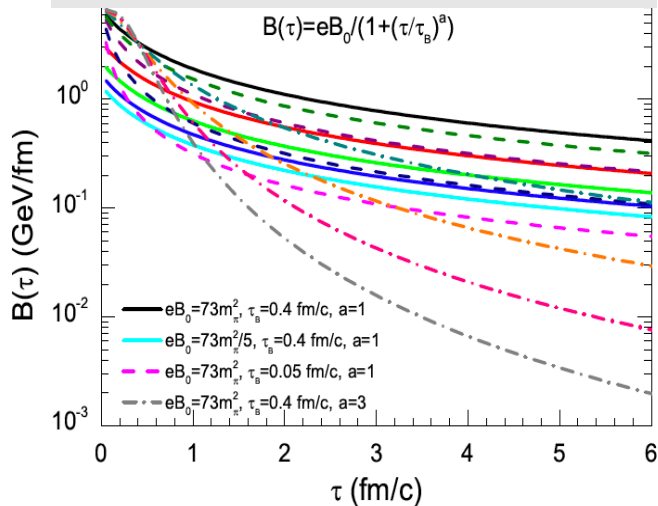
$$\rho(M) = \frac{1}{\pi} \frac{\Gamma/2}{(M - M_0)^2 + \Gamma^2/4},$$

$$\Delta \langle M \rangle = k \left(\int_{\tau_0}^{\tau_1} d\tau e B(\tau) \right)^n$$

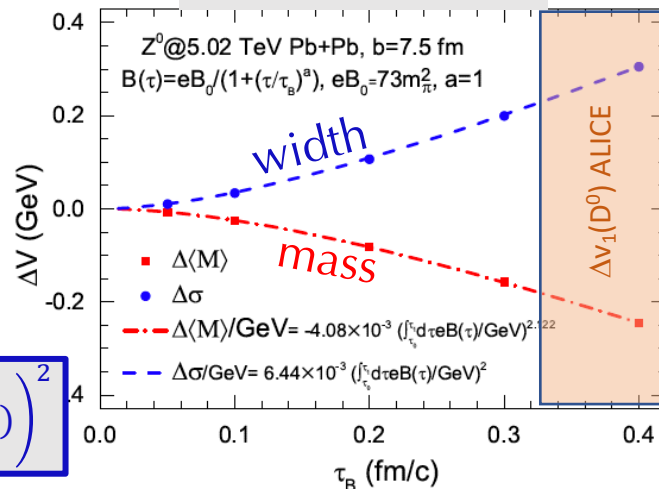
$$n = 2.16 \pm 0.16, \quad k = -[3.9 \pm 1.2] \cdot 10^{-3}$$

$$\Delta \sigma_{Z^0} = 6.4 \cdot 10^{-3} \left(\int_{\tau_0}^{\tau_1} d\tau e B(\tau) \right)^2$$

Wide range of $B(\tau)$ different pattern



Changing lifetime τ_B



Not accessible till now, may be Run 3-4 (CMS)

$\Delta V_1(\ell^+, \ell^-)$ would be even a more direct probe of B field
 peak expected at $p_T \sim 50 \text{ GeV}$ [Y. Sun, PLB 816(2021)] $\rightarrow$ Run 5-6?

On-shell & off-shell dynamics for charm

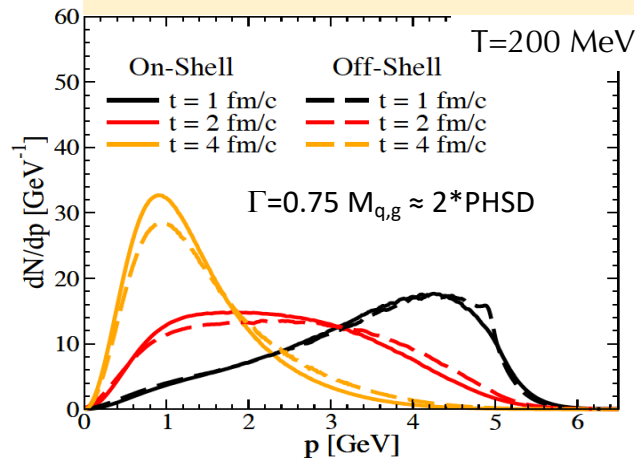
Extending collision integral to **off-shell dynamics**: solvable in a box at equilibrium

$$\begin{aligned}
 C[f] = & \int dm_i A(m_i) \int dm_f A(m_f) \\
 & \times \frac{1}{2E_p} \int \frac{d^3\mathbf{q}}{2E_q (2\pi)^3} \int \frac{d^3\mathbf{q}'}{2E_{q'} (2\pi)^3} \int \frac{d^3\mathbf{p}'}{2E_{p'} (2\pi)^3} \\
 & \times \frac{1}{\gamma_Q} \sum |\mathcal{M}_Q|^2 (2\pi)^4 \delta^4(p + q - p' - q') \\
 & \times [f(\mathbf{p}') \hat{f}(\mathbf{q}', m_f) - f(\mathbf{p}) \hat{f}(\mathbf{q}, m_i)] \quad (20)
 \end{aligned}$$

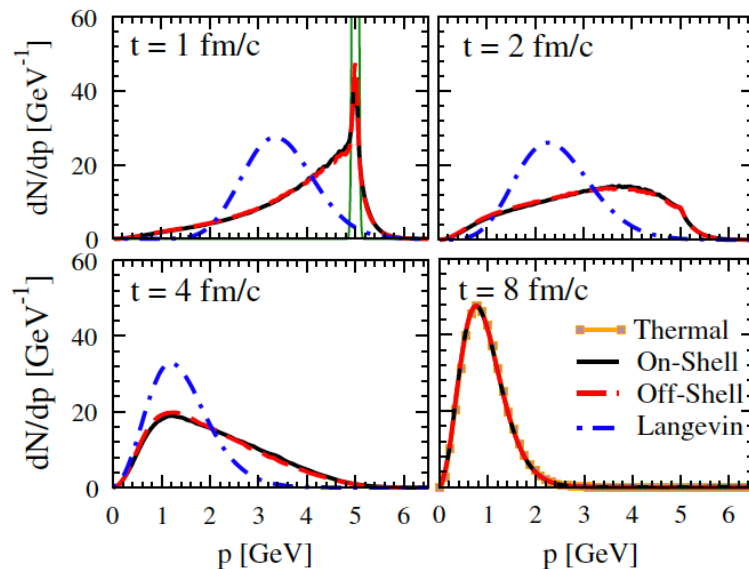
Spectral function for q & g

$$A_i^{BW}(m_i) = \frac{2}{\pi} \frac{m_i^2 \gamma_i^*}{(m_i^2 - M_i^2)^2 + (m_i \gamma_i^*)^2} \quad \text{off-shell} \approx \text{PHSD}$$

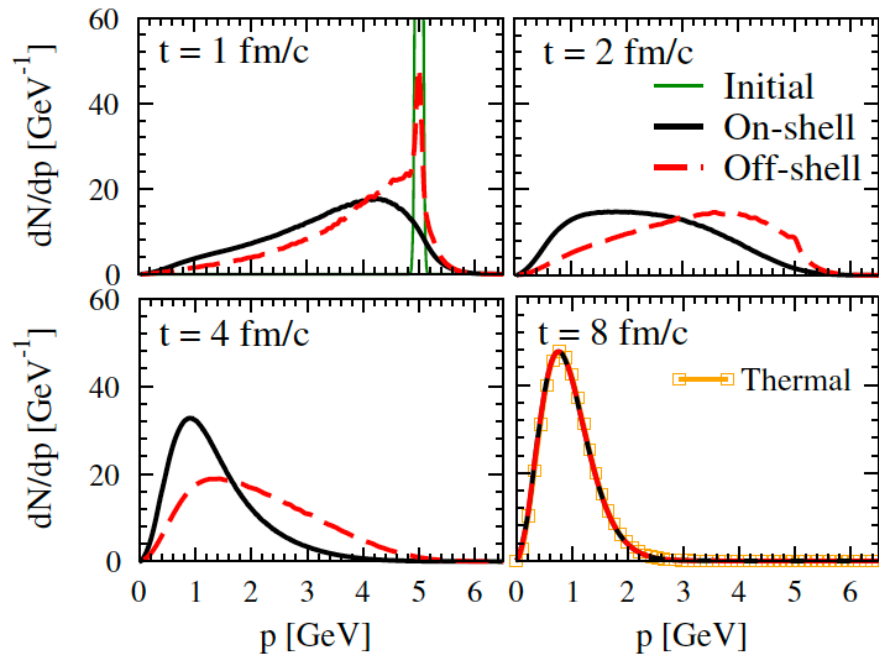
Evolution of charm at $p=5$ GeV
 ε off-shell = ε off-shell



+ a $k(p)$ making the drag off-shell=drag on-shell



Impact of off-shell dynamics on charm



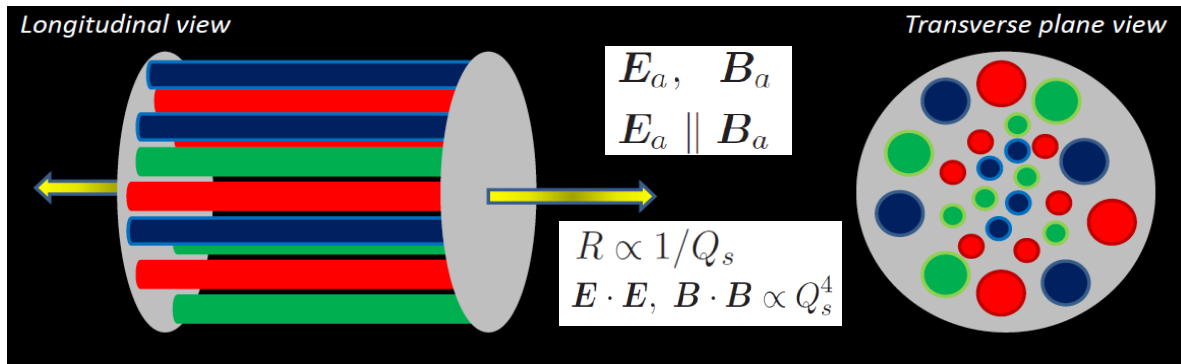
Bulk is not with the same energy density:

- energy density of off-shell case is smaller
- dynamics is Boltzmann-like: not gaussian

fluctuation around the average like in Langevin dynamics

A first study of HQ in a Glasma

What happens for $0^+ < t < 0.3-0.5 \text{ fm}/c$?



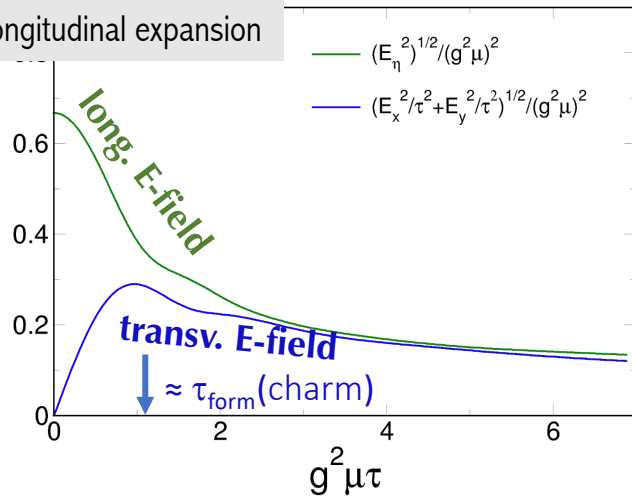
$$\langle \rho_A^a(x_T) \rho_A^b(y_T) \rangle = (g^2 \mu_A)^2 \delta^{ab} \delta^{(2)}(x_T - y_T),$$

Initialization by Mc-Lerran/Venugopalan model PRD49(1994)

$$\frac{dA_i^a(x)}{dt} = E_i^a(x), \quad (16)$$

$$\frac{dE_i^a(x)}{dt} = \sum_j \partial_j F_{ji}^a(x) - \sum_{b,c,j} f^{abc} A_j^b(x) F_{ji}^c(x). \quad (17)$$

Longitudinal expansion

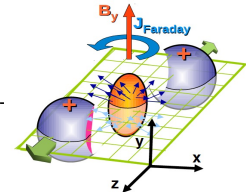


Formation time of transverse E-B fields $g^2 \mu \tau \approx 1 \approx \tau_{\text{form}}(\text{charm})$
after $\tau \cong Q_s^{-1}$, all components are equal

The very early stage has left some imprints?

Δv_1 from e.m. field?

Oliva, Plumari, V.G., JHEP 05 (2021)

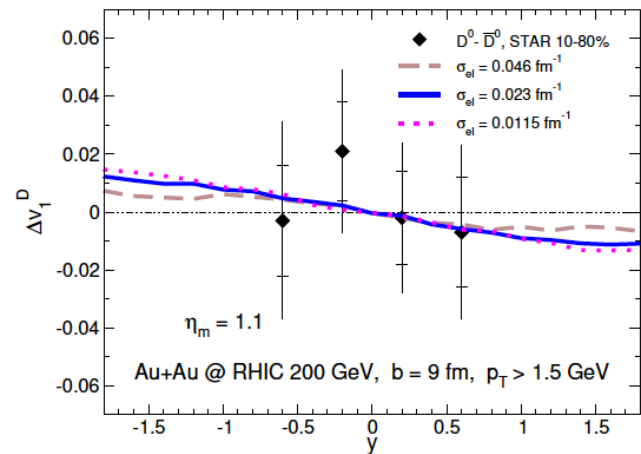
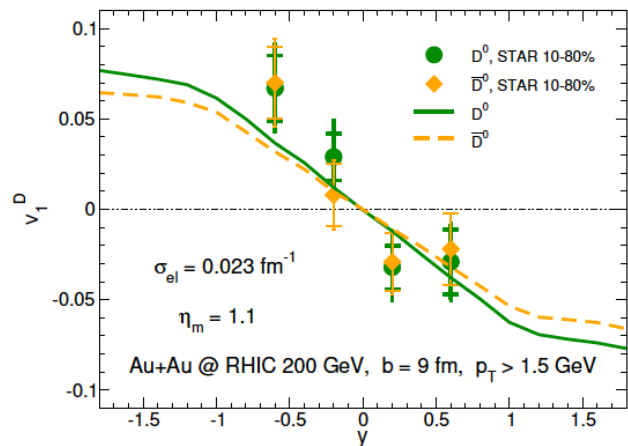


$$d(\Delta v_1)/dy|_{\text{exp}} = -0.011 \pm 0.024(\text{stat}) \pm 0.016(\text{syst})$$

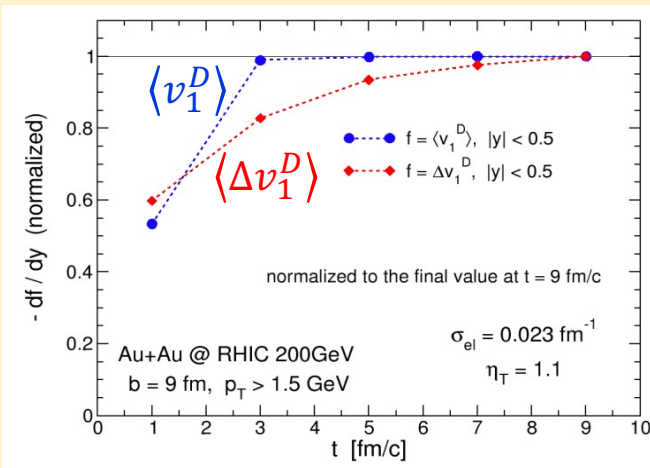
$$d(\Delta v_1)/dy|_{\text{th.}} = -0.01, \text{ L. Oliva et al.}$$

≈ 10 times larger than charged,
similar to S. Das et al., PLB768 (2017)

but could be **also consistent with 0!**



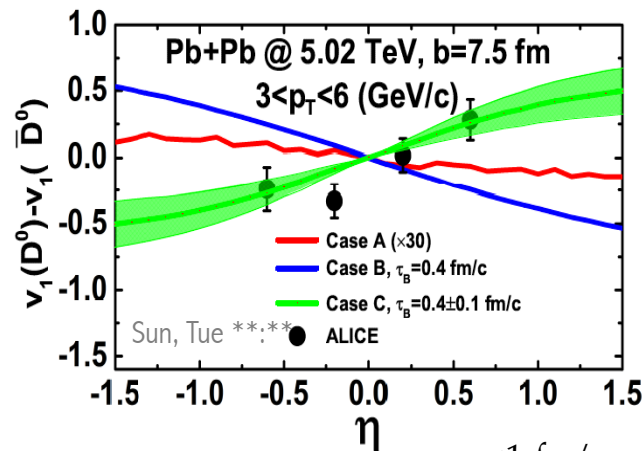
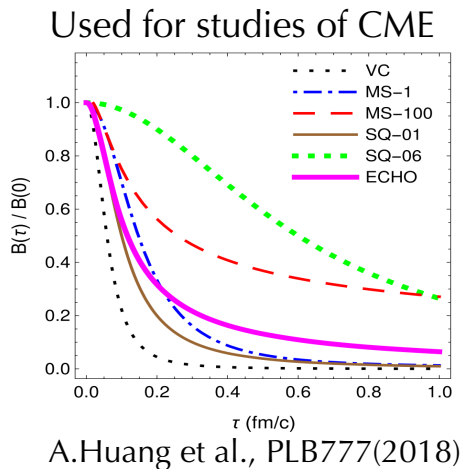
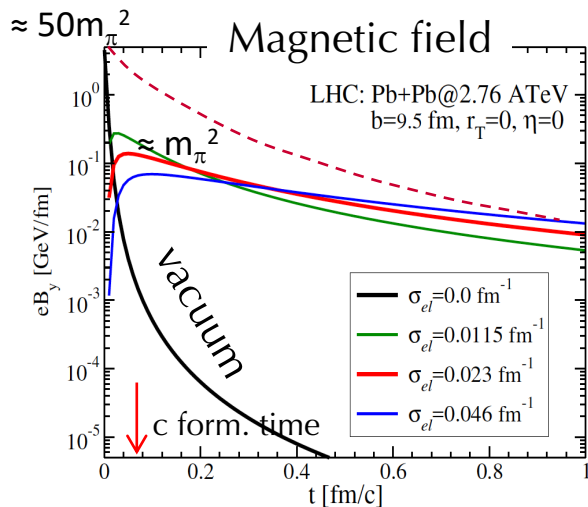
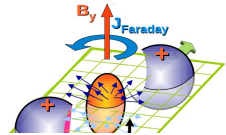
Time evolution



v_1 expected to be more
sensitive than v_2 to high T
(early time) $D_s(T)$!

Unexplored...

Electro-Magnetic field



$$B(\tau) = eB_0 / (1 + \tau^2 / \tau_B^2)$$

$\tau < 1 \text{ fm/c}$

$B(\tau) \approx B(\tau)$

$$B(\tau) = eB_0 / (1 + \tau / \tau_B)$$

$E_x(\tau) > E_x(\tau)$

like in:

K. Tuchin, PRC 88, 024911 (2013).

K. Tuchin, Adv. High Energy Phys. 2013, 1 (2013).

U. Gürsoy, D. Kharzeev, K. Rajagopal PRC 89, 054905 (2014).

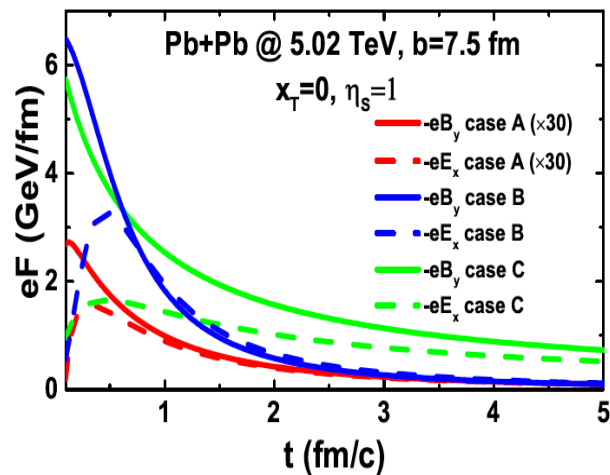
Assumptions:

- Medium σ_{el} at $t < 0$
- Electric Conductivity const. in T
- No Modification in the bulk due to currents
- No e-b-e fluctuations
- Chiral topological charge [arXiv:2002.05047, Tuchin]

Computation of early stage e.m. field is quite an issue:

- ✧ $eB_y(t=0)$ in the **vacuum**: $\approx 50 m_\pi^2$ @LHC but assuming a **medium** with $\sigma_{el} \approx 0.02 \text{ fm} \rightarrow eB_y(t=0) \approx m_\pi^2$ @LHC

E.m. field: a main source of uncertainty



Case A

E-B fields like Gursoy et al., PRC89(2014)

Medium at $t < 0$ + eq. medium $\sigma_{el}=0.023$ fm $^{-1}$

Case B and C [B_0 at $t=0$ vacuum value]

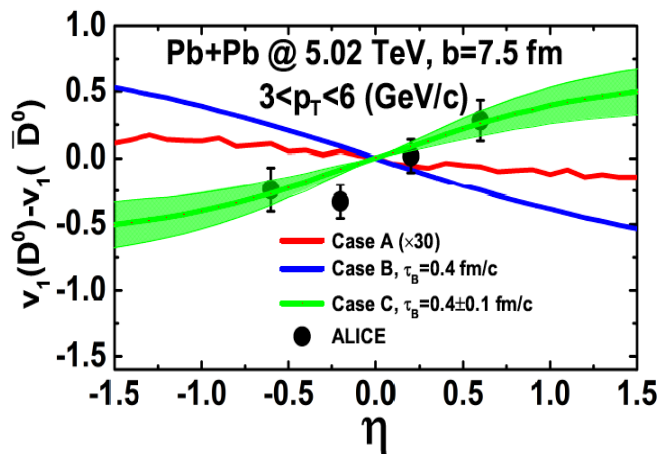
$$eB_y(x, y, \tau) = -B(\tau)\rho_B(x, y) \quad \tau_B=0.4 \text{ fm/c}$$

$$B(\tau) = eB_0/(1 + \tau^2/\tau_B^2)$$

$$B(\tau) = eB_0/(1 + \tau/\tau_B)$$

$$\nabla \times \mathbf{E} = -\partial \mathbf{B} / \partial t: \quad \text{assumption} \quad \frac{\partial E_z}{\partial x} \approx 0 \text{ small}$$

B and C similar B_y up to $t < 1$ fm/c



* e.m. field σ_{el} as for RHIC

$\rightarrow \Delta v_1(D^0)$ order magnitudes smaller than ALICE data + opposite sign

* e.m. with $B_y(t=0)$ as in vacuum

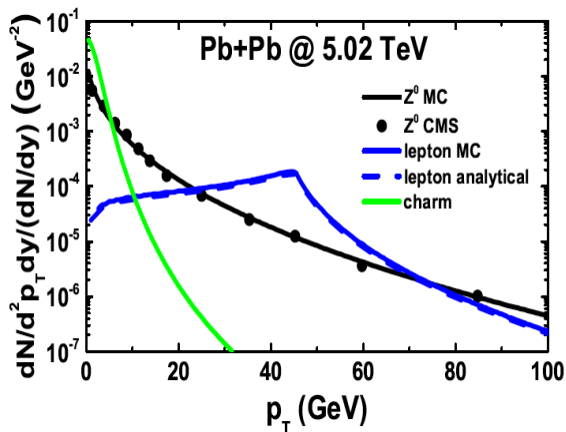
$\rightarrow$ Large $\Delta v_1(D^0)$ but **opposite** direction wrt to data

* e.m. with $B_y(t=0)$ as in vacuum, $\mathbf{E}_x \approx 0.5 \mathbf{B}_y$ ($t=0.5-1$ fm/c)

$\rightarrow \Delta v_1(D^0) \approx$ ALICE Data (1/t ideal MHD)

Time derivative of $B_y(t)$ even more relevant than absolute values⁵⁶

V_1 splitting for D^0 - $\underline{D}^0$ and l^+ - l^- from Z^0 decay and

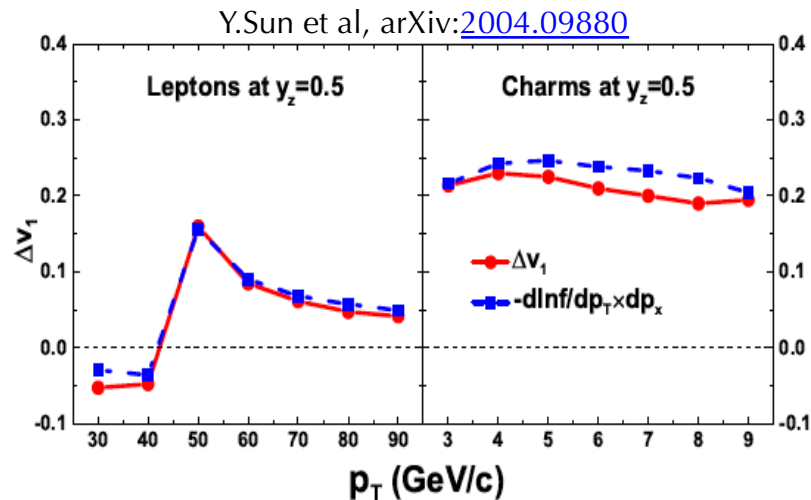


- No medium strong interaction
- $\tau_{\text{decay}}(Z^0) = \tau_{\text{form}}(\text{charm}) = 0.08 \text{ fm/c}$
- Massless more easily to drag + $qE_x - qv_z B_y \approx q(E_x - B_y)$
- Charge 1.5 times larger

Surprises:

- 1) $\Delta v_1(l^+, l^-) < \Delta v_1(D^0, \underline{D}^0)$ even if $\Delta p_x(l) \approx 2 * \Delta p_x(D)$
 - 2) even the sign of $\Delta v_1(l^+, l^-)$ can be opposite!?
- not because wins electric field

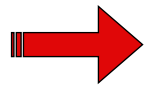
$$v_1(p_T, y) \approx \frac{\overline{\Delta p_x}(p_T, y) - \partial \ln f_a}{2 \partial p_T}.$$



Peak in $\Delta v_1(l^+, l^-)$ at $p_T \approx 50 \text{ GeV}$
 consistent with the large $\Delta v_1(D^0)$?

If $\Delta v_1 = v_1(D^0) - v_1(\underline{D}^0)$ is of electromagnetic origin $\rightarrow$ we'd have a proof of the formation of the QGP
Is there some complementary way of proving it?

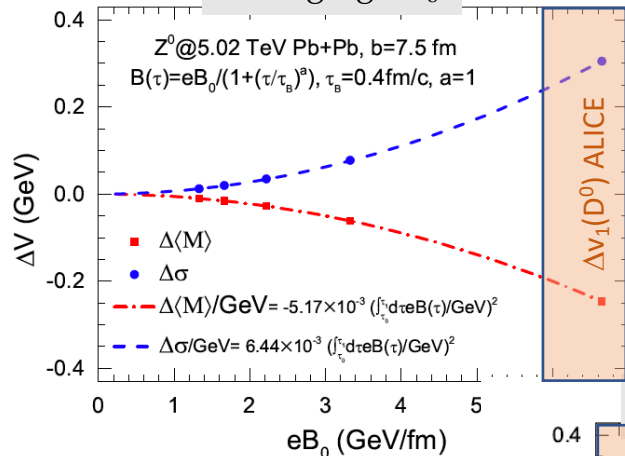
Is there a further way to pin down the e.m field strength?
Such a large splitting (in ALICE) has an electromagnetic origin?



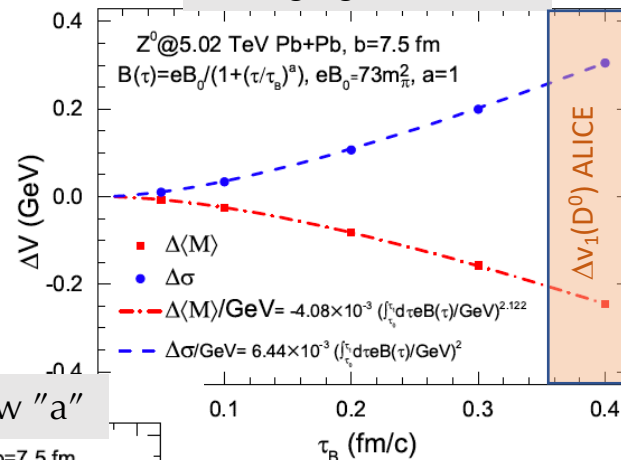
**Probing the electromagnetic fields in ultra-relativistic collisions
with leptons from Z_0 decay and charmed mesons**

Z⁰ mass and width modification in AA

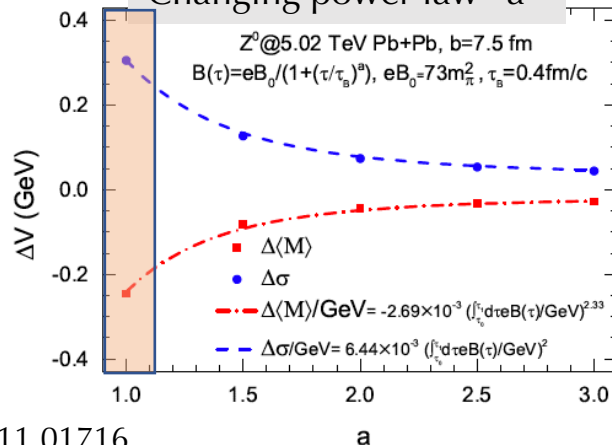
Changing eB₀



Changing lifetime τ_B



Changing power law "a"



$$\Delta\langle M \rangle = k \left(\int_{\tau_0}^{\tau_1} d\tau e B(\tau) \right)^n$$

$$n=2.16 \pm 0.16$$

$$k = -[2.69 \pm 5.17] \cdot 10^{-3}$$

$$\Delta\sigma_{Z^0} = k_\sigma \left(\int_{\tau_0}^{\tau_1} d\tau e B(\tau) \right)^2$$

$$k_\sigma = -6.44 \cdot 10^{-3}$$

To be done vs centralities, systems,...