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# Studies of the Structure of Excited Nucleons at Jefferson Lab

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*On behalf of  
The CLAS Collaboration*

Jan 2024



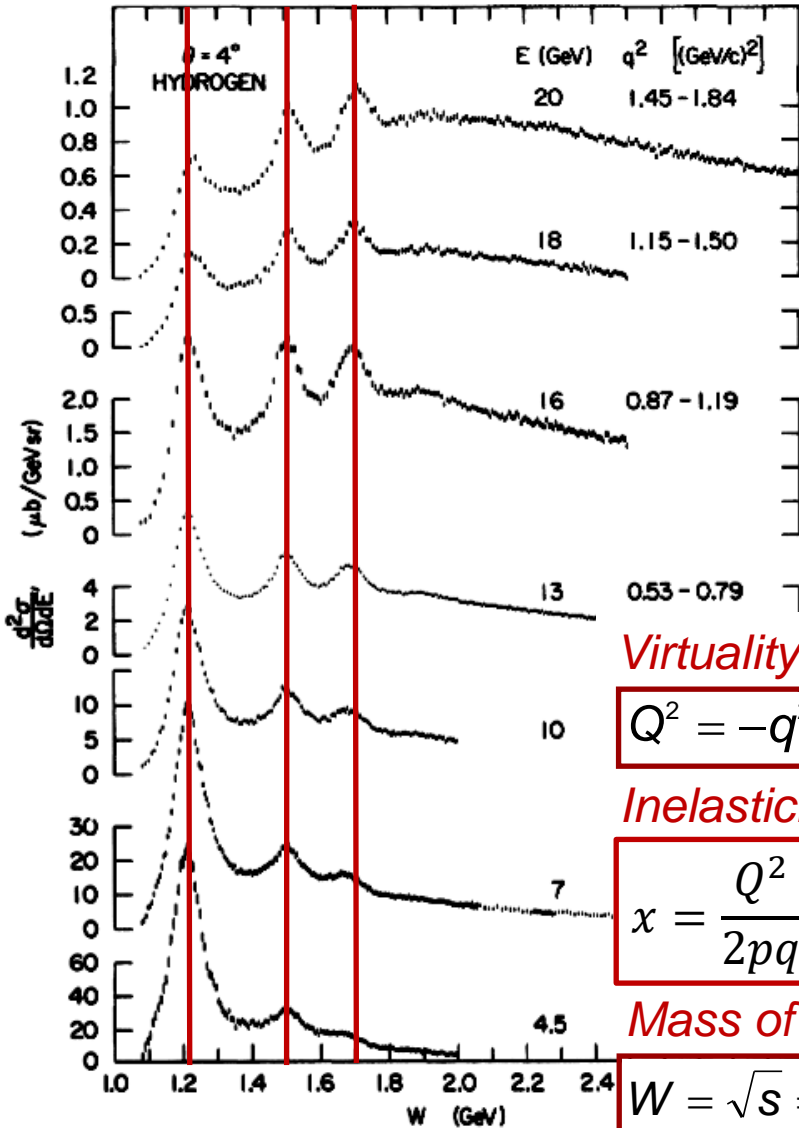
# The Proton and its Excitations

*People have always been fascinated by that are hidden from their view and by what might be found inside objects*



# Excitation of Proton Resonances

[Stein et al., Phys. Rev. D 12 (1975)]



*Virtuality of photon:*

$$Q^2 = -q^2 = (q_e^\mu - q_{e'}^\mu)^2$$

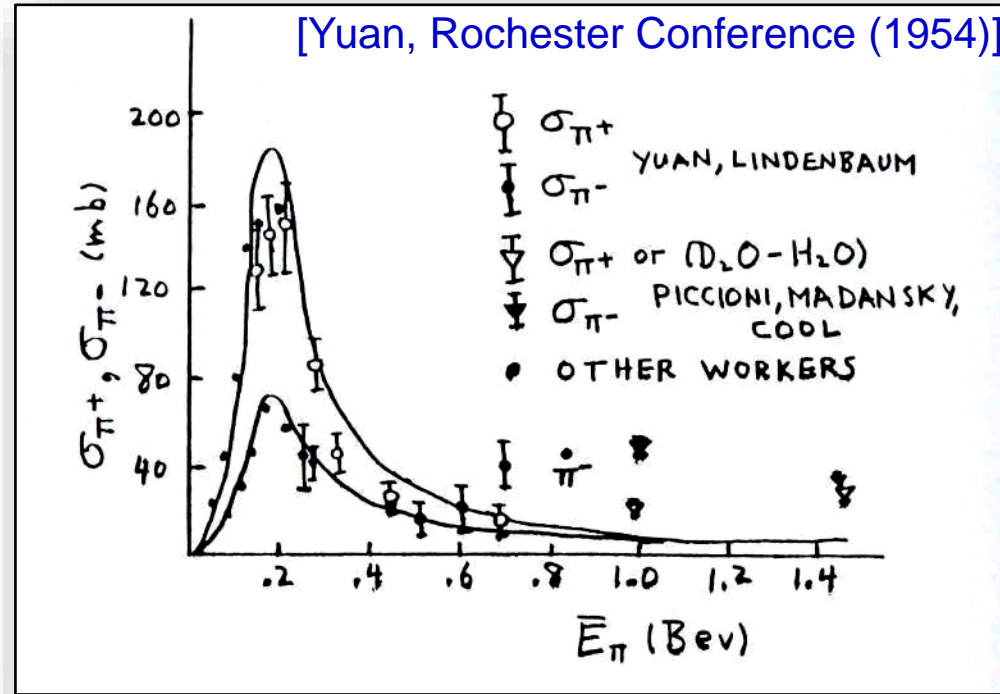
*Inelasticity of process:*

$$x = \frac{Q^2}{2pq} = Q^2 / (2Mv)$$

*Mass of excited proton:*

$$W = \sqrt{s} = \sqrt{(q^\mu + p_{\text{target}}^\mu)^2}$$

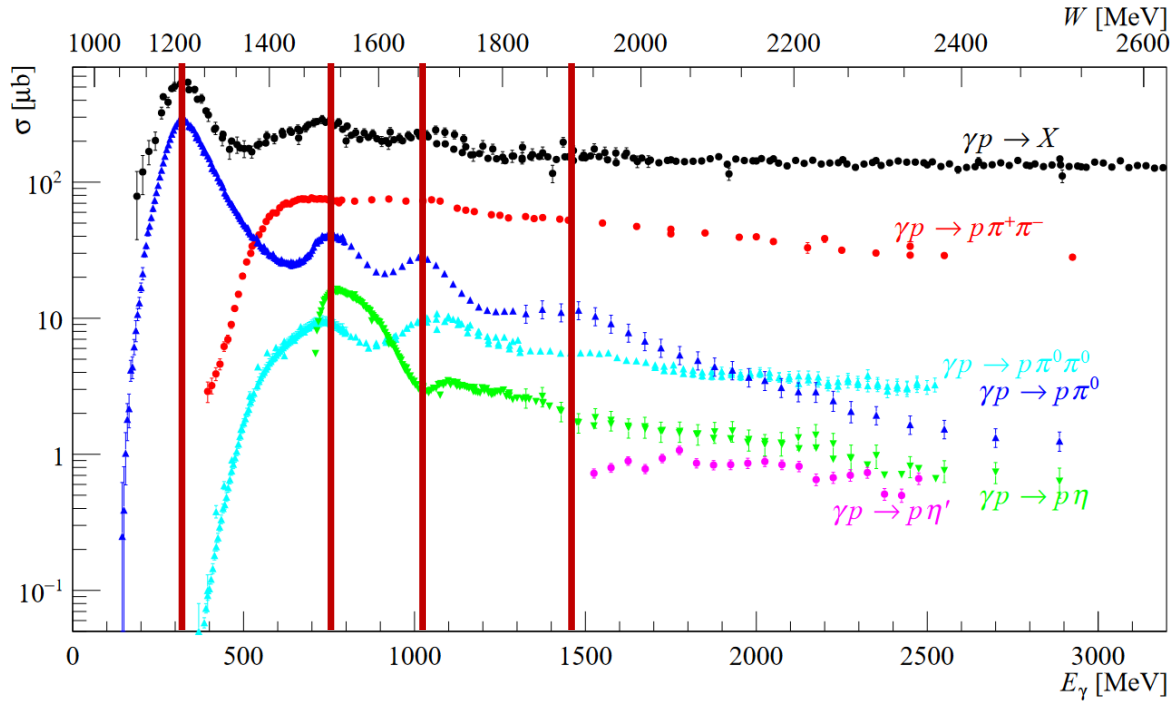
[Yuan, Rochester Conference (1954)]



- Charged *pion beams* revealed a clear **proton resonance** as early as 1954 (and established charge independence)
- *Electron scattering* on protons revealed **three resonance regions** in the 1970s

# The Virtue of Electro- (and Photo-) Excitations

Clean process with electromagnetic vertex well known from QED

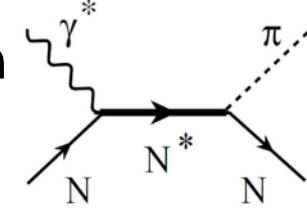


Study of many relevant observables:

- Excitation spectrum / quantum numbers
- Selective and exclusive reactions

## Single-pion production

as an example:



- $Q^2$  evolutions in electroproduction
- **Polarization** in photoproduction:

[Thiel, Afzal, Wunderlich, Prog. Part. Nucl. Phys. 125, 103949 (2022)]

Light baryon spectroscopy by meson-production reactions at electron accelerators

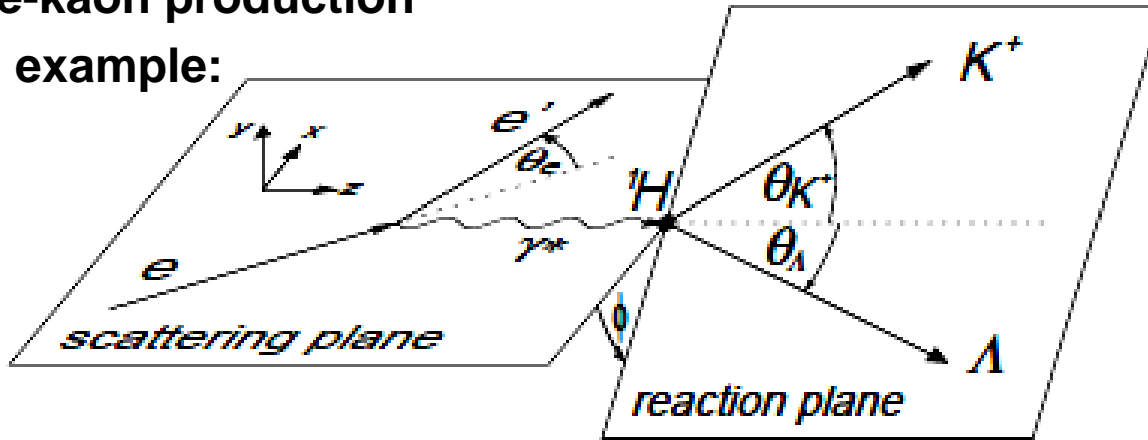
Beam		Target			Recoil			Target + Recoil								
		-	-	-	$x'$	$y'$	$z'$	$x'$	$x'$	$x'$	$y'$	$y'$	$y'$	$z'$	$z'$	$z'$
		$x$	$y$	$z$	-	-	-	$x$	$y$	$z$	$x$	$y$	$z$	$x$	$y$	$z$
unpolarized	$\sigma_0$	$T$			$P$			$T_{x'}$	$L_{x'}$		$\Sigma$	$T_{z'}$		$L_{z'}$		
linearly pol.	$\Sigma$	$H$	$P$	$G$	$O_{x'}$	$T$	$O_{z'}$	$L_{z'}$	$C_{z'}$	$T_{z'}$	$E$	$\sigma_0$	$F$	$L_{x'}$	$C_{x'}$	$T_{x'}$
circularly pol.		$F$		$E$	$C_{x'}$		$C_{z'}$	$O_{z'}$		$G$		$H$		$O_{x'}$		

# Separation of Cross Sections Into Structure Functions

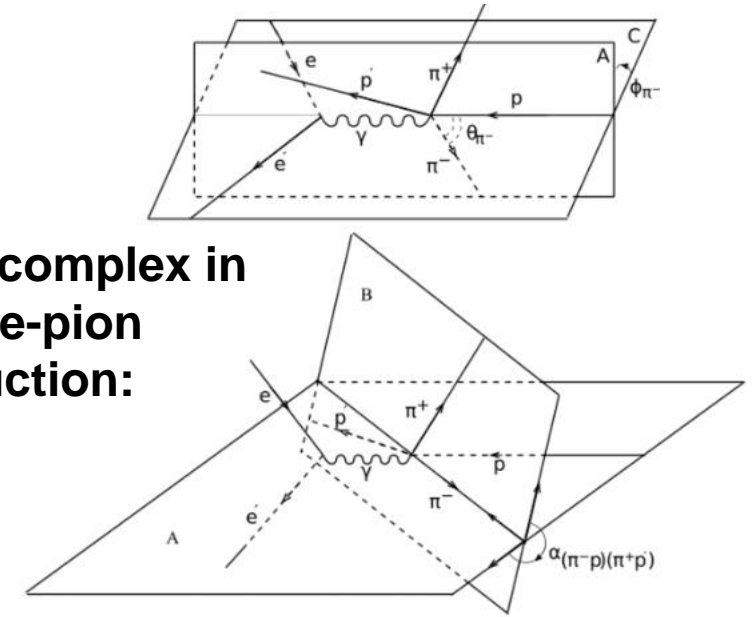
Five-fold differential cross section separates in **virtual photon flux** and **virtual photoproduction**

$$\frac{d\sigma}{dE' d\Omega_e' d\Omega_K^*} = \Gamma \frac{d\sigma}{d\Omega_K^*}$$

Single-kaon production  
as an example:



More complex in  
double-pion  
production:



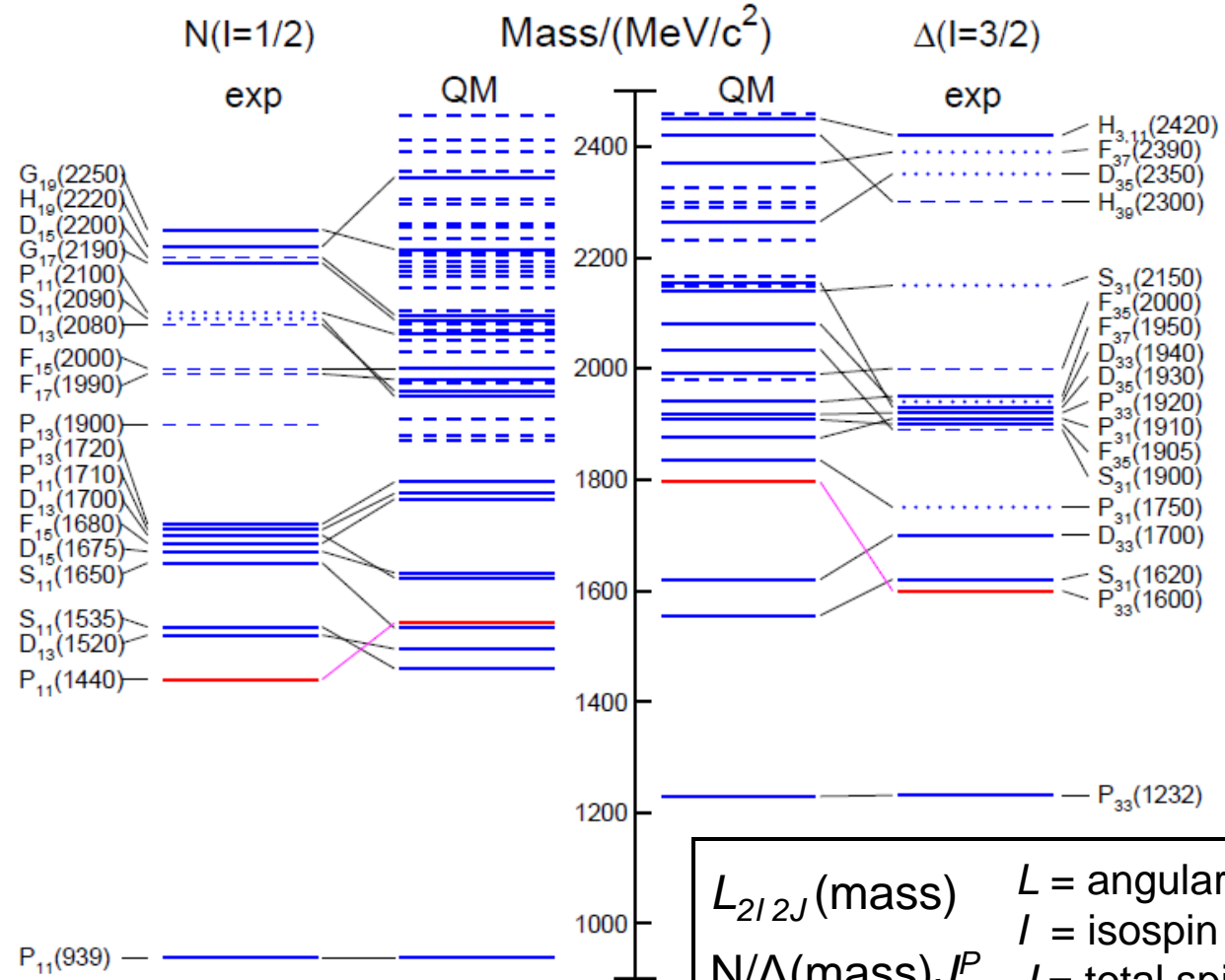
$$\frac{d\sigma}{d\Omega_K^*} = \sigma_T + \epsilon\sigma_L + \epsilon\sigma_{TT} \cos 2\phi + \sqrt{2\epsilon(1+\epsilon)}\sigma_{LT} \cos \phi + h\sqrt{2\epsilon(1-\epsilon)}\sigma_{LT'} \sin \phi$$

Degree-of-polarization of photon:  $\epsilon = \left(1 + 2\frac{|\vec{q}|^2}{Q^2} \tan^2 \theta/2\right)^{-1}$   
 Helicity of incoming electron:  $h$

[E. Amaldi, S. Fubini, and G. Furlan, Pion-Electroproduction (1979)]

[A. Donnachie & G. Shaw, Electromagnetic Interactions of Hadrons (1978)]

# N\* Spectrum in Experiments vs. Quark Models



State	2010	2020	$\pi N$	$K\Lambda$	$K\Sigma$	$\gamma N$
<b>N(1710)1/2<sup>+</sup></b>	***	****	****	**	*	****
<b>N(1875)3/2<sup>-</sup></b>		***	**	*	*	**
<b>N(1880)1/2<sup>+</sup></b>		***	*	**	**	**
<b>N(1895)1/2<sup>-</sup></b>		****	*	**	**	****
<b>N(1900)3/2<sup>+</sup></b>	**	****	**	**	**	****
<b>N(2000)5/2<sup>+</sup></b>	*	**	*			**
<b>N(2060)5/2<sup>-</sup></b>		***	**	*	*	***
<b>N(2100)1/2<sup>+</sup></b>	*	***	***	*		**
<b>N(2120)3/2<sup>-</sup></b>		***	**	**	*	***
<b><math>\Delta(1600)3/2<sup>+</sup></math></b>	***	****	***			****
<b><math>\Delta(1900)1/2<sup>-</sup></math></b>	**	***	***		**	***
<b><math>\Delta(2200)7/2<sup>-</sup></math></b>	*	***	**		**	***

**Some problems are evident:**

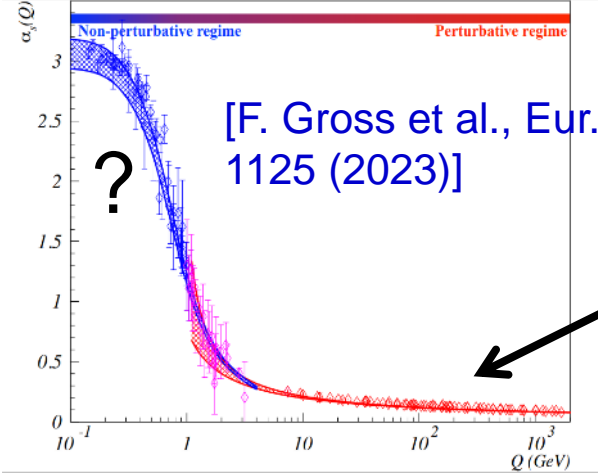
- Ordering and clustering of states
- Missing resonances
- Incomplete/uncertain data (\*/\*\*)

[PDG Review Part. Phys. (2022)]

The nucleon's excitation spectrum reflects its complexity where our knowledge is incomplete

# Connection to the Strong QCD Regime

Standard Model  $\alpha_s$  **diverges** as  $Q$  approaches zero and **QCD** becomes **non-perturbative**

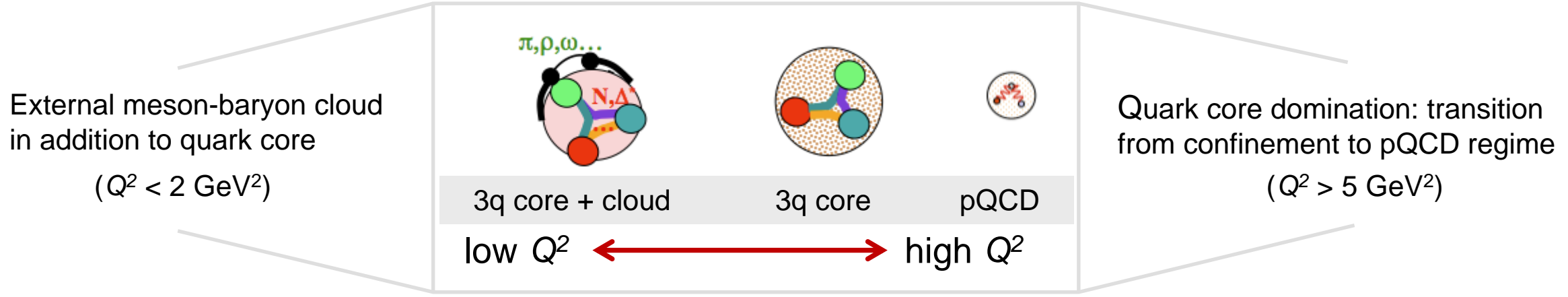


$$\mathcal{L} = \frac{1}{4g^2} G_{\mu\nu}^a G_{\mu\nu}^a + \sum_j \bar{q}_j (i\gamma^\mu D_\mu + m_j) q_j$$

where  $G_{\mu\nu}^a \equiv \partial_\mu A_\nu^a - \partial_\nu A_\mu^a + if_{bc}^a A_\mu^b A_\nu^c$   
and  $D_\mu \equiv \partial_\mu + it^a A_\mu^a$

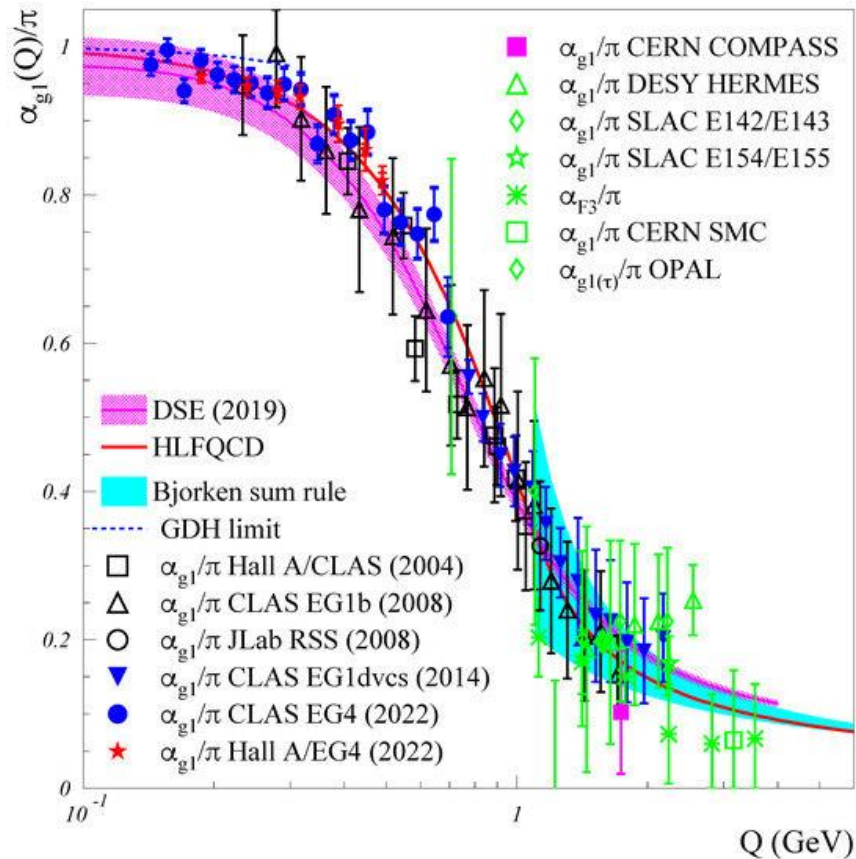
*That's it!*

[Frank Wilczek, Physics Today, August 2000]



Confined systems and hadronic degrees-of-freedom play key role for understanding QCD

# Non-Perturbative QCD Phenomena



[A. Deur et al., "Experimental Determination of the QCD Effective Charge  $\alpha_{g_1}(Q)$ ", Particles 5, 171 (2022)]

- For  $Q \ll 1$  GeV,  $\alpha_s(Q) \gtrsim 1$ , which is one of the crucial pieces leading to **quark confinement**
- Calculation of non-perturbative QCD phenomena can be performed numerically in **Lattice QCD**
- **Continuum QCD** methods such as Dyson-Schwinger and Bethe-Salpeter equations (DSE/BSE) do not require a discretization of spacetime
- Data show that the QCD effective charge  $\alpha_{g_1}(Q)$  becomes  $Q$ -independent at very low  $Q$
- **Data compare well with two recent predictions** based on DSE and on the AdS/CFT duality
- $\alpha_{g_1}(Q)$  approaches QCD running coupling  $\alpha_s(Q)$  and characterizes **magnitude of the strong interaction**

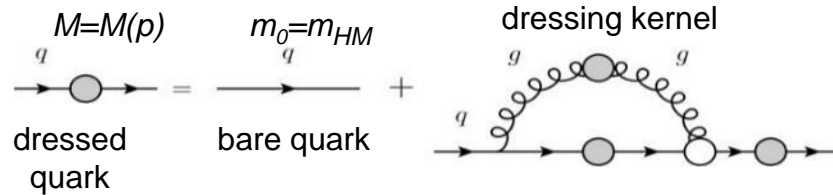
Experimental access to QCD observables through spin structure of neutron and proton



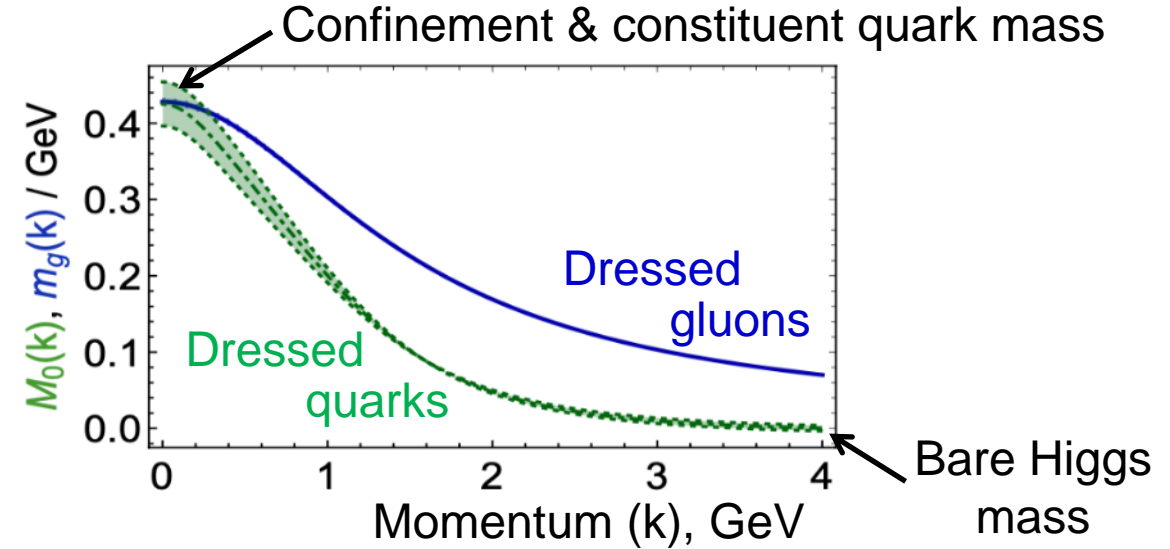
# QCD Dynamics with Dressed Quarks

## Concepts within Continuum Schwinger Method:

- Dressed quark mass depends on its momentum



- Emergence of hadron mass (EHM) from QCD
- Resonances probe EHM where sum of dressed quark masses is dominant contribution to mass
- Consistency on momentum evolution of dressed quark mass function to validate of insight into EHM

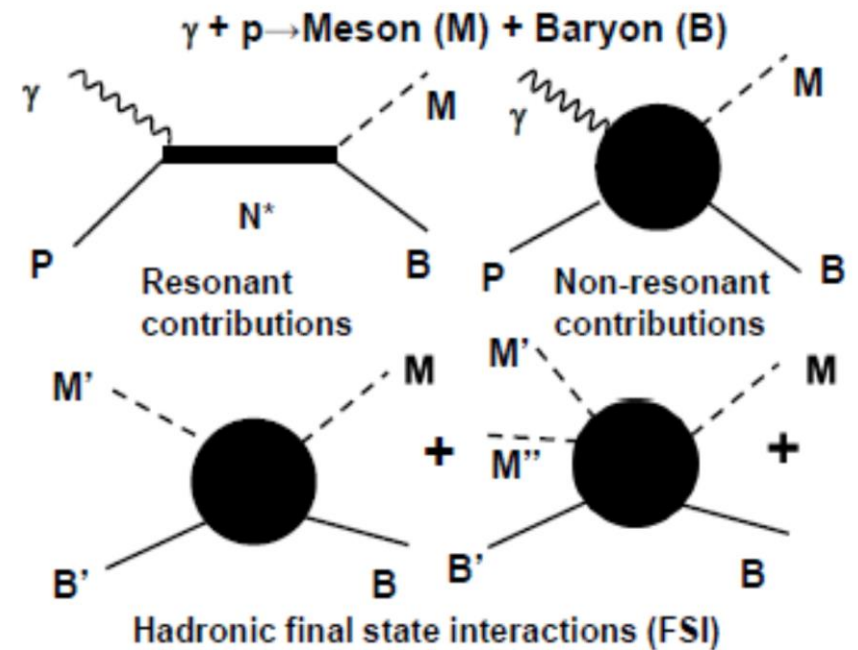


[M. Ding, C.D. Roberts, S.M. Schmidt, Emergence of Hadron Mass and Structure, Particles 6, 57 (2023)]

Hadron masses are an emergent feature of QCD

# Program of $N^*$ Physics at Electron Accelerators

- Study of **exclusive reaction channels** over a broad kinematic range:  $\pi N$ ,  $\omega N$ ,  $\varphi N$ ,  $\eta N$ ,  $\eta' N$ ,  $\pi\pi N$ ,  $KY$ ,  $K^*Y$ ,  $KY^*$
- **Common efforts** at Jefferson Lab, ELSA, MAMI, and others:
  - Separation of resonant and non-resonant contributions
- Extraction of **electrocouplings** from zero to high  $Q^2$ :
  - Quark mass momentum dependence shapes  $N^*$  states and  $Q^2$  evolution of electrocouplings
- Many facets of **non-perturbative** strong interaction are reflected in  $N^*$  states and **emergence from QCD**



Goal must be to explore the *spectrum* and *structure* of  $N^*$  states and their connection to QCD dynamics

*Good physics needs good tools*



# Design Model of The CLAS12 Spectrometer

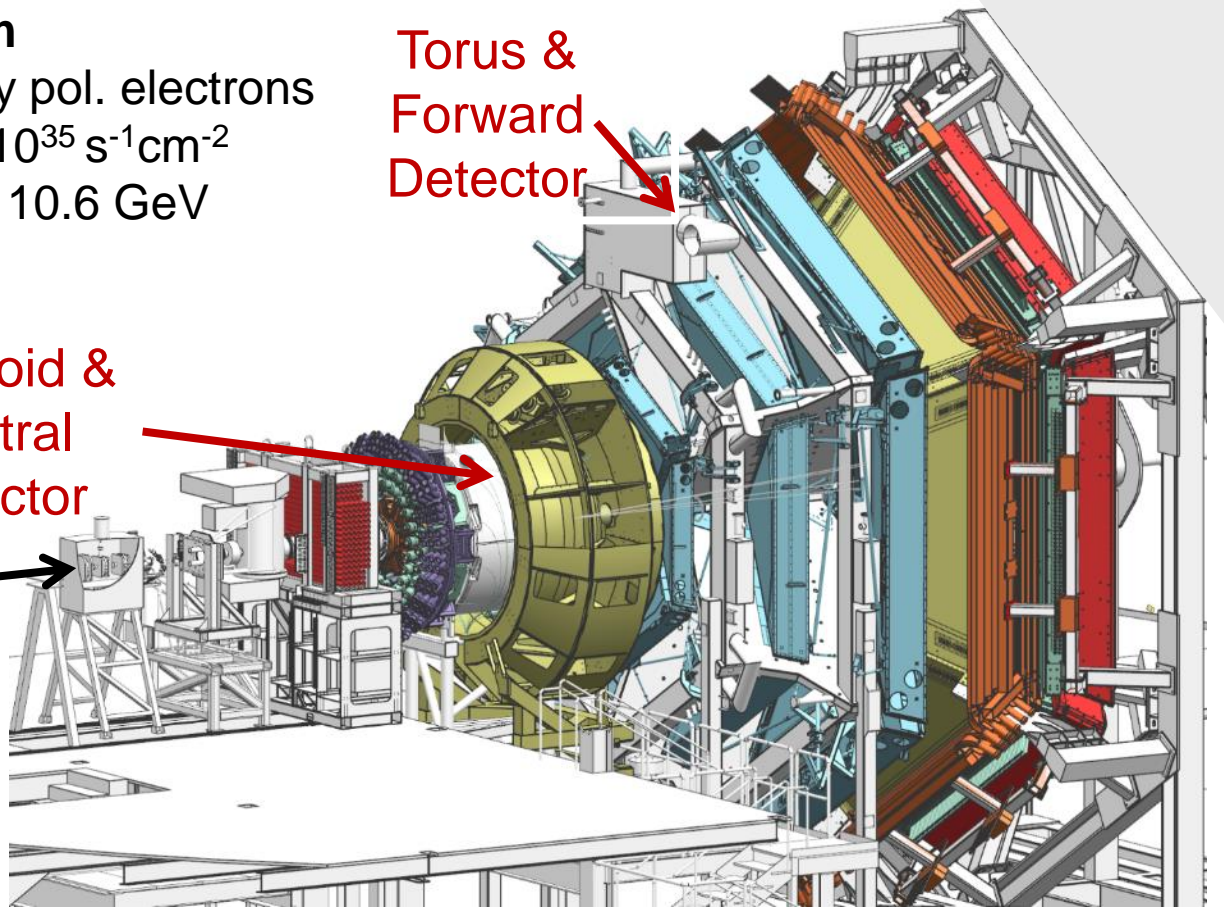
## Beam

- 85% longitudinally pol. electrons
- Max. luminosity:  $10^{35} \text{ s}^{-1} \text{ cm}^{-2}$
- Energies: up to  $\sim 10.6 \text{ GeV}$

Torus &  
Forward  
Detector

Solenoid &  
Central  
Detector

beam

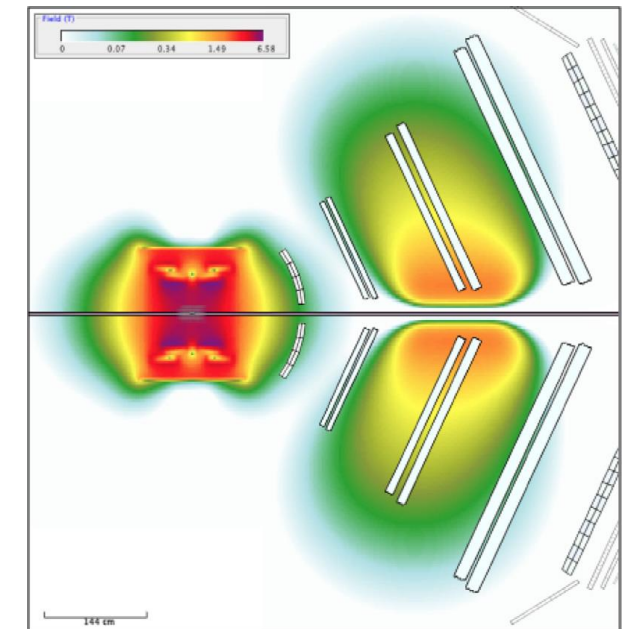


[V.D. Burkert et al., Nucl. Inst. and Meth. A 959, 163419 (2020)]

## Targets (org. by Run Groups)

- Proton (RG-A/K)
- Deuteron (RG-B)
- Nuclei (RG-M/D/E)
- Long. pol.  $\text{NH}_3/\text{ND}_3$  (RG-C)

## Magnetic Field

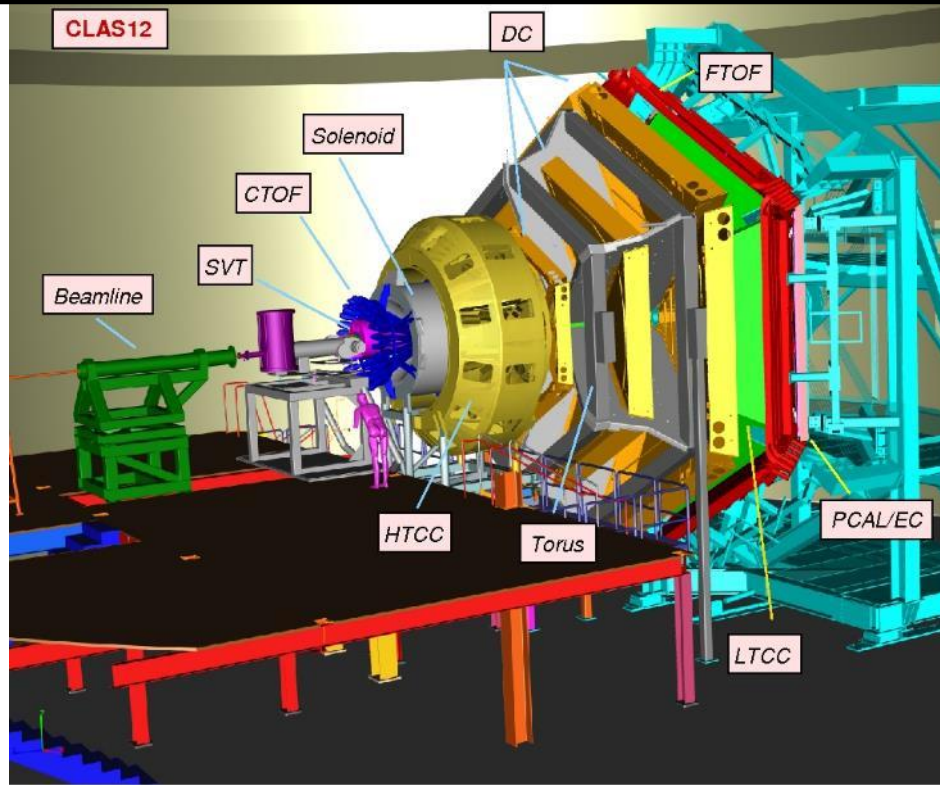


Ideal instrument to study exclusive meson electroproduction  
in the nucleon resonance region

# Subsystems of the CLAS12 Spectrometer

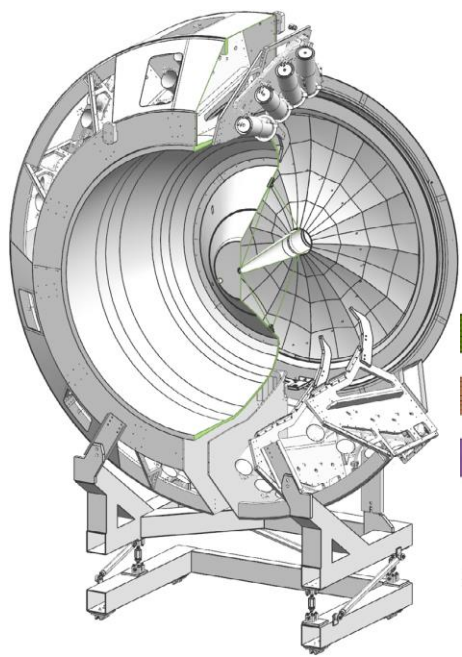
C  
E  
N  
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L

- Beamline
- Target
- Central Vertex Tracker
- Central Time of Flight
- Central Neutron Det.
- Back-Angle Neutron Det.

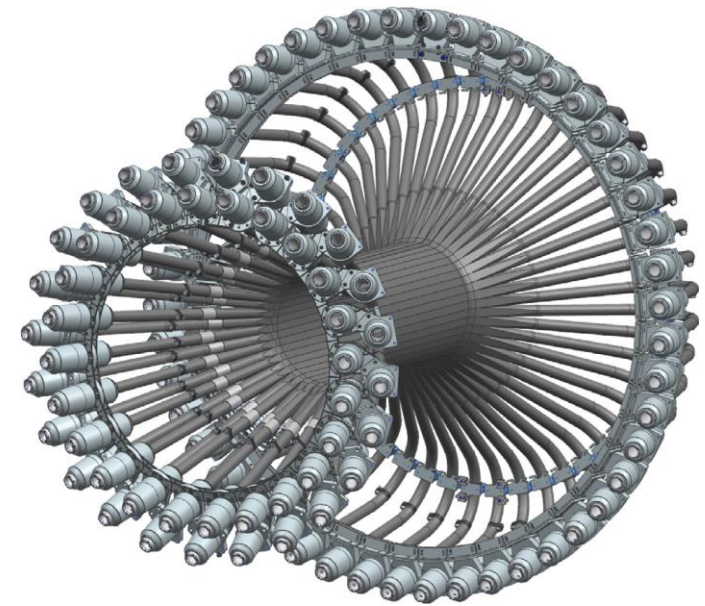
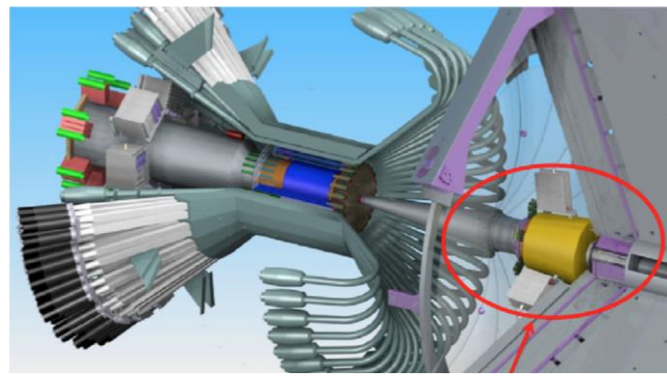
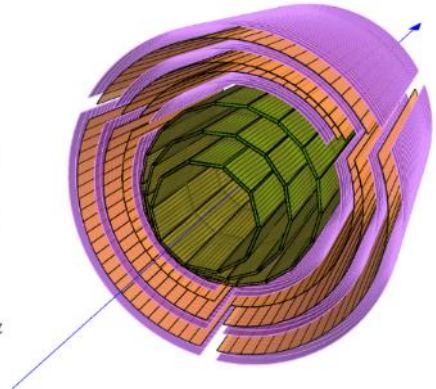
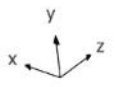


F  
O  
R  
W  
A  
R  
D

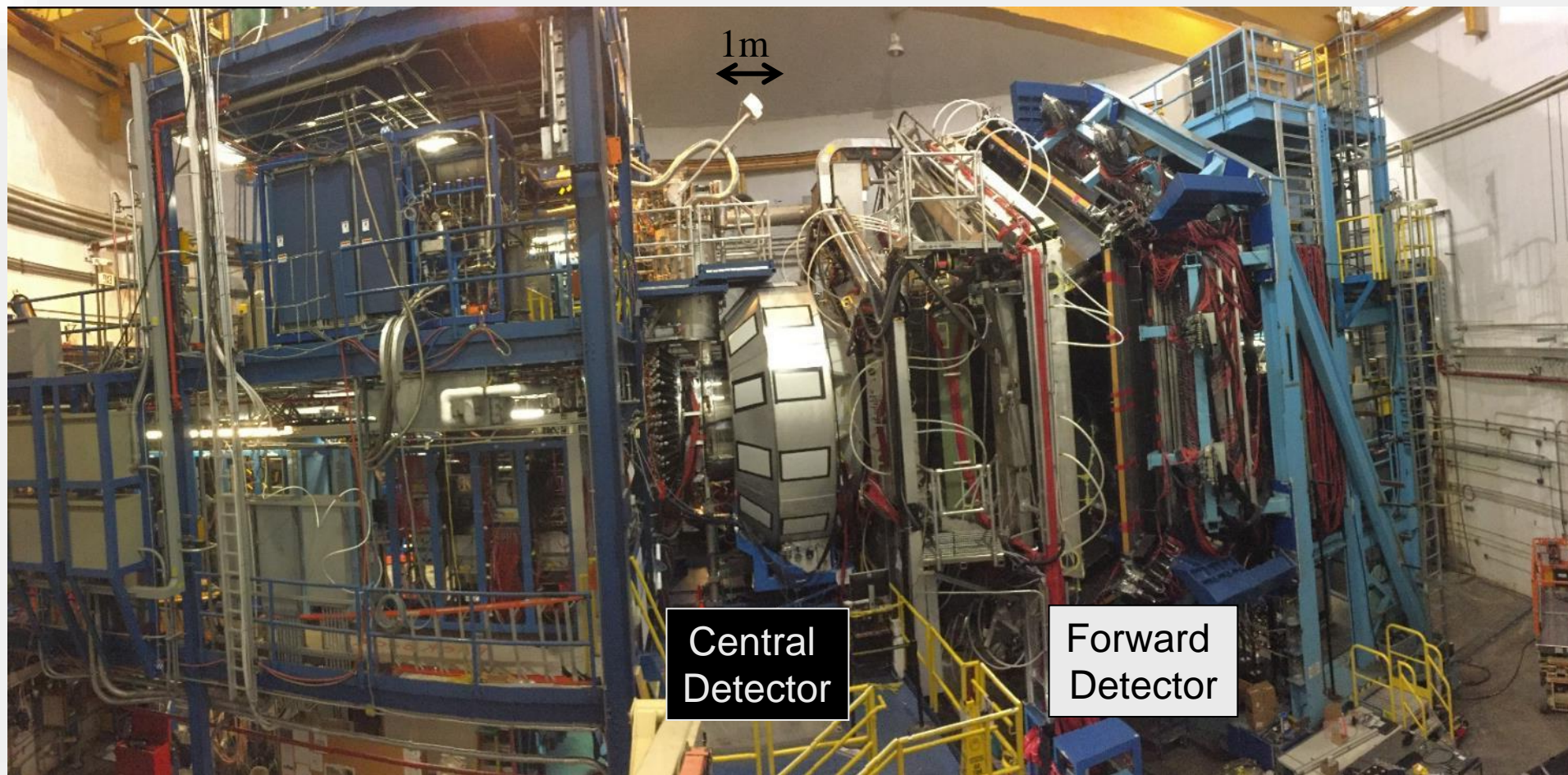
- High Threshold Cherenkov
- Forward Tagger
- Drift Chambers
- Low Threshold Cherenkov
- Ring Imaging Cherenkov
- Forward Time of Flight
- EM Calorimeter



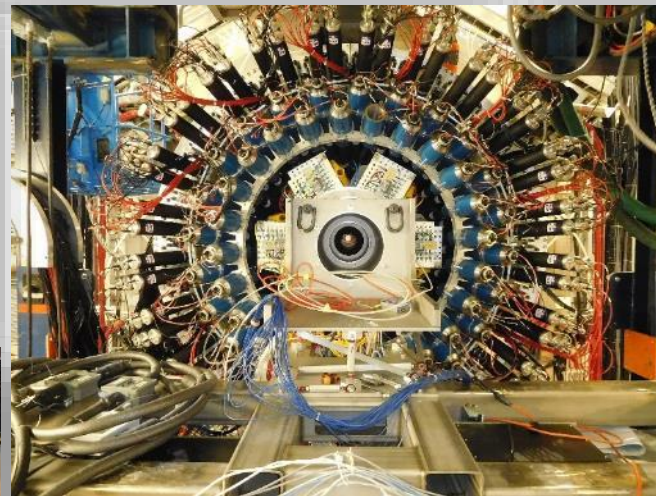
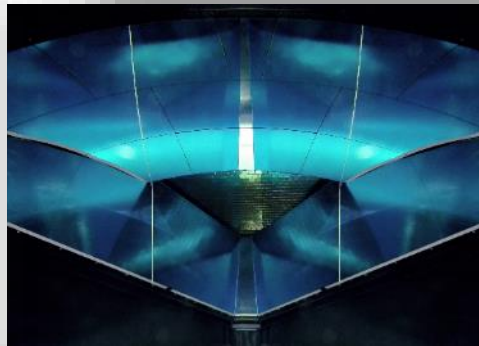
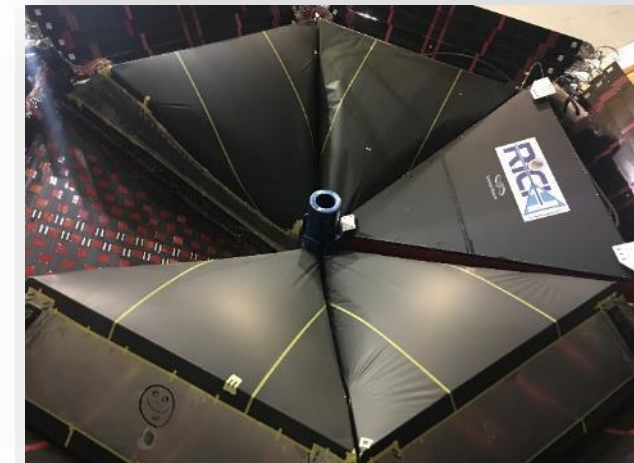
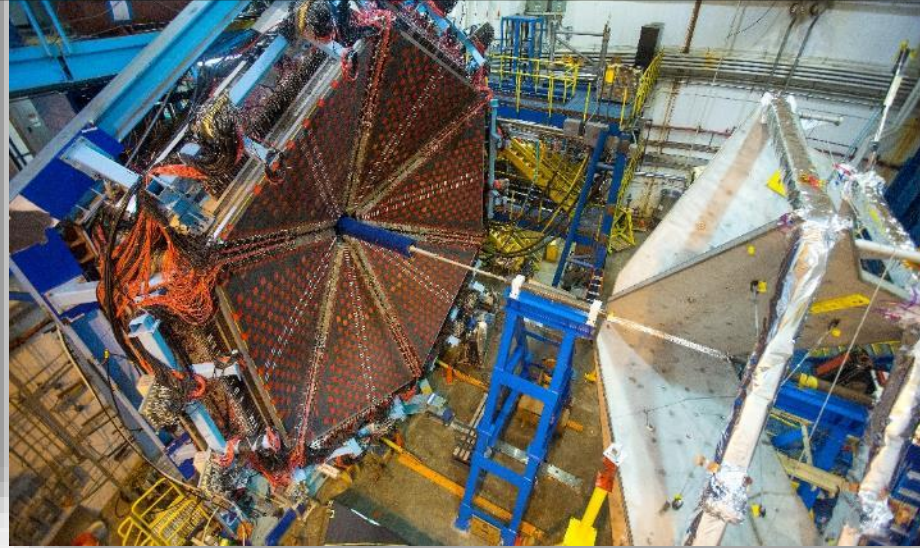
- SVT
- BMTZ
- BMTC



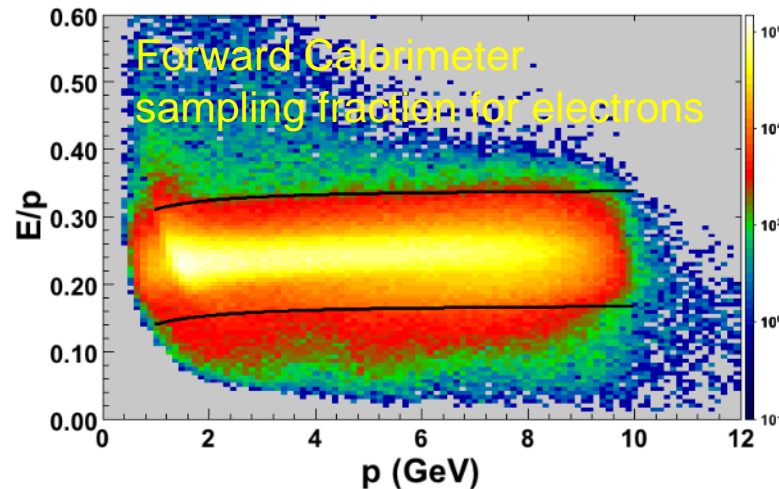
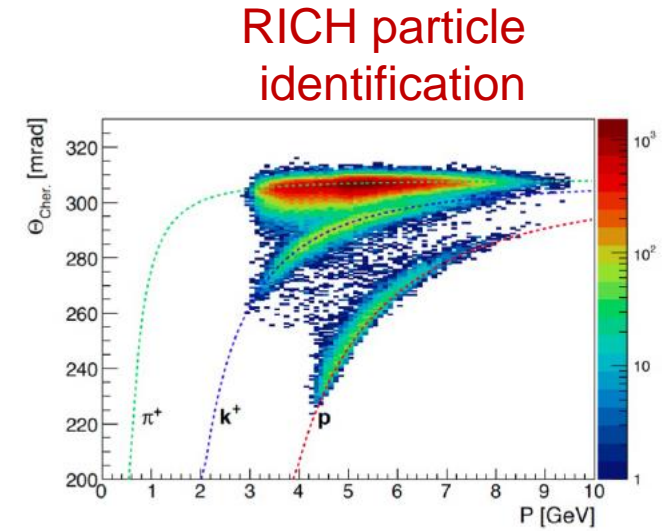
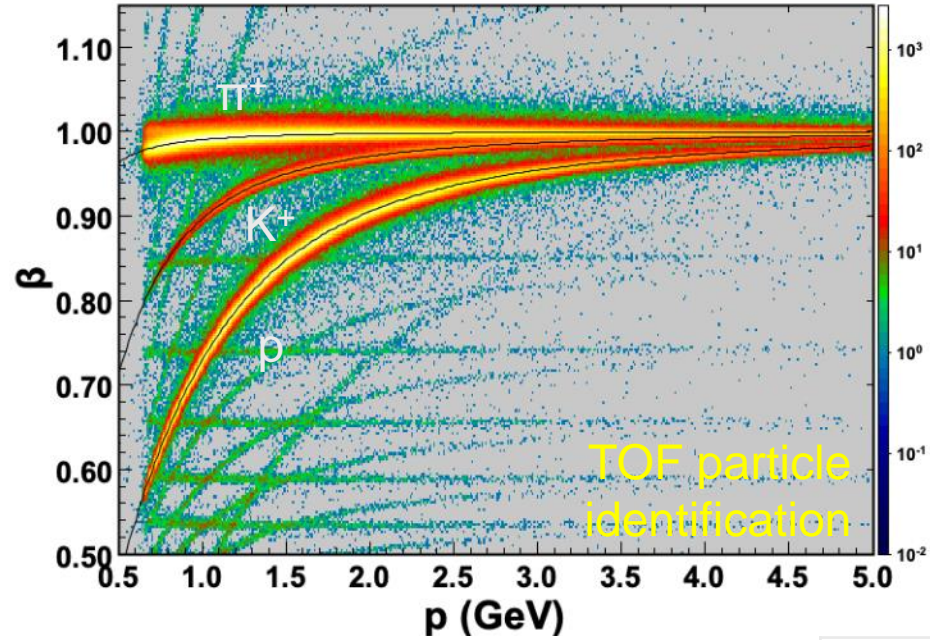
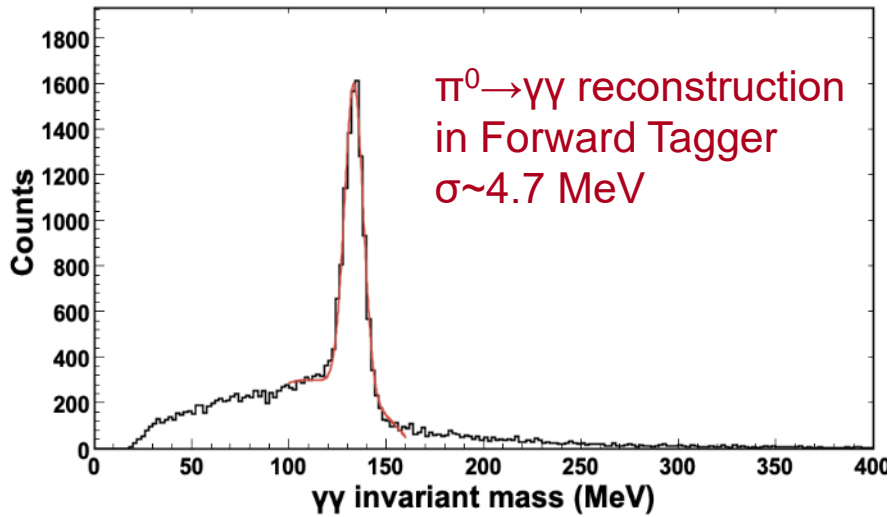
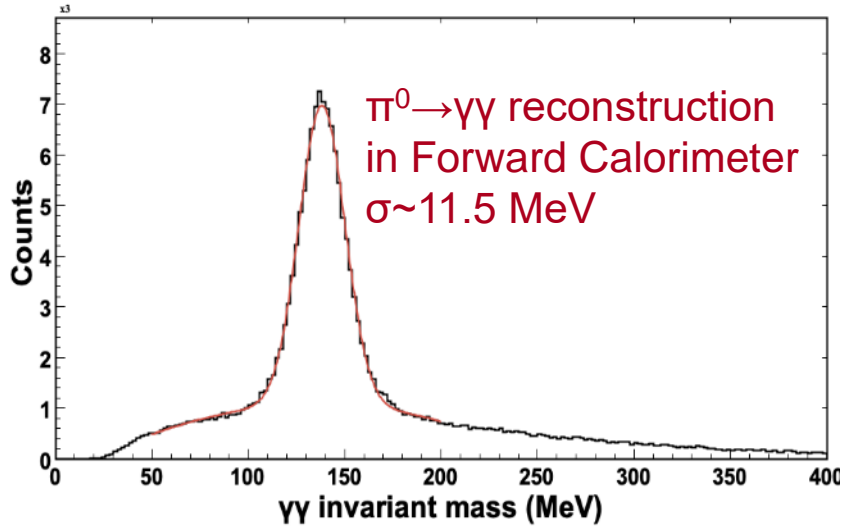
# Side View Photograph of CLAS12 Spectrometer



# CLAS12 Subsystems During Installation



# Event Reconstruction in CLAS12

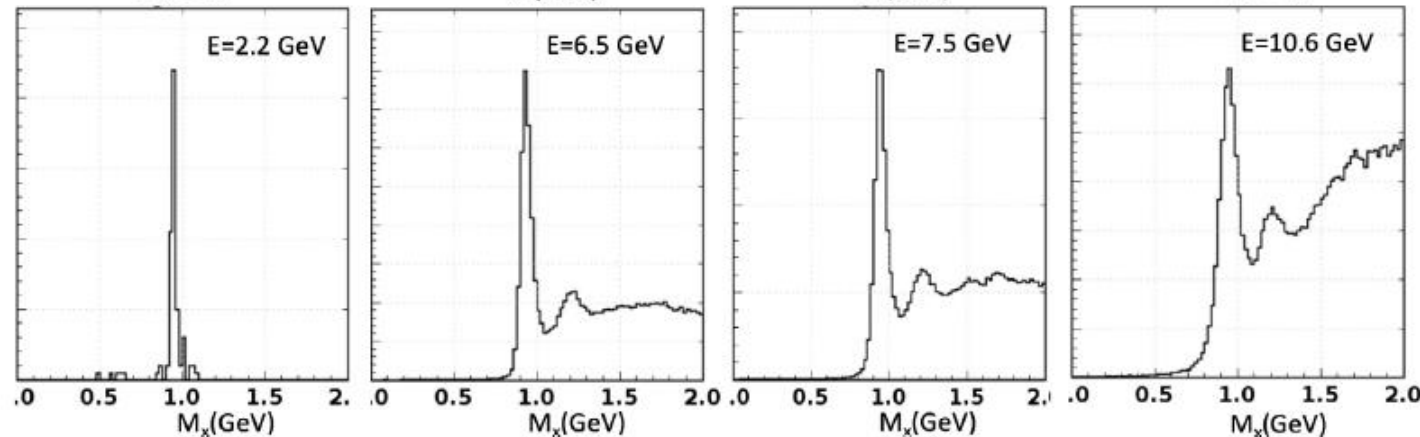
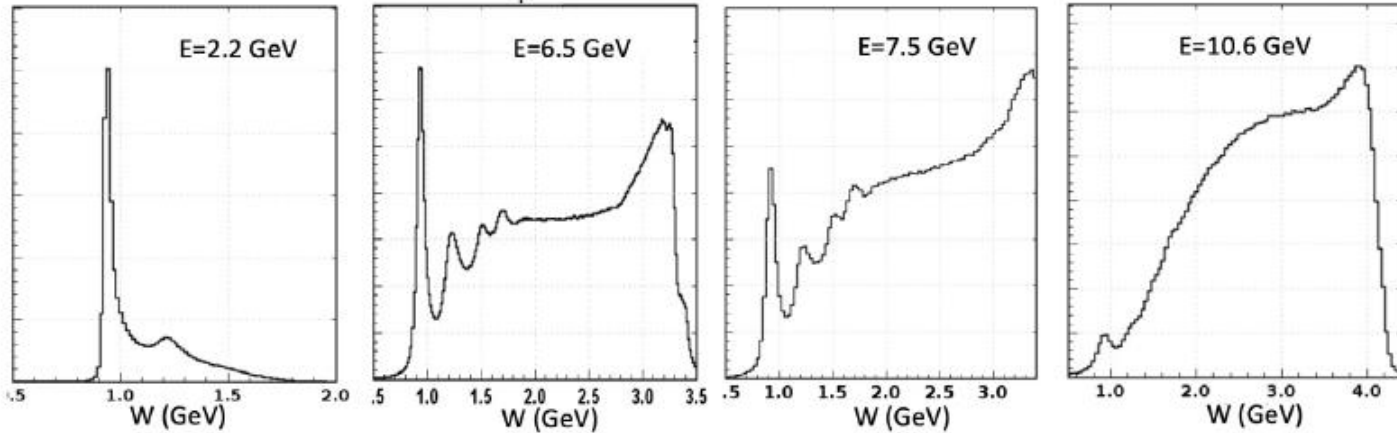


	Forward	Central
Angular coverage	5° – 35°	35° – 135°
Momentum resolution	dp/p < 1%	dp/p < 5%
θ resolution	1 mrad	5 – 10 mrad
φ resolution	1 mrad/sinθ	5 mrad/sinθ



# Exclusive and Inclusive Processes

Inclusive  $ep \rightarrow e'X$  spectra as sum over all exclusive channels



Examples of mass spectra  
at four different beam energies

Elastic peak and first 3  $N^*$  states,  
 $\Delta(1232)$ ,  $N(1520)$ , and  $N(1680)$ , visible

Examples of missing mass spectra  
in  $ep \rightarrow e'\pi^+X$  at the same energies

Sharp peak of undetected neutron,  
peak of  $\Delta^0(1232)$ , and indications of  
higher excitations visible

# CLAS & CLAS12 Nucleon Resonance Studies

*Not all bumps are resonances, not every resonance generates a bump in all observables*

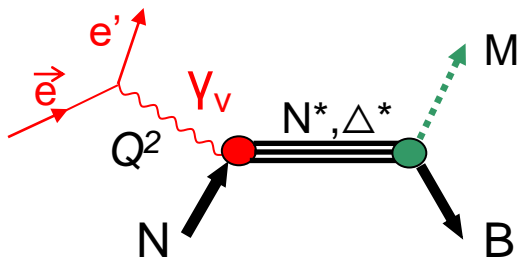


# Overview of Extractions of Electrocouplings

Reaction Channel	$N^*, \Delta^*$ States	$Q^2$ ranges of $\gamma_V p N^*$ Electrocouplings ( $\text{GeV}^2$ )
$\pi^0 p, \pi^+ n$	$\Delta(1232) 3/2^+$	0.16 – 6.0
	$N(1440) 1/2^+, N(1520) 3/2^-, N(1535) 1/2^-$	0.30 – 4.16
$\pi^+ n$	$N(1675) 5/2, N(1680) 5/2^+, N(1710) 1/2^+$	1.6 – 4.5
$\eta p$	$N(1535) 1/2^-$	0.2 – 2.9
$\pi^+ \pi^- p$	$N(1440) 1/2^+, N(1520) 3/2^-$	0.25 – 1.5
	$\Delta(1620) 1/2^-, N(1650) 1/2^-, N(1680) 5/2^+, \Delta(1700) 3/2^-, N(1720) 3/2^+, N'(1720) 3/2^+$	0.5 – 1.5

Analysis codes employed for extractions:

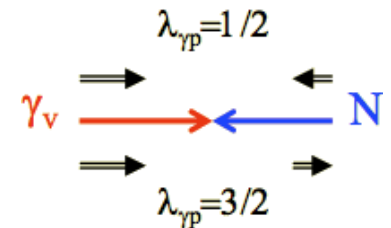
- Unitary Isobar Model (UIM)
- Fixed-t dispersion relations (DR)
- Data-driven reaction model for  $\pi^+ \pi^- N$  (JM09, JM16, JM19)
  - [I.G. Aznauryan et al., Int. J. Mod. Phys. E 22, 1330015 (2013)]
  - [V. Mokeev, Few-Body Syst. 57, 909 (2016)]
  - [V. Mokeev and D. Carman, Few-Body Syst. 63, 59 (2022)]



Helicity amplitudes:

$A_{1/2}, A_{3/2}$ : *transverse*

$S_{1/2}$ : *longitudinal*



# Amplitude Extraction using Breit-Wigner Parametrization

Cross sections of resonance  $r$  of mass  $M_r$  and width  $\Gamma_{tot}(M_r) = \Gamma_r$  and spin  $J_r$ :

$$\sigma_{L,T}^r(W, Q^2) = \frac{\pi}{q_\gamma^2} \sum_{N^*, \Delta^*} (2J_r + 1) \frac{M_r^2 \Gamma_{tot}(W) \Gamma_\gamma^{L,T}(M_r)}{(M_r^2 - W^2)^2 + M_r^2 \Gamma_{tot}^2(W)} \frac{q_\gamma}{K}$$

with following kinematic definitions:

$$q_\gamma = \sqrt{Q^2 + E_\gamma^2}, \quad E_\gamma = \frac{W^2 - Q^2 - M_N^2}{2W}, \quad K = \frac{W^2 - M_N^2}{2W}$$

Electromagnetic decay widths at the resonance point  $W = M_r$  given by:

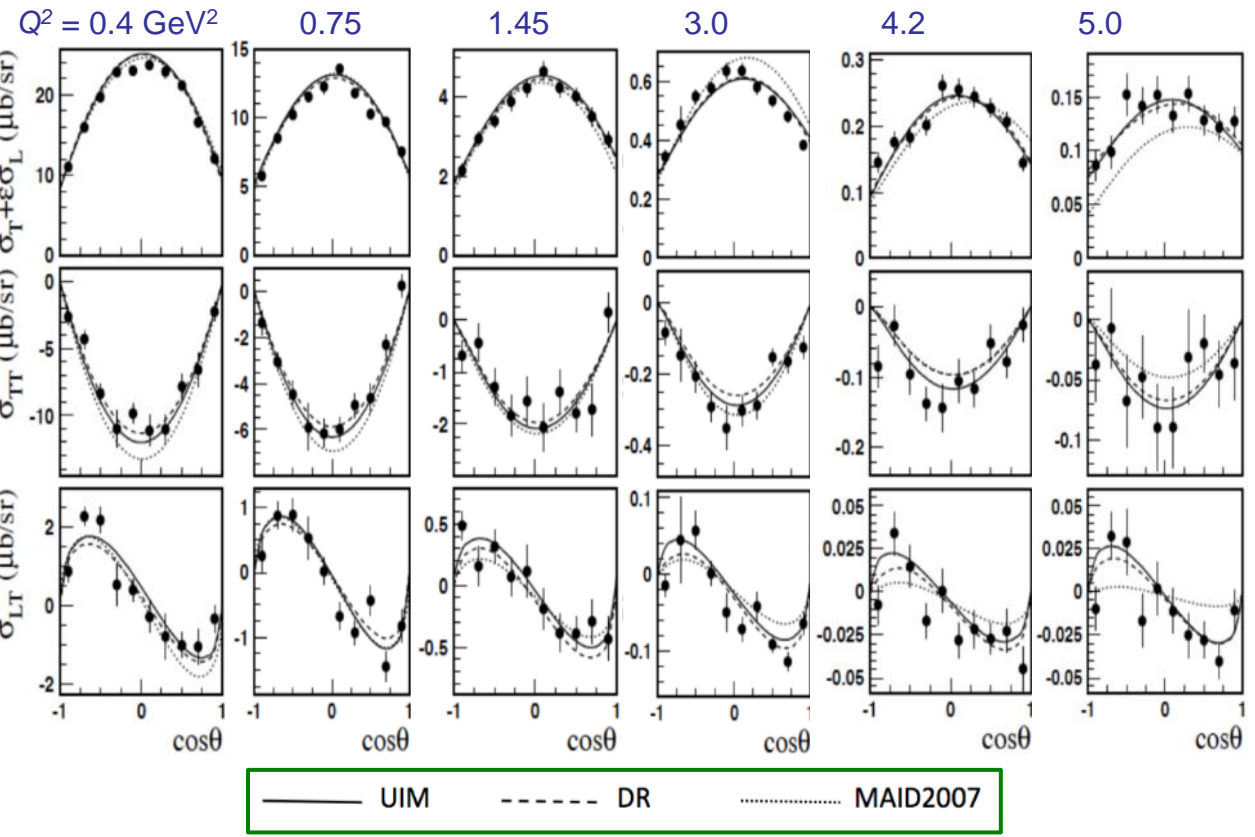
$$\Gamma_\gamma^L(M_r, Q^2) = 2 \frac{q_{\gamma,r}^2(Q^2)}{\pi} \frac{2M_N}{(2J_r + 1)M_r} |S_{1/2}(Q^2)|^2$$

$$\Gamma_\gamma^T(M_r, Q^2) = \frac{q_{\gamma,r}^2(Q^2)}{\pi} \frac{2M_N}{(2J_r + 1)M_r} (|A_{1/2}(Q^2)|^2 + |A_{3/2}(Q^2)|^2)$$

# CLAS N\* Electrocouplings – First Resonance Region

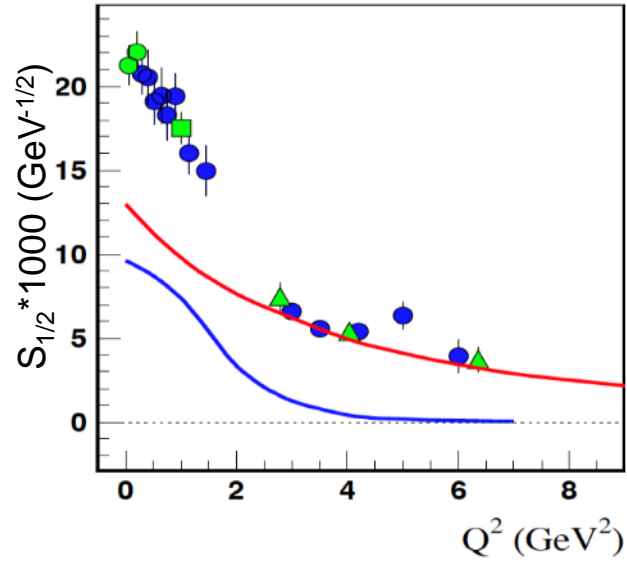
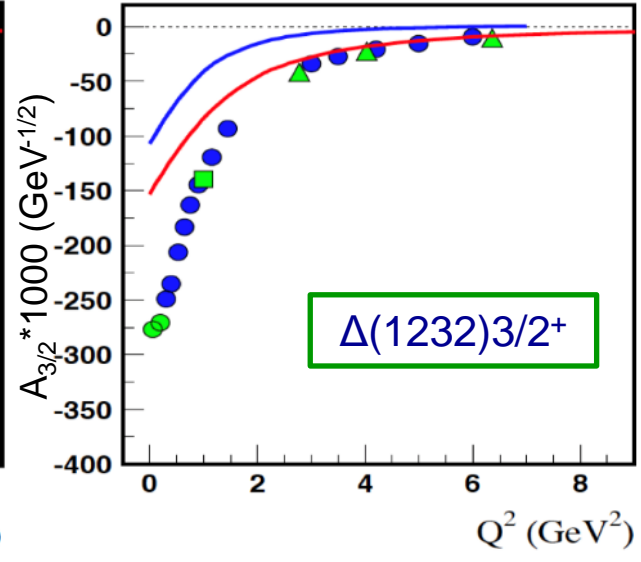
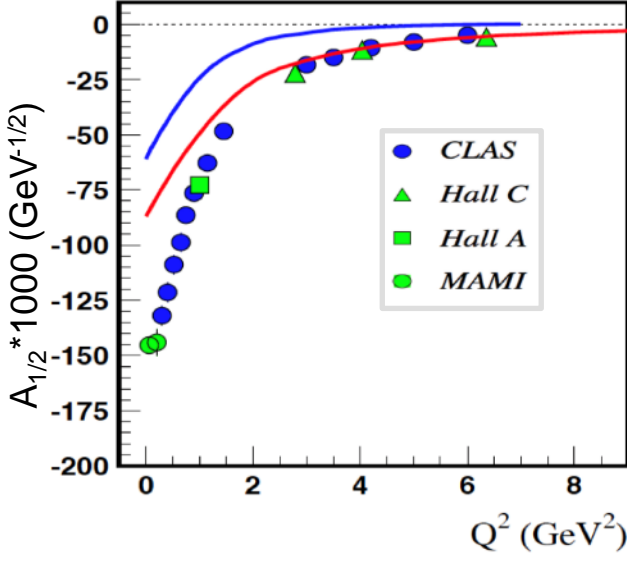
$$\gamma^* p \rightarrow \pi^0 p$$

W = 1.232 GeV



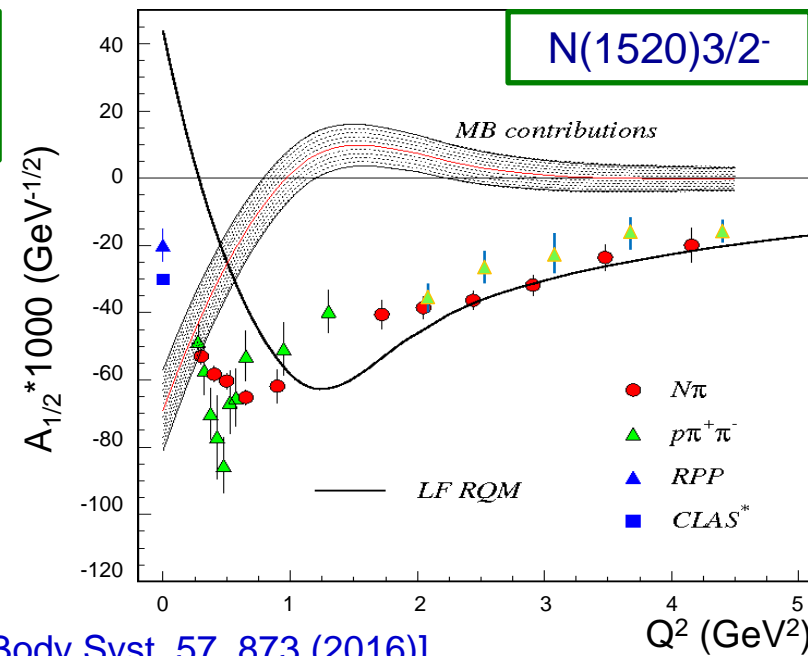
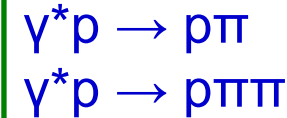
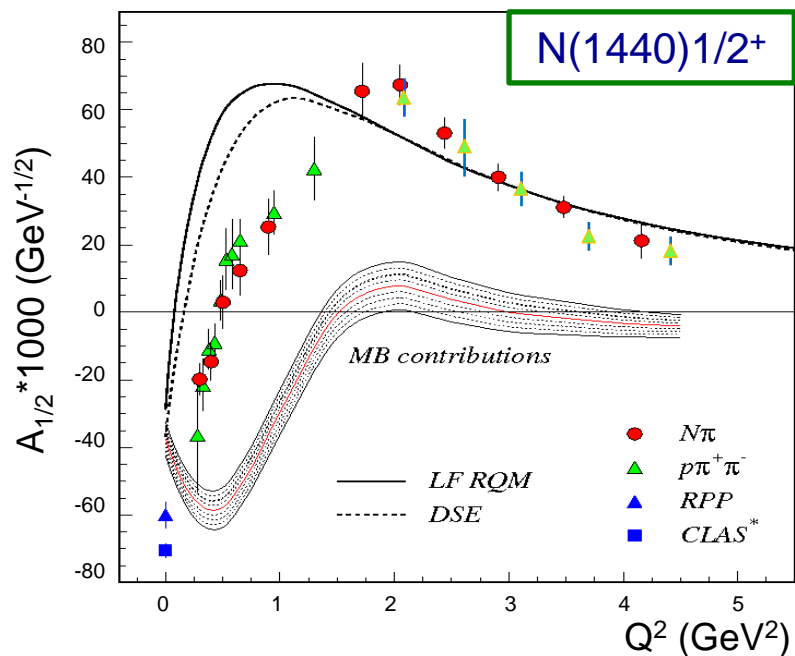
Good agreement between UIM and DR approaches

[I.G. Aznauryan et al., Phys. Rev. C 80, 055203 (2009)]



QCD calculations compatible with data where meson cloud does not contaminate evolution  $Q^2 \leq 2 \text{ GeV}^2$

# CLAS N\* Electrocouplings – Second Resonance Region



[V.D. Burkert, Few-Body Syst. 57, 873 (2016)]

## Electrocouplings reveal different interplay between meson-baryon cloud and quark core

Good agreement of the extracted N\* electrocouplings from Nπ and Nππ:

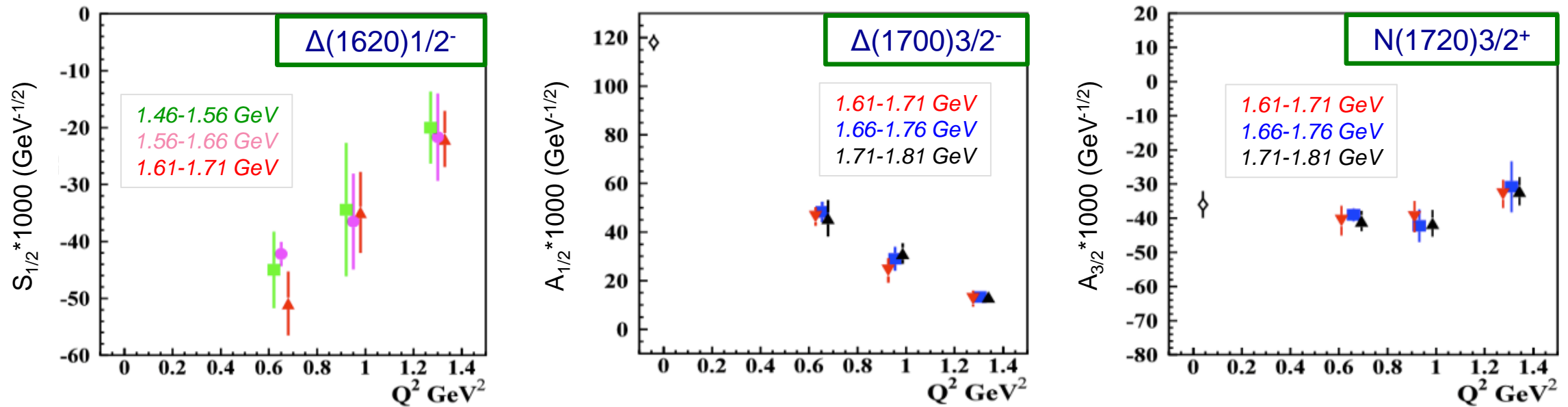
- Compelling evidence for reliability of results
- Different channels have very different mechanisms for non-resonant background

Need for data on the electrocouplings over broad range of  $Q^2$

# CLAS N\* Electrocouplings – Third Resonance Region

$$\gamma^* p \rightarrow p \pi \pi$$

Most high-lying N\* states decay mainly to N $\pi\pi$  with much smaller strength to N $\pi$



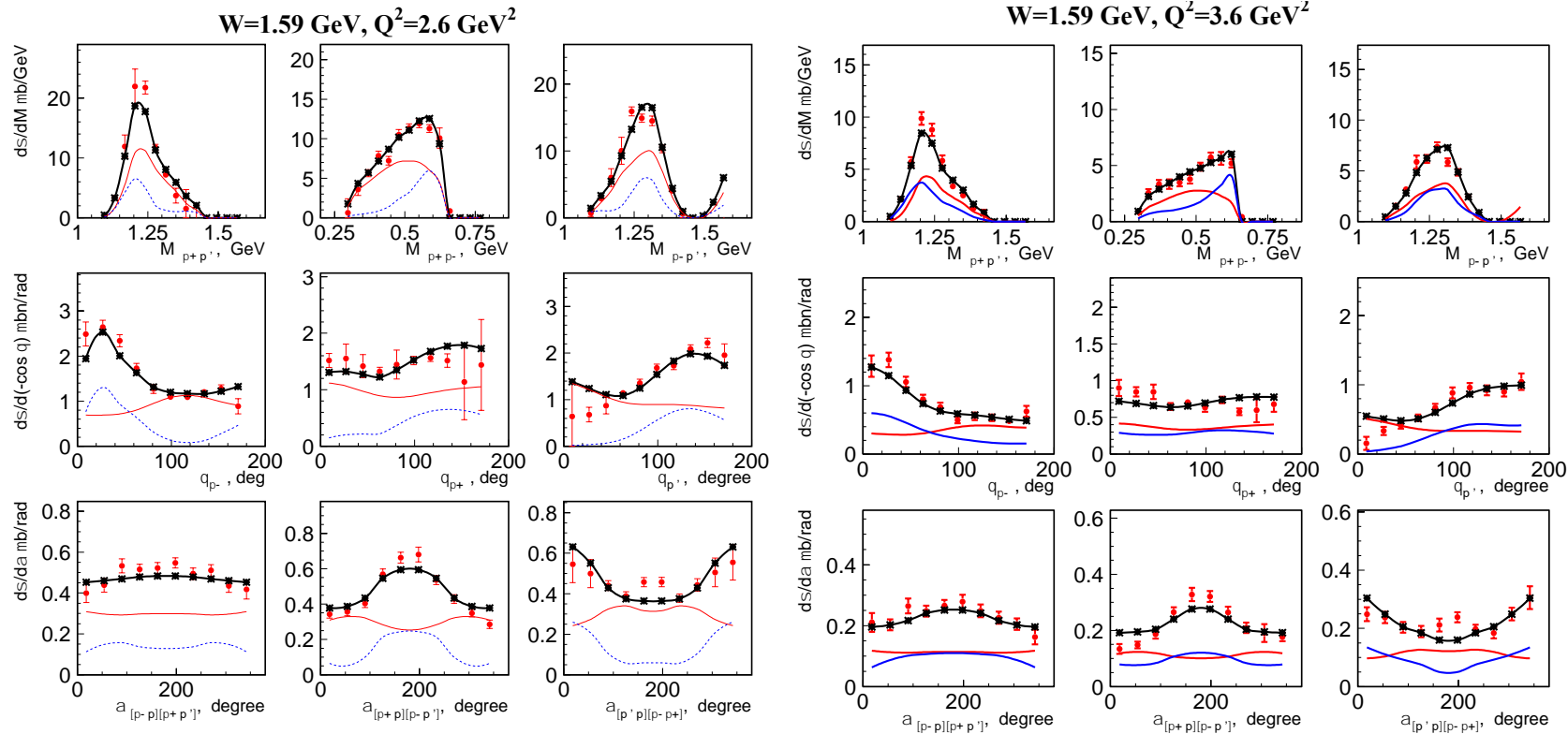
[Moakev, Aznauryan, IJMP 26, 1460080 (2014); Moakev et al., PRC 93, 025206 (2016); Carman, Joo, Moakev, FBS 61, 29 (2020)]

N $\pi\pi$  channel gave first electrocoupling results on higher-lying states up to 1.8 GeV

# Description of $\rho\pi^+\pi^-$ Data by a Reaction Model

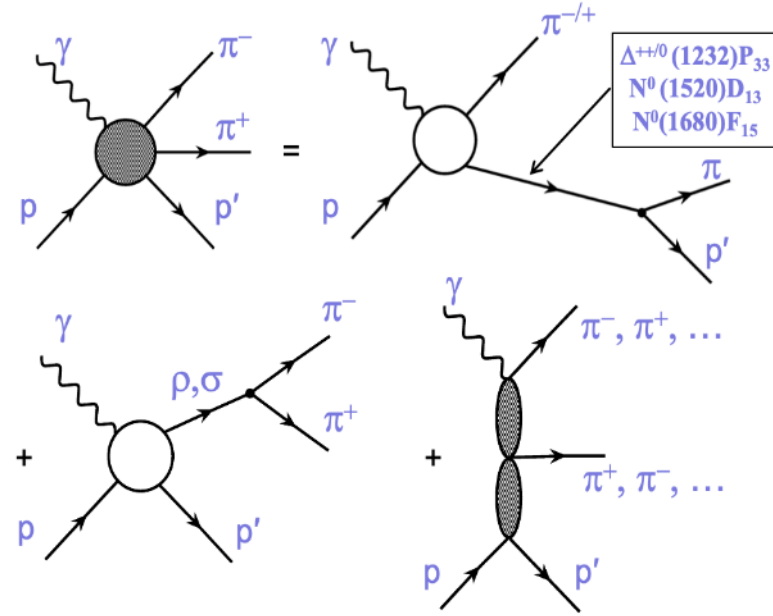
5-fold differential cross section  $\frac{d^5\sigma}{d^5\tau}$ , where the denominator consists of differentials for the five variables that define the final state kinematics

JLab-Moscow Reaction Model (JM)



— Full — Resonances — Background

[V.I. Moiseev et al., Phys. Rev. C 86, 035203 (2012)]

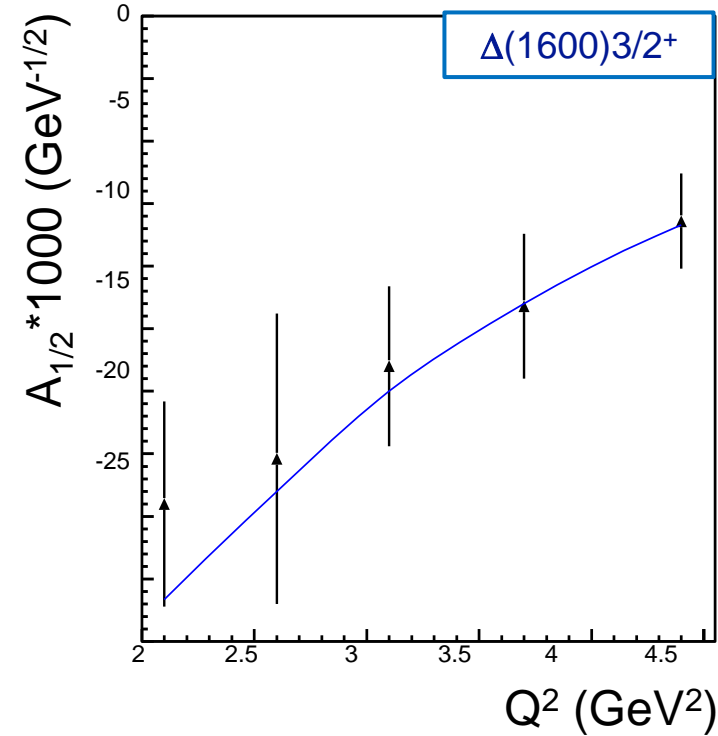
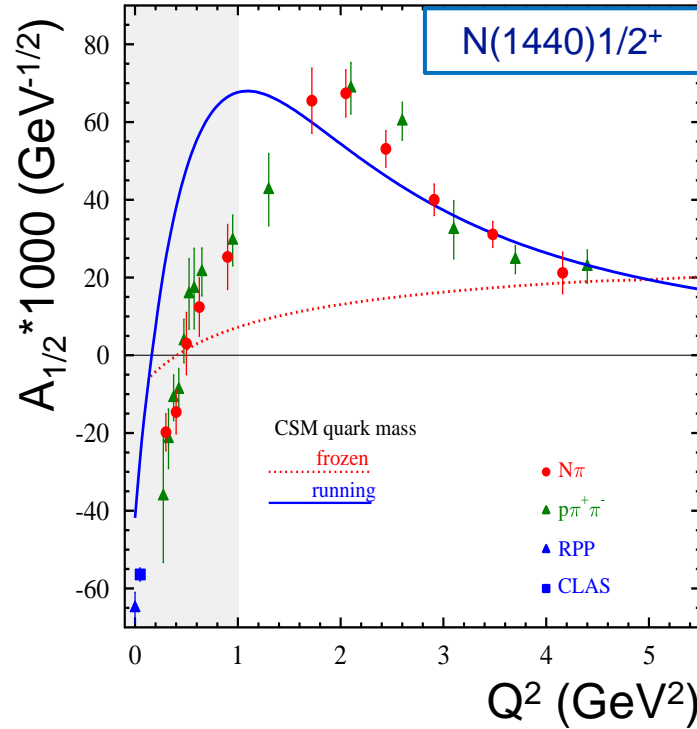
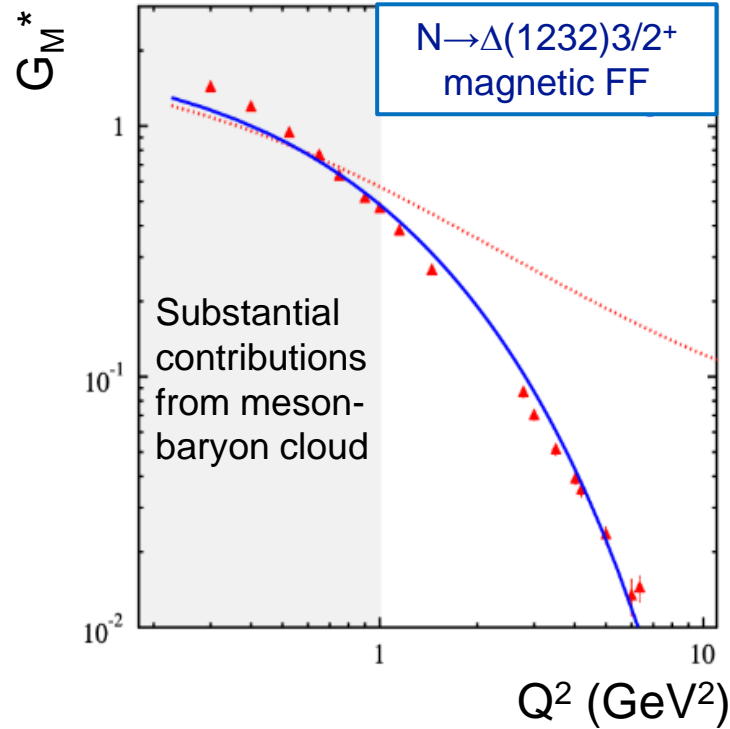


Model provides reasonable description of data for extraction of resonance electrocouplings



# Nucleon Resonance Electroexcitation Amplitudes

[D.S. Carman, R.W. Gothe, V.I. Mokeev, and C.D. Roberts, Particles 6, 416 (2023)]



Satisfactory description for  $\Delta(1232)3/2^+$ ,  $N(1440)1/2^+$ ,  $\Delta(1600)3/2^+$

Continuum QCD predictions:  
[Y. Lu et al., Phys. Rev. D 100, 034001 (2019)]

- Important evidence for the **different internal structures** of nucleon resonances
- Insight into **strong interaction dynamics underlying Emergence of Hadron Mass**
- Data compared to **Continuum Schwinger Method** with momentum-dependent quark masses

# Concluding Remarks on the CLAS N\* Program

## Study of N\* states is one of the key foundations of the CLAS physics program

- CLAS has provided a huge amount of data up to  $Q^2 \sim 5 \text{ GeV}^2$
- Electrocouplings of most N\* states  $< 1.8 \text{ GeV}$  have been extracted for the first time

Probed N\* structure is very complex and relates to fundamental QCD phenomena

## CLAS12 will extend these studies to $0.05 < Q^2 < 12 \text{ GeV}^2$ and $W < 2.4 \text{ GeV}$

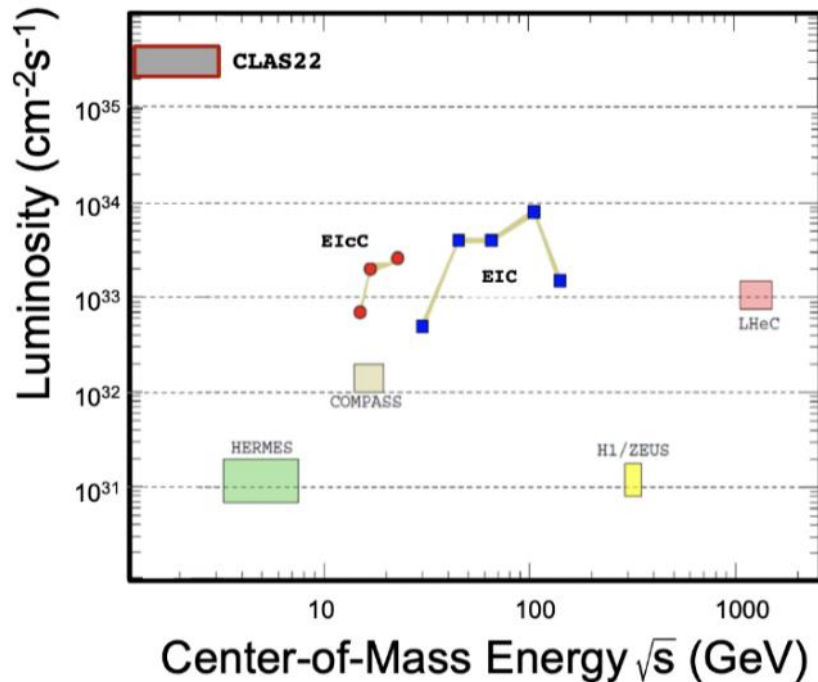
- Exclusive electroproduction of  $N\pi$ ,  $N\eta$ ,  $N\pi\pi$ ,  $KY$  reactions from unpolarized proton target with longitudinally polarized electron beam
- Data will provide access to higher-lying N\* states
- Goal is the understanding of active degrees of freedom that account for N\* structure vs. distance scale

RG-A	Spr. 18 126 mC	10.2 GeV, 10.6 GeV  50% of total
	Fall 18 99 mC	
	Spr. 19 58 mC	
RG-K	Fall 18 28 mC	6.3 GeV, 7.4 GeV  10% of total

Running since last week

# Opportunities with CEBAF at 22 GeV

Electrocouplings for  $\pi N$ ,  $KY$ , and  $\pi^+\pi^-p$  reaction with 22 GeV beam can be determined up to  $Q^2 \sim 30 \text{ GeV}^2$  for  $\mathcal{L} \sim 2 - 5 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$



A. Accardi et al., e-print:2306.09360 [nucl-ex]

The **high luminosity frontier** provides **JLab** a special advantage in comparison with EIC or ElcC.

It offers a unique opportunity to study Nature's simplest 3-body bound state and its electrocouplings with its resonances in a **large domain of momentum transfer**.

CLAS22 will map out the working of QCD from its **non-perturbative** behavior at low  $Q^2$  to its asymptotic regime where perturbative QCD can provide predictions, charting out the pattern of **dynamical chiral symmetry breaking**.