



UNIVERSITÀ  
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DI BRESCIA



# Measurement of anti-hydrogen acceleration in Earth's gravitational field

Marta Urioni on behalf of the ALPHA collaboration



Bormio Conference

**60<sup>th</sup> International Winter Meeting  
on Nuclear Physics**

**22 - 26 January 2024  
Bormio, Italy**

# Antimatter and gravity

- The theory of **General Relativity** has passed a number of stringent experimental tests ([Will, C.M. The confrontation between general relativity and experiment. Living Rev. Relativ. 2014, 17, 1–117](#))
- One of the principles of GR is the **Weak Equivalence Principle (WEP)**: all objects fall at the same rate, regardless of their internal composition or structure.

WEP is **expected to hold for antimatter**

A **deviation from WEP** could signal:

- incompleteness in our interpretation of gravity
- or the presence of new interactions (fifth forces), vector and scalar mediated forces that couple to some combination of baryon and lepton number ([arXiv:0808.3929](#))

# Antimatter and gravity

## Previous “free fall” experimental attempts:

- 1967: Fairbank and Witteborn tried to use positrons ([Phys. Rev. Lett. 19, 1049 \(1967\)](#))
- 1989: PS-200 experiment at CERN tried to use (4 K) antiprotons ([Nucl. Instr. and Meth. B, 485 \(1989\)](#))

Failed: charged particles are susceptible to electromagnetic fields that are stronger than gravity

**ALPHA** as well as **AEGIS** and **Gbar** study gravity on **anti-hydrogen** because of its neutrality

- How much of antiproton is antimatter? ([arXiv:1207.7358](#))

most of the inertial mass of an (anti)proton comes from its binding energy. Quark mass is ~1%

# Antihydrogen Laser PHysics Apparatus



**Aarhus**  
University,  
Denmark



**University of Brescia,**  
Italy



**University of British**  
Columbia, Canada



**University of California**  
Berkeley, USA



**University of Calgary,**  
Canada



**THE UNIVERSITY**  
of LIVERPOOL  
**University of Liverpool,**  
UK



**University of Manchester, UK**



**NRCN - Nuclear Res.**  
Center Negev, Israel



**Purdue University,**  
USA



**Federal University of**  
Rio de Janeiro,  
Brazil



**INFN (Pavia, Pisa)**  
Italy



**Stockholm**  
University,  
Sweden



**Simon Fraser University,**  
Canada



**TRIUMF**

**TRIUMF,**  
Canada



**University of Wales**  
Swansea, UK



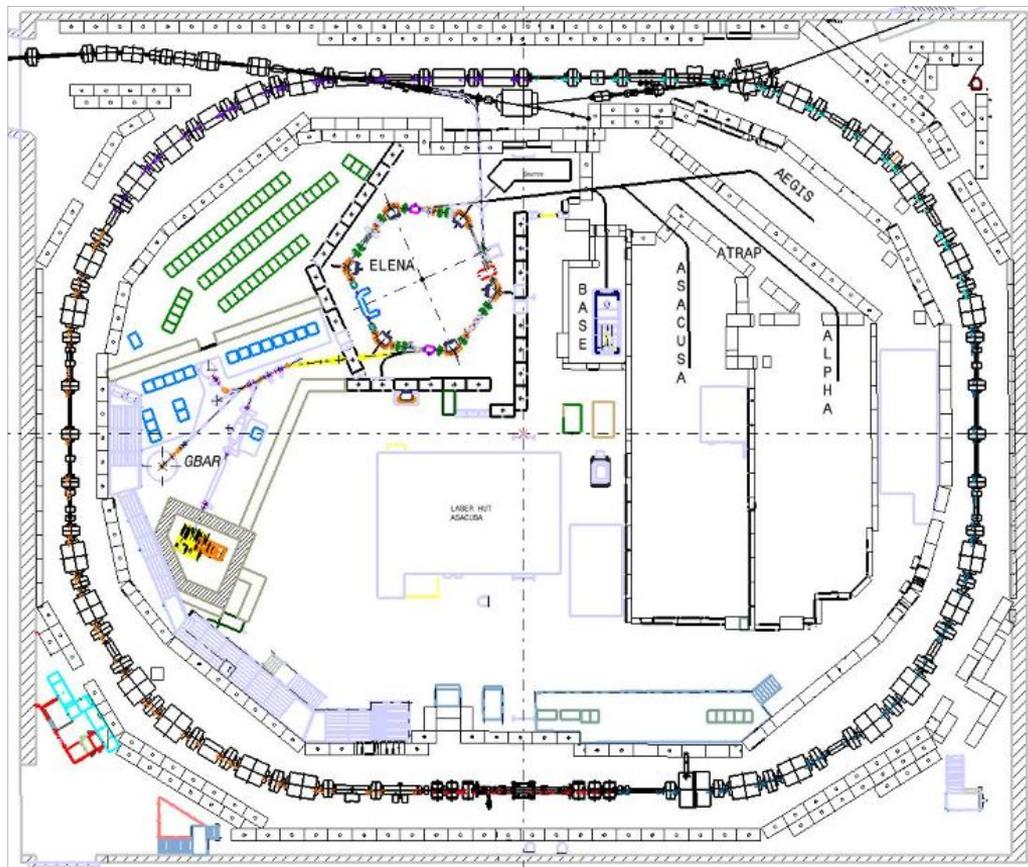
**The Cockcroft Institute**  
of Accelerator Science and Technology

**Cockcroft Institute, UK**



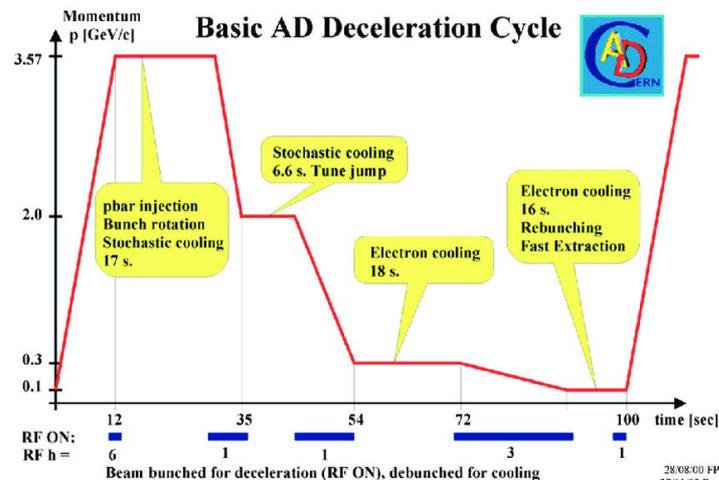
**York University,**  
Canada

# The antimatter Factory



**ALPHA** (*Antihydrogen Laser PHysics Apparatus*) located in the antimatter factory where antiprotons produced in a proton beam-target collision are decelerated:

- The **AD**: pbar to an energy of **5.3 MeV**
- The **ELENA** ring  $10^7$  pbar at **100 keV**

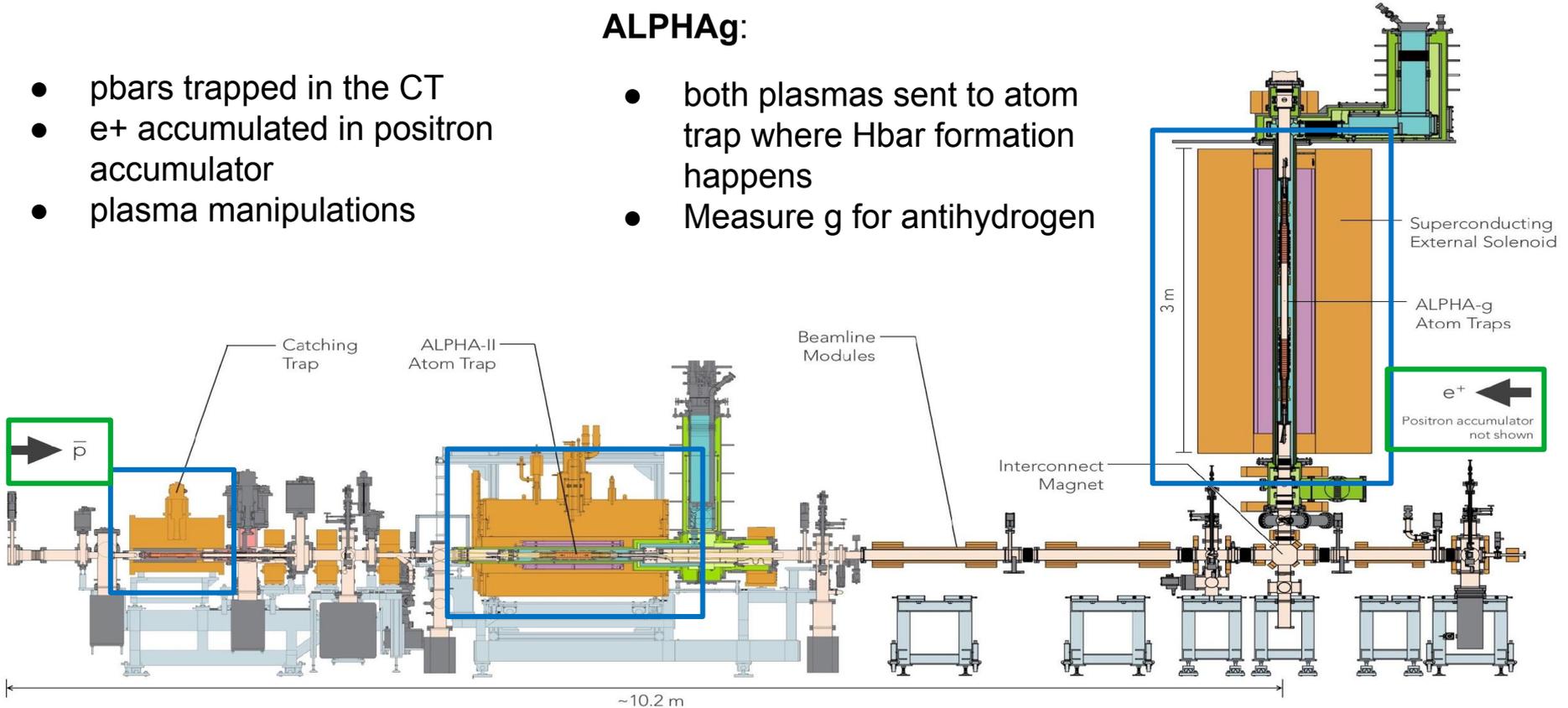


# ALPHA Schematic

## ALPHA-g:

- pbars trapped in the CT
- e+ accumulated in positron accumulator
- plasma manipulations

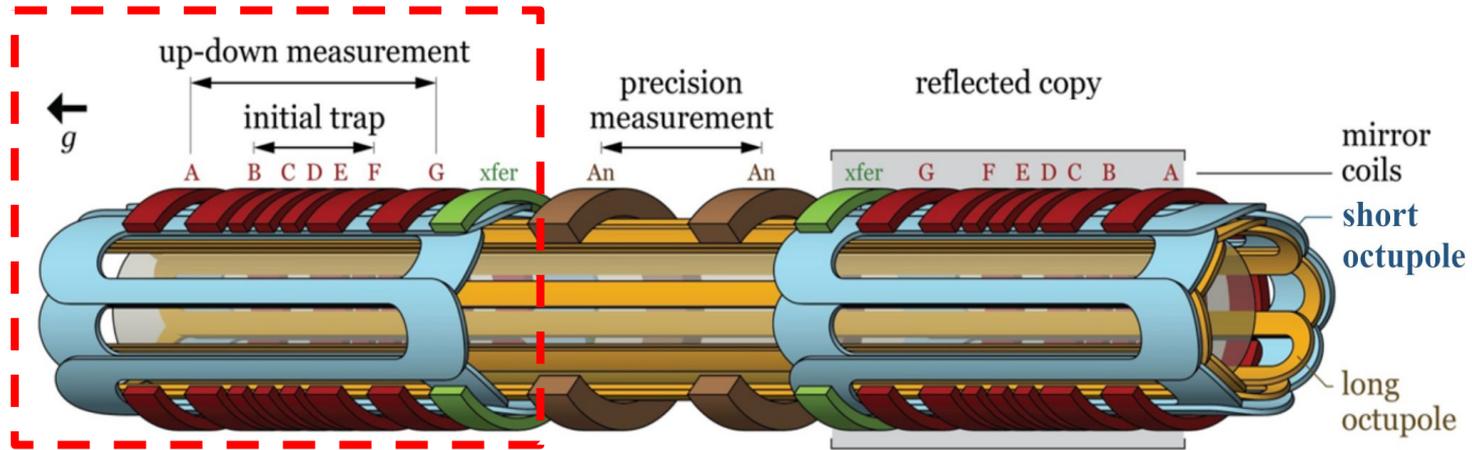
- both plasmas sent to atom trap where Hbar formation happens
- Measure g for antihydrogen



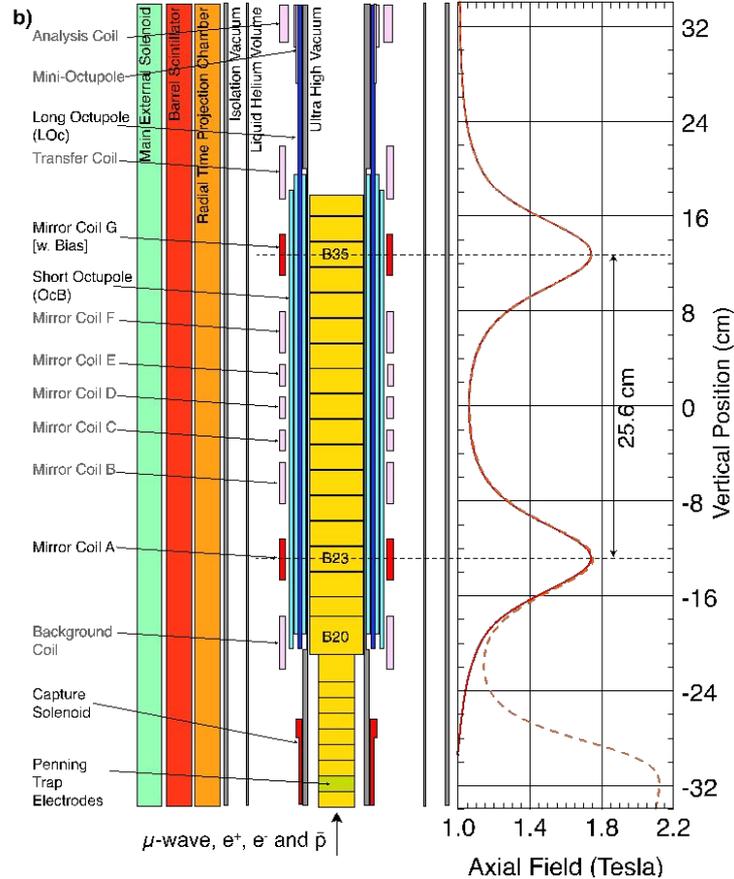
# ALPHA<sub>g</sub> magnets

In ALPHA<sub>g</sub>:

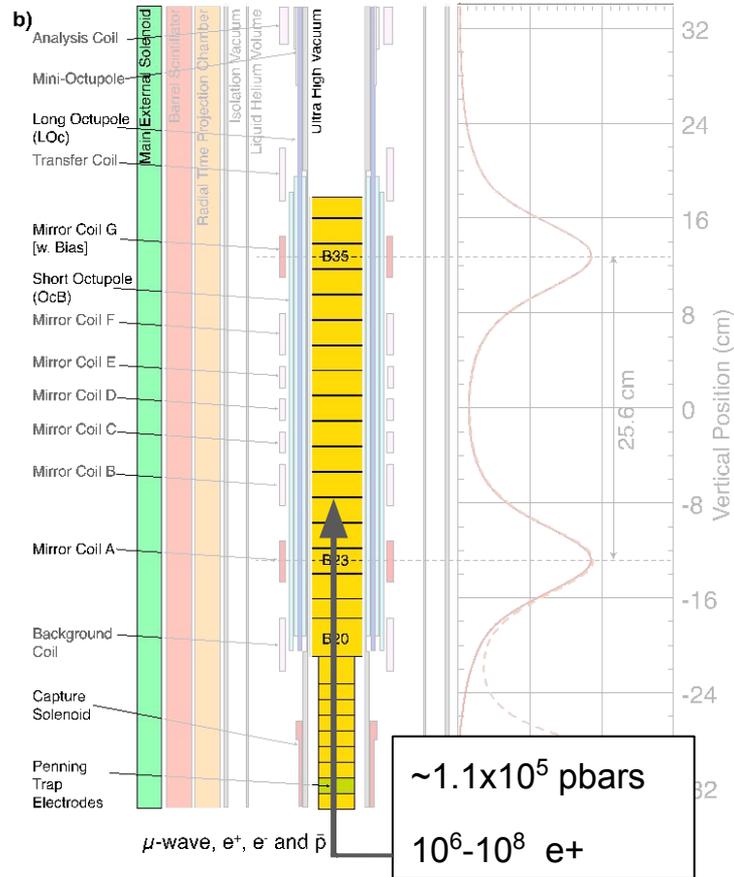
- Three trapping regions
- **Long+short octupoles:** minimise field errors due to fabrication tolerance in central (“precision”) region
- **Precision region:** designed to perform a 1% precision  $g$  measurement
- But in the 2022 measurement just the **long octupole** and the **bottom trap** were used



# Hbar production and detection in the bottom trap

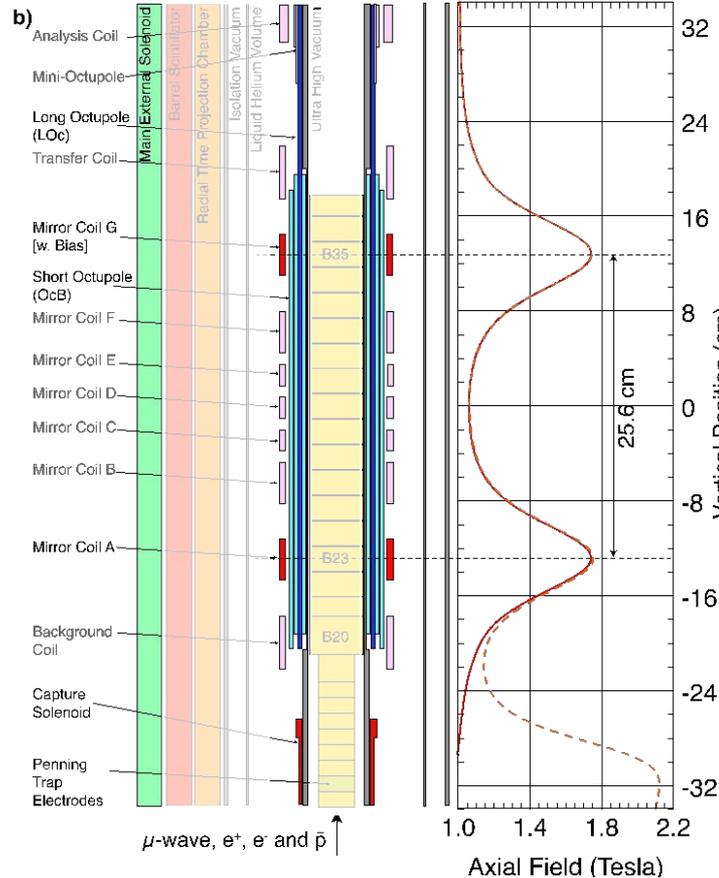


# Hbar production and detection in the bottom trap

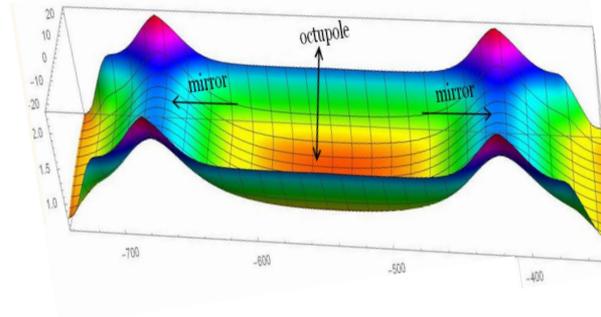


- antihydrogen is formed by gently **mixing** the clouds of **positrons** and **antiprotons**

# Hbar production and detection in the bottom trap



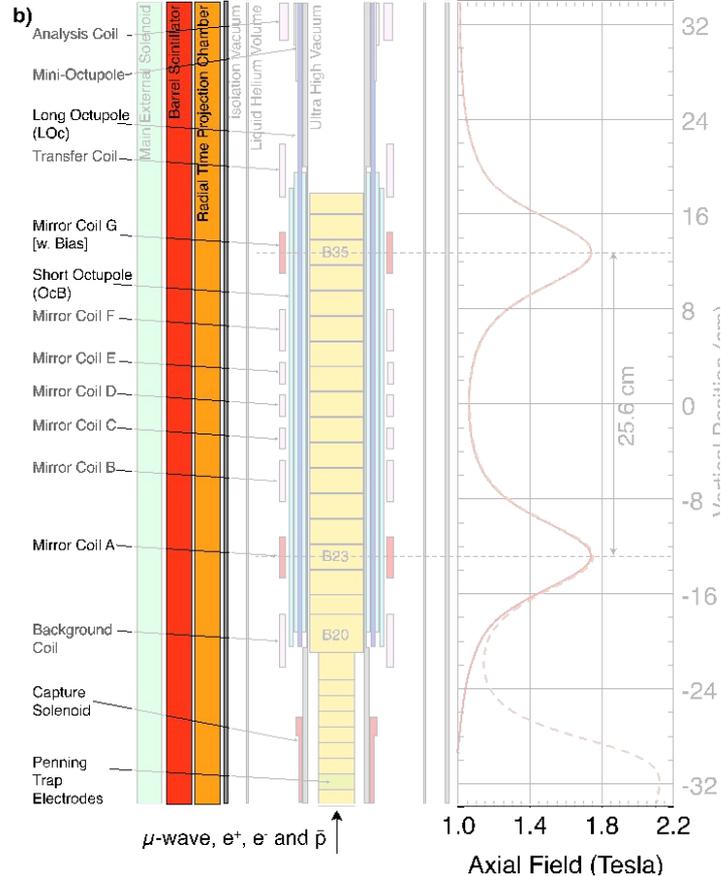
- antihydrogen is formed by gently **mixing** the clouds of **positrons** and **antiprotons**
- Hbar is then **trapped in the ALPHAg atom trap**



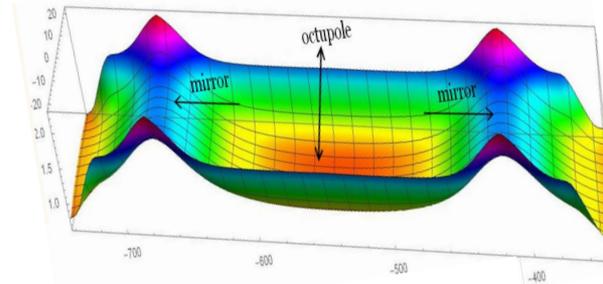
confinement  
potential  $U = -\mu_{\bar{H}} \cdot B$

$$\mu_{\bar{H}}^{\parallel} = \pm \mu_B$$

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confinement potential  $U = -\mu_{\bar{H}} \cdot B$

$$\mu_{\bar{H}}^{\parallel} = \pm \mu_B$$

- Hbar is **released** and annihilation vertex is reconstructed via:
  - **rTPC**
  - **Scintillators barrel veto**

# ALPHA<sub>g</sub> measurement procedure

- **Magnetic fields and gravitational field** act on Hbars:  $U = -\boldsymbol{\mu}_H \cdot \mathbf{B} + m_H gh$
- Goal: measure the **gravitational acceleration of Hbar**
- Assumptions:  $\mu_{\bar{H}} = \mu_H$  ,  $m_{\bar{H}} = m_H$  (*Phys. Rev. Lett.* 59, 26 – 6 July 1987), (*Nature* 475, 484–488 (2011))

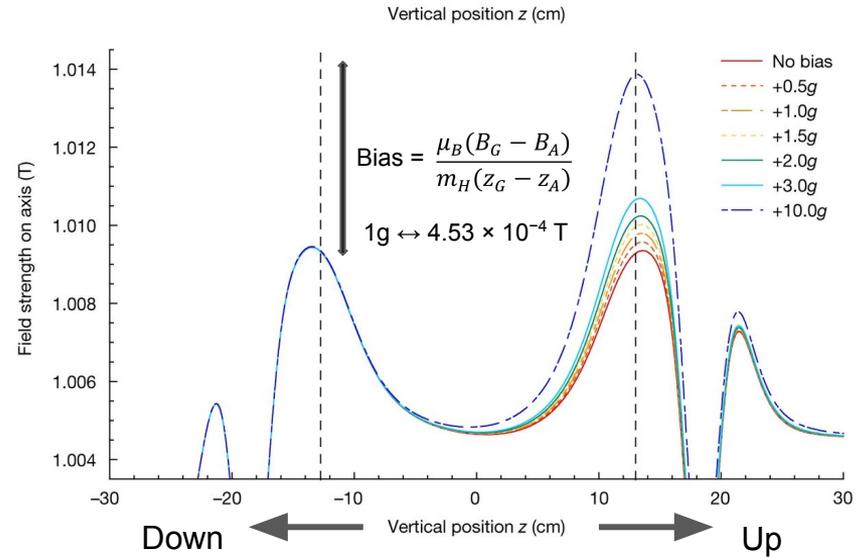
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## General concept:

- **measure total potential via the asymmetry A** between number of up annihilations and down annihilations when releasing vertically the Hbars

$$A_i^{raw} = (N_{u,i} - N_{d,i}) / S_i$$



# ALPHA<sub>g</sub> measurement procedure

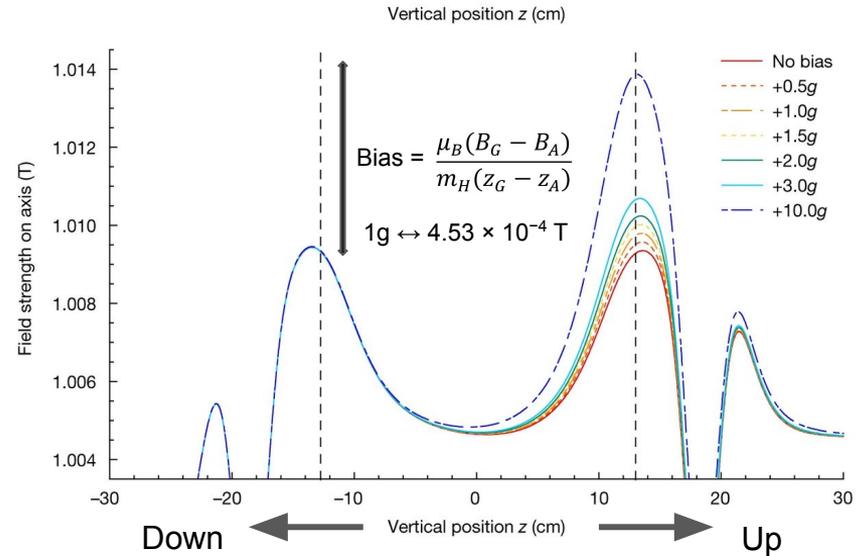
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  - via ancillary B field measurements
- This is **repeated at different magnetic field configurations** (Biases)



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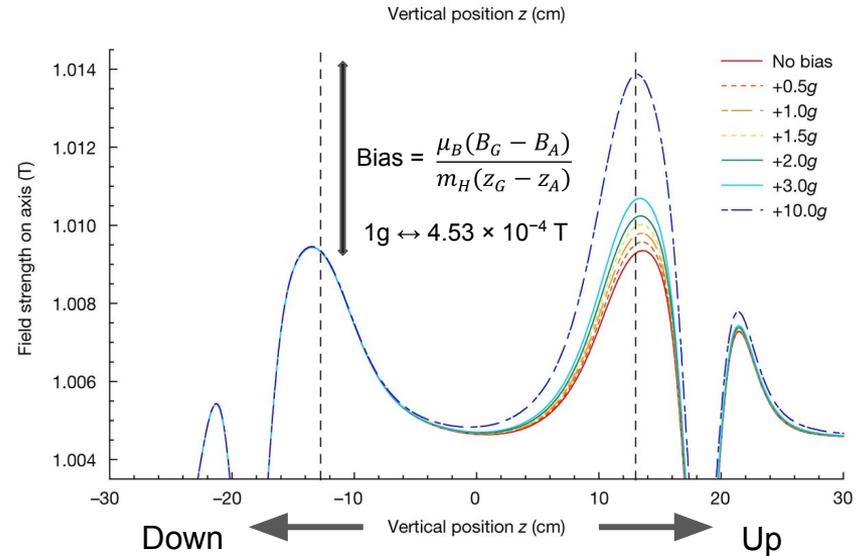
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## General concept:

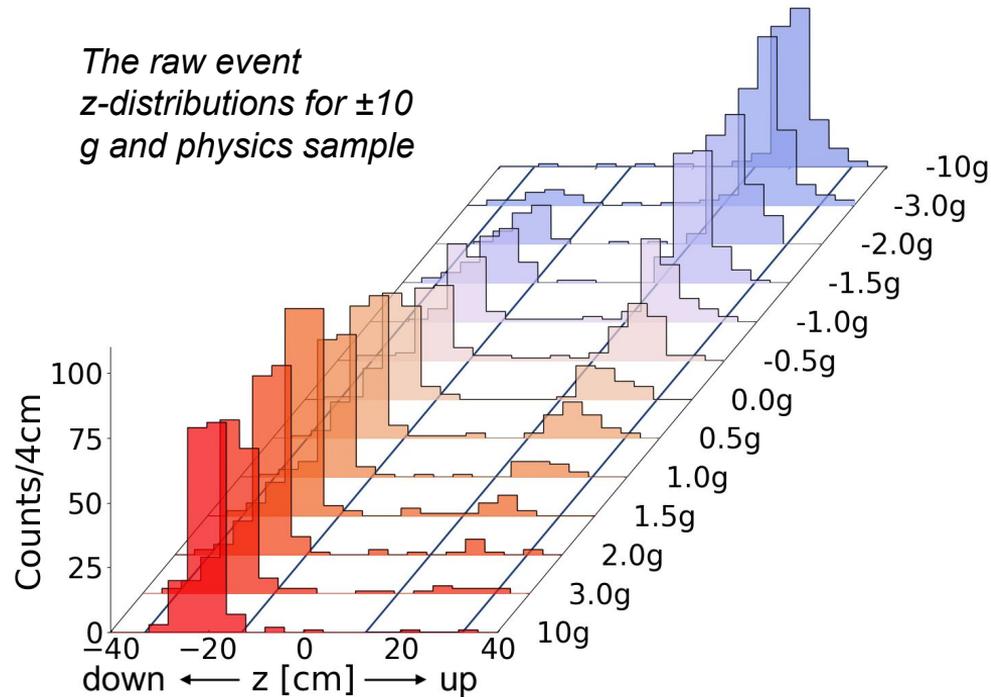
- **measure total potential** via the **asymmetry A** between number of up annihilations and down annihilations when releasing vertically the Hbars

$$A_i^{raw} = (N_{u,i} - N_{d,i}) / S_i$$

- **measure magnetic potential:**
  - via ancillary B field measurements
- This is **repeated** at **different** magnetic field configurations (Biases)
- subtraction of the effect of magnetic potential in order to **obtain the gravitational one**
  - in practice relation between potentials and asymmetry is obtained **from simulation**



# Analysed data



- **$\pm 10$  g calibration sample**, collected with a fast MAGB ramp-down of the upper/lower gate
- **Background enriched calibration sample** (with no antip in the experiment)
- **$\pm 3$  g,  $\pm 2$  g,  $\pm 1.5$  g,  $\pm 1$  g,  $\pm 0.5$  g, 0 g: physics sample**, with fast (20 s) ramp of the MAGB.

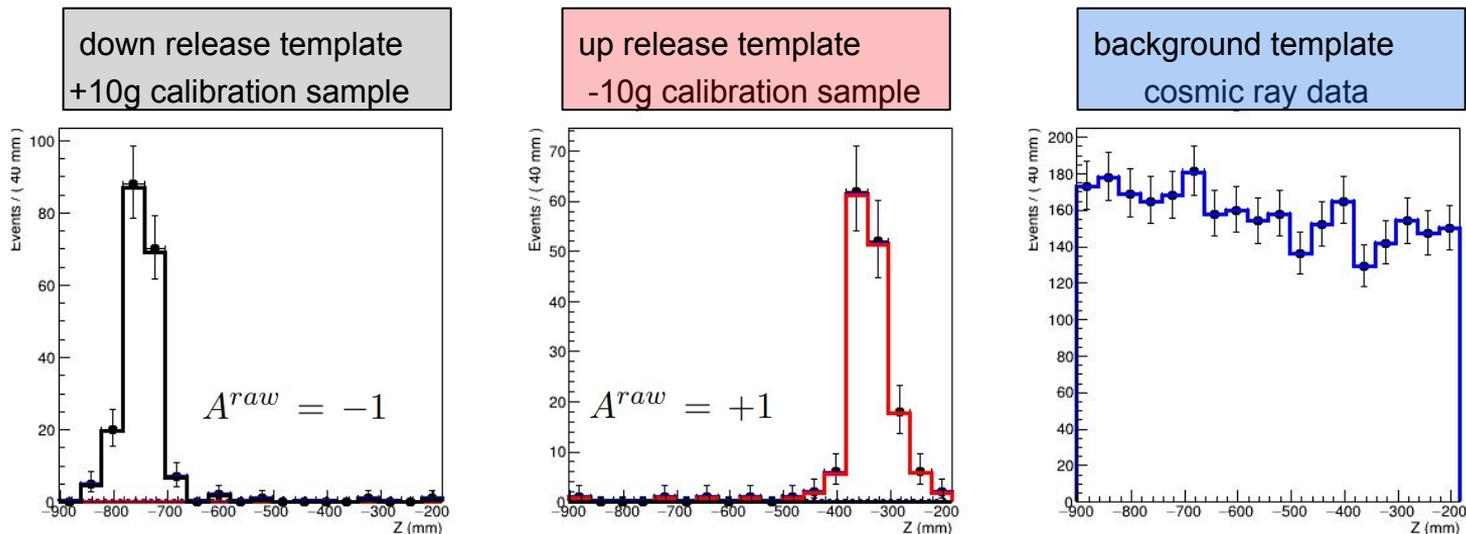
- *Calibration samples and LoC ramp-down*: to determine the detector response
- *Physics sample*: for the determination of the up-down annihilation asymmetries ( $A^{raw}$ ) for each bias

# Model definition and calibration

- Likelihood for the release ramp annihilation positions  $Z$  in a given bias configuration ( $i$  bias label):

$$\mathcal{L}_i(\mathbf{Z}_i | A_i^{raw}, S_i) \propto e^{-(S_i+B_i)} \prod_{z_e \in \mathbf{Z}_i} \left[ \frac{1}{2} S_i (1 - A_i^{raw}) f_d(z_e) + \frac{1}{2} S_i (1 + A_i^{raw}) f_u(z_e) + B_i f_b(z_e) \right]$$

PDF in  $z$  for upwards, downwards released Hbar, and background fixed by fitting



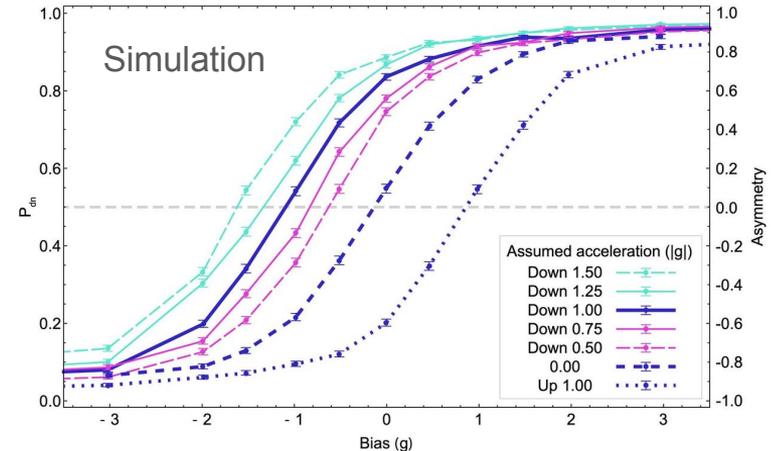
# The release asymmetry

- Likelihood for the release ramp annihilation positions  $Z$  in a given bias configuration ( $i$  bias label):

$$\mathcal{L}_i(\mathbf{Z}_i | A_i^{raw}, S_i) \propto e^{-(S_i+B_i)} \prod_{z_e \in \mathbf{Z}_i} \left[ \frac{1}{2} S_i (1 - A_i^{raw}) f_d(z_e) + \frac{1}{2} S_i (1 + A_i^{raw}) f_u(z_e) + B_i f_b(z_e) \right]$$

The MAGB likelihood on the *physics samples* depends on the number of signal events  $S_i$  and the raw asymmetry  $A_i^{raw}$ .

- To derive the release asymmetry  $A$ ,  $A^{raw}$  is corrected by the **detector efficiency asymmetry  $D$** .
- To obtain the gravitational acceleration of Hbar ( $a_g$ ) a **model of the Hbar release asymmetry  $A$  vs bias** is needed:
  - From simulation as field measurements are done in 1d and not in real time during the Hbar release



# Systematic uncertainties

- From the maximum of the **total likelihood**

$$\mathcal{L}(\mathbf{Z}|a_g, D, \mathbf{S}) = \prod_i \mathcal{L}_i[\mathbf{Z}_i|A_i^{raw}(a_g, D), \mathbf{S}]$$

Obtained  $a_g$  estimate with statistical uncertainty:  
 $a_g = 0.75 \pm 0.06$  g

- Different sources of **systematic uncertainty**, the most relevant are:
  - uncertainty **on  $D$**  evaluated by setting a gaussian constraint:
 
$$\mathcal{L}' = \mathcal{L} \cdot \frac{1}{\sqrt{2\pi\sigma_D^2}} \exp\left\{-\frac{(D - \mu_D)^2}{2\sigma_D^2}\right\}.$$
  - uncertainty **on the simulation** quoted separately and included in the final result

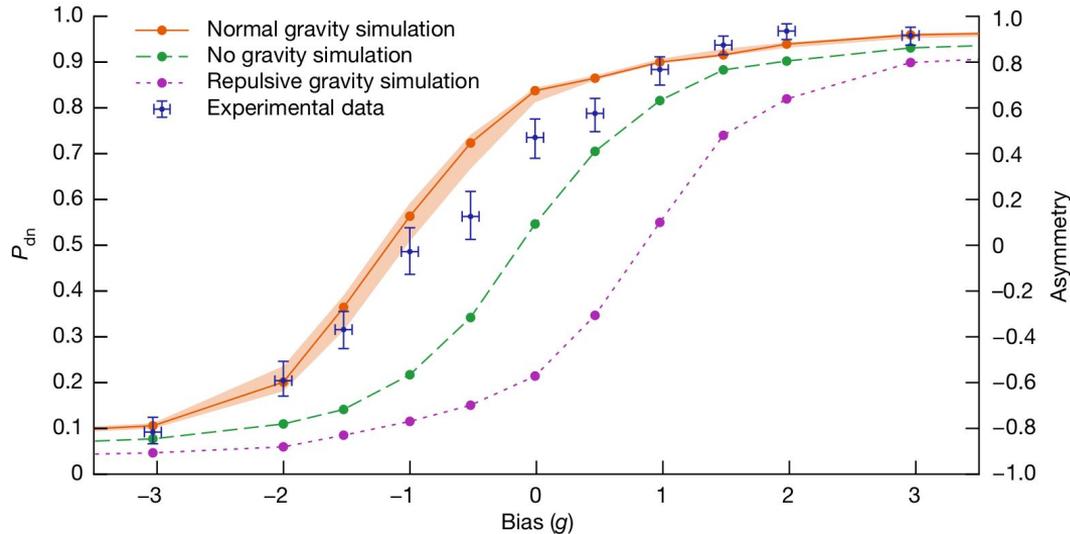
Source	Fast ramp $\sigma(g)$
Statistical	0.06
Systematics	
a) Efficiency correction	0.11
b) Calibration sample size	0.03
c) Calibration sample purity	0.00
d) Simulation sample size	0.02
e) Simulation interpolation	0.03
f) Calibration/physics	0.00
g) Fit bias (for $a_g < 0.5$ )	0.01
$\bar{H}$ simulation	
h) Energy distribution ( $A_i^{sim}$ slope)	0.03
i) Simulation $B$ -field on-axis tuning	0.06
l) Simulation off-axis model - 8-fold	$0.15 = 0.26/\sqrt{3}$

# Results

- After having treated properly the *systematic uncertainties* the local acceleration of Hbar towards the Earth is estimated to be:

$$a_g = [-0.75 \pm 0.06(stat.) \pm 0.12(syst.) \pm 0.16(model)] g.$$

- Compatible** with what is expected from General Relativity



Nature 621, 716–722  
(2023).

<https://doi.org/10.1038/s41586-023-06527-1>

# Conclusions

- **ALPHAg** has the goal of testing the **weak equivalence principle** on **anti-H**
- **Result:**
  - **Compatible** with what is expected from General Relativity
  - Demonstrated **sensitivity to gravity effects** on antihydrogen in the magnetic trap
- **Outlook:**
  - **reach 1% precision** via systematic uncertainty reduction, use of laser cooling and the precision trap
  - $10^{-6}$  precision goal probably not possible with this technique (other more precise techniques could be implemented in ALPHAg: atomic fountain and interferometry)

Backup

# Antimatter and gravity

## Previous “red shift” based experiments:

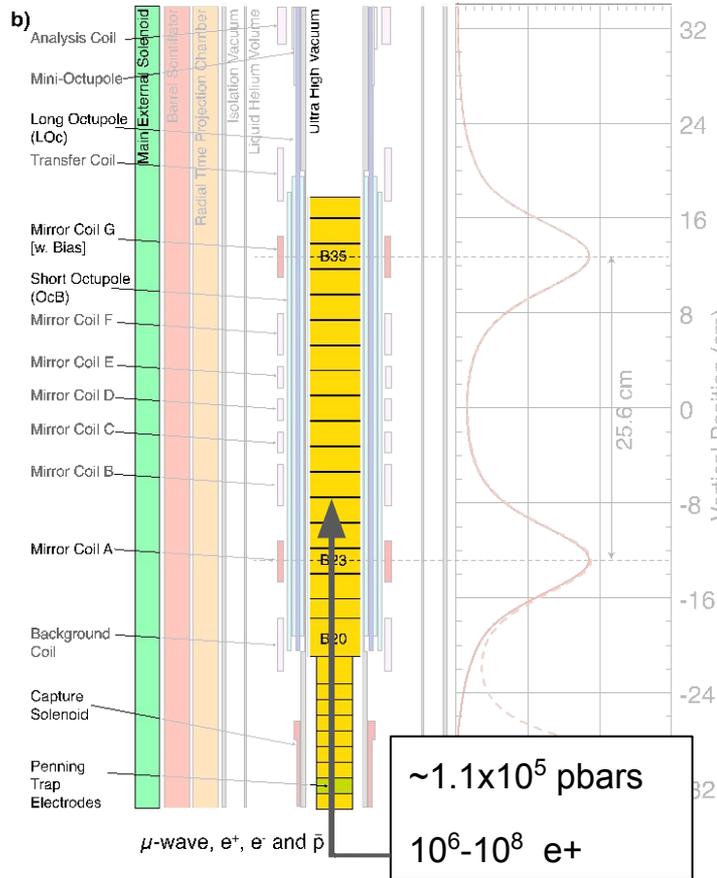
- K<sup>0</sup> – anti-K<sup>0</sup> oscillation rate (*Physics Letters B Volume 452, Issues 3–4, 22 April 1999, Pages 425-433*)
- measurements of cyclotron frequencies for the proton and the antiproton (*Phys. Rev. Lett. 66, 854 (1991)*)

● Haven't deviations from WEP on antimatter already been ruled out by previous experiments?  
even considering a photon as an e<sup>+</sup> e<sup>-</sup> pair a 5th force effect can appear in  $\hbar$  because it has baryon number unlike the photon ([arXiv:1207.7358](https://arxiv.org/abs/1207.7358))

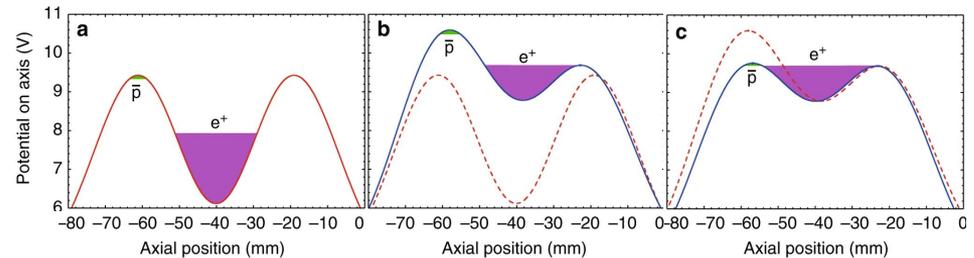
- How much of antiproton is antimatter? ([arXiv:1207.7358](https://arxiv.org/abs/1207.7358))

most of the inertial mass of an (anti)proton comes from its binding energy. Quark mass is ~1%

# Mixing plasmas



- Mixing charged plasmas in the Penning-Malmberg trap:
  - **electrodes:** plasma manipulations
  - **external solenoid (1T field):** radial confinement



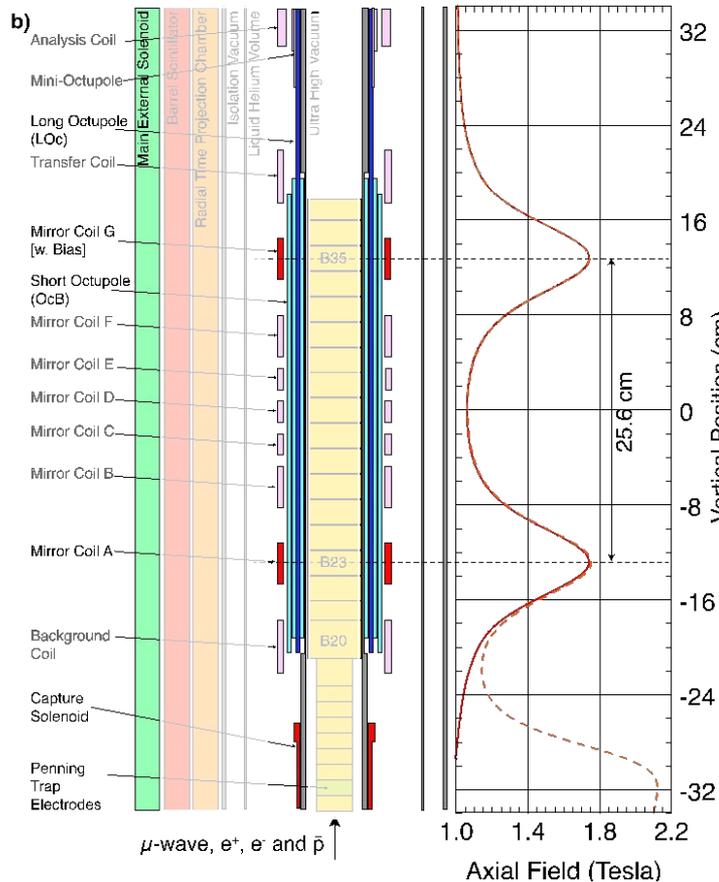
pbars and  $e^+$  in separated wells

Evaporative cooling on  $e^+$

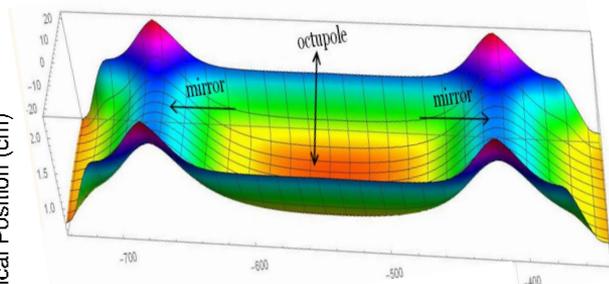
pbar well decrease

Anti-hydrogen is formed in a three-body recombination process (1 s mixing), then quickly cascade to the ground state ( $\tau < 0.5$  s)

# Trapping Hbar



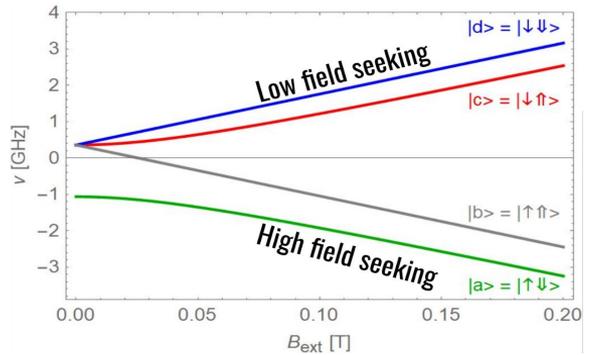
- Hbar Trapping in the Ioffe-Pritchard trap:
  - Magnets: **octupoles and mirrors**
  - external solenoid: background field



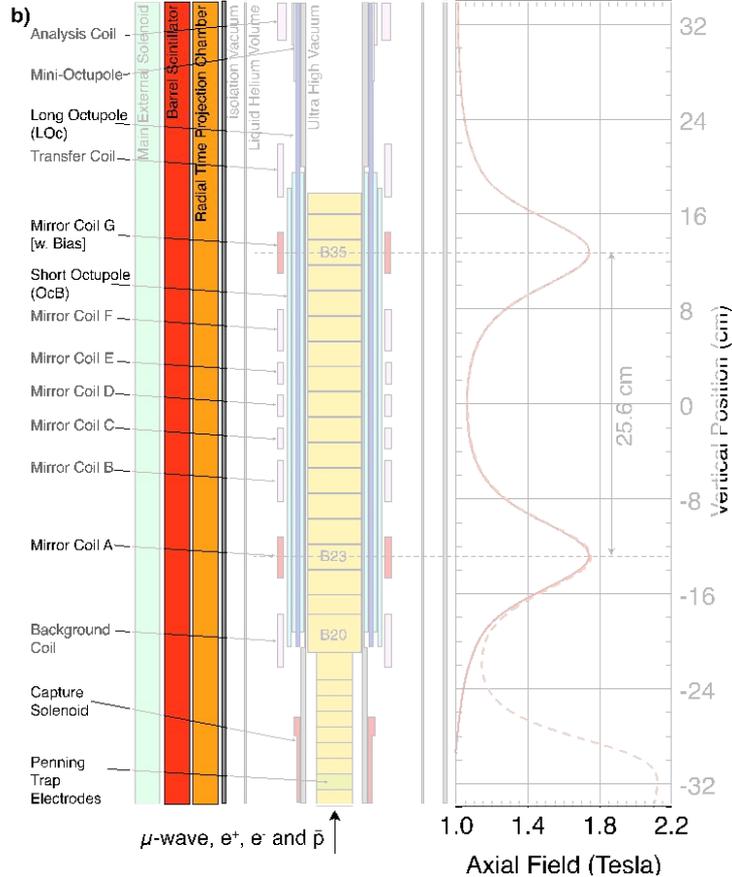
confinement potential  $U = -\mu_{\bar{H}} \cdot B$

$$\mu_{\bar{H}}^{\parallel} = \pm \mu_B$$

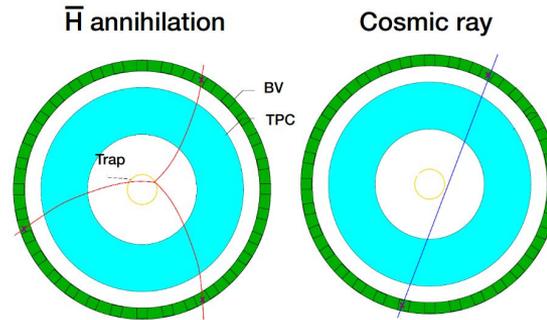
- Trappable Hbars:
- $E_{\text{kin}} < 0.54 \text{ K}$
  - Low field seeking states



# Hbar detection

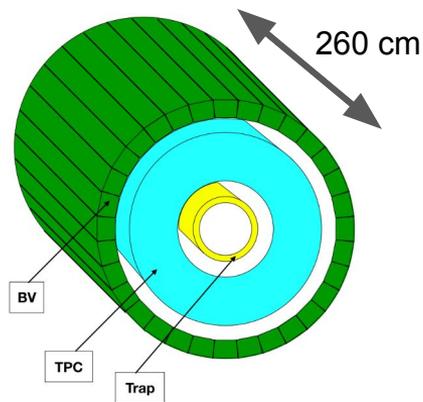


- Hbars can be **released by lowering the confining magnetic fields**
- Annihilation happens: products mostly pions
- Detectors:
  - **Radial field time-projection-chamber (rTPC)** filled with an Argon/CO<sub>2</sub> mixture: vertex reconstruction
  - **Scintillators Barrel Veto:** cosmic background suppression



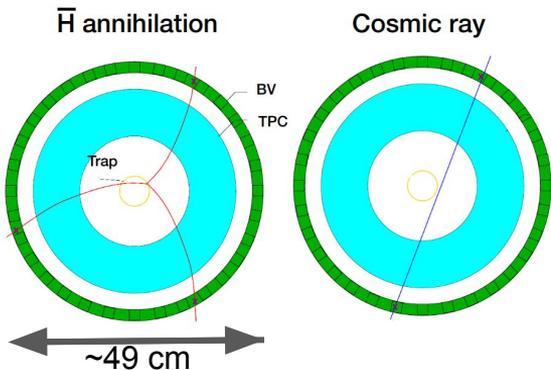
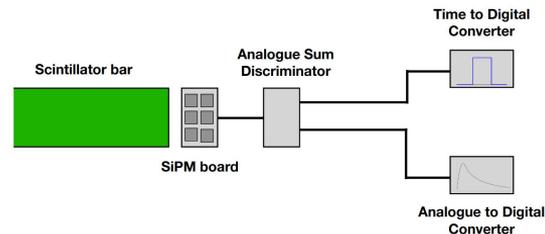
Diameter  $\sim 49$  cm  
Total height  $\sim 260$  cm

# ALPHA-g detectors



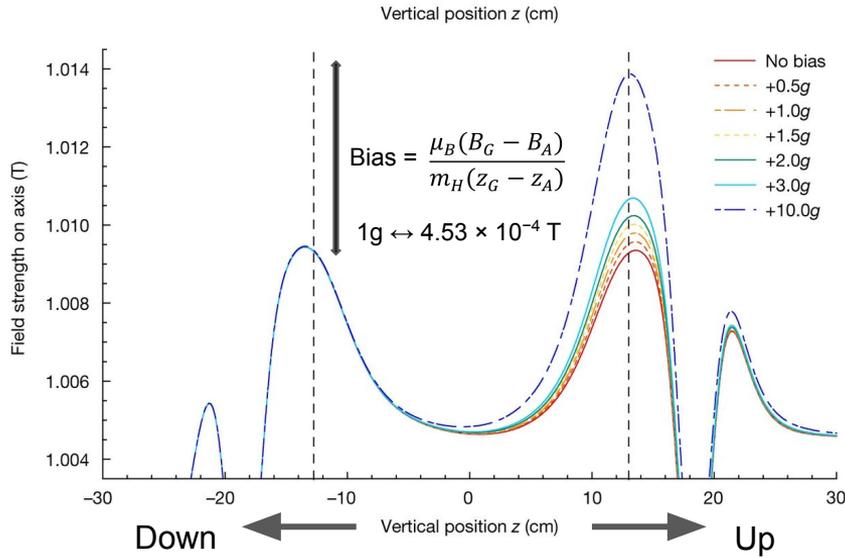
Main detectors of the ALPHA-g apparatus:

- **Radial Time Projection Chamber (TPC)**
- **Barrel Veto detector (BV):** 64 bars of plastic scintillator, each scintillator bar has a SiPM and is read out at both ends

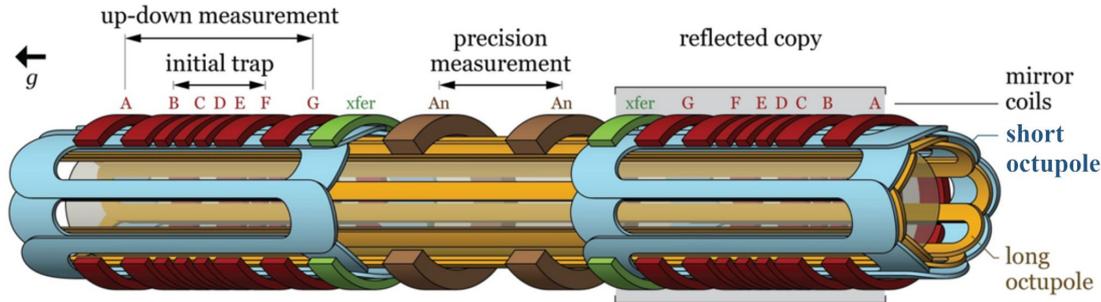


- The main **source of background** in this measurement is given by the **cosmic rays**
- The barrel veto was built with the purpose of reducing this background
- Background suppression: with a BDT classifier which is given as input 20 selection variables sensitive to the topological differences between annihilation events and cosmic ray events

# ALPHA-g magnets release sequence



- antiH accumulation in the bottom trap
- Long octupole for transverse confinement is released
- Magnetometry
- axial release during the Mirror A and G ramp-down (MAGB)
- Magnetometry
- short octupole for transverse confinement is released
- effect of gravity: difference between the number of top and bottom released atoms



# Model definition

- Likelihood for the release ramp annihilation positions  $\mathbf{Z}$  in a given bias configuration ( $i$  bias label):

$$\mathcal{L}_i(\mathbf{Z}_i | A_i^{raw}, S_i) \propto e^{-(S_i+B_i)} \prod_{z_e \in \mathbf{Z}_i} \left[ \frac{1}{2} S_i (1 - A_i^{raw}) f_d(z_e) + \frac{1}{2} S_i (1 + A_i^{raw}) f_u(z_e) + B_i f_b(z_e) \right]$$

For each bias ( $i$  bias label)

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## Expected yields

(1) Downwards released Hbar

$$N_{d,i} = \frac{1}{2} S_i (1 - A_i^{raw})$$

(2) Upwards released Hbar

$$N_{u,i} = \frac{1}{2} S_i (1 + A_i^{raw})$$

(3) Cosmic ray background

$$B_i$$

## Probability density functions

$$f_d(z_e)$$

$$f_u(z_e)$$

$$f_b(z_e)$$

In two  $z$  bins:  
[-32.8, -12.8] U [12.8, 32.8] cm

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(3) Cosmic ray background

$$B_i$$

## Parameters

- $S_i = N_i^u + N_i^d$ : total number of signal events ( Hbar annihilations)
- $A_i^{raw}$  asymmetry between upwards and downwards released Hbar:

$$A_i^{raw} = (N_{u,i} - N_{d,i}) / S_i$$

Not corrected by detector efficiency

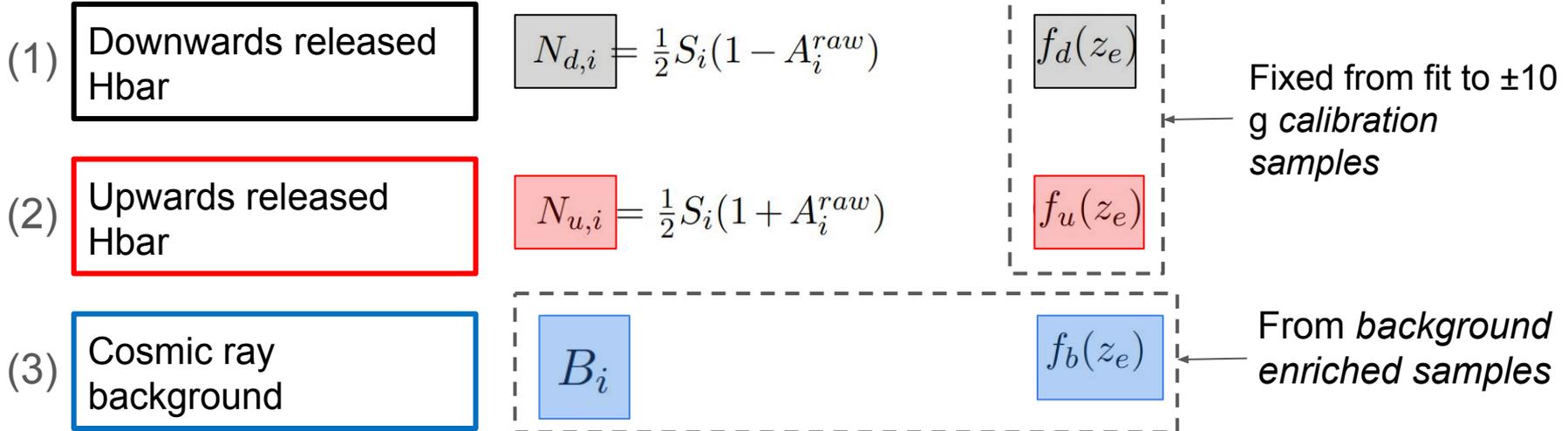
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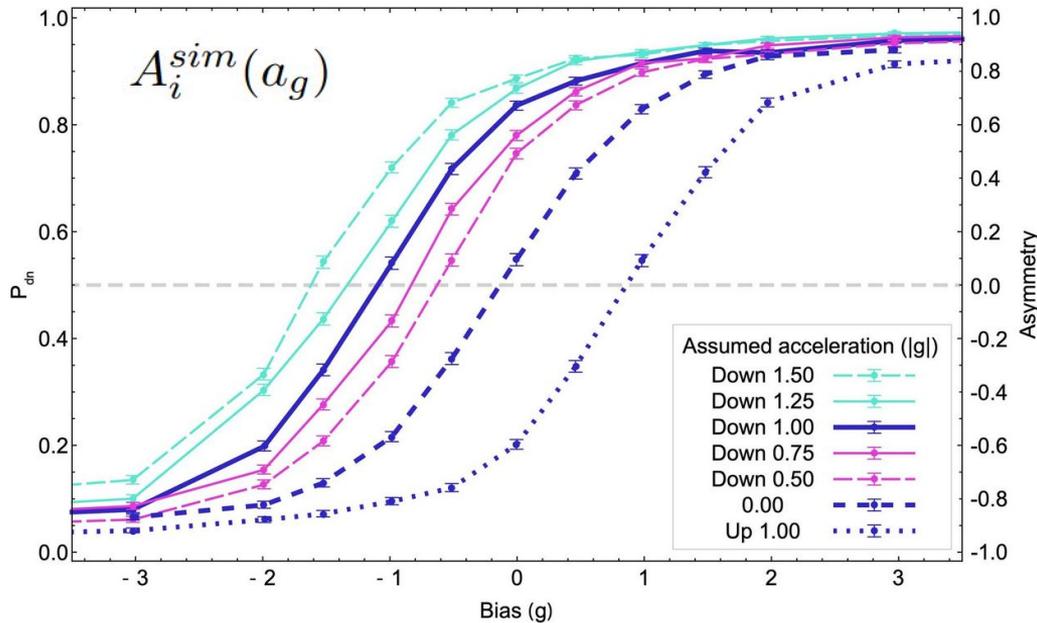
**Expected yields**

**Probability density functions**



# Regression with simulated model (S-curves)

- A model for the relation between the asymmetry and the total potential difference at the mirrors A and G is obtained via simulation:



- Modelling Initial energy distribution
- Modelling of magnetic fields
- Simulation of the trajectories of Hbar

GPR fitting used to extract the S-curves at intermediate  $a_g$  values

- Then, via simulation, it is possible to write the total likelihood in terms of  $a_g$ :

$$\mathcal{L}(\mathbf{Z}|a_g, D, \mathbf{S}) = \prod_i \mathcal{L}_i[\mathbf{Z}_i|A_i^{raw}(a_g, D), \mathbf{S}]$$

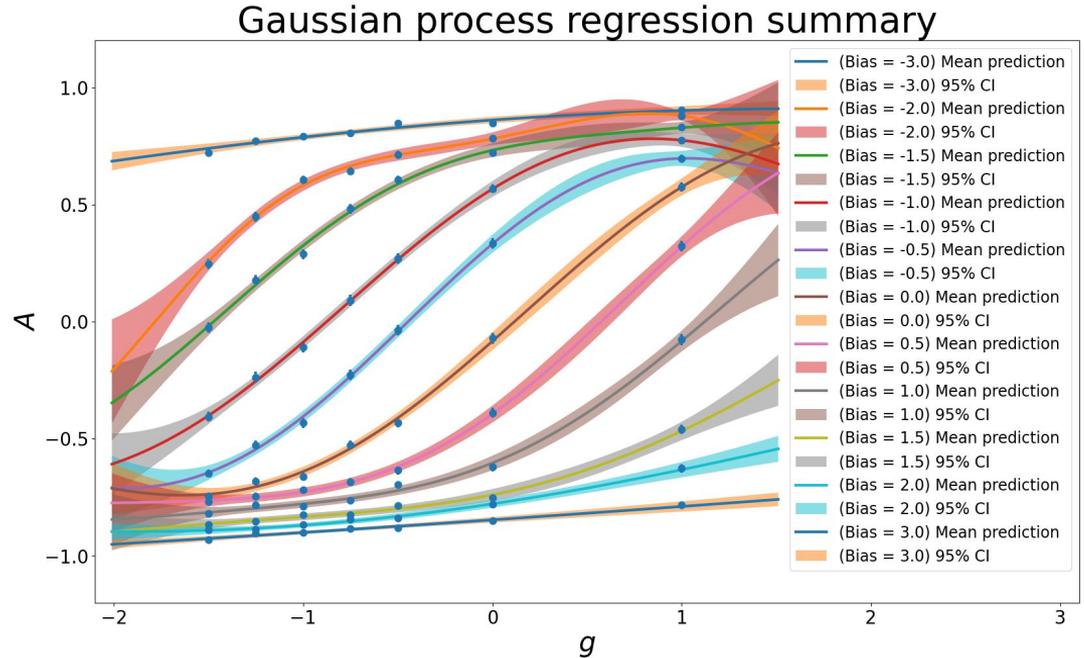
where 
$$A_i^{raw}(a_g, D) = \frac{A_i^{sim}(a_g) - D}{1 - A_i^{sim}(a_g)D}$$

# Simulated model systematic uncertainties

- Off-axis:
  - studying the impact of possible magnet misalignment on the S-curves.
  - effect of this misalignment on the S-curve intercept with  $A=0$  was evaluated.
  - The maximum shifts from the unperturbed configuration are found to be  $\pm 0.26$  g (corresponding to the “octupole 8-fold” configurations). interpreted here as a worst-case scenario

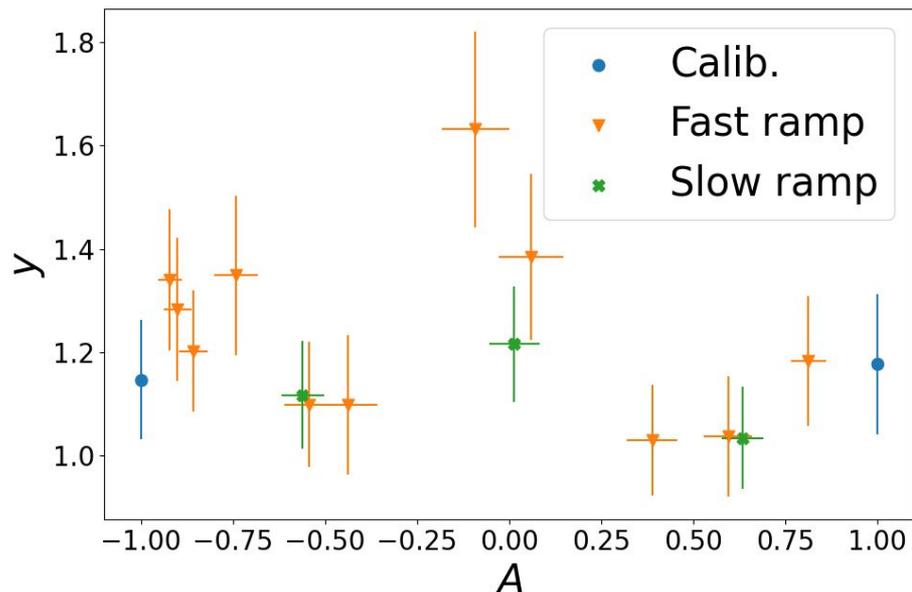
# GPR fitting of simulated S-curves

- Points: from simulation, error 1 sigma
- Lines: mean prediction from GPR
- Bands: 95 % confidence interval from GPR



# Efficiency asymmetry

Being  $\eta_u$  and  $\eta_d$  the efficiencies in detecting respectively *up* and *down* annihilations,  $D$  is defined as  $\frac{\eta_d - \eta_u}{\eta_u + \eta_d}$ .



Estimated assuming the proportionality between the LOc counts and the MAGB counts: LOc counts is proportional to the number of anti-H that were trapped

$$\frac{S_{i,o}}{S_i} = \kappa_i(1 + D_i A_i^{raw})$$

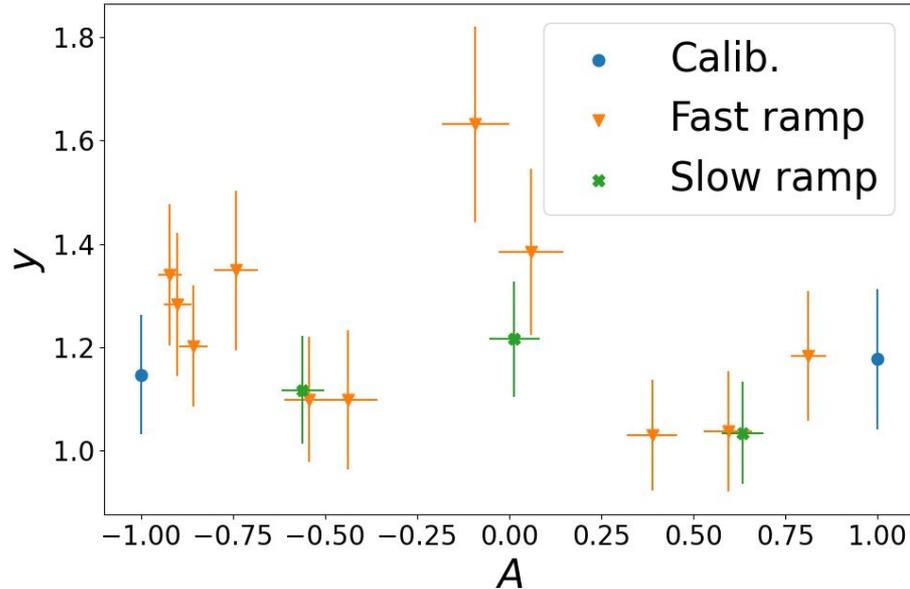
The different datasets highlighted in the plot were fitted with a linear model.

$$y = mx + q \quad \begin{aligned} y &= S_{i,o}/S_i \\ x &= A_i^{raw} \end{aligned}$$

The obtained efficiency asymmetry is

$$D = -0.03 \pm 0.06$$

# Efficiency asymmetry



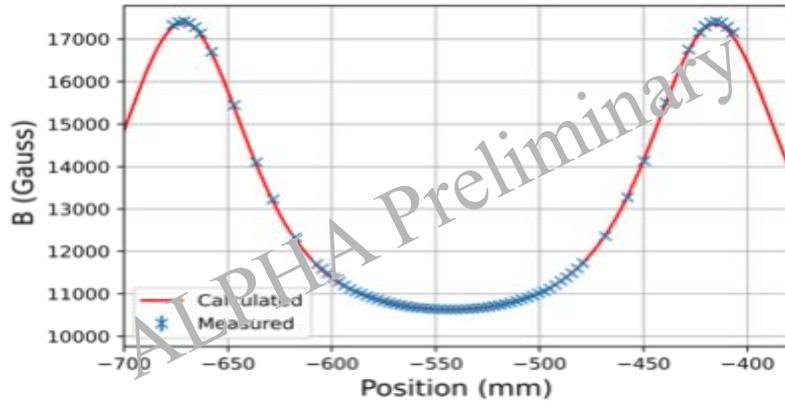
assumption of proportionality between LoC and the Hbar population before the MAGB ramp might not hold due to Hbar losses occurring between the two ramps

Systematic uncertainty on  $D$  is evaluated by varying the numerator of  $y = \frac{S_{i,o}}{S_i}$

and repeating the fit again for each variation.

Cyst uncertainty found to be 0.02, to be added in quadrature to the statistical uncertainty of 0.06

# Magnetometry



## Electron Cyclotron Resonance:

- Microwave heating of electron plasmas when microwave freq  $\sim$  cyclotron freq
- precision of the measurement:  $\sim 10^{-2}$  Gauss
- Slow measurement ( $\sim$  min)

(*Phys. Plasmas* 27, 032106 (2020);  
<https://doi.org/10.1063/1.5141999>)

## Magnetron-based magnetic field measurement:

- Measurement of magnetron frequency of electrons in Penning-Trap
- For understanding dynamic evolution of the fields
- precision of the measurement:  $\sim 1$  Gauss
- Fast measurement

