



Recent results and prospects on rare Kaon decays

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MITP Seminar

Open Questions and Future Directions in Flavour Physics

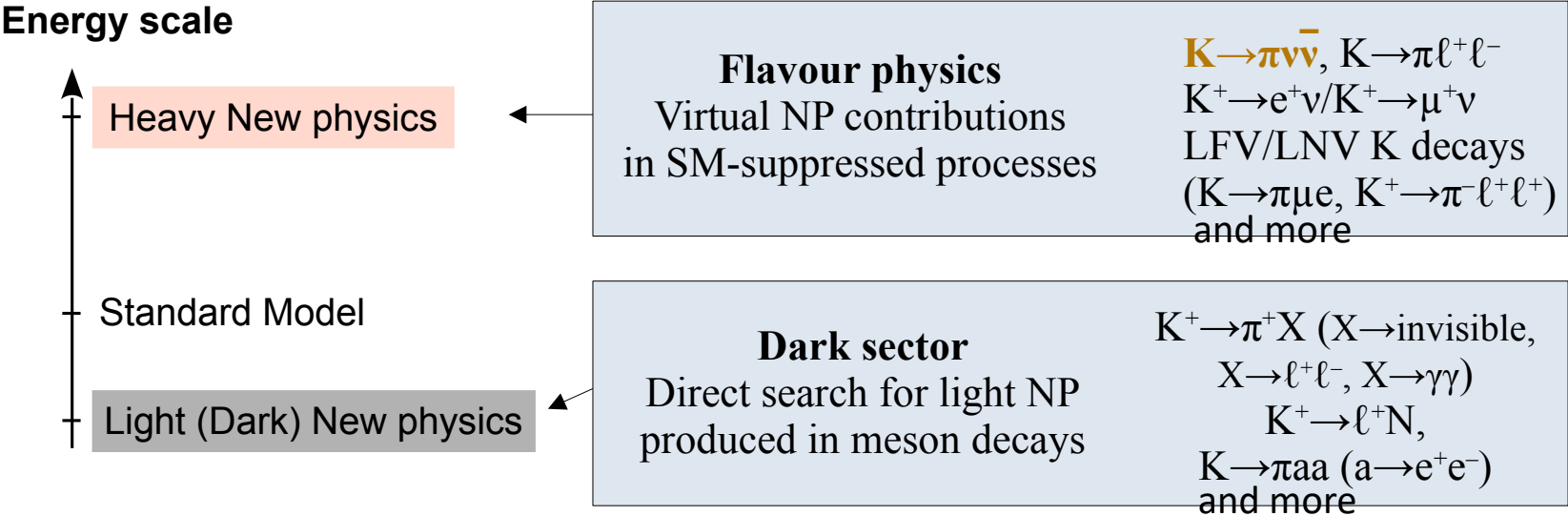
November 2024



Kaons: flavour physics laboratory@ CERN SPS

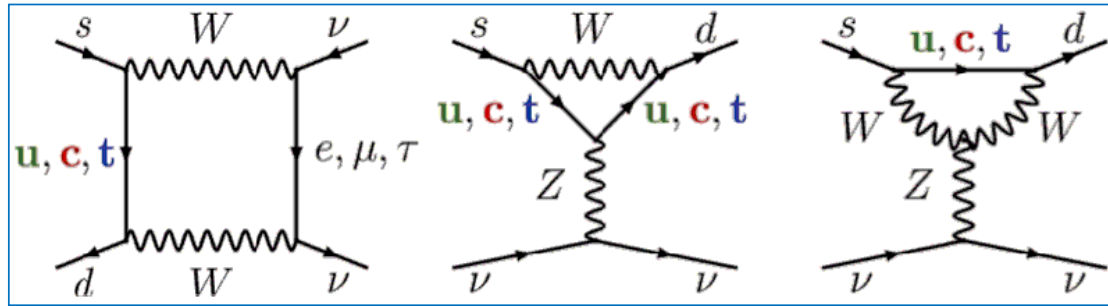
The quintessential precision frontier experiments:
few decay modes, simple final states, large statistics.

Sensitive probes of new physics:



$K^+ \rightarrow \pi^+ \nu \nu$

SM: box and penguin diagrams



FCNC process with highest CKM suppression

$$A \sim (m_t/m_W)^2 |V_{ts}^* V_{td}| \sim \lambda^5$$

Dominated by short-distance contribution (top quark)

t quark @ NLO QCD + 2-loop EW corrections,

c quark @ NNLO QCD + NLO EW corrections

Hadronic matrix element from $BR(K^\pm \rightarrow e^\pm \pi^0 \nu)$

“Free” from hadronic uncertainties

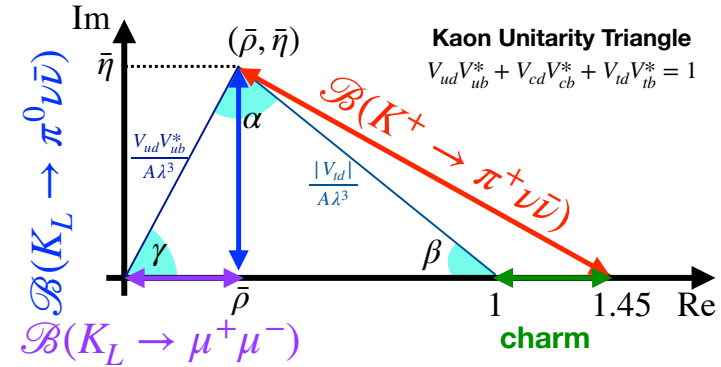
Exceptional SM precision

[arxiv:2105.02868]

Sources of uncertainty:

K^+ : SD ~ 2%, LD ~ 3%, Parametric ~ 7%

K^0 : SD ~ 2%, LD ~ 0.8%, Parametric ~ 11%



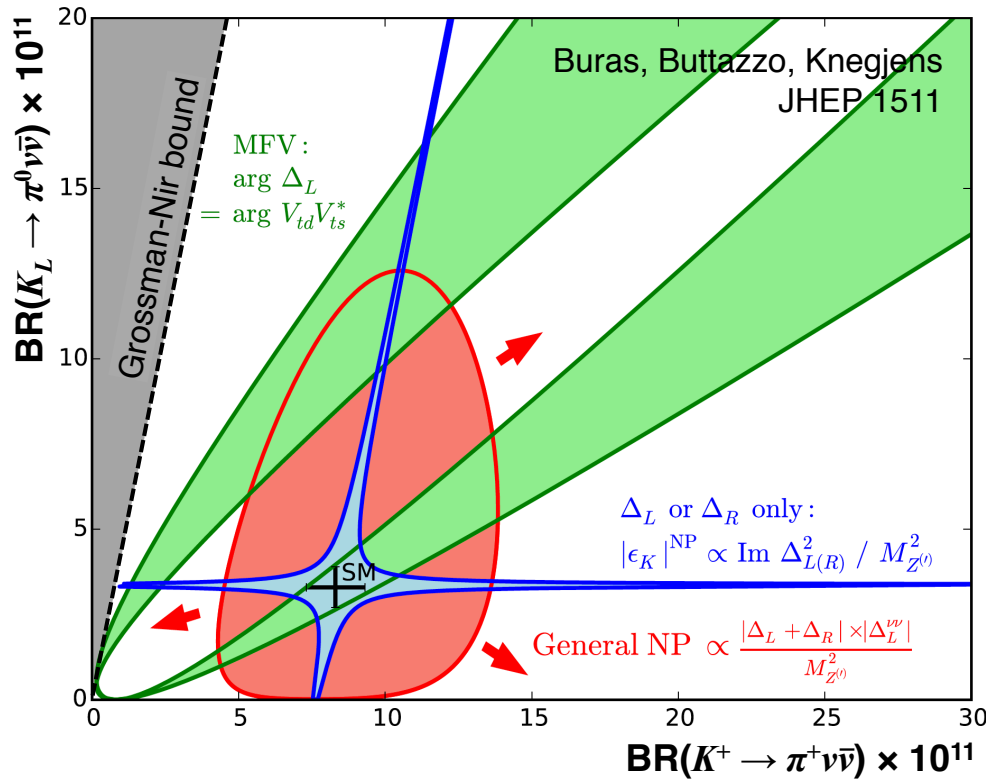
SM branching ratios

[JHEP09(2022)148]

Mode	$BR_{SM} \times 10^{11}$
$K^+ \rightarrow \pi^+ \nu \nu$	7.86 ± 0.61
$K^0 \rightarrow \pi^0 \nu \nu$	2.68 ± 0.30

Before NA62: BNL E787/E949 $Br(K^+ \rightarrow \pi^+ \nu \nu) = (1.73_{-1.05}^{+1.15}) \times 10^{-10}$

Sensitivity to new physics

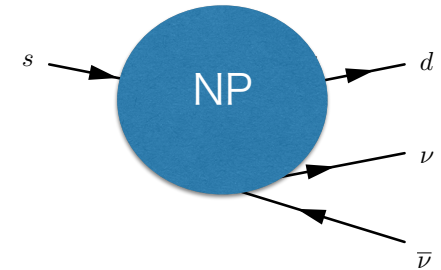


- Models with CKM-like flavor structure
 - Models with MFV
- Models with new flavor-violating interactions in which either LH or RH couplings dominate
 - Z/Z' models with pure LH/RH couplings
 - Littlest Higgs with T parity
- Models without above constraints
 - Randall-Sundrum

Grossman-Nir bound

$$\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) < 4.3 \mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$$

$$\frac{\text{BR}(K_L \rightarrow \pi^0 \nu \bar{\nu})}{\text{BR}(K^+ \rightarrow \pi^+ \nu \bar{\nu})} \times \frac{\tau_+}{\tau_L} \leq 1$$



- Simplified Z,Z' models [JHEP 1511 (2015) 166]
- Littlest Higgs with T-parity [EPJ C76 (2016) 182]
- Custodial Randall-Sundrum [JHEP 0903 (2009) 108]
- MSSM non-MFV [PEPT 2016 123B02, JHEP 0608 (2006) 064]
- LVF models [Eur Phys J C (2017) 77]

Important to have updated theory scenarios

Kaon rare decays

CERN: NA62 (K^+), LHCb (K_S)

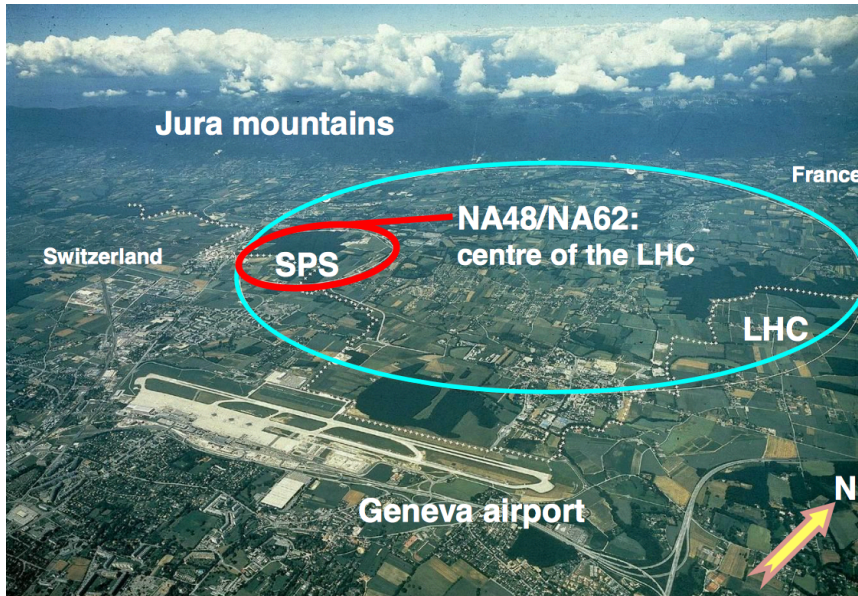


Screenshot

JPARC: KOTO, KOTO-II (K_L)

The NA62 experiment

Fixed-target experiment @ CERN North Area
400 GeV proton SPS beam



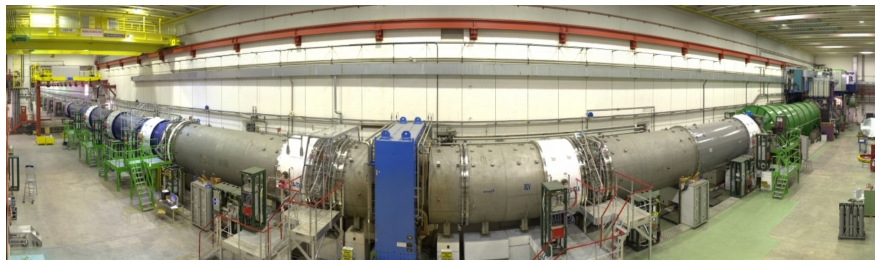
Main aim: measure
 $Br(K^+ \rightarrow \pi^+ \nu\nu)$ with
decay-in-flight technique

Broad physics programme:

- Kaon rare decays
- Searches for LFV/LNV
- Precision measurements
- Exotic searches

Timeline:

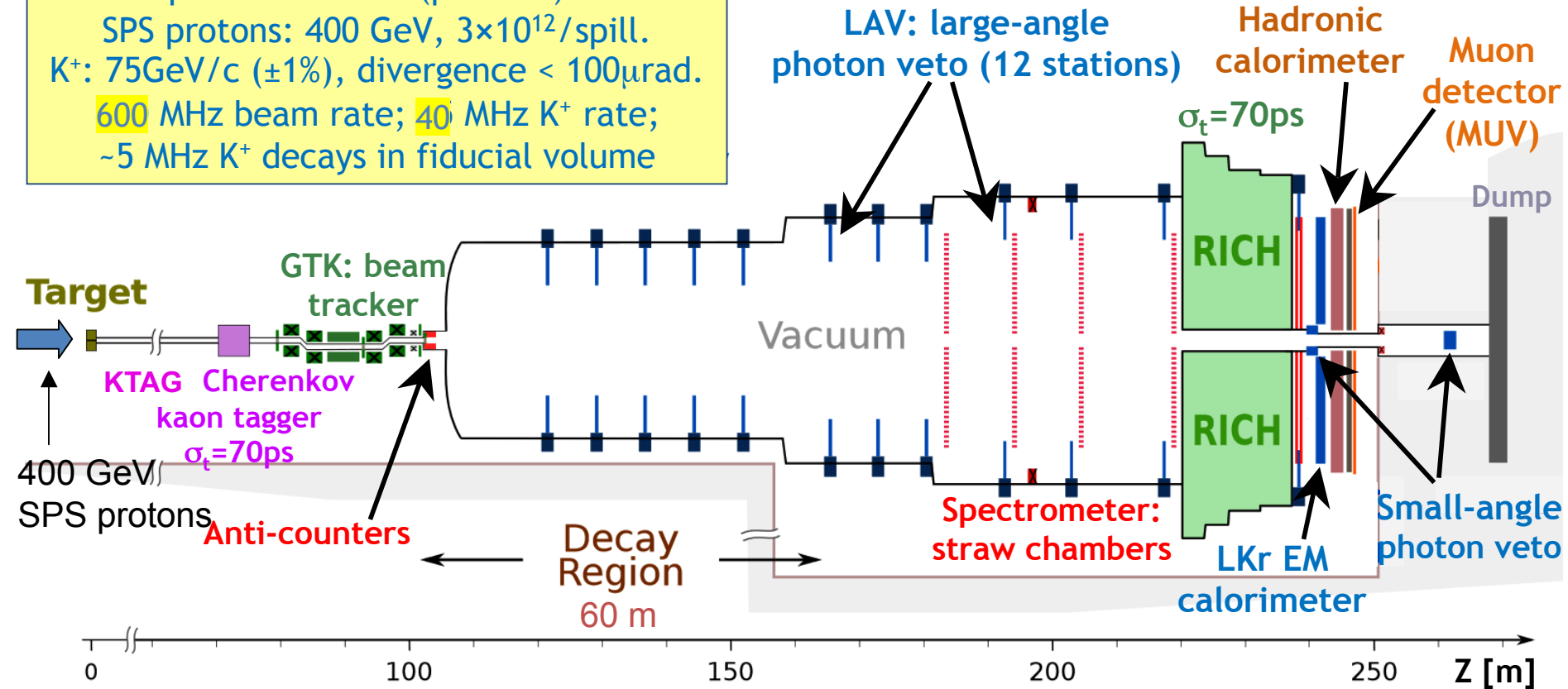
- 2016-2018: Run1 ($2.2 \cdot 10^{18}$ POT), first observation of $Br(K^+ \rightarrow \pi^+ \nu\nu)$
- 2021-LHC Long Shutdown 3: Run2 with improved detector



The NA62 beam and detector

NA62 collaboration,
JINST 12 (2017) P05025

Un-separated hadron ($p/\pi^+/K^+$) beam.
SPS protons: 400 GeV, 3×10^{12} /spill.
 K^+ : 75 GeV/c ($\pm 1\%$), divergence $< 100 \mu\text{rad}$.
600 MHz beam rate; 40 MHz K^+ rate;
 ~ 5 MHz K^+ decays in fiducial volume

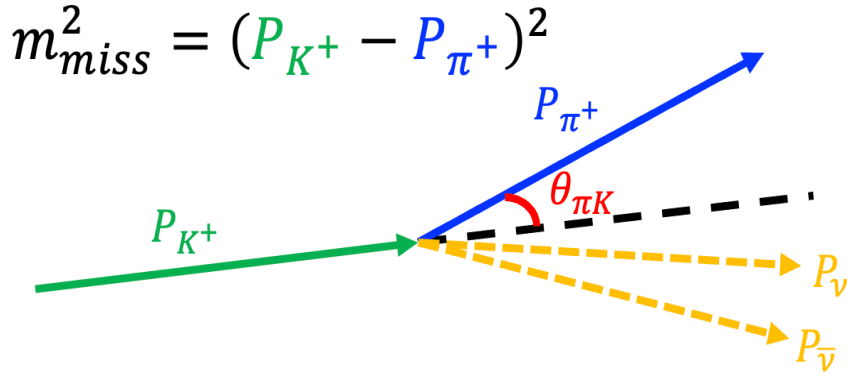


Un-separated hadron beam: find K^+
Boosted kaons (75 GeV)

NA62 technique

- Tag K^+ and measure momentum.
- Identify π^+ and measure momentum.
- Match K^+ and π^+ in time & form vertex.
 - Determine $m_{miss}^2 = (P_K - P_\pi)^2$
- Reject any additional activity.

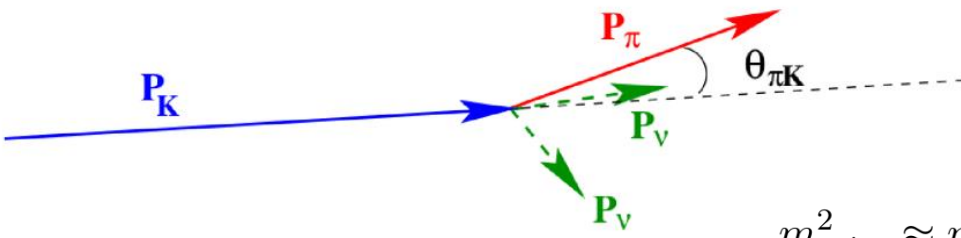
Decay mode	Branching Ratio [PDG]
$K^+ \rightarrow \mu^+ \nu_\mu$	$(63.56 \pm 0.11) \%$
$K^+ \rightarrow \pi^+ \pi^0$	$(20.67 \pm 0.08) \%$
$K^+ \rightarrow \pi^+ \pi^+ \pi^-$	$(5.583 \pm 0.024) \%$
$K^+ \rightarrow \pi^+ \pi^- e^+ \nu_e$	$(4.247 \pm 0.024) \times 10^{-5}$



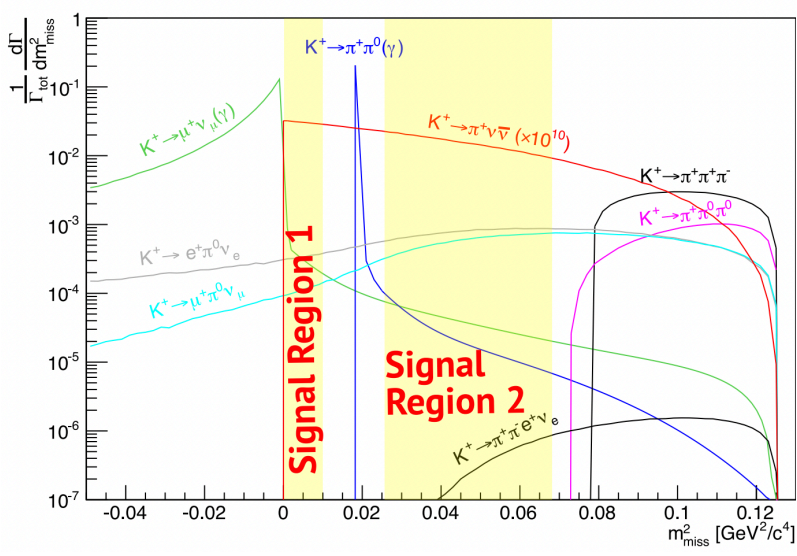
- $\mathcal{O}(100)$ ps timing between detectors
- $\mathcal{O}(10^4)$ background suppression from kinematics
- $> 10^7$ muon rejection
- $> 10^7$ rejection of π^0 from $K^+ \rightarrow \pi^+ \pi^0$ decays

Extreme challenge but... few decay modes, simple final states, large statistics. Maximum use of data for bckg evaluation.

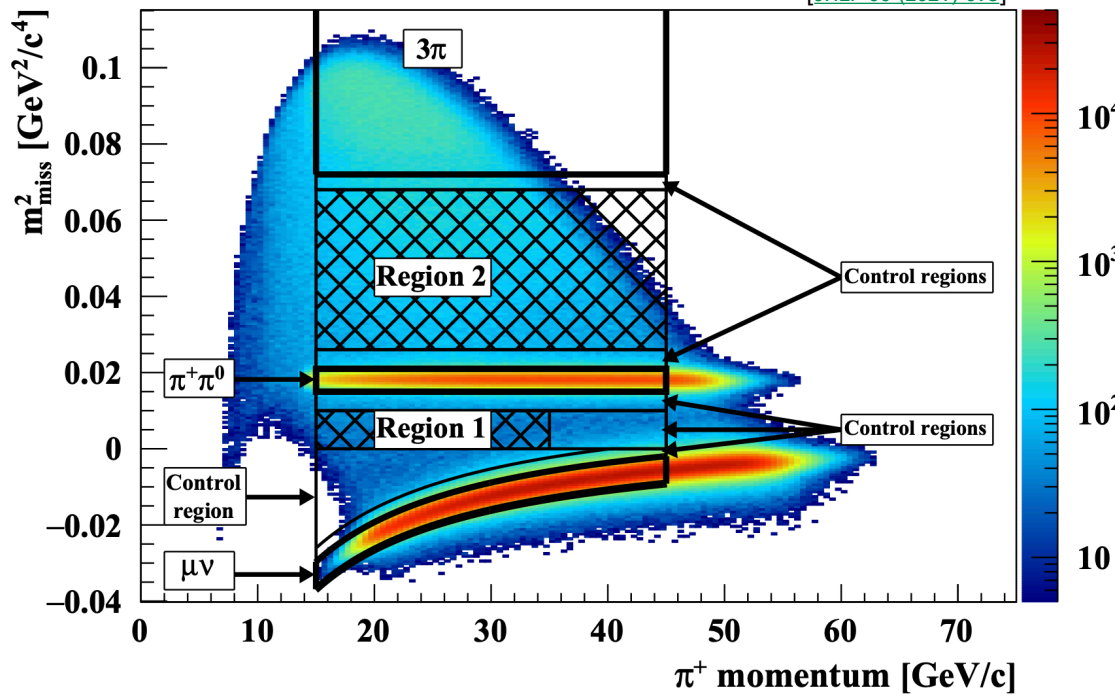
NA62 technique



$$m_{miss}^2 \approx m_K^2 \left(1 - \frac{|p_\pi|}{|p_K|}\right) + m_\pi^2 \left(1 - \frac{|p_K|}{|p_\pi|}\right) - |p_K||p_\pi|\theta_{\pi K}^2$$

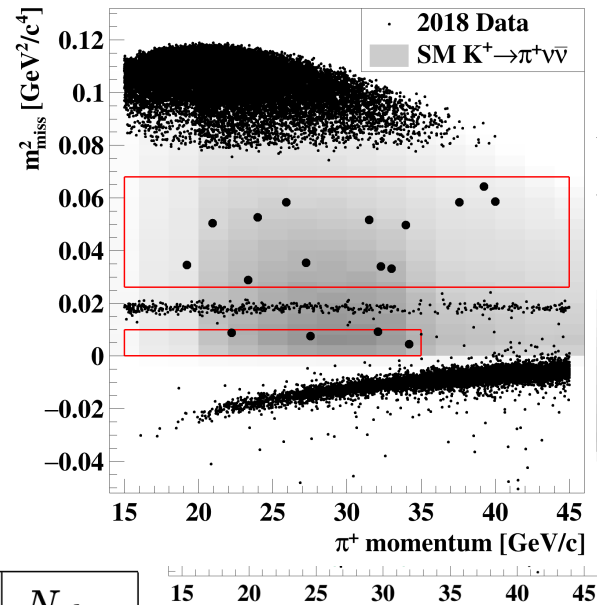
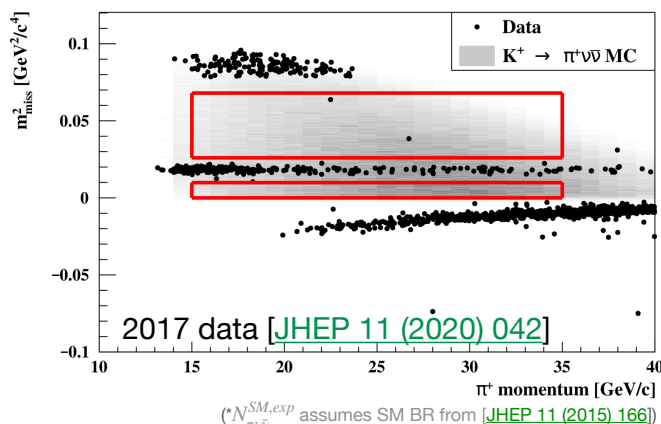
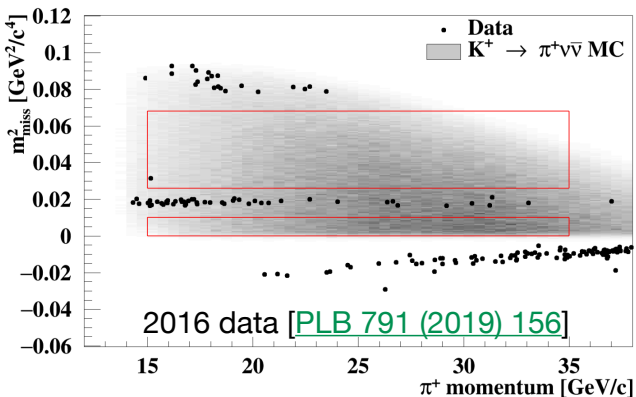


[JHEP 06 (2021) 093]



π^+ momentum range: 15–45 GeV/c

Result: 2016+2017+2018 data



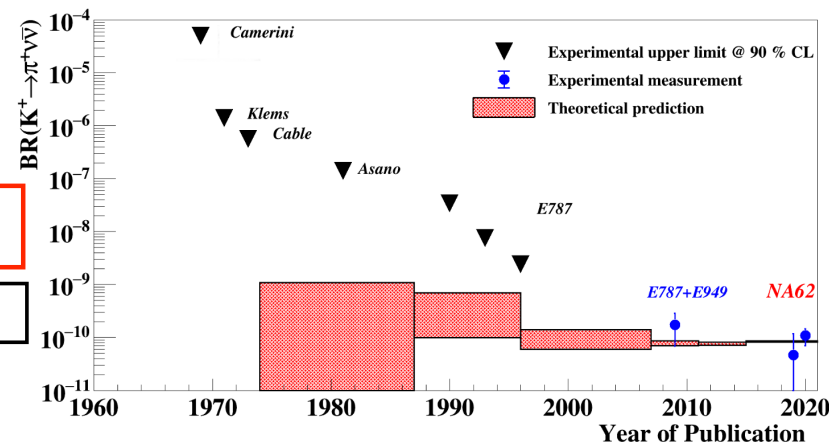
Data-taking year	[Reference]	N_{bg}	$N_{\pi\nu\bar{\nu}}^{SM,exp}$	N_{obs}
2016	[PLB 791 (2019) 156]	$0.152^{+0.093}_{-0.035}$	0.267 ± 0.020	1
2017	[JHEP 11 (2020) 042]	1.46 ± 0.33	2.16 ± 0.13	2
2018	[JHEP 06 (2021) 093]	$5.42^{+0.99}_{-0.75}$	7.58 ± 0.40	17
2016–18	[JHEP 06 (2021) 093]	$7.03^{+1.05}_{-0.82}$	10.01 ± 0.42	20

15 20 25 30 35 40 45

$N_{\pi\nu\bar{\nu}}^{SM,exp}$ assumes:
 $\mathcal{B}_{\pi\nu\bar{\nu}}^{SM} = 8.4 \times 10^{-11}$

$$\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (10.6^{+4.0}_{-3.4} |_{\text{stat}} \pm 0.9_{\text{syst}}) \times 10^{-11} \text{ at } 68\% \text{ CL}$$

In background-only hypothesis: $p = 3.4 \times 10^{-4} \Rightarrow \text{significance} = 3.4\sigma$.

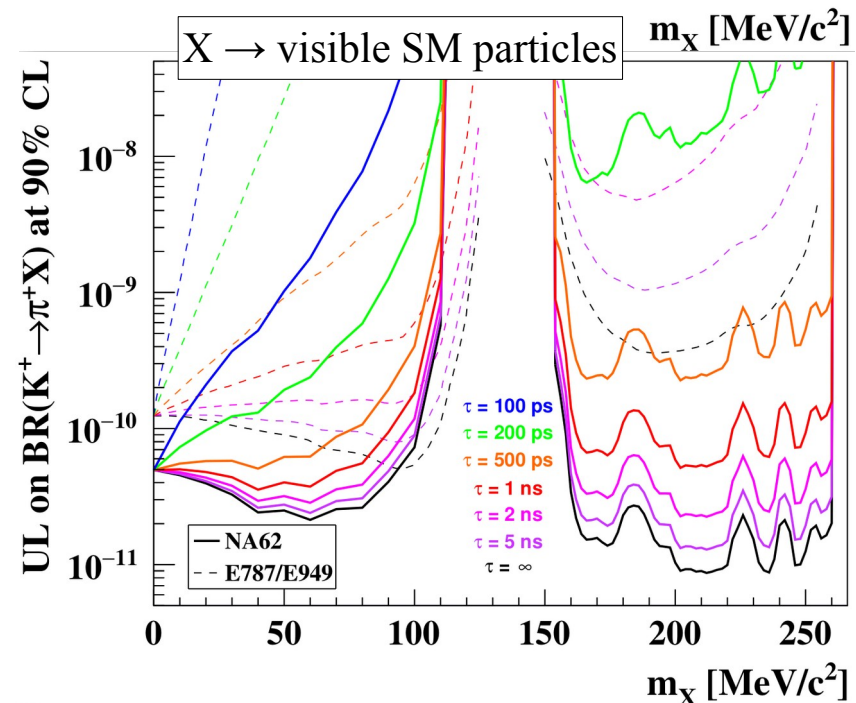
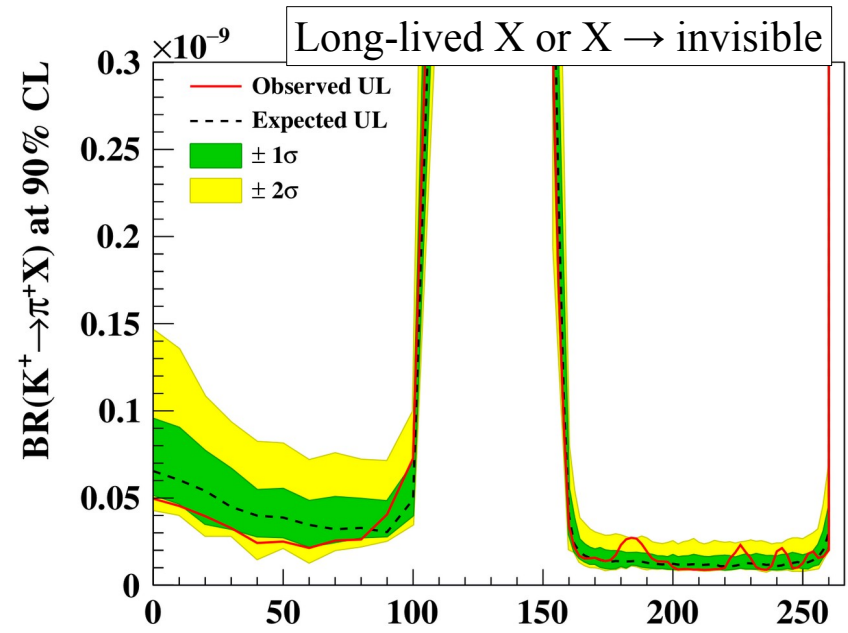
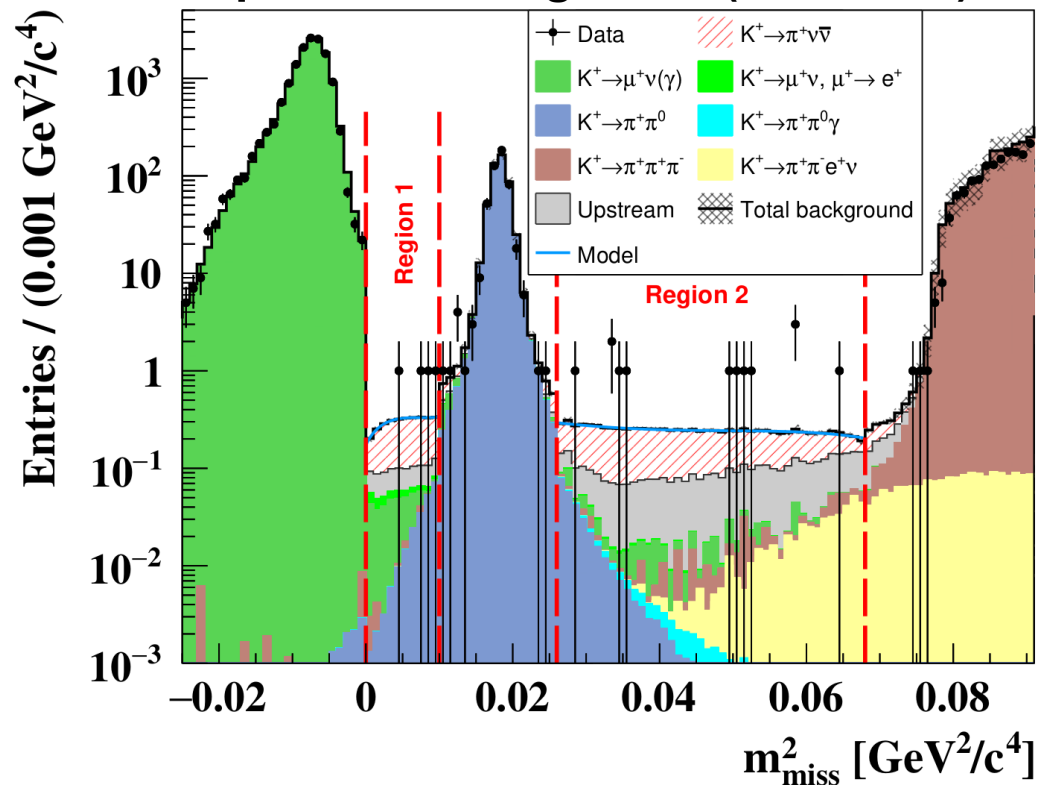


Search for $K^+ \rightarrow \pi^+ X_{inv}$

[JHEP 06 (2021) 093]

By-product of $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ analysis
 Peak search in **R1** ($0 \leq m_X \leq 110 \text{ MeV}/c^2$)
 and **R2** ($154 \leq m_X \leq 260 \text{ MeV}/c^2$)
 Acceptance scan over m_X and τ_X
 Main background: $K^+ \rightarrow \pi^+ \nu \bar{\nu}$

Squared missing mass (2018 data)

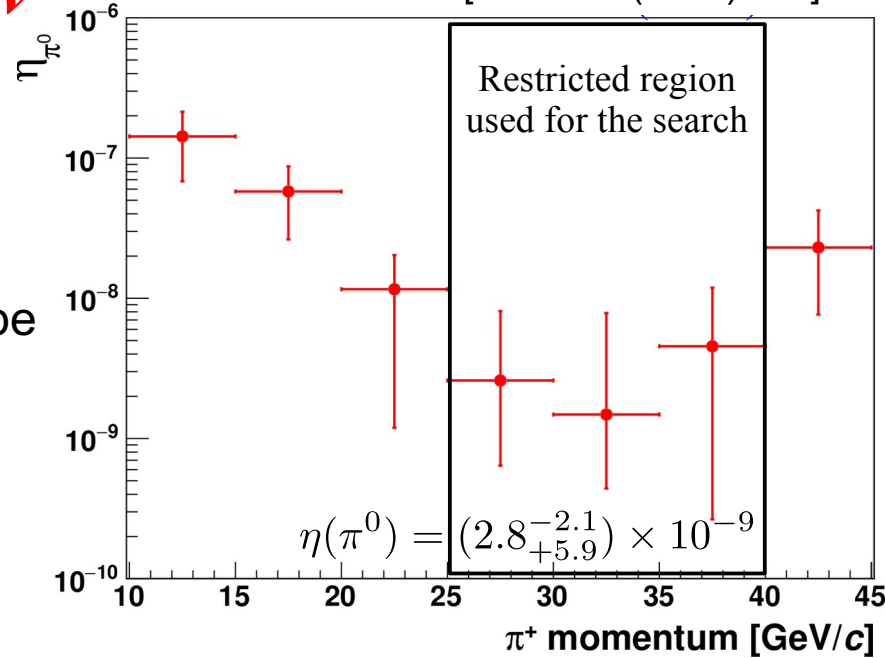


Search for $K^+ \rightarrow \pi^+ \pi^0_{inv}$

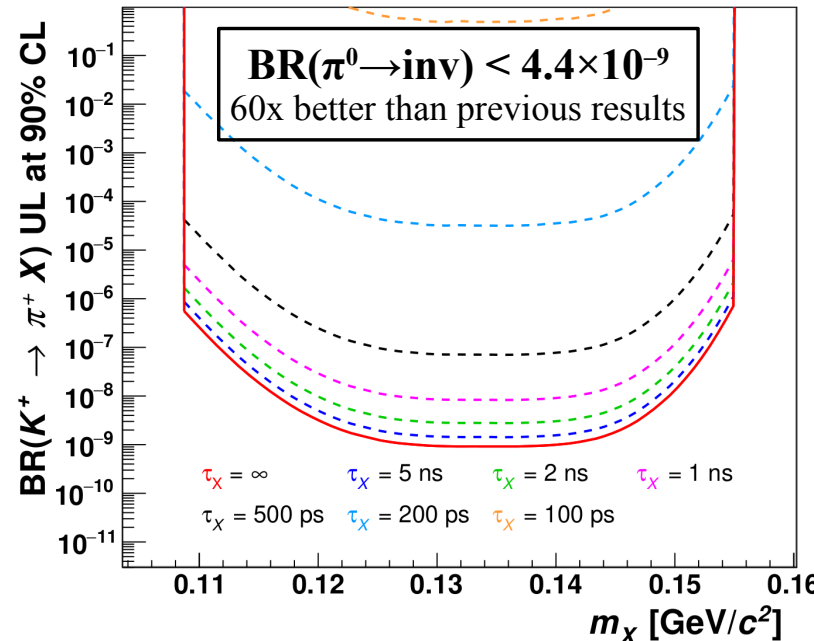
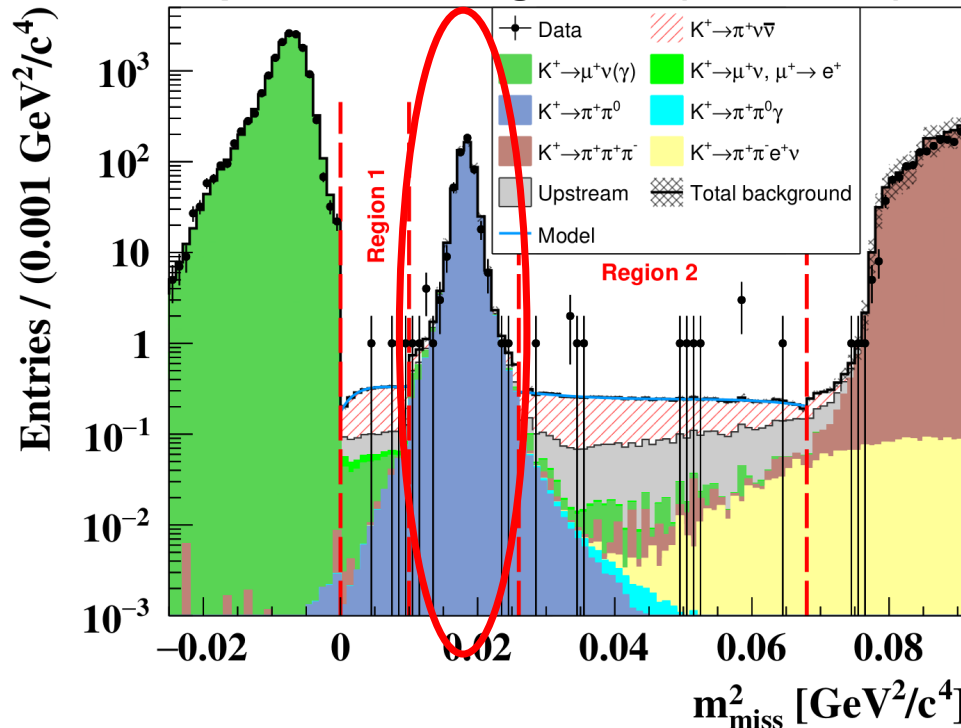
[JHEP 02 (2021) 201]

Basic event selection as $K^+ \rightarrow \pi^+ \nu \bar{\nu}$, but applied to $K^+ \rightarrow \pi^+ \pi^0$ region on 10% of Run1 data

Main $K^+ \rightarrow \pi^+ \pi^0$ ($\pi^0 \rightarrow \gamma \gamma$) background estimated from MC with single γ efficiency by tag-and-probe
 Expected $\pi^0 \rightarrow \gamma \gamma$ events: 10^{+22}_{-8} , observed: **12**.
 [reaching limits from γ -veto inefficiency]

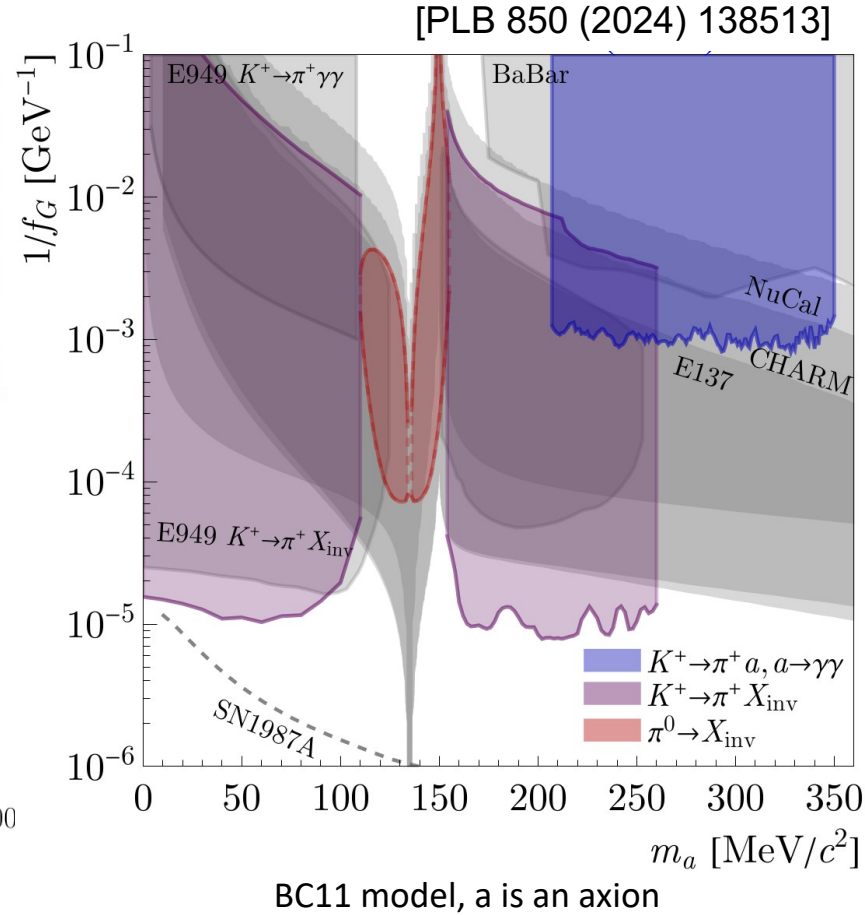
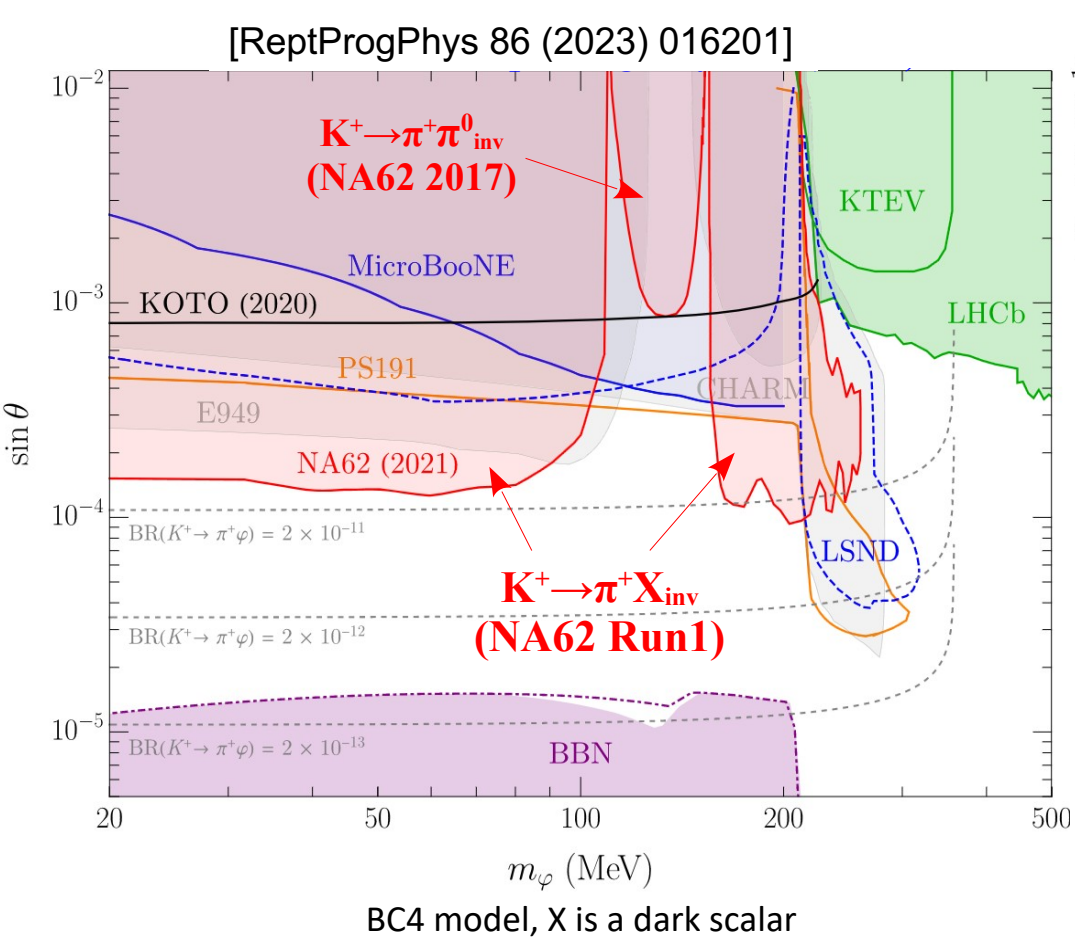


Squared missing mass (2018 data)



Interpretation of $K^+ \rightarrow \pi^+ X$

Limits on BRs for $K^+ \rightarrow \pi^+ X_{\text{inv}}$, $K^+ \rightarrow \pi^+ \pi^0_{\text{inv}}$, $K^+ \rightarrow \pi^+ X (X \rightarrow \gamma\gamma)$ translate to parameter space for hidden-sector portals



[BC models within the Physics Beyond Colliders framework]

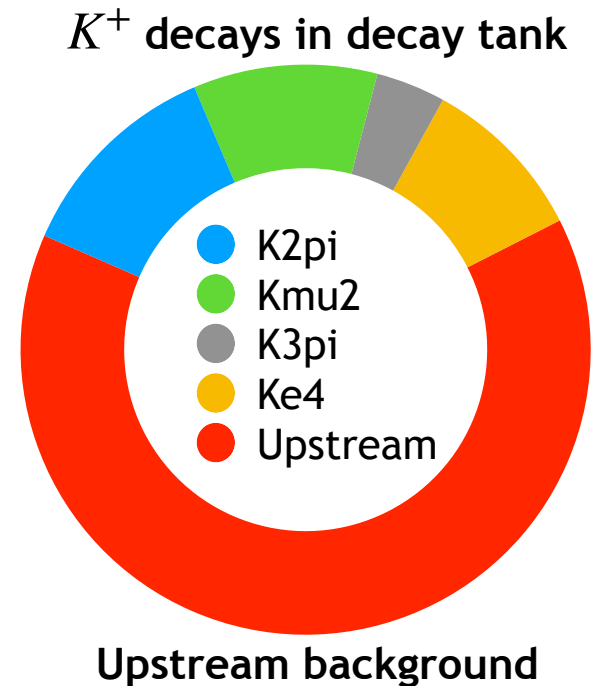
Upgrading NA62

2016–18 analysis proved NA62 technique.

Limitation: tight cuts to reject backgrounds \Rightarrow reduces signal efficiency.

To improve: need new tools to control background.

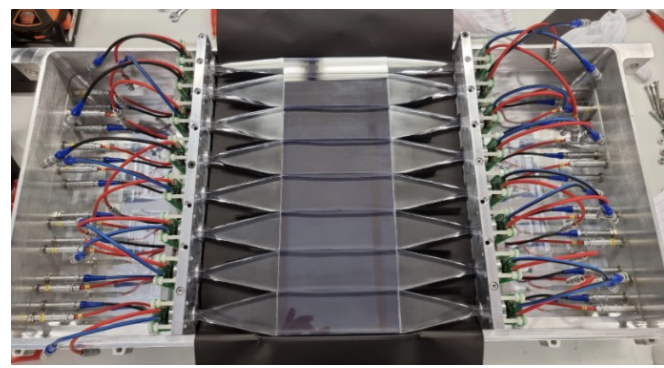
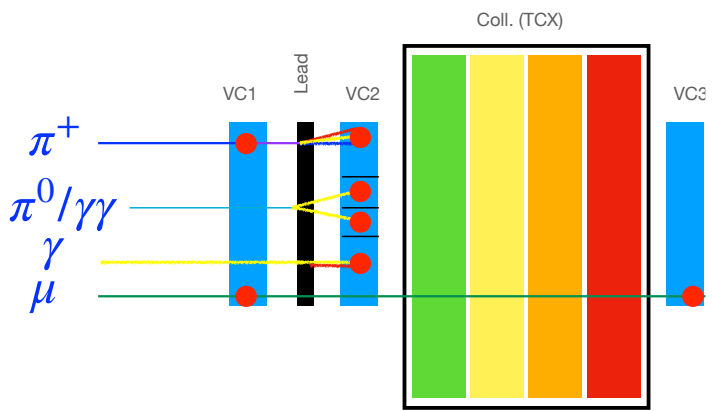
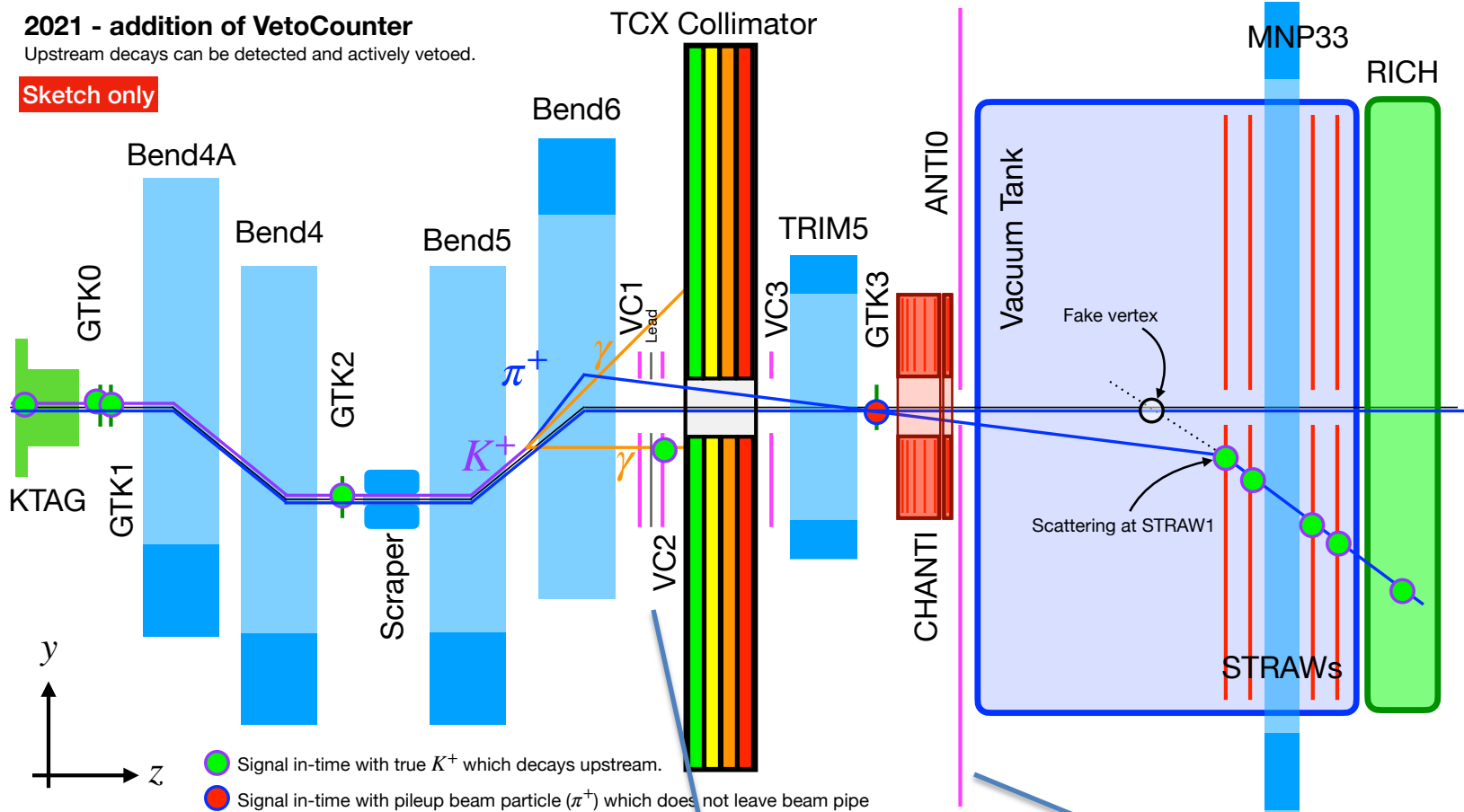
Background	N(exp) 2018 (S2)
Upstream	$2.76^{+0.90}_{-0.70}$
$K^+ \rightarrow \pi^+ \pi^0$	0.52 ± 0.05
$K^+ \rightarrow \mu^+ \nu$	0.45 ± 0.06
$K^+ \rightarrow \pi^+ \pi^- e^+ \nu$	0.41 ± 0.10
$K^+ \rightarrow \pi^+ \pi^+ \pi^-$	0.17 ± 0.08
Total	$4.31^{+0.91}_{-0.72}$



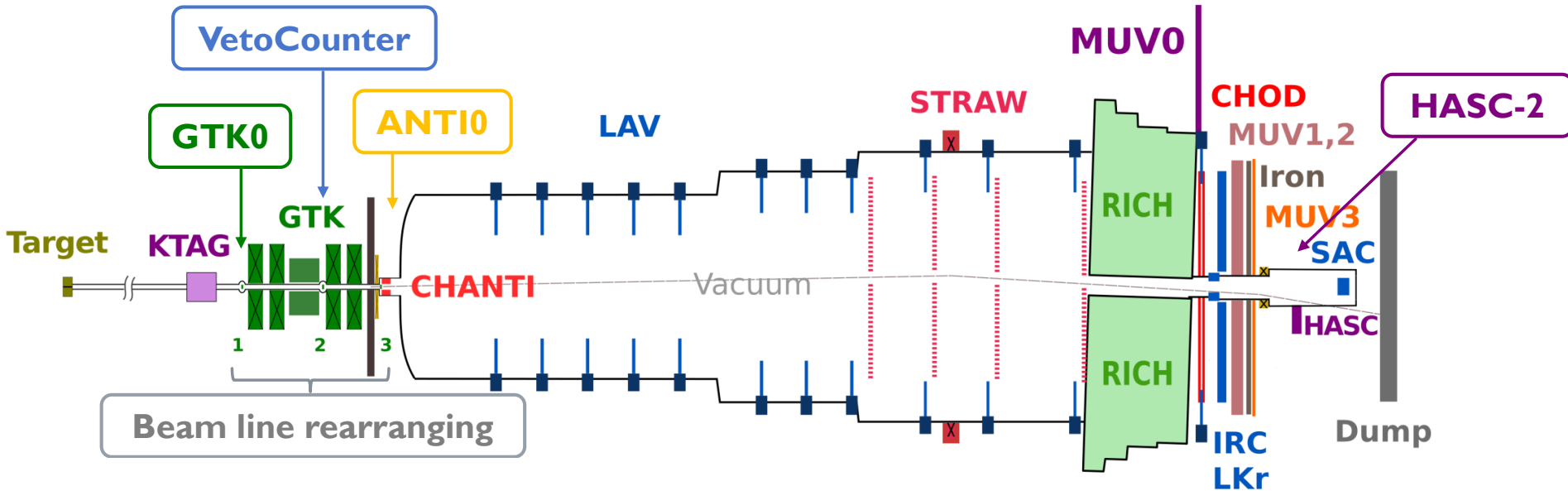
2021 - addition of VetoCounter

Upstream decays can be detected and actively vetoed.

Sketch only



2021-2022 detector improvements



Additional **GTK** station

Beam line rearranging to swipe away upstream π^+

VetoCounter to detect upstream decays

ANTI0 to veto accidental particles

HASC-2 to further suppress $K^+ \rightarrow \pi^+\pi^0$ decays

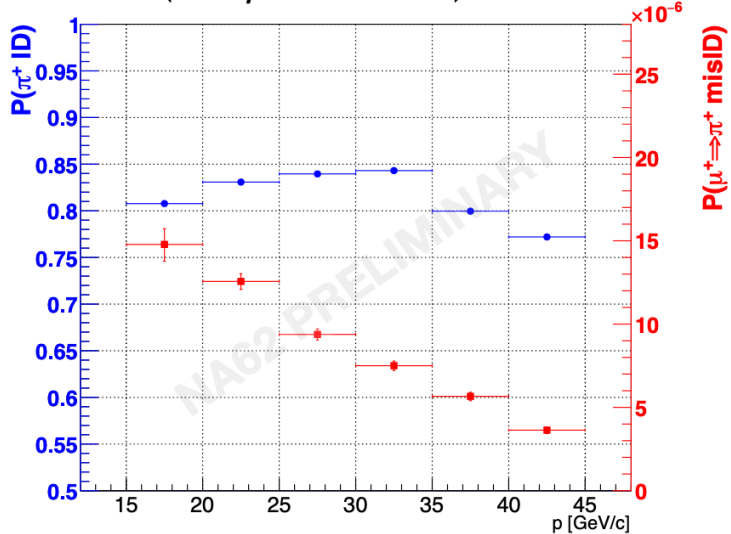
Intensity increased from 60% to 100% of nominal

Data taking pushing to the hardware limit of intensity for NA62

Particle identification performance (2021-22)

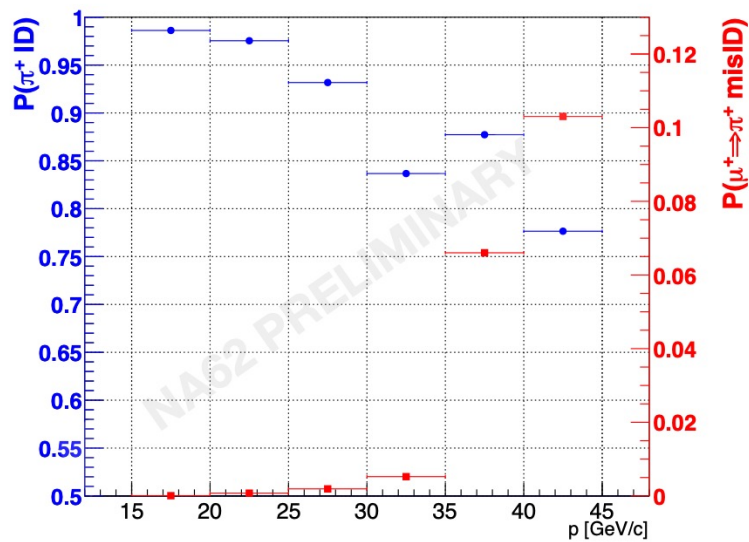
Calorimeters

Use BDT classifier for LKr & MUV1,2
+ MUV3 (fast μ^+ detector)



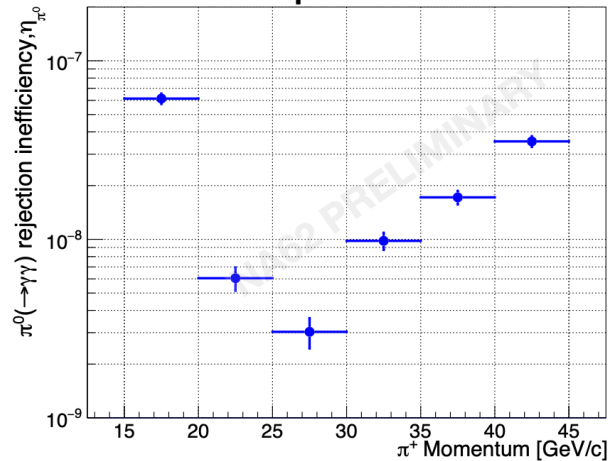
RICH

Designed to distinguish between π^+/μ^+ with 15 – 35 GeV/c.



Photon veto:

Control sample of $K^+ \rightarrow \pi^+ \pi^0$



$$\epsilon(\pi \text{ ID}) = (73.00 \pm 0.01) \%$$

$$P(\mu^+ \text{ misID as } \pi^+) = (1.3 \pm 0.2) \times 10^{-8}$$

$$\eta_{\pi^0} = (1.72 \pm 0.07) \times 10^{-8}$$

Signal sensitivity

Normalisation channel: $K^+ \rightarrow \pi^+\pi^0$, momentum range $p \in [15,45] \text{ GeV}/c$

Effective number of K^+ decays, N_K :

$$N_K = \frac{N_{\pi\pi} D_0}{\mathcal{B}_{\pi\pi} A_{\pi\pi}}$$

Number of normalisation events $\rightarrow N_{\pi\pi} D_0$
 Downscaling factor of normalisation trigger (generally 400) $\rightarrow D_0$
 Branching ratio of $K^+ \rightarrow \pi^+\pi^0$ decay $\rightarrow \mathcal{B}_{\pi\pi}$
 Acceptance of normalisation selection $\rightarrow A_{\pi\pi}$

Single event sensitivity:

(Branching ratio corresponding to expectation of 1 event)

$$\mathcal{B}_{SES} = \frac{1}{N_K \epsilon_{RV} \epsilon_{trig} A_{\pi\nu\bar{\nu}}}$$

Random veto efficiency $\rightarrow \epsilon_{RV}$
 Trigger efficiency (ratio) $\rightarrow \epsilon_{trig}$
 Signal selection acceptance $\rightarrow A_{\pi\nu\bar{\nu}}$

Number of expected SM events:

(For comparison to previous results use $\mathcal{B}_{\pi\nu\bar{\nu}}^{SM} = 8.4 \times 10^{-11}$ [[JHEP 11 \(2015\) 166](#)], but results are independent of this choice)

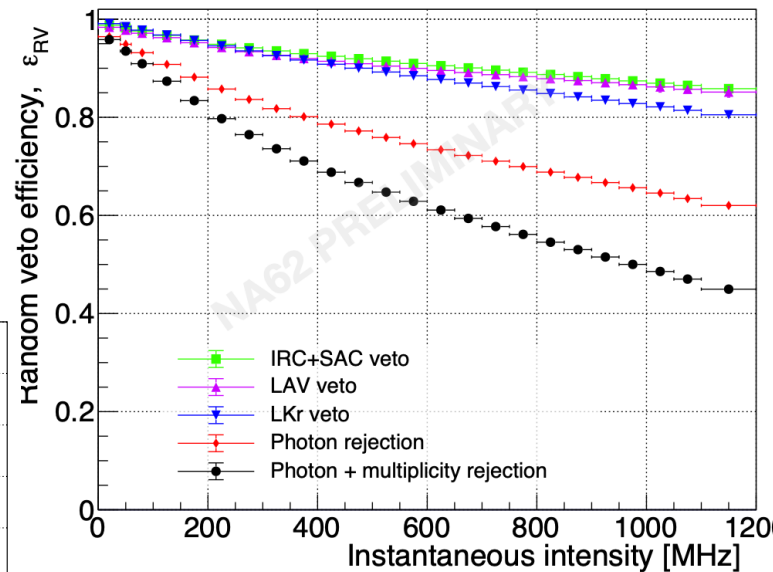
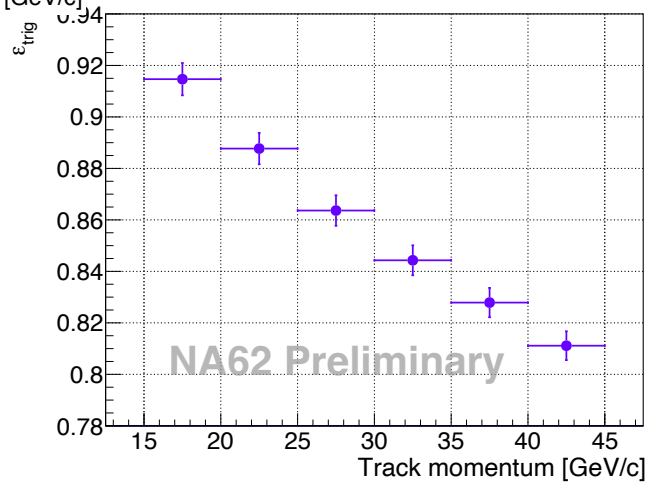
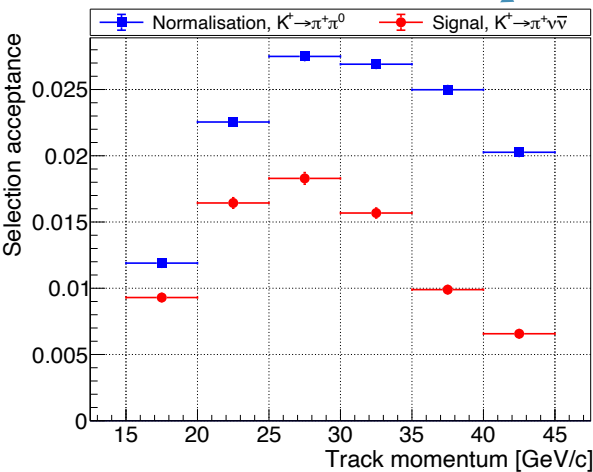
$$N_{\pi\nu\bar{\nu}}^{SM} = \frac{\mathcal{B}_{\pi\nu\bar{\nu}}^{SM}}{\mathcal{B}_{SES}}$$

Single-event sensitivity (2021-2022 data)

$$N_{\pi\nu\nu}^{\text{SM,exp}} = \frac{\text{BR}(\pi\nu\nu)_{\text{SM}}}{\text{SES}} = \frac{\text{BR}(\pi\nu\nu)_{\text{SM}}}{\text{BR}(\pi\pi\pi)} \frac{A_{\pi\nu\nu}}{A_{\pi\pi\pi}} (N_{\pi\pi\pi} \times D_0) \epsilon_{\text{trig}} \epsilon_{\text{RV}}$$

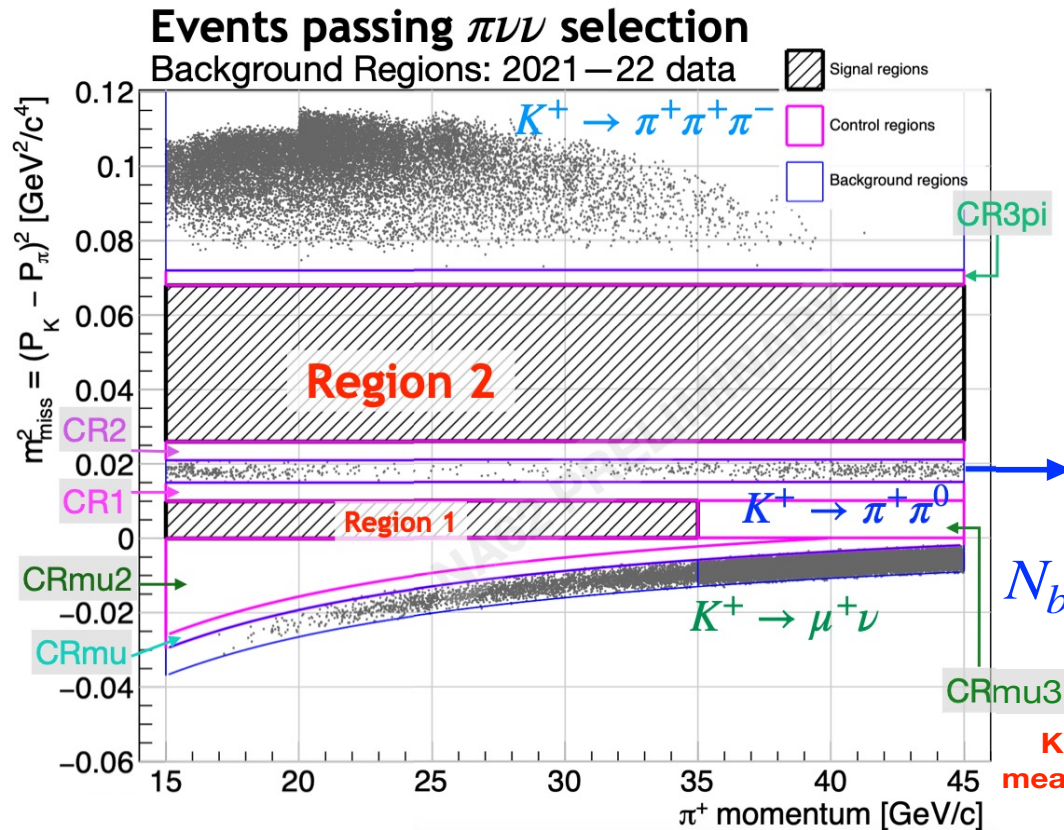
With respect to 2018 analysis:

- Improvements in energy reconstruction
- "Bayesian" $K^+ - \pi^+$ matching
- Increased signal yield
- More precise ϵ_{trig} and ϵ_{RV} evaluation



[Random veto (RV): efficiency loss due to beam activity]

Background evaluation (2021-2022 data)



Backgrounds from kinematic misconstruction tails in m_{miss}^2

Number of events passing signal selection in background region

$$N_{bg} = N_{bkgR} \cdot f_{tail} = N_{bkgR} \cdot \frac{N_{SR}^{CS}}{N_{bkgR}^{CS}}$$

Kinematic tail fraction: measured in control sample

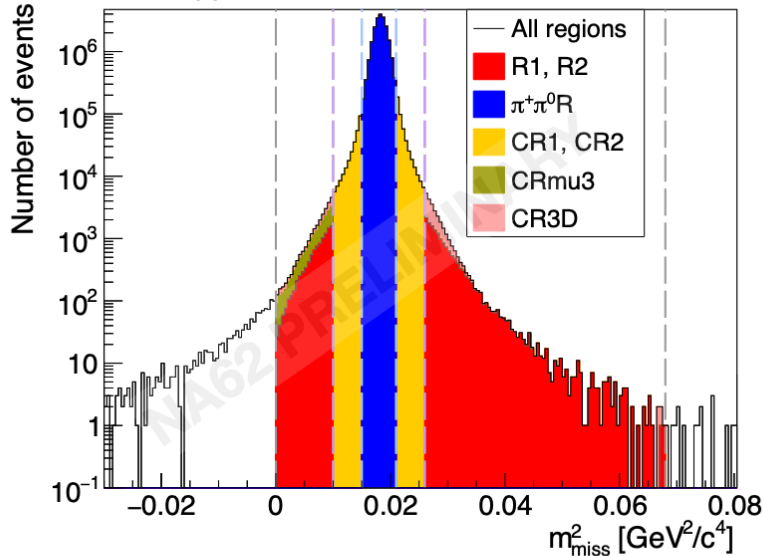
Control sample events in Signal Regions

Control sample events in Background Region

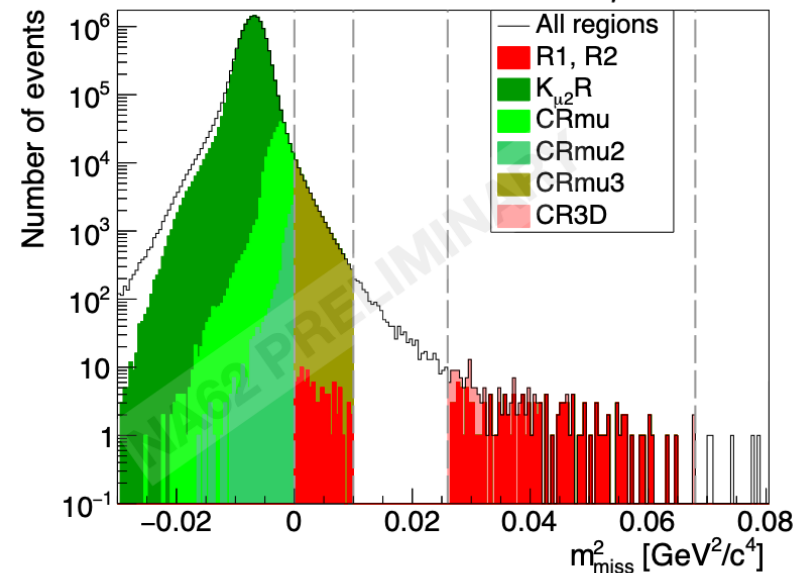
Backgrounds: kaon decays (2021-2022 data)



control sample of $K^+ \rightarrow \pi^+ \pi^0$ events with $\pi^0 \rightarrow \gamma\gamma$ and 2 photons detected in LKr:



control sample of $K^+ \rightarrow \mu^+ \nu$ events with RICH PID= π^+ and Calo PID= μ^+ :



- <1% contribution from $K^+ \rightarrow \mu^+ \nu$ followed by $\mu^+ \rightarrow e^+ \nu \nu$.

$$N_{bg}(K^+ \rightarrow \pi^+ \pi^0 (\gamma)) = 0.83 \pm 0.05$$

$$N_{bg}(K^+ \rightarrow \mu^+ \nu) = 0.9 \pm 0.2$$

$K^+ \rightarrow \pi^+ \pi^0 \gamma$: included with “kinematic tails” estimation

$K^+ \rightarrow \mu^+ \nu \gamma$: not included in “kinematic tails” estimation if γ overlaps μ^+ at LKr (leading to misID as π^+)

- Suppression: based on $(P_K - P_\mu - P_\gamma)^2$ and E_γ with $\gamma =$ LKr cluster (mis)associated to muon.
 - Necessary for 2021–22 data, since Calorimetric PID degraded at higher intensities.
- Estimation: min. Bias data control sample with signal in MUV3 : $N_{bg}(K^+ \rightarrow \mu^+ \nu \gamma) = 0.8 \pm 0.4$
- Validation: data sample without $K^+ \rightarrow \mu^+ \nu \gamma$ veto and PID = “less pion-like” (Calo BDT bins below π^+ bin).

Backgrounds: upstream (2021-2022 data)

$$N_{bg} = \sum_i N_i f_{cda} P_i^{match}$$

N Upstream Reference Sample:
signal selection but invert CDA cut (CDA>4mm)

f_{cda} Scaling factor : bad cda \rightarrow good cda

P_{match} Probability to pass $K^+ - \pi^+$ matching

Upstream reference sample contains all known upstream mechanisms.

- N provides normalisation.

f_{CDA} depends only on geometry.

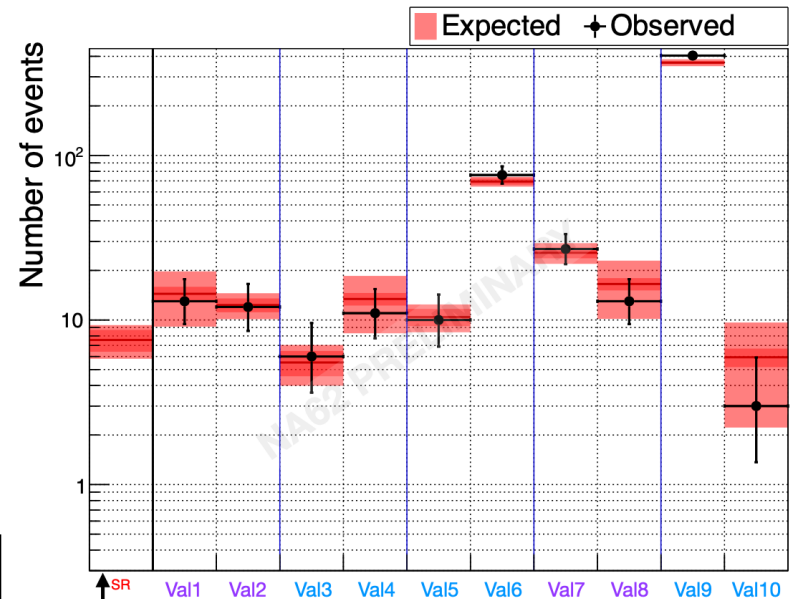
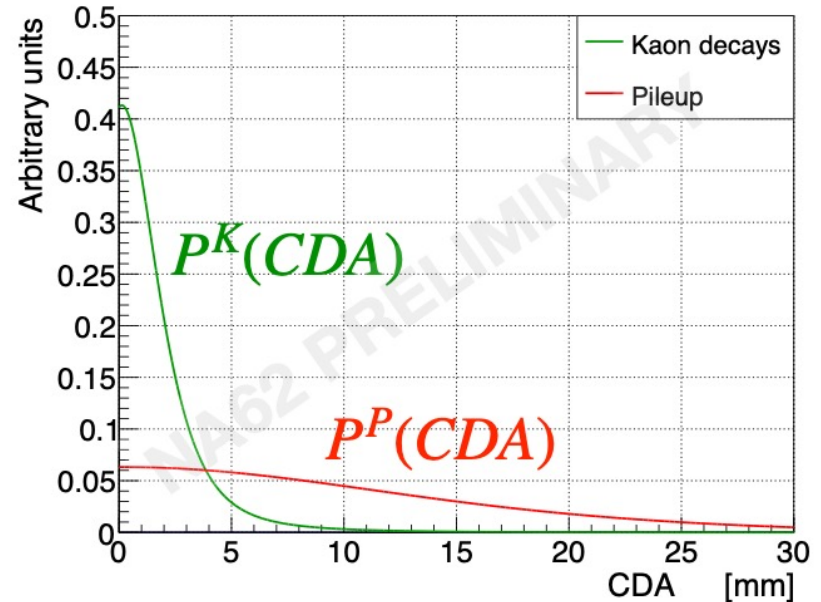
P_{match} depends on $(\Delta T_+, N_{GTK})$.

(Time matching, intensity/pileup estimator)

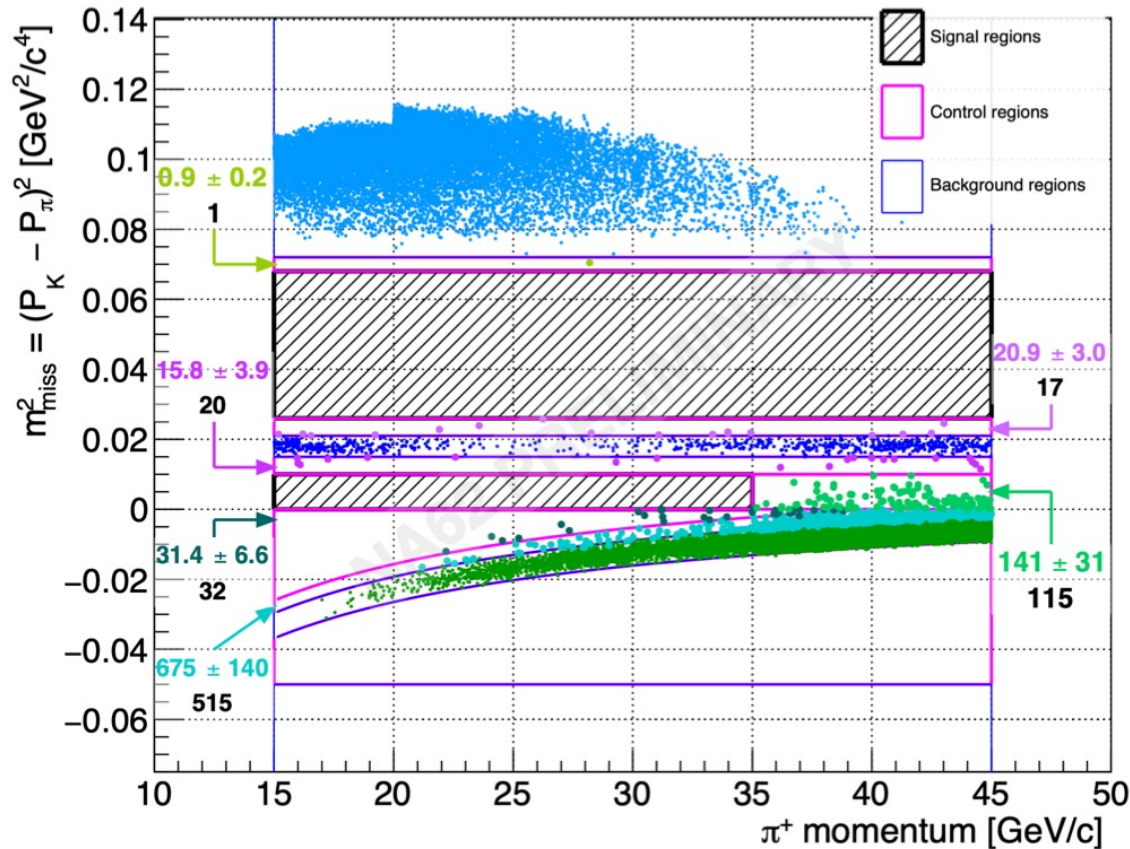
Invert & loosen upstream vetos to enrich with different mechanisms:

- Interaction-enriched: Val1,2,7,8
- Accidental-enriched: Val3,4,5,6,9,10
- All independent.

$$N_{bg}(\text{Upstream}) = 7.4^{+2.1}_{-1.8}$$



Background evaluation (2021-22 data)

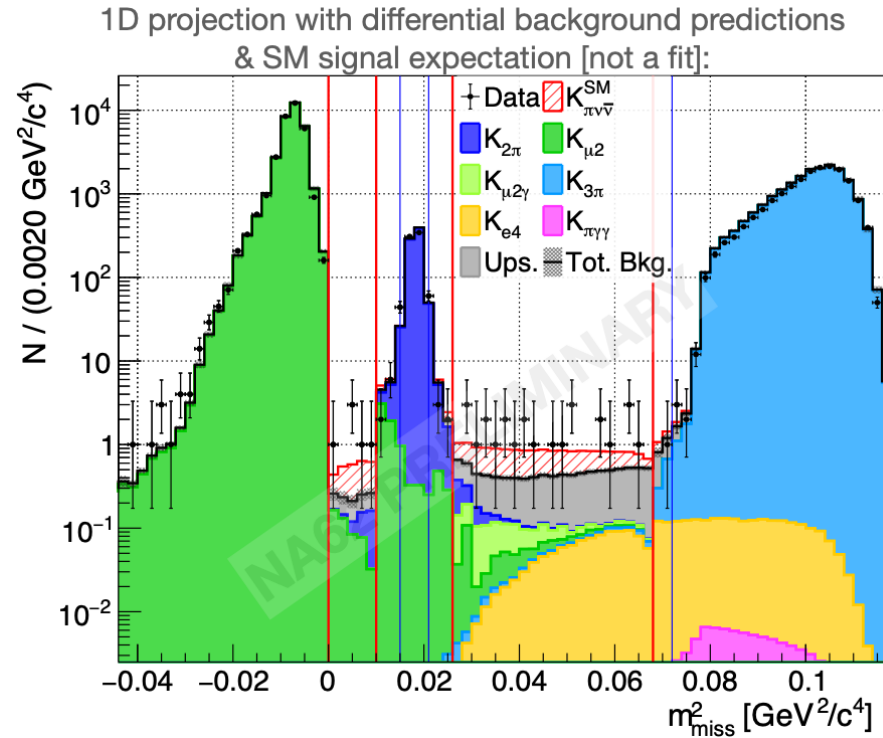
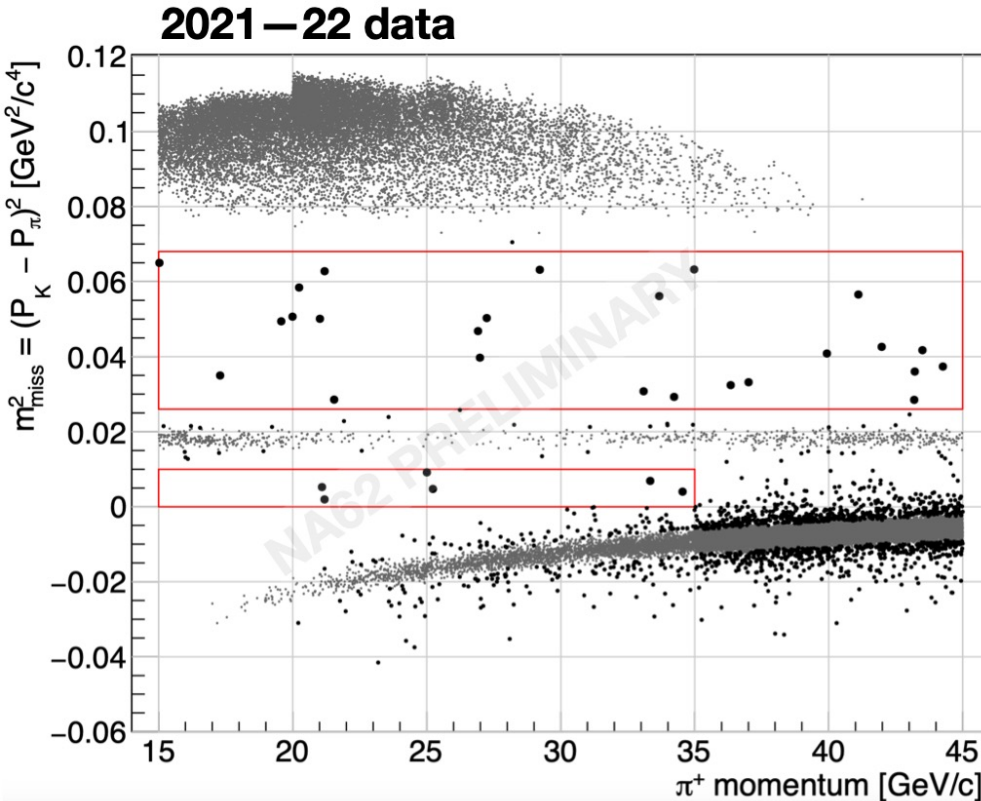


$K^+ \rightarrow \pi^+\pi^0(\gamma)$	0.83 ± 0.05
$K^+ \rightarrow \pi^+\pi^0$	0.76 ± 0.04
$K^+ \rightarrow \pi^+\pi^0\gamma$	0.07 ± 0.01
$K^+ \rightarrow \mu^+\nu(\gamma)$	1.70 ± 0.47
$K^+ \rightarrow \mu^+\nu$	0.87 ± 0.19
$K^+ \rightarrow \mu^+\nu\gamma$	0.82 ± 0.43
$K^+ \rightarrow \pi^+\pi^+\pi^-$	0.11 ± 0.03
$K^+ \rightarrow \pi^+\pi^-e^+\nu$	$0.89^{+0.34}_{-0.28}$
$K^+ \rightarrow \pi^0\ell^+\nu$	< 0.001
$K^+ \rightarrow \pi^+\gamma\gamma$	0.01 ± 0.01
Upstream	$7.4^{+2.1}_{-1.8}$
Total	$11.0^{+2.1}_{-1.9}$

Sensitivity for $\text{BR} \sim \sqrt{S + B}/S = 0.5$

- Similar but improved with respect to 2018 analysis for same amount of data.

Signal regions (2021-22 data)



Expected SM signal: $N_{\pi\nu\bar{\nu}}^{SM} \approx 10$

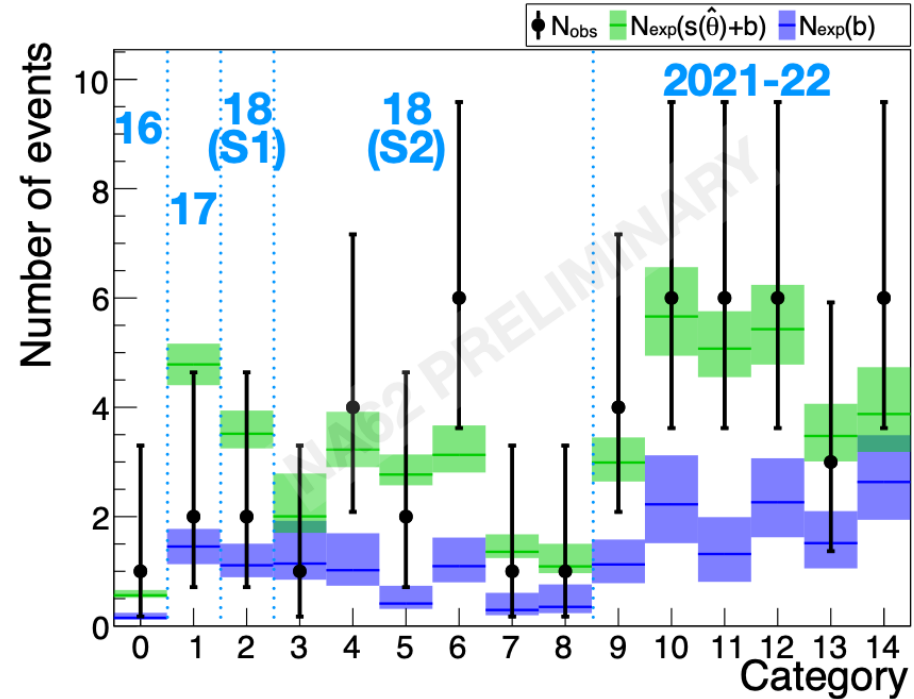
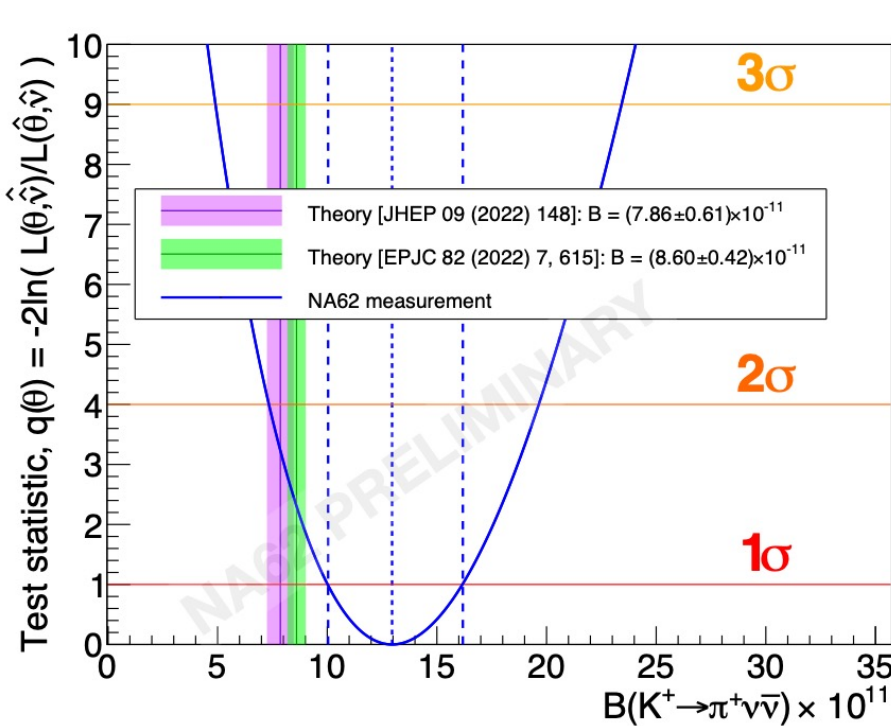
Expected background: $N_{bg} = 11.0^{+2.1}_{-1.9}$

Observed: $N_{obs} = 31$

$$\mathcal{B}_{21-22}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (16.0^{+5.0}_{-4.5}) \times 10^{-11} = (16.0 \text{ }^{+4.8}_{-4.2})_{stat} \text{ }^{+1.4}_{-1.3})_{syst} \times 10^{-11}$$

Combining NA62 results: 2016-22

Integrating 2016–22 data: $N_{bg} = 18_{-2}^{+3}$, $N_{obs} = 51$



Background-only hypothesis **p-value** = $2 \times 10^{-7} \Rightarrow$ **significance** $Z > 5$

$$B_{16-22}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (13.0_{-2.9}^{+3.3}) \times 10^{-11}$$

$$B_{16-22}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (13.0 \left(\begin{smallmatrix} +3.0 \\ -2.7 \end{smallmatrix} \right)_{stat} \left(\begin{smallmatrix} +1.3 \\ -1.2 \end{smallmatrix} \right)_{syst}) \times 10^{-11}$$

$K^+ \rightarrow \pi^+ \nu \bar{\nu}$ result in context

BNL E787/E949 experiment

[Phys.Rev.D 79 (2009) 092004]

$$\mathcal{B}_{\pi\nu\bar{\nu}}^{16-18} = (10.6^{+4.1}_{-3.5}) \times 10^{-11}$$

[JHEP 06 (2021) 093]

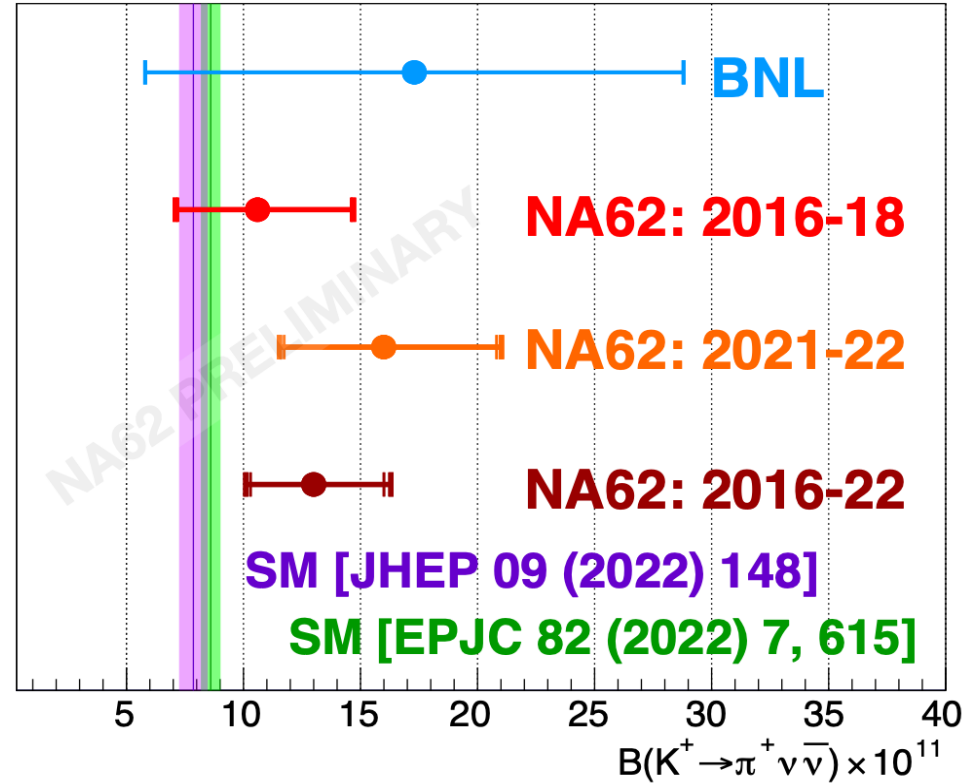
$$\mathcal{B}_{\pi\nu\bar{\nu}}^{21-22} = (16.0^{+5.0}_{-4.5}) \times 10^{-11}$$

$$\mathcal{B}_{\pi\nu\bar{\nu}}^{16-22} = (13.0^{+3.3}_{-2.9}) \times 10^{-11}$$

NA62 results are consistent
Central value moved up

Fractional uncertainty decreased:
40% to 25%

New: NA62 result from 2021-22 data
[CERN EP Seminar 24/9/24, paper in preparation]

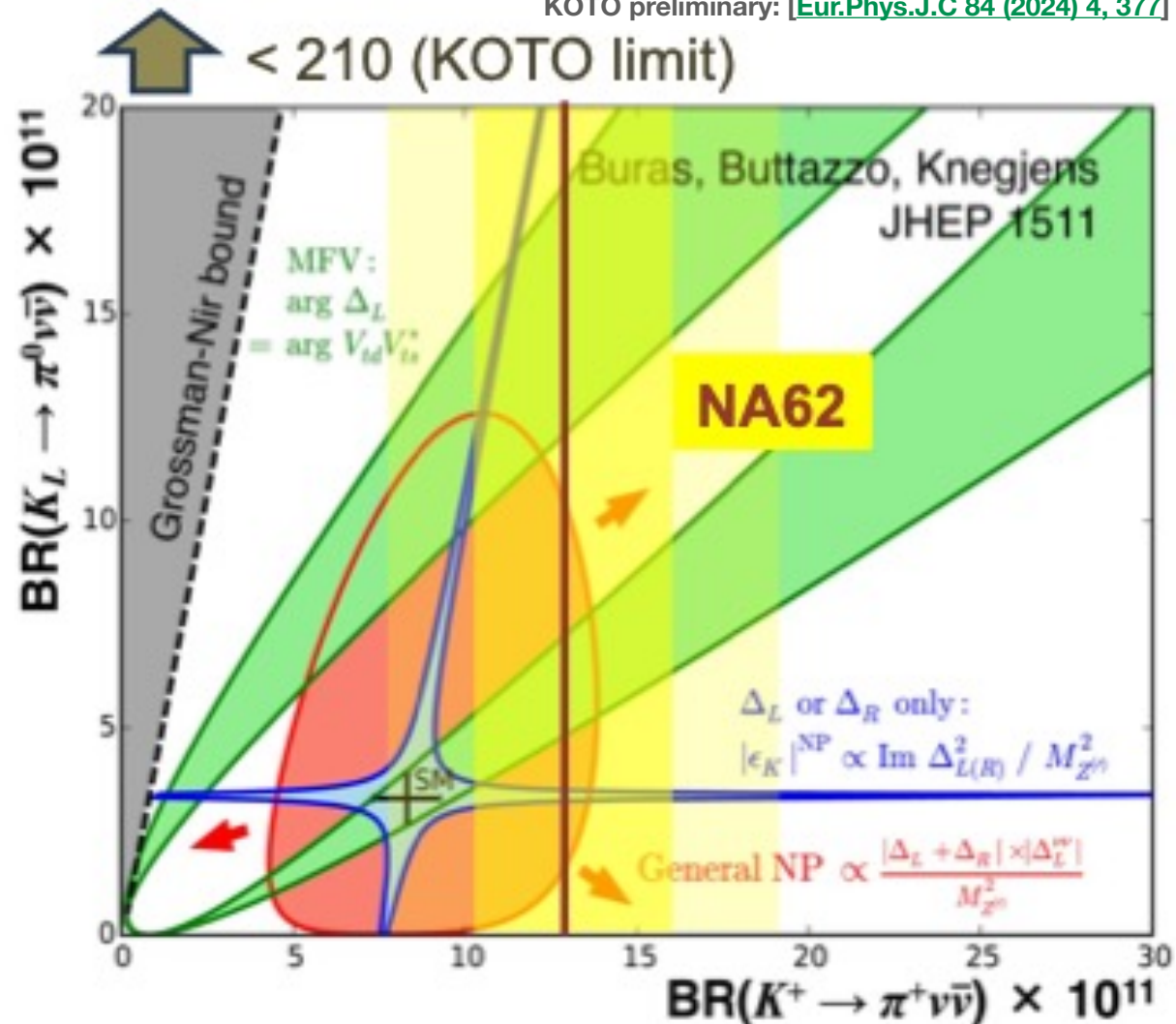


**Rarest decay process
ever measured !**

Implications of $K^+ \rightarrow \pi^+ \nu \bar{\nu}$

Part of parameter space already ruled out

KOTO preliminary: [\[Eur.Phys.J.C 84 \(2024\) 4, 377\]](#)



Fractional uncertainty: 25%
Still consistent with SM

Need full NA62 data-set
to clarify SM tension

Next target:
at least x3 improved
precision to match
parametric theoretical
uncertainty by LS3

2σ range : $[7.4 - 19.7] \times 10^{-11}$

$$\mathcal{B}_{\pi\nu\bar{\nu}}^{16-22} = (13.0_{-2.9}^{+3.3}) \times 10^{-11}$$

Anatomy of $K^+ \rightarrow \pi^+ \nu \bar{\nu}$

Kaon decays induced by scalar or tensor BSM operators

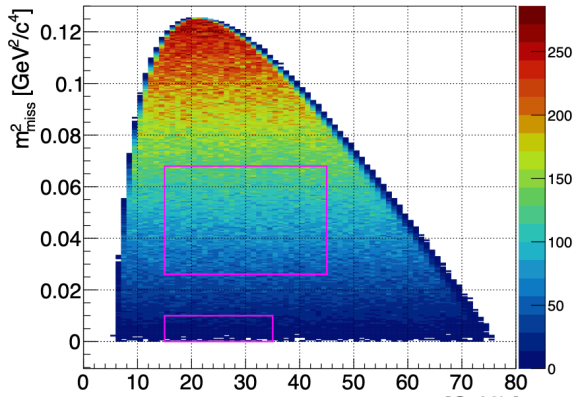
$$\text{BR}(K \rightarrow \pi \nu \bar{\nu}) = \text{BR}_{\text{SM}}(K \rightarrow \pi \nu \bar{\nu}) + \sum_j \text{BR}_{\text{LNV}}(K \rightarrow \pi \nu_i \nu_j)$$

$$\mathcal{B}(K^+ \rightarrow \pi^+ \nu \hat{\nu}) = J_V^{K^+} f_V^{K^+} + J_S^{K^+} f_S^{K^+} + J_T^{K^+} f_T^{K^+} \quad \text{J=current, f Wilson coeff}$$

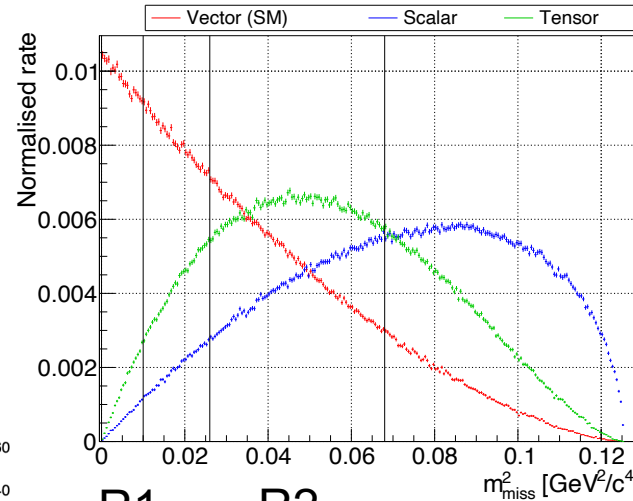
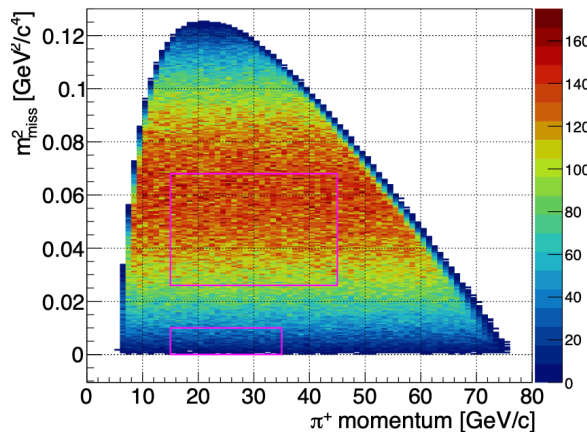
$$\mathcal{B}(K_L \rightarrow \pi^+ \nu \hat{\nu}) = J_V^{K_L} f_V^{K_L} + J_S^{K_L} f_S^{K_L} + J_T^{K^+} f_T^{K_L}$$

[JHEP 12 (2020)186,
arXiv:2405.06742,
Eur. Phys. J. C (2024) 84: 680]

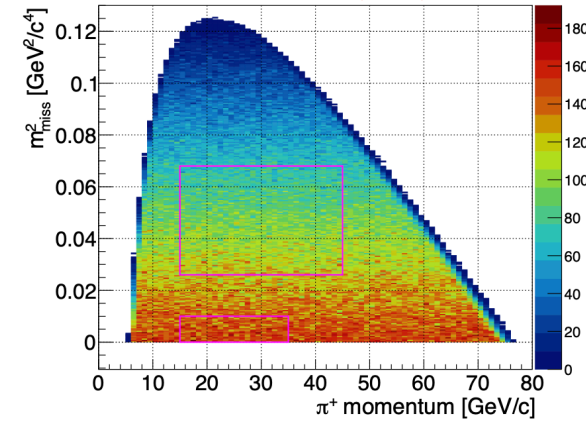
Scalar



Tensor



Vector (SM)



Probing 3-generation BSM

[Allwicher, Bordone, Isidori,
Piazza, Stanzione,
doi.org/10.48550/arXiv.2410.21444]

EFT with dimension-six semileptonic operators
built in terms of SM fields.

Minimally-broken $U(2)^5$ flavor symmetry acting
on the lightest two SM families.

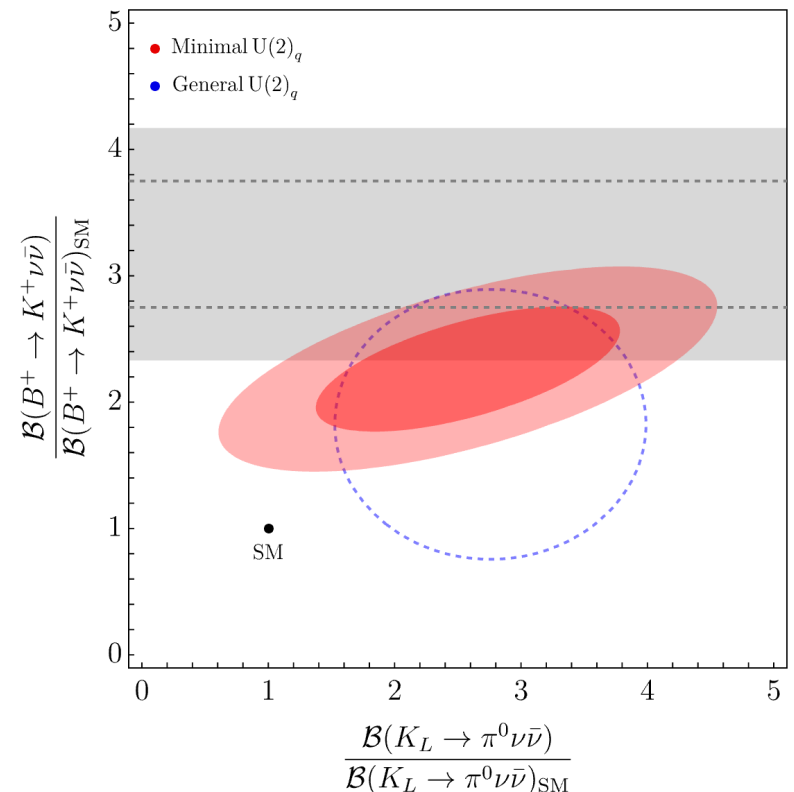
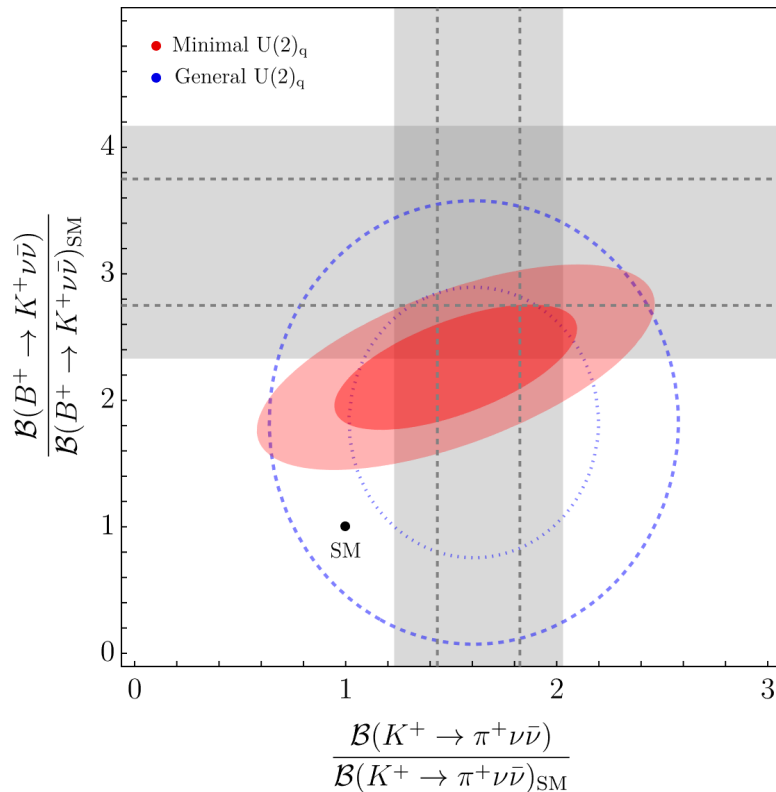
Reduce the number of relevant operators to 5

$$B(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (12.3 \pm 3.2) \times 10^{-11}$$

$$B(K_L \rightarrow \pi^0 \nu \bar{\nu}) = (6.7 \pm 2.2) \times 10^{-11}$$

$$\mathcal{B}(K^+ \rightarrow \pi^+ \nu \bar{\nu})^{\text{SM}} = (8.09 \pm 0.63) \times 10^{-11}$$
$$\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu})^{\text{SM}} = (2.58 \pm 0.30) \times 10^{-11}$$

(for comparison)

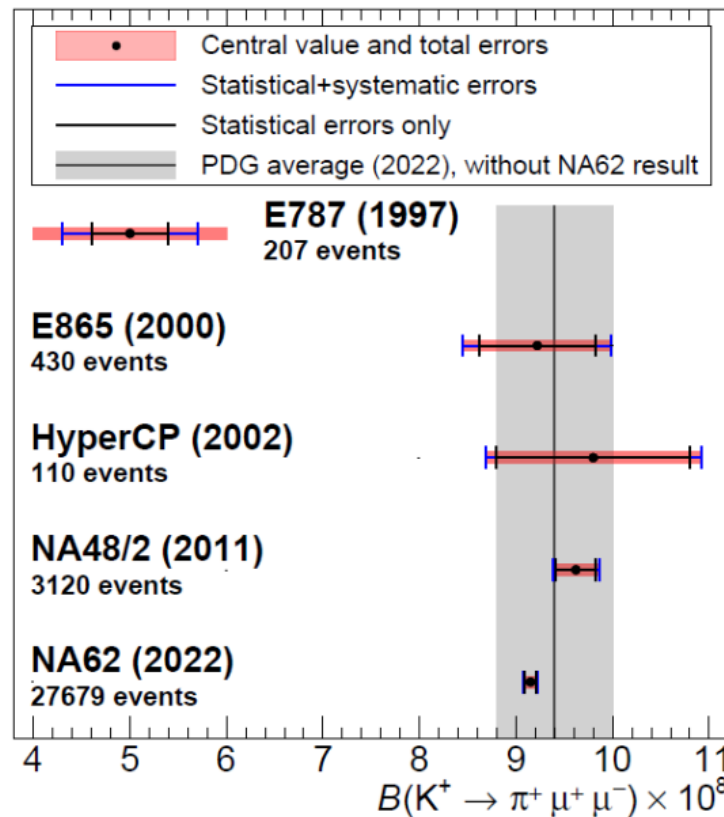
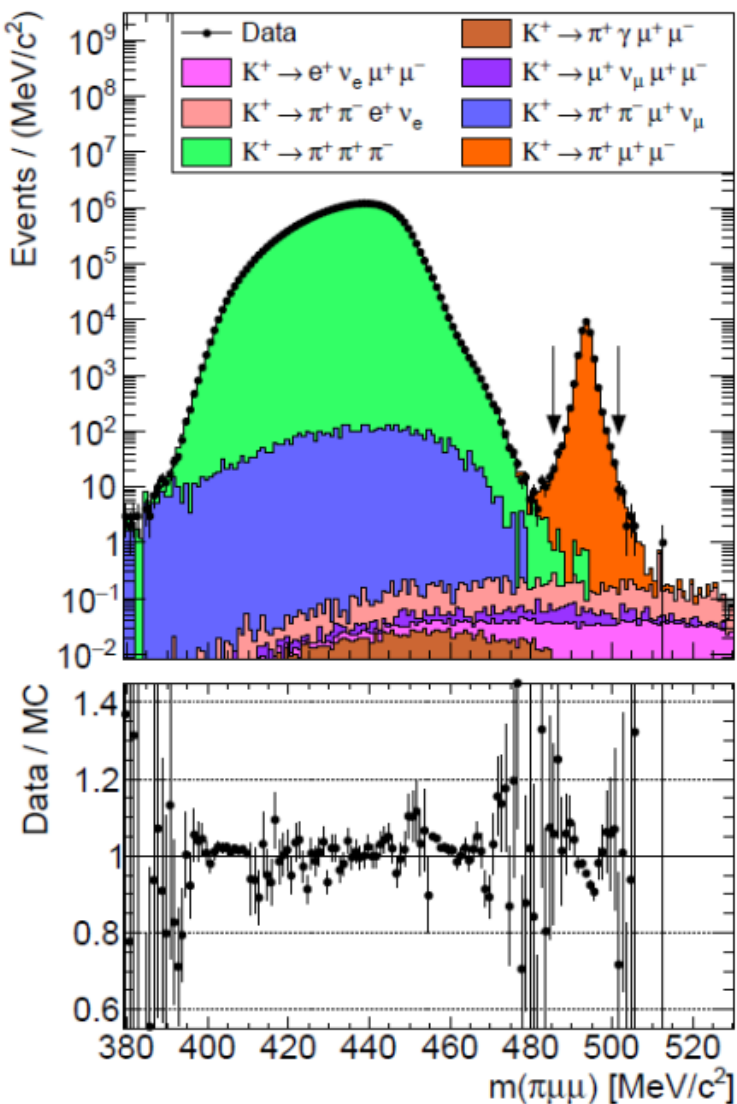


NA62: $K^+ \rightarrow \pi^+ \mu^+ \mu^-$

[doi:10.1007/JHEP11(2022)011]

FCNC decay, long-distance mediated by photon exchange

Together with electron channel tests LFU



$$BR(K^+ \rightarrow \pi^+ \mu^+ \mu^-) = (9.15 \pm 0.08) \times 10^{-8}$$

$$A_{FB} = \frac{\mathcal{N}(\cos \theta_{K\mu} > 0) - \mathcal{N}(\cos \theta_{K\mu} < 0)}{\mathcal{N}(\cos \theta_{K\mu} > 0) + \mathcal{N}(\cos \theta_{K\mu} < 0)} \quad \theta_{K\mu} \text{ between } K \text{ and } \mu^- \text{ in the } \mu\mu \text{ rest frame}$$

$$A_{FB} = (0.0 \pm 0.7) \times 10^{-2} \text{ @ 68\% CL}$$

NA62: $K^+ \rightarrow \pi^+ \mu^+ \mu^-$

$$W(z) = G_F M_K^2 (a + bz) + W^{\pi\pi}(z)$$

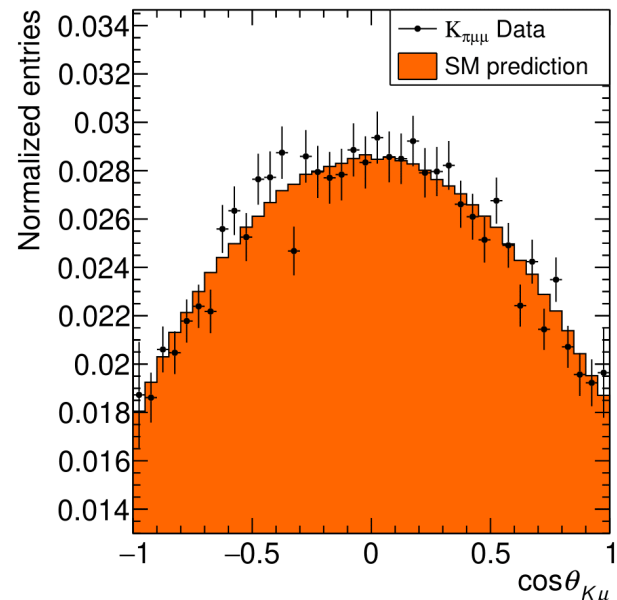
$$z = m(\mu^+ \mu^-)^2 / M_K^2$$

Measurement	$K_{\pi\mu\mu}$ candidates	$\mathcal{B}_{\pi\mu\mu} \times 10^8$
E787 [8]	207	$5.0 \pm 0.4_{\text{stat}} \pm 0.7_{\text{syst}} \pm 0.6_{\text{ext}} = 5.0 \pm 1.0$
E865 [9]	430	$9.22 \pm 0.60_{\text{stat}} \pm 0.49_{\text{syst}} = 9.22 \pm 0.77$
HyperCP [10]	110	$9.8 \pm 1.0_{\text{stat}} \pm 0.5_{\text{syst}} = 9.8 \pm 1.1$
NA48/2 [11]	3120	$9.62 \pm 0.21_{\text{stat}} \pm 0.11_{\text{syst}} \pm 0.07_{\text{ext}} = 9.62 \pm 0.25$
NA62, this result	27679	$9.15 \pm 0.06_{\text{stat}} \pm 0.03_{\text{syst}} \pm 0.04_{\text{ext}} = 9.15 \pm 0.08$

Table 2. Comparison with the previous measurements of the $K_{\pi\mu\mu}$ branching fraction.

Measurement	Signal candidates	a_+	b_+	$\rho(a_+, b_+)$
E865, $K_{\pi ee}$ [14]	10300	-0.587 ± 0.010	-0.655 ± 0.044	—
NA48/2, $K_{\pi ee}$ [15]	7253	-0.578 ± 0.016	-0.779 ± 0.066	-0.913
NA48/2, $K_{\pi\mu\mu}$ [11]	3120	-0.575 ± 0.039	-0.813 ± 0.145	-0.976
NA62, $K_{\pi\mu\mu}$, this result	27679	-0.575 ± 0.013	-0.722 ± 0.043	-0.972

Table 3. Comparison with the previous measurements of the $K^\pm \rightarrow \pi^\pm \ell^+ \ell^-$ form factor parameters. The E865 $K_{\pi ee}$ measurement [14] does not provide the systematic uncertainties, nor the correlation coefficient of the form factor parameters.



A lot more data available, and coming.

Uncertainties are stat-related

Also, electron channel to come

	δa_+	δb_+	$\delta \mathcal{B}_{\pi\mu\mu} \times 10^8$	$\delta A_{\text{FB}} \times 10^2$
<i>Statistical uncertainty</i>	0.012	0.040	0.06	0.7
Trigger efficiency	0.002	0.008	0.02	0.1
Reconstruction and particle identification	0.002	0.007	0.02	0.1
Size of the simulated $K_{\pi\mu\mu}$ sample	0.002	0.007	0.01	0.1
Beam and accidental activity simulation	0.001	0.002	0.01	—
Background	0.001	0.001	—	—
<i>Total systematic uncertainty</i>	0.003	0.013	0.03	0.2
$K_{3\pi}$ branching fraction	0.001	0.003	0.04	—
$K_{\pi\mu\mu}$ radiative corrections	0.003	0.009	0.01	0.2
Parameters α_+ and β_+	0.001	0.006	—	—
<i>Total external uncertainty</i>	0.003	0.011	0.04	0.2
<i>Total uncertainty</i>	0.013	0.043	0.08	0.7

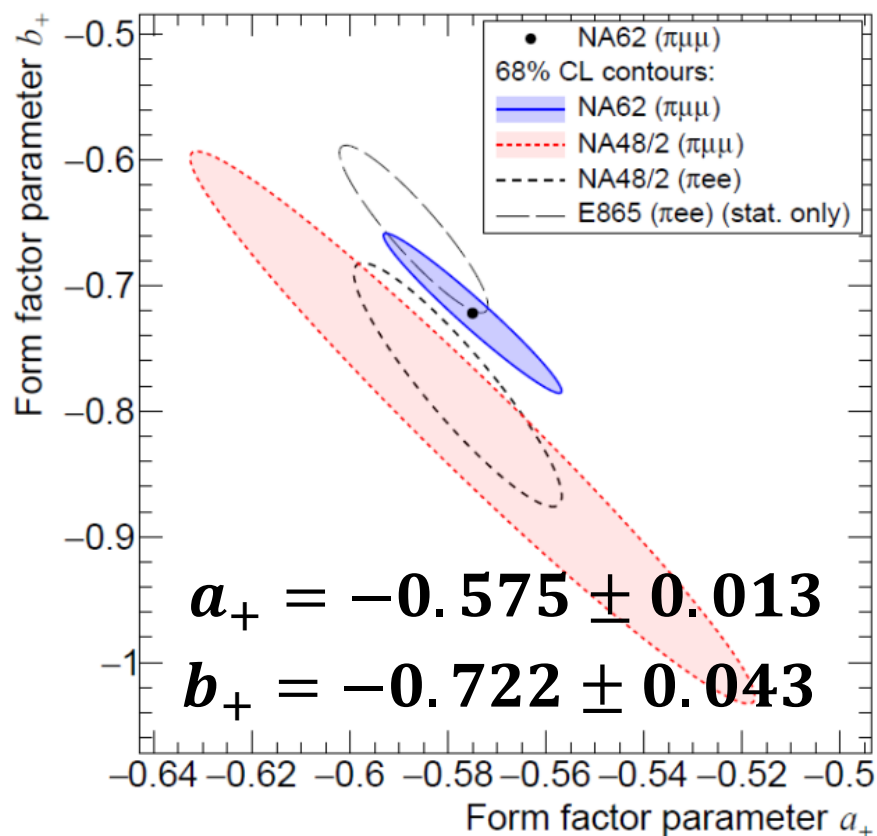
Table 1. Summary of uncertainties.

NA62: $K^+ \rightarrow \pi^+ \mu^+ \mu^-$

$$W(z) = G_F M_K^2 (a + bz) + W^{\pi\pi}(z)$$

$$z = m(\mu^+ \mu^-)^2 / M_K^2$$

[JHEP09(2022)148]

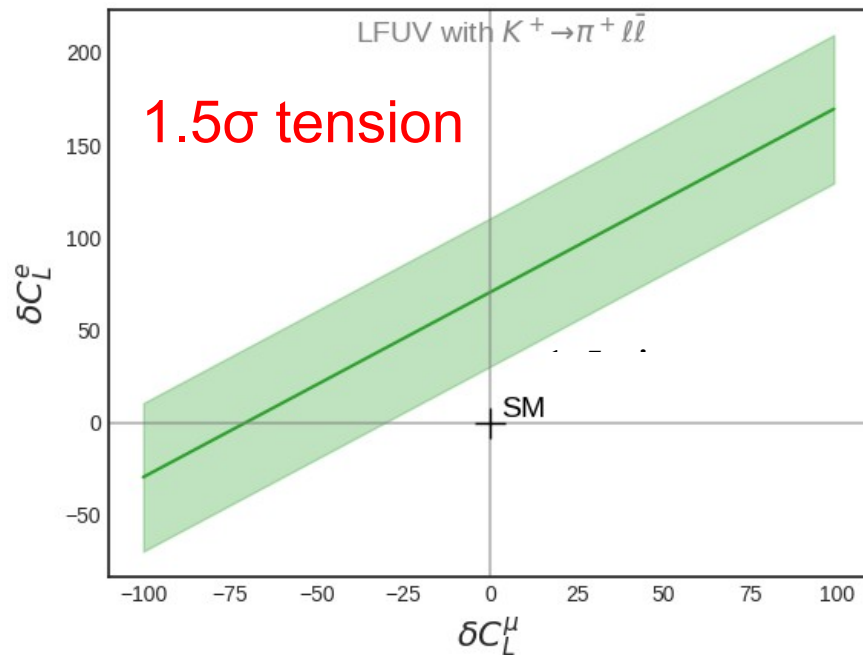


[doi:10.1007/JHEP11(2022)011]

$$a_+^{\mu\mu} - a_+^{ee} = -\sqrt{2} \operatorname{Re} [V_{td} V_{ts}^* (C_9^\mu - C_9^e)]$$

Sensitive to LFUV in SD contributions

[PRD93 (2016) 074038]



Kaons at JPARC

KEK, NDA, Osaka, Yamagata,
Jeonbuk, Korea, Pusan, NTU, Chicago

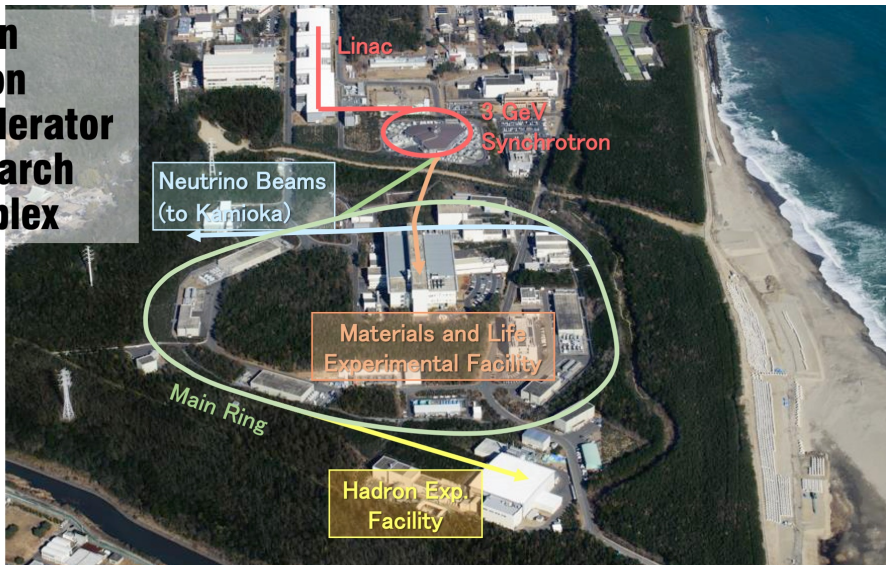


30 GeV proton from Main Ring of J-PARC

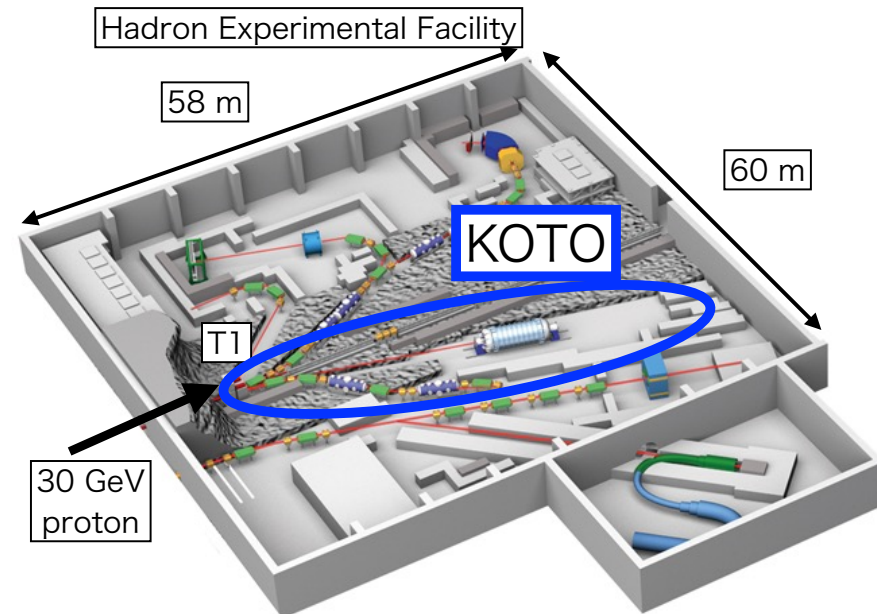
Slow extraction : 2-s spill / 4.2-s cycle

Beam power : 82 kW as of June 2024

**Japan
Proton
Accelerator
Research
Complex**



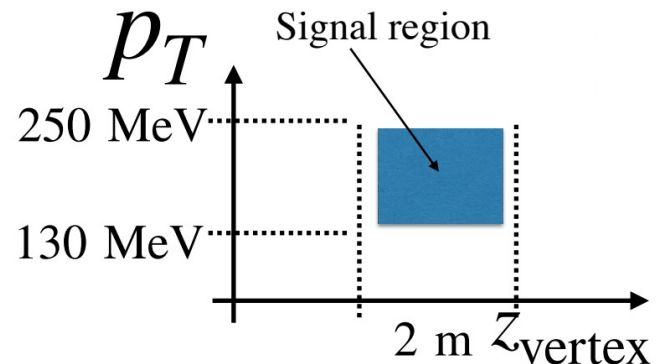
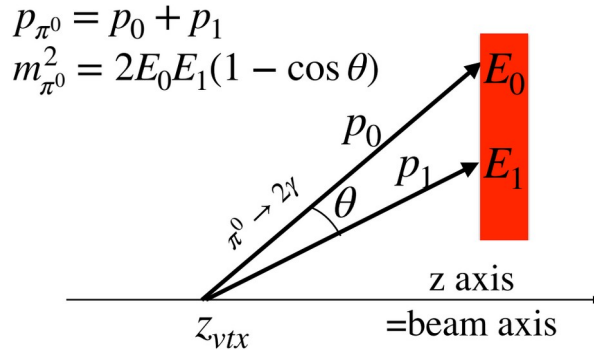
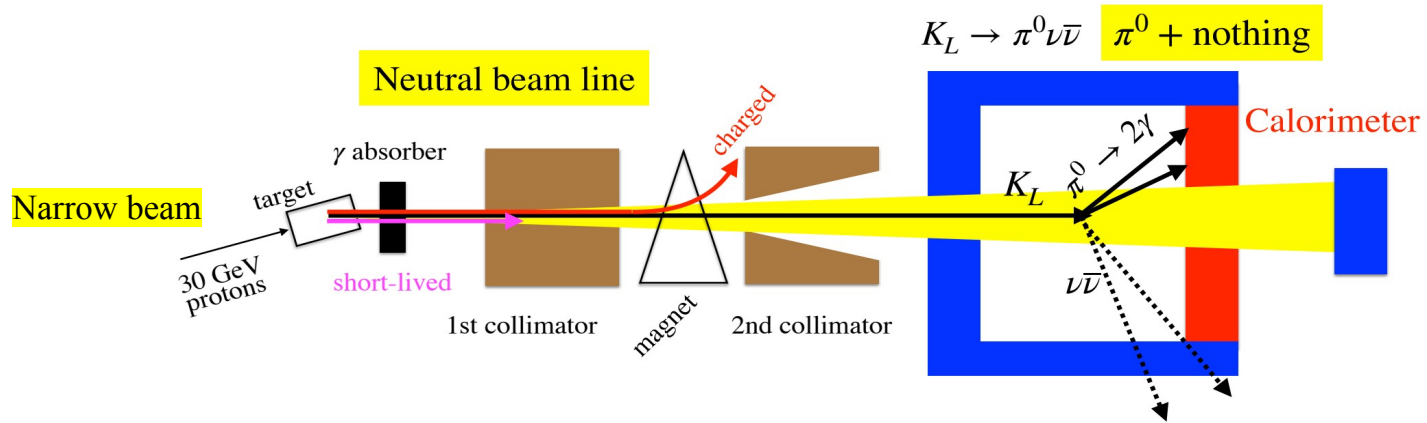
- T1 target at Hadron experimental facility
- Beam extraction angle : 16°
- 20-m beamline + KOTO Detector



KOTO concept

Key points of KOTO experiment:

- 1) K_L pencil beam, only K_L direction known
 → only PT information can be used (to reject $K_L \rightarrow \gamma\gamma$)
- 2) Z_{vtx} reconstructed assuming 2 clusters from π^0 decay
- 3) Charged and photon vetoes to reject background



KOTO result of 2021 data analysis

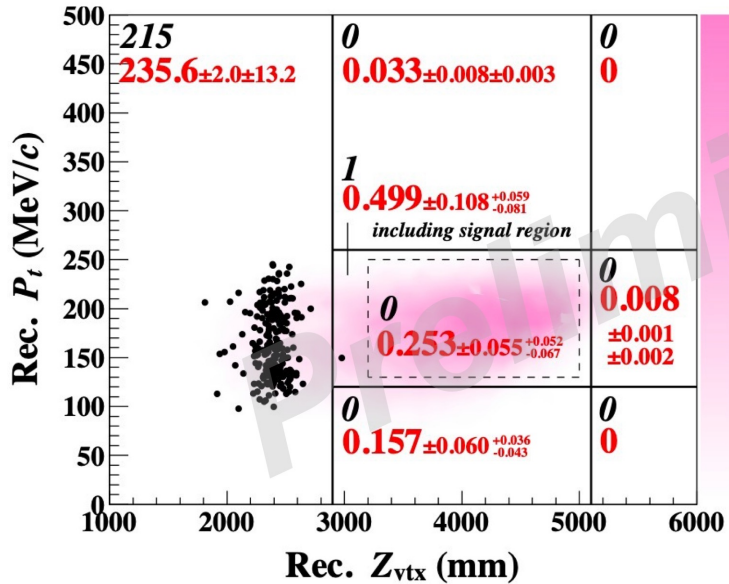
KEK, NDA, Osaka, Yamagata,
Jeonbuk, Korea, Pusan, NTU, Chicago



Final PT vs Z plot

Black: observed
Red: expected BG
Contour: signal MC

Single Event Sensitivity =
 $(9.26 \pm 0.03_{\text{stat}} \pm 0.75_{\text{syst}}) \times 10^{-10}$



$N_{\text{observed}} = 0$

$BR(K_L \rightarrow \pi^0 \nu \bar{\nu}) < 2.1 \times 10^{-9}$ (90% C.L.)

We will submit the paper on this result soon.

Obtained the world best limit.

List of the backgrounds

Source	Estimated value
Upstream π^0	0.060 ± 0.046 (stat.) ± 0.007 (syst.)
$K_L \rightarrow 2\pi^0$	0.059 ± 0.022 (stat.) $^{+0.051}_{-0.060}$ (syst.)
K^\pm	0.042 ± 0.014 (stat.) $^{+0.004}_{-0.029}$ (syst.)
Scattered and halo K_L ($K_L \rightarrow 2\gamma$)	0.045 ± 0.010 (stat.) ± 0.006 (syst.)
Hadron cluster BG	0.024 ± 0.004 (stat.) ± 0.006 (syst.)
η production in CV	0.023 ± 0.010 (stat.) ± 0.005 (syst.)
Sum	0.253 ± 0.055 (stat.) $^{+0.052}_{-0.067}$ (syst.)

MC statistics

Statistics of the control data for inefficiency evaluation

Aim to reach SM sensitivity by 2027

Rare kaon decays after 2030

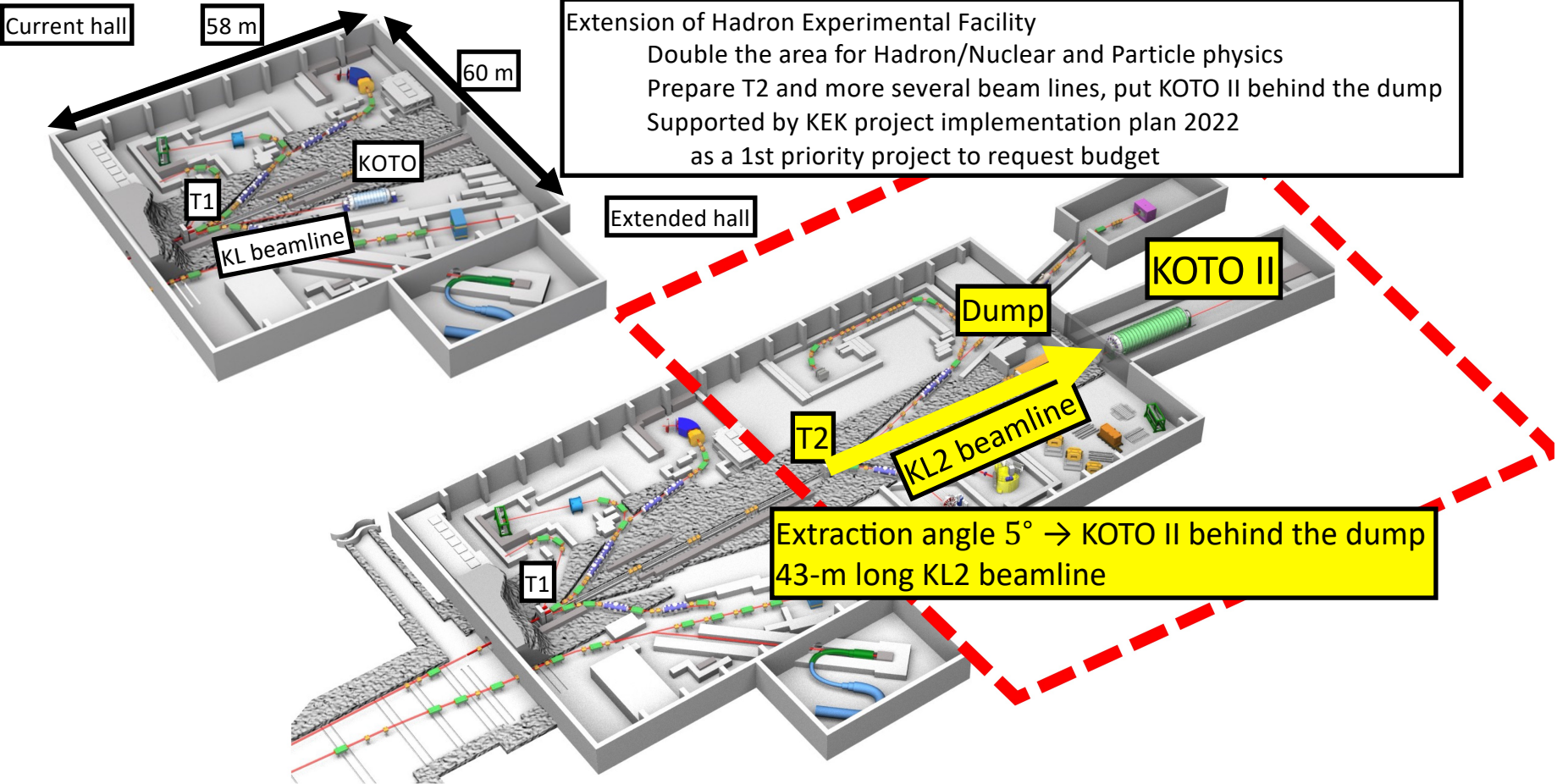
Unfortunately, HIKE (high-intensity kaons) at CERN was not approved

CERN: LHCb (K_S)



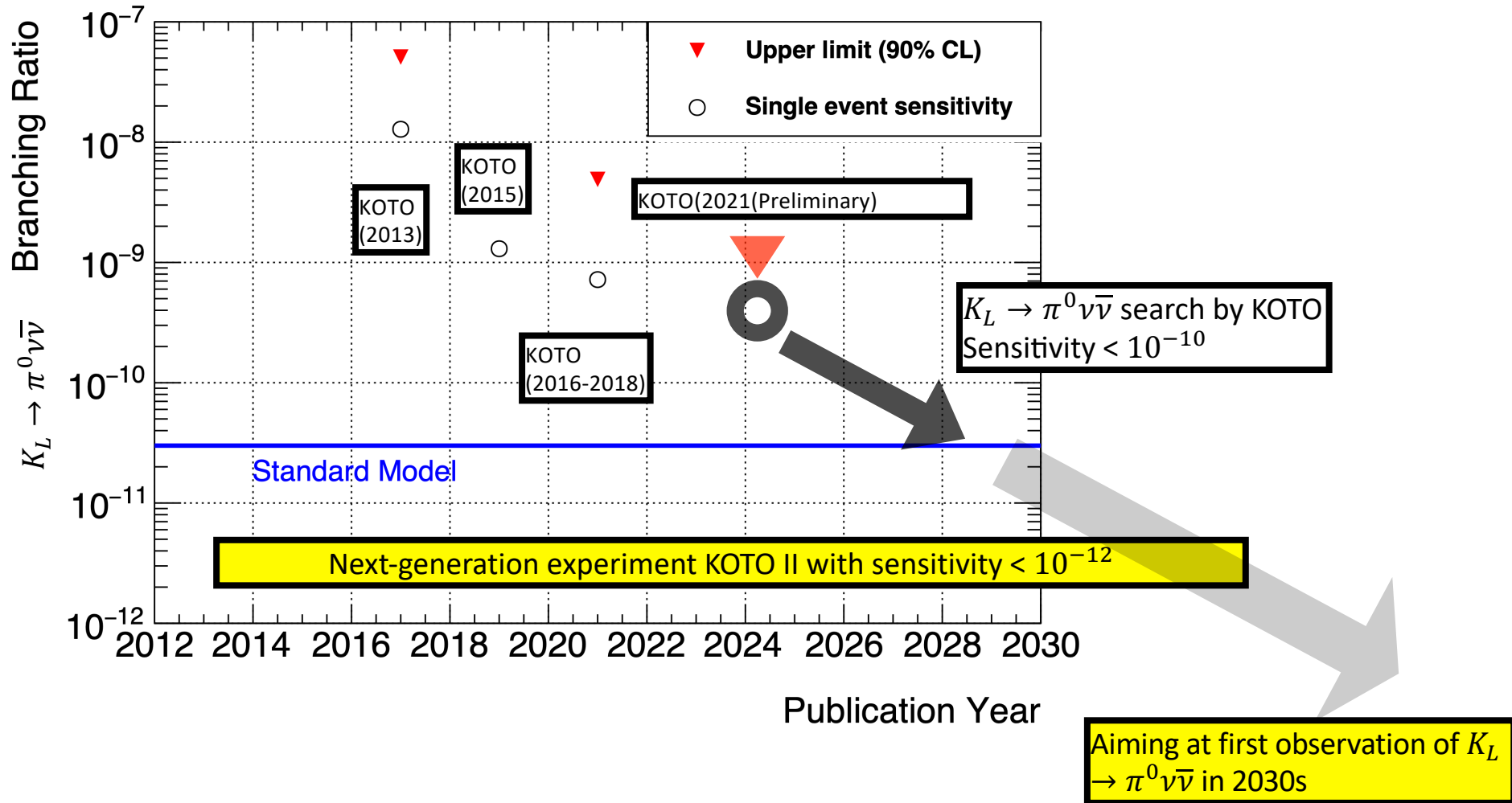
JPARC: KOTO-II (K_L)

KOTO-II and Extension of J-PARC hadron hall



Prospects for $K^0 \rightarrow \pi^0 \nu \bar{\nu}$

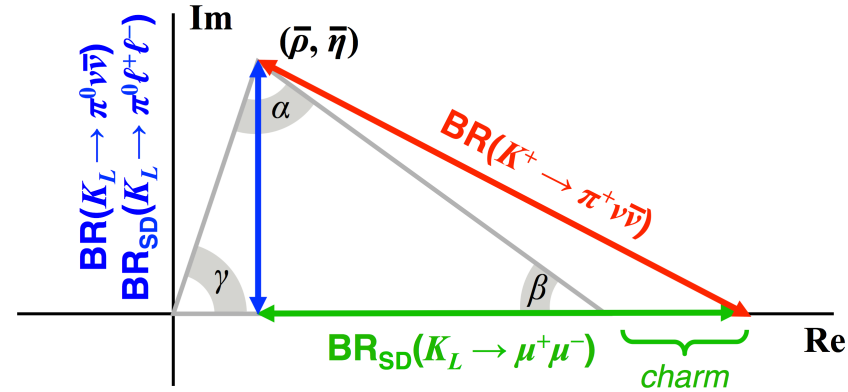
KEK, NDA, Osaka, Yamagata,
Jeonbuk, Korea, Pusan, NTU, Chicago



Aim to collect O(50) with B/S=1 events in 2030s

$K_L \rightarrow \pi^0 \ell^+ \ell^-$

$K_L \rightarrow \pi^0 \ell^+ \ell^-$ CPV amplitude constrains UT η



Contributions from long-distance physics

- SD CPV amplitude: γ/Z exchange
- LD CPC amplitude from 2γ exchange
- LD indirect CPV amplitude: $K_L \rightarrow K_S$

• $K_S \rightarrow \pi^0 \ell^+ \ell^-$ will help reducing theoretical uncertainties, measure $|a_S|$

- measured NA48/1 with limited statistics
- planned by LHCb Upgrade

• $K_L \rightarrow \pi^0 \ell^+ \ell^-$ can be used to explore helicity suppression in FCNC decays, give unique access to SD BSM effects in the photon coupling via the tau loop

$$\mathcal{B}(K_L \rightarrow \pi^0 e^+ e^-) = 3.54^{+0.98}_{-0.85} \left(1.56^{+0.62}_{-0.49} \right) \times 10^{-11}$$

$$\mathcal{B}(K_L \rightarrow \pi^0 \mu^+ \mu^-) = 1.41^{+0.28}_{-0.26} \left(0.95^{+0.22}_{-0.21} \right) \times 10^{-11}$$

(2 sets of values corresponding to constructive (destructive) interference btw direct and indirect CP-violating contributions)

[arXiv:hep-ph/0404127, arXiv:hpe-ph/0404136, arXiv:hep-ph/0606081]
 [arXiv:0705.2025, arXiv:1812.00735, arXiv:1906.03046,
<https://indico.cern.ch/event/1196830/>]

Experimental bounds from KTeV:

$$\mathcal{BR}(K_L \rightarrow \pi^0 e^+ e^-) < 28 \times 10^{-11}$$

$$\mathcal{BR}(K_L \rightarrow \pi^0 \mu^+ \mu^-) < 38 \times 10^{-11}$$

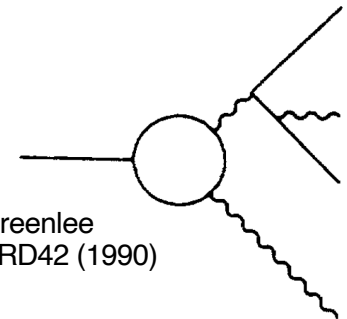
Phys. Rev. Lett. 93 (2004) 021805
 Phys. Rev. Lett. 84 (2000) 5279–5282

Main background: $K_L \rightarrow \ell^+ \ell^- \gamma \gamma$

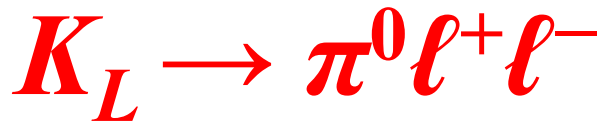
- Like $K_L \rightarrow \ell^+ \ell^- \gamma$ with hard bremsstrahlung

$$\mathcal{BR}(K_L \rightarrow e^+ e^- \gamma \gamma) = (6.0 \pm 0.3) \times 10^{-7} \quad E_\gamma^* > 5 \text{ MeV}$$

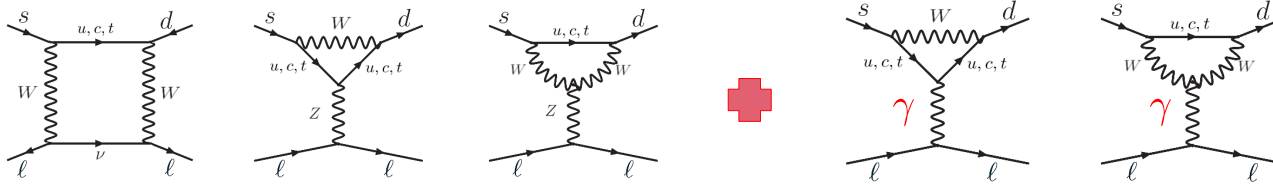
$$\mathcal{BR}(K_L \rightarrow \mu^+ \mu^- \gamma \gamma) = 10^{+8}_{-6} \times 10^{-9} \quad m_{\gamma\gamma} > 1 \text{ MeV}$$



Greenlee PRD42 (1990)



[D'Ambrosio, Iyer, Mahmoudi, Neshatpour
2206.14748, 2311.04878, 2404.03643]

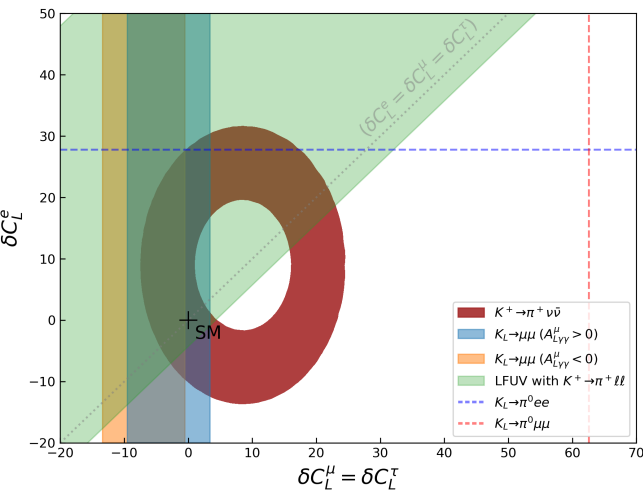


Access to
photon coupling
Can be used to explore helicity
suppression in FCNC decays,
give unique access to SD BSM
effects in γ coupling via τ loop

Lepton Flavour Universality Violation:

We assume NP contributions of the charged and neutral leptons related to each other by the $SU(2)_L$ gauge symmetry and we work in the chiral basis

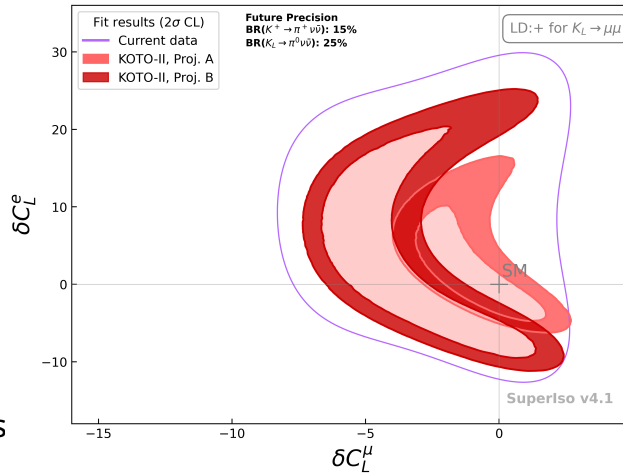
$$\delta C_L^\ell \equiv \delta C_9^\ell = -\delta C_{10}^\ell \quad \delta C_L^e \neq \delta C_L^\mu = \delta C_L^\tau$$



Bounds from individual observables:

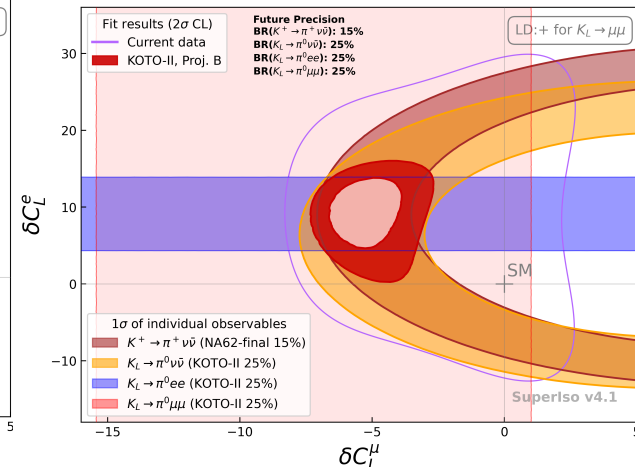
Coloured regions: 68% CL measurements

Dashed lines: 90% upper limits



Projection A

Observables already measured are kept, others assumed at their SM values, all with target precision of KOTO-II



Projection B

All measurements give current best-fit point with target precision of KOTO-II

Summary

Kaon physics: sensitive probe to both “heavy” and “light” new physics

Heavy New Physics probed via flavour physics observables

Light New Physics probed via production searches in K decays

NA62 new result on 2016-22 data:

$$\mathcal{B}_{16-22}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (13.0_{-2.9}^{+3.3}) \times 10^{-11} = \left(13.0 \left(\begin{array}{c} +3.0 \\ -2.7 \end{array} \right)_{\text{stat}} \left[\begin{array}{c} +1.3 \\ -1.2 \end{array} \right]_{\text{syst}} \right) \times 10^{-11}$$

First observation of this decay (significance $> 5 \sigma$)

Rarest particle decay ever observed !

NA62 will continue to take data until LS3: large stat will also more investigations

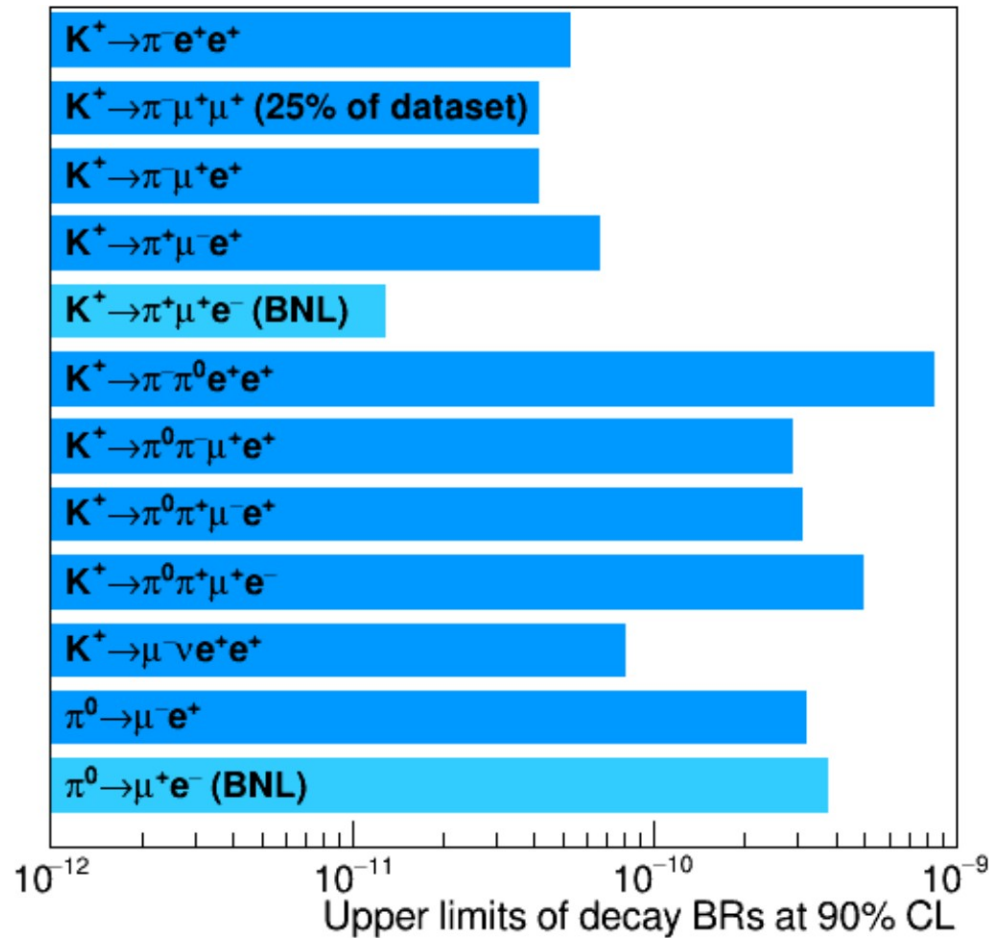
KOTO-II, the successor to KOTO, aims at first observation of $K_L \rightarrow \pi^0 \nu \nu$ by 2030s.

Increasingly important to combine K^+ and K_L measurements, and with other flavour measurements

Additional material

Other LFV / LNV results

LFV/LNV K^+ and π^0 decays, NA62 Run1



NA62: UL on BRs of LNV/LFV K^+ and π^0 decays $\sim O(10^{-9}-10^{-11})$