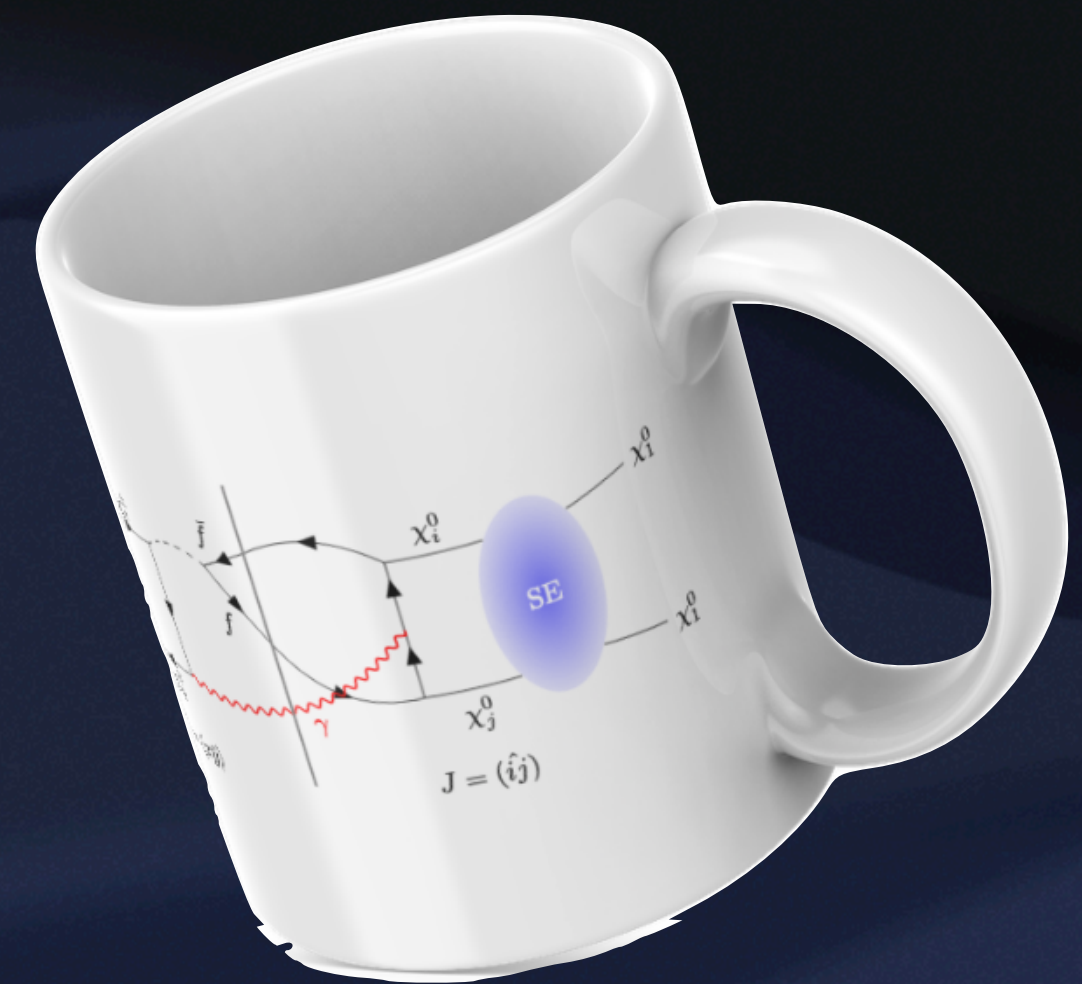


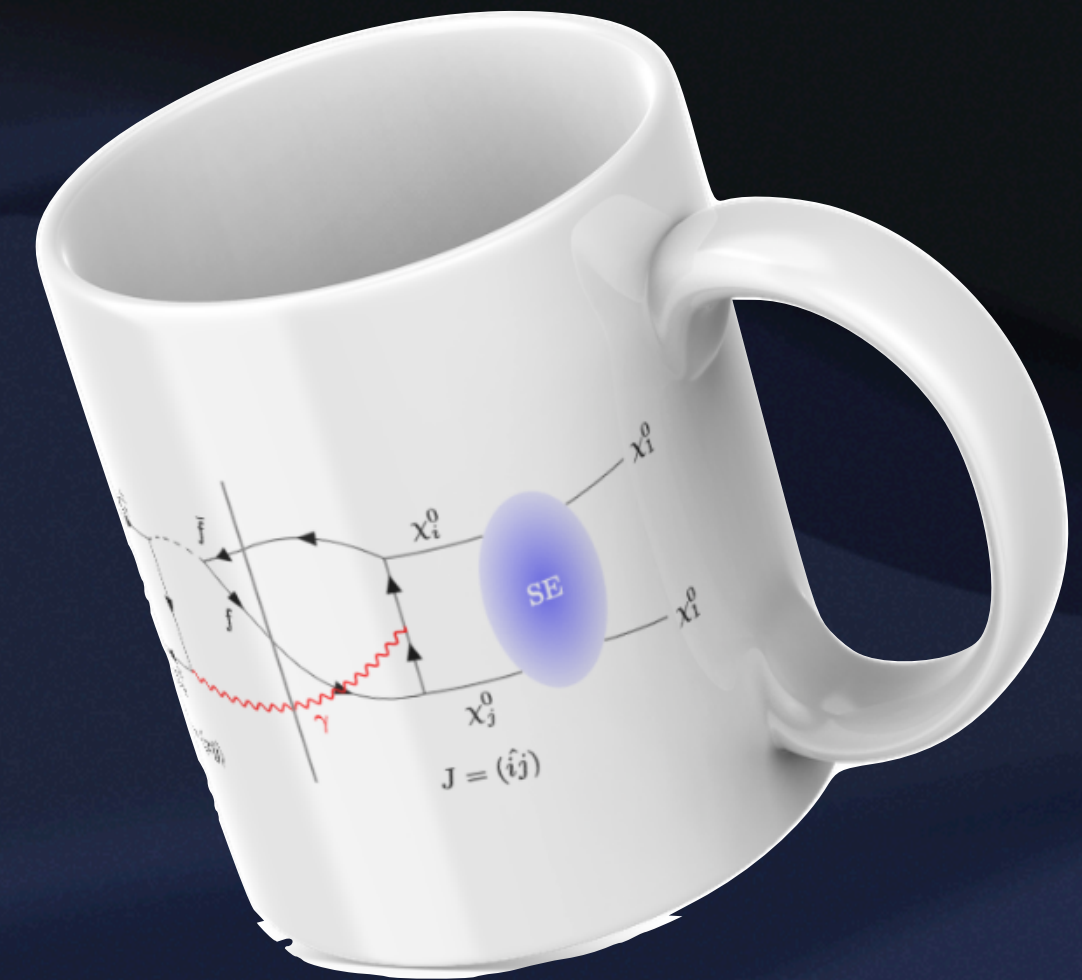
TBA

The Dark Matter Landscape
MITP 2024



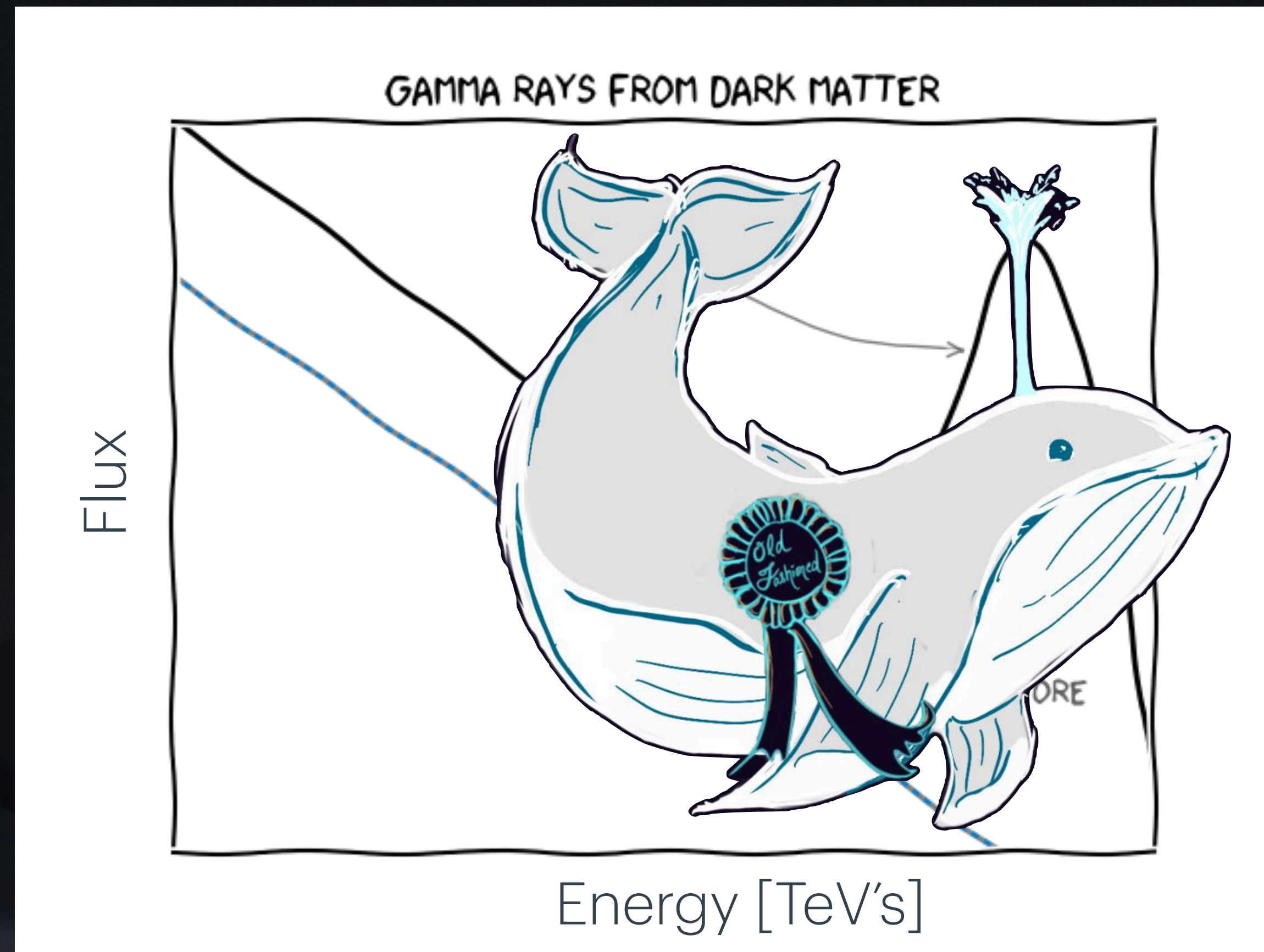
The Basics of Annihilation*

The Dark Matter Landscape
MITP 2024

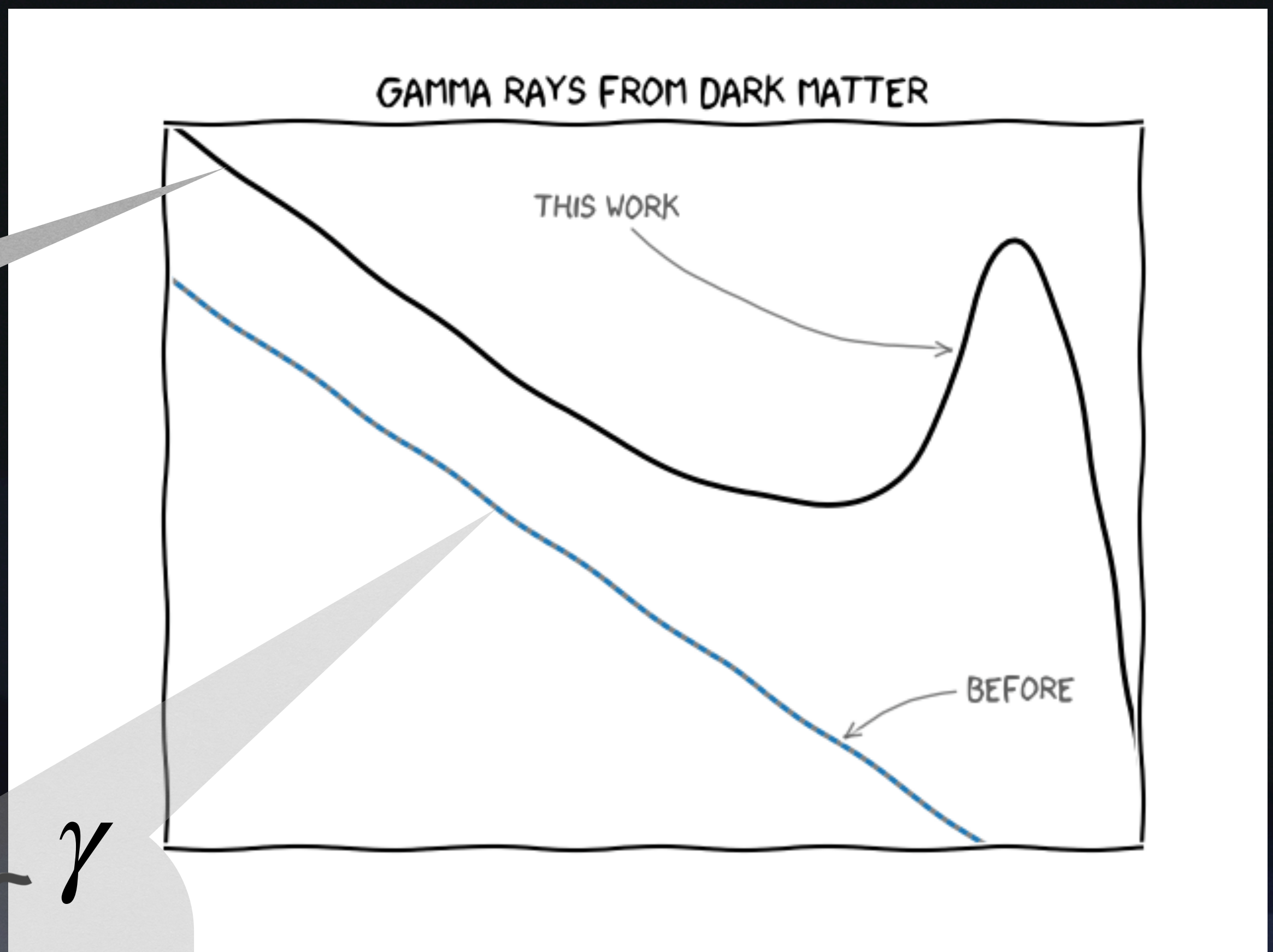
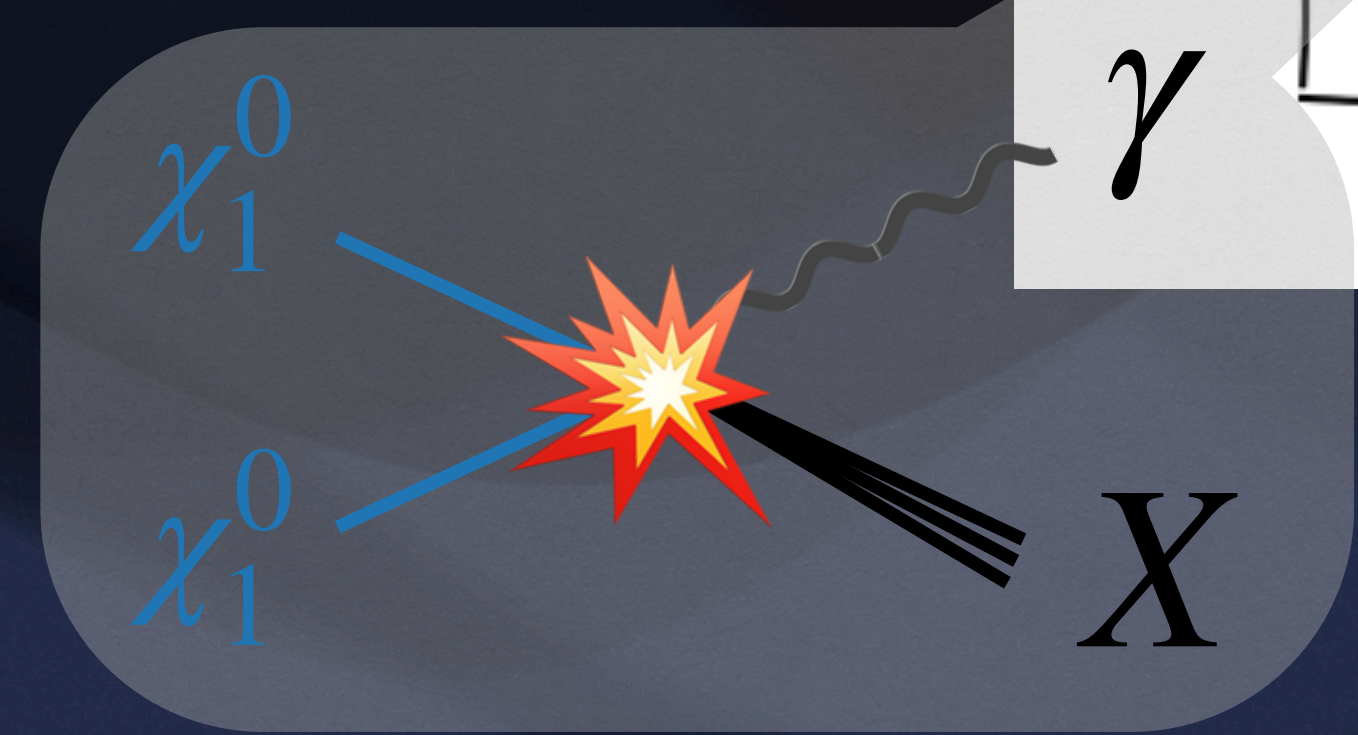
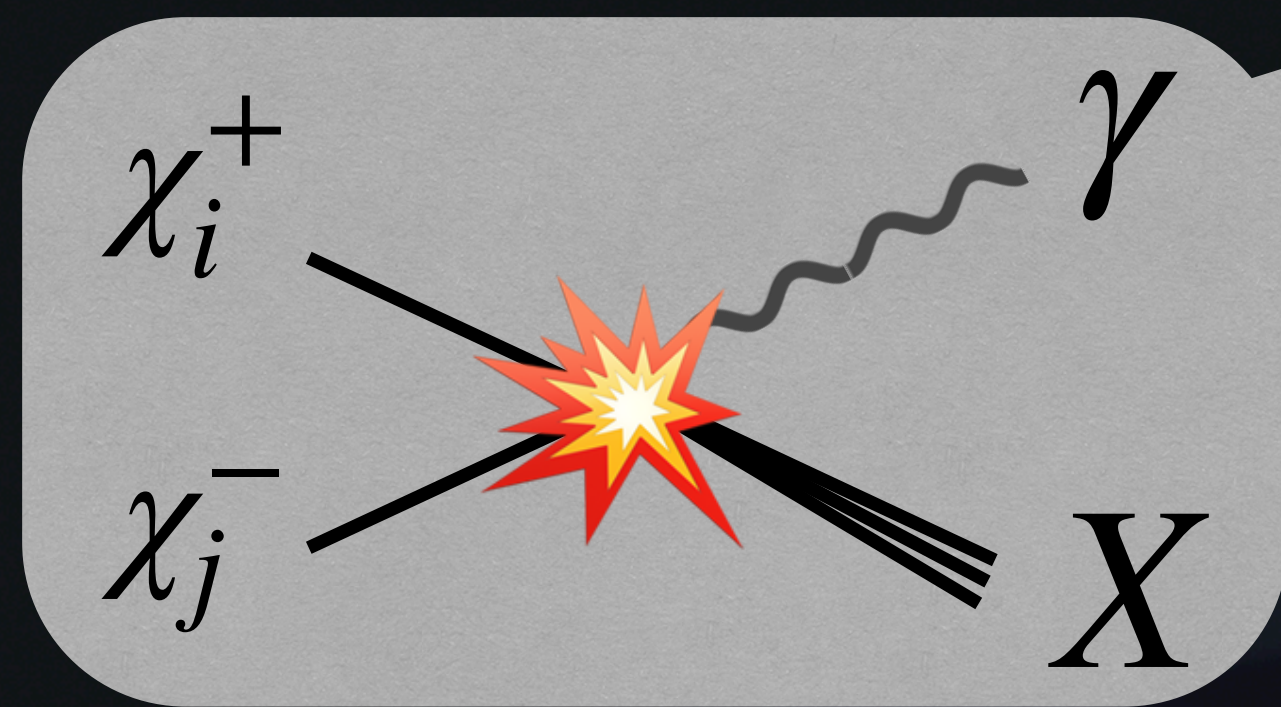


Intro

Very rough and (deliberately) misleading picture



Credit: W. Linda Xu



2410.XXXXX

Resummed photon spectrum from **MOTOKINO**
~~interacting spin 1 dark matter annihilation~~

Motoko Fujiwara^{a*}, Martin Vollmann^{b†}

^a*Physik-Department, Technische Universität München,
James-Franck-Straße, 85748 Garching, Germany*

^b*Institute for Theoretical Physics, University of Tübingen, Auf der Morgenstelle 14, 72076
Tübingen, Germany*

arXiv:2310.11067

Sommerfeld effect for continuum gamma-ray spectra from
Dark Matter annihilation

Barbara Jäger^{id}, Martin Vollmann^{id}

Institute for Theoretical Physics, University of Tübingen,
Auf der Morgenstelle 14, 72076 Tübingen, Germany

October 18, 2023

October 18, 2023

Auf der Morgenstelle 14, 72076 Tübingen, Germany
Institute for Theoretical Physics, University of Tübingen

Outline

Motivation

Indirect detection

Sommerfeld factor

Endpoint resummations

Plots

Conclusions

Motivation

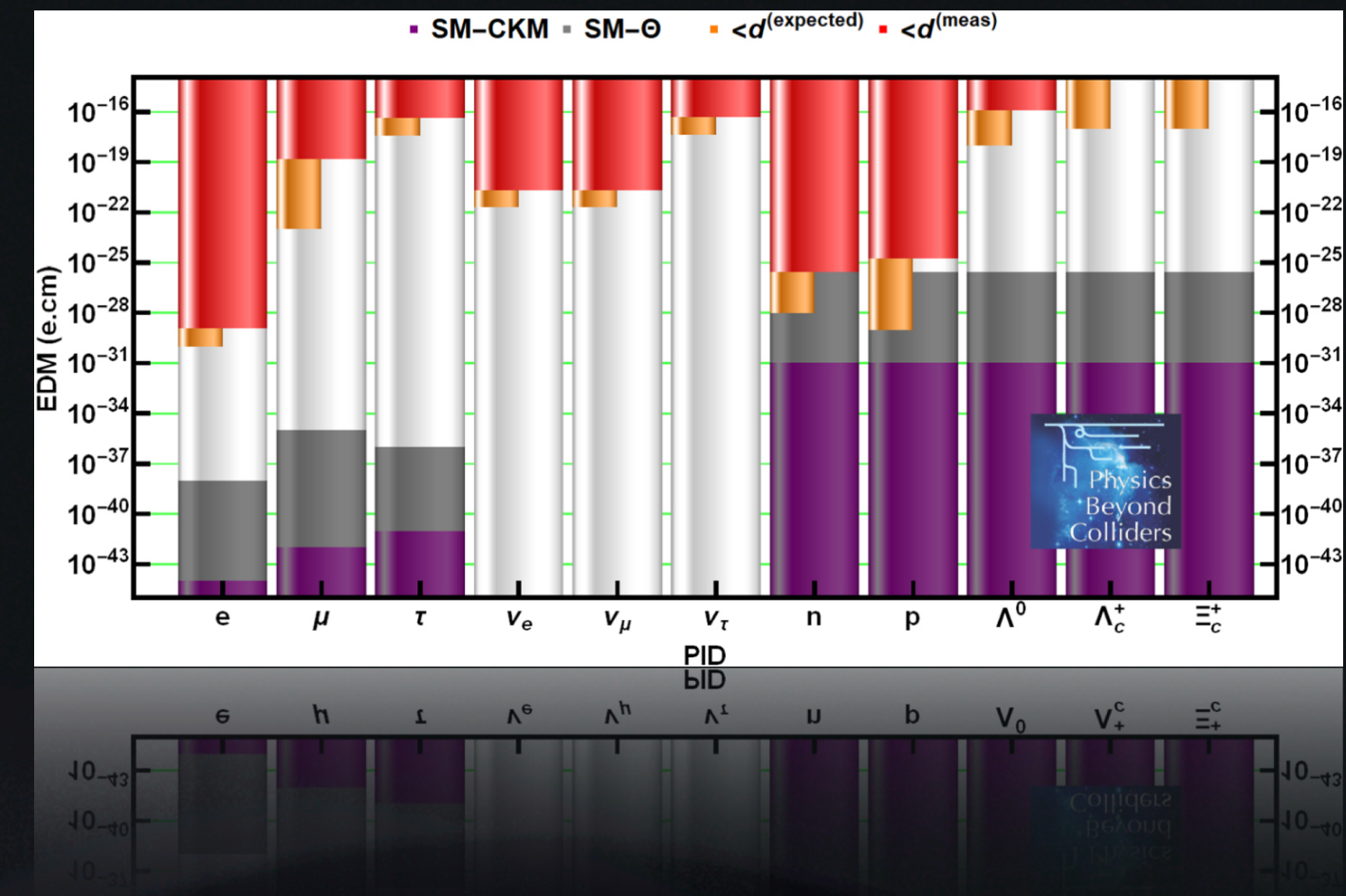
WIMP: the devil that you know

Did you know that...

- There is experimental evidence for **Dark Matter**
- There is experimental evidence for **electroweak interactions**
- Although there is no experimental evidence for the **freeze-out mechanism**
 - ▶ still the simplest!

High-scale SUSY

- Unification of gauge couplings improved
- No SUSY CP problem (EDMs)
- Pure wino/higgsino -> very predictive scenarios
 - Maybe detectable with next-generation γ -ray telescopes (e.g. Rodd, Safdi, Xu [2405.13104](#))
- Naturalness



But really... Why?



And why you should still care!

- WIMPs are **not** dead yet!
- The miracle is still a miracle
- If you want to rule them out better be sure that you didn't overlook anything

NEED ACCURATE THEORETICAL PREDICTIONS

- The physics is fun and the “spare parts” are useful as long as there are electroweak interactions in nature

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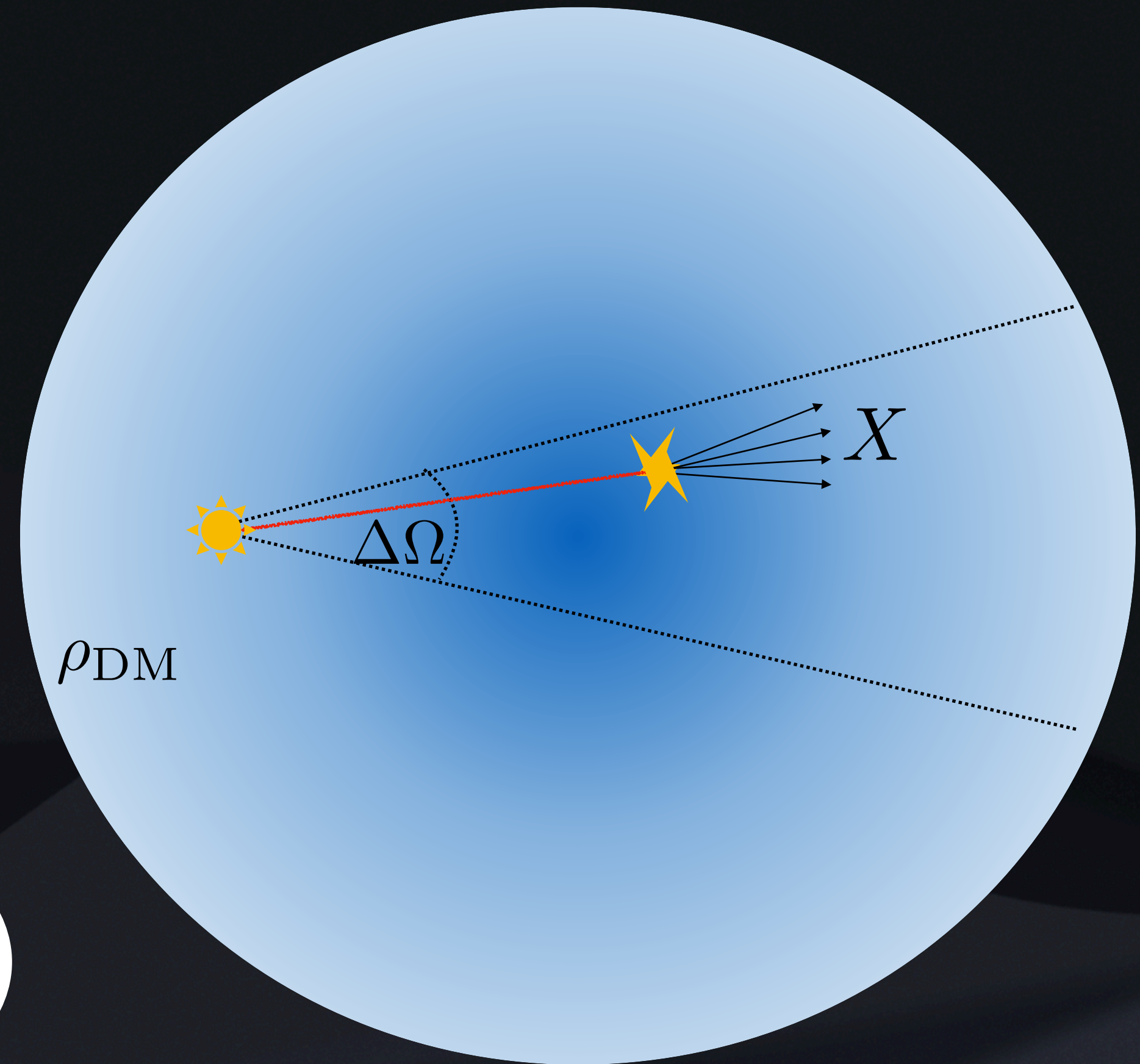
Conclusions

Indirect detection

Gamma-ray flux formula

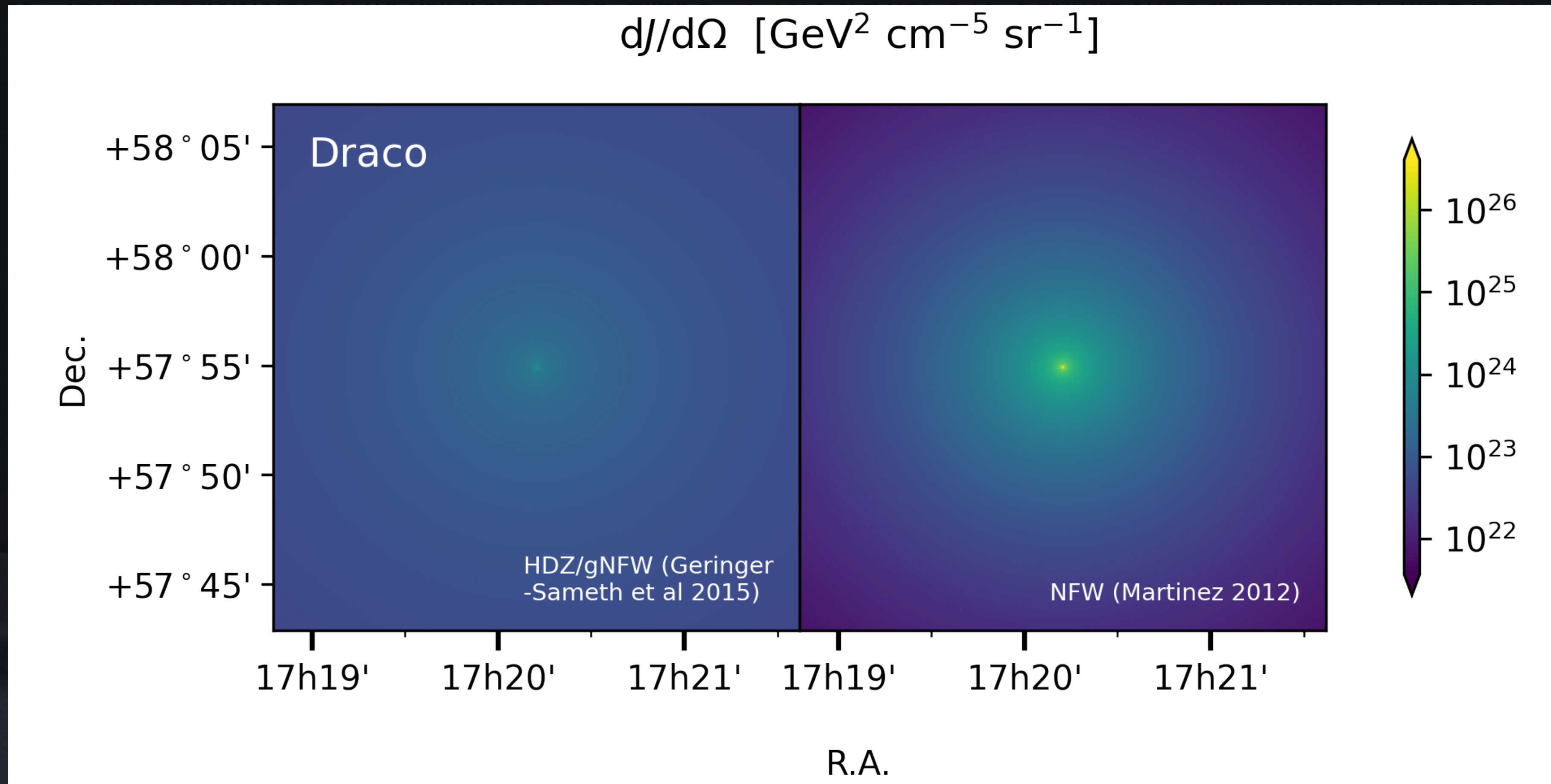
$$\Phi_\gamma = \frac{1}{8\pi m_\chi^2} \times J \times \frac{d\sigma\nu}{dE_\gamma}$$

$$J = \int d\Omega \int_{l.o.s.} ds \rho_{\text{DM}}^2$$

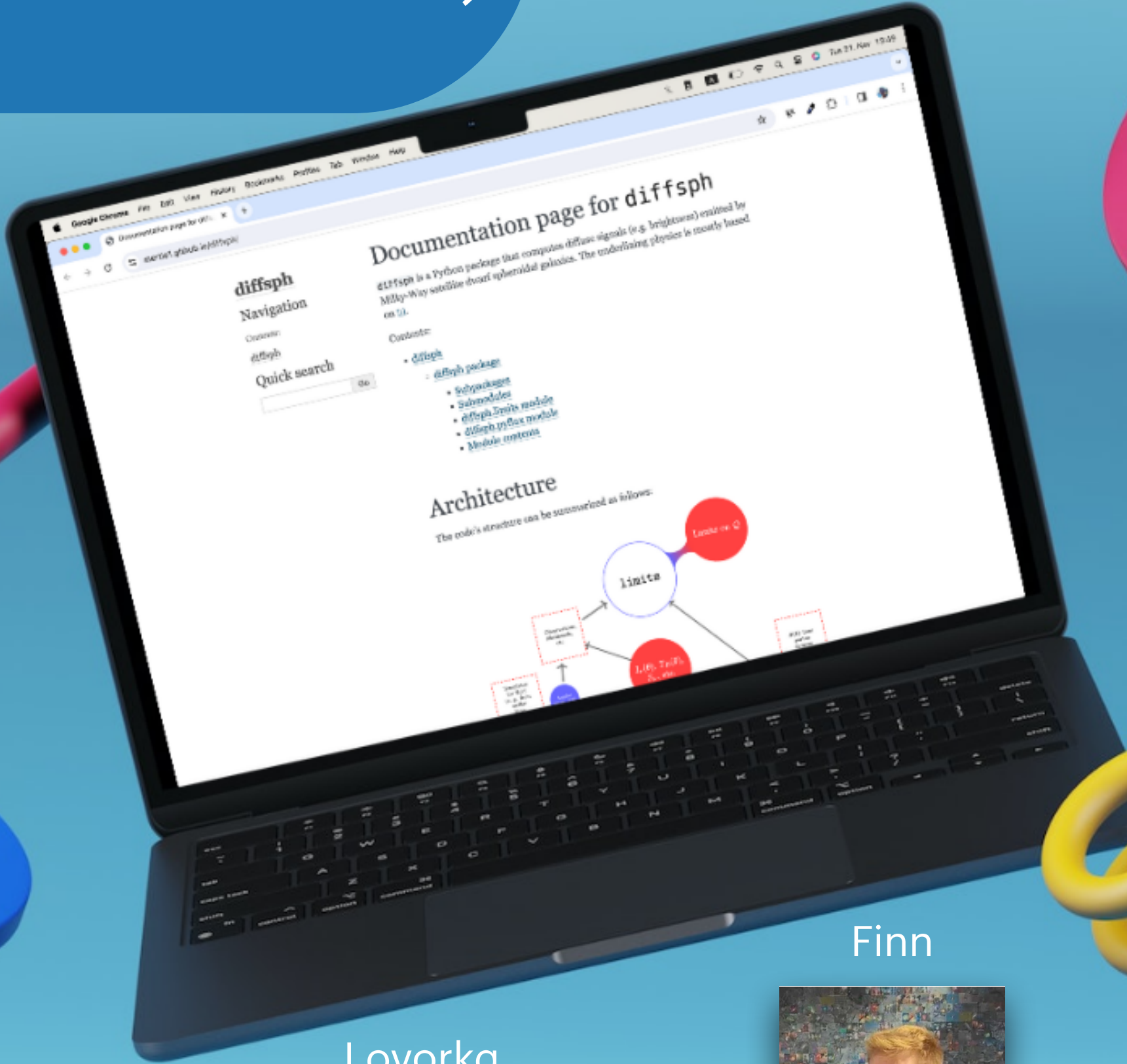
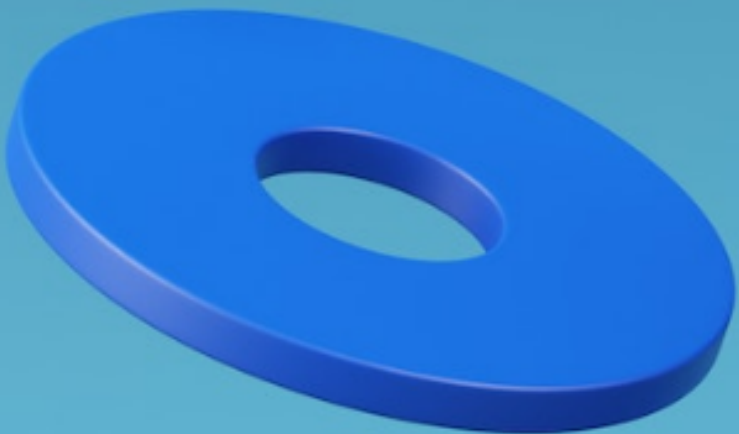
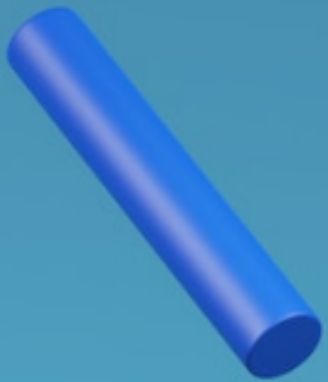


Example (Ad break)

Draco dwarf galaxy with diffSph [2401.05255]



diffSph (2401.05255)



Finn

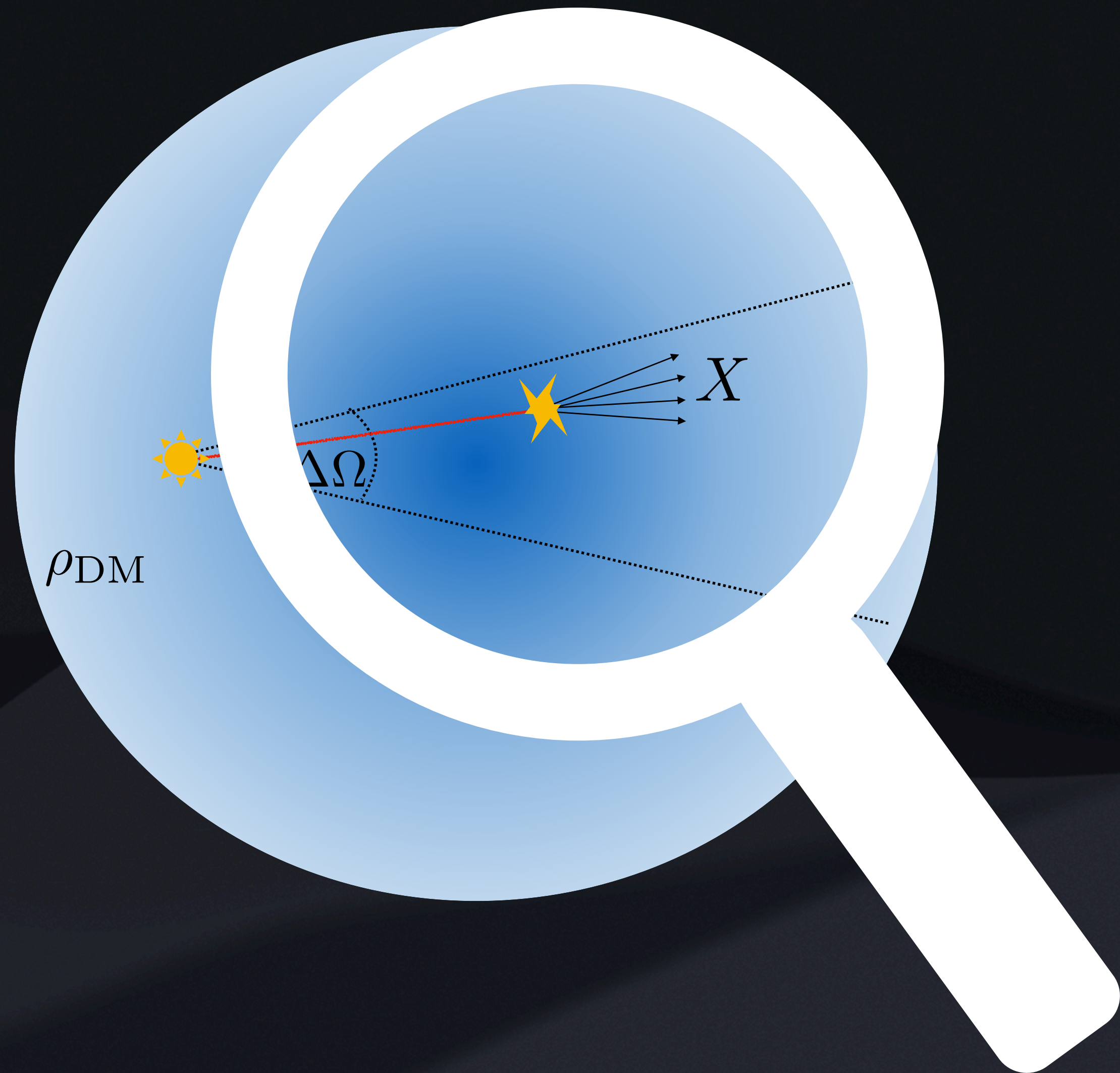


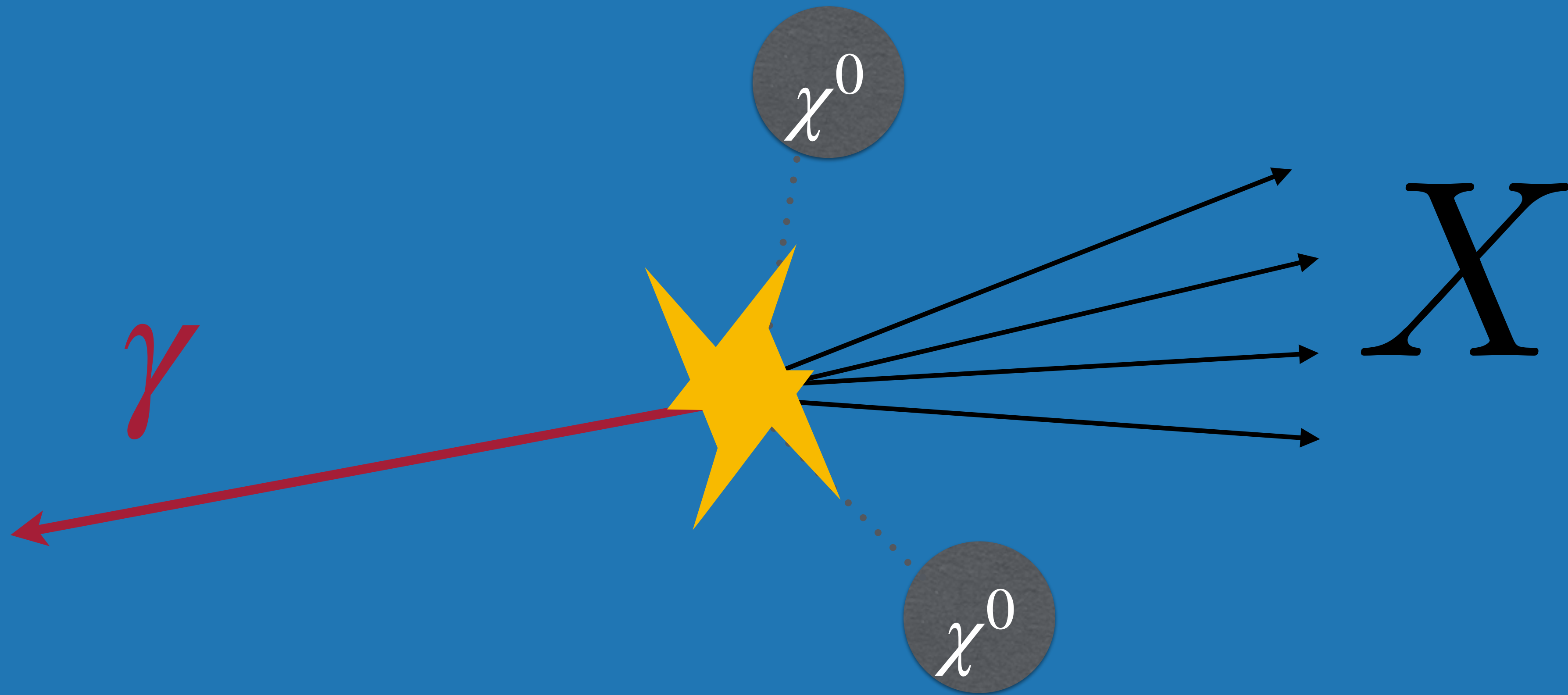
Lovorka



Gamma-ray flux formula

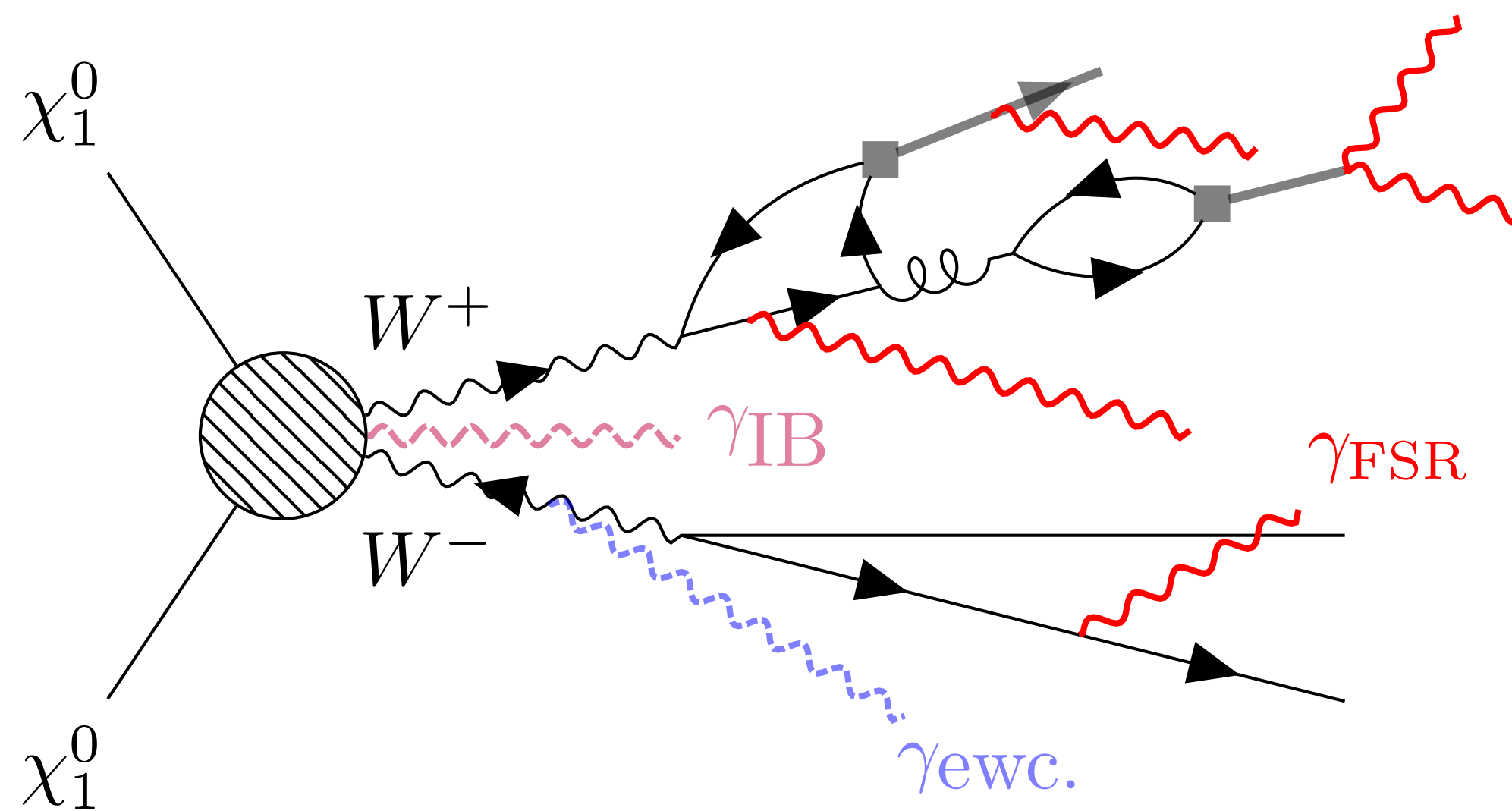
$$\Phi_{\gamma} = \frac{1}{8\pi m_{\chi}^2} \times J \times \frac{d\sigma_{\nu}}{dE_{\gamma}}$$





The problem:

Obtain the annihilation spectrum



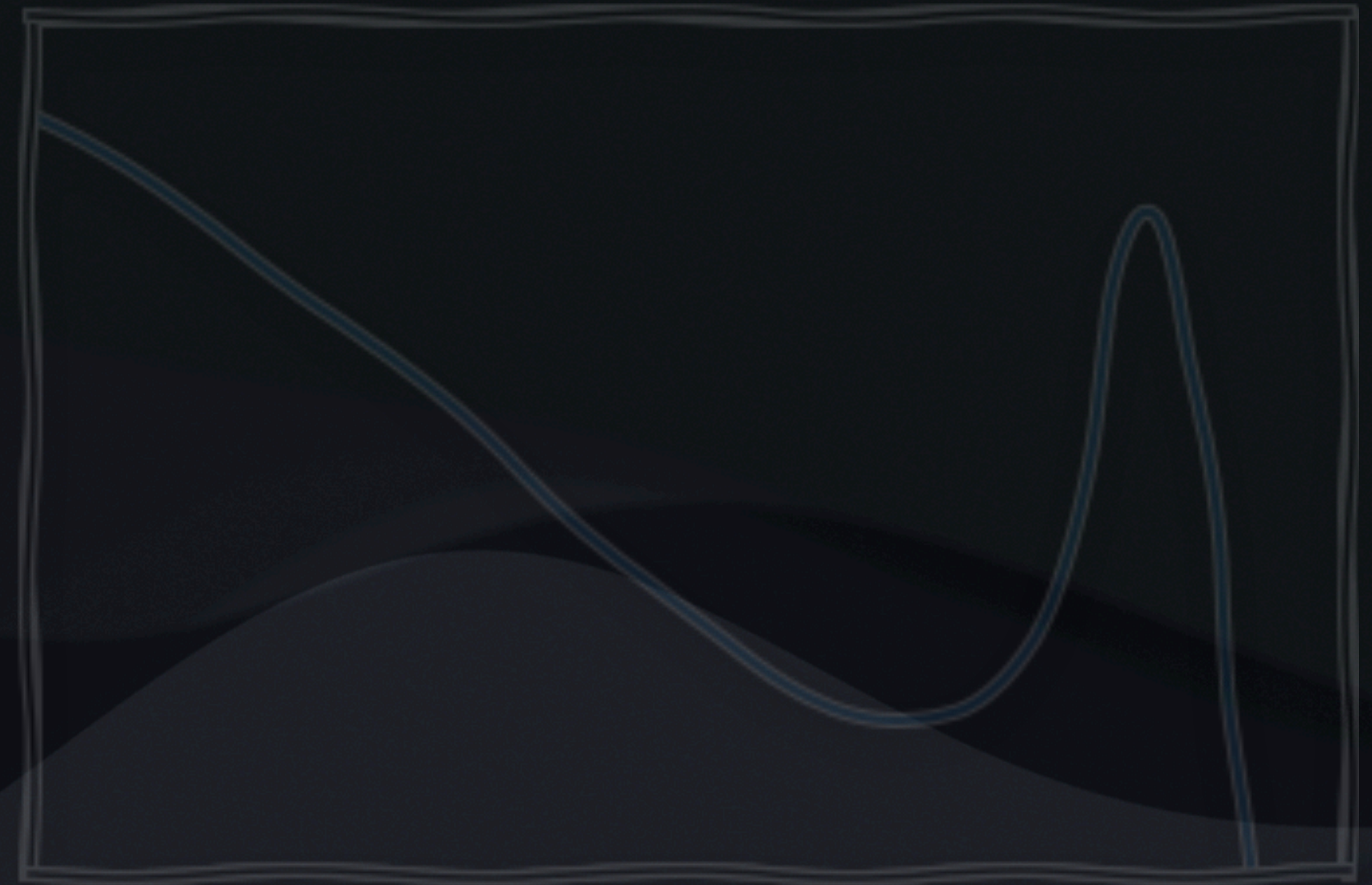
$$\frac{d\sigma_\gamma}{dE_\gamma}$$

TBA

The Basics of Annihilation

	Fixed-order $2 \rightarrow 2$ (tree) + Parton Shower
	Fixed-order $2 \rightarrow 3$ (tree) + Parton Shower
	Fixed-order $2 \rightarrow 2$ + Parton Shower + Sommerfeld factor
	Fixed-order $2 \rightarrow 3$ + Parton Shower + Sommerfeld factor

flux



energy

2000-2010s

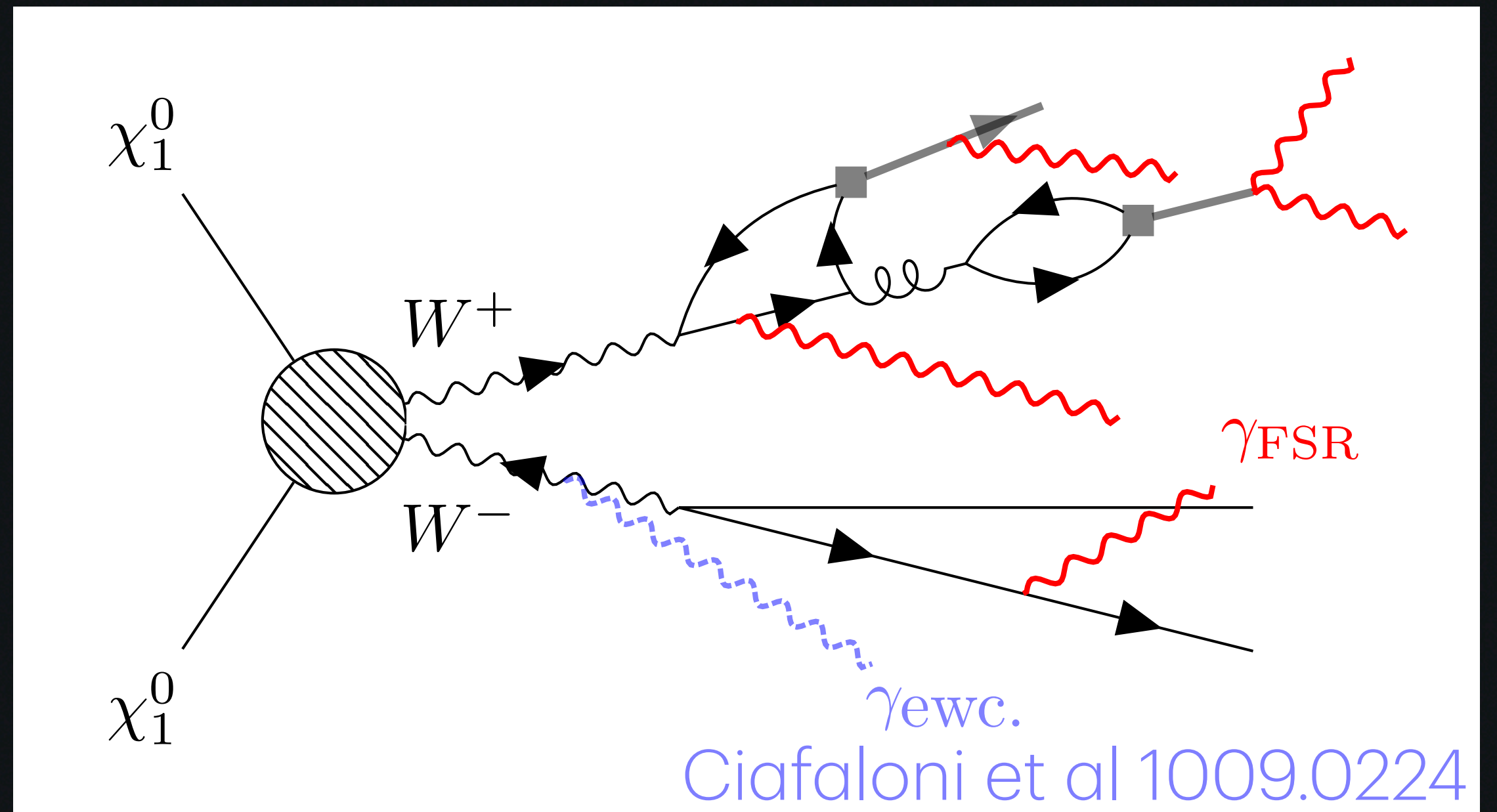


Fixed-order 2 → 2 (tree)
+ Parton Shower

Helicity suppression

If $m_{DM} \gg m_b, m_\tau$ (and $v \ll c$):

$$\langle \sigma v \rangle_{b\bar{b}} \propto \frac{m_b^2}{m_{DM}^2} \rightarrow 0$$



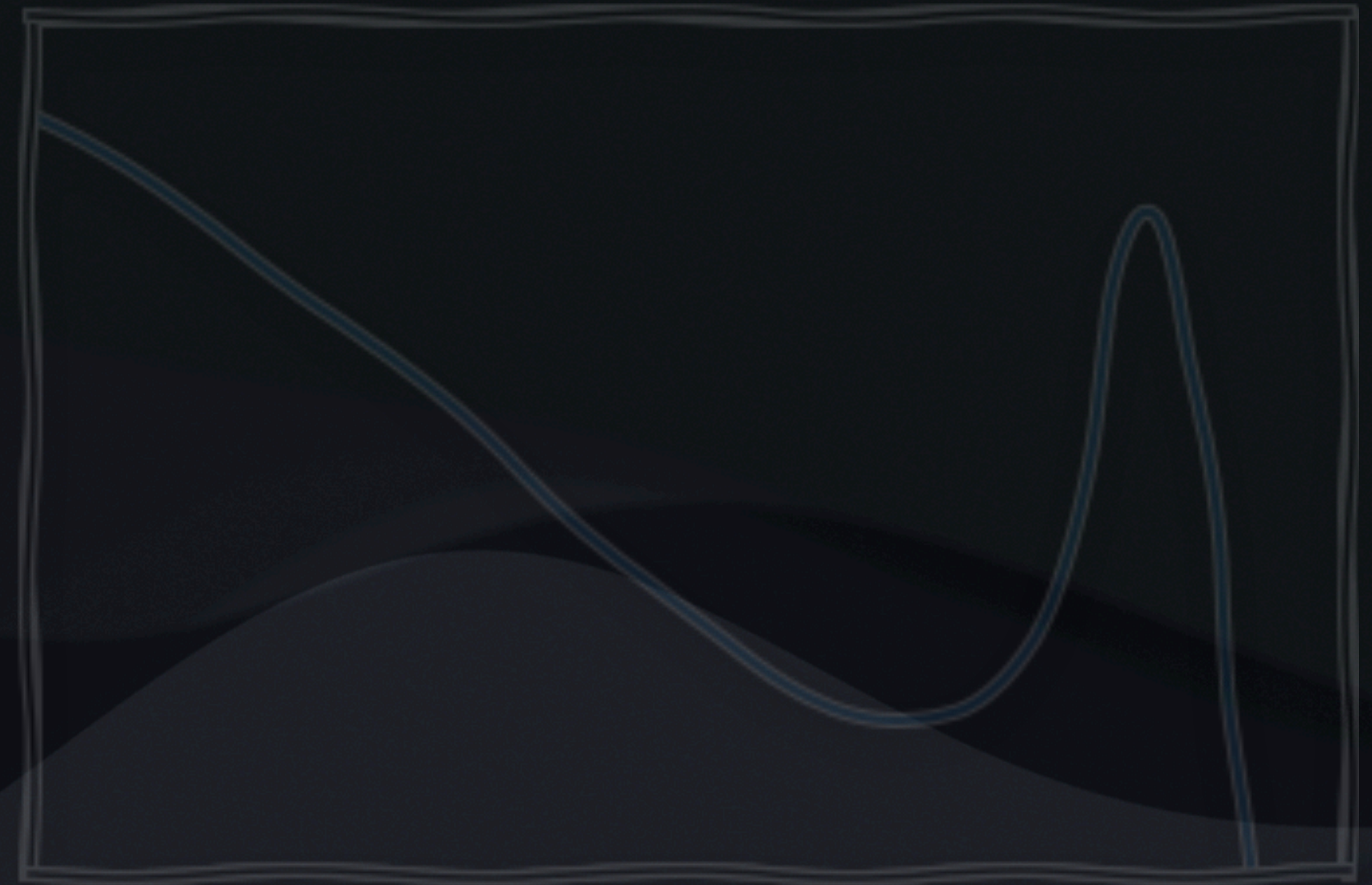
$$\frac{d\sigma v}{dE_\gamma} = \cancel{(\sigma v)_{b\bar{b}}} \frac{dN_{b\bar{b}}^{MC}}{dE_\gamma} + \cancel{(\sigma v)_{\tau^+\tau^-}} \frac{dN_{\tau^+\tau^-}^{MC}}{dE_\gamma} + \dots$$

TBA

The Basics of Annihilation

	Fixed-order $2 \rightarrow 2$ (tree) + Parton Shower
	Fixed-order $2 \rightarrow 3$ (tree) + Parton Shower
	Fixed-order $2 \rightarrow 2$ + Parton Shower + Sommerfeld factor
	Fixed-order $2 \rightarrow 3$ + Parton Shower + Sommerfeld factor

flux

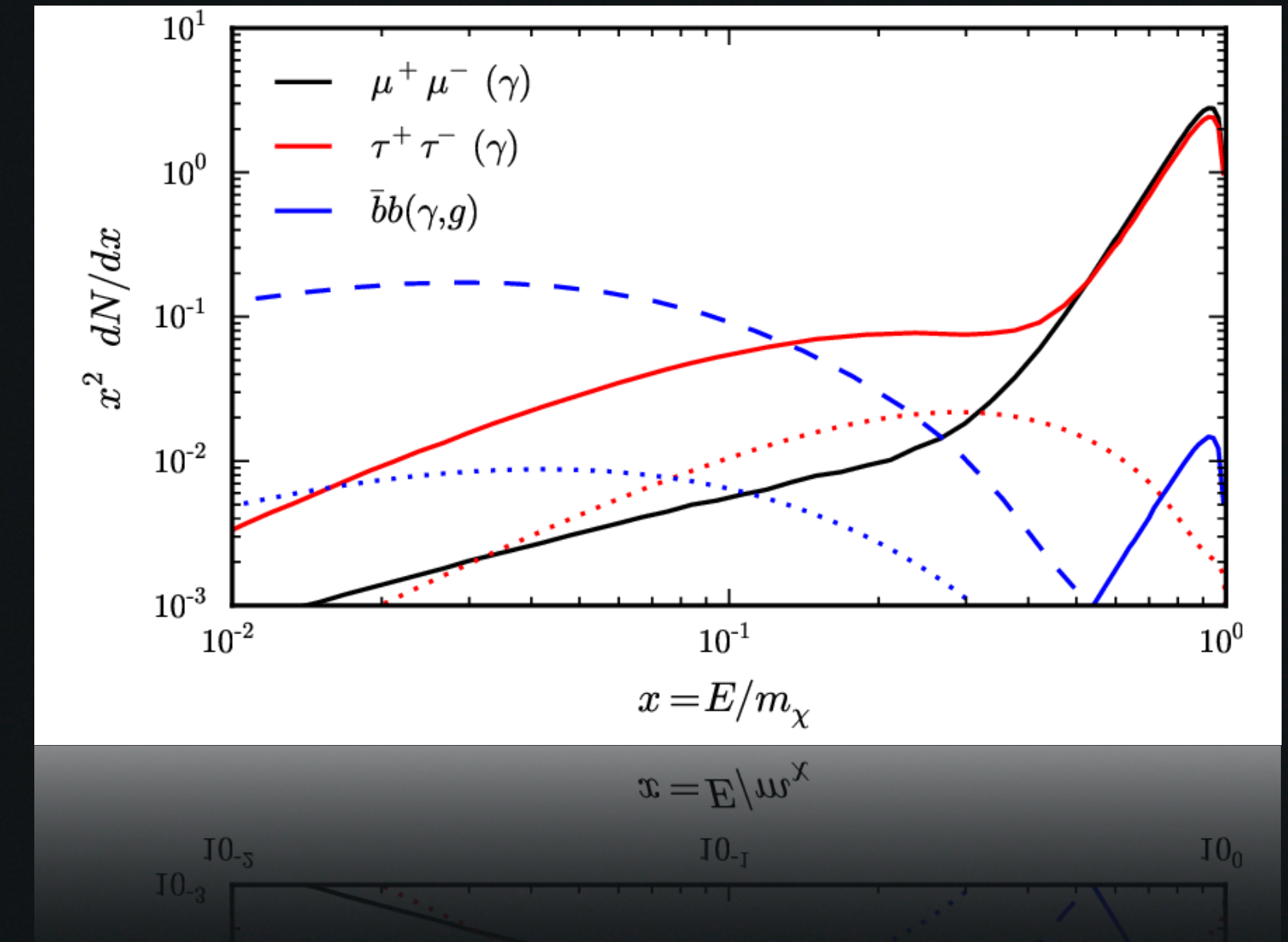


energy

2000-2010s



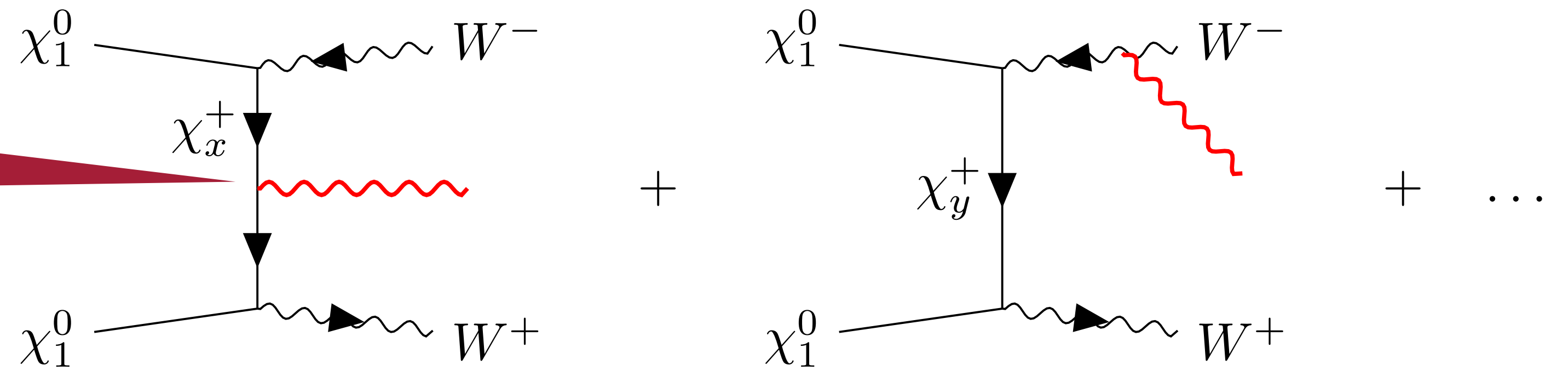
Fixed-order 2 → 3 (tree)
+ Parton Shower



Internal bremsstrahlung




Lift helicity suppression

- 2 → 2 process $\langle \sigma v \rangle_{b\bar{b}} \propto \frac{m_b^2}{m_{DM}^2} \rightarrow 0$
- 2 → 3 process $\langle \sigma v \rangle_{b\bar{b}\gamma} \neq 0$

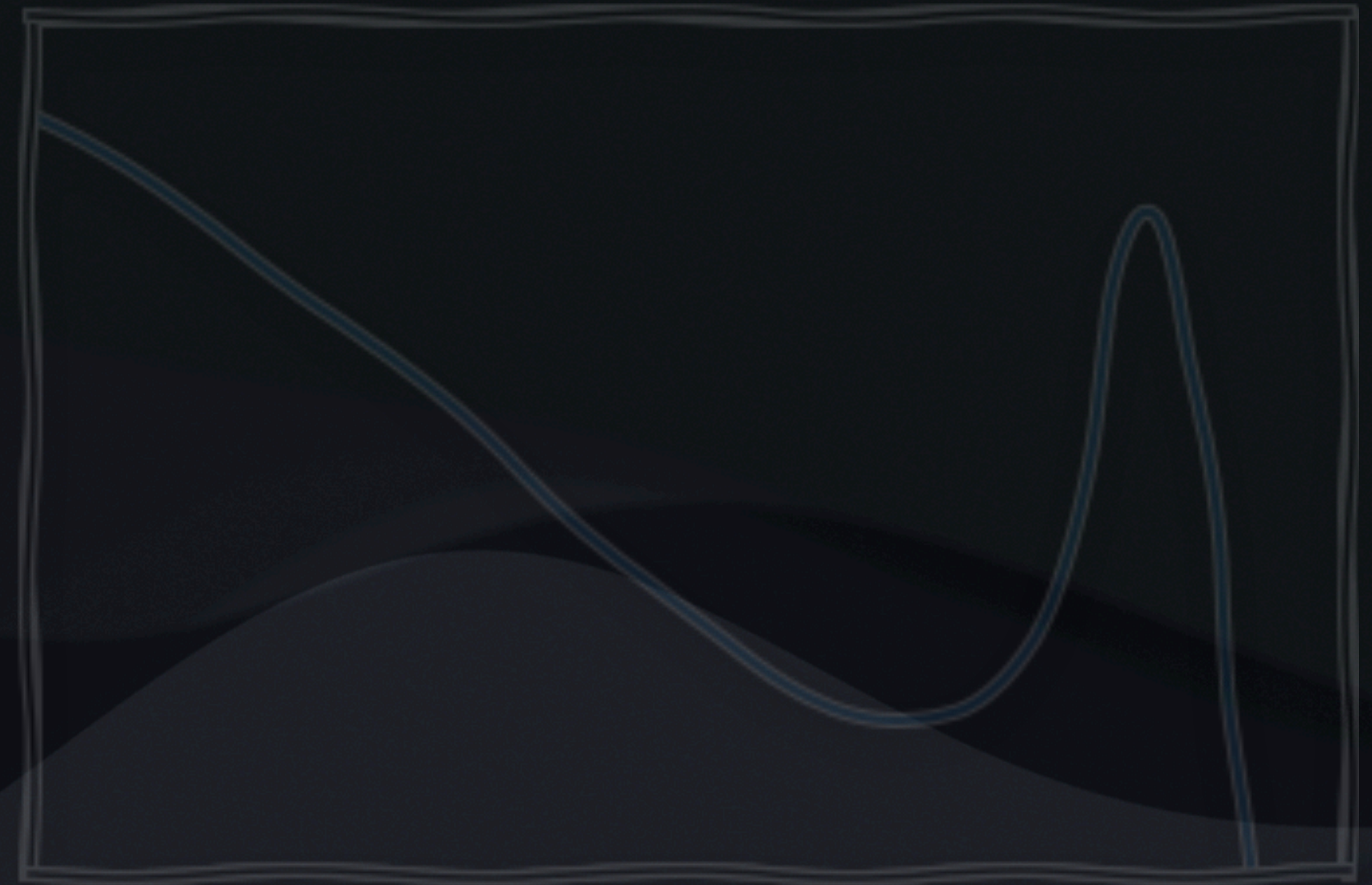


TBA

The Basics of Annihilation

	Fixed-order $2 \rightarrow 2$ (tree) + Parton Shower
	Fixed-order $2 \rightarrow 3$ (tree) + Parton Shower
	Fixed-order $2 \rightarrow 2$ + Parton Shower + Sommerfeld factor
	Fixed-order $2 \rightarrow 3$ + Parton Shower + Sommerfeld factor




flux



energy

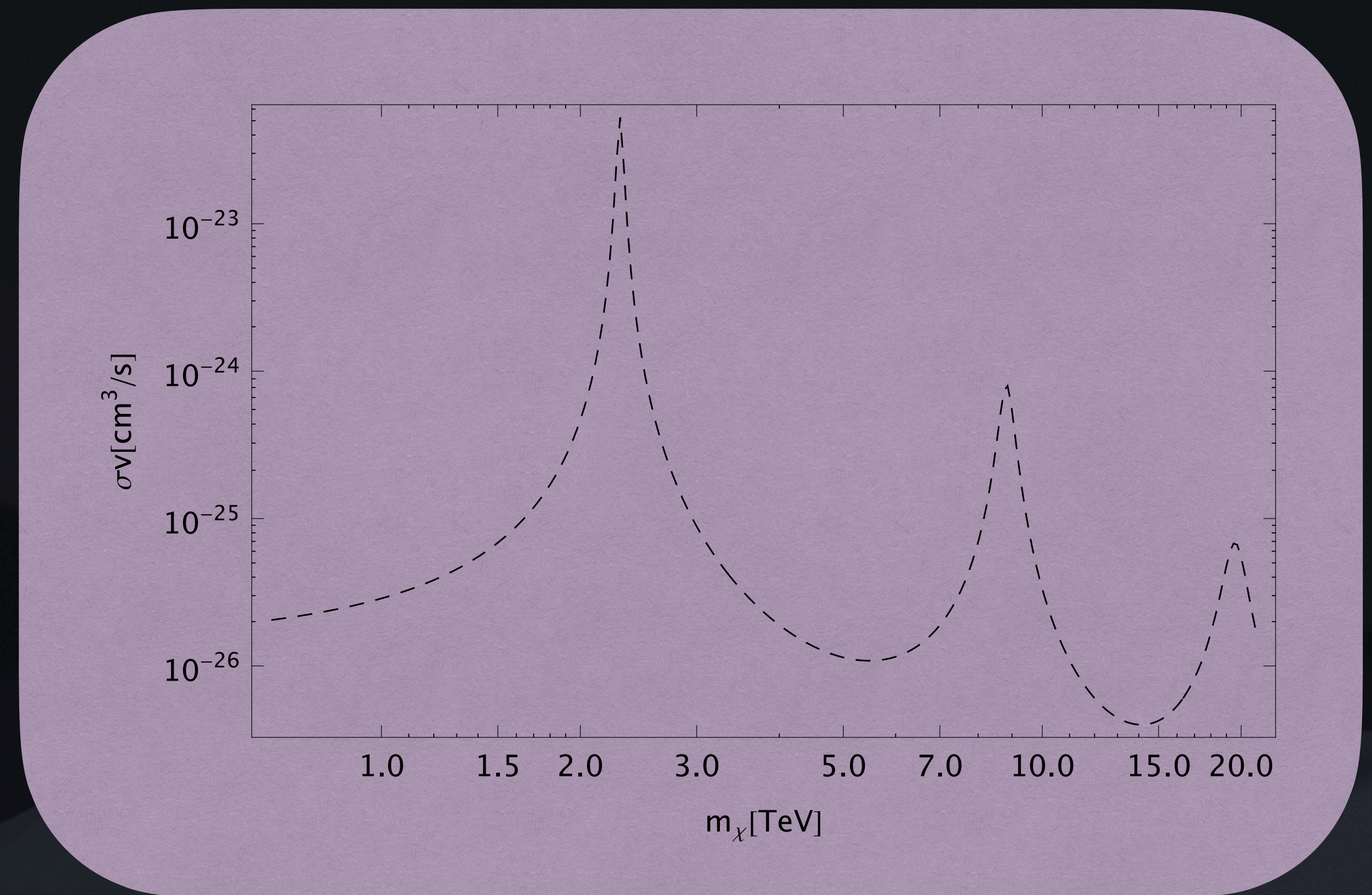
TBA

The Basics of Annihilation

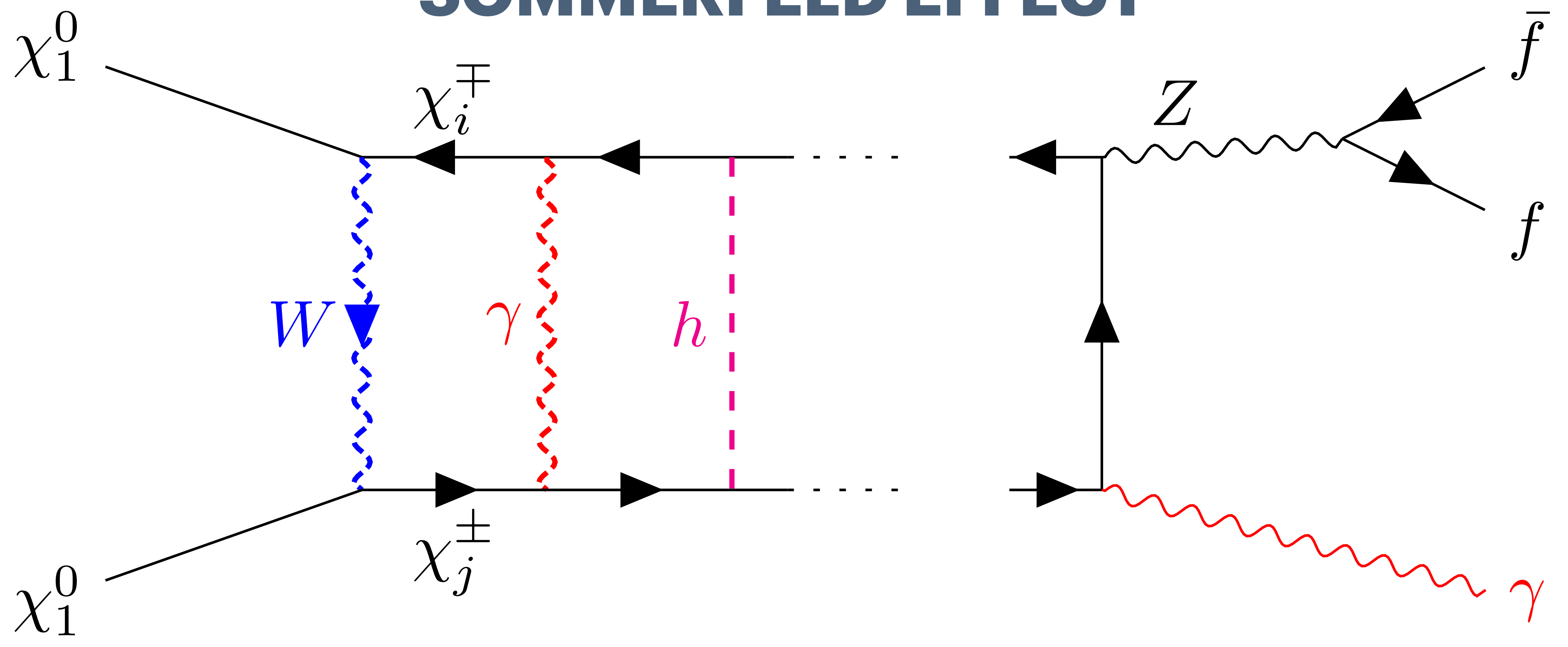
	Fixed-order $2 \rightarrow 2$ (tree) + Parton Shower
	Fixed-order $2 \rightarrow 3$ (tree) + Parton Shower
	Fixed-order $2 \rightarrow 2$ + Parton Shower + Sommerfeld factor
	Fixed-order $2 \rightarrow 3$ + Parton Shower + Sommerfeld factor

Hisano, Matsumoto, Nojiri [hep-ph/0307216](https://arxiv.org/abs/hep-ph/0307216)

Arkani-Hamed, Slatyer, Weiner [0810.0713](https://arxiv.org/abs/0810.0713)



SOMMERFELD EFFECT



Resummation

Breakdown of perturbative expansion when $m_\chi \gg m_W$

$$\frac{d\sigma\nu}{dE_\gamma} \sim \# \alpha_{ew}^3 + \alpha_{ew}^4 \left(\text{Gorilla} + \dots \right) + \alpha_{ew}^5 \left(\text{Gorilla} \# \times \text{Lion} + \dots \right) + \dots$$

Tree (LO) 1-loop (NLO) 2-loop (NNLO)

Resummation





Goal: factor out the “gorillas”

$$\frac{d\sigma\nu}{dE_\gamma} = f\left(\alpha_{ew} \times \text{gorilla}\right) \times \left(\# \alpha_{ew}^3 + \mathcal{O}(\alpha_{ew}^4)\right)$$

“safe” to use perturbation theory

TBA

The Basics of Annihilation

	Fixed-order $2 \rightarrow 2$ (tree) + Parton Shower
	Fixed-order $2 \rightarrow 3$ (tree) + Parton Shower
	Fixed-order $2 \rightarrow 2$ + Parton Shower + Sommerfeld factor
	Fixed-order $2 \rightarrow 3$ + Parton Shower + Sommerfeld factor

flux



energy

2020s (before our paper came out)



Fixed-order 2 \rightarrow 2
+ Parton Shower +
Sommerfeld factor

- Incomplete (missing shower for e.g. $\chi^0\chi^0 \rightarrow H^\pm W^\mp$)
- Helicity-suppressed cross sections still suppressed
- ...



Fixed-order 2 \rightarrow 3
+ Parton Shower +
Sommerfeld factor

- Only extrapolations from our endpoint factorization formulas available and for pure wino/higgsino

Outline

Motivation

Indirect detection

Sommerfeld factor

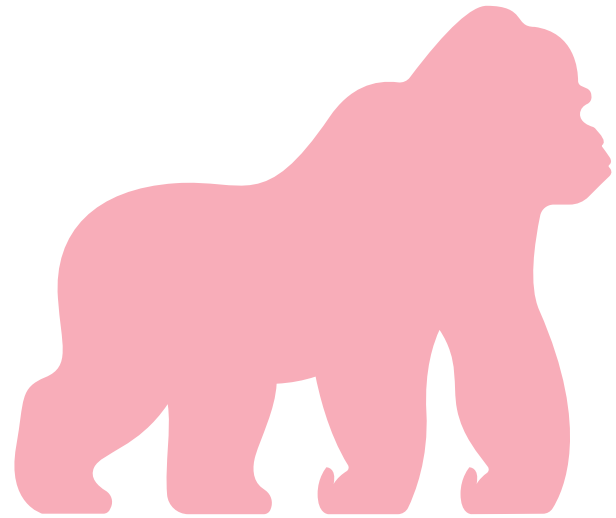
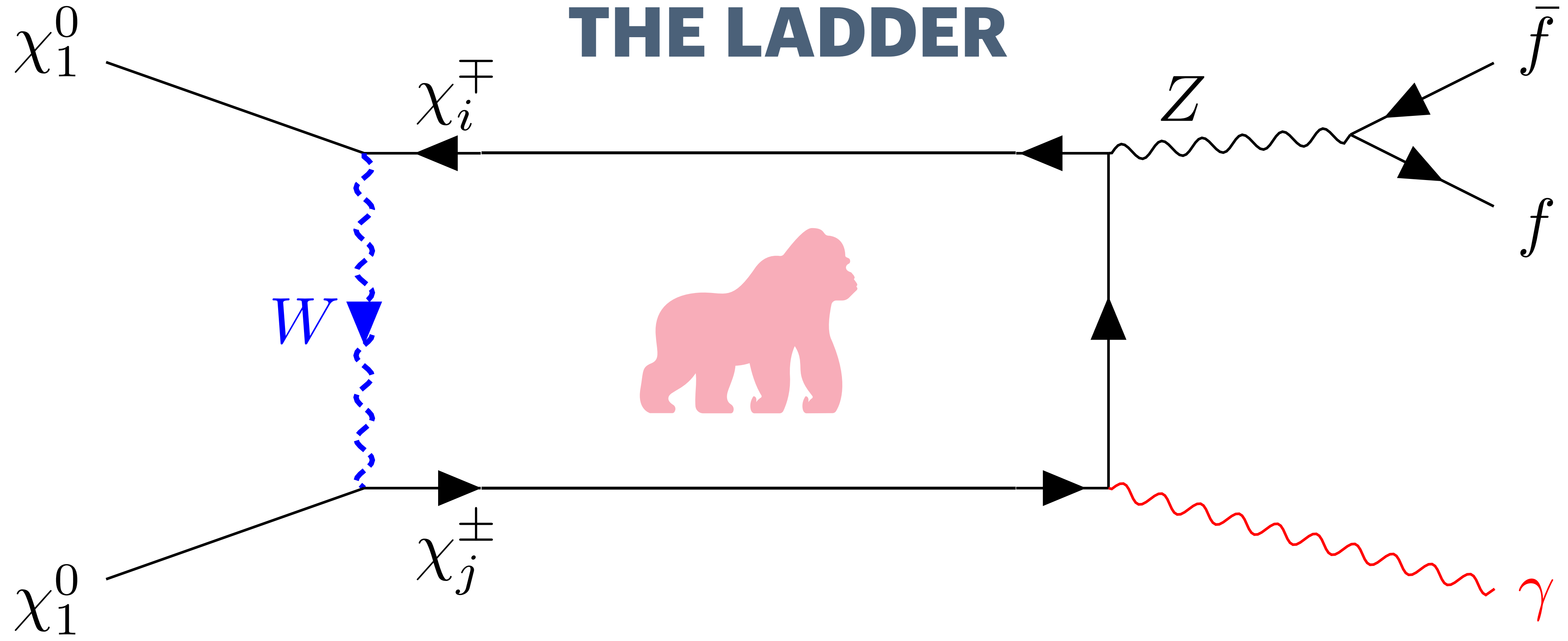
Endpoint resummations

Plots

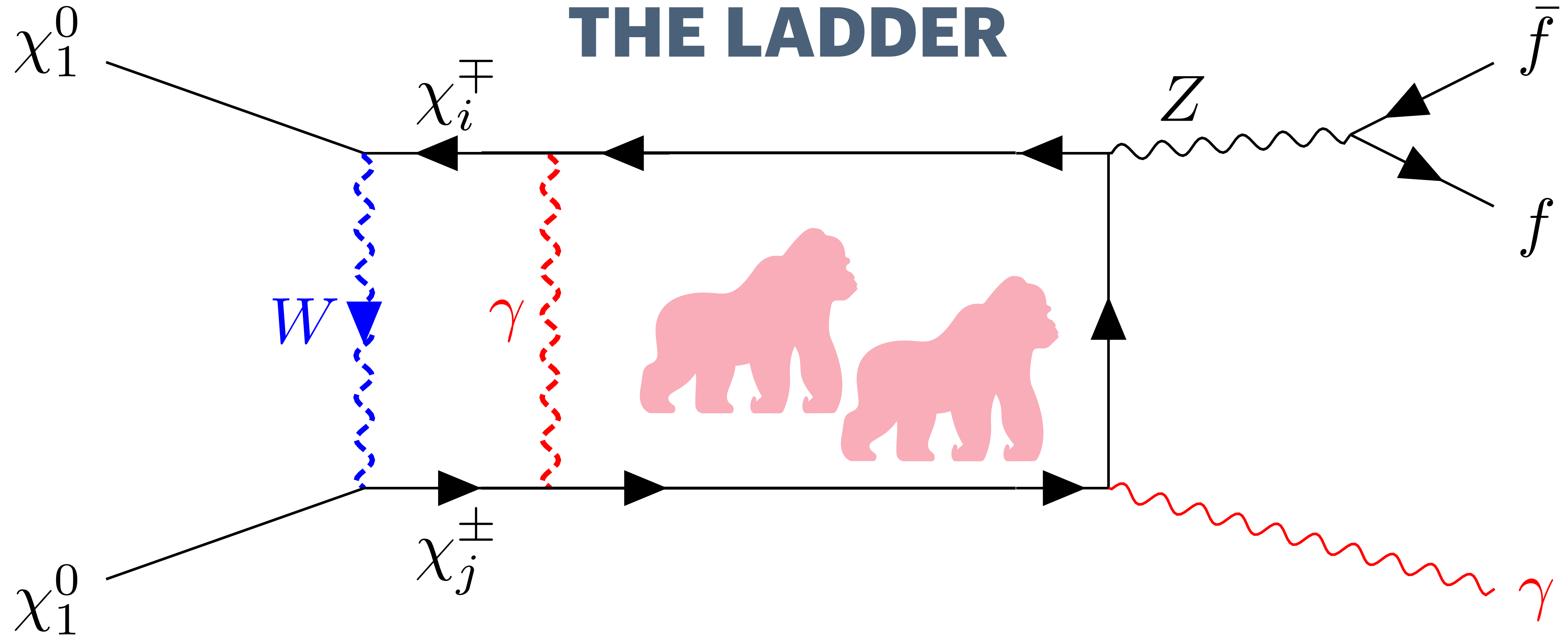
Conclusions

Sommerfeld factor

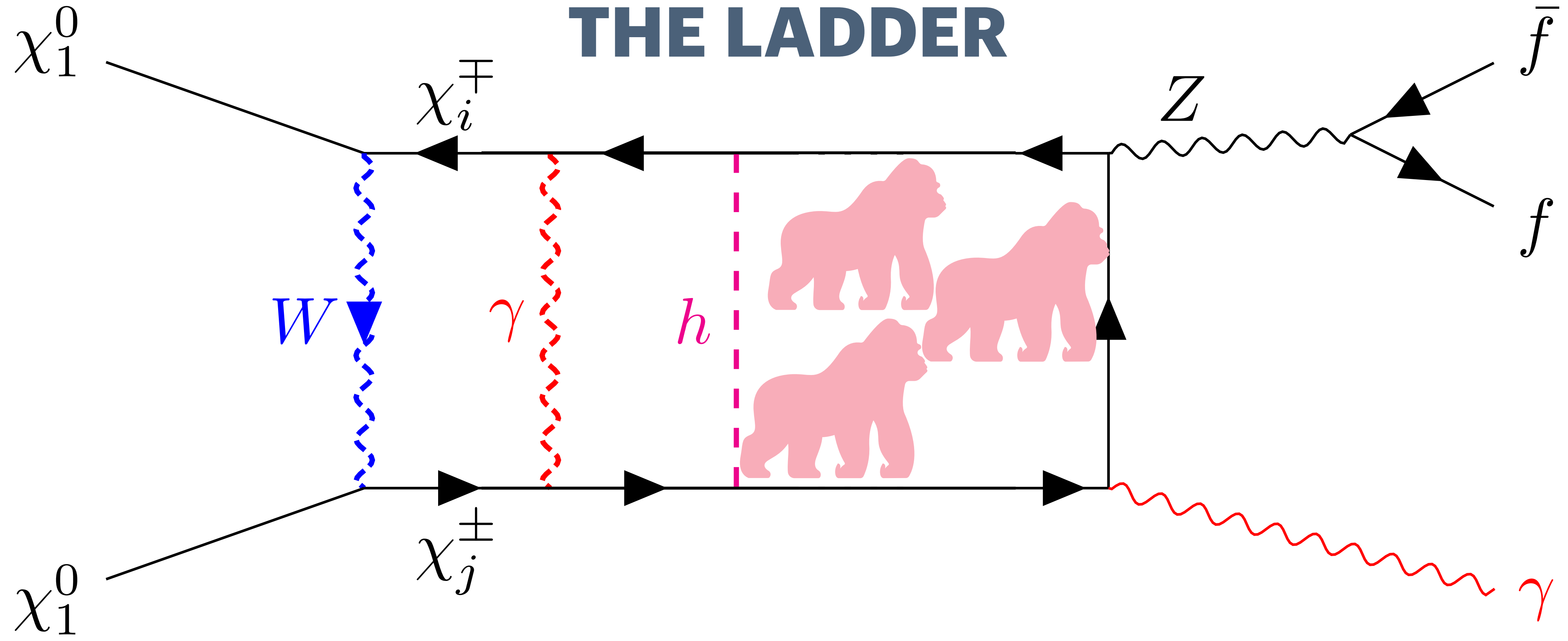
THE LADDER



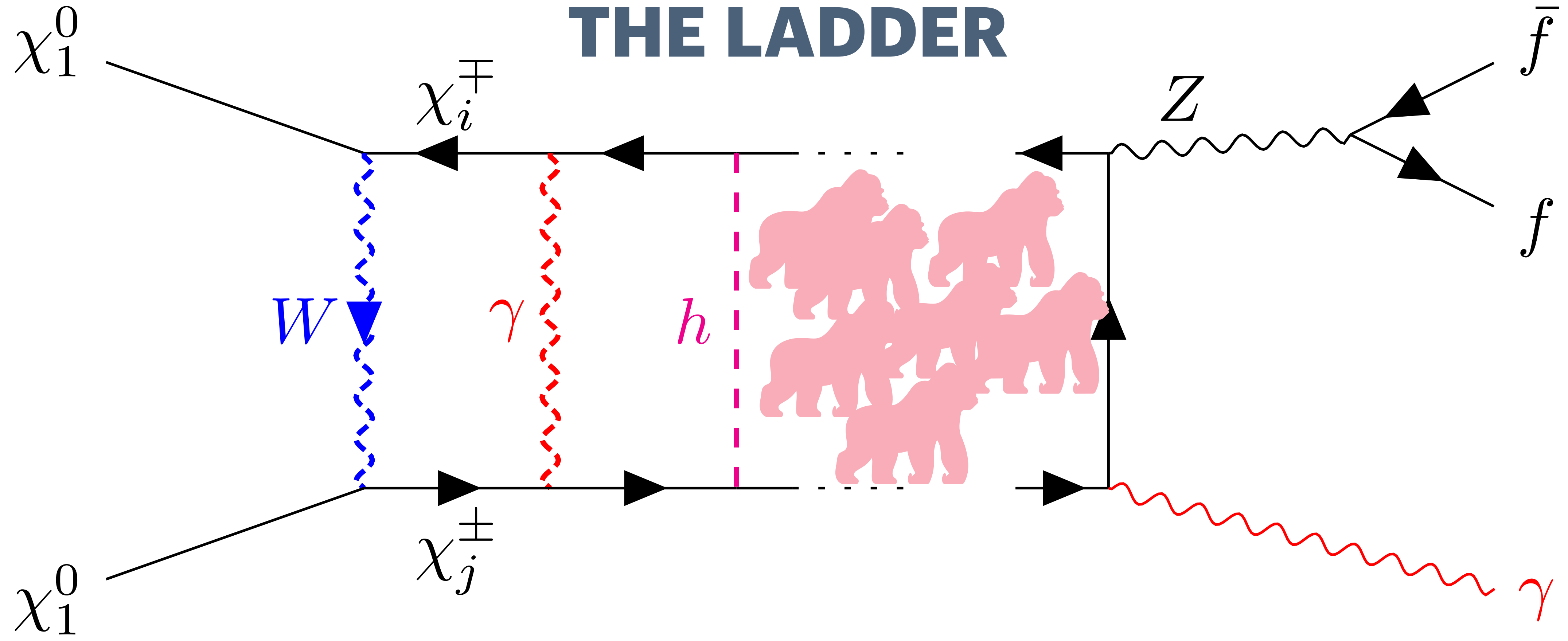
THE LADDER



THE LADDER



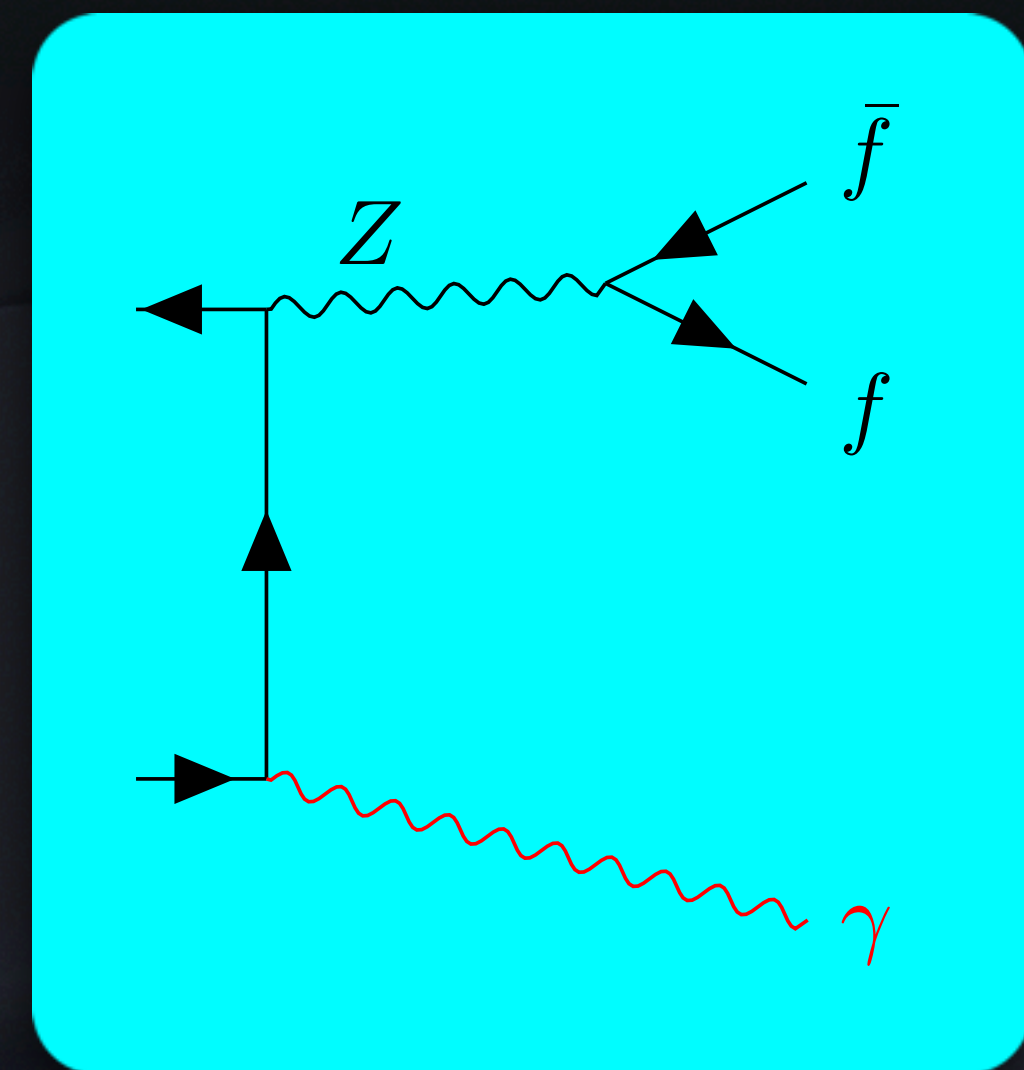
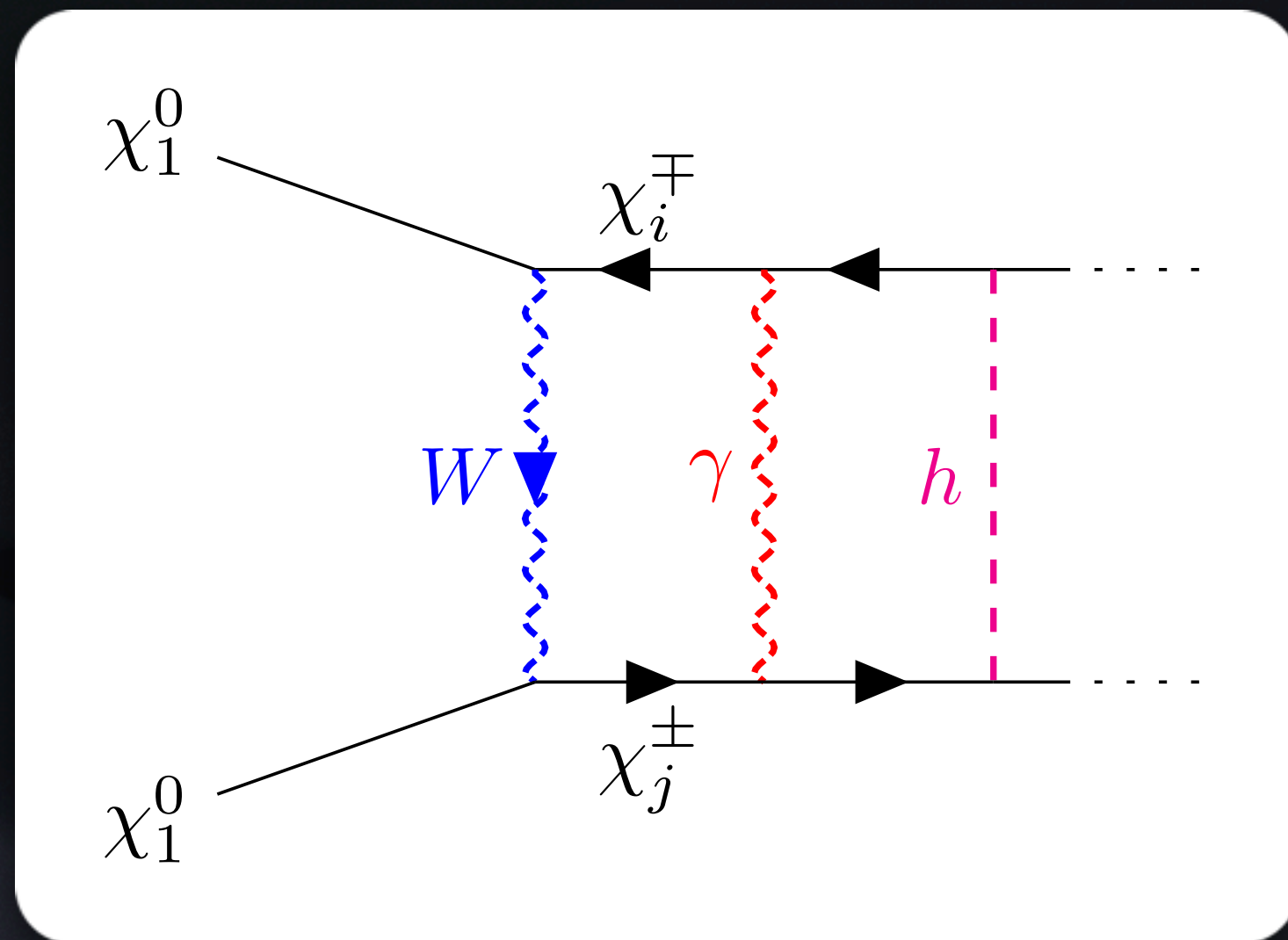
THE LADDER



Resummation

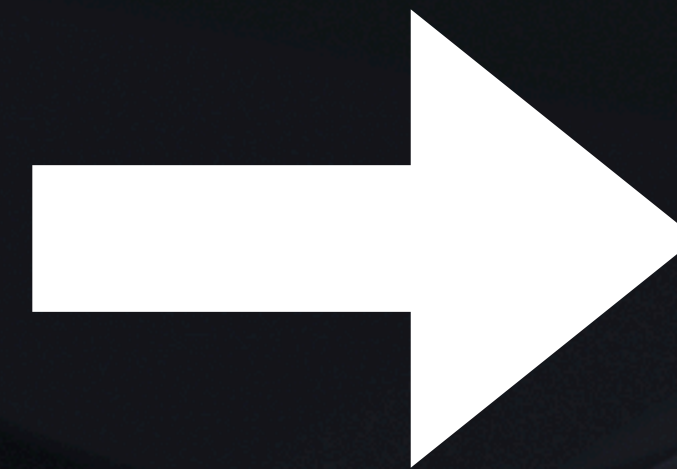
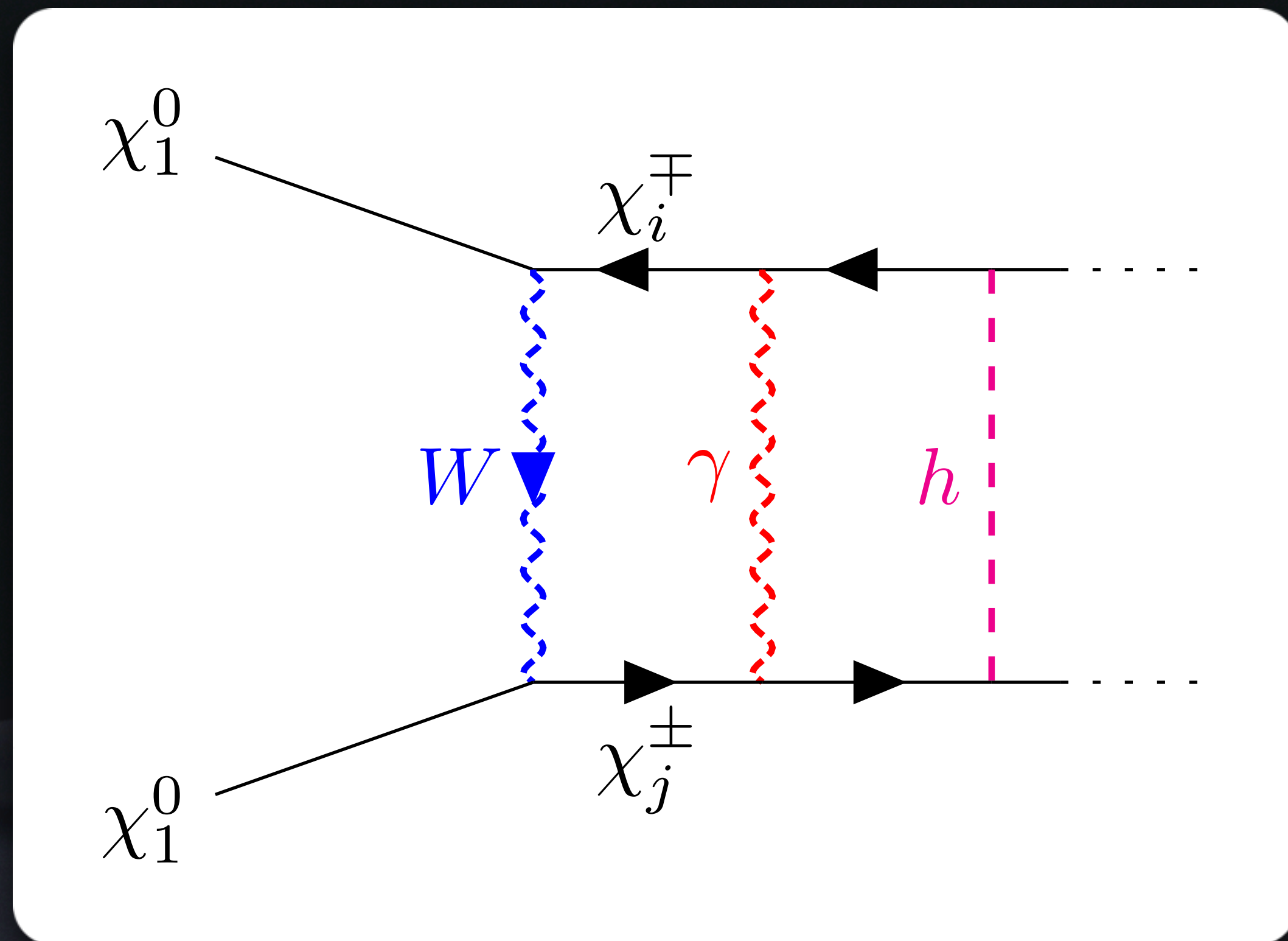
Goal: factor out the “gorillas”

$$\frac{d\sigma}{dE_\gamma} = f\left(\alpha_{ew} \times \text{gorilla}\right) \times \left(\# \alpha_{ew}^3 + \mathcal{O}(\alpha_{ew}^4)\right)$$



Sommerfeld factor

Reframe the question: QFT \rightarrow Quantum Mechanics



Sommerfeld factor

Putting all things together

$$\frac{d\sigma\nu}{dE_\gamma} = 2 \sum_{I,J} S_{IJ} \left[\frac{d(\tilde{\sigma}\nu)}{dE_\gamma} \right]_{IJ}$$

Quantum mechanics
(ladder) ↓

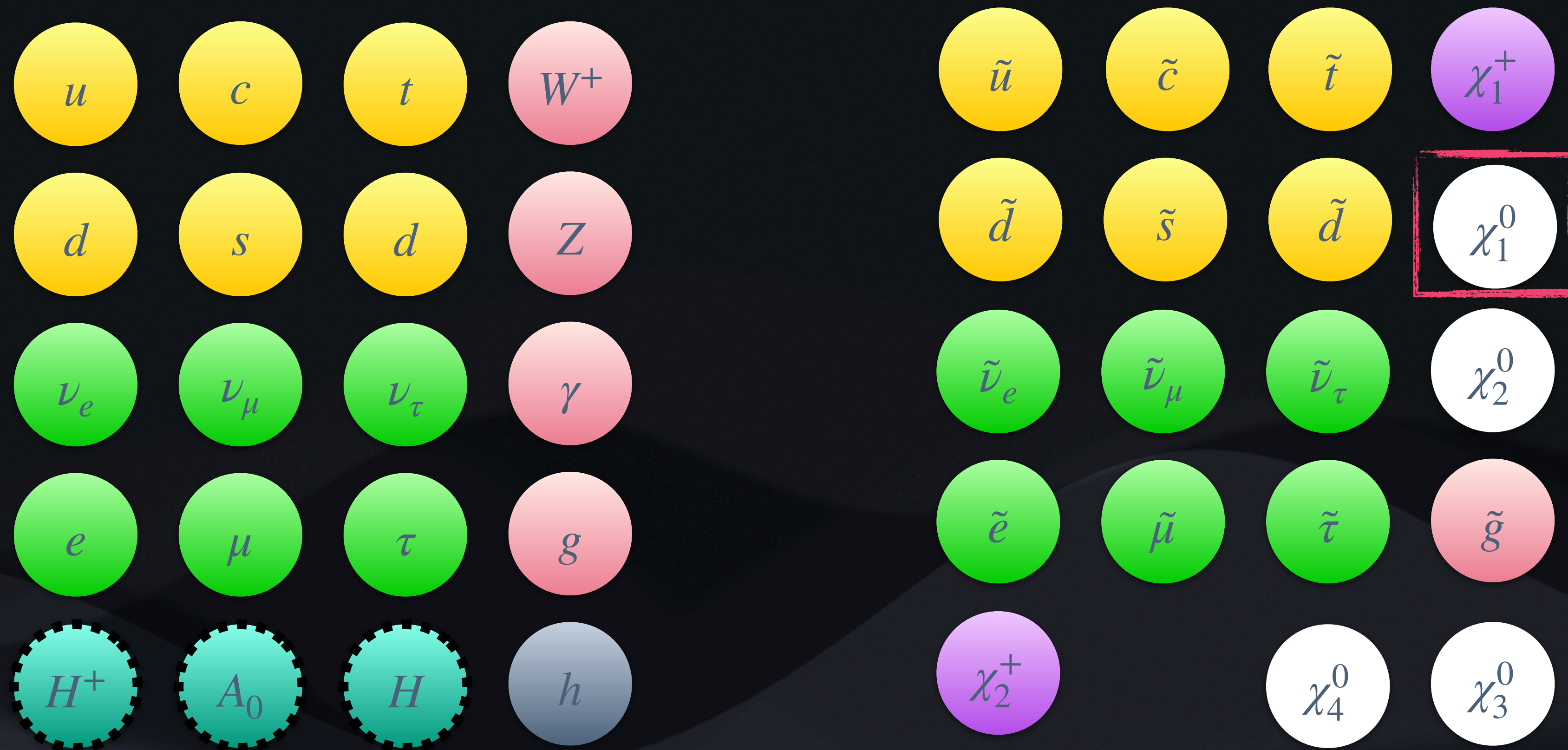
↑ Particle pairs

↑ QFT perturbation theory

Go to the blackboard I

The MSSM in a nutshell

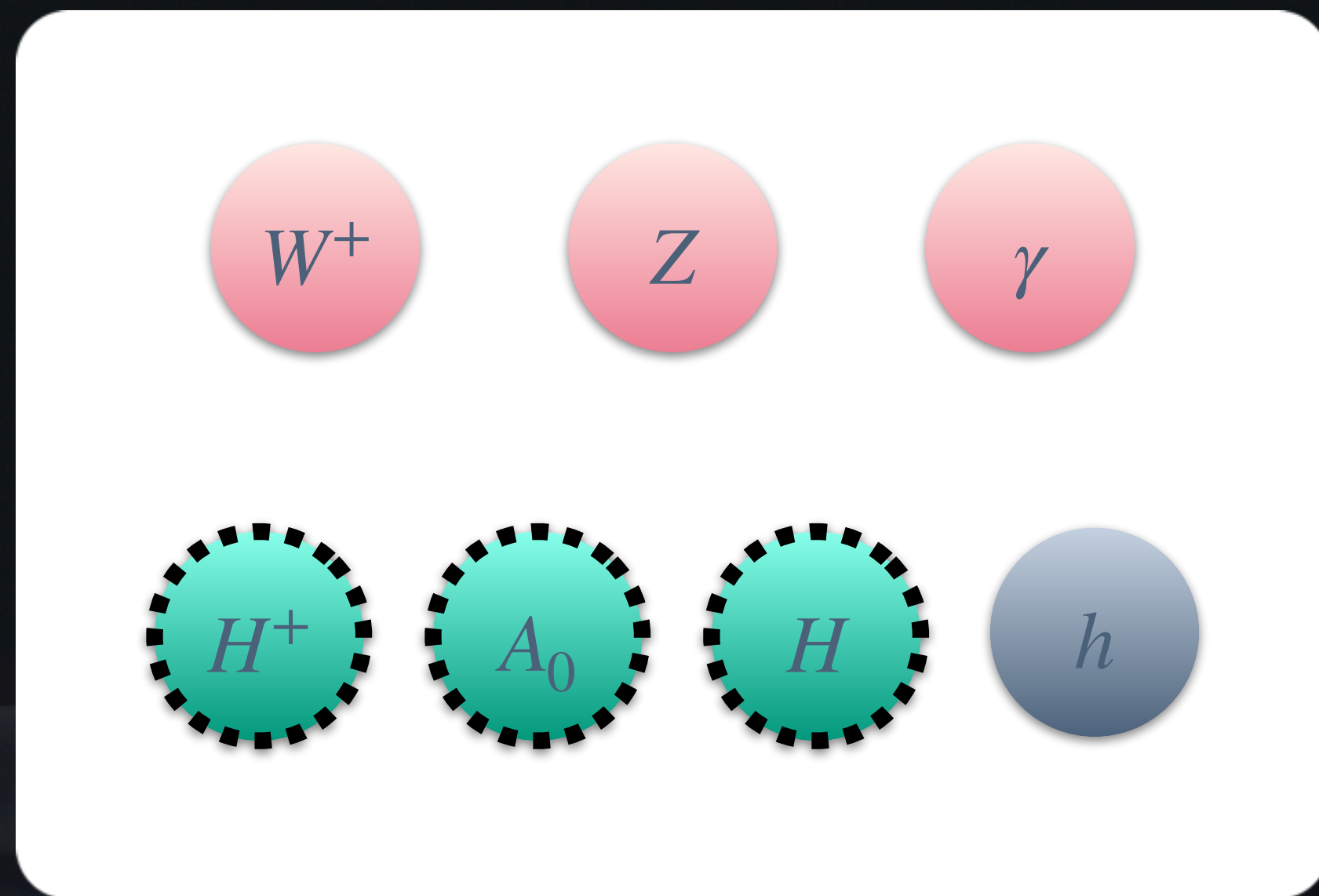
Particles and more particles



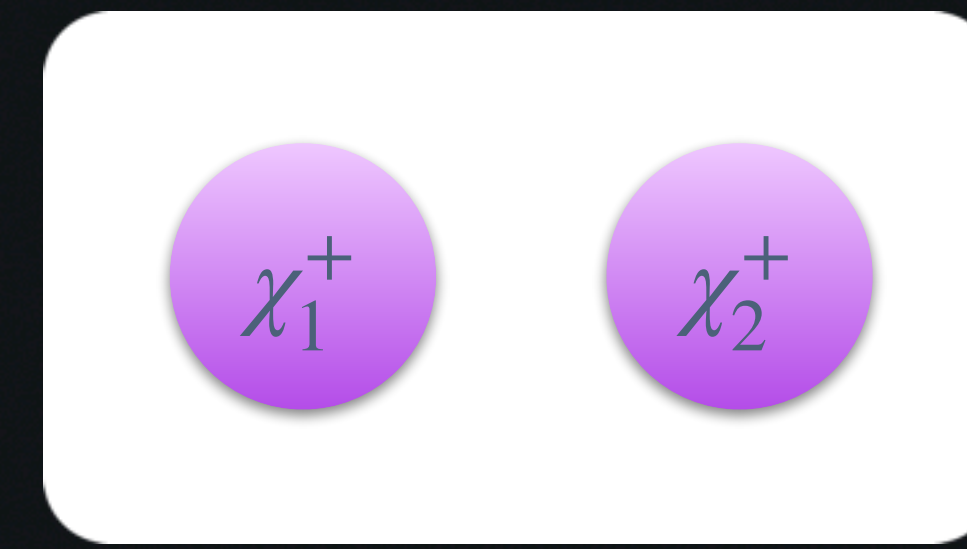
The MSSM in a nutshell

Neutralino/chargino sector

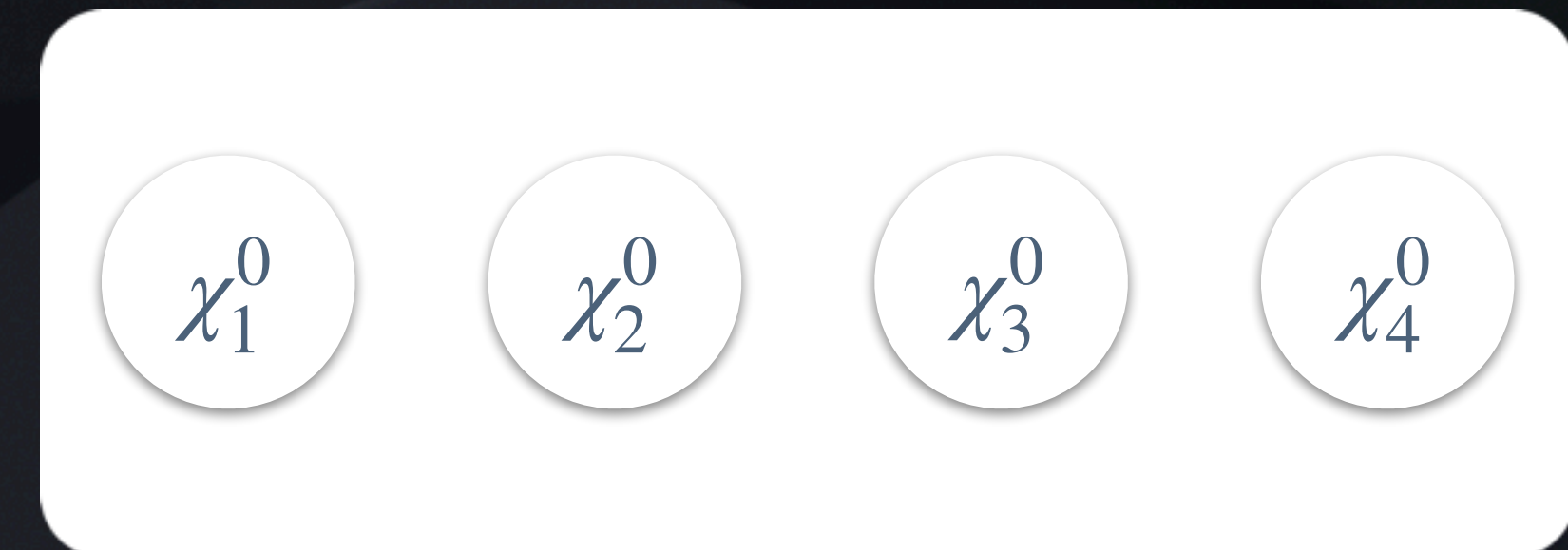
Mediators



Charginos



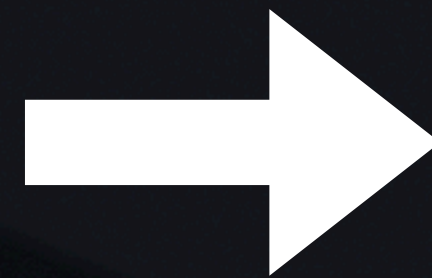
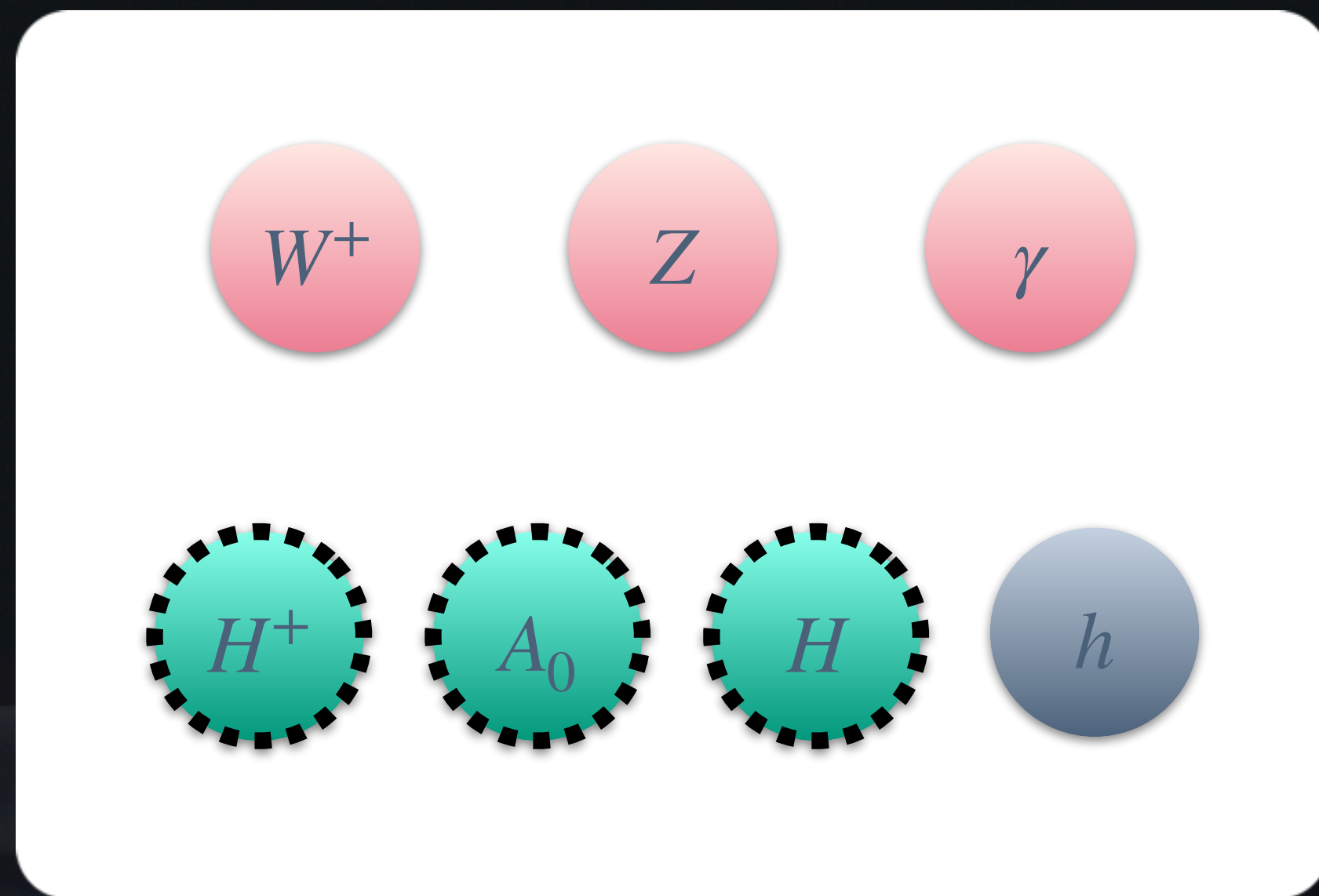
Neutralinos



Sommerfeld effect in the MSSM

Dark Matter NR potential

Mediators

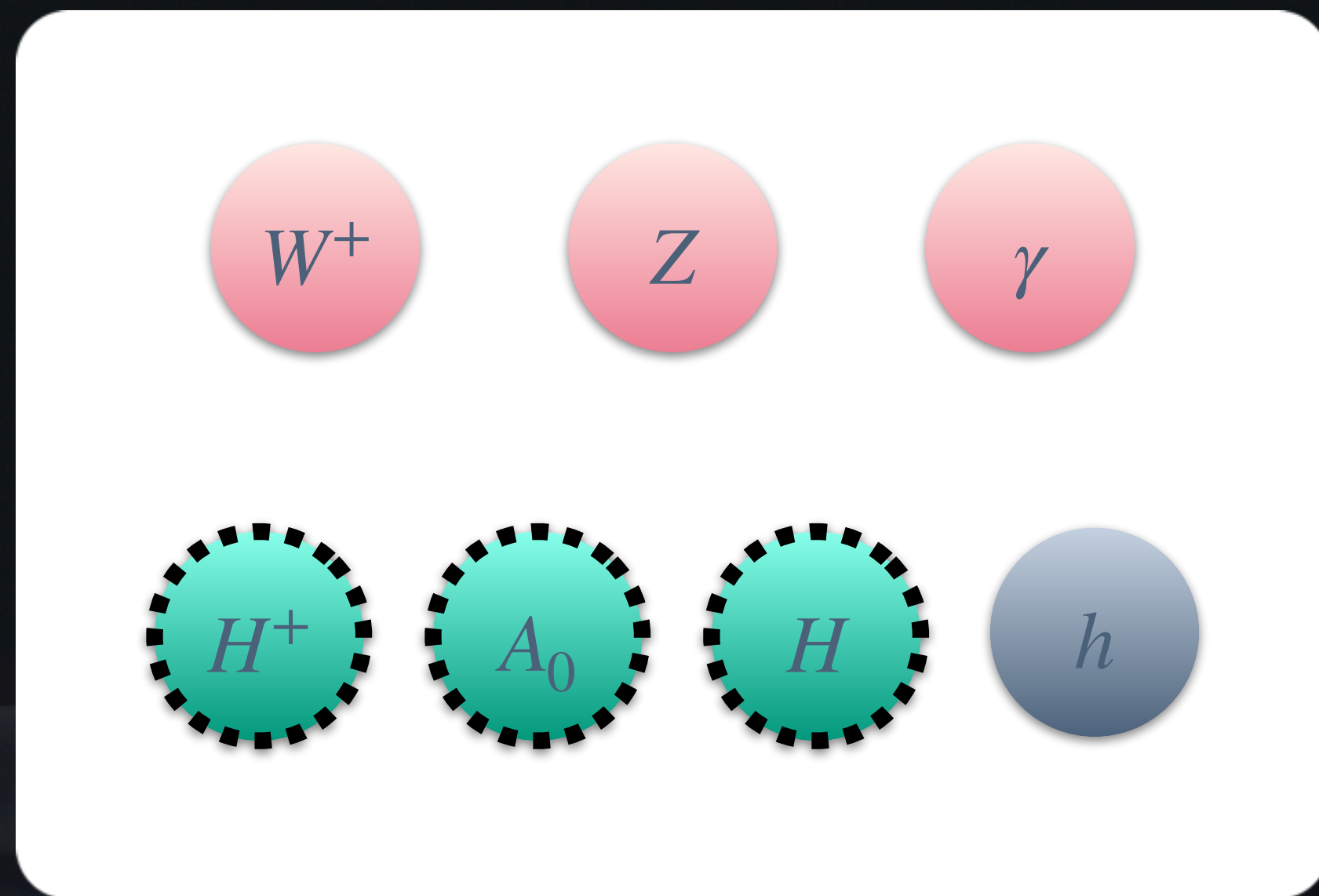


$$V(r) \sim \frac{\alpha}{r} + \frac{\alpha_{ew} e^{-m_W r}}{r} + \frac{\alpha_{ew} e^{-m_Z r}}{r} + \dots$$

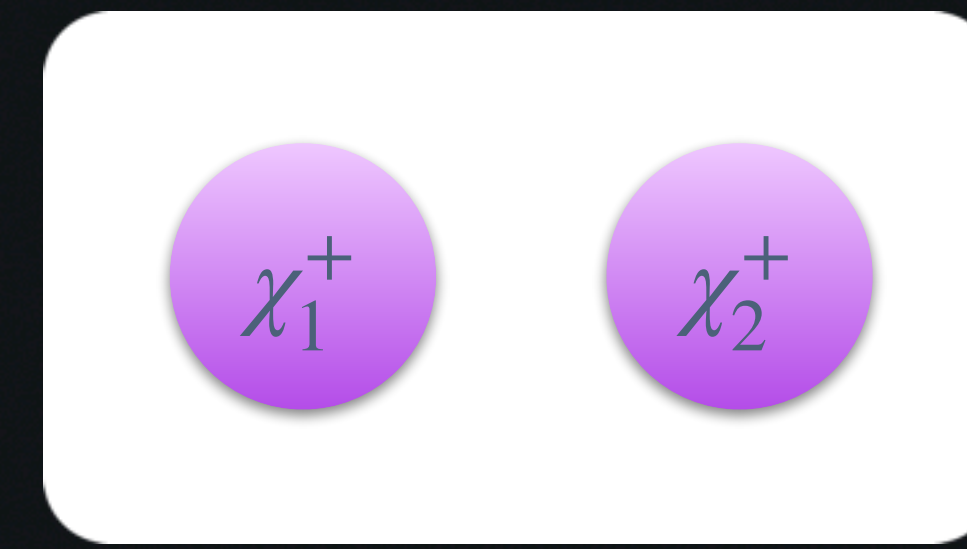
Sommerfeld effect in the MSSM

Dark Matter NR potential

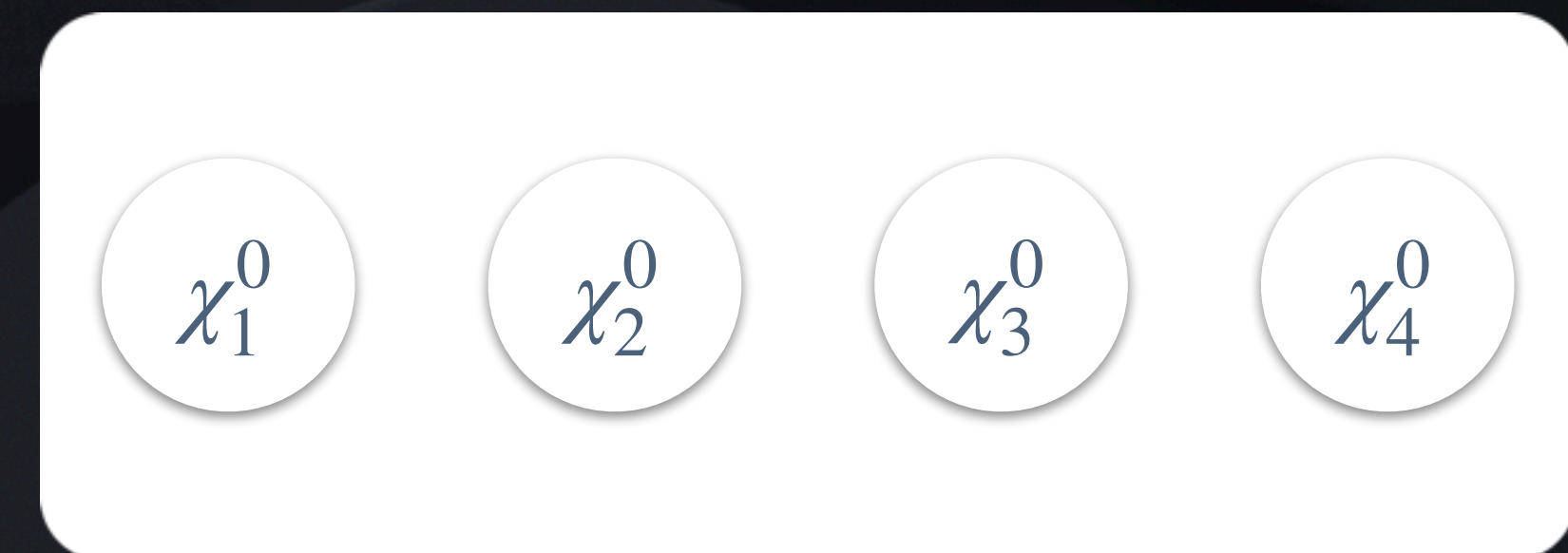
Mediators



Charginos



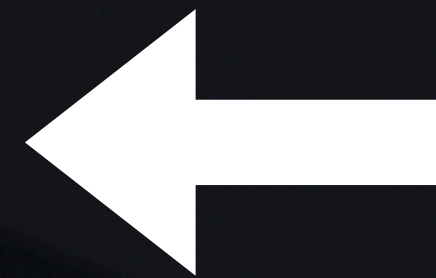
Neutralinos



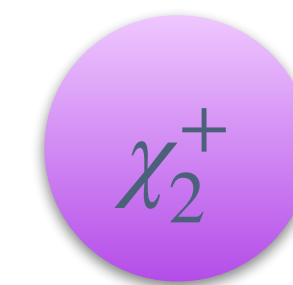
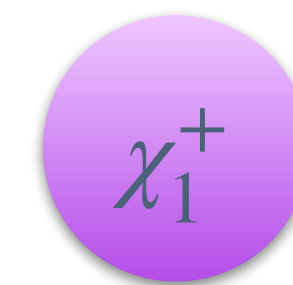
Sommerfeld effect in the MSSM

Dark Matter NR potential

$$V(r) \rightarrow V_{IJ}(r)$$



Charginos



Neutralinos



Sommerfeld effect in the MSSM

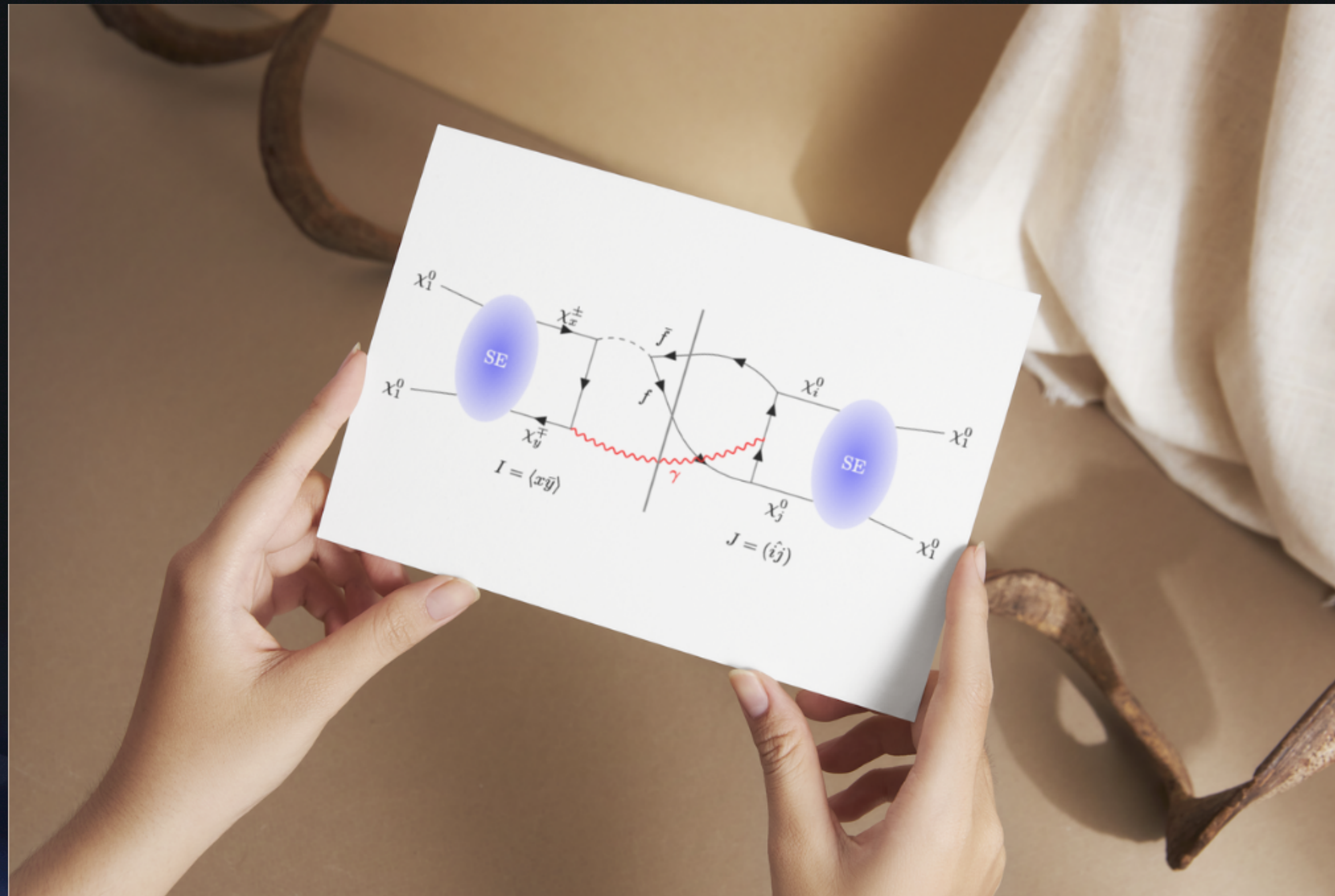
$$\frac{d \sigma \nu}{d E_\gamma} = 2 \sum_{I,J} S_{IJ} \left[\frac{d(\tilde{\sigma} \nu)}{d E_\gamma} \right]_{IJ}$$

14×14 matrix

↑

105 independent terms

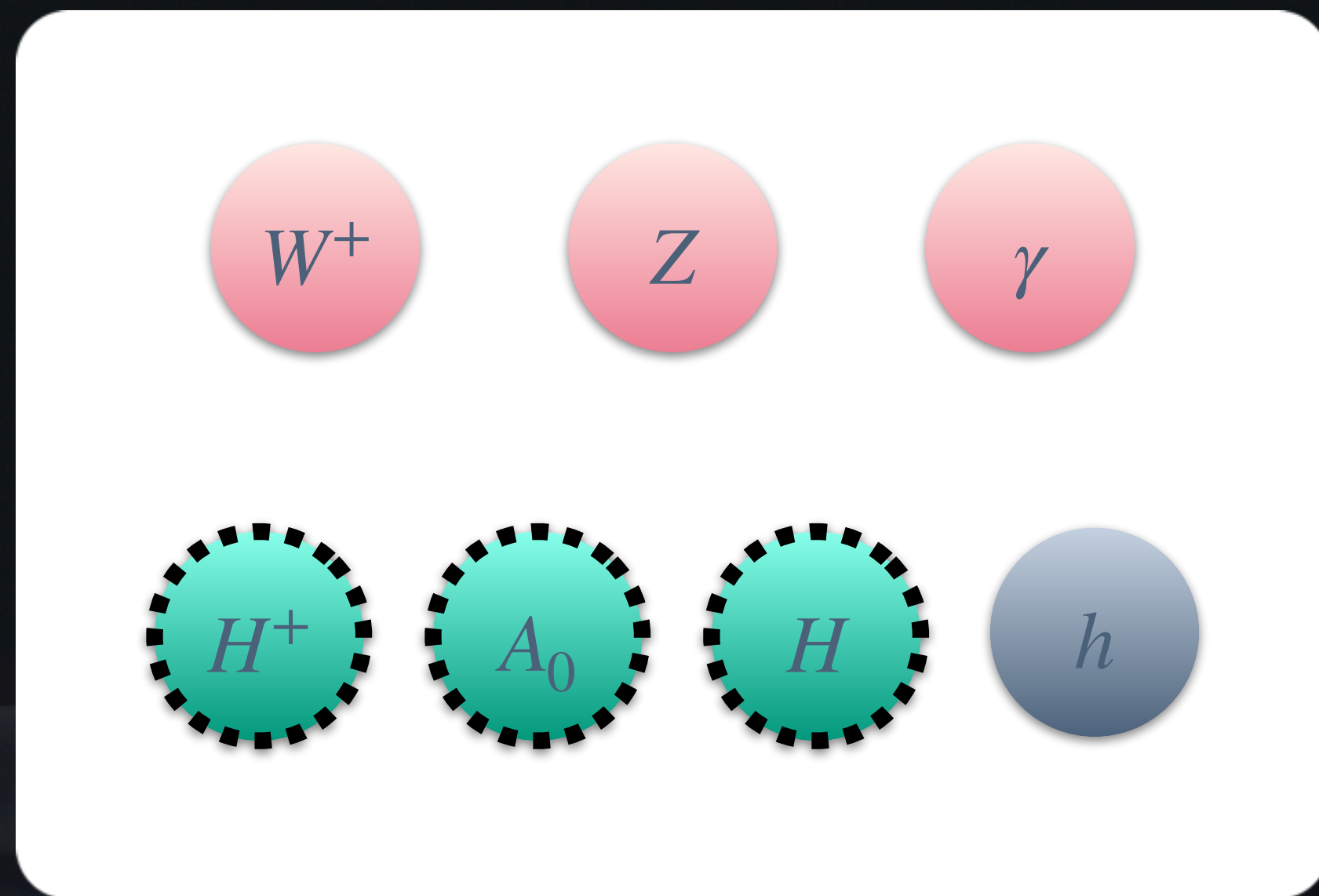
Jäger Vollmann 2023
arXiv: 2310.11067



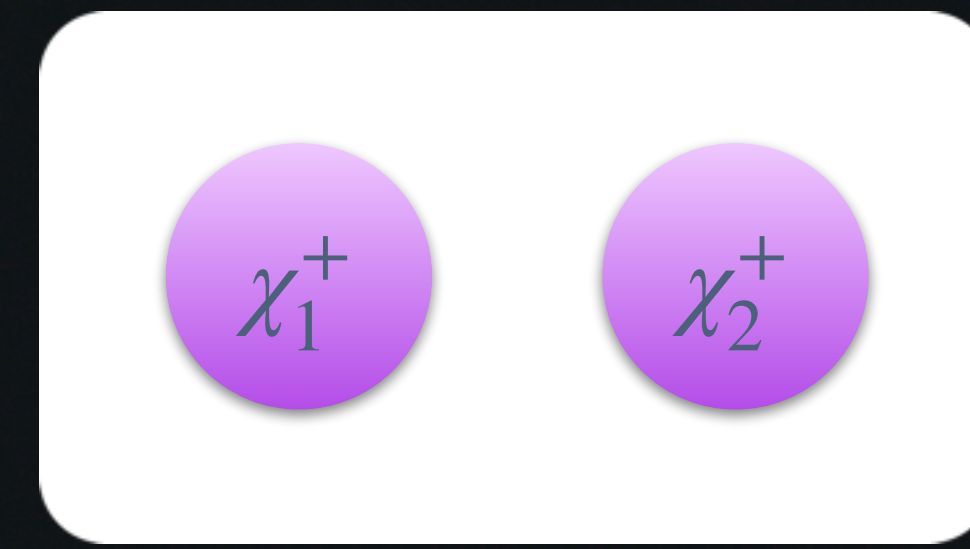
The MSSM in a nutshell

Neutralino/chargino sector

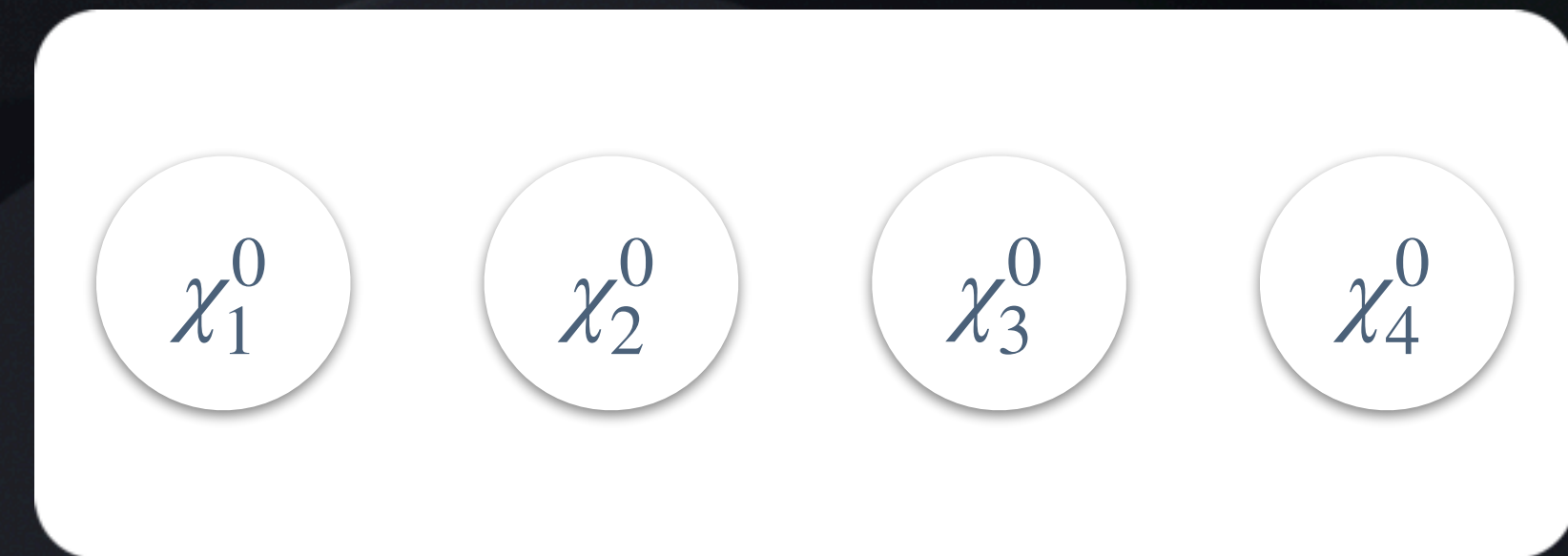
Mediators



Charginos



Neutralinos



Pure wino

Neutralinos



Charginos



Mediators



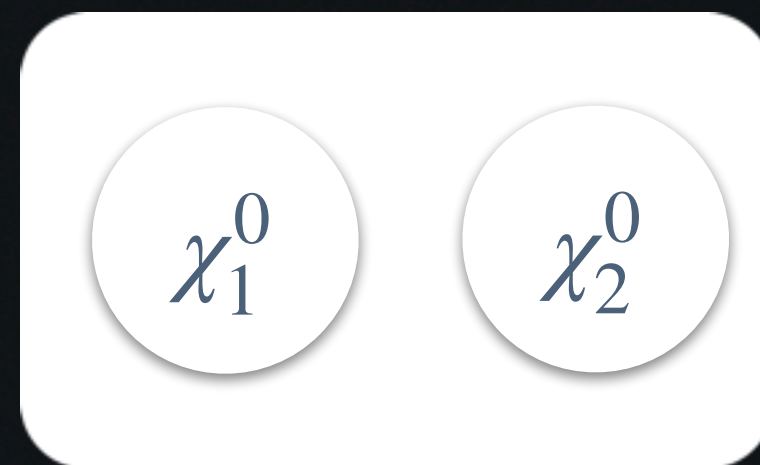
$$V(r) = \begin{pmatrix} 0 & -\sqrt{2}\alpha_2 \frac{e^{-m_W r}}{r} \\ -\sqrt{2}\alpha_2 \frac{e^{-m_W r}}{r} & -\frac{\alpha}{r} - \alpha_2 c_W^2 \frac{e^{-m_Z r}}{r} \end{pmatrix}$$

Further properties:

- $m_{\chi_1^0}^{\text{wimp}} \simeq 3 \text{ TeV}$
- $\frac{m_{\chi_1^+} - m_{\chi_1^0}}{m_{\chi_1^0}} \simeq 5.5 \times 10^{-5}$
- No couplings to quarks or gluons

Pure higgsino (see Linda's & Graham's slides)

Neutralinos



Charginos



Mediators



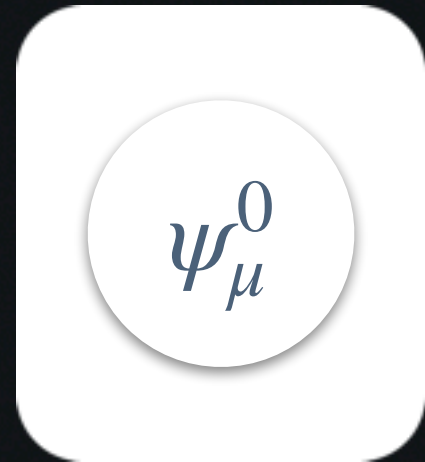
$$V(r) = \begin{pmatrix} 0 & -\frac{\alpha_2}{4c_W^2} \frac{e^{-m_Z r}}{r} & -\frac{\alpha_2}{2\sqrt{2}} \frac{e^{-m_W r}}{r} \\ -\frac{\alpha_2}{4c_W^2} \frac{e^{-m_Z r}}{r} & 0 & -\frac{\alpha_2}{2\sqrt{2}} \frac{e^{-m_W r}}{r} \\ -\frac{\alpha_2}{2\sqrt{2}} \frac{e^{-m_W r}}{r} & -\frac{\alpha_2}{2\sqrt{2}} \frac{e^{-m_W r}}{r} & -\frac{\alpha}{r} - \frac{\alpha_2 (s_W^2 - c_W^2)^2}{4c_W^2} \frac{e^{-m_Z r}}{r} \end{pmatrix}$$

Further properties:

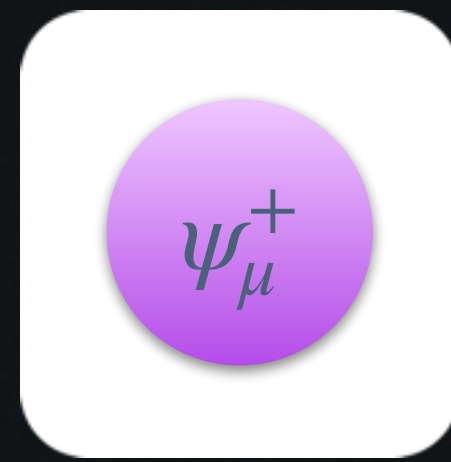
- $m_{\chi_1^0}^{\text{wimp}} \simeq 1 \text{ TeV}$
- $\frac{m_{\chi_1^+} - m_{\chi_1^0}}{m_{\chi_1^0}} \simeq 3.5 \times 10^{-4}$
- No couplings to quarks or gluons
 - Small admixture with wino/bino required in order to avoid direct-detection constraints

Motokino

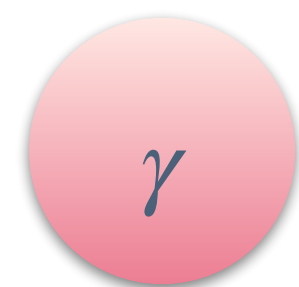
Motokino DM



Charged Motokino



Mediators



$$V^{\text{even } S}(r) = \begin{pmatrix} 0 & -\sqrt{2}\alpha_2 \frac{e^{-m_W r}}{r} \\ -\sqrt{2}\alpha_2 \frac{e^{-m_W r}}{r} & -\frac{\alpha}{r} - \alpha_2 c_W^2 \frac{e^{-m_Z r}}{r} \end{pmatrix}$$

Further properties:

- $m_{\psi^0}^{\text{wimp}}$ depend on th. parameters
- No couplings to quarks or gluons
- Identical potential as for wino DM

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Conclusions

Endpoint resumptions

TBA

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	Fixed-order $2 \rightarrow 2$ (tree) + Parton Shower
	Fixed-order $2 \rightarrow 3$ (tree) + Parton Shower
	Fixed-order $2 \rightarrow 2$ + Parton Shower + Sommerfeld factor
	Fixed-order $2 \rightarrow 3$ + Parton Shower + Sommerfeld factor

flux



energy

TBA

The Basics of Annihilation

	Fixed-order $2 \rightarrow 2$ (tree) + Parton Shower
	Fixed-order $2 \rightarrow 3$ (tree) + Parton Shower
	Fixed-order $2 \rightarrow 2$ + Parton Shower + Sommerfeld factor
	Fixed-order $2 \rightarrow 3$ + Parton Shower + Sommerfeld factor



All-order $2 \rightarrow N$ **next-to-leading (prime) Sudakov logs**
+ Parton Shower +
Sommerfeld factor

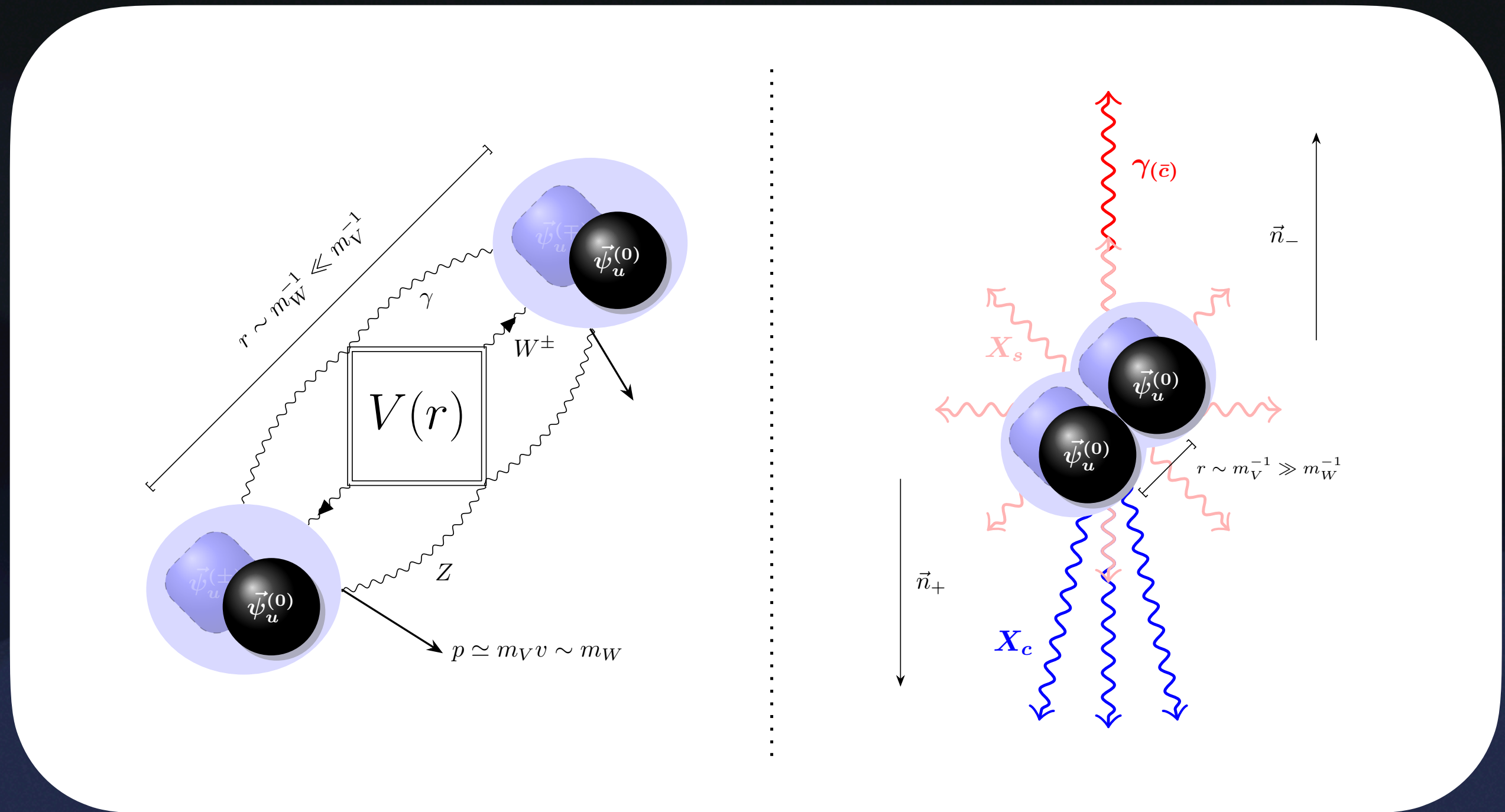


All-order 2 → N **next-to-leading (prime) Sudakov logs**
 + Parton Shower +
 Sommerfeld factor

Baumgart, Cohen et al — [1712.07656](#)

Beneke, Broggio, Hasner, MV, Urban — [1903.08702](#)

Fujiwara, Vollmann — [2411.XXXX](#)



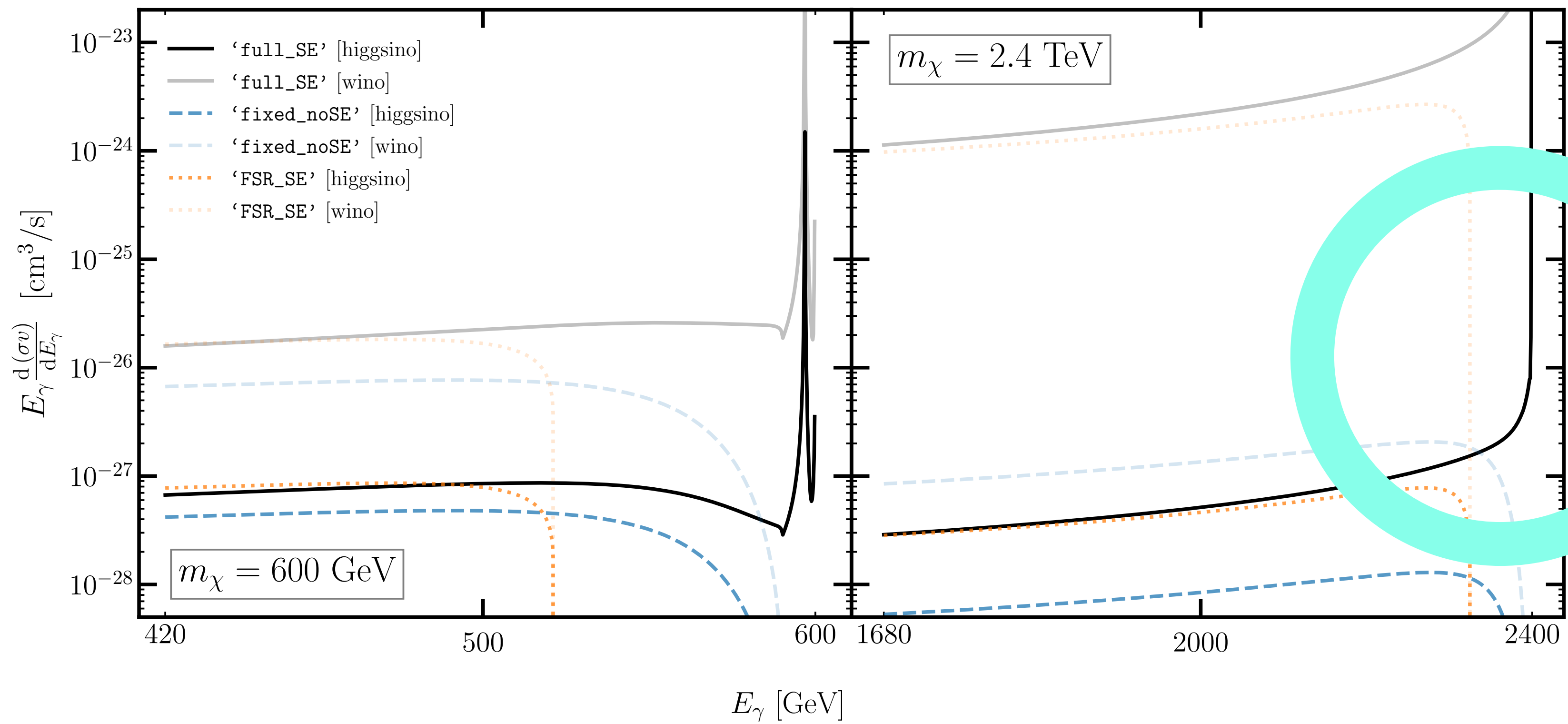
Resummation

Goal: factor out the “gorillas”

$$\frac{d\sigma\nu}{dE_\gamma} = f\left(\alpha_{ew} \times \text{gorilla}\right) \times \left(\# \alpha_{ew}^3 + \mathcal{O}(\alpha_{ew}^4)\right)$$

“safe” to use perturbation theory

?



Sudakov double-log resummation

Soft-collinear effective field theory approach

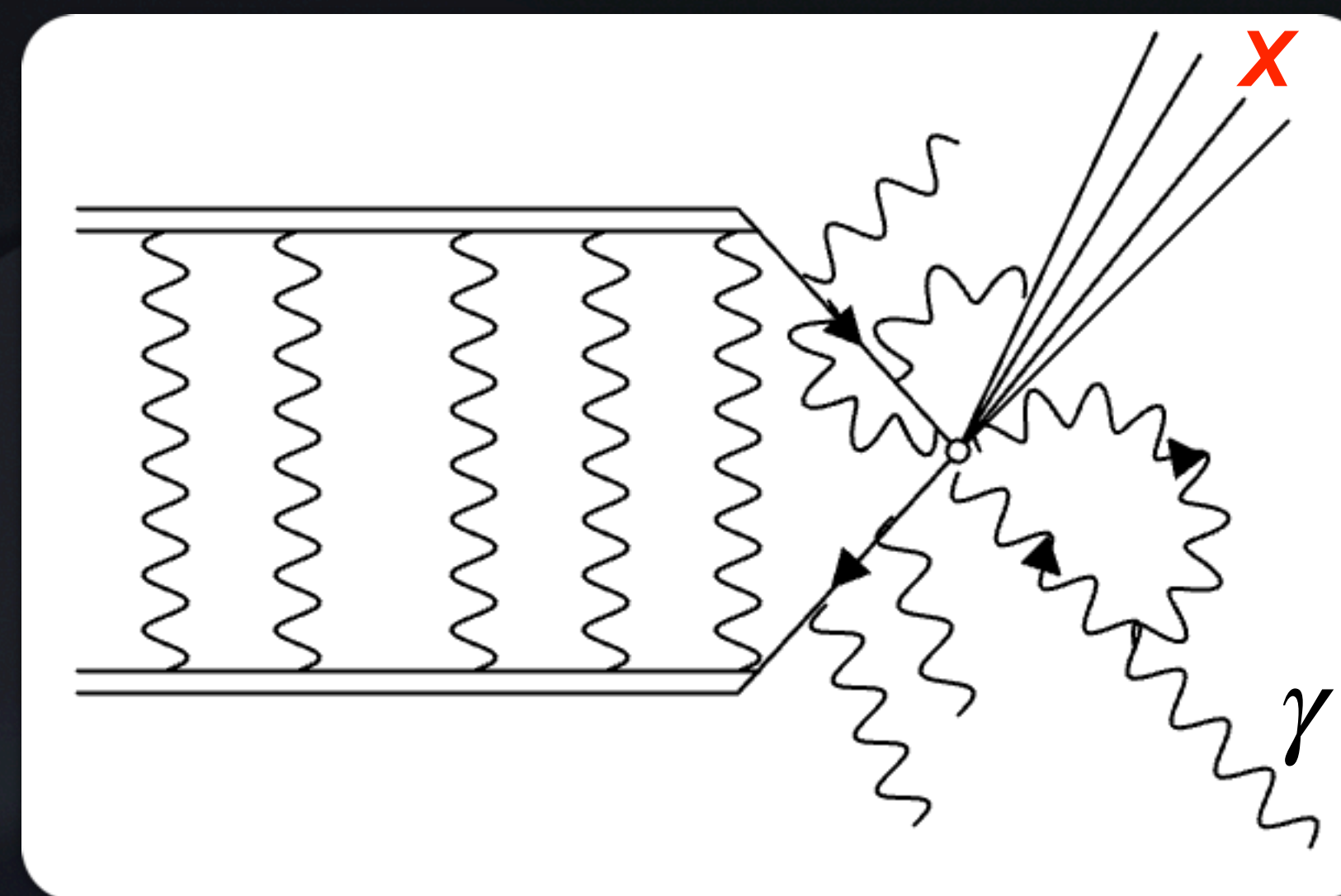
$$\left[\frac{d(\tilde{\sigma}_\gamma)^S}{dE_\gamma} \right]_{IJ} = \frac{1}{(\sqrt{2})^{n_{id}}} \frac{1}{9} \frac{2}{\pi m_V} \sum_{\mathcal{J}, \bar{\mathcal{J}}=0,2} \sum_{i,j} \kappa_{ij}^S H_{\mathcal{J}, \bar{\mathcal{J}}}^{S;i,j} Z_\gamma^{33} \times \int d\omega J(4m_V(m_V - E - \omega/2)) W_{\mathcal{J}, \bar{\mathcal{J}}; IJ}(\omega)$$

Six Motokino-annihilation operators

$$\begin{aligned} \mathcal{O}_{\mathcal{J}}^{(0)} &= \tilde{\Upsilon}_{u\alpha}^A \eta_{u\alpha}^{\beta\gamma} \tilde{\Upsilon}_{u\beta}^B T_{\mathcal{J}}^{ABCD} \tilde{\mathcal{A}}_{\perp c, \mu}^C(s n_+) \eta_{\perp}^{\mu\nu} \tilde{\mathcal{A}}_{\perp \bar{c}, \nu}^D(t n_-), \\ \mathcal{O}_{\mathcal{J}}^{(2)1} &= \tilde{\Upsilon}_{u\alpha}^A \tilde{\Upsilon}_{u\beta}^B T_{\mathcal{J}}^{ABCD} (\eta_{\perp}^{\alpha\mu} \eta_{\perp}^{\beta\nu} + \eta_{\perp}^{\alpha\nu} \eta_{\perp}^{\beta\mu}) \tilde{\mathcal{A}}_{\perp c, \mu}^C(s n_+) \tilde{\mathcal{A}}_{\perp \bar{c}, \nu}^D(t n_-) - \frac{2}{3} \mathcal{O}_{\mathcal{J}}^{(0)} \\ \mathcal{O}_{\mathcal{J}}^{(2)2} &= \tilde{\Upsilon}_{u\alpha}^A (n_+ - n_-)^\alpha \tilde{\Upsilon}_{u\beta}^B (n_+ - n_-)^\beta T_{\mathcal{J}}^{ABCD} \tilde{\mathcal{A}}_{\perp c, \mu}^C(s n_+) \eta_{\perp}^{\mu\nu} \tilde{\mathcal{A}}_{\perp \bar{c}, \nu}^D(t n_-) \\ &\quad + \frac{4}{3} \mathcal{O}_{\mathcal{J}}^{(0)}; \end{aligned}$$

$$+ \frac{3}{4} \mathcal{O}_{\mathcal{J}}^{(2)}$$

Endpoint $\rightarrow m_X^2 \ll 4m_\chi^2$



Go to the blackboard II

Outline

Motivation

Indirect detection

Sommerfeld factor

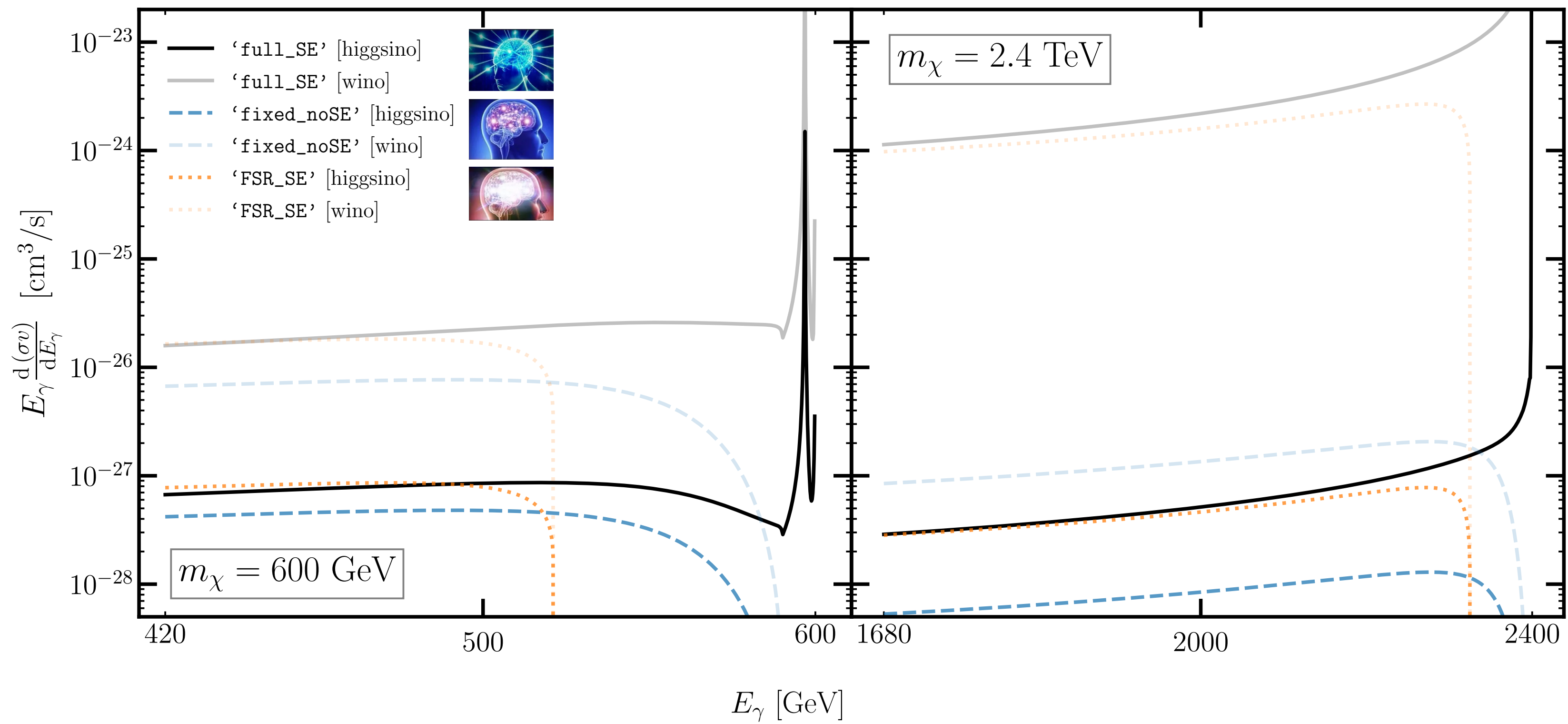
Endpoint resummations

Plots

Conclusions

Plots

Without further due...



Meme legend



Fixed-order 2 \rightarrow 3
(tree)
+ Parton Shower

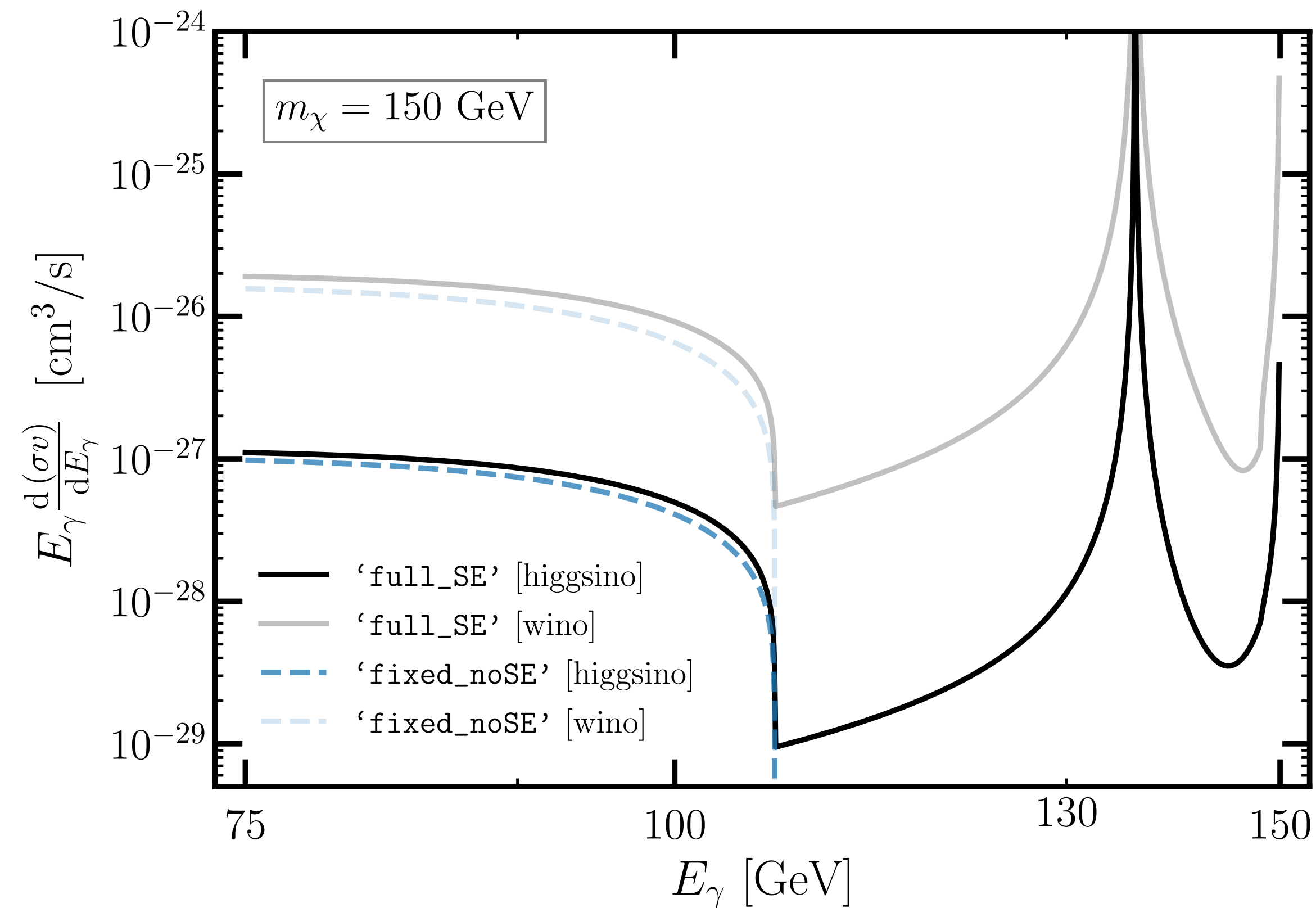
Fixed-order 2 \rightarrow 2
+ Parton Shower +
**Sommerfeld
factor**

Fixed-order 2 \rightarrow 3
+ Parton Shower +
**Sommerfeld
factor**

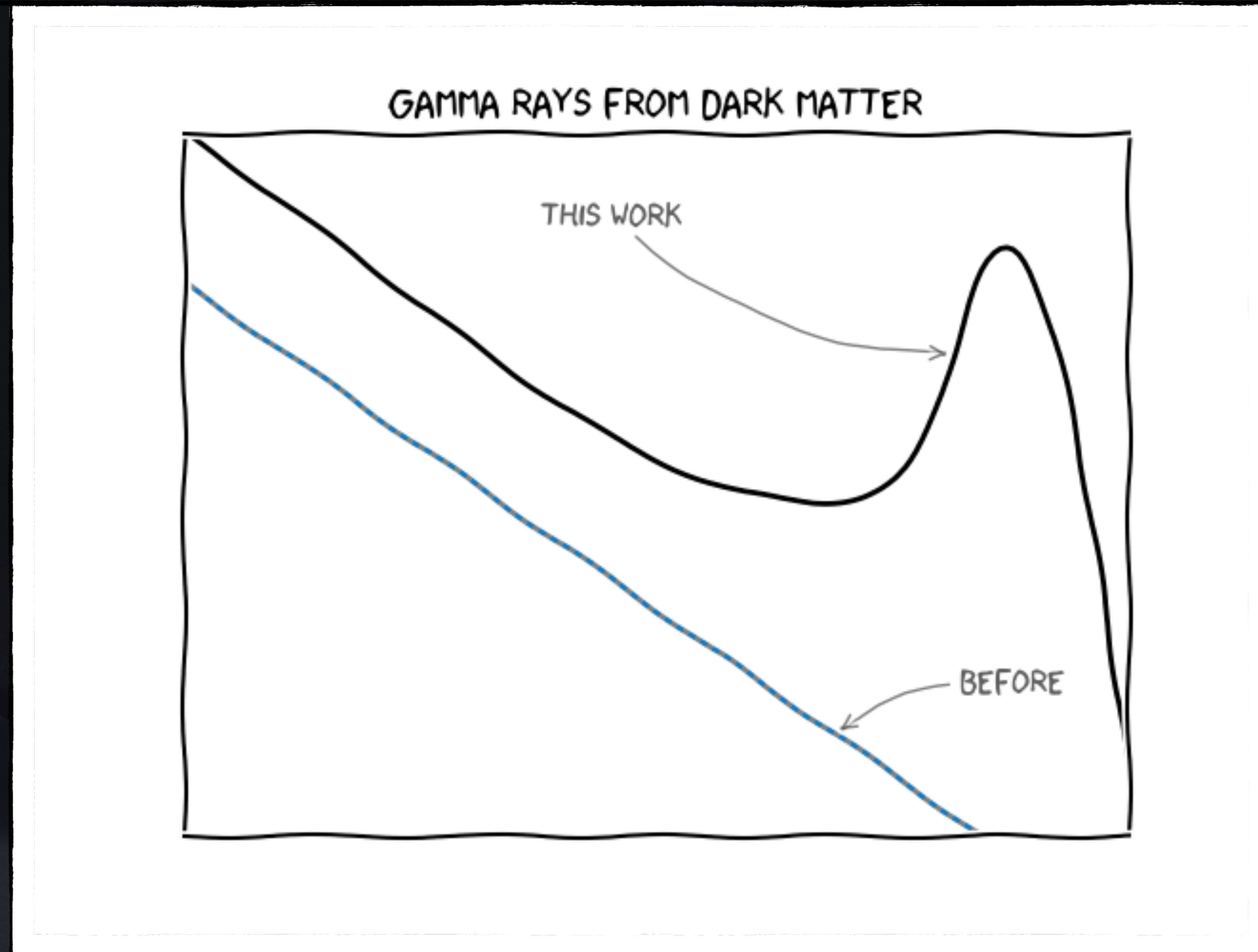
— ‘full_SE’ [higgsino]
— ‘full_SE’ [wino]
- - - ‘fixed_noSE’ [higgsino]
- - - ‘fixed_noSE’ [wino]
... ‘FSR_SE’ [higgsino]
... ‘FSR_SE’ [wino]

Lighter winos/higgsinos

Kinematic $W^+W^-\gamma$ threshold “lifted” by the Sommerfeld effect

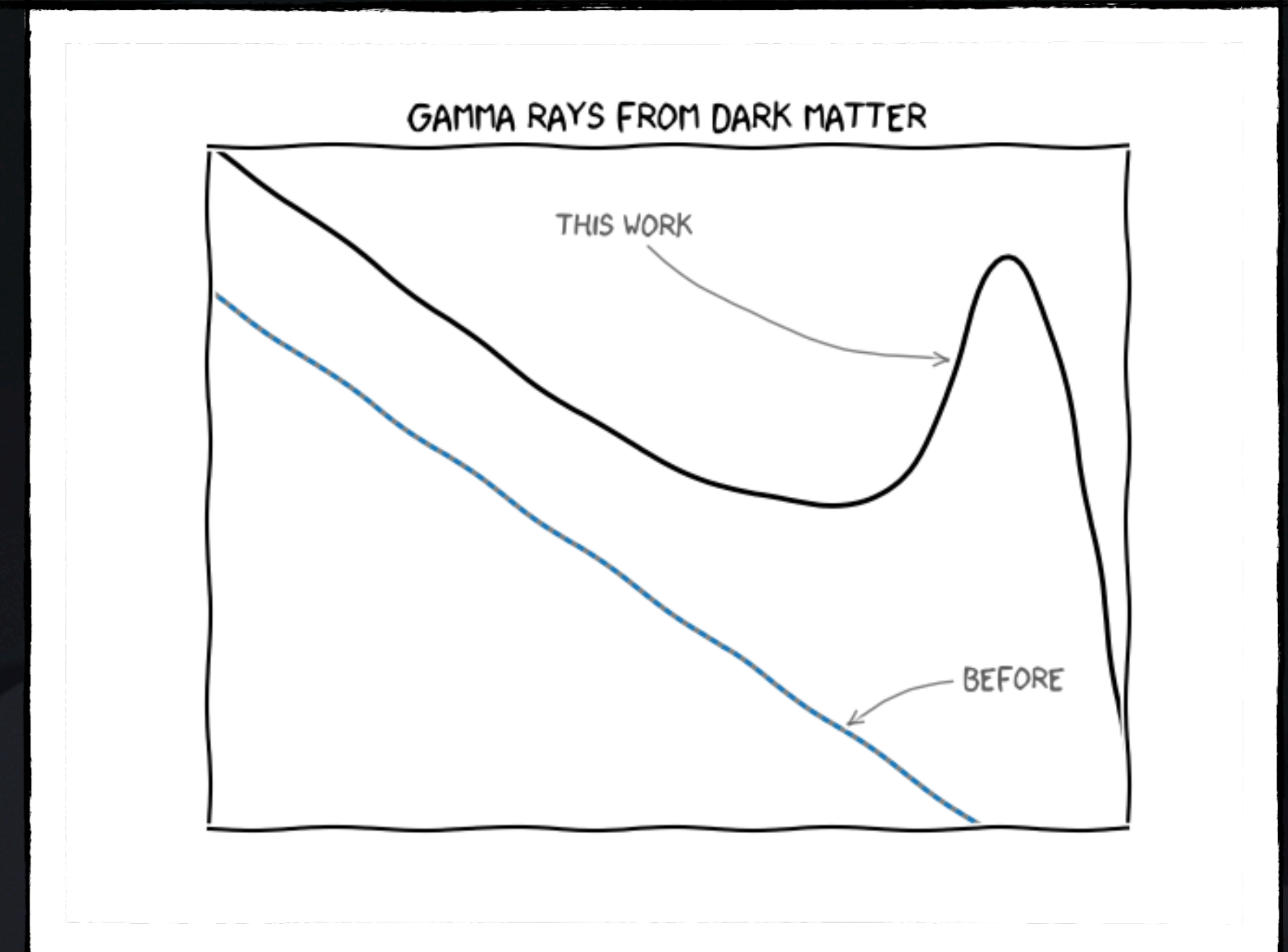
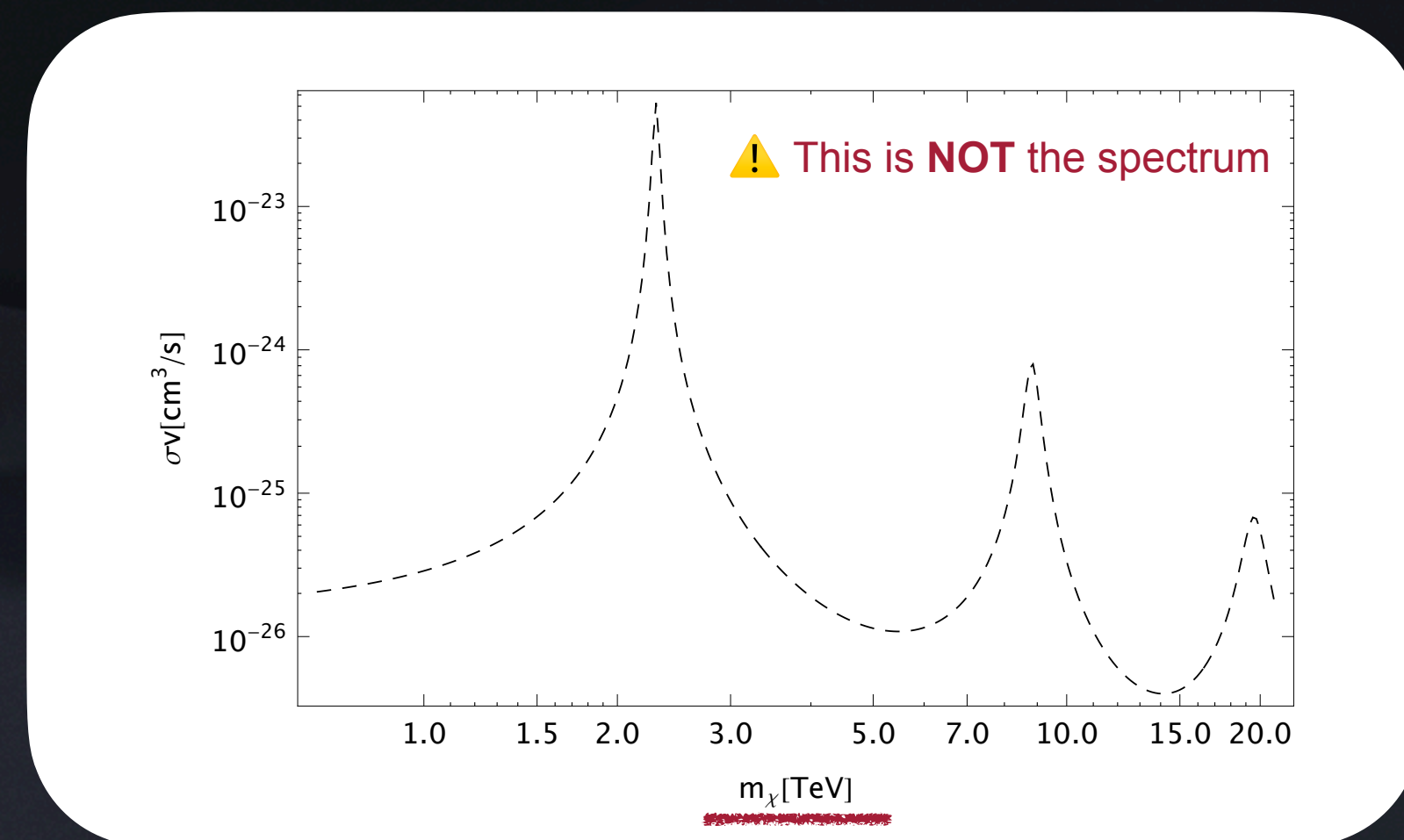
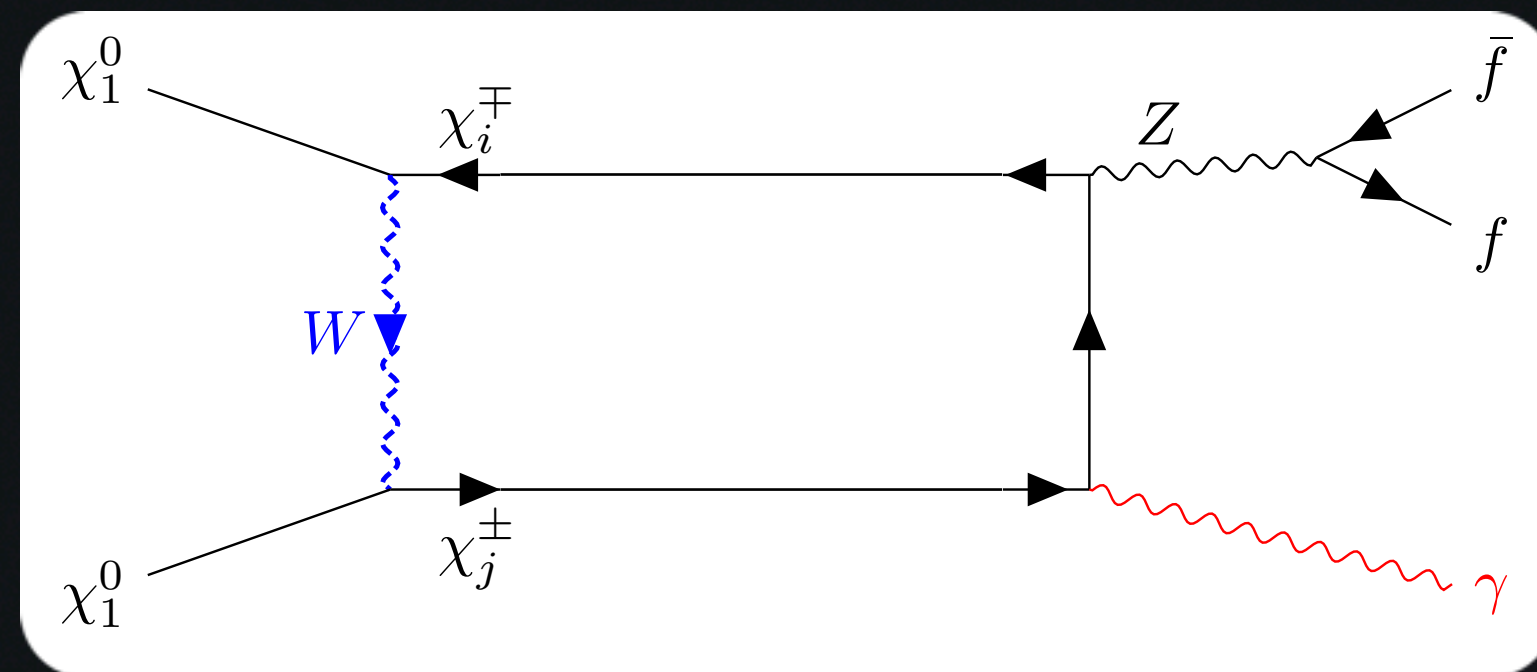


What's going on ?



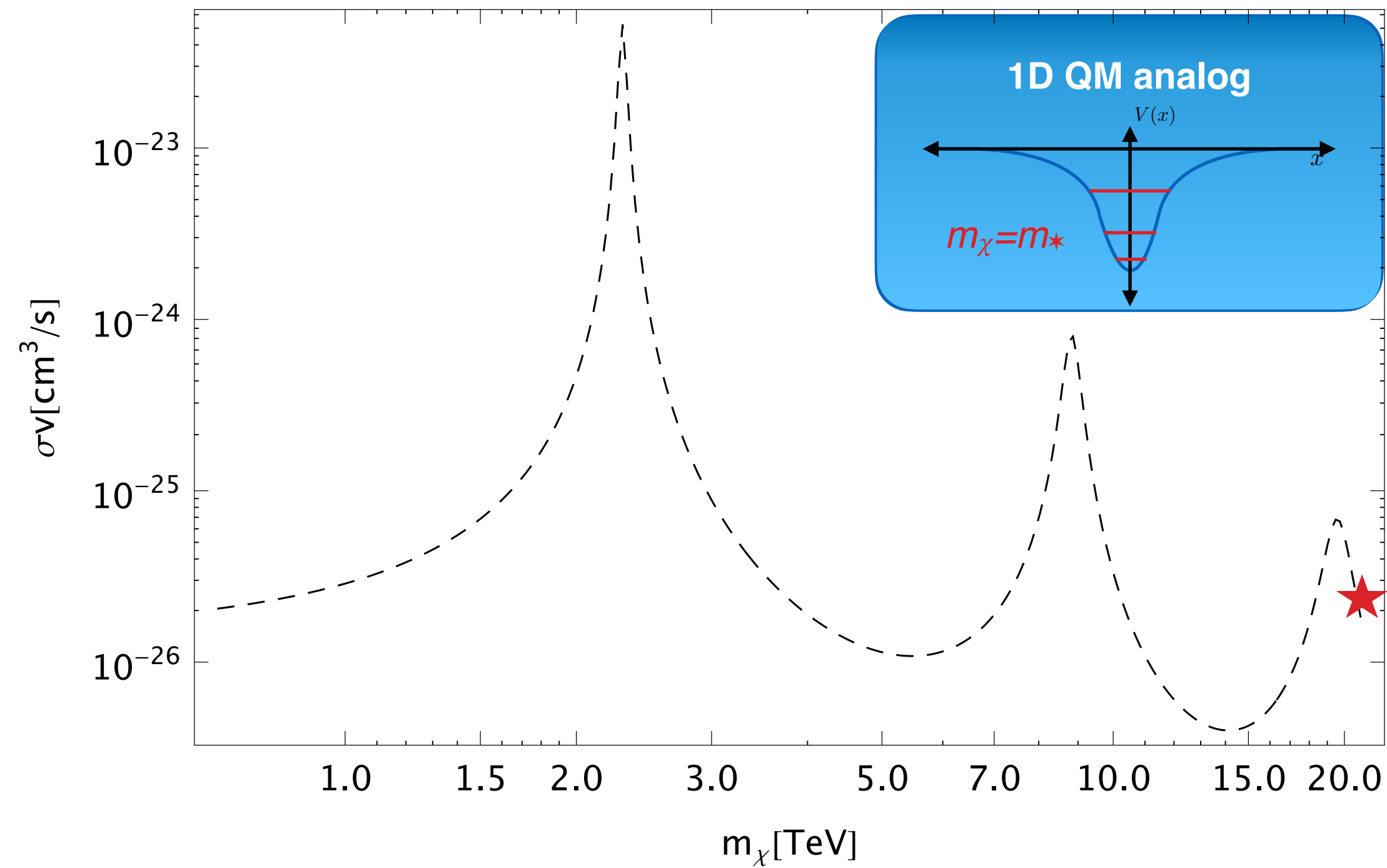
What's going on ?

Charginos are electrically charged / Sommerfeld resonances



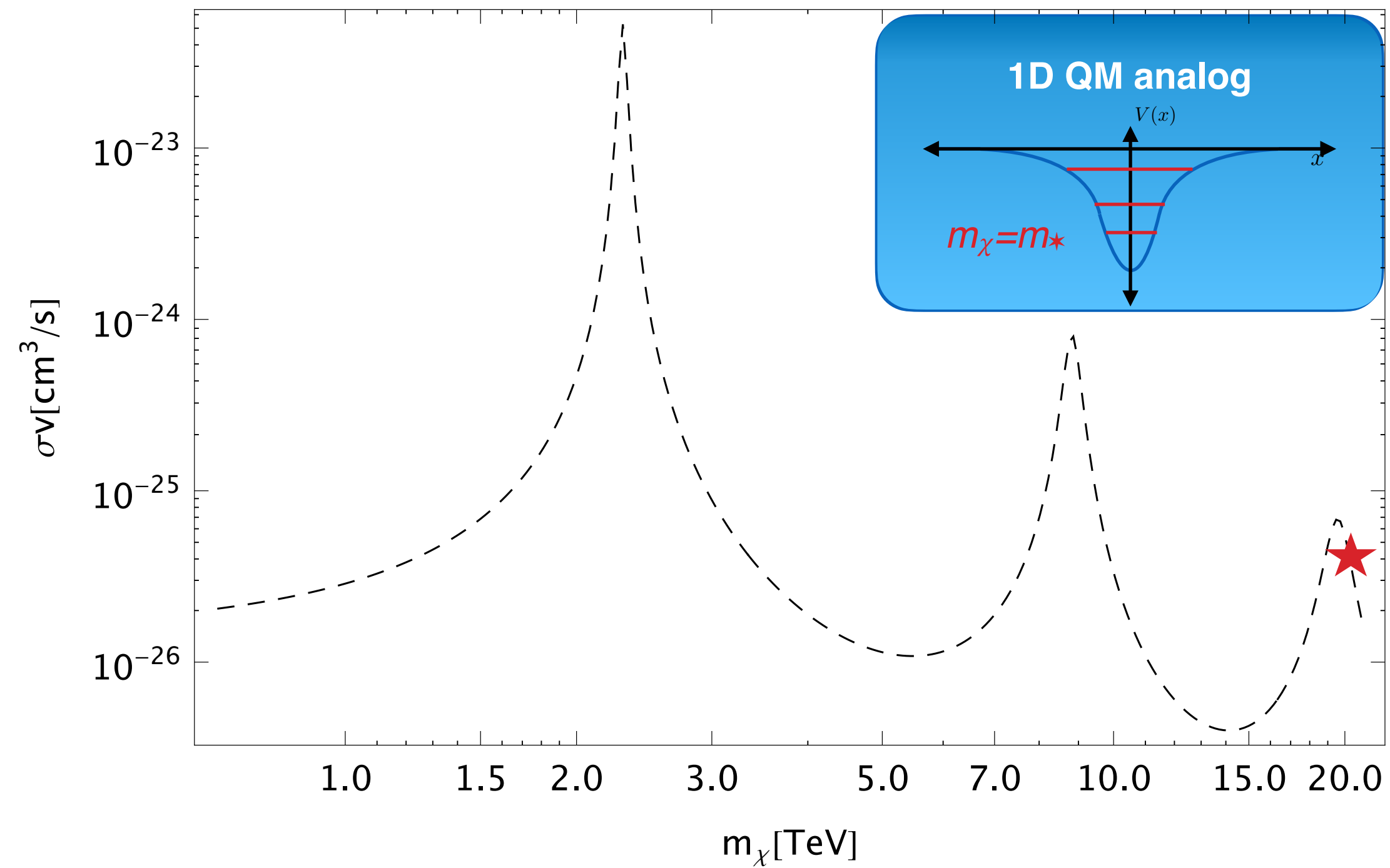
What's going on ?

Sommerfeld resonances



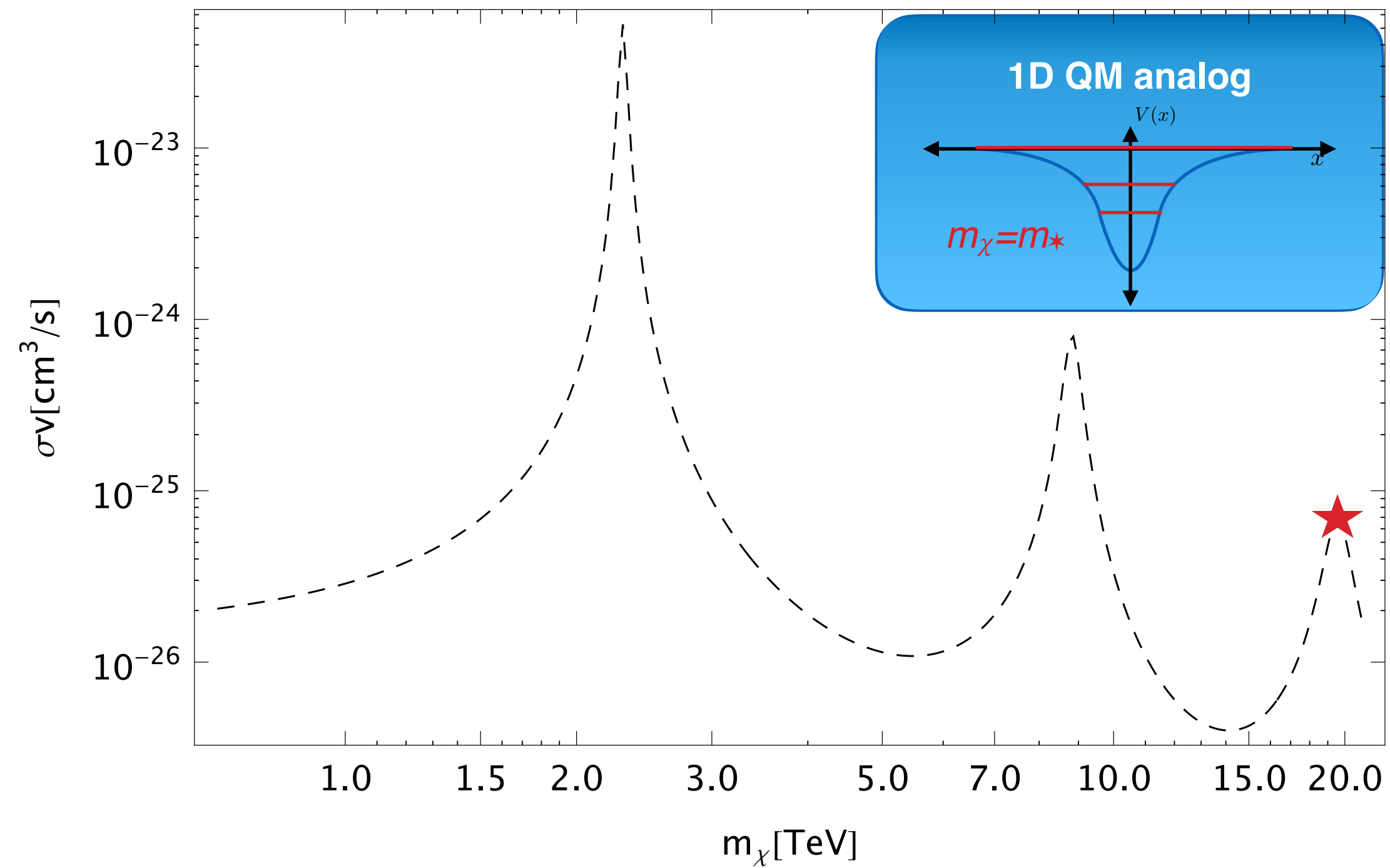
What's going on ?

Sommerfeld resonances



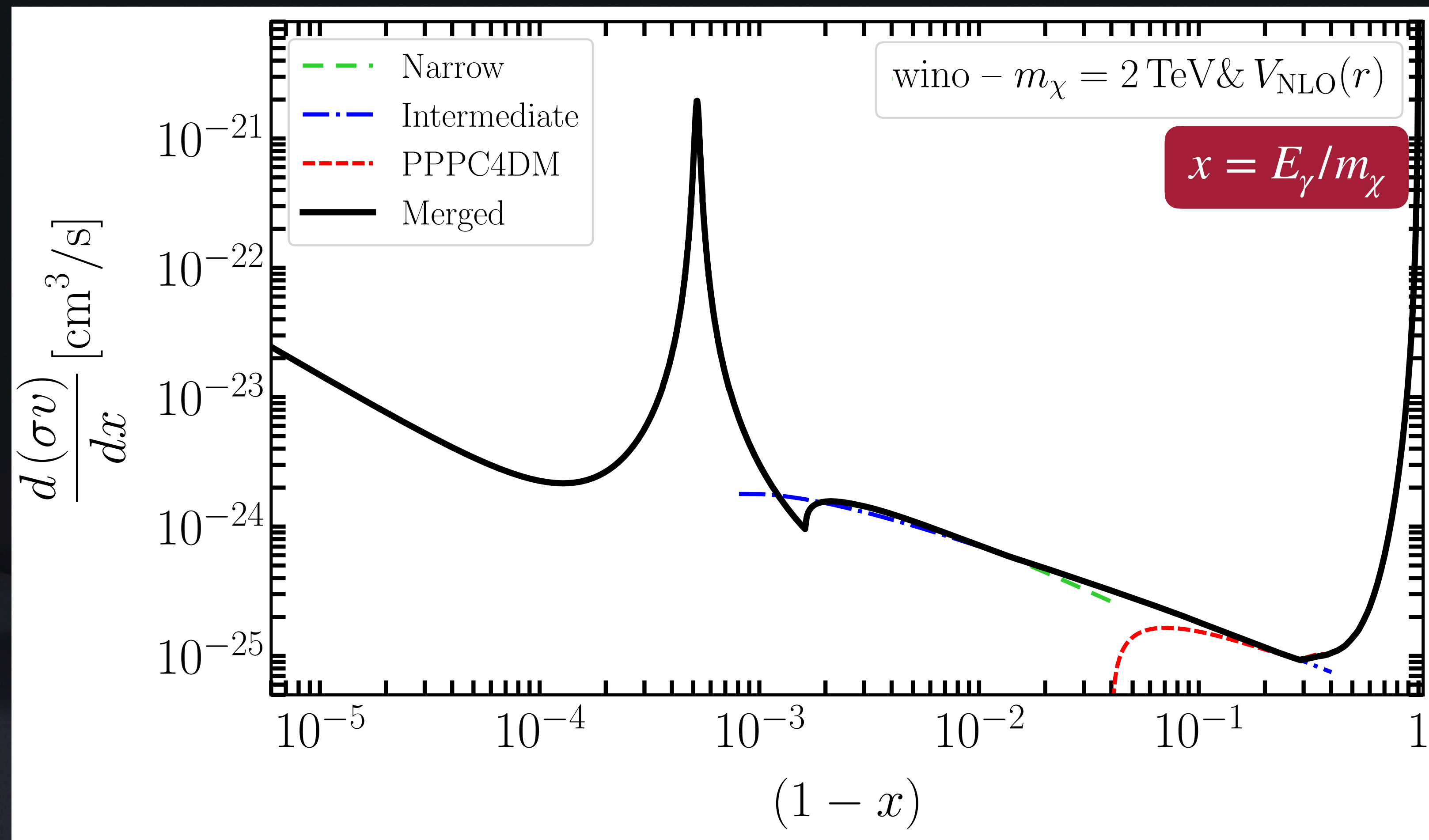
What's going on ?

Sommerfeld resonances

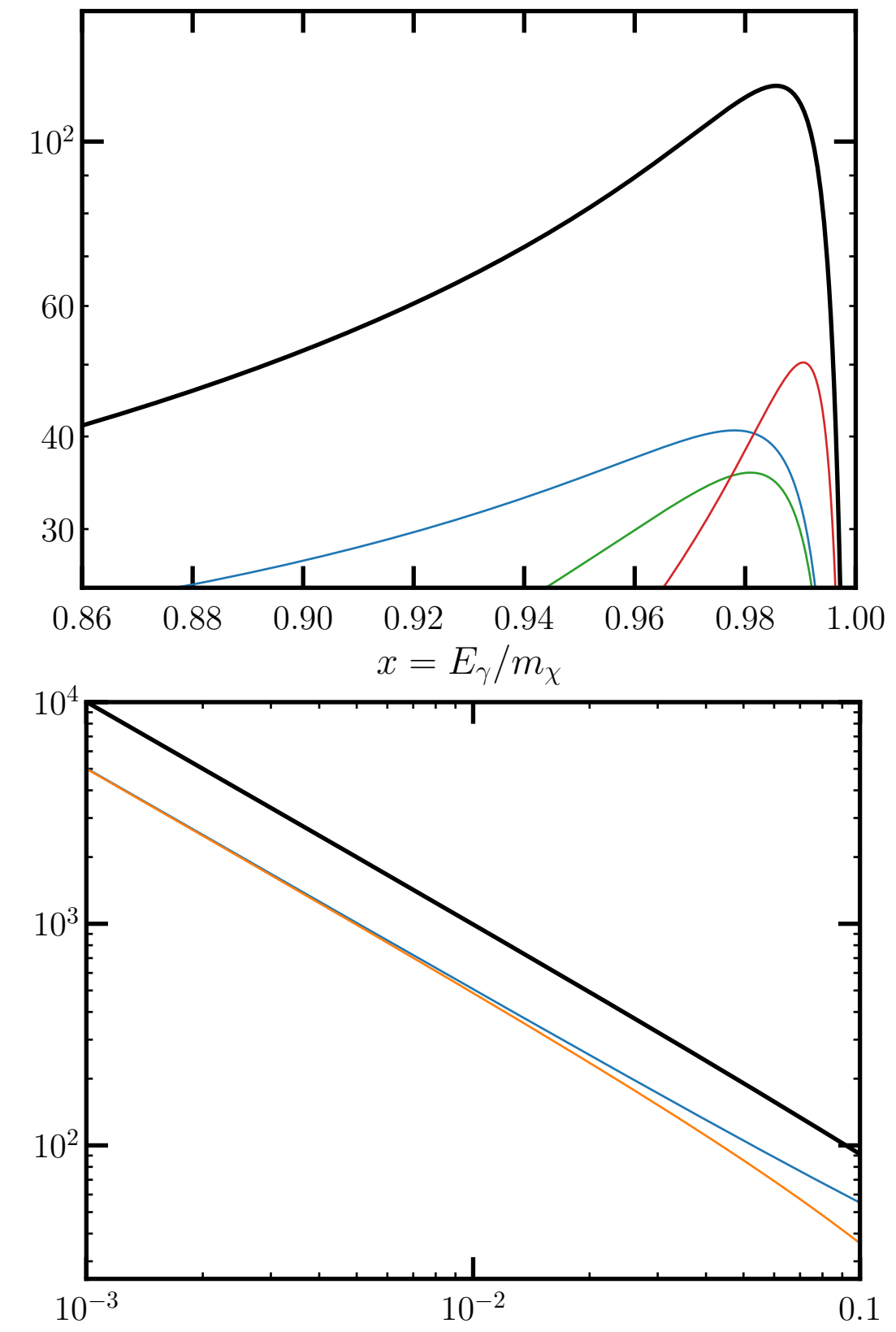
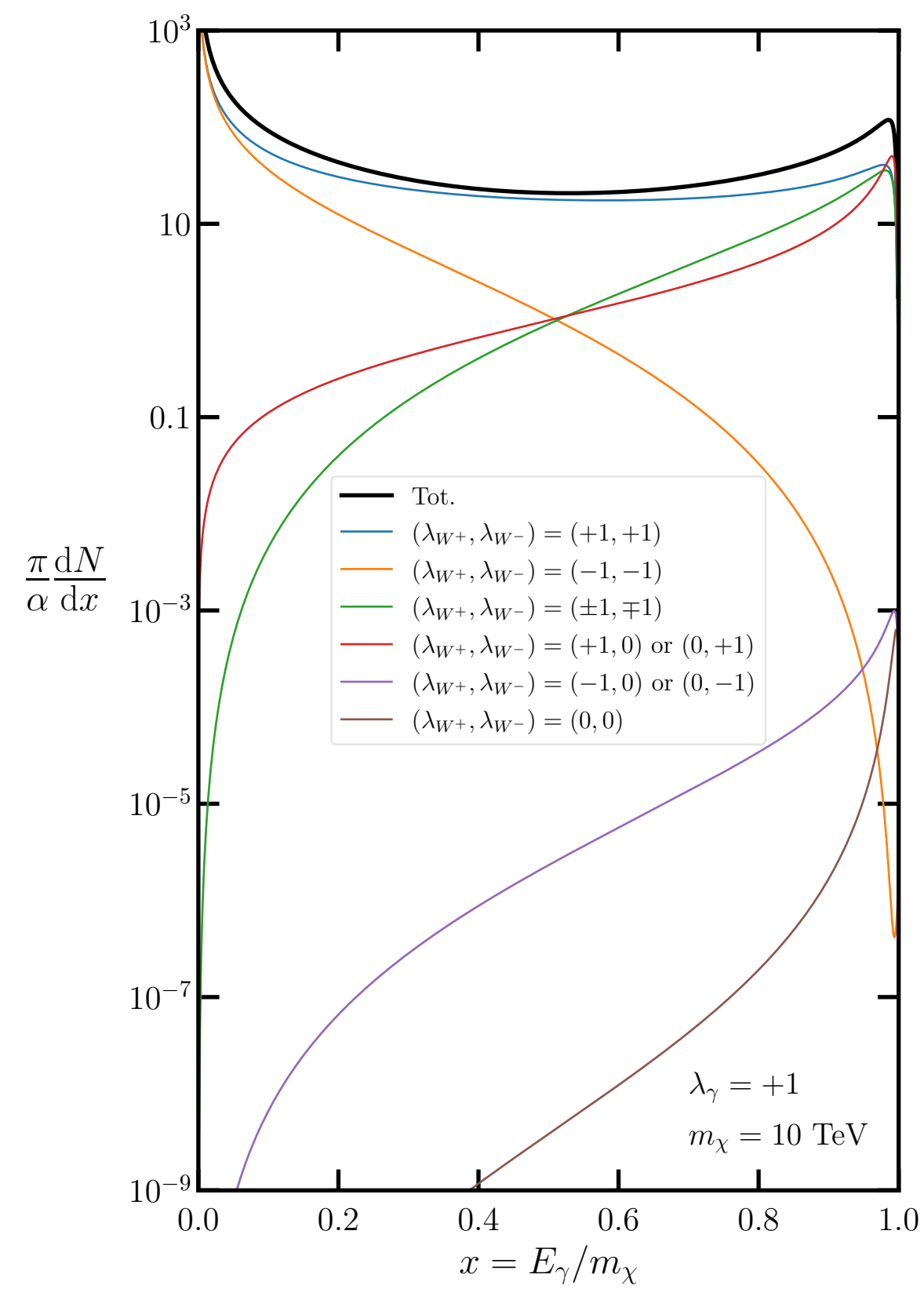


DM γ Spec

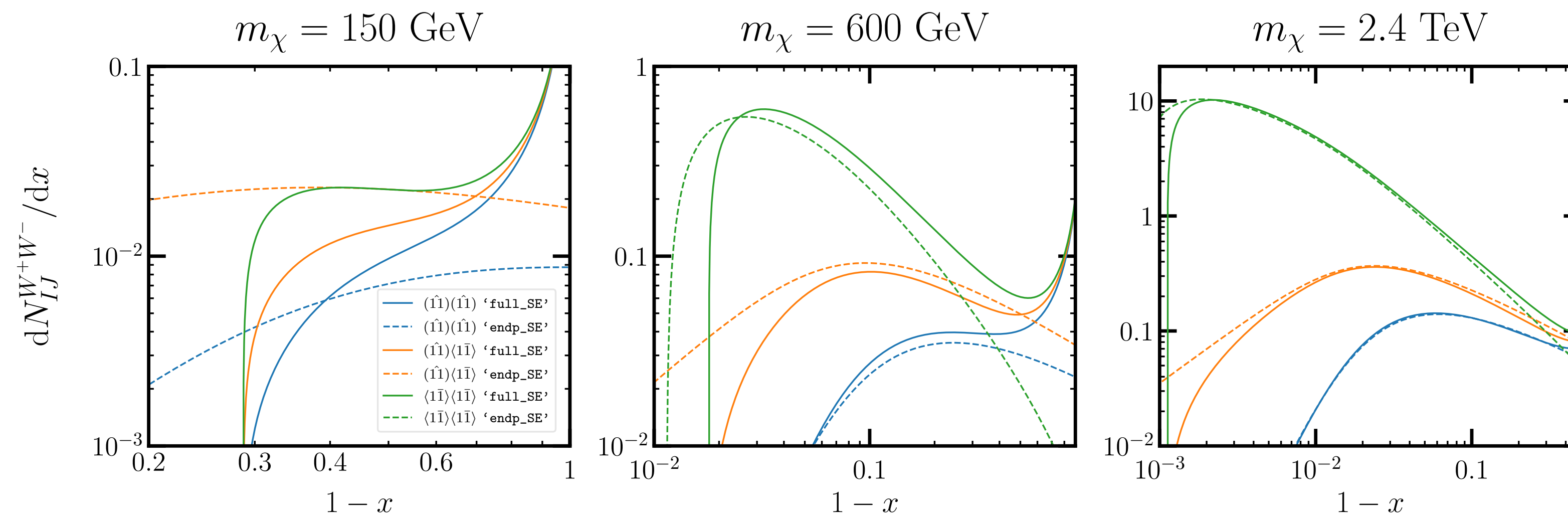
<https://dmyspec.hepforge.org/>



More results to brag about



More results to brag about



Outline

Motivation

Indirect detection

Sommerfeld factor

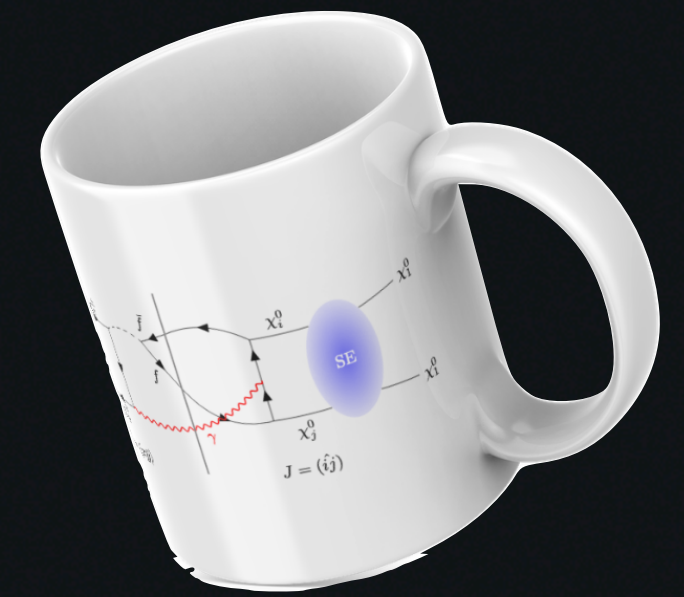
Endpoint resummations

Plots

Conclusions

Conclusions

Conclusions



- TeV-scale WIMP Dark Matter is still “a thing” in 2024
- Cherenkov telescopes are excellent instruments to search for DM
- Beautiful and complex phenomenology for indirect detection
 - Sommerfeld effect, internal bremsstrahlung, resonances, spectral lines, radiative electroweak effects, ...
- Armed with sophisticated EFT tools tackled these obstacles
 - ready for implementation in future observations
- Further explorations in the remaining 2020s **crucial**



CEN
WINDKRAFT
ANZ



Uhr

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THE DM LANDSCAPE