

Medium modification of jets: angular scales and EEC

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based on:

C. Andres, F. Dominguez, R.K. Elayavalli, J. Holguin, C. Marquet, I. Moutl, **PRL 130 (2023) 26, 262301**

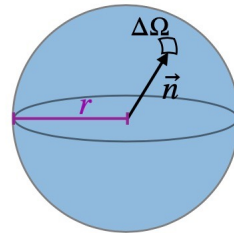
C. Andres, F. Dominguez, J. Holguin, C. Marquet, I. Moutl, **JHEP 09 (2023) 088**

C. Andres, F. Dominguez, J. Holguin, C. Marquet, I. Moutl, **2307.15110** + paper in preparation

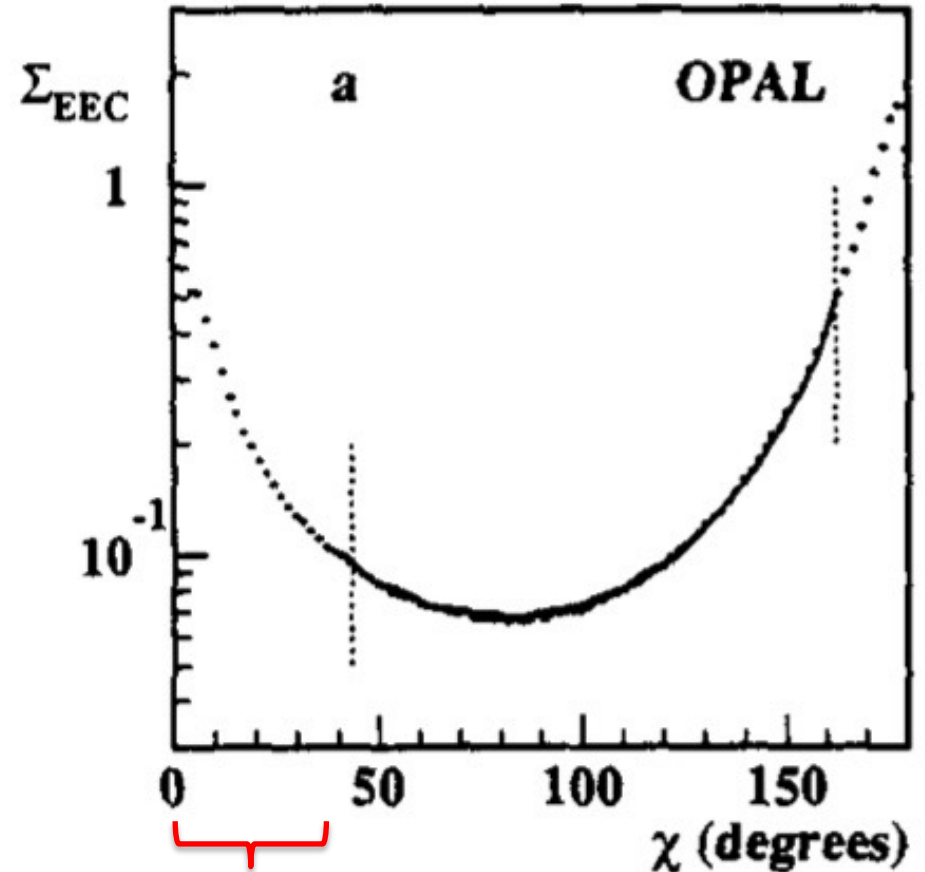
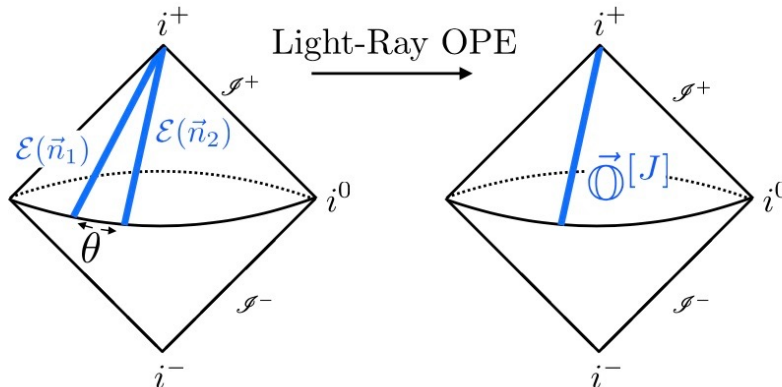
Small-angle limit of EEC

light-ray OPE in the collinear limit

$$\mathcal{E}(\vec{n}) = \lim_{r \rightarrow \infty} \int_0^\infty dt r^2 n^i T_{0i}(t, r\vec{n})$$

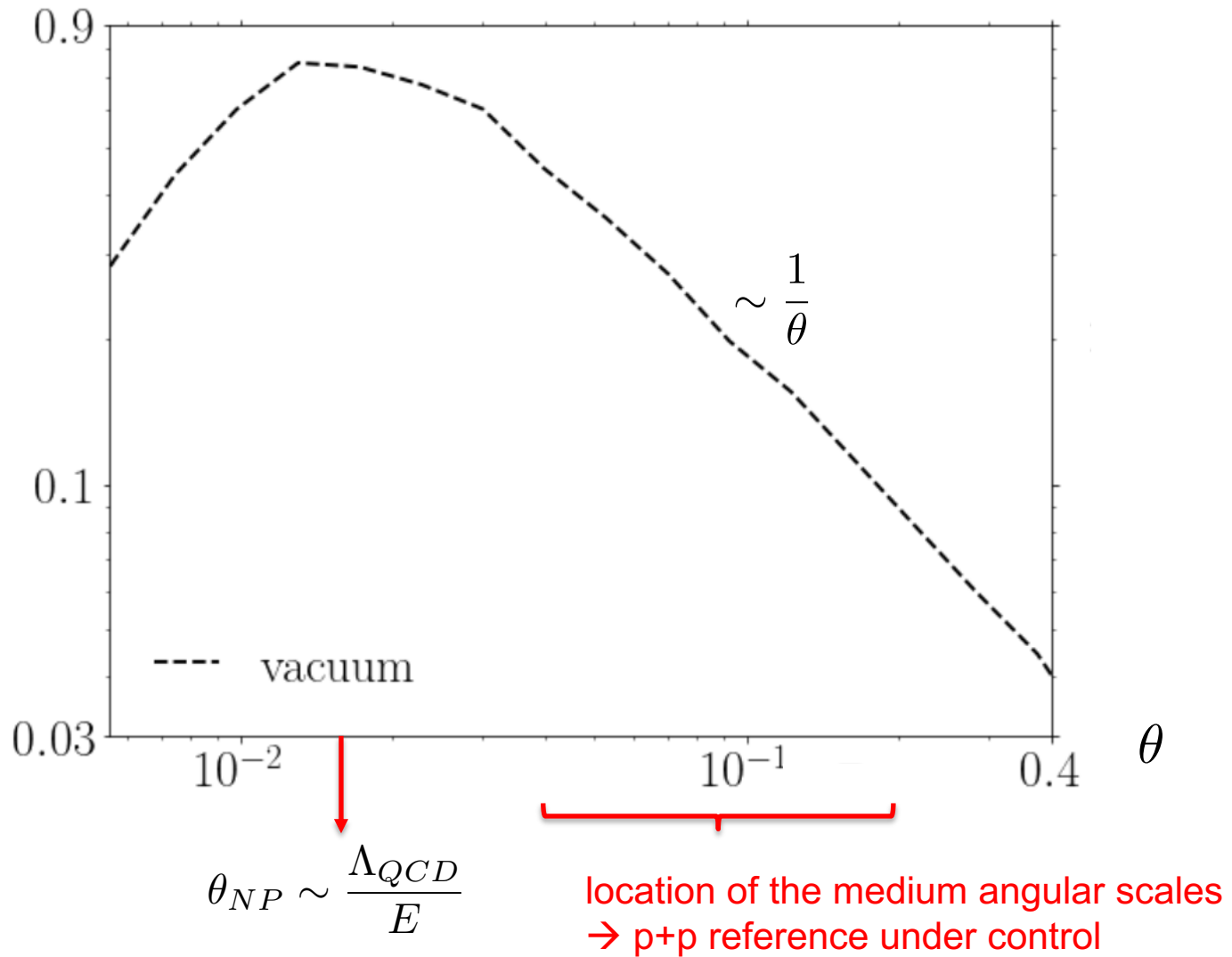


$$\mathcal{E}(\hat{n}_1)\mathcal{E}(\hat{n}_2) = \sum c_i \theta^{\tau_i - 4} \mathcal{O}_i(\hat{n}_1)$$



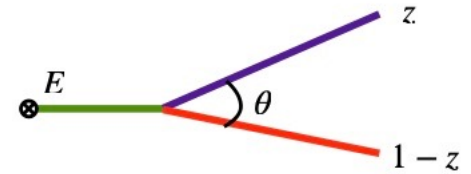
our focus
is here

EEC in p+p



EEC from inclusive cross-section

$$\frac{d\Sigma^{(n)}}{d\theta} = \int d\vec{n}_{1,2} \frac{\langle \mathcal{E}^n(\vec{n}_1) \mathcal{E}^n(\vec{n}_2) \rangle}{Q^{2n}} \delta(\vec{n}_2 \cdot \vec{n}_1 - \cos \theta)$$



For a quark jet at leading order in the splittings, $Q = E$ the energy of the jet

$$\frac{d\Sigma^{(n)}}{d\theta} = \frac{1}{\sigma_{qg}} \int dz \frac{d\sigma_{qg}}{d\theta dz} z^n (1-z)^n + \mathcal{O}\left(\frac{\mu_s}{E}\right)$$

μ_s a softer scale over which the cross section is inclusive

EEC in p+p collisions

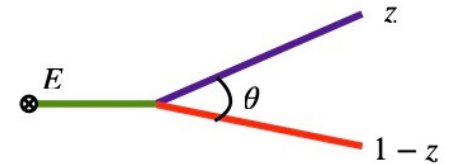
D. Hoffman, J. Maldacena [0803.1467](#)
 H. Chen, I. Mout, J. Sandor, H. X. Zhu [2202.04085](#)

- At leading order

$$\frac{d\sigma_{qg}^{\text{vac}}}{d\theta dz} = \frac{\alpha_s C_F \sigma}{\pi} \frac{1 + (1-z)^2}{z \theta}$$



$$\frac{d\Sigma^{(1)}}{d\theta} \sim \frac{1}{\theta}$$

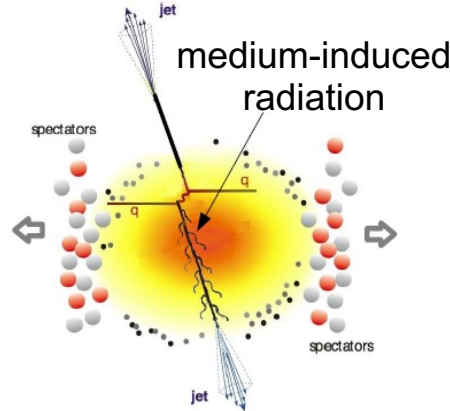


- Collinear emissions can be resummed using CFT techniques changing the scaling only by an anomalous dimension

$$\frac{d\Sigma^{(1)}}{d\theta} \sim \frac{1}{\theta^{1-\gamma(3)}}$$

$\gamma(3)$ is the twist-2 spin-3
 QCD anomalous dimension

EEC in heavy-ion collisions



- We factor out the vacuum cross section and define the modification factor F_{med}

$$\frac{d\sigma_{qg}}{d\theta dz} = (1 + F_{\text{med}}(z, \theta)) \frac{d\sigma_{qg}^{\text{vac}}}{d\theta dz} \quad F_{\text{med}}(z, \theta) \xrightarrow{\theta < \theta_L} 0$$

- We do not expect medium modification at small angles, thus vacuum collinear resummation should still be valid

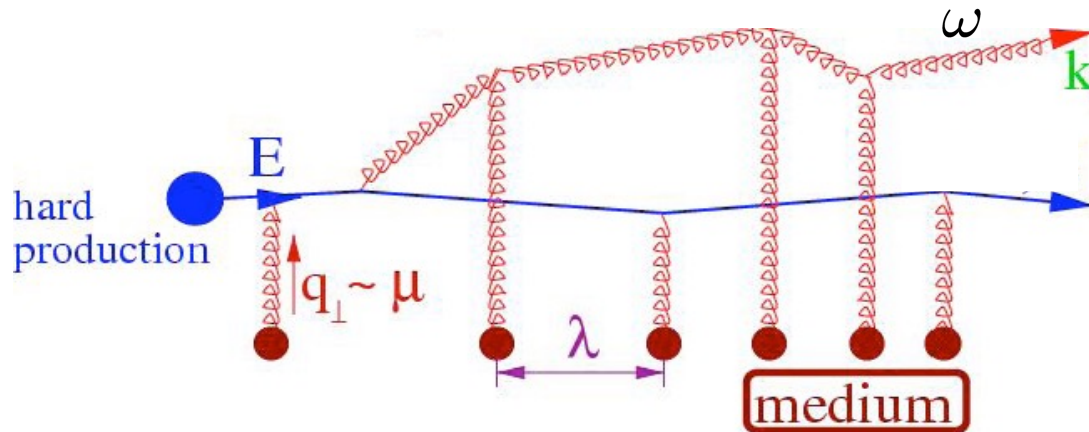
$$\frac{d\Sigma^{(n)}}{d\theta} = \frac{1}{\sigma_{qg}} \int dz \left(g^{(n)}(\theta, \alpha_s) + F_{\text{med}}(z, \theta) \right) \frac{d\sigma_{qg}^{\text{vac}}}{d\theta dz} z^n (1-z)^n \left(1 + \mathcal{O}\left(\frac{\mu_s}{E}\right) + \mathcal{O}\left(\frac{\Lambda_{\text{QCD}}}{\theta Q}\right) \right)$$

$$g^{(1)} = \theta^{\gamma(3)} + \mathcal{O}(\theta)$$

Medium-induced radiation

Baier, Dokshitzer, Mueller, Peigne and Schiff (1997)
Zakharov (1997)

computed in the context of parton energy loss



the accumulated transverse momentum
picked up by a gluon of formation time t

$$p_T^2 = \mu^2 \frac{t}{\lambda} = \hat{q} t$$

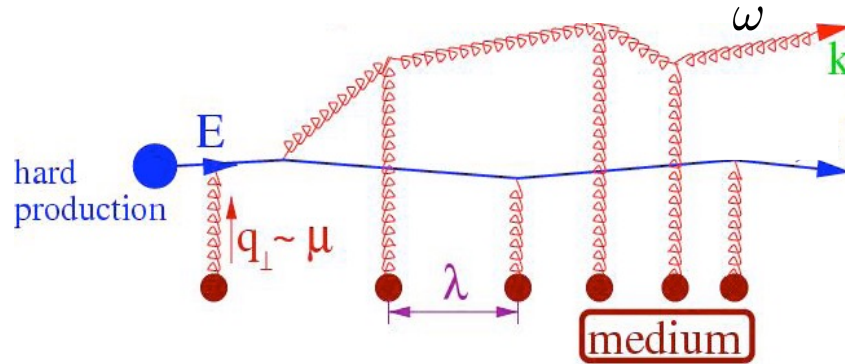
average p_T^2 picked up
in each scattering

mean free path

$$\hat{q} \equiv \mu^2 / \lambda \sim T^3$$

the relevant medium parameter needed
along with the length L

Radiative energy loss in pQCD



- emission of the radiated gluon

its formation time ω/k_{\perp}^2 must be smaller than the medium length L : $\omega < L k_{\perp}^2$

it must pick up enough transverse momentum: $k_{\perp}^2 < \hat{q} L \equiv Q_s^2$

maximum radiated gluon energy $\omega_c = \hat{q} L^2$

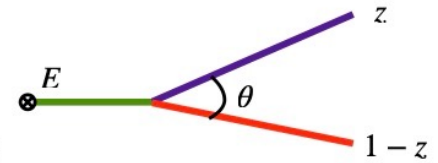
total energy lost by the quark $\Delta E \propto \alpha_s \omega_c$

- how does medium-induced radiation affect jet substructure ?
let's look at the Lund plane, then compute the EEC

Time and angular scales

Dominguez, Milhano, Salgado, Tywoniuk, Vila, 1907.03653

- For a static medium of length L within the harmonic approximation with jet quenching parameter \hat{q} one can read off the relevant scales directly from the formulas



- ♦ (Vacuum) formation time:

$$t_f = \frac{2}{z(1-z)E\theta^2}$$

$$\theta_L \sim (EL)^{-1/2}$$

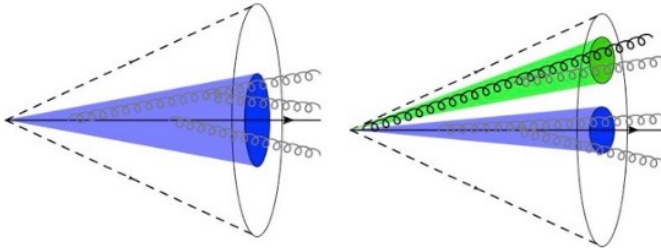
Below θ_L all emissions have a formation time larger than L

- ♦ Decoherence time:

$$t_d \sim (\hat{q}\theta^2)^{-1/3}$$

$$\theta_c \sim (\hat{q}L^3)^{-1/2}$$

Below θ_c splittings do not lose color coherence and the medium does not resolve them

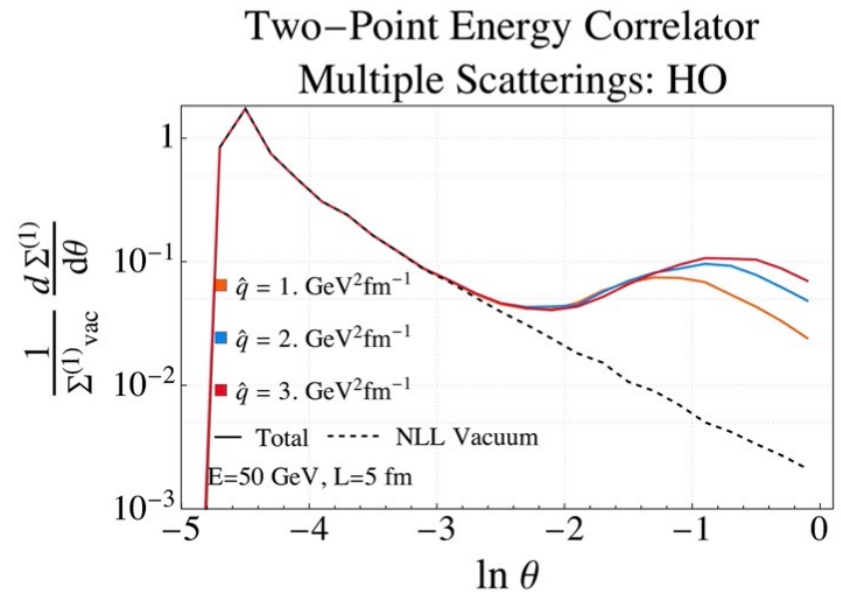
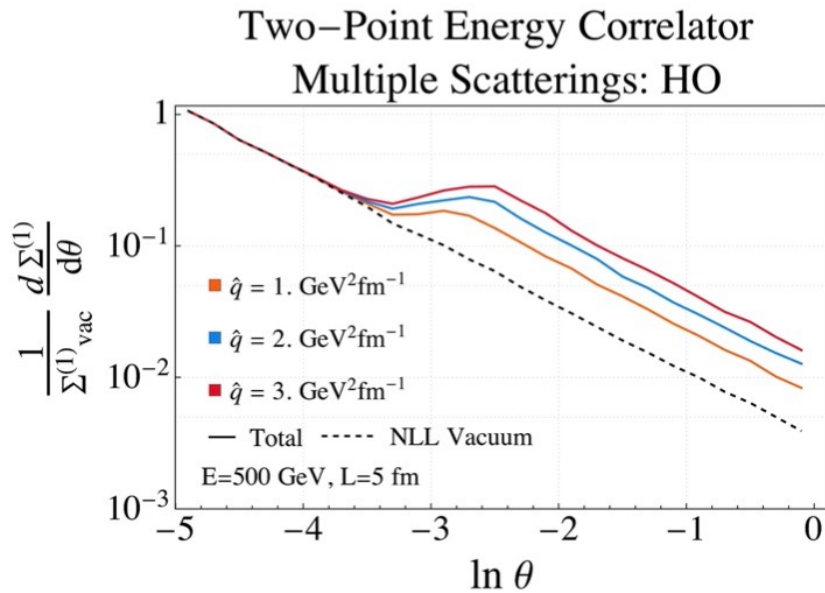


If $\theta_L > \theta_c$ then θ_c becomes irrelevant

Brick-QGP hemisphere-jet EEC

$$\theta_c > \theta_L$$

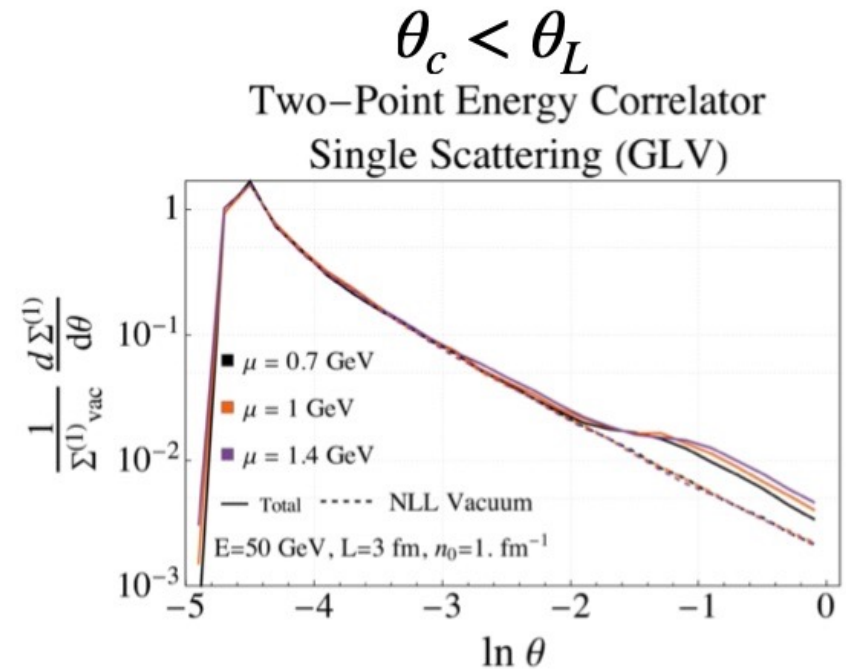
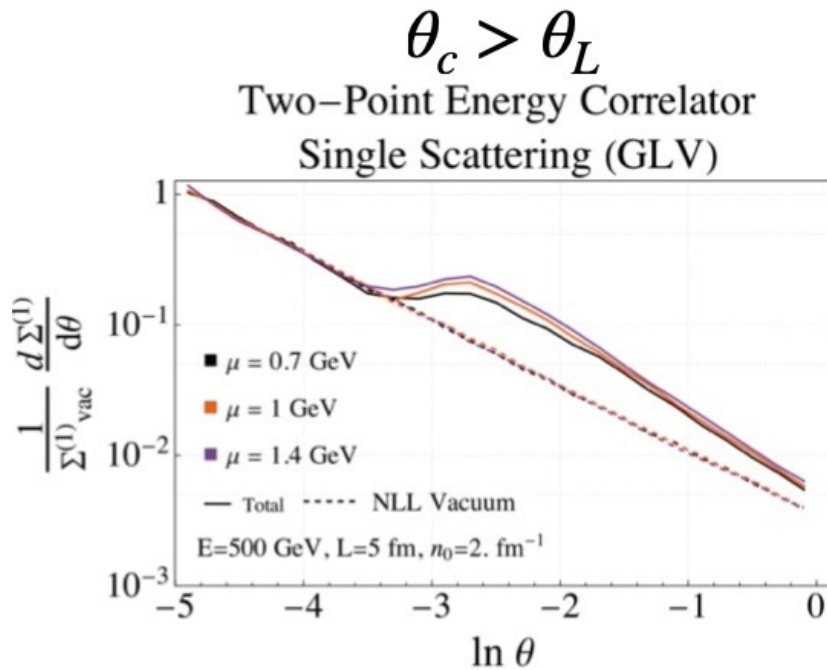
$$\theta_c < \theta_L$$



- No enhancement at small angles. Onset angle seems independent of \hat{q} as expected
- Varying \hat{q} has different effects in the two regions

Single hard scattering (GLV)

Gyulassy, Levai and Vitev (2000-2001)



- onset of medium effects is not as sharp in the GLV case
- the coherence transition is very smooth: mild difference in behavior when varying the medium parameters in the two regions

Conclusions

- Energy-Energy correlators (EECs) for jet substructure in p+p collisions
 - correlations functions of the energy flow operator formulated in QFTs
 - obey factorization theorems and computed to high accuracy in QCD
 - now being measured at RHIC and the LHC
- EECs for jet substructure in heavy-ion collisions
 - complementary approach to traditional observables
 - novel attempt to try and identify the scales of jet evolution inside the QGP, in particular those related to color coherence
- Work in progress

more realistic calculations (dynamic QGP, experimental constrains, ...)