



Opportunities with B_c semileptonic decays

Fulvia De Fazio
INFN Bari

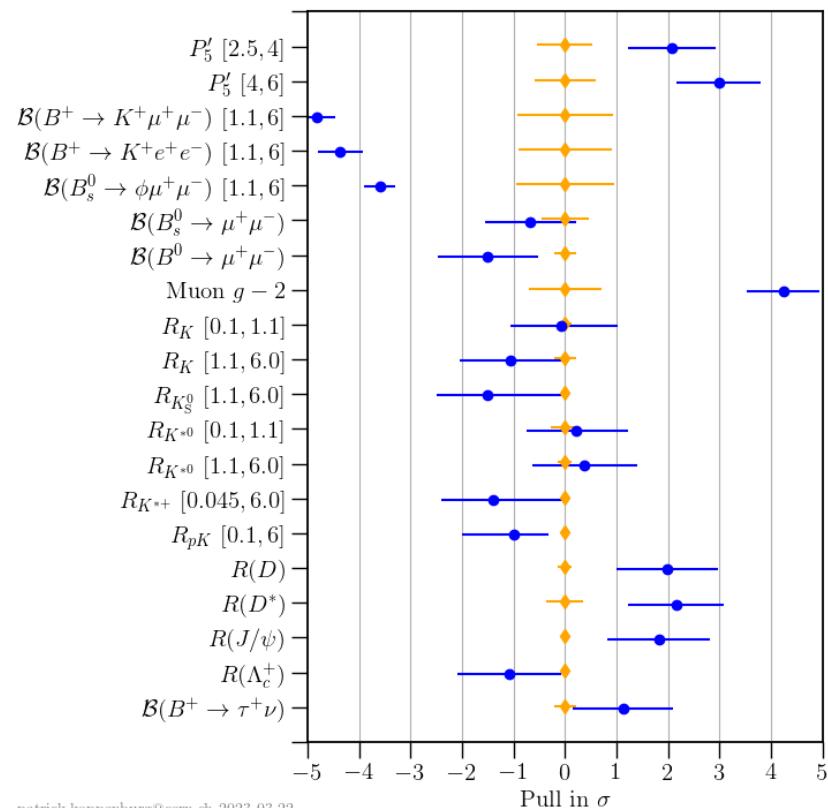
Pushing the limits of theoretical physics

10th anniversary of MITP

Mainz, May 12th, 2023

based on works in collaboration with
P. Colangelo, F. Lopalco, N. Losacco, M. Novoa-Brunet

- Semileptonic B_c decays: motivations
- Spin symmetry + NRQCD : relations among FF in the SM and BSM
- Application to $B_c \rightarrow J/\psi$ and $B_c \rightarrow \eta_c$ form factors
- Application to B_c to P-wave charmonia and insights on X(3872)
- Other semileptonic B_c decays: $c \rightarrow s, d$ transitions
- Summary



➤ $b \rightarrow c$ transitions

- Precisely measure $|V_{cb}|$:
insights on the tension from inclusive/exclusive determinations
- Anomalies shown up in modes induced by $b \rightarrow c \ell \nu_\ell$ transition



Look for new modes/observables/correlations

➤ other quark-level transitions (e.g. $c \rightarrow s, d$)

- do anomalies show up?



Look for new modes/observables/correlations

B_c

- discovered at Tevatron in 1998
- $m_{B_c} = 6.274.47 \pm 0.27 \pm 0.17 \text{ GeV}$
- $\tau_{B_c} = 0.510 \pm 0.009 \text{ ps}$
- decays weakly
- possible modes: annihilation, b transitions, c transitions (dominant)

Motivations:

1. explore BSM effects
2. $B_c \rightarrow \text{charmonium}$: probe the structure of the charmonia produced in the decay



control of theoretical uncertainties in phenomenological analyses
requires reliable determination of the hadronic form factors

possibility to exploit NRQCD methods + HQ spin symmetry

Explore BSM effects: SMEFT \rightarrow systematic extension of the SM

- NP exists at a high scale $\Lambda \gg M_W$
- NP gauge group contains the SM group
- SM gauge fields contained
- SM an effective theory at the scale M_W

Buchmuller et al, NPB 268 (1986) 621
Grzadkowski et al., JHEP 10 (2010) 085

Weinberg operator: ν oscillations

$$\mathcal{L}_{SM} = \mathcal{L}_{SM}^{(4)} + \frac{1}{\Lambda} C_{\nu\nu}^{(5)} Q_{\nu\nu}^{(5)} + \frac{1}{\Lambda^2} \sum_k C_k^{(6)} Q_k^{(6)} + \mathcal{O}\left(\frac{1}{\Lambda^3}\right)$$

$$\mathcal{L}^{kin} + \mathcal{L}^{gauge} + \mathcal{L}^{Higgs} + \mathcal{L}^{Yukawa}$$

accidental symmetries

- violates accidental symmetries
- source of (SM) CP violation
- fermion mass terms

NP

Generalized effective Hamiltonian

SM

$$H_{\text{eff}}^{b \rightarrow c \ell \bar{\nu}} = \frac{G_F}{\sqrt{2}} V_{cb} \left[(1 + \epsilon_V^\ell) (\bar{c} \gamma_\mu (1 - \gamma_5) b) (\bar{\ell} \gamma^\mu (1 - \gamma_5) \nu_\ell) \right. \\ + \epsilon_R^\ell (\bar{c} \gamma_\mu (1 + \gamma_5) b) (\bar{\ell} \gamma^\mu (1 - \gamma_5) \nu_\ell) \\ + \epsilon_S^\ell (\bar{c} b) (\bar{\ell} (1 - \gamma_5) \nu_\ell) \\ + \epsilon_P^\ell (\bar{c} \gamma_5 b) (\bar{\ell} (1 - \gamma_5) \nu_\ell) \\ \left. + \epsilon_T^\ell (\bar{c} \sigma_{\mu\nu} (1 - \gamma_5) b) (\bar{\ell} \sigma^{\mu\nu} (1 - \gamma_5) \nu_\ell) \right]$$

complex
lepton flavour dependent couplings

Generalized effective Hamiltonian

SM

$$H_{\text{eff}}^{b \rightarrow c \ell \bar{\nu}} = \frac{G_F}{\sqrt{2}} V_{cb} \left[(1 + \epsilon_V^\ell) (\bar{c} \gamma_\mu (1 - \gamma_5) b) (\bar{\ell} \gamma^\mu (1 - \gamma_5) \nu_\ell) \right. \\ + \epsilon_R^\ell (\bar{c} \gamma_\mu (1 + \gamma_5) b) (\bar{\ell} \gamma^\mu (1 - \gamma_5) \nu_\ell) \\ + \epsilon_S^\ell (\bar{c} b) (\bar{\ell} (1 - \gamma_5) \nu_\ell) \\ + \epsilon_P^\ell (\bar{c} \gamma_5 b) (\bar{\ell} (1 - \gamma_5) \nu_\ell) \\ \left. + \epsilon_T^\ell (\bar{c} \sigma_{\mu\nu} (1 - \gamma_5) b) (\bar{\ell} \sigma^{\mu\nu} (1 - \gamma_5) \nu_\ell) \right]$$

larger set of form factors required wrt the SM case

complex
lepton flavour dependent couplings

➤ $B_c \rightarrow \eta_c, J/\psi$

1S-wave charmonia $J^{PC}=(0^-, 1^-)$

Motivations:

1. explore BSM effects

- $B_c \rightarrow \eta_c, J/\psi$ 1S-wave charmonia $J^{PC}=(0^-, 1^-)$
- $B_c \rightarrow \chi_{c0}, \chi_{c1}, \chi_{c2}, h_c$ 1P-wave charmonia $J^{PC}=(0^{++}, 1^{++}, 2^{++}, 1^{+-})$
- $B_c \rightarrow \chi'_{c0}, \chi'_{c1}, \chi'_{c2}, h'_c$ 2P-wave charmonia $J^{PC}=(0^{++}, 1^{++}, 2^{++}, 1^{+-})$


Motivations:

1. explore BSM effects

2. $B_c \rightarrow$ charmonium: probe the structure of the charmonia produced in the decay

→ question: can $X(3872)$ be identified with $\chi_{c1}(2P)$?

X(3872)

- discovered by Belle in 2003, confirmed by CDF, D0, BaBar,...
- in 2015 LHCb: $J^P=1^{++}$  candidate for identification with $\chi_{c1}(2P)$
- other possible interpretations
 - tetraquark
 - $D D^*$ molecule (proximity to the threshold)
 -
- isospin violation disfavors the charmonium interpretation (but phase space suppression is at work)
- the preference of $\psi(2S) \gamma$ wrt $J/\psi \gamma$ favours the interpretation as $\chi_{c1}(2P)$

look for further information:

does X(3872) fulfill the expectations for the production of $\chi_{c1}(2P)$ in semileptonic B_c decays?

Semileptonic B_c decays to charmonium

$B_c \rightarrow \eta_c$:

$$\langle \eta_c(v') | \bar{Q}' \gamma_\mu Q | B_c(v) \rangle = \sqrt{m_P m_{B_c}} [\textcolor{red}{h}_+(w) (v + v')_\mu + \textcolor{red}{h}_-(w) (v - v')_\mu]$$

$$\langle \eta_c(v') | \bar{Q}' Q | B_c(v) \rangle = \sqrt{m_P m_{B_c}} \textcolor{blue}{h}_S(w) (1 + w)$$

$$\langle \eta_c(v') | \bar{Q}' \sigma_{\mu\nu} Q | B_c(v) \rangle = -i \sqrt{m_P m_{B_c}} \textcolor{blue}{h}_T(w) (v_\mu v'_\nu - v_\nu v'_\mu)$$

$$w = v \cdot v'$$

$B_c \rightarrow J/\psi$:

$$\langle J/\psi(v', \epsilon) | \bar{Q}' \gamma_\mu Q | B_c(v) \rangle = i \sqrt{m_V m_{B_c}} \textcolor{red}{h}_V(w) \epsilon_{\mu\nu\alpha\beta} \epsilon^{*\nu} v'^\alpha v^\beta$$

$$\langle J/\psi(v', \epsilon) | \bar{Q}' \gamma_\mu \gamma_5 Q | B_c(v) \rangle = \sqrt{m_V m_{B_c}} [\textcolor{red}{h}_{A_1}(w) (1 + w) \epsilon_\mu^* - \textcolor{red}{h}_{A_2}(w) (\epsilon^* \cdot v) v_\mu - \textcolor{red}{h}_{A_3}(w) (\epsilon^* \cdot v) v'_\mu]$$

$$\langle J/\psi(v', \epsilon) | \bar{Q}' \gamma_5 Q | B_c(v) \rangle = -\sqrt{m_V m_{B_c}} \textcolor{blue}{h}_P(w) (\epsilon^* \cdot v)$$

$$\begin{aligned} \langle J/\psi(v', \epsilon) | \bar{Q}' \sigma_{\mu\nu} Q | B_c(v) \rangle = & -\sqrt{m_V m_{B_c}} \epsilon^{\mu\nu\alpha\beta} [\textcolor{blue}{h}_{T_1}(w) \epsilon_\alpha^* (v + v')_\beta + \textcolor{blue}{h}_{T_2}(w) \epsilon_\alpha^* (v - v')_\beta \\ & + \textcolor{blue}{h}_{T_3}(w) (\epsilon^* \cdot v) v_\alpha v'_\beta] \end{aligned}$$

SM

NP

Semileptonic B_c decays to charmonium

$B_c \rightarrow \chi_{c0}$:

$$\langle \chi_{c0}(v') | \bar{c} \gamma_\mu \gamma_5 b | B_c(v) \rangle = \sqrt{m_{\chi_{c0}} m_{B_c}} [g_+(w)(v + v')_\mu + g_-(w)(v - v')_\mu]$$

$$\langle \chi_{c0}(v') | \bar{c} \gamma_5 b | B_c(v) \rangle = \sqrt{m_{\chi_{c0}} m_{B_c}} g_P(w)$$

$$\langle \chi_{c0}(v') | \bar{c} \sigma_{\mu\nu} b | B_c(v) \rangle = \sqrt{m_{\chi_{c0}} m_{B_c}} g_T(w) \epsilon_{\mu\nu\alpha\beta} v^\alpha v'^\beta$$

$B_c \rightarrow h_c$:

$$\begin{aligned} \langle h_c(v', \epsilon) | \bar{c} \gamma_\mu b | B_c(v) \rangle &= \sqrt{m_{h_c} m_{B_c}} \left[f_{V_1}(w) \epsilon_\mu^* \right. \\ &\quad \left. + (\epsilon^* \cdot v) (f_{V_2}(w)(v + v')_\mu + f_{V_3}(w)(v - v')_\mu) \right] \end{aligned}$$

$$\langle h_c(v', \epsilon) | \bar{c} \gamma_\mu \gamma_5 b | B_c(v) \rangle = i \sqrt{m_{h_c} m_{B_c}} f_A(w) \epsilon_{\mu\alpha\beta\sigma} \epsilon^{*\alpha} v^\beta v'^\sigma$$

$$\langle h_c(v', \epsilon) | \bar{c} b | B_c(v) \rangle = \sqrt{m_{h_c} m_{B_c}} (\epsilon^* \cdot v) f_S(w)$$

$$\begin{aligned} \langle h_c(v', \epsilon) | \bar{c} \sigma_{\mu\nu} b | B_c(v) \rangle &= i \sqrt{m_{h_c} m_{B_c}} \left[f_{T_1}(w) (\epsilon_\mu^*(v + v')_\nu - \epsilon_\nu^*(v + v')_\mu) \right. \\ &\quad + f_{T_2}(w) (\epsilon_\mu^*(v - v')_\nu - \epsilon_\nu^*(v - v')_\mu) \\ &\quad \left. + f_{T_3}(w) (\epsilon^* \cdot v) (v_\mu v'_\nu - v_\nu v'_\mu) \right]. \end{aligned}$$

$B_c \rightarrow \chi_{c1}$:

$$\begin{aligned} \langle \chi_{c1}(v', \epsilon) | \bar{c} \gamma_\mu b | B_c(v) \rangle &= i \sqrt{m_{\chi_{c1}} m_{B_c}} \left[g_{V_1}(w) \epsilon_\mu^* \right. \\ &\quad \left. + (\epsilon^* \cdot v) [g_{V_2}(w)(v + v')_\mu + g_{V_3}(w)(v - v')_\mu] \right] \end{aligned}$$

$$\langle \chi_{c1}(v', \epsilon) | \bar{c} \gamma_\mu \gamma_5 b | B_c(v) \rangle = \sqrt{m_{\chi_{c1}} m_{B_c}} g_A(w) \epsilon_{\mu\alpha\beta\sigma} \epsilon^{*\alpha} v^\beta v'^\sigma$$

$$\langle \chi_{c1}(v', \epsilon) | \bar{c} b | B_c(v) \rangle = i \sqrt{m_{\chi_{c1}} m_{B_c}} g_S(w) (\epsilon^* \cdot v)$$

$$\begin{aligned} \langle \chi_{c1}(v', \epsilon) | \bar{c} \sigma_{\mu\nu} b | B_c(v) \rangle &= \sqrt{m_{\chi_{c1}} m_{B_c}} \left[g_{T_1}(w) (\epsilon_\mu^*(v + v')_\nu - \epsilon_\nu^*(v + v')_\mu) \right. \\ &\quad + g_{T_2}(w) (\epsilon_\mu^*(v - v')_\nu - \epsilon_\nu^*(v - v')_\mu) \\ &\quad \left. + g_{T_3}(w) (\epsilon^* \cdot v) (v_\mu v'_\nu - v_\nu v'_\mu) \right] \end{aligned}$$

$B_c \rightarrow \chi_{c2}$:

$$\langle \chi_{c2}(v', \eta) | \bar{c} \gamma_\mu b | B_c(v) \rangle = \sqrt{m_{\chi_{c2}} m_{B_c}} i k_V(w) \epsilon_{\mu\alpha\beta\sigma} \eta^{*\alpha\tau} v_\tau v'^\beta v'^\sigma$$

$$\langle \chi_{c2}(v', \eta) | \bar{c} \gamma_\mu \gamma_5 b | B_c(v) \rangle = \sqrt{m_{\chi_{c2}} m_{B_c}} [k_{A_1}(w) \eta_{\mu\alpha}^* v^\alpha + \eta_{\alpha\beta}^* v^\alpha v'^\beta (k_{A_2}(w) v_\mu + k_{A_3}(w) v'_\mu)]$$

$$\langle \chi_{c2}(v', \eta) | \bar{c} \gamma_5 b | B_c(v) \rangle = \sqrt{m_{\chi_{c2}} m_{B_c}} k_P(w) \eta_{\alpha\beta}^* v^\alpha v'^\beta$$

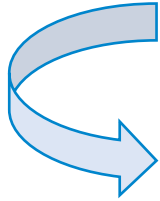
$$\begin{aligned} \langle \chi_{c2}(v', \eta) | \bar{c} \sigma_{\mu\nu} \gamma_5 b | B_c(v) \rangle &= i \sqrt{m_{\chi_{c2}} m_{B_c}} [k_{T_1}(w) (\eta_\mu^{*\alpha} v_\alpha v_\nu - \eta_\nu^{*\alpha} v_\alpha v_\mu) + \\ &\quad + k_{T_2}(w) (\eta_\mu^{*\alpha} v_\alpha v'_\nu - \eta_\nu^{*\alpha} v_\alpha v'_\mu) + k_{T_3}(w) \eta_{\alpha\beta}^* v^\alpha v'^\beta (v_\mu v'_\nu - v_\nu v'_\mu)] \end{aligned}$$

SM

NP

HQ limit: decoupling of the HQ

- Heavy-light mesons \rightarrow HQ spin & flavour symmetry
- Heavy-heavy mesons \rightarrow HQ spin symmetry

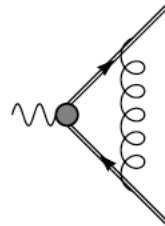


relations among the FF in selected kinematical ranges

Heavy-light mesons:

FF of weak matrix elements between heavy-light mesons are all described by the Isgur-Wise function

Heavy-heavy meson decays



IR divergent for 2 HQs with the same v

- Infrared divergences regulated in the HQ limit by the kinetic energy operator O_π
- O_π breaks flavour symmetry \rightarrow only spin symmetry

Thacker and Lepage, PRD43 (1991) 196

Heavy-Light mesons:

HQET

N. Isgur, M.B. Wise, PLB 232 (89) 113
PLB 237 (90) 527



$$p_Q = m_Q v + k$$

$$k \simeq \mathcal{O}(\Lambda_{QCD}) \ll m_Q$$



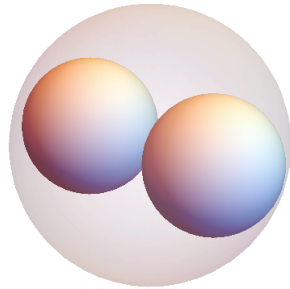
residual momentum

HQET Lagrangian: expansion in k/m_Q

Heavy-Heavy mesons:

NRQCD

W.E. Caswell, G.P. Lepage, PLB 167 (86) 437
G.T. Bodwin, E. Braaten, G.P. Lepage, PRD51 (95) 1125



non relativistic quarks
relative velocity \tilde{v}

NRQCD Lagrangian: expansion in $1/m_Q$
terms further organized: expansion in powers of \tilde{v}

different power counting

see also: A.Gunawardana and G.Paz, JHEP07(2017) 137

- expansion parameters for a system with 2 Heavy Quarks:
 1. relative HQ 3-velocity (hadron rest-frame) (NRQCD)
 2. inverse HQ mass $1/m_Q$ (HQET)

- HQ field:

$$Q(x) = e^{-im_Q v \cdot x} \psi(x) = e^{-im_Q v \cdot x} (\psi_+(x) + \psi_-(x)) \quad \psi_{\pm}(x) = P_{\pm} \psi(x) = \frac{1 \pm \not{v}}{2} \psi(x)$$

➡
$$Q(x) = e^{-im_Q v \cdot x} \left(1 + \frac{i \not{D}_{\perp}}{2m_Q} + \frac{(-iv \cdot D)}{2m_Q} \frac{i \not{D}_{\perp}}{2m_Q} + \dots \right) \psi_+(x) \quad D_{\perp\mu} = D_{\mu} - (v \cdot D) v_{\mu}$$

➡
$$\mathcal{L}_{QCD} = \bar{\psi}_+(x) \left(iv \cdot D + \frac{(iD_{\perp})^2}{2m_Q} + \frac{g}{4m_Q} \sigma \cdot G_{\perp} + \frac{i \not{D}_{\perp}}{2m_Q} \frac{(-iv \cdot D)}{2m_Q} (i \not{D}_{\perp}) + \dots \right) \psi_+(x)$$

power counting in NRQCD

$$\psi_+ \sim \tilde{v}^{3/2}$$

$$D_\perp \sim \tilde{v}$$

$$D_t \sim \tilde{v}^2$$

$$E_i = G_{0i} \sim \tilde{v}^3 \quad B_i = \frac{1}{2} \epsilon_{ijk} G^{jk} \sim \tilde{v}^4$$

$$\mathcal{L}_{QCD} = \bar{\psi}_+(x) \left(iv \cdot D + \frac{(iD_\perp)^2}{2m_Q} + \frac{g}{4m_Q} \sigma \cdot G_\perp + \frac{i \not{D}_\perp}{2m_Q} \frac{(-iv \cdot D)}{2m_Q} (i \not{D}_\perp) + \dots \right) \psi_+(x)$$

$\mathcal{O}(\tilde{v}^2)$ LO

$\mathcal{O}(\tilde{v}^4)$ NLO

$$\mathcal{L}_0 = \bar{\psi}_+(x) \left(iv \cdot D + \frac{(iD_\perp)^2}{2m_Q} \right) \psi_+(x)$$

$$\mathcal{L}_1 = \mathcal{L}_{1,1} + \mathcal{L}_{1,2}$$

$$\langle C | \bar{Q}' \Gamma Q | B_c \rangle$$

$$C = \eta_c, J/\psi$$

$$C = \chi_{c0}, \chi_{c1}, \chi_{c2}, h_c$$

follow the same steps as for heavy-light mesons

Falk & Neubert, PRD47 (93) 2965

I. expand the current:

$$\bar{Q}'(x) \Gamma Q(x) = J_0 + \left(\frac{J_{1,0}}{2m_Q} + \frac{J_{0,1}}{2m_{Q'}} \right) + \left(-\frac{J_{2,0}}{4m_Q^2} - \frac{J_{0,2}}{4m_{Q'}^2} + \frac{J_{1,1}}{4m_Q m_{Q'}} \right)$$

$$J_0 = \bar{\psi}'_+ \Gamma \psi_+$$

$$J_{1,0} = \bar{\psi}'_+ \Gamma i \vec{D}_\perp \psi_+$$

$$J_{2,0} = \bar{\psi}'_+ \Gamma (i v \cdot \vec{D}) i \vec{D}_\perp \psi_+$$

$$J_{0,1} = \bar{\psi}'_+ \left(-i \overleftarrow{D}'_\perp \right) \Gamma \psi_+$$

$$J_{0,2} = \bar{\psi}'_+ i \overleftarrow{D}'_\perp (i v' \cdot \overleftarrow{D}) \Gamma \psi_+$$

$$J_{1,1} = \bar{\psi}'_+ \left(-i \overleftarrow{D}'_\perp \right) \Gamma (i \vec{D}_\perp) \psi_+$$

II: exploit spin symmetry:

doublet of negative parity states:

$$(B_c, B_c^*) \longrightarrow$$

$$\mathcal{M}(v) = P_+(v) [B_c^{*\mu} \gamma_\mu - B_c \gamma_5] P_-(v)$$

$$(\eta_c, J/\psi) \longrightarrow$$

$$\mathcal{M}'(v') = P_+(v') [\Psi^{*\mu} \gamma_\mu - \eta_c \gamma_5] P_-(v')$$

4-plet of positive parity states

$$(\chi_{c0,1,2}, h_c)$$



$$\mathcal{M}'^\mu(v') = P_+(v') \left[\chi_{c2}^{\mu\nu} \gamma_\nu + \frac{1}{\sqrt{2}} \chi_{c1,\gamma} \epsilon^{\mu\alpha\beta\gamma} v'_\alpha \gamma_\beta + \frac{1}{\sqrt{3}} \chi_{c0} (\gamma^\mu - v'^\mu) + h_c^\mu \gamma_5 \right] P_-(v')$$

$$v'_\mu \mathcal{M}'^\mu = 0$$

analogous for 2P charmonia

III. trace formalism:

$$\langle C | \bar{Q}' \Gamma D_{\mu_1} D_{\mu_2} \dots Q | B_c \rangle = -\text{Tr} \left[\mathcal{F}_{\mu \mu_1 \mu_2 \dots} \bar{\mathcal{M}}'^{\mu} \Gamma \mathcal{M} \right]$$



universal functions: the same for all the members of the multiplet of final states

relations among the various modes

III. trace formalism: at LO in the HQ expansion all the matrix elements involve a single universal function

$$\langle M'(v') | J_0 | M(v) \rangle = -\Xi(w) v_\mu \text{Tr} [\overline{\mathcal{M}}'^\mu \Gamma \mathcal{M}]$$

III. trace formalism: At LO in the HQ expansion all the matrix elements involve a single universal function

$$\langle M'(v') | J_0 | M(v) \rangle = -\Xi(w) v_\mu \text{Tr} [\overline{\mathcal{M}}'^\mu \Gamma \mathcal{M}]$$

$\mathcal{O}(1/m_Q)$

$$\langle M'(v') | \bar{\psi}'_+ \Gamma i \overrightarrow{D}_\alpha \psi_+ | M(v) \rangle = -\text{Tr} [\Sigma_{\mu\alpha}^{(b)} \overline{\mathcal{M}}'^\mu \Gamma \mathcal{M}]$$

$$\langle M'(v') | \bar{\psi}'_+ (-i \overleftarrow{D}_\alpha) \Gamma \psi_+ | M(v) \rangle = -\text{Tr} [\Sigma_{\mu\alpha}^{(c)} \overline{\mathcal{M}}'^\mu \Gamma \mathcal{M}]$$

$$\Sigma_{\mu\alpha}^{(Q)} = \Sigma_1^{(Q)} g_{\mu\alpha} + \Sigma_2^{(Q)} v_\mu v_\alpha + \Sigma_3^{(Q)} v_\mu v'_\alpha + \Sigma_4^{(Q)} v_\mu \gamma_\alpha + \Sigma_5^{(Q)} \gamma_\mu v_\alpha + \Sigma_6^{(Q)} \gamma_\mu v'_\alpha + \Sigma_7^{(Q)} i \sigma_{\mu\alpha}$$

constraints: $\Sigma_i^{(b)}(w) - \Sigma_i^{(c)}(w) = 0 \quad i = 1, 4, 5, 6, 7$

$$\Sigma_2^{(b)}(w) - \Sigma_2^{(c)}(w) = \tilde{\Lambda} \Xi,$$

$$\Sigma_3^{(b)}(w) - \Sigma_3^{(c)}(w) = -\tilde{\Lambda}' \Xi(w).$$

III. trace formalism: At LO in the HQ expansion all the matrix elements involve a single universal function

$$\langle M'(v') | J_0 | M(v) \rangle = -\Xi(w) v_\mu \text{Tr} [\overline{\mathcal{M}}'^\mu \Gamma \mathcal{M}]$$

$\mathcal{O}(1/m_Q)$

$$\begin{aligned} \langle M'(v') | \bar{\psi}'_+ \Gamma i \vec{D}_\alpha \psi_+ | M(v) \rangle &= -\text{Tr} [\Sigma_{\mu\alpha}^{(b)} \overline{\mathcal{M}}'^\mu \Gamma \mathcal{M}] \\ \langle M'(v') | \bar{\psi}'_+ (-i \overleftarrow{D}_\alpha) \Gamma \psi_+ | M(v) \rangle &= -\text{Tr} [\Sigma_{\mu\alpha}^{(c)} \overline{\mathcal{M}}'^\mu \Gamma \mathcal{M}] \end{aligned}$$

$\mathcal{O}(1/m_Q)^2$

$$\begin{aligned} \langle M'(v') | \bar{\psi}'_+ \Gamma i \vec{D}_\alpha i \vec{D}_\beta \psi_+ | M(v) \rangle &= -\text{Tr} [\Omega_{\mu\alpha\beta}^{(b)} \overline{\mathcal{M}}'^\mu \Gamma \mathcal{M}] \\ \langle M'(v') | \bar{\psi}'_+ i \overleftarrow{D}_\alpha i \overleftarrow{D}_\beta \Gamma \psi_+ | M(v) \rangle &= -\text{Tr} [\Omega_{\mu\alpha\beta}^{(c)} \overline{\mathcal{M}}'^\mu \Gamma \mathcal{M}] \end{aligned}$$

constraints:

$$\Omega_{\mu\alpha\beta}^{(b)} - \Omega_{\mu\alpha\beta}^{(c)} = (\tilde{\Lambda} v_\alpha - \tilde{\Lambda}' v'_\alpha) \Sigma_{\mu\beta}^{(b)} + (\tilde{\Lambda} v_\beta - \tilde{\Lambda}' v'_\beta) \Sigma_{\mu\alpha}^{(c)}$$

other corrections from the expansion of the states
(non-local corrections)

$$\begin{aligned}
 \langle M'(v') | i \int d^4x \, T [J_0(0), \mathcal{L}_1(x)] | M(v) \rangle = \\
 -\frac{1}{4m_b} \underbrace{\left(-\frac{i}{2} \right) \text{Tr} [\Upsilon_{2\mu\alpha\beta}^{(b)} \overline{\mathcal{M}}'^\mu \Gamma P_+ \sigma^{\alpha\beta} \mathcal{M}]}_{G^{(b)}} - \frac{1}{2m_b^2} \underbrace{\text{Tr} [\Upsilon_{1\mu}^{(b)} \overline{\mathcal{M}}'^\mu \Gamma \mathcal{M}]}_{K^{(b)}}, \\
 \langle M'(v') | i \int d^4x \, T [J_0(0), \mathcal{L}'_1(x)] | M(v) \rangle = \\
 -\frac{1}{4m_c} \underbrace{\left(-\frac{i}{2} \right) \text{Tr} [\Upsilon_{2\mu\alpha\beta}^{(c)} \overline{\mathcal{M}}'^\mu \sigma^{\alpha\beta} P'_+ \Gamma \mathcal{M}]}_{G^{(c)}} - \frac{1}{2m_c^2} \underbrace{\text{Tr} [\Upsilon_{1\mu}^{(c)} \overline{\mathcal{M}}'^\mu \Gamma \mathcal{M}]}_{K^{(c)}},
 \end{aligned}$$



other universal functions involved

- relations among the form factors of the same decay mode

$B_c \rightarrow J/\psi$

$$h_{T_1}(w) = \frac{1}{2} \left((1+w)h_{A_1}(w) - (w-1)h_V(w) \right)$$

$$h_{T_2}(w) = \frac{1+w}{2(m_b+3m_c)} \left((m_b-3m_c)h_{A_1}(w) + 2m_c(h_{A_2}(w) + h_{A_3}(w)) - (m_b-m_c)h_V(w) \right)$$

$$h_{T_3}(w) = h_{A_3}(w) - h_V(w)$$

$$h_P(w) = \frac{1}{m_b+3m_c} \left((1+w)(m_b h_{A_1}(w) + 2m_c h_V(w)) + (-m_b + (w-2)m_c)h_{A_2}(w) - (w m_b + (2w-1)m_c)h_{A_3}(w) \right)$$

$B_c \rightarrow \eta_c$

$$h_-(w) = \frac{m_b-m_c}{2(m_b+3m_c)}(1+w) \left(3h_{A_1}(w) - h_{A_2}(w) - h_{A_3}(w) - 2h_V(w) \right)$$

$$h_T(w) - h_+(w) = -\frac{m_b+m_c}{2(m_b+3m_c)}(1+w) \left(3h_{A_1}(w) - h_{A_2}(w) - h_{A_3}(w) - 2h_V(w) \right)$$

$$h_T(w) - h_S(w) = -\frac{m_b+m_c}{(m_b+3m_c)} \left(3h_{A_1}(w) - h_{A_2}(w) - h_{A_3}(w) - 2h_V(w) \right).$$

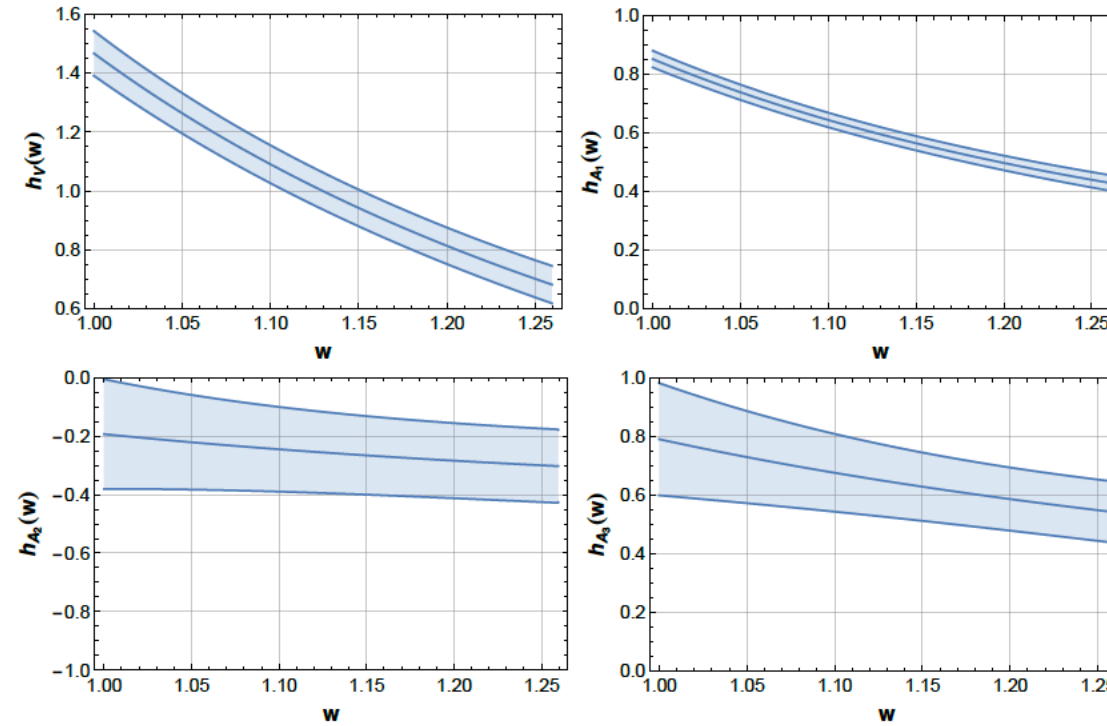
all related to

$h_V(w)$
 $h_{A_1}(w)$ $h_{A_2}(w)$ $h_{A_3}(w)$

P.Colangelo, F. Loperco, N. Losacco,
M. Novoa Brunet, FDF
arXiv:2205.08933,
JHEP09 (2022) 028

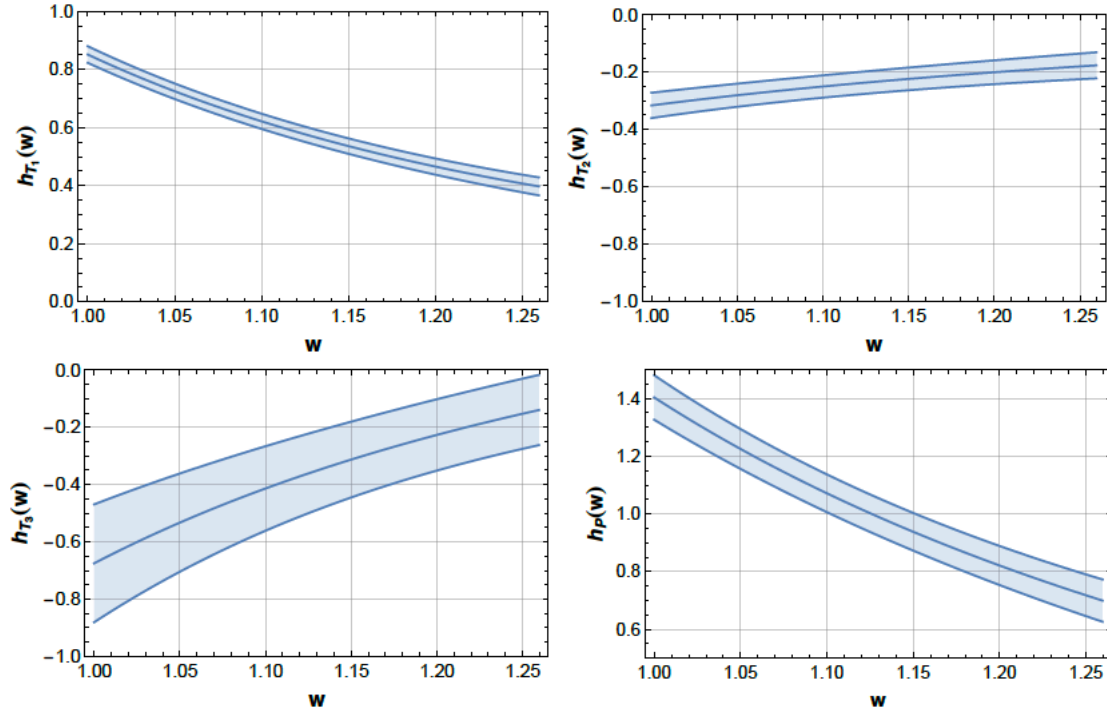
available lattice results

HPQCD Collab.
PRD 102 (2020) 094518
arXiv:2007.06957

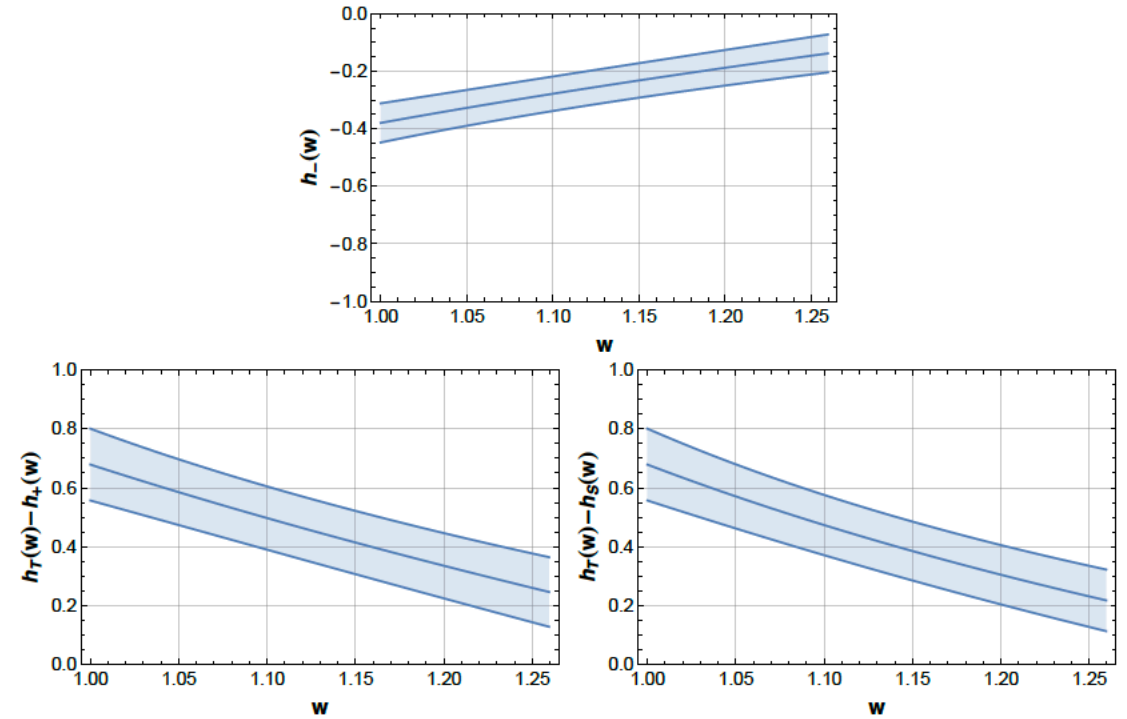


results

$$B_c \rightarrow J/\psi$$



$$B_c \rightarrow \eta_c$$



P.Colangelo, F. Loperco, N. Losacco,
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arXiv:2205.08933,
JHEP09 (2022) 028

- relations among the form factors of the same decay mode

P.Colangelo, F. LOPARCO, N. Losacco,
M. Novoa Brunet, FDF
PRD 106 (2022) 094005
arXiv:2208.13398

- $B_c \rightarrow \chi_{c0}$

$$g_T(w) = -\frac{1}{w+1} [2g_-(w) + g_P(w)]$$

- $B_c \rightarrow \chi_{c1}$

$$g_{T_2}(w) = -\frac{1}{2} [g_{V_1}(w) - (1+w)g_A(w)]$$

$$g_{T_3}(w) = -\frac{1}{2(w-1)} [g_{V_1}(w) + 4g_{V_2}(w)] + \frac{1}{2}g_A(w) + \frac{1}{w-1} [g_S(w) + g_{T_1}(w)]$$

- $B_c \rightarrow \chi_{c2}$

$$k_{T_1}(w) = -wk_V(w) + k_{A_2}(w) + wk_{A_3}(w) + k_P(w)$$

$$k_{T_2}(w) = k_V(w) - k_{A_1}(w) - k_{A_2}(w) - wk_{A_3}(w) - k_P(w)$$

$$k_{T_3}(w) = -k_V(w) + k_{A_3}(w)$$

- $B_c \rightarrow h_c$

$$f_{T_2}(w) = \frac{1}{2} [f_{V_1}(w) + (1+w)f_A(w)]$$

$$f_{T_3}(w) = \frac{1}{2(w-1)} [f_{V_1}(w) + 4f_{V_2}(w)] + \frac{1}{2}f_A(w) - \frac{1}{w-1} [f_S(w) - f_{T_1}(w)]$$

- relations among the form factors of pairs of decay modes

- $B_c \rightarrow \chi_{c0}$ and $B_c \rightarrow \chi_{c1}$

$$(w+1)g_+(w) - (w-1)g_-(w) + g_P(w) = \frac{w+1}{\sqrt{6}} \{2g_{V_1}(w) + (w+1)g_{V_2}(w) - (w-1)[g_{V_3}(w) + g_A(w)] - g_S(w) + 2g_{T_1}(w)\}$$

- $B_c \rightarrow h_c$ and $B_c \rightarrow \chi_{c1}$

$$\begin{aligned} f_{V_1}(w) + (w-1)f_A(w) - 2f_{T_1}(w) = \\ \sqrt{2}\{g_{V_1}(w) + (w+1)g_{V_2}(w) - (w-1)g_{V_3}(w) - g_S(w)\} \\ 3f_{V_1}(w) + 2(w+1)f_{V_2}(w) - (w-1)[2f_{V_3}(w) - f_A(w)] - 2[f_S(w) + f_{T_1}(w)] = \\ \sqrt{2}\{g_{V_1}(w) - (w-1)g_A(w) + 2g_{T_1}(w)\} \end{aligned}$$

$$g_+(w) = 0$$

$$g_S(w) = g_{T_1}(w) = 0$$

$$k_{A_2}(w) = k_{T_3}(w) = 0$$

$$f_{V_1}(w) = f_{V_3}(w) = f_A(w) = f_{T_1}(w) = f_{T_2}(w) = 0$$

$$\text{---} \chi_{c0}$$

$$\text{---} \chi_{c1}$$

$$\text{---} \chi_{c2}$$

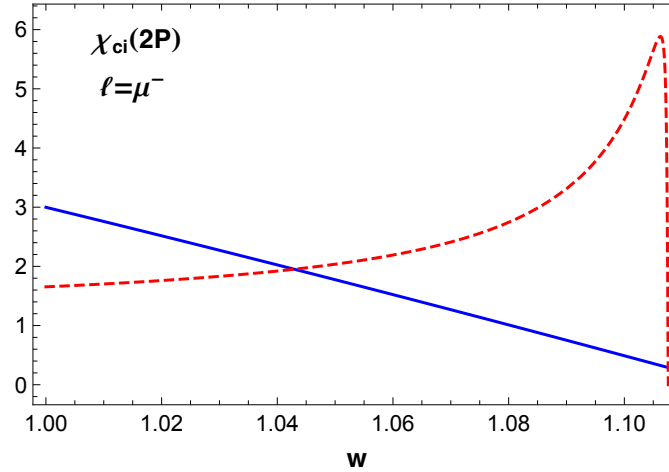
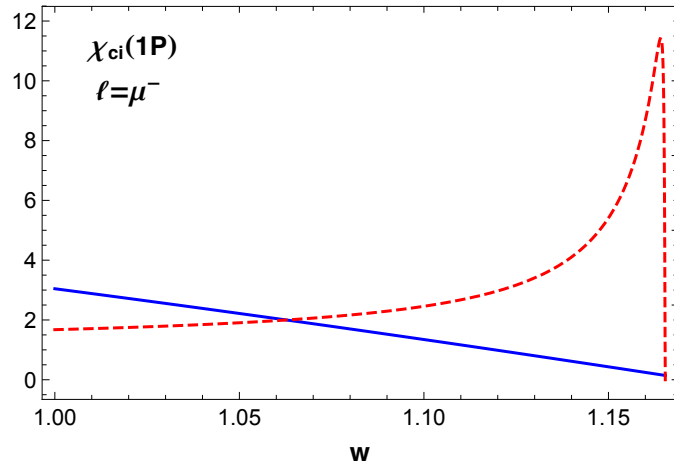
$$\text{---} h_c$$

$$\begin{aligned} \Xi(w) &= \frac{\sqrt{3}}{(w+1)} g_-(w) = -\frac{\sqrt{3}}{(w+1)} g_T(w) = \frac{\sqrt{3}}{(w^2-1)} g_P(w) \\ &= \frac{\sqrt{2}}{(w^2-1)} g_{V_1}(w) = -\frac{2\sqrt{2}}{(w-1)} g_{V_2}(w) = \frac{2\sqrt{2}}{(w+1)} g_{V_3}(w) = \frac{\sqrt{2}}{(w+1)} g_A(w) = \frac{\sqrt{2}}{(w+1)} g_{T_2}(w) \\ &= -k_V(w) = \frac{1}{w+1} k_{A_1}(w) = -k_{A_3}(w) = -k_P(w) = -k_{T_1}(w) = -k_{T_2}(w) \\ &= -f_{V_1}(w) = -f_{V_2}(w) = -\frac{1}{w+1} f_S(w) = f_{T_3}(w) \end{aligned}$$

$B_c \rightarrow (\chi_{c0}, \chi_{c1}, \chi_{c2}, h_c)$ exploiting FF relations at LO

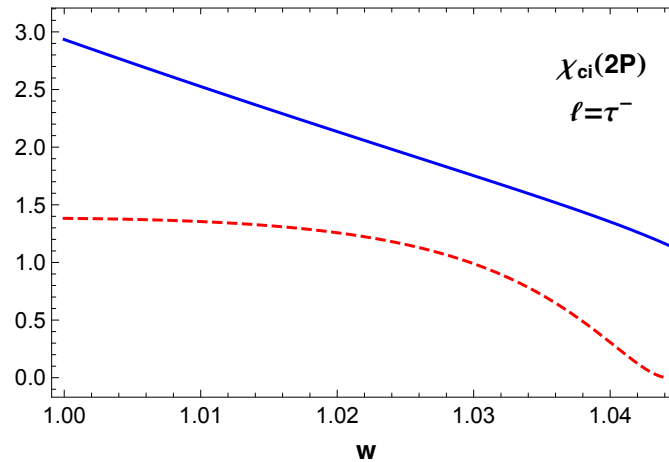
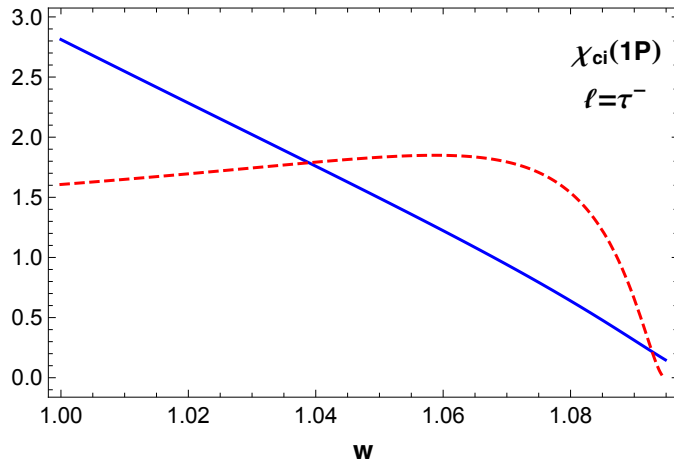
$$\frac{d\Gamma(B_c \rightarrow \chi_{c1} \ell \bar{\nu})/dw}{d\Gamma(B_c \rightarrow \chi_{c0} \ell \bar{\nu})/dw} \quad \frac{d\Gamma(B_c \rightarrow \chi_{c2} \ell \bar{\nu})/dw}{d\Gamma(B_c \rightarrow \chi_{c1} \ell \bar{\nu})/dw}$$

→ the universal function cancels in the ratio

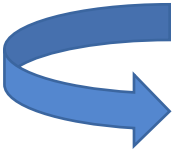


— $\frac{\Gamma(B_c \rightarrow \chi_{c1} \ell \bar{\nu}_\ell)}{\Gamma(B_c \rightarrow \chi_{c0} \ell \bar{\nu}_\ell)}$

- - - $\frac{\Gamma(B_c \rightarrow \chi_{c2} \ell \bar{\nu}_\ell)}{\Gamma(B_c \rightarrow \chi_{c1} \ell \bar{\nu}_\ell)}$



- constraint at LO both in SM and for generic NP


$$2\frac{d\Gamma}{dw}(B_c \rightarrow \chi_{c0}\ell\bar{\nu}_\ell) + \frac{d\Gamma}{dw}(B_c \rightarrow \chi_{c1}\ell\bar{\nu}_\ell) - \frac{d\Gamma}{dw}(B_c \rightarrow \chi_{c2}\ell\bar{\nu}_\ell) = 0.$$

to be satisfied by the three members of the 4-plet

$B_c \rightarrow (\chi_{c0}, \chi_{c1}, \chi_{c2}, h_c)$ exploiting FF relations at LO

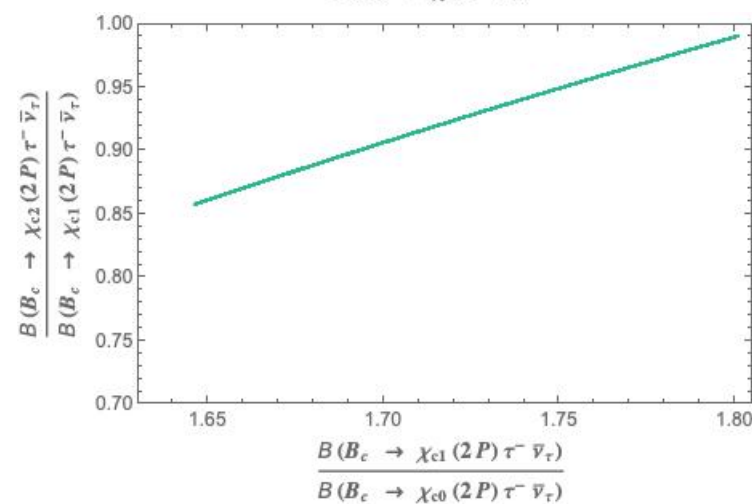
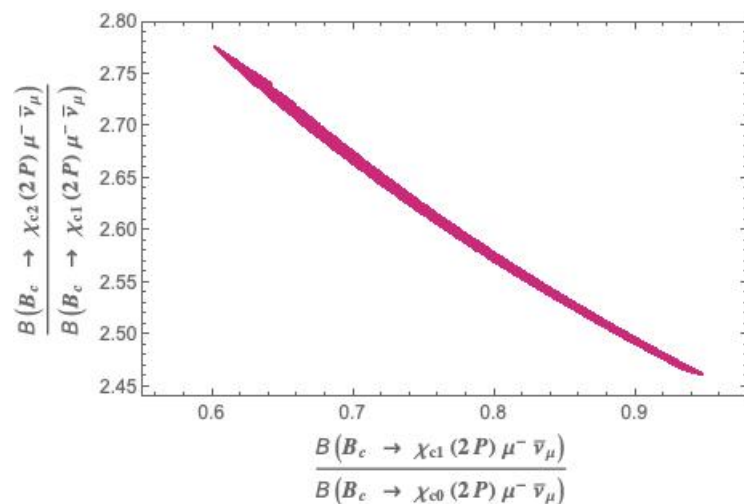
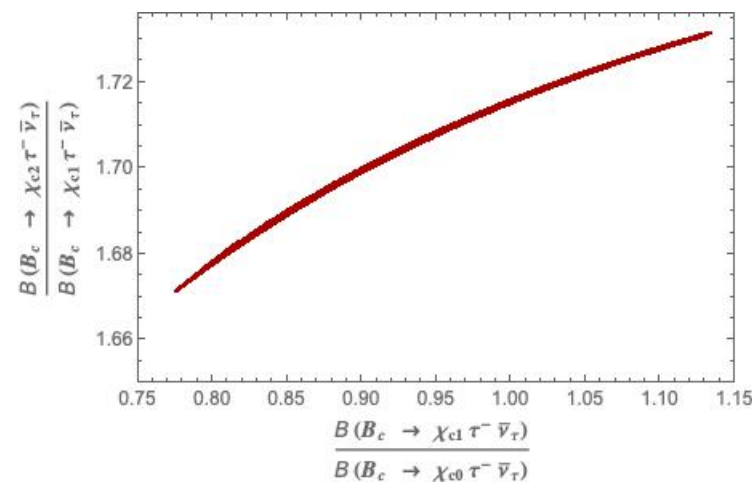
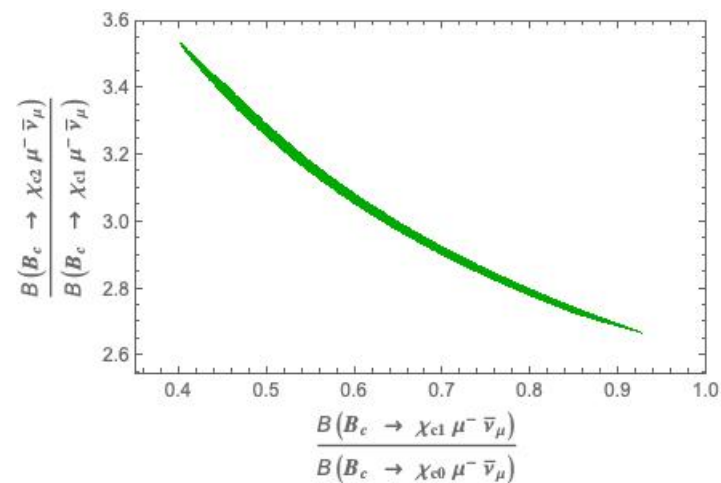
parametrization:

$$\Xi(w) = \Xi_0 + \Xi_1(w - 1) + \Xi_2(w - 1)^2$$

$$\Xi_0 \in [0.1, 1], \Xi_1 \in [-1, 0] \text{ and } \Xi_2 \in [-1, 1]$$

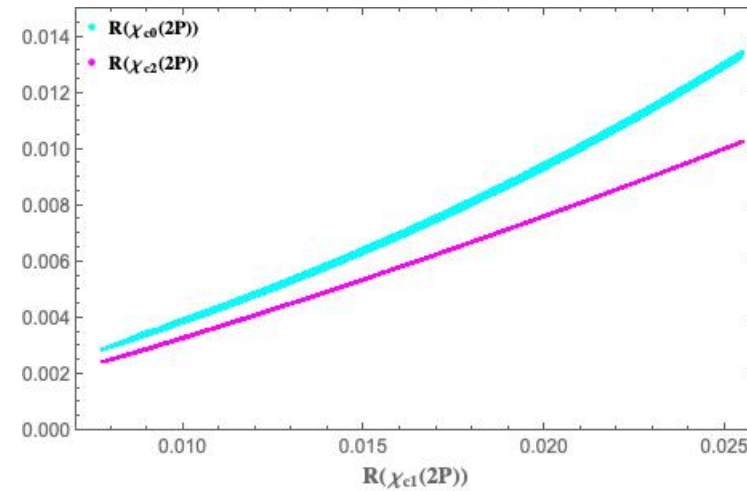
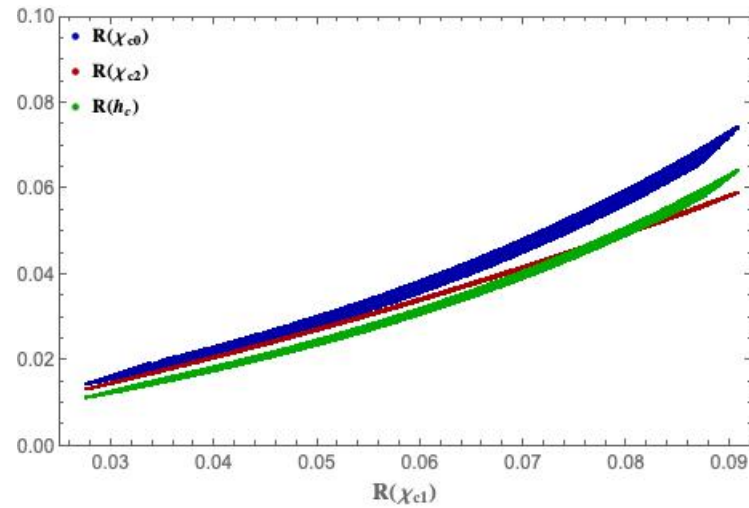
fulfill $\mathcal{B}(B_c^+ \rightarrow \chi_{c0}\pi^+) = (2.4 \pm_{0.8}^{0.9}) \times 10^{-5}$

correlations predicted:



tests of LFU:

$$R(C) = \frac{\Gamma(B_c \rightarrow C \tau \bar{\nu}_\tau)}{\Gamma(B_c \rightarrow C \mu \bar{\nu}_\mu)}$$



At NLO the number of universal functions increase. However:

- they enter in different modes, model independent predictions
- can be used also in other processes
- model independent: tests of direct computations (should satisfy the effective theory predictions)
- Once reliable determinations for a few form factors are available (i.e. by lattice QCD) the others are predicted
- a reduced number of structures contributes close to $w=1$:

$$\begin{aligned} \lim_{w \rightarrow 1} \frac{1}{\tilde{\Gamma}} \frac{d\Gamma}{dw} (B_c \rightarrow \chi_{c0} \ell \bar{\nu}_\ell) &= 18 \hat{m}_\ell^2 (\epsilon_b + \epsilon_c)^2 \left[\Sigma_{\chi_{c1},1}^{(b)}(1) \right]^2 \\ \lim_{w \rightarrow 1} \frac{1}{\tilde{\Gamma}} \frac{d\Gamma}{dw} (B_c \rightarrow \chi_{c1} \ell \bar{\nu}_\ell) &= 12 \left[2(1 - r_1)^2 + \hat{m}_\ell^2 \right] \left[\epsilon_b \Sigma_{\chi_{c1},1}^{(b)}(1) - \epsilon_c \Sigma_{\chi_{c1},1}^{(c)}(1) \right]^2 \\ \lim_{w \rightarrow 1} \frac{1}{\tilde{\Gamma}} \frac{d\Gamma}{dw} (B_c \rightarrow h_c \ell \bar{\nu}_\ell) &= 6 \left[2(1 - r_h)^2 + \hat{m}_\ell^2 \right] \left[(\epsilon_b - \epsilon_c) \Sigma_{\chi_{c1},1}^{(b)}(1) + 2\epsilon_c \Sigma_{\chi_{c1},1}^{(c)}(1) \right]^2 \end{aligned}$$

$$\hat{m}_\ell^2 = \frac{m_\ell^2}{m_{B_c}^2}$$

$$r = m_C / m_{B_c} \quad C = m_{\chi_{c0}}, \chi_{c1}, \chi_{c2}, h_c$$

$$\epsilon_b = \frac{1}{2m_b} \quad \epsilon_c = \frac{1}{2m_c}$$

if $X(3872)$ is $\chi_{c1}(2P)$ these relations should be fulfilled (hard task...)

Semileptonic B_c decays: $c \rightarrow s, d$ transitions

$B_c \rightarrow B_{s,d}$

$$\langle P(p') | \bar{q} \gamma_\mu Q | B_c(p) \rangle = f_+^{B_c \rightarrow P}(q^2) \left(p_\mu + p'_\mu - \frac{m_{B_c}^2 - m_P^2}{q^2} q_\mu \right) + f_0^{B_c \rightarrow P}(q^2) \frac{m_{B_c}^2 - m_P^2}{q^2} q_\mu ,$$

$$\langle P(p') | \bar{q} Q | B_c(p) \rangle = f_S^{B_c \rightarrow P}(q^2) ,$$

$$\langle P(p') | \bar{q} \sigma_{\mu\nu} Q | B_c(p) \rangle = -i \frac{2f_T^{B_c \rightarrow P}(q^2)}{m_{B_c} + m_P} (p_\mu p'_\nu - p_\nu p'_\mu) ,$$

$$\langle P(p') | \bar{q} \sigma_{\mu\nu} \gamma_5 Q | B_c(p) \rangle = -\frac{2f_T^{B_c \rightarrow P}(q^2)}{m_{B_c} + m_P} \epsilon_{\mu\nu\alpha\beta} p^\alpha p'^\beta$$

4 FFs

$B_c \rightarrow B_{s,d}^*$

$$\langle V(p', \epsilon) | \bar{q} \gamma_\mu Q | B_c(p) \rangle = -\frac{2V^{B_c \rightarrow V}(q^2)}{m_{B_c} + m_V} i \epsilon_{\mu\nu\alpha\beta} \epsilon^{*\nu} p^\alpha p'^\beta ,$$

$$\begin{aligned} \langle V(p', \epsilon) | \bar{q} \gamma_\mu \gamma_5 Q | B_c(p) \rangle &= (m_{B_c} + m_V) \left(\epsilon_\mu^* - \frac{(\epsilon^* \cdot q)}{q^2} q_\mu \right) A_1^{B_c \rightarrow V}(q^2) - \frac{(\epsilon^* \cdot q)}{m_{B_c} + m_V} \left((p + p')_\mu - \frac{m_{B_c}^2 - m_V^2}{q^2} q_\mu \right) A_2^{B_c \rightarrow V}(q^2) \\ &\quad + (\epsilon^* \cdot q) \frac{2m_V}{q^2} q_\mu A_0^{B_c \rightarrow V}(q^2) , \end{aligned}$$

$$\langle V(p', \epsilon) | \bar{q} \gamma_5 Q | B_c(p) \rangle = -\frac{2m_V}{m_Q + m_q} (\epsilon^* \cdot q) A_0^{B_c \rightarrow V}(q^2) ,$$

$$\langle V(p', \epsilon) | \bar{q} \sigma_{\mu\nu} Q | B_c(p) \rangle = T_0^{B_c \rightarrow V}(q^2) \frac{\epsilon^* \cdot q}{(m_{B_c} + m_V)^2} \epsilon_{\mu\nu\alpha\beta} p^\alpha p'^\beta + T_1^{B_c \rightarrow V}(q^2) \epsilon_{\mu\nu\alpha\beta} p^\alpha \epsilon^{*\beta} + T_2^{B_c \rightarrow V}(q^2) \epsilon_{\mu\nu\alpha\beta} p'^\alpha \epsilon^{*\beta} ,$$

$$\begin{aligned} \langle V(p', \epsilon) | \bar{q} \sigma_{\mu\nu} \gamma_5 Q | B_c(p) \rangle &= i T_0^{B_c \rightarrow V}(q^2) \frac{\epsilon^* \cdot q}{(m_{B_c} + m_V)^2} (p_\mu p'_\nu - p_\nu p'_\mu) \\ &\quad + i T_1^{B_c \rightarrow V}(q^2) (p_\mu \epsilon_\nu^* - \epsilon_\mu^* p_\nu) + i T_2^{B_c \rightarrow V}(q^2) (p'_\mu \epsilon_\nu^* - \epsilon_\mu^* p'_\nu) \end{aligned}$$

6 FFs

$$\langle P(v, k) | \bar{q} \gamma_\mu Q | B_c(v) \rangle = 2\sqrt{m_{B_c} m_P} \left(\Omega_1(y) v_\mu + a_0 \Omega_2(y) k_\mu \right),$$

$$\langle P(v, k) | \bar{q} Q | B_c(v) \rangle = 2\sqrt{m_{B_c} m_P} \left(\Omega_1(y) + a_0 \Omega_2(y) v \cdot k \right),$$

$$\langle P(v, k) | \bar{q} \sigma_{\mu\nu} Q | B_c(v) \rangle = -2i\sqrt{m_{B_c} m_P} a_0 \Omega_2(y) (v_\mu k_\nu - v_\nu k_\mu)$$

$$\langle V(v, k, \epsilon) | \bar{q} \gamma_\mu Q | B_c(v) \rangle = 2i\sqrt{m_{B_c} m_V} a_0 \Omega_2(y) \epsilon_{\mu\nu\alpha\beta} \epsilon^{*\nu} k^\alpha v^\beta,$$

$$\langle V(v, k, \epsilon) | \bar{q} \gamma_\mu \gamma_5 Q | B_c(v) \rangle = 2\sqrt{m_{B_c} m_V} \left(\epsilon_\mu^* (\Omega_1(y) + v \cdot k a_0 \Omega_2(y)) - (v_\mu - \frac{k_\mu}{m_V}) \epsilon^* \cdot k a_0 \Omega_2(y) \right),$$

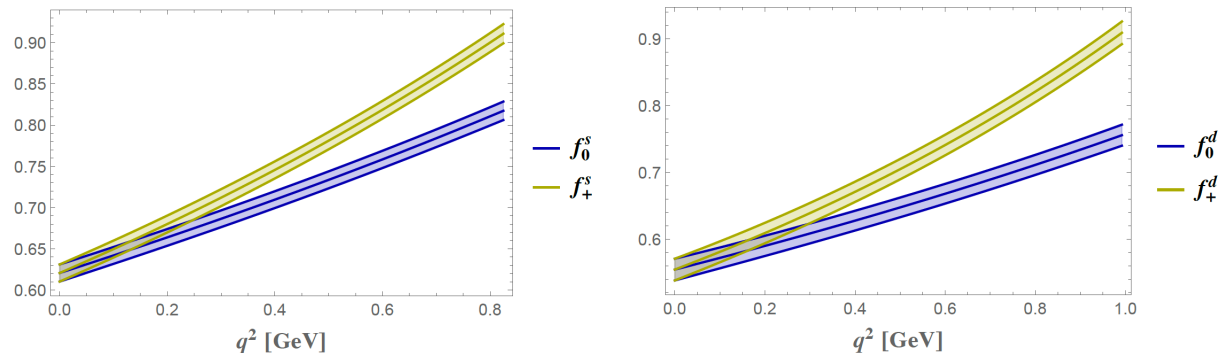
$$\langle V(v, k, \epsilon) | \bar{q} \sigma_{\mu\nu} Q | B_c(v) \rangle = -2\sqrt{m_{B_c} m_V} \left(\epsilon_{\mu\nu\alpha\beta} \epsilon^{*\alpha} v^\beta \Omega_1(y) + \epsilon_{\mu\nu\alpha\beta} \epsilon^{*\alpha} k^\beta a_0 \Omega_2(y) \right),$$

$$\langle V(v, k, \epsilon) | \bar{q} \sigma_{\mu\nu} \gamma_5 Q | B_c(v) \rangle = 2i\sqrt{m_{B_c} m_V} \left(\epsilon_\nu^* (v_\mu \Omega_1(y) + k_\mu a_0 \Omega_2(y)) - \epsilon_\mu^* (v_\nu \Omega_1(y) + k_\nu a_0 \Omega_2(y)) \right)$$



all expressed in terms of Ω_1 and Ω_2

lattice results for f_+ and f_0

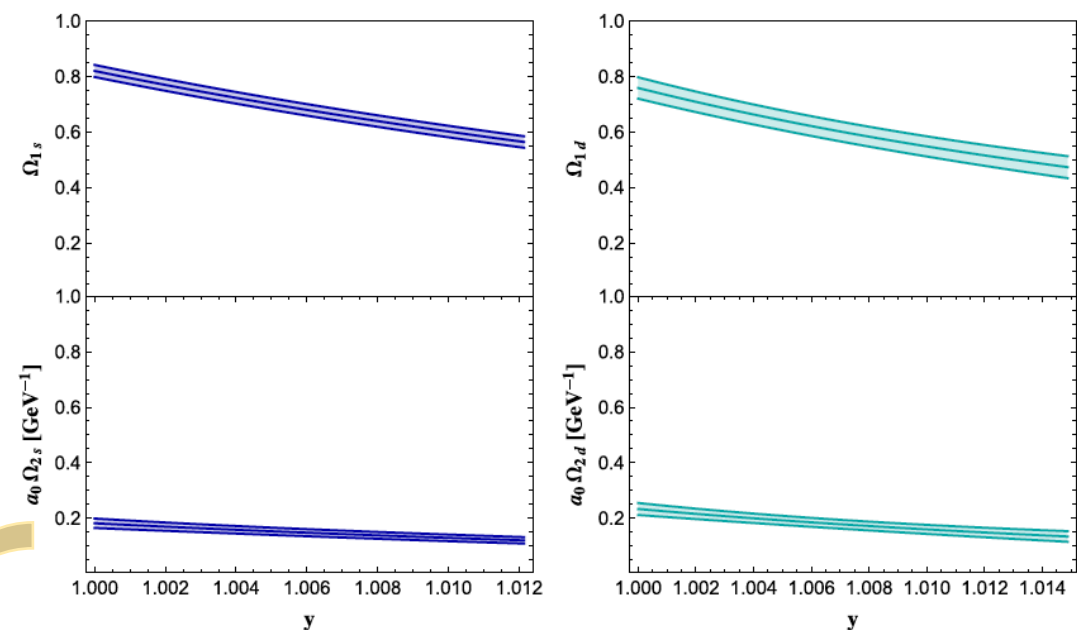


obtained from data in
HPQCD Collab. PRD102 (2020) 014513

translated into Ω_1 and Ω_2 :

$$\Omega_1 = \frac{m_{B_c} + m_P}{2q^2 \sqrt{m_{B_c} m_P}} ((m_{B_c} - m_P)^2 (f_0 - f_+) + q^2 f_+)$$

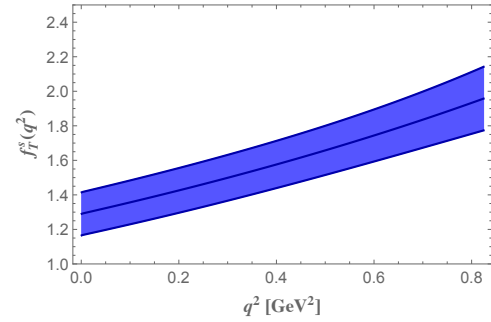
$$a_0 \Omega_2 = \frac{1}{2q^2 \sqrt{m_{B_c} m_P}} ((m_{B_c}^2 - m_P^2) (f_+ - f_0) + q^2 f_+)$$



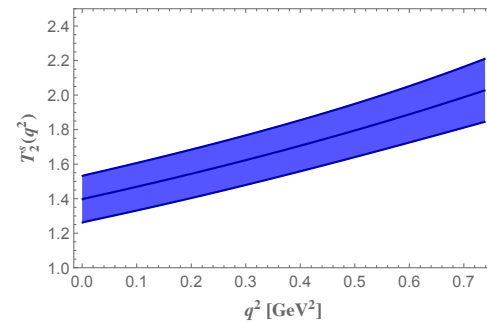
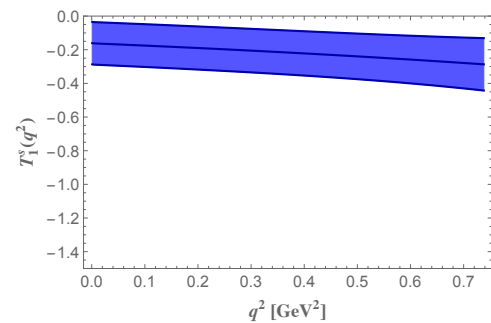
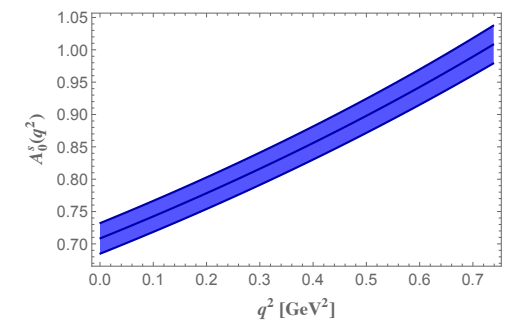
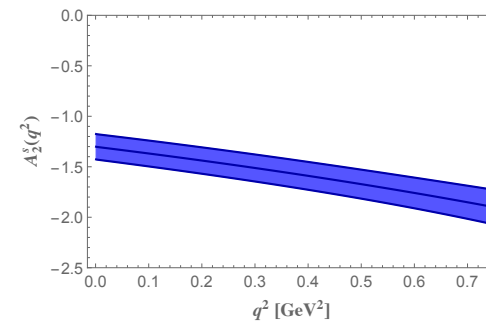
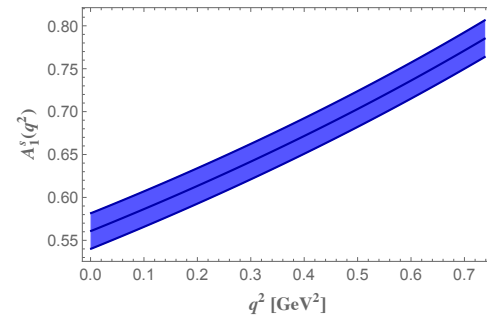
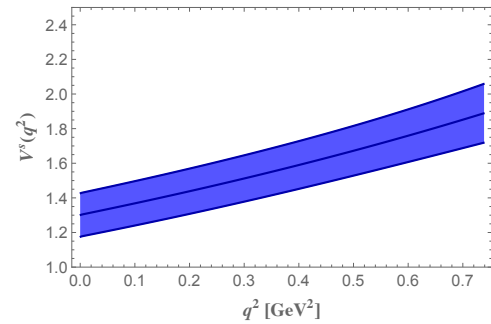
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all other FFs derived from these functions

$$B_c \rightarrow B_s \ell \nu_\ell$$

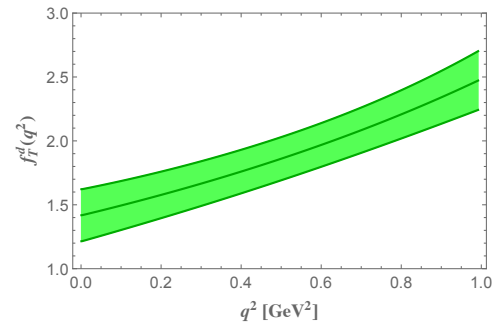


$$B_c \rightarrow B_s^* \ell \nu_\ell$$

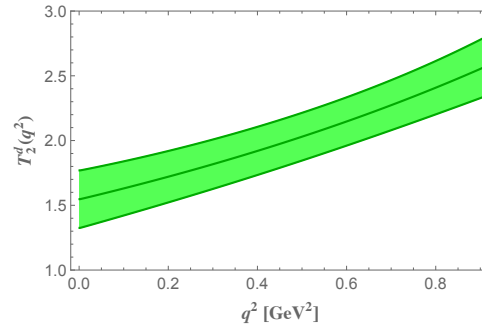
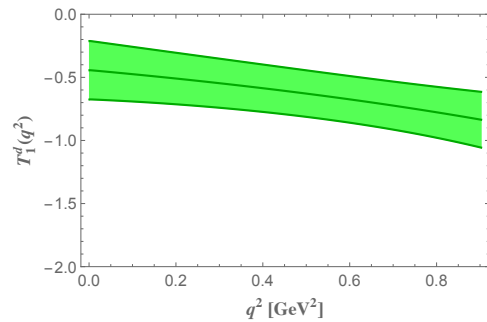
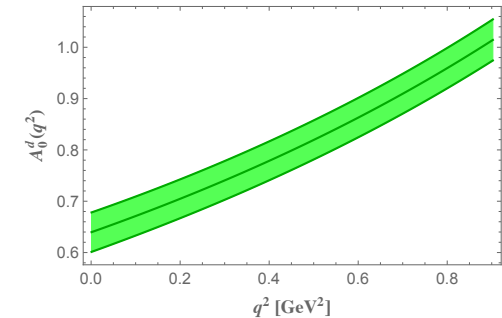
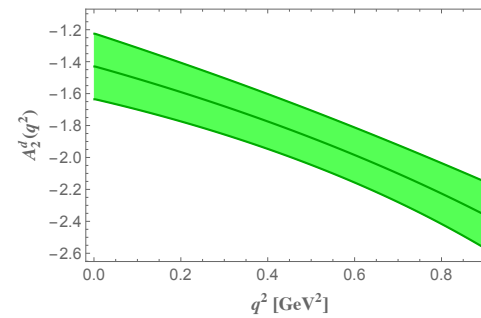
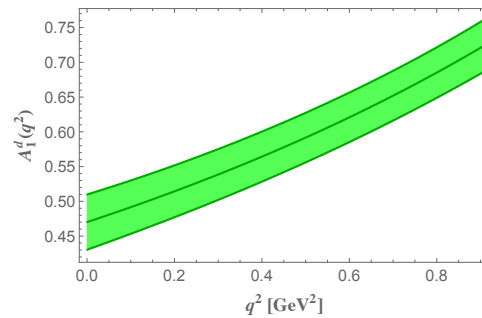
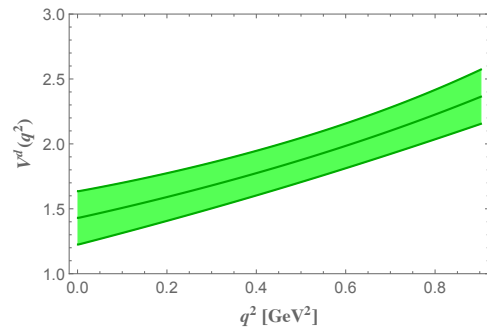


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$$B_c \rightarrow B_d \ell \nu_\ell$$



$$B_c \rightarrow B_d^* \ell \nu_\ell$$



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Results

$$B_c \rightarrow B^{(*)}_s \ell \nu_\ell$$

$$\mathcal{B}(B_c^+ \rightarrow B_s \mu^+ \nu_\mu) = 0.0125 (4) \left(\frac{|V_{cs}|}{0.987} \right)^2$$

$$\mathcal{B}(B_c^+ \rightarrow B_s e^+ \nu_e) = 0.0131 (4) \left(\frac{|V_{cs}|}{0.987} \right)^2$$

$$\mathcal{B}(B_c^+ \rightarrow B_s^* \mu^+ \nu_\mu) = 0.030 (1) \left(\frac{|V_{cs}|}{0.987} \right)^2$$

$$\mathcal{B}(B_c^+ \rightarrow B_s^* e^+ \nu_e) = 0.032 (1) \left(\frac{|V_{cs}|}{0.987} \right)^2$$

SM branching fractions

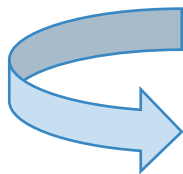
$$B_c \rightarrow B^{(*)}_d \ell \nu_\ell$$

$$\mathcal{B}(B_c^+ \rightarrow B_d \mu^+ \nu_\mu) = 8.3 (5) \times 10^{-4} \left(\frac{|V_{cd}|}{0.221} \right)^2$$

$$\mathcal{B}(B_c^+ \rightarrow B_d e^+ \nu_e) = 8.7 (5) \times 10^{-4} \left(\frac{|V_{cd}|}{0.221} \right)^2$$

$$\mathcal{B}(B_c^+ \rightarrow B_d^* \mu^+ \nu_\mu) = 20 (1) \times 10^{-4} \left(\frac{|V_{cd}|}{0.221} \right)^2$$

$$\mathcal{B}(B_c^+ \rightarrow B_d^* e^+ \nu_e) = 21 (1) \times 10^{-4} \left(\frac{|V_{cd}|}{0.221} \right)^2$$



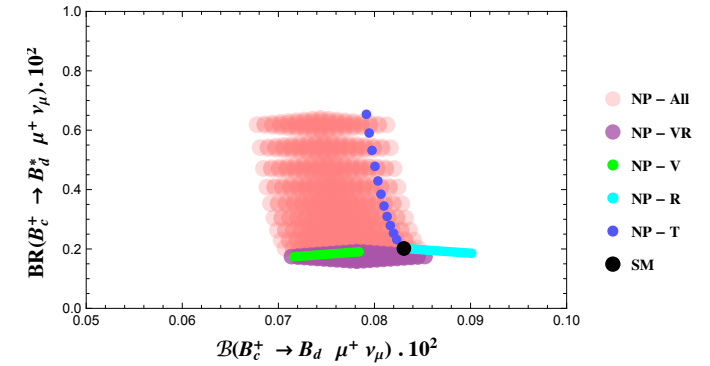
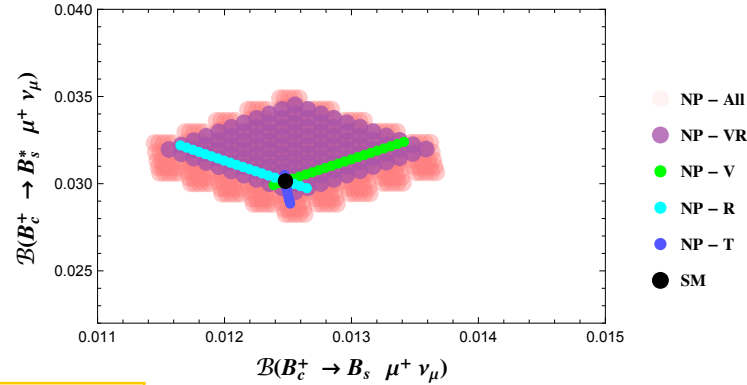
small uncertainty: role of the HQSS relations

branching ratios

NP couplings from
D. Becirevic, F. Jaffredo, A. Penuelas, O. Sumnsari,
JHEP05 (2021) 175

Forward-Backward lepton asymmetry

$$\mathcal{A}_{FB}(q^2) = \left(\frac{d\Gamma}{dq^2} \right)^{-1} \left[\int_0^1 d\cos\theta \frac{d^2\Gamma}{dq^2 d\cos\theta} - \int_{-1}^0 d\cos\theta \frac{d^2\Gamma}{dq^2 d\cos\theta} \right]$$



different pattern of correlations:

the presence of R would produce

- anticorrelated BRs
- anticorrelated AFB ($B_c \rightarrow B_s^* \mu \nu_\mu$) and $B(B_c \rightarrow B_s \mu \nu_\mu)$
- correlated AFB ($B_c \rightarrow B_s^* \mu \nu_\mu$) and $B(B_c \rightarrow B_s \mu \nu_\mu)$
- large impact of T on AFB
- large impact of T on BR in $c \rightarrow d$

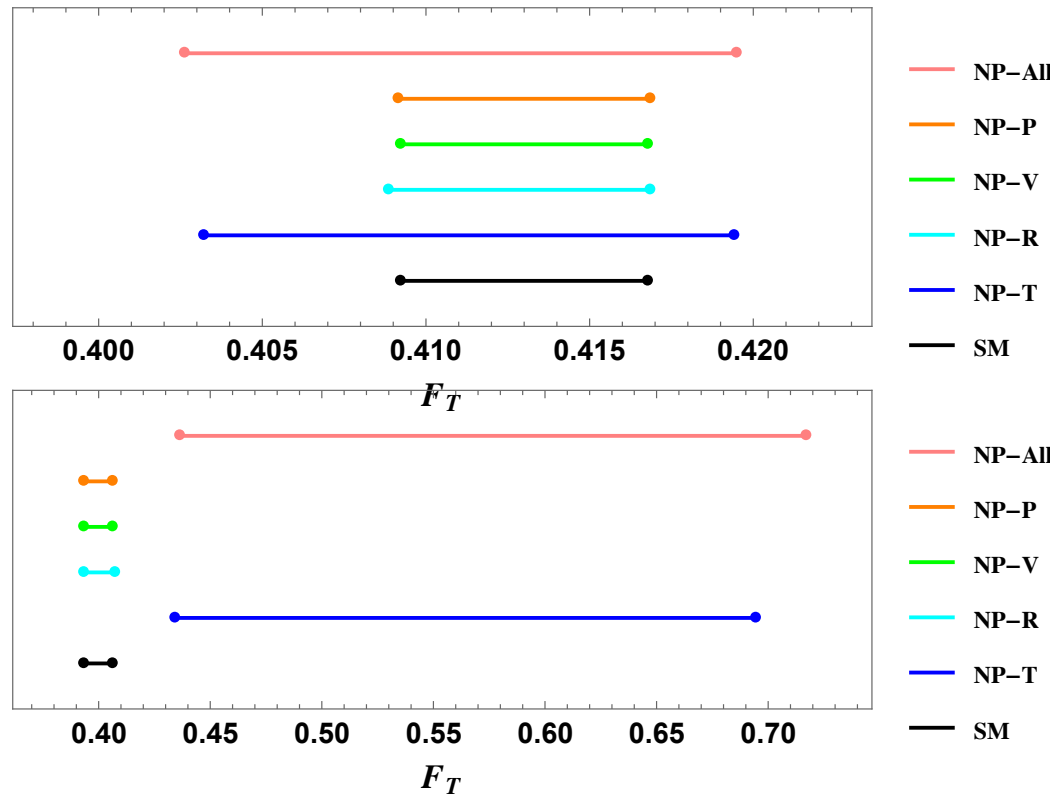
P. Colangelo, F. Loparco, FDF, PRD103 (2021) 075019

$$B_c \rightarrow B_{s,d}^* \mu \nu_\mu$$

fraction of transversely polarized $B_{s,d}^*$

$$B_c \rightarrow B_s^* \mu \nu_\mu$$

$$B_c \rightarrow B_d^* \mu \nu_\mu$$



$c \rightarrow s$: $F_T < 0.5$ in SM and NP
 $c \rightarrow d$: T can reverse the hierarchy

B_c decays represent an interesting testing ground for

- determination of V_{cb}
- flavour anomalies
- probing the structure of the hadrons in the final state

predictions based on NRQCD + HQE

- relations among FFs
- relations to be fulfilled by modes with final hadrons connected by HQSS
- tests of explicit calculations