

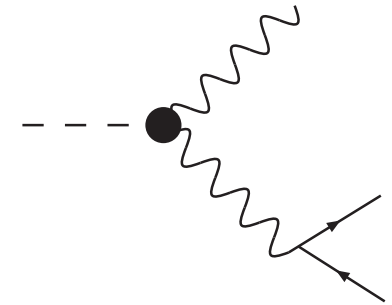
EFFECTIVE FIELD THEORY OF HIGGS-BOSON PROPERTIES

Gerhard Buchalla

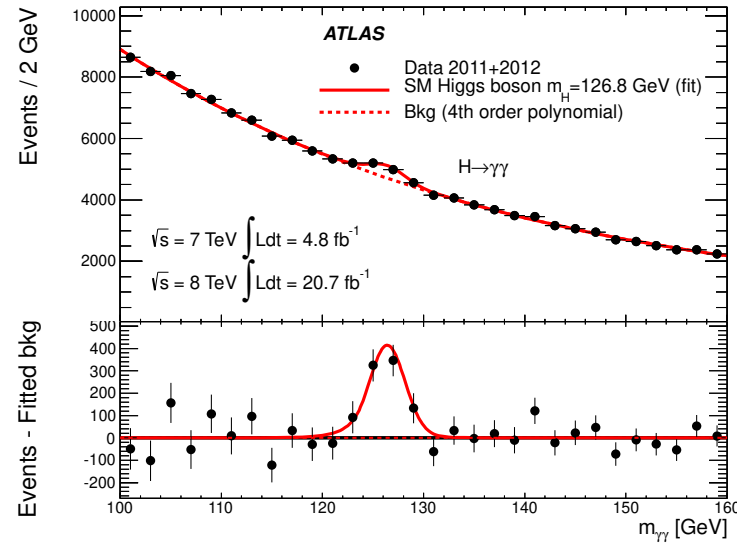
LMU München

Matthias Fest MITP – May 2023

- Anomalous Higgs couplings
- Electroweak chiral Lagrangian (HiggsEFT)
- Applications



*G.B., Oscar Catà, Alejandro Celis, Marc Knecht, Claudius Krause
Gudrun Heinrich, Marius Höfer, Christoph Müller-Salditt, Florian Pandler*



no other new particles so far; $m_h \ll \Lambda$

→ Effective Field Theory

- quarks, leptons, $SU(3)_C$, $SU(2)_L$, $U(1)_Y$
- Goldstones φ^a , $U = \exp(2i\varphi^a T^a / v)$
- light Higgs h

$$U \rightarrow g_L U g_R^\dagger, \quad h \rightarrow h, \quad g_{L,R} \in SU(2)_{L,R}$$

relation to Higgs doublet:

$$(\tilde{\Phi}, \Phi) \equiv (v + h)U$$

$$\begin{aligned}
 \mathcal{L}_{SM} = & -\frac{1}{2}\langle G_{\mu\nu}G^{\mu\nu}\rangle - \frac{1}{2}\langle W_{\mu\nu}W^{\mu\nu}\rangle - \frac{1}{4}B_{\mu\nu}B^{\mu\nu} + \bar{\psi}i\not{D}\psi \\
 & + \frac{v^2}{4}\langle D_\mu U^\dagger D^\mu U\rangle \left(1 + 2\frac{h}{v} + \left(\frac{h}{v}\right)^2\right) \\
 & + \frac{1}{2}\partial_\mu h\partial^\mu h - v^4 \left(\frac{\lambda}{2}\left(\frac{h}{v}\right)^2 + \frac{\lambda}{2}\left(\frac{h}{v}\right)^3 + \frac{\lambda}{8}\left(\frac{h}{v}\right)^4\right) \\
 & - v \left[\bar{q}\hat{Y}_u U P_{+r} \left(1 + \frac{h}{v}\right) + \text{h.c.} + \dots\right]
 \end{aligned}$$

- $U = \exp(2i\varphi^a T^a / v)$
- \mathcal{L}_{SM} , renormalizable

$$\begin{aligned}
 \mathcal{L}_{LO} = & -\frac{1}{2}\langle G_{\mu\nu}G^{\mu\nu}\rangle - \frac{1}{2}\langle W_{\mu\nu}W^{\mu\nu}\rangle - \frac{1}{4}B_{\mu\nu}B^{\mu\nu} + \bar{\psi}i\not{D}\psi \\
 & + \frac{v^2}{4}\langle D_\mu U^\dagger D^\mu U\rangle \left(1 + F_1\frac{h}{v} + F_2\left(\frac{h}{v}\right)^2 + \dots\right) \\
 & + \frac{1}{2}\partial_\mu h\partial^\mu h - v^4\left(V_2\left(\frac{h}{v}\right)^2 + V_3\left(\frac{h}{v}\right)^3 + V_4\left(\frac{h}{v}\right)^4 + \dots\right) \\
 & - v\left[\sum_{n=0}^{\infty}\bar{q}\hat{Y}_u^{(n)}UP_{+r}\left(\frac{h}{v}\right)^n + \text{h.c.} + \dots\right]
 \end{aligned}$$

- $U = \exp(2i\varphi^a T^a / v)$, $F_i - F_{i,SM} \sim \xi \equiv v^2 / f^2$, etc.
- \mathcal{L}_{LO} non-renormalizable, cut-off $\Lambda = 4\pi f \rightarrow \text{EW}\chi\text{L}$

- **particle content** of SM, mass gap
gauge bosons and fermions weakly coupled to Higgs dynamics
- **symmetries**: SM gauge symmetries
conservation of lepton and baryon number
conservation *at lowest order* of custodial symmetry,
CP invariance in the Higgs sector, (fermion flavour).
- **power counting** by chiral dimensions \Leftrightarrow loop expansion

Loop counting \equiv chiral counting

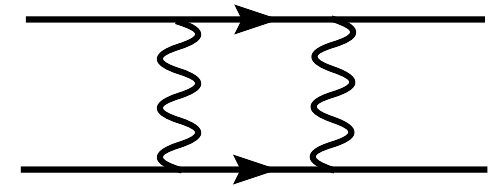
Urech; Knecht, Neufeld, Rupertsberger, Talavera; G.B., Catà, Krause

chiral dimensions: $[A_\mu, \varphi, h]_c = 0, \quad [\partial_\mu, g, y, \psi\bar{\psi}]_c = 1$

loop order: $2L + 2 = \Sigma$ (*chiral dim.*)

examples:

$$m_h^2 = \lambda v^2$$



$\Rightarrow [\mathcal{L}_{LO}]_c = 2, \quad [\text{NLO}]_c = 4 \quad (\text{local terms; } D^n, n \geq 0)$

$$UhD^4, \quad g^2 X^2 Uh, \quad gXUhD^2, \quad y^2\psi^2UhD, \quad y\psi^2UhD^2, \quad y^2\psi^4Uh$$

One-loop renormalization and RGE

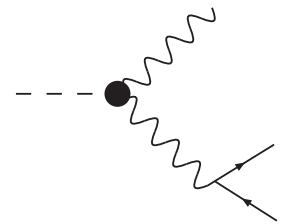
$$e^{iS_{eff}} \sim \int d\varphi_i d\chi d\bar{\chi} e^{i \int d^D x \mathcal{L}_2(\varphi_i, \chi, \bar{\chi})}$$

NLO counterterms: *G.B., Catà, Celis, Knecht, Krause; Alonso et al.*

super-heat-kernel expansion: *Neufeld, Gasser, Ecker*

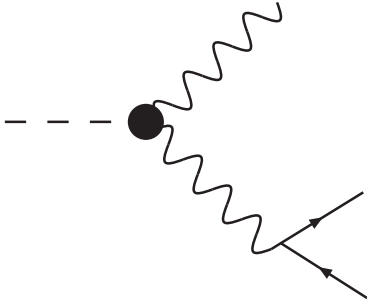
hVV coupling F_1 :

$$\begin{aligned} \frac{F_1(\mu)}{2} &\approx \frac{F_1(v)}{2} + (4F_2 - F_1^2) \frac{N_c m_t^4}{8\pi^2 v^2 m_h^2} \ln \frac{\mu}{v} \\ &\approx \frac{F_1(v)}{2} + (4F_2 - F_1^2) 0.125 \end{aligned}$$

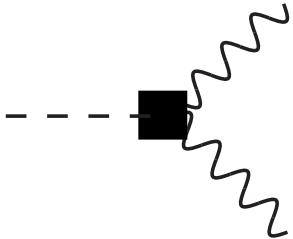
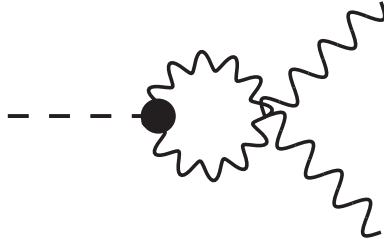
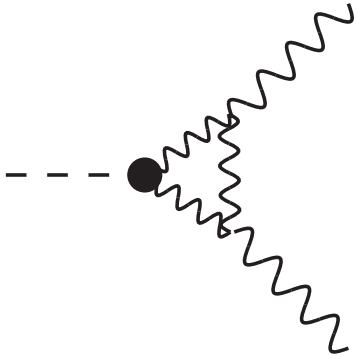
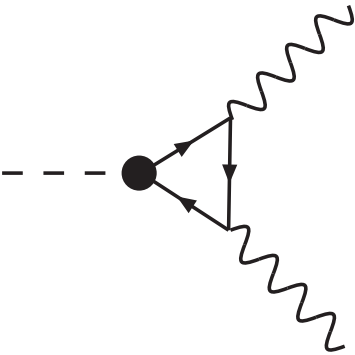


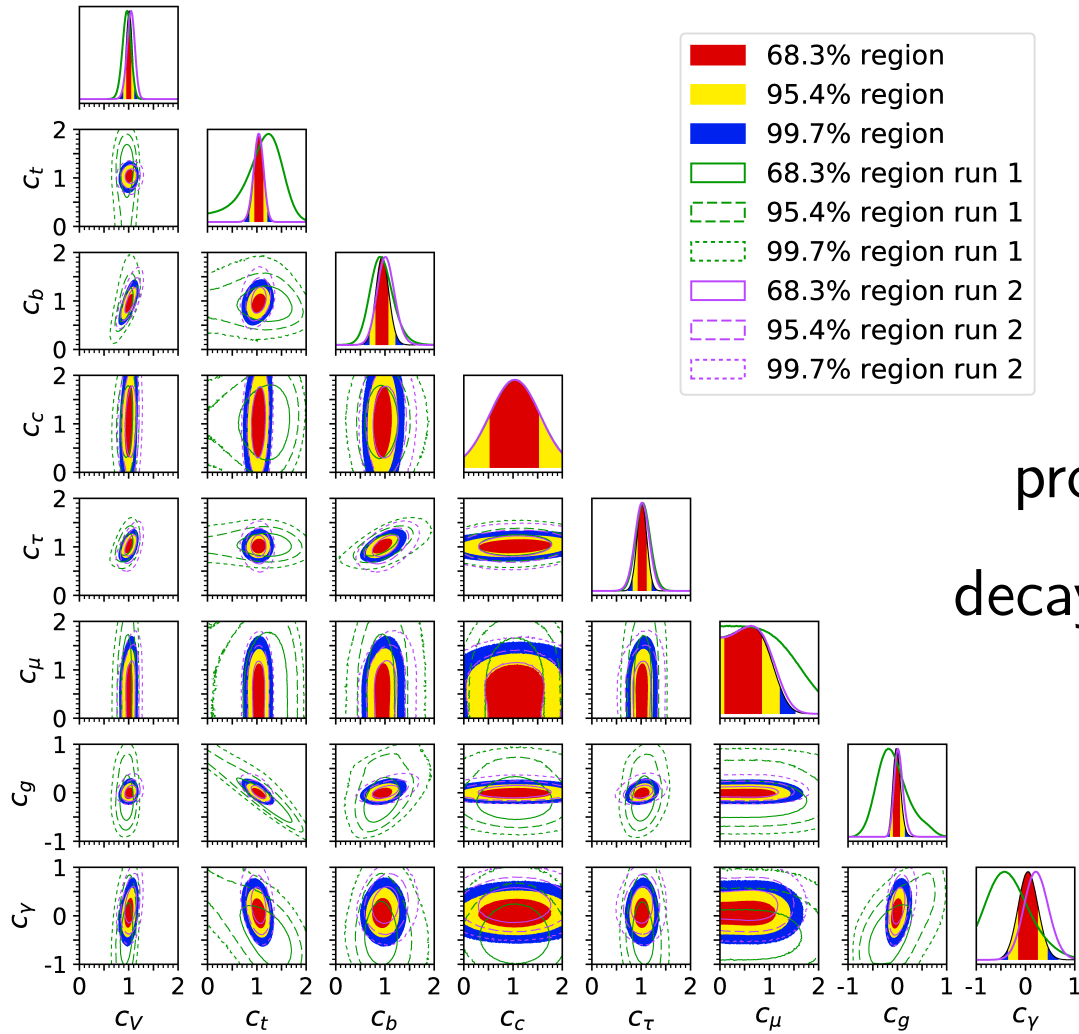
Applications

$$h \rightarrow Zl^+l^-$$



$$h \rightarrow \gamma\gamma$$



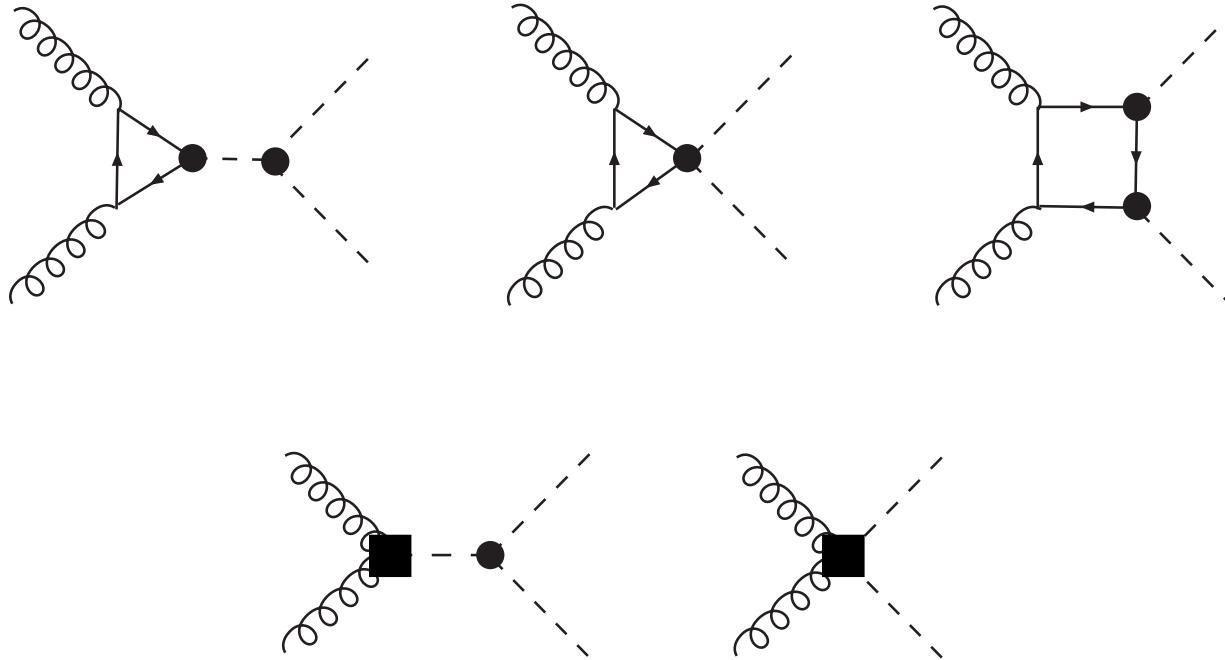


production: $ggh, Wh/Zh, VBF, t\bar{t}h$

decay: $h \rightarrow \gamma\gamma, WW, ZZ, b\bar{b}, \tau\bar{\tau}, \dots$

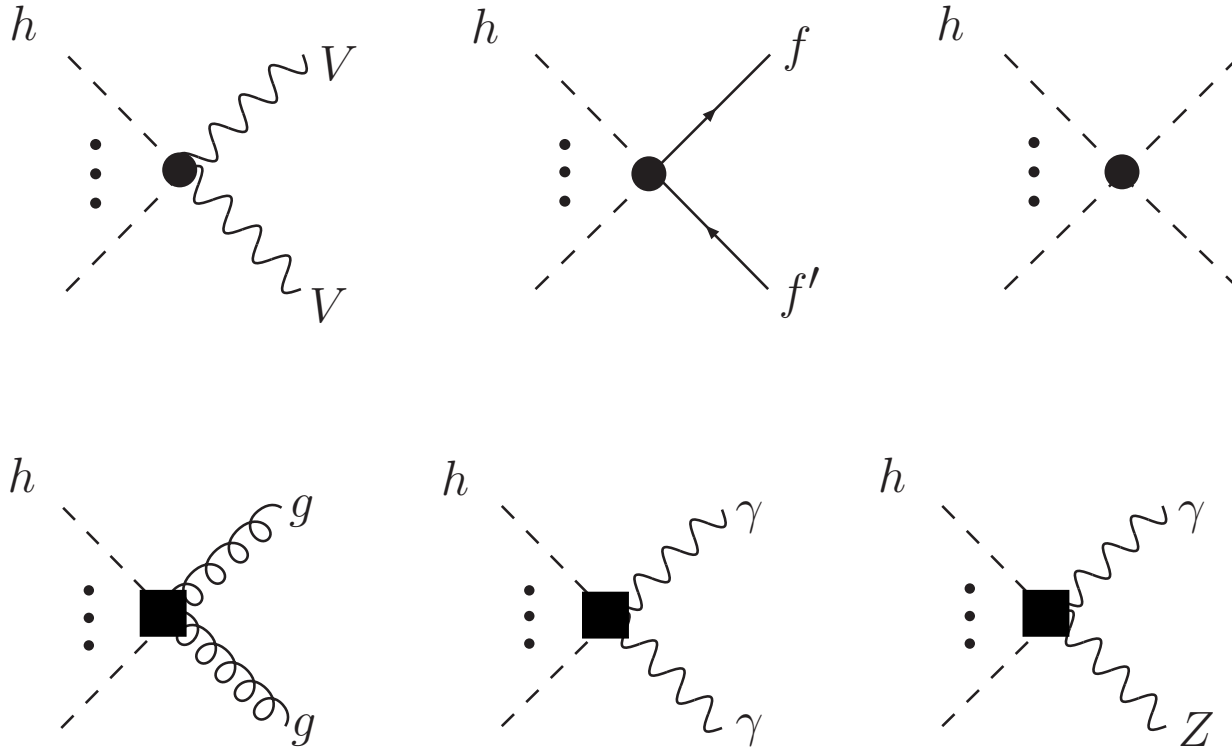
de Blas, Eberhardt, Krause, '18

Higgs-pair production in gluon fusion



*Gröber, Mühlleitner, Spira, Streicher
Borowka, Greiner, Heinrich, Jones, Kerner, Schlenk, Zirke
G.B., Capozzi, Celis, Heinrich, Scyboz*

- natural framework for anomalous Higgs couplings
- consistent EFT, systematic improvement possible
- well adapted to LHC precision with 300 fb^{-1} (Run 2 and 3)
- QFT justification of κ -framework



$$\begin{aligned} \mathcal{L} = & 2c_V \left(m_W^2 W_\mu^+ W^{-\mu} + \frac{1}{2} m_Z^2 Z_\mu Z^\mu \right) \frac{h}{v} - c_t y_t \bar{t} t h - c_b y_b \bar{b} b h - c_\tau y_\tau \bar{\tau} \tau h \\ & + \frac{e^2}{16\pi^2} c_{\gamma\gamma} F_{\mu\nu} F^{\mu\nu} \frac{h}{v} + \frac{g_s^2}{16\pi^2} c_{gg} \langle G_{\mu\nu} G^{\mu\nu} \rangle \frac{h}{v} \end{aligned}$$

$$\Lambda = 4\pi f$$

f

v

$$\xi = \frac{v^2}{f^2} \rightarrow \text{dim. exp.}$$

$$\frac{1}{16\pi^2} \approx \frac{f^2}{\Lambda^2} \rightarrow \text{loop exp.}$$

