Importance of Non-Perturbative Effects for the Exclusion or Discovery of Dark Matter Models

Julia Harz

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Pushing the limits of theoretical physics





Pushing the limits of the WIMP





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Forbes

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The 'WIMP Miracle' Hope For Dark Matter Is Dead



Ethan Siegel Senior Contributor Starts With A Bang Contributor Group O Science

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NEWS · 02 OCTOBER 2020

Last chance for WIMPs: physicists launch all-out hunt for dark-matter candidate

Researchers have spent decades searching for the elusive particles – a final generation of detectors should leave them no place to hide.



Pushing the limits of the WIMP

- no observations at the LHC, direct or indirect detection so far that supports the *minimal* WIMP model
- **Reasons** could be manifold:

(1) completely **different type** of DM (PBHs, etc.)

(2) another DM generation mechanism, e.g. freeze-in instead of freeze-out

- (3) more **complex WIMP** models can evade bounds
- (4) "exceptions" in the **DM abundance calculation** that were previously not considered (5) ...



 X_i

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Indirect detection

SM

SM

DM

DM

Direct

detection

Pushing the limits of the WIMP

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- **Reasons** could be manifold:

(1) completely **different type** of DM (PBHs, etc.)

- (2) another DM generation mechanism, e.g. freeze-in instead of freeze-out
- (3) more **complex WIMP** models can evade bounds
- (4) "exceptions" in the **DM abundance calculation** that were previously not considered X_{X_i} (5) ...

If we want to rule out WIMP models conclusively, we have to consider possible subtleties.



Importance of non-perturbative effects for the exclusion of DM models



Collider Search

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Community effort: LHC DM working group

Recently common focus on white paper about t-channel DM models

Closing in on *t*-channel simplified dark matter models

Chiara Arina^a, Benjamin Fuks^{b,c}, Luca Mantani^a, Hanna Mies^d, Luca Panizzi^{e,f} and Jakub Salko^e

^a Centre for Cosmology, Particle Physics and Phenomenology (CP3), Université catholique de Louvain, B-1348 Louvain-la-Neuve, Belgium
 ^b Sorbonne Université, CNRS, Laboratoire de Physique Théorique et Hautes Énergies, LPTHE, F-75005 Paris, France
 ^c Institut Universitaire de France, 103 boulevard Saint-Michel, F-75005 Paris, France
 ^d Institute for Theoretical Particle Physics and Cosmology, RWTH Aachen University, D-52056 Aachen, Germany
 ^e Department of Physics and Astronomy, Uppsala University, Box 516, SE-751 20 Uppsala, Sweden
 ^f School of Physics and Astronomy, University of Southampton, Highfield, Southampton SO17 1BJ, UK

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ABSTRACT

Keywords: Dark matter simplified models, collider searches, cosmological bounds

A comprehensive analysis of c

A comprehensive analysis of cosmological and collider constraints is presented for three simplified models characterised by a dark matter candidate (real scalar, Majorana fermion and real vector) and a coloured mediator (fermion, scalar and fermion respectively) interacting with the right-handed up quark of the Standard Model. Constraints from dark matter direct and indirect detection and relic density are combined with bounds originating from the re-interpretation of a full LHC run 2 ATLAS search targeting final states with multiple jets and missing transverse energy. Projections for the high-luminosity phase of the LHC are also provided to assess future exclusion and discovery reaches, which show that analogous future search strategies will not allow for a significant improvement compared with the present status. From the cosmological point of view, we demonstrate that thermal dark matter is largely probed (and disfavoured) by constraints from current direct and indirect detection experiments. These bounds and their future projections have moreover the potential of probing the whole parameter space when combined with the expectation of the high-luminosity phase of the LHC.





 M_{χ} (GeV)



Importance of non-perturbative effects for the exclusion of DM models

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Community effort: non-perturbative effects in DM



Non-perturbative effects such as Sommerfeld effect and bound state formation can significantly alter the theoretical prediction of the DM relic abuandance.



Community effort: non-perturbative effects in DM

- Development of **formalism** to describe boundstate formation (and • Sommerfeld effect) for dark matter abundance at zero-T incl. nonequilibrium dynamics Von Harling, Petraki (2014), Petraki, Postma, Wiechers (2015), Petraki, Postma, de Vries (2016)
- Demonstrating **phenomenological impact** on EW and strongly . coupled WIMP scenarios e.g. Asadi, Baumgart, Fitzpatrick, Krupczak, Slatyer (2016), Mitridate, Strumia, Smirnov, Redi (2017), JH, Petraki (2018), JH. Petraki (2018). JH. Petraki (2019)
- Development of **finite-T treatment** of bound state formation while still in • ionization equilibrium Kim, Laine (2017), Biondini, Laine (2018), Biondini (2018), Covi, Binder, Mukaida (2018)
- Phenomenology of finite-T treatment of bound state formation while still • in ionization equilibrium Biondini, Voal (2018), Biondini, Voal (2019)
- Presenting finite-T treatment beyond ionization equilibrium and comparison to other methods Binder, Blobel, JH, Mukaida (2020)





Common conclusion:

bound state formation and Sommerfeld effect can significantly affect relic abundance prediction



What is the goal?

→ How do bound state formation and Sommerfeld effect impact our understanding of the thought-to-be excluded parameter space?

Becker, Copello, JH, Mohan, Sengupta (2022)



Importance of non-perturbative effects for the exclusion of DM models Julia Harz

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Simplified t-channel dark matter model

Universal framework for t-channel DM models

Arina, Fuks, Mantani (2020)

$$\mathcal{L} \supset \sum_{i} (D_{\mu}X_{i})^{\dagger} (D^{\mu}X_{i}) + g_{\mathrm{DM},ij} X_{i}^{\dagger} \bar{\chi} P_{R} q_{j} + g_{\mathrm{DM},ij}^{*} X_{i} \bar{q}_{j} P_{L} \chi$$

	$SU(3)_c \times SU(2)_L \times U(1)_Y$	
χ	(1, 1, 0)	
	(3, 1, +2/3)	u_R
X	(3, 1, -1/3)	d_R
	(3, 1, -1/6)	q_L

Assumptions:

- dark sector odd under Z₂ symmetry
- χ : Majorana singlet and lightest dark particle \rightarrow dark matter candidate
- X_i : scalar particle with 3 generations with same mass m_x
- g_{DM}: diagonal, democratic coupling



 X_i

 \bar{q}_i

 q_i

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Simplified t-channel dark matter model

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	$SU(3)_c \times SU(2)_L \times U(1)_Y$	
χ	(1, 1, 0)	
	(3, 1, +2/3)	u_R
X	(3, 1, -1/3)	d_R
	(3, 1, -1/6)	q_L

Relevant parameters:

$$g_{
m DM}$$

 $m_{\chi} = m_{
m DM}$
 $\varDelta = m_X - m_{
m DM}$



Importance of non-perturbative effects for the exclusion of DM models

 \bar{q}_i

 q_i

 χ

 X_i

Contributing processes to the relic abundance



$$\frac{dn}{dt} + 3Hn = -\langle \sigma v \rangle (n^2 - n_{\rm eq}^2)$$



Contributing processes to the relic abundance



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Contributing processes to the relic abundance

$$\mathcal{L} \supset \sum_{i} (D_{\mu}X_{i})^{\dagger} (D^{\mu}X_{i}) + g_{\mathrm{DM},ij} X_{i}^{\dagger} \bar{\chi} P_{R} q_{j} + g_{\mathrm{DM},ij}^{*} X_{i} \bar{q}_{j} P_{L} \chi$$



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Towards new standards in the relic abundance prediction



 $\left(\frac{\alpha}{v_{\rm rel}}\right)^n \sim 1$ $\sigma_{\rm eff} v_{\rm rel} = \sigma^{\rm tree} v_{\rm rel} \times S_0$ **Bound state formation**



 $\langle \sigma_{\rm eff} v_{\rm rel} \rangle = \langle \sigma_{\rm ann} v_{\rm rel} \rangle + \langle \sigma_{\rm BSF} v_{\rm rel} \rangle_{\rm eff}$

bound state formation and **subsequent** decay open up a new effective DM **annihilation** channel

> JH, Petraki (2019), JH, Petraki (2018)



 $\sigma_{\rm eff} v_{\rm rel} = \sigma^{\rm NLO} v_{\rm rel}$

abundance

first study of theoretical error on relic abundance

JH, Herrmann, Klasen, Kovarik, et al. (2015+)

Sommerfeld effect

Relevant if

•



• When $lpha \sim v_{
m rel}$, exchange of *n* gluons lead to $\left(rac{lpha}{v_{
m rel}}
ight)^n \sim 1$

momentum exchange

of unbound particles

Bohr momentum

$$\left[-\frac{\nabla^2}{2\mu} + V^{\rm S}_{[\hat{\mathbf{R}}]}(\mathbf{r})\right]\phi_{\mathbf{k}}(\mathbf{r}) = \mathcal{E}_{\mathbf{k}}\phi_{\mathbf{k}}(\mathbf{r}) \qquad \text{with} \qquad V^{S}_{[\hat{\mathbf{R}}]}(r) = -\frac{\alpha_s^S C_{[\hat{\mathbf{R}}]}}{r}$$

 $=rac{\mulpha_g}{\mu v_{
m rel}}$ > 1



$$\sigma_{\rm SE} = S_0 \left(\frac{\alpha_s^S C_{[\hat{\mathbf{R}}]}}{v_{\rm rel}} \right) \, \sigma_0 = \frac{2\pi \alpha_s^S C_{[\hat{\mathbf{R}}]}}{v_{\rm rel}(1 - e^{-2\pi \alpha_s^S C_{[\hat{\mathbf{R}}]}/v_{\rm rel}})} \, \sigma_0$$

 α



Bound state formation and decay





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Bound state formation

$$\left[-\frac{\nabla^2}{2\mu} + V_{\text{scatt}}(\mathbf{r})\right]\phi_{\mathbf{k}}(\mathbf{r}) = \mathcal{E}_{\mathbf{k}}\phi_{\mathbf{k}}(\mathbf{r}) \qquad \qquad \mathcal{E}_{\mathbf{k}} \equiv \frac{\mathbf{k}^2}{2\mu} = \frac{\mu v_{\text{rel}}^2}{2} > 0$$
$$\left[-\frac{\nabla^2}{2\mu} + V_{\text{bound}}(\mathbf{r})\right]\psi_{n\ell m}(\mathbf{r}) = \mathcal{E}_{n\ell}\psi_{n\ell m}(\mathbf{r}) \qquad \qquad \mathcal{E}_{n\ell} \equiv -\frac{\mu^2\alpha^2}{n^22\mu} < 0$$



scattering state radiative bound state transition



Bound state formation



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Bound state formation

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Importance of non-perturbative effects for the exclusion of DM models

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Complete Boltzmann equation

$$\frac{dn}{dt} + 3Hn = -\langle \sigma_{\rm eff} v \rangle (n^2 - n_{\rm eq}^2)$$
$$\langle \sigma_{\rm eff} v_{\rm rel} \rangle = \sum_{ij} \langle S\left(\frac{\alpha}{v_{ij}}\right) \cdot \sigma_{ij} v_{ij} \rangle \frac{n_{\rm eq,i}}{n_{\rm eq}} \frac{n_{\rm eq,j}}{n_{\rm eq}} + \langle \sigma_{\rm BSF} v_{\rm rel} \rangle_{\rm eff} \left(\frac{n_{\rm eq,X}}{n_{\rm eq}}\right)^2$$





Impact of non-perturbative effects on mass plane





Impact on minimal dark matter coupling strength

Identify lower bound on g_{DM} in order not to overproduce DM





Impact on minimal dark matter coupling strength

Identify lower bound on g_{DM} in order not to overproduce DM



$X_i X_j^\dagger \to gg$	$g_s^4 e^{-2x\delta}$	$ \mathcal{M} ^2\sim rac{2}{7}[1]+rac{5}{7}[8]$
$\overline{X_i X_j \to q_i q_j}$	$g_{\rm DM}^4 e^{-2x\delta}$	$ \mathcal{M} ^2 \sim rac{1}{3}[\mathbf{ar{3}}] + rac{2}{3}[\mathbf{ar{6}}]$
$\overline{X_i X_i \to q_i q_i}$	$g_{\rm DM}^4 e^{-2x\delta}$	$ \mathcal{M} ^2 \sim [6]$
$X_i X_j^{\dagger} \to q_i \bar{q}_j$	$(\alpha g_{\rm DM}^2 + \beta g_s^2)^2 e^{-2x\delta}$	$egin{aligned} \mathcal{M} ^2 &\sim f_1\left(g_{\mathrm{DM}},g_s ight)\left[1 ight] \ &+ f_8\left(g_{\mathrm{DM}},g_s ight)\left[8 ight] \end{aligned}$

- Non-perturbative effects result in corrections on minimal g_{DM}
- Depending on parameter space: positive or negative correction

Becker, Copello, JH, Mohan, Sengupta (2022)



Impact on parameter space of t-channel model



→ Non-perturbative effects increase region of parameter space leading to underabundant DM
 → prediction of higher DM masses and larger mass splittings in freeze-out scenario

Becker, Copello, JH, Mohan, Sengupta (2022)



Interplay with direct detection

Spin dependent (SD) direct detection:

- Contribution at tree-level
- most stringent constraints from SD proton scattering
- PICO-60 limits



Spin independent (SI) direct detection:

- only at one-level
- Including RGE running leads to enhancement
- most stringent limits from Xenon1T



\rightarrow upper limit on g_{DM}

Mohan, Sengupta, Tait, Yan and Yuan (2019)



Constraints from LHC



• mono-jet + ETmiss search by ATLAS [arXiv:1711.03301]



• multi-jets + ETmiss search by CMS [arXiv:1704.07781]

\rightarrow constraints set upper limit on g_{DM}

Becker, Copello, JH, Mohan, Sengupta (2022)



Impact of SE and BSF on exclusion limits



- DD and LHC searches set upper bound on g_{DM}
- Requirement of non-overproduction sets lower bound on g_{DM}
- LHC searches constrain mainly larger Δm , SI stronger than SD for $\Delta m < m_{DM}$ Becker, Copello, JH, Mohan, Sengupta (2022)

Impact of SE and BSF on exclusion limits



- \rightarrow Correction on g_{DM} due to SE and BSF lead to altered exclusion limits
- → parameter space that was previously thought to be excluded opens up again!

Becker, Copello, JH, Mohan, Sengupta (2022)



Impact of SE and BSF on exclusion limits



- based on tree-level calculations only, viable parameter space thought to be $(m_{DM}, \Delta m) < (1 \text{ TeV}, 30 \text{ GeV})$
- including SE extended to $(m_{DM}, \Delta m) < (1.4 \text{ TeV}, 40 \text{ GeV})$
- including BSF extended to $(m_{DM}, \Delta m) < (2.4 \text{ TeV}, 50 \text{ GeV})$

→ Including SE alone not a good approximation!

Becker, Copello, JH, Mohan, Sengupta (2022)



How to constrain the underabundant region?

Alternative mechanism needed, as dark sector out-of-equilibrium:

ightarrow Identify $g_{
m DM} < ilde{g}_{
m DM}$ below which dark sector is out-of-equilibrium

$$\Gamma_{X \to \chi q} \frac{Y_X^{\rm eq}}{Y_\chi^{\rm eq}} < H$$

 $\rightarrow\,$ possibility to generate dark matter abundance via freeze-in mechanism

How constrained is this parameter space already by long-lived particle searches?

Becker, Copello, JH, Mohan, Sengupta (2022)



Interplay with long-lived particle searches



Becker, Copello, JH, Mohan, Sengupta (2022)



Interplay with long-lived particle searches

Could e.g. a freeze-in mechanism account for the missing dark matter?



→ LLP searches efficiently constrain parameter space for alternative DM production, e.g. via freeze-in



Beyond WIMP freeze-out



See e.g.: Garny, Heisig (2021), Bollig, Vogl (2021), Decant, Heisig, Hooper, Lopez-Honorez (2021, 2022)

→ all include now also Sommerfeld effect and bound state formation!!!



Potential of bound state formation at colliders

$$\sigma(pp \to \mathcal{B}(XX^{\dagger})) = \frac{\pi^2}{8m_{\mathcal{B}}^3} \mathcal{P}_{gg} \left(\frac{m_{\mathcal{B}}}{13 \text{ TeV}}\right) \Gamma(\mathcal{B}(XX^{\dagger}) \to gg)$$

- Resonant production of bound state and subsequent decay (e.g. into photons)
- Dedicated searches, see e.g. ATLAS coll. Phys. Lett. B 775 (2017) 105
- Efficient for large range of g_{DM}, as long as Γ_X < E_B (g_{DM} < g_s, when bound states are efficiently produced)





Potential of bound state formation at colliders



limits relatively weak (300 GeV)
 BUT: closes gap between prompt and LLP searches

Becker, Copello, JH, Mohan, Sengupta (2022)



Future prospects



- Remember: HSPC no strict exclusion limit (BSF@LHC is!)
- Highly testable: parameter space can be almost entirely probed (but three regions remain unconstrained!)
- BSF effects enlarge parameter range that still needs to be tested

Becker, Copello, JH, Mohan, Sengupta (2022)



Future prospects for bound states at colliders



BSF@LHC has potential to unambiguously close parameter space for small DM masses and mass splittings

Becker, Copello, JH, Mohan, Sengupta (2022)



Going beyond finite temperature...

- Development of finite-T treatment of bound state formation while still in ionization equilibrium
 Kim, Laine (2017), Biondini, Laine (2018), Biondini (2018), Covi. Binder, Mukaida (2018)
- **Phenomenology of finite-T** treatment of bound state formation while still in **ionization equilibrium** Biondini, Voal (2018), Biondini, Voal (2019)
- Presenting finite-T treatment beyond ionization equilibrium and comparison to other methods
 Binder, Blobel, JH, Mukaida (2020)
- Non-relativistic effective field theory at finite-T treatment

Biondini, Brambilla, Qerimi, Vairo (2023)



→ very active research field both from phenomenological aspect as well as methodological one



Importance of non-perturbative effects for the exclusion of DM models

0.20 0.15 0.15 0.00 $\Omega_{DM}h^2=0.119$ 0.00 $\Omega_{DM}h^2=0.119$ +SE +LO BSF +NLO BSF 0.00 5000 $10\,000$ $15\,000$ $m_{\chi}[GeV]$

Going beyond coannihilation...

- Non-perturbative effects are not limited to coannihilation scenarios (t-channel model just an example to rise awareness)
- Corrections expected for massless mediators when ν ~ α (Coulomb potential)
- Corrections expected for massive mediators when v ~ α and $\mathbf{m}_{med} \ll \mathbf{m}_{DM}$ (Yukawa potential)







Conclusions

- Sommerfeld effect and bound state formation can
 - $\rightarrow\,$ alter interpretation of experimental exclusion limits
 - $\rightarrow\,$ change expected model parameters in case of a discovery
- Parameter space thought to be excluded remains still viable
- Application of a simple flat correction factor not sufficient
- Bound state searches at LHC can close gap for low DM masses
- Not limited to t-channel DM model example or coannihilation

→ For conclusive statements non-pertubative effects are crucial to be taken into account!











The Dark Matter Landscape: From Feeble to Strong Interactions

Organizers: Mathias Becker, JH, Laura Lopez Honorez, Tracy Slatyer, Juri Smirnov

August 26th – September 13th 2024



Thank you for your attention!







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