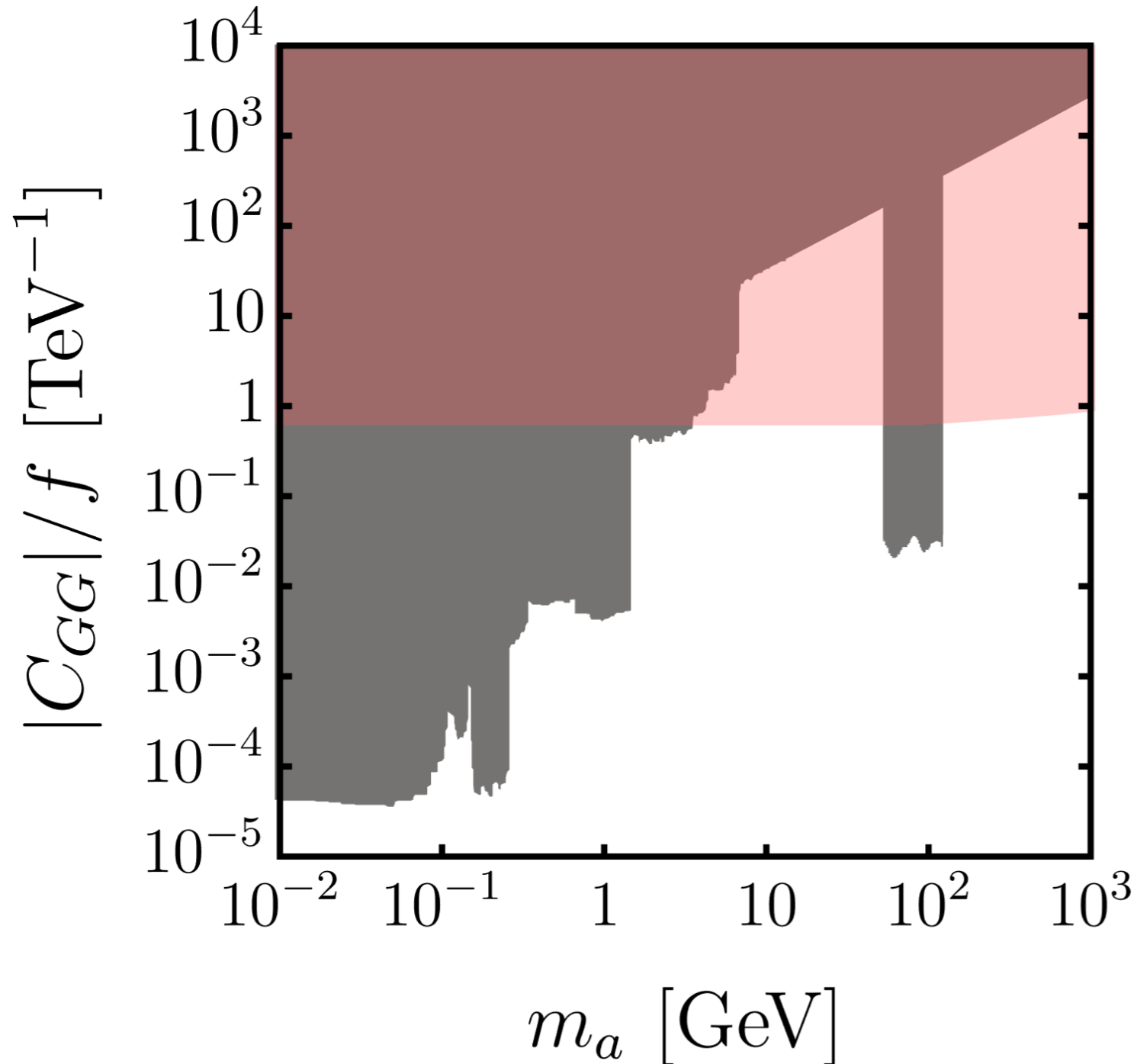


# Model-Independent Bounds on Axion-Like Particles from the Standard Model Effective Field Theory



**Anne Galda**

based on

**arXiv: 2105.01078**

and

**arXiv: 2307.10372**

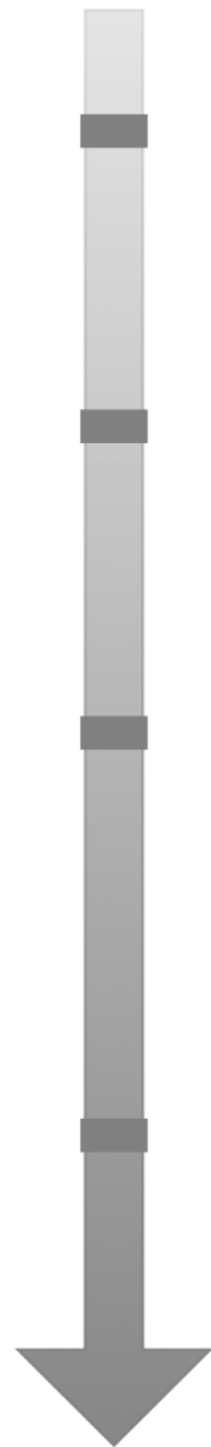
In collaboration with

S. Renner and M. Neubert

and

A. Biekötter, J. Fuentes-Martín

and M. Neubert



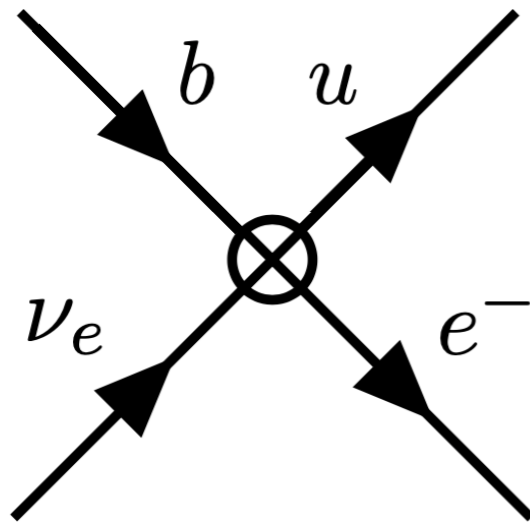
**Introduction to Effective Field Theories**

**Renormalization-Group Evolution**

**Axion-Like Particles and  
ALP-SMEFT Interference**

**Model-Independent Bounds on ALPs**

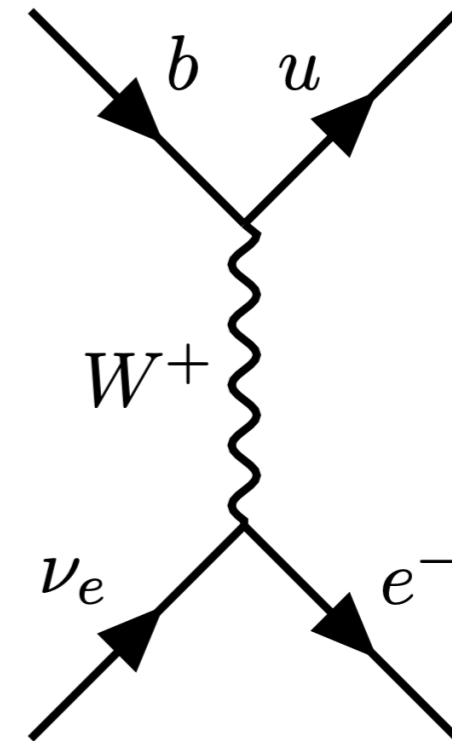
# Effective Field Theories



local  
4-fermi interaction

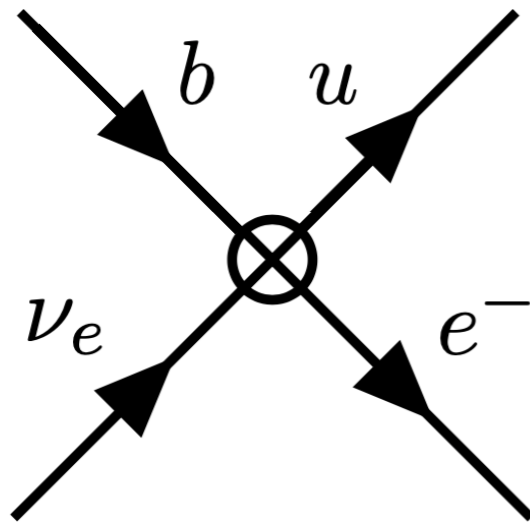


What connects  
these interactions?



full  
Standard-Model interaction

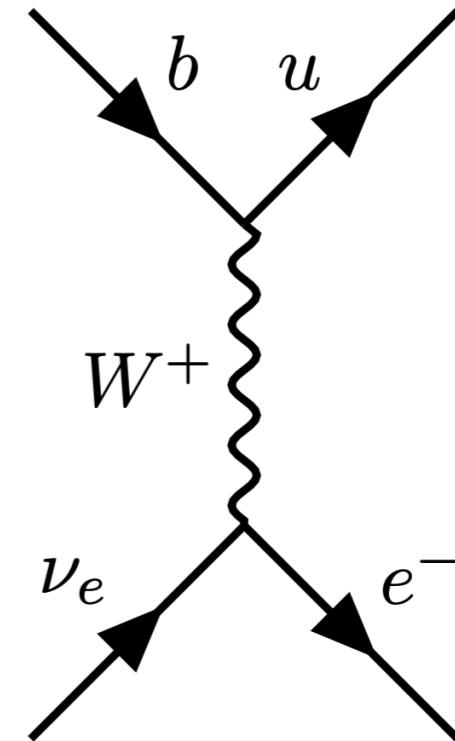
# Effective Field Theories



local  
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**Effective Field Theories!**

# Effective Field Theories

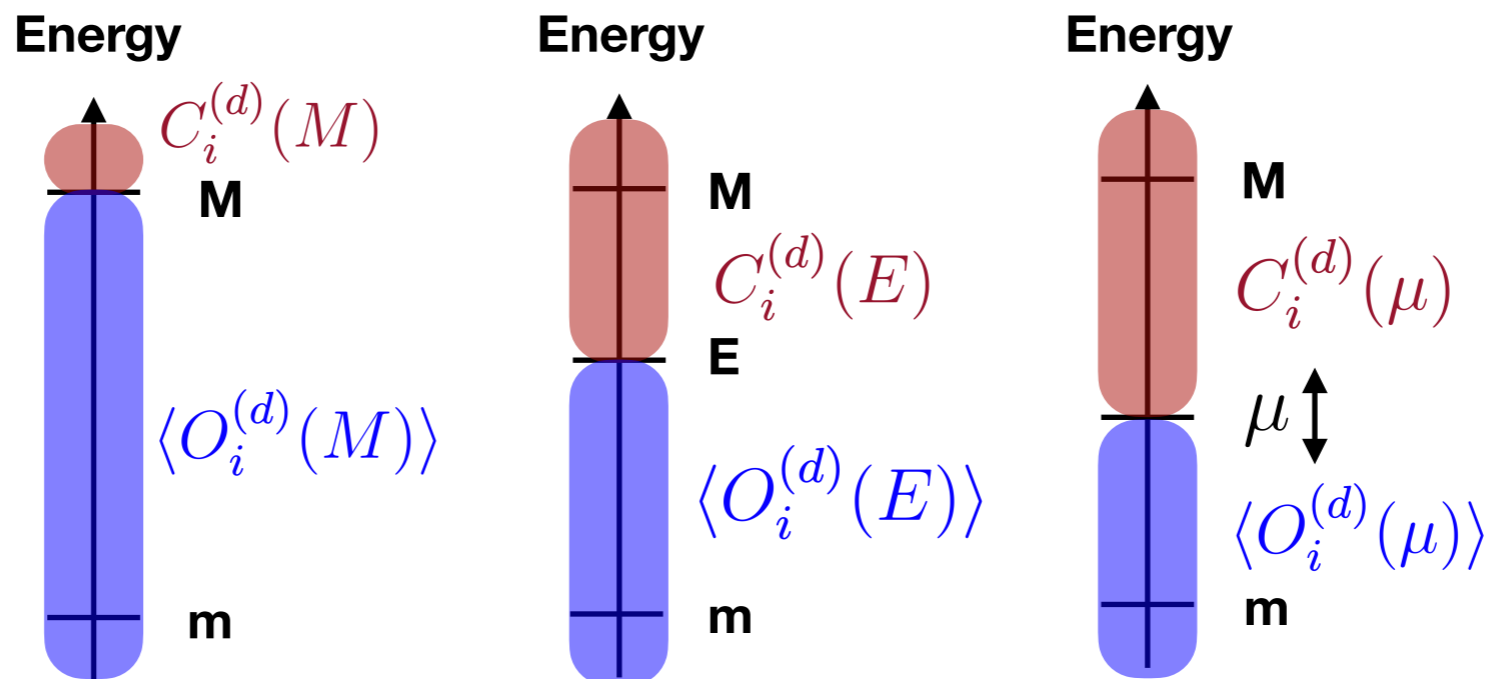
**Basic idea:** At a given scale, determine the relevant degrees of freedom!

↳ **Operator-Product Expansion**

$$\mathcal{L}_{\text{eff}} = \sum_d \frac{1}{\Lambda^{d-4}} \sum_{i=1}^{n_d} C_i^{(d)}(\mu) O_i^{(d)}(\mu)$$

**Wilson coefficients:** Parametrize the (heavy) UV-physics

**Operators:** Built out of the relevant degrees of freedom

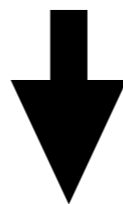




Factorisation scale  $\mu$  is arbitrary

↳ Unobservable quantity

$$\frac{d}{d \ln \mu} \mathcal{L}_{\text{eff}} = \sum_d \frac{1}{\Lambda^{d-4}} \sum_{i=1}^{n_d} C_i^{(d)}(\mu) O_i^{(d)}(\mu) = 0$$



$$\left( \frac{d C_i^{(d)}(\mu)}{d \ln \mu} \right) O_i^{(d)}(\mu) + C_i^{(d)}(\mu) \left( \frac{d O_i^{(d)}(\mu)}{d \ln \mu} \right) = 0$$

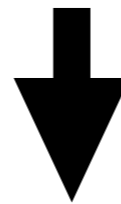
# Effective Field Theories



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↳ **define:**

$$\frac{d O_i^{(d)}(\mu)}{d \ln \mu} \equiv -\gamma_{ij}(\mu) O_j^{(d)}(\mu)$$

**“anomalous dimension matrix”**

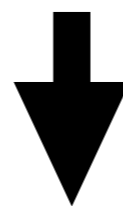
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**“anomalous dimension matrix”**

**Renormalization-Group Evolution Equation**

$$\frac{d C_i^{(d)}(\mu)}{d \ln \mu} = \gamma_{ji}(\mu) C_j^{(d)}(\mu)$$



# RG Evolution Equation

---

$$\frac{d C_i^{(d)}(\mu)}{d \ln \mu} = \gamma_{ji}(\mu) C_j^{(d)}(\mu)$$

↪ Central equation of this talk!

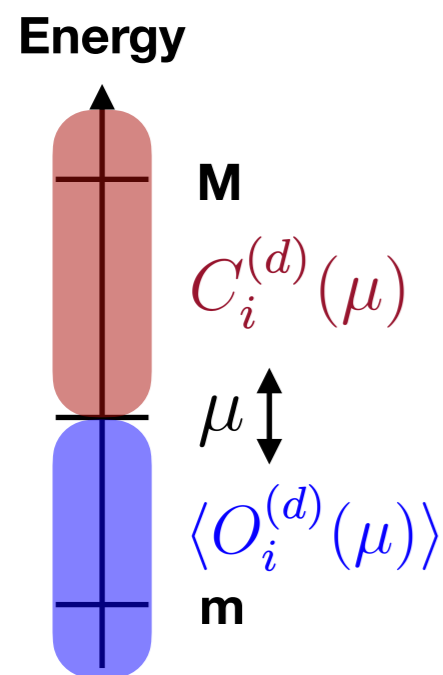
- Describes the scale  $\mu$  dependence of the Wilson coefficients (couplings).
- Anomalous dimension matrix  $\gamma_{ji}(\mu)$  couples the equations of different Wilson coefficients.  
↪ (Very) large set of coupled differential equations!
- Even if a Wilson coefficient is zero at a high scale, it can still be generated via a “running effect”!

# The Standard Model Effective Field Theory (SMEFT)

Assume there are **new, unknown particles coupling to the known Standard Model particles.**

↪ What would be the consequences?

- If the new particle is heavy, it is not a valid degree of freedom at “low” energies!
- This means it will not appear as an external state in scattering amplitudes.
- **But:** it can still modify physical processes by modifying Wilson coefficients (“couplings”)



New, unknown particles can generate operators made purely out of SM particles that are zero in the SM!

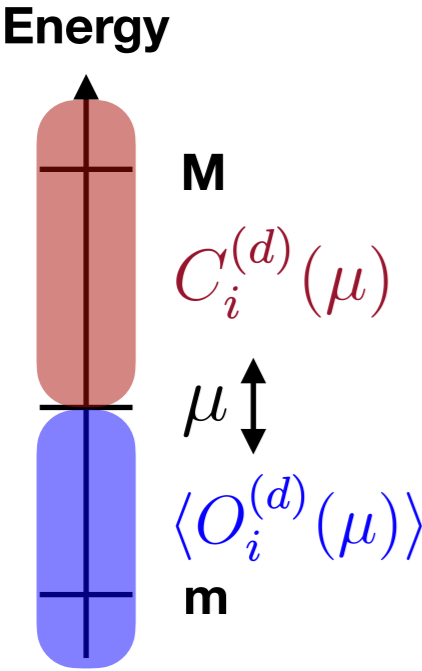
↪ **Generation of higher dimensional operators!**

# The Standard Model Effective Field Theory (SMEFT)

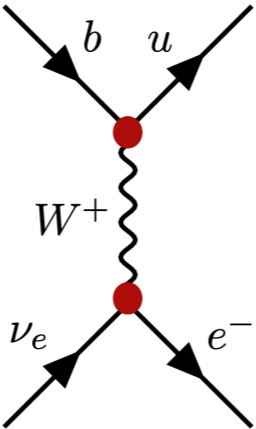
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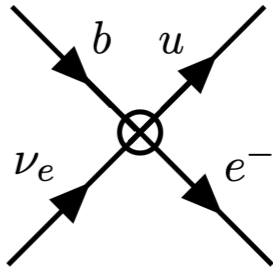
SM analogy:



Two dim-4 operators

Low energies:

One dim-6 operator



# The Standard Model Effective Field Theory (SMEFT)

## Minimal basis: “Warsaw” basis

[Grzadkowski, Iskrzynski, Misiak, Rosiek (2010)]

$X^3$		$\varphi^6$ and $\varphi^4 D^2$		$\psi^2 \varphi^3$			
$Q_G$	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_\varphi$	$(\varphi^\dagger \varphi)^3$	$Q_{e\varphi}$	$(\varphi^\dagger \varphi)(\bar{l}_p e_r \varphi)$		
$Q_{\tilde{G}}$	$f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_{\varphi\Box}$	$(\varphi^\dagger \varphi)\Box(\varphi^\dagger \varphi)$	$Q_{u\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p u_r \tilde{\varphi})$		
$Q_W$	$\varepsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$Q_{\varphi D}$					
$Q_{\tilde{W}}$	$\varepsilon^{IJK} \tilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$						
$X^2 \varphi^2$		$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$	
$Q_{\varphi G}$	$\varphi^\dagger \varphi G_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eW}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	$Q_{ee}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$	$Q_{le}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{\varphi \tilde{G}}$	$\varphi^\dagger \varphi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eB}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{uu}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{lu}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
$Q_{\varphi W}$	$\varphi^\dagger \varphi W_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uG}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{dd}$	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{ld}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
$Q_{\varphi \tilde{W}}$	$\varphi^\dagger \varphi \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uW}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{eu}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{qe}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{\varphi B}$	$\varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu}$	$Q_{uB}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{ed}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
$Q_{\varphi \tilde{B}}$	$\varphi^\dagger \varphi \tilde{B}_{\mu\nu} B^{\mu\nu}$	$Q_{dG}$		$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$
$Q_{\varphi WB}$	$\varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$	$Q_{dW}$		$Q_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$
$Q_{\varphi \tilde{W}B}$	$\varphi^\dagger \tau^I \varphi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	$Q_{dB}$				$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$
			$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$	$B$ -violating			
			$Q_{ledq}$	$(\bar{l}_p^j e_r)(\bar{d}_s^j q_t^j)$	$Q_{duq}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(d_p^\alpha)^T C u_r^\beta] [(q_s^{\gamma j})^T C l_t^k]$	
			$Q_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$	$Q_{qqu}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(u_s^\gamma)^T C e_t]$	
			$Q_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \varepsilon_{jk} (\bar{q}_s^k T^A d_t)$	$Q_{qqq}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jn} \varepsilon_{km} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^{\gamma m})^T C l_t^n]$	
			$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	$Q_{duu}$	$\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_s^\gamma)^T C e_t]$	
			$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$			

Parametrization of new heavy physics in terms of SM fields

at dimension-6: **59 operators**  
[omitting flavor indices]

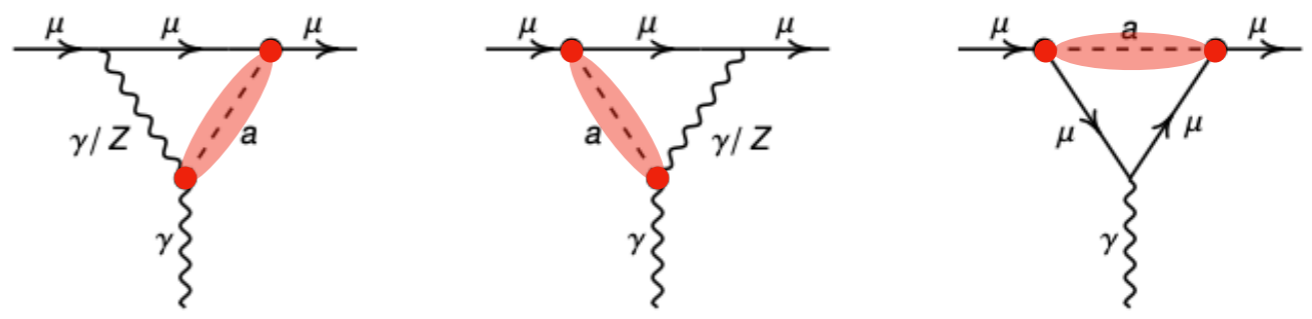
# Axions and Axion-Like Particles (ALPs)

➔ **Peccei-Quinn solution to the strong CP-problem** [Peccei, Quinn (1977); Weinberg (1978); Wilczek (1978)]

$$\mathcal{L} = \frac{\theta\alpha_s}{8\pi} G_{\mu\nu}^a \tilde{G}^{a,\mu\nu} + \frac{a}{f_a} \frac{\alpha_s}{8\pi} G_{\mu\nu}^a \tilde{G}^{a,\mu\nu} + \dots$$

➔ **Potential Dark Matter candidates** [Preskill, Wise, Wilczek (1983)]

➔ **Give a contribution to  $a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = 4.2\sigma$**  [B. Abi et al. (2021)]



**Most general Lagrangian for a classically shift symmetric, gauge singlet, pseudoscalar ALP:**

$$\mathcal{L}_{\text{eff}}^{D \leq 5} = \frac{1}{2} (\partial_\mu a)(\partial^\mu a) - \frac{m_{a,0}^2}{2} a^2 + \frac{\partial^\mu a}{f} \sum_F \bar{\psi}_F \mathbf{c}_F \gamma_\mu \psi_F$$

$$+ c_{GG} \frac{\alpha_s}{4\pi} \frac{a}{f} G_{\mu\nu}^a \tilde{G}^{\mu\nu,a} + c_{WW} \frac{\alpha_2}{4\pi} \frac{a}{f} W_{\mu\nu}^A \tilde{W}^{\mu\nu,A} + c_{BB} \frac{\alpha_1}{4\pi} \frac{a}{f} B_{\mu\nu} \tilde{B}^{\mu\nu}$$

[H. Georgi, D. B. Kaplan, L. Randall (1986)]

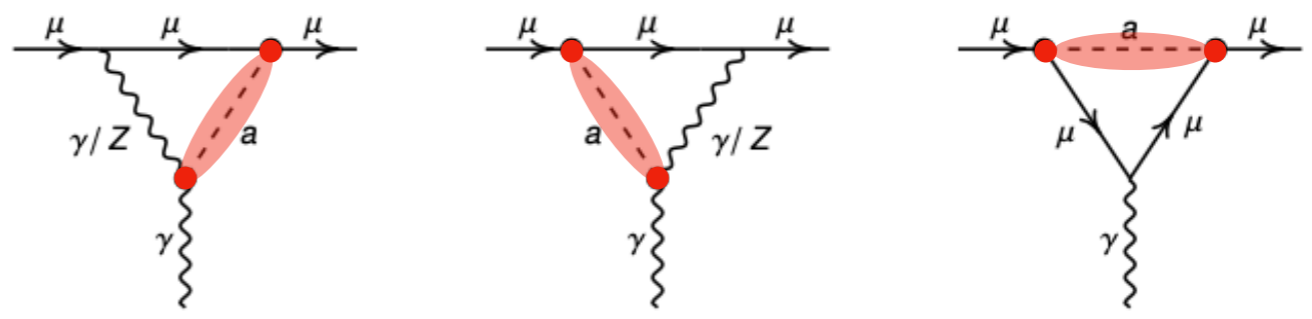
# Axions and Axion-Like Particles (ALPs)

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Most general Lagrangian for a classically shift symmetric, gauge singlet, pseudoscalar ALP:

field redefinition

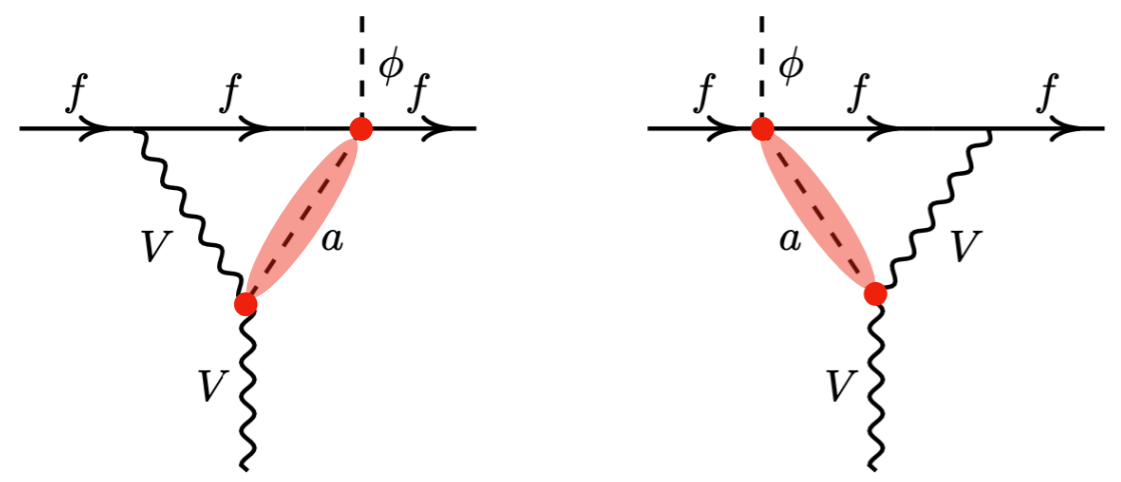
$$\mathcal{L}_{\text{SM+ALP}}^{D=5'} = C_{GG} \frac{a}{f} G_{\mu\nu}^a \tilde{G}^{\mu\nu,a} + C_{WW} \frac{a}{f} W_{\mu\nu}^I \tilde{W}^{\mu\nu,I} + C_{BB} \frac{a}{f} B_{\mu\nu} \tilde{B}^{\mu\nu} - \frac{a}{f} \left( \bar{Q} \tilde{H} \tilde{Y}_u u_R + \bar{Q} H \tilde{Y}_d d_R + \bar{L} H \tilde{Y}_e e_R + \text{h.c.} \right)$$

$$\psi_F \rightarrow \psi_F + i \frac{a}{f} \mathbf{c}_F \psi_F$$

flavor universal ALP:  $\tilde{Y}_u \equiv i \mathbf{Y}_u C_u$ ,  $\tilde{Y}_d \equiv i \mathbf{Y}_d C_d$ ,  $\tilde{Y}_e \equiv i \mathbf{Y}_e C_e$

# ALP-SMEFT Interference

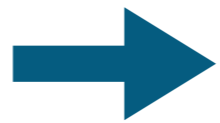
Virtual ALP-exchange with only SM external states in one-loop diagrams, i.e.:



$\sim 1/\epsilon$  where  $\epsilon \rightarrow 0$

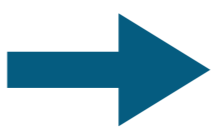
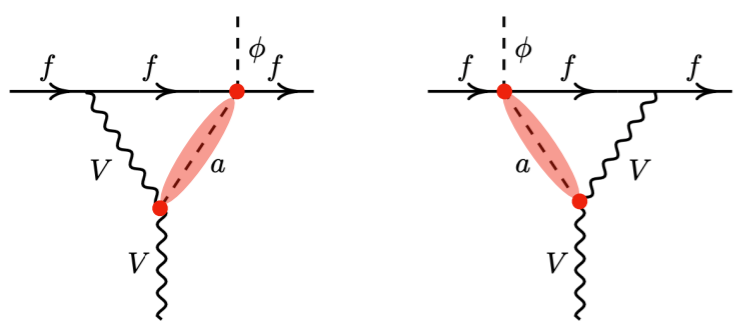
**UV-divergent amplitudes!**

Physics needs to be finite!



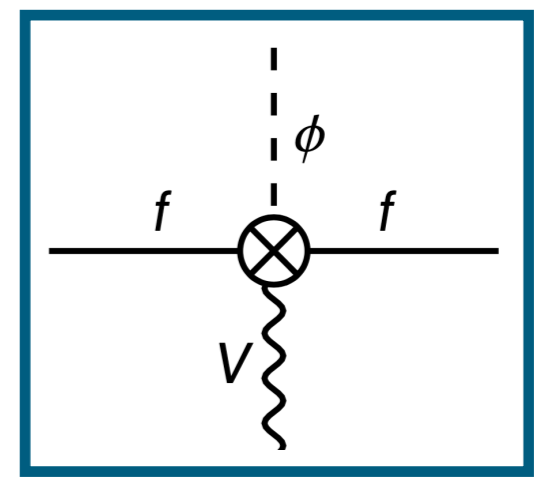
Divergence needs to be absorbed!

Shrink loop to a point:



$C_0^{\text{dipole}}$

x

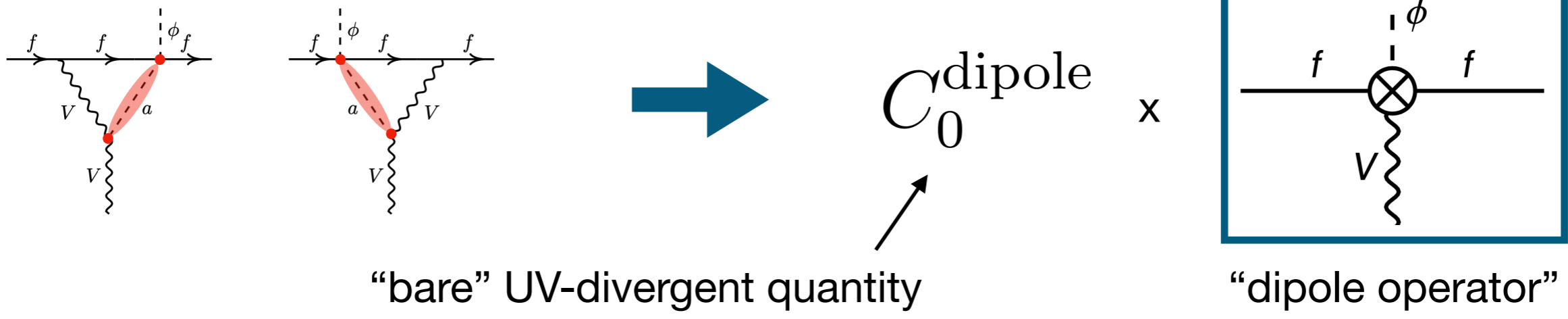


“bare” UV-divergent quantity

“dipole operator”

# ALP-SMEFT Interference

## Shrink loop to a point:



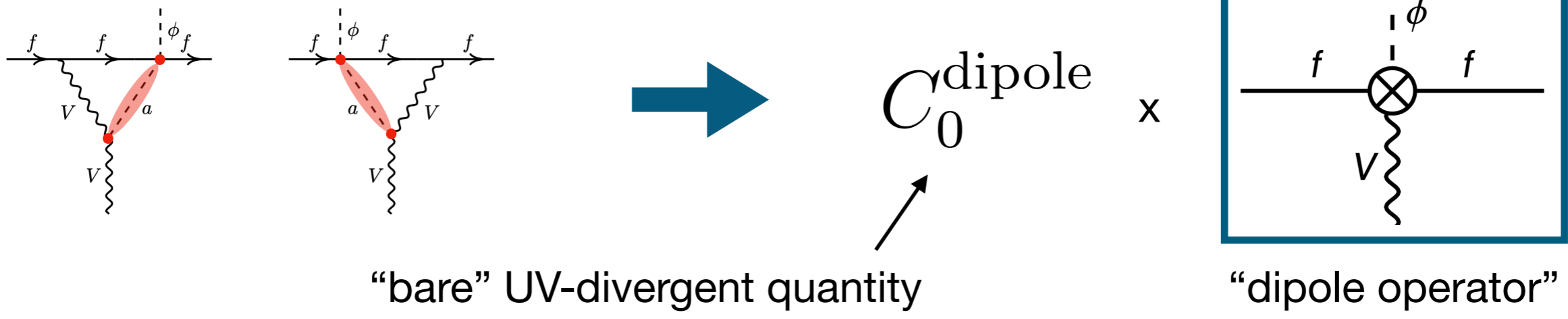
## In detail: (still schematically)

$$\mathcal{A}^{\text{dipole}} = \frac{1}{(4\pi f)^2} f(C_\alpha^{\text{ALP}}, C_\beta^{\text{ALP}}) \left( \frac{1}{\epsilon} + \ln \left( \frac{\mu^2}{M^2} \right) + \dots \right) \langle \mathcal{O}^{\text{dipole}} \rangle$$



# ALP-SMEFT Interference

## Shrink loop to a point:



## In detail: (still schematically)

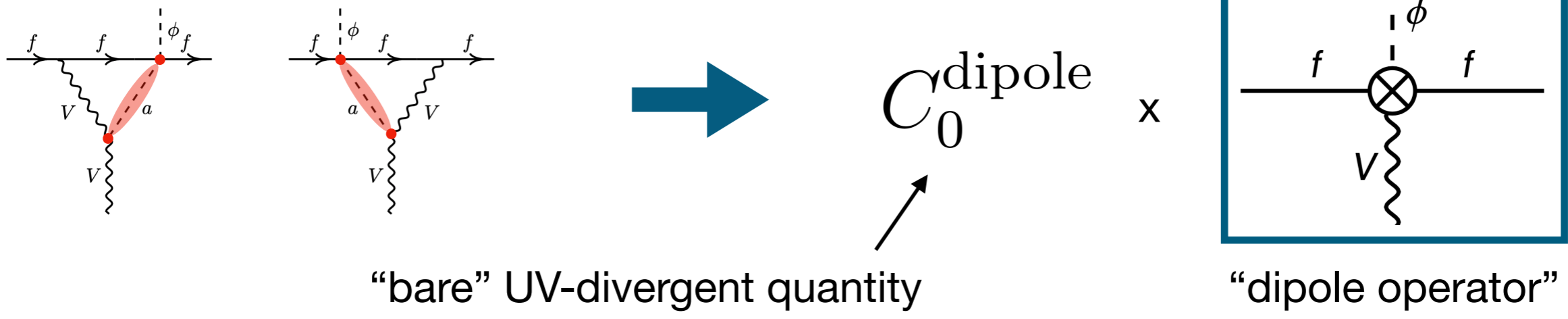
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Absorption of the pole in the bare dipole operator Wilson coefficient:

$$C_0^{\text{dipole}} = - \frac{1}{(4\pi f)^2} f(C_\alpha^{\text{ALP}}, C_\beta^{\text{ALP}}) \left( \frac{1}{\epsilon} + \ln\left(\frac{\mu^2}{M^2}\right) + \dots \right)$$

# ALP-SMEFT Interference

## Shrink loop to a point:



## In detail: (still schematically)

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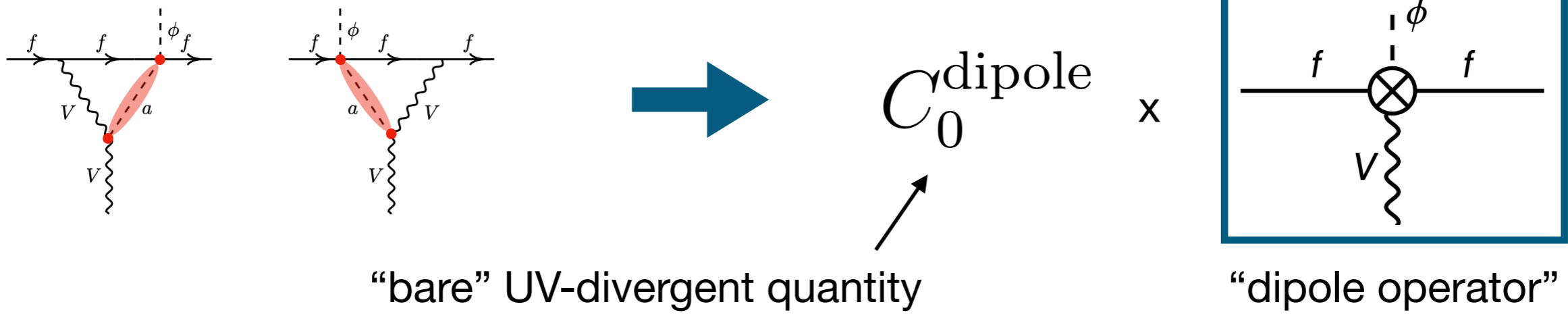
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$$C_{\text{ren}}^{\text{dipole}} = - \frac{1}{(4\pi f)^2} f(C_\alpha^{\text{ALP}}, C_\beta^{\text{ALP}}) \left( \cancel{\frac{1}{\epsilon}} + \ln\left(\frac{\mu^2}{M^2}\right) + \dots \right)$$

# ALP-SMEFT Interference

## Shrink loop to a point:



## In detail: (still schematically)

$$C_{\text{ren}}^{\text{dipole}} = - \frac{1}{(4\pi f)^2} f(C_{\alpha}^{\text{ALP}}, C_{\beta}^{\text{ALP}}) \left( \cancel{\frac{1}{\epsilon}} + \ln \left( \frac{\mu^2}{M^2} \right) + \dots \right)$$

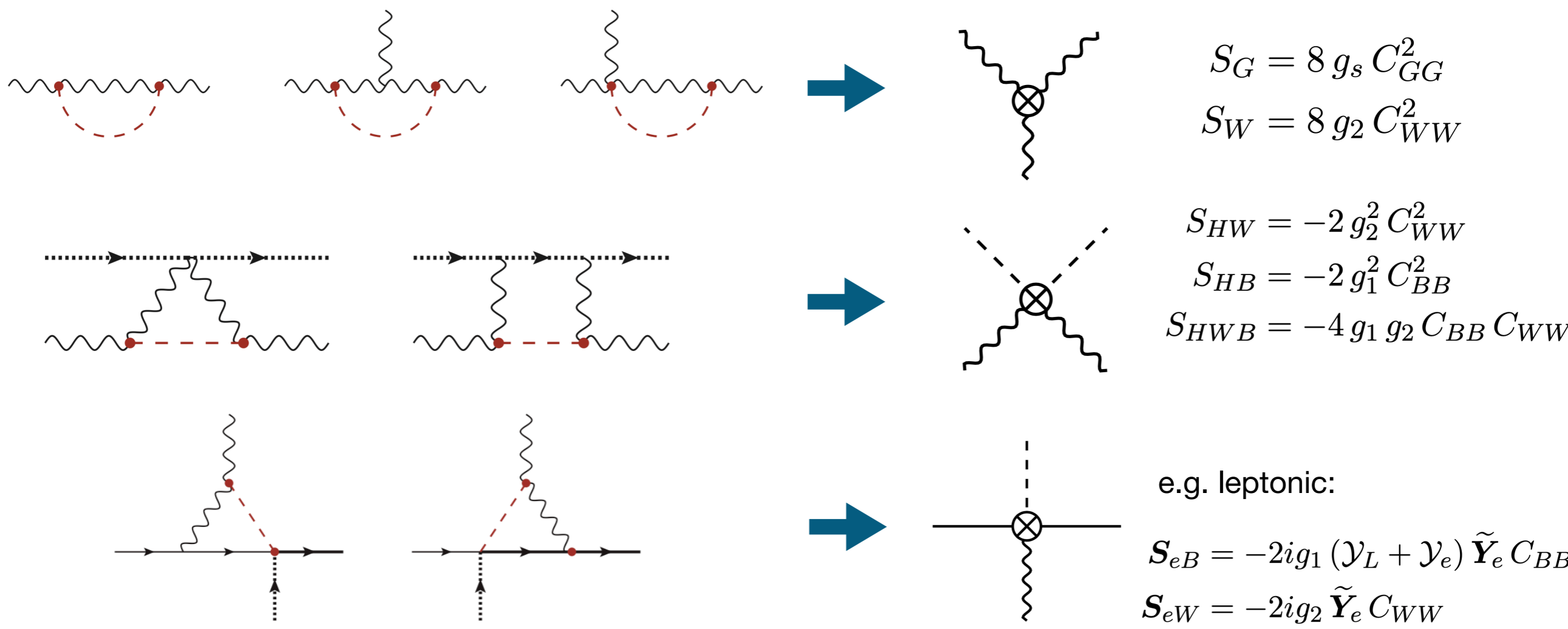
↓ Derivative wrt. scale

$$\frac{d}{d \ln \mu} C_{\text{ren}}^{\text{dipole}} = - \frac{2}{(4\pi f)^2} f(C_{\alpha}^{\text{ALP}}, C_{\beta}^{\text{ALP}}) \equiv \frac{S^{\text{dipole}}}{(4\pi f)^2}$$

# ALP-SMEFT Interference

A consistent effective theory **necessarily** includes the **dimension-6 SMEFT Lagrangian!**

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \mathcal{L}_{\text{SM}+\text{ALP}} + \mathcal{L}_{\text{SMEFT}}$$



...etc!

[AG, Neubert, Renner (2021)]

# ALP-SMEFT Interference

---

Main message of this talk:

Dimension-6 SMEFT Wilson coefficients are generated via modification of the Renormalization Group evolution even if the ALP is very light!

$$\frac{d}{d \ln \mu} C_i^{\text{SMEFT}} - \gamma_{ji}^{\text{SMEFT}} C_j^{\text{SMEFT}} = \frac{S_i}{(4\pi f)^2} \quad (\text{for } \mu < 4\pi f)$$

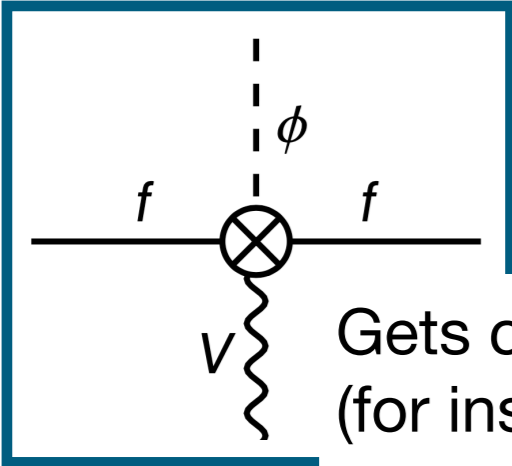
[AG, Neubert, Renner (2021)]

# ALP constraints from SMEFT fits

$$\frac{d}{d \ln \mu} C_i^{\text{SMEFT}} - \gamma_{ji}^{\text{SMEFT}} C_j^{\text{SMEFT}} = \frac{S_i}{(4\pi f)^2} \quad (\text{for } \mu < 4\pi f)$$

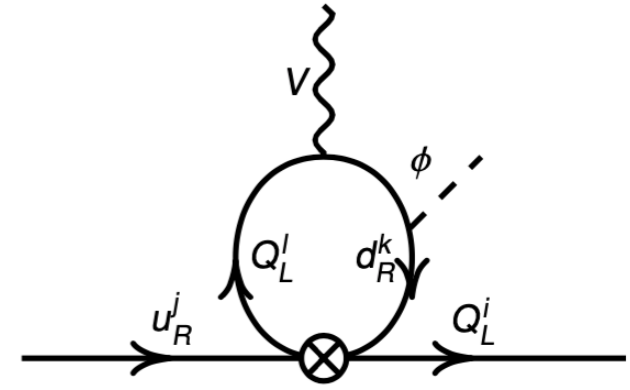


- Large set of coupled differential equations!

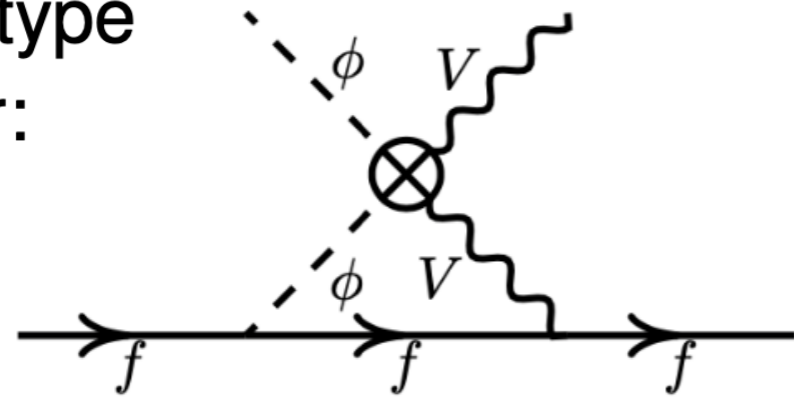


Gets contributions from (for instance)

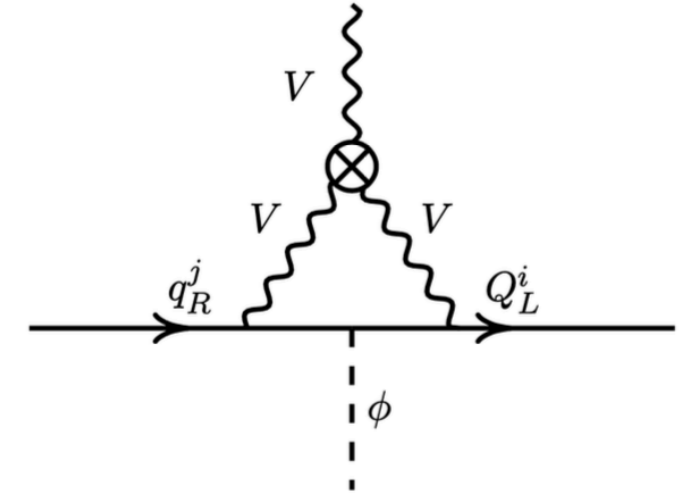
four-fermion operator:



$Q_{HV(V')}$ -type operator:



Weinberg operator:



# ALP constraints from SMEFT fits

$$\frac{d}{d \ln \mu} C_i^{\text{SMEFT}} - \gamma_{ji}^{\text{SMEFT}} C_j^{\text{SMEFT}} = \frac{S_i}{(4\pi f)^2} \quad (\text{for } \mu < 4\pi f)$$

- Large set of coupled differential equations!
- Solved numerically using a modified version of `DsixTools` [Celis, Fuentes-Martín, Vicente, Virto (2017), Fuentes-Martín, Ruiz-Femenia, Vicente, Virto (2020)]

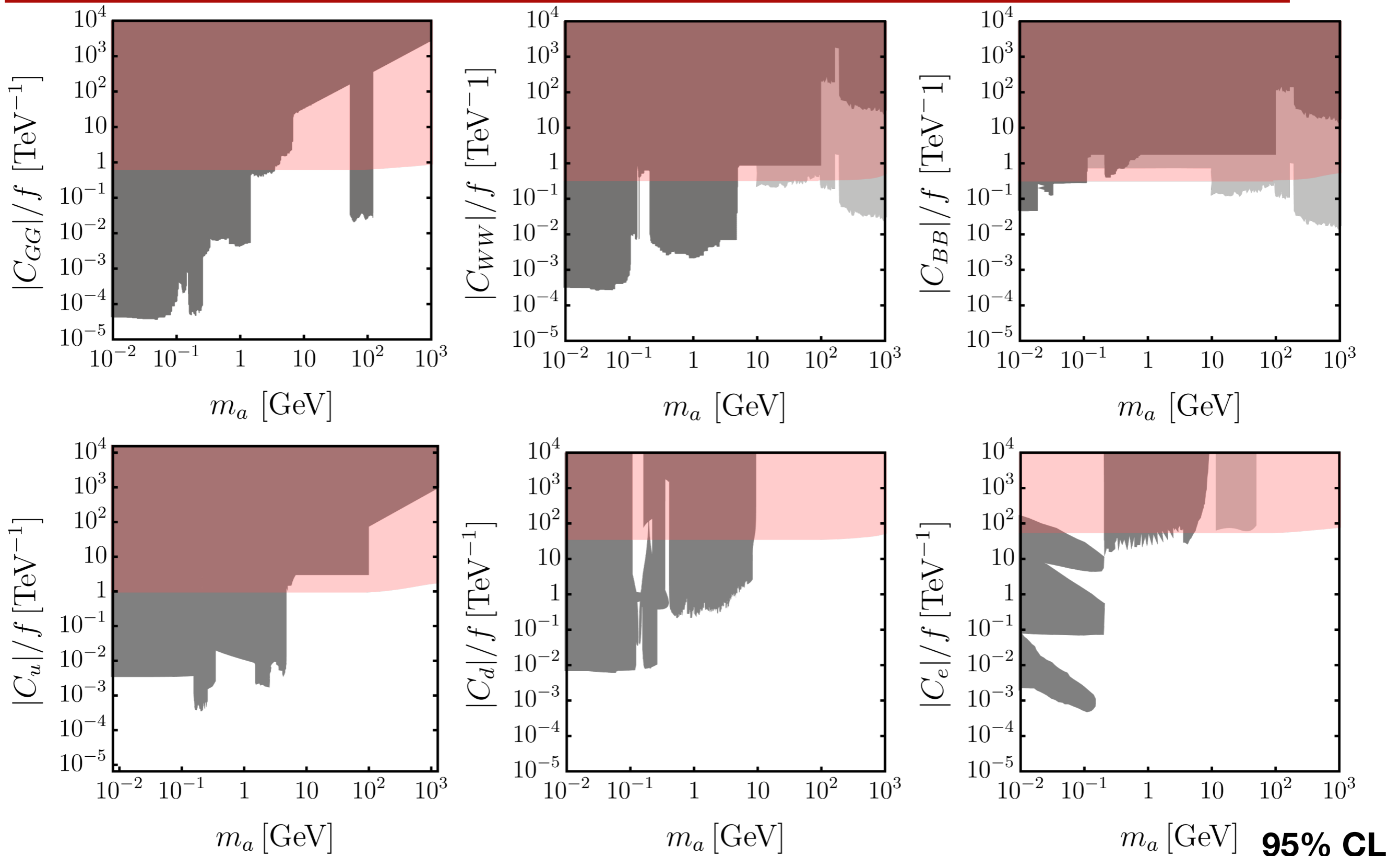
**Result:** SMEFT Wilson coefficients at a low scale  $\mu$  in terms of ALP-couplings at the scale  $\Lambda$ .

We use SMEFT constraints from low-energy, Higgs and top data in a  $\chi^2$  fit to constrain the ALP-coefficients.

$$\chi^2(C_i) = \left[ \vec{d} - \vec{p}(C_i) \right]^T \mathbf{V}^{-1} \left[ \vec{d} - \vec{p}(C_i) \right]$$

from e.g. [Ellis, Madigan, Mimasu, Sanz, You (2021)]

# Model-Independent Bounds on Axion-Like Particles

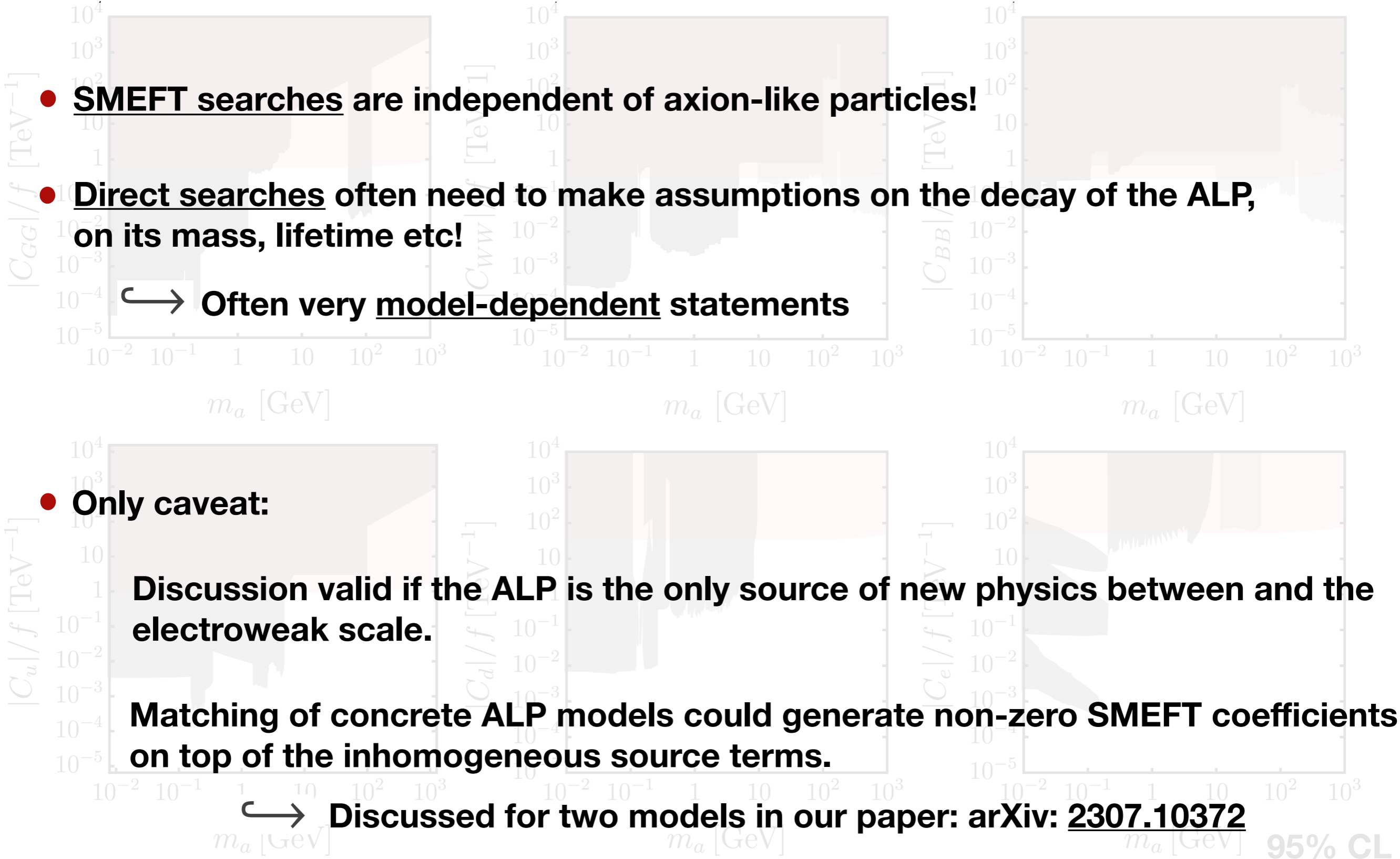


red: our new model-independent bounds

gray: direct, model-dependent bounds



# Model-Independent Bounds on the Axion-Like Particles



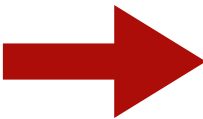
red: our new model-independent bounds

gray: direct, model-dependent bounds

# Summary

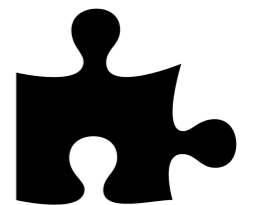
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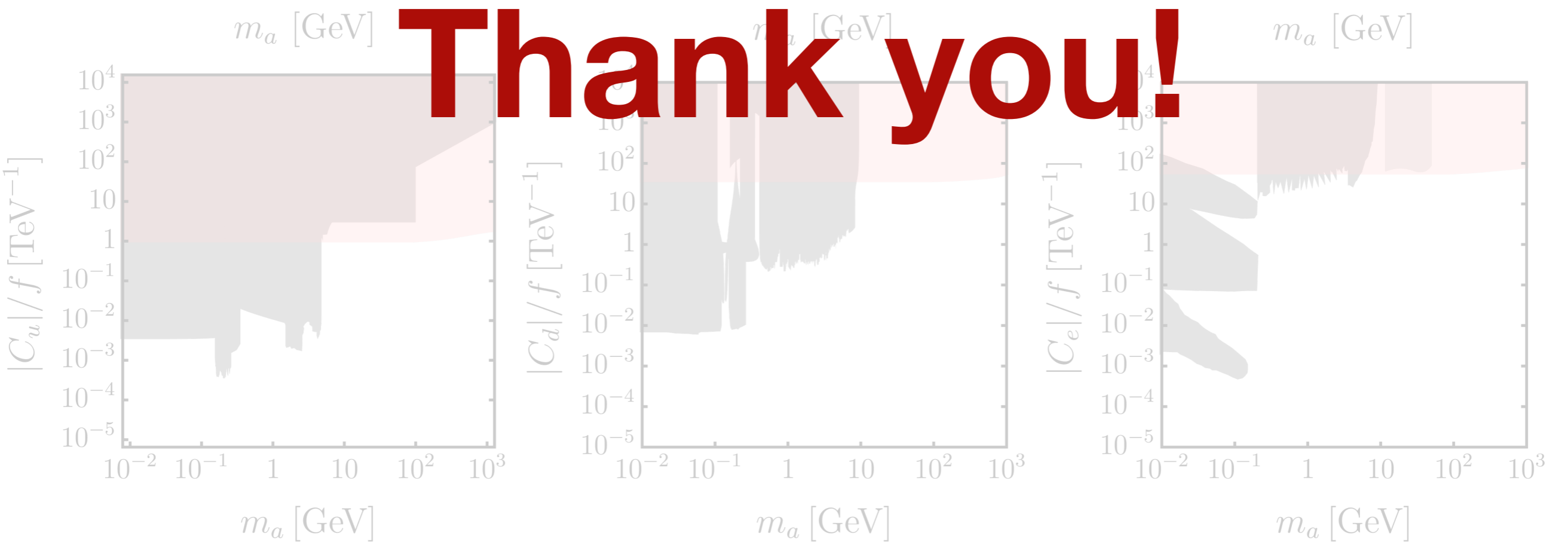
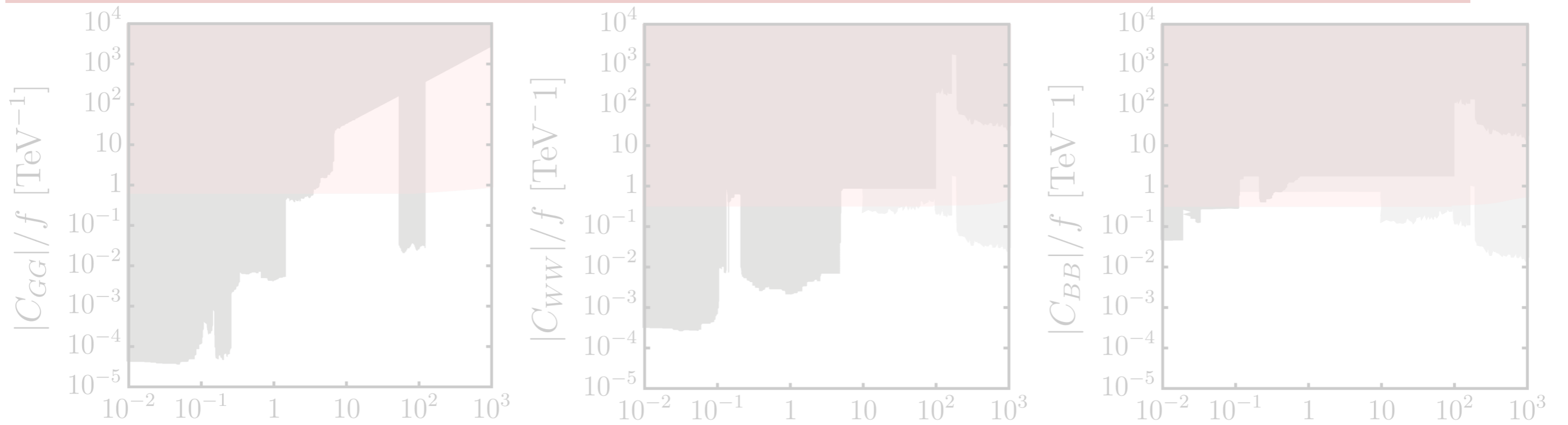
In this talk we have seen..

- ✓ how to derive the RG evolution equations for Wilson coefficients.
  - ✓ that ALPs couple to the SM via dimension-5 interactions (or higher).
  - ✓ that divergences from one-loop virtual ALP exchange with external SM particles are absorbed in SMEFT Wilson coefficients and the ALP thus generates nearly the whole dim-6 SMEFT basis at one-loop order .
  - ✓ how RG running and ALP-independent SMEFT bounds can be used to obtain model-independent bounds on ALP coefficients.
-  Indirect bounds from global fits are a model-independent way to constrain ALPs and the results are competitive to or even exceed current constraints!



**ALPs generate nearly all dimension-6  
SMEFT operators at one-loop order  
allowing for a derivation of  
model-independent bounds!**





**Thank you!**