### Machine Learning in Particle Theory - MITP Summer School 2023

### **Eilam Gross**

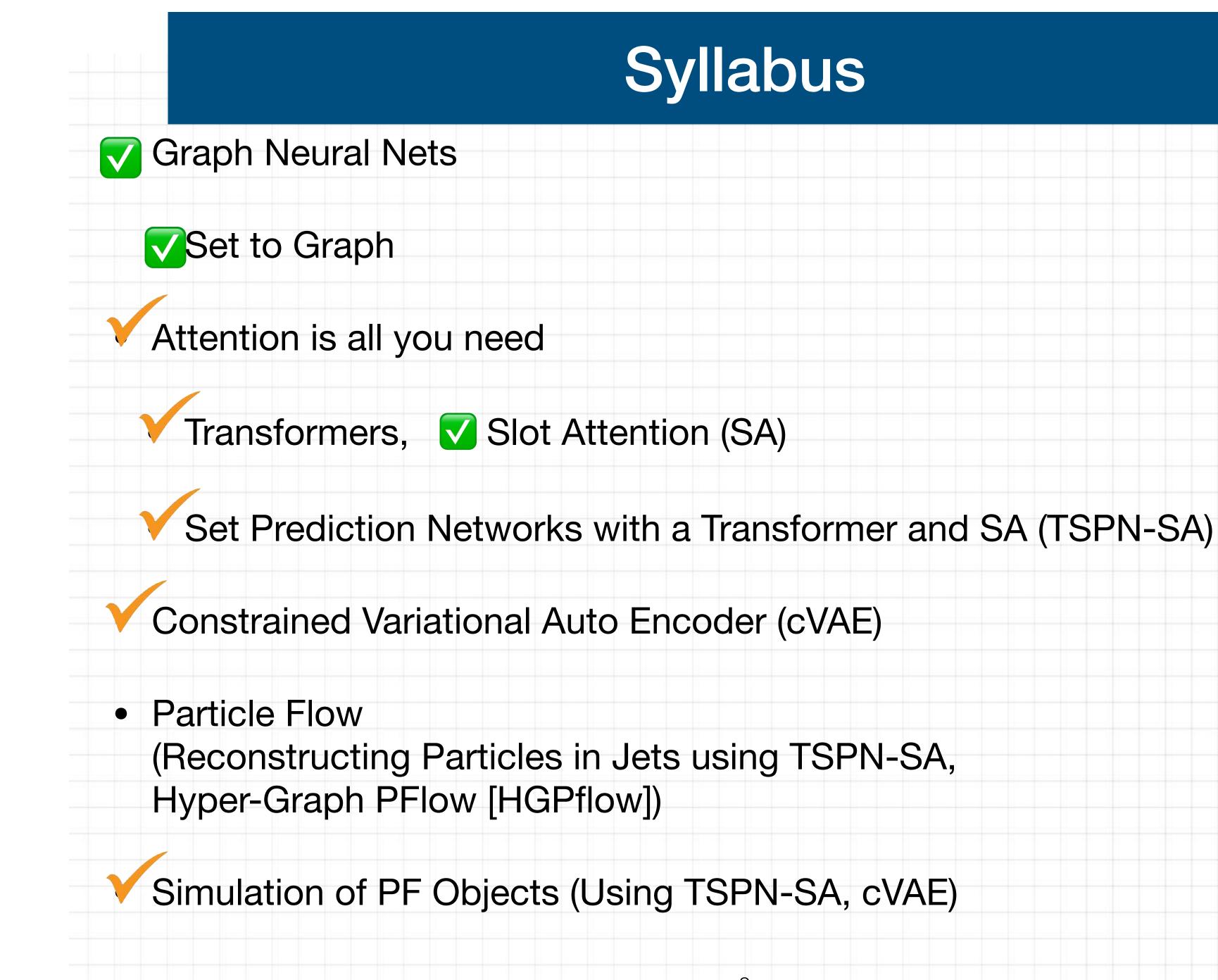
### Particle Flow with Deep Learning

Lecture 1: GNN+Attention

Lecture 2: Transformers + Set Generation (with the help of **N. Kakati** and **N. Soybelman**)

• Lecture 3: Hyper Graphs + TSPN Particle Flow (with the help of N. Kakati)

Eilam Gross, Weizmann, 2023



### Syllabus

### **Attention Is All You Need**

### https://arxiv.org/abs/1706.03762

Ashish Vaswani\*

Google Brain avaswani@google.com Noam Shazeer\*Niki Parmar\*Google BrainGoogle Researchnoam@google.comnikip@google.com

Llion Jones\* Google Research llion@google.com

Aidan N. Gomez\* † University of Toronto aidan@cs.toronto.edu

Illia Polosukhin\* <sup>‡</sup>
illia.polosukhin@gmail.com

Jakob Uszkoreit\* Google Research usz@google.com

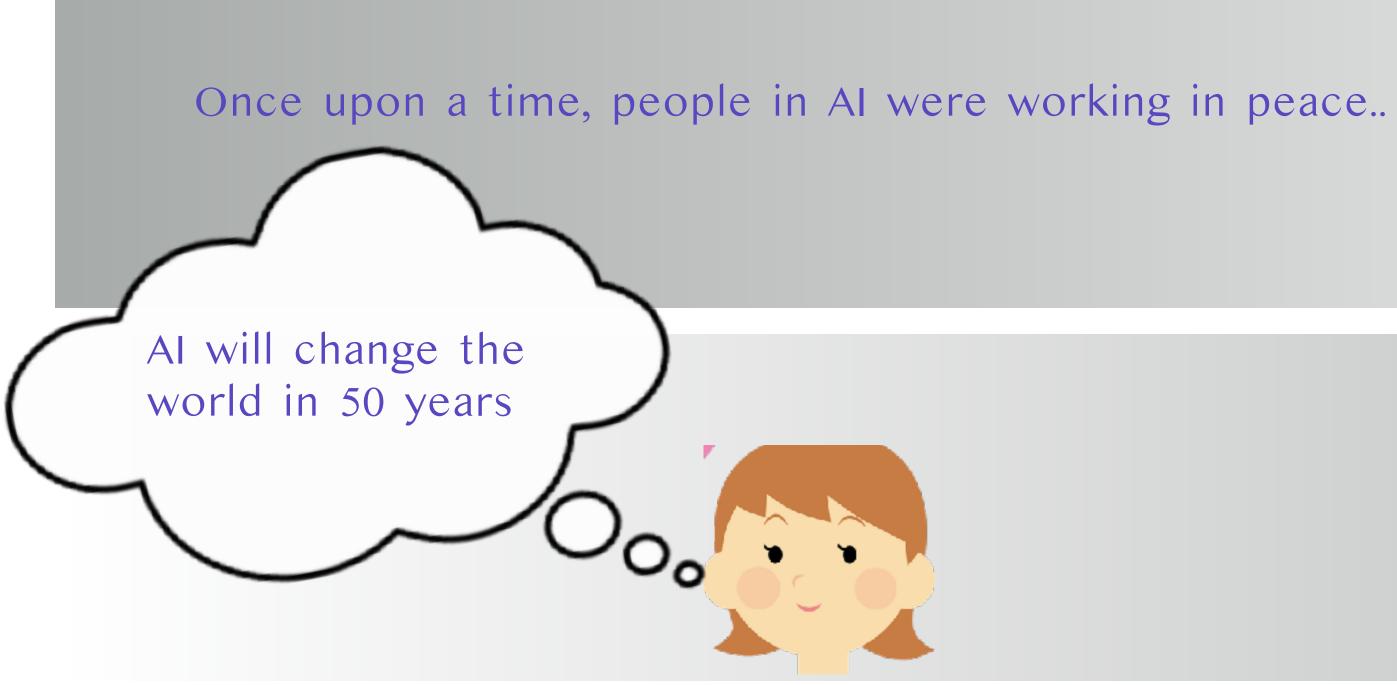
Łukasz Kaiser\*

Google Brain lukaszkaiser@google.com

A T - 4

# Attention is All You Need

Level 1 N. Kakati



#### One bright summer morning, a paper showed up

Weizmann Institute of Science



#### The field was making good progress

#### **Attention Is All You Need**

Ashish Vaswani\* Google Brain avaswani@google.com

Noam Shazeer\* Google Brain noam@google.com

Niki Parmar\* Google Research nikip@google.com

Jakob Uszkoreit\* Google Research usz@google.com

Llion Jones\* Google Research llion@google.com

Aidan N. Gomez\* † University of Toronto aidan@cs.toronto.edu

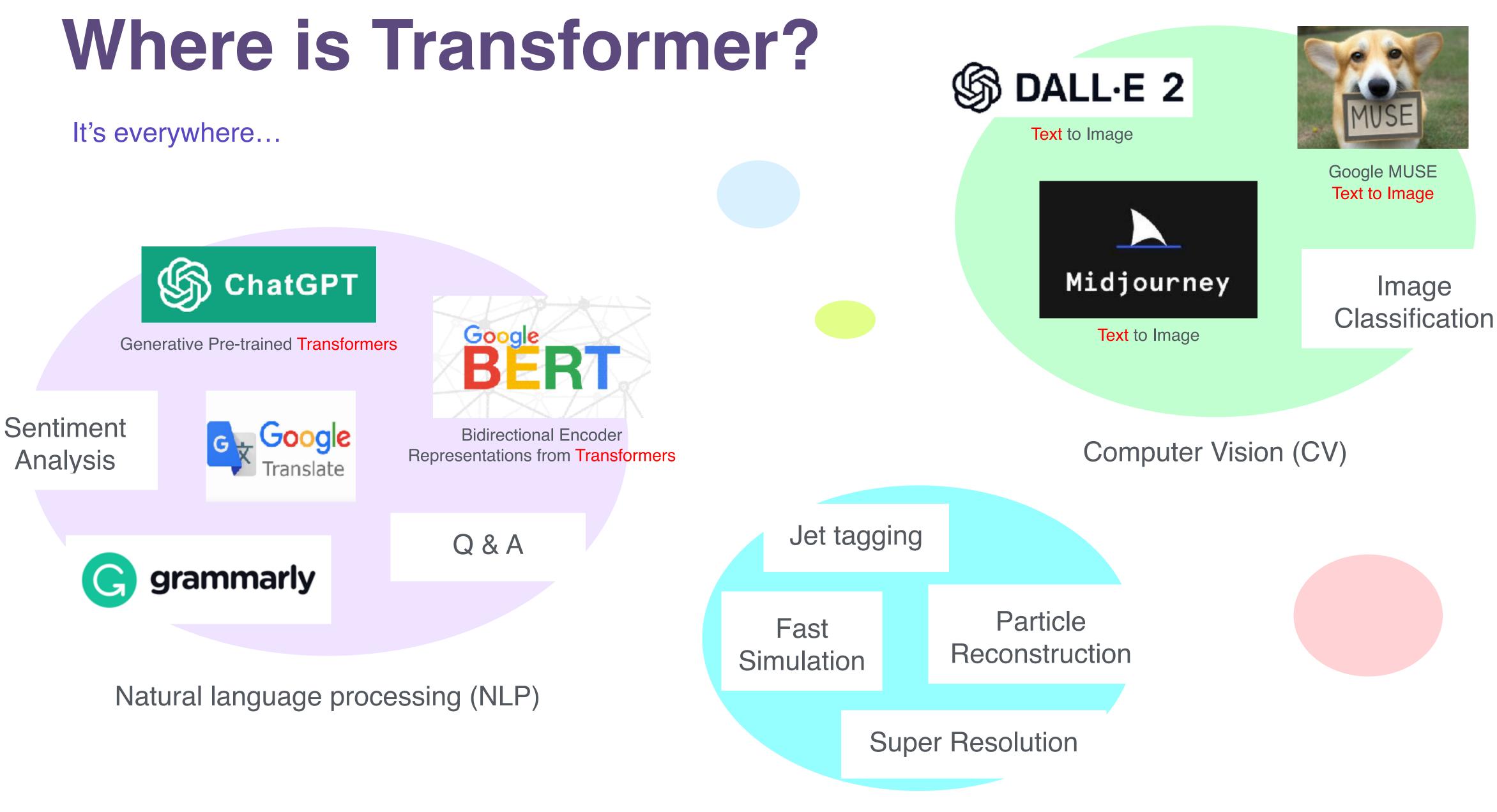
Łukasz Kaiser\* Google Brain lukaszkaiser@google.com

Illia Polosukhin\* ‡ illia.polosukhin@gmail.com

#### **AND THEN EVERYTHING CHANGED!**







Weizmann Institute of Science

# What is a Transformer?

- Looks very complicated
- It'll make sense once we understand the components

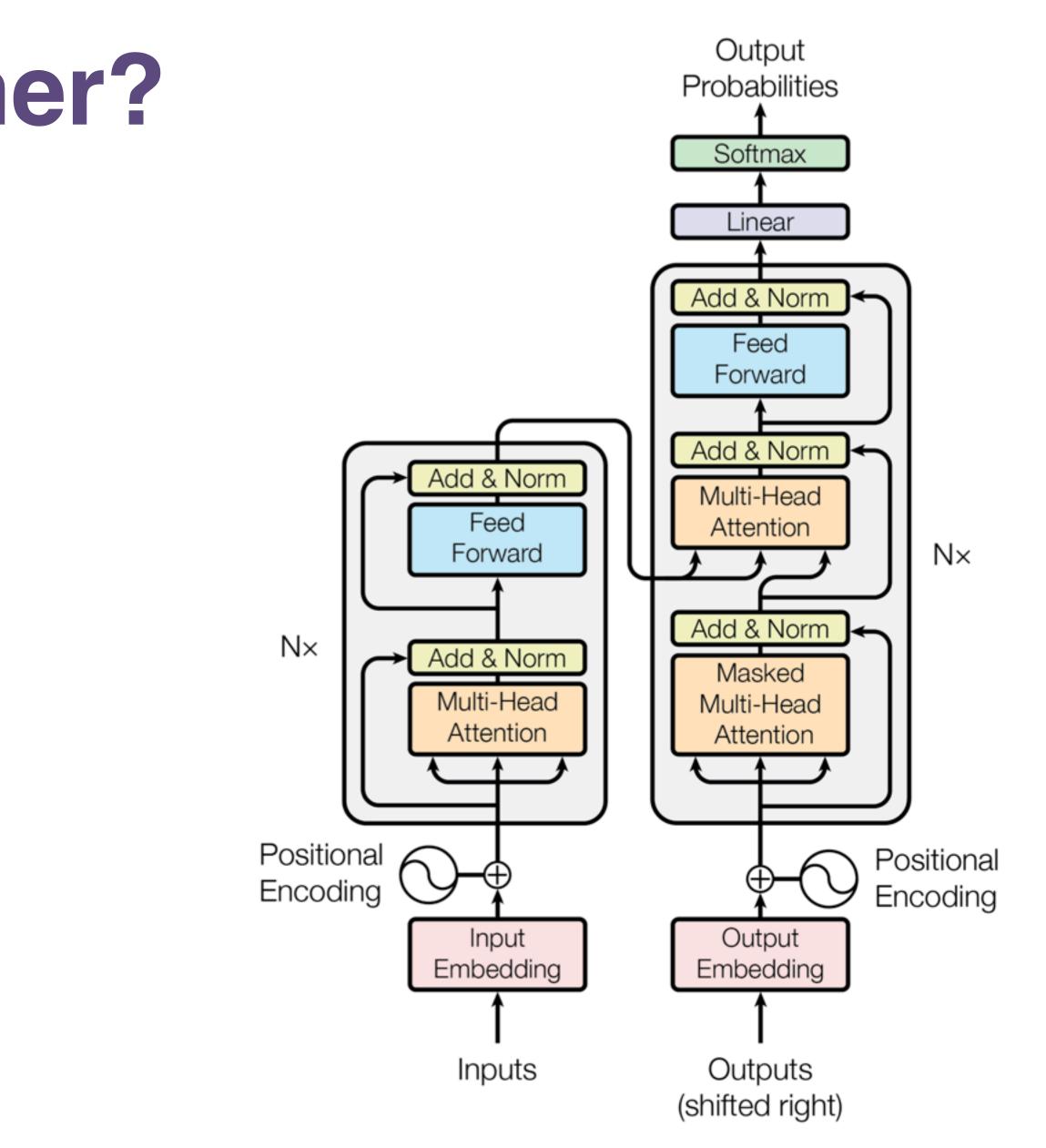
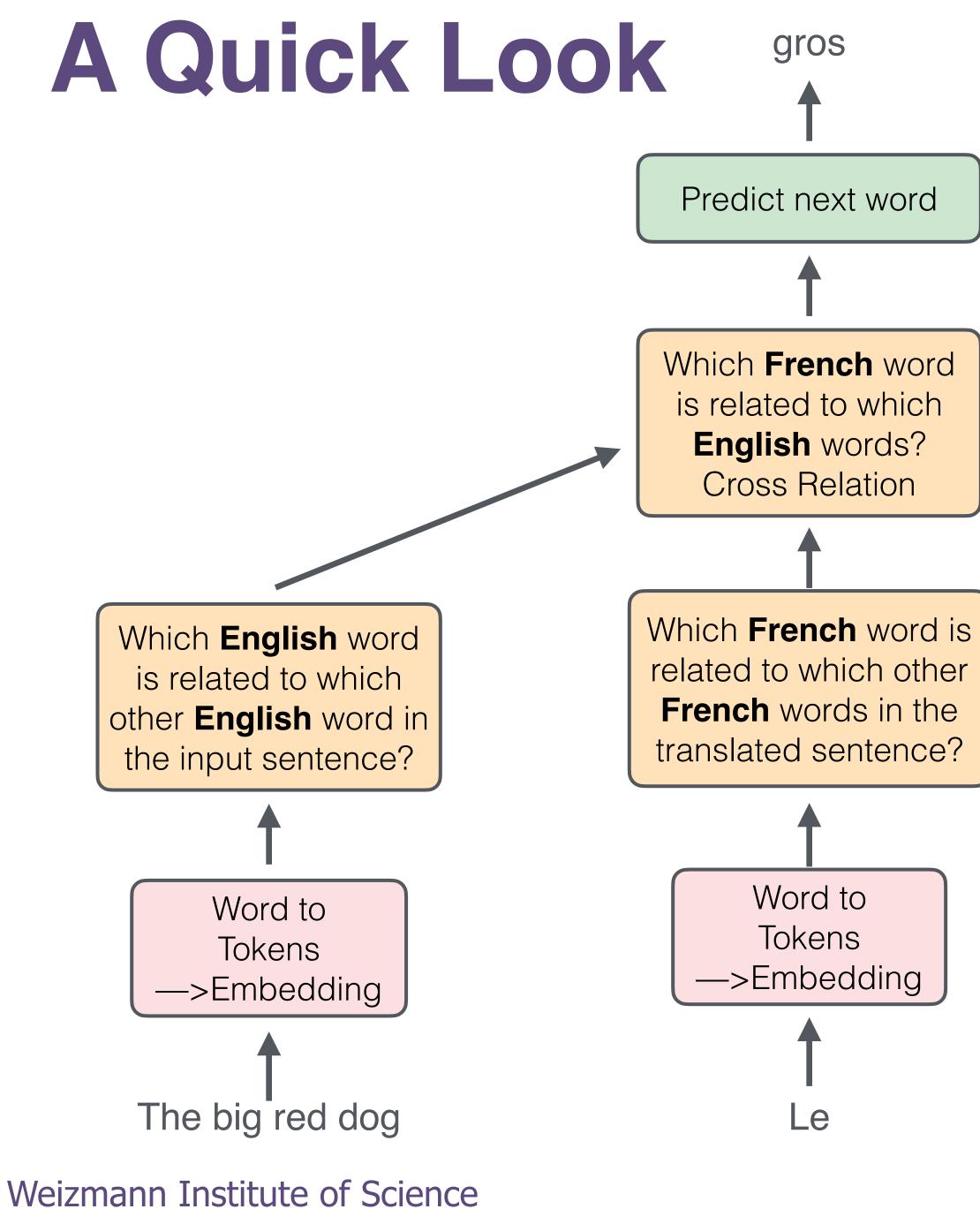
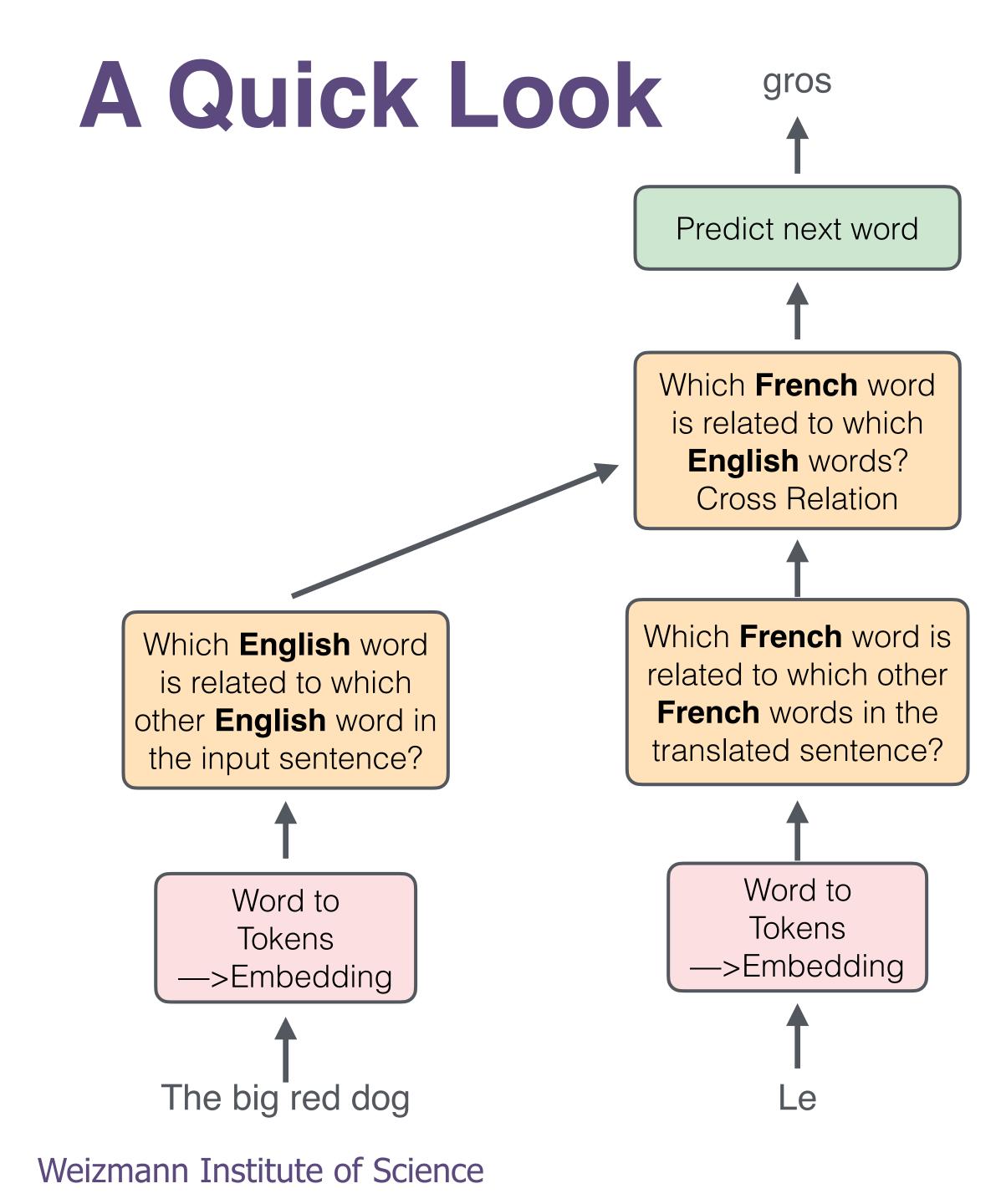


Figure 1: The Transformer - model architecture.



- We are doing translation ◆
  - English to French
- English sentence +
  - The big red dog
- Someone told you that the first word in + French is "Le"
  - You need to predict the next words one by one and complete the sentence





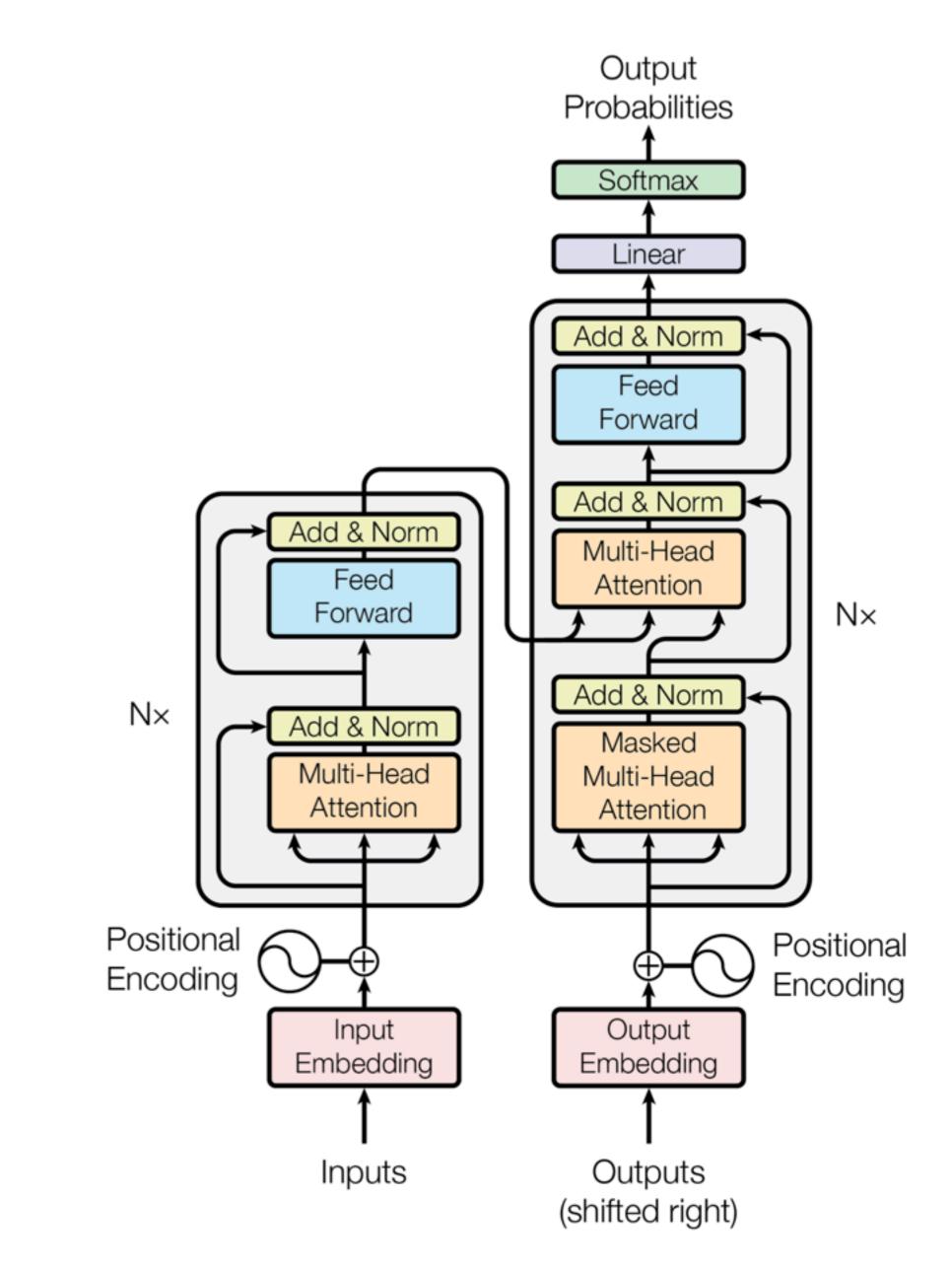


Figure 1: The Transformer - model architecture.

# Attention is All You Need

### Level 2 N. Kakati

- Pretty good explanation here

  - YouTube channel link
- This part of the lecture is mainly based on that video

https://www.youtube.com/watch?v=TQQIZhbC5ps



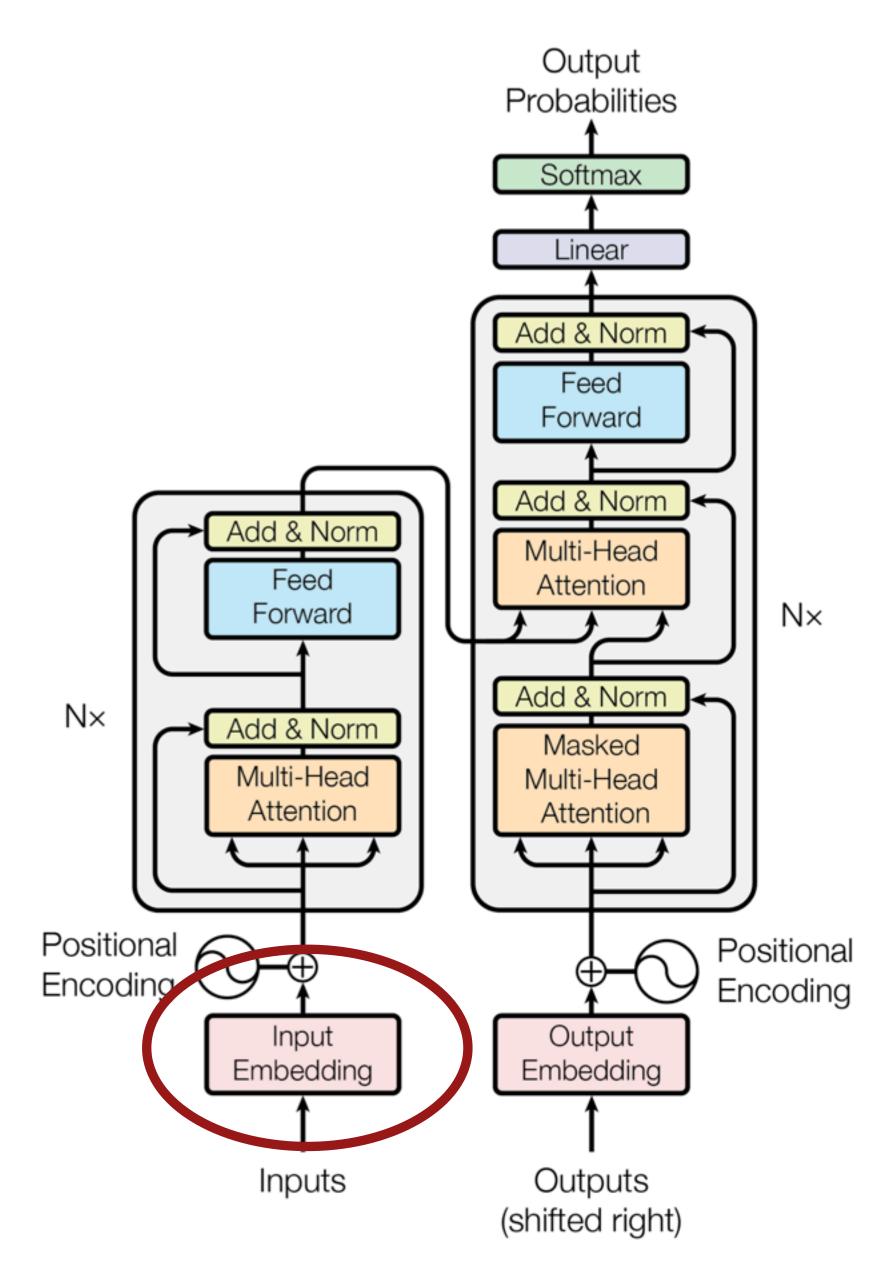
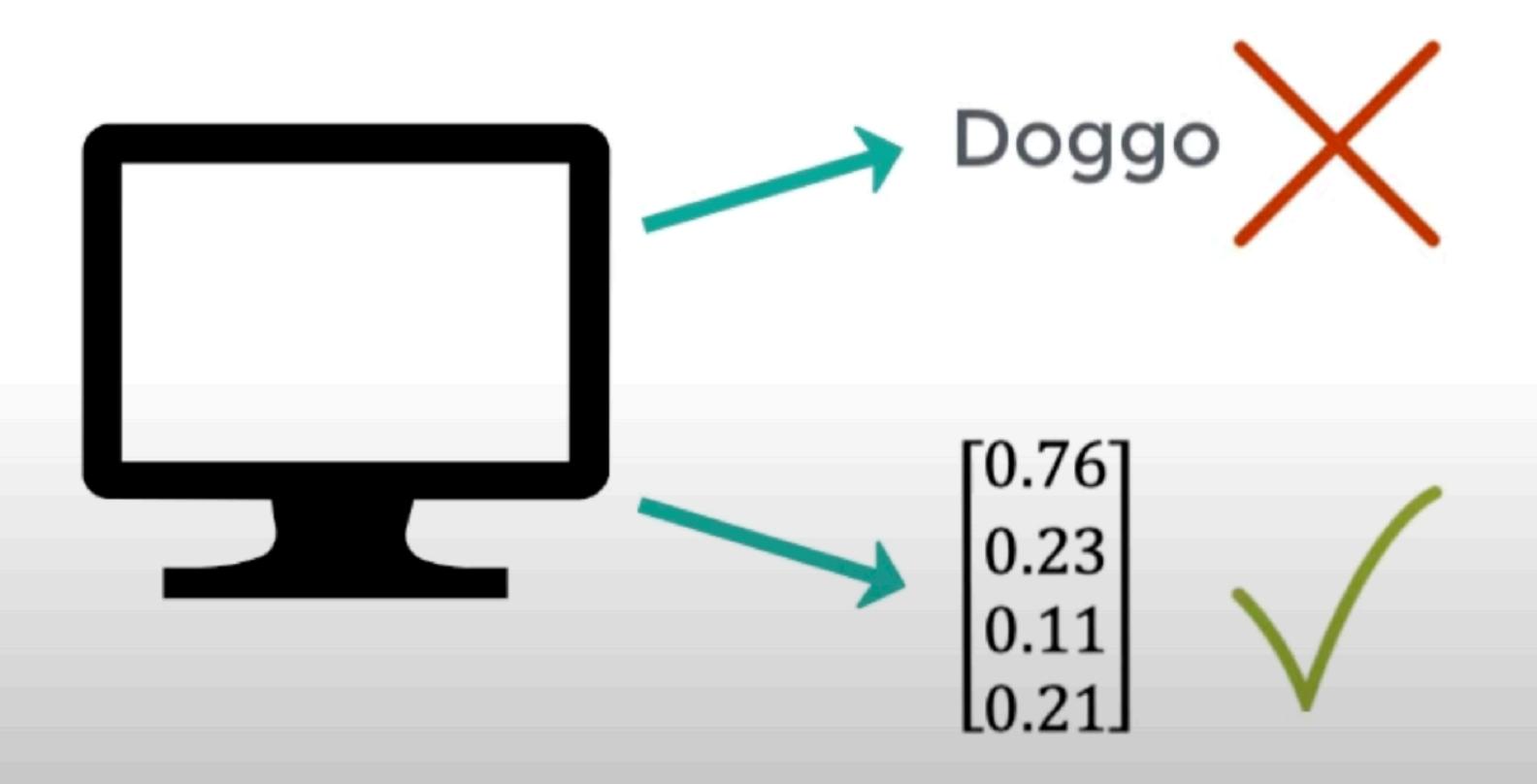


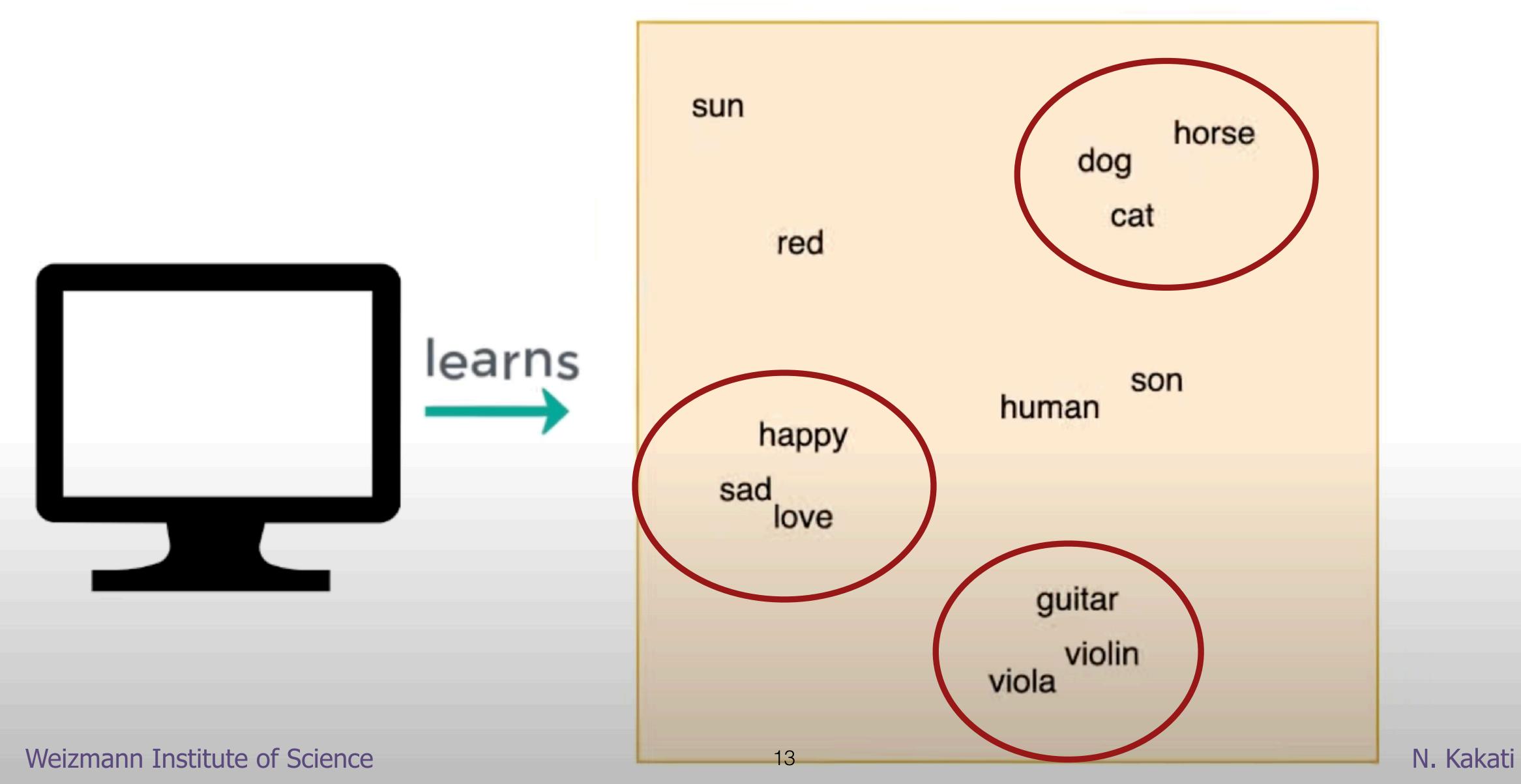
Figure 1: The Transformer - model architecture.





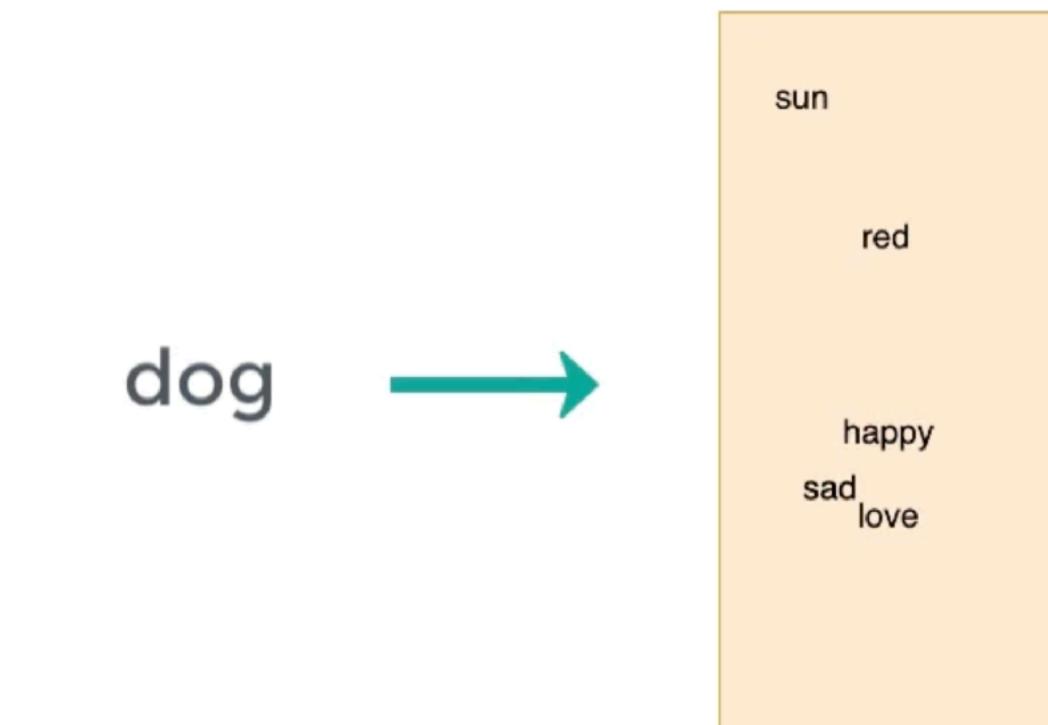
Weizmann Institute of Science





#### **Embedding space**

### Embedding



Weizmann Institute of Science





### [0.37] 0.99 0.01 0.08]



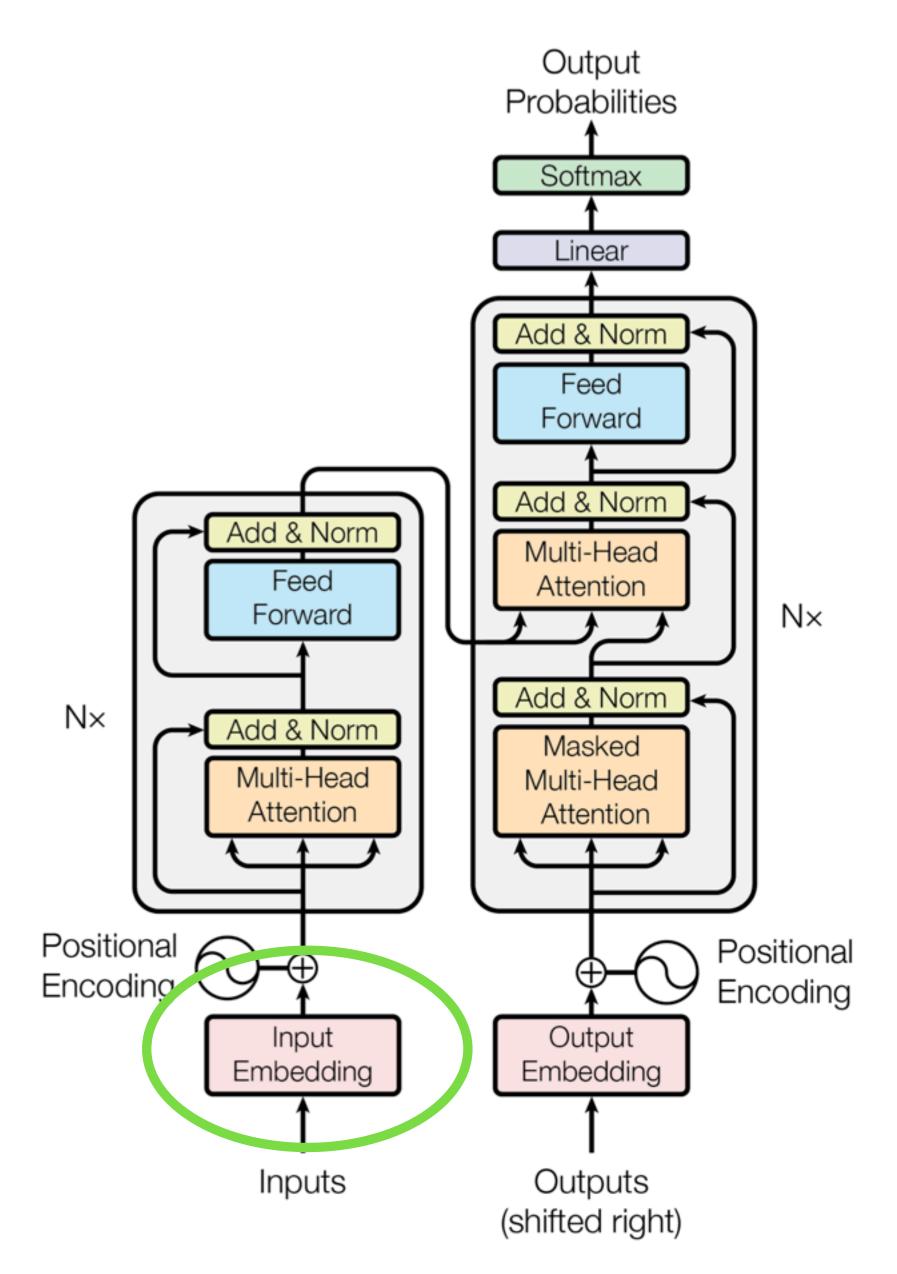


Figure 1: The Transformer - model architecture.

### **Positional encoding**

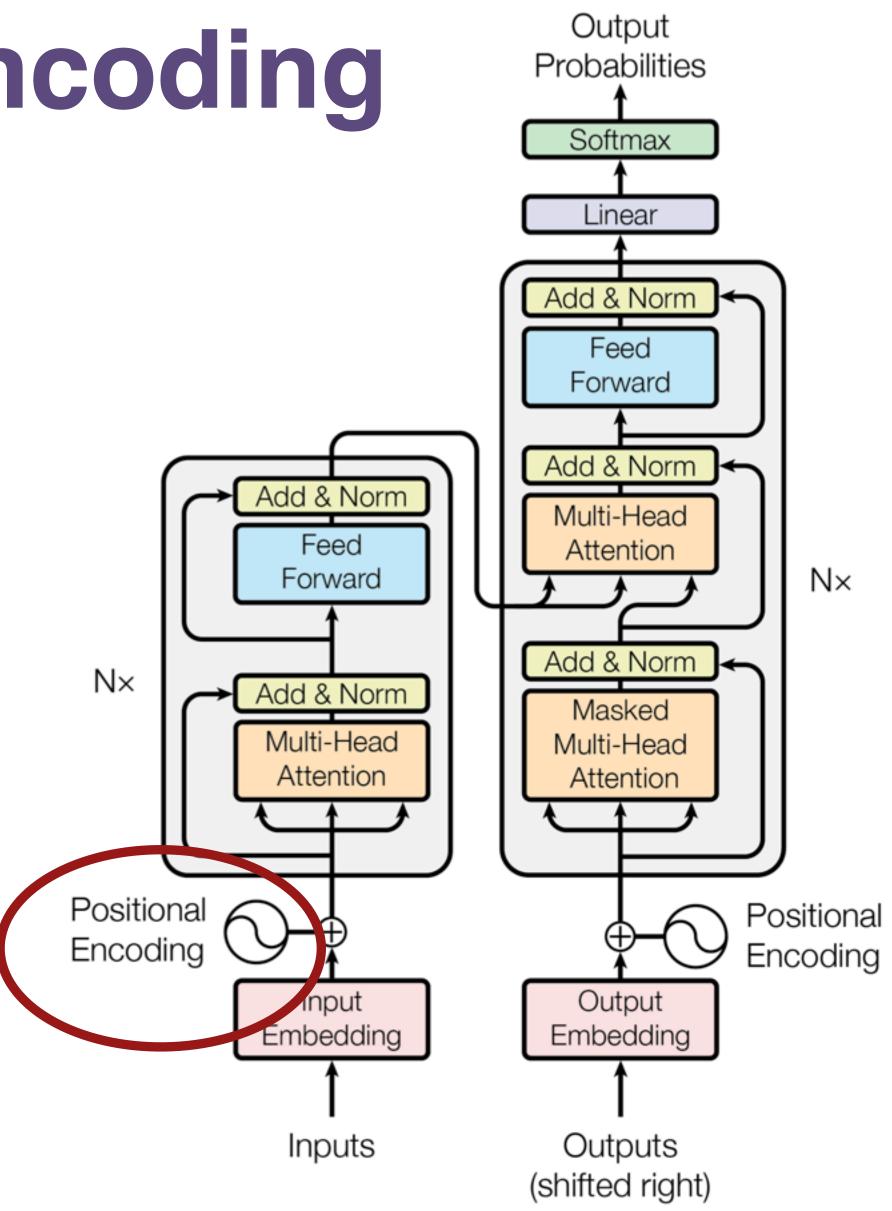
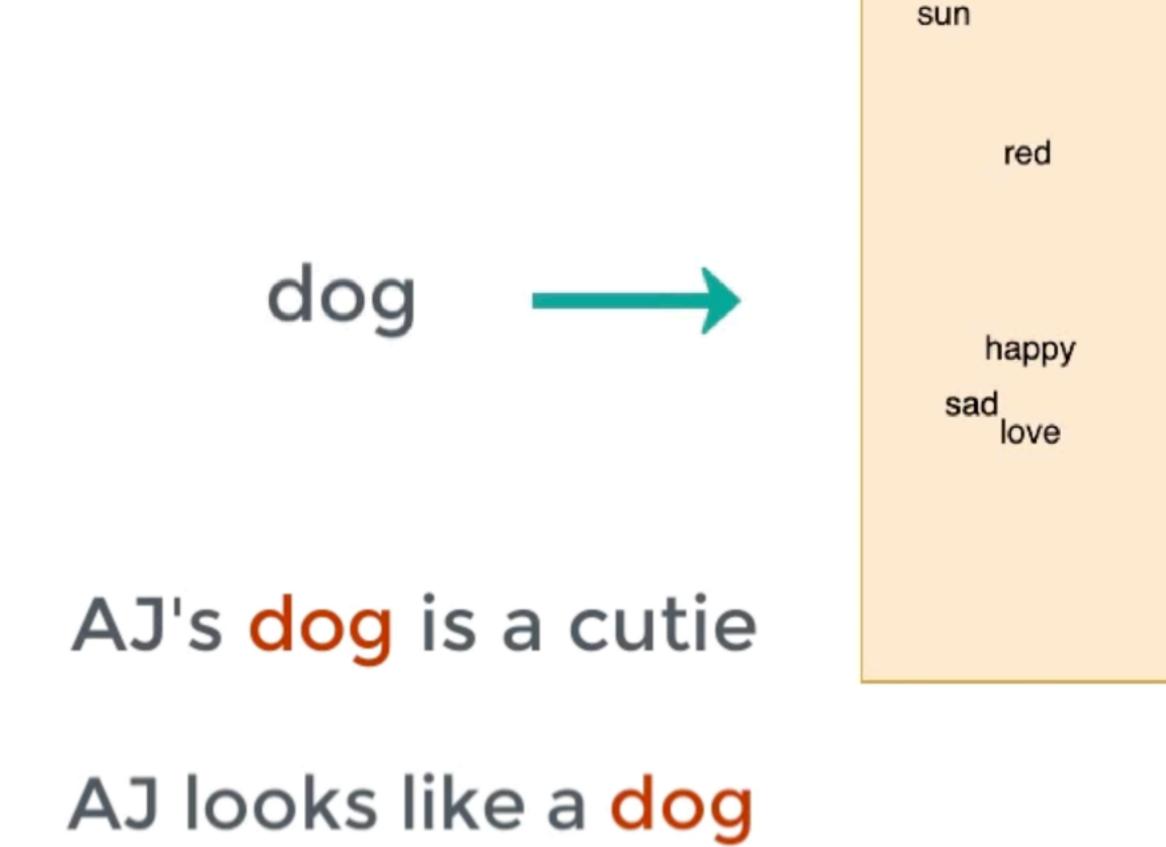
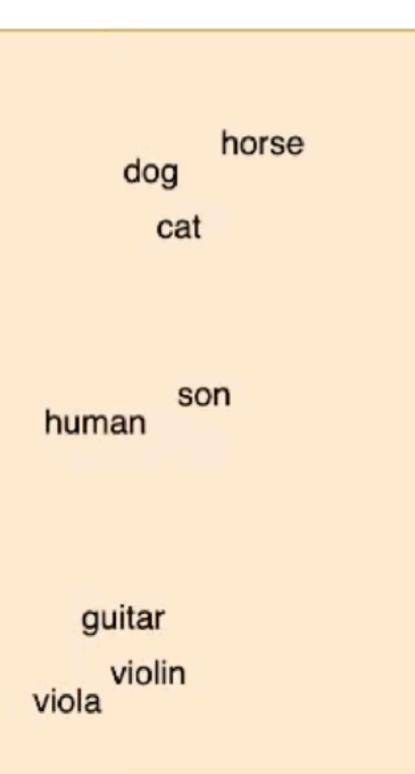


Figure 1: The Transformer - model architecture.

## **Positional encoding**



Weizmann Institute of Science





### 0.37 0.99 0.01 0.08

# **Positional Encoding**

Weizmann Institute of Science

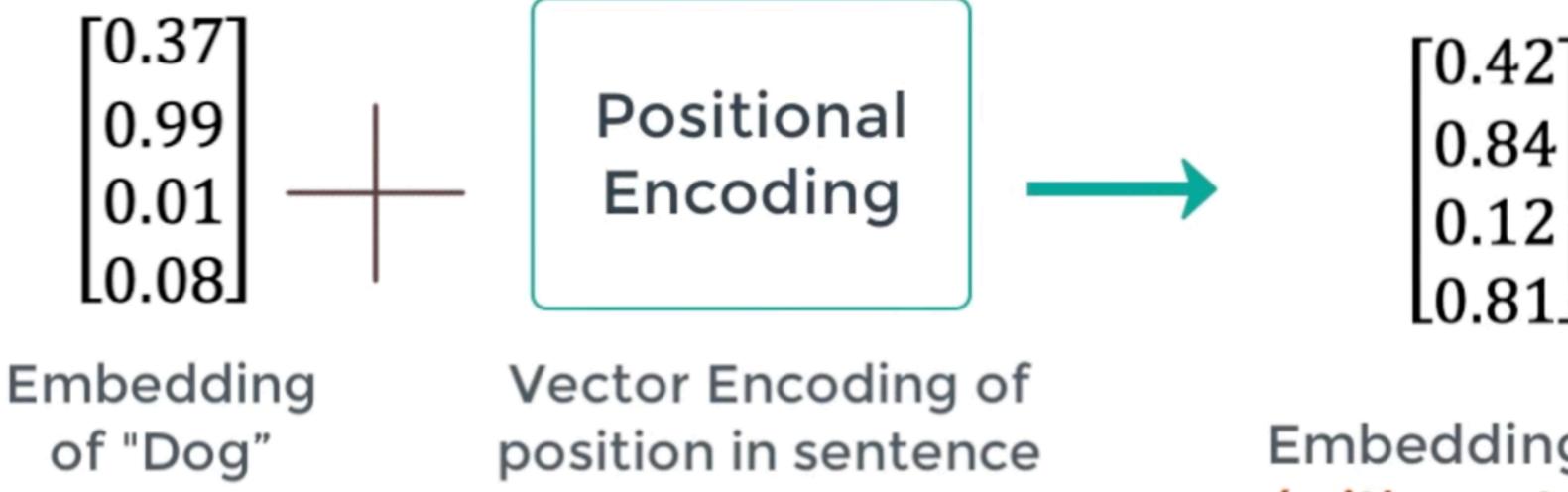


#### Positional encoder: Vector that gives context based on position of word in sentence





## **Positional Encoding**



Weizmann Institute of Science



Embedding of Dog (with context info)

### **Positional encoding**

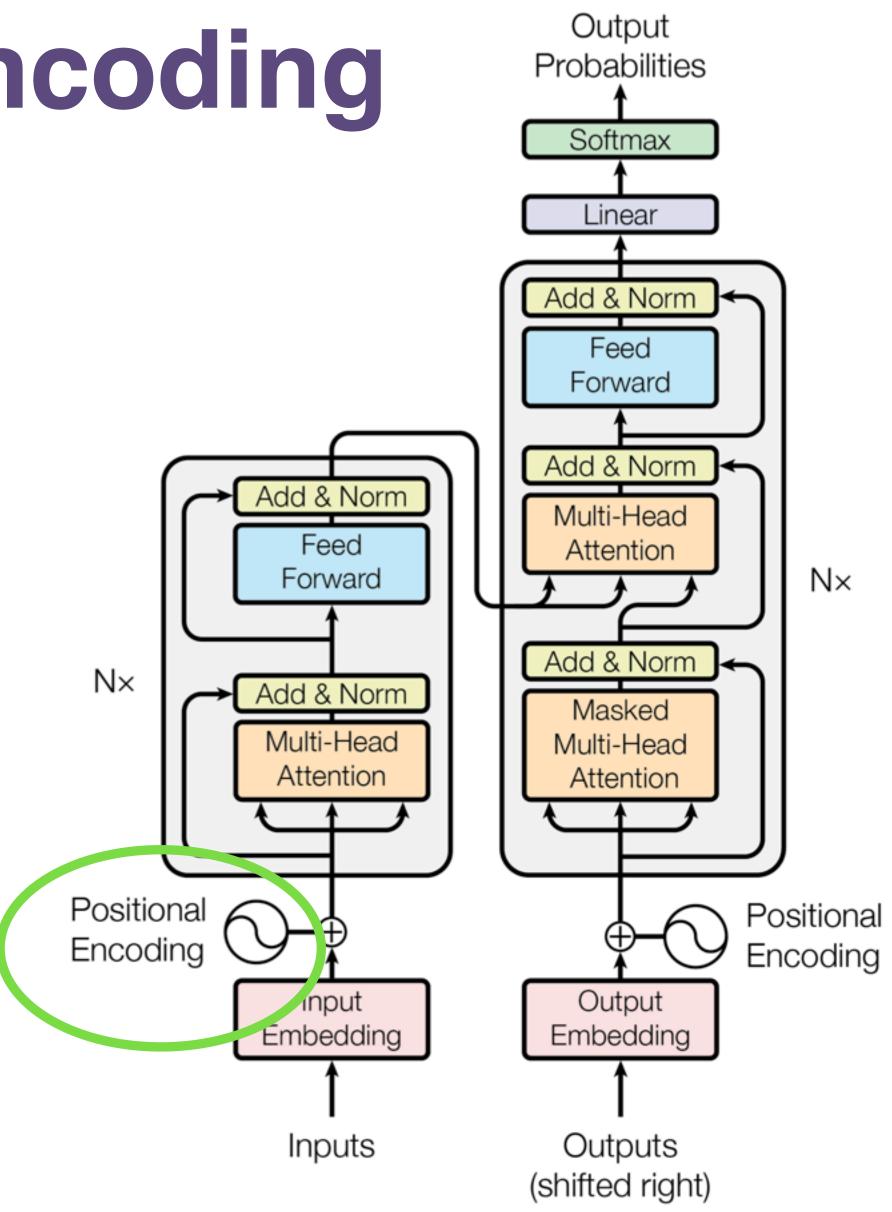


Figure 1: The Transformer - model architecture.

### Attention

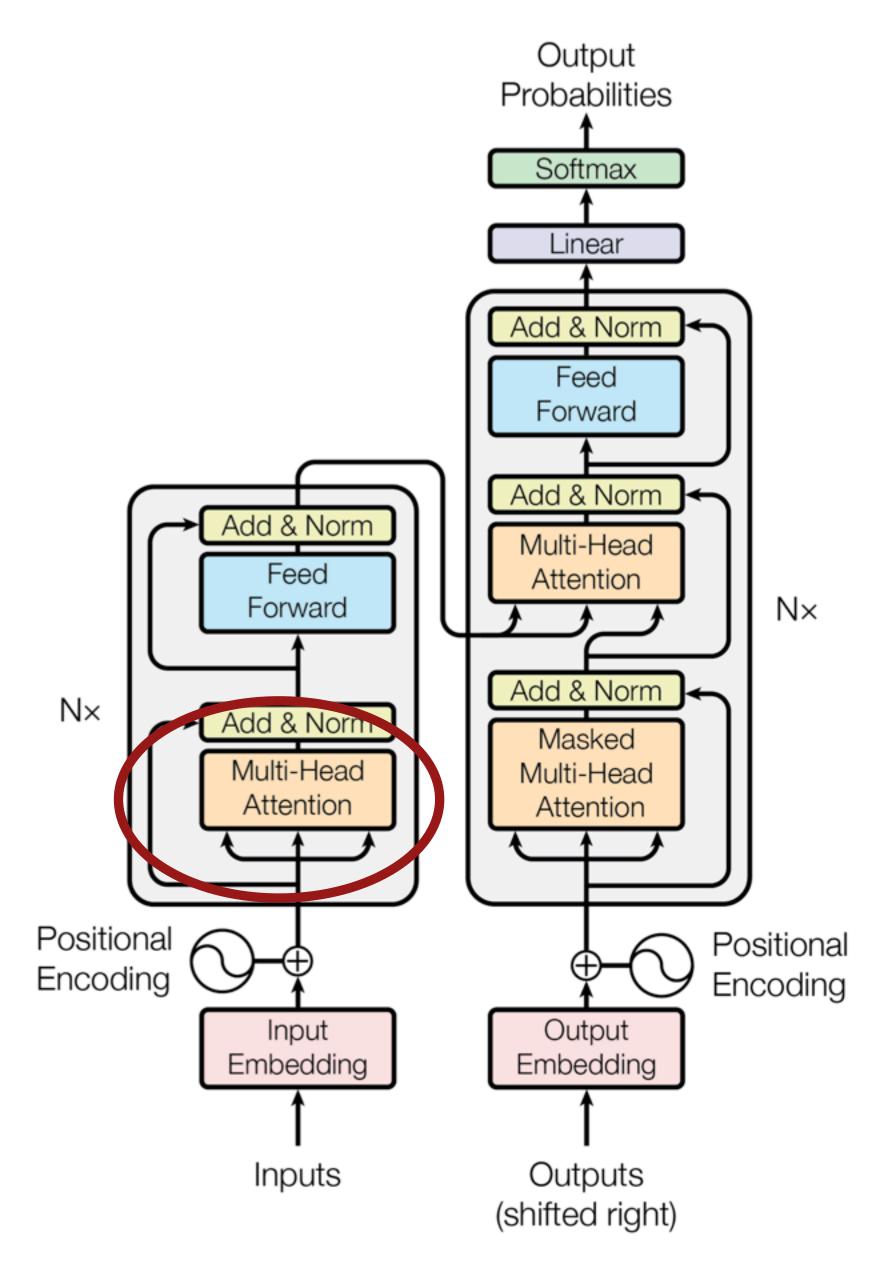


Figure 1: The Transformer - model architecture.

### Attention

How relevant one word is to the others?

# The big red dog big $\rightarrow$ The big red dog red -> The big red dog dog -> The big red dog

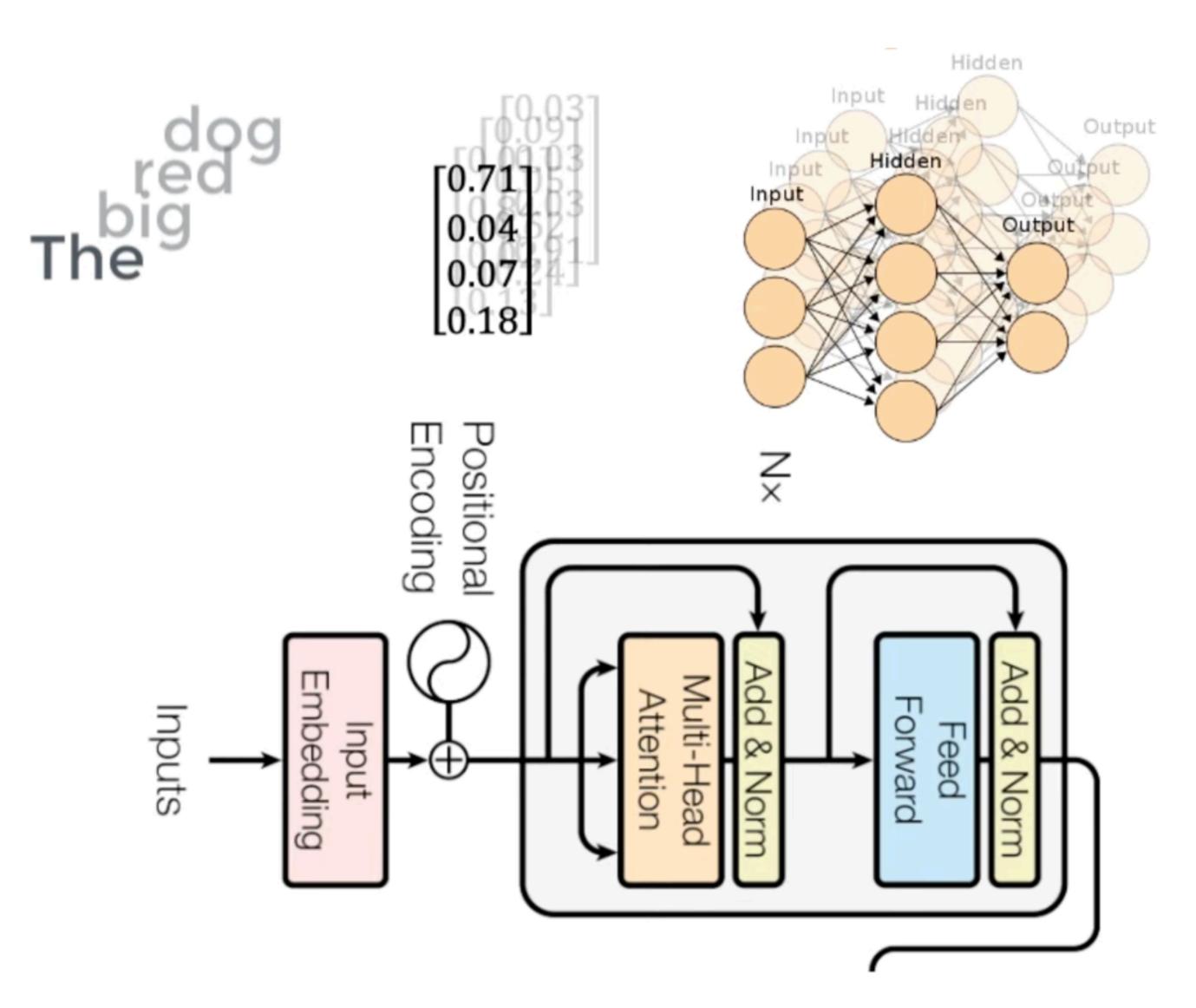
Weizmann Institute of Science

#### Attention matrix

[0.71	0.04	0.07	0.18]
[0.01	0.84	0.02	0.13
[0.09	0.05	0.62	0.24
[0.03	0.03	0.03	0.91



### FeedForward



# Attention + FeedForward

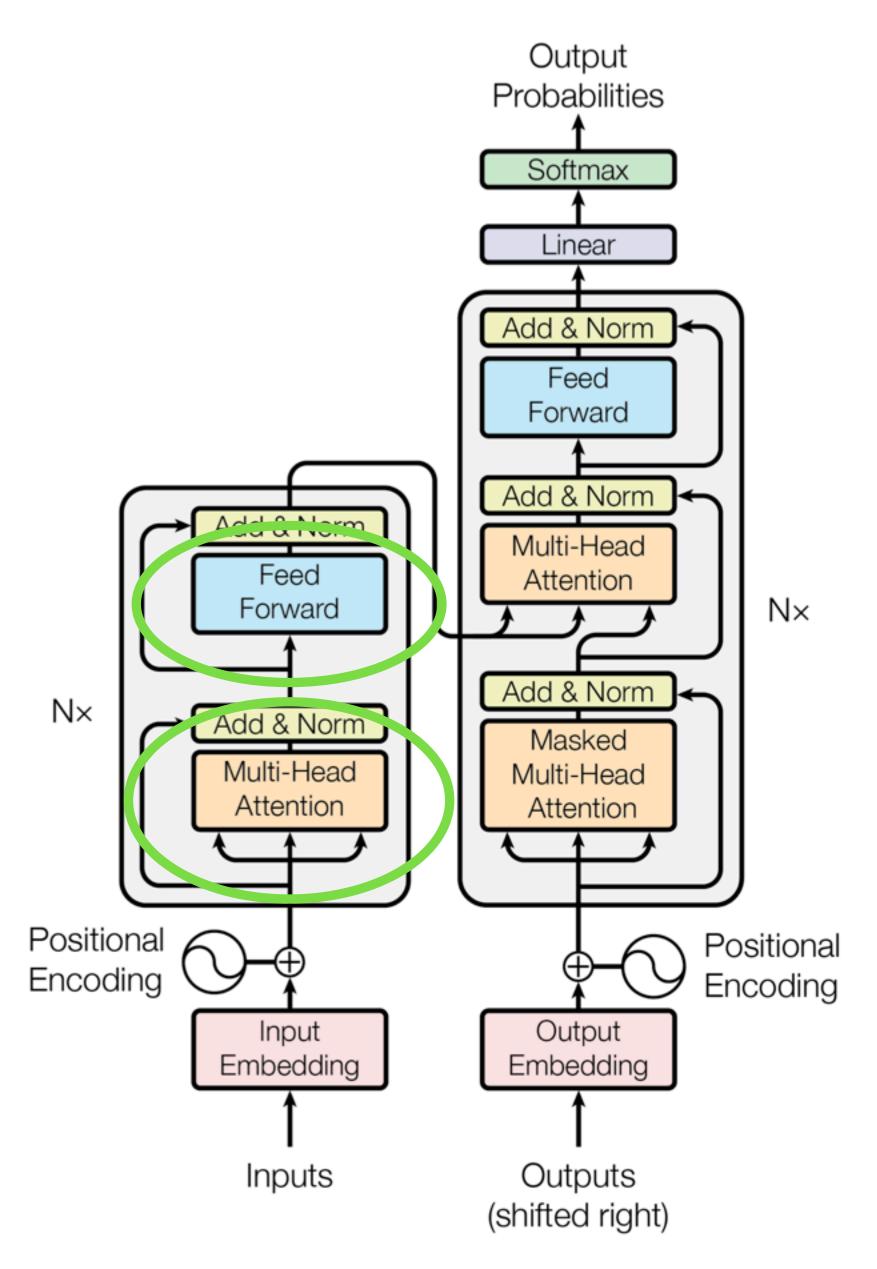


Figure 1: The Transformer - model architecture.



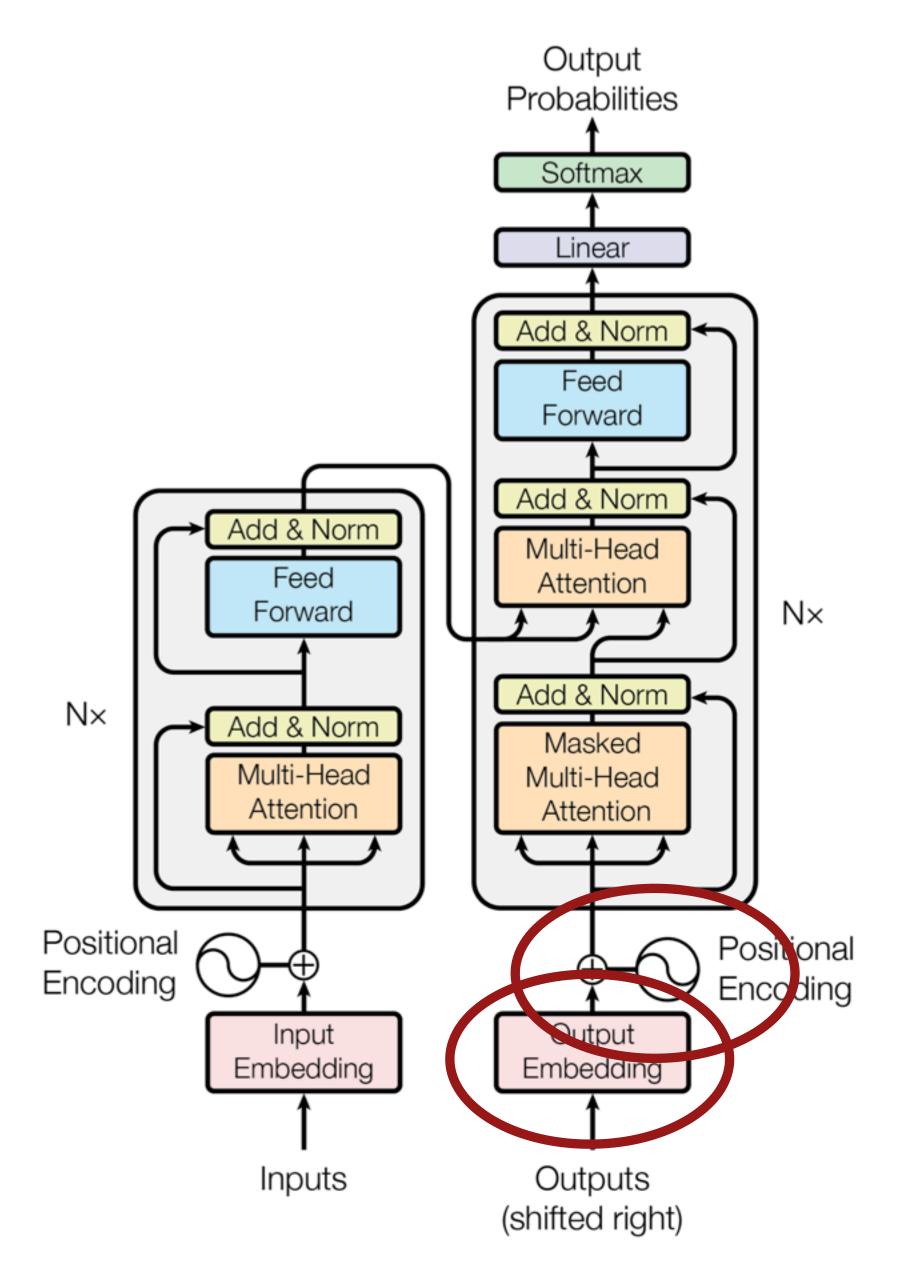


Figure 1: The Transformer - model architecture.



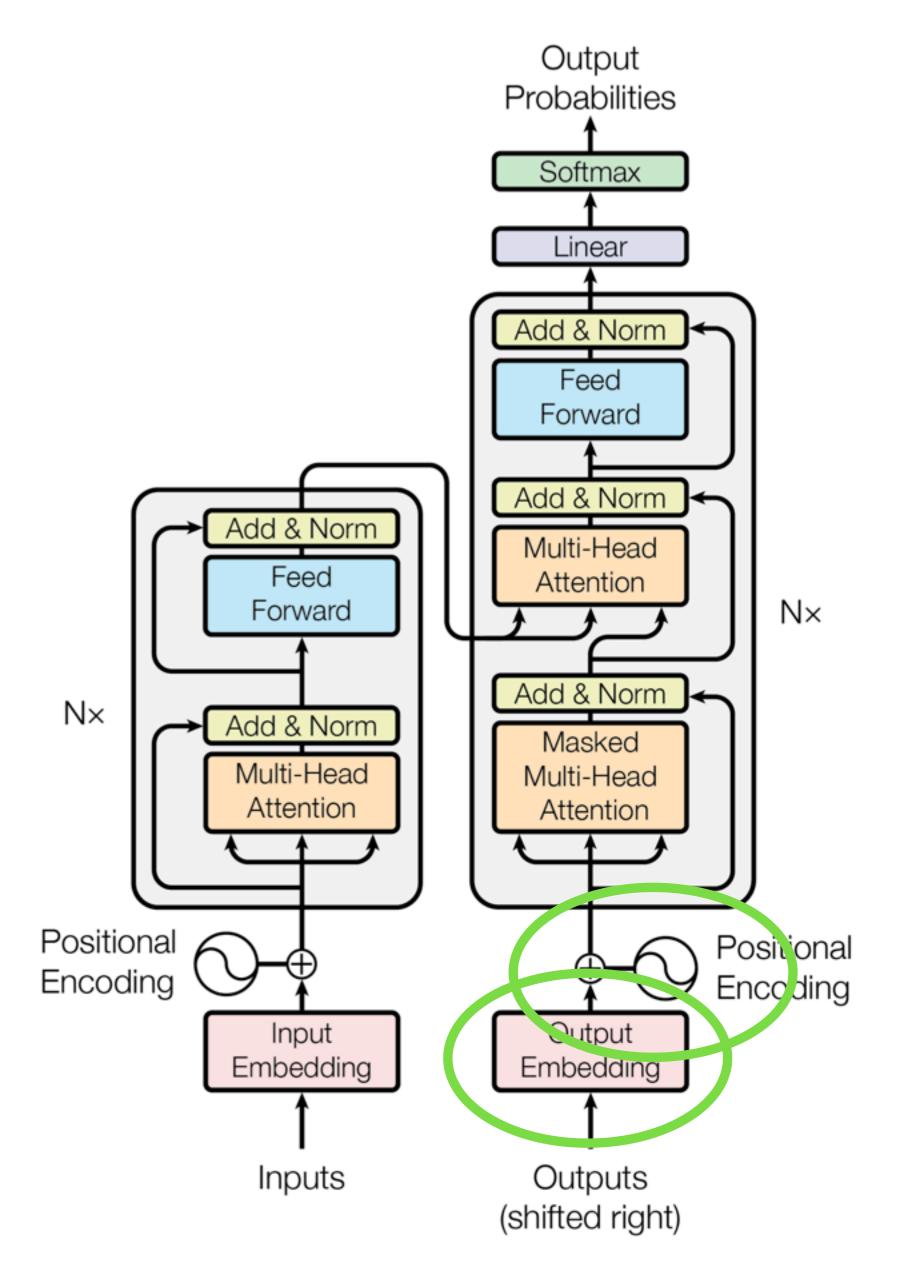


Figure 1: The Transformer - model architecture.

### Masked attention

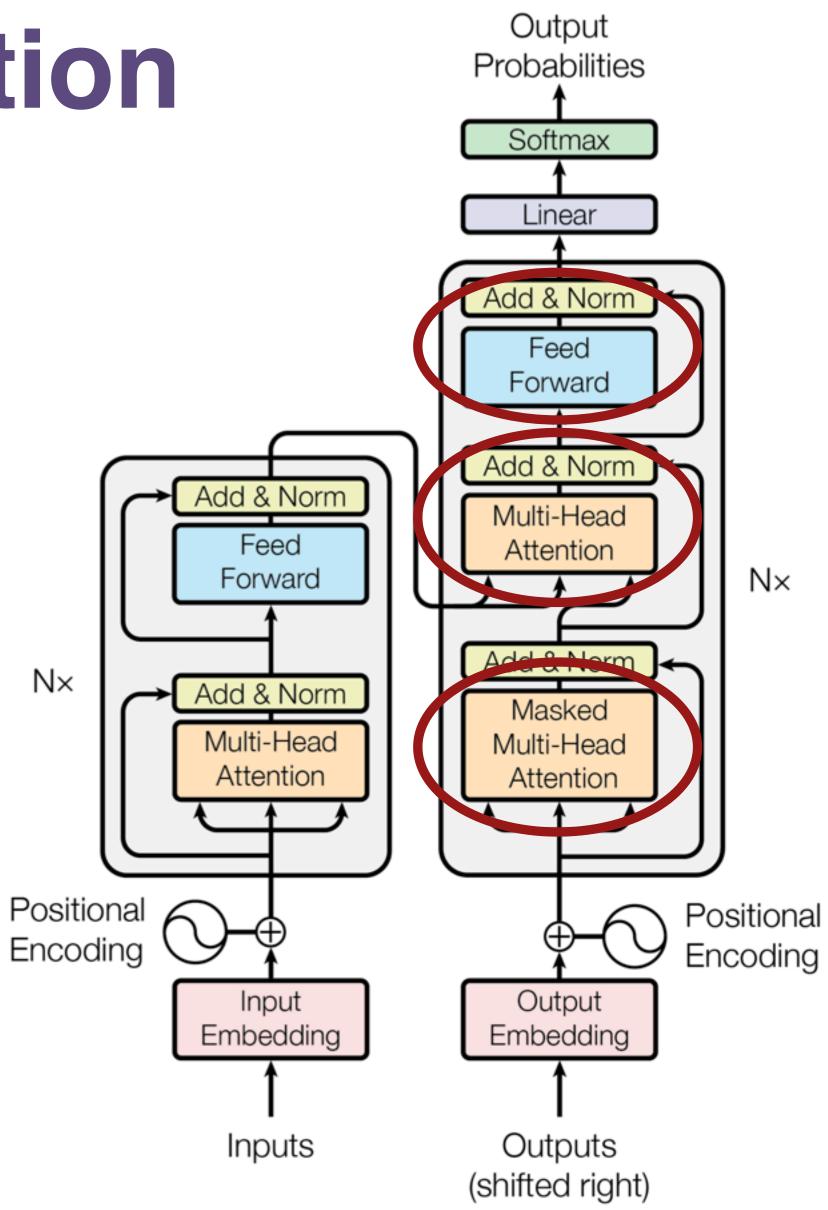


Figure 1: The Transformer - model architecture.

### Self attention



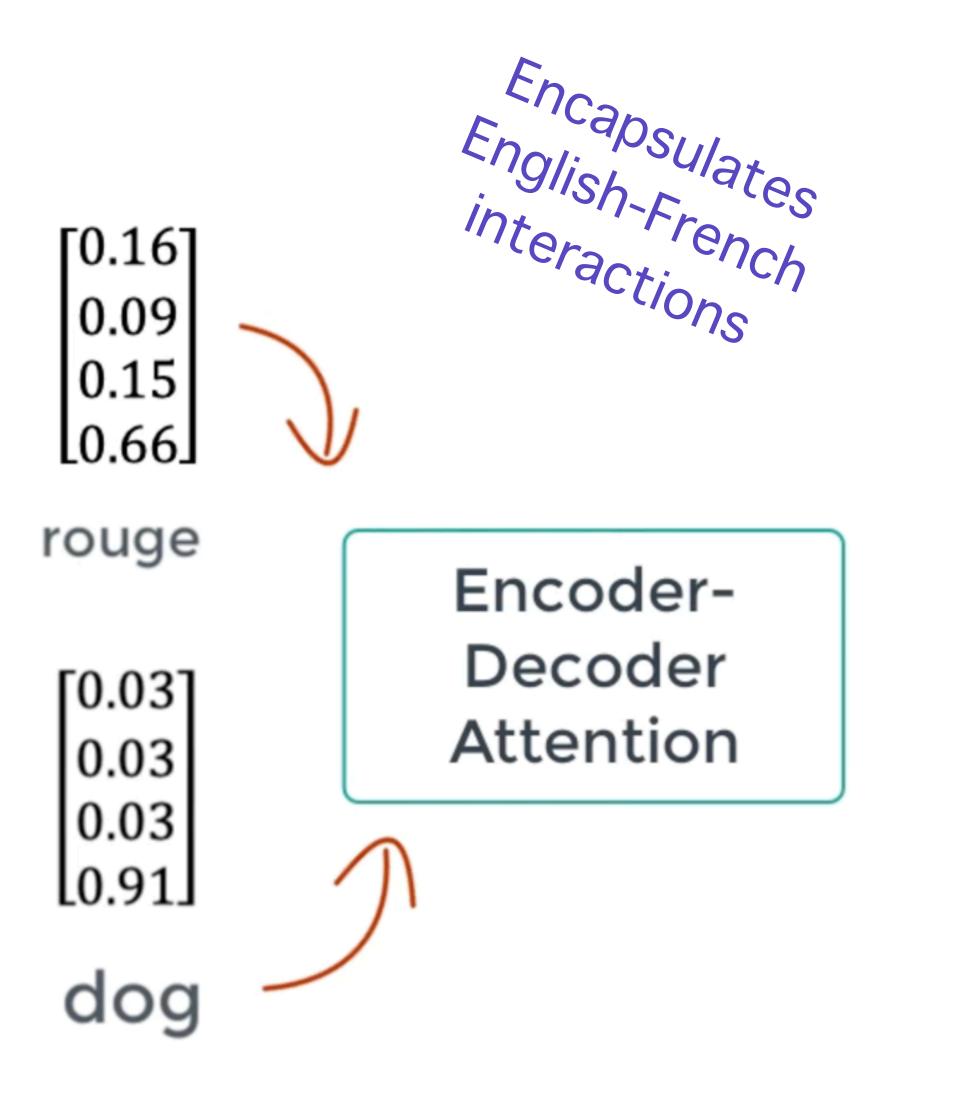
Weizmann Institute of Science

# Le gros chien rouge gros $\longrightarrow$ Le gros chien rouge chien $\rightarrow$ Le gros chien rouge rouge -> Le gros chien rouge

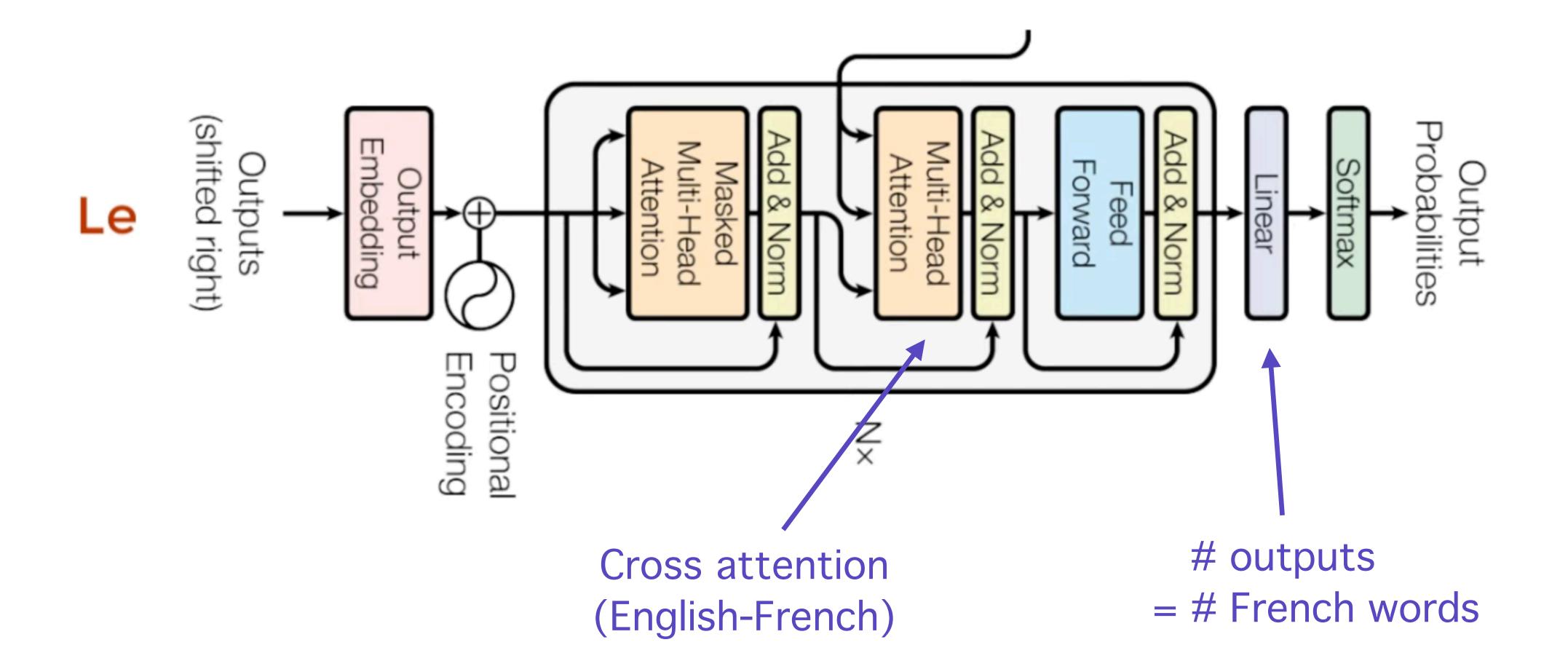
### **Cross attention**

[1] 0 0	$\begin{bmatrix} 0.1 \\ 0.9 \\ 0 \\ 0 \end{bmatrix}$	0.05 0.40 0.55 0
Le	gros	chien
0.71 0.04 0.07 0.18	[0.01] 0.84 0.02 0.13]	[0.09] 0.05 0.62 0.24]
The	big	red

Weizmann Institute of Science



### **Cross attention**



# That's pretty much it. Now let's look at some details we dropped



## "Multihead" attention

- There can be multiple relationships to learn
  - Positional
    - ➡ "Is there" question. "There is" affirmative
  - Subject verb relationship
- Let's have multiple attentions
  - Multihead attention
- We'll combine all of them once they are computed

#### Weizmann Institute of Science

### The $\rightarrow$ The big red dog big $\rightarrow$ The big red dog red $\rightarrow$ The big red dog dog $\rightarrow$ The big red dog

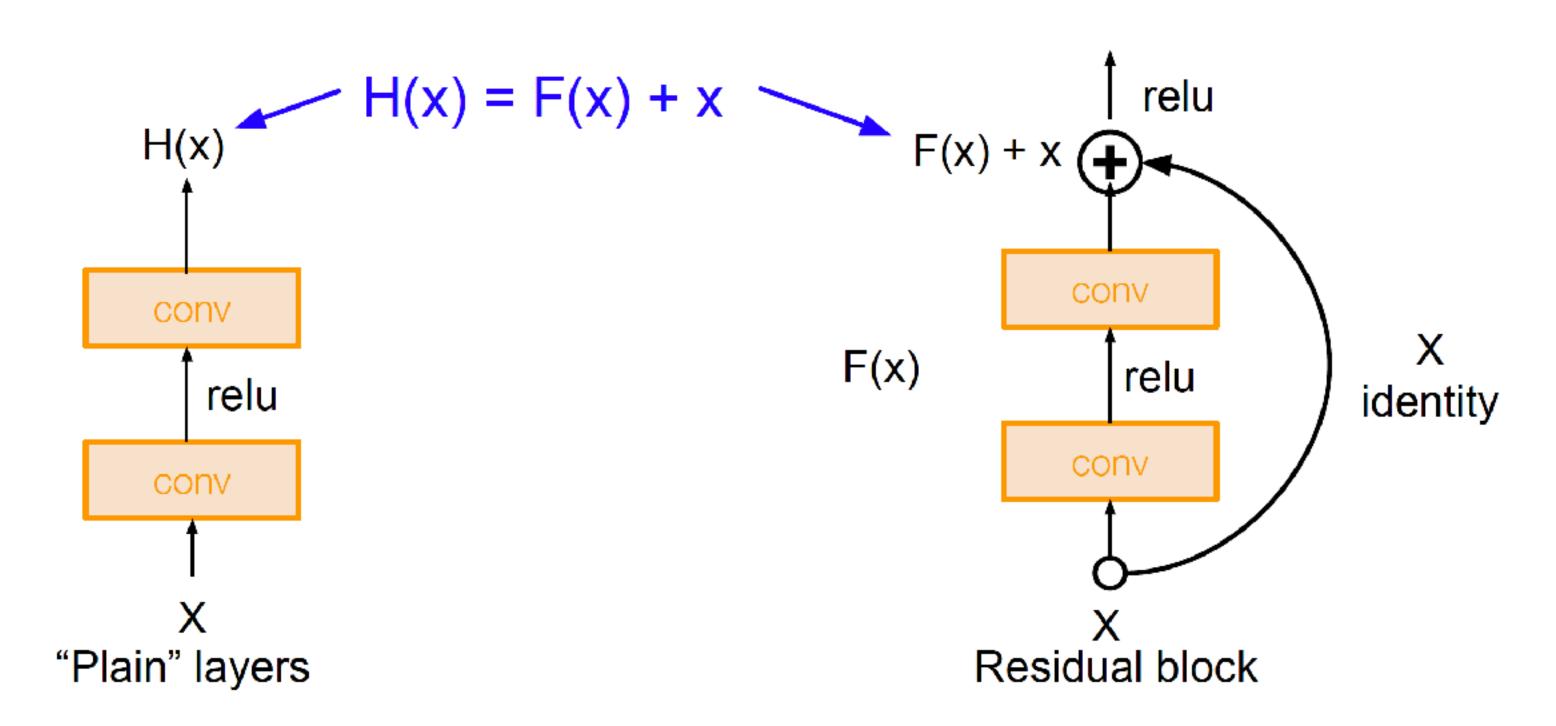
### The $\rightarrow$ The big red dog big $\rightarrow$ The big red dog red $\rightarrow$ The big red dog dog $\rightarrow$ The big red dog

### "Masked" attention

- + The initial problem we talked about
  - ➡ English: The big red dog.
  - → French: Le gros chien rouge
- But, when we start we only know the first French word
  - While computing attention, during training, we only need to look at the first word
  - Mask the rest  $\rightarrow$  Masked attention

Le  $\rightarrow$  Le gros chien rouge gros  $\rightarrow$  Le gros chien rouge chien  $\rightarrow$  Le gros chien rouge rouge  $\rightarrow$  Le gros chien rouge

### Add & Norm (RESIDUAL NETWORK)



Weizmann Institute of Science

Use layers to fit residual F(x) = H(x) - xinstead of H(x) directly

### Add & Norm

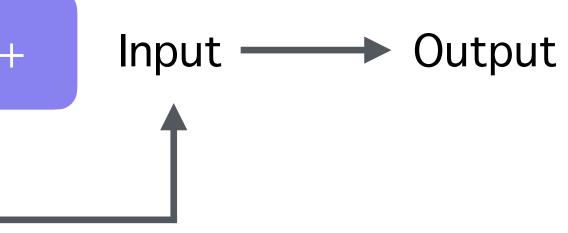
#### Add = skip connections



- + Helps remembering where it started from
- Useful in deeper networks (in general)

#### Norm = normalize (layer-wise or batch-wise)

Weizmann Institute of Science



### Now we understand the principle

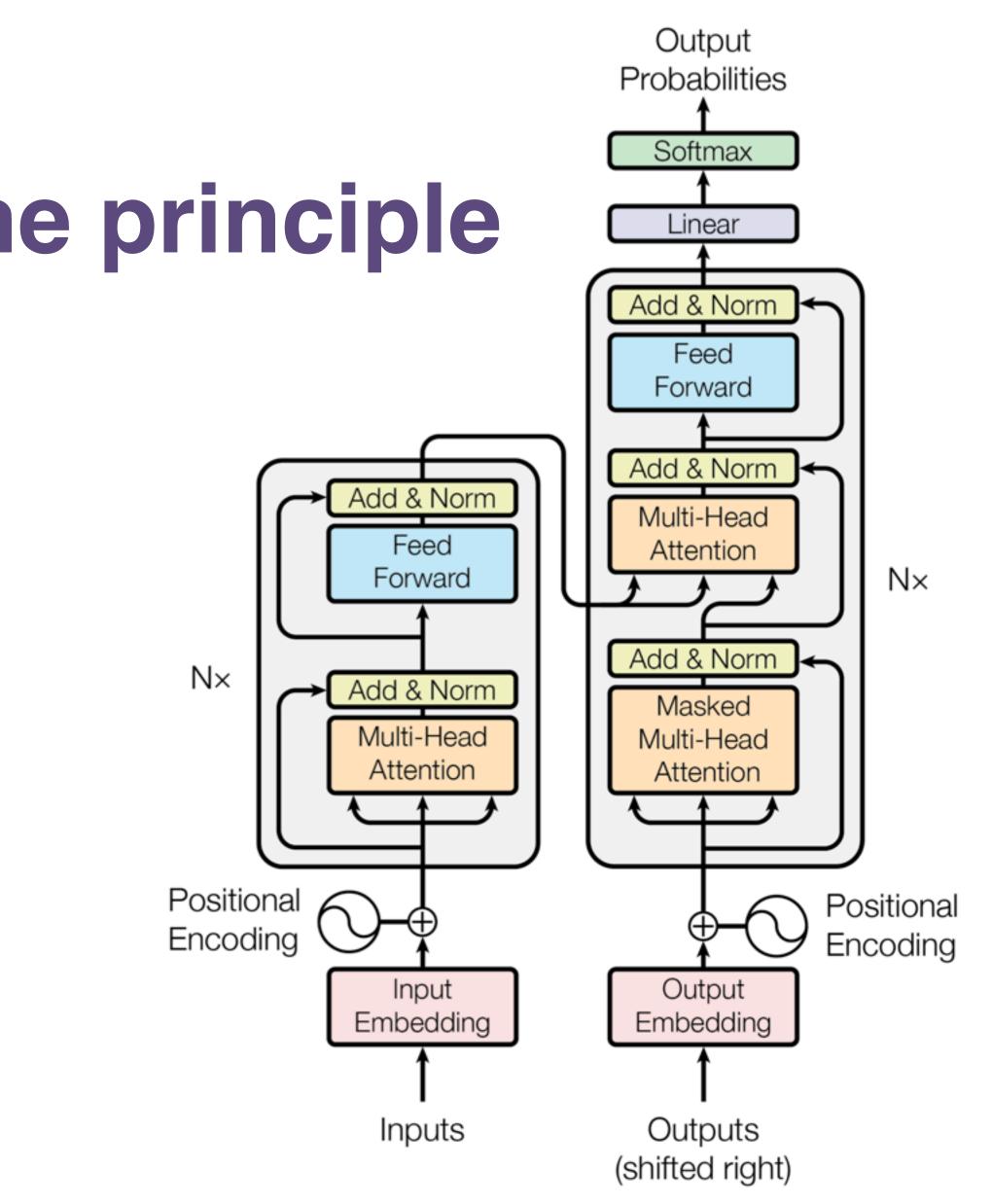


Figure 1: The Transformer - model architecture.

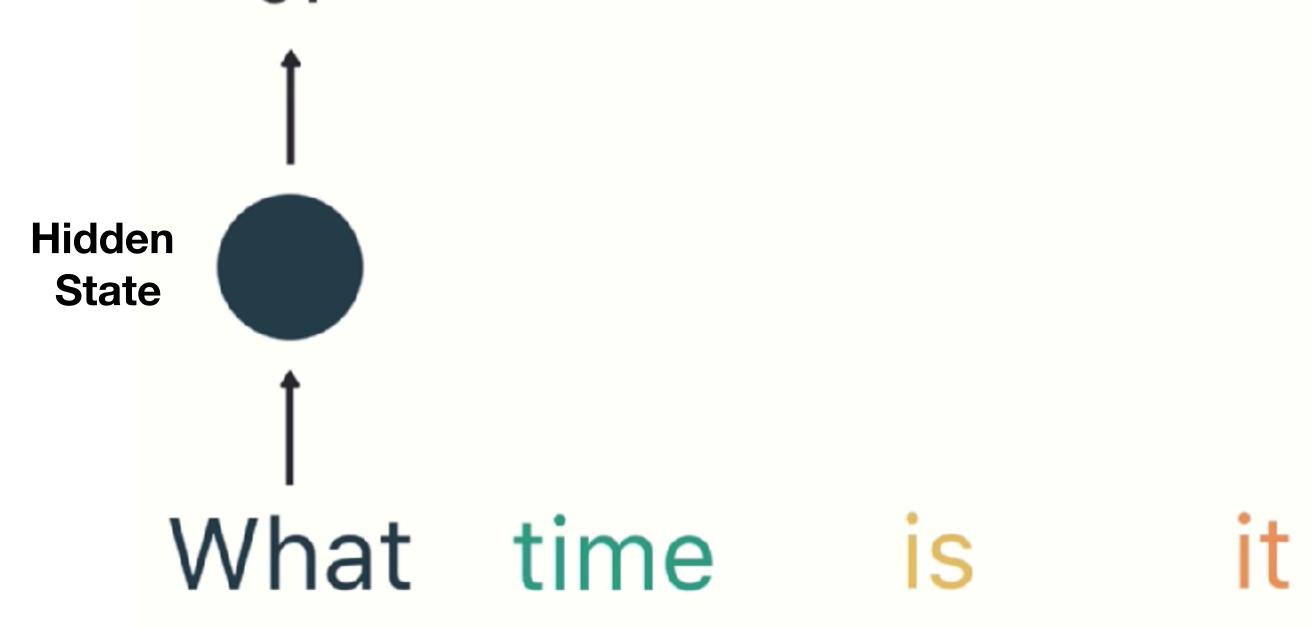
# Attention is Al You Need Level 3 E. Gross

Jay Alammar: The Illustrated Transformer Mehreen Saeed: Positional Encoding https://arxiv.org/abs/1706.03762

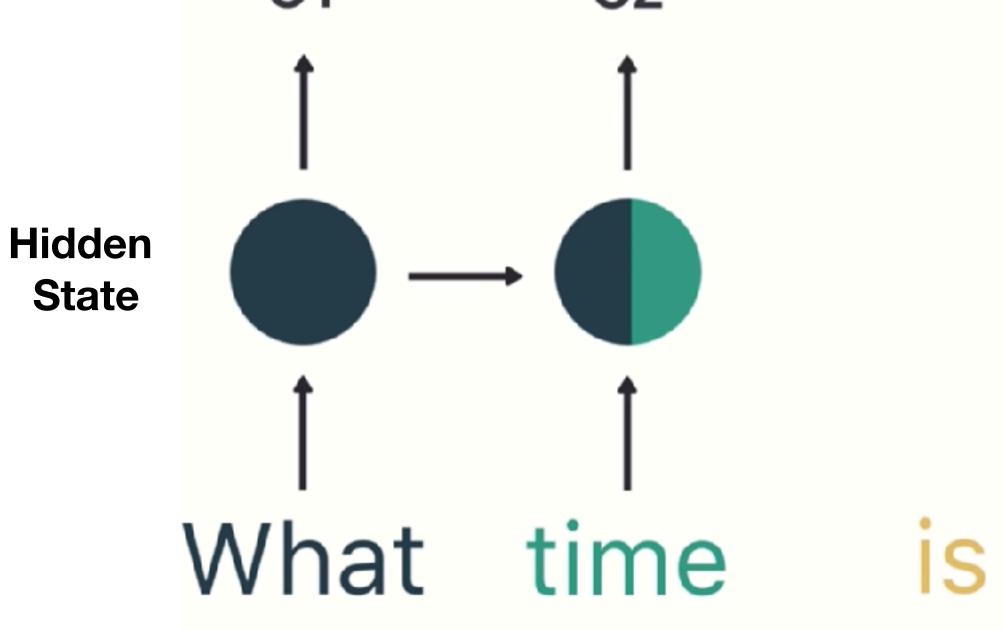
# RNN's are good at processing sequence data for predictions

https://www.youtube.com/watch?v=LHXXI4-IEns

- How do we do it?
- We use hidden states as memory (they represent information from all previous states)

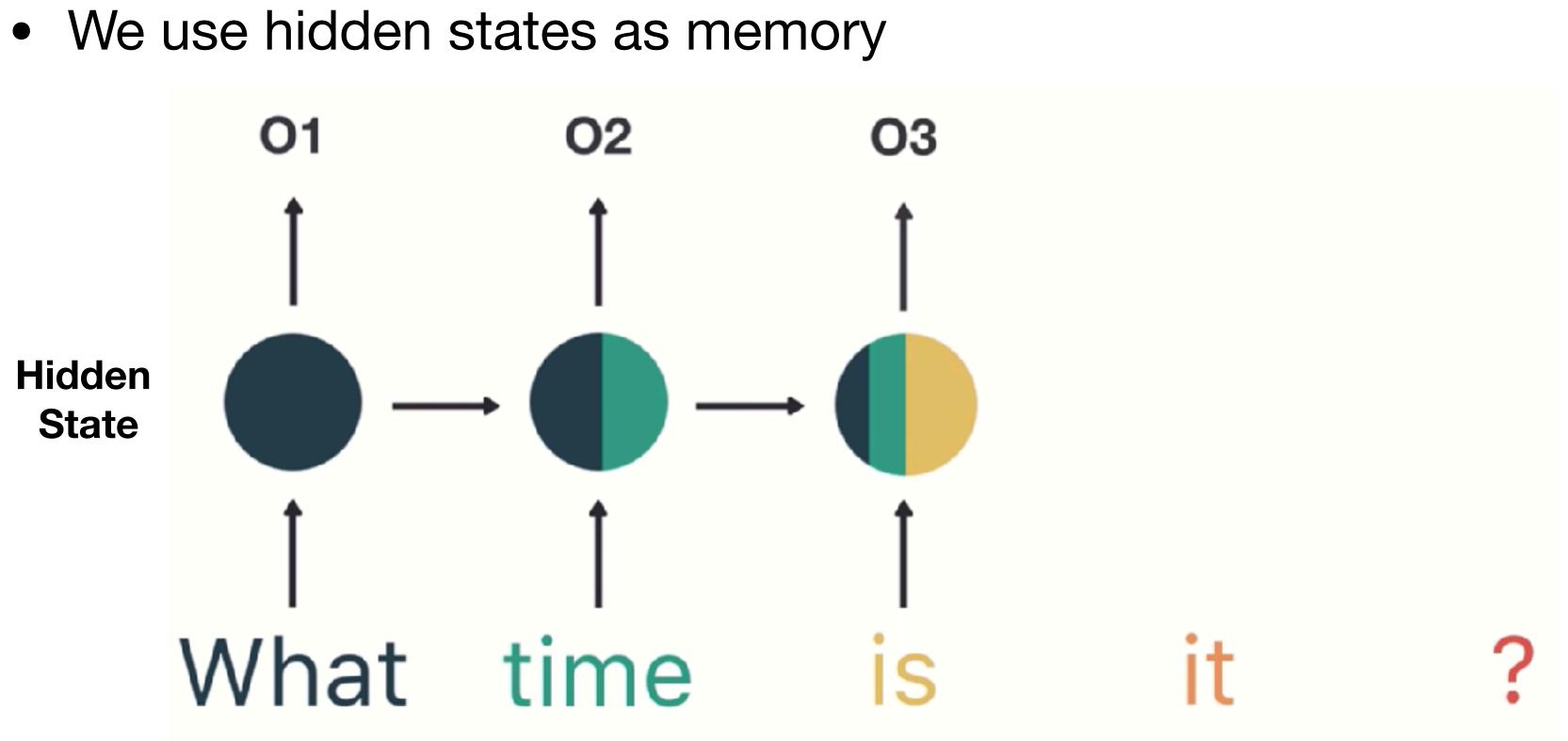


- How do we do it?
- We use hidden states as memory (they represent information from all previous states)



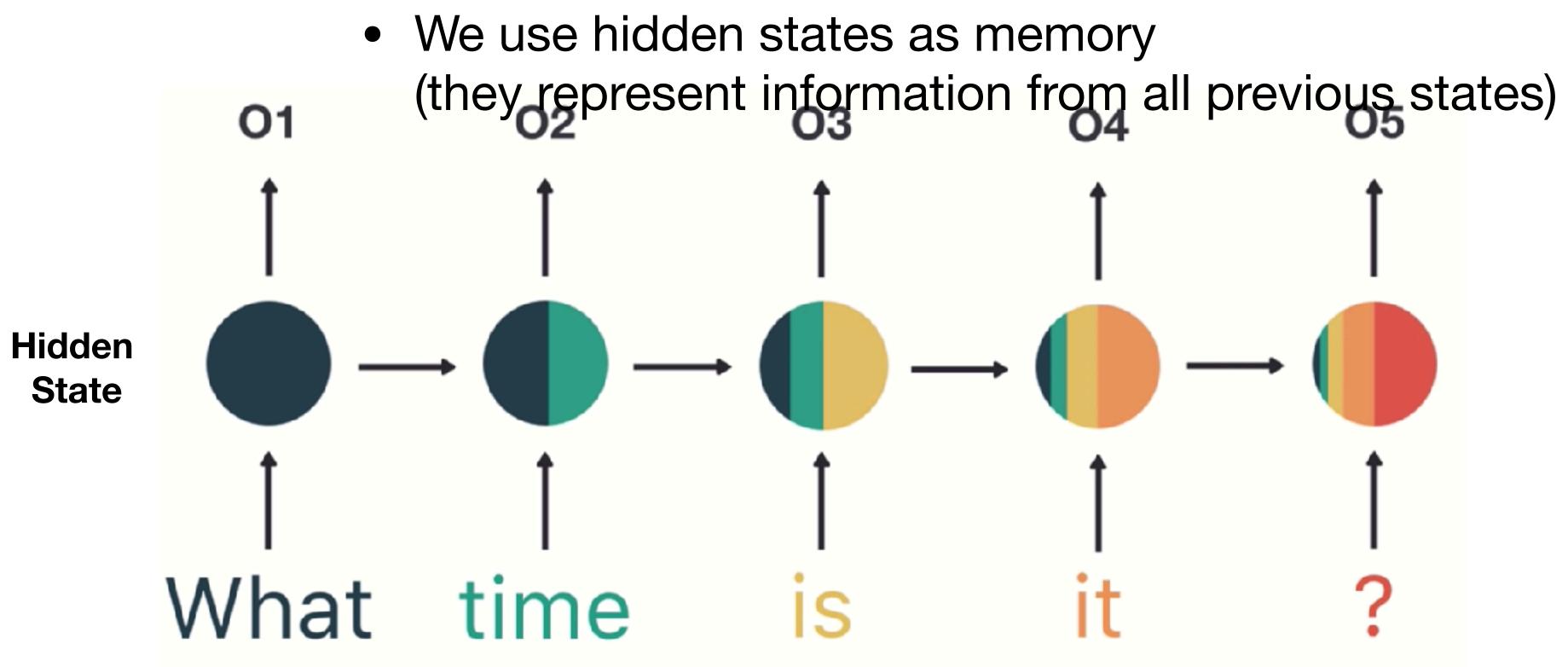
it

- How do we do it?

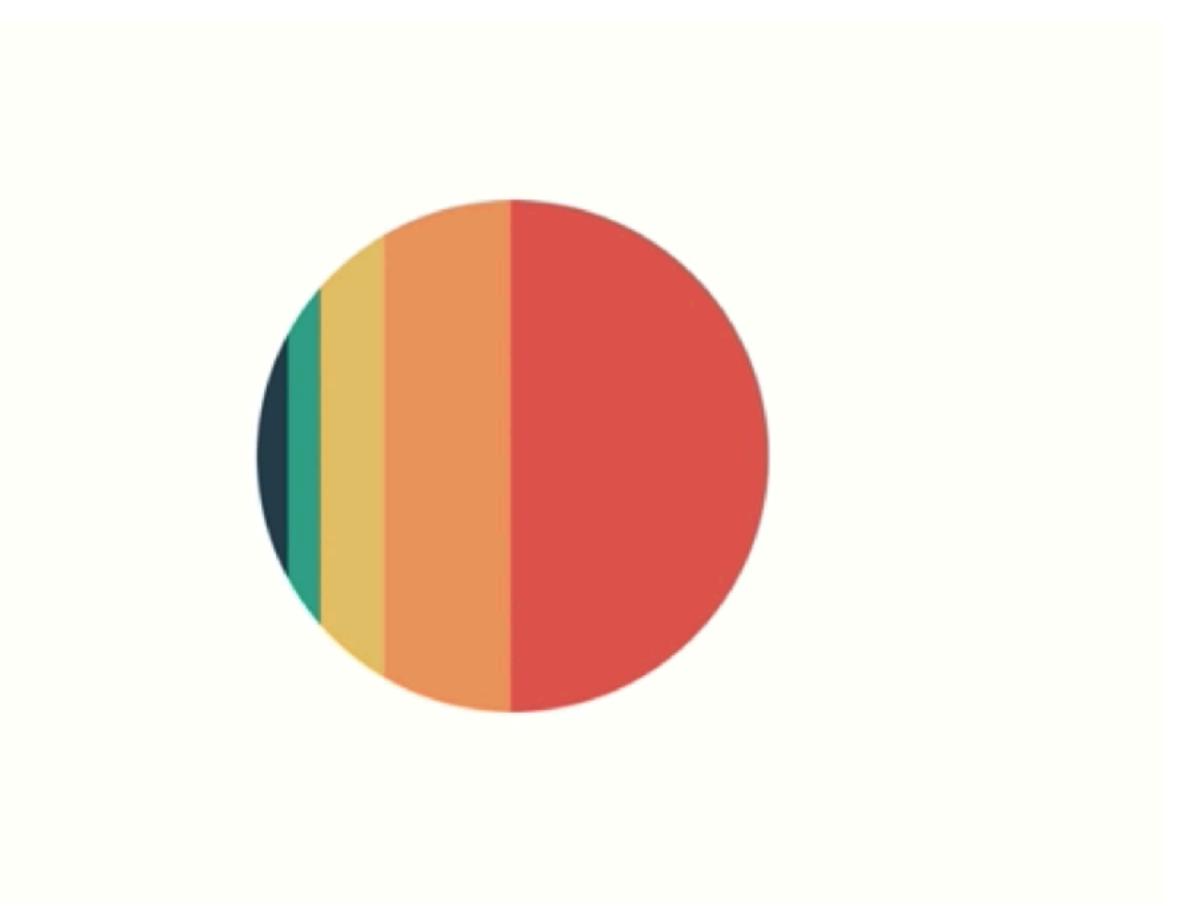


https://www.youtube.com/watch?v=LHXXI4-IEns

#### **Recurrent Neural Net in a NutShell** • How do we do it?



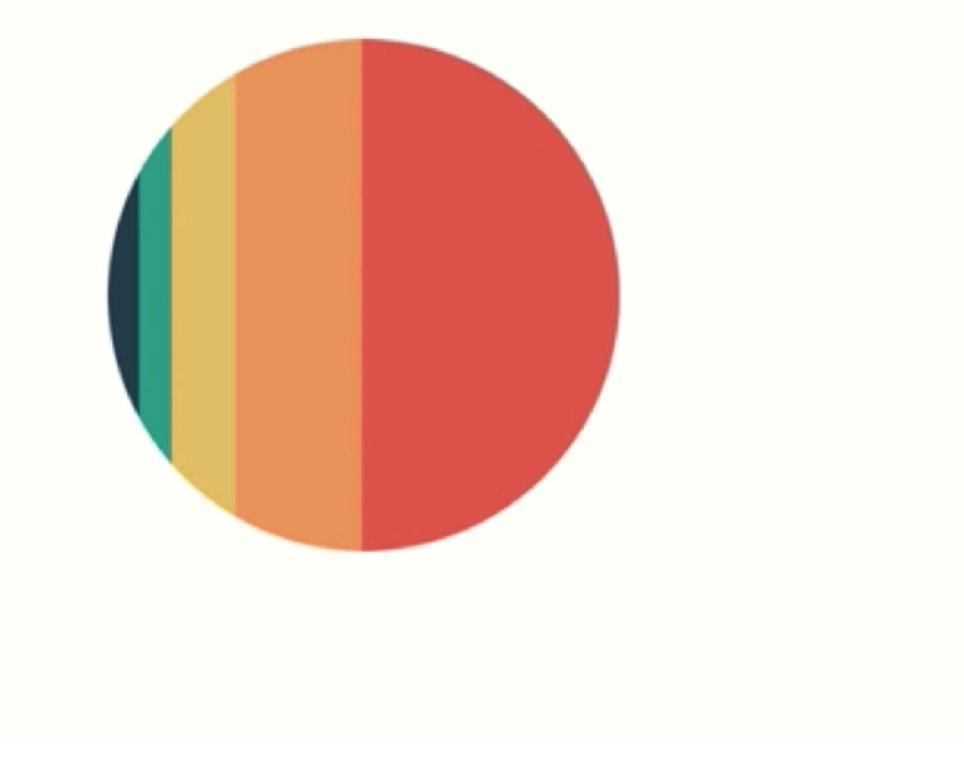
#### **Recurrent Neural Net in a NutShell** Issue of RNN with Short Time Memory



https://www.youtube.com/watch?v=LHXXI4-IEns

#### **Recurrent Neural Net in a NutShell** Issue of RNN with Short Time Memory

- Back propagation with time -> Vanishing Gradient We do not learn very early layers....



https://www.youtube.com/watch?v=LHXXI4-IEns

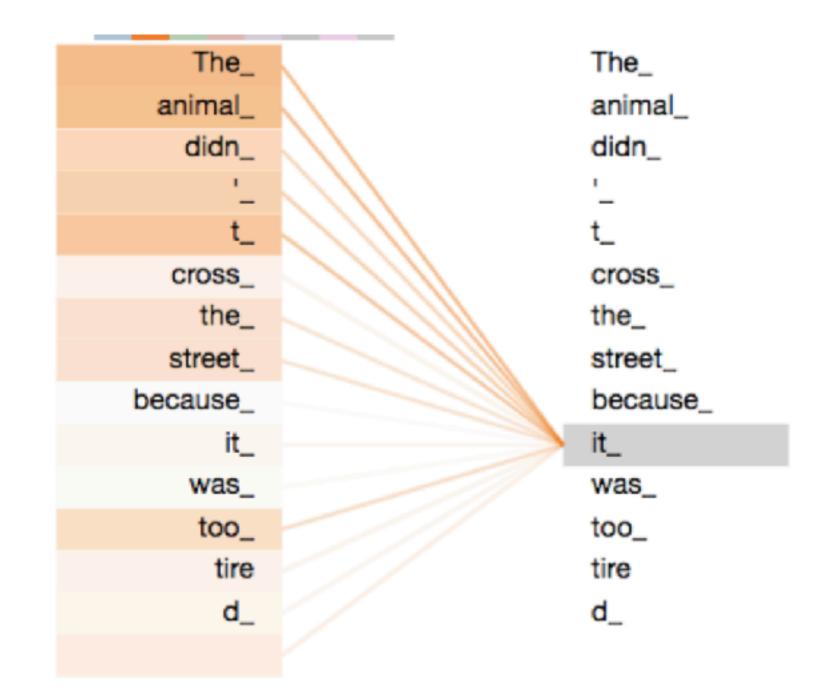
## **Transformer Keypoints**

- RNN: Seq to Seq Suffers from long term memory Transformer not sequential like RNN once
- Introduce the concept of Self Attention
- Multi Head Attention

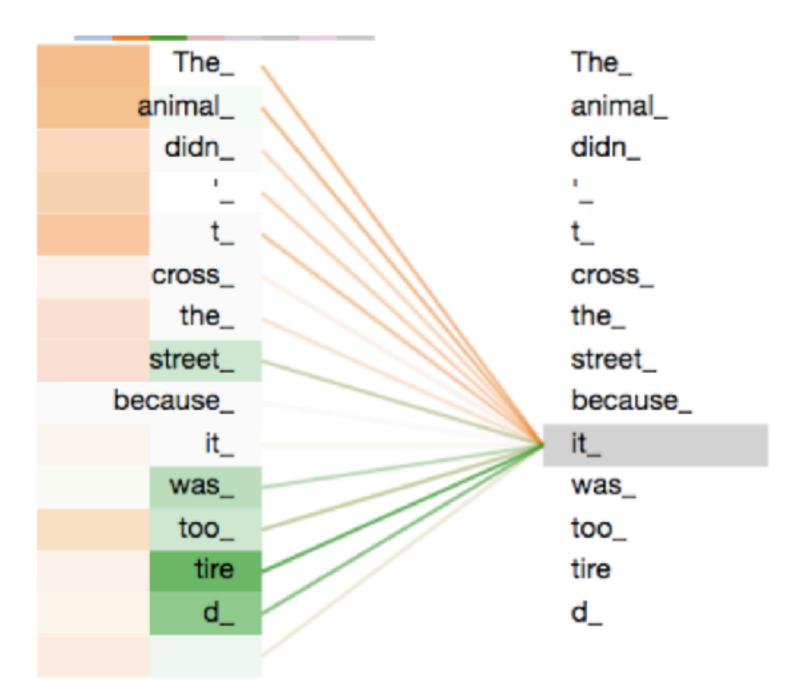
**God commanded Abraham** to sacrifice his son in order to test his faith

All input fed once through the model and calculation is performed

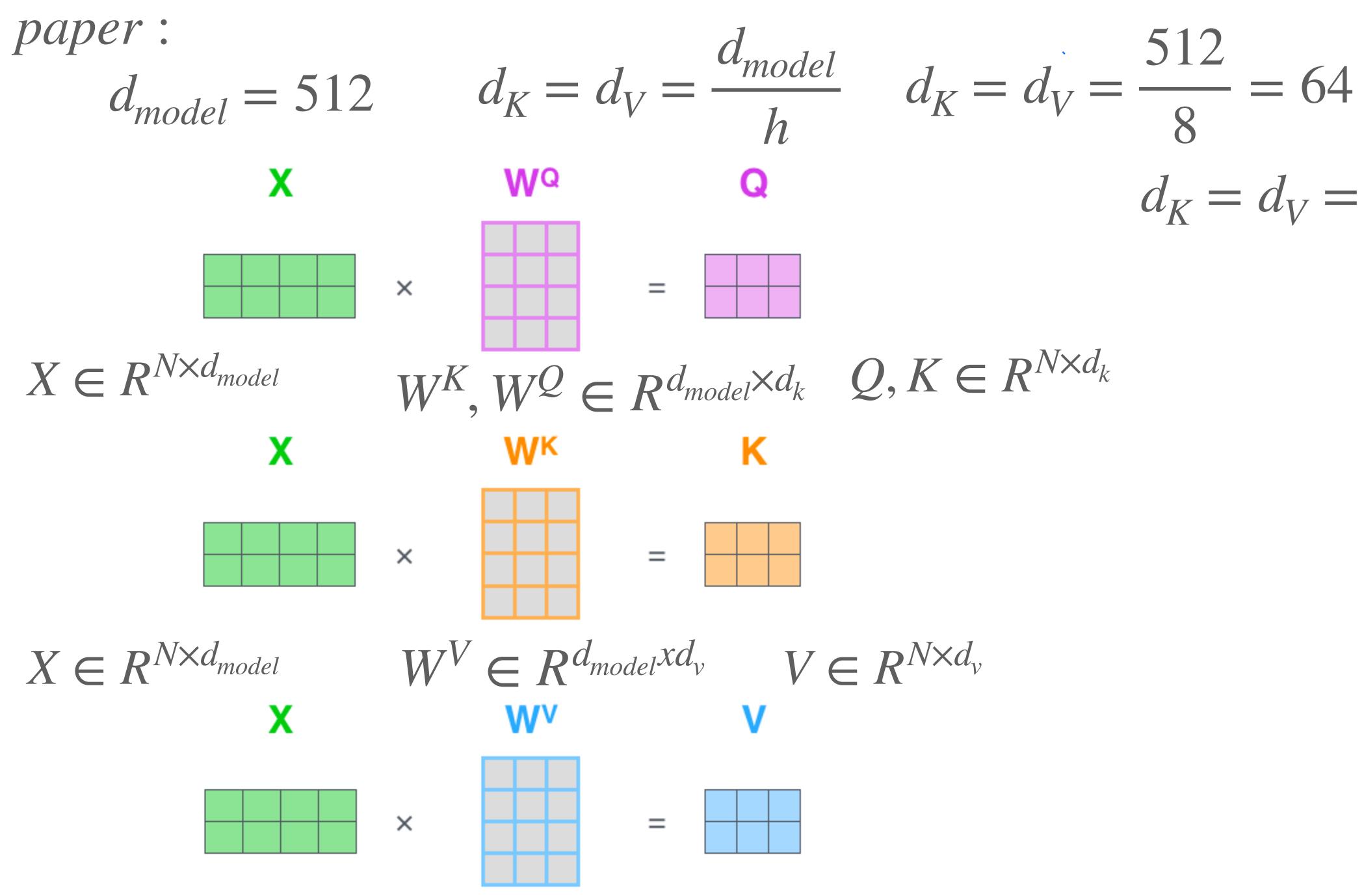
#### One Attention



http://jalammar.github.io/illustrated-transformer/

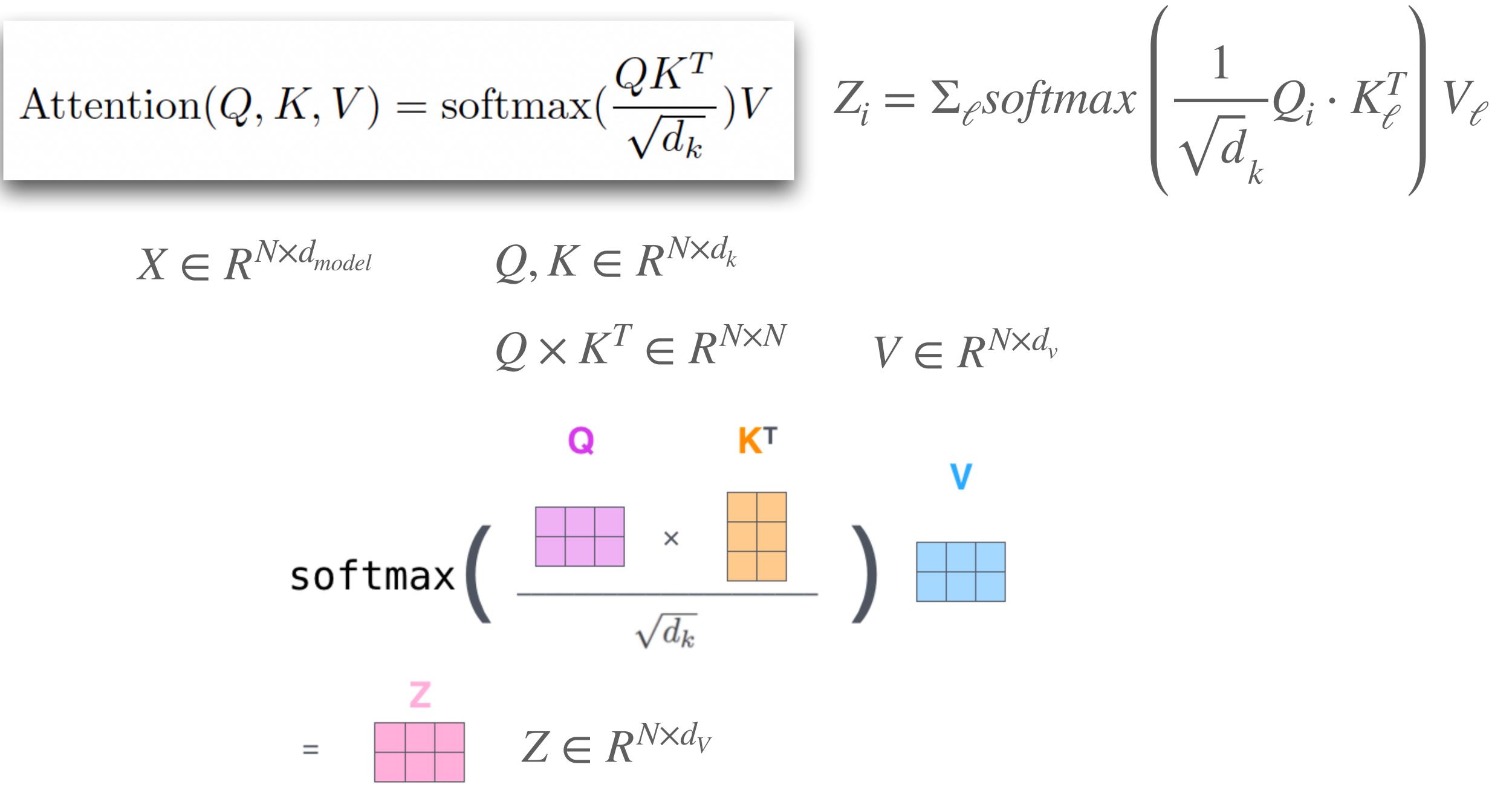


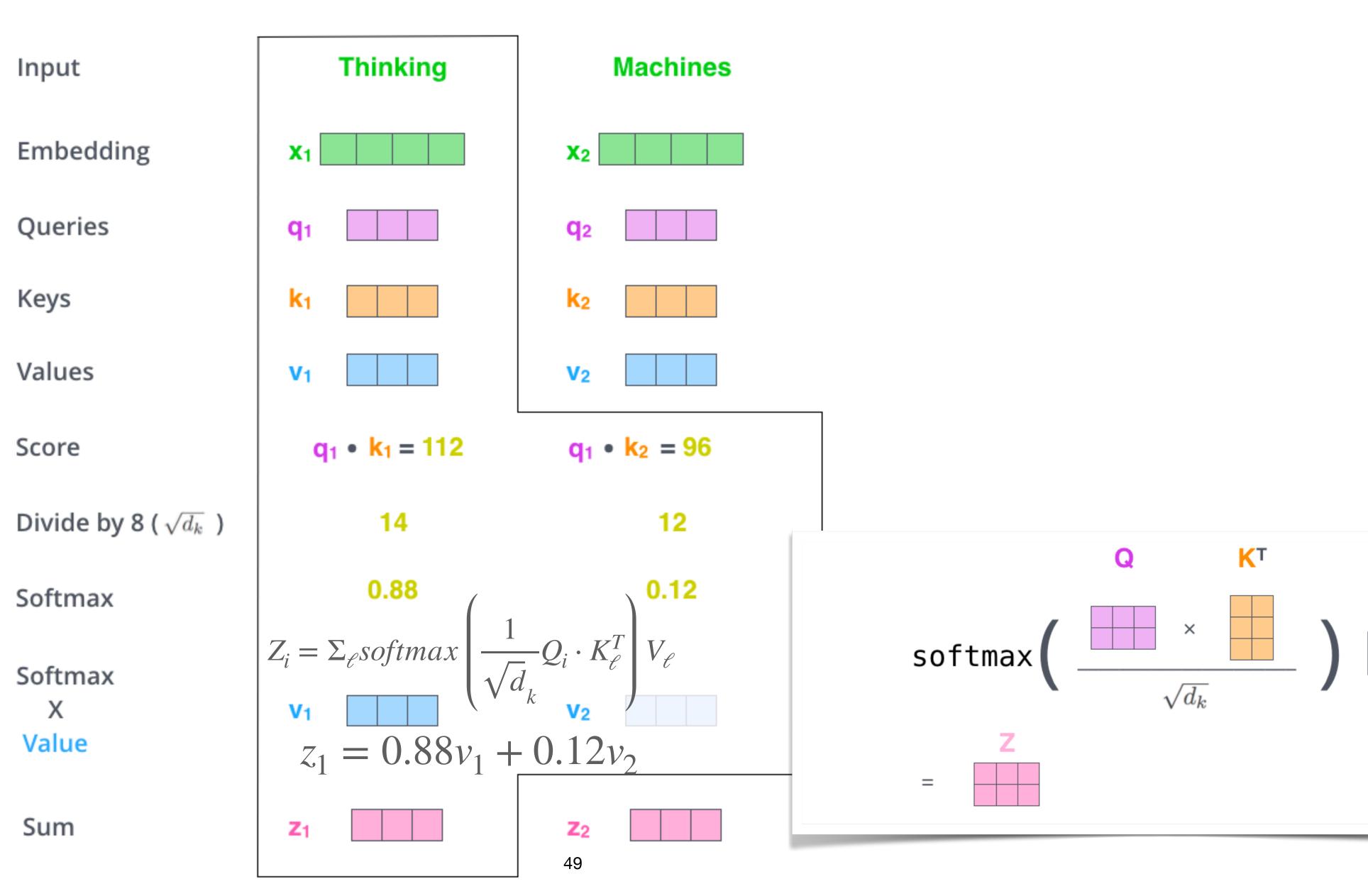
two Heads



 $d_{K} = d_{V} = \frac{d_{model}}{h}$ 









 $head_i = Attention(Q_i, K_i, V_i)$ 

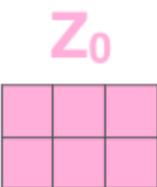
 $X \in R^{N \times d_{model}}$ 



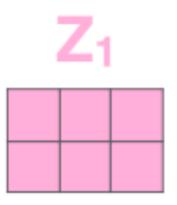
 $d_K = d_V = \frac{d_{model}}{h}$ 

ATTENTION HEAD #0

ATTENTION HEAD #1



 $Z \in R^{N \times d_V}$ 

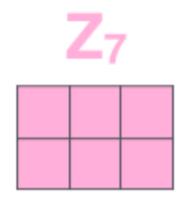


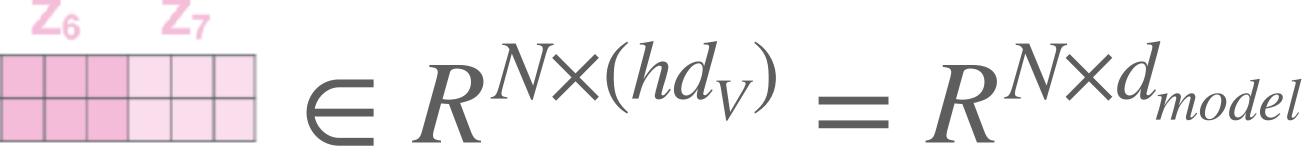
Z<sub>0</sub>  $Z_3 Z_4 Z_5 Z_6 Z_7$  $Z_2$ Z<sub>1</sub>  $Concat(head_1, ..., head_h)$ 

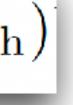
Calculating attention separately in eight different attention heads

...

ATTENTION HEAD #7



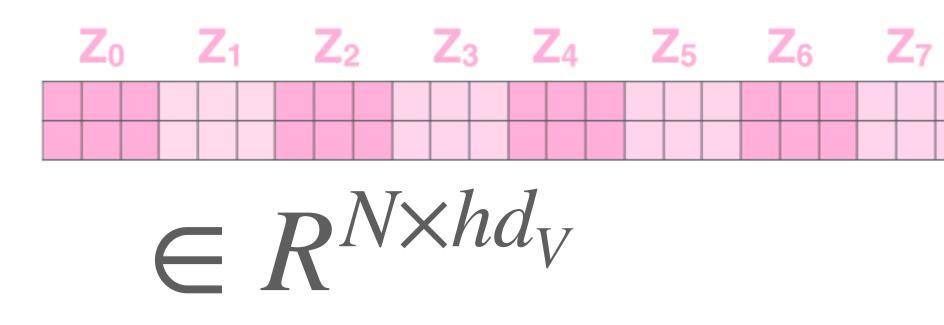






 $MultiHead(Q, K, V) = Concat(head_1, ..., head_h)W^O$ 

1) Concatenate all the attention heads



3) The result would be the Z matrix that captures information from all the attention heads. We can send this forward to the FFNN



2) Multiply with a weight matrix W<sup>o</sup> that was trained jointly with the model

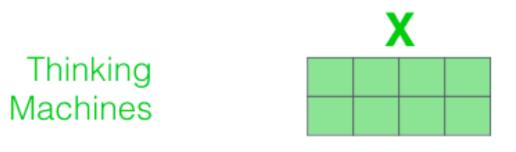
Х

 $W^{O} \in R^{hd_{V} \times d_{model}}$ 

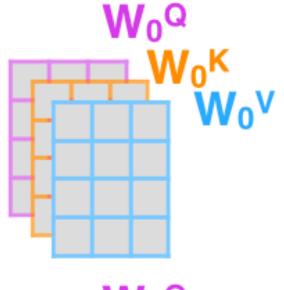
_	_	_	_	
_				
_				14/0
				Wo

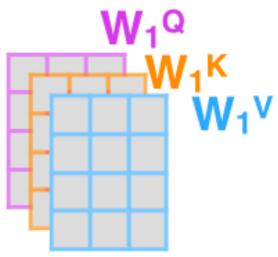
#### 1) This is our 2) We embed input sentence\* each word\*

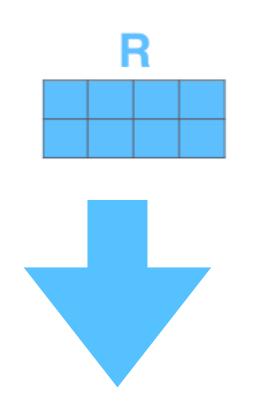
3) Split into 8 heads.
We multiply X or
R with weight matrices

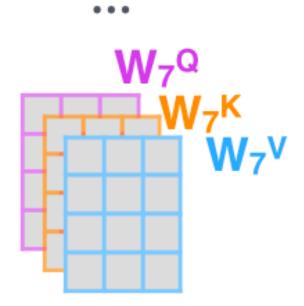


\* In all encoders other than #0, we don't need embedding. We start directly with the output of the encoder right below this one



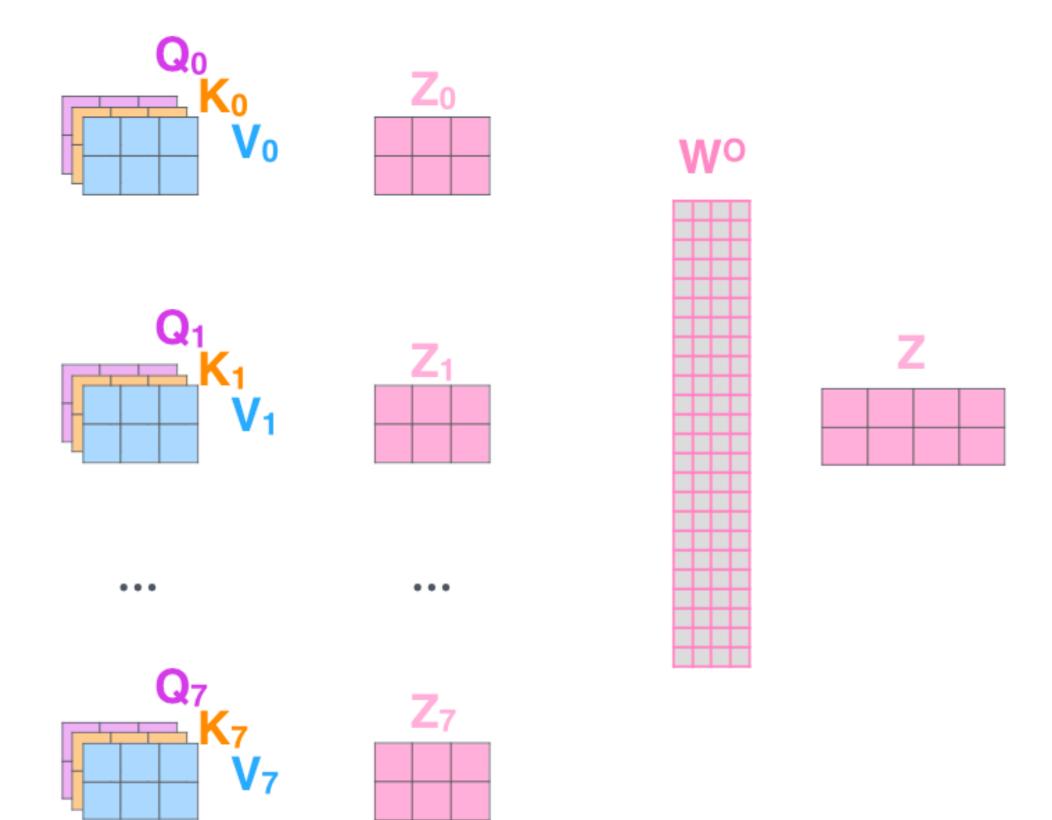


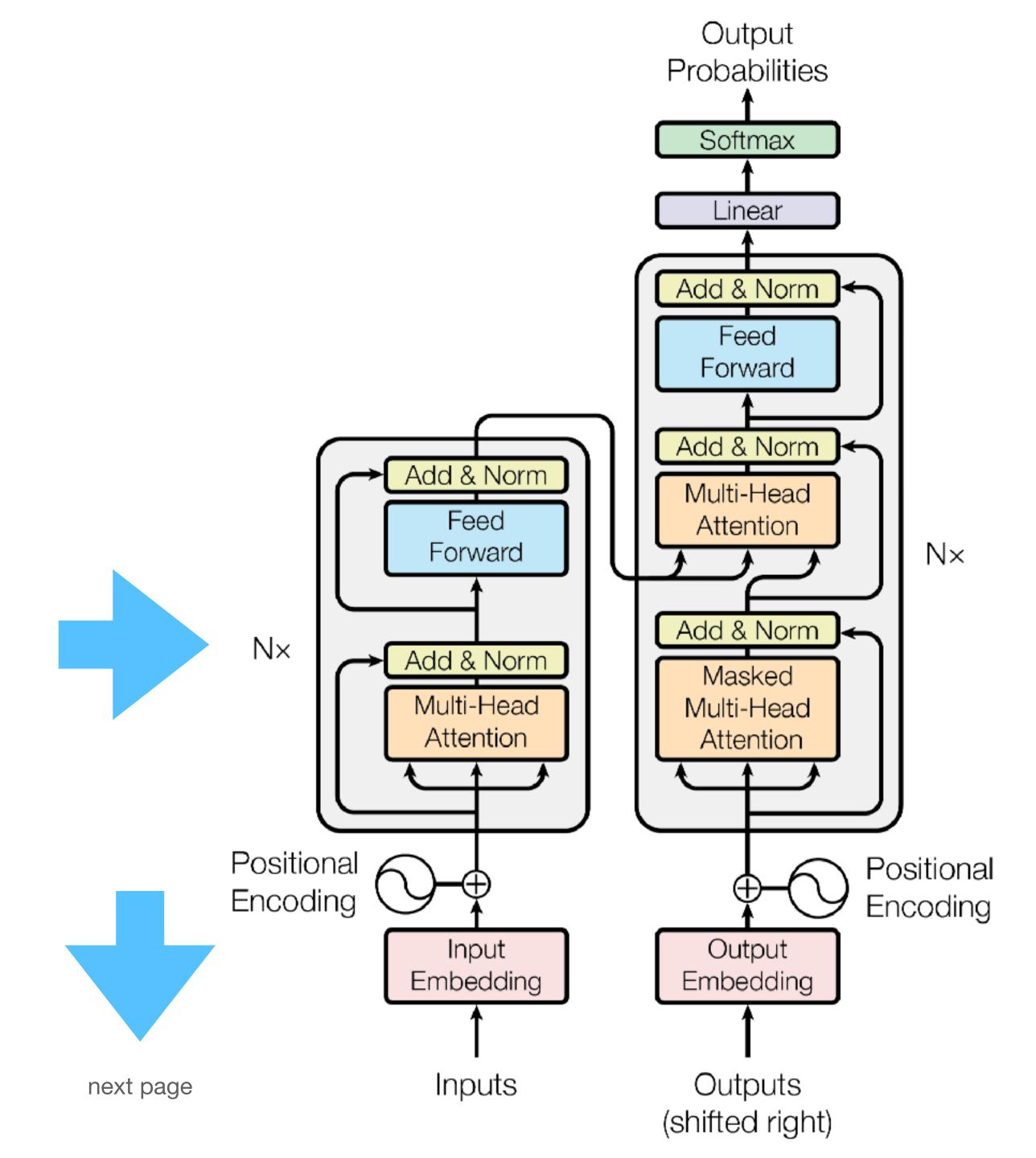


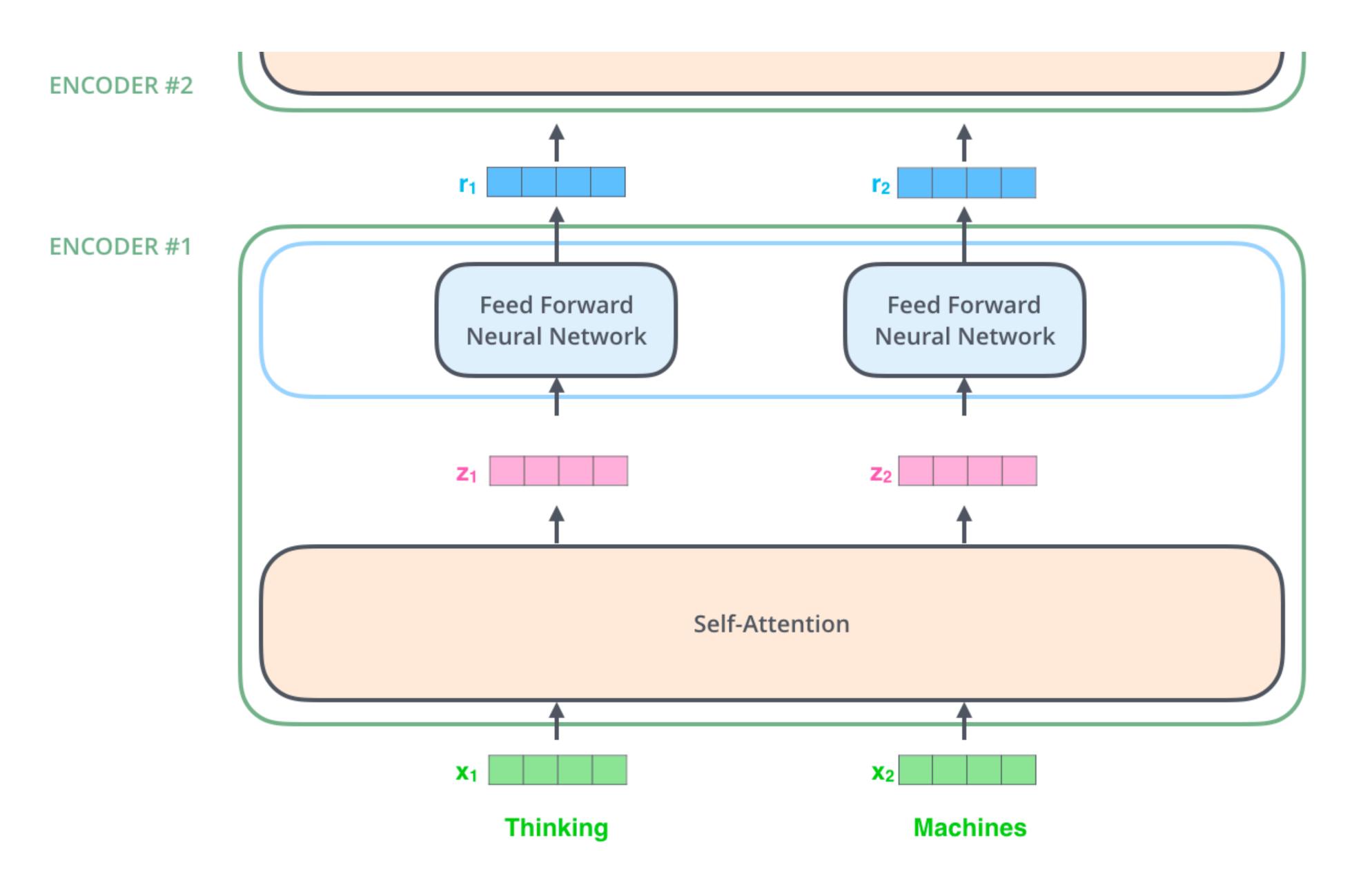


next page

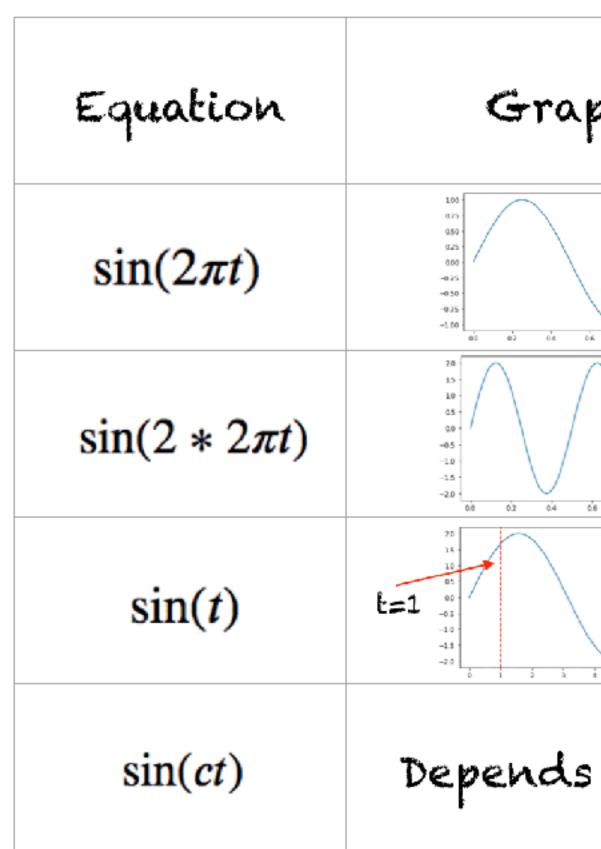
4) Calculate attention using the resulting Q/K/V matrices 5) Concatenate the resulting Z matrices, then multiply with weight matrix W<sup>O</sup> to produce the output of the layer







#### Sequence Length = L Varies 2i=0,....,L

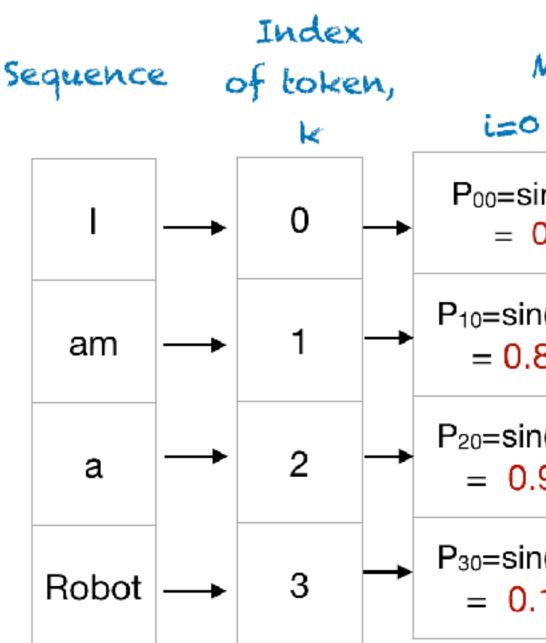


 $PE_{(pos,2i)} = sin(pos/10000^{2i/d_{model}})$  $PE_{(pos,2i+1)} = cos(pos/10000^{2i/d_{model}})$ 

ph	Frequency	Wavelength
	1	1
06 08 10	2	1/2
	1/2π	2π
s on c	c/2 <i>π</i>	2 <i>π</i> /c

https://machinelearningmastery.com/a-gentle-introduction-to-positional-encoding-in-transformer-models-part-1/

Sequence Length = L Varies 2i=0,....,d\_model



https://machinelearningmastery.com/a-gentle-introduction-to-positional-encoding-in-transformer-models-part-1/

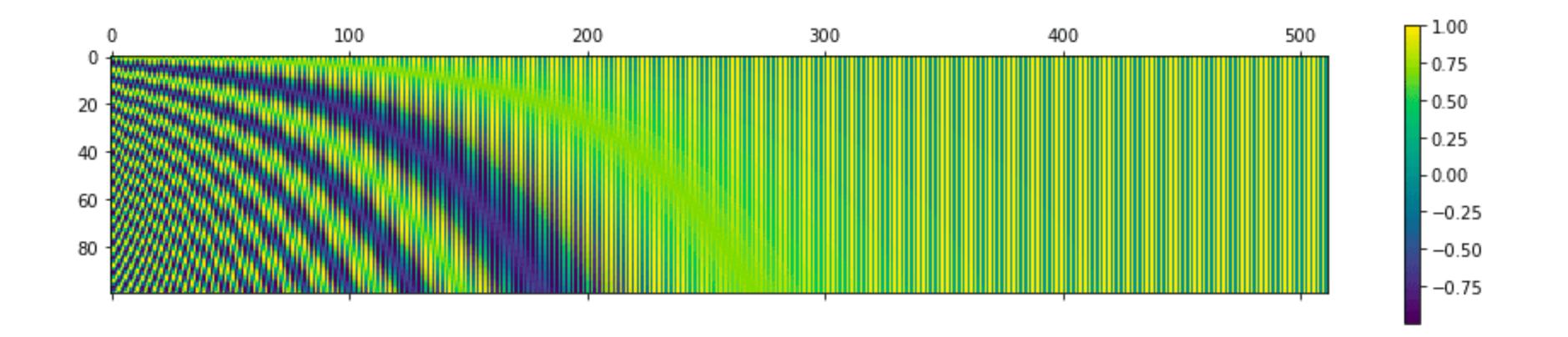
 $PE_{(pos,2i)} = sin(pos/10000^{2i/d_{model}})$  $PE_{(pos,2i+1)} = cos(pos/10000^{2i/d_{model}})$ 

Positional Encoding Matrix with d=4, n=100

>	i=0	i=1	i=1
in(0)	P <sub>01</sub> =cos(0)	P <sub>02</sub> =sin(0)	P <sub>03</sub> =cos(0)
<mark>0</mark>	= 1	= 0	= 1
n(1/ <b>1</b> )	$P_{11}=\cos(1/1)$	$P_{12}=sin(1/10)$	$P_{13}=\cos(1/10)$
<mark>84</mark>	= 0.54	= 0.10	= 1.0
n(2/1)	P <sub>21</sub> =cos(2/1)	P <sub>22</sub> =sin(2/10)	$P_{23}=\cos(2/10)$
. <mark>91</mark>	= -0.42	= 0.20	= 0.98
n(3/ <b>1</b> )	P <sub>31</sub> =cos(3/1)	$P_{32} = sin(3/10)$	P <sub>33</sub> =cos(3/10)
.14	= -0.99	= 0.30	= 0.96

#### Positional Encoding Matrix for the sequence 'I am a robot'

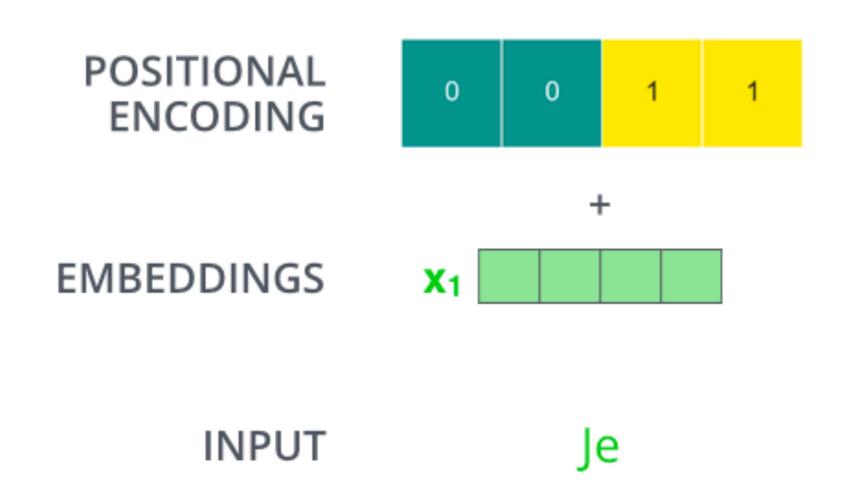
## Sequence Length = L Varies $2i=0,...,d_model$



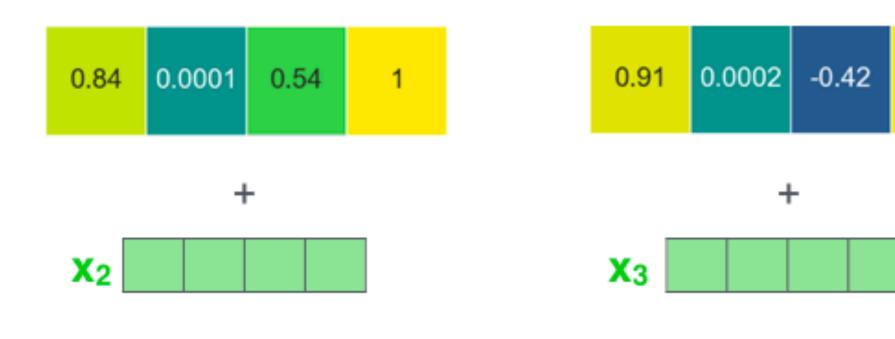
The positional encoding matrix for n=10,000, d=512, sequence length=100

https://machinelearningmastery.com/a-gentle-introduction-to-positional-encoding-in-transformer-models-part-1/

 $PE_{(pos,2i)} = sin(pos/10000^{2i/d_{model}})$  $PE_{(pos,2i+1)} = cos(pos/10000^{2i/d_{model}})$ 



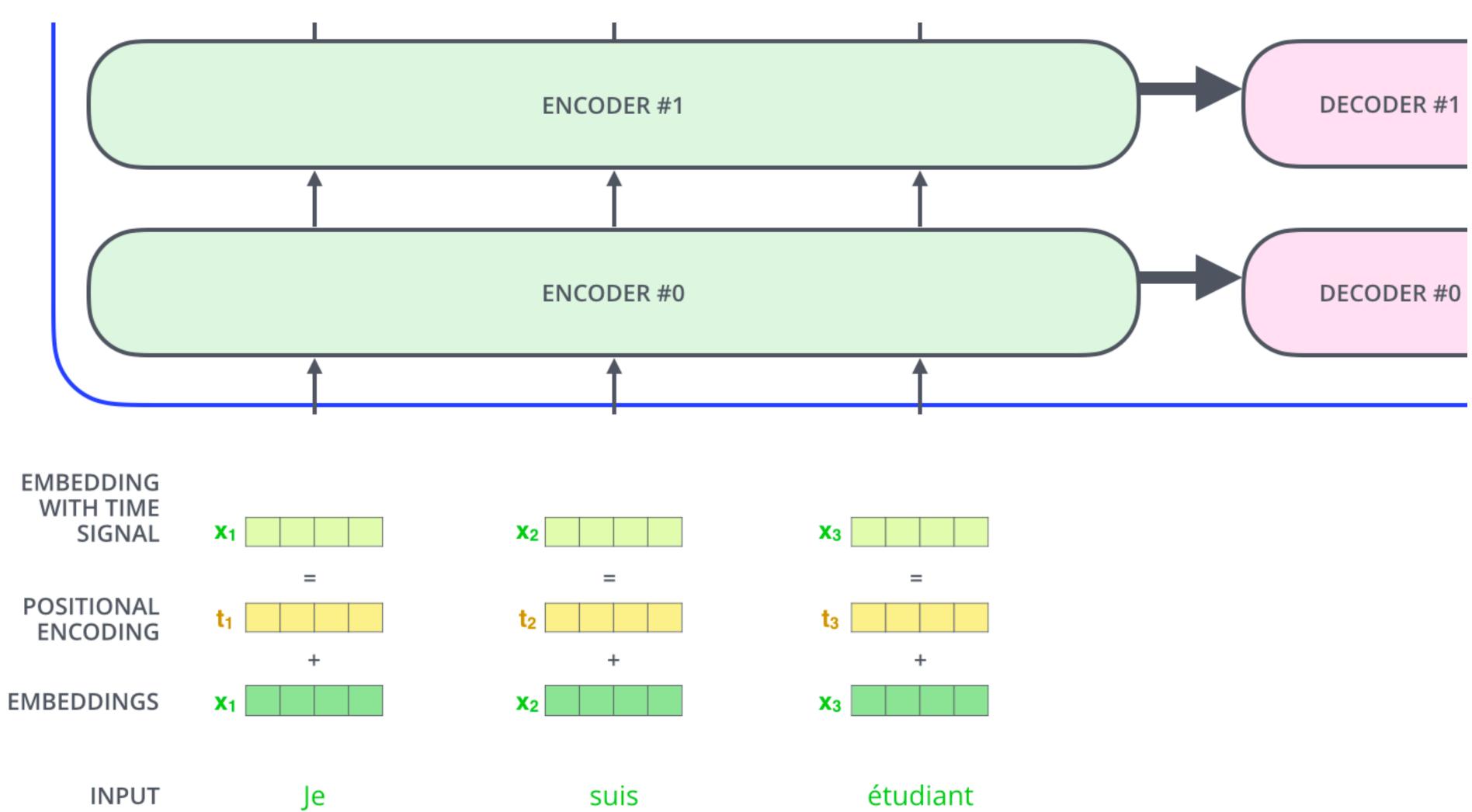




suis

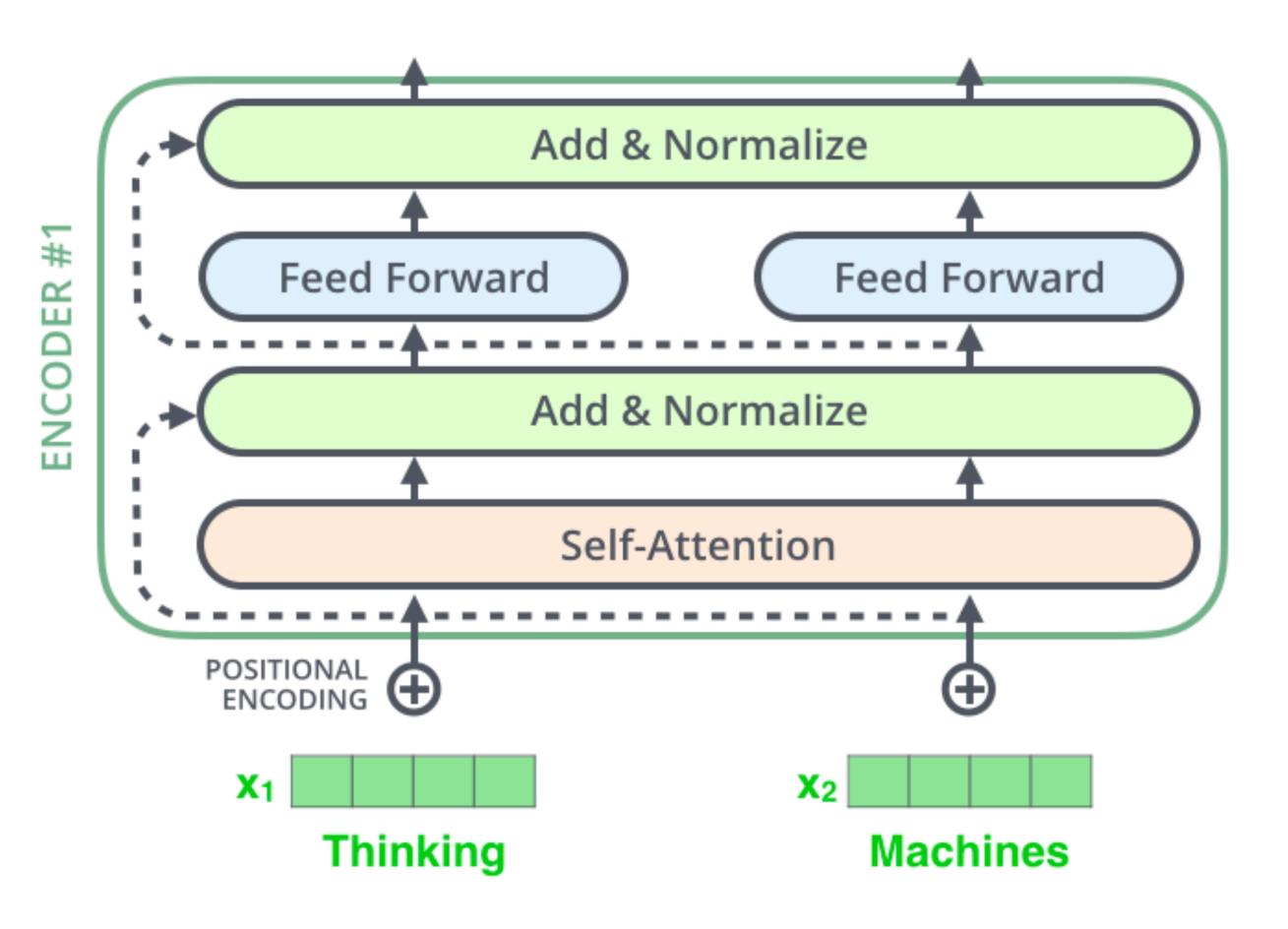
étudiant

1

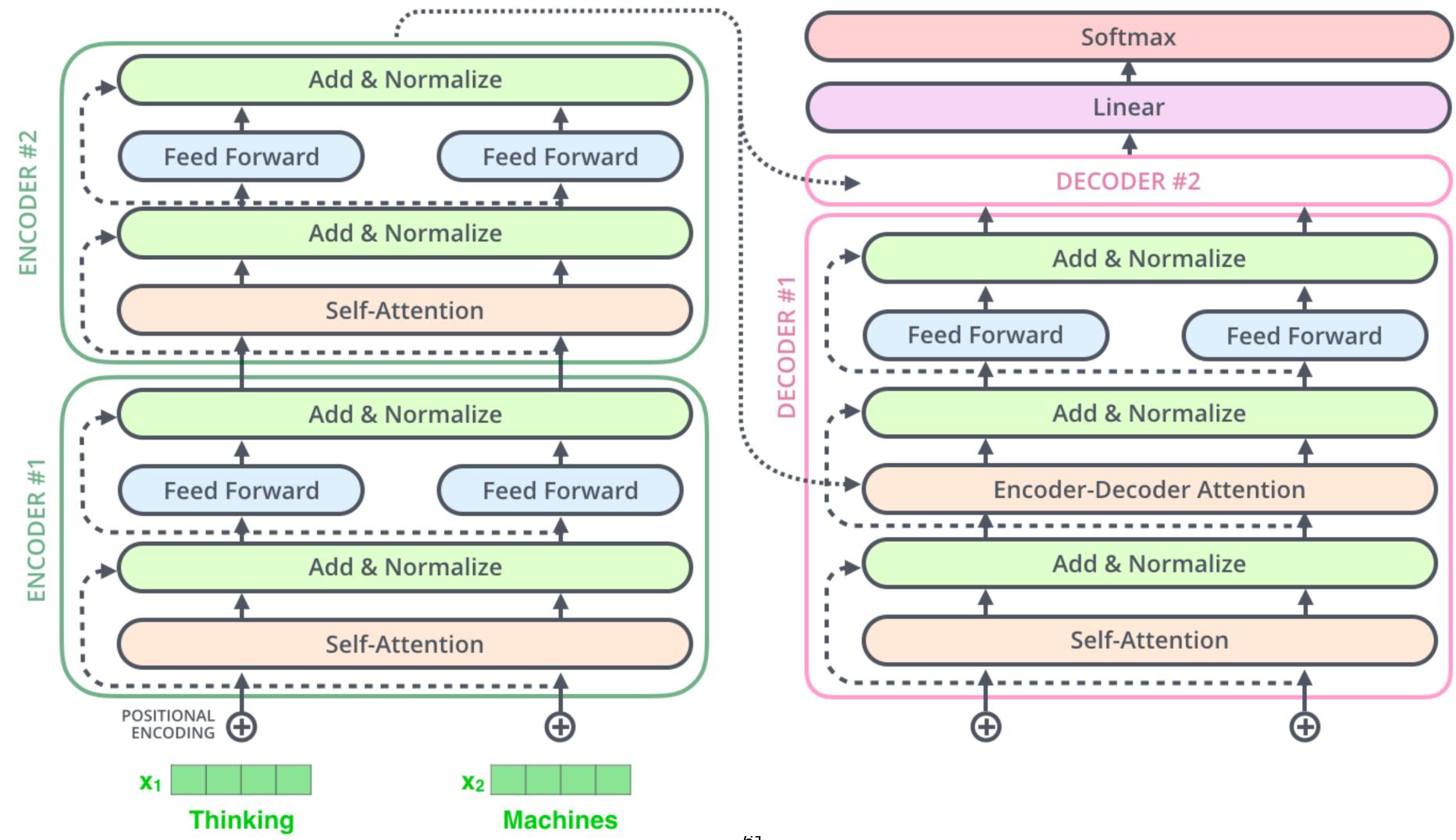


étudiant

## **Residual Net**

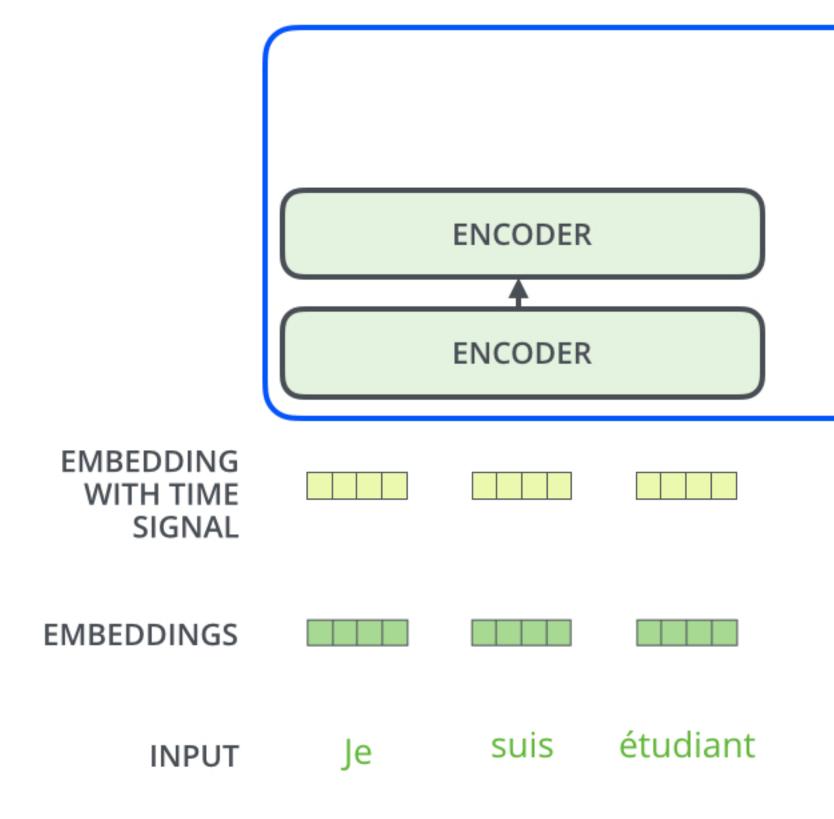


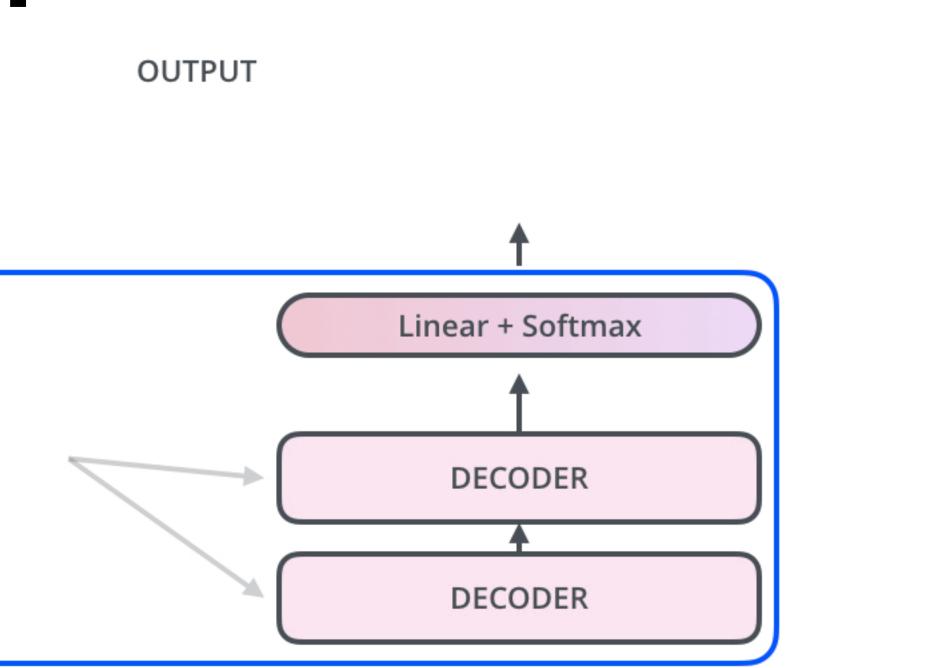
## **Stack 6 Encoders & Decoders**



## **Cross Attention**

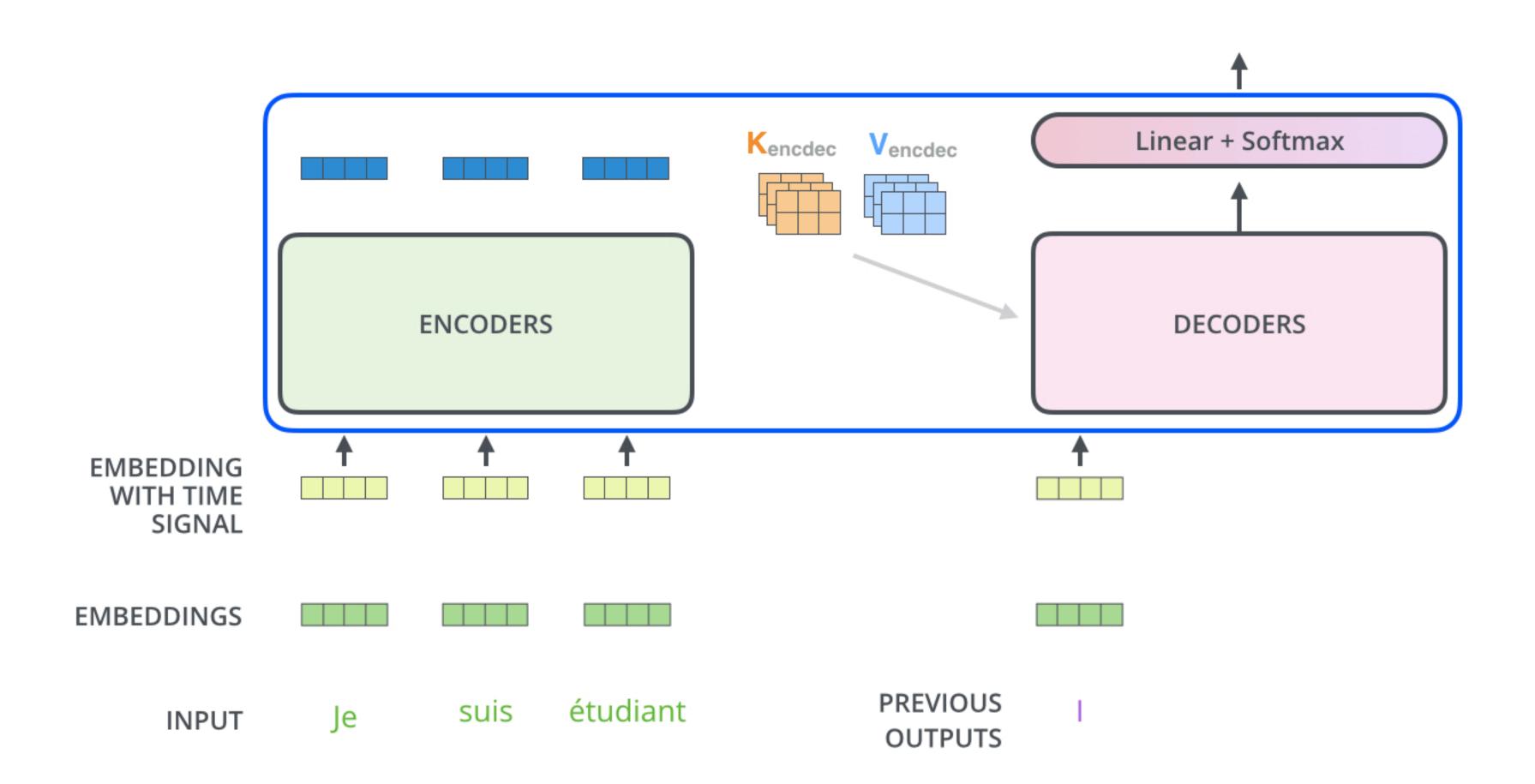
Decoding time step: 1 2 3 4 5 6





## Decoder

Decoding time step: 1 2 3 4 5 6



#### OUTPUT

## Softmax

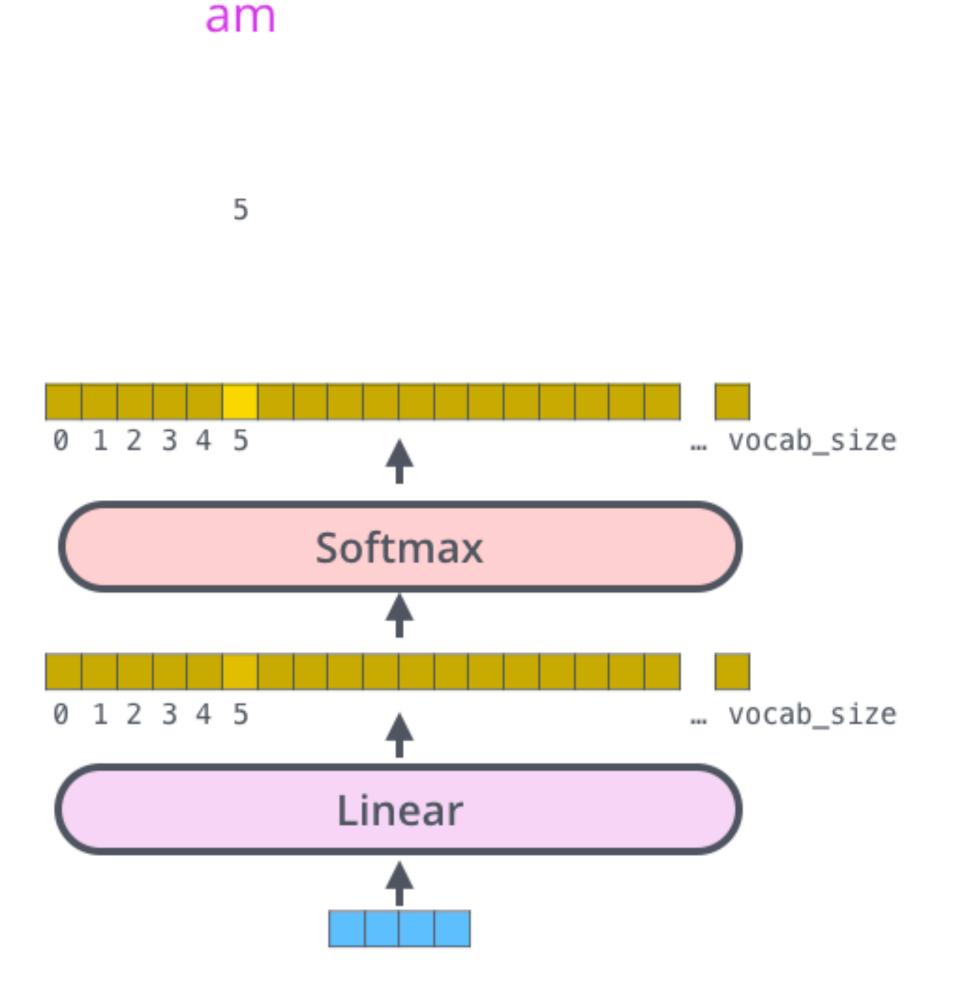
Which word in our vocabulary is associated with this index?

Get the index of the cell with the highest value (argmax)

log\_probs

logits

Decoder stack output





### End of Lecture 2

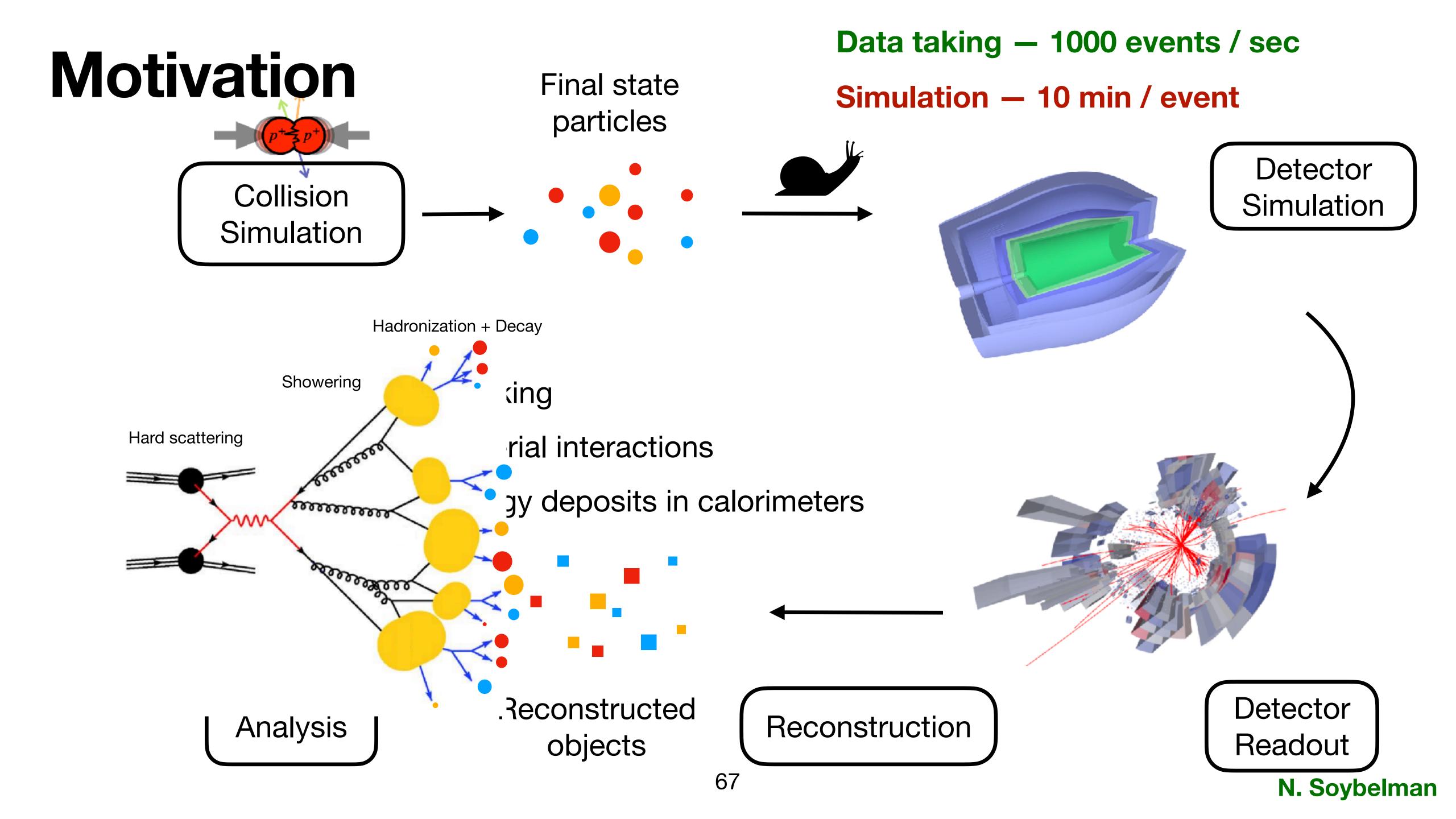
### **Fast Simulation for Particle** Reconstruction with GNN and Slot Attention

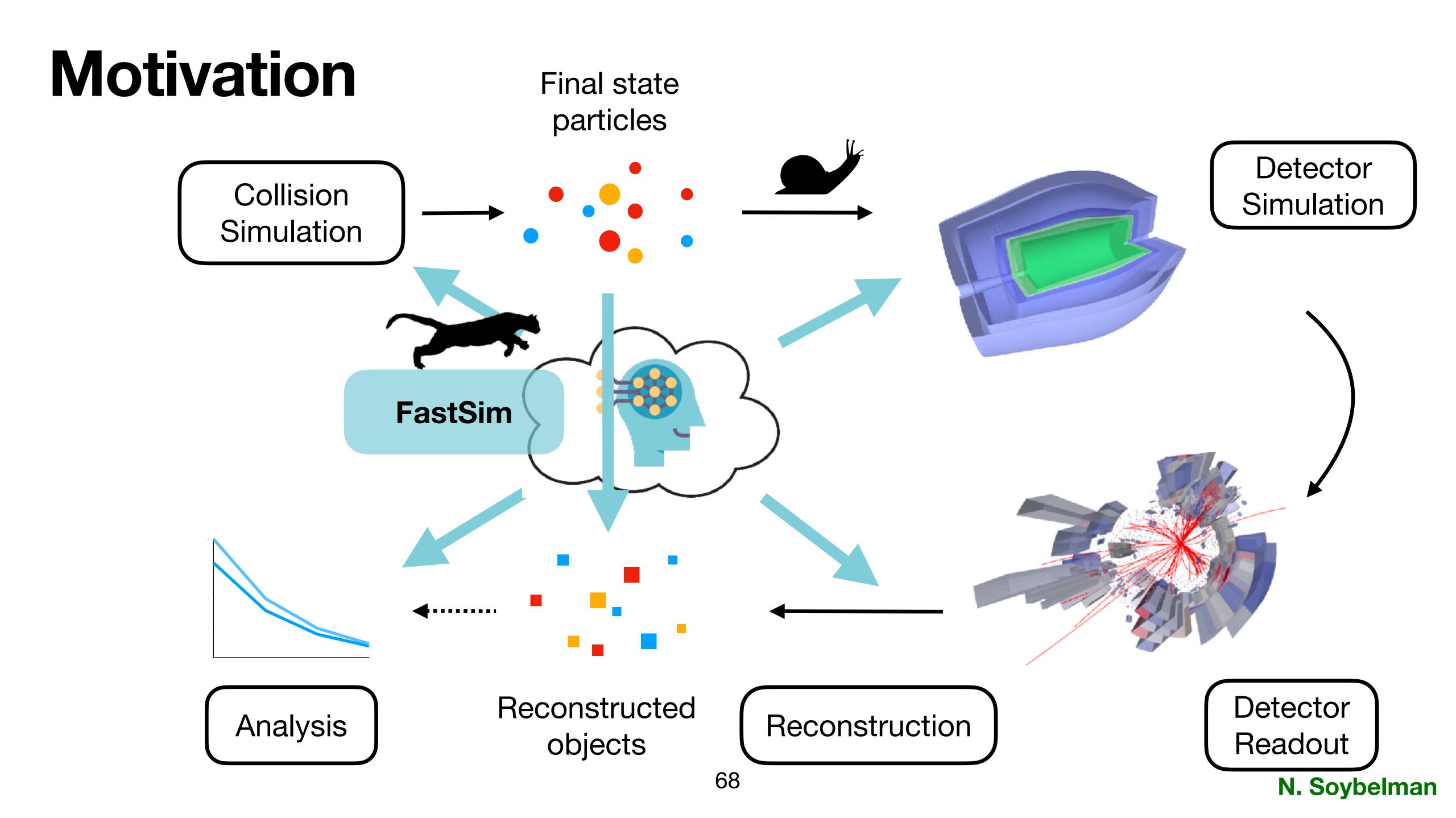
#### **Conditional Generative Modelling of Reconstructed Particles at Collider Experiments**

#### Jonathan Shlomi<sup>2</sup>, <u>Nathalie Soybelman<sup>2</sup></u>

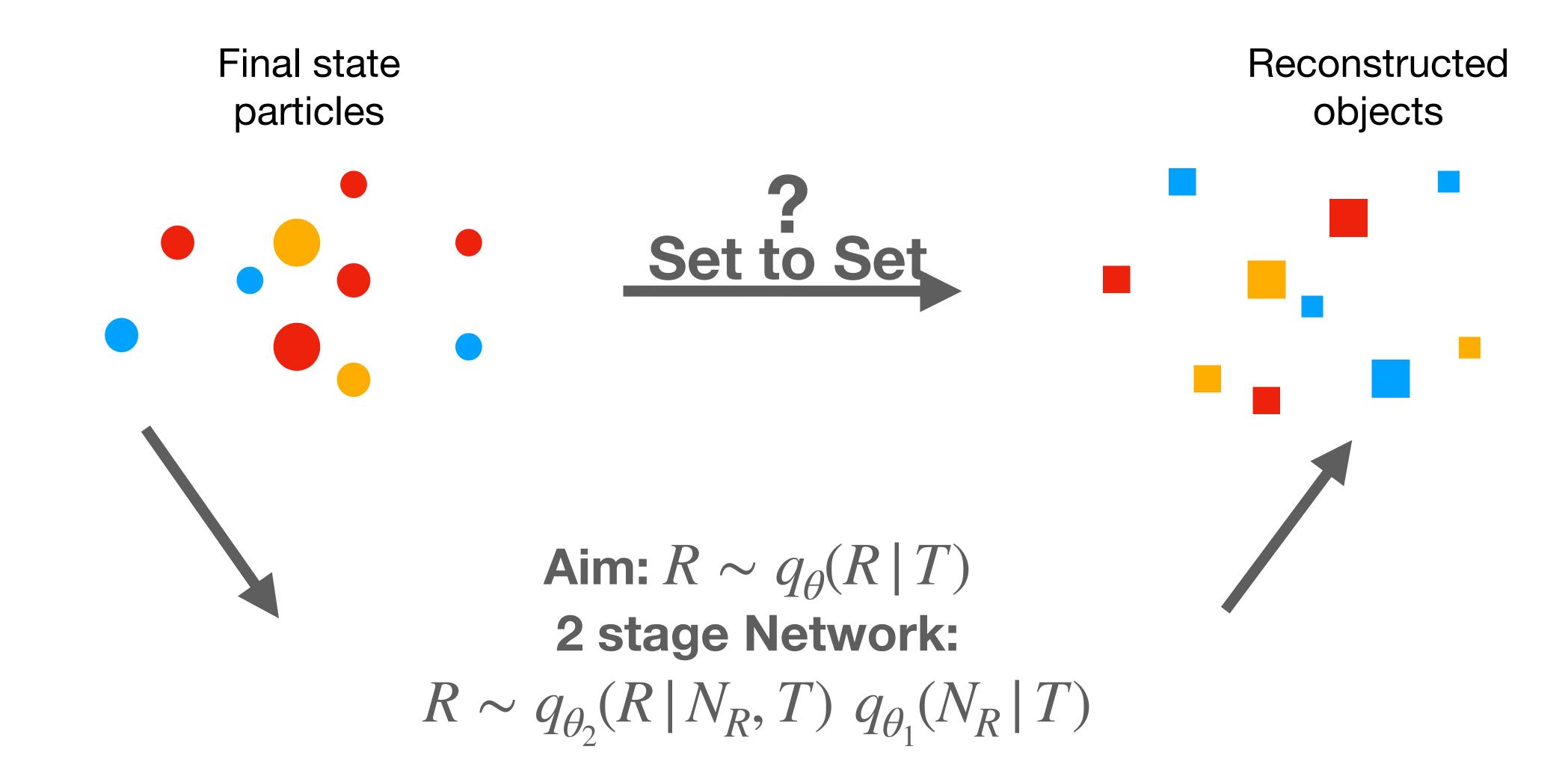
- University of Genova
- <sup>2</sup> Weizmann Institue of Science
- <sup>3</sup> ICEPP, University of Tokyo
- <sup>4</sup> Technical University of Munich
- <sup>5</sup> Sapienza University of Rome

Francesco Armando Di Bello<sup>1</sup>, Etienne Dreyer<sup>2</sup>, Sanmay Ganguly<sup>3</sup>, Eilam Gross<sup>2</sup>, Lukas Heinrich<sup>4</sup>, Marumi Kado<sup>4,5</sup>, Nilotpal Kakati<sup>2</sup>,





## Problem to solve

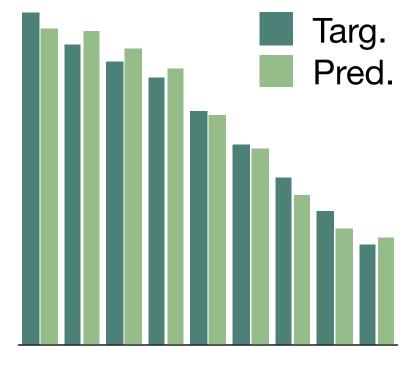




 $p(R) = \int dT \ p(R|T)p(T))$ 

#### Marginal distributions



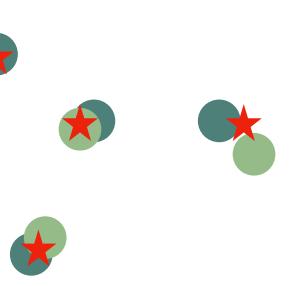






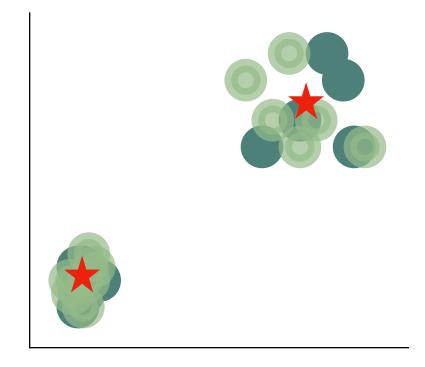
Feature

#### $(d_0, z_0, q/p_T, \theta, \phi)$ $P(f_R | f_T)$ Reconstruct **Resolution** constituents



Feature 1

Feature 2



Feature 1

70

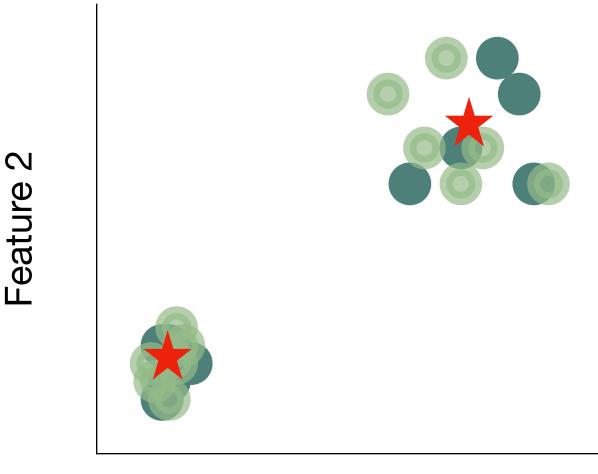
N. Soybelman



## **Goals: RESOLUTION** How to obtain the correct resolution?

- **Resolution depends on features**
- $\rightarrow$  difficult to learn smearing from one reconstructed sample per
- truth event
- $\longrightarrow$  need in principle very large dataset
  - Solution
  - Introduce *replicas:*

  - i.e. replicas for the SAME truth event



#### Feature 1

7 1

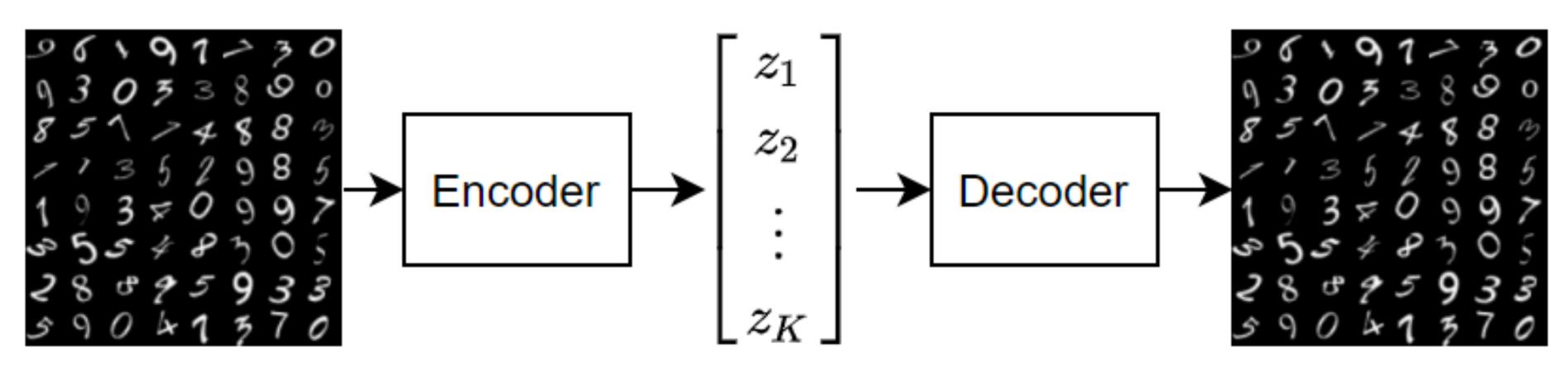
# Generate many reconstructions per truth event,

**N. Soybelman** 

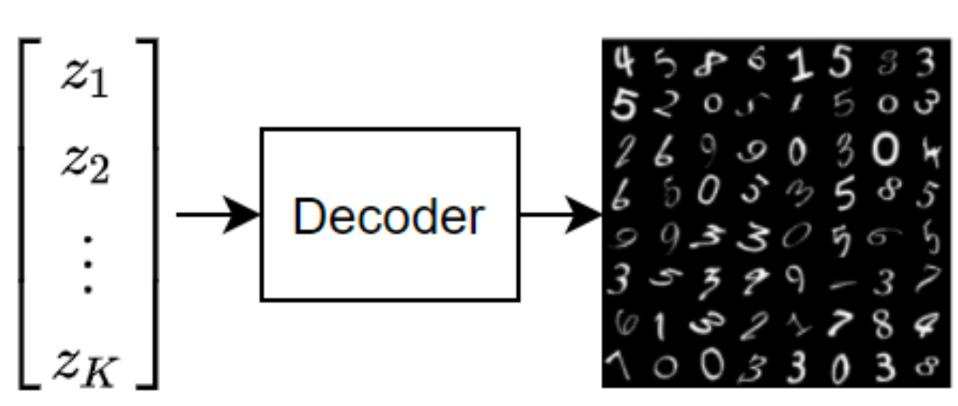
## Dataset

- SET of CHARGED particles within a single jet
- Detector Simulation GEANT based COCOA (tomorrow)
- 1-12 charged particles/jet
- Toy example: Smeared tracks as targets
- Reconstruction efficiency, no fakes  $\longrightarrow n_{reco} \leq n_{truth}$
- 100 replicas per event (train on 25 for speed)

## Variational Auto Encoder



#### Input Images



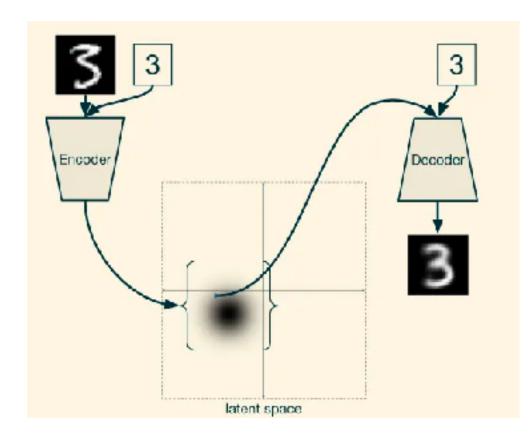
#### Random Vectors

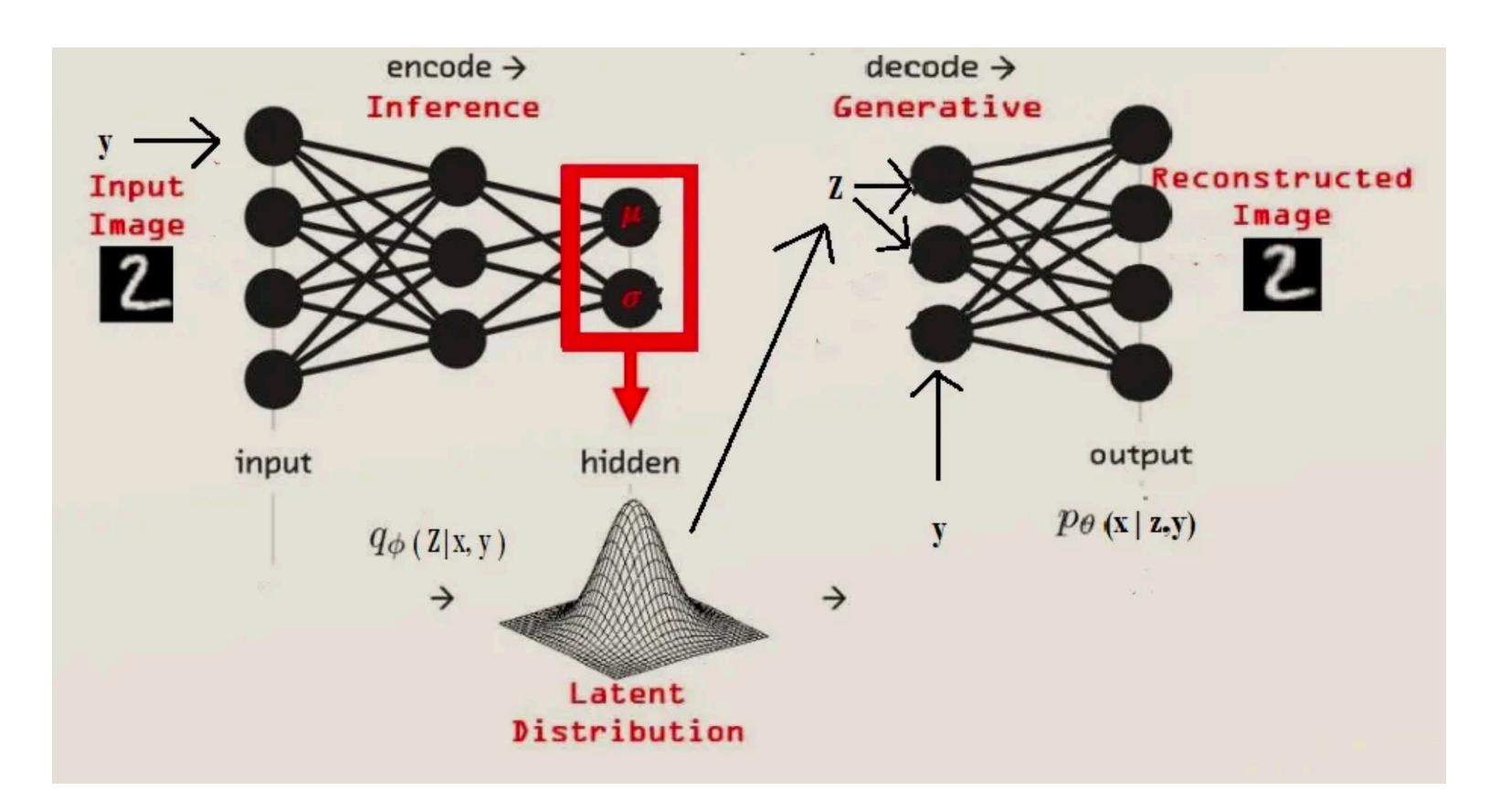
#### Image Encodings

Reconstructed Images

Generated Images

### cVAE





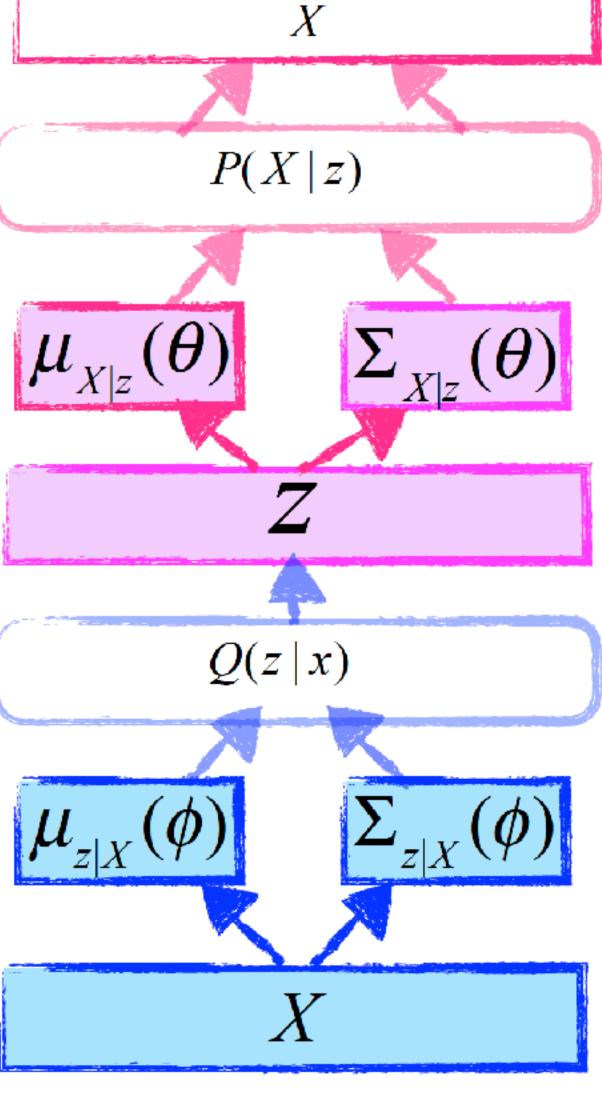
#### Variational Auto Encoder as Baseline VAE in a NUTSHELL Start by picking a prior to Z, p(Z)~N(0,1) Â The details are in the conditional P(X|Z)P(X|z) The decoder learns the distribution of x z, it learns two functions $\mu_{X|z}(\theta)$ Sample x|z from $x|z \sim \mathcal{N}(\mu_{x|z}, \Sigma_{x|z})$

$$\mu_{X|z}(\theta) \quad \Sigma_{X|z}(\theta)$$

• To ensure that the latent space contains z that lead to a DATA-like X the encoder learns an **approximate** distribution of **P(Z|X); Q(Z|X)** by learning two functions

$$\mu_{z|X}(\phi) \quad \Sigma_{z|X}(\phi)$$

from which Z x is sampled



### VAE

of original input X

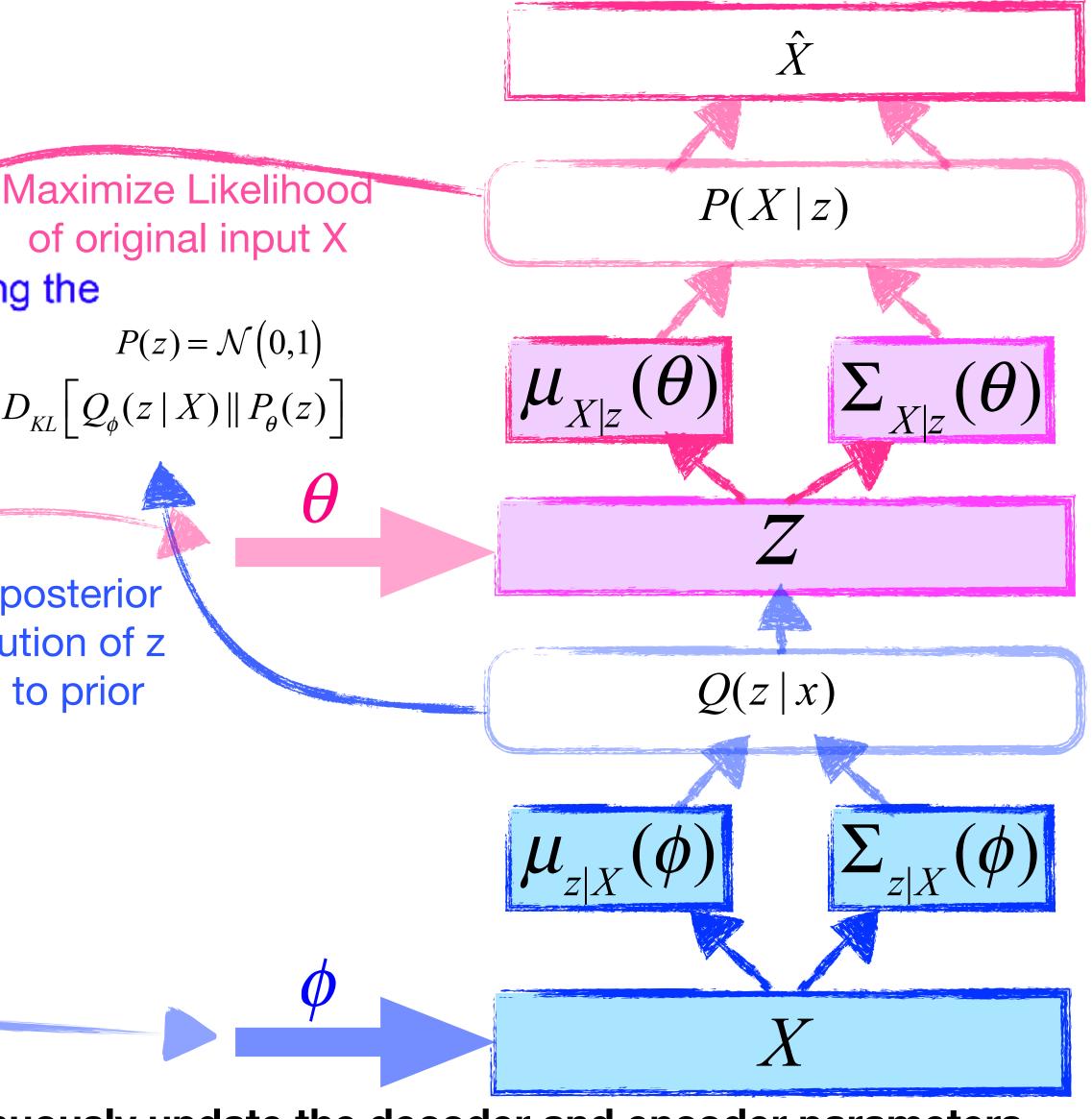
Putting it all together: maximizing the likelihood lower bound

 $\log P_{\theta}(X) \leq E_{z \sim Q_{\phi}(z|X)} [\log(P_{\theta}(X|z)] - D_{KL} \left[ Q_{\phi}(z|X) \| P_{\theta}(z) \right]$ 

Make posterior distribution of z close to prior

For every minibatch of input data: compute this forward pass, and then backprop!

We update our model by continuously update the decoder and encoder parameters, Φ and θ



### VAE

of original input X

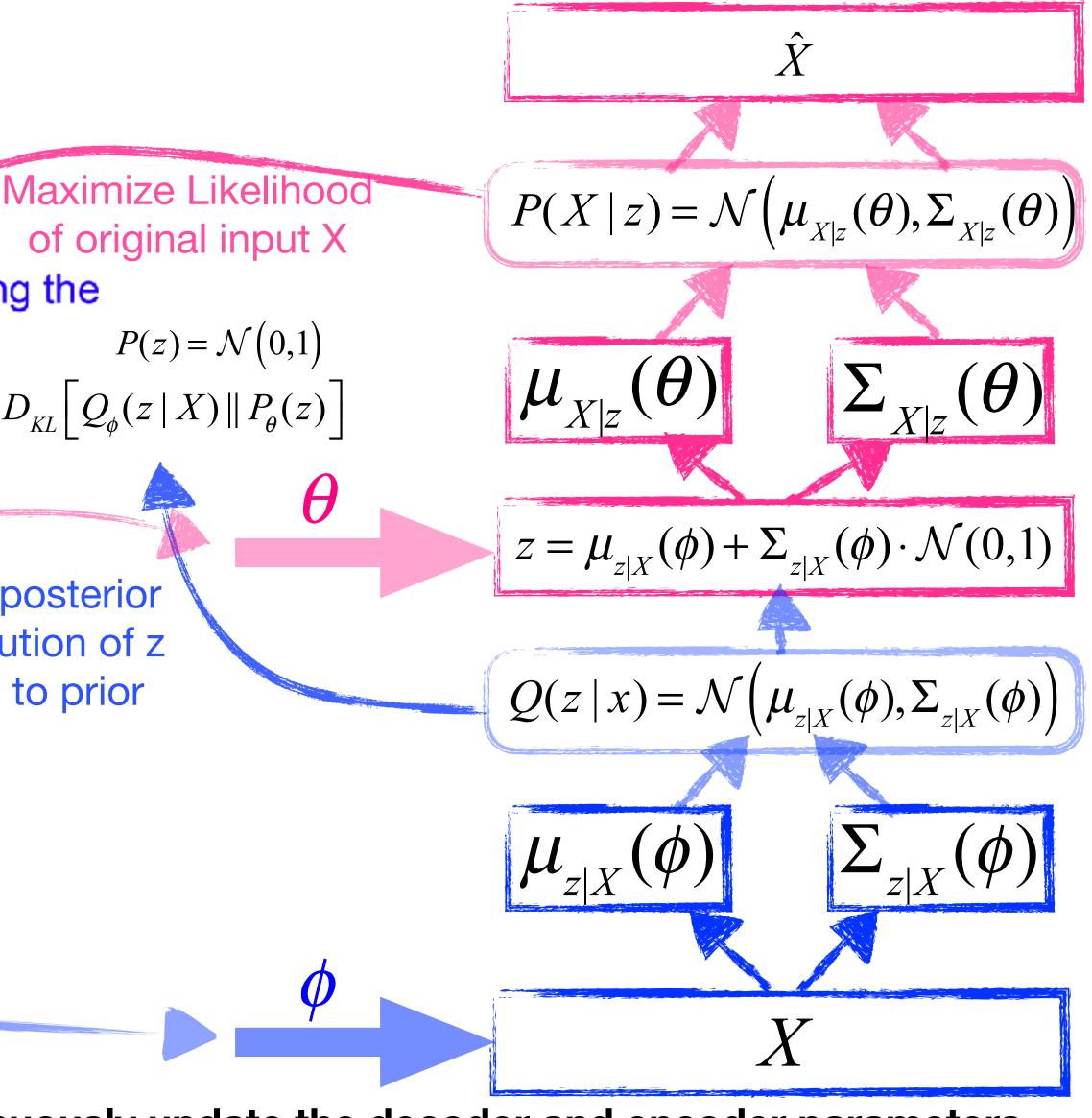
Putting it all together: maximizing the likelihood lower bound

 $\log P_{\theta}(X) \leq E_{z \sim Q_{\phi}(z|X)}[\log(P_{\theta}(X|z)] - D_{KL} \left[ Q_{\phi}(z|X) \| P_{\theta}(z) \right]$ 

Make posterior distribution of z close to prior

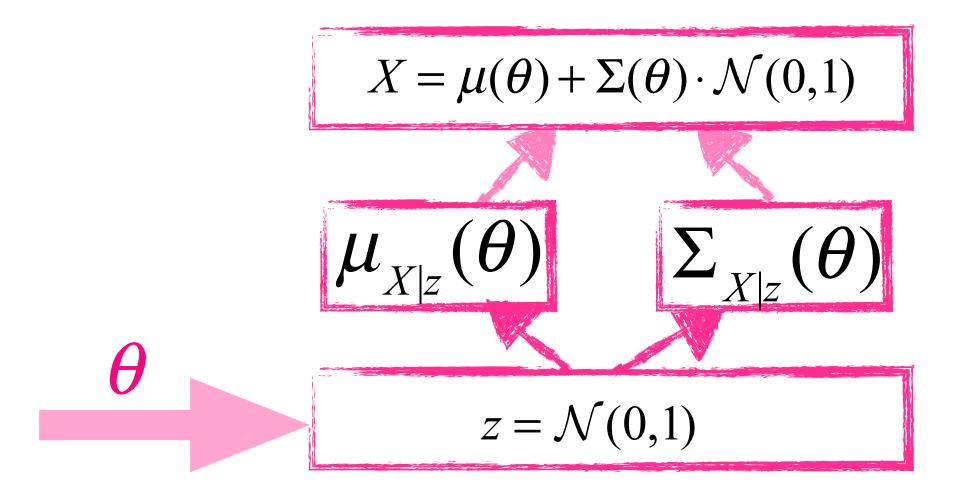
For every minibatch of input data: compute this forward pass, and then backprop!

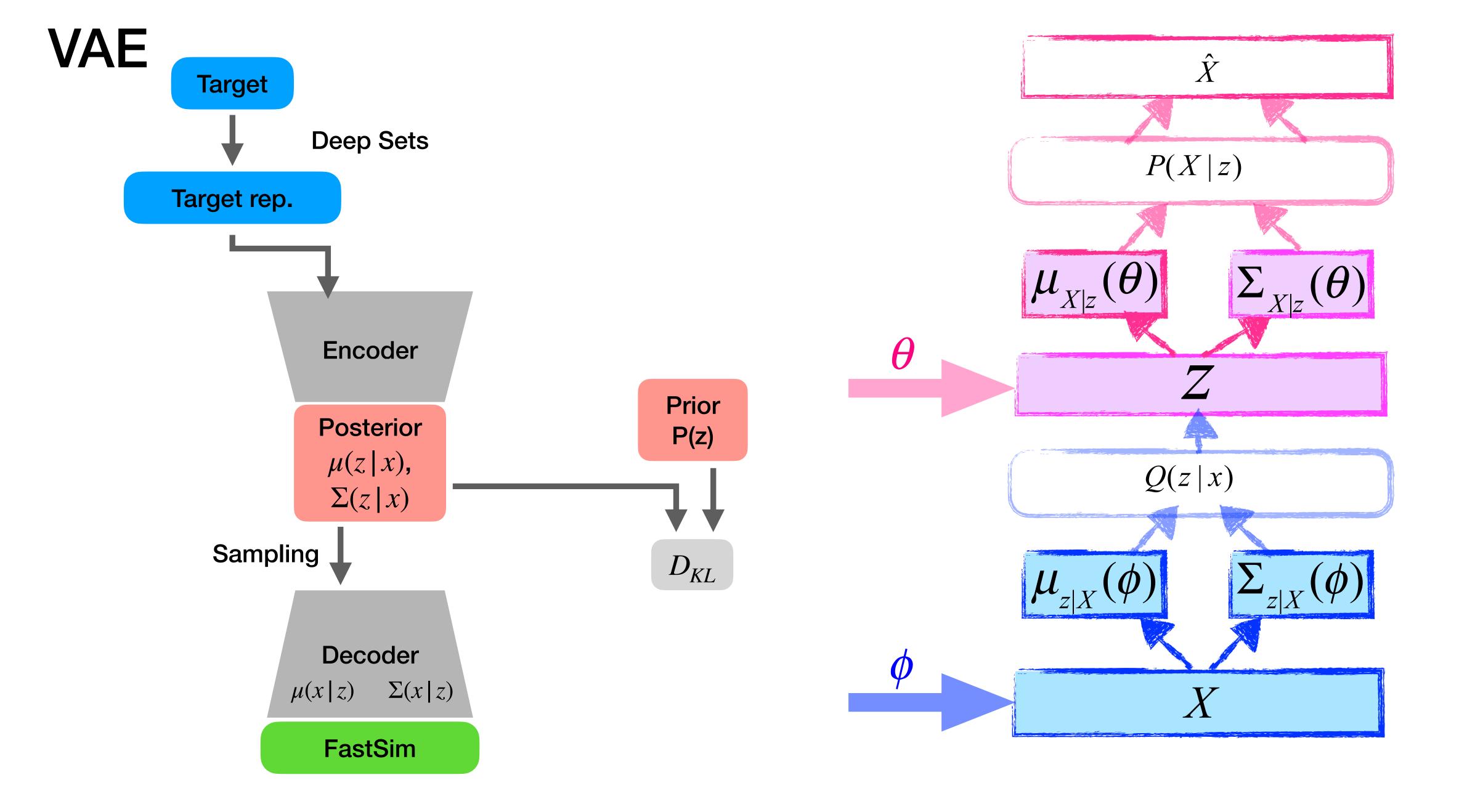
Φ and θ



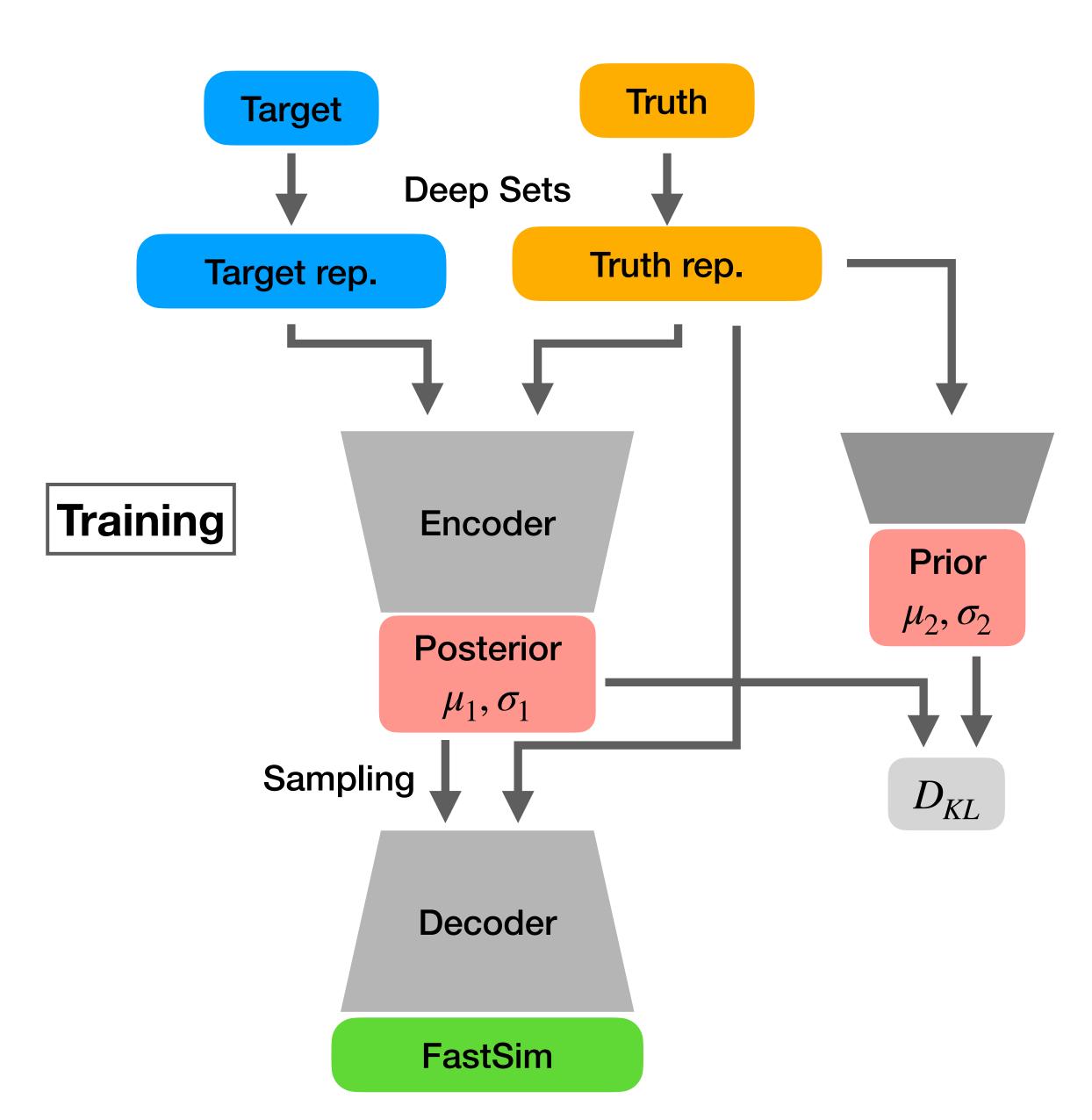
We update our model by continuously update the decoder and encoder parameters,

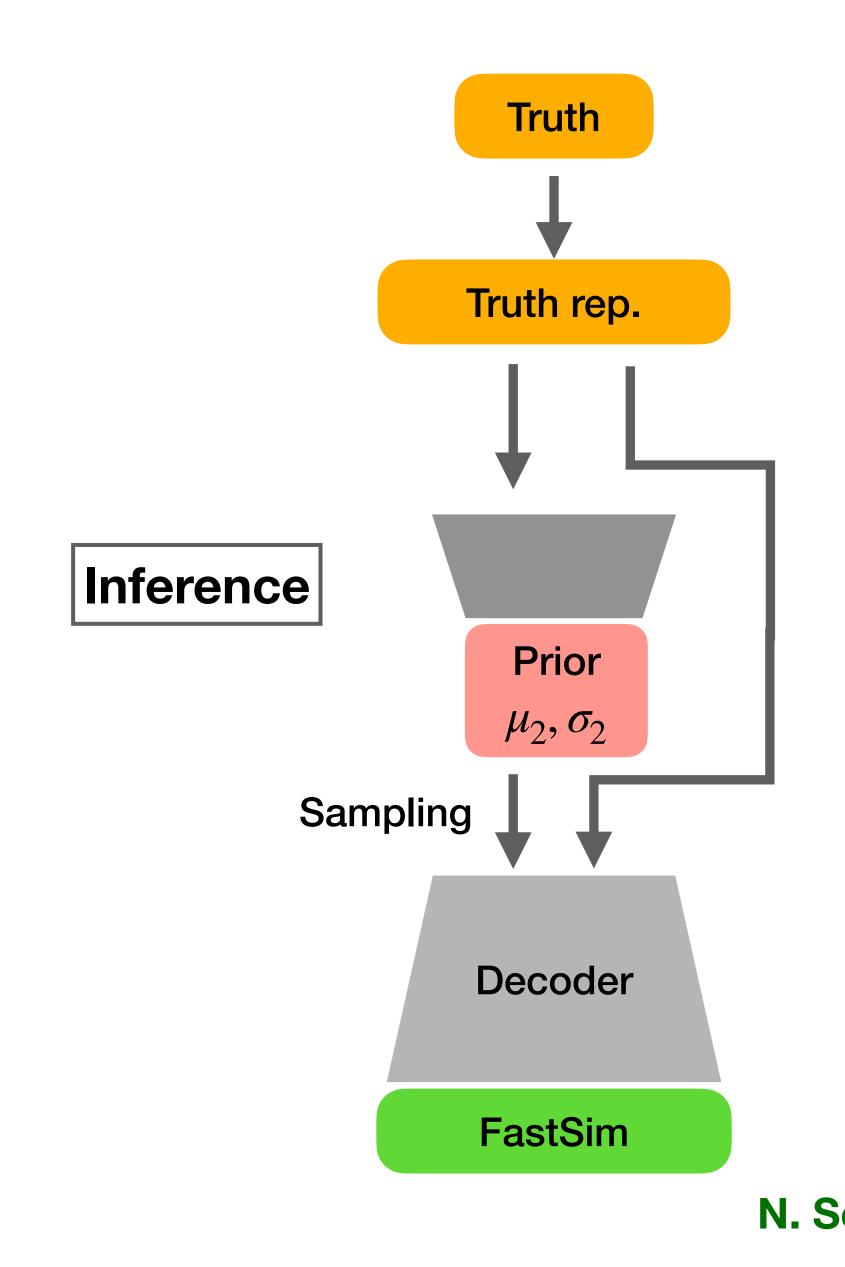






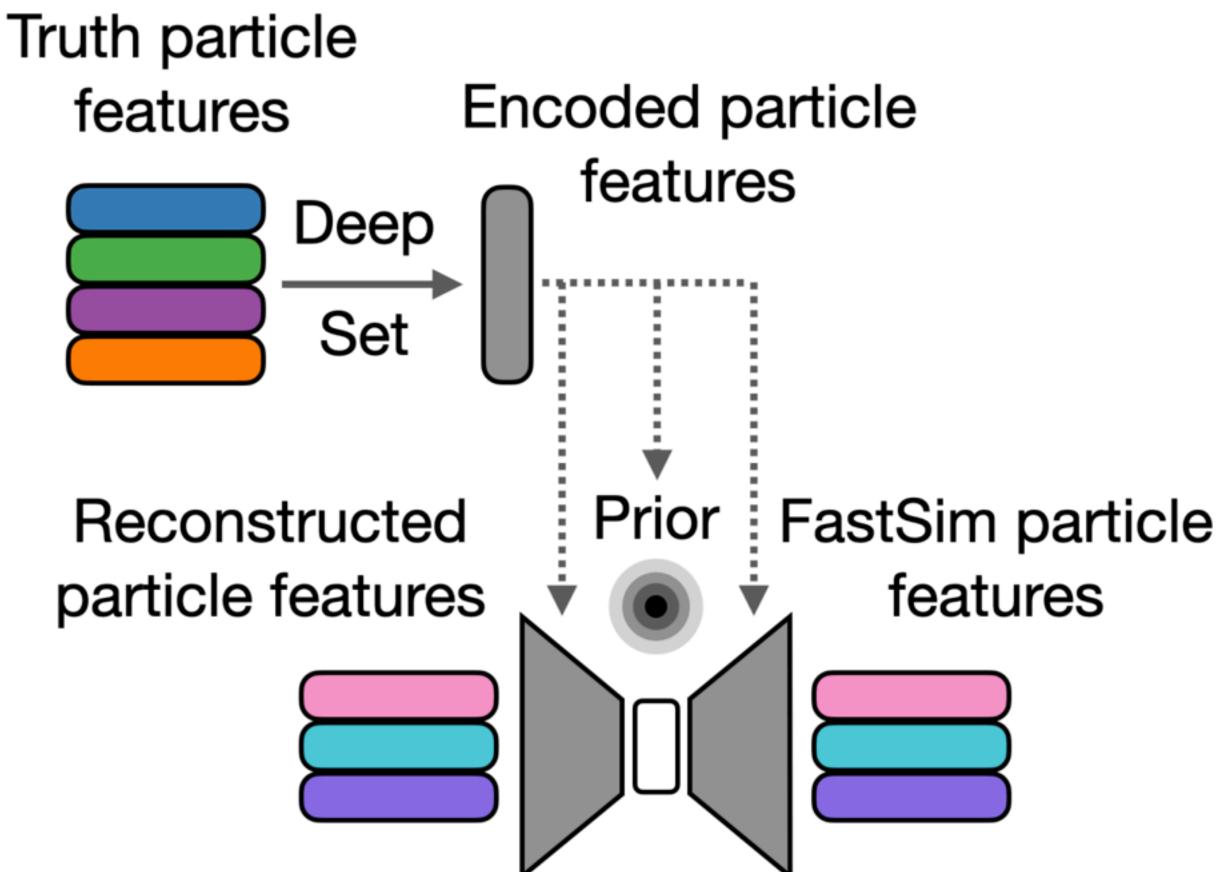
### cVAE Architecture

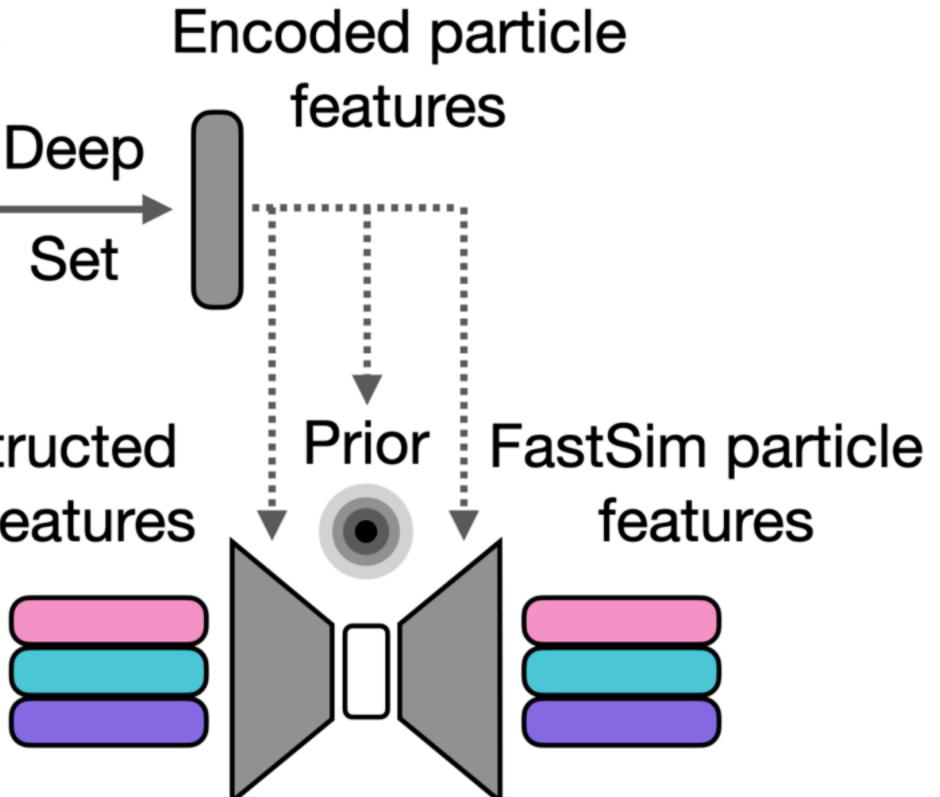


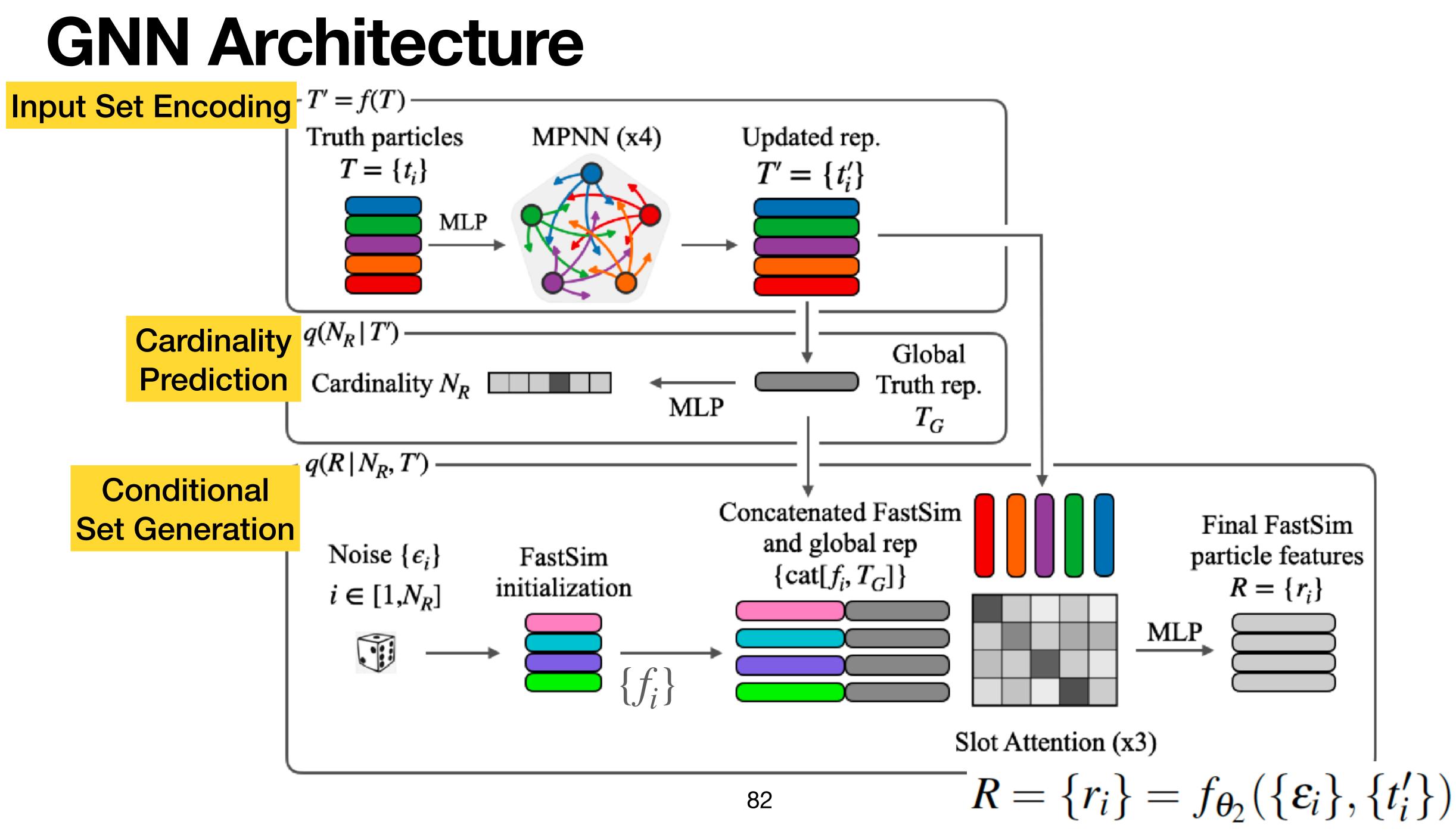




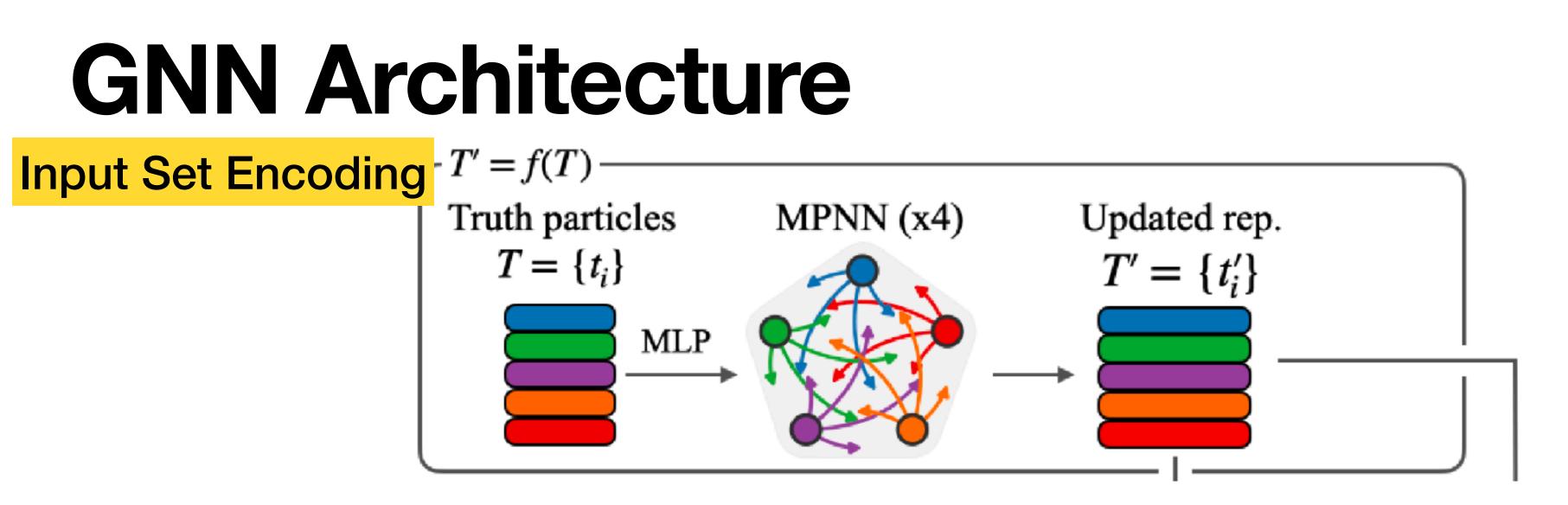
### **cVAE** Architecture



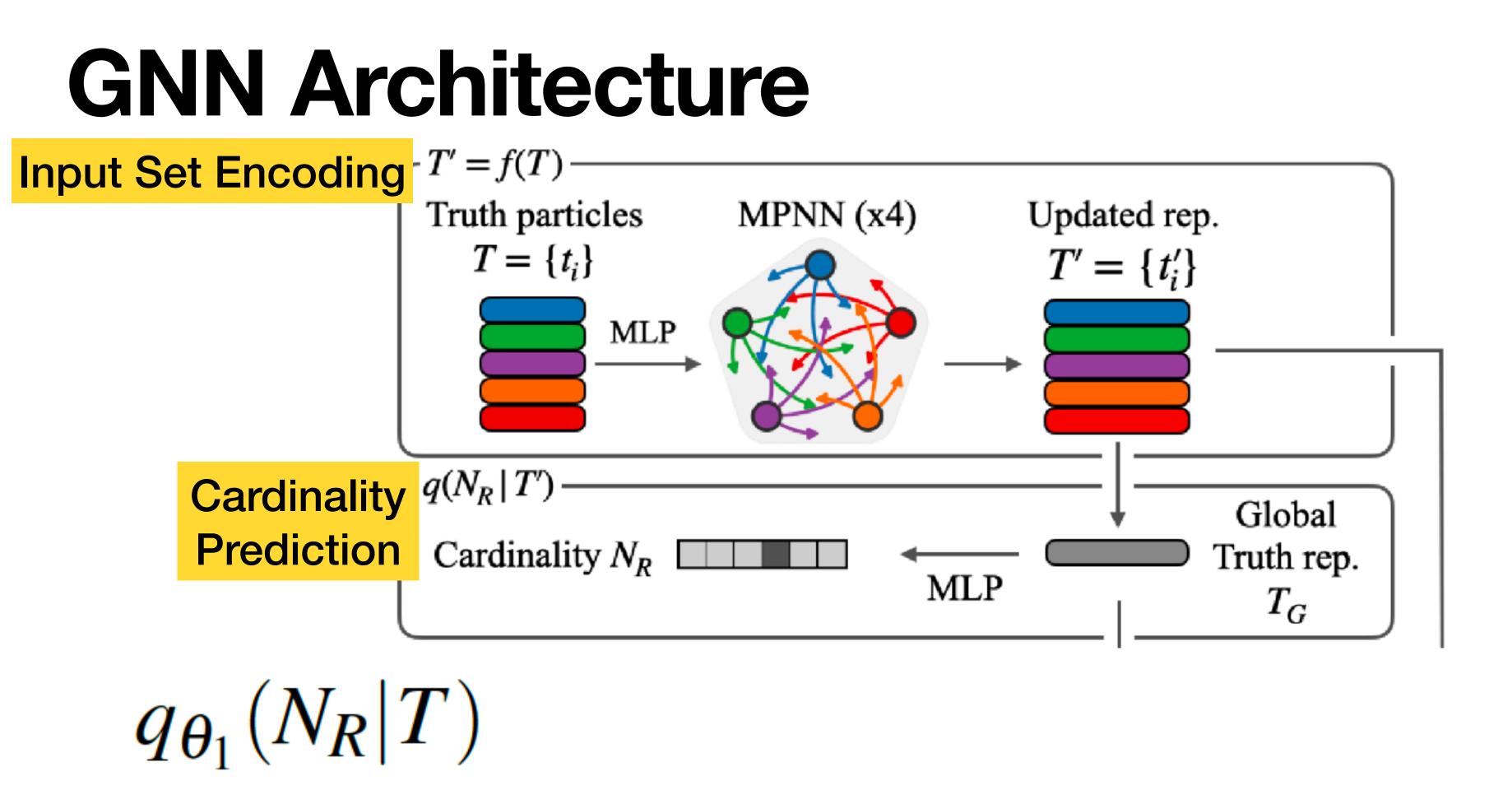


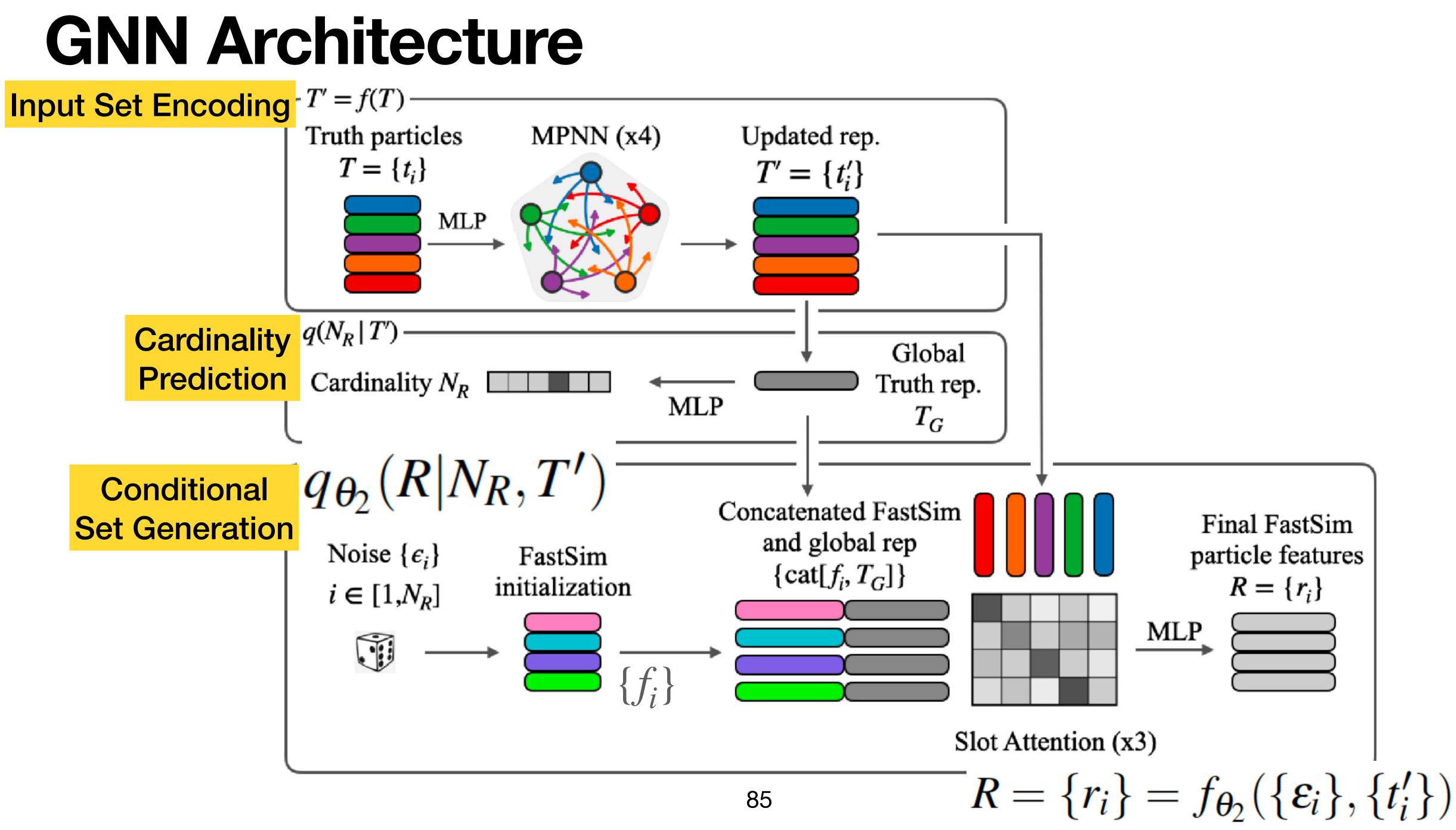






### $\{f_i\} = \{p_{T,i}, \eta_i, \phi_i\}$

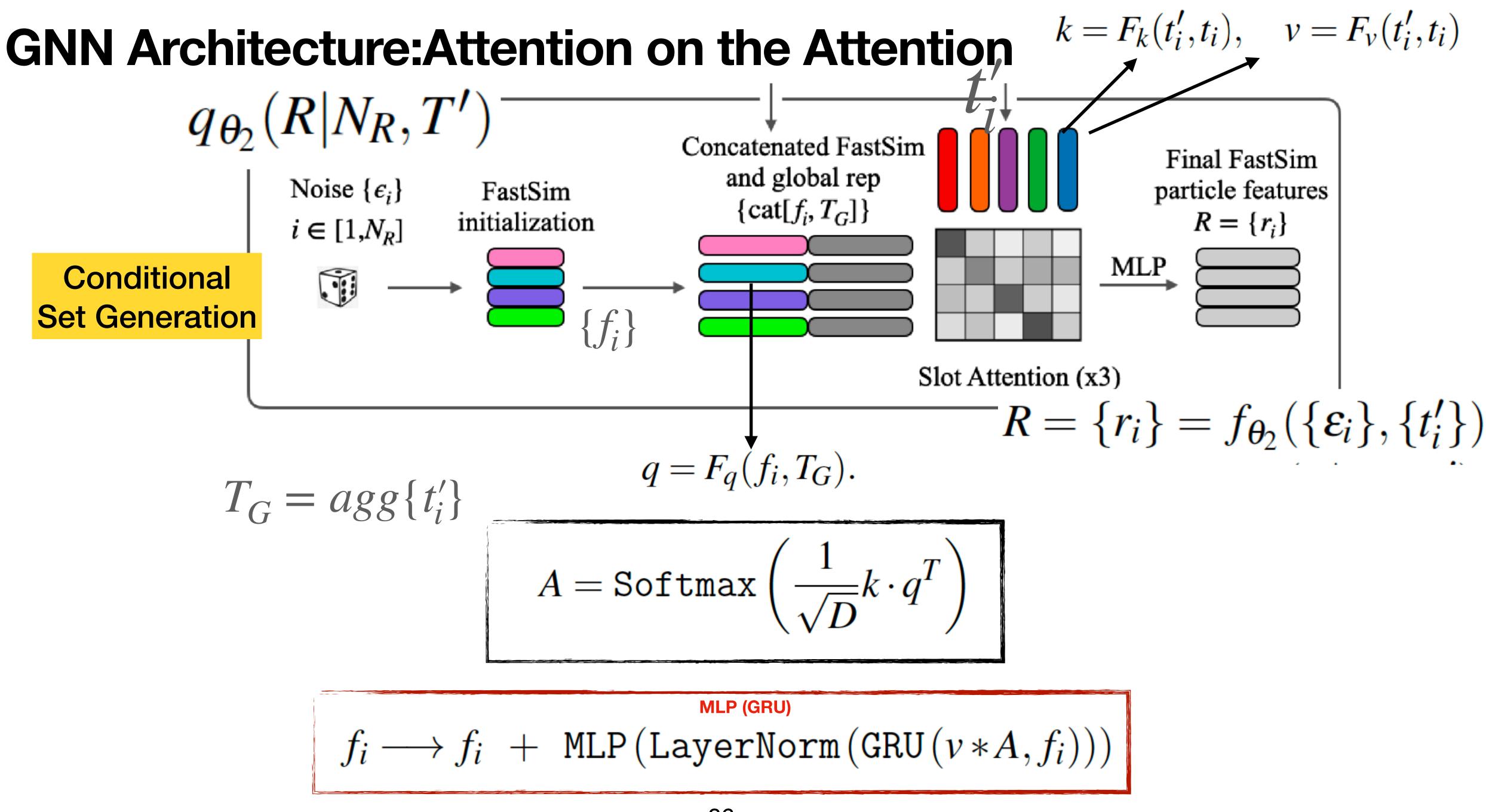






# $q_{\theta_2}(R|N_R,T')$

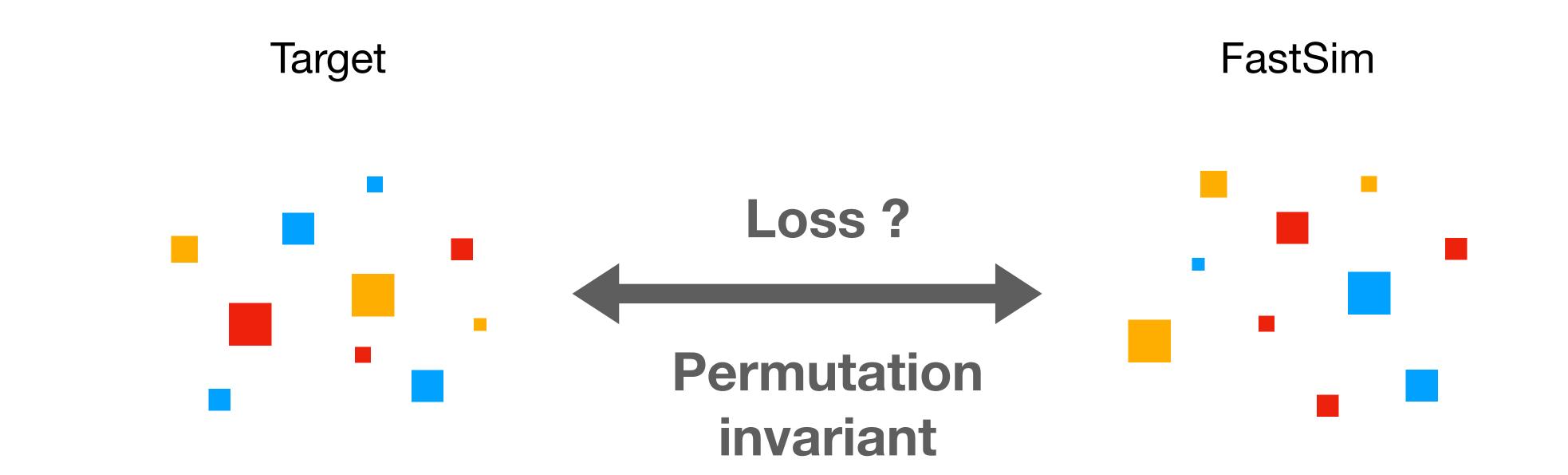
Conditional **Set Generation** 



$$A = \texttt{Sof}$$

$$f_i \longrightarrow f_i + MLP(L$$

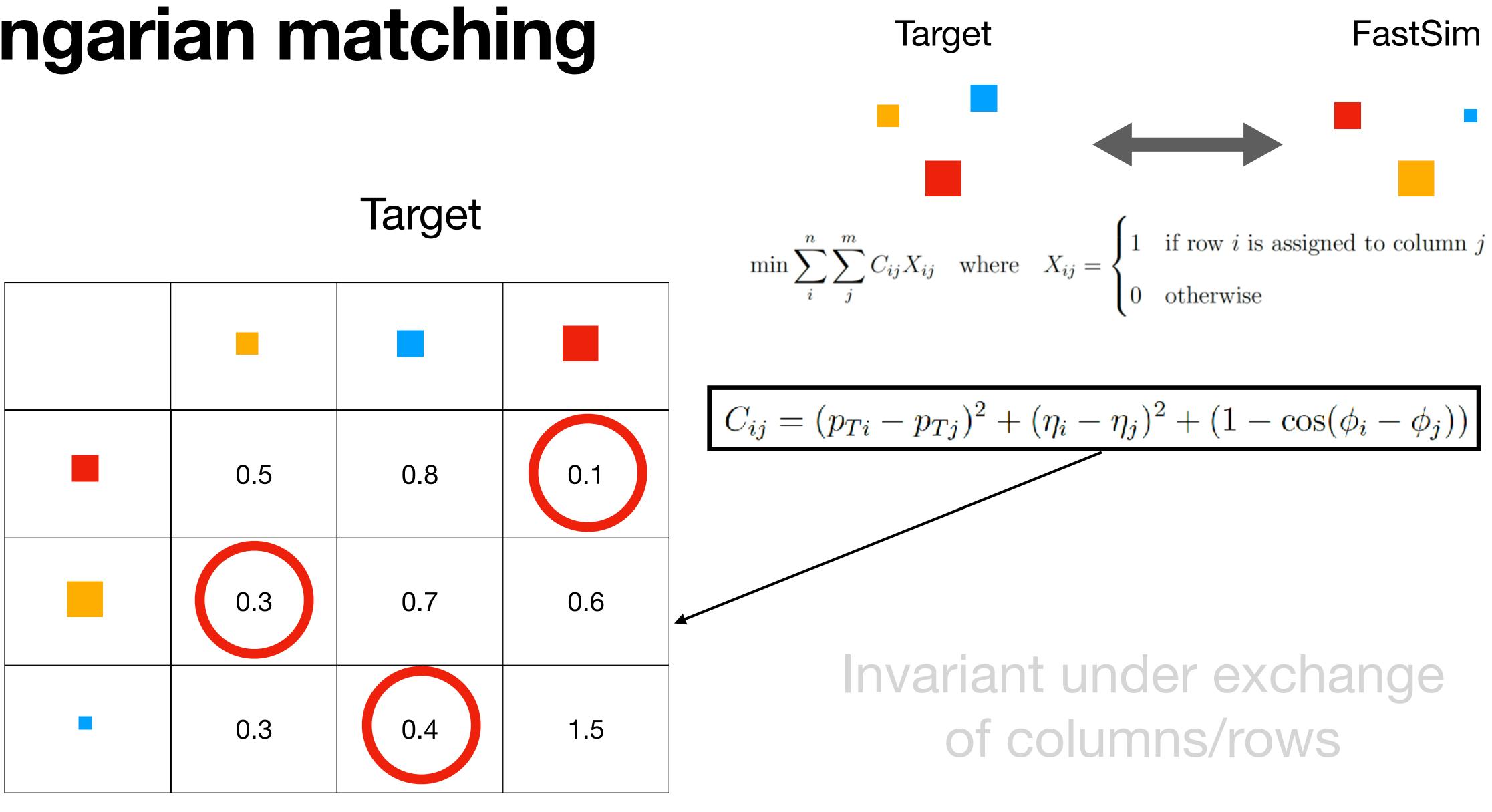
### Set to Set problem





## Hungarian matching

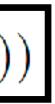




FastSim

N. Soybelman







## "Double Hungarian"

#### Replicas —> Set of Sets

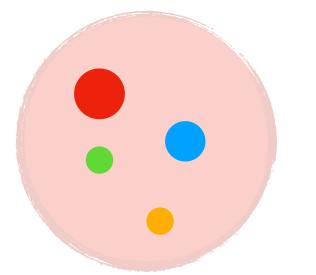
Construct a a samplebased similarity measure between the two distributions  $q_{\phi}(R \mid T, N)$  $p(R \mid T, N)$  $MMD^{2}(p,q) = \mathbb{E}_{x,x'\sim p}k(x,x') + \mathbb{E}_{y,y'\sim q}k(y,y') - 2\mathbb{E}_{x\sim p,y\sim q}k(x,y)$  $x_i = (p_{T,i}, \eta_i, \phi_i)$   $y_i = (p'_{T,i}, \eta'_i, \phi'_i)$  $k(x, y) = ||x - y||^2$ Hungarian MMD vanishes when p=q but is time consuming  $L_{proxy} = min_{x_i, y_j} k(x_i, y_j)$ 

 $p(R \mid T, N)$ 

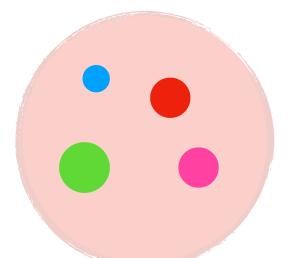
Reconstructed Replicas

 $q_{\phi}(R \mid T, N)$ 

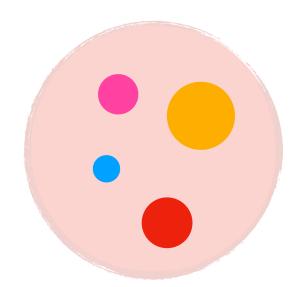
Predicted Replicas









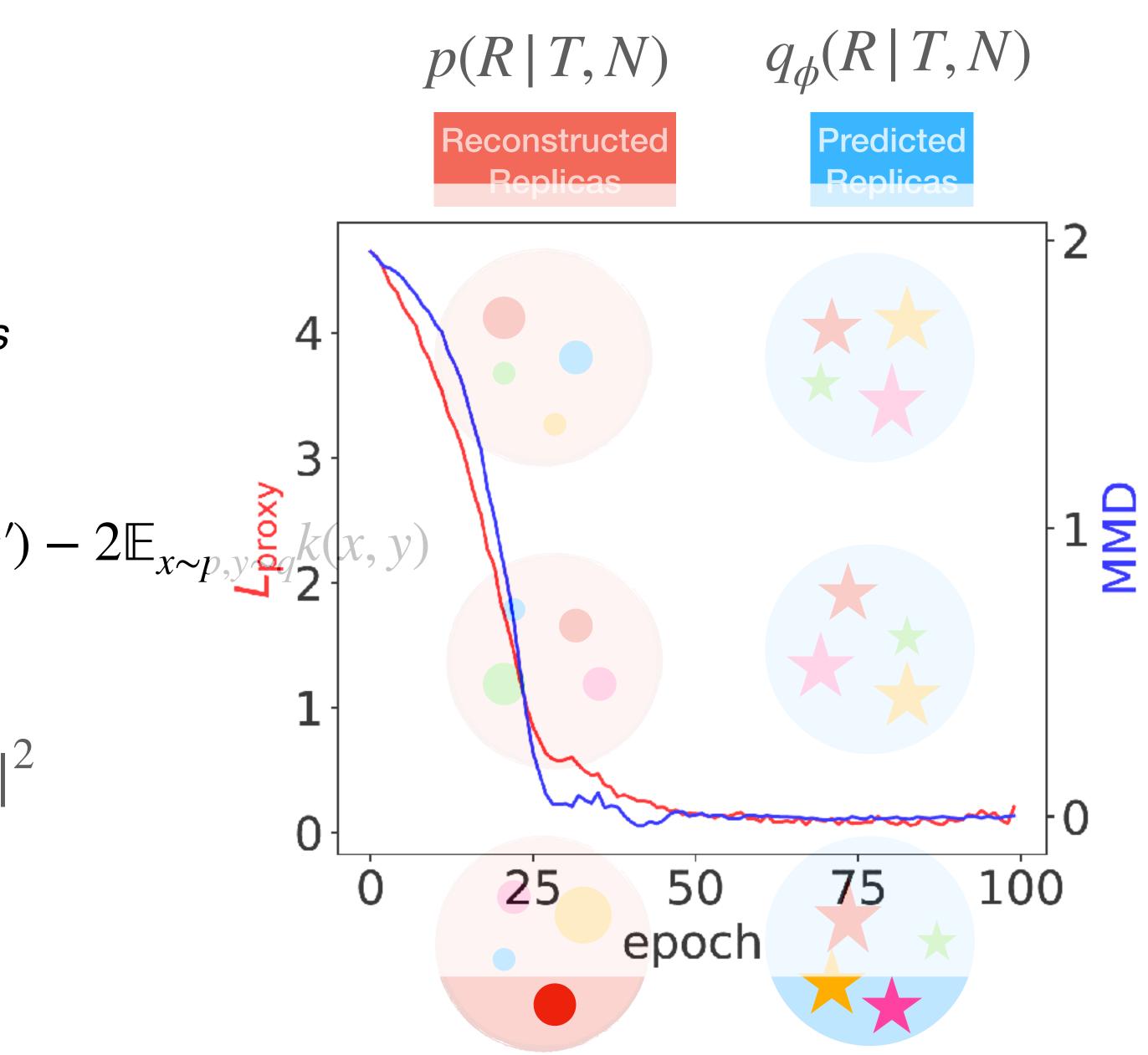




## "Double Hungarian"

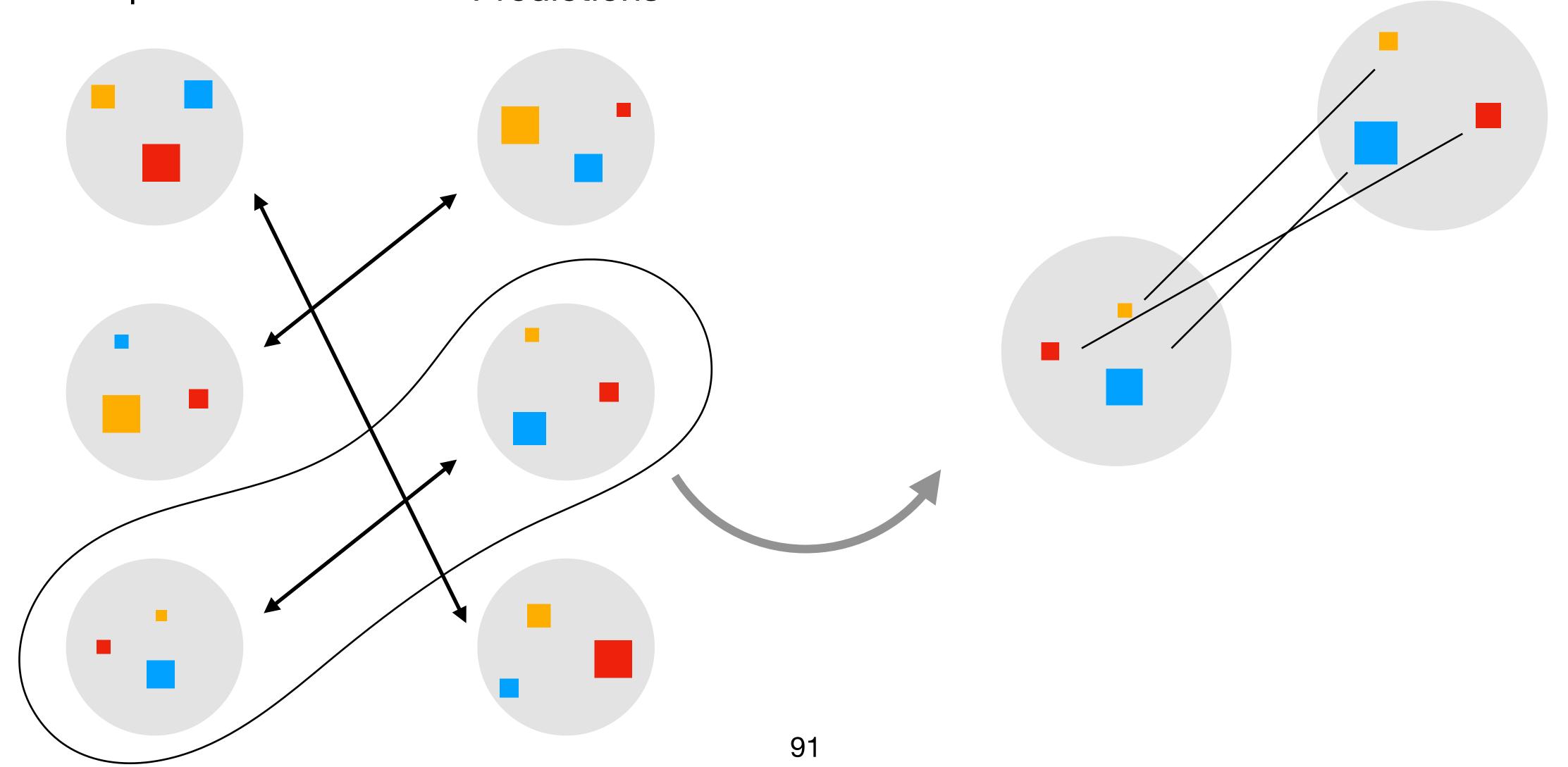
#### Replicas —> Set of Sets

Construct a a samplebased similarity measure between the two distributions  $q_{\phi}(R \mid T, N)$  $p(R \mid T, N)$  $MMD^{2}(p,q) = \mathbb{E}_{x,x'\sim p}k(x,x') + \mathbb{E}_{y,y'\sim q}k(y,y') - 2\mathbb{E}_{x\sim p,y} \sum_{q=1}^{\infty} k(x,x') + \mathbb{E}_{y,y'\sim q}k(y,y') - 2\mathbb{E}_{x\sim p,y} \sum_{q=1}^{\infty} k(x,x') + \mathbb{E}_{y,y'\sim q}k(y,y') - 2\mathbb{E}_{x\sim p,y} \sum_{q=1}^{\infty} k(x,x') + \mathbb{E}_{y,y'\sim q}k(y,y') - 2\mathbb{E}_{x\sim p,y} \sum_{q=1}^{\infty} k(x,y') + \mathbb{E}_{y,y'\sim q}k(y,y') - 2\mathbb{E}_{x\sim p,y} \sum_{q=1}^{\infty} k(y,y') + \mathbb{E}_{y,y'\sim q}k(y,y') - 2\mathbb{E}_{y,y'\sim q}k(y,y') + \mathbb{E}_{y,y'\sim q}k(y,y$  $x_i = (p_{T,i}, \eta_i, \phi_i)$   $y_i = (p'_{T,i}, \eta'_i, \phi'_i)$  $k(x, y) = ||x - y||^2$ Hungarian MMD vanishes when p=q but is time consuming  $L_{proxy} = min_{x_i, y_j} k(x_i, y_j)$ 



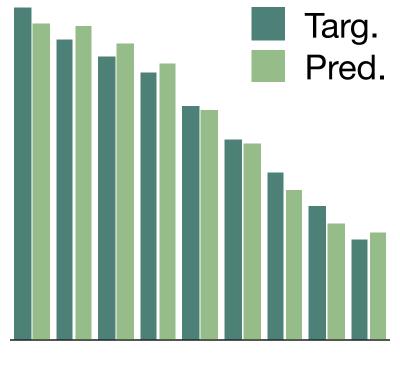
## "Double Hungarian"

Replicas Predictions





#### Marginal distributions



 $\sim$ Feature ?



Feature

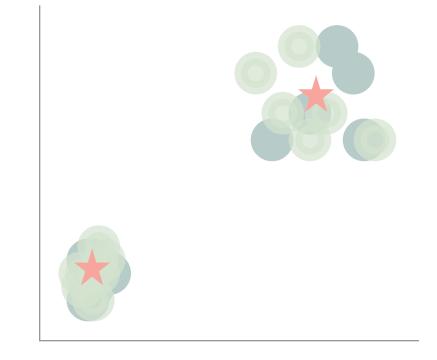


#### Resolution



Feature 1

Feature 2

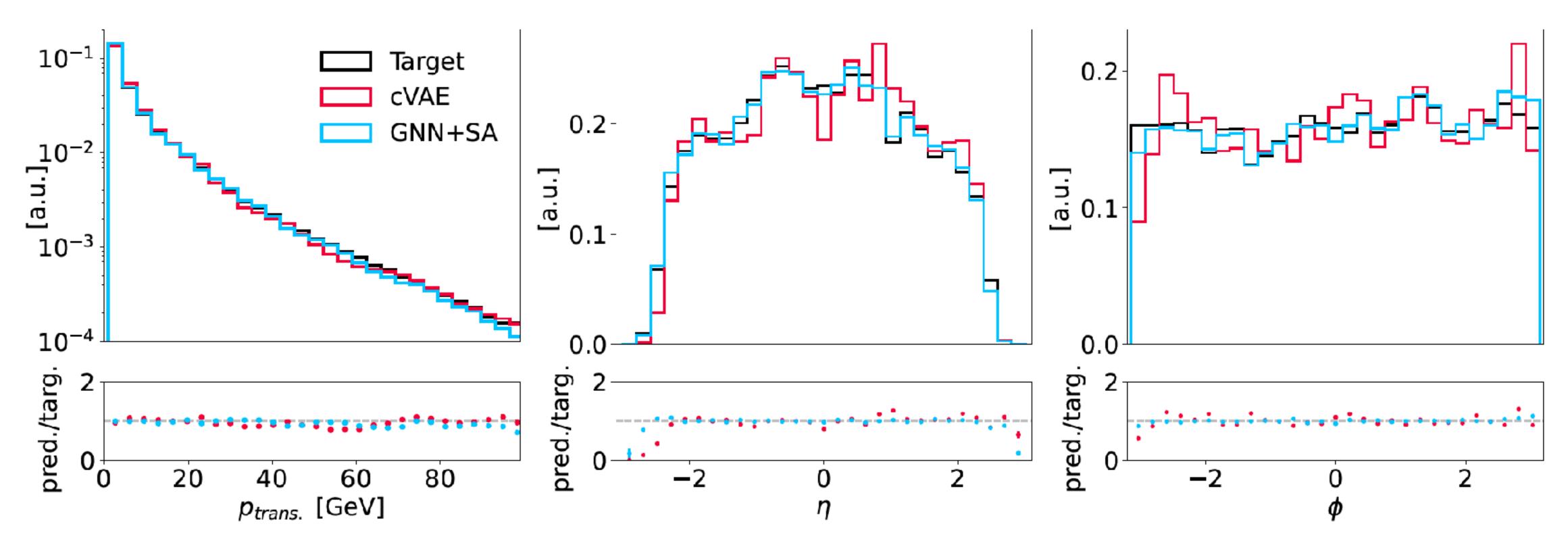


Feature 1

N. Soybelman



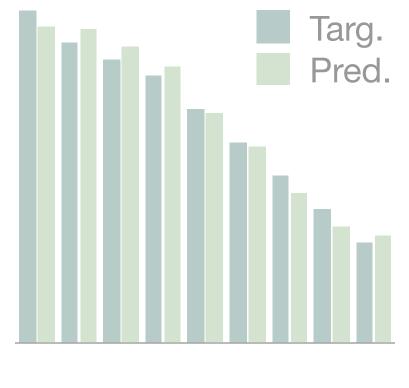
## **Marginal distributions**



1D marginal distributions similarly good for both cVAE and GNN



#### Marginal distributions



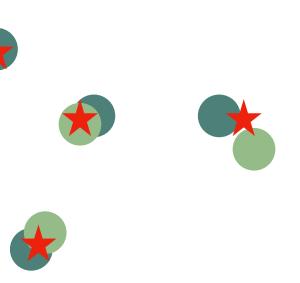
Feature 2



Feature

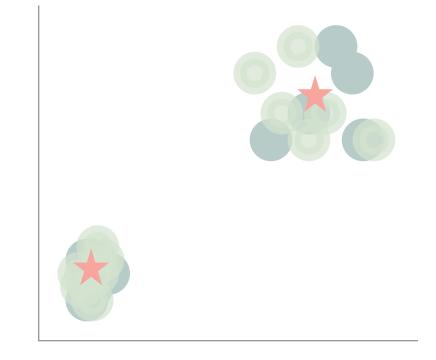


#### Resolution



Feature 1

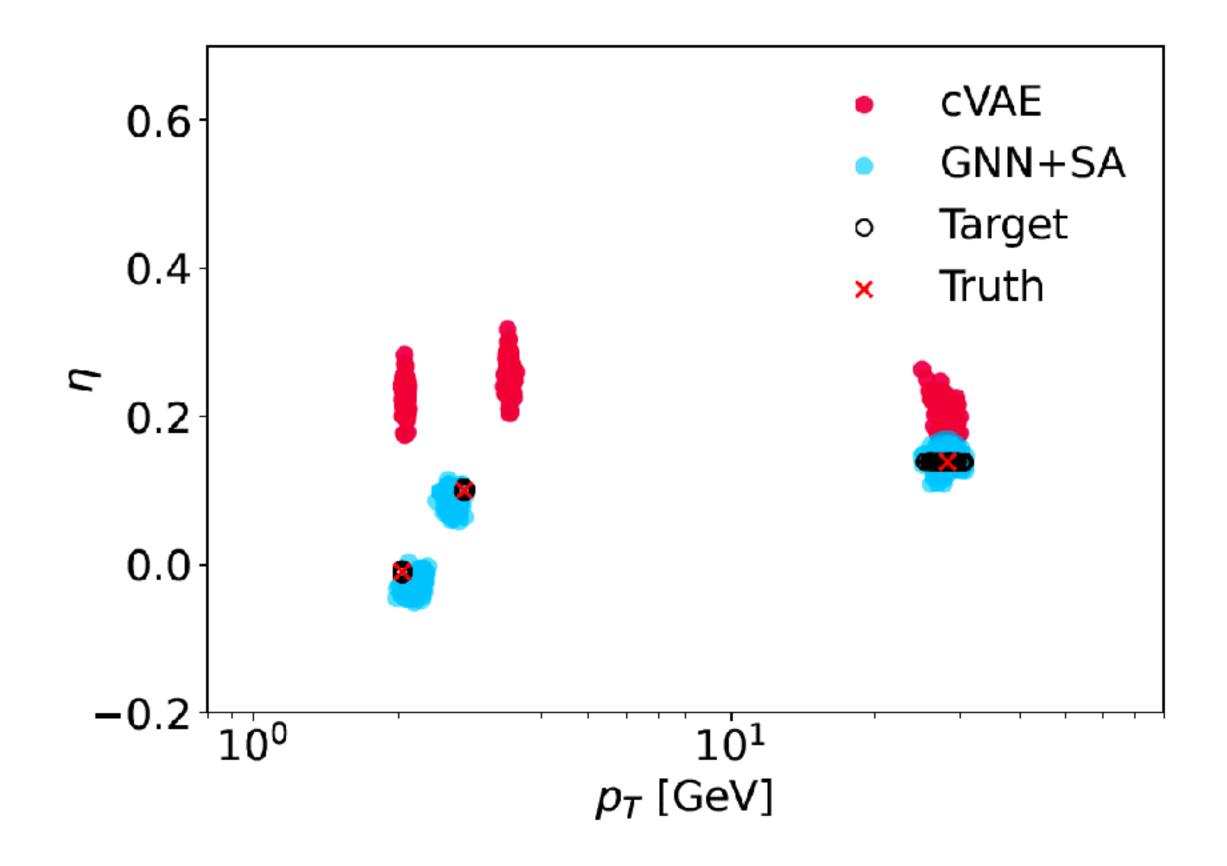
Feature 2

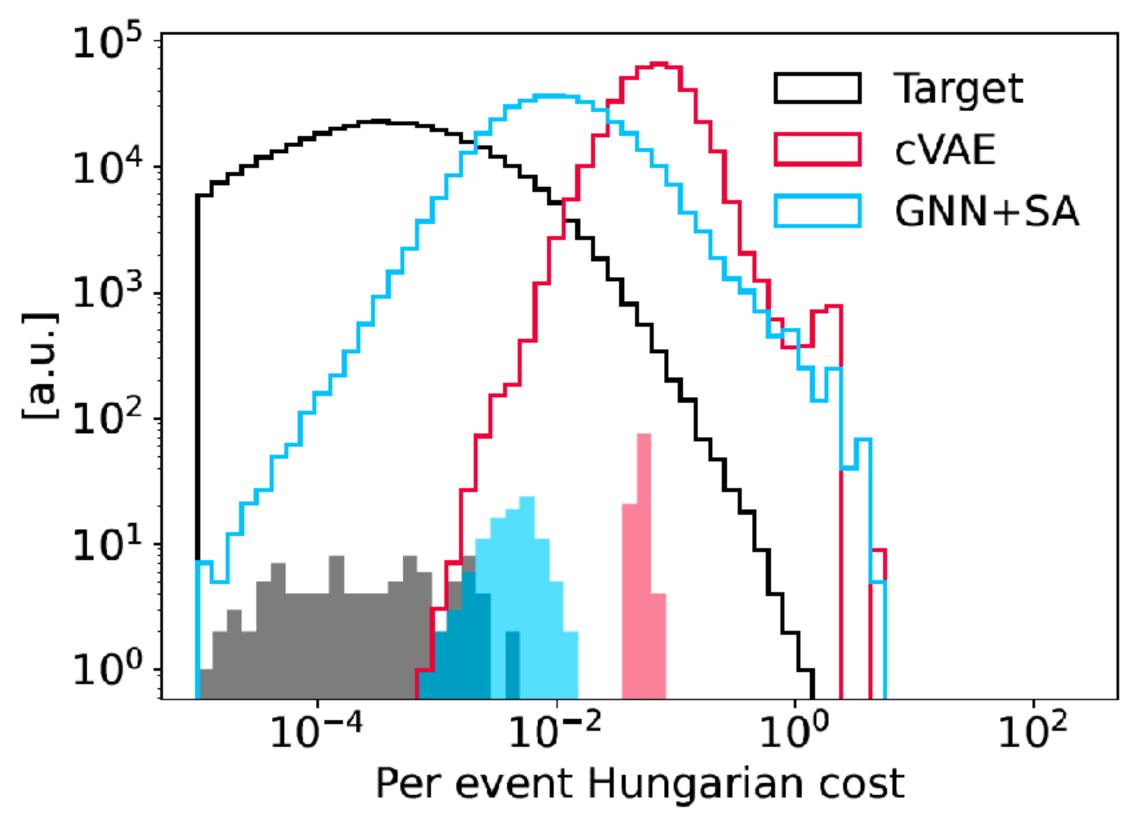


Feature 1



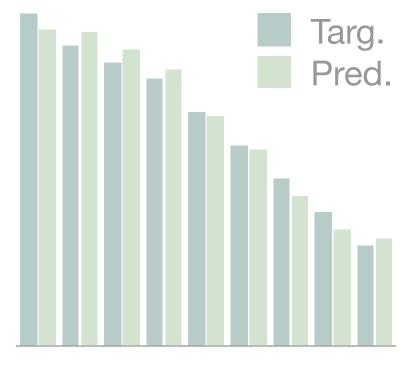
### **Reconstruct Constituents**







#### Marginal distributions



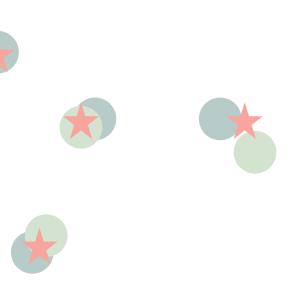
 $\sim$ Feature ?



Feature

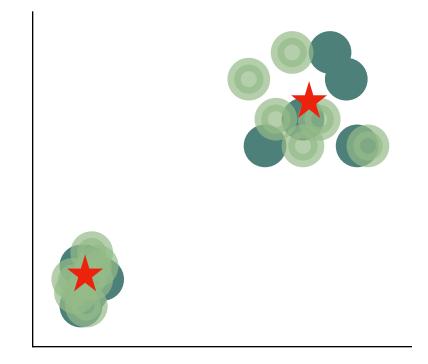
### Reconstruct constituents

#### Resolution



Feature 1

Feature 2

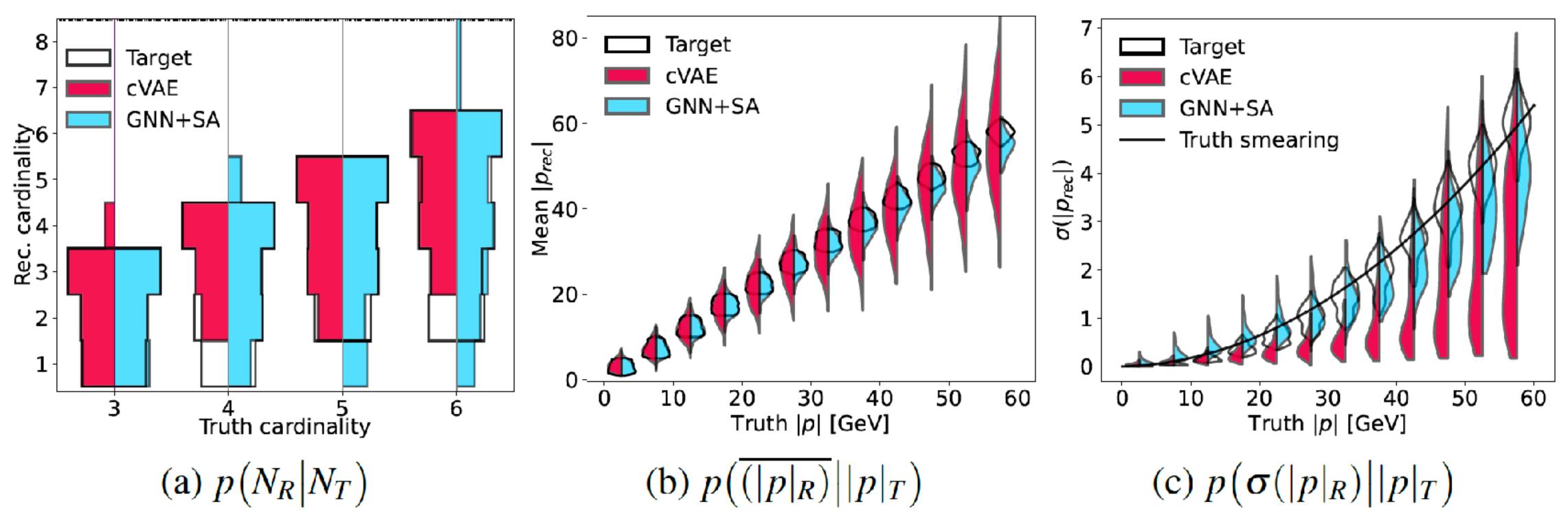


Feature 1

96



### Resolution



## Conclusion

Investigated feasibility of set generation via attention-based GNN architecture, using

replicas important to learn the resolution

- distributions can be deceptive

the target distribution. It performs better in predicting mean and variance of constituents

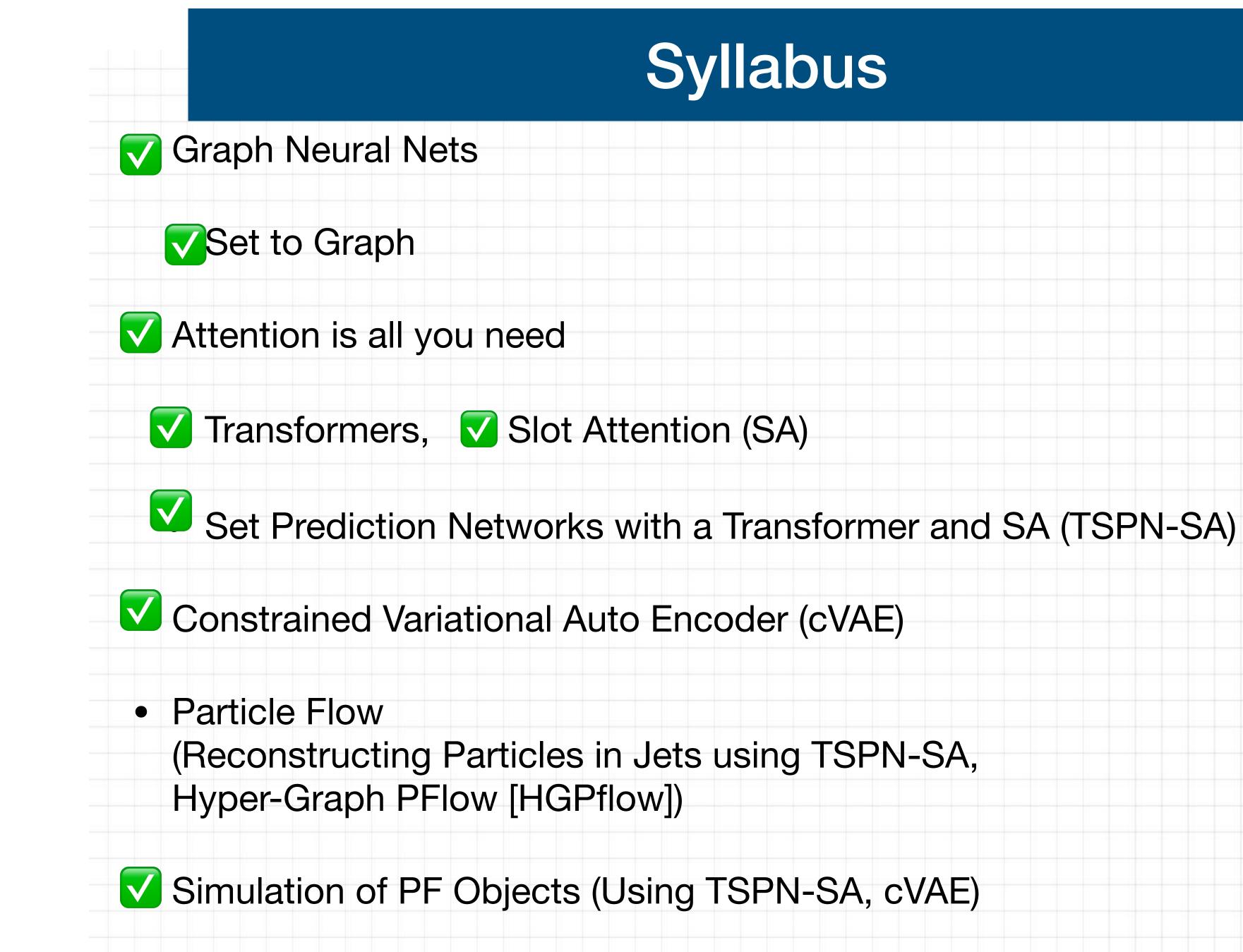
#### Marginal distribution well-modeled by baseline (cVAE) and GNN with Slot att, however, 1D

#### The GNN+SA model outperforms the baseline model and better captures key properties of









### Syllabus

99