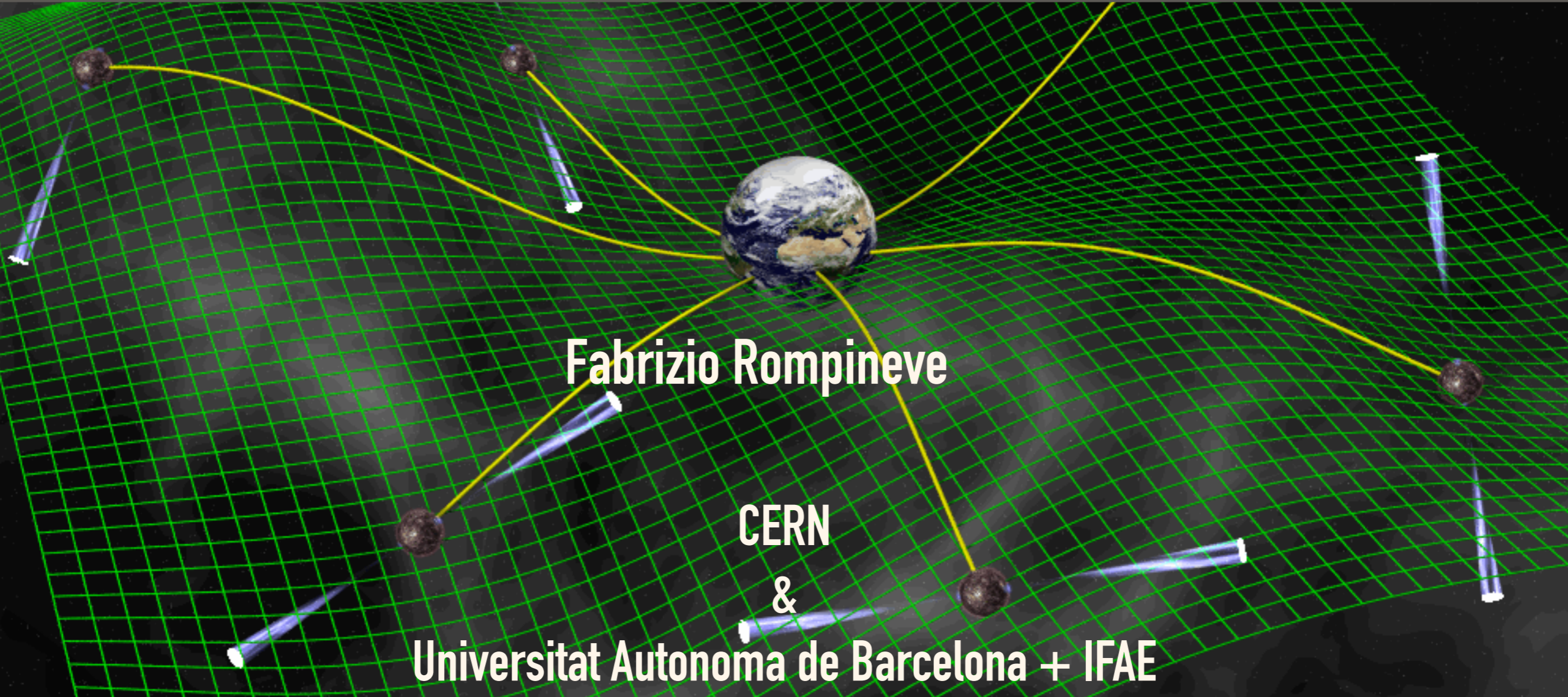


# Features of Early Universe Gravitational Waves at PTAs



Fabrizio Rompineve

CERN  
&

Universitat Autònoma de Barcelona + IFAE

MITP workshop:  
“Pulsars: A Star-way to  
New Physics”

based on  
G. Franciolini, D. Racco, FR 2306.17136  
V. Dandoy, V. Domcke, 2302.07901

R.Z. Ferreira, A. Notari, O. Pujolàs, 2204.04228

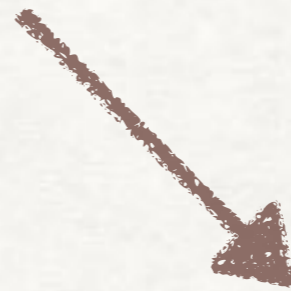


Background from CERN courier, credit: D. Champion

See talks by Natalia,  
Andrea & Luke

## Origin of PTA GWs

See talks by Eric,  
Geraldine, Ken, Valerie,  
Dani, Frederik



**Supermassive Black Hole  
Binaries (SMBHBs)**

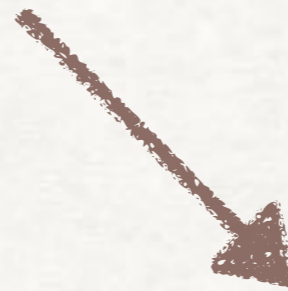
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(Requires new physics beyond  
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**Early Universe/Particle Physics**

(Requires new physics beyond  
the Standard Model, SM)

**Uncertain theory  
prediction**

(May require beyond standard  
astro modeling)

**Theory "Uncertainty":**

Several candidate sources possible,  
No one clearly better motivated than others

**Challenges:**

GW spectrum often model dependent,  
case-by-case numerical simulations required,  
Degeneracies between  
different sources

# **DIRECTIONS/OPPORTUNITIES FOR PARTICLE PHYSICS/COSMOLOGY @ PTAS**

# DIRECTIONS/OPPORTUNITIES FOR PARTICLE PHYSICS/COSMOLOGY @ PTAS

*Robust discriminating features*

*Set constraints*

*Motivated models for signal  
interpretation*

# DIRECTIONS/OPPORTUNITIES FOR PARTICLE PHYSICS/COSMOLOGY @ PTAS

*In this talk*

*Robust discriminating features*

*Model-independent impact of  
Standard Model physics on  
broad class of GW sources*

*Set constraints*

*Scalar-induced Gravitational  
Waves*

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*Cosmic Domain Walls*

# DIRECTIONS/OPPORTUNITIES FOR PARTICLE PHYSICS/COSMOLOGY @ PTAS

G. Franciolini, D. Racco, FR 2306.17136

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For non-transient,  
see talk by Geraldine, Ken!

# SUB-HUBBLE TRANSIENT SOURCES

*Broad class of (new physics) sources is active at a definite epoch/  
temperature (Then shuts off)*

$$H \sim \frac{T^2}{M_p}, M_p \equiv (8\pi G)^{-1/2}$$

$$t_\star \lesssim H^{-1}(T_\star)$$

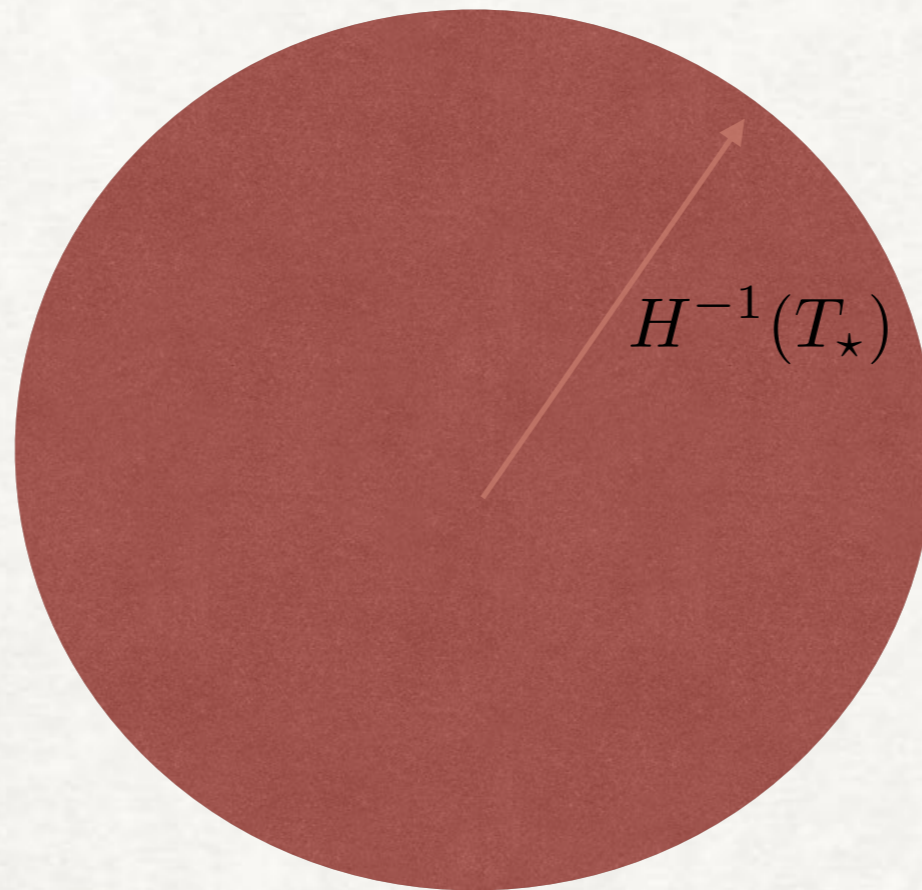
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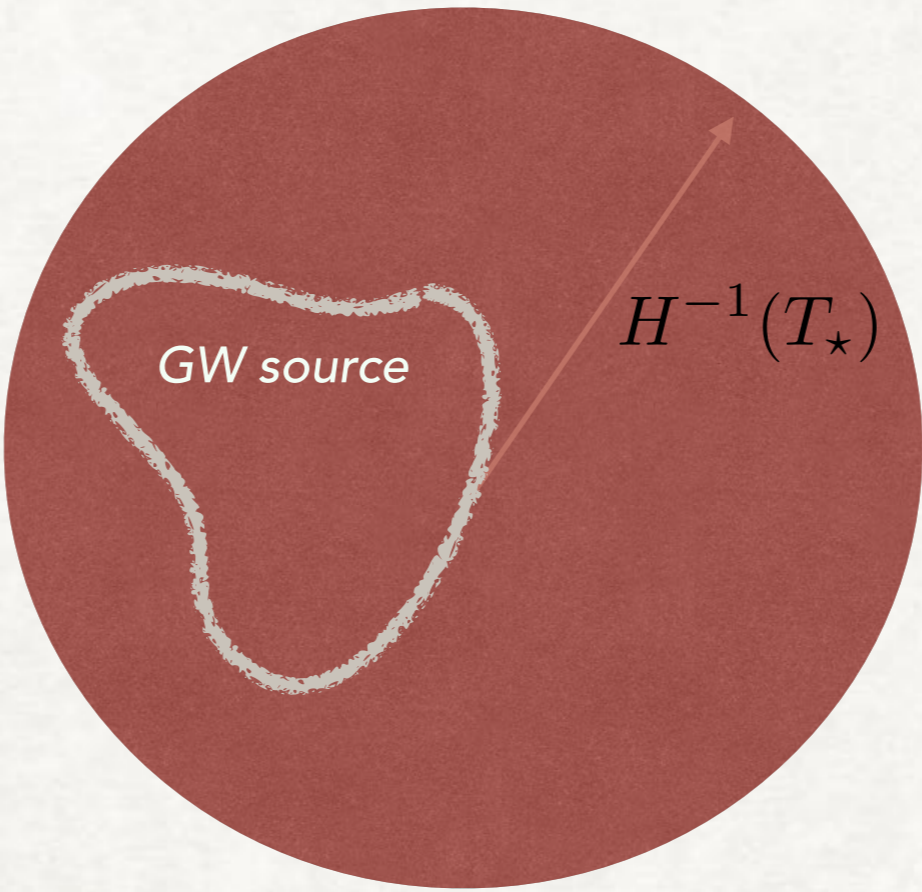
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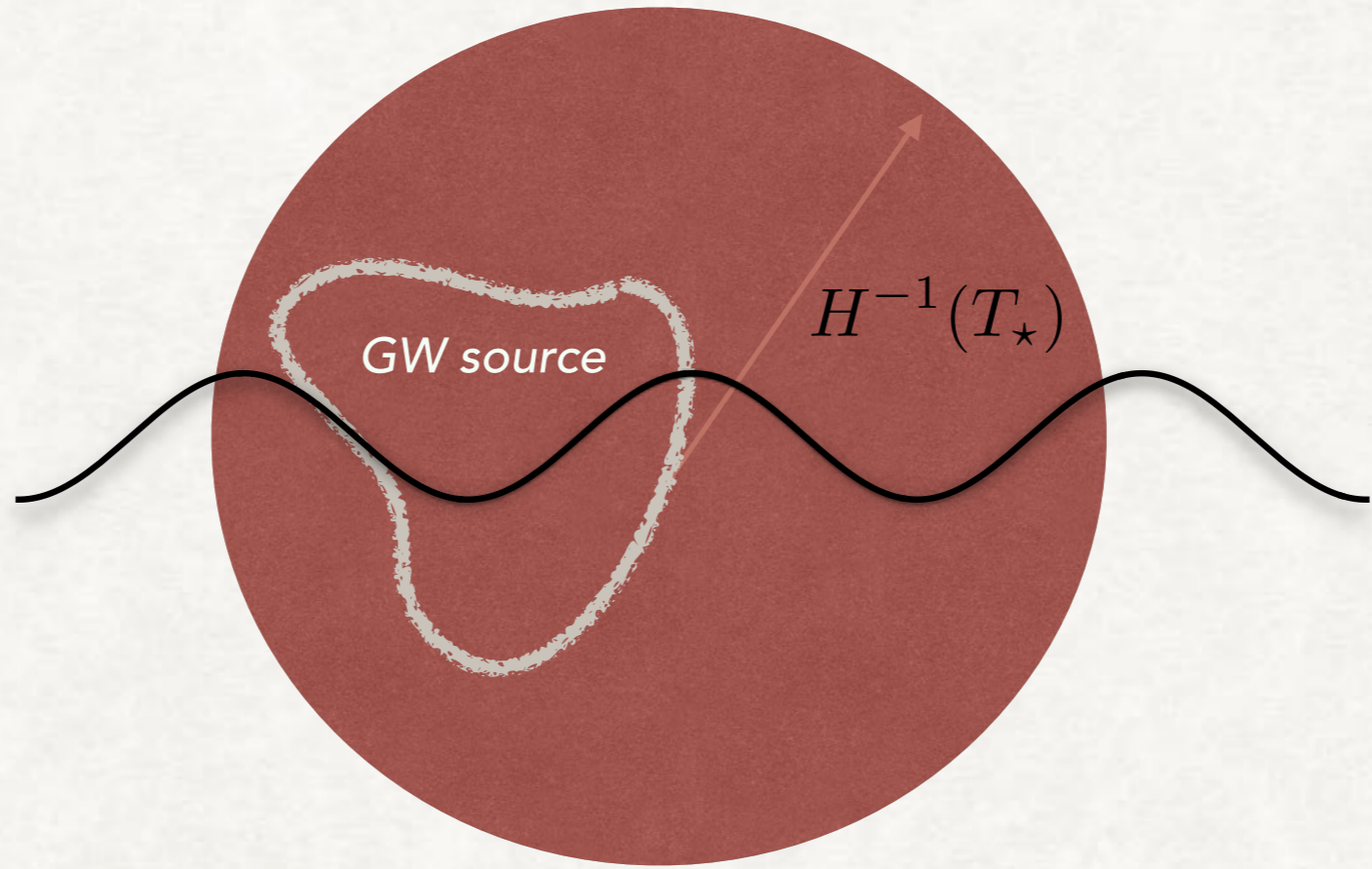
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Typical GW  
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$$f_\star \gtrsim 1/t_\star$$



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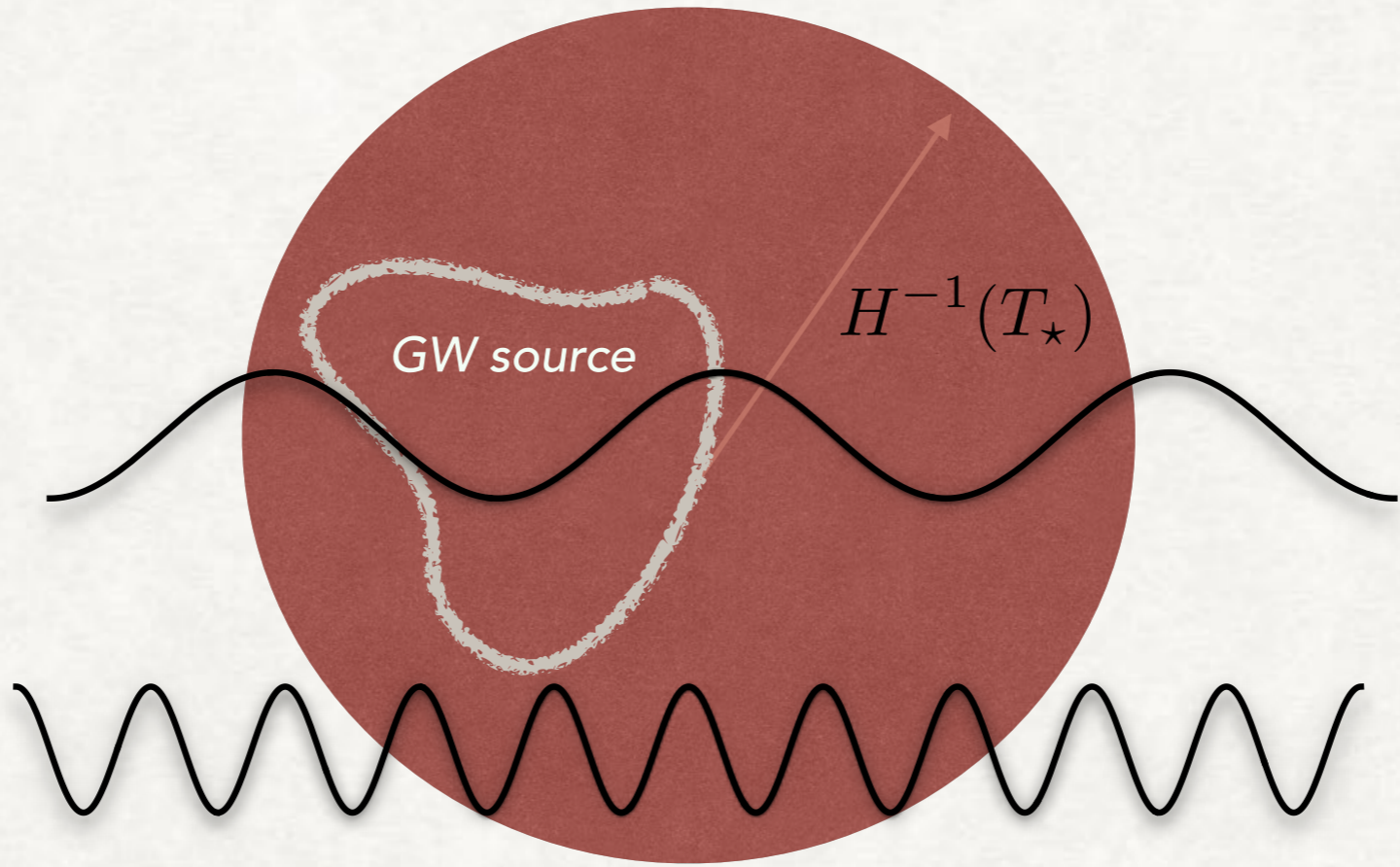
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Peak and high frequency tail probe  
microscopic properties of the  
source  
(Model-dependent)

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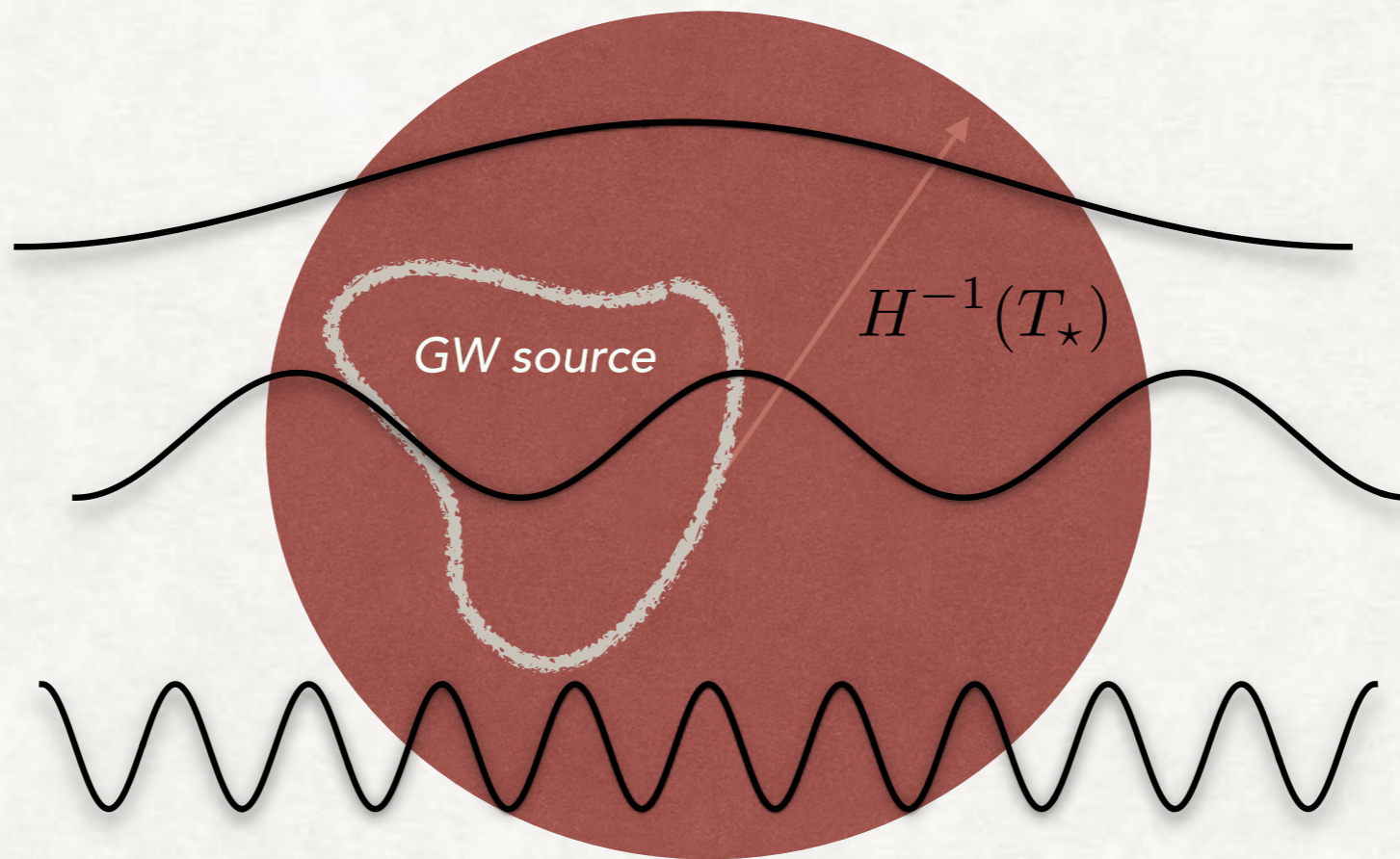
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$$\lambda_{\text{gw}} \gg H^{-1}(T_\star)$$

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Super-horizon  
modes cannot  
know about details  
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(Causality):  
Model-  
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Peak and high frequency tail probe  
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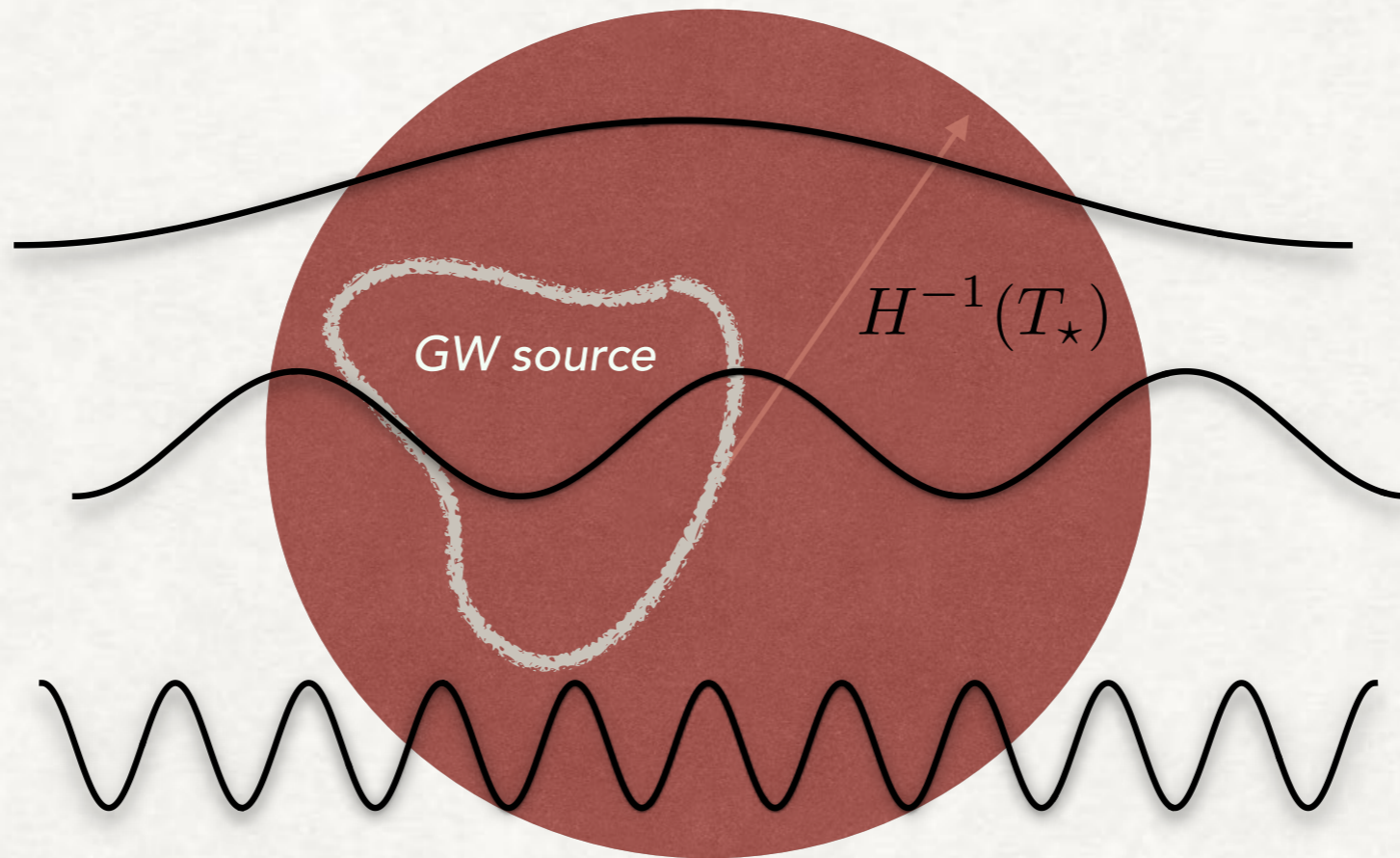
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Super-horizon  
modes cannot  
know about details  
of source  
(Causality):  
Model-  
independent

Overdamped  
harmonic  
oscillator:  
Power is  
suppressed!

Peak and high frequency tail probe  
microscopic properties of the  
source  
(Model-dependent)

# COSMOLOGICAL GW SPECTRUM

$$\Omega_{\text{gw}}(f) \equiv \frac{d\rho_{\text{gw}}}{d \ln f} / (3H_0^2 M_p^2)$$

Modes that are super-horizon at the time when sub-Hubble source is active

$$\lambda_{\text{gw}} \gg H_{\star}^{-1}$$

Model-independent

$$\sim f^3$$

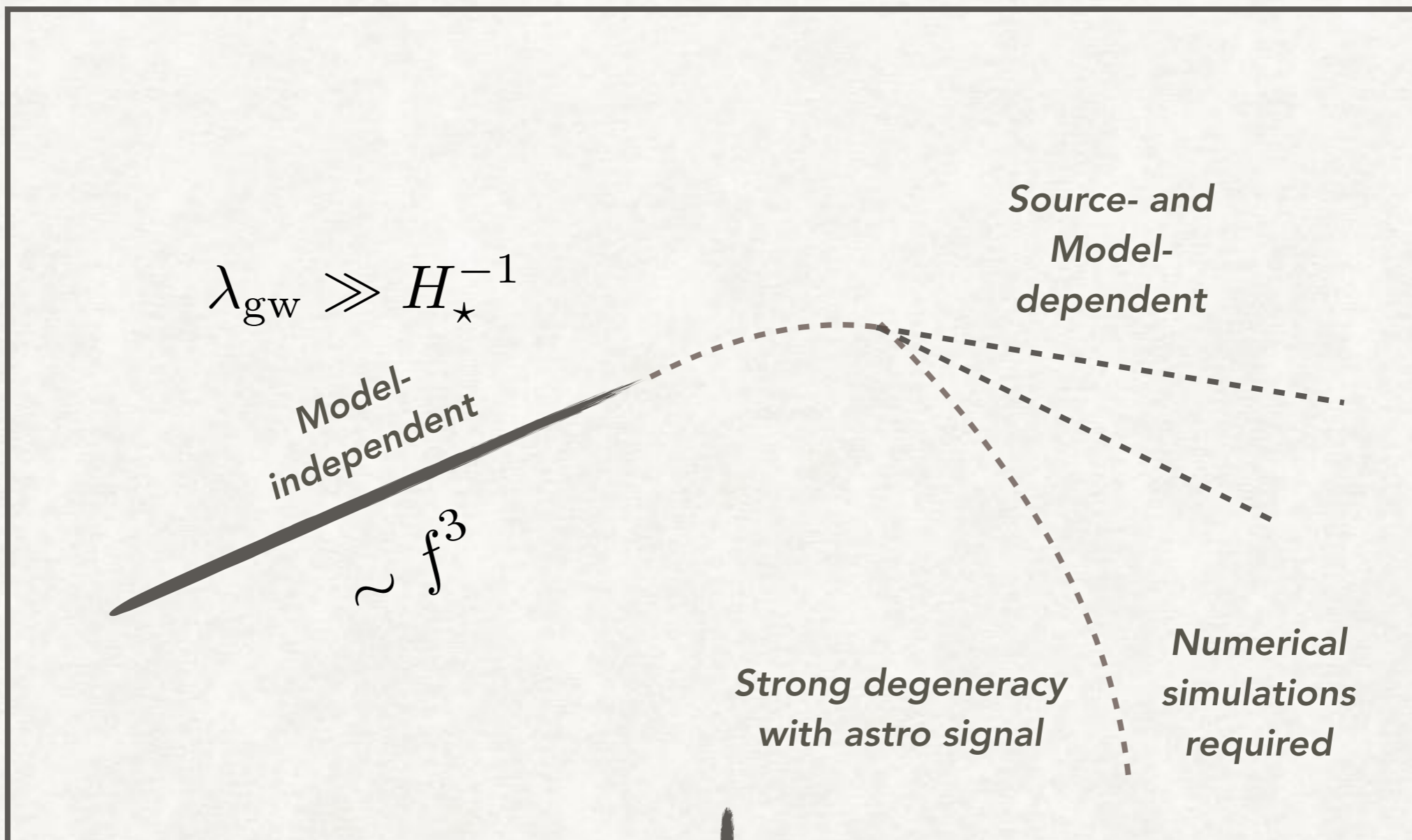
$$h_c(f) \simeq 10^{-9} \left( \frac{\text{nHz}}{f} \right) \sqrt{\Omega_{\text{gw}} h^2}$$

$$1 \quad f / f_{\star}$$



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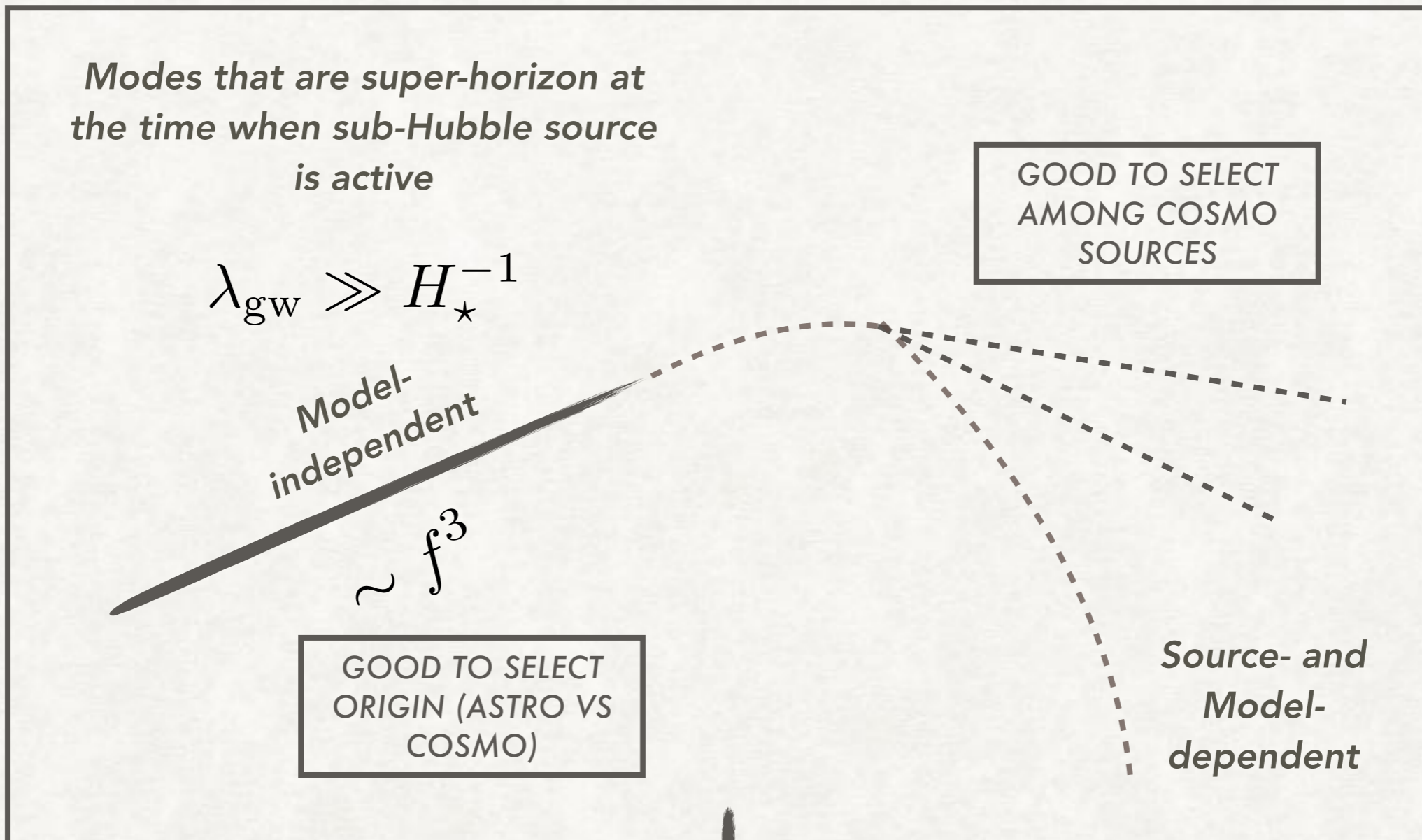


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$$f / f_*$$

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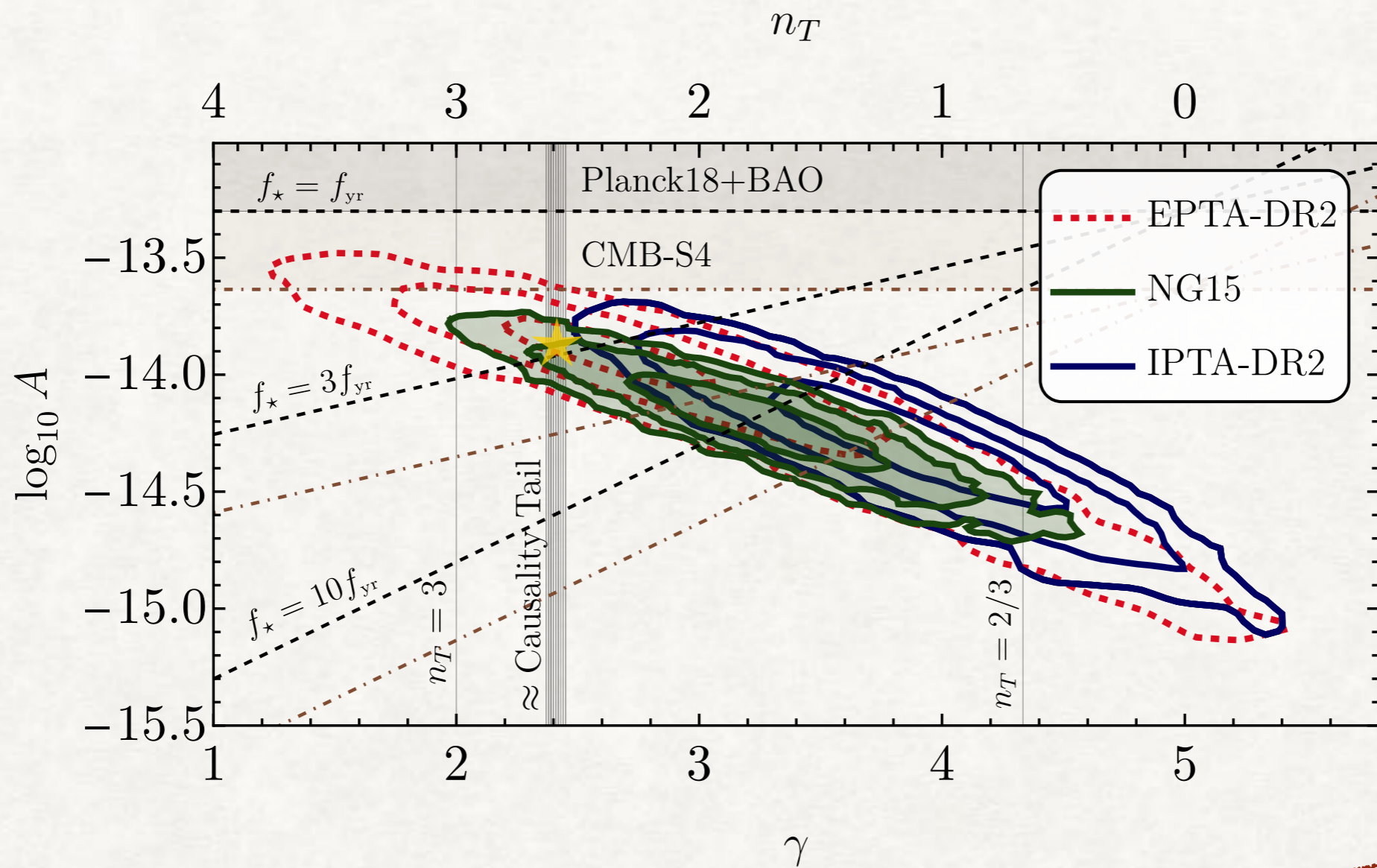
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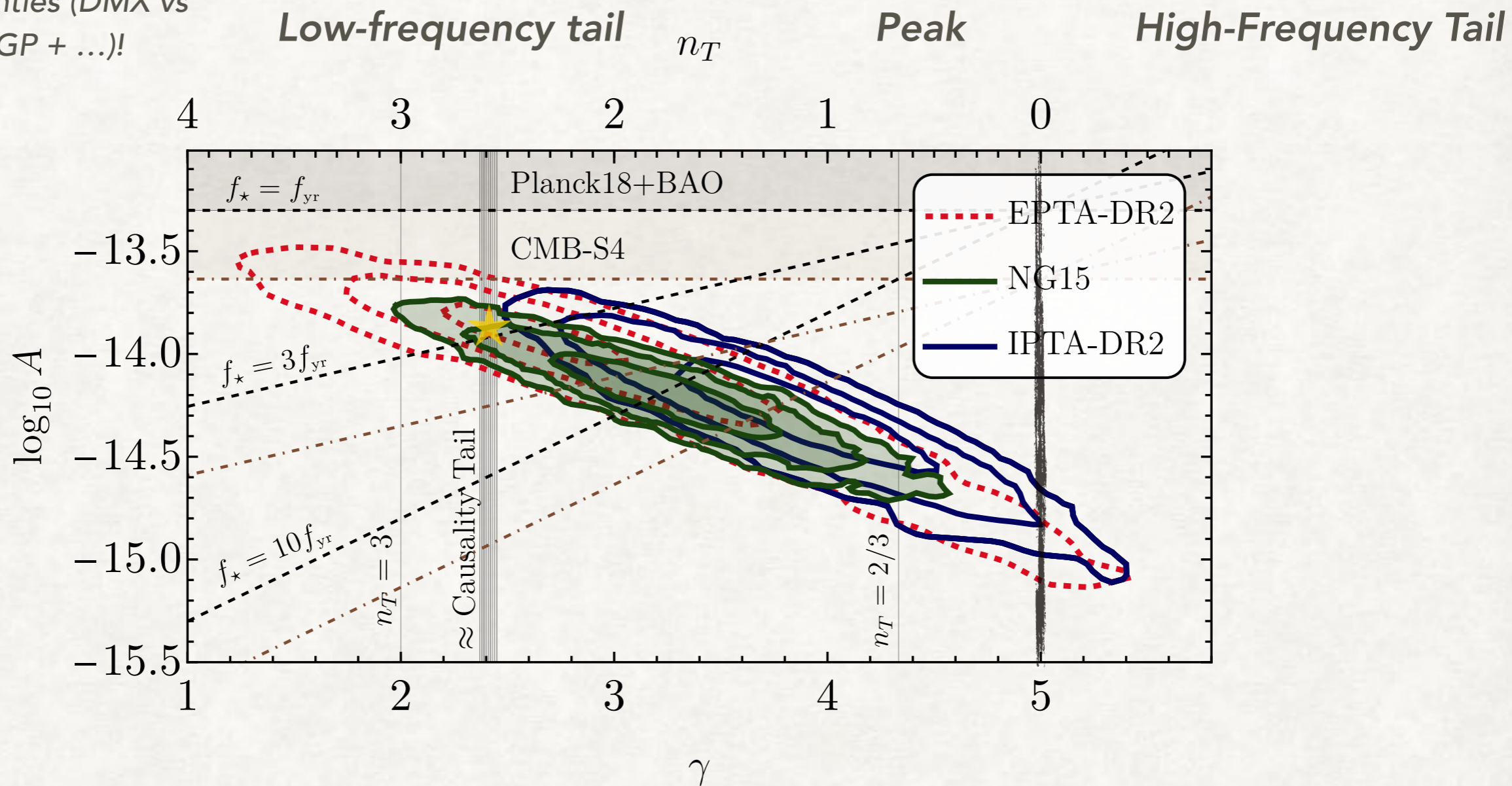
# DATA



$$\Omega_{\text{gw}} h^2 \simeq 10^{-8} \left( \frac{A}{5 \cdot 10^{-15}} \right)^2 \left( \frac{f}{f_{\text{yr}}} \right)^{5-\gamma} \equiv n_T$$

# DATA

**Caveat:**  
 Determination of tilt  
 suffers from  
 uncertainties (DMX vs  
 DMGP + ...)!

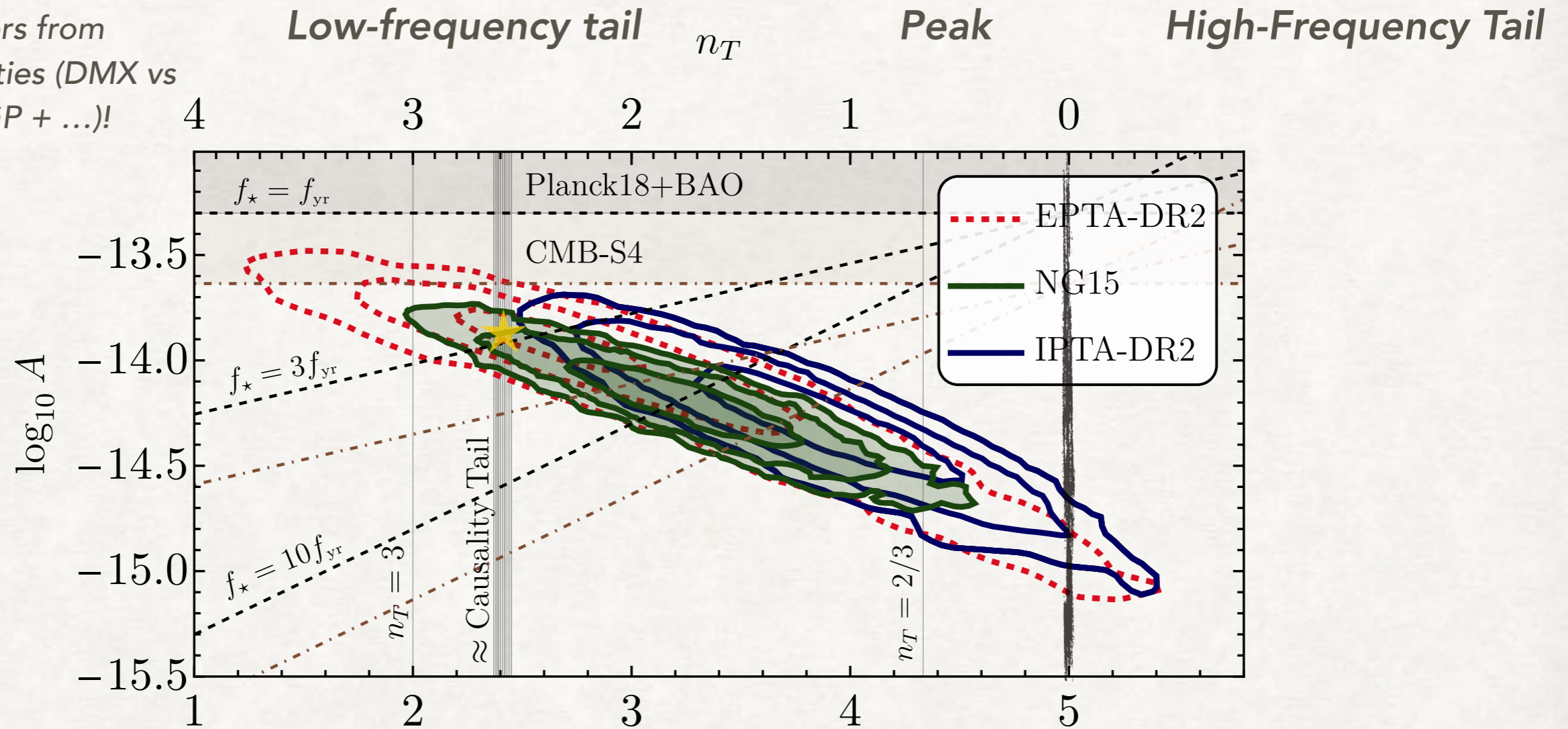


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# MODEL-INDEPENDENT CONSTRAINT FROM COSMOLOGY

**Caveat:**

Determination of tilt  
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$f_\star \equiv$  Cutoff of power-law/  
peak

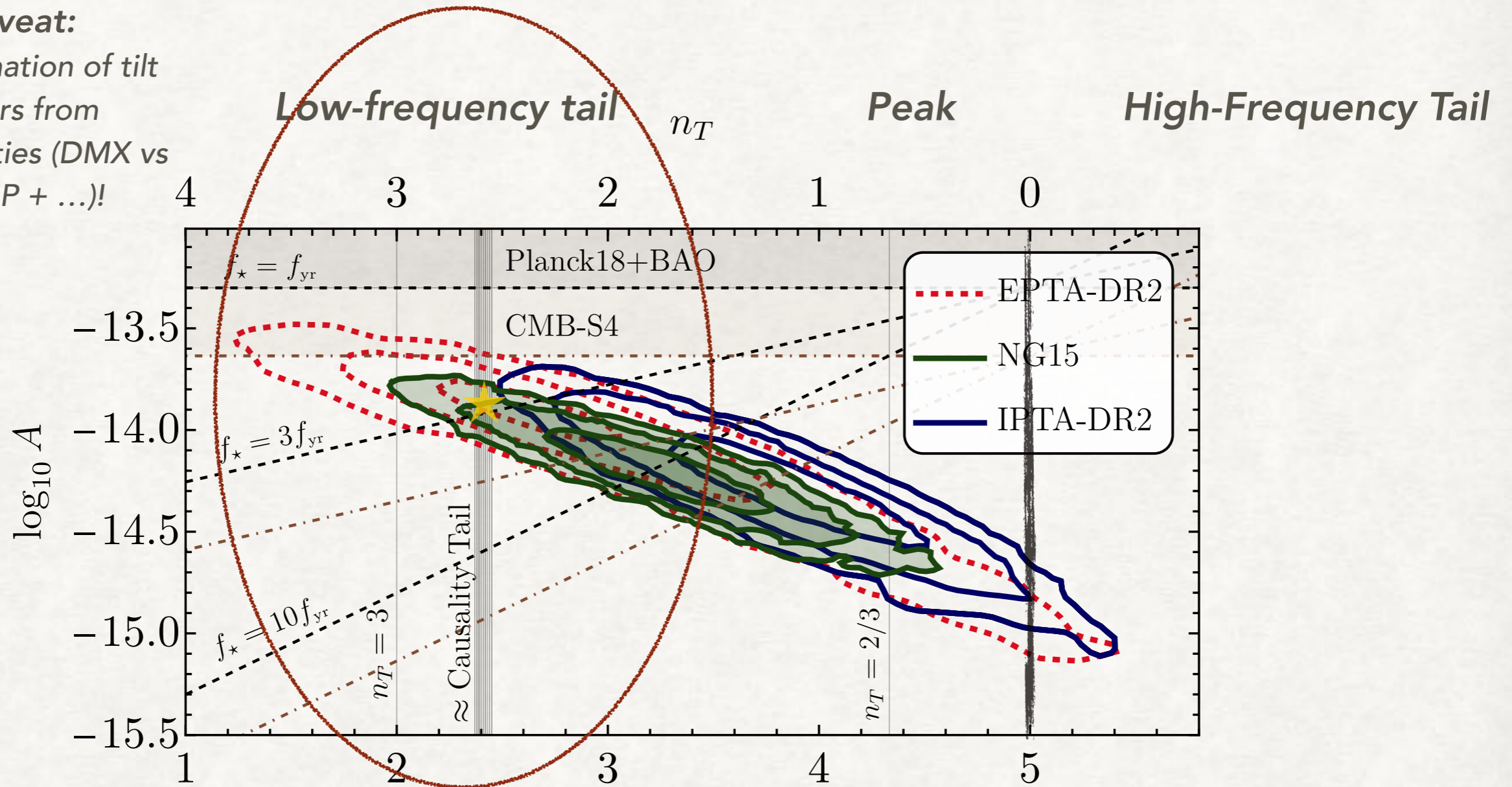
$\gamma$   
Prior for any search for cosmological backgrounds

$$\Delta N_{\text{eff}}^{\text{gw}} \equiv \frac{\rho_{\text{gw}}}{\rho_{\nu,1}} \Big|_{\text{cmb}} \leq 0.28(0.06), 95\% \text{C.L.} \Rightarrow A \leq 5(1) \cdot 10^{-14} \left( \frac{f_{\text{yr}}}{f_\star} \right)^{\frac{5-\gamma}{2}}$$

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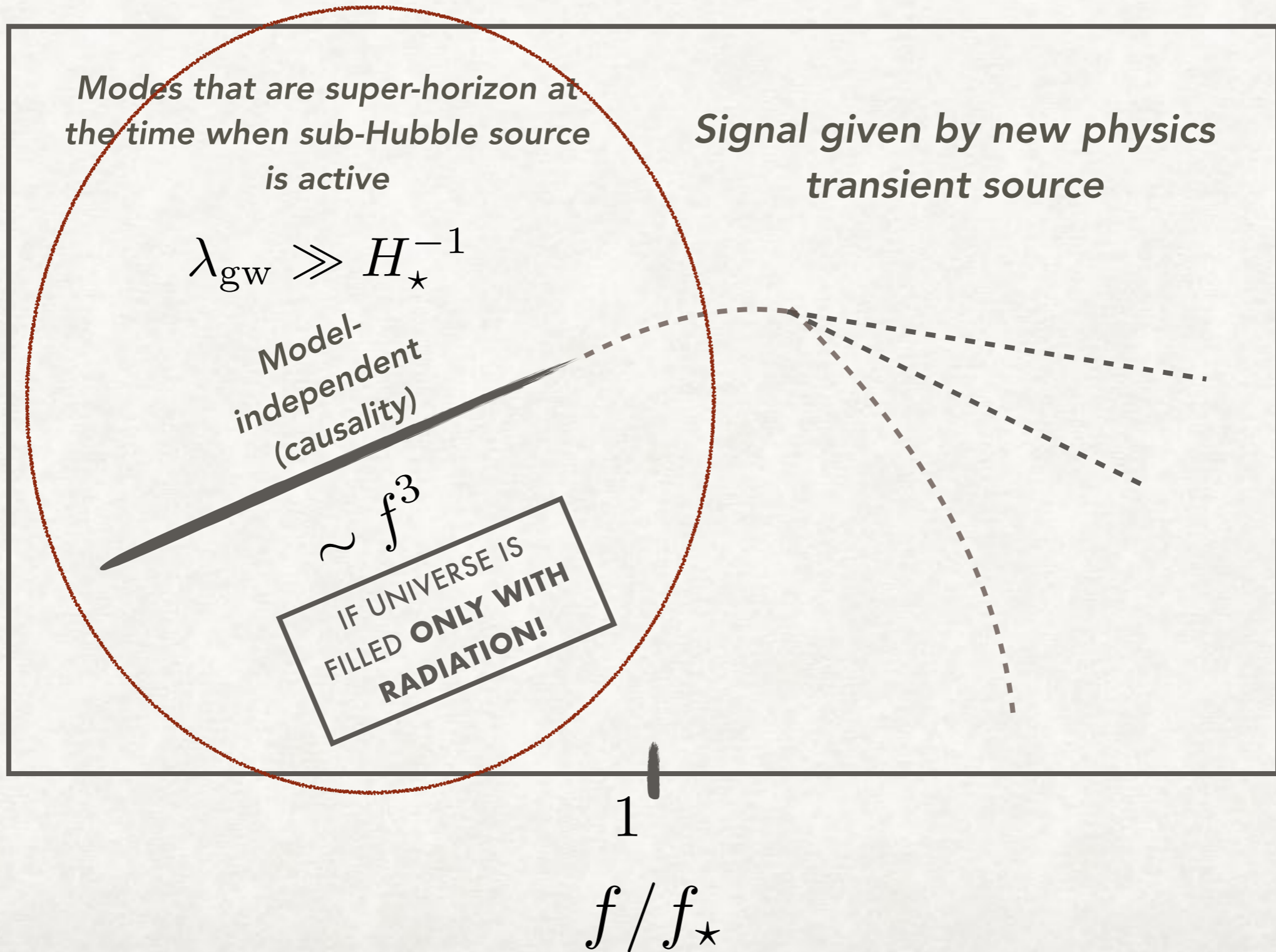
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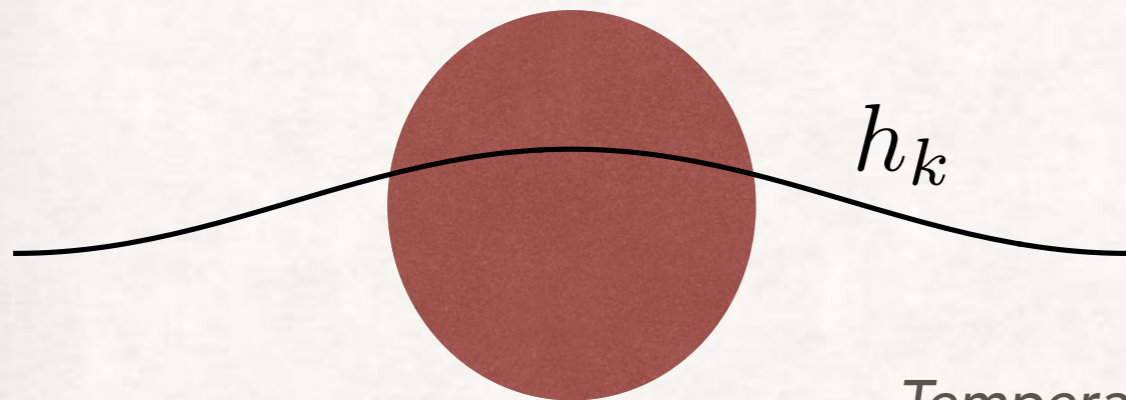
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# DISTINCTIVE FEATURES IN THE CAUSALITY TAIL

$$\Omega_{\text{gw}}(f) \equiv \frac{d\rho_{\text{gw}}}{d \ln f} / (3H_0^2 M_p^2)$$



# A FORTUITOUS COINCIDENCE

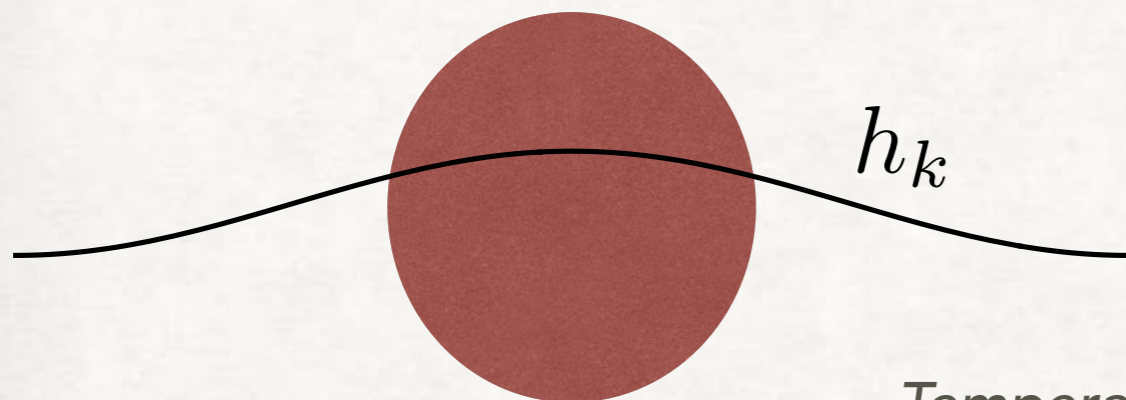


$$k \ll aH(T_*)$$

*Temperature  
until which  
source is active*



# A FORTUITOUS COINCIDENCE

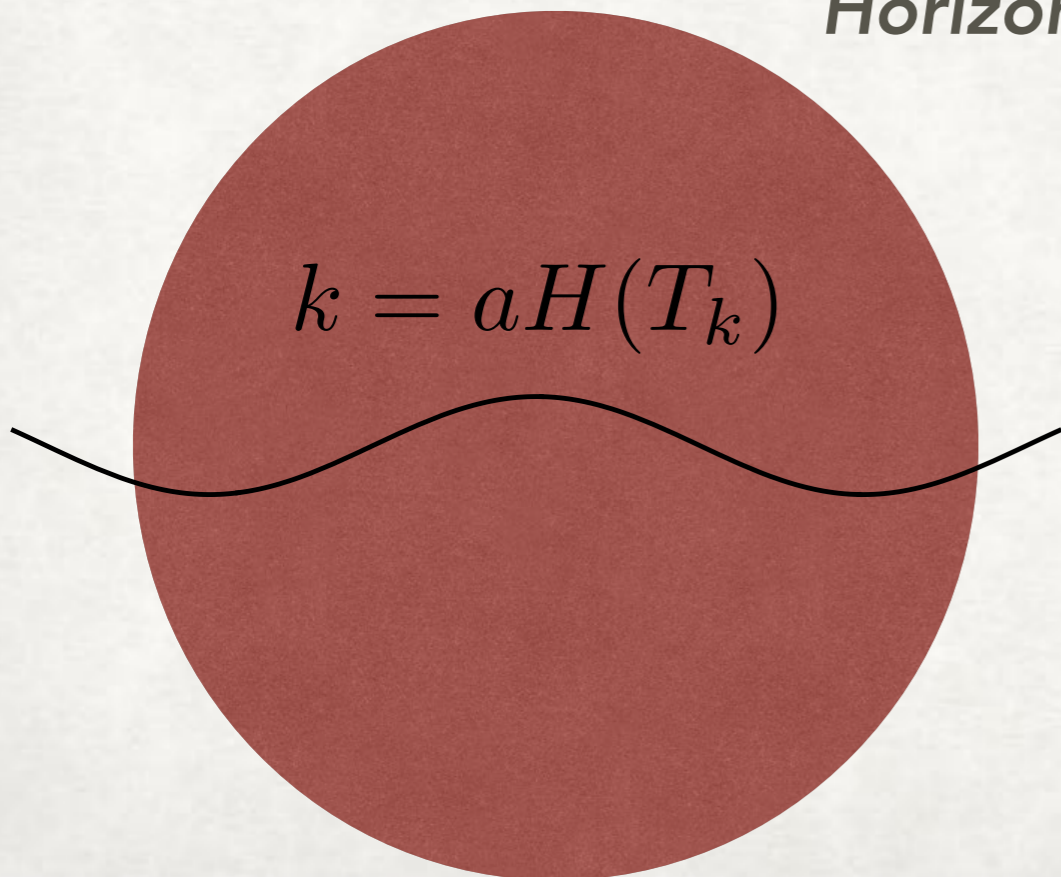


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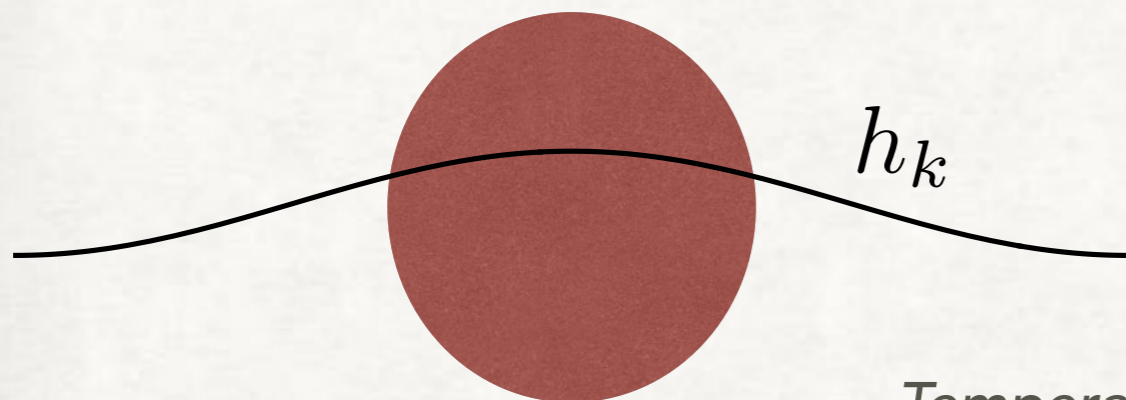
Temperature  
until which  
source is active



**Frozen until  
Horizon entry**



# A FORTUITOUS COINCIDENCE



$h_k$

Frequency of "Causality Tail" modes

$$k \ll aH(T_*)$$

Temperature  
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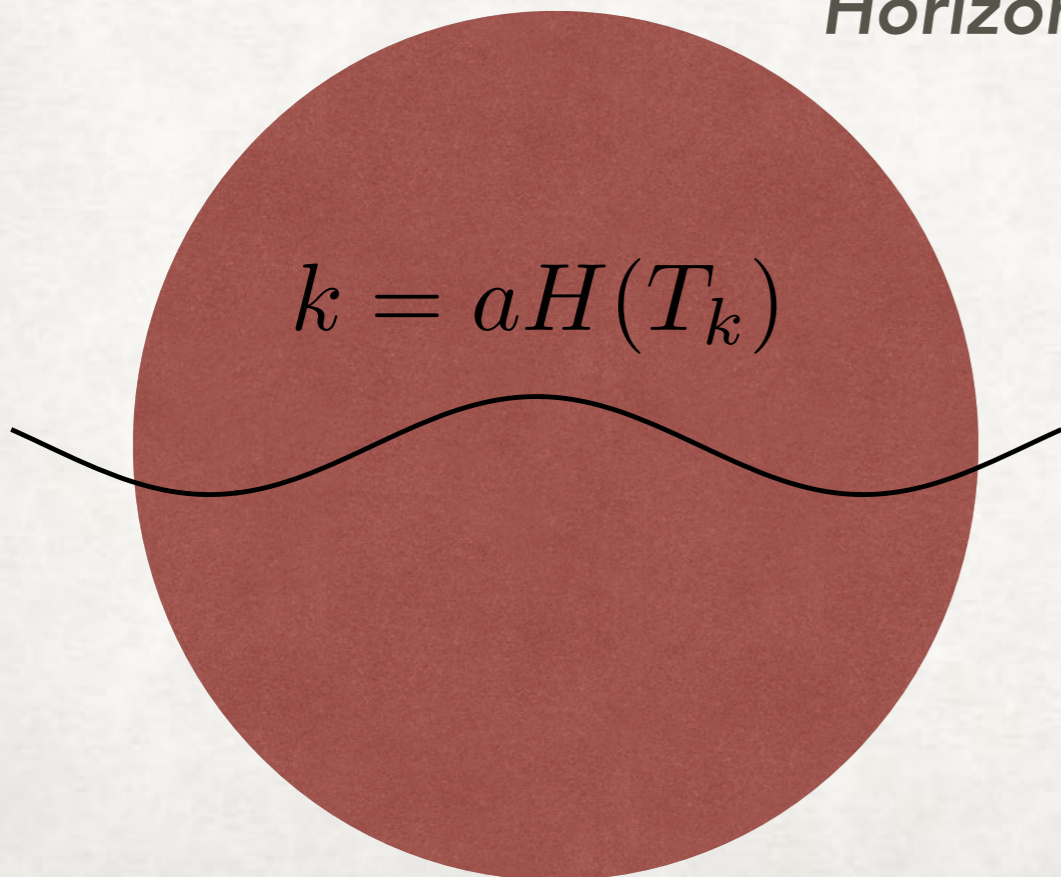
$$f = \frac{k}{2\pi} = aH(T_k)$$



Frozen until  
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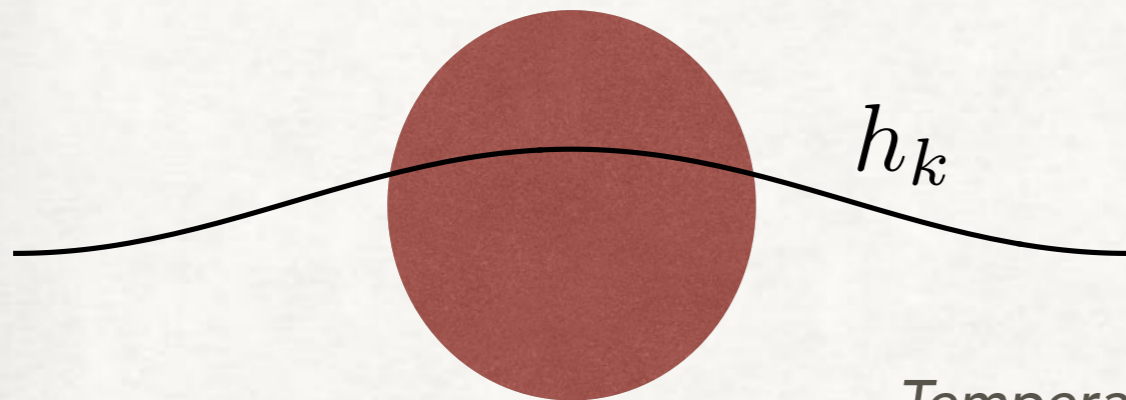
Redshift



$$k = aH(T_k)$$

$$f \simeq 3.0 \text{ nHz} \cdot \left( \frac{g_{*,s}(T)}{20} \right)^{1/6} \left( \frac{T}{150 \text{ MeV}} \right).$$

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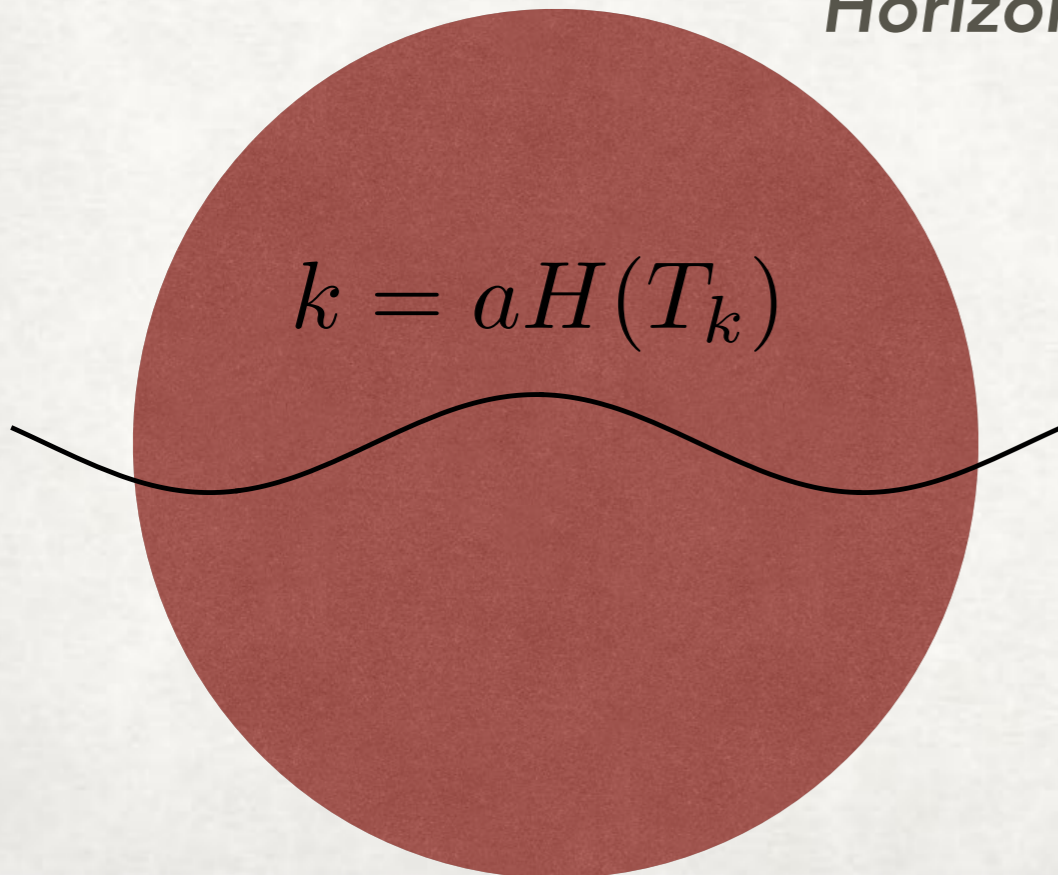
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*Notice: different from usual relation for peak frequency!*

Region where PTAs are most sensitive coincides with modes that enter horizon during confinement of strong interactions (QCD)!

# QCD EFFECTS ON COSMOLOGICAL EVOLUTION

*Under most reasonable  
Circumstances*

*QCD crossover not expected to produce GWs*

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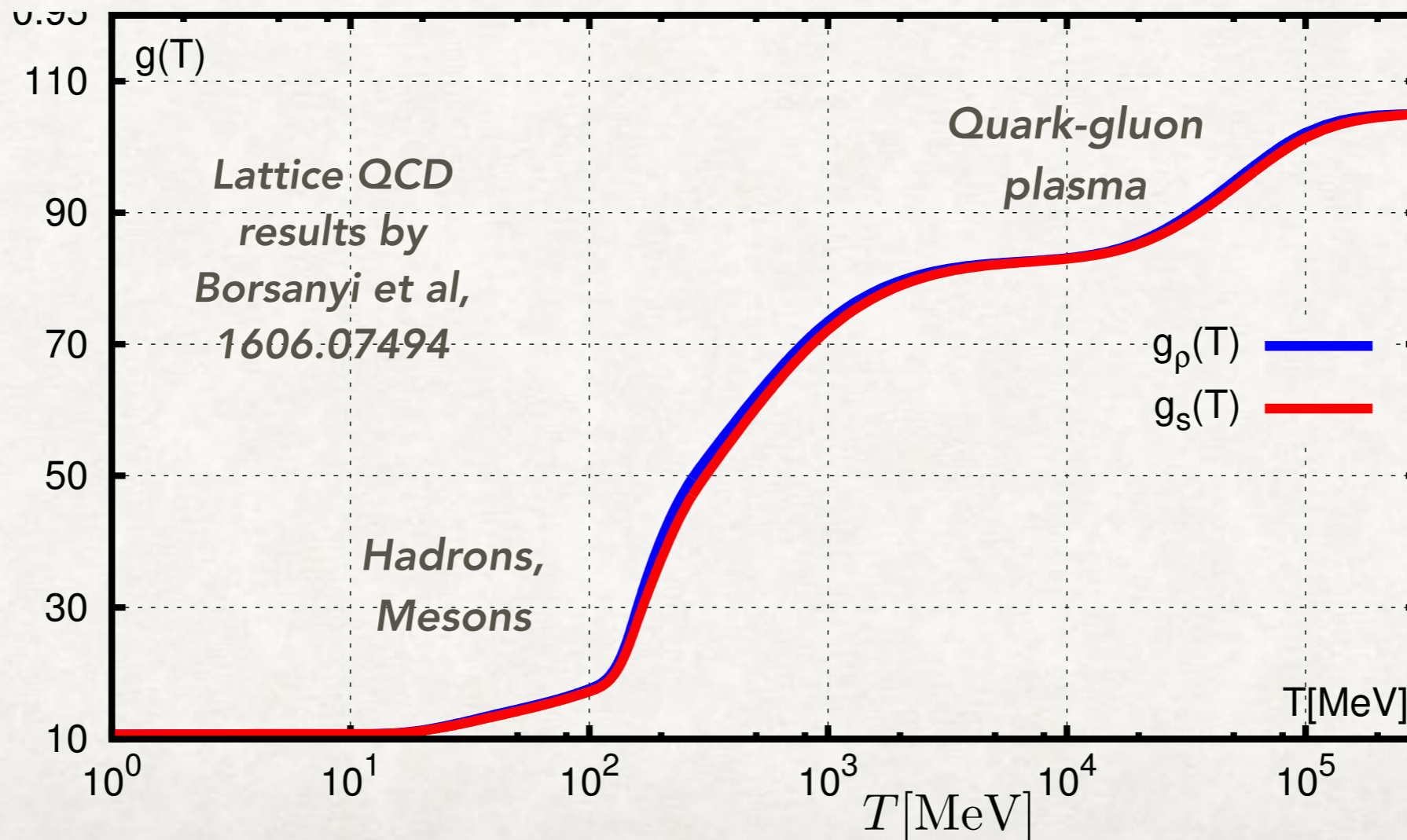
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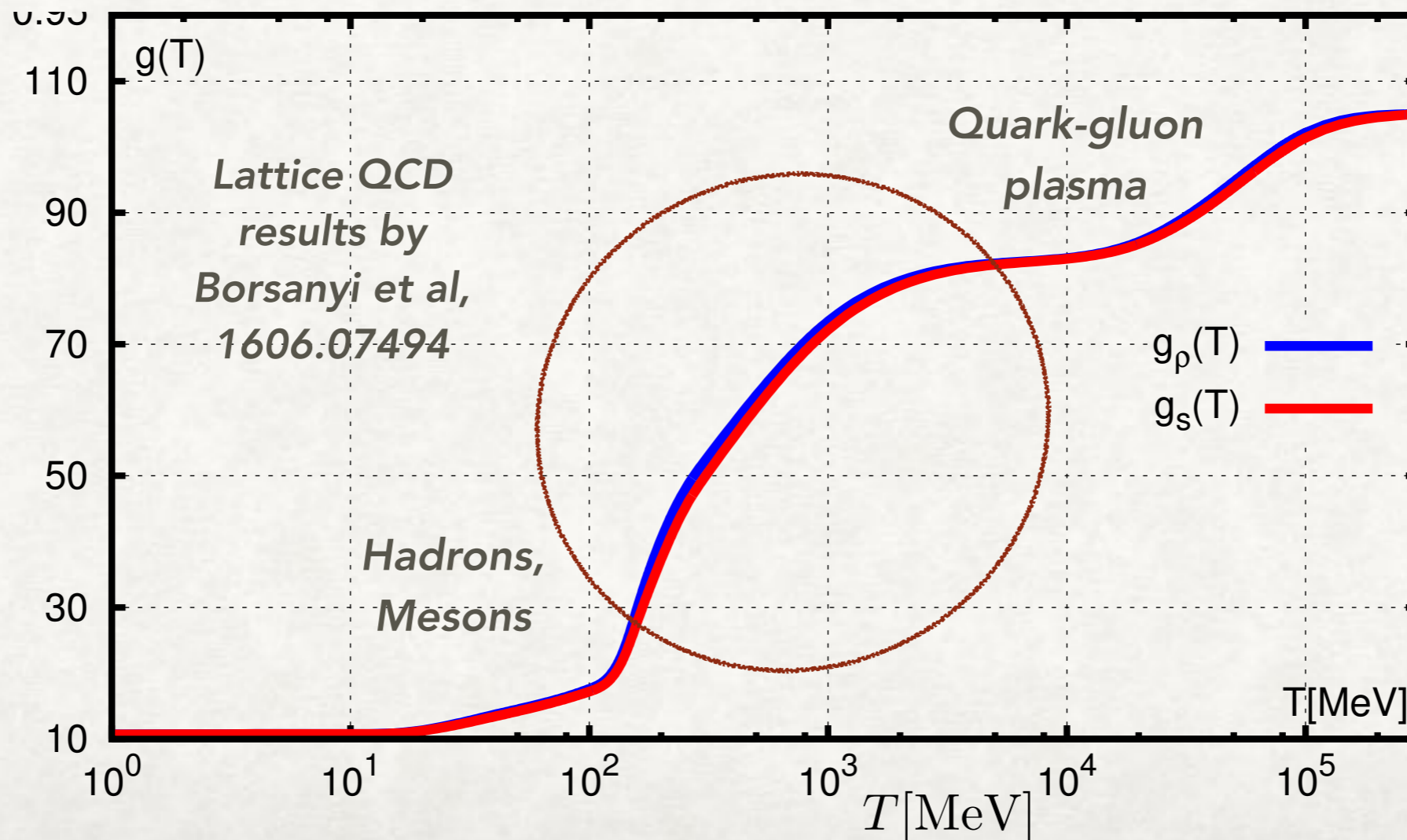
Nonetheless it affects cosmological evolution

Many particles become non-relativistic (hadronization) and  
their entropy is transferred to remaining light d.o.f.s

Energy and Entropy  
Densities

$$s \sim g_{*,s} T^3$$

$$\rho \sim g_* T^4$$



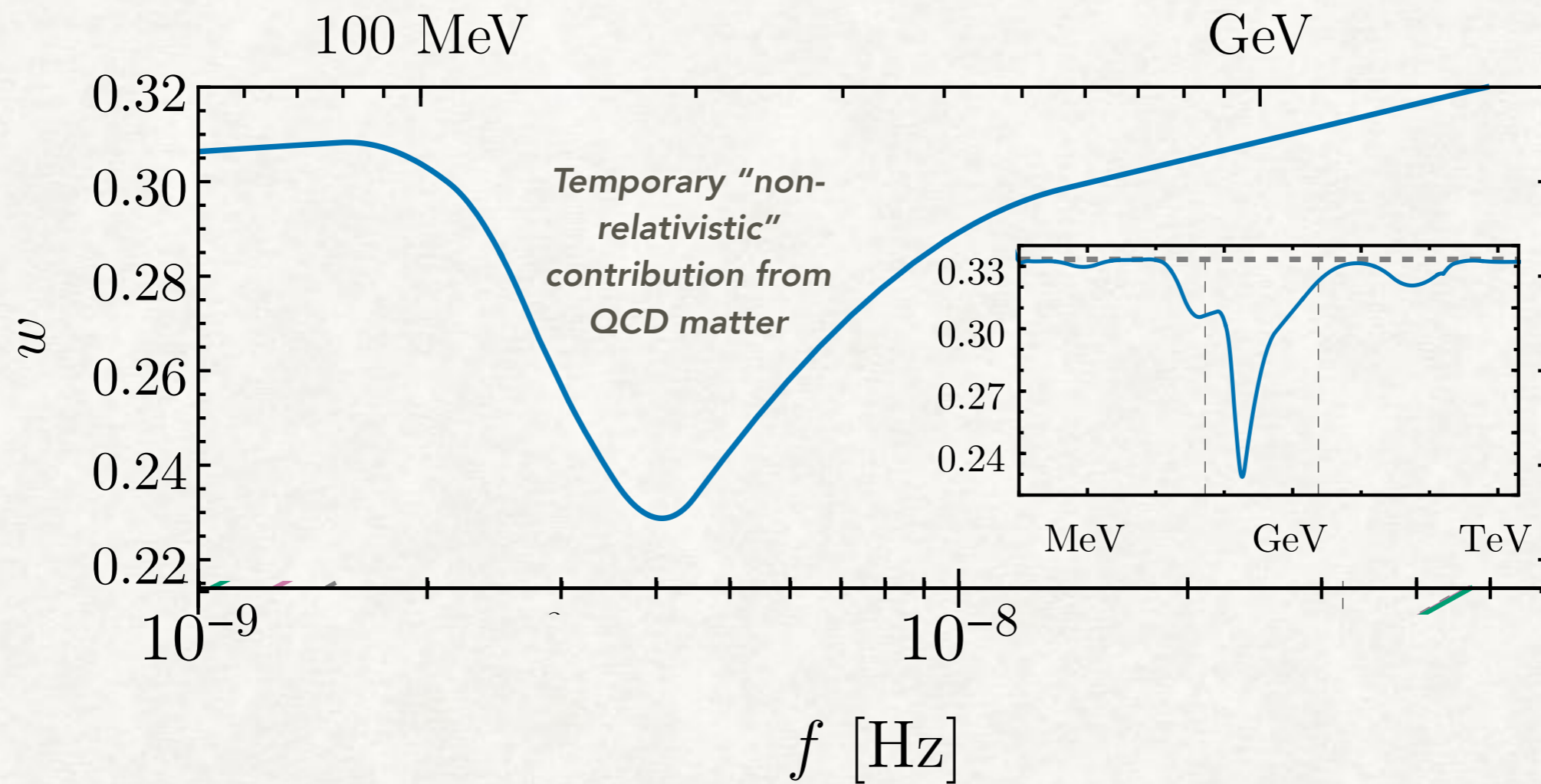
# EQUATION OF STATE

$$w \equiv \frac{p}{\rho} = \frac{4}{3} \frac{g_{*,s}(T)}{g_*(T)} - 1$$



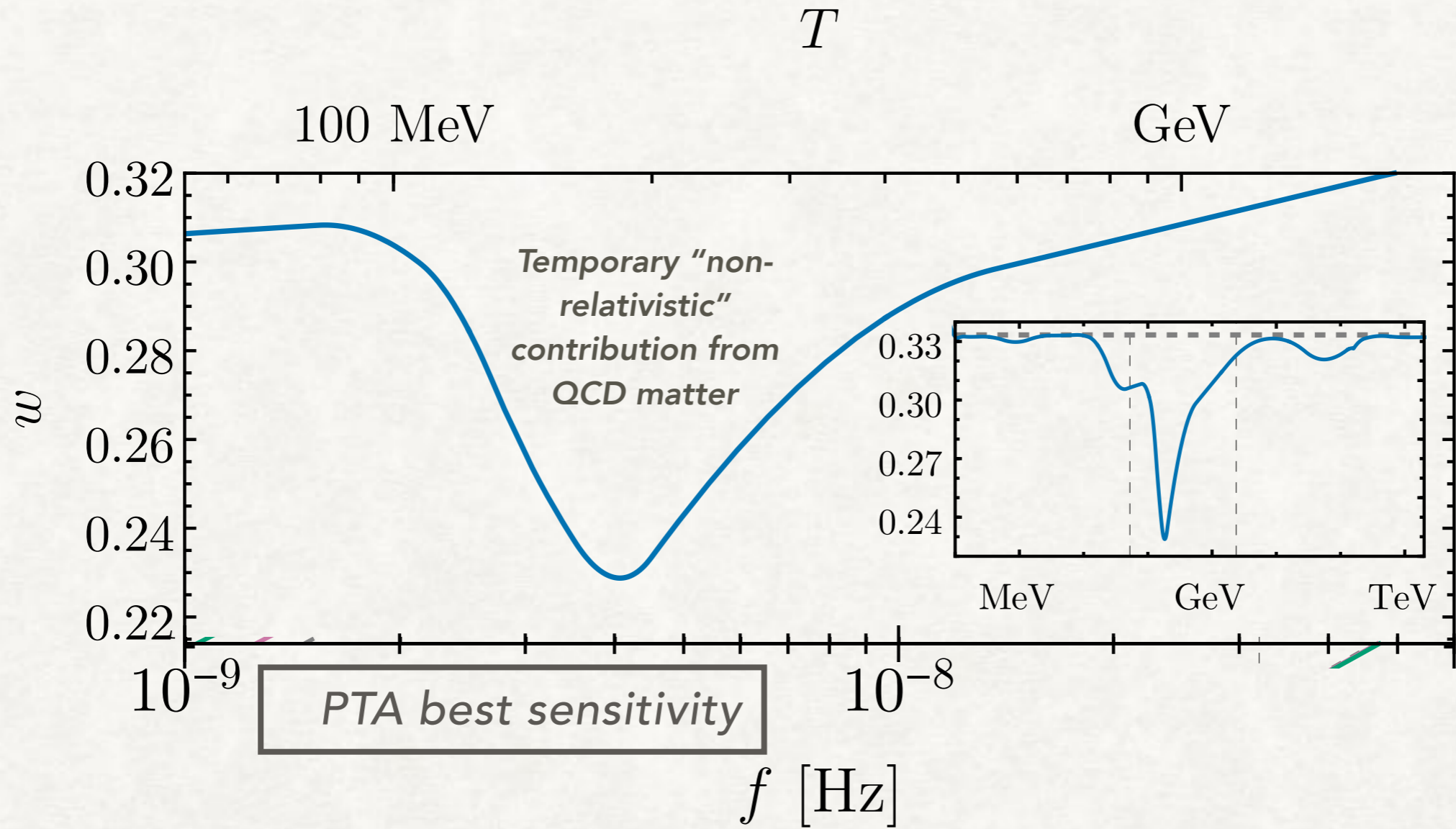
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# EQUATION OF STATE

Standard Model prediction:  
 ~30% deviation from radiation domination around QCD crossover!



$$w \equiv \frac{p}{\rho} = \frac{4}{3} \frac{g_{*,s}(T)}{g_*(T)} - 1$$

# IMPRINTS OF QCD ON GWS

*Low-frequency super-horizon GW modes evolve differently from sub-horizon modes*

*They are less excited (overdamped) by the source*

*But their amplitude stays frozen until horizon re-entry!*

See:

*../Hook, Racco, Marques-Tavares 20*

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$$\frac{d\Omega_{\text{gw}}}{d \ln f} \Big|_{\text{Early Universe}} = \frac{d\rho_{\text{gw}}}{d \ln f} \Big|_{f \ll f_\star} \propto f^{3+2\frac{3w-1}{3w+1}}$$

*Background Equation of State*



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*f* ≪ *f*<sub>★</sub>

Background Equation of State

*Shallower Causality Tail spectrum for*  $0 \leq w < 1/3$

See:

../Hook, Racco, Marques-Tavares 20

# IMPRINTS OF THE QCD CROSSOVER ON CAUSALITY TAIL

Low-frequency super-horizon GW modes evolve differently from sub-horizon modes

They are less excited (overdamped) by the source

But their amplitude stays frozen until horizon re-entry

Causality Tail Spectral Shape depends on



$$\frac{d\Omega_{\text{gw}}}{d \ln f} \Big|_{\text{Early Universe}} = \frac{d\rho_{\text{gw}}}{d \ln f} \rho_{\text{rad}}$$

$$\propto f^{3+2\frac{3w-1}{3w+1}}$$

Background  
Equation of State

**Intuition:**

Sub-horizon modes dilute faster for  $w < 1/3$   
than in radiation domination

See:

../Hook, Racco, Marques-Tavares 20

$$\rho_{\text{sub}} \sim a^{-4} \quad a(t) \propto t^{\frac{2}{3(1+w)}}$$

# IMPRINTS OF THE QCD CROSSOVER ON CAUSALITY TAIL

*Spectral shape of low-frequency causality tail is independent of the microphysics of the source*

*See: Watanabe, Komatsu 06/  
Schettler + 10*

*But depends on*

*Background  
Equation of State*

$$\frac{d\Omega_{\text{gw}}}{d \ln f} \Big|_{\text{Early Universe}} = \frac{d\rho_{\text{gw}}}{d \ln f} \rho_{\text{rad}}$$

$$\propto f^{3+2\frac{3w-1}{3w+1}}$$

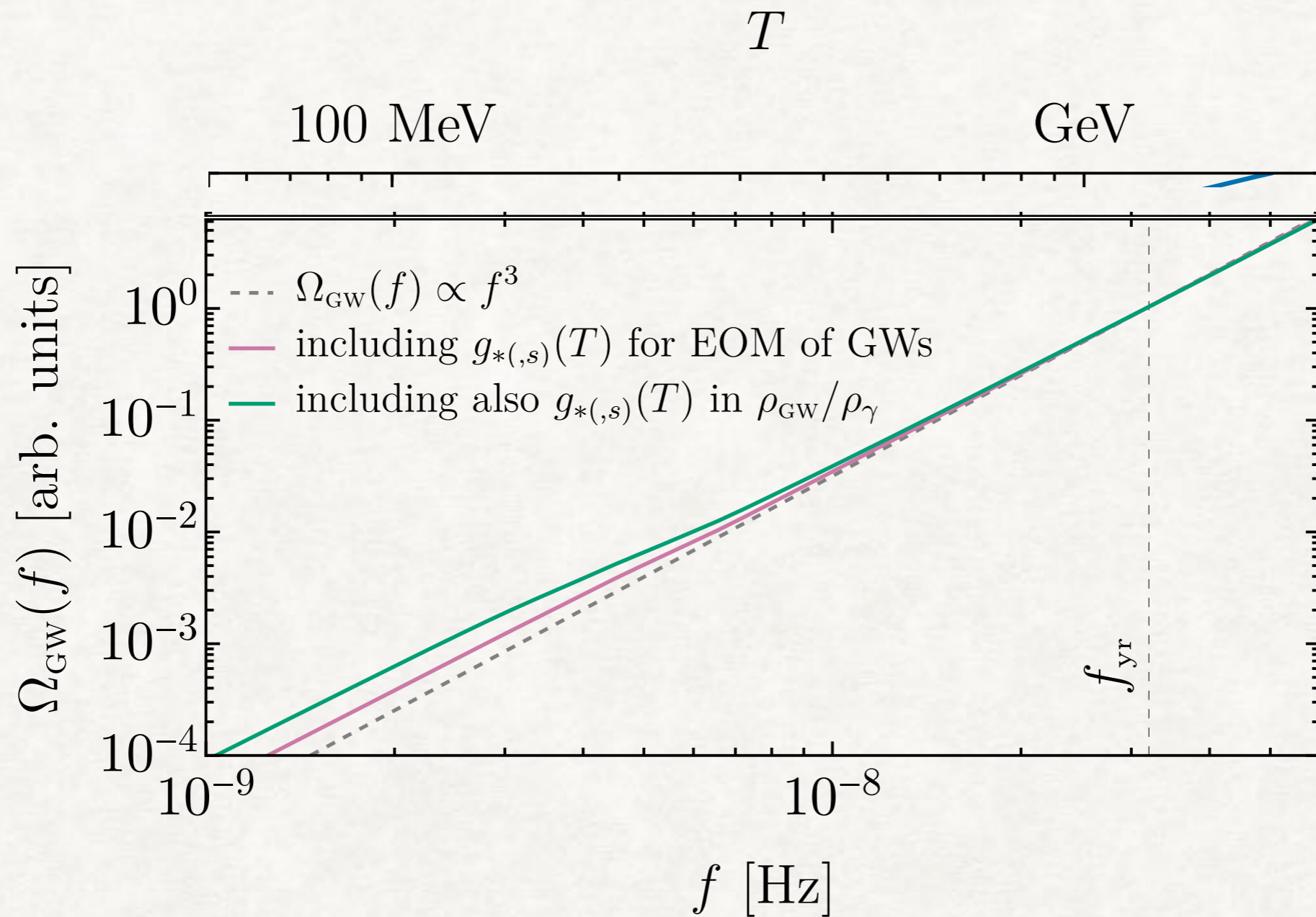
$$\propto g_{*,s}^{-\frac{4}{3}} g_*$$

*Additional effect*

*Redshifts as*

*Entropy injections  
only to Standard  
Model bath  
(GWs are decoupled)*

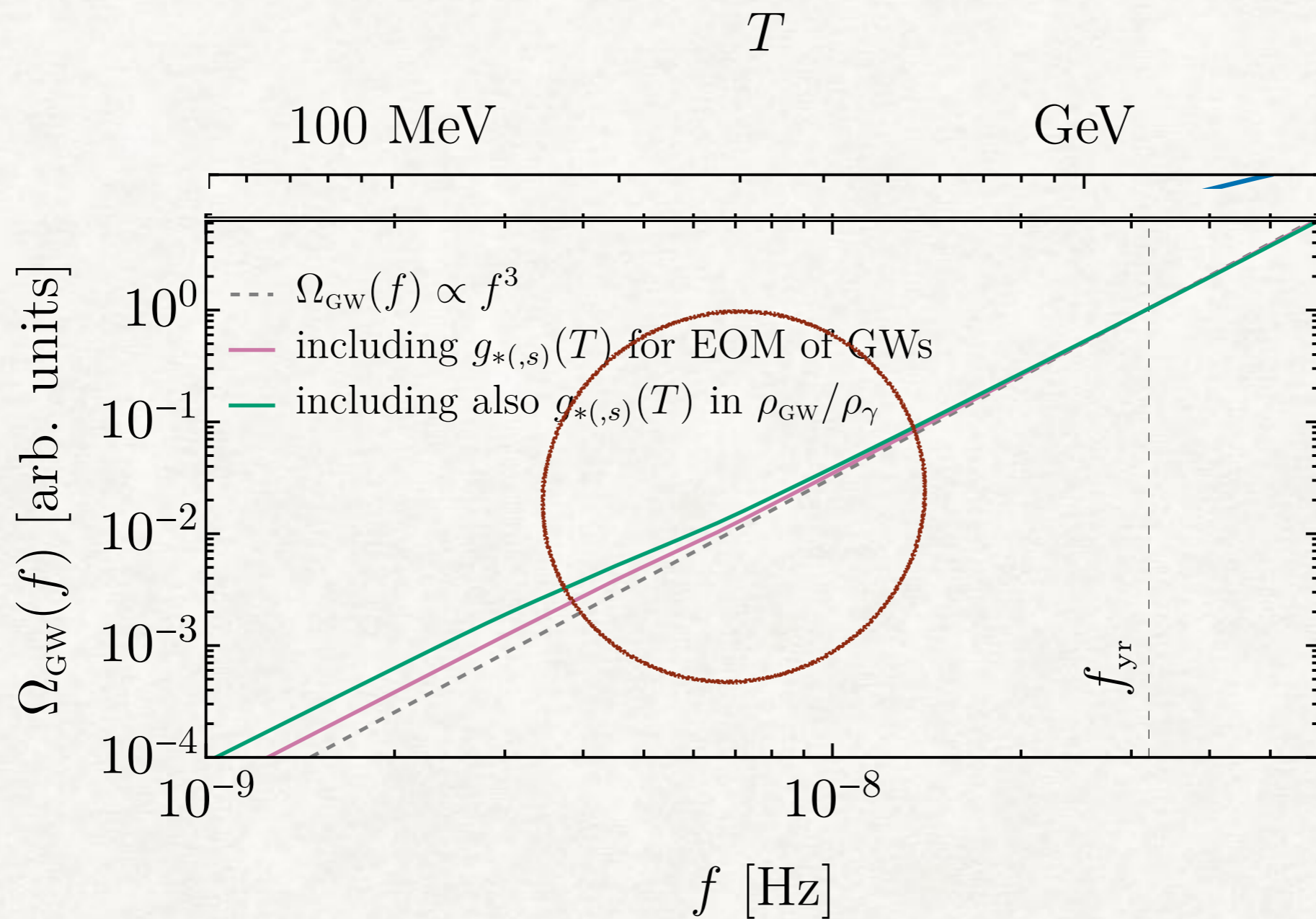
# THE CAUSALITY TAIL IN THE PTA BAND



**Relevant for all  
early Universe  
sources active  
slightly before  
QCD crossover!**



# THE CAUSALITY TAIL IN THE PTA BAND

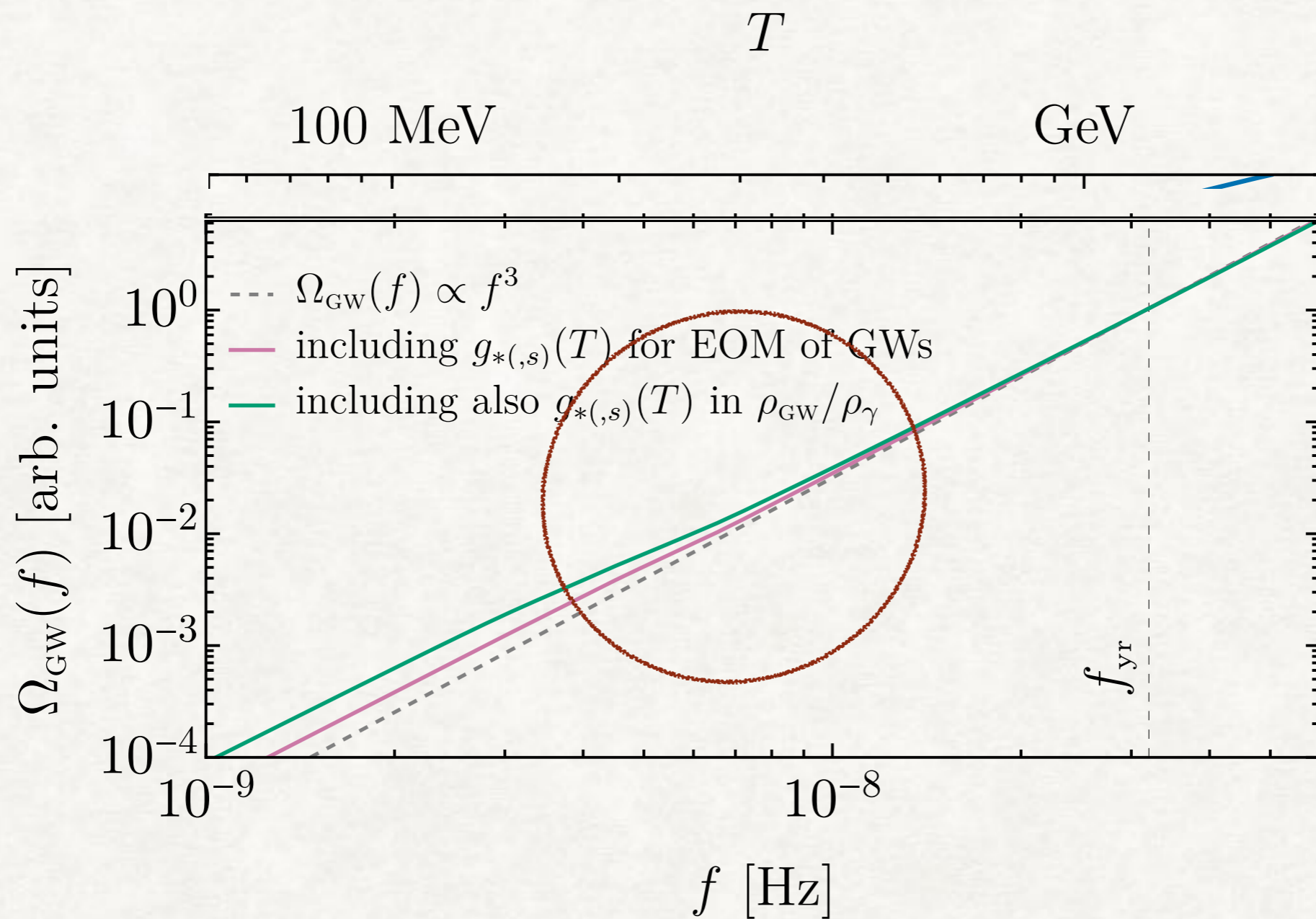


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*SM predicts distinctive frequency-dependent shape of the signal  
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*Amplitude in first bins 2-3 times larger than naive spectrum!*

# THE CAUSALITY TAIL IN THE PTA BAND



*Relevant for all sources active slightly before QCD crossover!*

*Tabulated spectrum provided for future searches!*

*SM predicts distinctive frequency-dependent shape of the signal (not simple power law)*

*Amplitude in first bins 2-3 times larger than naive spectrum!*

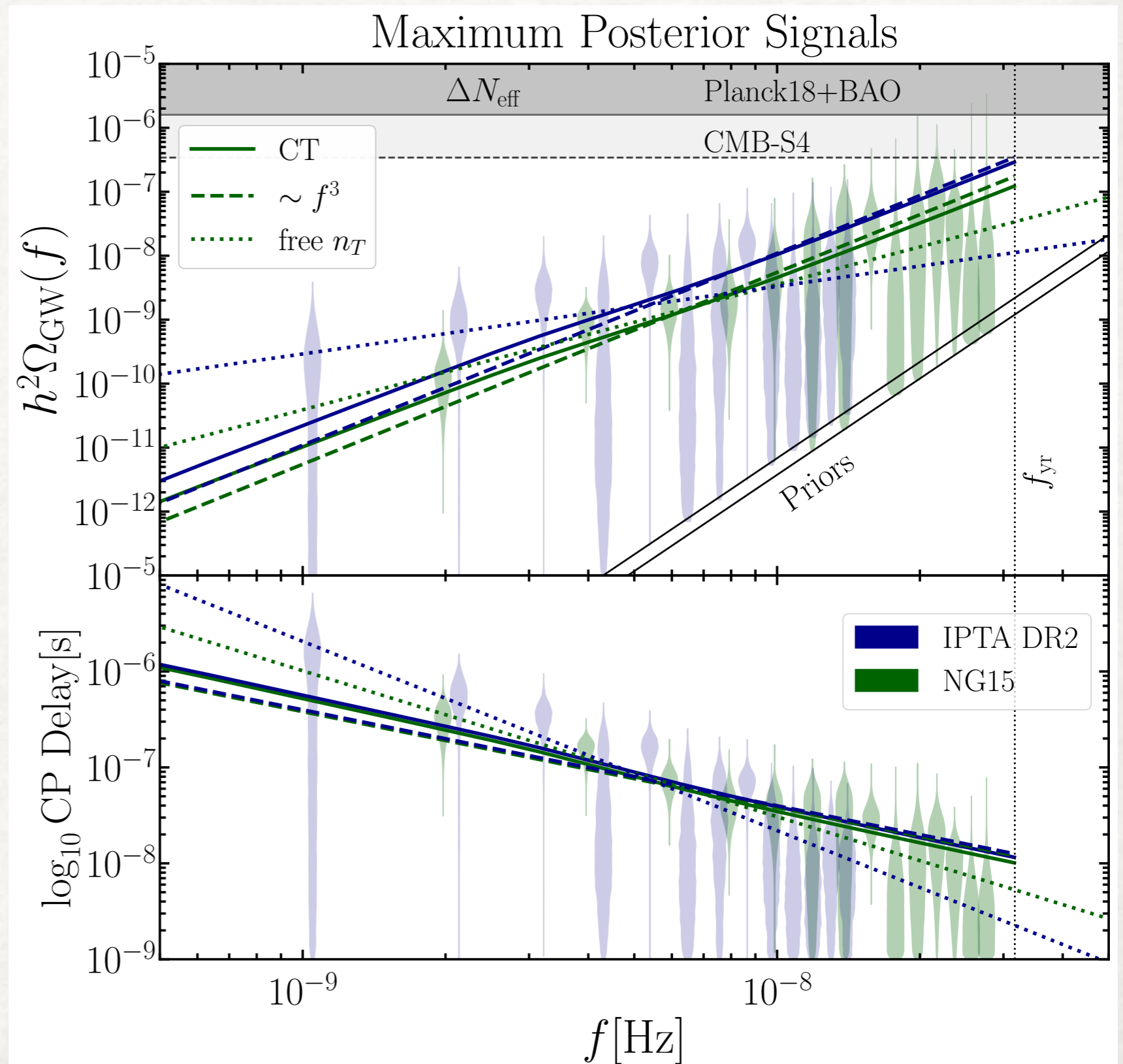
# IS THE SIGNATURE OBSERVABLE?

Bayesian analysis in  
International PTA DR2  
and NG15 datasets  
enterprise PTArcade

Bayes factor  
(Including CMB prior!)

$$\mathcal{B}_{\text{CT vs } f^3} \simeq 20 - 40$$

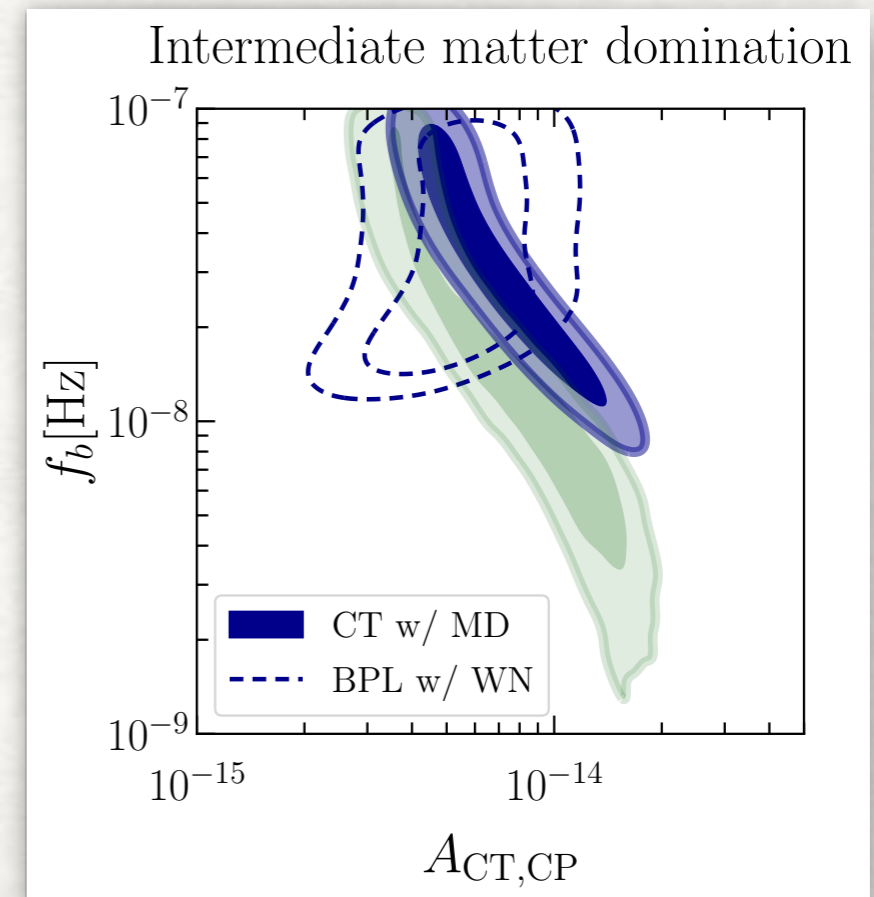
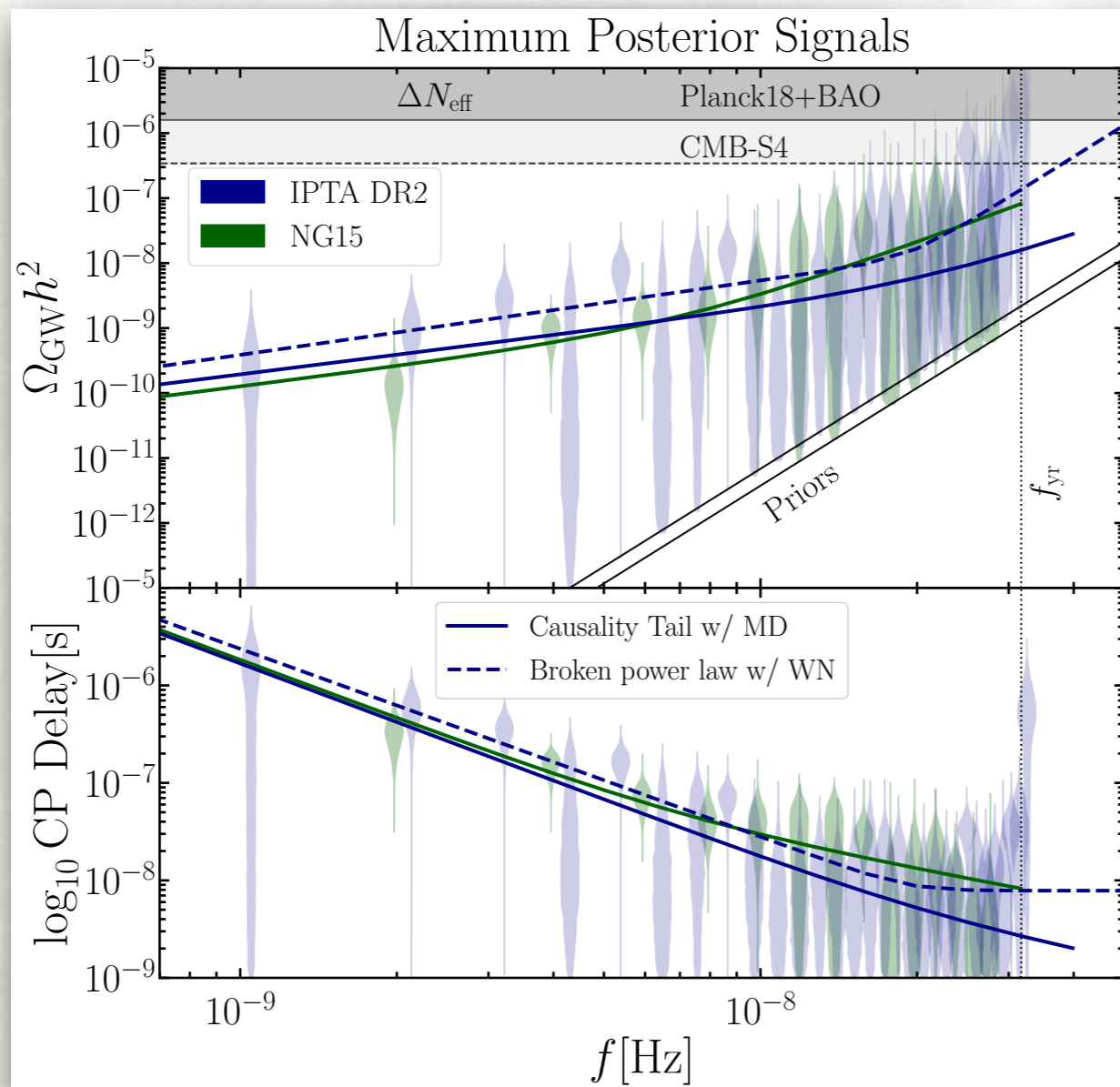
PTA data able to see  
SM physics in GWs!



# EXPLORING THE COSMOLOGICAL HISTORY

Also possible to test non-standard expansion histories,  
such as Matter Domination (low reheating)

$$w \rightarrow 0 \Rightarrow \Omega_{\text{gw}} h^2 (f \ll f_*) \propto f$$

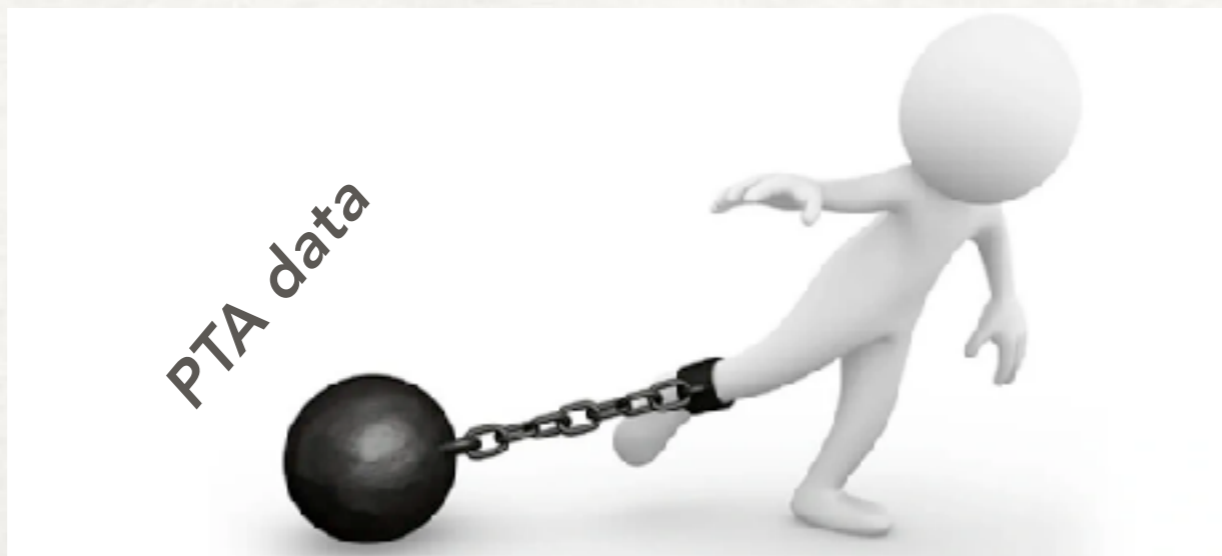


# DIRECTIONS/OPPORTUNITIES FOR PARTICLE PHYSICS/COSMOLOGY @ PTAS

V. Dandoy, V. Domcke, FR 2302.07901

*Set constraints*

*Scalar-induced Gravitational  
Waves*



# SCALAR-INDUCED GWS (SIGW)

*Scalar (curvature) & tensor perturbations  
generated independently during inflation,  
Then stretched to super horizon scales*

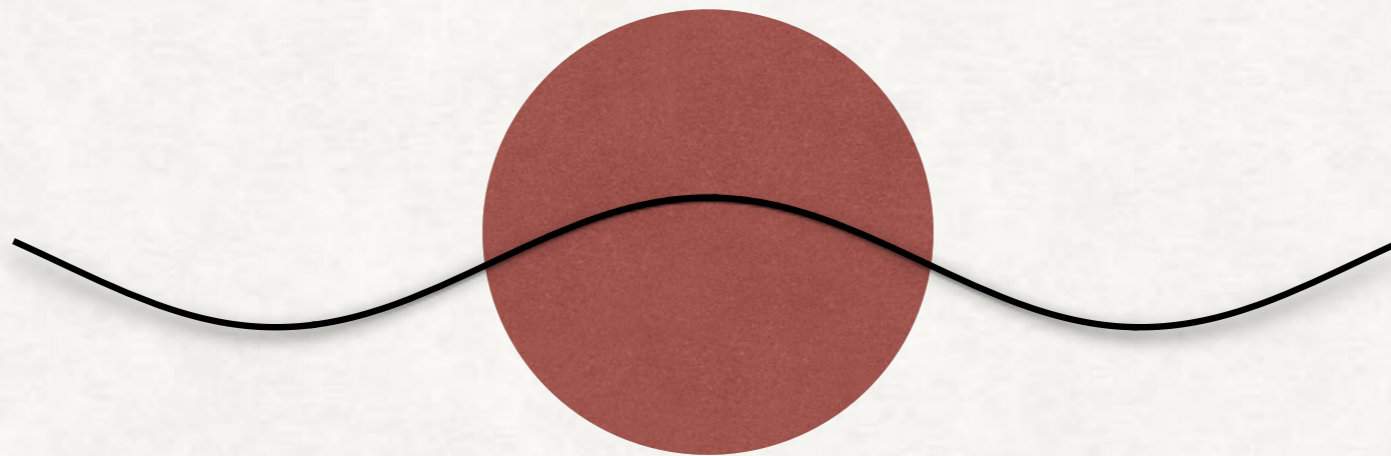
$$k_{\star} = \frac{2\pi}{\lambda_{\star}} \ll aH$$



# SCALAR-INDUCED GWS (SIGW)

*Scalar (curvature) & tensor perturbations  
generated independently during inflation,  
Then stretched to super horizon scales*

$$k_{\star} = \frac{2\pi}{\lambda_{\star}} \ll aH$$



# SCALAR-INDUCED GWS

*Re-enter the Hubble sphere at some epoch after inflation*

$$k_{\star} = \frac{2\pi}{\lambda_{\star}} \simeq aH|_{\star}$$

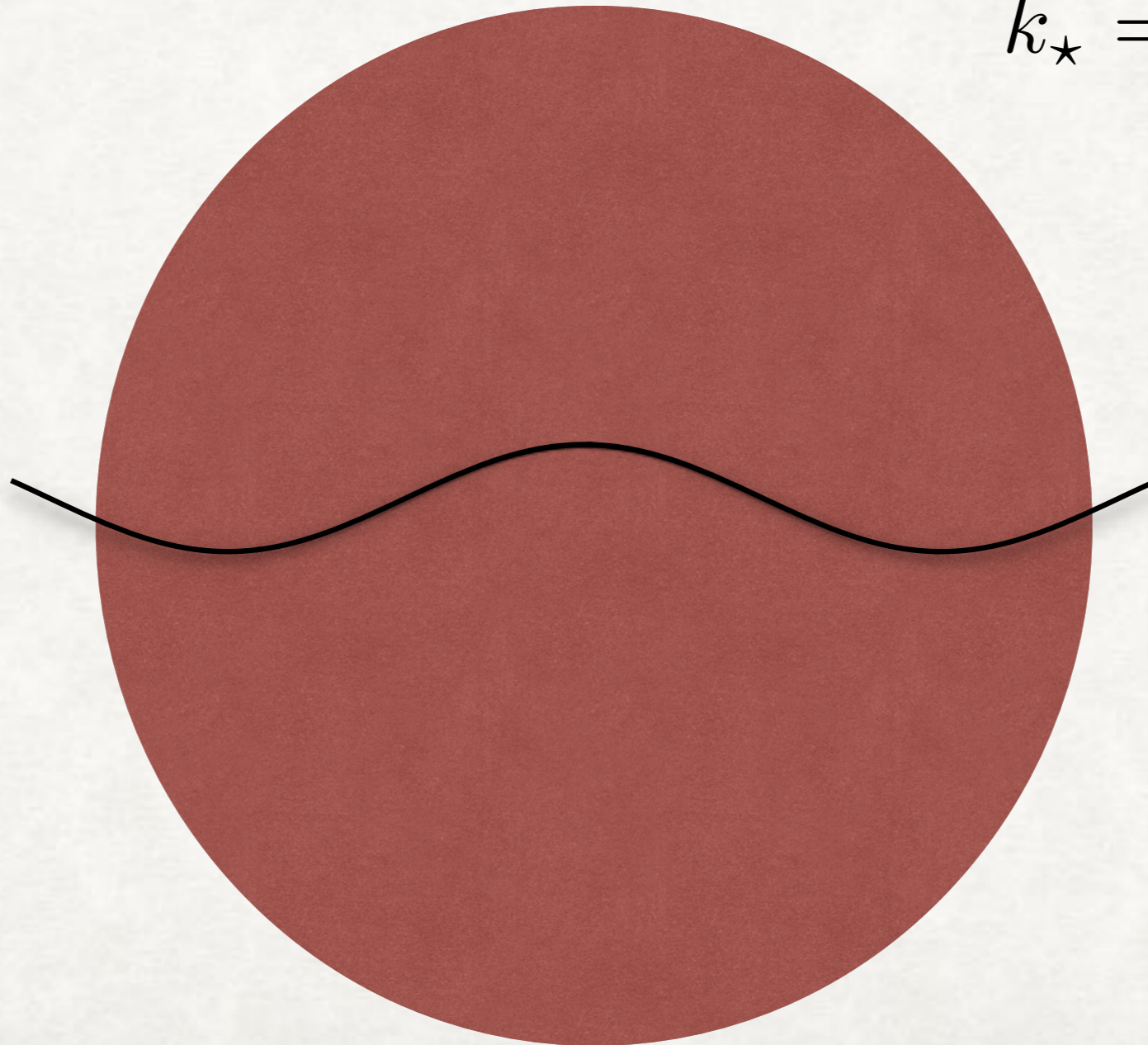




# SCALAR-INDUCED GWS

*Re-enter the Hubble sphere at some epoch after inflation*

$$k_{\star} = \frac{2\pi}{\lambda_{\star}} \simeq aH|_{\star}$$



# SCALAR-INDUCED GWS

*At CMB scales, scalar spectrum is small and approximately scale invariant, tensors yet to be detected*

$$\Delta_{\zeta}^2(k) \equiv A_{\zeta} \left( \frac{k}{0.05 \text{ Mpc}^{-1}} \right)^{n_s-1} \sim 10^{-9}, \quad \Delta_t^2(k) \sim r \Delta_{\zeta}^2(k) \lesssim 10^{-11}$$
$$n_s \simeq 0.97 \quad \Rightarrow \quad \Omega_{\text{gw}} h^2 \lesssim 10^{-17}$$

*These perturbations are independent at first order in GR perturbation theory*

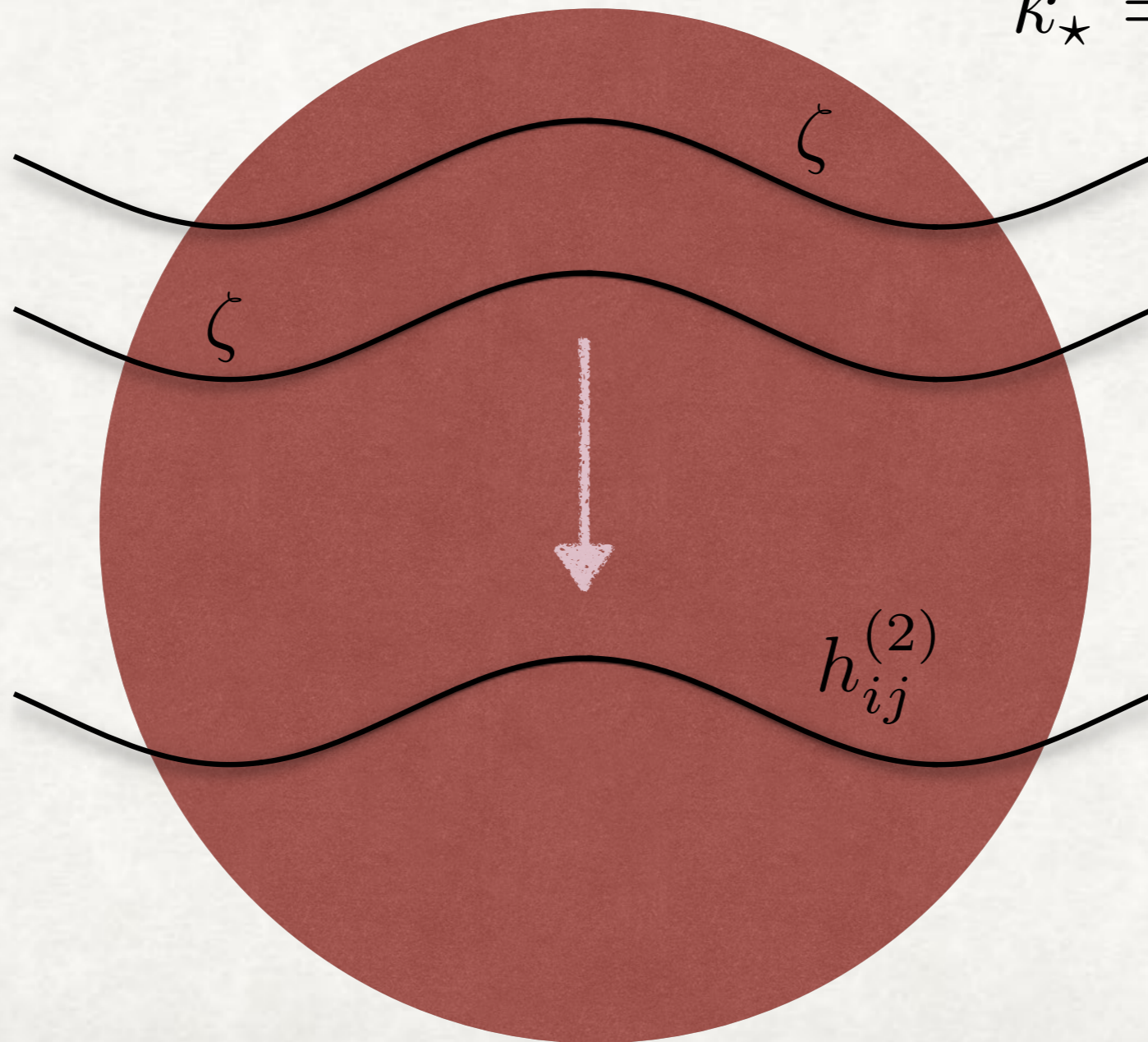
*At NLO, (two) first order scalar perturbations source second order tensor perturbations*

$$h_{ij}^{(2)''} + 2\mathcal{H}h_{ij}^{(2)'} + k^2 h_{ij}^{(2)} = S_{ij}^{TT}(\Phi^{(1)}, \Psi^{(1)})$$

# SCALAR-INDUCED GWS

Most significant production occurs at horizon re-entry of similar-k perturbations (causality limited afterwards)

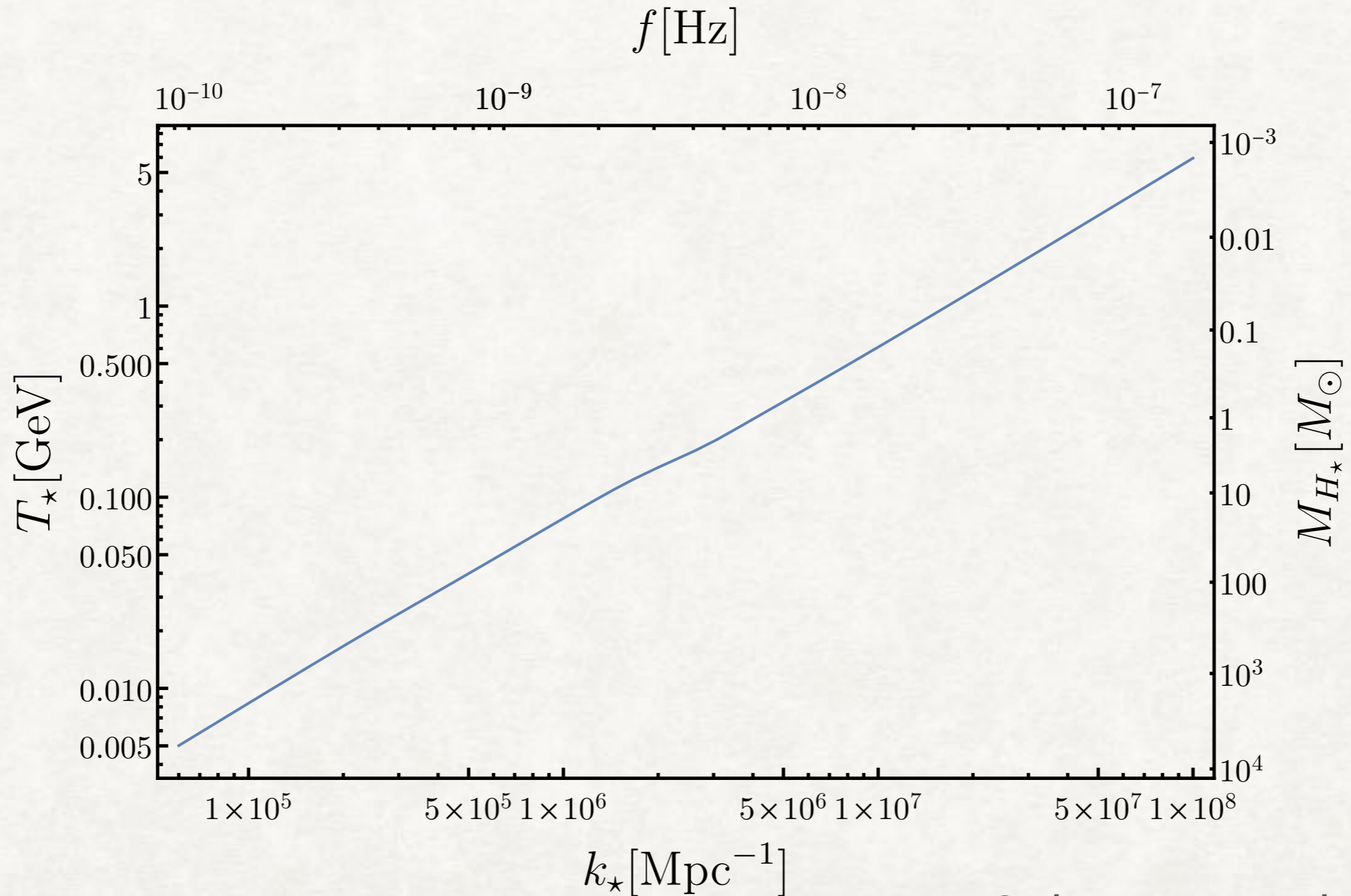
$$k_{\star} = \frac{2\pi}{\lambda_{\star}} \simeq aH|_{\star}$$



$$\Omega_{\text{gw}} \sim A_{\zeta}^2$$

# SCALAR-INDUCED GWS

*Observable only if curvature power spectrum at small scales is much bigger than at CMB scales*

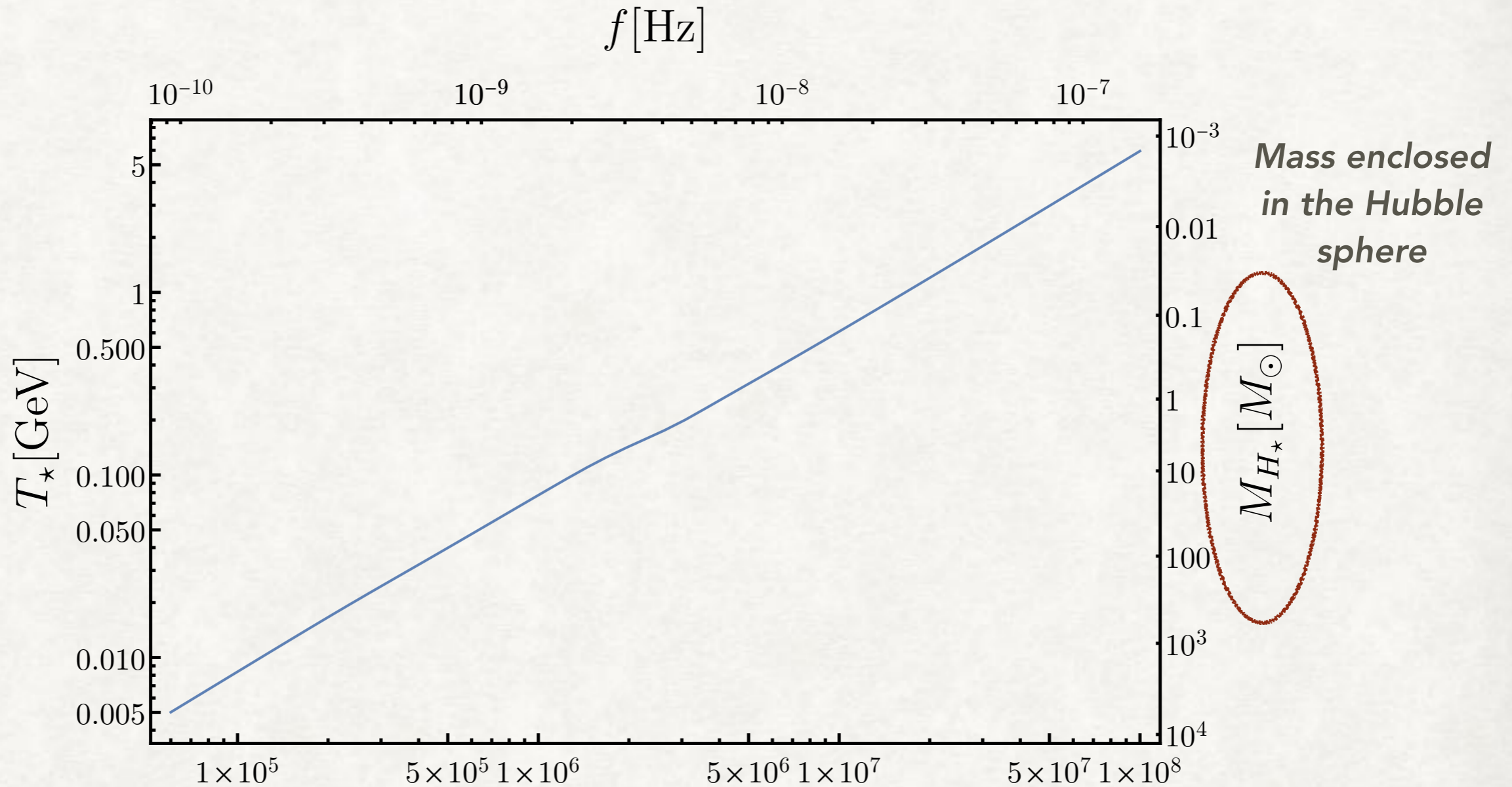


$\gg 0.05 \text{ Mpc}^{-1}$

*Scalar spectrum only weakly constrained at these scales!*

# PRIMORDIAL BLACK HOLES

*If amplitude is sufficiently large, scalar perturbations undergo gravitational collapse and form **Primordial Black Holes (PBHs)***



$$k_* [\text{Mpc}^{-1}] \gg 0.05 \text{ Mpc}^{-1}$$

*Scalar spectrum only weakly constrained at these scales!*

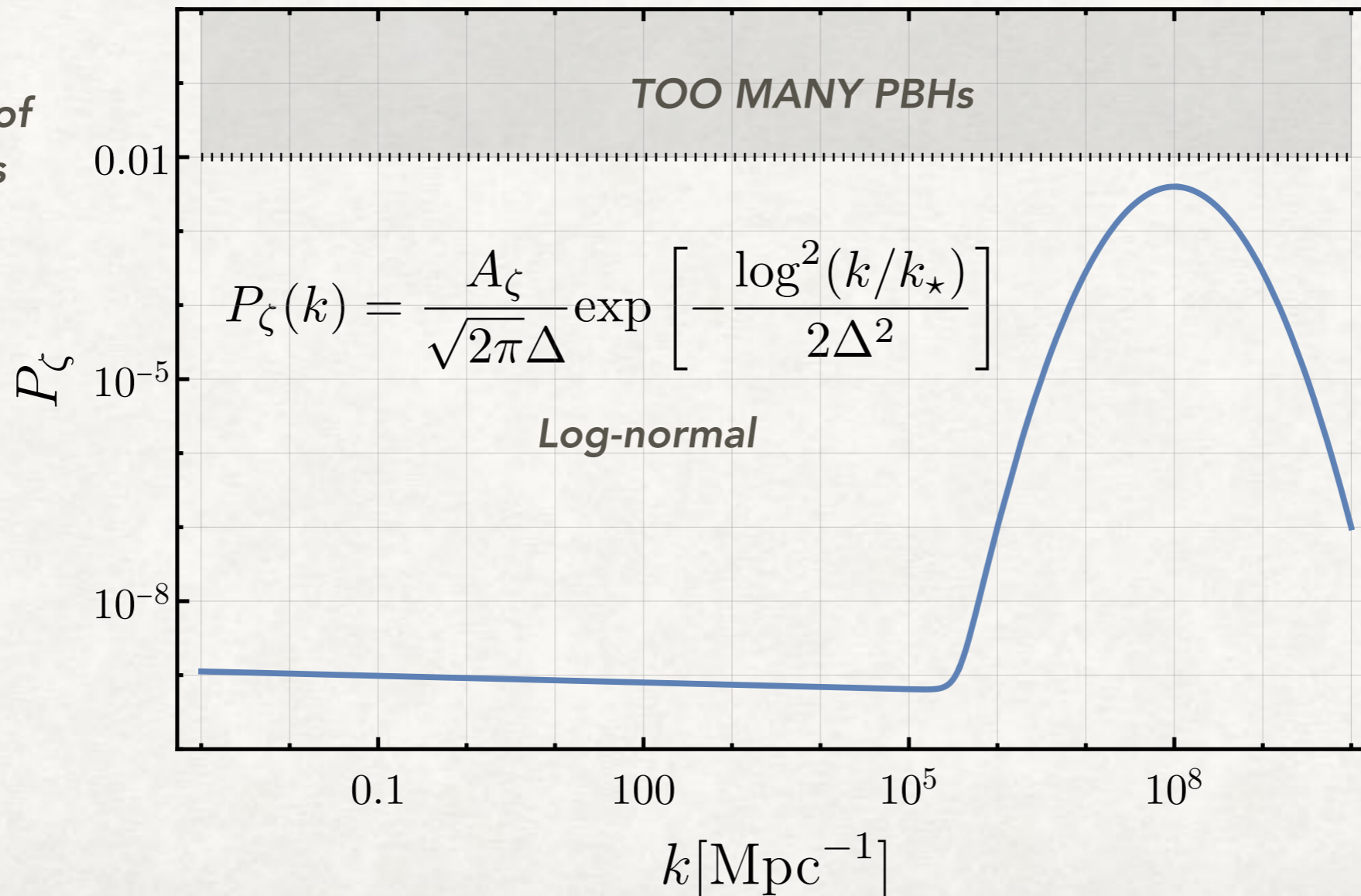
# SCALAR-INDUCED GWS

*Warning:*  
enhancement  
requires strong  
deviations from slow-  
roll, non-minimal  
inflationary model

*Spectral shape of GW signal determined by shape  
of power spectrum at small scales*

*Simple parametrisation to capture possible enhancement*

*Common  
magnitude of  
constraints*



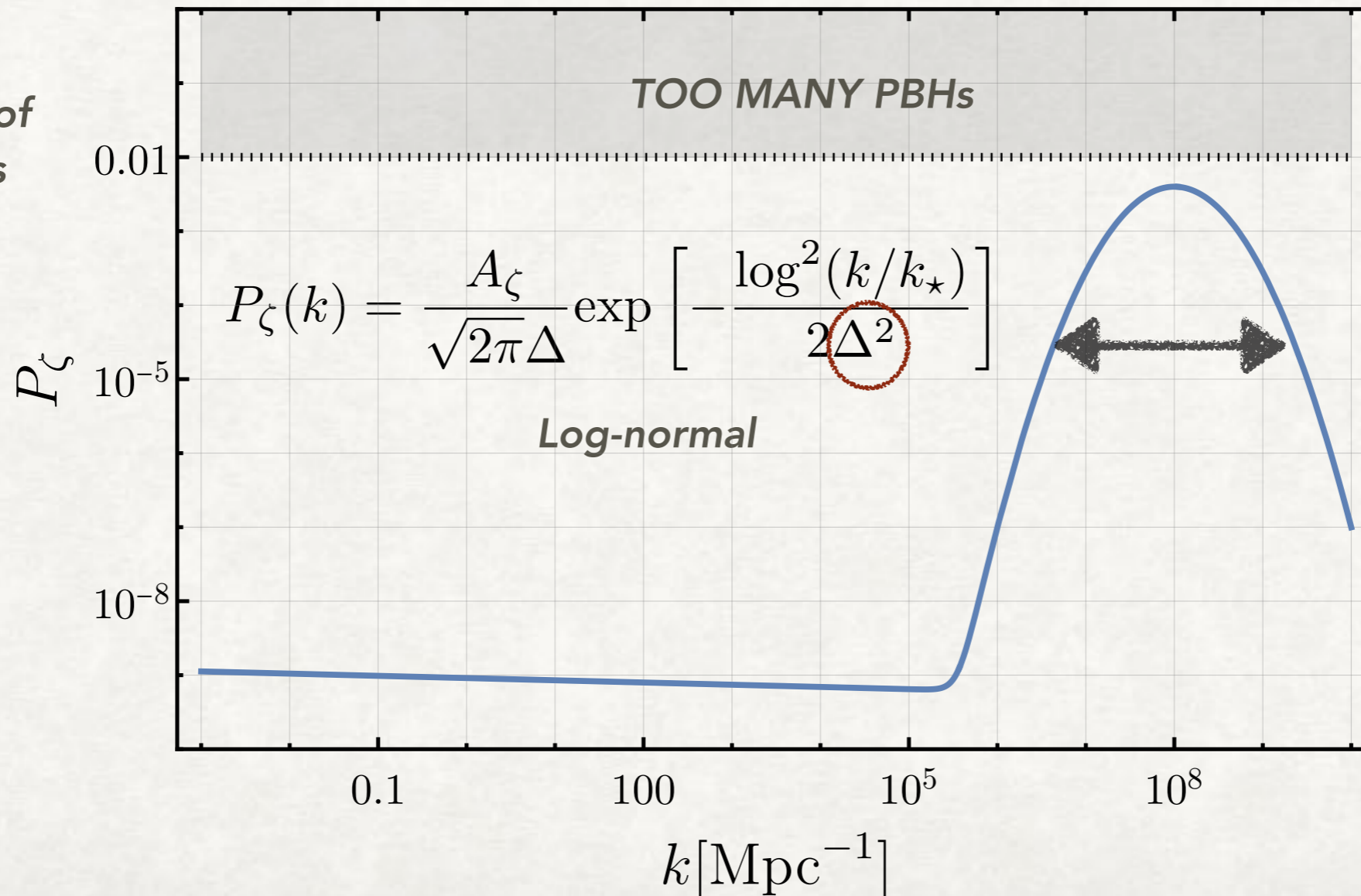
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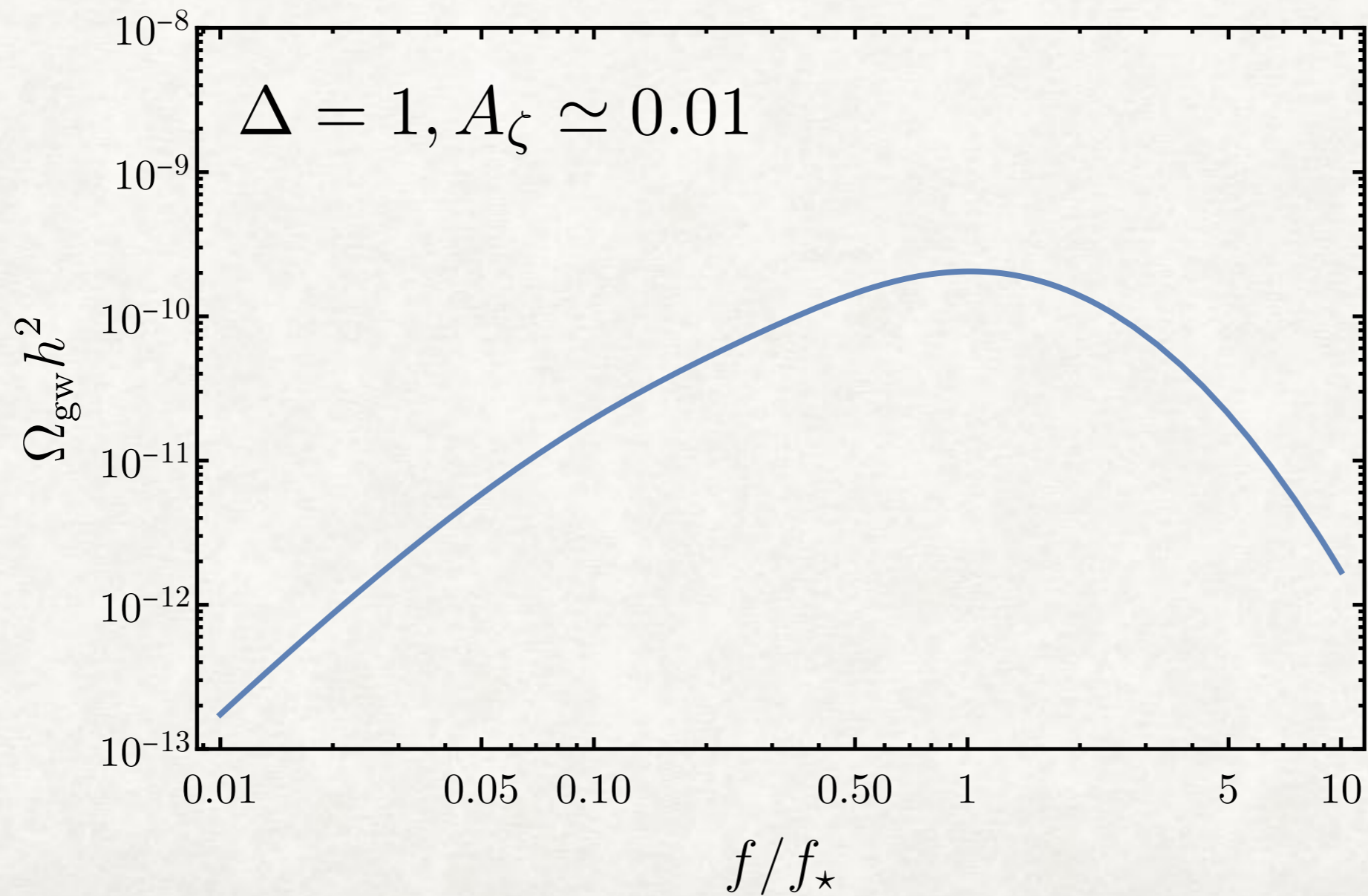
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# SCALAR-INDUCED GWS

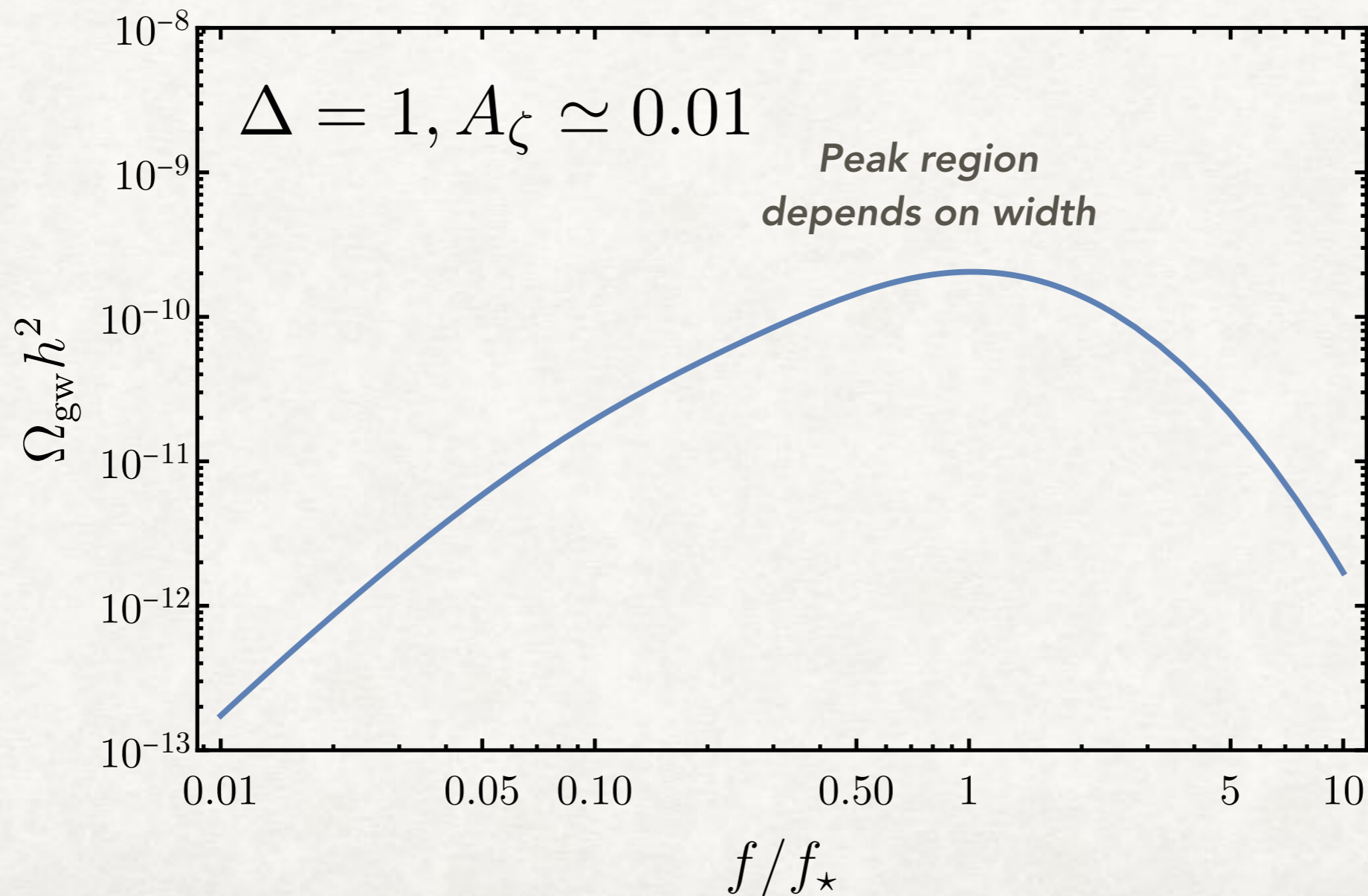
$$P_\zeta(k) = \frac{A_\zeta}{\sqrt{2\pi}\Delta} \exp\left[-\frac{\log^2(k/k_\star)}{2\Delta^2}\right]$$





# SCALAR-INDUCED GWS

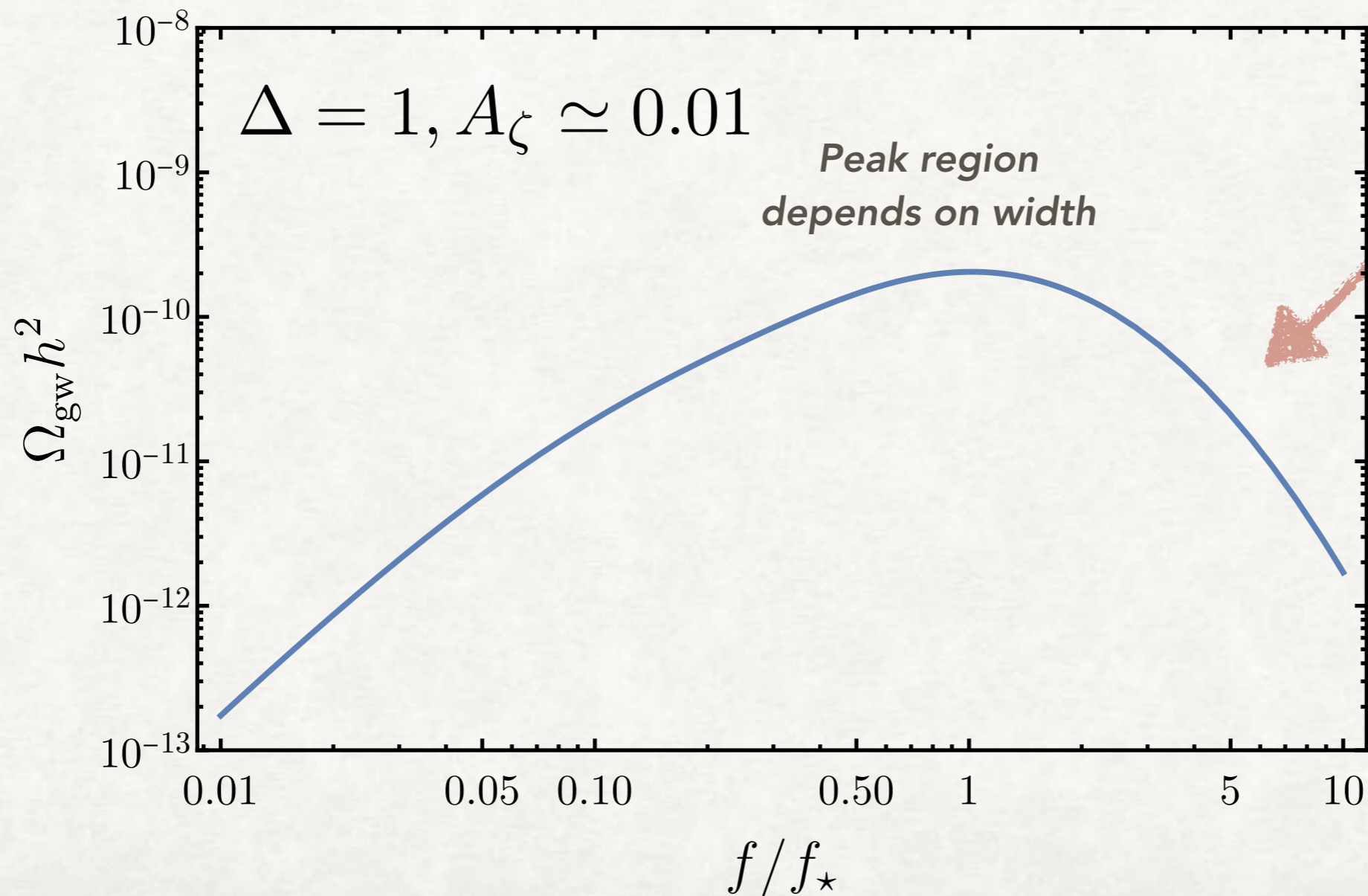
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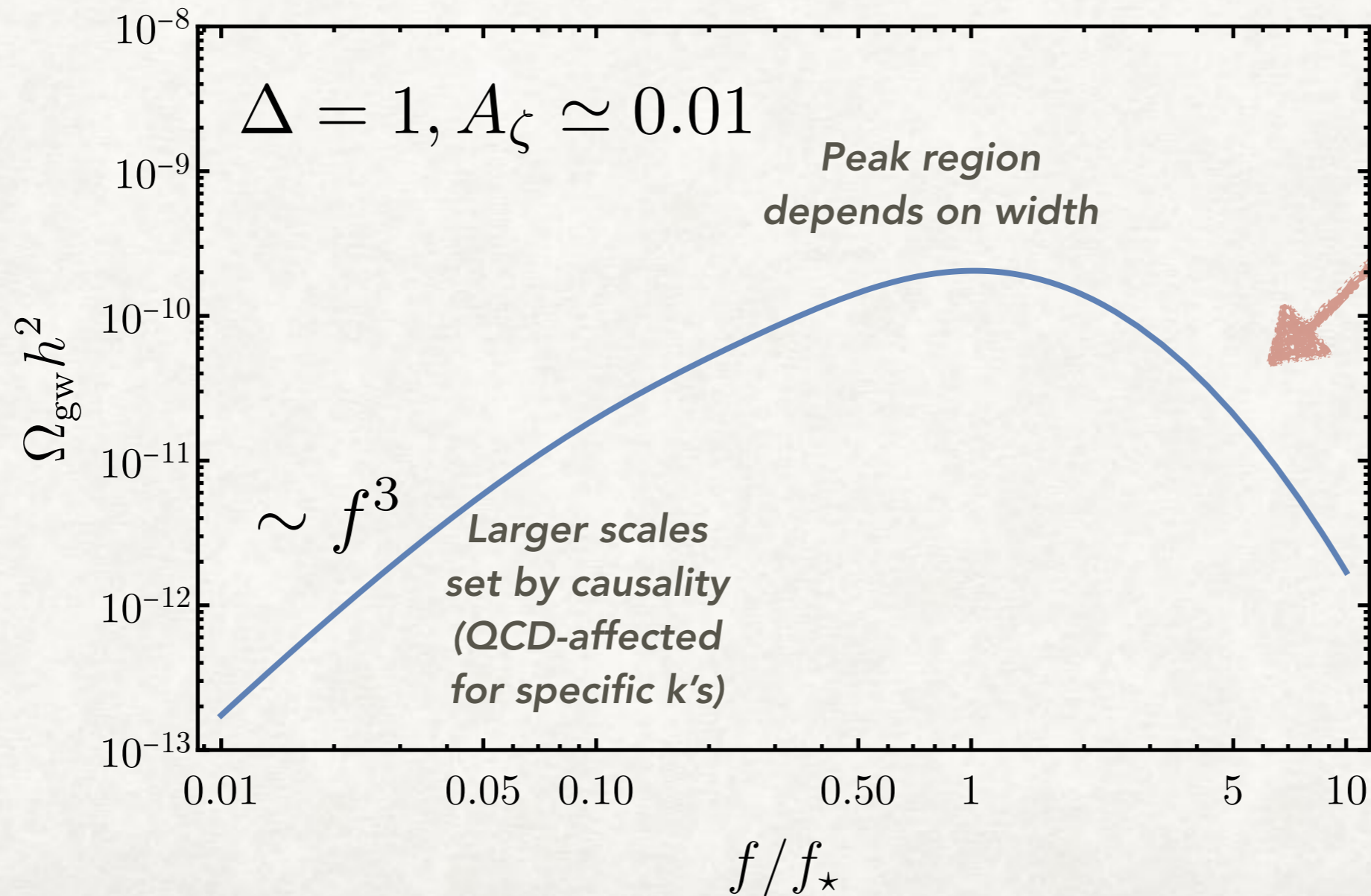
*(Smaller) Scales  
re-enter earlier,  
no  
enhancement*



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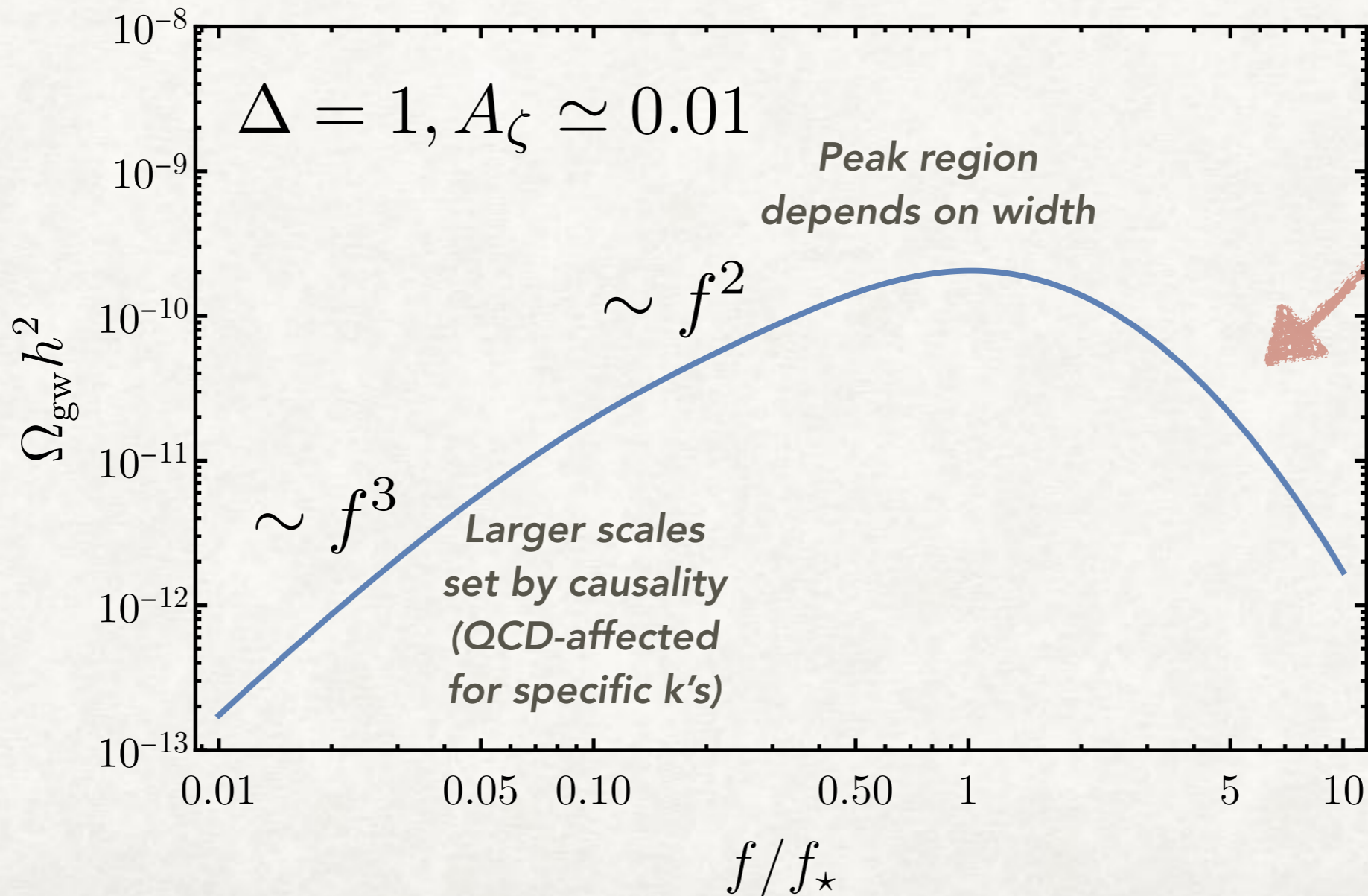
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(Smaller) Scales  
re-enter earlier,  
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# RELEVANCE OF & FOR PTAS

*Non-observation (or incompatible spectrum) of GWs provide way to (indirectly) constrain the power spectrum at small scales*

*Scenario does not require new physics at low temperatures, evades constraints on dark sectors*

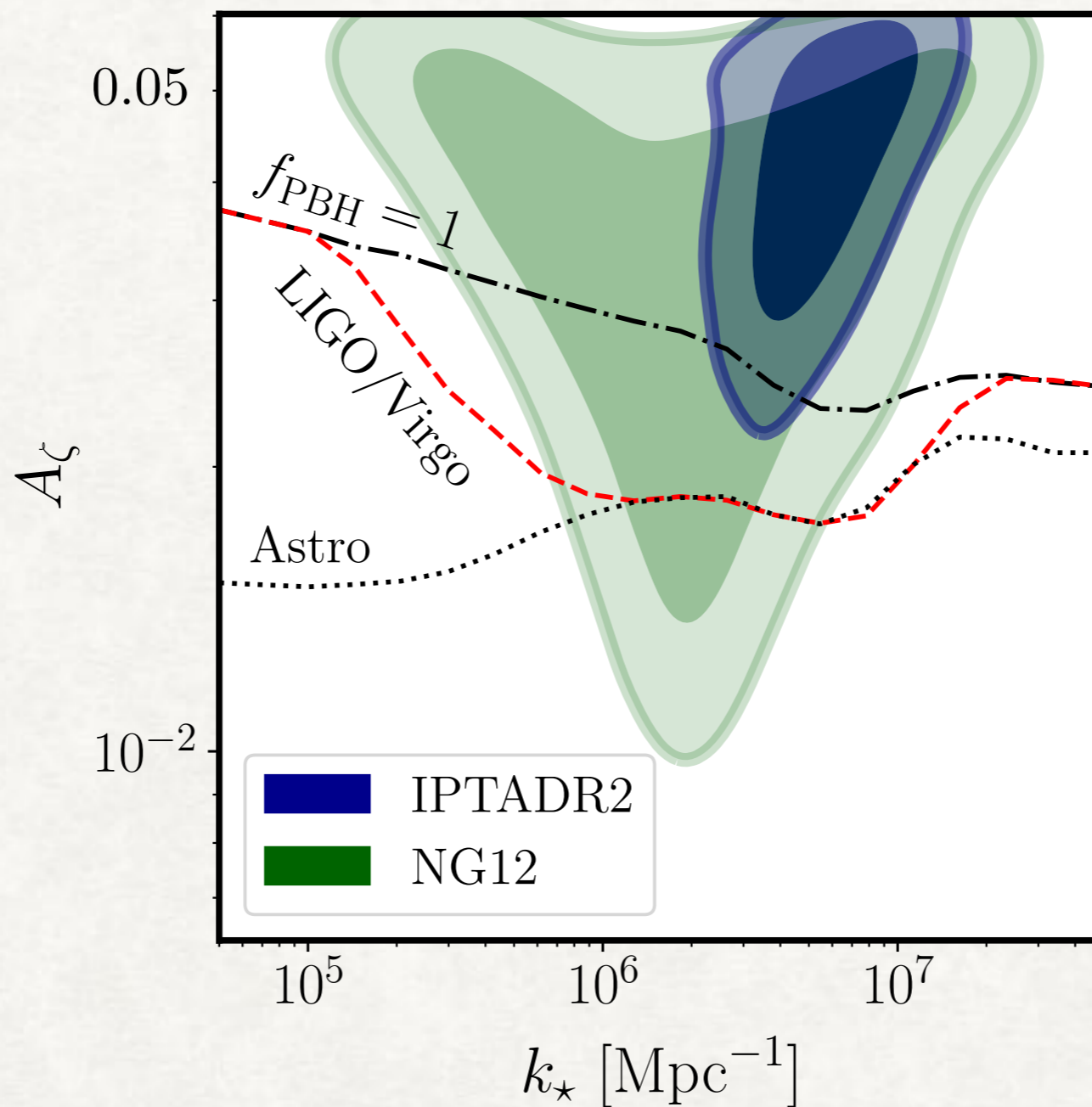
*Connection with PBHs in interesting mass region (LIGO/Virgo)*

# DETECTION ANALYSIS

Analytical approx by  
Pi, Sasaki  
implemented (and  
improved) in  
**enterprise**

$$f_{\text{PBH}} \equiv \Omega_{\text{PBH}} / \Omega_{\text{cdm}}$$

Scalar induced GWs only



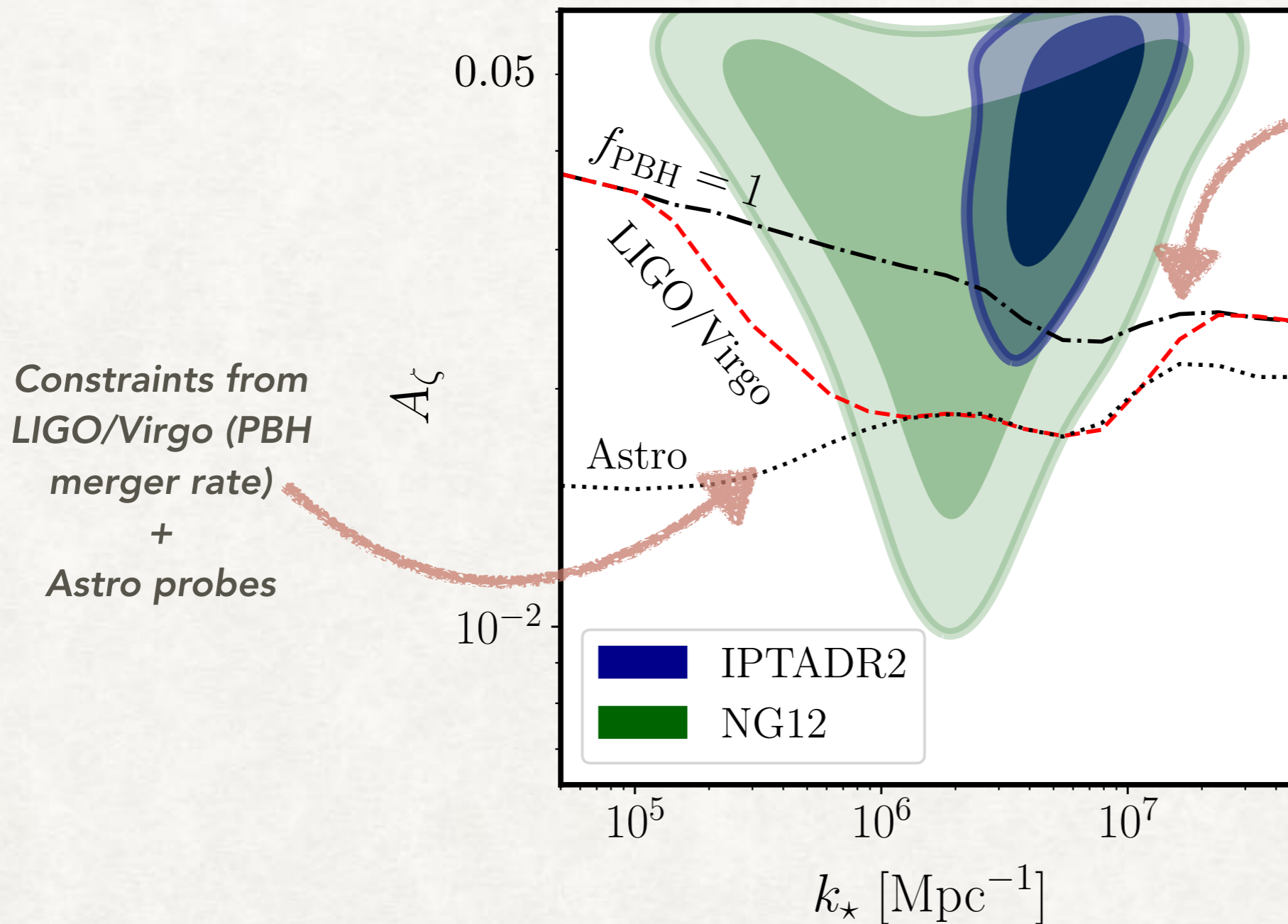
*After NG12, several papers claiming interpretation in terms of SIGW*

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Indirect constraints  
from PBHs  
(**Uncertain**,  
We assessed to the  
state-of-the-art  
understanding)

See talk by Valerie!

Analysis  
For Gaussian  
perturbations

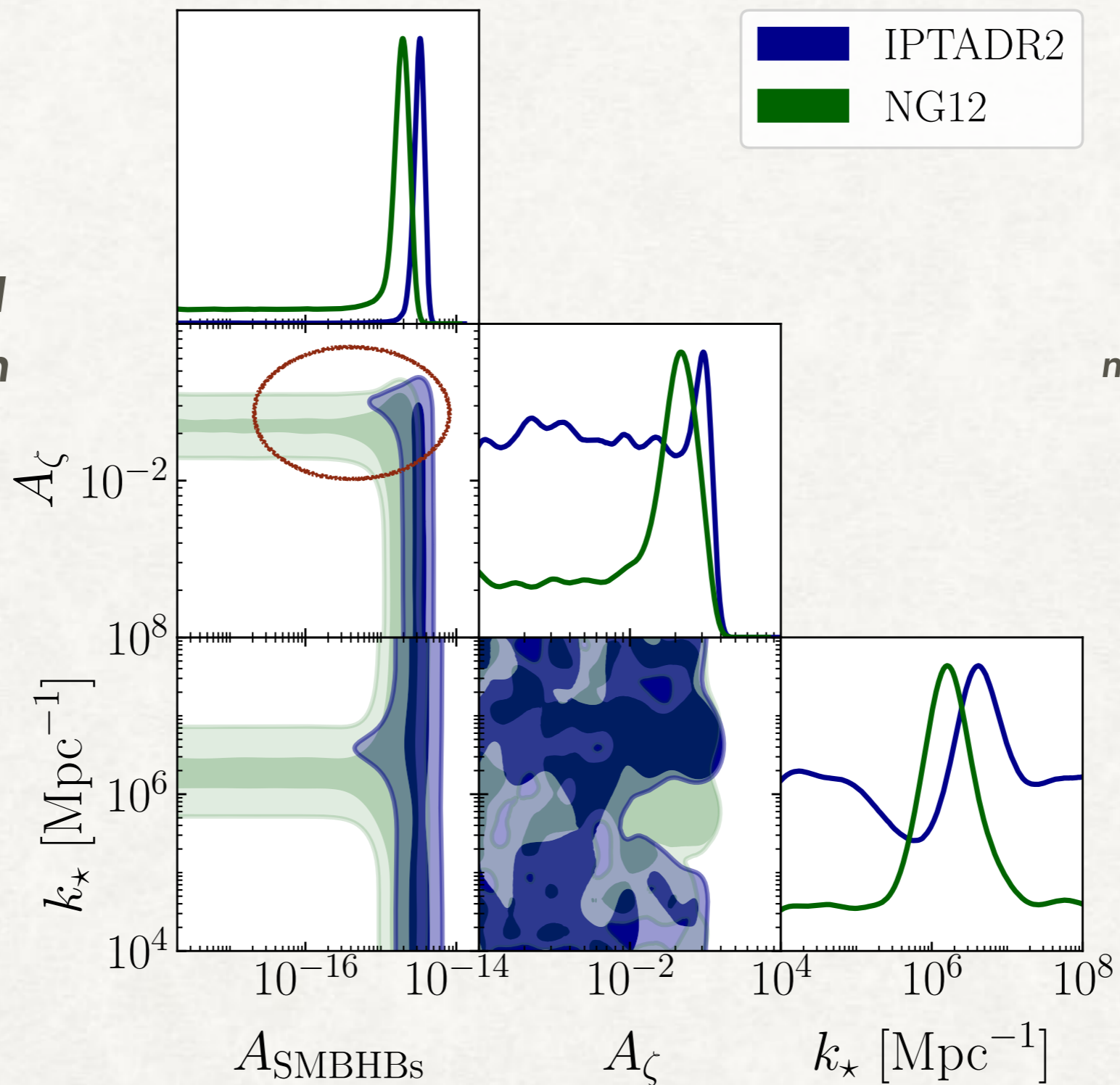
See also talk by  
Dani!

PTA interpretation in terms of SIGW faces challenge!

# DETECTION ANALYSIS INCLUDING SMBHBS & PRIOR

$$\Delta = 1$$

*Prior from PBH overproduction included!*



*SMBHBs signal modeled as power law with*

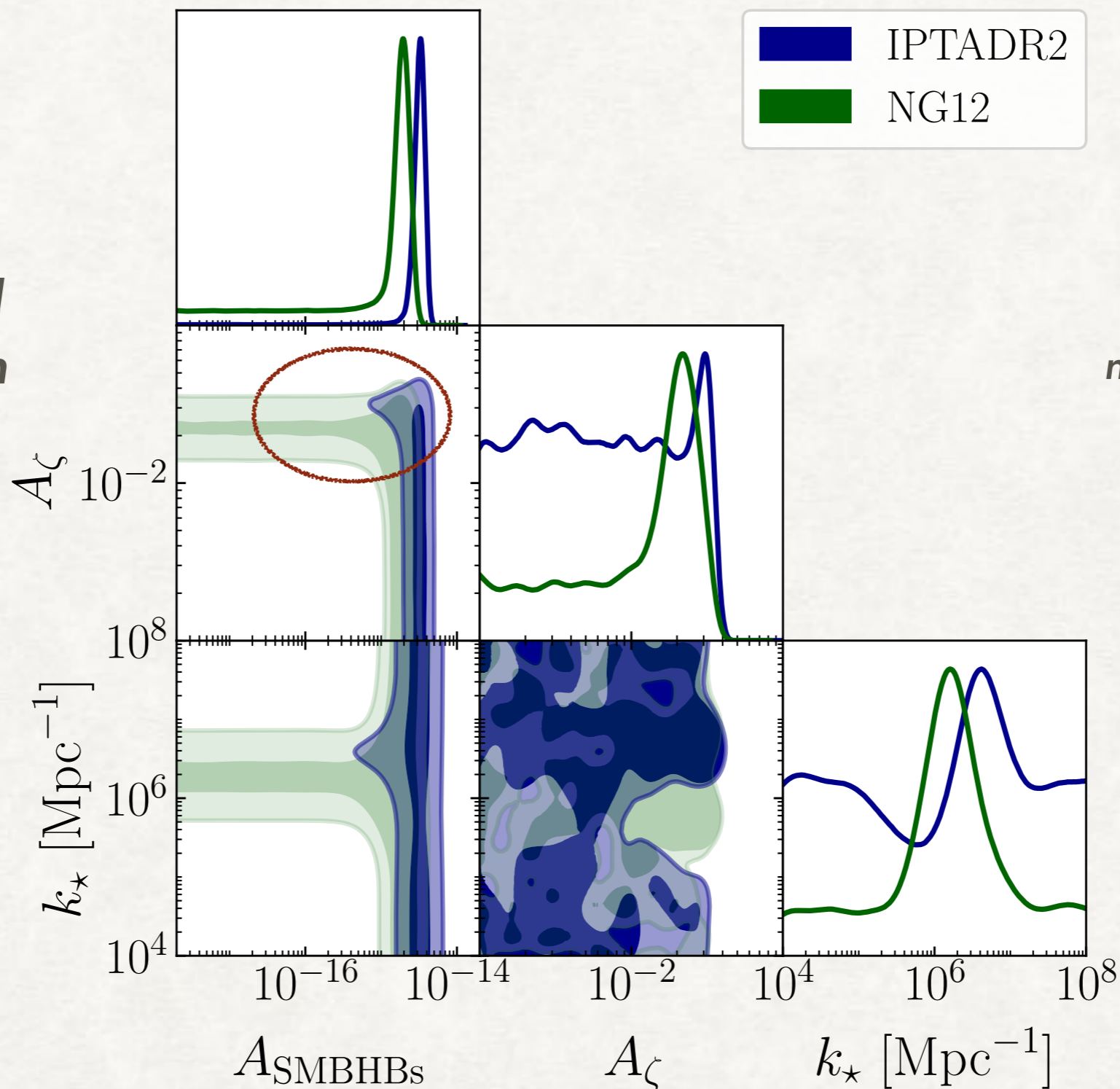
$$\gamma = 13/3$$



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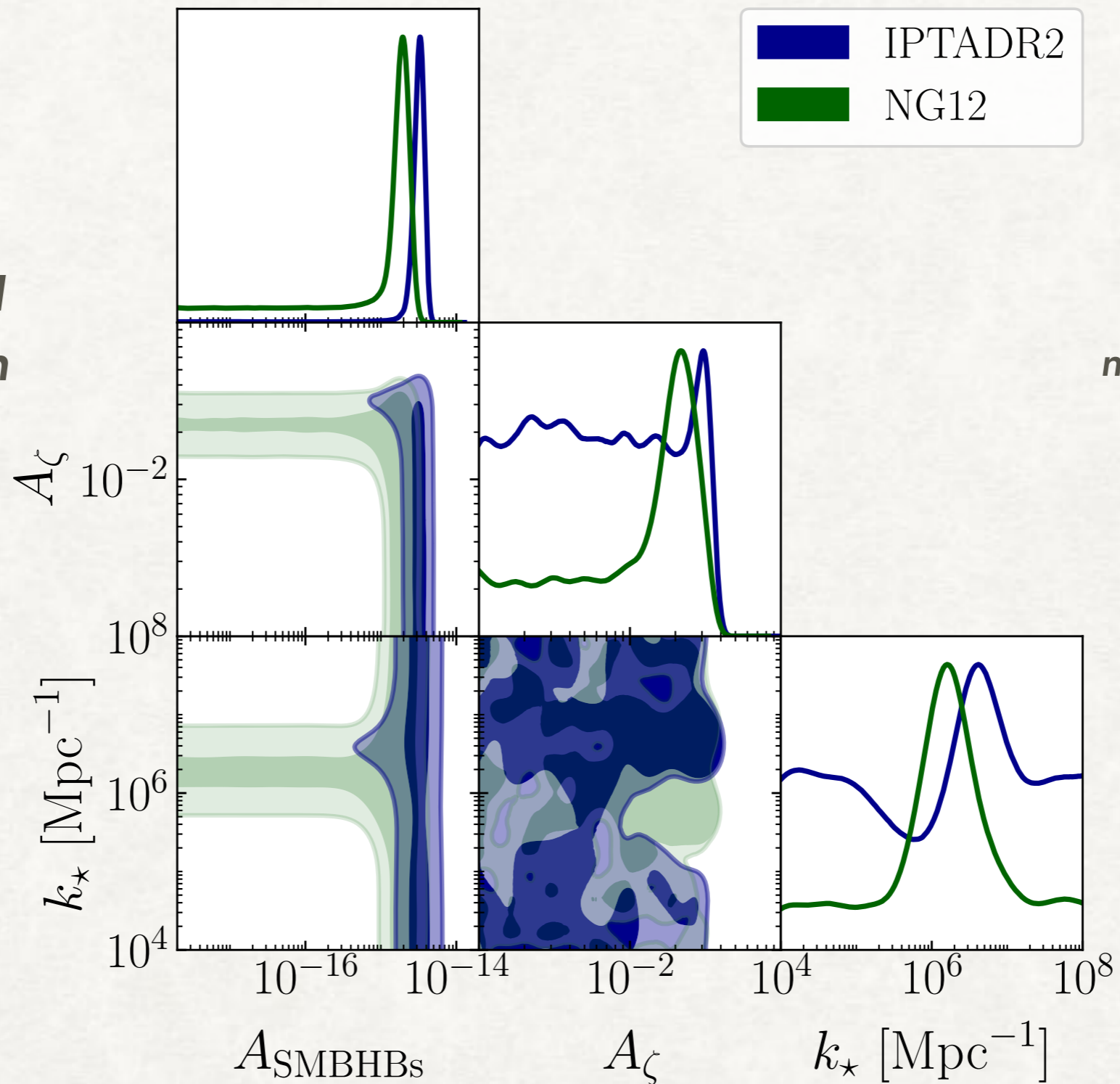
$$\gamma = 13/3$$

*Upper prior on PBH overproduction severely constrains interpretation of IPTA DR2!*

# DETECTION ANALYSIS INCLUDING SMBHBs

$$\Delta = 1$$

*Prior from PBH overproduction included!*



*SMBHBs signal modeled as power law with*

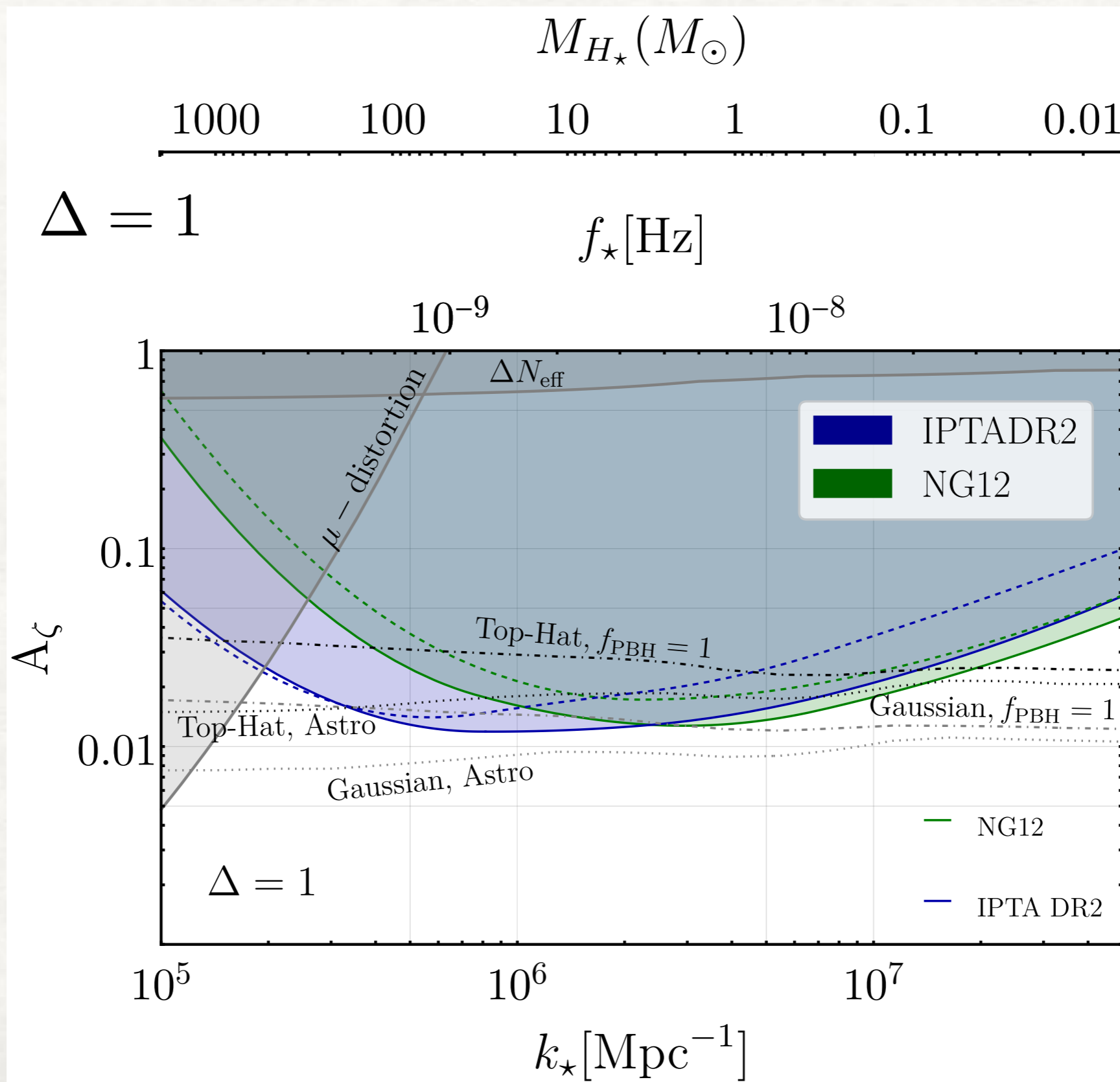
$$\gamma = 13/3$$

$$\mathcal{B}(\text{SMBHB vs SIGW}) \simeq 10^2$$

# CONSTRAINT ANALYSIS

Other constraints shown only for comparison, ours are independent!

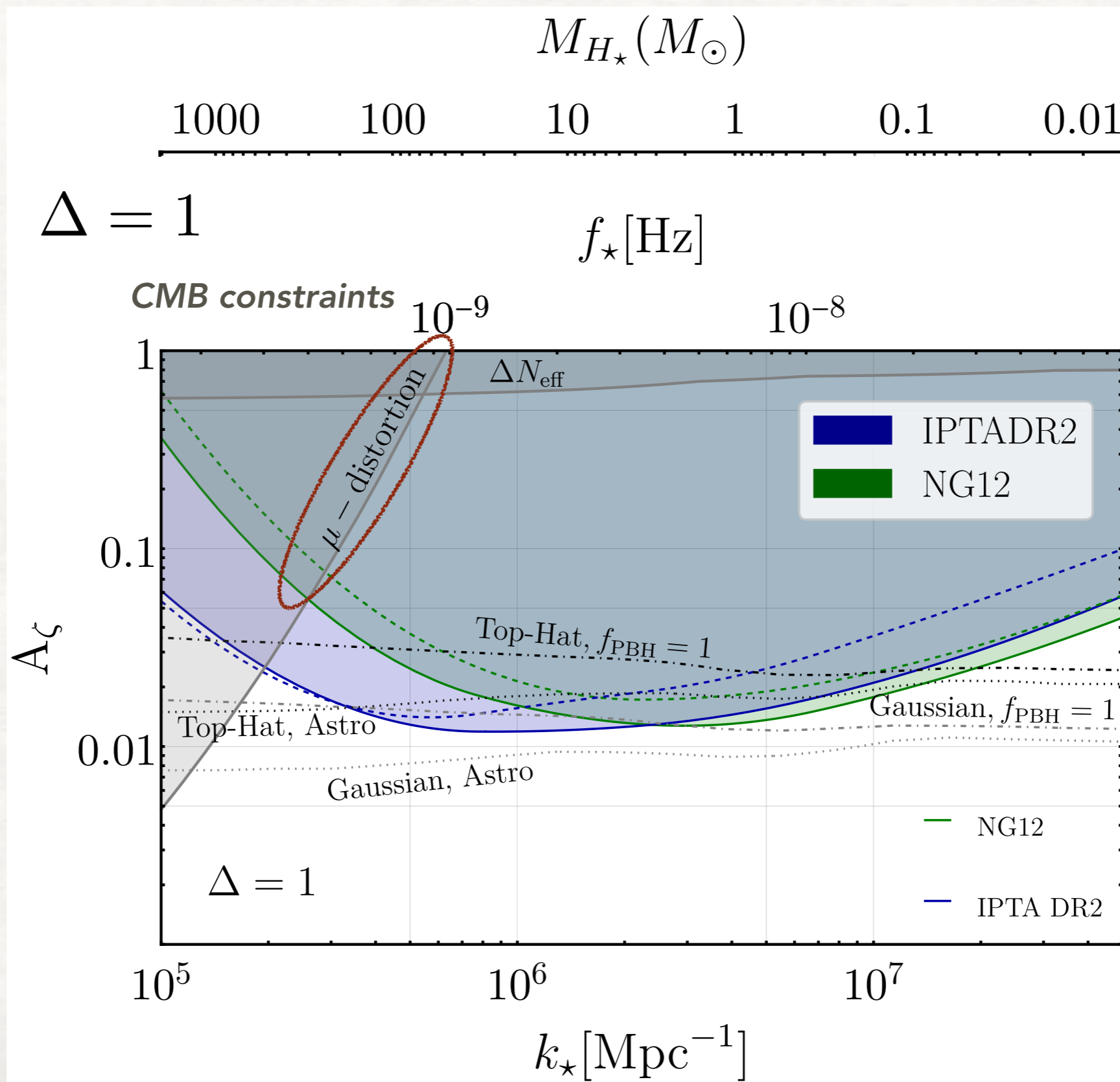
Here we include a signal from SMBHBs (different strategy from NG15)



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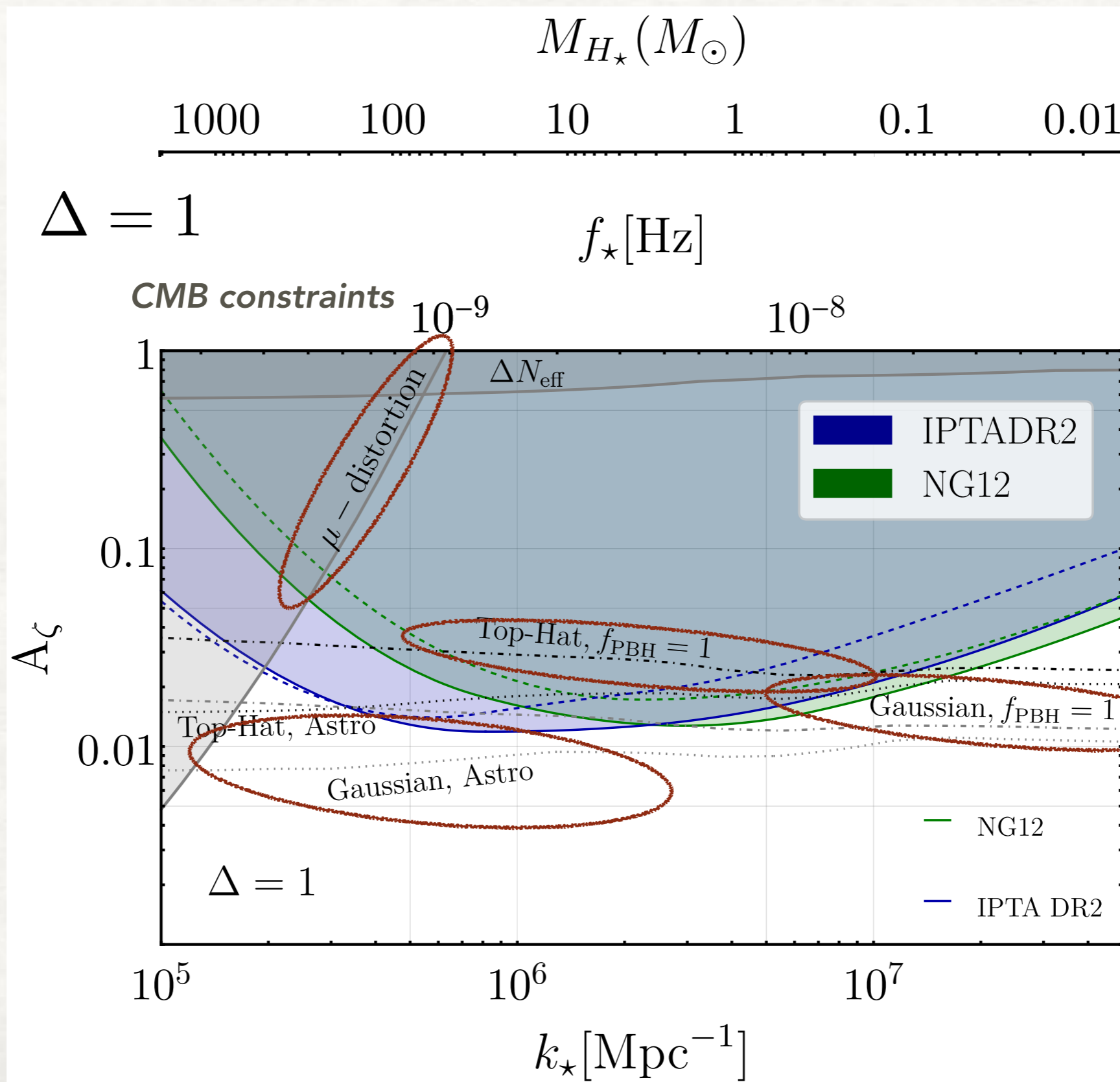
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# CONSTRAINT ANALYSIS

Other constraints shown only for comparison, ours are independent!

Here we include a signal from SMBHBs (different strategy from NG15)



Constraints from PBHs  
See talk by Valerie!

Stronger constraints for smaller widths

# DIRECTIONS/OPPORTUNITIES FOR PARTICLE PHYSICS/COSMOLOGY @ PTAS

**R.Z. Ferreira, A. Notari, O. Pujolàs, FR 2204.04228**

*Motivated models for signal  
interpretation*

*Cosmic Domain Walls*

# CHALLENGE OF EARLY UNIVERSE INTERPRETATION FROM TRANSIENT SOURCES

$$t_{\star}^{-1}$$

$t_{\star} \equiv$  Time/length scale of the source

$$\Omega_{\text{gw}} h^2 \simeq 10^{-8} \left( \frac{10.75}{g_{\star}(T_{\star})} \right)^{\frac{1}{3}} \left( \frac{\alpha_{\star}/(1 + \alpha_{\star})}{0.1} \right)^2 \epsilon \left( \frac{t_{\star}^{-1}}{H_{\star}}, \dots \right) \mathcal{S}(f/f_{\star})$$

$$\epsilon_{\star} \propto \left( \frac{H_{\star}}{t_{\star}^{-1}} \right)^p \leq 1$$

See also talk  
by Eric!

$$\epsilon_{\star} \lesssim 10^{-2}$$

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*Spectral shape*

**Suppression factor:**  
sub-Hubble time/length-scale of  
source + velocity + ...

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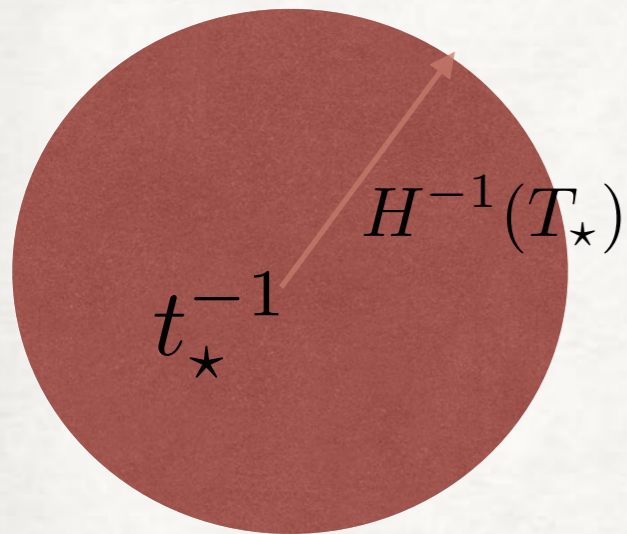
$$\epsilon_{\star} \propto \left( \frac{H_{\star}}{t_{\star}^{-1}} \right)^p \leq 1 \quad p=1, 2$$

See also talk  
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Requires  
unusual PT &  
cosmo

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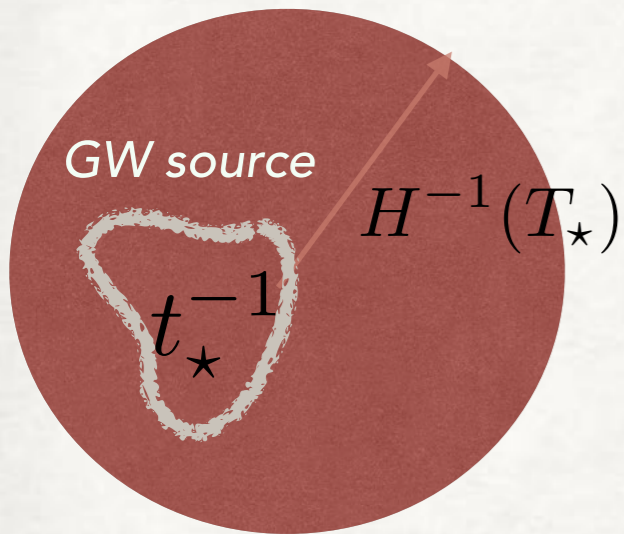
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# CHALLENGE OF EARLY UNIVERSE INTERPRETATION FROM TRANSIENT SOURCES



$t_*$   $\equiv$  Time/length scale of the source

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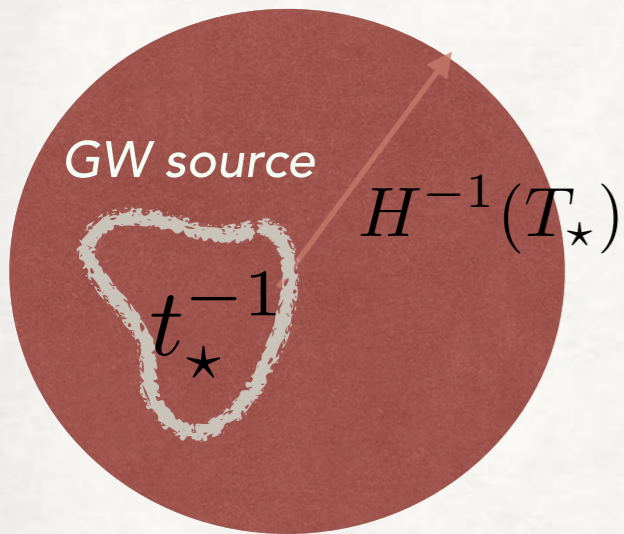
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# CHALLENGE OF EARLY UNIVERSE INTERPRETATION FROM TRANSIENT SOURCES



$t_*$   $\equiv$  Time/length scale of the source

How much of the Universe is in the source

$$\Omega_{\text{gw}} h^2 \simeq 10^{-8} \left( \frac{10.75}{g_*(T_*)} \right)^{\frac{1}{3}} \left( \frac{\alpha_*/(1 + \alpha_*)}{0.1} \right)^2 \epsilon \left( \frac{t_*^{-1}}{H_*}, \dots \right) \mathcal{S}(f/f_*)$$

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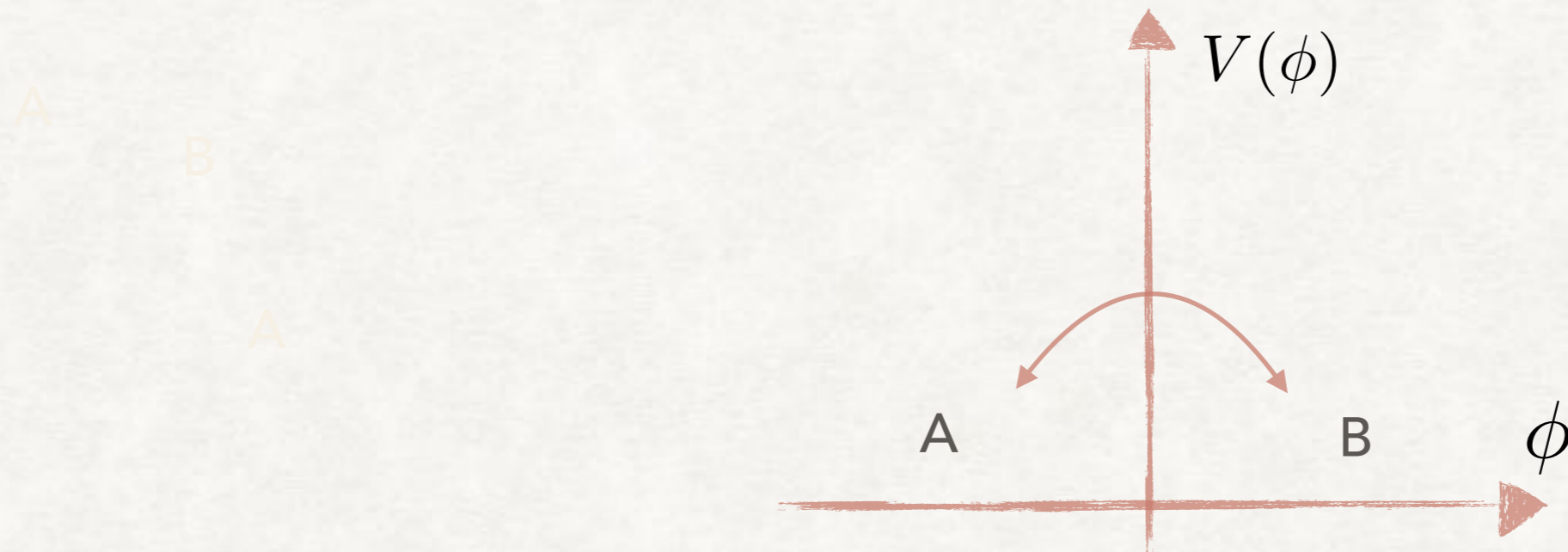
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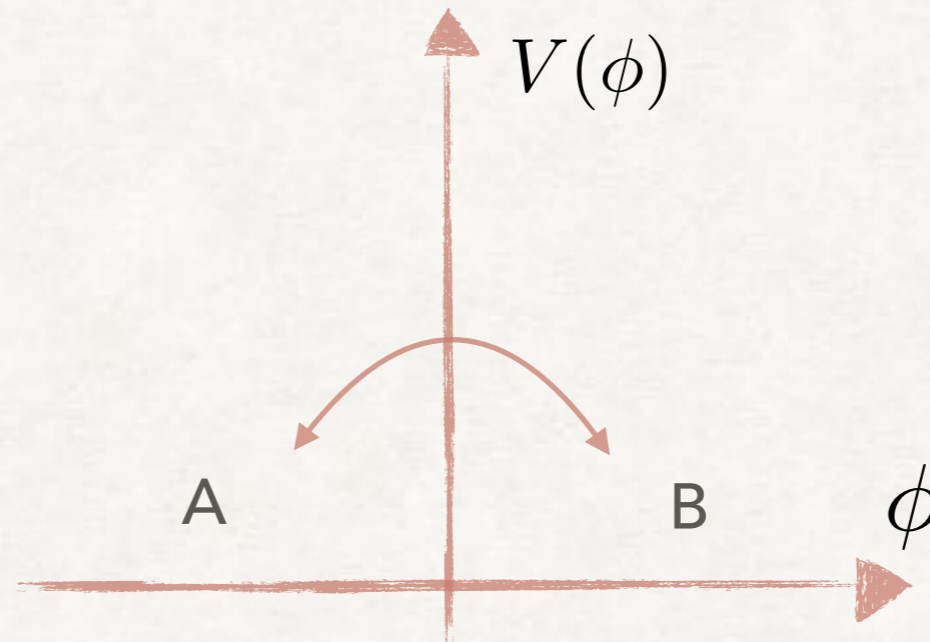
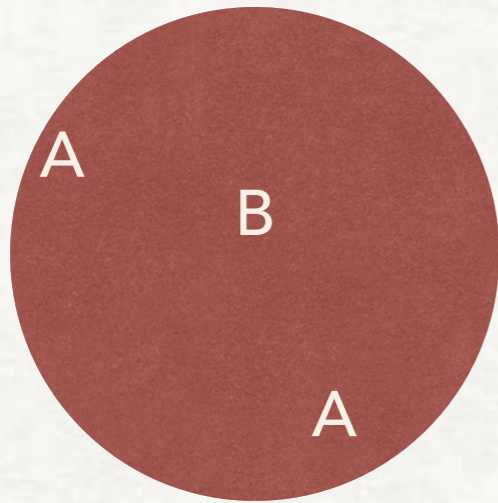
# AN "ATTRACTIVE" POSSIBILITY: DOMAIN WALLS

*Two-dimensional defects associated to (spontaneous) breaking of discrete symmetries*



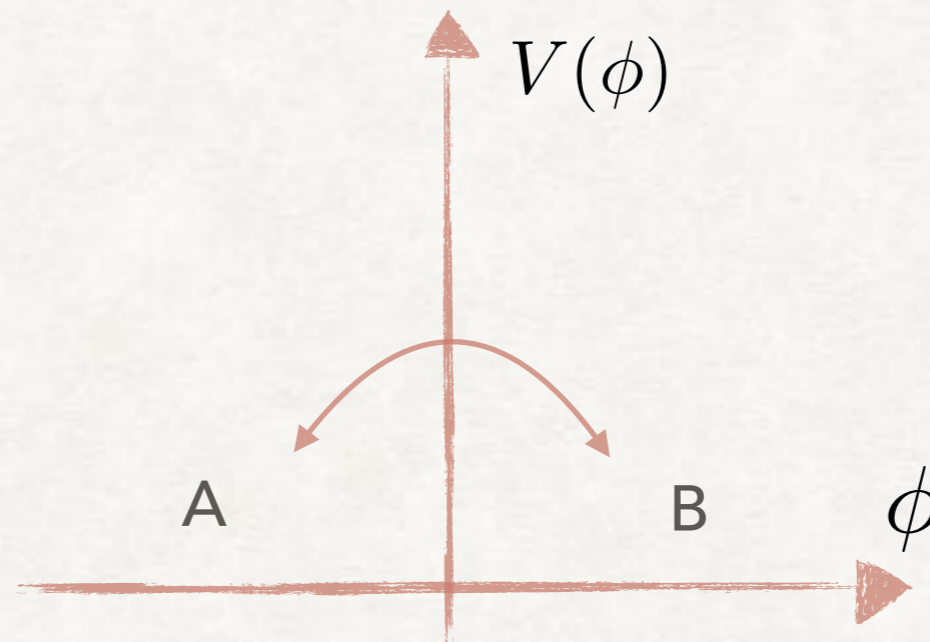
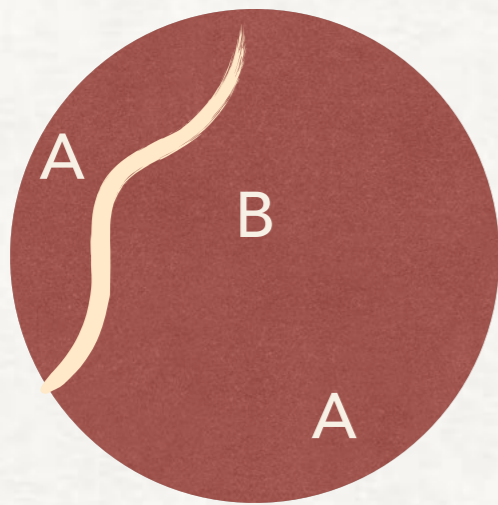
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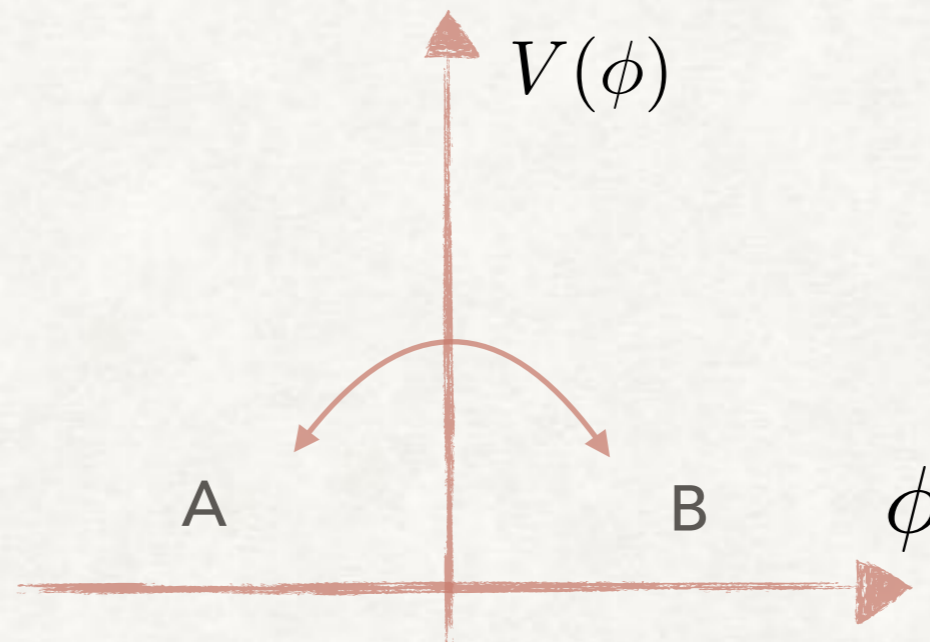
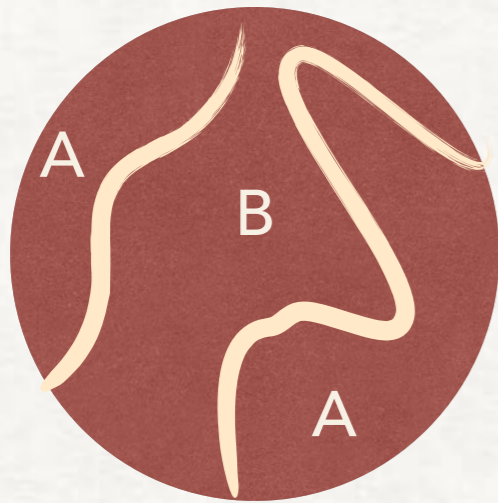
*Two-dimensional defects associated to  
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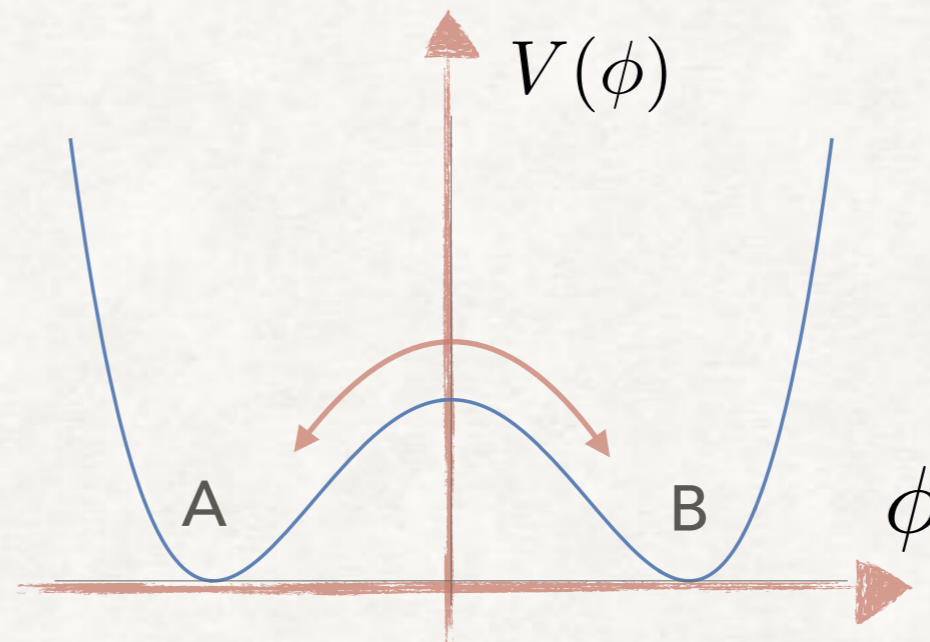
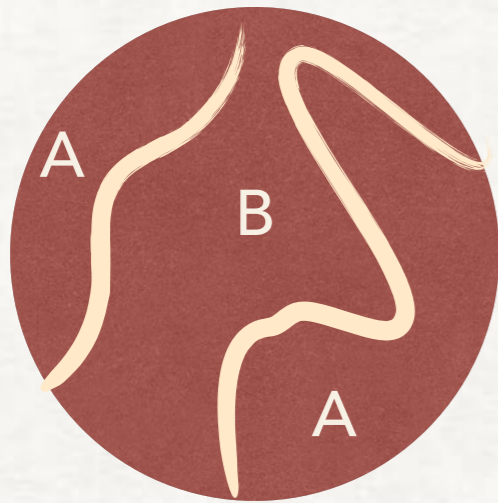
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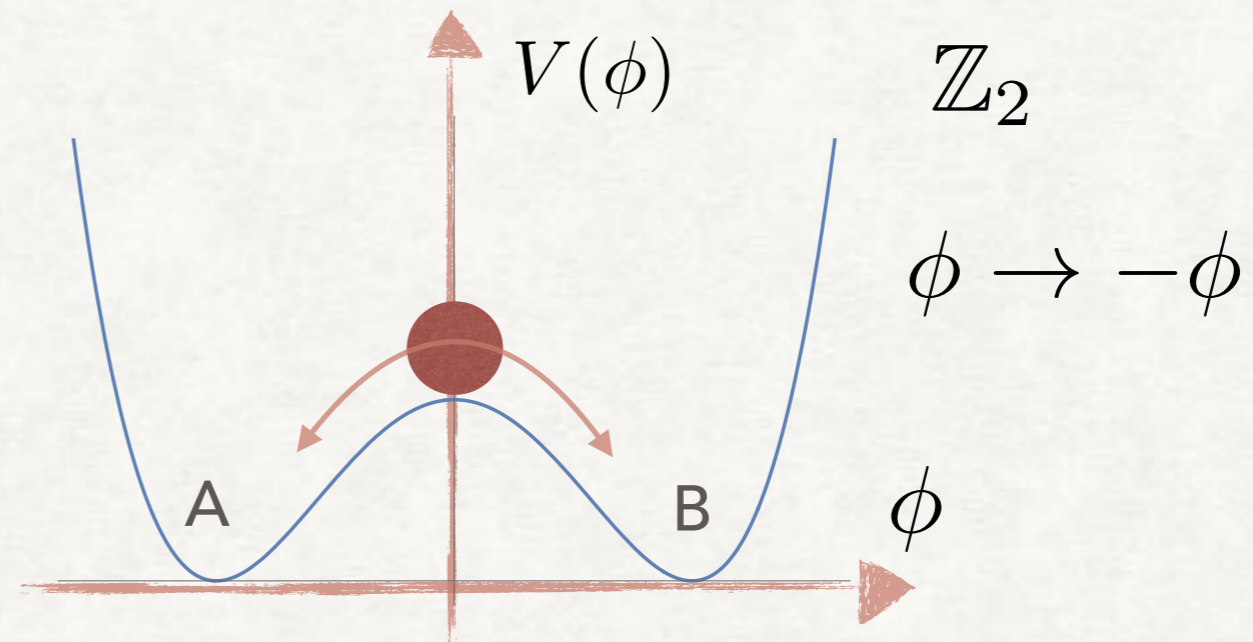
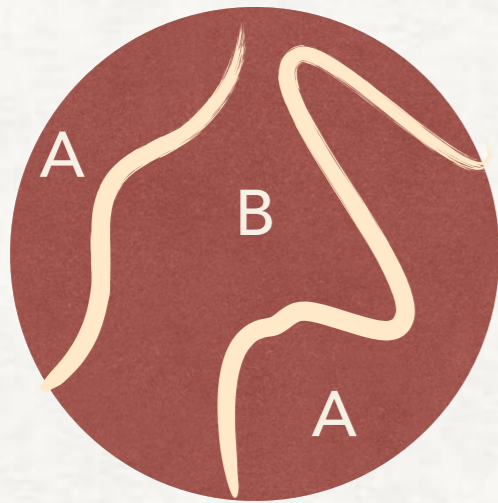
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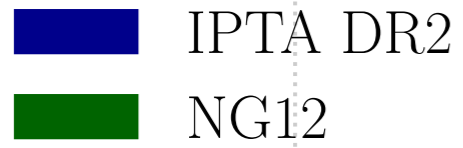
*Two-dimensional defects associated to (spontaneous) breaking of discrete symmetries*



***Crucial advantage: Scaling Regime***

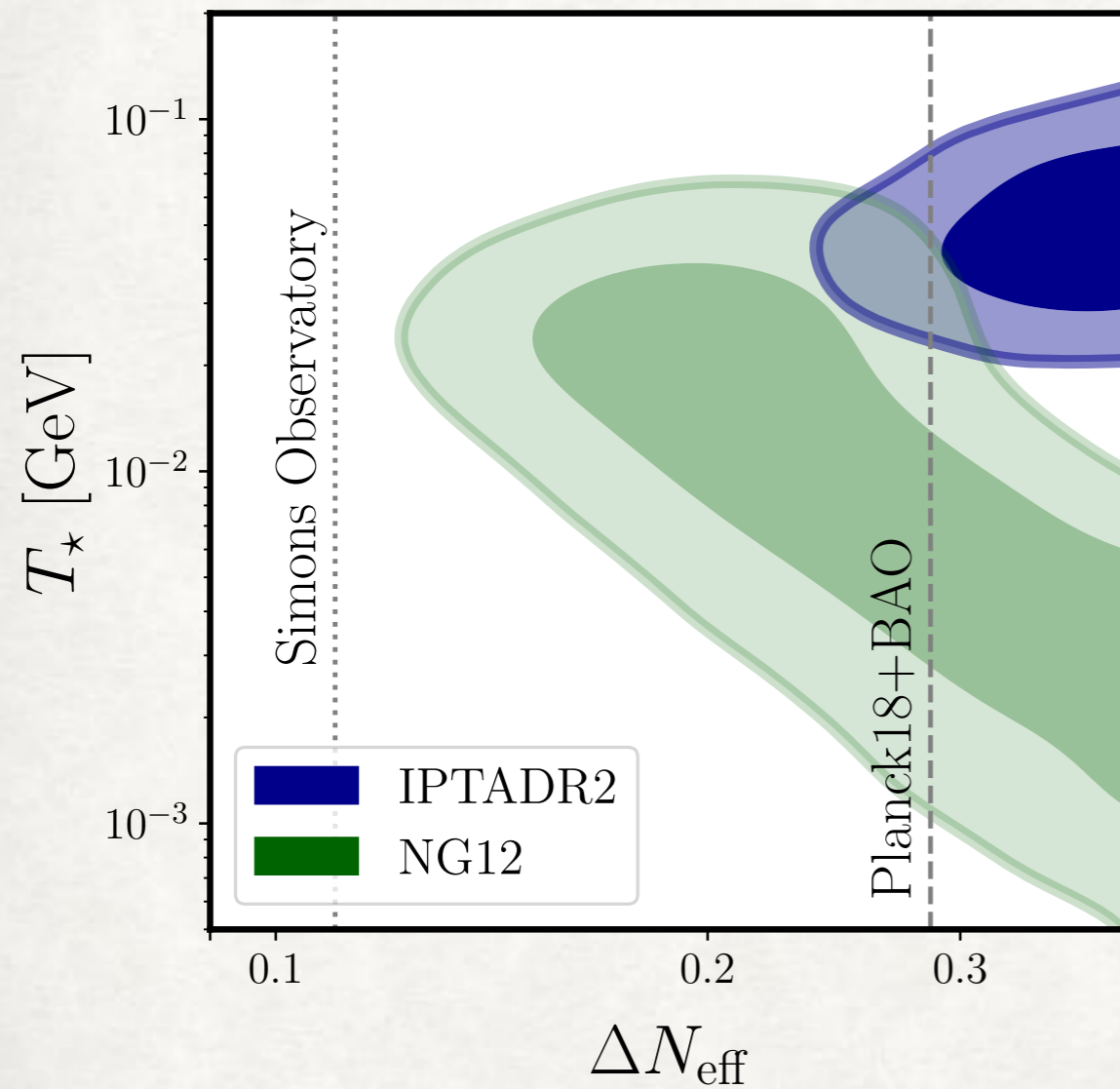
*Wall network is dominated by fixed number ( $\sim 1$ -few) of Hubble-sized wall*

# DOMAIN WALLS IN PTA DATASETS (2022)

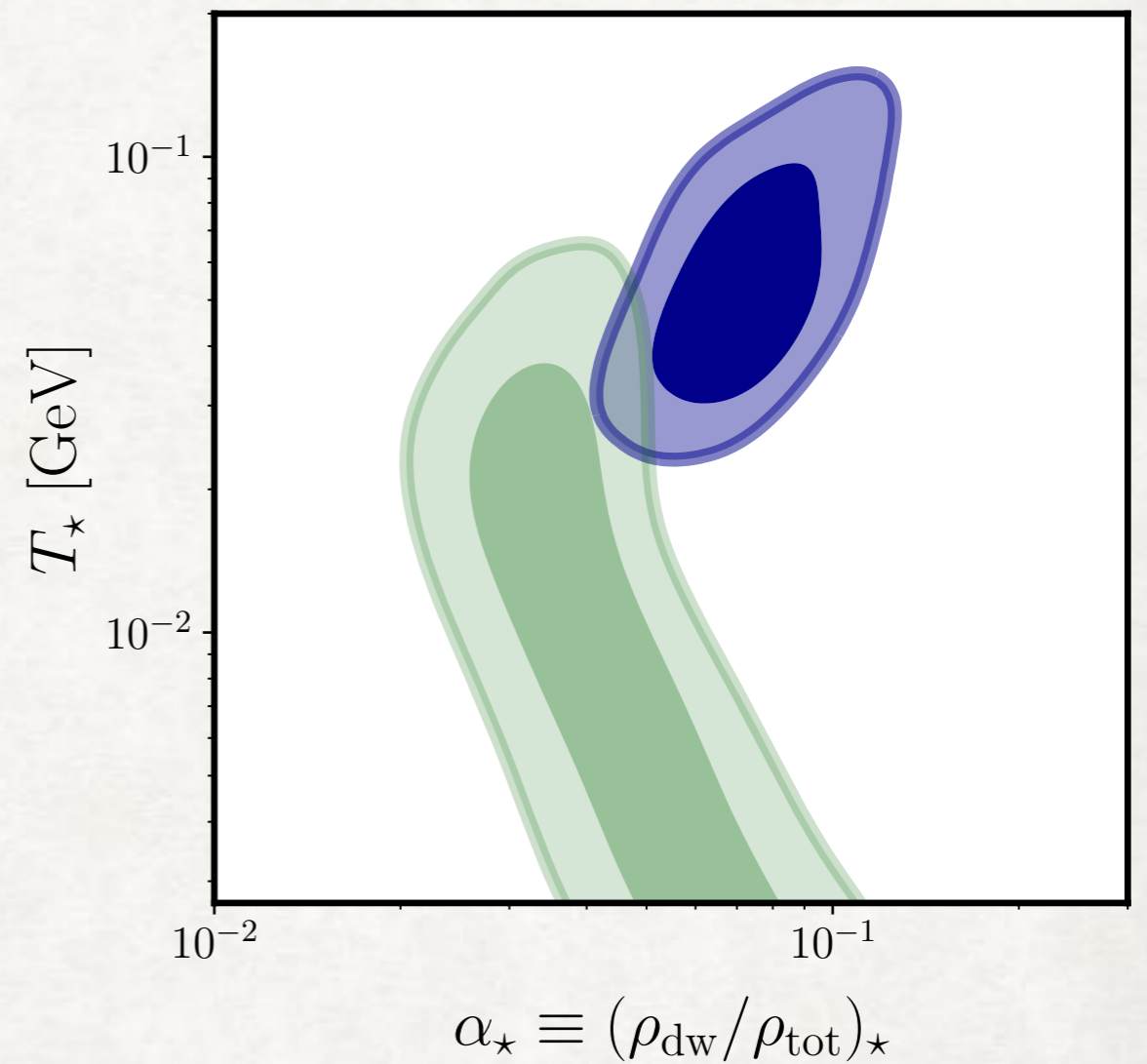


enterprise

Decay to Dark Radiation



Decay to Standard Model

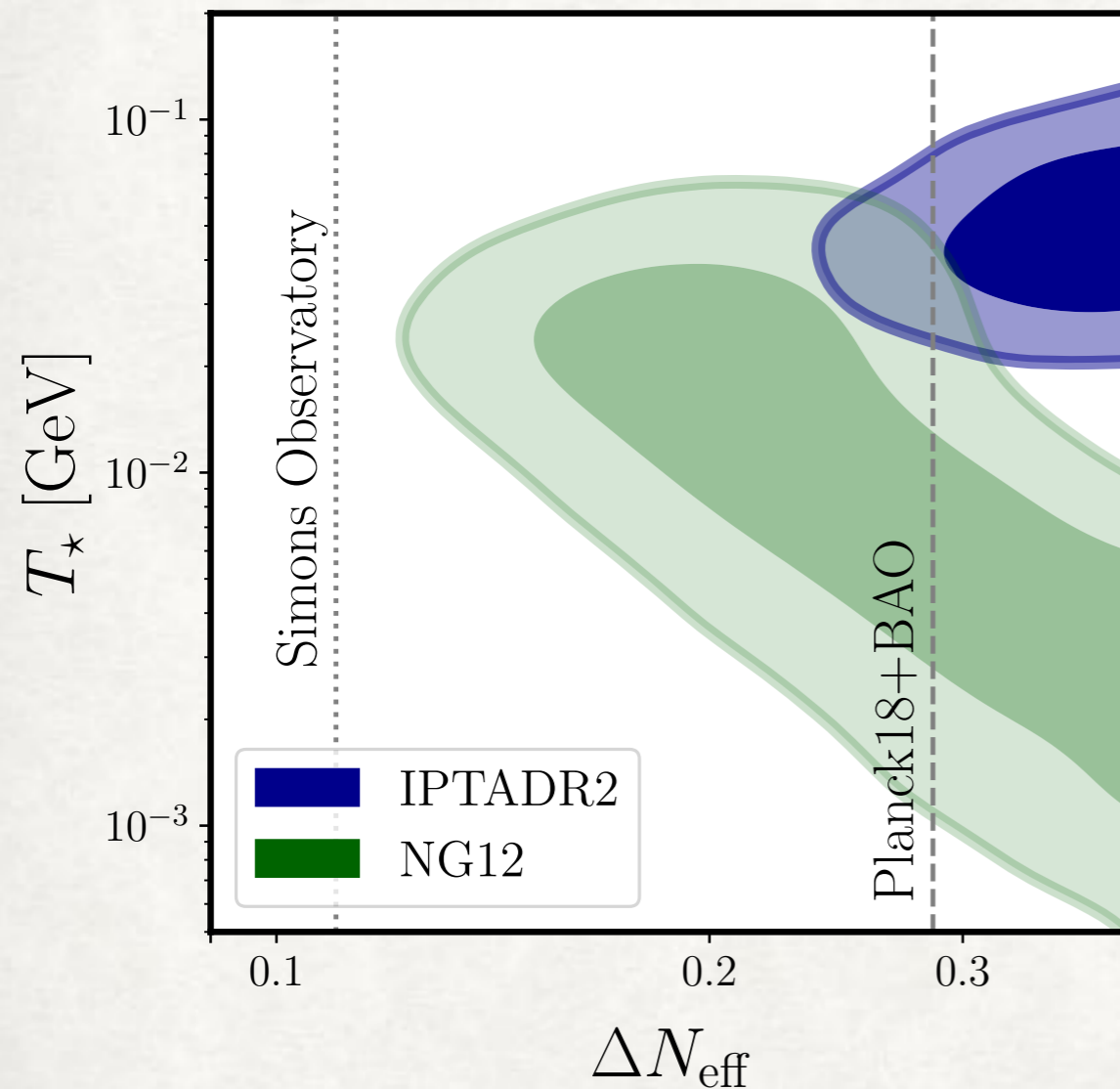


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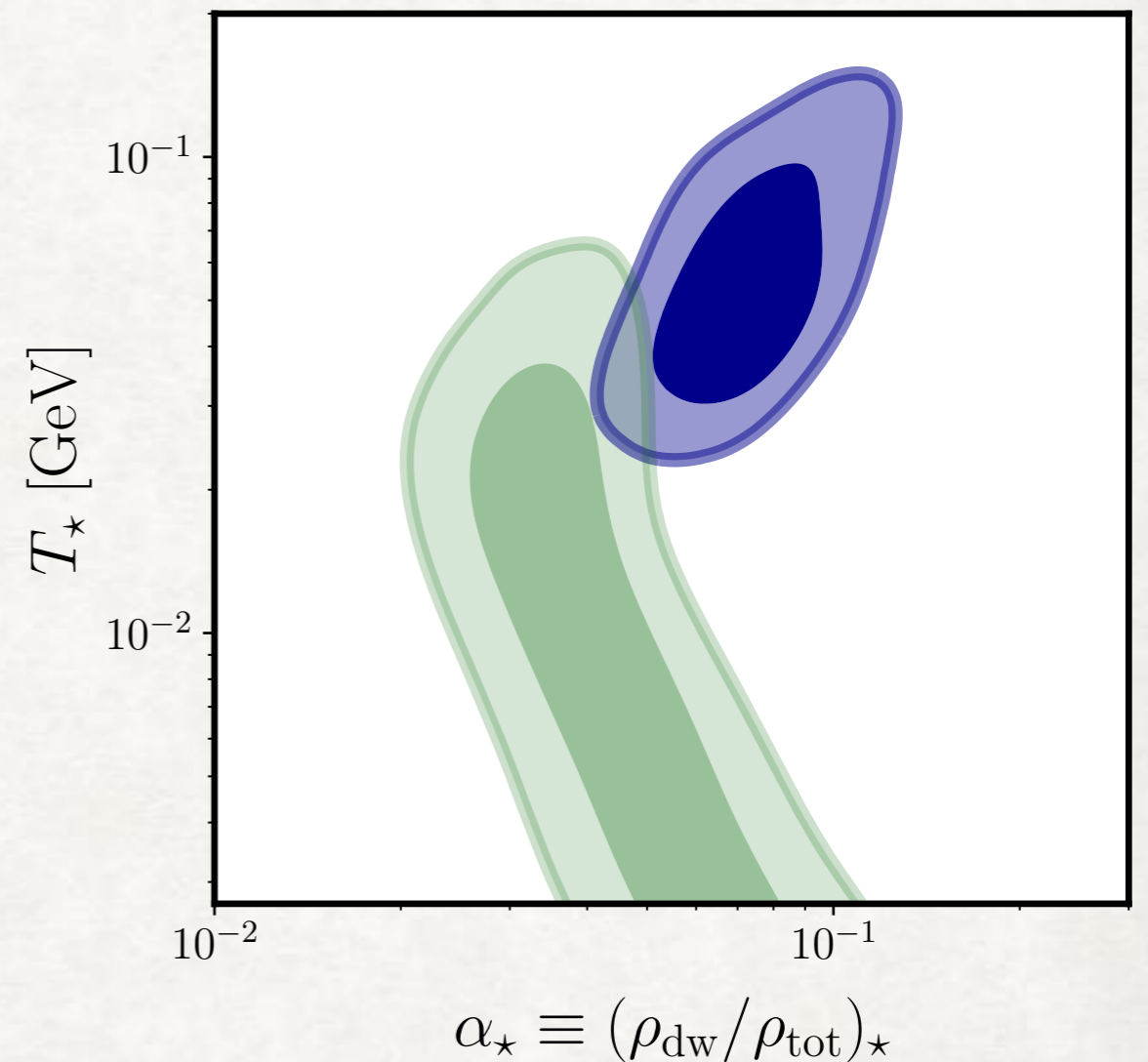


enterprise

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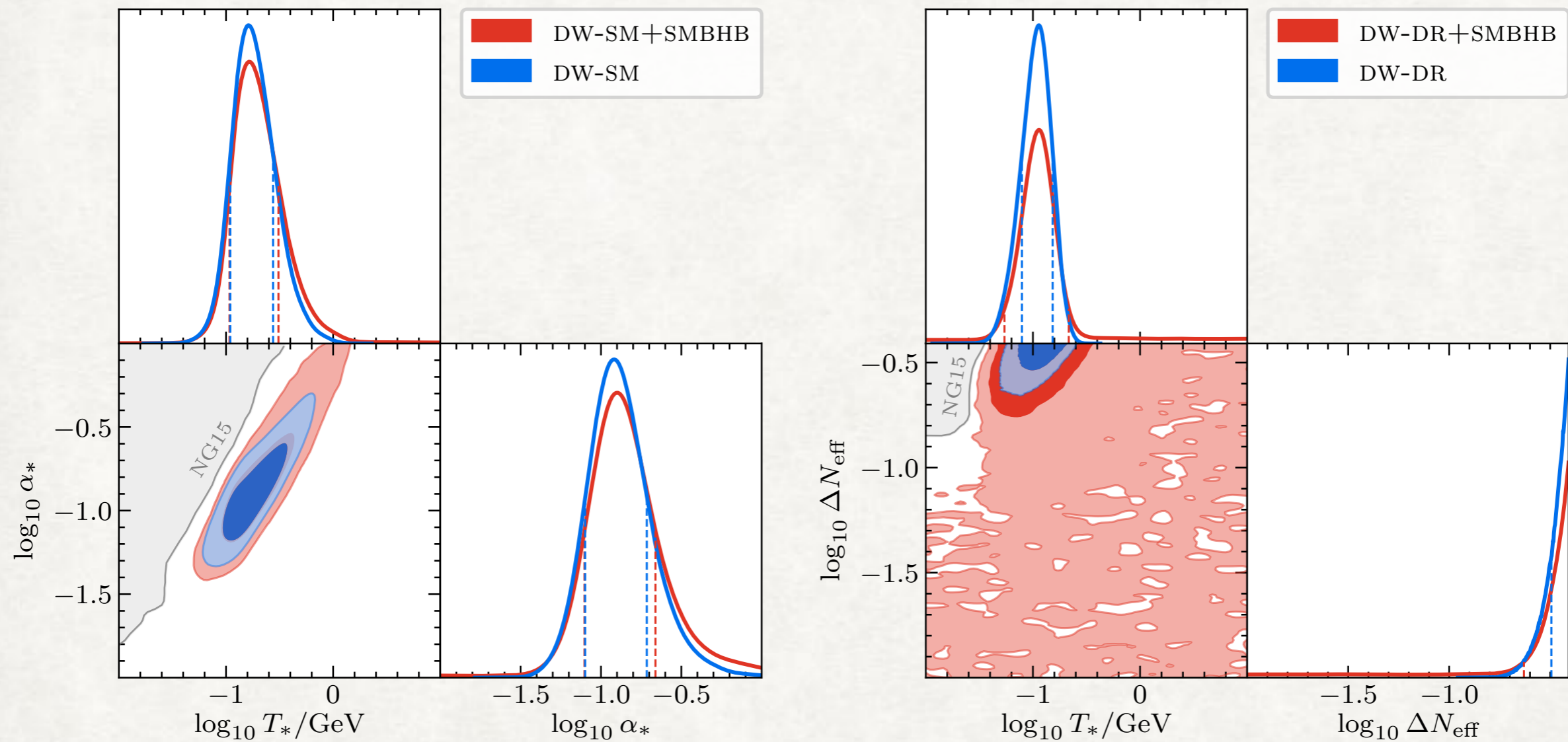


Decay to Standard Model

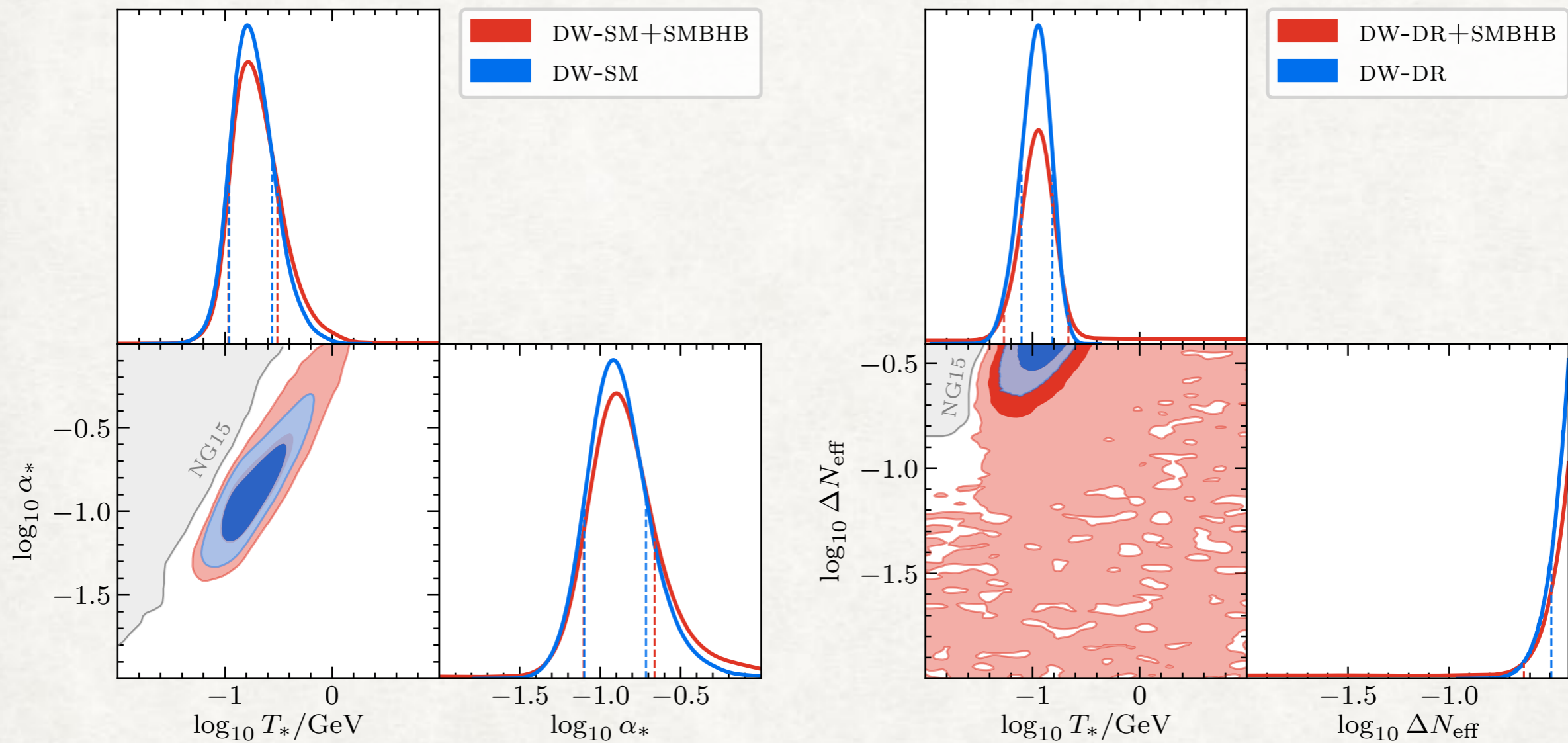


*Prior from BBN included, CMB severely  
constrains "dark" scenario*

# DOMAIN WALLS IN NANOGRAV 15 (2023)



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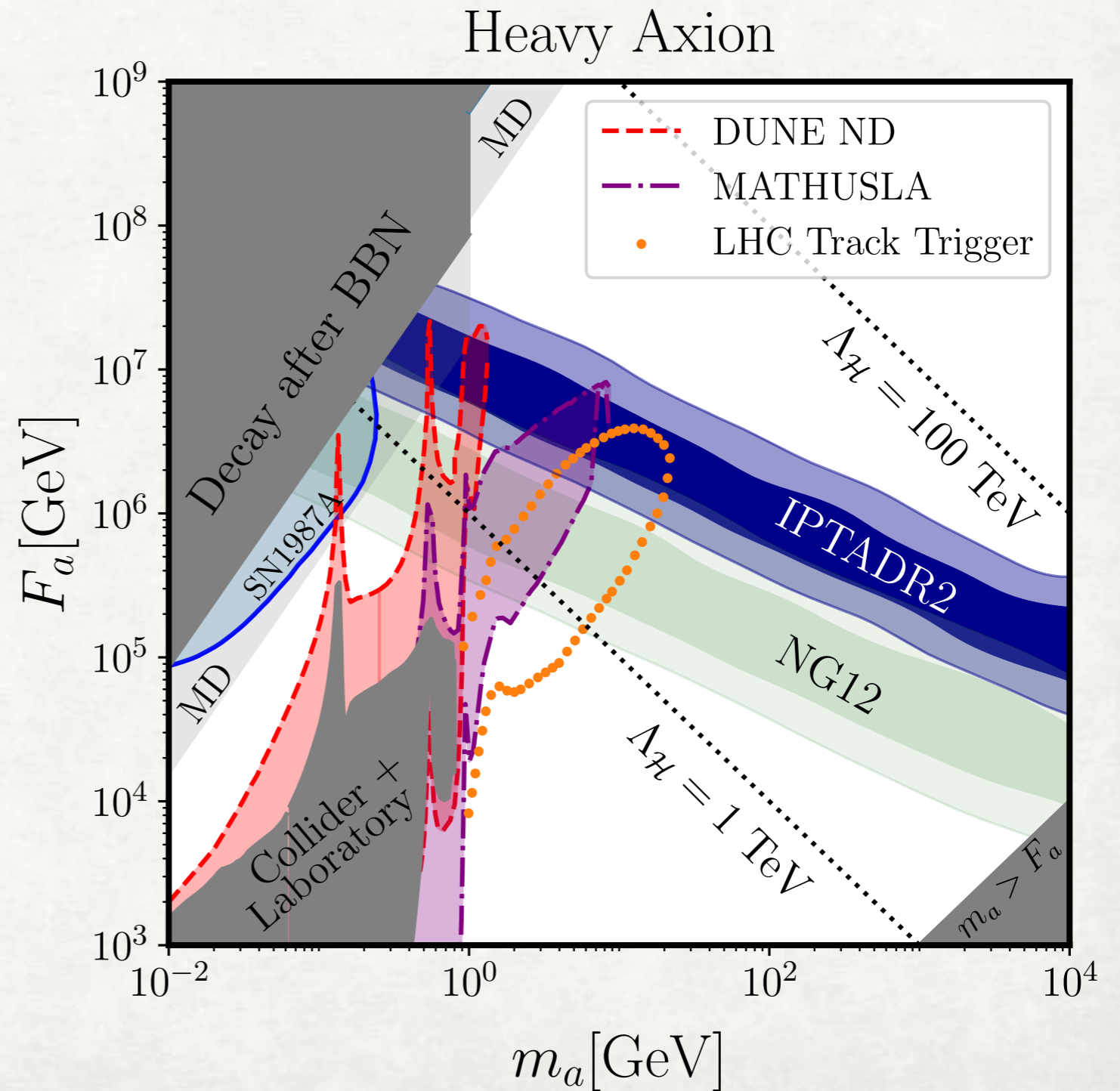


*Similar to IPTA DR2 results*

# AN INTERESTING SCENARIO WITH COMPLEMENTARY PROBES

$$U(1) \rightarrow \mathbb{Z}_{N_{\text{dw}}} \rightarrow I$$

$$\Lambda_{\mathcal{H}} \gg \Lambda_{\text{QCD}}$$





# AN INTERESTING SCENARIO WITH COMPLEMENTARY PROBES

$$U(1) \rightarrow \mathbb{Z}_{N_{\text{dw}}} \rightarrow I$$

Analogous to QCD axion

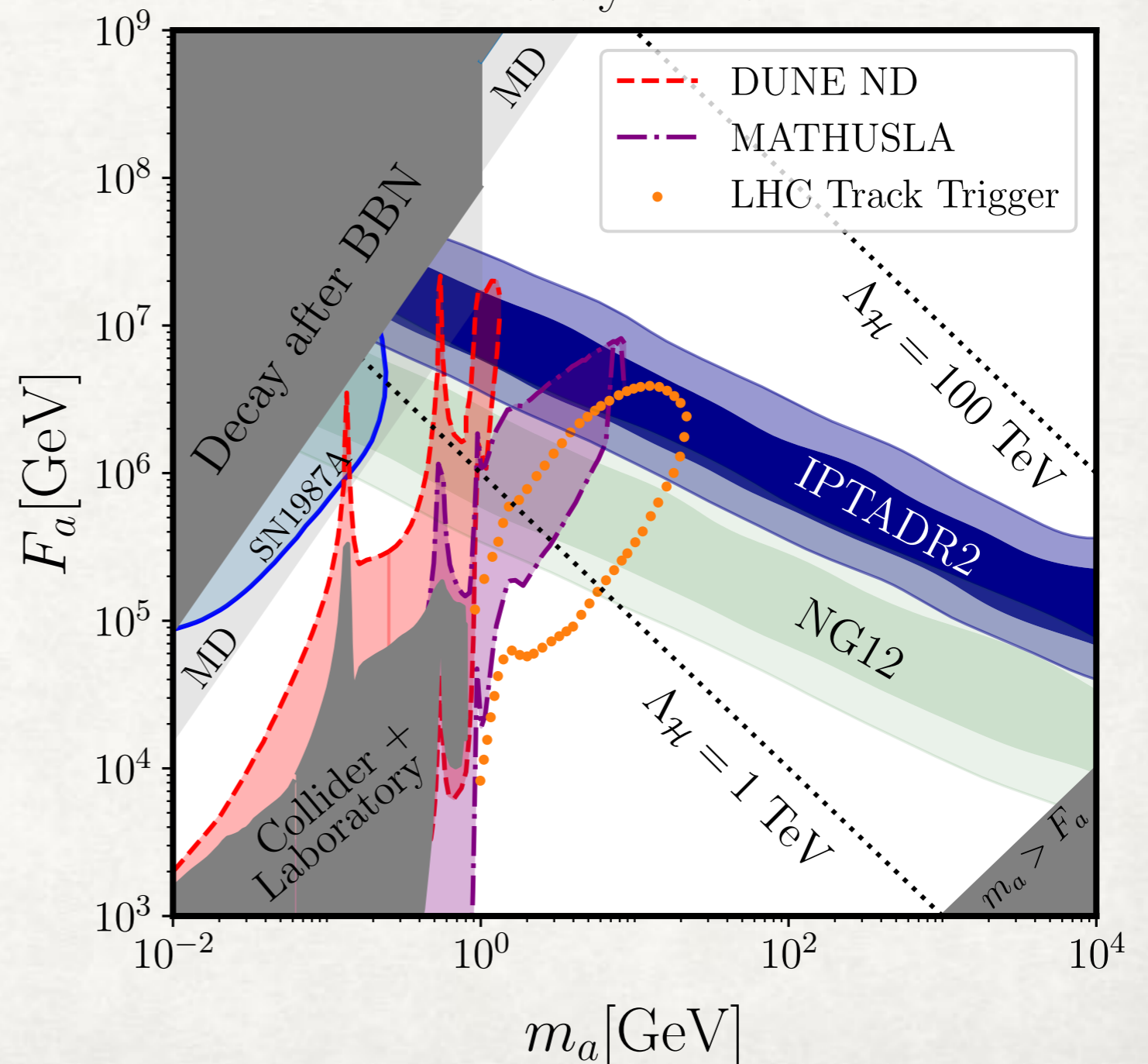
But different confinement scale

$$\Lambda_{\mathcal{H}} \gg \Lambda_{\text{QCD}}$$

If also coupled to QCD,  
complementary  
signatures at colliders!  
(& possibly inducing  
annihilation?)

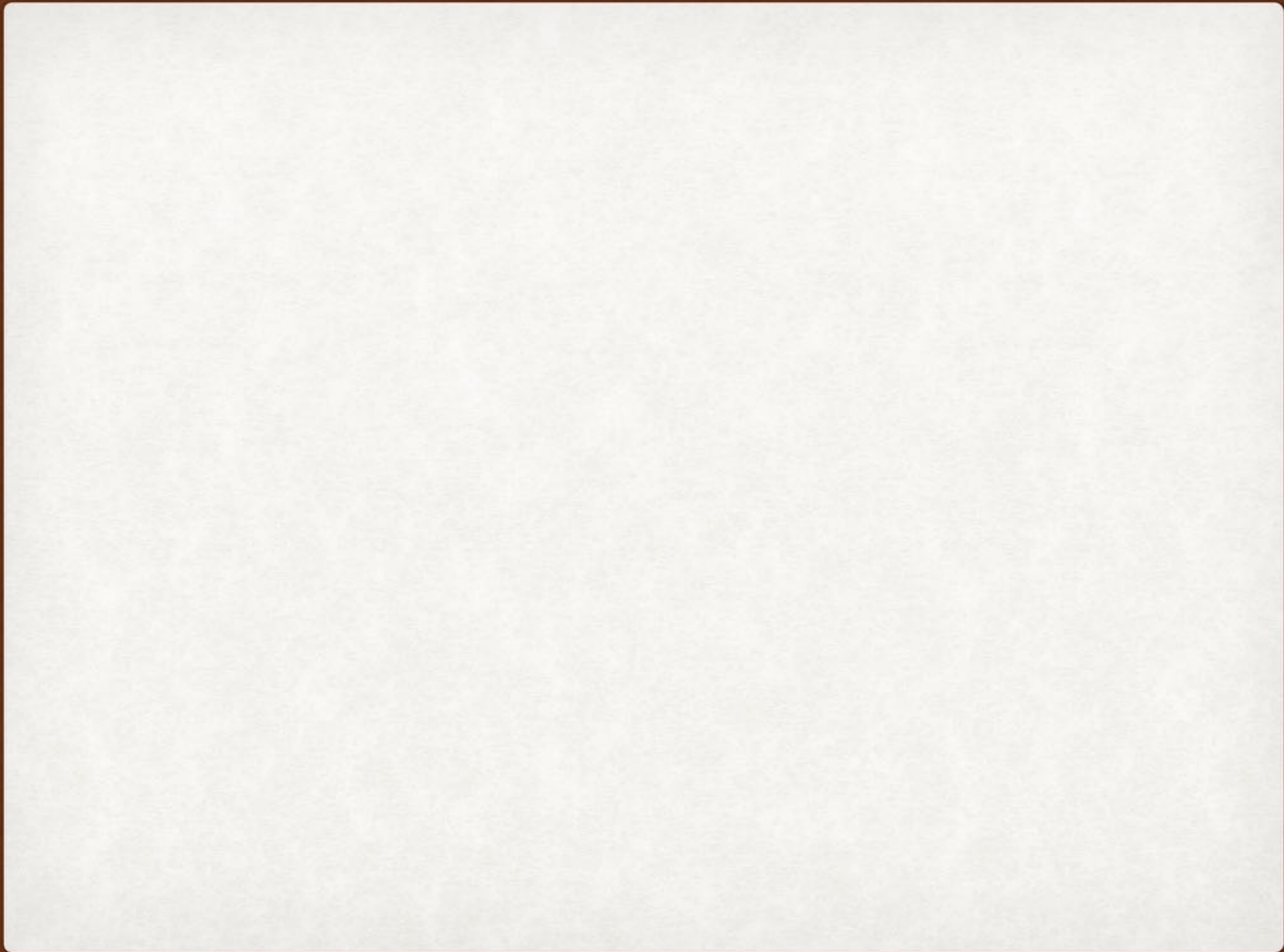
See also: Higaki+ 16/  
Blasi, Mariotti, Rase,  
Sevrin/Kitajima+/-...

Heavy Axion



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*Cosmic Domain Walls interesting because of scaling, complementary signals at lab/colliders for axion models*