### 



#### **Final-state interactions in neutrino experiments**

#### Outline

1 How FSI in exclusive one-nucleon knockout is described: Optical potential approach

- 2 Comparison of the optical potential and the NEUT cascade
- 3 What is the input to the cascade ?
- 4 Intermediate-energy measurements: neutrinos from Kaon decay-at-rest



Electron and neutrino scattering: Similar in theory, not in experiment



#### Exclusive electron scattering: Missing energy distributions



**‡** Fermilab



Direct 1-proton knockout from a nuclear shell

Alexis Nikolakopoulos | Neutrino Scattering at Low and Intermediate Energies, MITP 27 June 2023

Fermilab

#### Optical potential approach



$$\begin{aligned} (H_{ij} - E) |\phi_j\rangle &= -V_{j0} |\phi_0\rangle \ (i, j > 0) \bullet \\ \downarrow \\ \left[ H^{free} + V_{00}^{nA} + V_{0j} \frac{1}{E - H_{ij} + i\eta} V_{j0} - E \right] |\phi_0\rangle \ \bullet \end{aligned}$$

Coupled channels problem  $\rightarrow$  Effective one-body problem as a formal solution  $\clubsuit$  Fermilab

#### Optical potential approach



$$\begin{bmatrix} H^{free} + V_{00}^{nA} + V_{0j} \frac{1}{E - H_{ij} + i\eta} V_{j0} - E \end{bmatrix} |\phi_0\rangle \bullet \\ \approx \begin{bmatrix} H^{free} + \mathcal{V}^{opt} - E \end{bmatrix} |\phi_0\rangle$$

Coupled channels problem  $\rightarrow$  Effective one-body problem with optical potential

**‡** Fermilab

#### The (empirical) relativistic optical potential

#### PHYSICAL REVIEW C

VOLUME 47, NUMBER 1

JANUARY 1993

#### Global Dirac phenomenology for proton-nucleus elastic scattering

E. D. Cooper, S. Hama, and B. C. Clark Department of Physics, The Ohio State University, Columbus, Ohio 43210

R. L. Mercer

IBM Thomas J. Watson Research Center, Yorktown Heights, New York 10598 (Received 31 August 1992)

Target	$T_p$ (MeV)					
			EDAD-fit			
		EDAI-fit	fit 1	fit 2	fit 3	Reference
<sup>12</sup> C	29.00	420.2	435.5	433.1	422.7	[6]
	30.30	415.9	429.0	425.6	414.2	[7]
	49.00	358.8	363.0	348.4	327.7	[6]
	49.48	357.4	361.8	347.0	326.1	[8]
	61.40	323.3	335.6	317.0	294.8	[9]
	65.00	313.5	329.0	309.7	287.4	[10]
	122.00	202.2	269.0	254.4	230.5	[11]
	160.00	177.8	252.3	246.4	215.2	[11]
	200.00	177.6	243.0	243.9	205.0	[11-13]
	300.00	201.1	233.0	235.4	194.9	[14]
	398.00	215.8	227.4	218.6	199.1	[15]
	494.00	227.2	223.7	203.0	211.6	[16]
	797.50	238.4	235.3	209.9	250.0	[17,18]
	1040.00	198.6	259.4	243.8	232.2	[19,20]

Fit to elastic proton-nucleus scattering data

8





#### Exclusive electron scattering with Optical potential: 'standard approach'





FIG. 11. The reduced cross section ( $\sigma_{red}$ ) of the <sup>16</sup>O(e,e'p) reaction as a function of the recoil momentum  $p_m$  for the transitions to the  $1/2^-$  ground state and to the  $3/2^-$  excited state of <sup>15</sup>N, in

#### Benchmarking intranuclear cascade models for neutrino scattering with relativistic optical potentials

A. Nikolakopoulos<sup>(0)</sup>,<sup>1,2,\*</sup> R. González-Jiménez<sup>(0)</sup>,<sup>3</sup> N. Jachowicz,<sup>1</sup> K. Niewczas,<sup>1,4</sup> F. Sánchez<sup>(0)</sup>,<sup>5</sup> and J. M. Udías<sup>(0)</sup>



🛠 Fermilab

Where do the protons go ?: explicit modeling of 'rescattering'

Neutrino event generators use intra-nuclear cascade models (INCs)

- Hadrons move in the nucleus on classical trajectories
- Density and in-medium cross section determine mean-free-path
- Interaction produces secondary hadrons that are propagated through
- Stochastically determines final-state content

#### Black box

INC( $\alpha_i$ ) = P( $\beta_f | \alpha_i$ ) Produce a distribution of configurations  $\beta_f$ From some input state  $\alpha_i$ 



辈 Fermilab

#### Thinking about INCs: knockout cross sections

Production 
$$Q + A \rightarrow p + X$$
 of a state  $|pX\rangle = |p\rangle$  (exclusive)  
 $|\langle \Psi_i | J^{\mu} | p \rangle|^2 = |\sum_{\alpha} \langle \Psi_i | J^{\mu} | \psi_{\alpha} \rangle \langle \psi_{\alpha} | p \rangle|^2$   
 $\approx \sum_{\alpha} \langle \Psi_i | J^{\mu} | \psi_{\alpha} \rangle^2 \langle \psi_{\alpha} | p \rangle^2$  Classical approximation

Replace formal sum by energy-momentum conserving single-nucleon states

$$\sum_{p} \langle \Psi_i | J^{\mu} | \psi_p(p_{as}) \rangle^2 \langle \psi_p(p_{as}) | p \rangle^2 \qquad \qquad p_{as} = p_Q + p_A - p_X$$

Fermilab

And approximate by cascade:

$$\sum_{p} \langle \Psi_i | J^{\mu} | \psi_p(p_{as}) \rangle^2 P(\vec{p}, \vec{p}_{as})$$

#### Thinking about INCs: knockout cross sections

 $\sum \langle \Psi_i | J^{\mu} | \psi_p(p_{as}) \rangle^2 P(\vec{p}, \vec{p}_{as})$ INC Inclusive cross section

- Classical approximation
- Truncation of sum
- Loss of full info (J,s,r,p<sub>x</sub>,...)

• ...

This is generally how the INC is used in neutrino event generators

But...

Not all approaches deal with states that have a suitable  $p_{as}$ Many approaches don't provide nucleon information at all  $\rightarrow$  The generator has to 'make them up'

The asymptotic momentum might not capture the optimal degrees-of-freedom: E.g. At low energy transfer: excitation energy and spin-parity are better



#### Cascade model with rROP inputs



$$\tilde{E}_m = E_i - E_l - T_p$$

#### T2K flux-folded calculations

- Cascade moves strength from shell model peaks to larger E<sub>m</sub> => Rescattering into different final states
- Strength of shell model peaks after INC agrees with ROP predictions
- A 'consistent' picture emerges between inclusive and exclusive results



#### Cascade model with rROP inputs



$$\tilde{E}_m = E_i - E_l - T_p$$

#### T2K flux-folded calculations

- Cascade moves strength from shell model peaks to larger E<sub>m</sub>
   => Rescattering into different final states
- Strength of shell model peaks agrees with ROP predictions
- Make kinematic cuts like in (e,e'p)
  - => Remove the rescattering
  - => exclusive conditions





#### Discrepancies at low-T<sub>N</sub>



### What the INC can learn from optical potentials



### T2K flux-folded calculations

The INC = ROP for high  $T_n$ 

For  $T_p < 100$  differences of up to 100% !

Constraints for cascades: Reaction cross section

### This study:

- Brings the constraints from the analysis of *elastic* and total cross sections
- Gives a quantummechanical benchmark in the low-T<sub>N</sub> region



Thinking about INCs

 $INC(\alpha_i) = P(\beta_f | \alpha_i)$ : Inputs  $\alpha_i$ : **p**, **r** of a set of hadrons

In v-interactions kinematics are given by a nuclear model e.g. plane-wave impulse approximation Local Fermi gas

What if there is no suitable **p** available ?



# From inclusive to semi-inclusive one-nucleon knockout in neutrino event generators

Alexis Nikolakopoulos <sup>1,\*</sup>, Steven Gardiner <sup>1</sup>, Afroditi Papadopoulou <sup>2</sup>, Stephen Dolan <sup>3</sup> and Raúl González-Jiménez <sup>4</sup> [arXiv:2302.12182]

The question: How do event generators generate hadrons from the **inclusive** cross section ?



Implementation of the SuSAv2-MEC 1p1h and 2p2h models in GENIE and analysis of nuclear effects in T2K measurements

S. Dolan,  $^{1,\,2,\,3}$  G.D.  $\rm Megias, ^{1,\,2,\,4}$  and S. Bolognesi^2

Implementation of the CRPA model in the GENIE event generator and analysis of nuclear effects in low-energy transfer neutrino-nucleus interactions

S. Dolan,  $^1$  A. Nikolakopoulos,  $^2$  O. Page,  $^3$  S. Gardiner,  $^4$  N. Jachowicz,  $^2$  and V. Pandey  $^5$ 

Implementation of SuSAv2, HF-CRPA, LFG+RPA (Valencia), SuSA-MEC, ... provide the **inclusive** cross section

=> The information on outgoing nucleon is not available

(Similar issues with MEC responses, Resonance production, ...)

🚰 Fermilab

# From inclusive to semi-inclusive one-nucleon knockout in neutrino event generators

Alexis Nikolakopoulos <sup>1,\*</sup>, Steven Gardiner <sup>1</sup>, Afroditi Papadopoulou <sup>2</sup>, Stephen Dolan <sup>3</sup> and Raúl González-Jiménez <sup>4</sup> [arXiv:2302.12182]

$$P(E_l, \theta_l, T_N, \Omega_N) = \sum_{M_B} \frac{d^4 \sigma(E_e, M_B)}{dE_{e'} d \cos \theta_{e'} d\Omega_N}.$$

We generate events for (e,e'p) in RDWIA with **real potential** 

• Full consistent description of exclusive kinematics 1e1p



## From inclusive to semi-inclusive one-nucleon knockout in neutrino event generators

Alexis Nikolakopoulos<sup>1,\*</sup>, Steven Gardiner<sup>1</sup>, Afroditi Papadopoulou<sup>2</sup>, Stephen Dolan<sup>3</sup> and Raúl González-Jiménez<sup>4</sup>



We generate events for (e,e'p) in RDWIA with **real potential** 

- Full consistent description of exclusive kinematics 1e1p
- Integrate over the proton → get the correct inclusive cross section (=includes 'elastic' FSI!)



# From inclusive to semi-inclusive one-nucleon knockout in neutrino event generators

Alexis Nikolakopoulos<sup>1,\*</sup>, Steven Gardiner<sup>1</sup>, Afroditi Papadopoulou<sup>2</sup>, Stephen Dolan<sup>3</sup> and Raúl González-Jiménez<sup>4</sup>

 $P(E_l, \theta_l, T_N, \Omega_N)$ 

Replace by 'factorized approach'

We get the GENIE version of the kinematics based on **the same** inclusive cross section! We generate events for (e,e'p) in RDWIA with **real potential** 

- Full consistent description of exclusive kinematics 1e1p
- Integrate over the proton → get the correct inclusive cross section (=includes 'elastic' FSI!)
- For every event we **replace** the nucleon kinematics by the GENIE prediction (SuSAv2 implementation)



$$\frac{\mathrm{d}\sigma(E_{\nu})}{\mathrm{d}E_{l}\mathrm{d}\cos\theta_{l}} = G^{2}\frac{k_{l}}{E_{\nu}}L_{\mu\nu}\int\mathrm{d}\Omega_{N}\sum_{n,\kappa}H_{n,\kappa}^{\mu\nu}(\omega,q,\Omega_{N},E_{n,\kappa})$$

Lost nucleon information  $\rightarrow$  Need to generate it in GENIE

1. Draw initial nucleon  $\mathbf{p}_{m}$  from  $p^{2}$  n(p) (e.g. LFG)

**!!** 2. Compute 
$$E_m^2 = p_m^2 + M_N^2$$

3.  $E_N = E_m + \omega - E_b(q)$ 



**‡** Fermilab



$$\frac{\mathrm{d}\sigma(E_{\nu})}{\mathrm{d}E_{l}\mathrm{d}\cos\theta_{l}} = G^{2}\frac{k_{l}}{E_{\nu}}L_{\mu\nu}\int\mathrm{d}\Omega_{N}\sum_{n,\kappa}H_{n,\kappa}^{\mu\nu}(\omega,q,\Omega_{N},E_{n,\kappa})$$

Lost nucleon information  $\rightarrow$  Need to generate it in GENIE

1. Draw initial nucleon  $\mathbf{p}_{m}$  from  $p^{2} n(p)$  (e.g. LFG)



$$\frac{\mathrm{d}\sigma(E_{\nu})}{\mathrm{d}E_{l}\mathrm{d}\cos\theta_{l}} = G^{2}\frac{k_{l}}{E_{\nu}}L_{\mu\nu}\int\mathrm{d}\Omega_{N}\sum_{n,\kappa}H_{n,\kappa}^{\mu\nu}(\omega,q,\Omega_{N},E_{n,\kappa})$$

Lost nucleon information  $\rightarrow$  Need to generate it in GENIE

1. Draw initial nucleon  $\mathbf{p}_m$  from  $p^2 n(p)$  (e.g. LFG)

112. Compute 
$$E_m^2 = p_m^2 + M_N^2$$
  
3.  $E_N = E_m + \omega - E_b(q)$   
4.  $k_N^2 = E_N^{2-} M_N^2$   
11  $|\mathbf{p}_m + \mathbf{q}| \neq k_N = \sqrt{E_N^2 - M_N^2}$   
 $\Rightarrow \mathbf{k}_N = \frac{k_N}{|\mathbf{p}_m + \mathbf{q}|} (\mathbf{p}_m + \mathbf{q})$ 



Serious differences in angular distributions!

Fermilab

$$\frac{\mathrm{d}\sigma(E_{\nu})}{\mathrm{d}E_{l}\mathrm{d}\cos\theta_{l}} = G^{2}\frac{k_{l}}{E_{\nu}}L_{\mu\nu}\int\mathrm{d}\Omega_{N}\sum_{n,\kappa}H_{n,\kappa}^{\mu\nu}(\omega,q,\Omega_{N},E_{n,\kappa})$$

Lost nucleon information  $\rightarrow$  Need to generate it in GENIE



Results for e4nu kinematics E=1.159 including the GENIE cascade!

Fermilab

Shape differences biggest in  $P_{\tau}$  and angular distributions

#### Thinking about INCs

INC( $\alpha_i$ ) = P( $\beta_f | \alpha_i$ ) : Inputs  $\alpha_i$ : **p**, **r** of a set of hadrons



Works well even at low-T<sub>p</sub>!

But **should it ?** Could more variables be used as input to the INC ? At low excitation energy outgoing nucleon kinematics are almost meaningless

🛠 Fermilab

#### Muon neutrinos from stopped Kaon's in the absorber



**MiniBooNE** 

KDAR produces  $v_{\mu}$  with  $E_{\nu}$  = 236 MeV

Can be a challenge for FSI modeling

#### Electron scattering in KDAR phase-space: <sup>40</sup>Ca

(See N. Jachowicz Talk on Monday)



#### Sk-HF CRPA w cut-off CRPA

Clear contribution from Collective d.o.f

→ transition region between 'quasielastic' and collective d.o.f

辈 Fermilab

#### MiniBooNE comparison: Model comparisons & Total cross sections



Shape-only comparisons of different models

Model	$\Delta \chi^2$	$\chi^2$ Prob.	$\sigma \ (10^{-39} {\rm cm}^2)$
Nuance	2.64	0.45	1.4
NuWro	2.07	0.56	1.3 + 0.4 (np-nh)
GENIE	0.95	0.81	1.75
Martini	2.15	0.54	1.3 + 0.2 (np-nh)
Singh	3.90	0.27	0.91
CRPA	3.20	0.36	1.58
RMF	3.49	0.27	1.56
RFG	1.69	0.64	1.66
RFG34	4.16	0.25	1.38
MB data	-	-	$2.7 \pm 1.2$

Total cross sections

Most ~ $1.5 - 1.7$	10 <sup>-39</sup> cm2/N
RFG34 & NUANCE ~ 1.4	10 <sup>-39</sup> cm2/N
Singh ~ 0.91	10 <sup>-39</sup> cm2/N

see also [Prog.Part.Nucl.Phys. 129 (2023) 104019] **Control** Control Co

#### JSNS<sup>2</sup> measurement (from Hyoungku Jeon talk NuFACT22)

Measure the total visible energy:

 $E_{vis} = E_v - m_\mu - T_x$ 

Sensitive to specific decay channel of nucleus



Fermilab

#### JSNS<sup>2</sup> measurement

#### Missing energy spectrum ( $\nu$ , $\mu$ p)



Fermilab

Clear smearing of spectrum in data Need good final-state approach

## Conclusions

- The ROP and INC approaches use nucleon-nucleus scattering to constrain FSI in different ways.
- A consistent comparison of the NEUT INC and optical potential shows that there is quantitative agreement at large kinetic energies.
   For small kinetic energy the differences are up to 100% !!
- The ROP should be more reliable in this comparison, but the true answer is unknown! Should measure (e,e'p) over large phase space with cut on missing energy
- Results of the generator will depend crucially on the input to the INC!
- Current implementations (necessarily) use unrealistic approximations
- Should be expected to break down at low excitation energies
- Unfactorized Events for flux-averaged signals over the whole phase space can be generated combined with INC provides inclusive and exclusive CS
   → You can use these for validation/error estimation/... of your own INC/simulation/...