

# 1S-3S Spectroscopy on hydrogen/deuterium atoms

Pauline Yzombard, Paul Martin, Simon Thomas, Hugo Tortel, Lucile Julien, François Biraben,  
François Nez



Sorbonne Université, CNRS, ENS, Collège de France



# Interest of H-like atoms spectroscopy ? In short

Ultra-accurate theory  $\Leftrightarrow$  highly resolved experiments

Proportional to  $R_\infty$

Internal energy of an atom:  $E = h f \approx (E_{\text{Dirac}} + E_{\text{QED}} + E_{\text{nucleous\_radius\_effect}})$

$\Rightarrow$  Spectroscopist point of view: 3 unknowns ( $R_\infty$ , QED,  $r_N$ )

-  $\alpha, me/mp, me/h$  very-well known by other experimental measurements

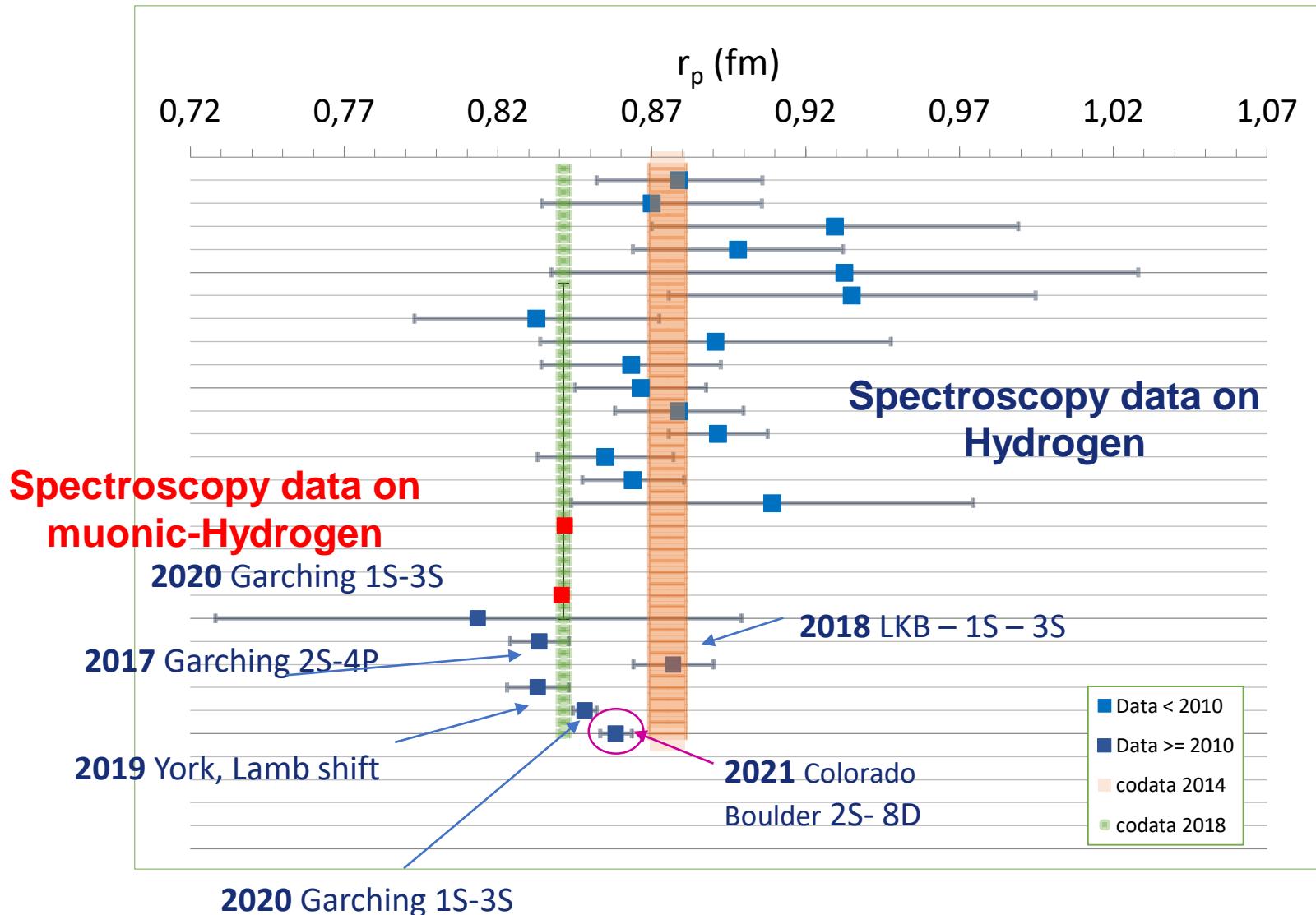
If QED exact (so fixed)  $\Rightarrow$  2 unknowns left:  $R_\infty$  and  $r_N$

$$f_{a-b} + f_{c-d} \Rightarrow R_\infty + r_N$$

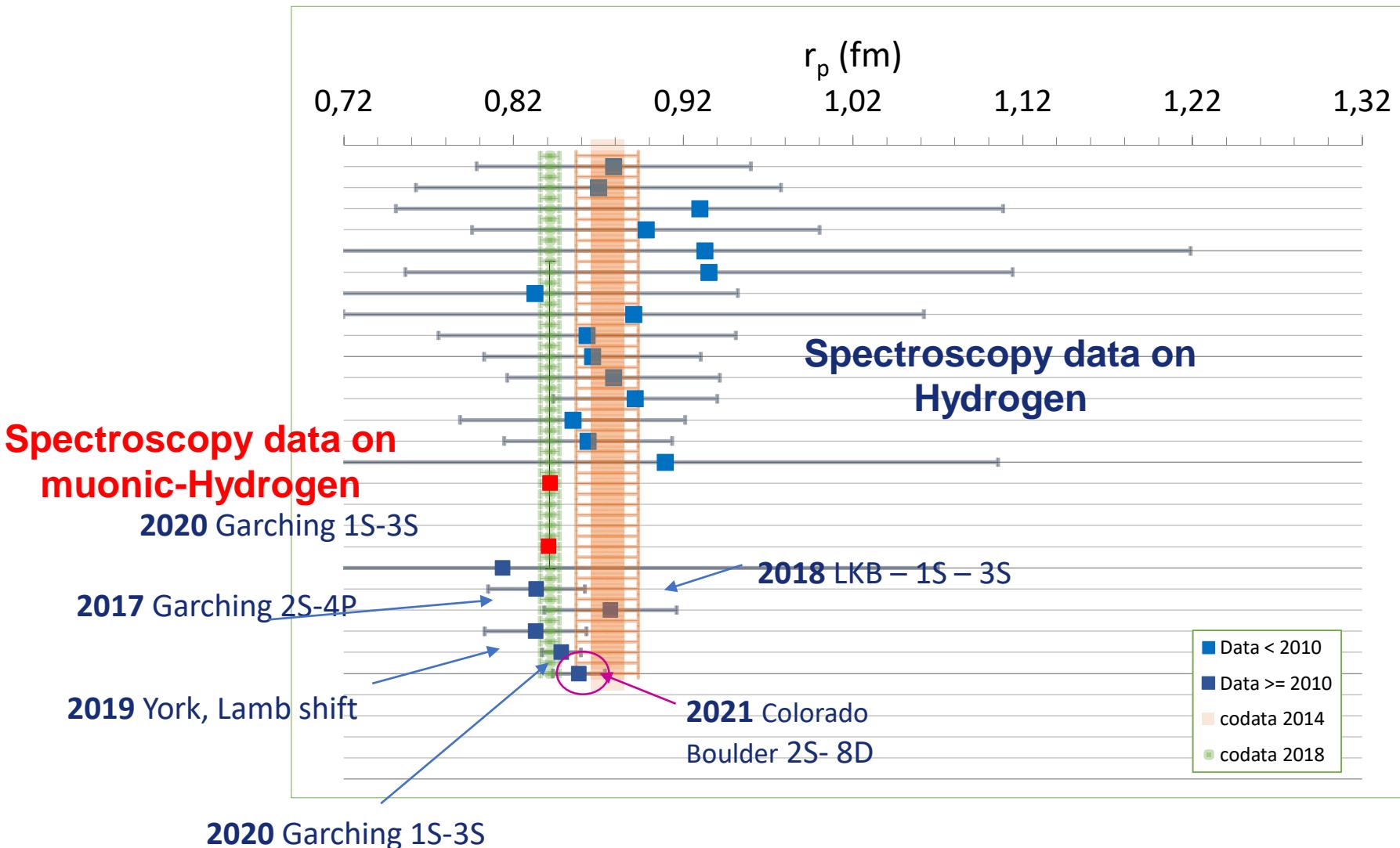
$\Rightarrow$  Requires only 2 transitions to be determined

$\Rightarrow$  With 3 and more: tests on consistancies can be done !

# The proton radius puzzle ? 1 sigma



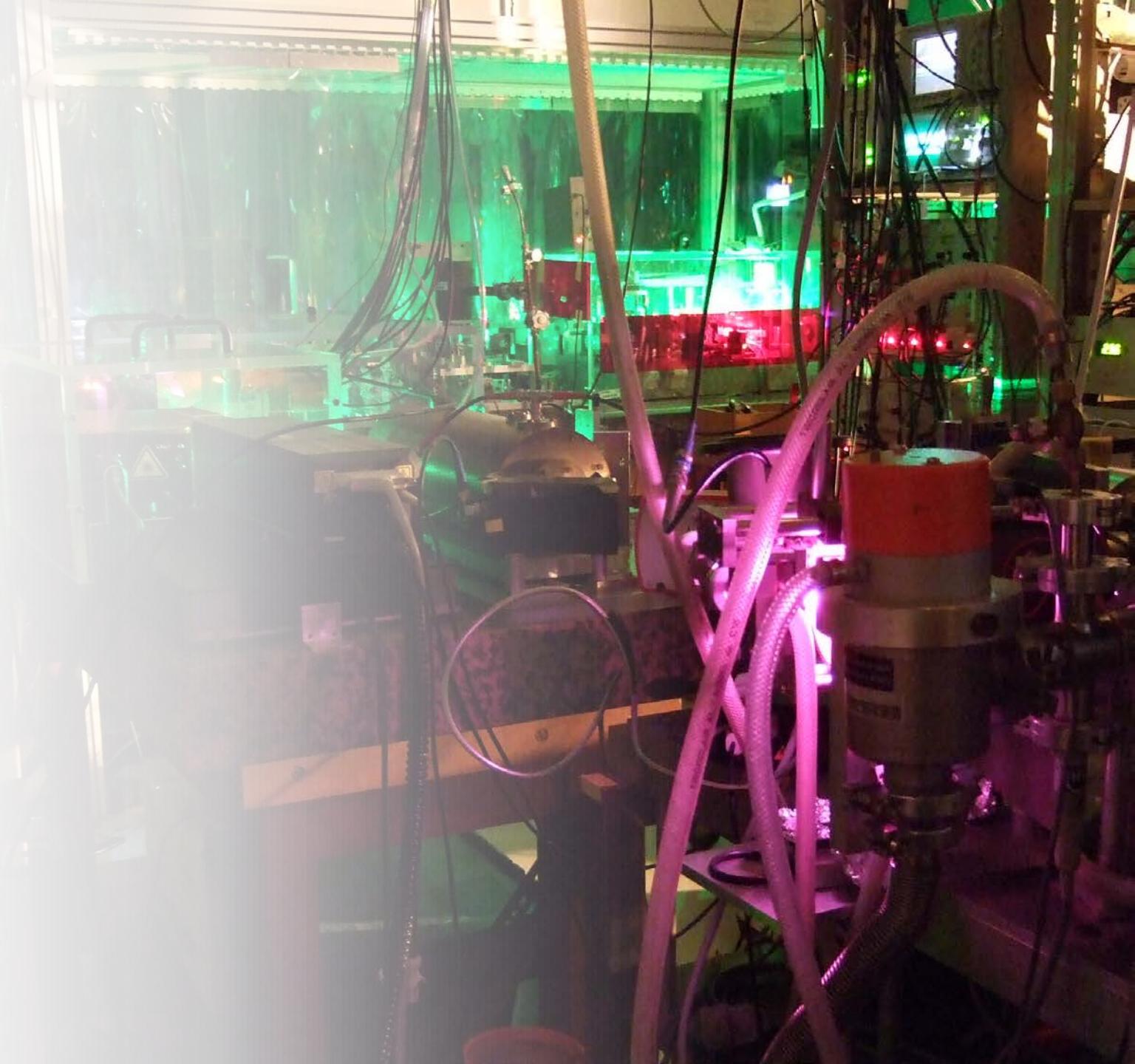
# The proton radius puzzle ? 3 sigmas



# Overview

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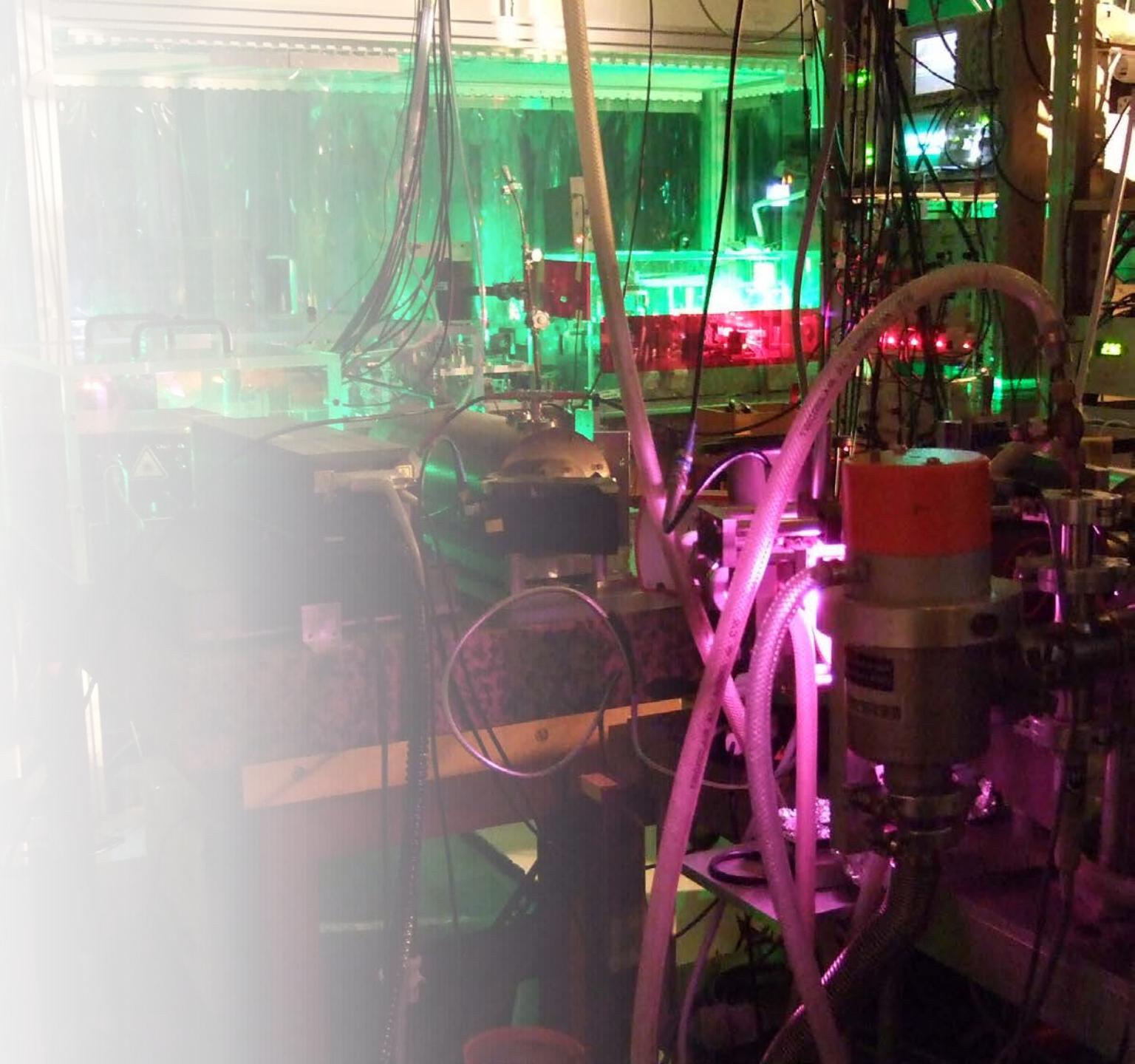
- 1S-3S Hydrogen spectroscopy
  - The experiment and some of the latest improvements
  - Dealing with systematics
  - A new systematics effect ?
  - What next ?



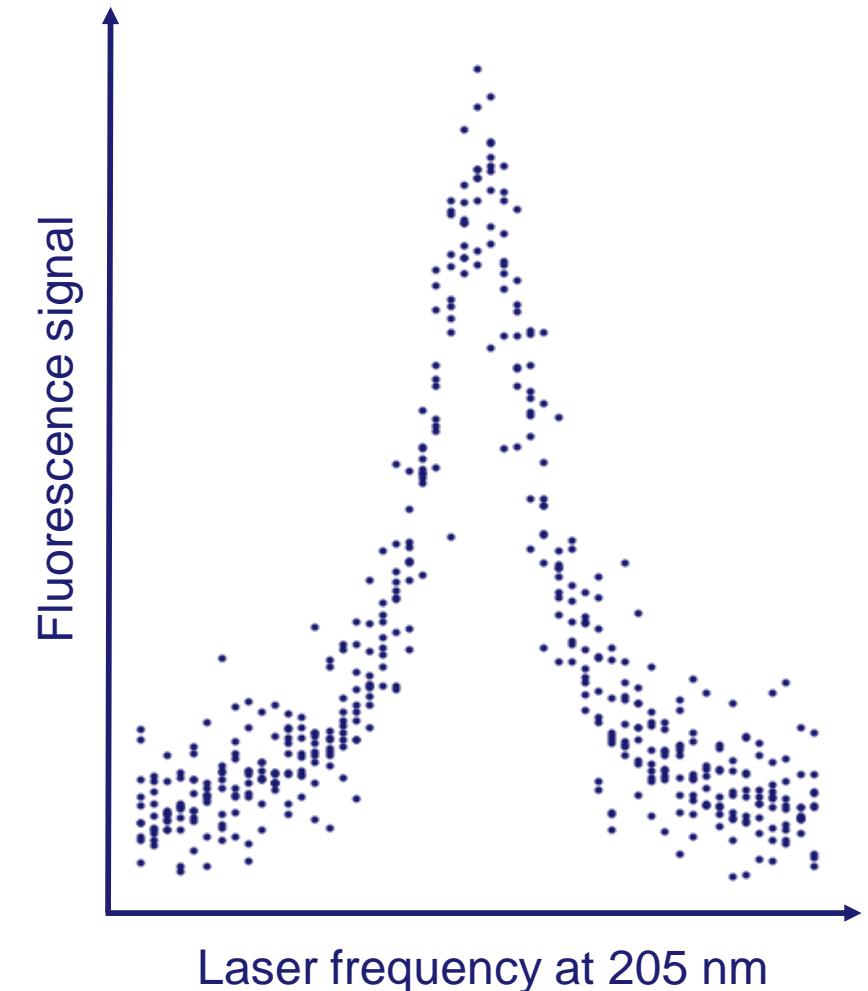
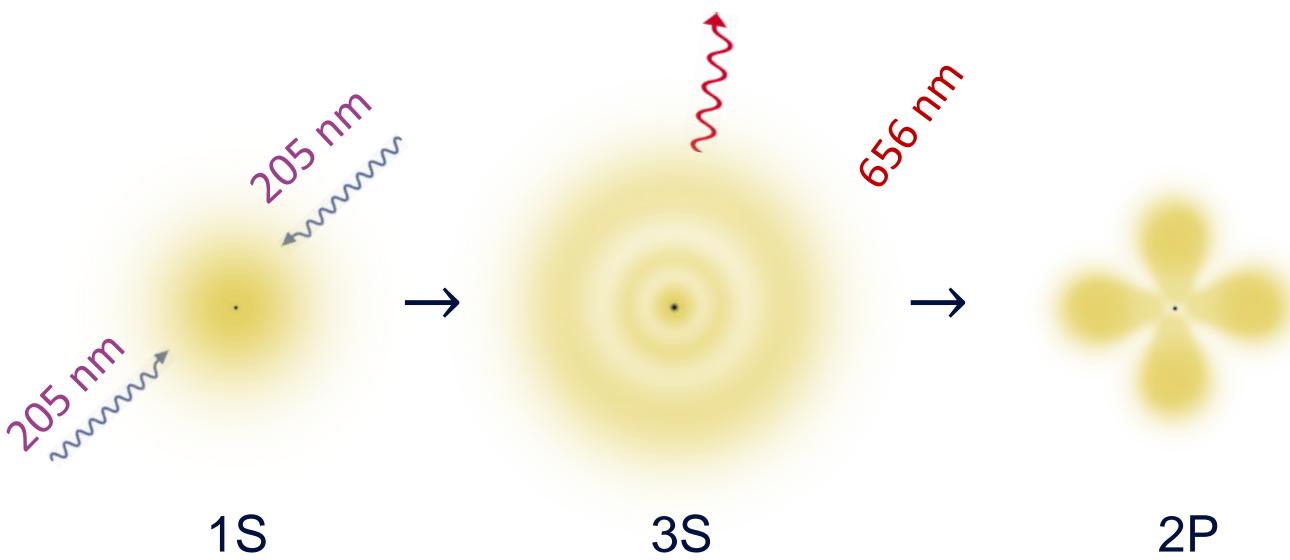
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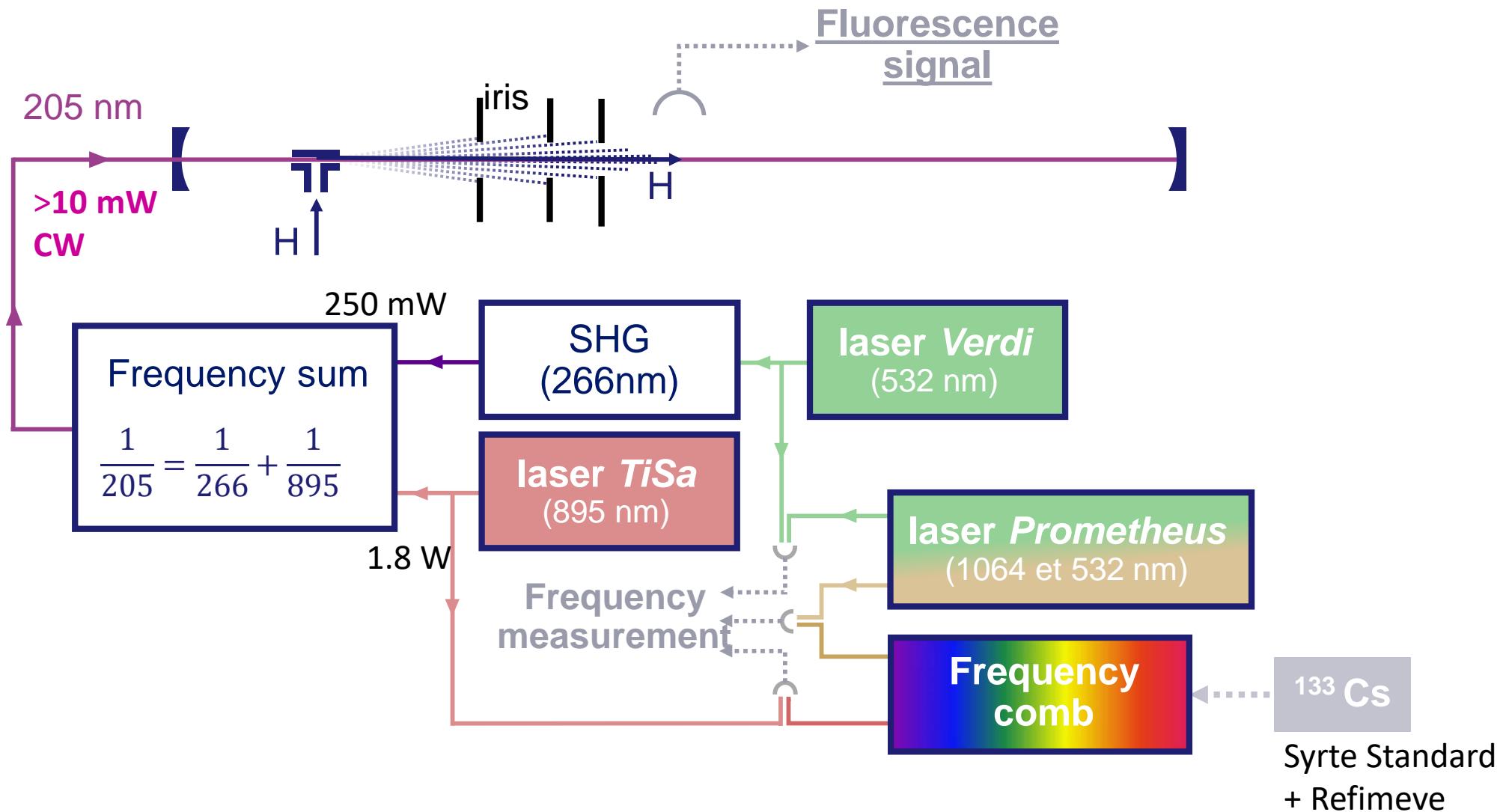
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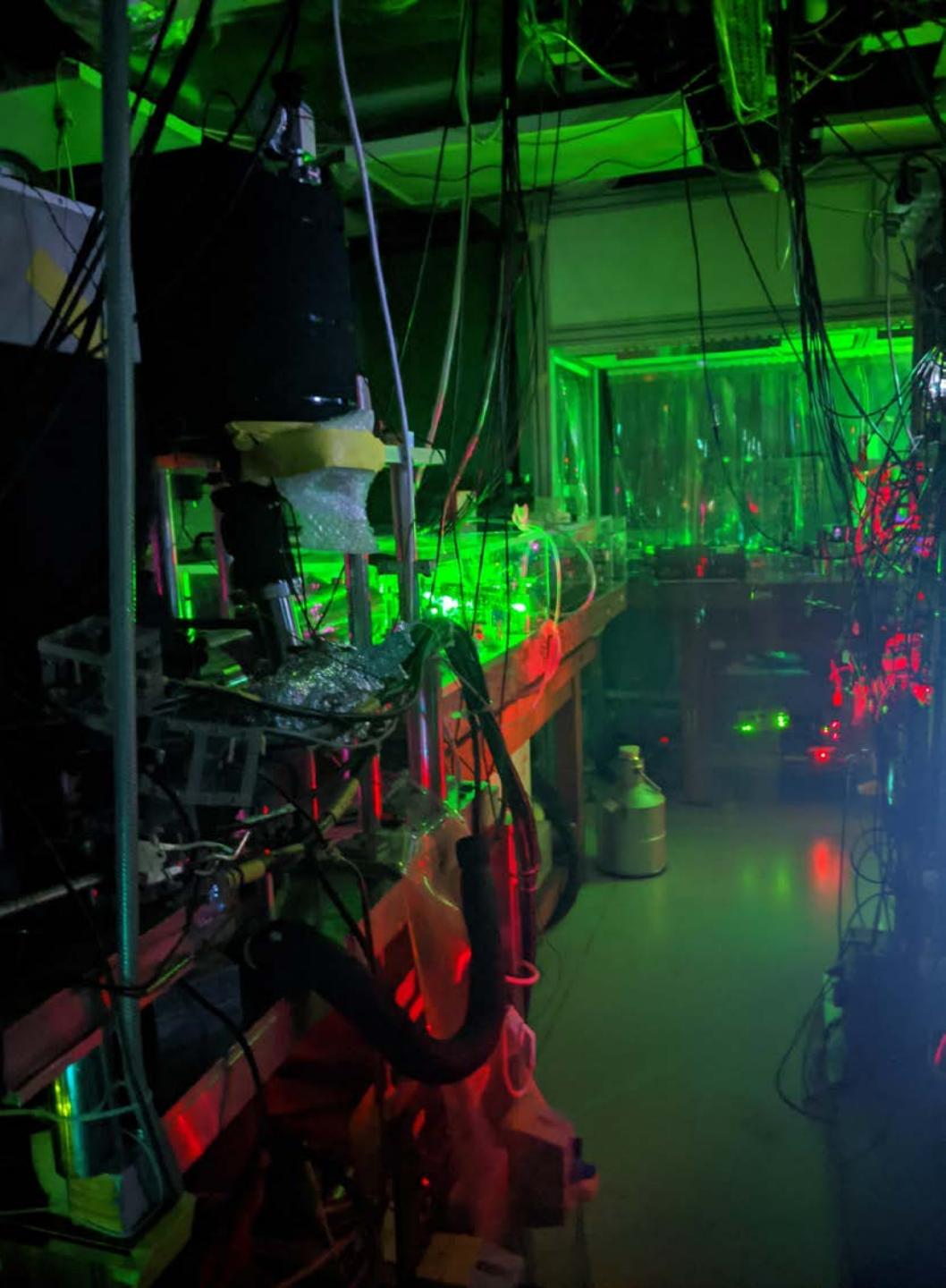
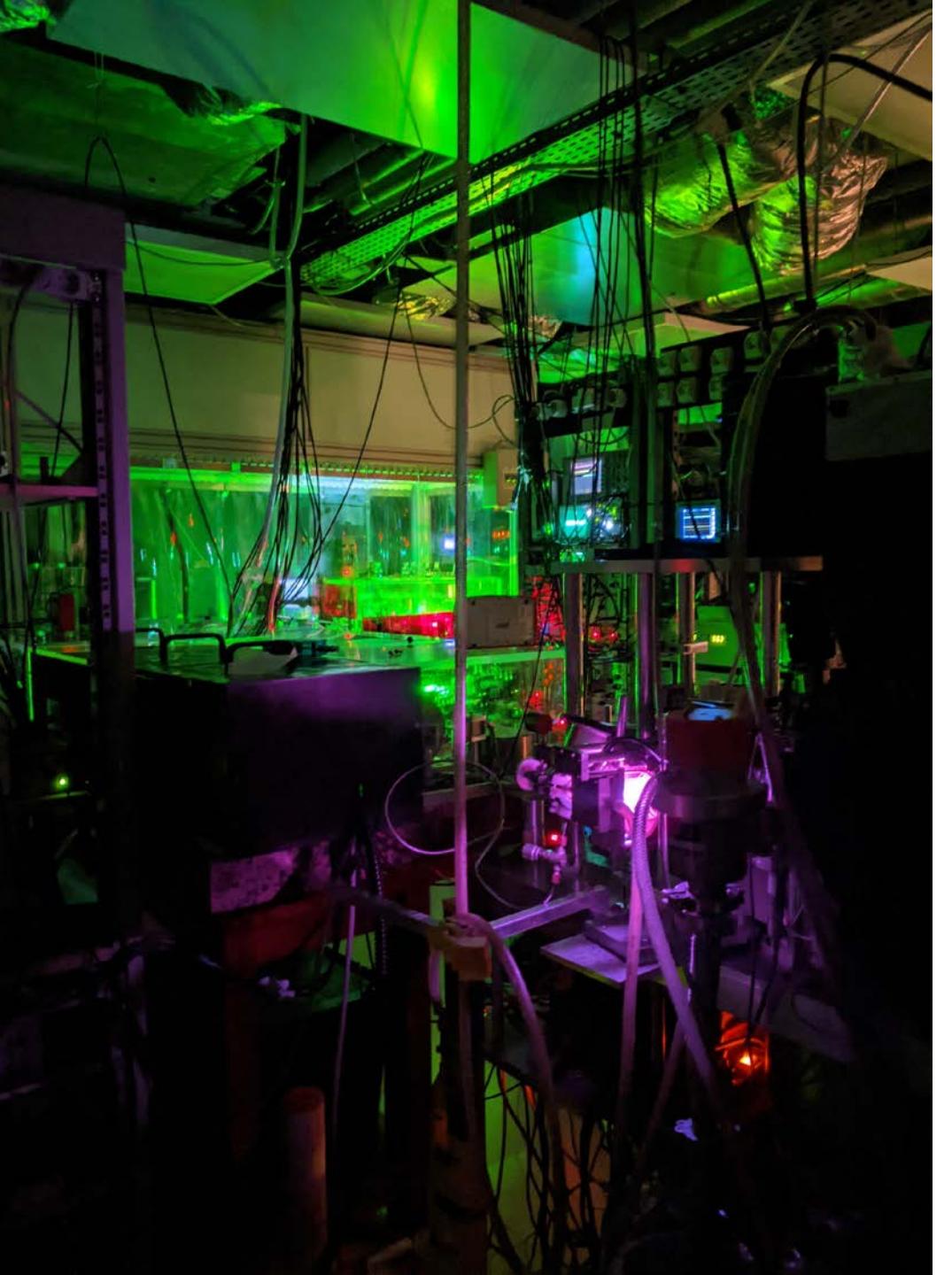
# 1S–3S Hydrogen CW spectroscopy



# Overview of the experiment



# Overview of the experiment



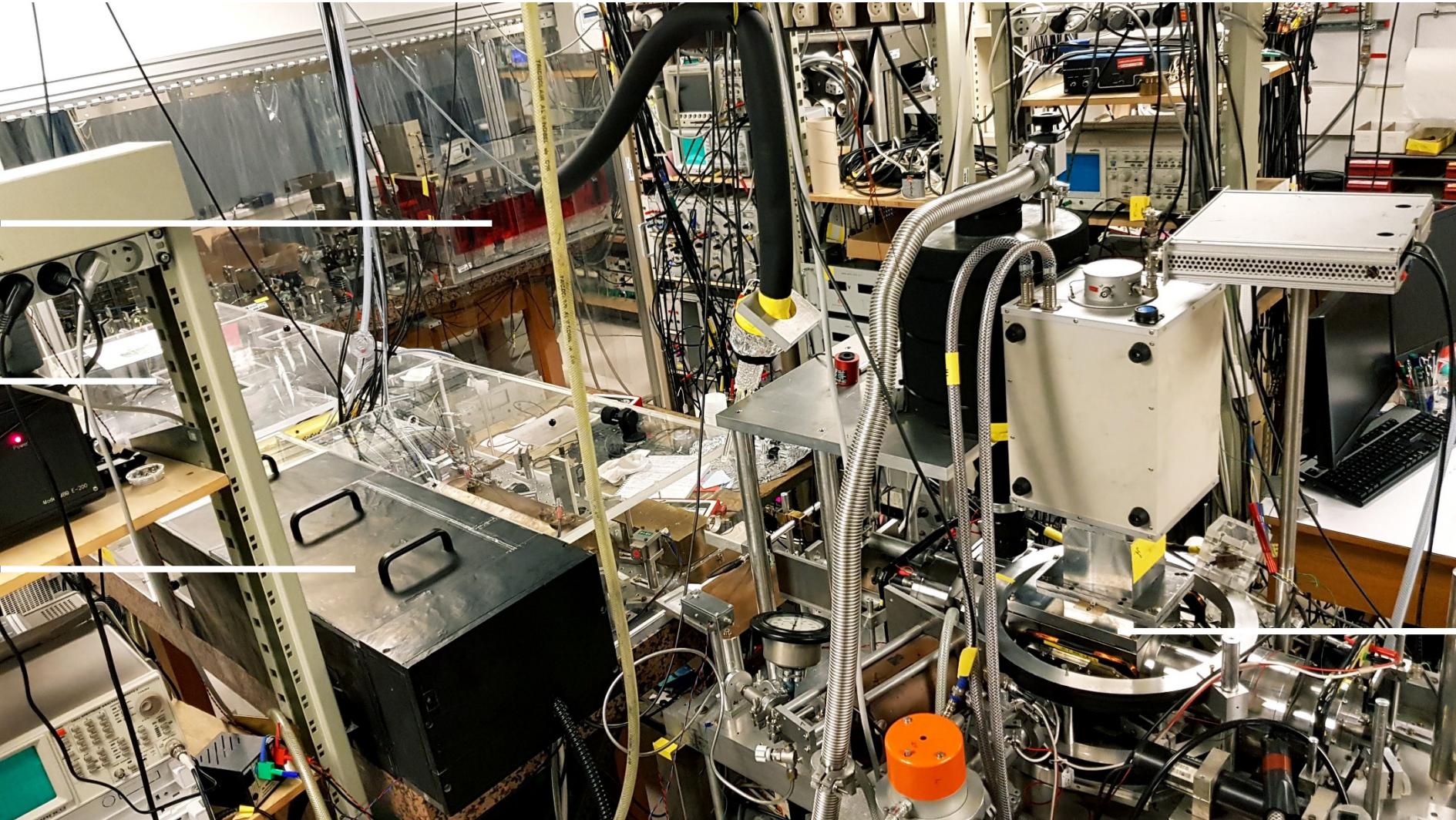
# With some light ON

TiSa  
895nm

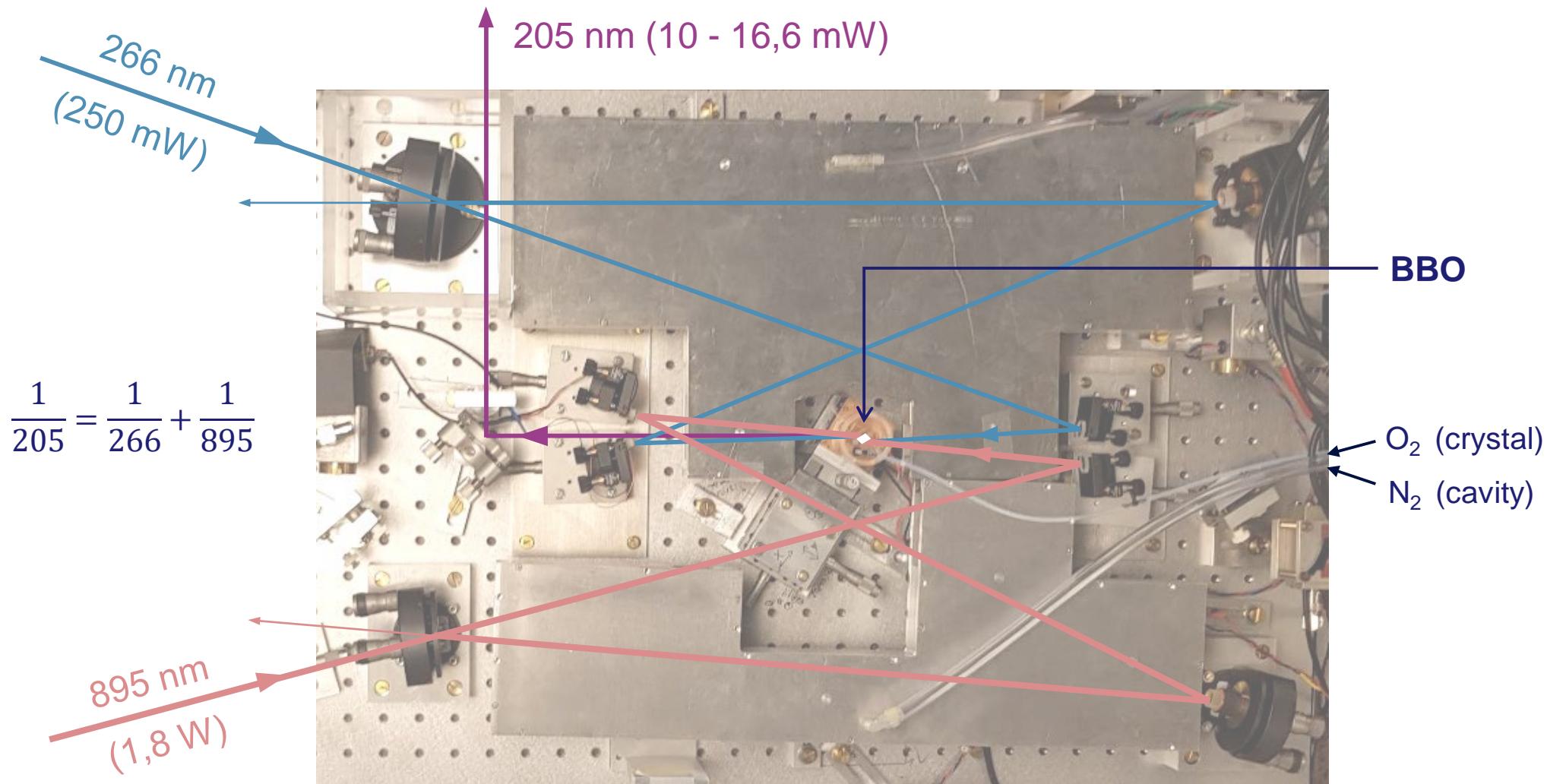
205nm  
generation

Verdi  
266nm

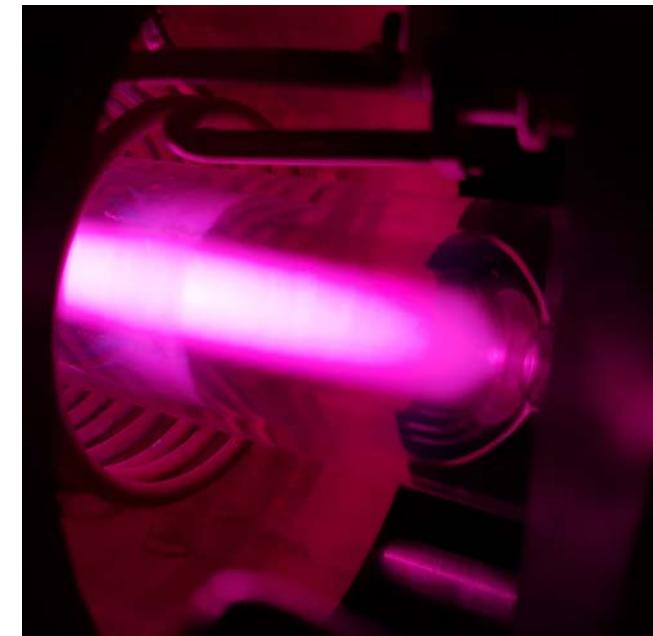
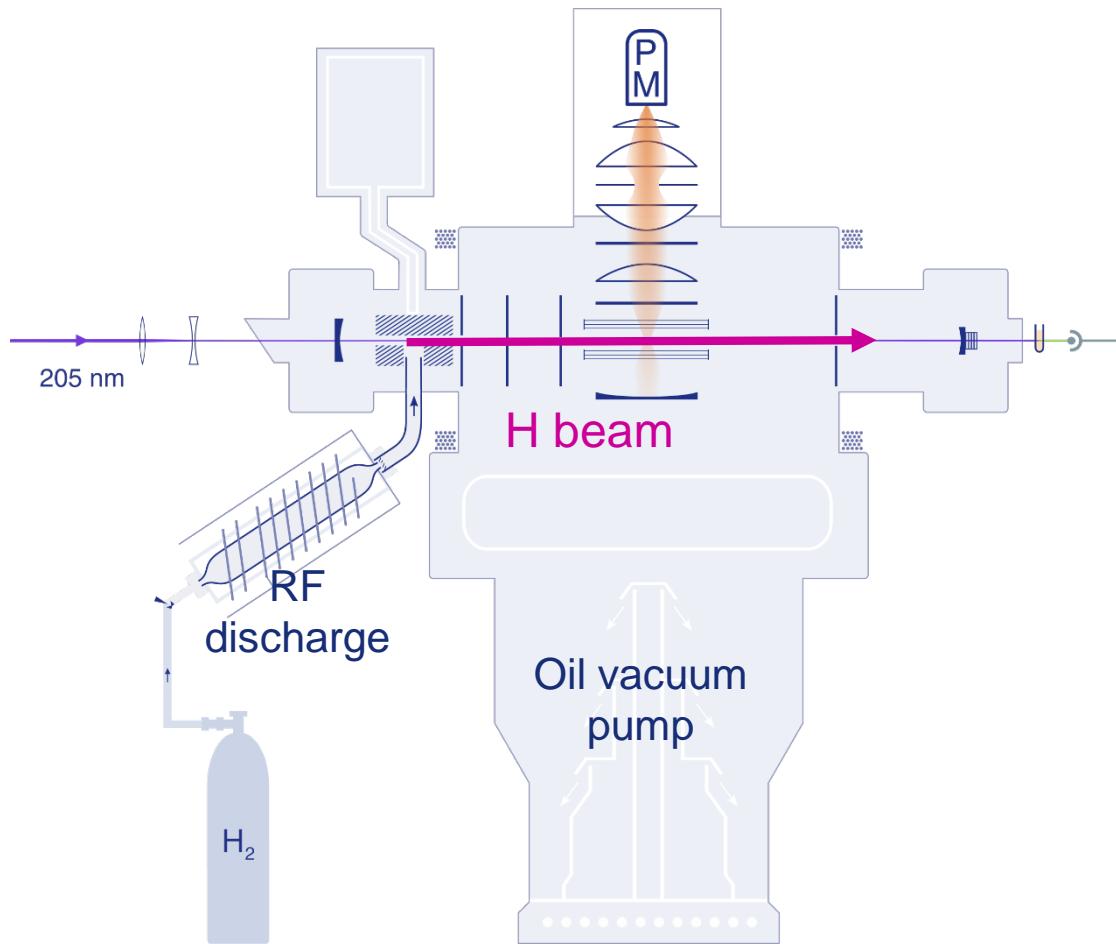
(old) H  
beam



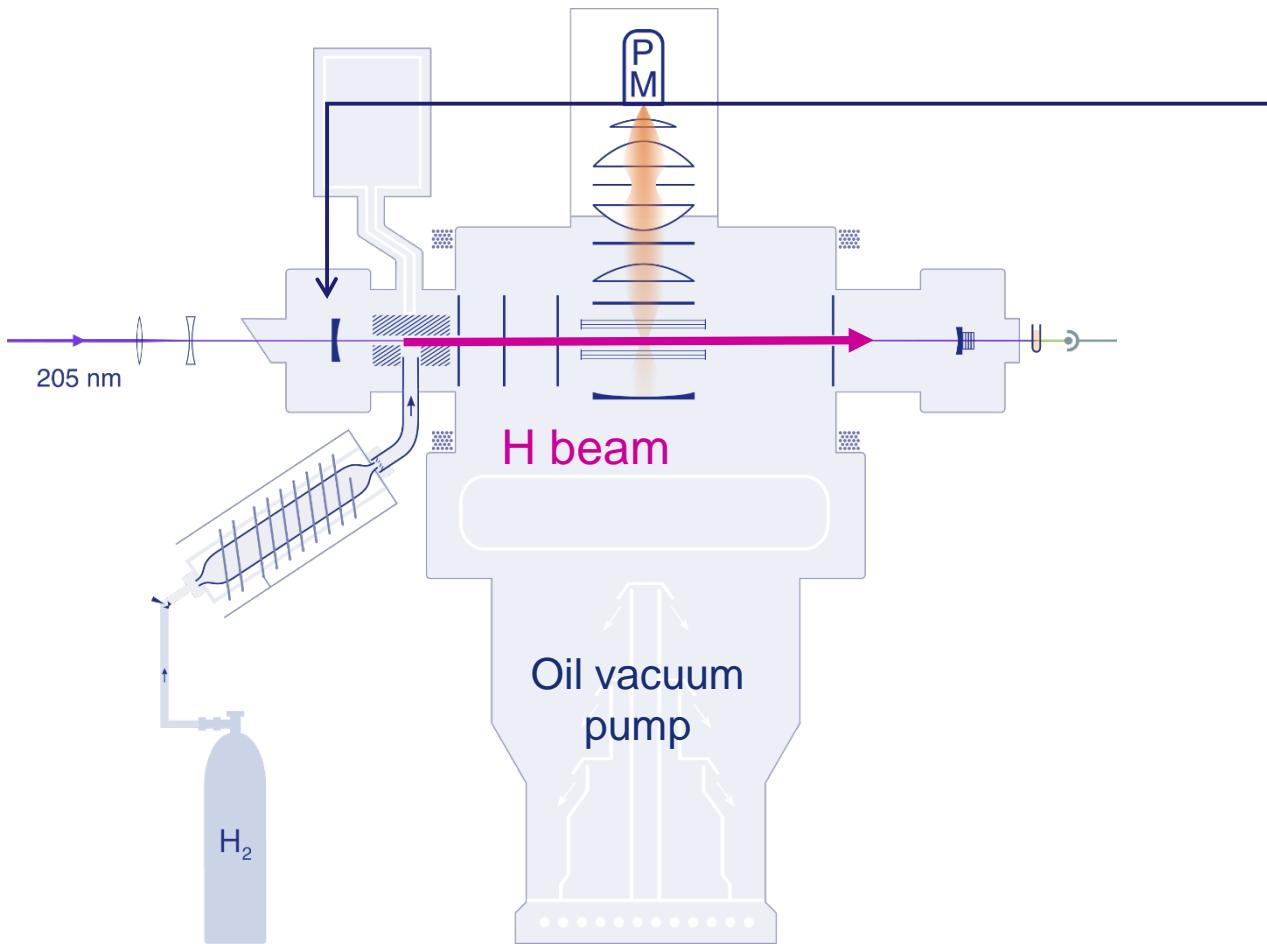
# CW 205nm laser generation



# Schematic of the «old » H beam experiment



# Schematic of the «old » H beam experiment



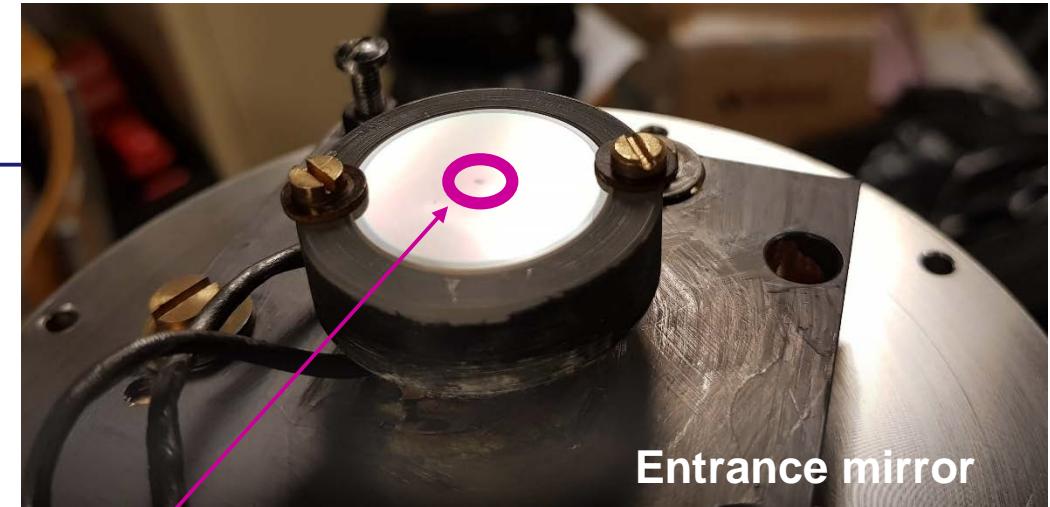
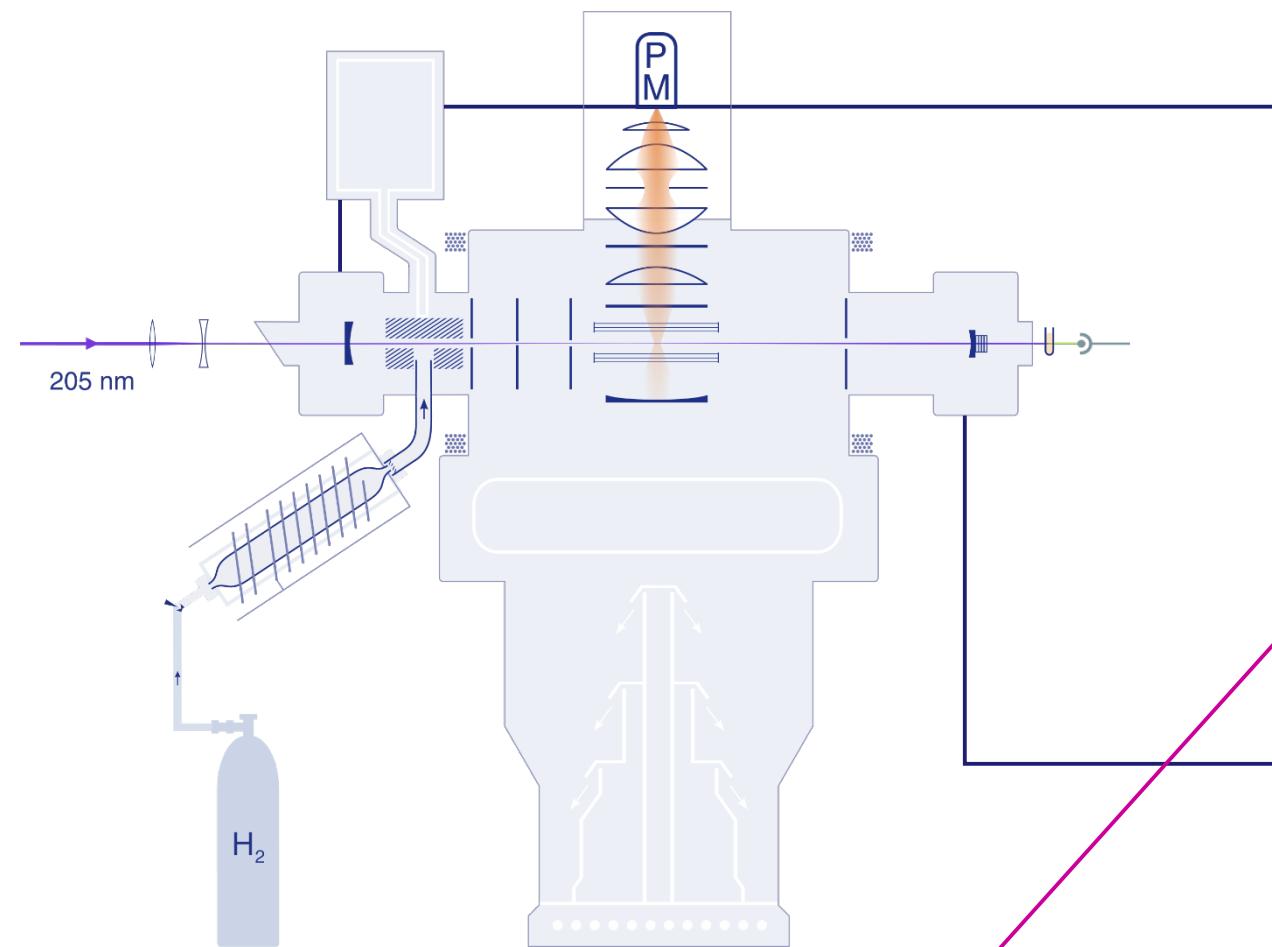
**Crucial point:**  
the enhancement 205nm cavity (Fabry Perot) is under vacuum

Theoretical power build-up factor

$$S = T_e / (1 - \sqrt{R_e R_s})^2 \approx 40$$

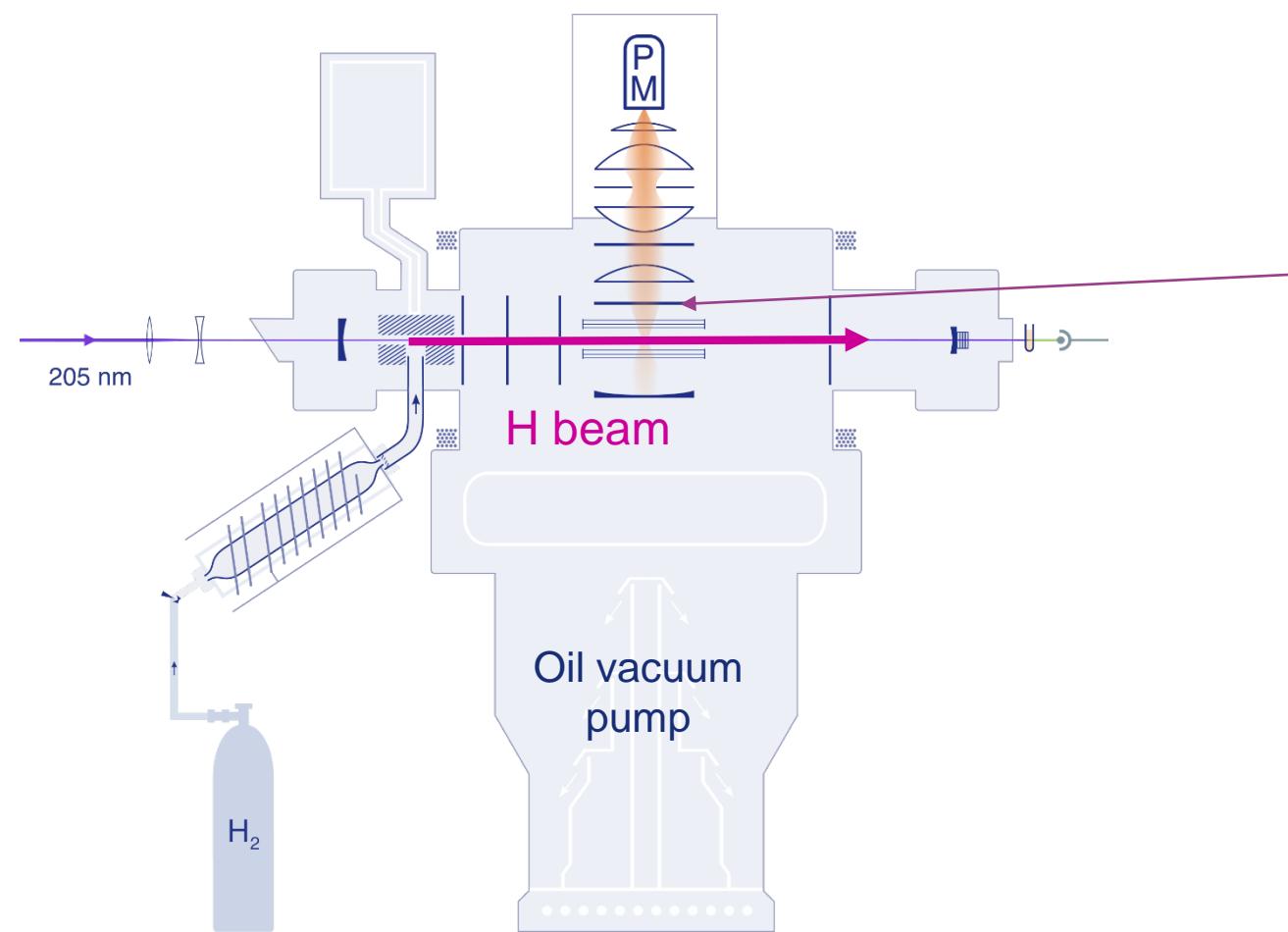
But using UV degrades the mirrors...

# Schematics of the «old » H beam experiment



Pollution of the mirrors  $\Rightarrow$  breaking vacuum every 2 days to clean

# Schematic of the «old » H beam experiment



New: Installation of a dichroic

⇒ Blocks the fluorescence due to 205 nm  
⇒ drastic reduction of the background signal !

# Spectroscopy 1S-3S on Deuterium

**Some of the results obtained during the *PhD thesis S. Thomas***  
**- dec. 2021**

*Based on a new campaign measurement on Deuterium atoms:*

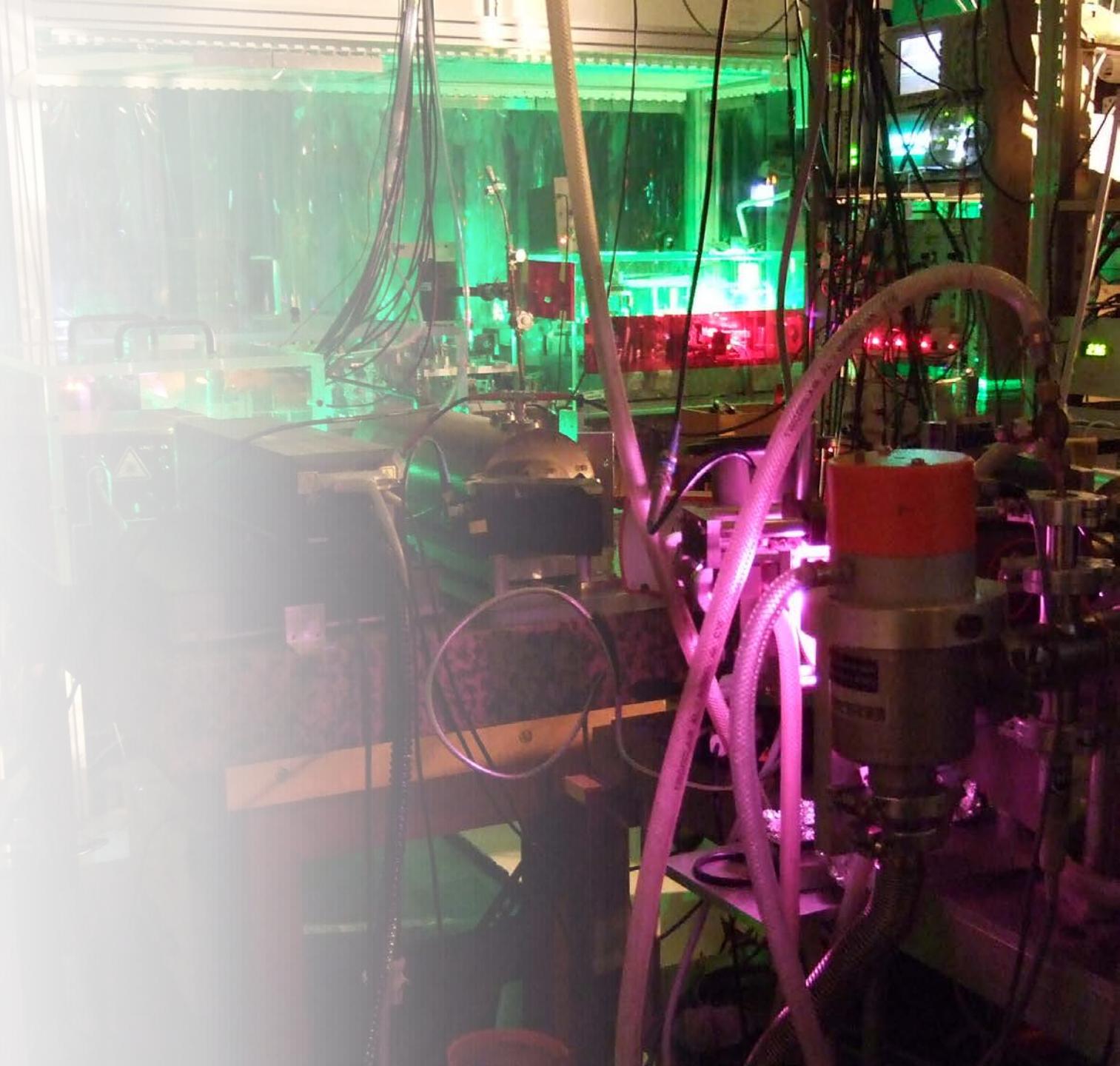
**From 20 October to 17 December 2020**

- 9434 spectra
- 3 values of pressure
- 4 values of magnetic field (x 2 direction): **a new B weak field B~20G**
- measurement of the laser intensity (AC. Stark shift estimation)

# Overview

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- 1S-3S Hydrogen/Deuterium spectroscopy
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  - **Dealing with systematics**
  - A new systematics effect ?
  - What next ?



# Dealing with systematics ...

1S - 3S spectroscopy on electronic hydrogen:

A few  $10^{-12}$  relative uncertainty targeted

**One of the main works:** identifying systematics effects and try to compensate or characterize them !

# Pressure shift

Origin: Collisions with rest gas in the chamber

=> broadening  $\sim 2$  kHz << negligible (natural linewidth 1 MHz)

=> non negligible shift of the center of the line

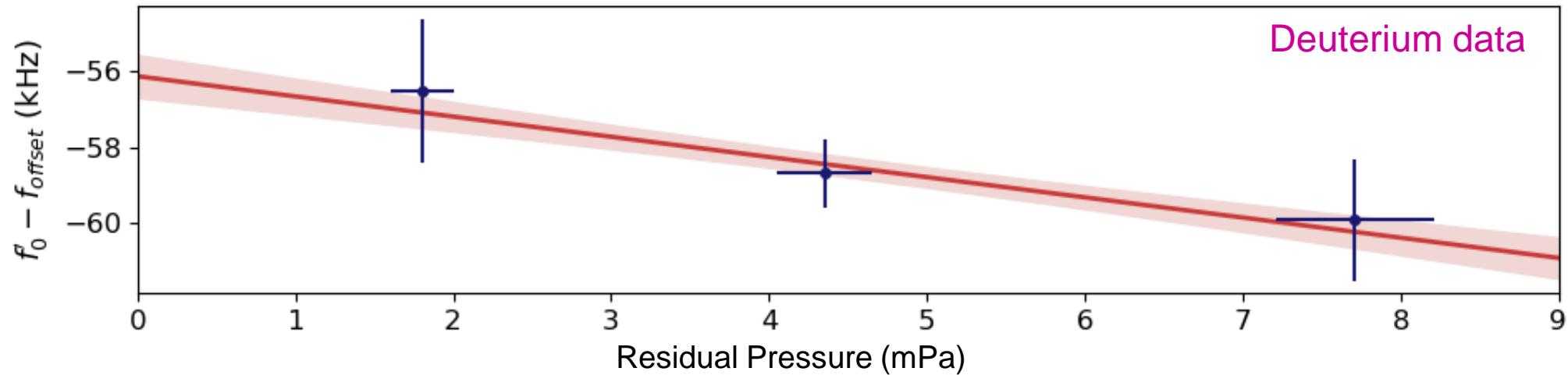


Figure taken from Ph.D thesis S. Thomas (2021)

$$f'_0 - f_{\text{offset}} = -0,527(344) \times P_f - 56,1(1,97) \text{ kHz}$$

For our Deuterium data at 4.35 (10) mPa :  $\Delta f_{\text{col}} = 2,32(1,51)$  kHz.

# Light shift (AC Stark shift)

- Proportional to the laser intensity inside the interaction chamber

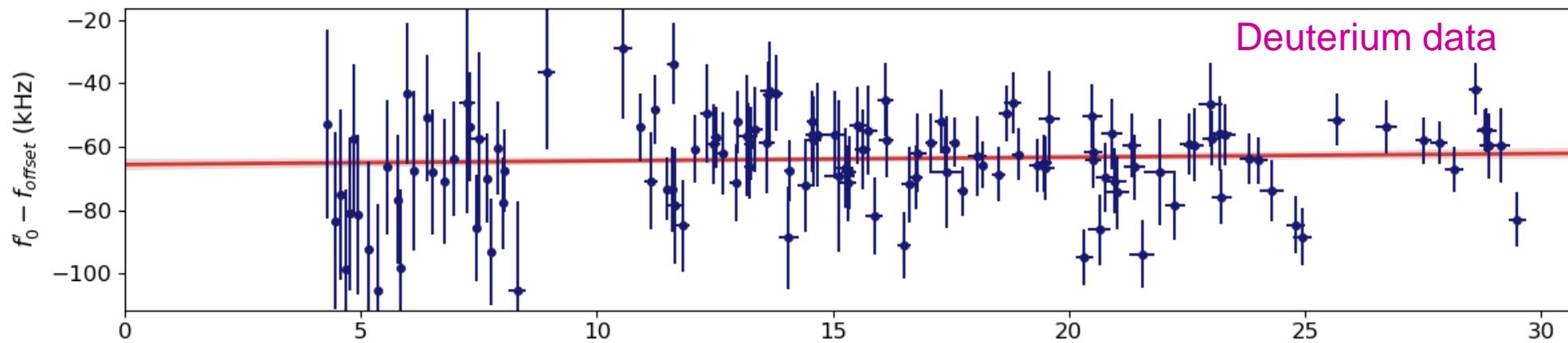


Figure taken from Ph.D thesis S. Thomas (2021)

$$f'_0 - f_{\text{offset}} = 0,115(176) \times P_{205} - 65,57(3,51) \text{ kHz} \text{ (pour } P_{205} \text{ en } \mu\text{W)}$$

⇒ Typically ~ 1-2 kHz shift

Transmitted 205nm light  
(through the exit mirror of the Fabry  
Perot cavity & pickup window)

# 2<sup>nd</sup> Order Doppler effect

*Our main source of uncertainty*

The diagram illustrates the 2<sup>nd</sup> Order Doppler effect. A black circle represents a particle moving with velocity  $\vec{v}$  in a magnetic field  $\vec{B}$ . Two purple wavy lines represent photons emitted by the particle. The left photon is moving away from the particle at an angle, and the right photon is moving towards it. The emitted frequencies are given by the equations:

$$h\nu \left(1 - \frac{v}{c} + \frac{v^2}{2c^2}\right)$$
$$h\nu \left(1 + \frac{v}{c} + \frac{v^2}{2c^2}\right)$$

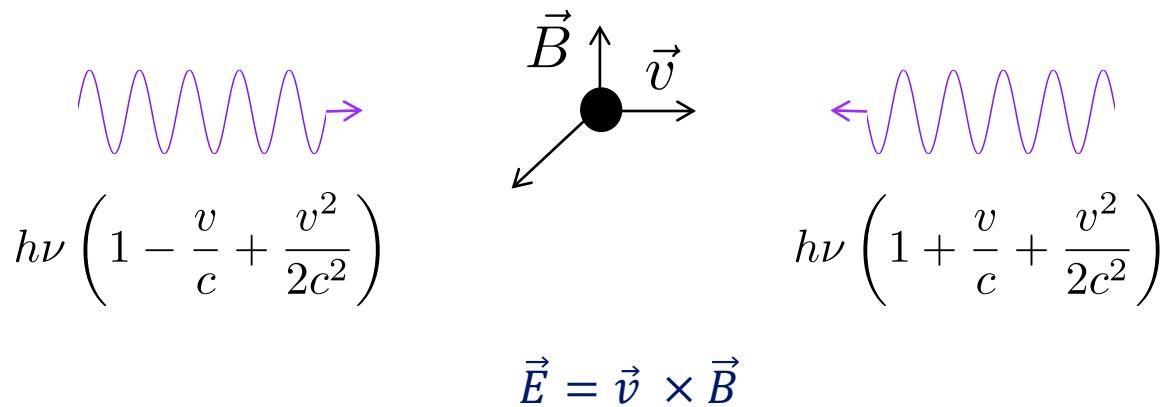
$$\delta_{Doppler}^{(2)} = -\nu_{at} \frac{v^2}{2c^2}$$

Need to determine the **velocity distribution** of the H beam ...

And no 1-photon transition easily achievable ( 121nm laser) for  
1<sup>st</sup> order Doppler broadening measurement

# 2<sup>nd</sup> Order Doppler effect

*Compensating it ?*


$$h\nu \left( 1 - \frac{v}{c} + \frac{v^2}{2c^2} \right)$$
$$h\nu \left( 1 + \frac{v}{c} + \frac{v^2}{2c^2} \right)$$
$$\vec{E} = \vec{v} \times \vec{B}$$

**Idea principle:** inducing a Motional Stark effect

$$\delta_{Doppler}^{(2)} = -\nu_{at} \frac{v^2}{2c^2}$$

$$\delta_{Stark} = \frac{E^2}{\Delta\nu_{SP}} = \frac{v^2 B^2}{\Delta\nu_{SP}}$$

To compensate 2<sup>nd</sup> order Doppler

# 2<sup>nd</sup> Order Doppler effect

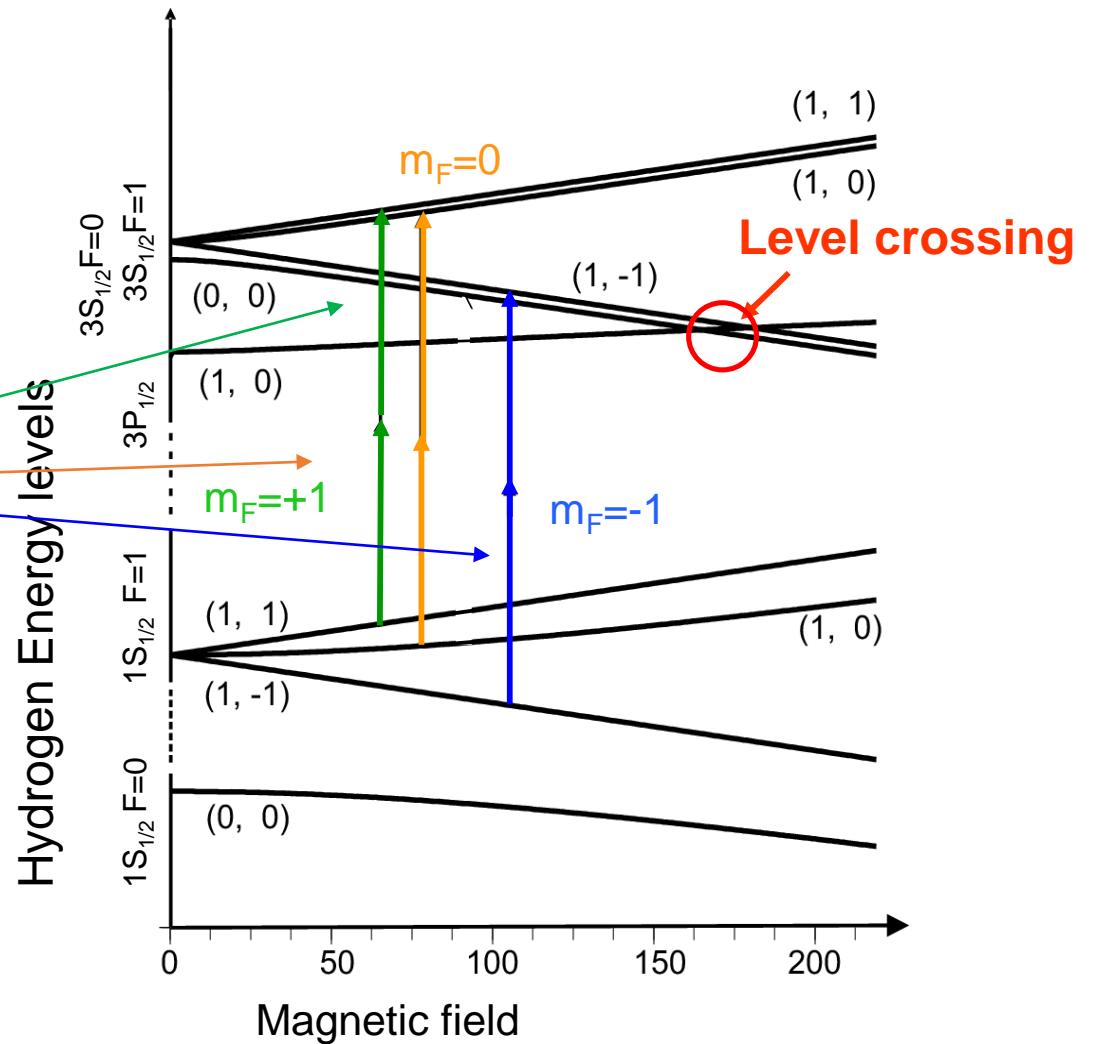
Avoiding it ?

Hydrogen energy levels

But Zeeman effect has to be taken into account !

2- $\gamma$  transition Selection rules  
 $\Delta m_F = 0$

$\Rightarrow$  3 transitions driven  
 $m_F=0$      $m_F=+1$      $m_F=-1$



# 2<sup>nd</sup> Order Doppler effect

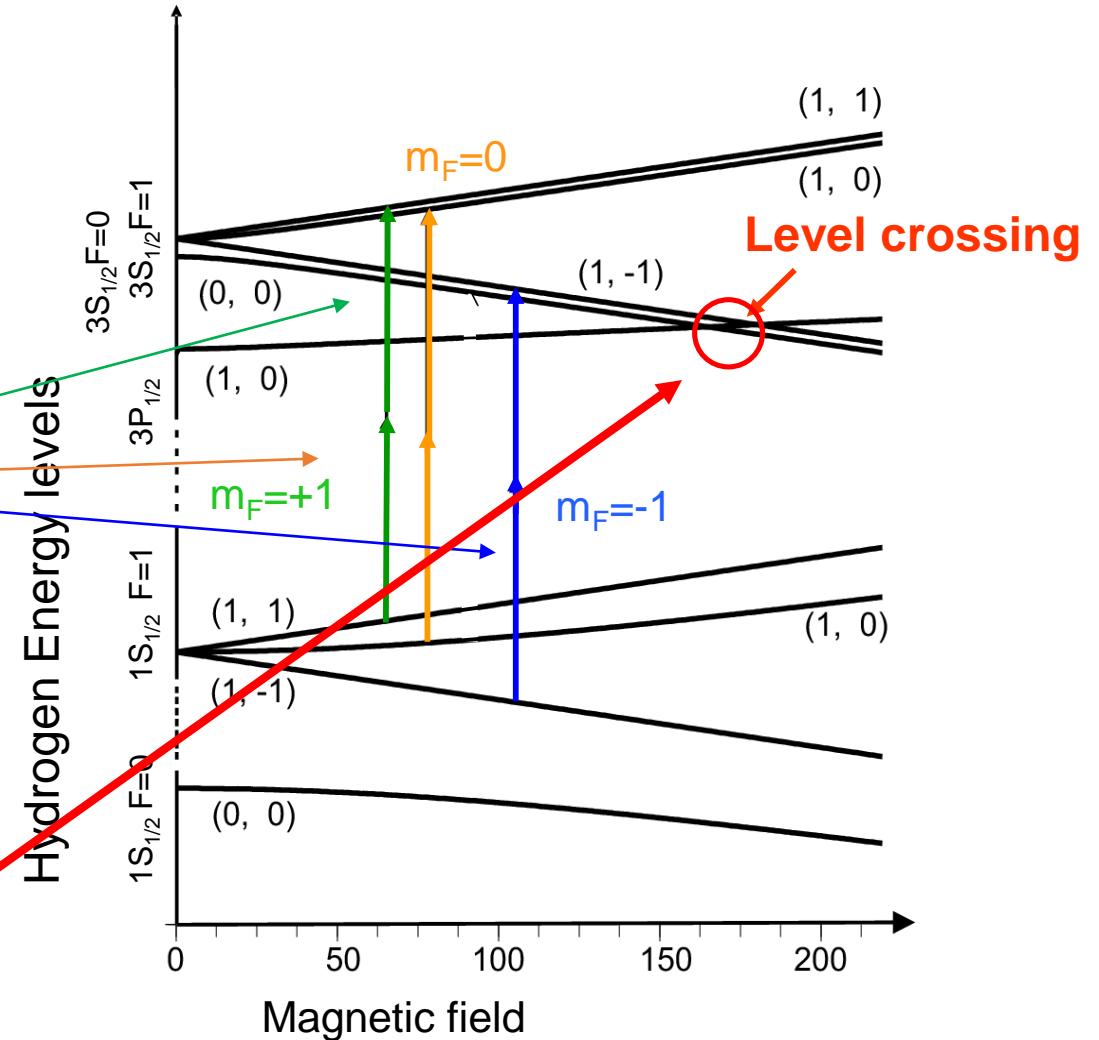
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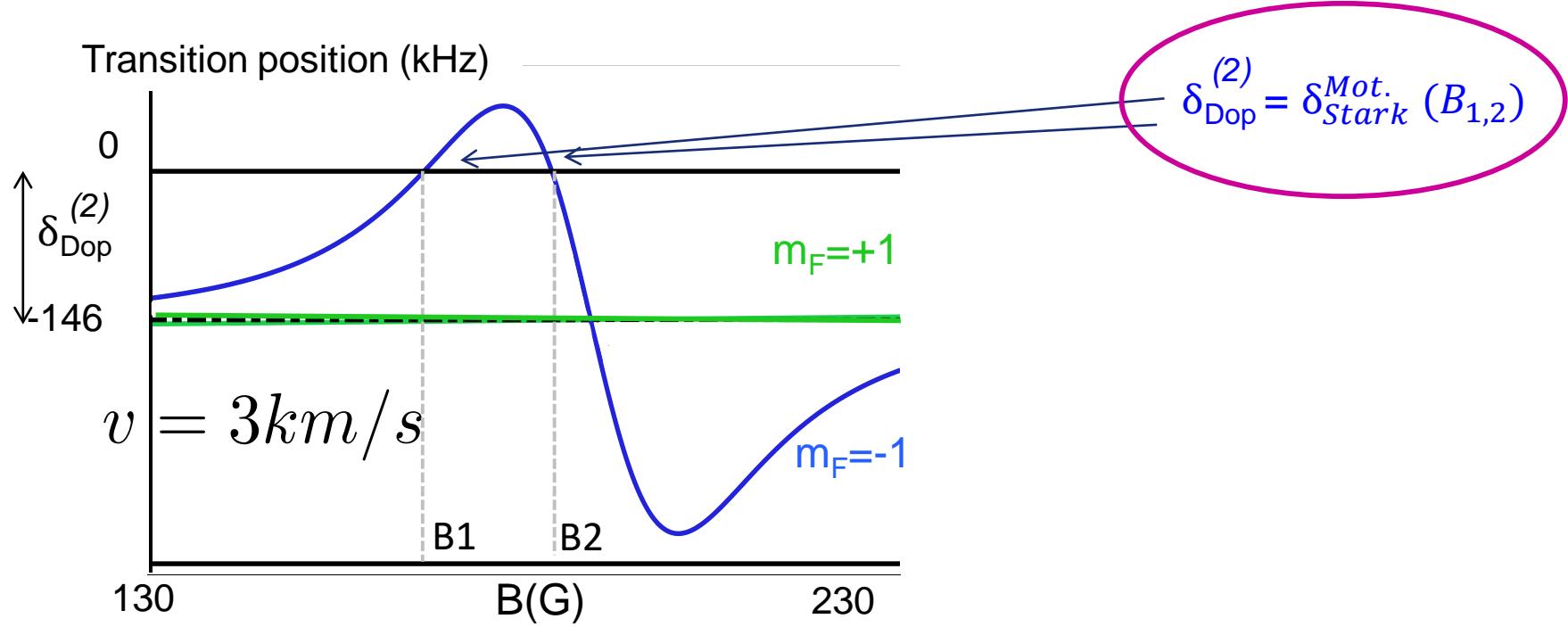
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Motional Stark:  
mixing S – P states = anti-crossing

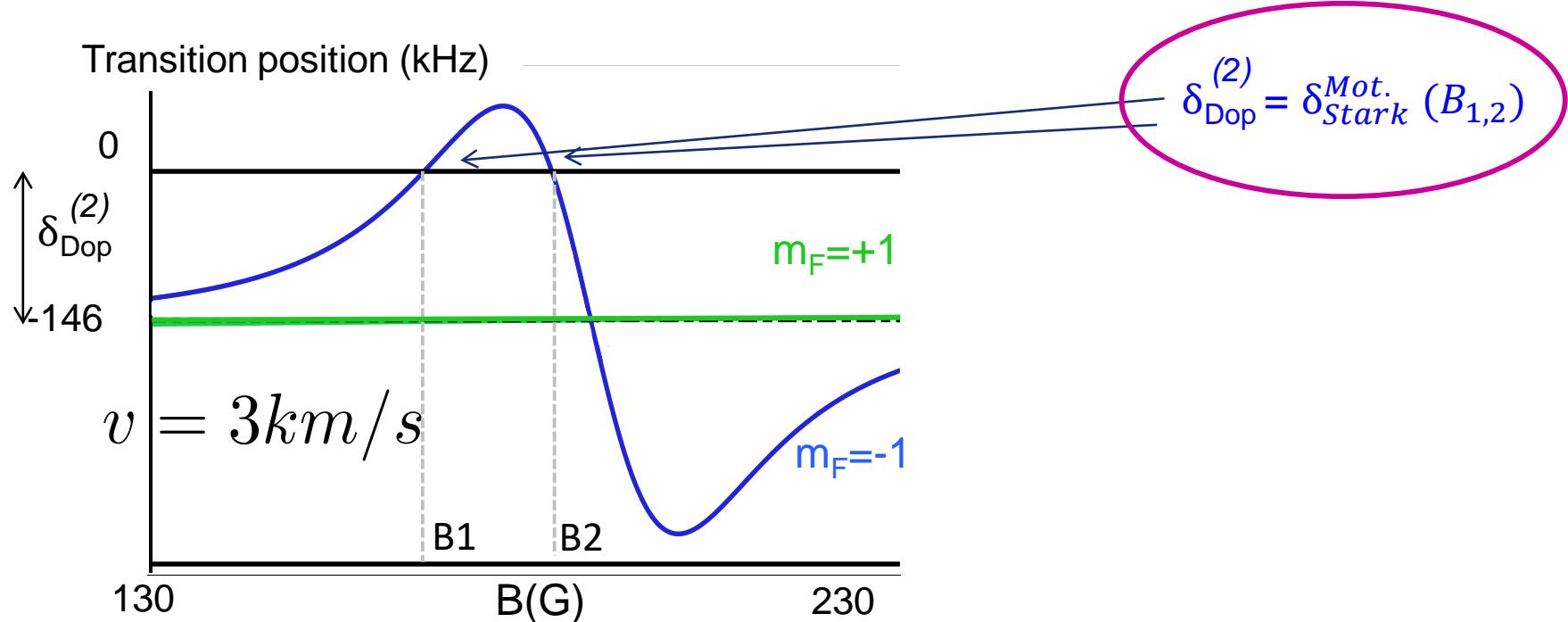


# Avoiding 2<sup>nd</sup> order Doppler effect



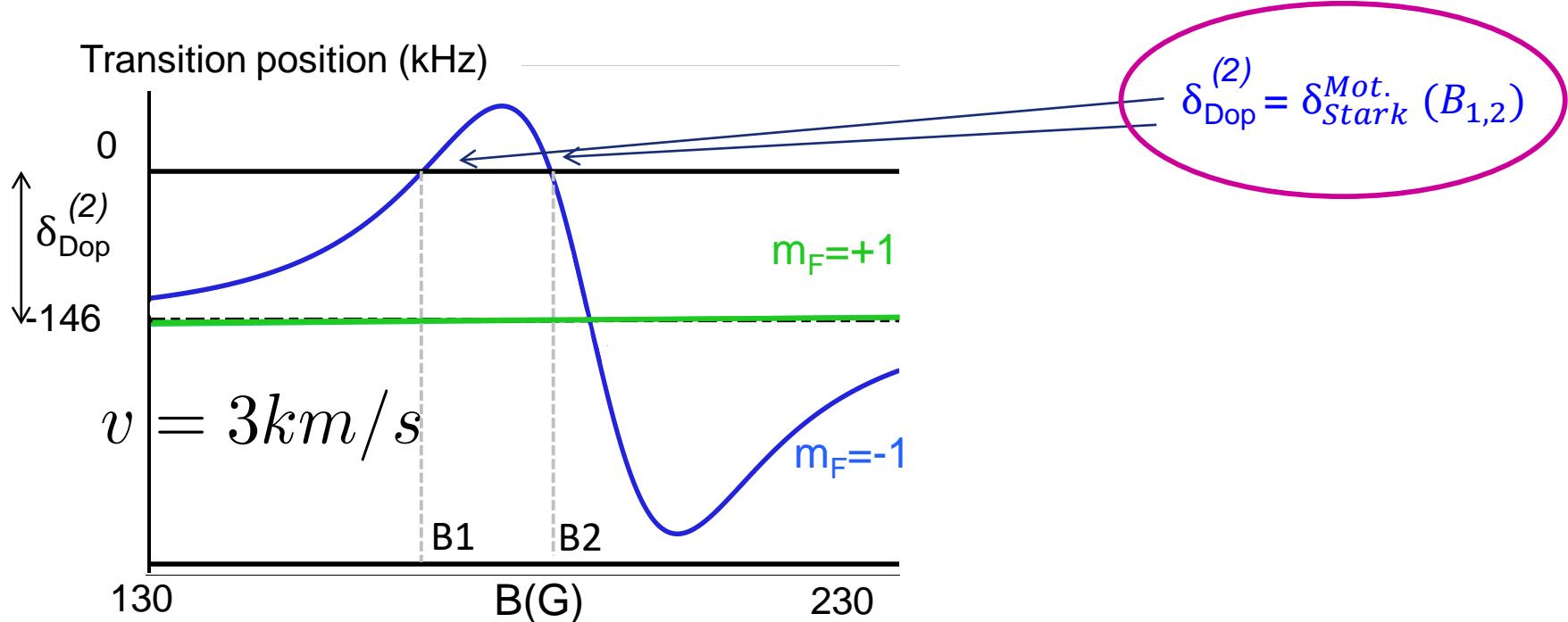
- Total compensation of 2<sup>nd</sup> Ord. Doppler for  $B = B_1$  and  $B_2$  for  $mF=-1$  transition

# Avoiding 2<sup>nd</sup> order Doppler effect



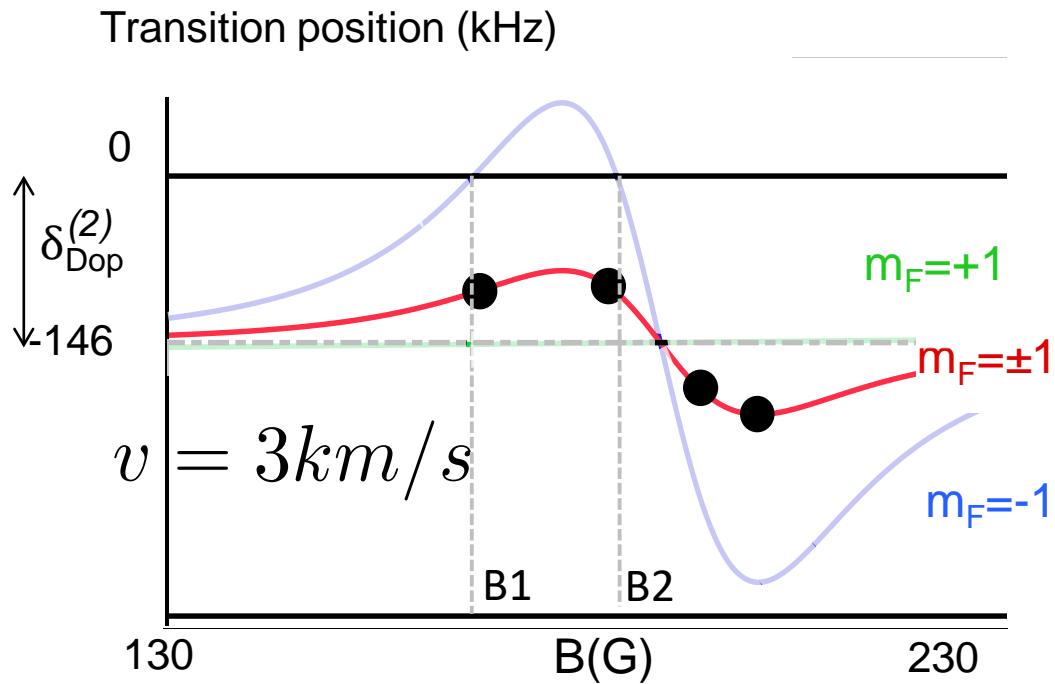
- Total compensation of 2<sup>nd</sup> Ord. Doppler for  $B = B1$  and  $B2$  for  $mF=-1$  transition
- For  $v=3 \text{ km/s}$ : the transitions  $m_F=-1$  and  $m_F=1$  are split by  $\sim 146 \text{ kHz}$  for  $B = B1$  and  $B2$ .

# Avoiding 2<sup>nd</sup> order Doppler effect



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- The 3S natural bandwidth  $\sim 1 \text{ MHz}$
- The two lines cannot be resolved  $\Rightarrow$  **Both lines are excited**

# Avoiding 2<sup>nd</sup> order Doppler effect



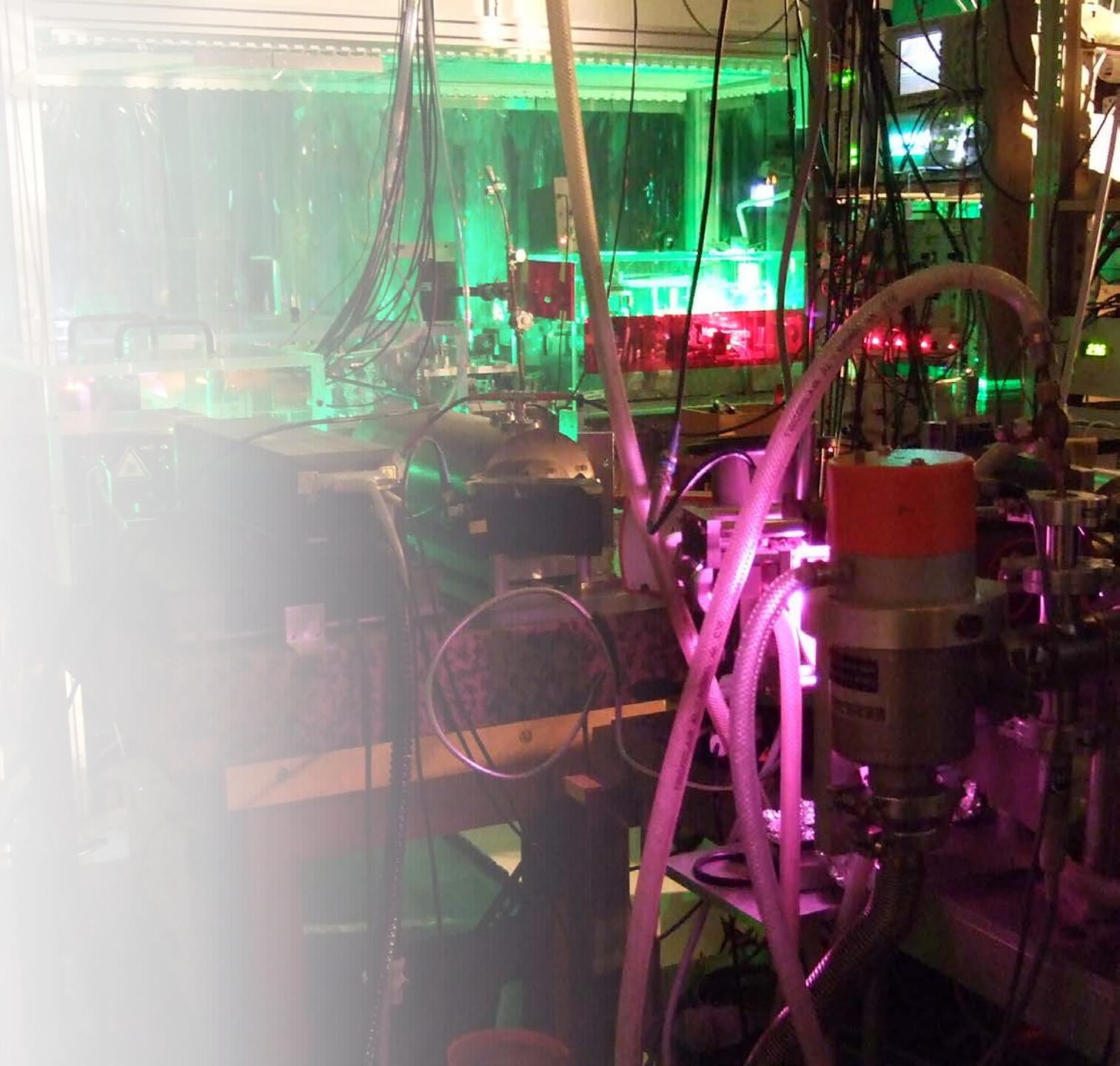
The two lines cannot be resolved  $\Rightarrow$  **partial compensation only** due to Motional Stark

$\Rightarrow$  **Determination of the velocity distribution** by fitting the dispersion curve with several data points for different  $B$  (« red » profile)

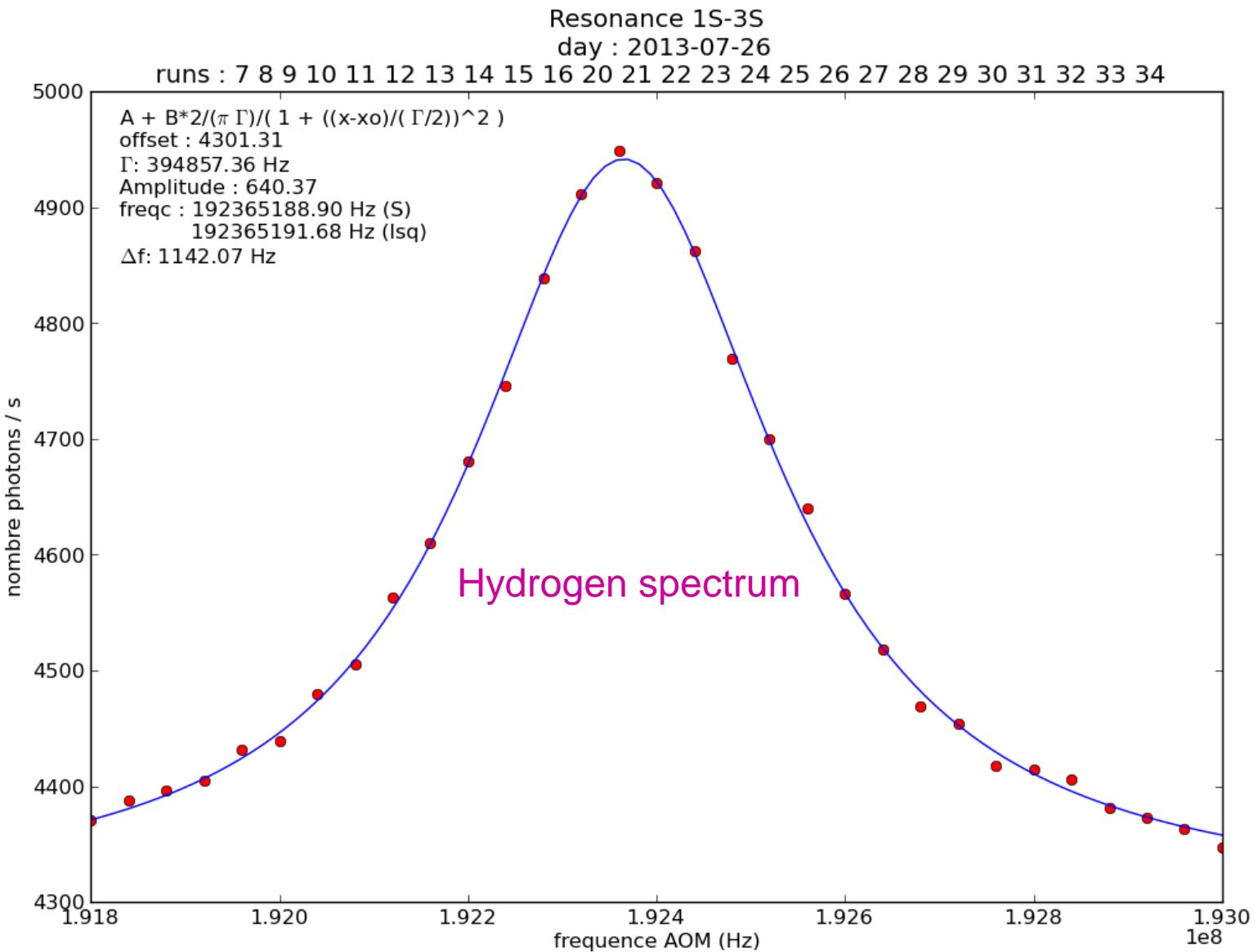
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# Typical signal of the 1S-3S transition – in the past

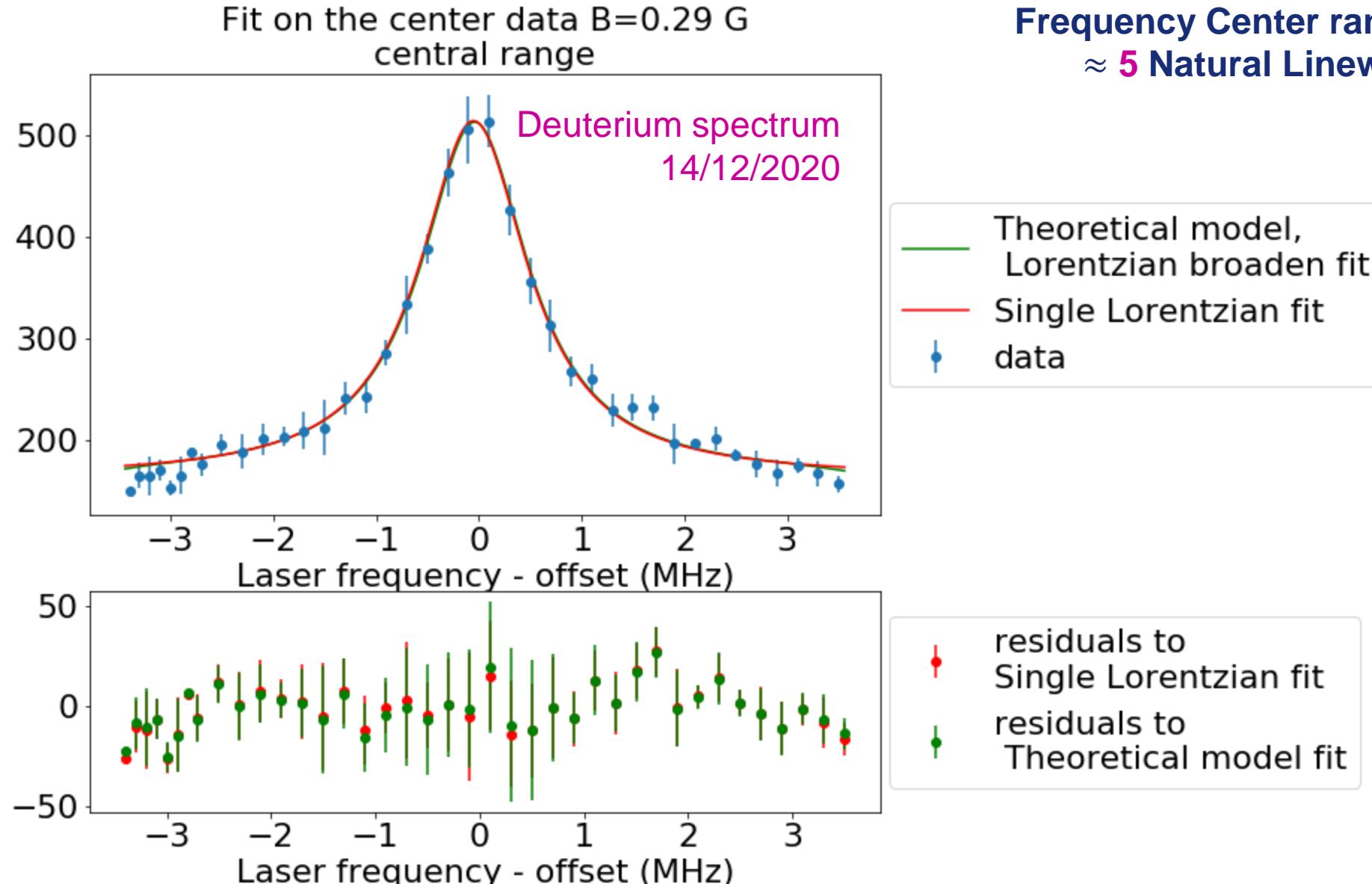


On day average

# Improvements of the experiment during the last years

- Work to reduce the Background signal:
  - ⇒ installation of a dichroic mirror to block the 205nm fluorescence detection system (collection optics)

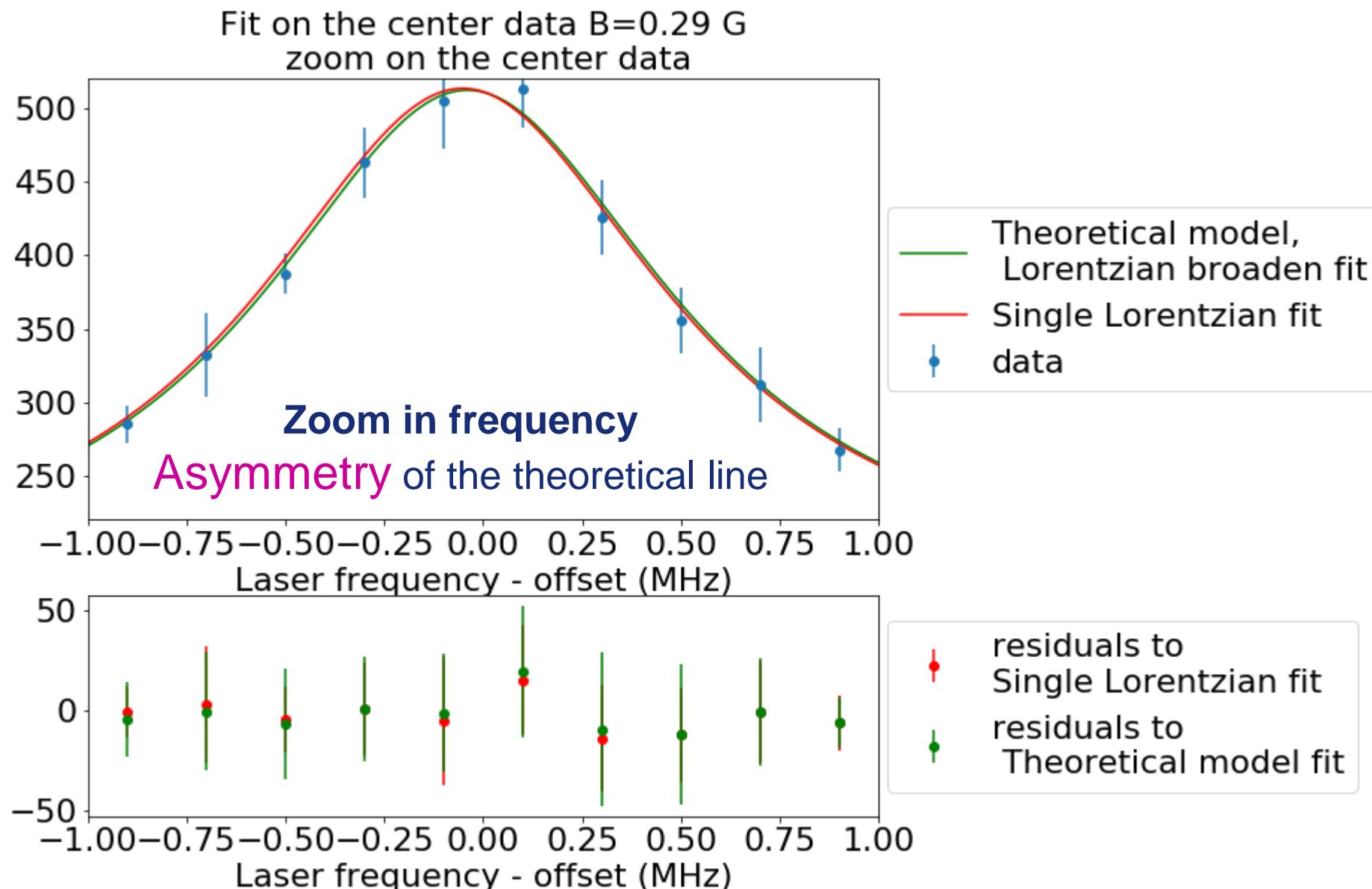
# Good background reduction



Frequency Center range scan  
≈ 5 Natural Linewidth

# Good background reduction

Deuterium spectrum  
14/12/2020, run 38  
 $B=0.29$  G

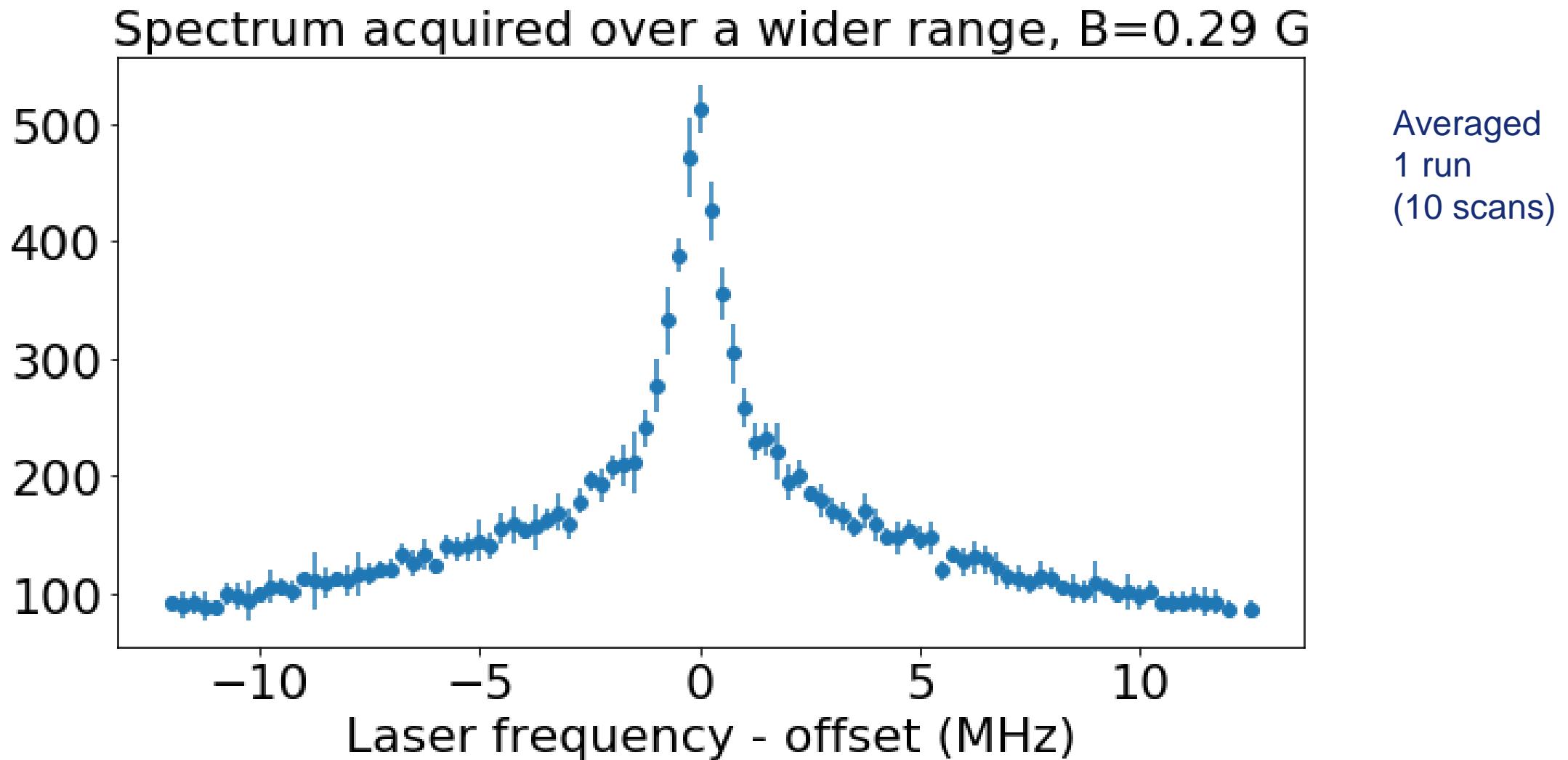


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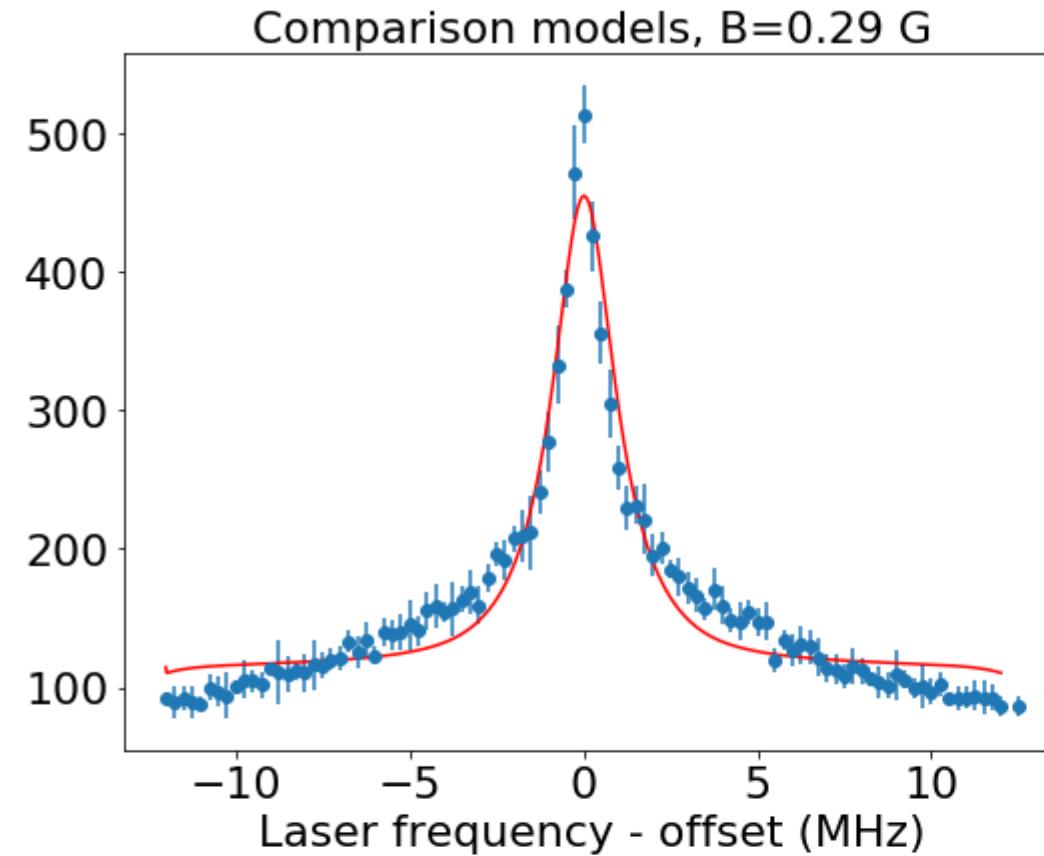
- Work to increase the frequency stability and tunability of the laser
  - **Before:** usual scan  $\pm 2.5 - 3$  MHz scan ( $\approx 5$  Natural Linewidth) –  $\sim 6\text{ min}$  for 1 run (= 10 scans)
  - possible up to  $\pm 5$  MHz ( $\approx 10$  Natural Linewidth) –  $\sim 11\text{ min}$
  - **New system:**  $\pm 10 - 30$  MHz scan possible ( $\approx 20 - 60$  Natural Linewidth)  $\sim 20\text{ min}$

# With a wider laser frequency scan:

Deuterium spectrum  
14/12/2020, run 38  
 $B=0.29$  G

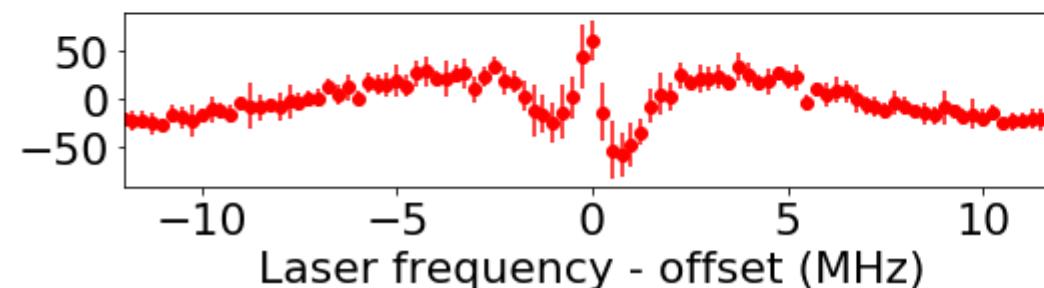


# Which fit model ?



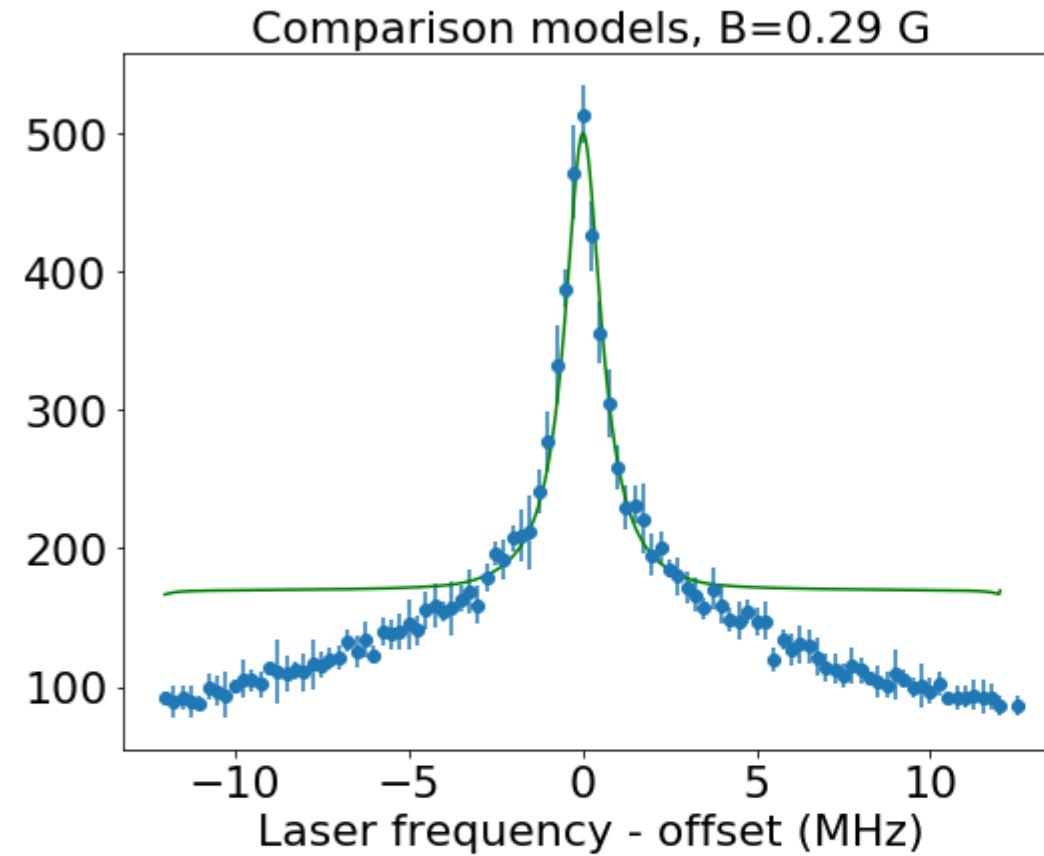
$$F(v_L) = F_{theo}(v_L, v_0, \sigma_0)$$

Fitting range : all data



Residuals to Theo fit only  
over whole range

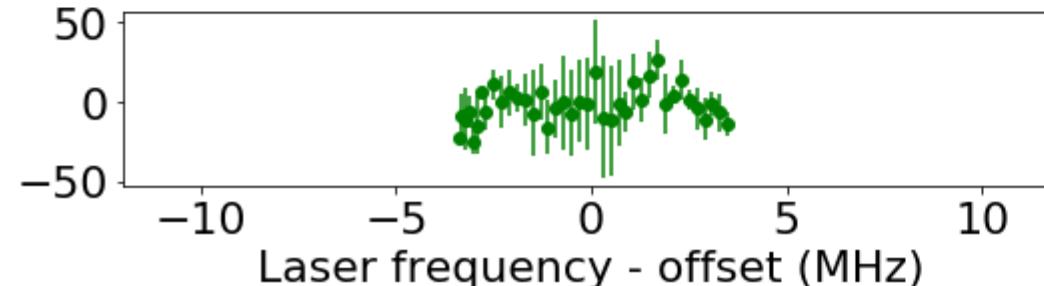
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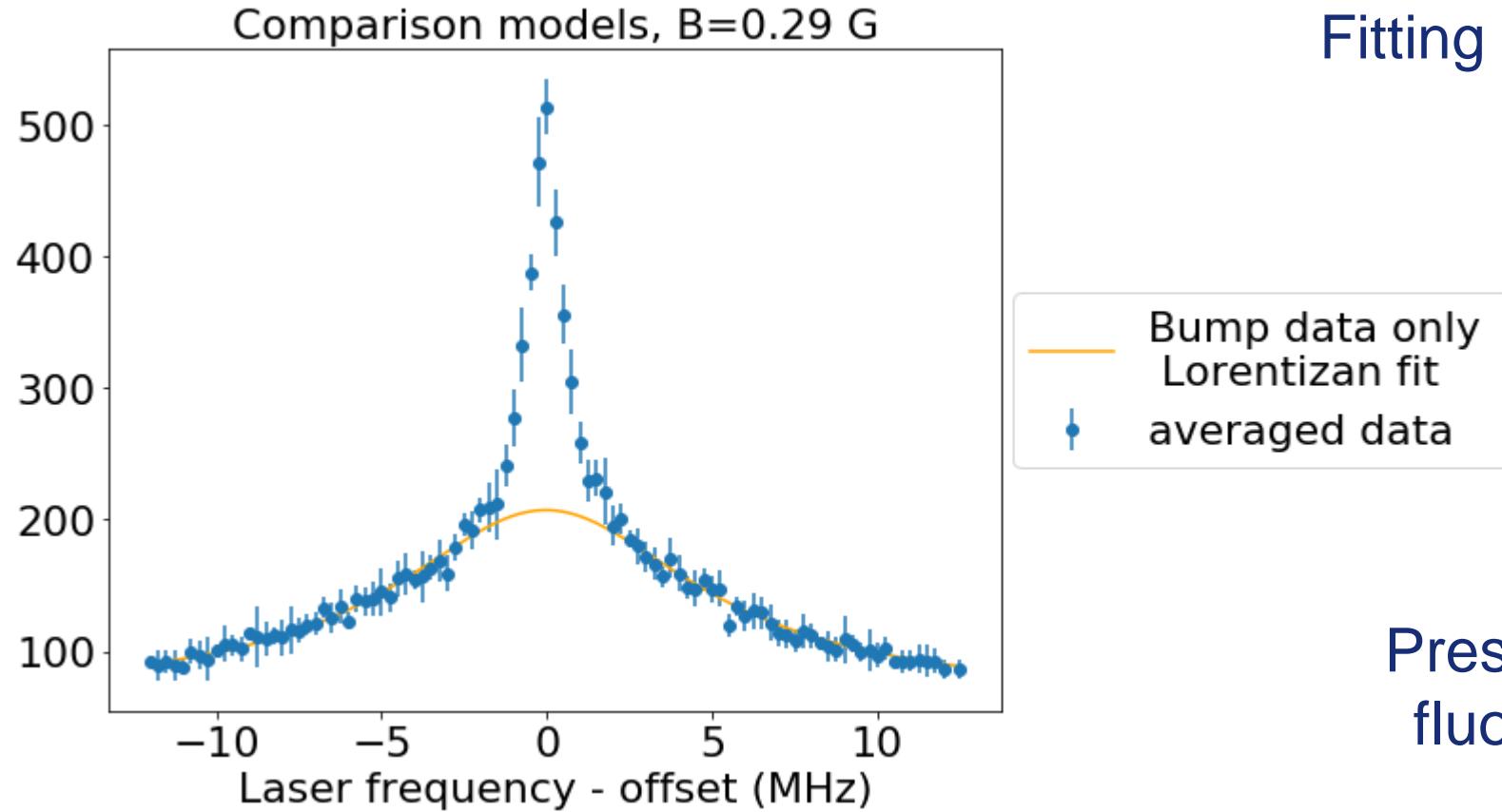
Fitting range : central data only

Theo curve fit only, fit over central range  
averaged data



Residuals to Theo fit only  
over central range

# Which fit model ?



$$F(\nu_L) = \text{Lor}(\nu_L, \nu_{Bump}, \Gamma_{Bump})$$

Fitting range : edge data only

Presence of a “Pedestal  
fluorescence signal” =  
“Bump” signal

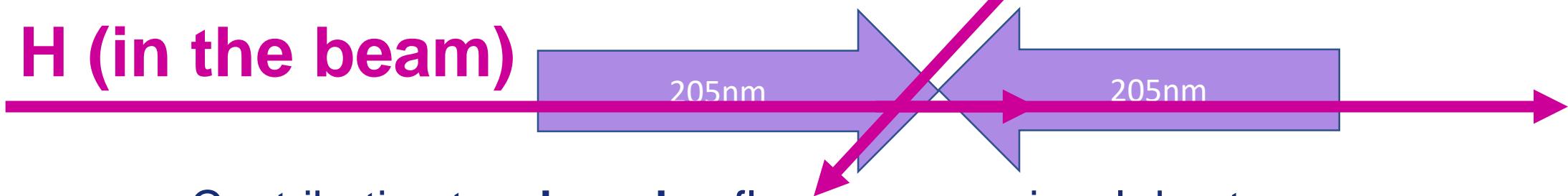
# Which fit model ?

Origin of this pedestal ?

Presence of residual H gas in the chamber.

H (residual gas in the chamber)

H (in the beam)

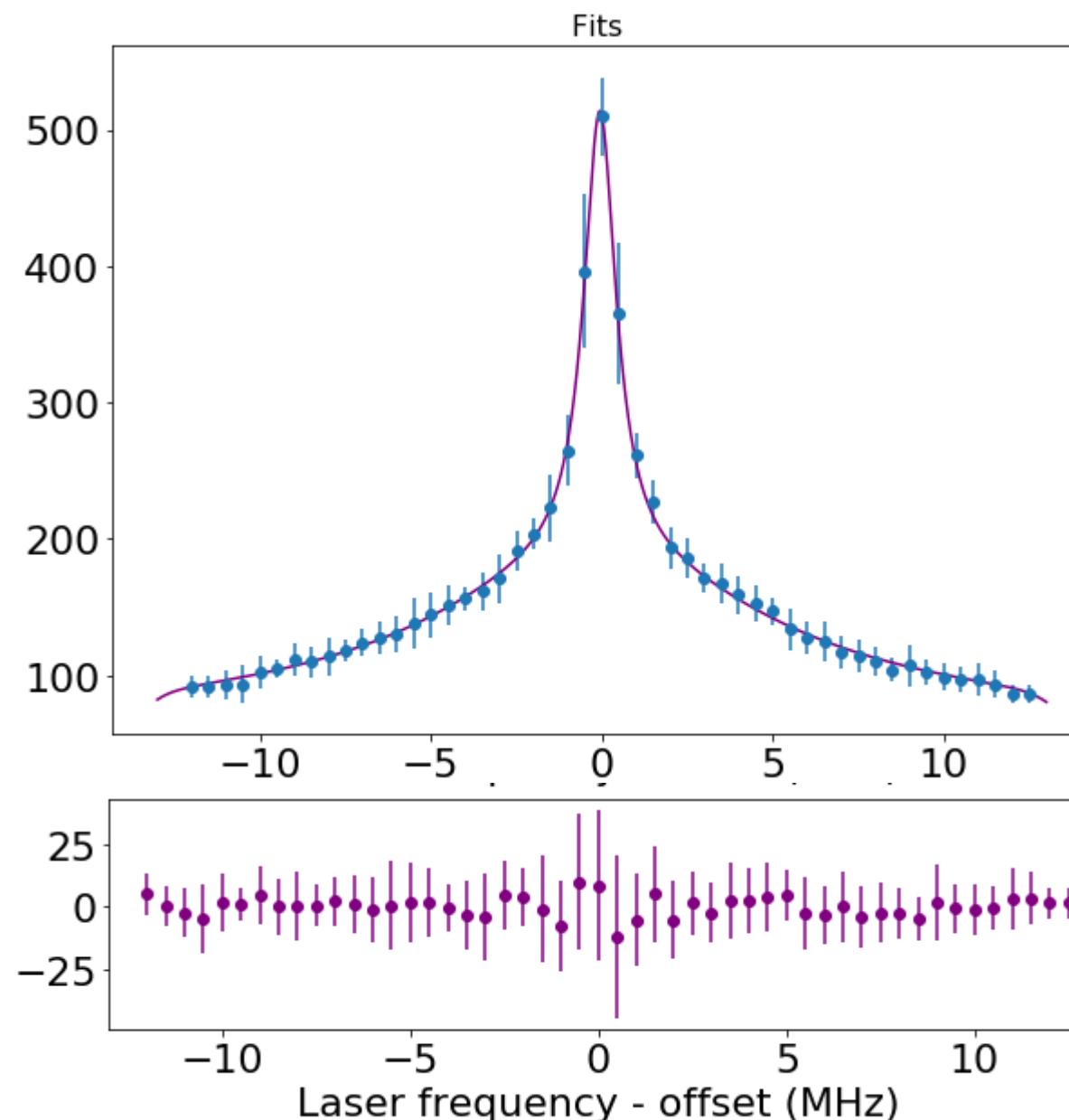


=> Contribution to a **broaden** fluorescence signal due to **short interaction time**

New model to fit:

$$F(\nu_L) = F_{theo}(\nu_L, \nu_0, \sigma_0) + F_{theo}(\nu_L, \nu_B, \sigma_B) + B$$

# Which fit model ?

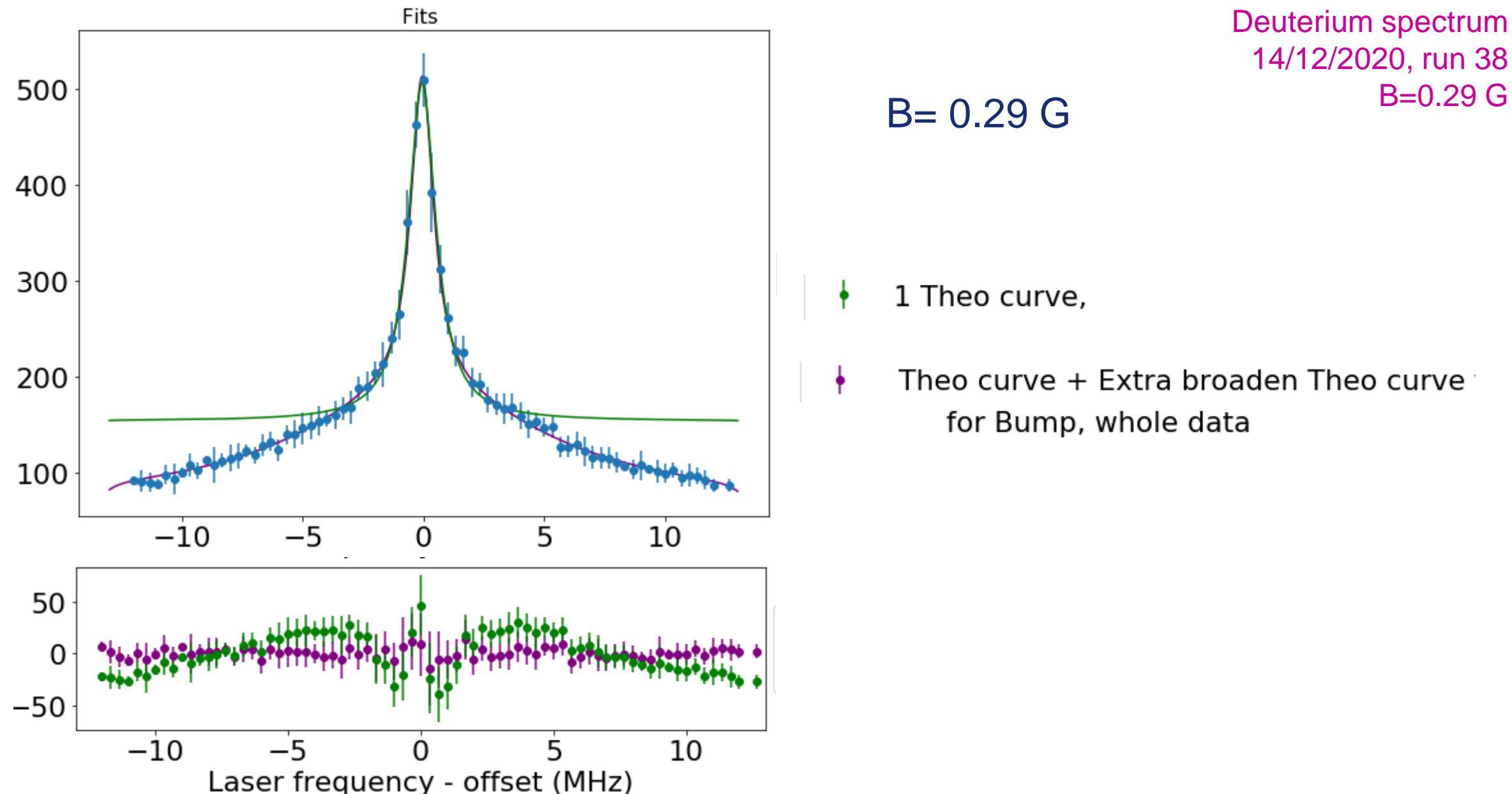


$$F(\nu_L) = F_{theo}(\nu_L, \nu_0, \sigma_0) + F_{theo}(\nu_L, \nu_B, \sigma_B)$$

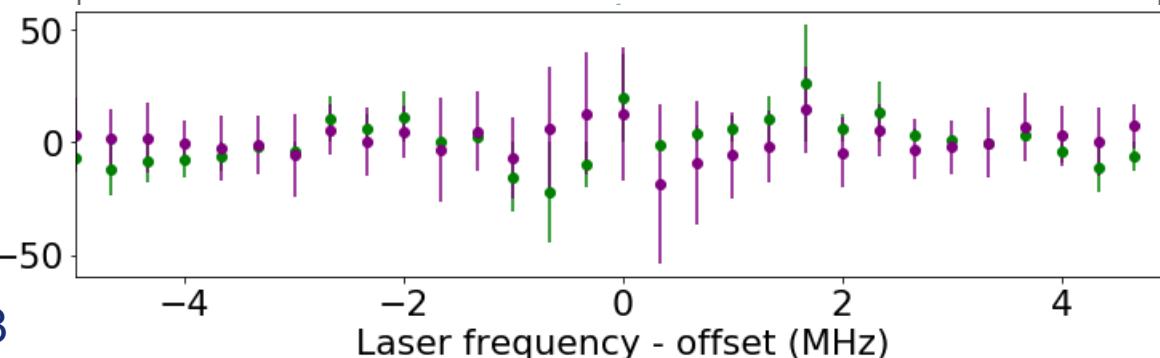
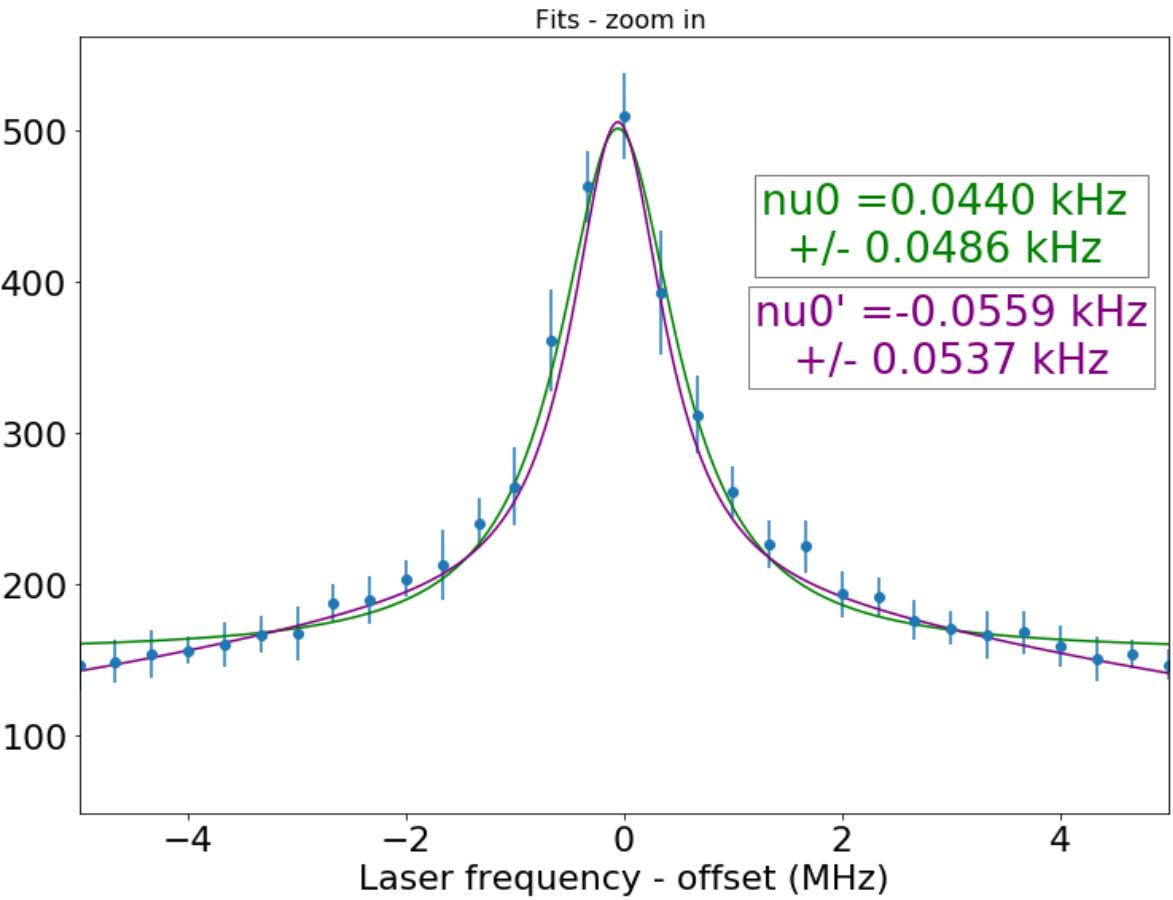
Fitting range : all data

• Theo curve + Extra broaden Theo curve  
for Bump, whole data

# Difference in the fit result of the different models ?



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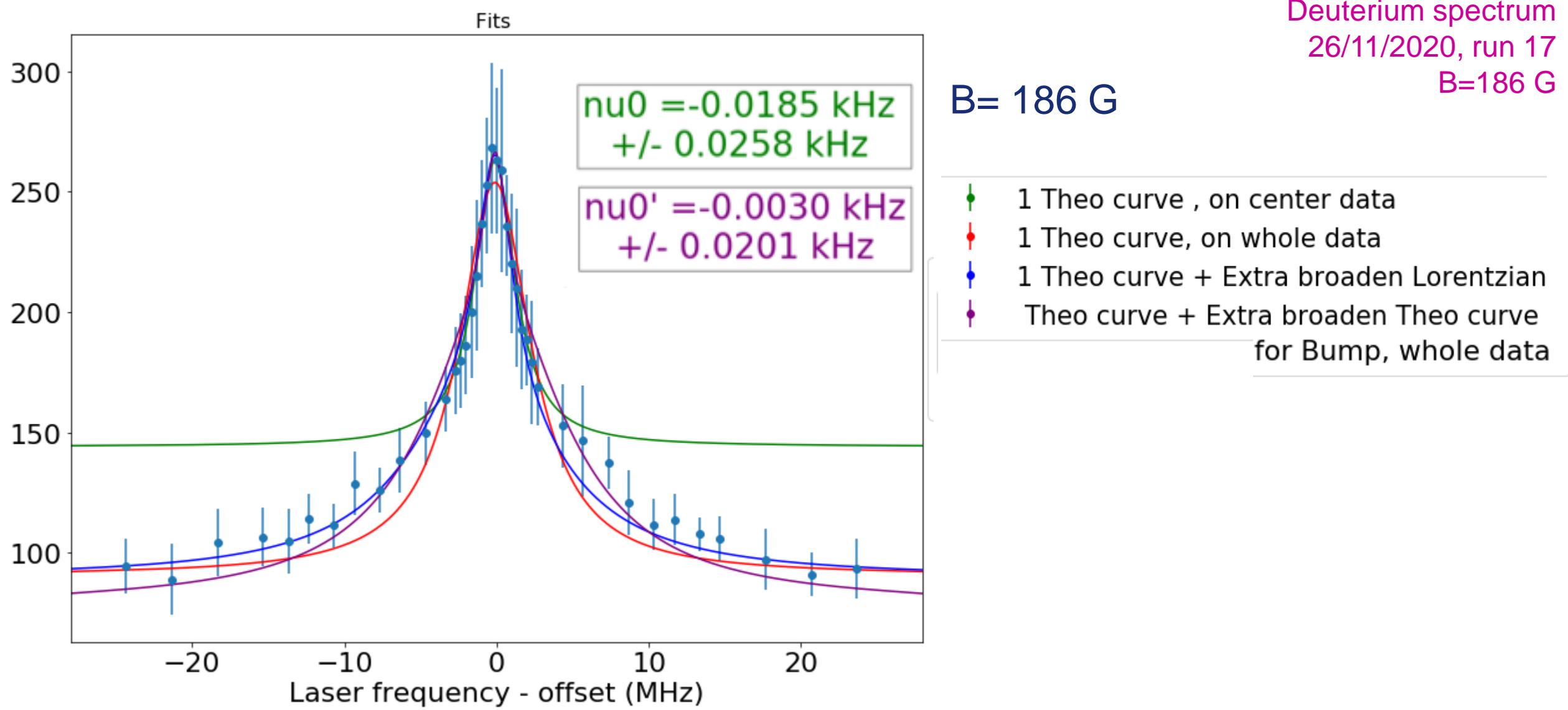


Deuterium spectrum  
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- 1 Theo curve,
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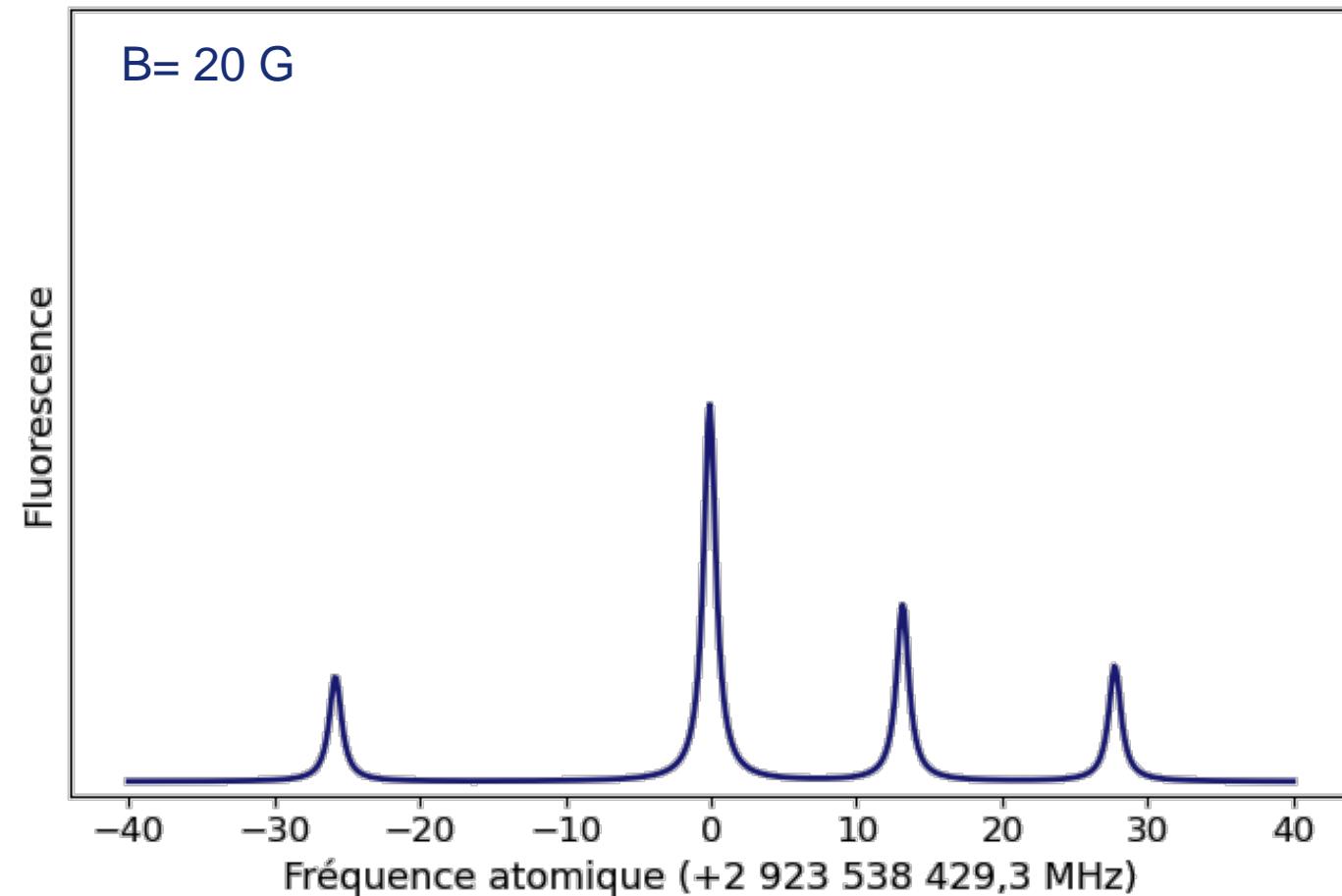
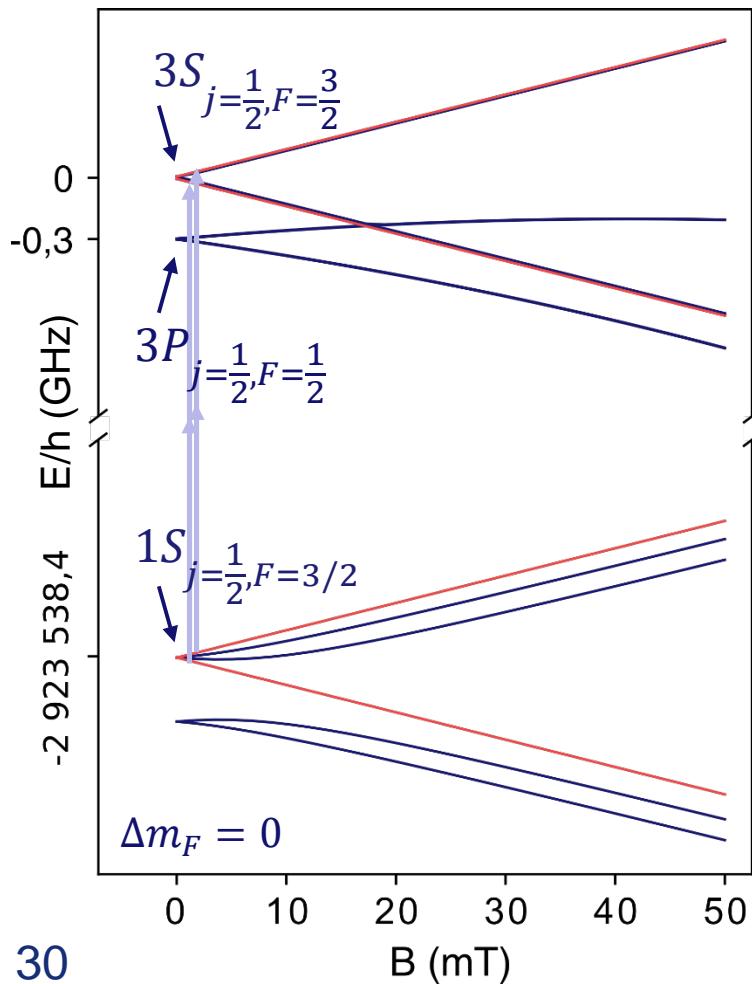
# Difference in the fit result of the different models ?



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Story more complex at weak B field:  $B \sim 20$  G

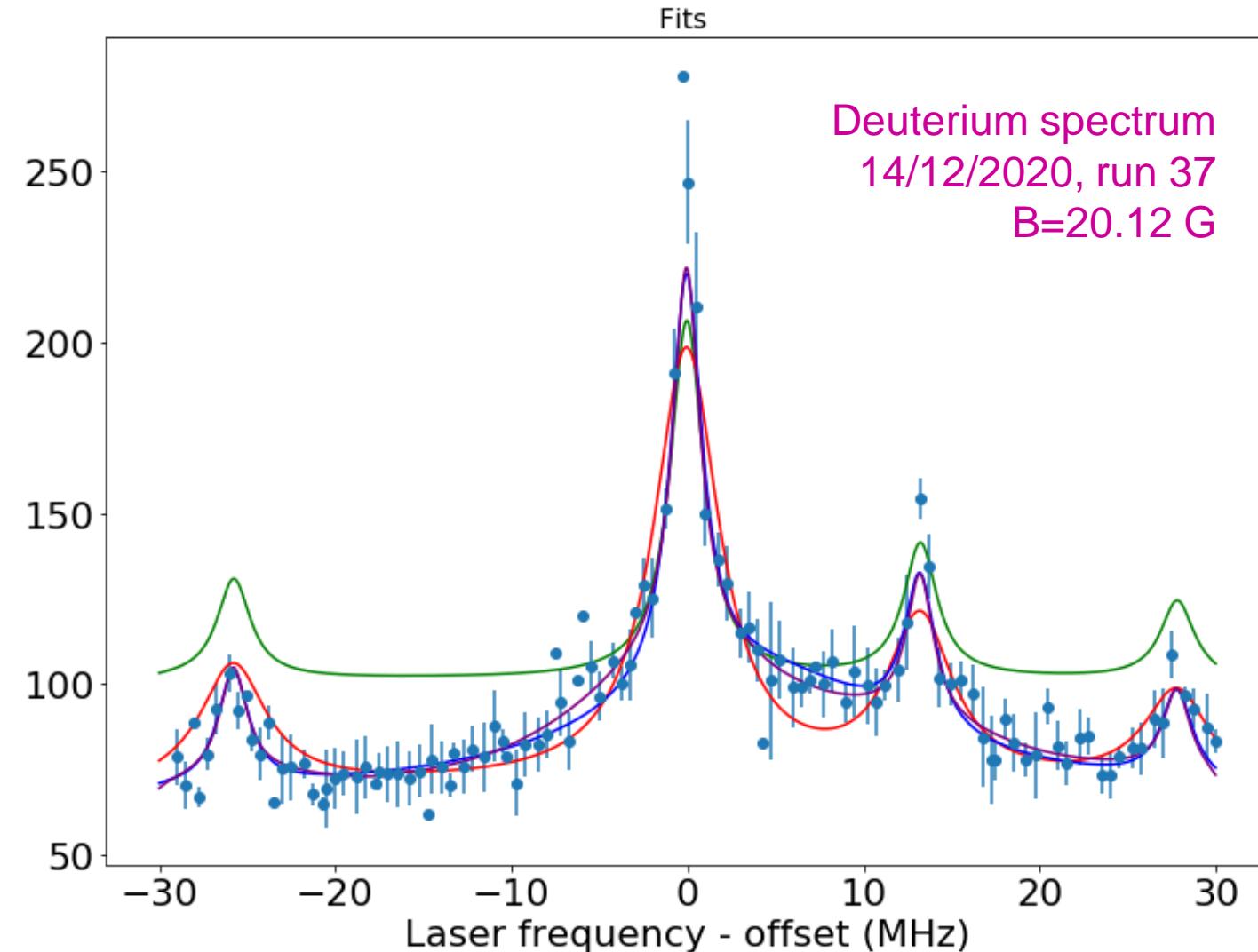
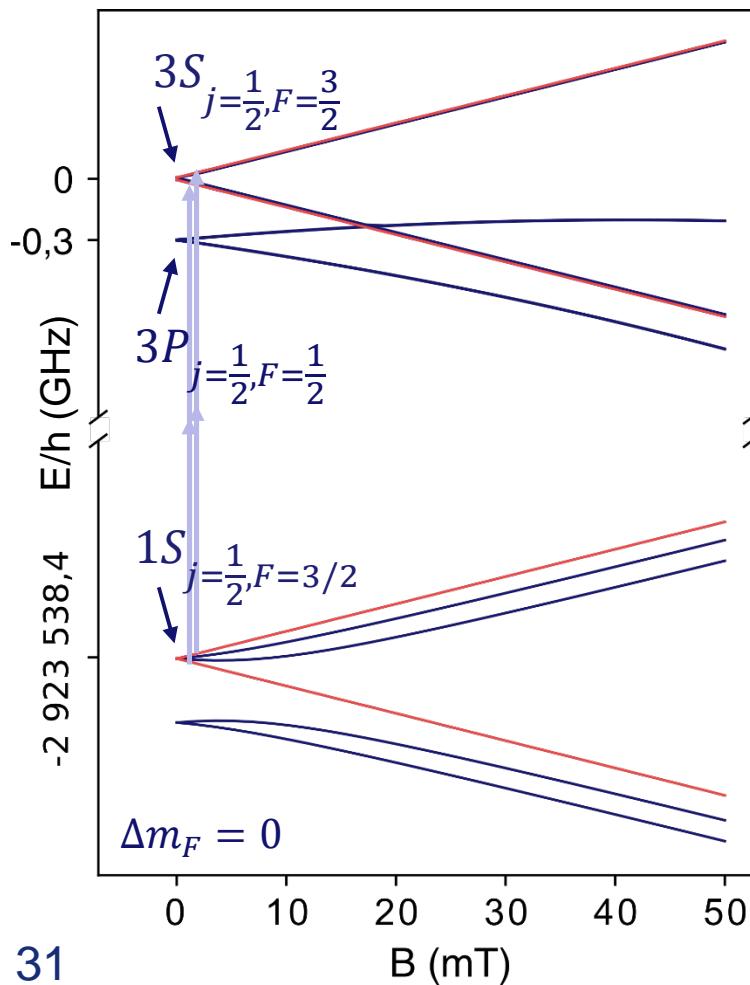
Deuterium Energy levels



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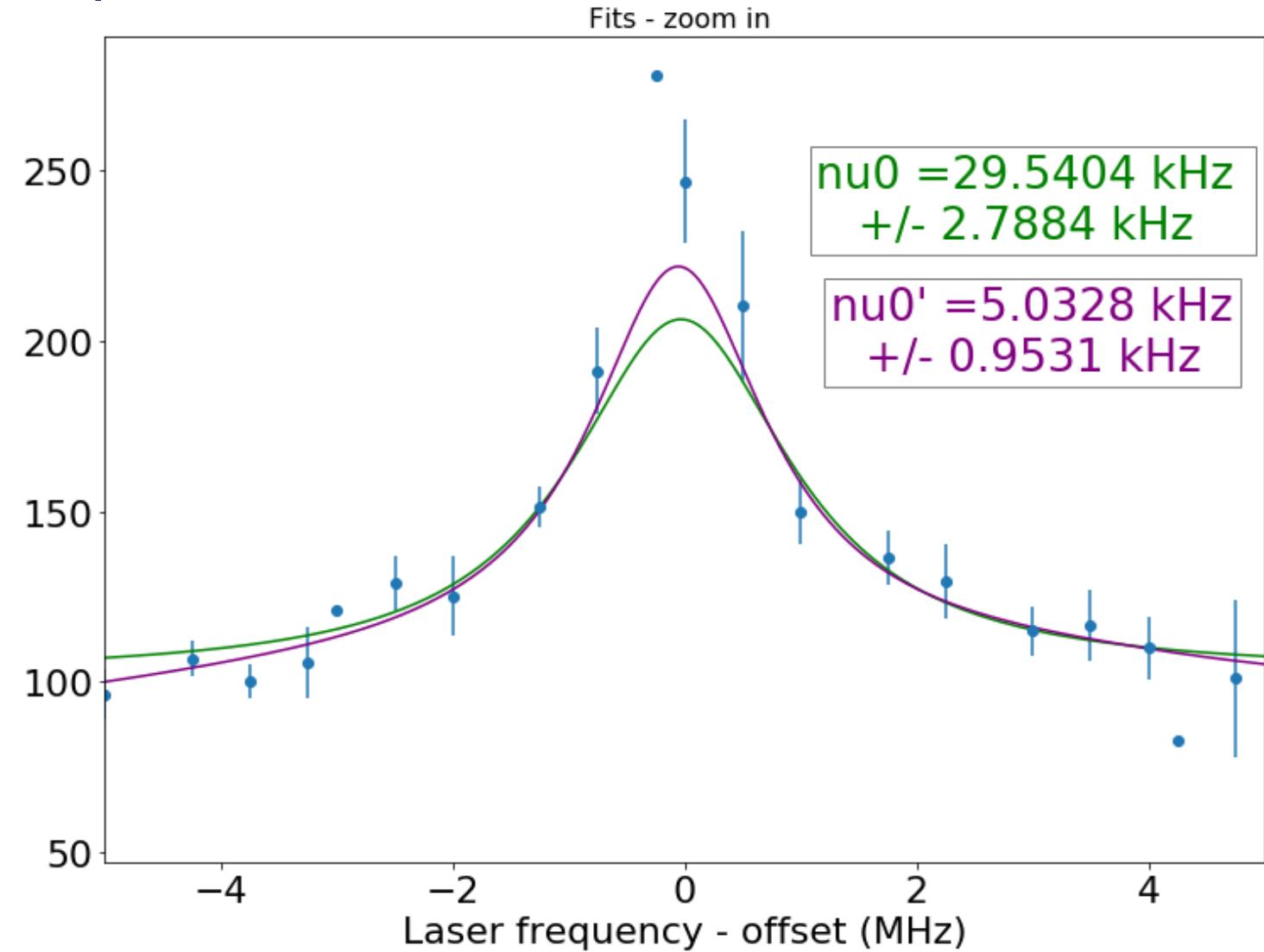
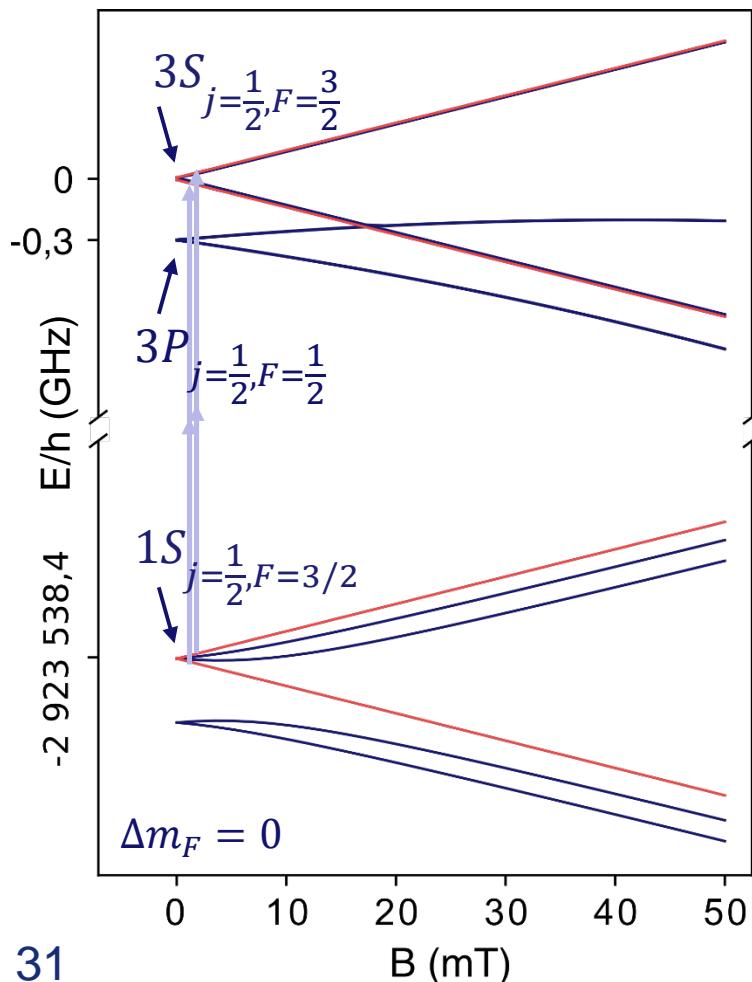
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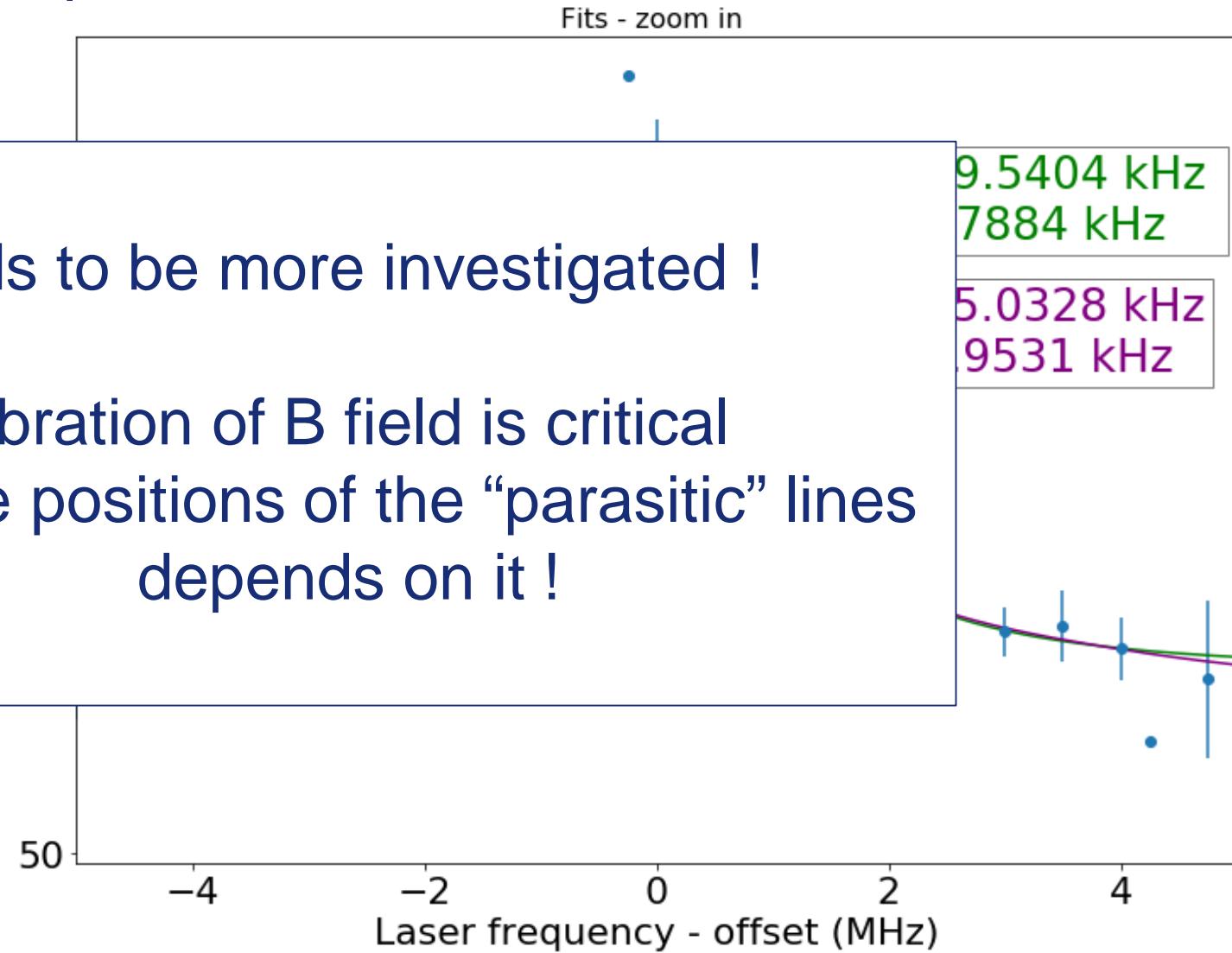
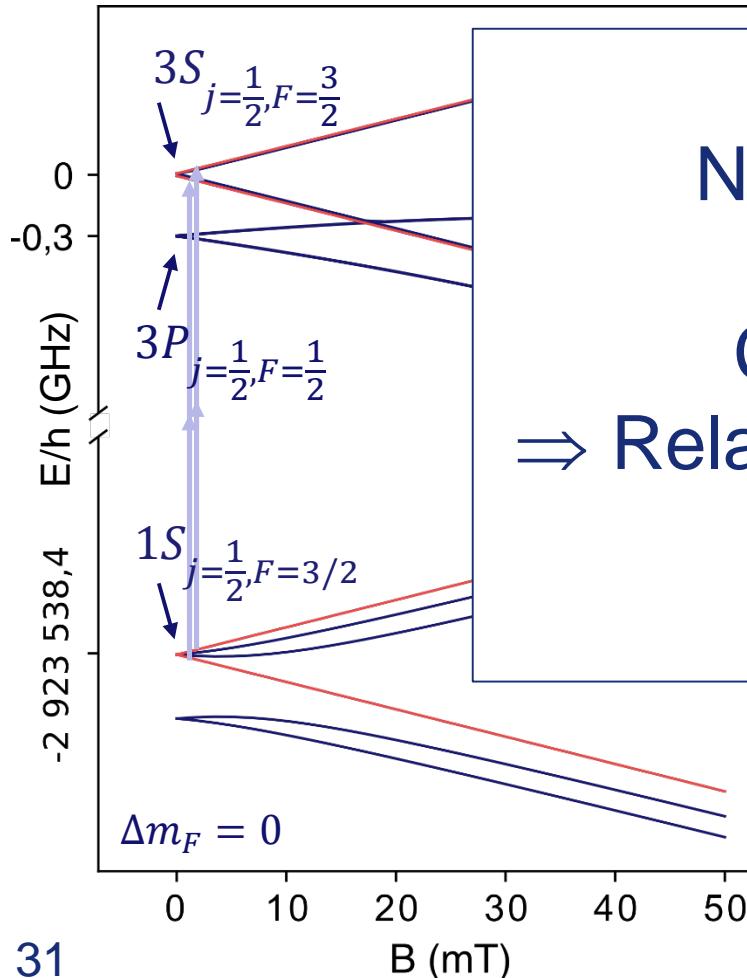
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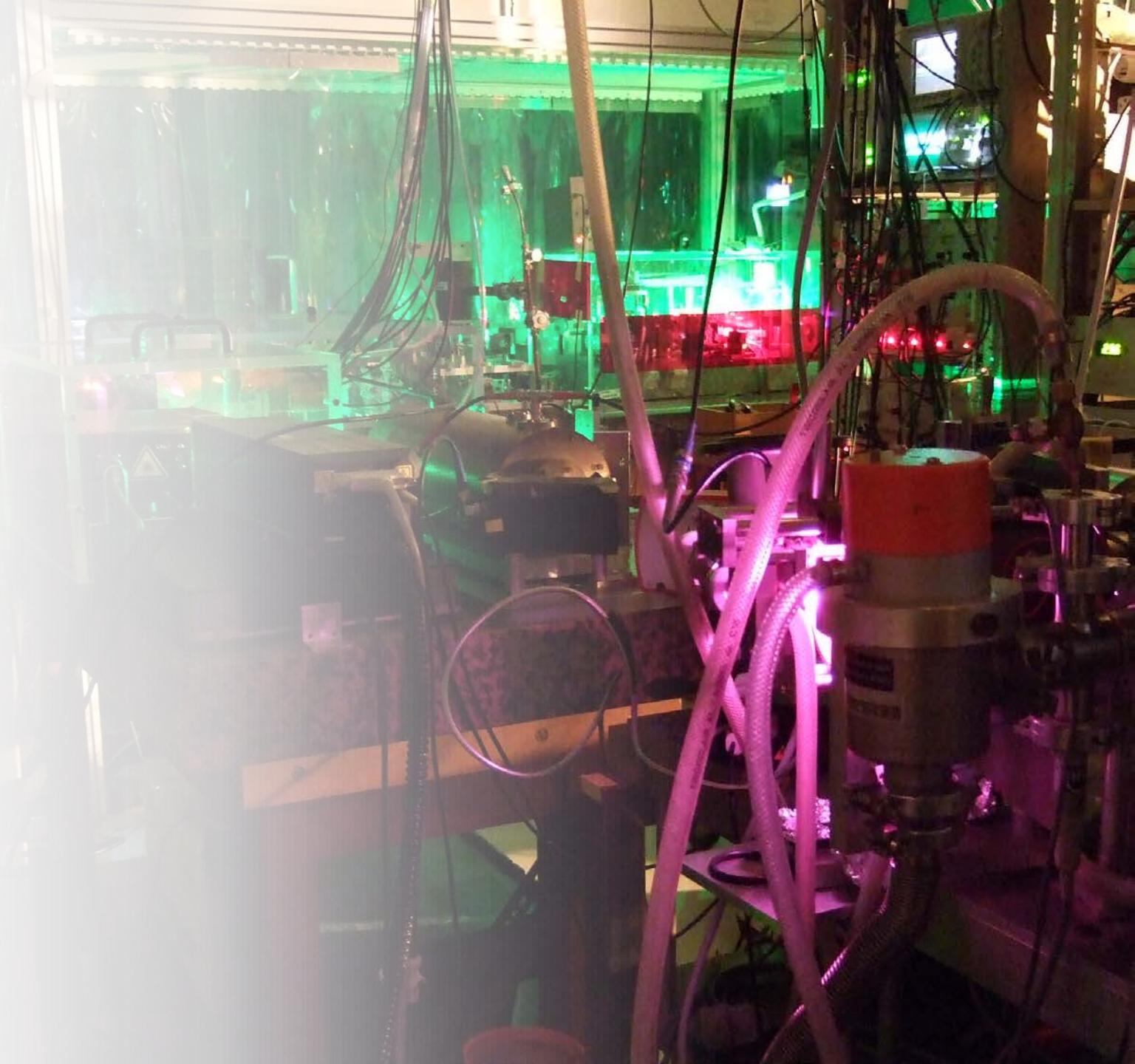
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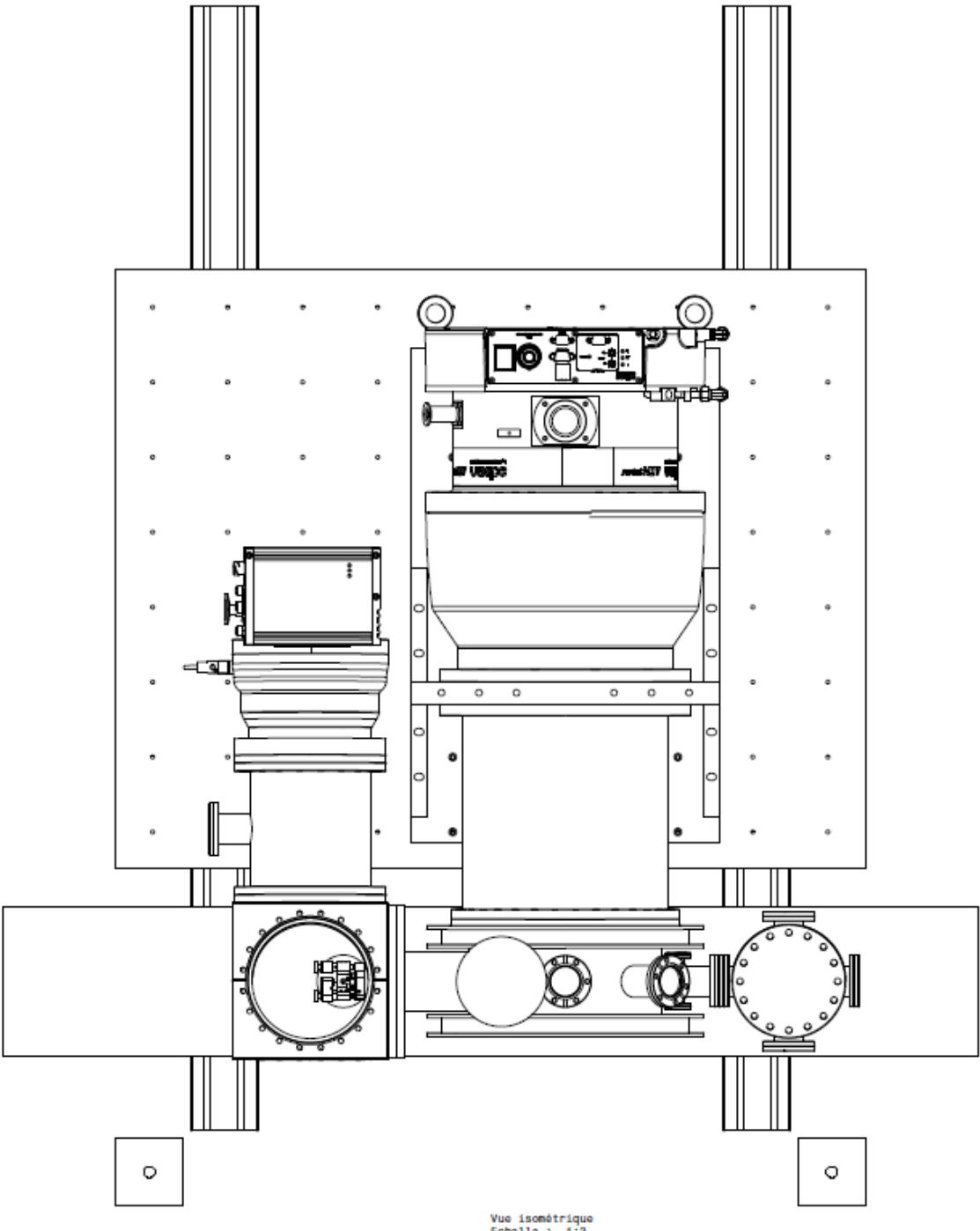
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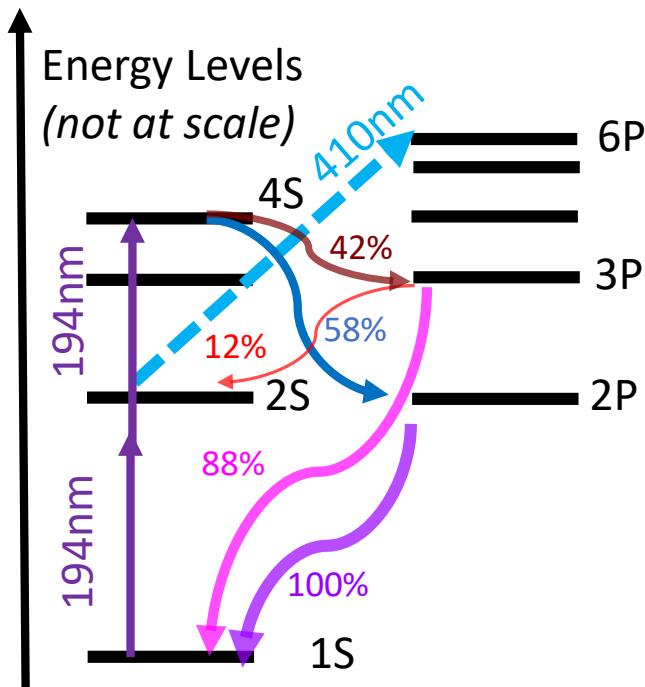
# The new H beam experiment

- Based on dry pumps !
- New design to decoupled the mirrors' cavity of the 205nm from the vibrations of the turbo pumps

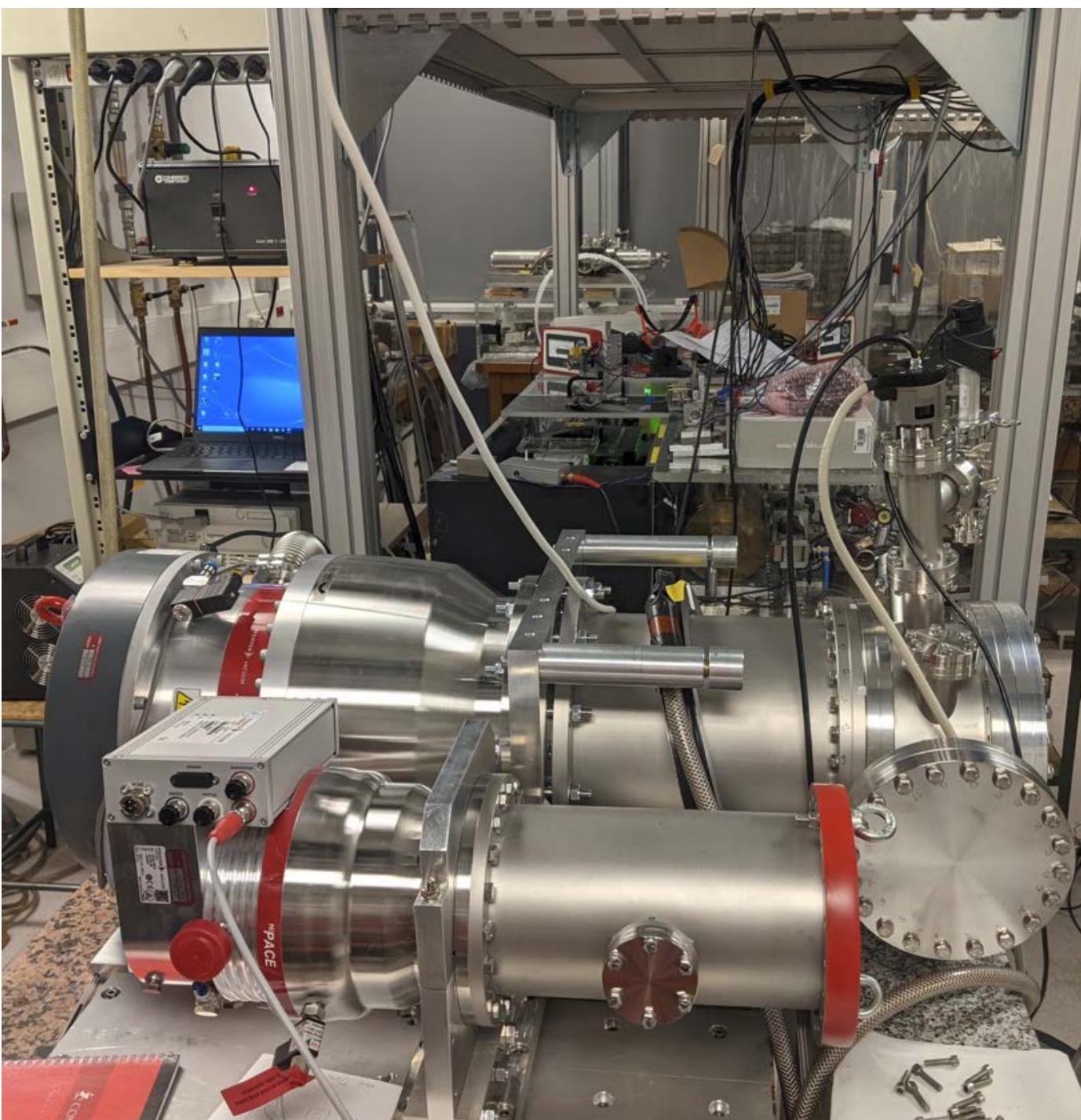


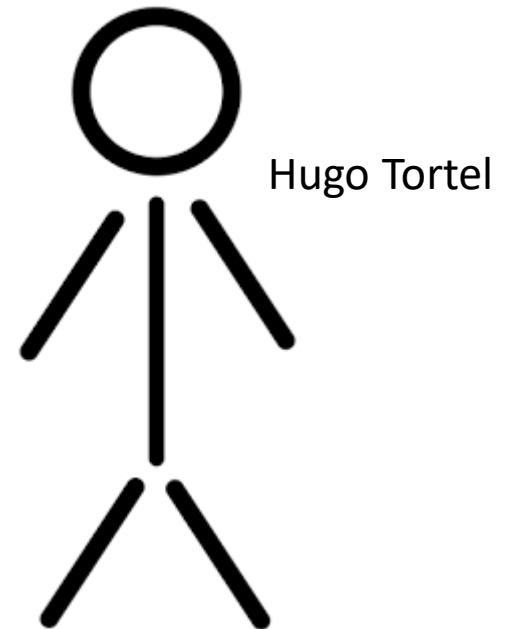
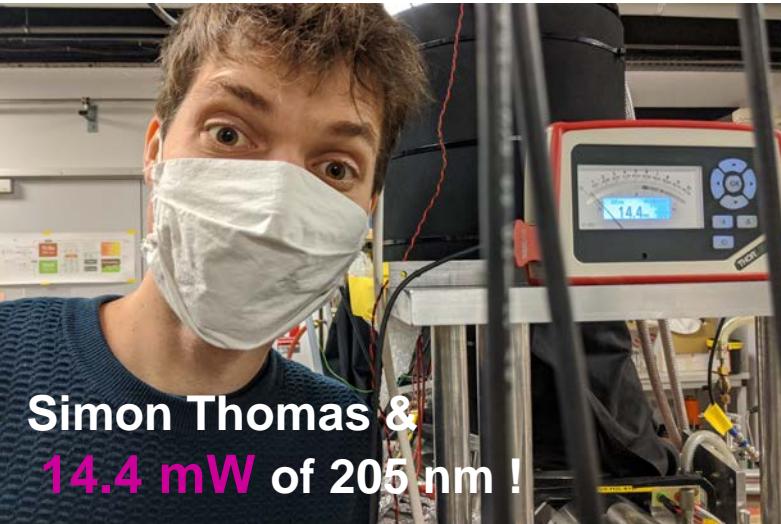
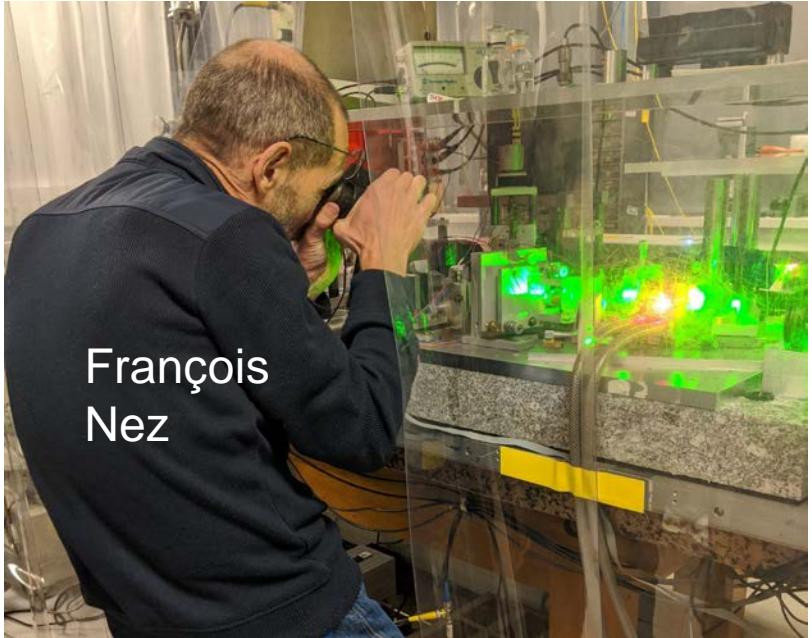
# The new H beam experiment

- For 1S-3S then 1S-4S



1S-4S spectroscopy





Thanks for your attention