

# Jet quenching and quantum algorithms

Felix Ringer

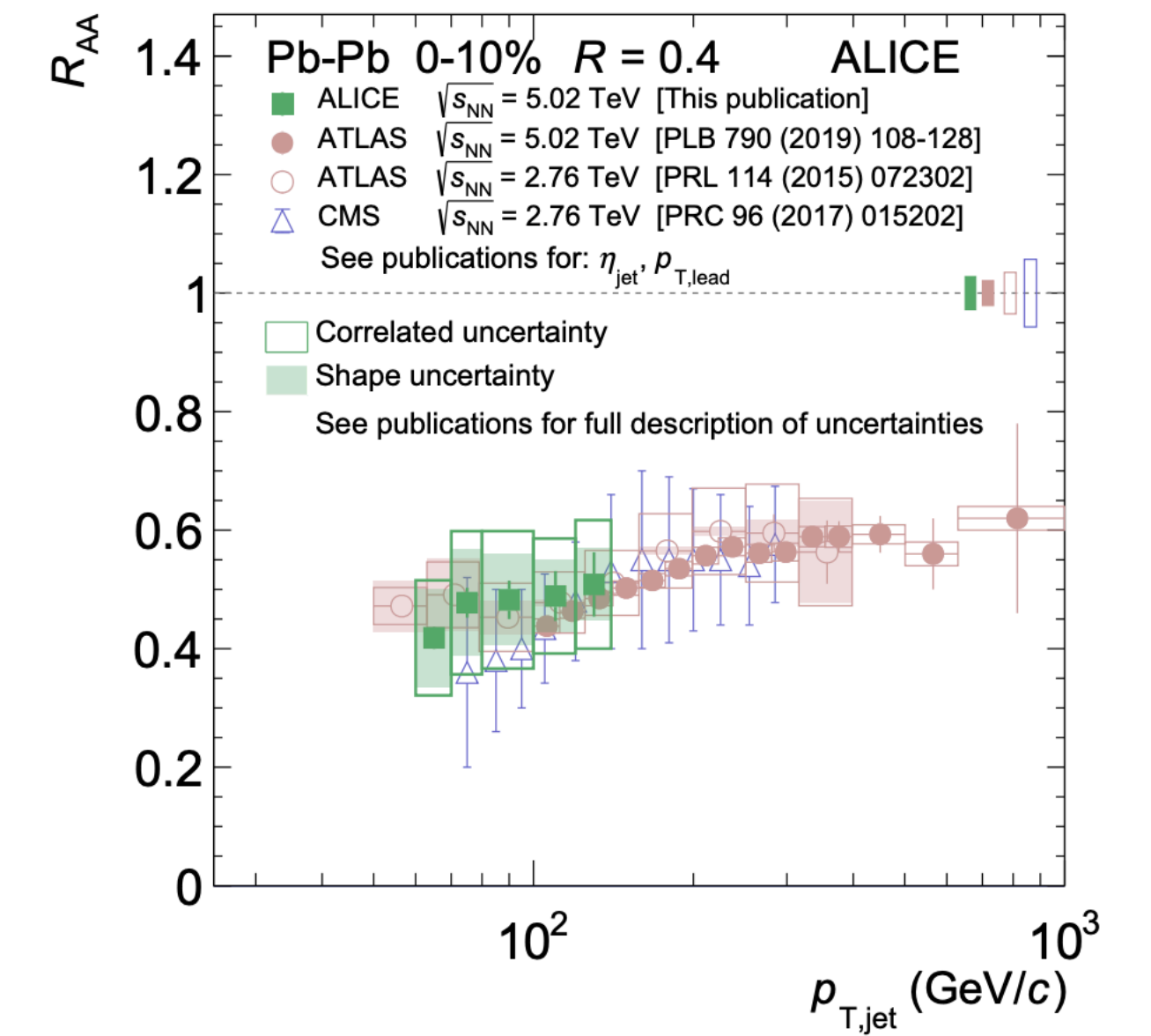
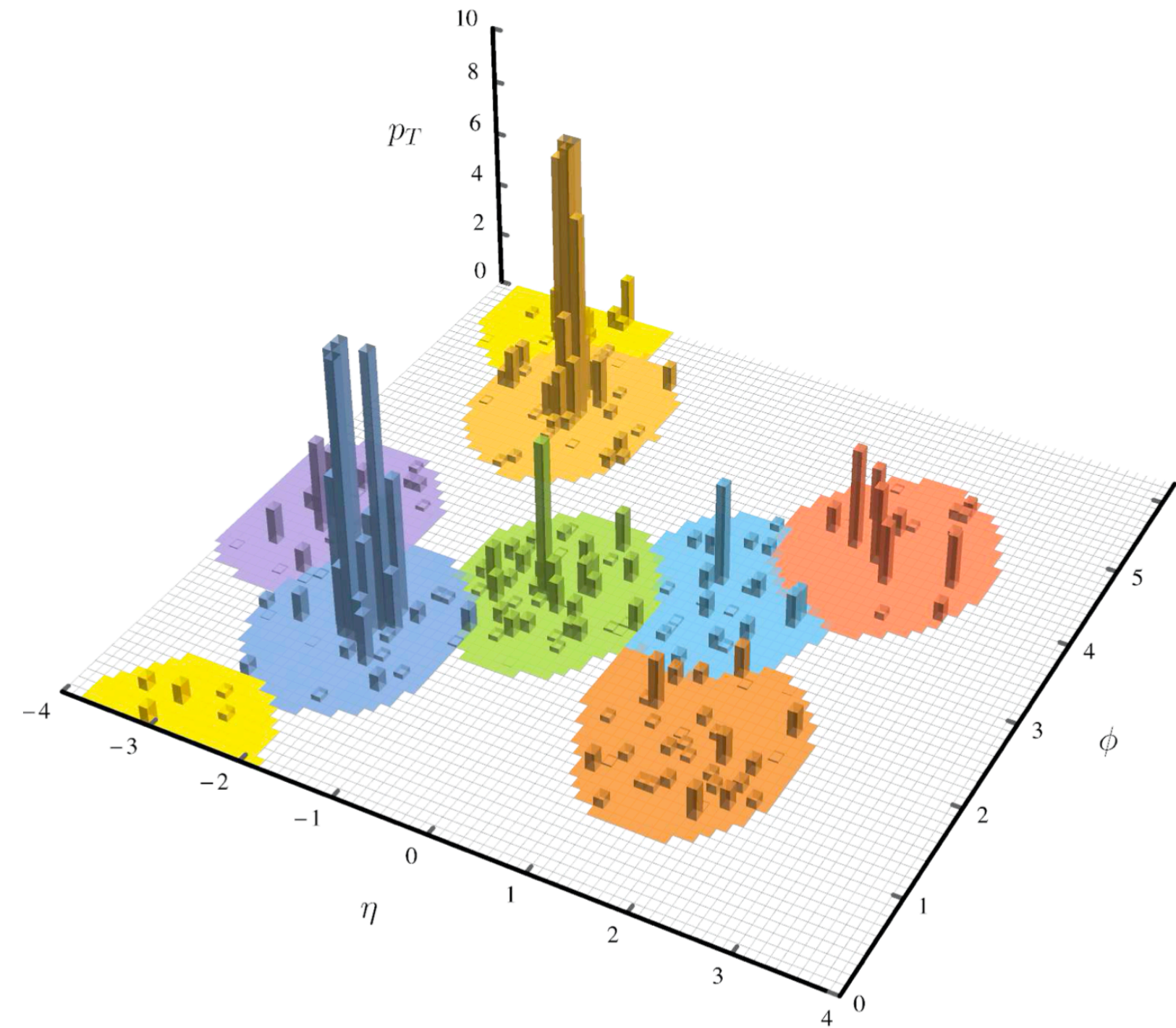
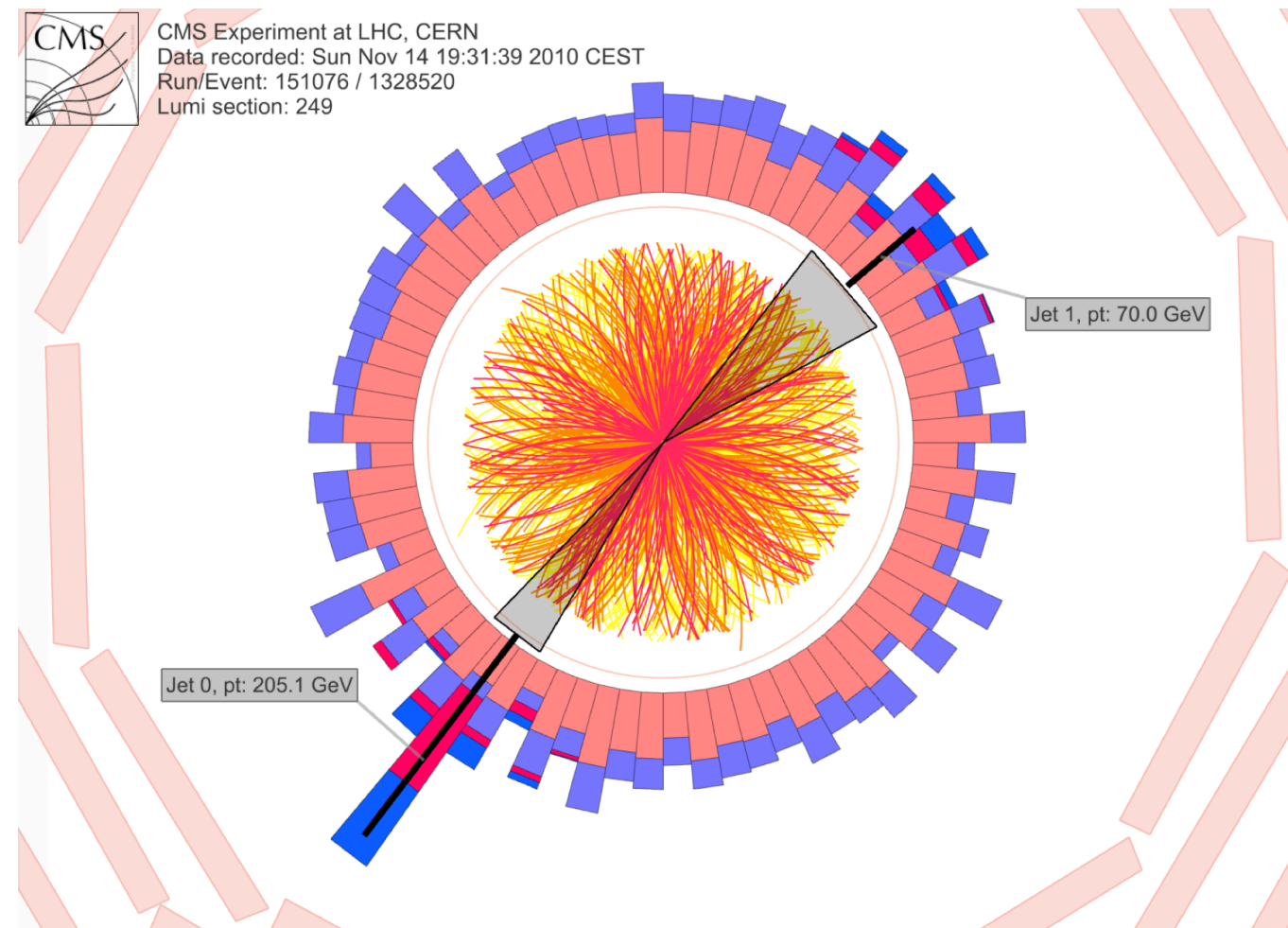
YITP, Stony Brook University

The Quantumness of Hard Probes, MITP, Mainz, 01/19/22



SIMONS FOUNDATION

# Jet quenching and energy loss



ALICE, PRC 101 (2020) 034911

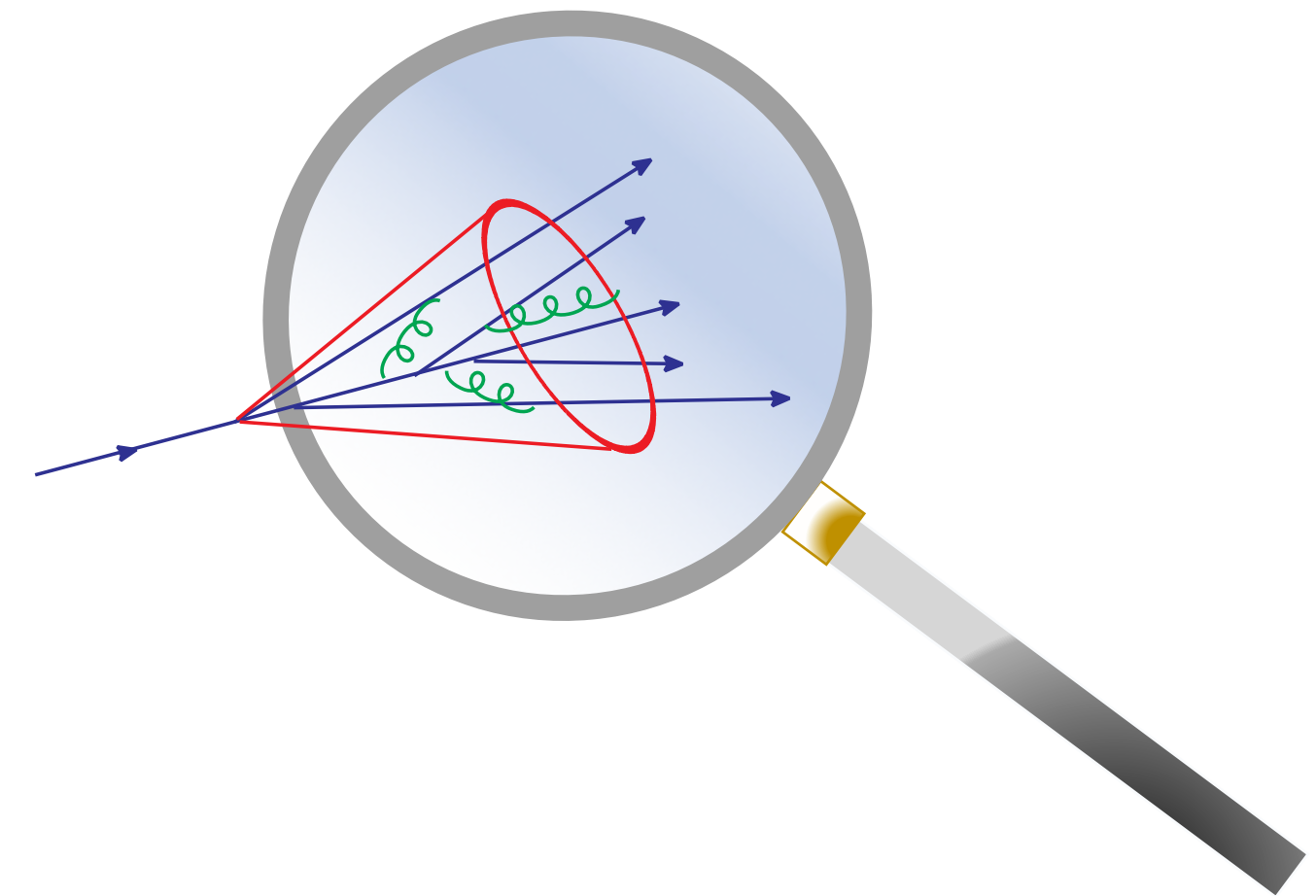
see talks by Yacine Mehtar-Tani and Varun Vaidya

# Factorization in heavy-ion collisions

- Test of factorization & universality
- Extension of vacuum factorization theorems to the medium case
- In-medium jet functions

$$\frac{d\sigma_{pp \rightarrow \text{jet}+X}}{d\eta dp_T} = \sum_{ijk} f_{i/p} \otimes f_{j/p} \otimes H_{ijk} \otimes J_k^{\text{med}}$$

Applications to jet substructure?

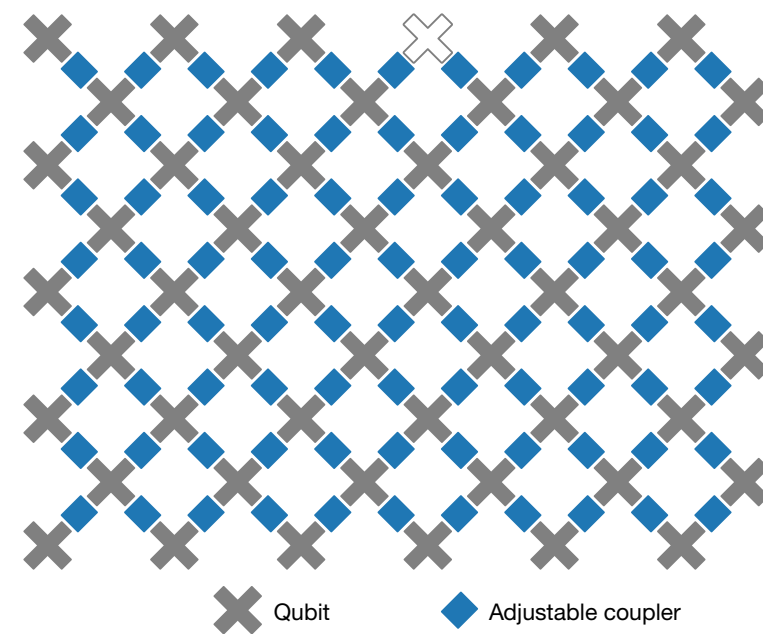
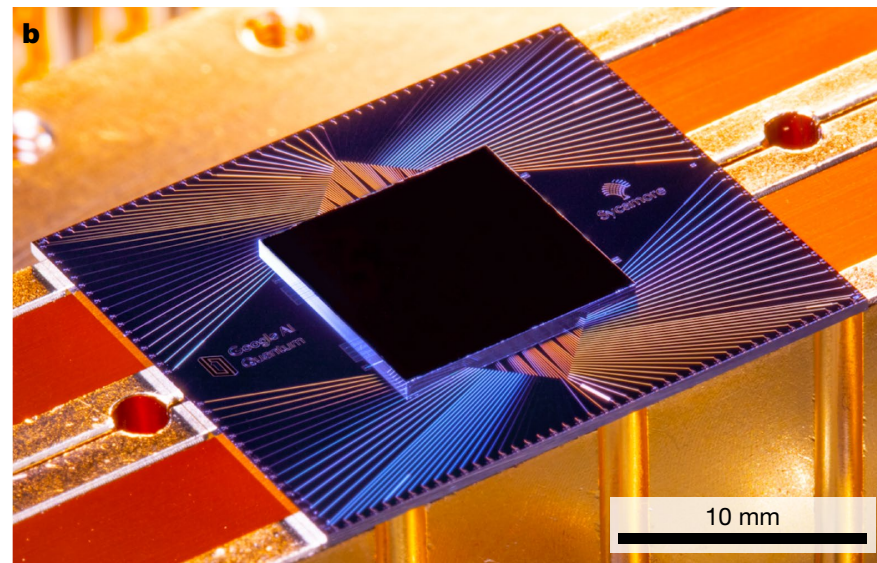


# Applications of quantum computing

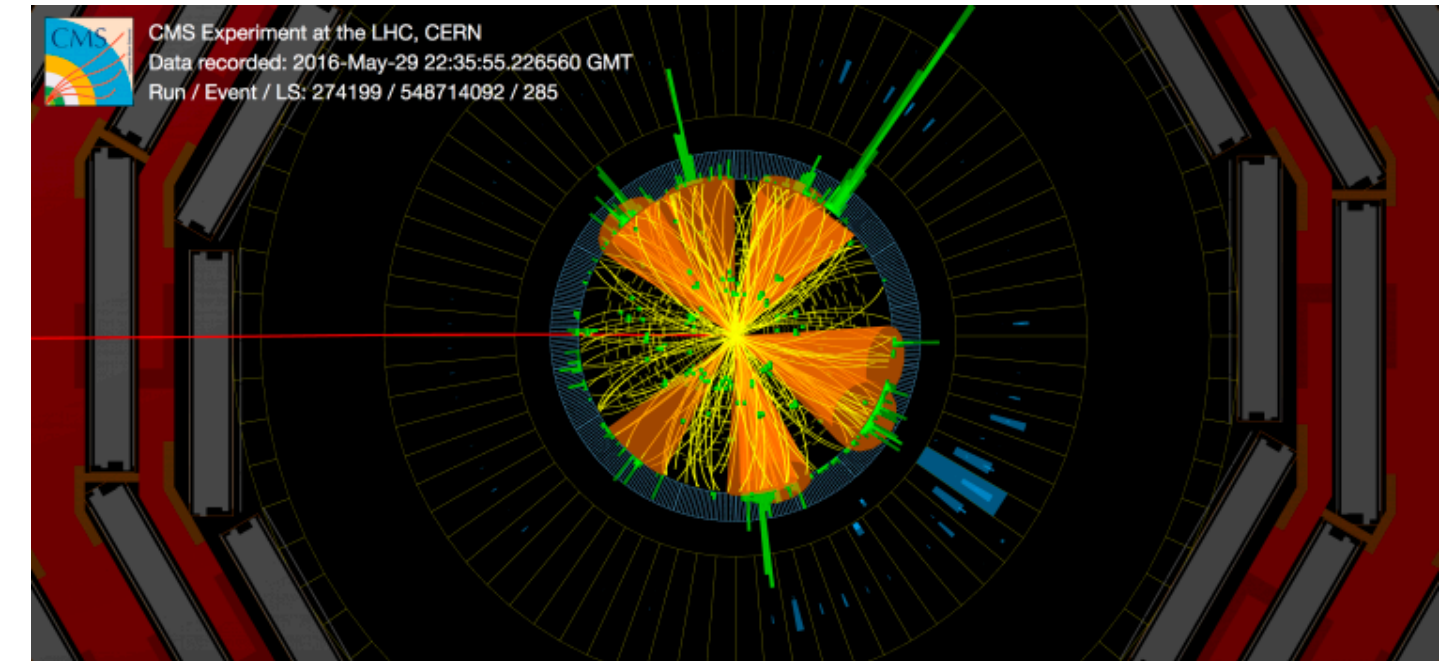


Article

## Quantum supremacy using a programmable superconducting processor



Universal simulations of QCD from first principles?



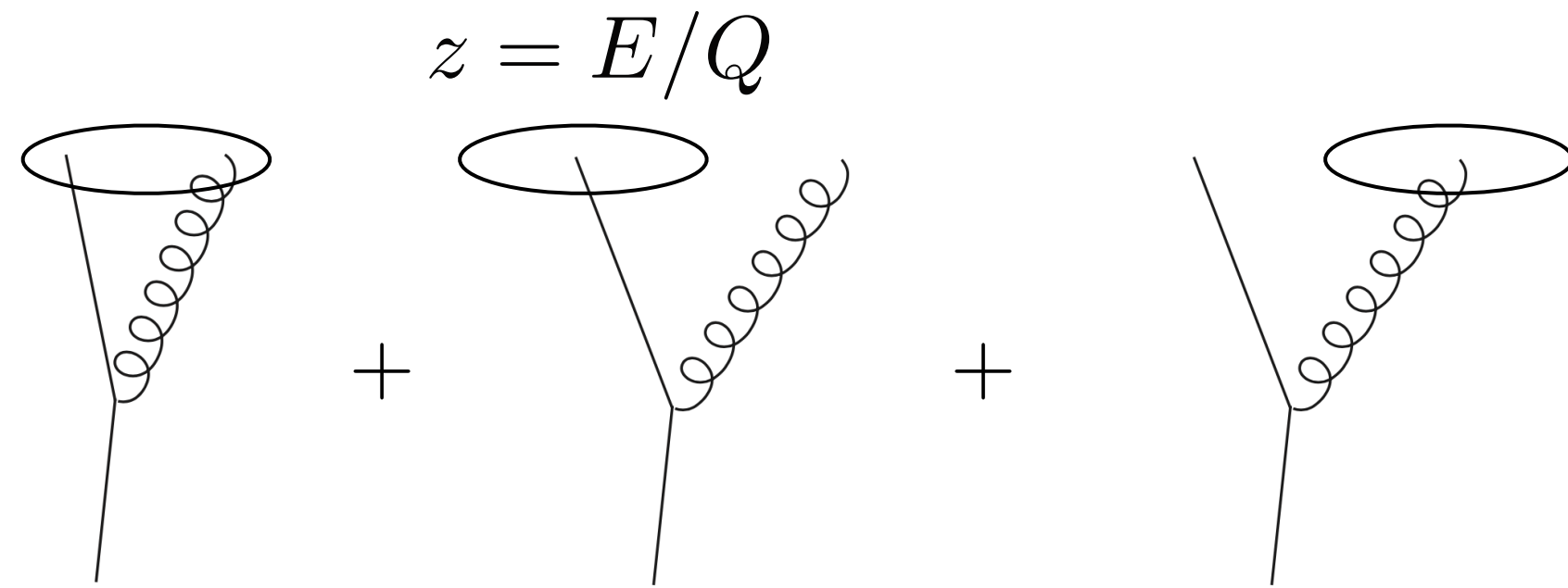
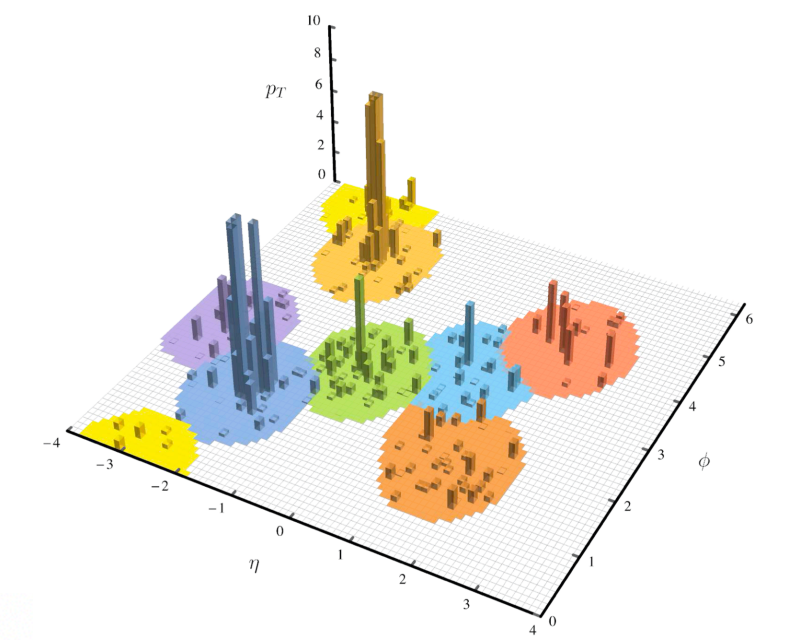
Random circuit sampling *Martinis et al. '19*

# Outline

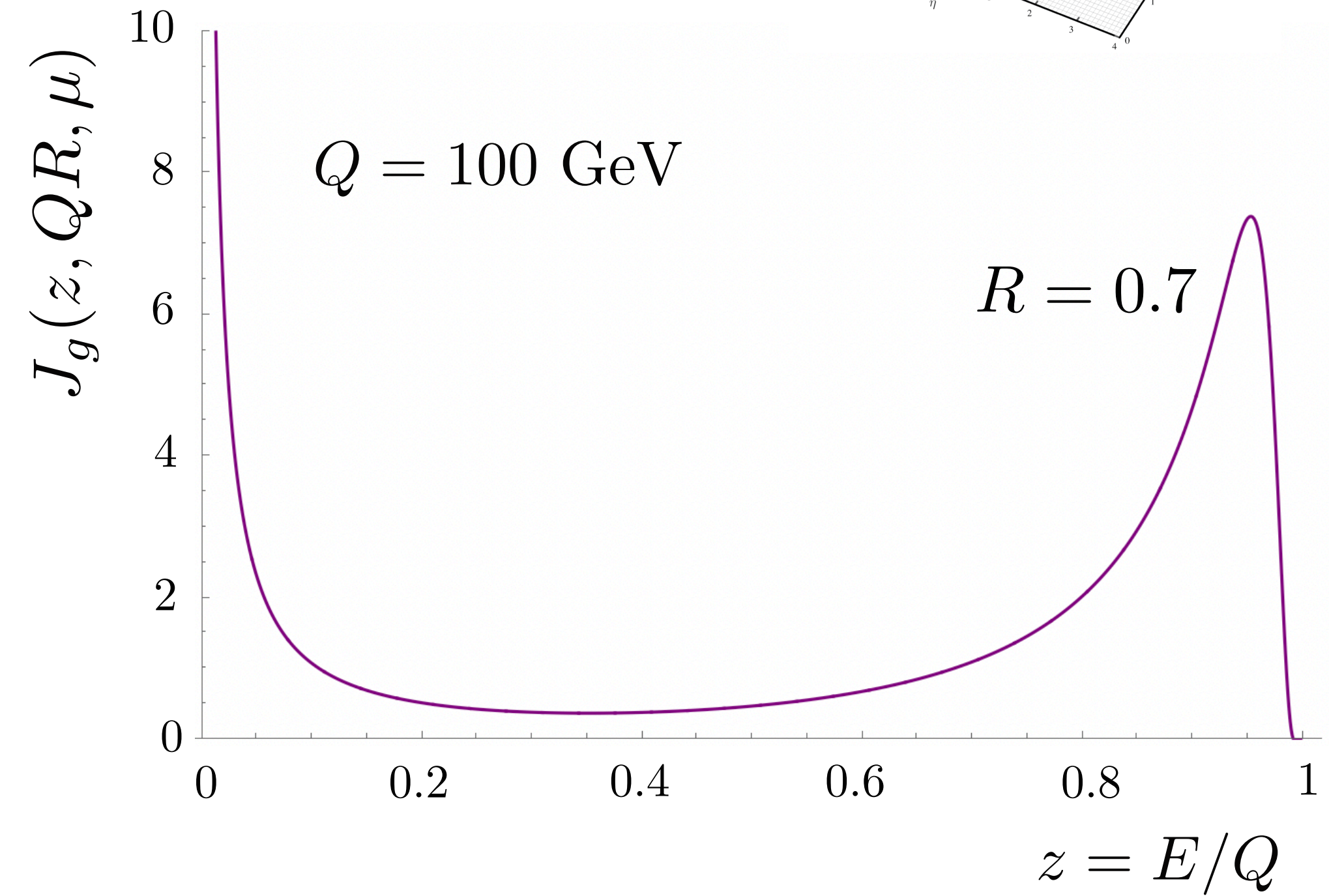
- Introduction
- QCD factorization in heavy-ion collisions
- Quantum simulations of open quantum systems
- Conclusions

# Inclusive jet cross sections

• **NLO**  $J_i(z, QR, \mu)$



$$J_q(z, QR, \mu) = \delta(1 - z) + \frac{\alpha_s}{2\pi} \left( \ln \left( \frac{\mu^2}{Q^2 R^2} \right) - 2 \ln z \right) [P_{qq}(z) + P_{gq}(z)] + \dots$$



Dasgupta, Dreyer, Salam, Soyez `14  
 Kaufmann, Mukherjee, Vogelsang `15  
 Kang, Ringer, Vitev `16  
 Dai, Kim, Leibovich `16  
 Liu, Moch, Ringer `18, `19

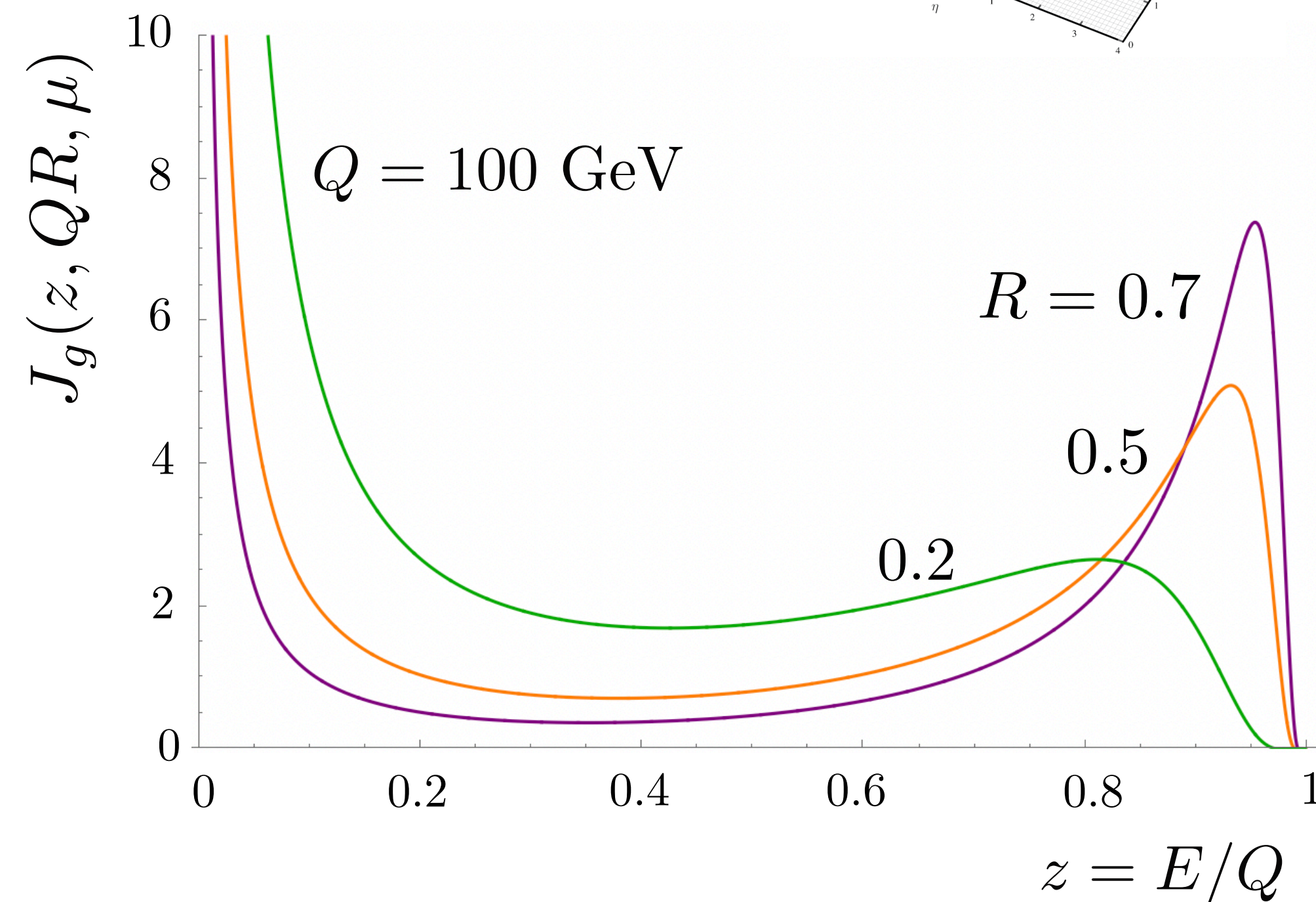
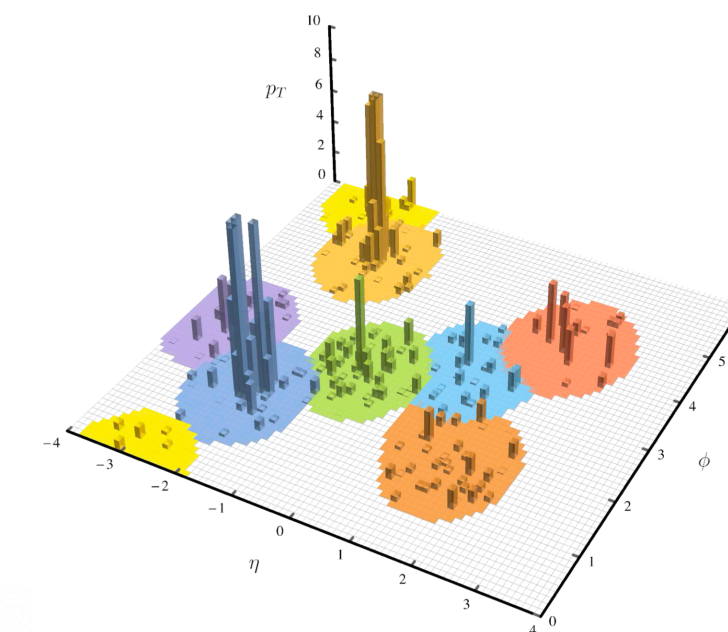
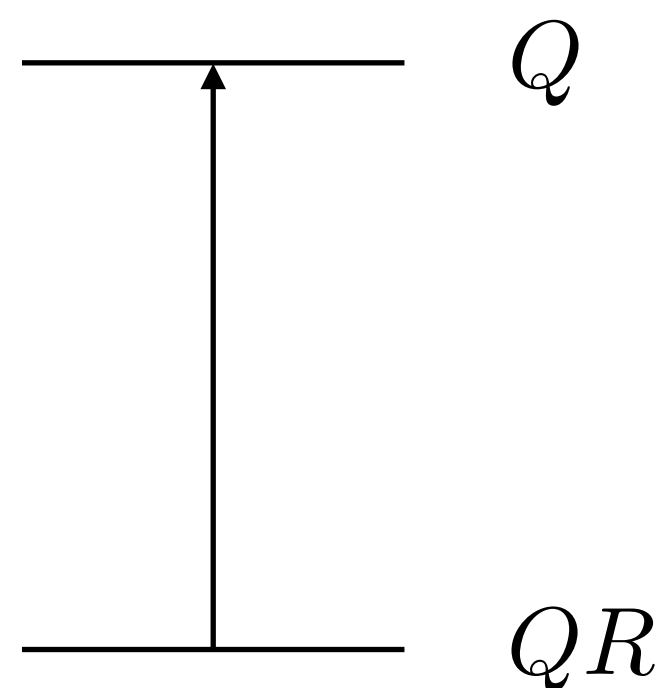
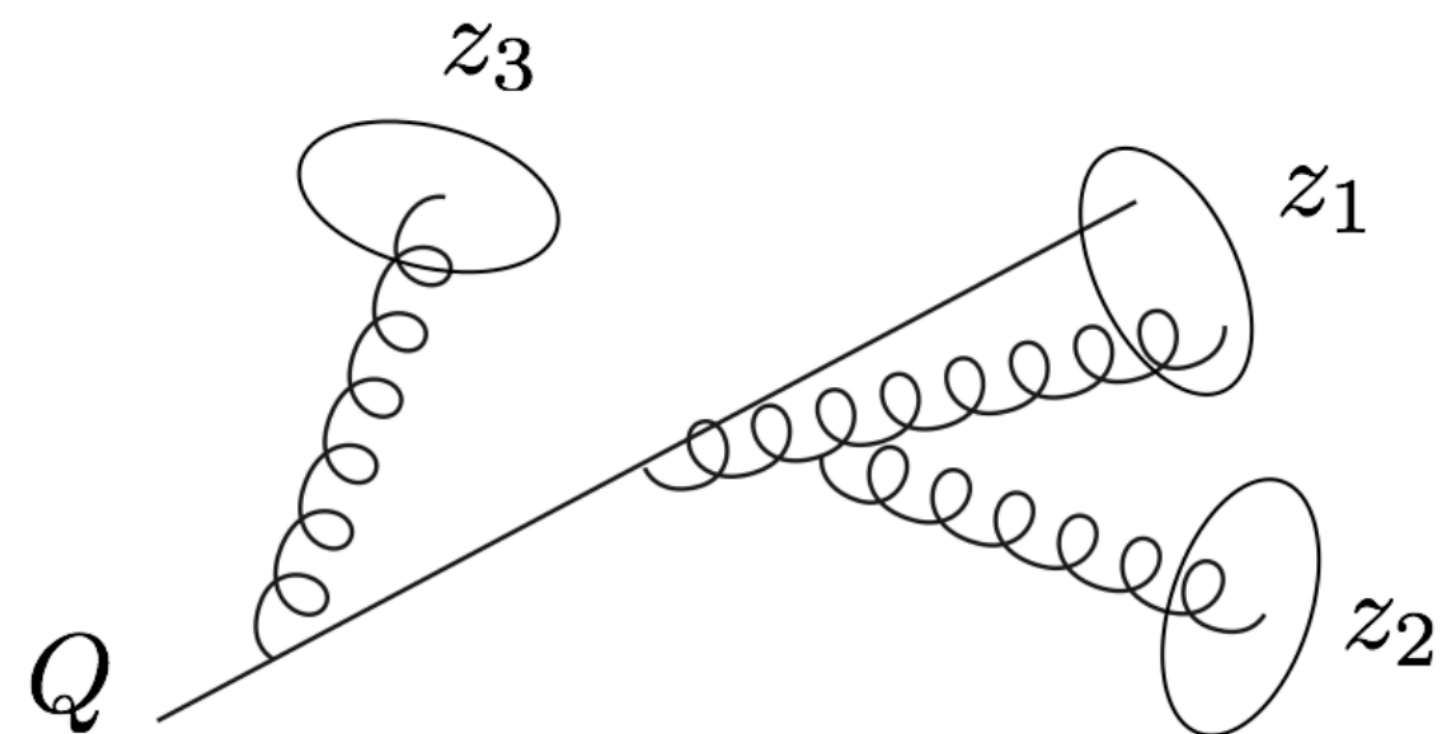
# Inclusive jet cross sections

- **NLO**  $J_i(z, QR, \mu)$

- **QCD evolution**

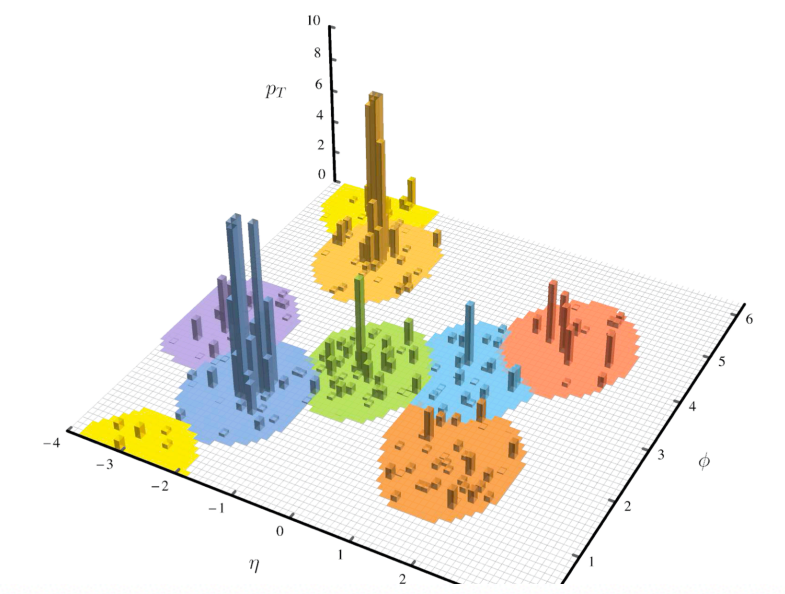
$$\mu \frac{d}{d\mu} J_i = \frac{\alpha_s}{2\pi} \sum_j P_{ji} \otimes J_j$$

DGLAP like hadron fragmentation functions



Dasgupta, Dreyer, Salam, Soyez `14  
 Kaufmann, Mukherjee, Vogelsang `15  
 Kang, Ringer, Vitev `16  
 Dai, Kim, Leibovich `16  
 Liu, Moch, Ringer `18, `19

# Inclusive jet cross sections



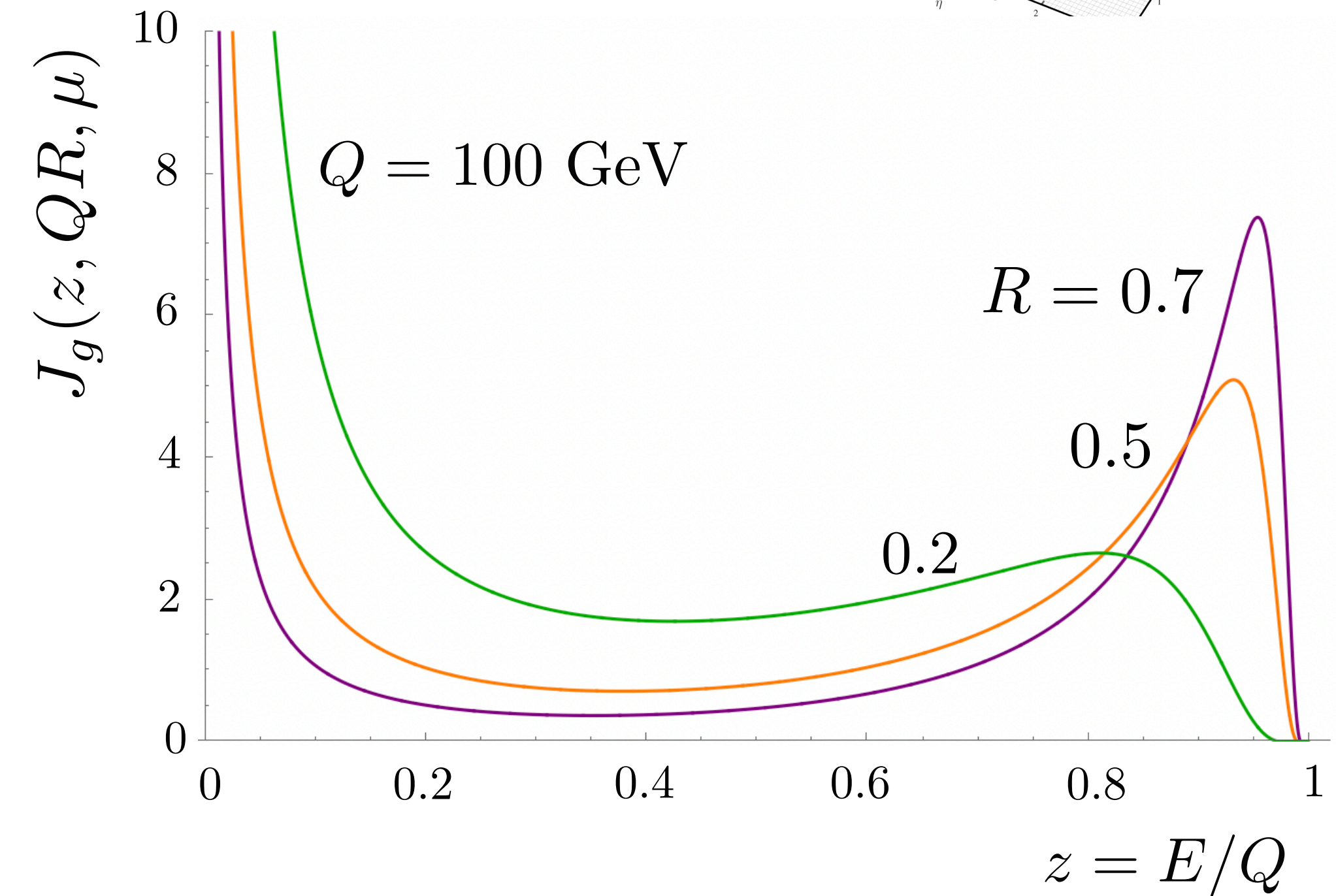
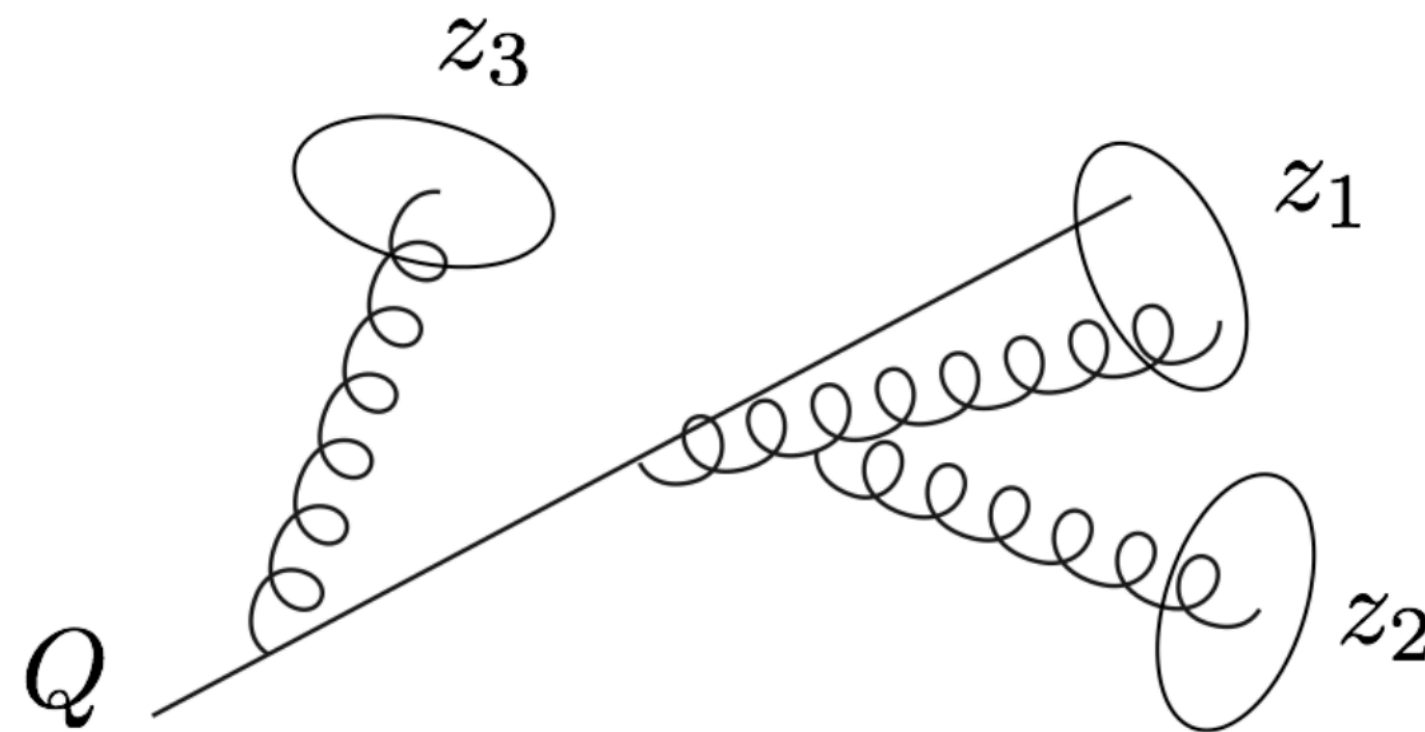
- **NLO**  $J_i(z, QR, \mu)$

- **QCD evolution**

$$\mu \frac{d}{d\mu} J_i = \frac{\alpha_s}{2\pi} \sum_j P_{ji} \otimes J_j$$

- **Factorization**

$$\frac{d\sigma_{pp \rightarrow \text{jet} + X}}{d\eta dp_T} = \sum_{ijk} f_{i/p} \otimes f_{j/p} \otimes H_{ijk} \otimes J_k$$



Dasgupta, Dreyer, Salam, Soyez '14  
 Kaufmann, Mukherjee, Vogelsang '15  
 Kang, Ringer, Vitev '16  
 Dai, Kim, Leibovich '16  
 Liu, Moch, Ringer '18, '19

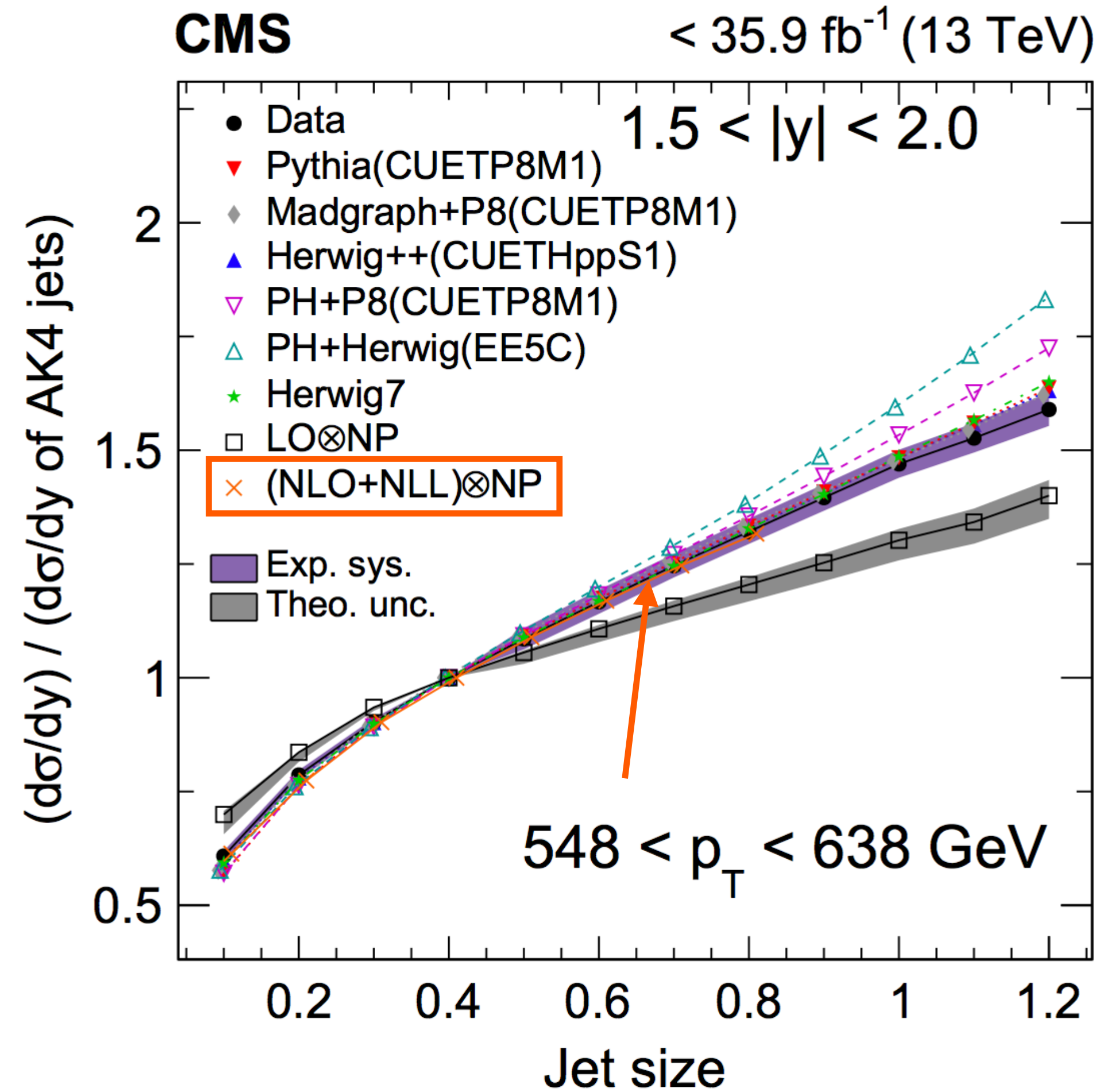


# Inclusive jet cross sections

- Phenomenology

- Jet substructure

$$f_q J_q(\theta_g) + f_g J_g(\theta_g)$$



Liu, Moch, FR `17, 18

CMS, JHEP 12 (2020) 82  
see also recent results from ALICE

# Inclusive jets in heavy-ion collisions

- **Factorization** - can we systematically extend vacuum factorization theorems in vacuum to heavy-ion collisions?

$$\frac{d\sigma_{pp \rightarrow \text{jet}+X}}{d\eta dp_T} = \sum_{ijk} f_{i/p} \otimes f_{j/p} \otimes H_{ijk} \otimes J_k$$



Heavy-ion collisions

- **Universality** - consistent description of multiple observables?

$$f_q J_q(\theta_g) + f_g J_g(\theta_g)$$

- Phenomenological approach first

# Inclusive jets in heavy-ion collisions

Qiu, FR, Sato, Zurita '19

- Proton-proton

$$\frac{d\sigma^{pp \rightarrow \text{jet}+X}}{dp_T d\eta} = \sum_{a,b,c} f_{a/p} \otimes f_{b/p} \otimes H_{ab}^c \otimes J_c$$

$$\mu^2 \frac{d}{d\mu^2} J_i = \sum_j P_{ji} \otimes J_j$$



- Heavy-ion

$$\frac{d\sigma^{AA \rightarrow \text{jet}+X}}{dp_T d\eta} = \sum_{a,b,c} f_{a/A} \otimes f_{b/A} \otimes H_{ab}^c \otimes J_c^{\text{med}}$$

$$\mu^2 \frac{d}{d\mu^2} J_i = \sum_j P_{ji} \otimes J_j + \frac{1}{\mu^2} \Gamma \otimes T$$

Initial state e.g. nPDFs

Medium jet functions

see also Kang, FR, Vitev '16

- Modified evolution not considered here
- Could be constrained phenomenologically

# Inclusive jets in heavy-ion collisions

Qiu, FR, Sato, Zurita '19

- Introduce medium modified jet function at the jet scale

$$J_c^{\text{med}}(z, p_T R, \mu_J) = W_c(z) \otimes J_c(z, p_T R, \mu_J)$$

$$W_c(z) = \epsilon_c \delta(1-z) + N_c z^{\alpha_c} (1-z)^{\beta_c}$$

- Momentum sum rule

$$\int_0^1 dz z J_c(z, p_T^c R, \mu) = 1$$

- Monte Carlo sampling approach

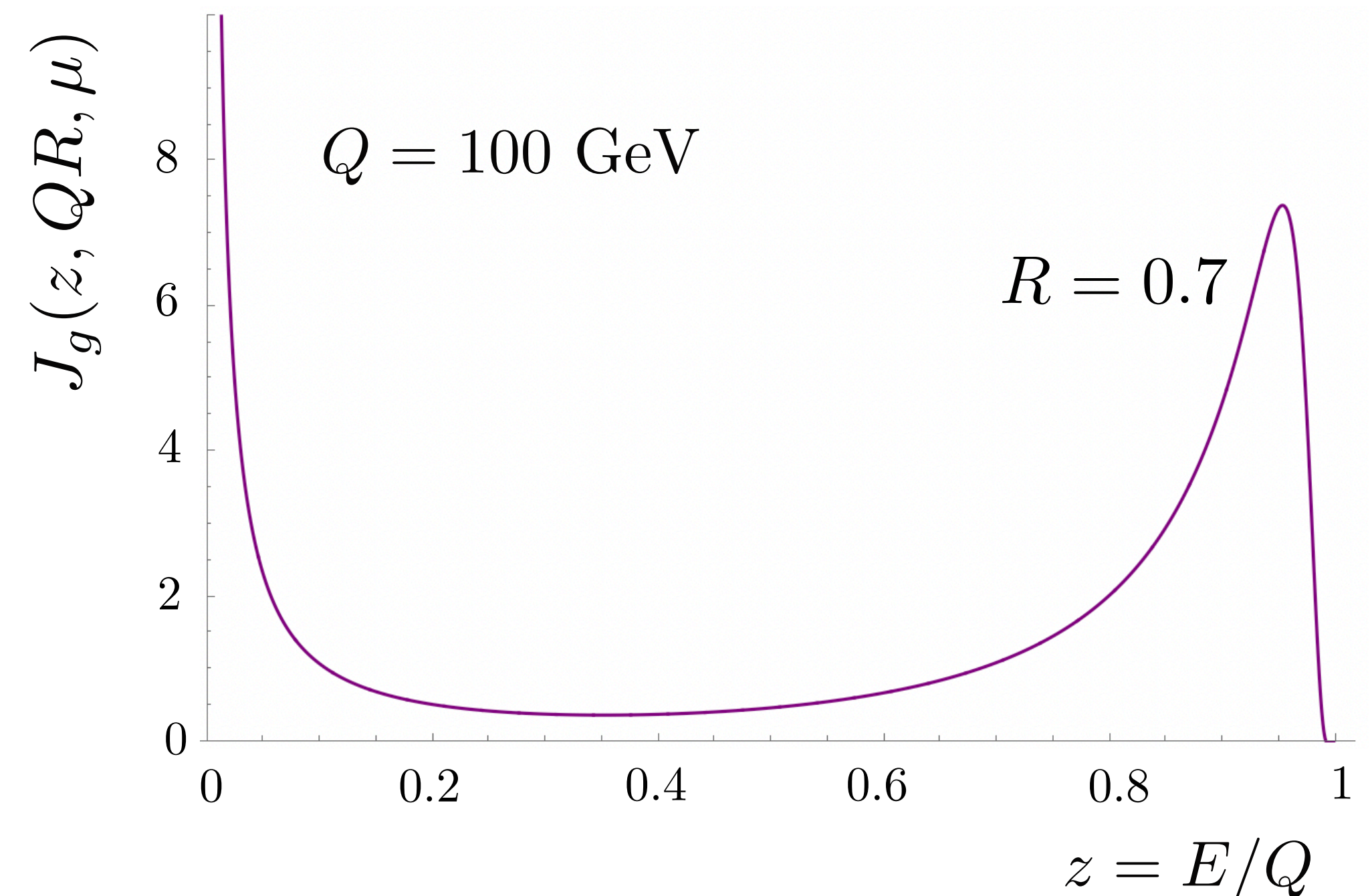
NNPDF '17, JAM '16

nPDFs

Eskola, Paakkinen, Paukkunen, Salgado '17, Kovarik et al. '16  
de Florian, Sassot, Zurita, Stratmann '12

nFFs

Sassot, Stratmann, Zurita '10



# Inclusive jets in heavy-ion collisions

Qiu, FR, Sato, Zurita '19

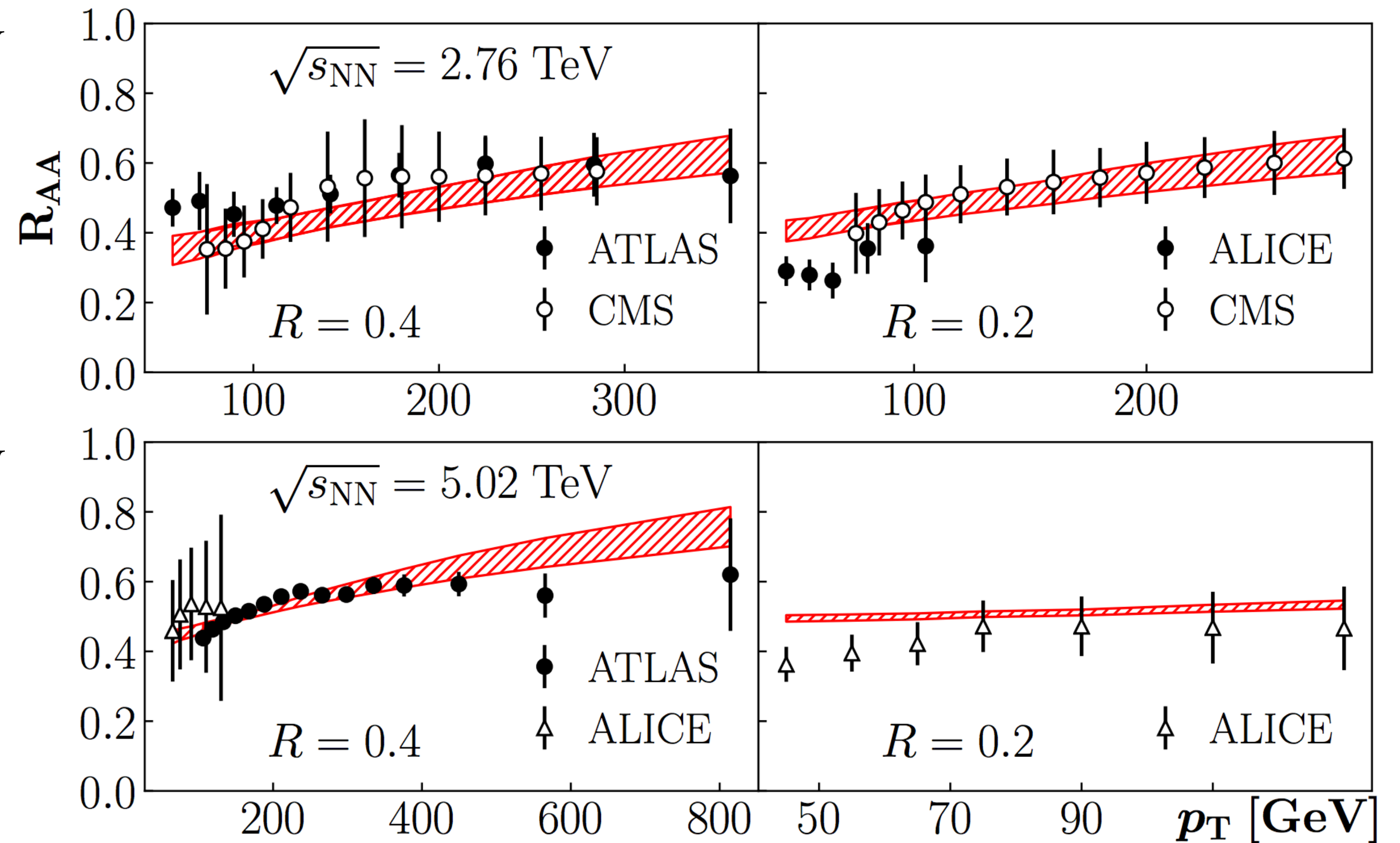
- Fit to data similar to PDFs and fragmentation functions

$$\sqrt{s_{NN}} = 2.76 \text{ TeV}$$

$$\chi^2/\text{d.o.f.} = 1.1$$

$$\sqrt{s_{NN}} = 5.02 \text{ TeV}$$

$$\chi^2/\text{d.o.f.} = 1.7$$

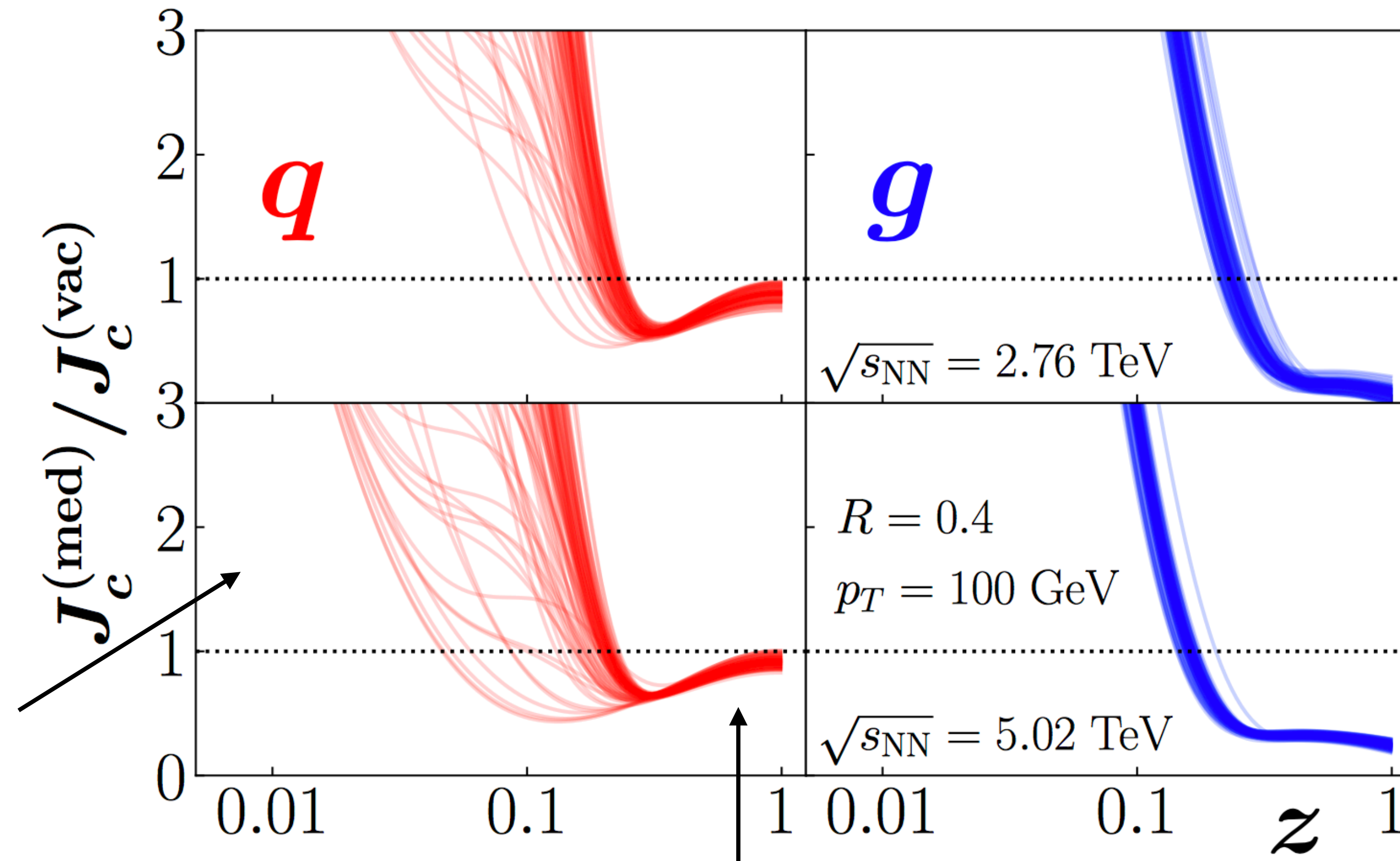


ALICE, PLB 746 (2015) 1  
 ATLAS, PRL 114 (2015) 072302  
 CMS, PRC 96 (2017) 015202  
 ALICE preliminary  
 ATLAS, PLB 790 (2019) 108

# In-medium jet functions

Qiu, FR, Sato, Zurita '19

- Suppression at large- $z$  compensated for by enhancement at small- $z$



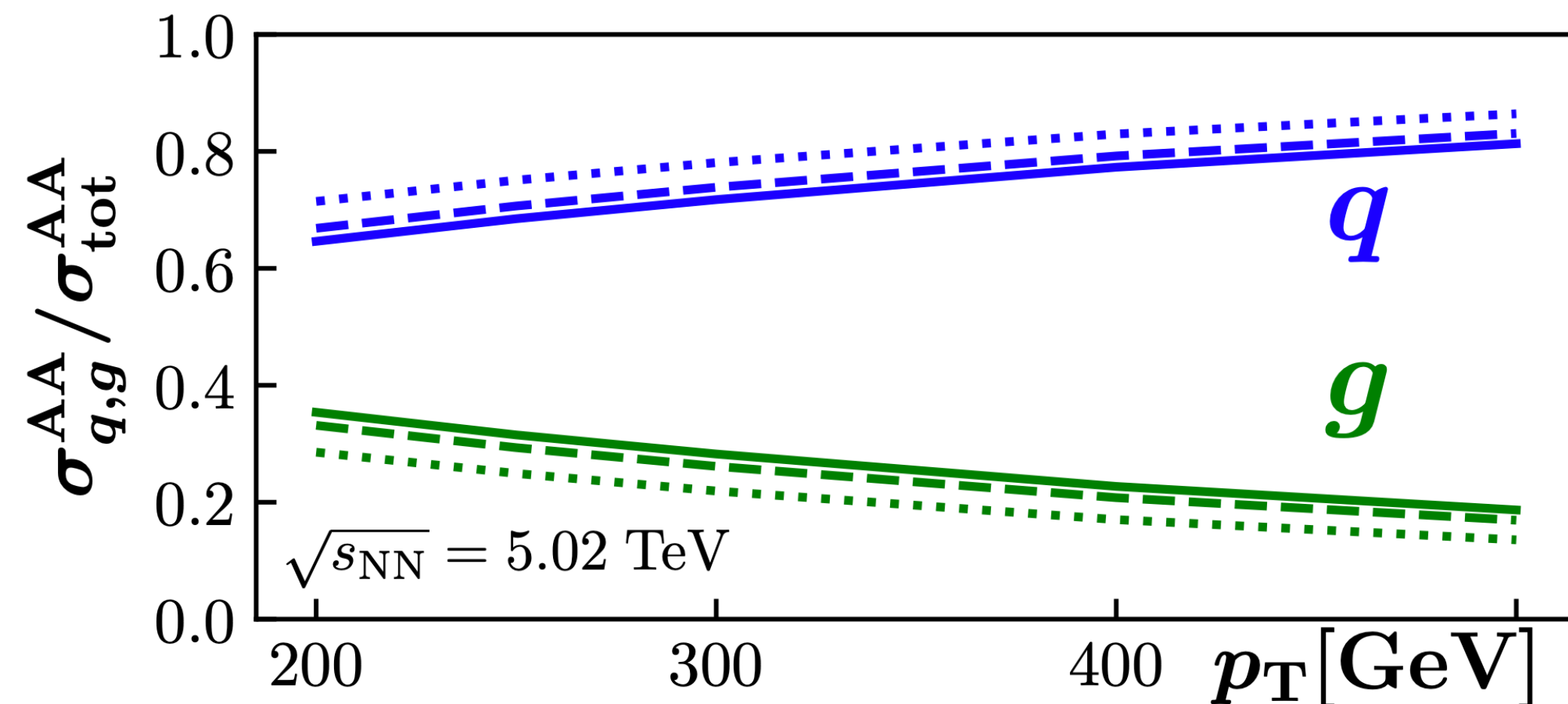
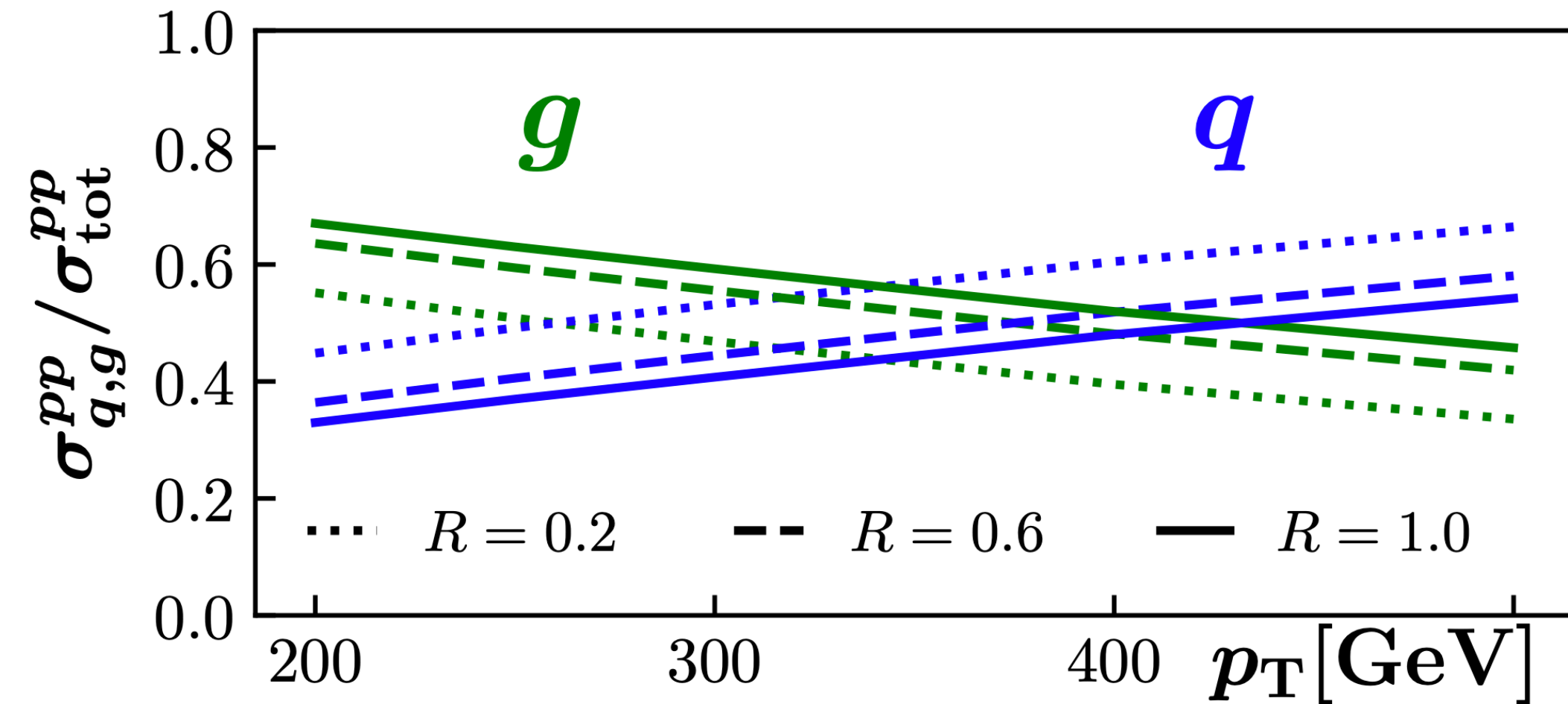
Small- $z$  region generally less constrained

Potentially requires threshold resummation for  $z \rightarrow 1$

# In-medium quark/gluon fractions

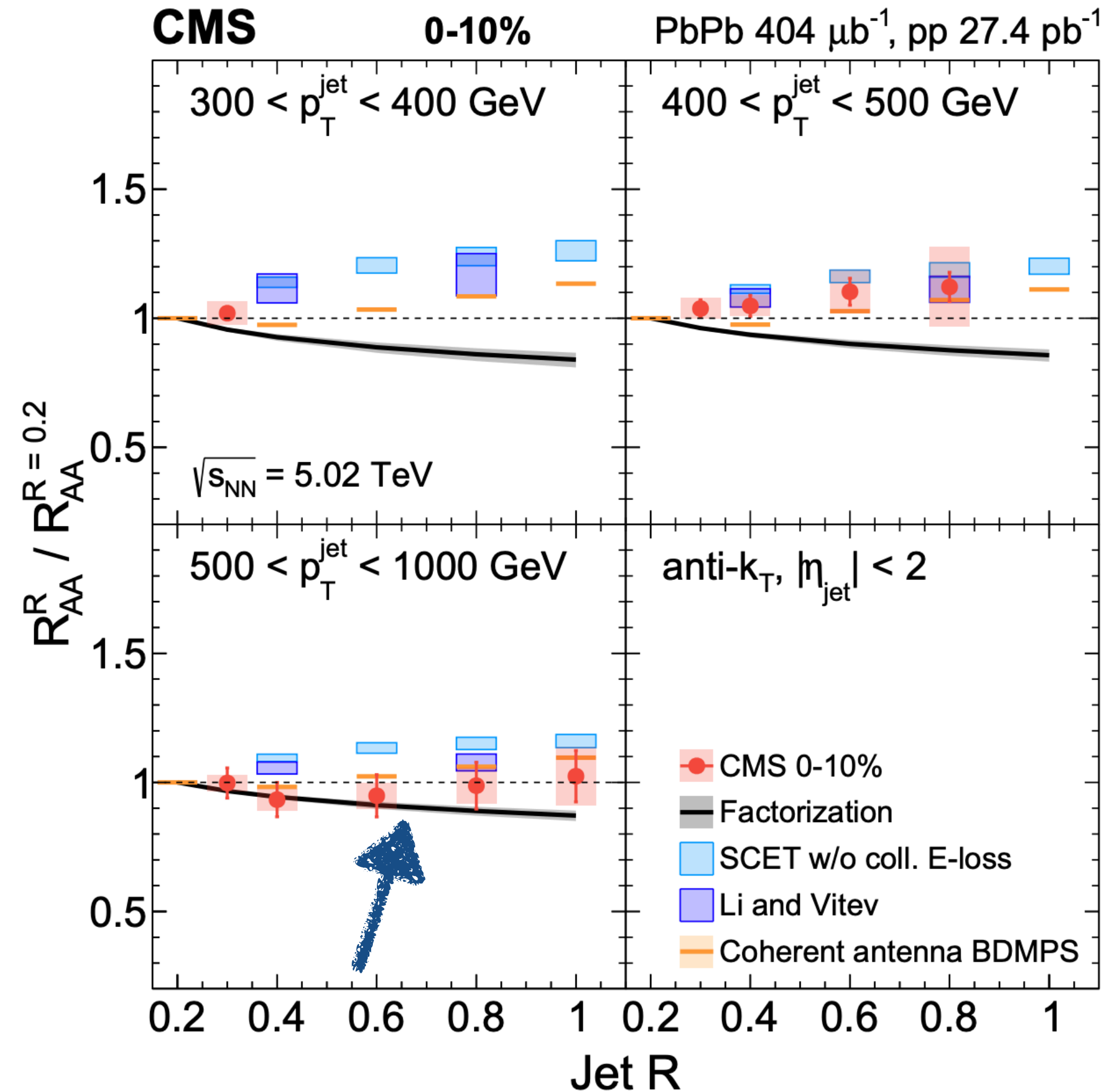
- Quark/gluon fractions defined at leading power in  $R^2$
- Significant shift toward quark jets in the medium
- Should be the same for all JSS observables measured on an inclusive jet sample

$$f_q J_q(\theta_g) + f_g J_g(\theta_g)$$



# Inclusive jet $R_{AA}$ - radius dependence

- CMS measurement
- Hadron  $R_{AA}$  for  $R \rightarrow 0$
- Could be included in an updated fit

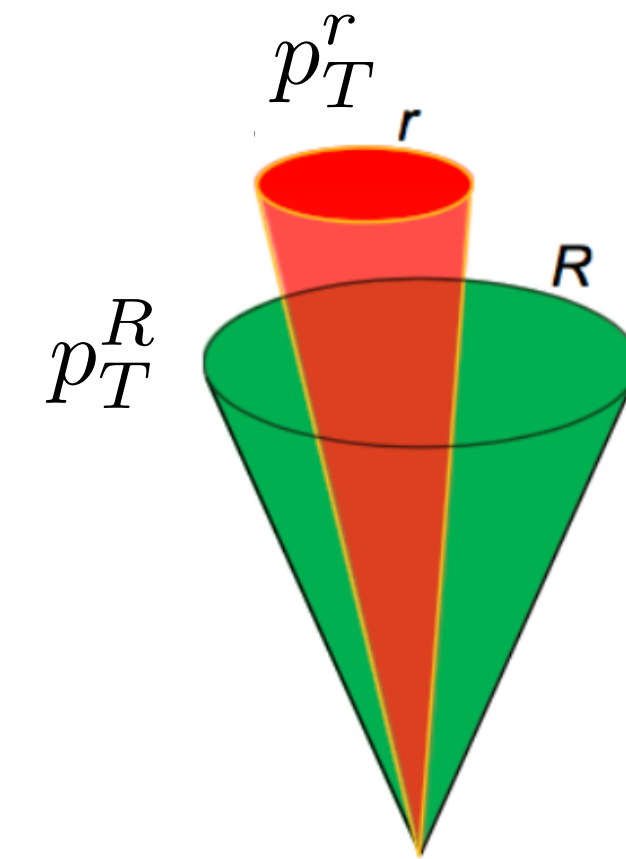
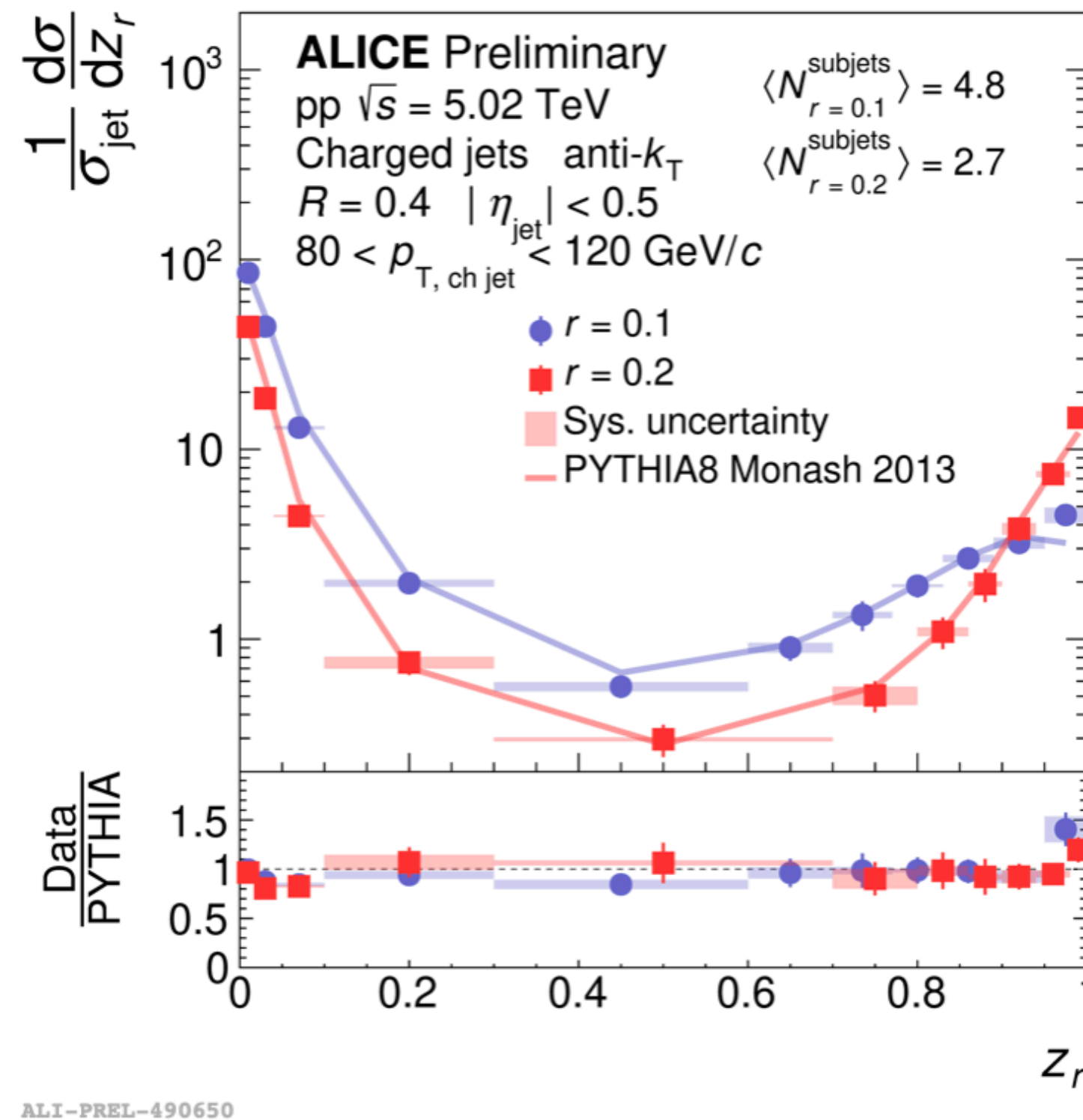


CMS, JHEP 05 (2021) 284



# Applications to jet substructure

- Leading & inclusive subjets in pp



$$z_r = p_T^r / p_T^R$$

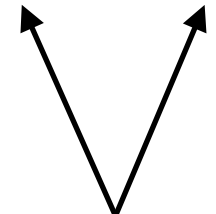
<https://alice-figure.web.cern.ch/node/19990>

Figures from J. Mulligan, LHCP '21

see Dai, Kim, Leibovich '16  
 Kang, FR, Waalewijn '17  
 Neill, FR, Sato '21

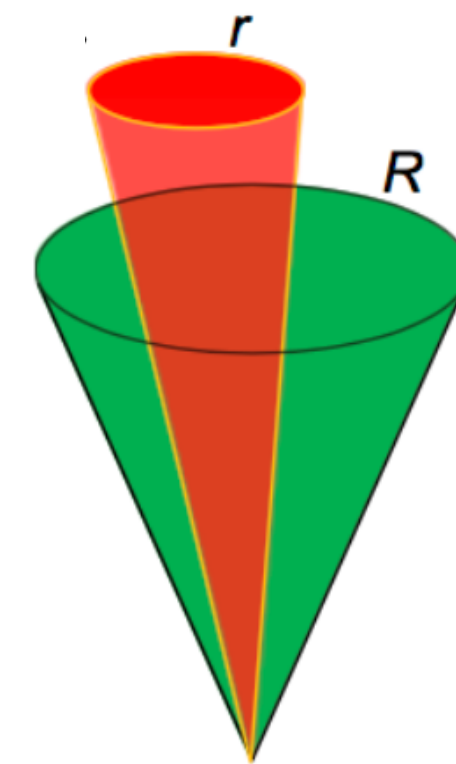
# Applications to jet substructure

- Subjet modification in AA

$$\frac{d\sigma}{dp_T d\eta dz_r} \sim \sum_{abcd} f_a \otimes f_b \otimes H_{abc} \otimes J_{cd}^{\text{med}} \times J_d^{\text{med}}(z_r)$$


- Extracted from inclusive jet data alone
- Test of universality

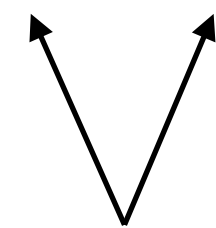
$$z_r = p_T^r / p_T^R$$



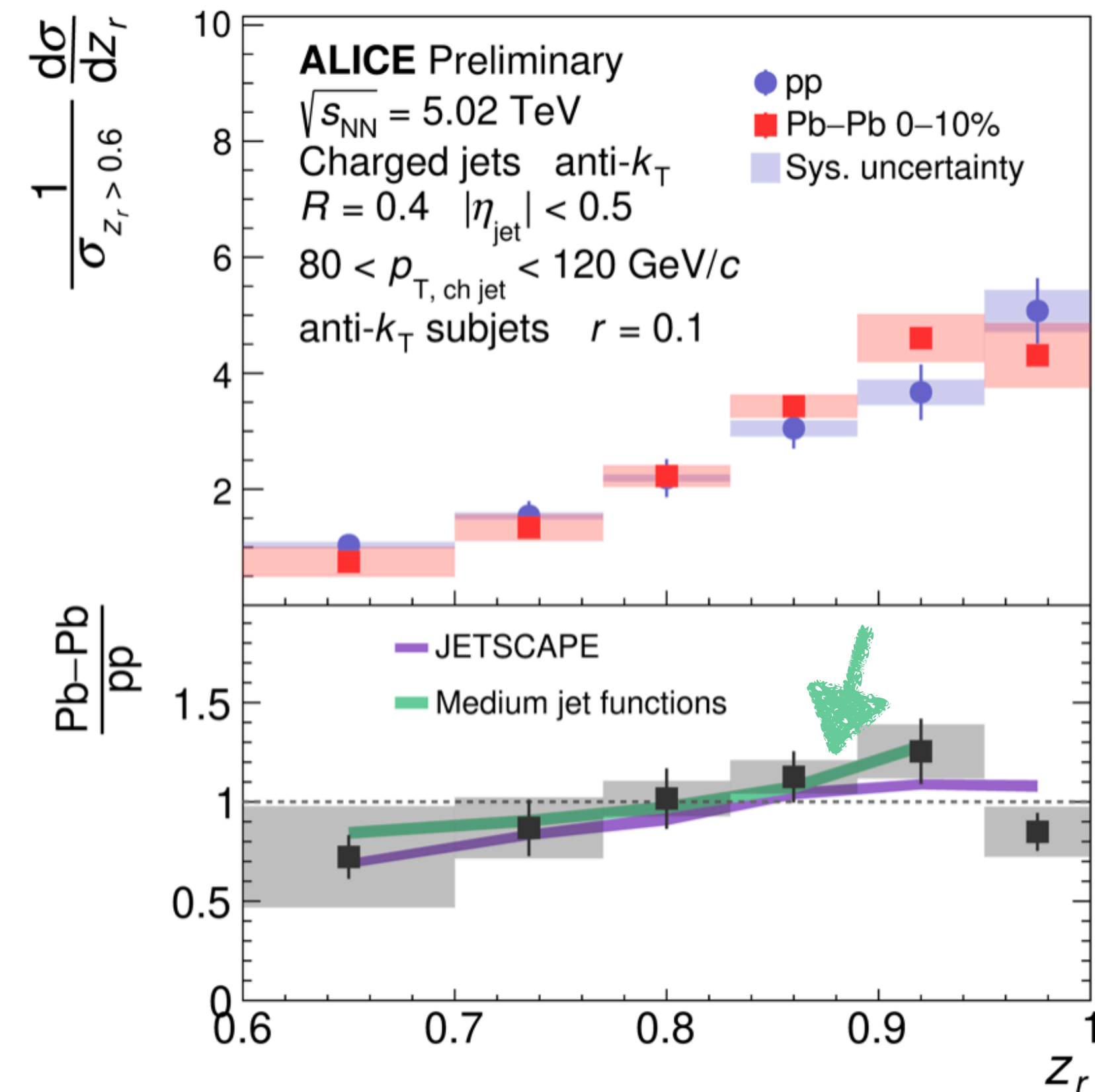
# Applications to jet substructure

- Subjet modification in AA

$$\frac{d\sigma}{dp_T d\eta dz_r} \sim \sum_{abcd} f_a \otimes f_b \otimes H_{abc} \otimes J_{cd}^{\text{med}} \times J_d^{\text{med}}(z_r)$$



- Extracted from inclusive jet data alone
- Test of universality



ALI-PREL-490655

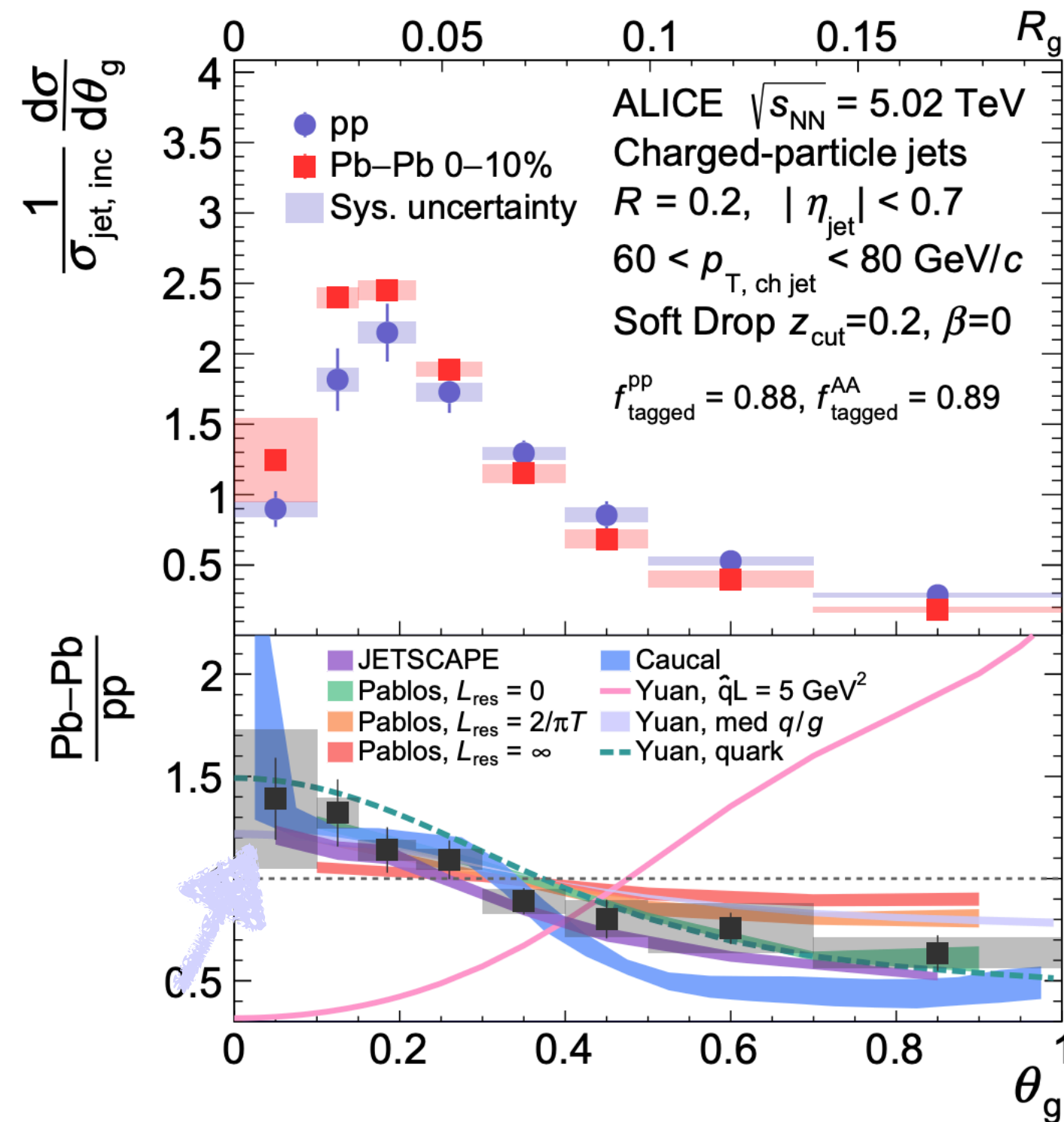
<https://alice-figure.web.cern.ch/node/19990>

Figure from J. Mulligan, LHCP `21

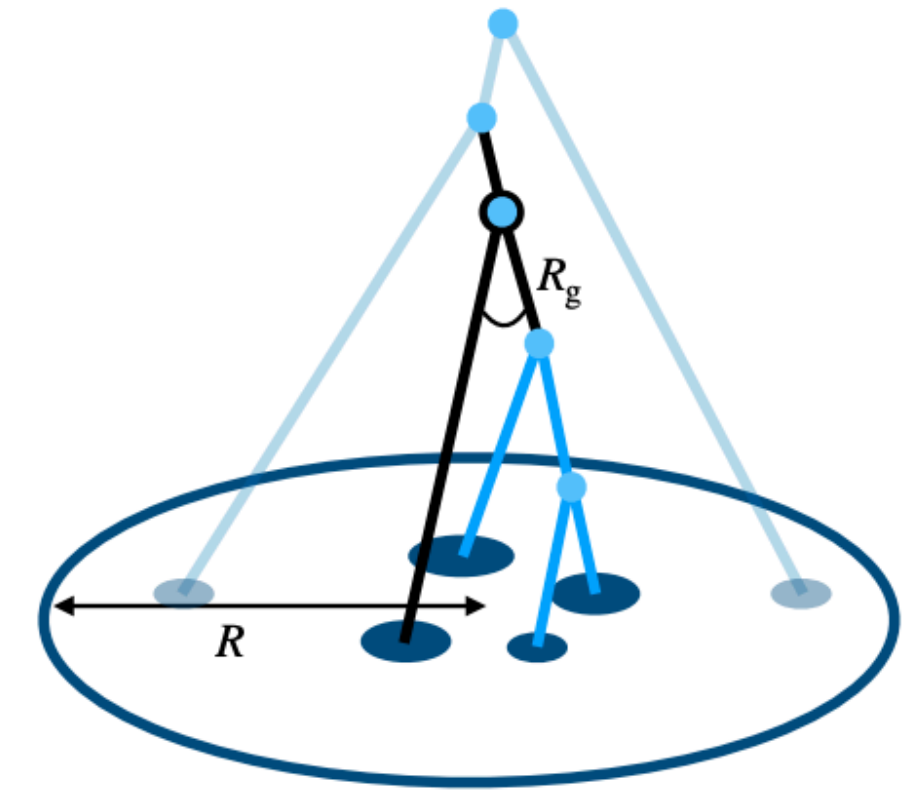
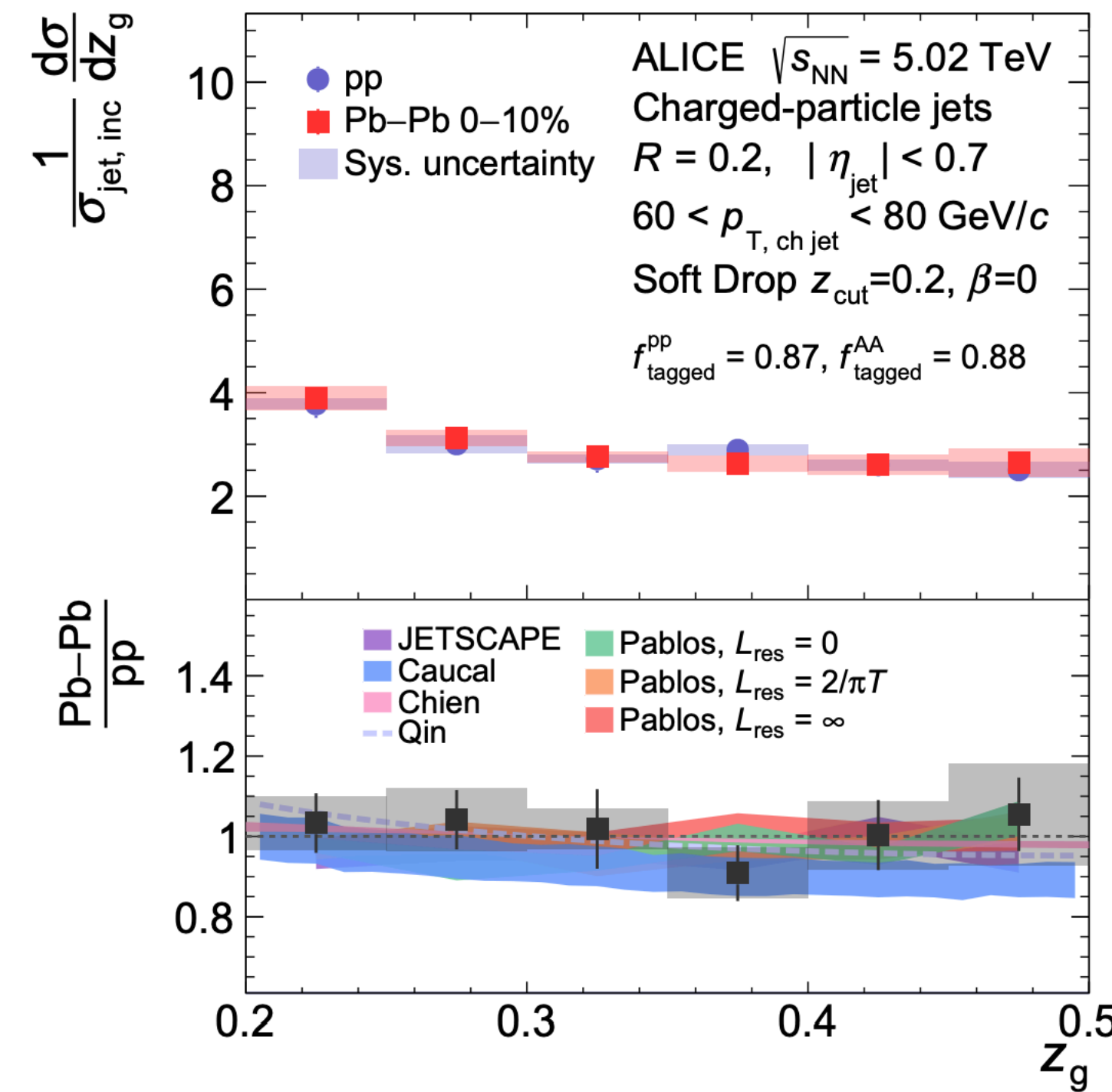
# Applications to jet substructure

- Groomed radius  $R_g$ , medium jet functions and  $p_T$  broadening

- Momentum sharing fraction  $z_g$ , no sensitivity to medium jet functions



ALICE, 2107.12984



Factorization

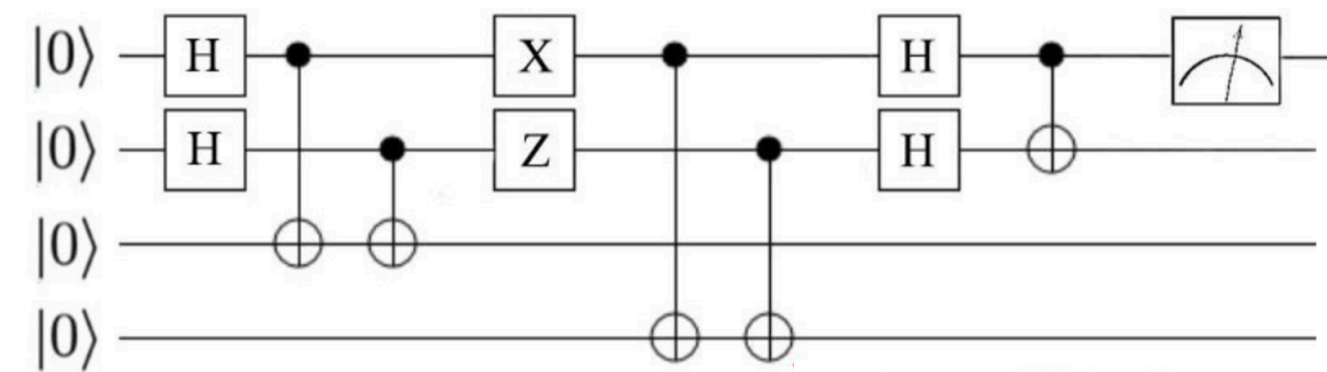
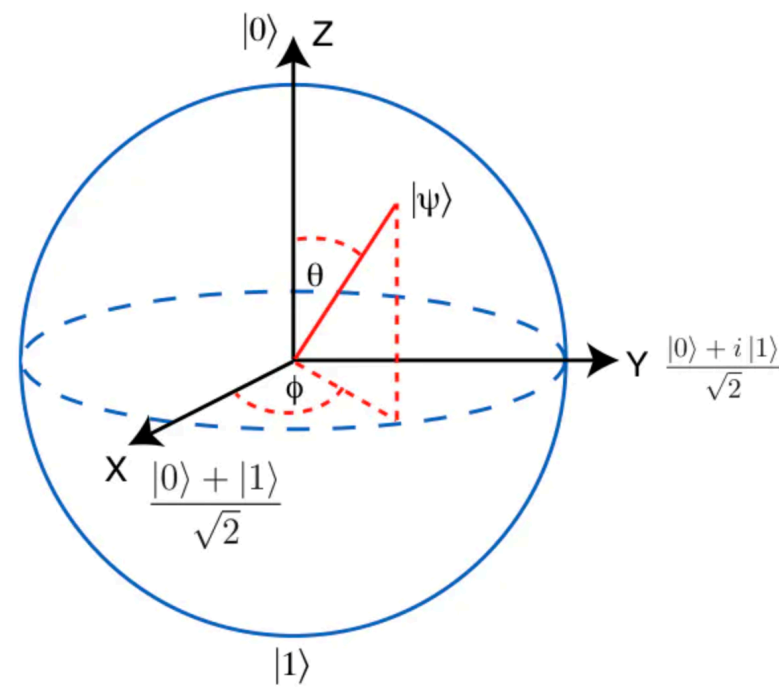
$$f_q J_q(\theta_g) + f_g J_g(\theta_g)$$

# Outline

- Introduction
- QCD factorization in heavy-ion collisions
- Quantum simulations of open quantum systems
- Conclusions

# Quantum computing

- Universal gate set: single-qubit rotations and CNOT



IBM Q

rigetti

Google

IONQ

Honeywell

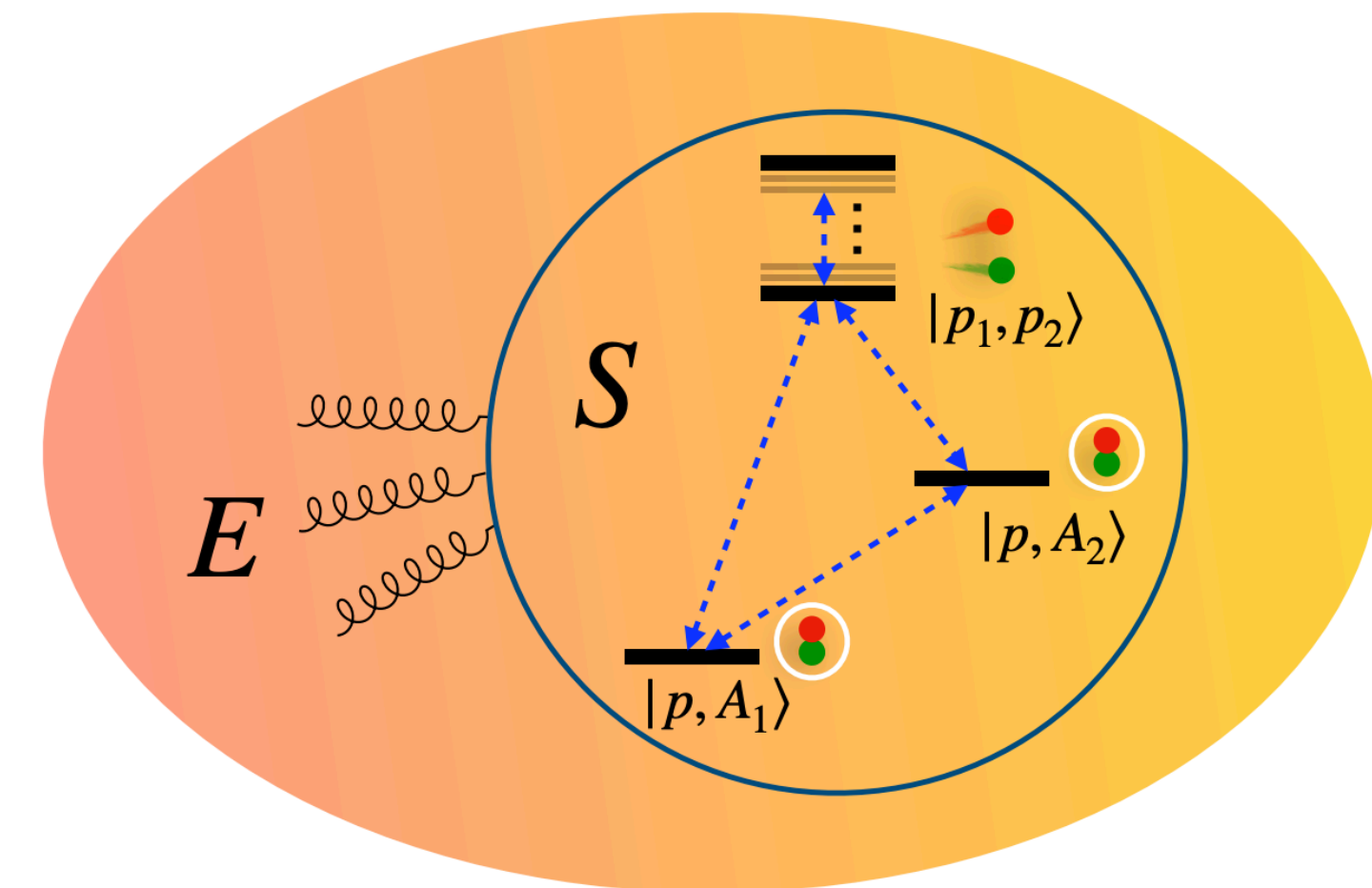
Microsoft

...

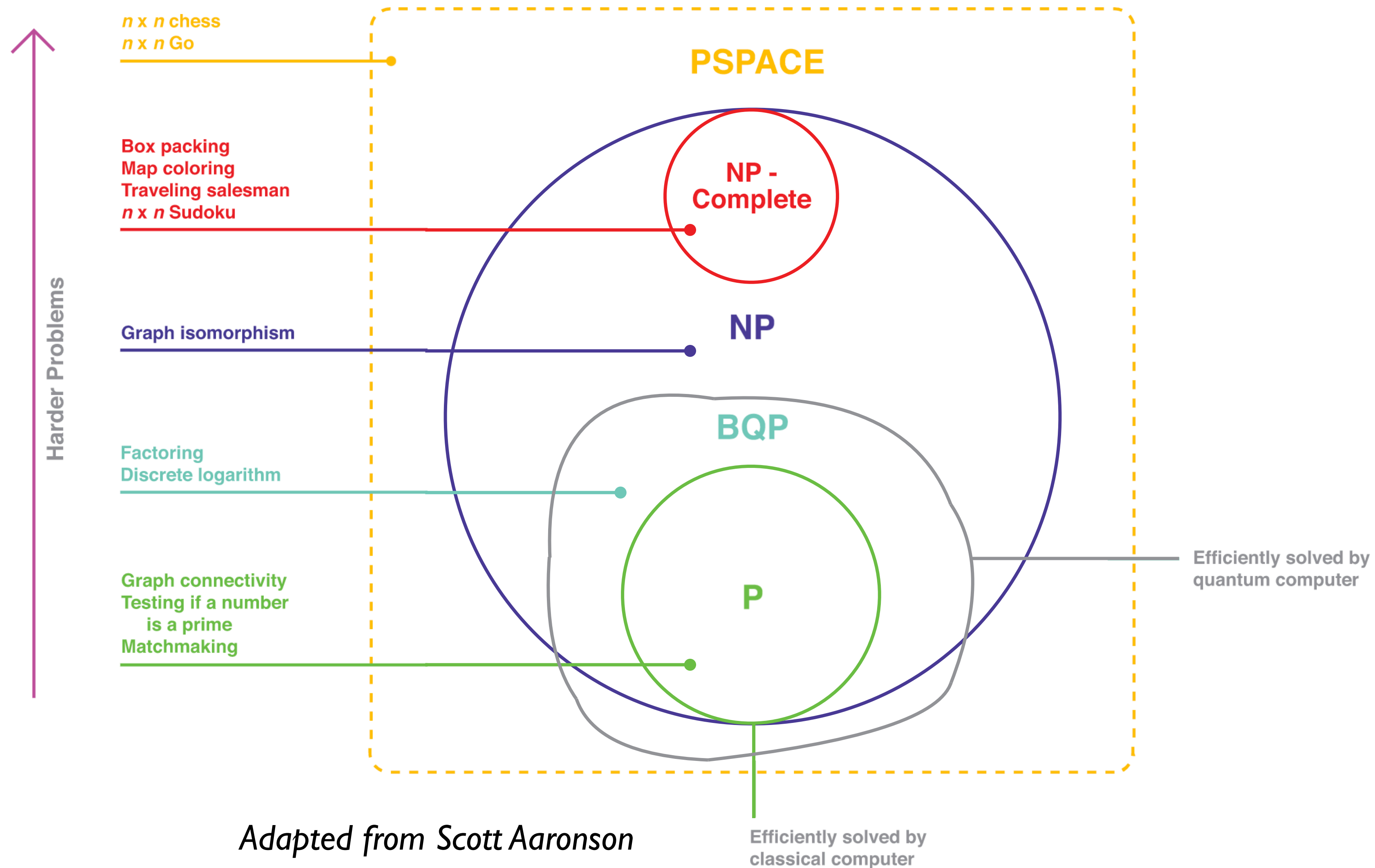
- Simulation of open quantum systems
- Extension of 2-level system

*see talk by Bert de Jong*

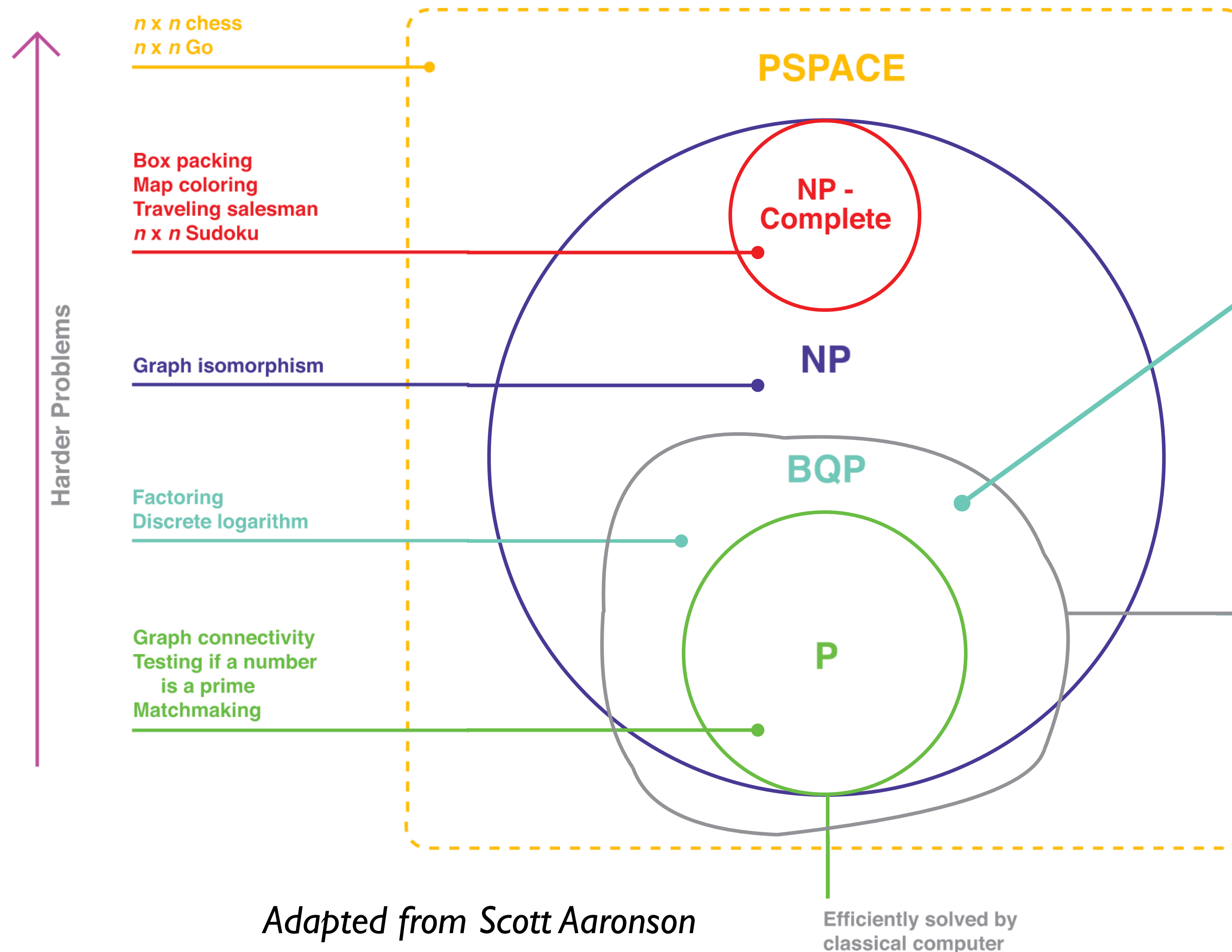
*See also e.g. Cohen, Lamm, Lawrence, Yamauchi '21, Barata, Salgado '21*



# Computational complexity



# Computational complexity



- Standard Model/QCD?

- Scalar field theory

*Jordan, Lee, Preskill '10-'14*

$$|\langle X | U(t, t_0) | AA \rangle|^2$$

Significant resources at high energies

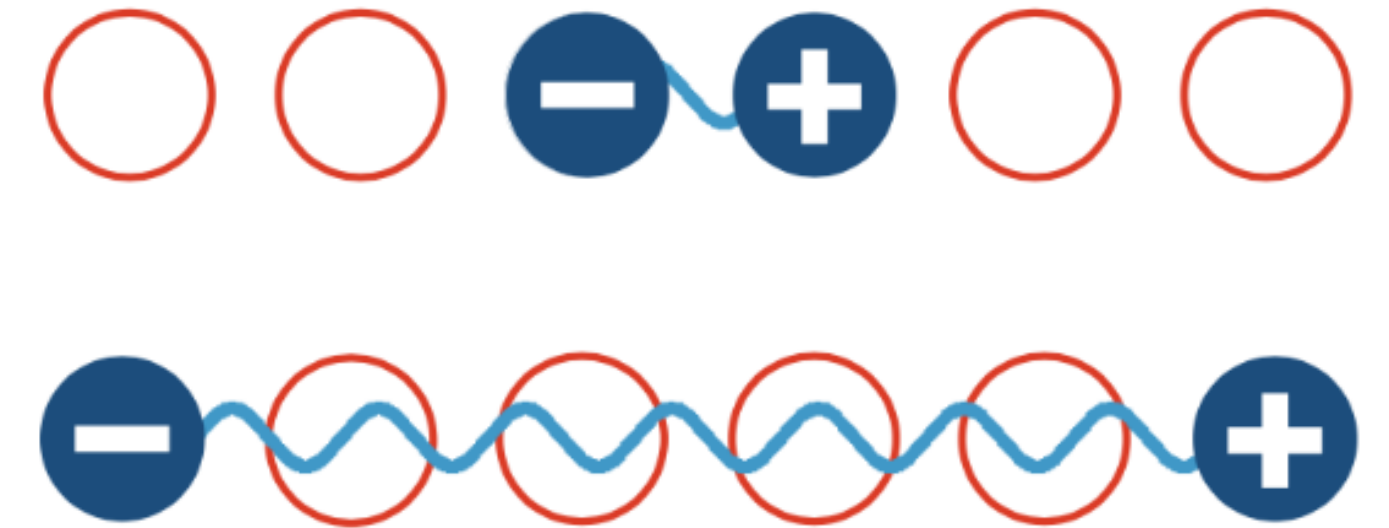
Focus on isolated phase space, jets, and low energy



# Schwinger model

- 1+1 dimensional version of QED *Schwinger '62*
- Simplest field theory with fermions and a U(1) gauge field
- Spontaneous chiral symmetry breaking
- Confining potential  $\sim r$
- Model for hadronization & string breaking in QCD e.g. Pythia
- Anomalous soft photon production

*Loshaj, Kharzeev '13*



$$\mathcal{L} = \bar{\psi}(i\not{D} - m)\psi - \frac{1}{4}F^{\mu\nu}F_{\mu\nu}$$

# Hamiltonian of the Schwinger model

Kogut, Susskind '70s

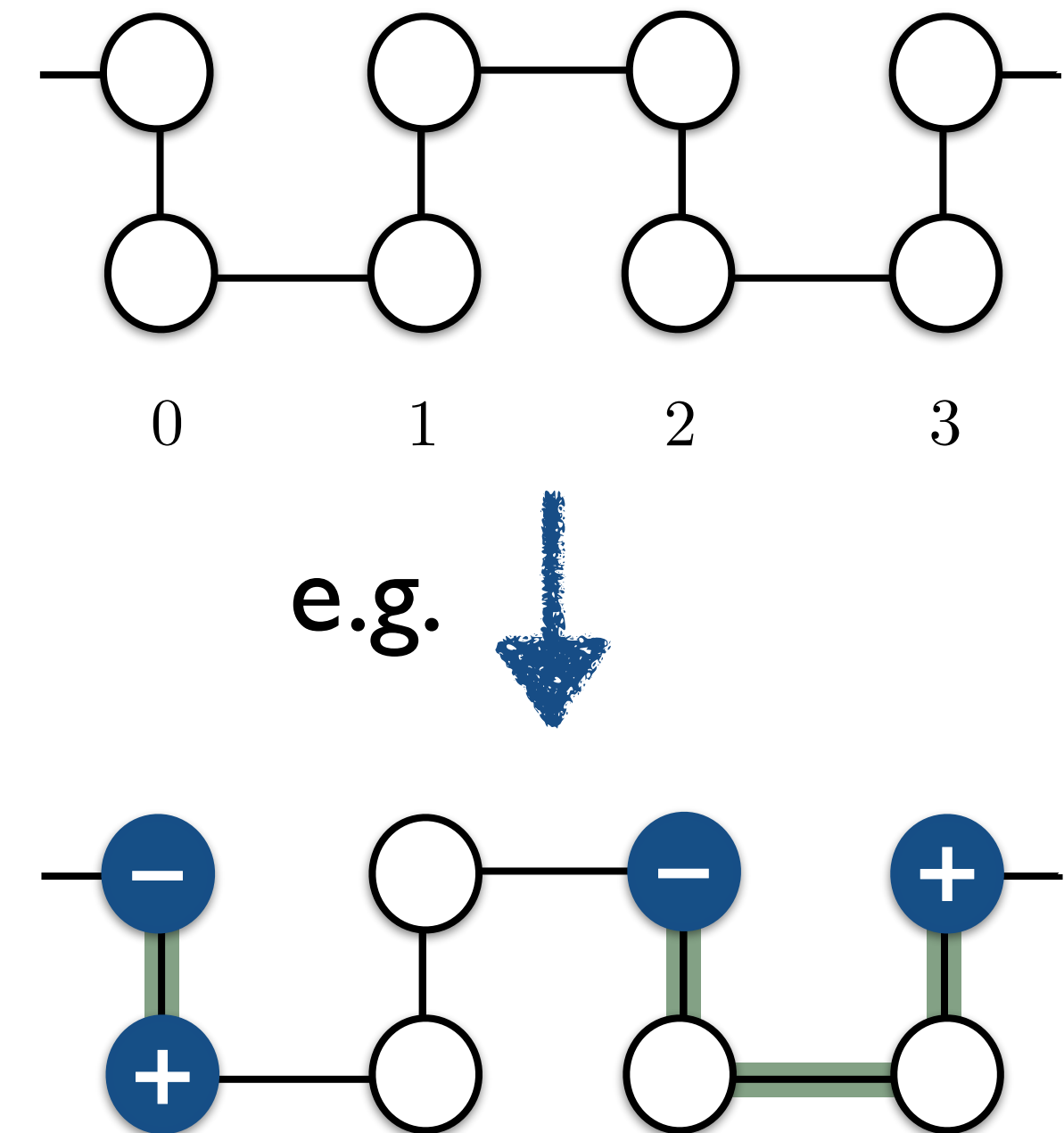
- Time continuous, 1-dimensional spatial lattice  $x = na$
- Continuum limit  $a \rightarrow 0$

$$H_S = \frac{1}{2a} \sum_{n=0}^{N_f-1} (\sigma^+(n) L_n^- \sigma^-(n+1) + \sigma^+(n+1) L_n^+ \sigma^-(n))$$

$$+ \sum_{n=0}^{N_f-1} \left( \frac{ae^2}{2} \ell_n^2 + m(-1)^n \frac{\sigma_z(n) + 1}{2} \right)$$

- Study real-time evolution

$$|\psi(t)\rangle = U|\psi(0)\rangle = e^{-iH_S t} |\psi(0)\rangle$$



# Hamiltonian of the Schwinger model

Kogut, Susskind '70s

- Time continuous, 1-dimensional spatial lattice  $x = na$
- Continuum limit  $a \rightarrow 0$

$$H_S = \frac{1}{2a} \sum_{n=0}^{N_f-1} (\sigma^+(n) L_n^- \sigma^-(n+1) + \sigma^+(n+1) L_n^+ \sigma^-(n))$$

$$+ \sum_{n=0}^{N_f-1} \left( \frac{ae^2}{2} \ell_n^2 + m(-1)^n \frac{\sigma_z(n) + 1}{2} \right)$$

Different constraints e.g. zero momentum  $\mathbf{k} = 0$ ,  $N = 4$

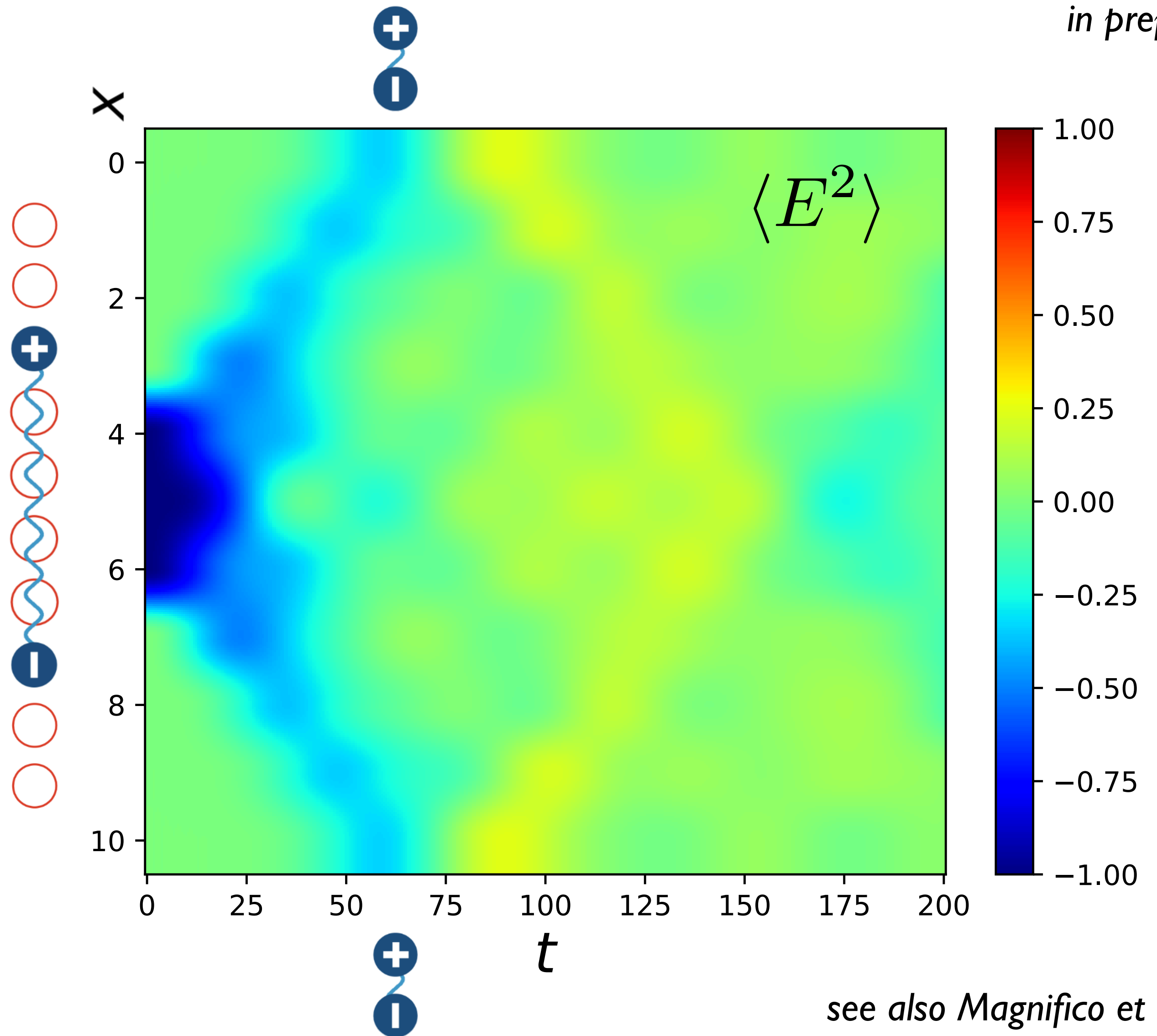
Savage et al. '18



$$H_S^{\mathbf{k}=0,+} = \begin{pmatrix} -4m & \frac{\sqrt{2}}{a} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ \frac{\sqrt{2}}{a} & \frac{ae^2}{2} - 2m & \frac{1}{a} & \frac{1}{\sqrt{2a}} & \frac{1}{\sqrt{2a}} & \frac{1}{\sqrt{2a}} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{1}{a} & ae^2 & 0 & 0 & 0 & \frac{1}{2a} & \frac{1}{a} & \frac{1}{2a} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{1}{\sqrt{2a}} & 0 & ae^2 & 0 & 0 & 0 & 0 & \frac{1}{\sqrt{2a}} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & \frac{1}{\sqrt{2a}} & 0 & 0 & ae^2 & 0 & 0 & \frac{1}{\sqrt{2a}} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & \frac{1}{2a} & 0 & 0 & 0 & \frac{3}{2}ae^2 - 2m & 0 & 0 & \frac{1}{2a} & \frac{1}{2a} & \frac{1}{2a} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & \frac{1}{a} & 0 & \frac{1}{\sqrt{2a}} & 0 & 0 & \frac{3}{2}ae^2 + 2m & 0 & 0 & \frac{1}{2a} & 0 & \frac{1}{2a} & \frac{1}{a} & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & \frac{1}{2a} & \frac{1}{\sqrt{2a}} & 0 & \frac{1}{\sqrt{2a}} & 0 & 0 & \frac{3}{2}ae^2 + 2m & 0 & \frac{1}{2a} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & \frac{1}{2a} & \frac{1}{2a} & 0 & 2ae^2 & 0 & 0 & 0 & \frac{1}{2a} & \frac{1}{2a} & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & \frac{1}{2a} & 0 & \frac{1}{2a} & 0 & 2ae^2 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & \frac{1}{2a} & \frac{1}{2a} & 0 & 0 & 0 & 2ae^2 & 0 & \frac{1}{2a} & \frac{1}{2a} & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & \frac{1}{a} & 0 & 0 & 0 & 0 & 2ae^2 + 4m & 0 & \frac{1}{a} & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & \frac{1}{2a} & 0 & \frac{1}{2a} & 0 & \frac{5}{2}ae^2 - 2m & 0 & \frac{1}{2a} & \frac{1}{a} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & \frac{1}{a} & \frac{5}{2}ae^2 + 2m & \frac{1}{a} & \frac{1}{\sqrt{2a}} & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & \frac{1}{a} & 3ae^2 & 0 & \frac{1}{a} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & \frac{1}{\sqrt{2a}} & 0 & 3ae^2 & \frac{1}{\sqrt{2a}} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & \frac{1}{a} & \frac{1}{\sqrt{2a}} & \frac{7}{2}ae^2 - 2m & \frac{1}{a} & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & \frac{1}{a} & 4ae^2 - 4m & 0 & 0 \end{pmatrix}$$

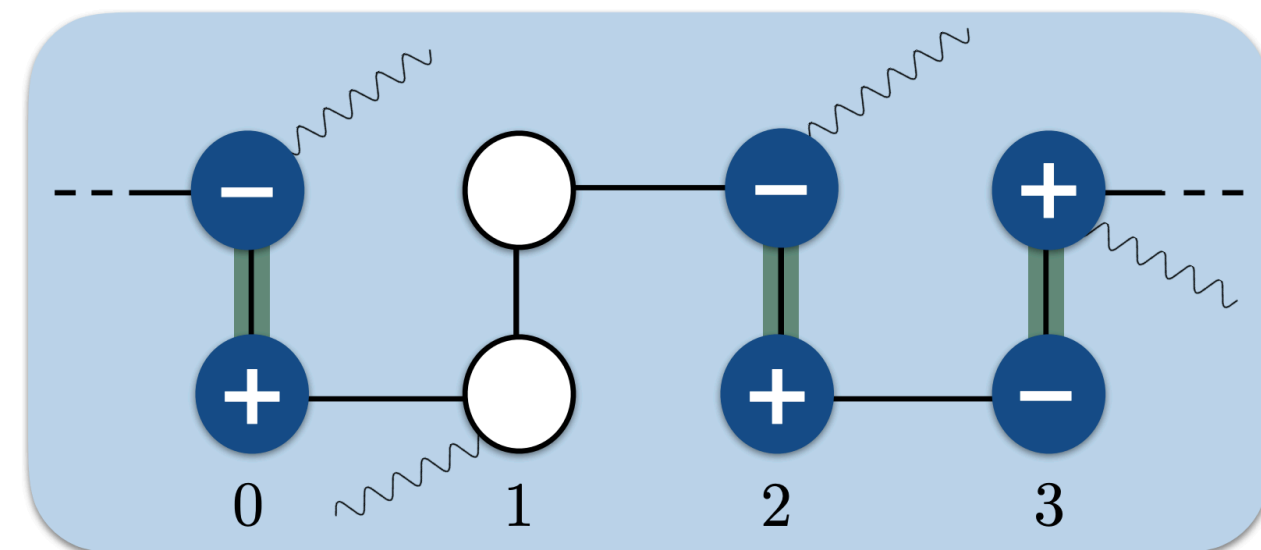
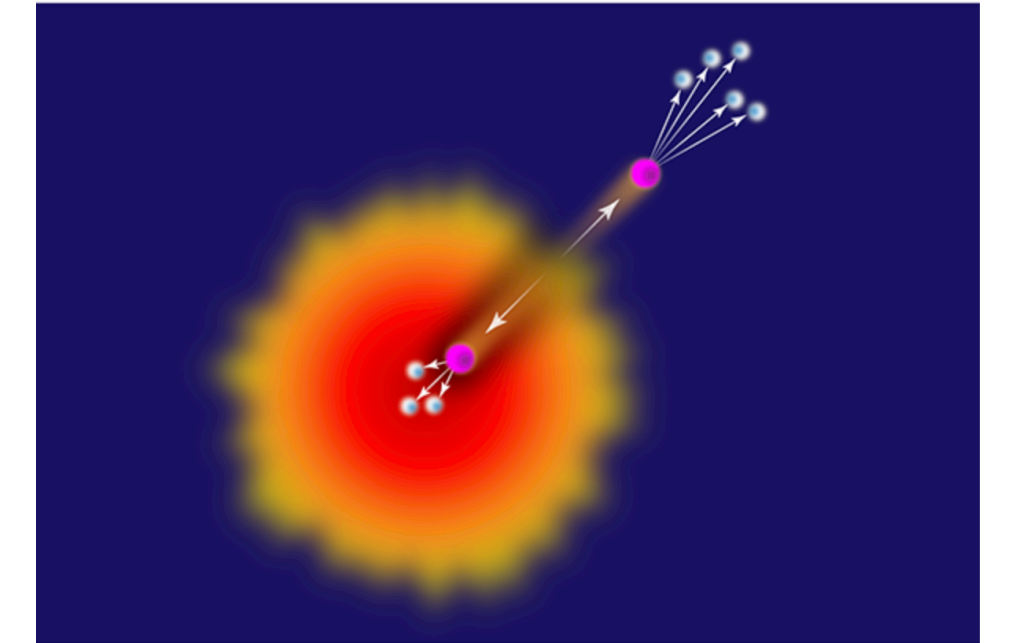
# The string-breaking mechanism

- Model of the hadronization
- Real-time evolution
- Vacuum evolution
- Study as an OQS *in progress*



# Open quantum systems

- Couple system to a thermal environment
- Schwinger model + thermal scalar field theory
- Yukawa-type interaction
- Non-equilibrium dynamics
- Eventually approximates thermalization



Jong, Lee, Mulligan, Ploskon, FR, Yao `21

$$H = H_S + H_E + H_I \quad \text{where}$$

$$H_E = \int dx \left[ \frac{1}{2} \Pi^2 + \frac{1}{2} (\nabla \phi)^2 + \frac{1}{2} m_\phi^2 \phi^2 + \frac{1}{3!} g \phi^3 \right]$$

$$H_I = \lambda \int dx \phi(x) \bar{\psi}(x) \psi(x) = \int dx O_E(x) O_S(x)$$

$$\text{where } O_E(x) = \lambda \phi(x)$$

$$O_S(x) = \bar{\psi}(x) \psi(x)$$

# Open quantum systems

- Time evolve the density matrix - von Neumann equation

*see talks by Yukinao Akamatsu,  
Nora Brambilla, Michael Strickland*

$$\rho = \sum_n p_n |\psi_n\rangle \langle \psi_n| \quad \frac{d\rho(t)}{dt} = -i[H, \rho(t)]$$

- Trace out environmental degrees of freedom

$$\rho_S^{(\text{int})}(t) = \text{Tr}_E(\rho^{(\text{int})}(t))$$

- Assume environment is in thermal equilibrium

$$\rho_E^{(\text{int})}(t) = \rho_E = \frac{e^{-\beta H_E}}{\text{Tr}_E e^{-\beta H_E}}$$

- Can be formally solve as  $\rho_S^{(\text{int})}(t) = \text{Tr}_E(U(t)\rho^{(\text{int})}(0)U^\dagger(t))$

$$\text{with } U(t) = \mathcal{T} \exp\left(-i \int_0^t H_I^{(\text{int})}(t') dt'\right)$$

# Hamiltonian of the Schwinger model

Jong, Lee, Mulligan, Ploskon, FR, Yao '21

- Work in the Quantum Brownian Motion limit

$\tau_R \gg \tau_E \longrightarrow$  Markovian approximation

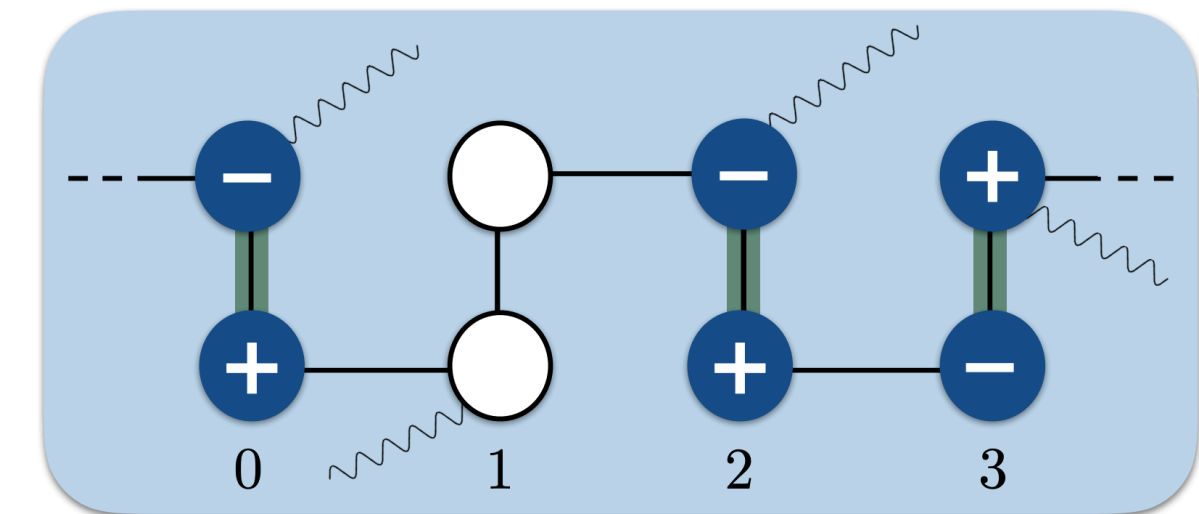
$\tau_S \gg \tau_E \longrightarrow$  Valid if  $T \gg H_S$



- Lindblad equation for  $k = 0$

$$\frac{d\rho_S(t)}{dt} = -i[H_S, \rho_S(t)] + L\rho_S(t)L^\dagger - \frac{1}{2}\{L^\dagger L, \rho_S(t)\}$$

with  $L = \sqrt{aN_f D(k_0 = 0, k = 0)} \left( O_S - \frac{1}{4T} [H_S, O_S] \right)$



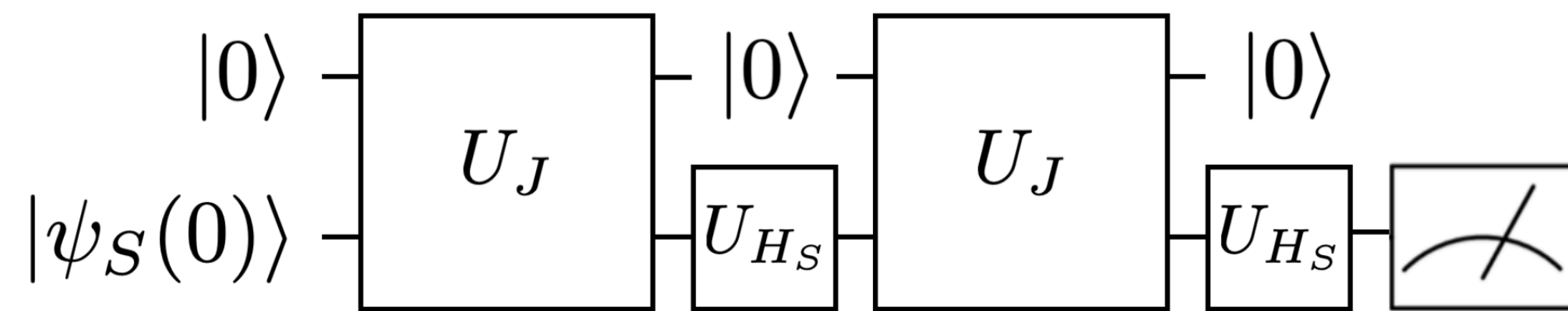
# Quantum algorithm for non-unitary evolution

Jong, Lee, Mulligan, Ploskon, FR, Yao '21

- Time evolve the density matrix instead of pure states

$$\frac{d\rho_S(t)}{dt} = -i[H_S, \rho_S(t)] + L\rho_S(t)L^\dagger - \frac{1}{2}\{L^\dagger L, \rho_S(t)\}$$

- Stinespring dilation theorem



where

$$U_J = e^{-iJ\sqrt{\Delta t}}$$

$$J = \begin{pmatrix} 0 & L^\dagger \\ L & 0 \end{pmatrix}$$

$$U_{H_S} = e^{-iH_S\sqrt{\Delta t}}$$

- Time-irreversible

- Evolve for  $N_{\text{cycle}}$  in small time steps  $\Delta t$

see also e.g. Cleve, Wang '16

Hu, Xia, Kais '20

Jong, Metcalf, Mulligan, Ploskon, FR, Yao '20

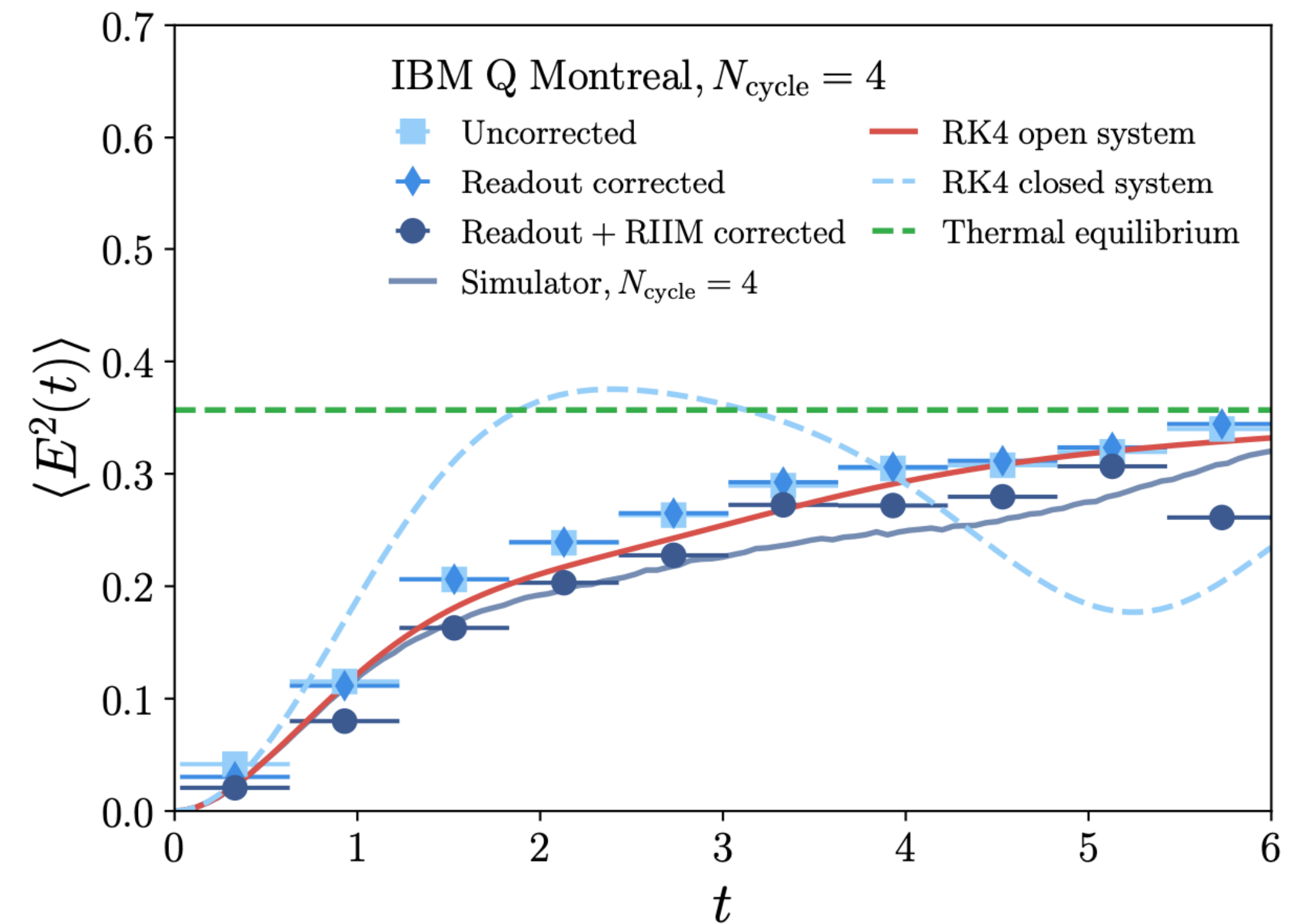
Metcalf, Kemper, Jong et al. '21



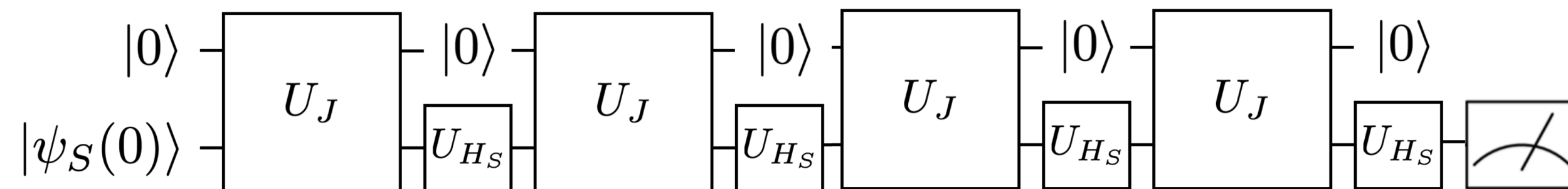
# Simulation on IBMQ

Jong, Lee, Mulligan, Ploskon, FR, Yao '21

- Vacuum fluctuations
- Readout and gate error mitigation  
*see talk by Bert de Jong*
- 6 qubits with up to 200 CNOT and 500 single-qubit gates
- Approximate preparation of thermal state from non-equilibrium dynamics



Electric field

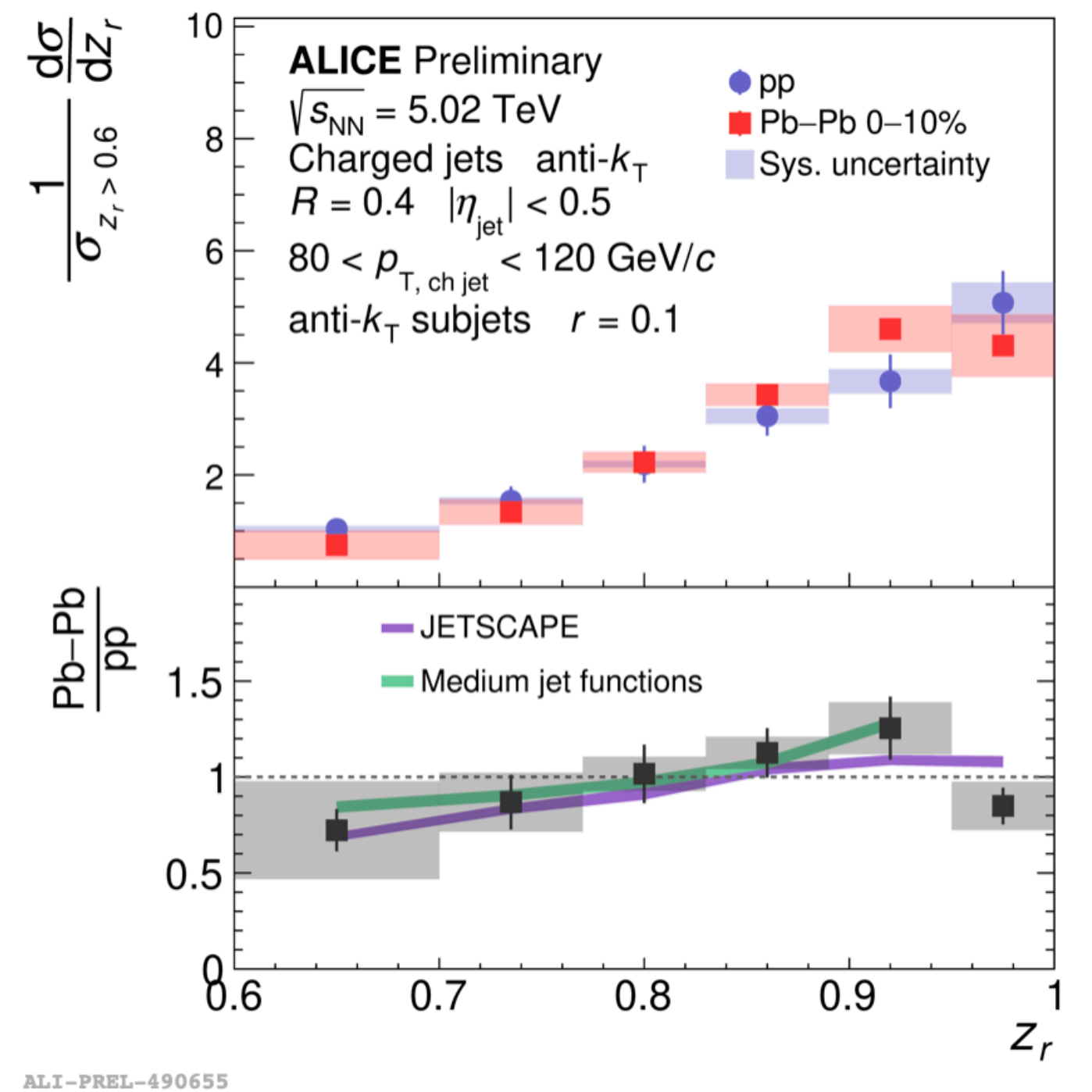
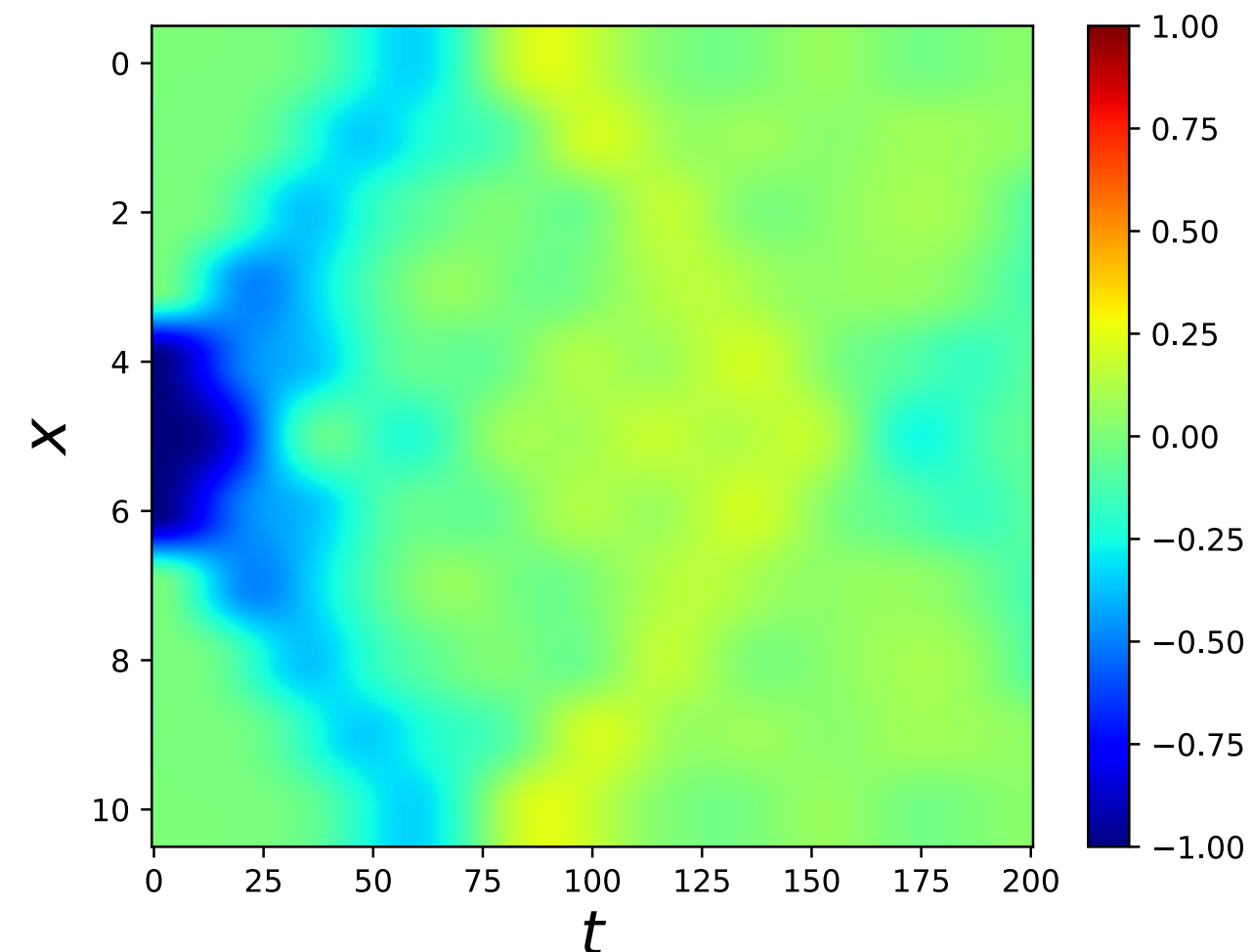


# Outline

- Introduction
- QCD factorization in heavy-ion collisions
- Quantum simulations of open quantum systems
- Conclusions

# Conclusions

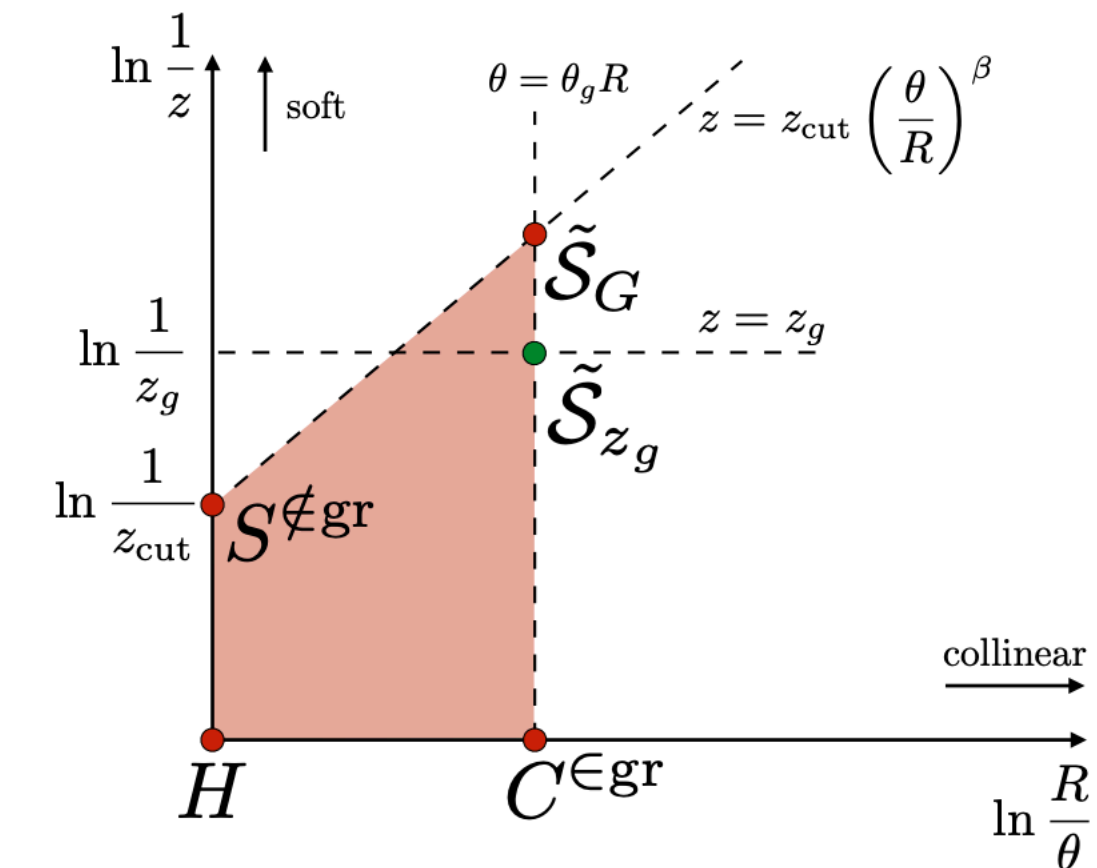
- Exploration of QCD factorization in heavy-ion collisions
- Medium jet functions
- Motivates further theory studies
- Quantum computing may allow for first principles simulations of QCD scattering
- Open quantum systems
- Development in early stages



# Factorization for $z_g$

Cal, Lee, FR, Waalewijn '21

$$\frac{d\sigma}{dp_T d\eta dz_g d\theta_g} = \sum_i f_i(p_T, \eta, R, \mu) \times \tilde{\mathcal{G}}_i(z_g, \theta_g, p_T R, z_{\text{cut}}, \beta, \mu)$$



with

$$\tilde{\mathcal{G}}_i = \Theta(1/2 > z_g > z_{\text{cut}} \theta_g^\beta) \tilde{H}_i(p_T R, \mu) C_i^{\text{E-gr}}(\theta_g p_T R, \mu) \times S_i^{\text{not-gr}}(z_{\text{cut}} p_T R, \beta, \mu) \tilde{\mathcal{S}}_G(z_{\text{cut}} \theta_g^{1+\beta} p_T R, \beta, \mu) \times S_i^{\text{NG}}(z_{\text{cut}}) \left[ \frac{d}{dz_g} \frac{d}{d\theta_g} \tilde{\mathcal{S}}_{z_g}(z_g \theta_g p_T R, \mu) + \tilde{\mathcal{S}}_{i,1}^{\text{NG}}(z_g \theta_g, z_g) + \tilde{\mathcal{S}}_{i,2}^{\text{NG}}\left(z_g \theta_g, \frac{z_g}{z_{\text{cut}} \theta_g^\beta}\right) \right]$$

