# MITP Scientific Programme "Fundamental Parameters From Lattice QCD" – Summary –

G.M. von Hippel







Mainz Institute of Theoretical Physics Johannes Gutenberg-Universität Mainz

Mainz, August 31 - September 11, 2015

## Too many excellent talks to review



## Too many excellent talks to review



## Too many excellent talks to review



## Ariadne's thread

# CE Risk getting lost in detail

## Ariadne's thread



To avoid getting lost, follow a red thread

## Red thread #1: Systematic errors

- Big topic in many talks (explicitly or implicitly)
  - As statistics increase, precision is limited by systematics
- How to estimate?
  - Sources with controllable parameters (a,  $m_{\pi}$ , L)
    - Fits with or without priors
    - Variations of fit range or fit function
  - Sources without controllable parameters (*N<sub>f</sub>*, HQ action, ...)
    - Often not assessed
    - Can at most be guesstimated
  - Combined systematics
    - Error budgets now standard
    - Extended Frequentist's Method
    - May not necessarily add to 100%
  - Remain somewhat subjective

## Red thread #1: Systematic errors

- Big topic in many talks (explicitly or implicitly)
  - As statistics increase, precision is limited by systematics
- How to combine?
  - Important issue especially for FLAG, CKMfitter, PDG ....
  - Even more subjective than estimation
    - Does one believe the quoted errors?
    - What kind of thing is a systematic error?
  - Wide range of methods
    - Linear vs. Quadratic addition
    - Range method used by PDG, except for lattice [S. Bethke's Talk]
    - Rfitter method used by CKMfitter [J. Charles' Talk]
    - Weighted average using Schmelling's method used by FLAG [R. Horsley's Talk]
  - No consensus ...
    - ... no problem?

## Red thread #2: Isospin breaking

- Another recurring topic
- $\alpha_{\textit{rmQED}} \approx 1/137 \rightsquigarrow$  need QED beyond 1% level
- Strong isospin breaking from  $m_{
  m d}-m_{
  m u}$  of similar size
- Different proposals on the market:
  - QCD+QED simulations
  - reweighting methods
  - RM123 method [V. Lubicz's Talk]
- Significant effort required in any case
  - direct methods: implementation of Gauss law, new ensembles needed
  - Rome method: Bloch-Nordsieck treatment of IR divergences, four-point functions and higher needed [V. Lubicz's Talk]
- Cannot be avoided



#### [V. Lubicz's's Talk]

## Red thread #3: Disconnected diagrams

- Mentioned repeatedly, with different emphasis
- A leading source of systematic error in various contexts:
  - $(g-2)_{\mu}$  [T. Izubuchi's Talk]
  - running of electroweak couplings [G. Herdoíza's Talk]
  - direct CP violation [C. Kelly's Talk]
  - decays like  $D_s^+ 
    ightarrow \eta' \ell^+ \nu_\ell$  [S. Collins' Talk]
- Some interesting quantities are purely disconnected:
  - strangeness form factors of nucleon [J. Green's Talk]
- Many clever methods used
  - dilution, hierarchical probing
  - (generalized) HPE, TSM
- Still massive statistics needed to get reasonable signal
  - ... but at least we know how to do that

#### mixed representation: disconnected contribution

▶  $x_0 \rightarrow \infty$ 

 $\frac{G_{\text{disc}}^{(\ell+A_S),(\ell-s)}(X_0)}{G^{\rho\rho}(X_0)} \longrightarrow 1$ data 🛏 relative difference 0.06  $\Delta \Pi^{pZ}(Q^2)/\Pi^{pZ}(Q^2)$ 0.05  $G_{disc}/G^{pp}$ ан. Пары 0.04 0 10 0 6 10 0 20 $Q^2/GeV^2$ 

4% : conservative estimate for systematic error from neglecting disconnected contribution at  $Q^2 \sim 4 \text{ GeV}^2$ 

[V. Gülpers et al., lattice 2015]

[G. Herdoíza's Talk]

#### Technically challenging

Quark line diagrams for studying  $\eta$  and  $\eta'$ .



Disconnected diagrams which may give a large contribution due to the anomaly also due to sum over *l* = *u*, *d*, *s*.



Sensitivity to the topology of the gauge field configurations.

First step, determine the physical basis for  $\eta/\eta'$ .

#### [S. Collin's Talk]

## Red thread #4: Scale setting

- Not mentioned quite so often
- $\bullet$  Still likely to be relevant at the 1% level
- Different quantities have different strengths and weaknesses
  - $f_K$  statistically precise, but Z factors needed, isospin/QED?
  - $m_{\Omega}$  no Z factors needed, sss state, but noisy
  - $m_{\Upsilon(2S)} m_{\Upsilon(1S)}$  statistically precise, no Z factors needed, but with heavy-quark EFT uncertainties
  - $r_0$ ,  $r_1$ ,  $t_0$ ,  $w_0$  very precise, but not directly physical
- Impact on running of couplings
  - of same order as current statistical errors [G. Herdoíza's Talk]
- Will also need to be addressed

 $\Delta \alpha_{\text{QED}}^{\text{had}}(Q^2)$ : systematic effects

$$D(Q^2) = \frac{3\pi}{\alpha} \frac{d}{d \log(Q^2)} \Delta \alpha_{\text{QED}}^{\text{had}}(Q^2)$$



Padé [1,2] with O(a) lattice artefacts and quadratic form in  $M_{PS}^2$ 

#### [G. Herdoíza's Talk]

- Quantities that are ambiguous have a built-in limit on precision
- Quark masses
  - pole mass has renormalon ambiguity of  $\sim$  180 MeV [G. Bali's Talk]
  - masslessness of up quark scheme-dependent [M. Creutz's Talk]
- Are these therefore even precision quantities?

## Red thread #6: Coordination of Efforts

- An aim of this Scientific Programme
- Good news:
  - Lattice and phenomenology communities talk to each other
  - PDG now uses FLAG average for lattice [S. Bethke's Talk]
- Other than good news:
  - CKMfitter cannot use FLAG average [Discussion 31/08]
  - UTfit could not participate in averaging discussion
- Future directions:
  - Some kind of "Les Houches Accord" for lattice data?
  - Possible? Desirable? Necessary?
  - To some extent, FLAG's (★, ○, ■) system can be seen as a step in this direction

## Summary (of the Summary)

- Systematics are becoming dominant source of uncertainty in lattice QCD, especially for flavour quantities
- Treatment remains somewhat subjective, especially when averaging results from different sources
- At the 1% level, isospin breaking and scale setting issues must be tackled
- There are promising approaches to isospin breaking
- Disconnected diagrams require massive statistics
- Scale setting may need further effort

... for your participation!