Chiral Effective Field Theory and Nuclear Forces: overview and applications

Kai Hebeler Mainz, July 27, 2022

TALENT school @MITP: Effective field theories in light nuclei











The nuclear landscape:







since year ~2010

110

100

90

80

Ζ

open-shell nuclei: multi-reference IMSRG, Gorkov Greens function, Bogoliubov coupled cluster

polynomial scaling









The computation, handling and storage of **3N interactions** is one of the key limitations for state-of-the-art many-body calculations

110

100

90

80

Ζ



nuclear structure and reaction observables









- requires extreme amounts of computational resources
- currently limited to 1- or 2-nucleon systems
- current accuracy insufficient for precision nuclear structure

Quantum Chromodynamics



Quantum Chromodynamics



ab initio many-body frameworks

Faddeev, Quantum Monte Carlo, no-core shell model, coupled cluster ...



nuclear interactions and currents

Quantum Chromodynamics

nuclear structure and reaction observables

ab initio many-body frameworks

Faddeev, Quantum Monte Carlo, no-core shell model, coupled cluster ...



Nuclear effective degrees of freedom



- if a nucleus is probed at high energies, nucleon substructure is resolved
- at low energies, details are not resolved

Nuclear effective degrees of freedom



- if a nucleus is probed at high energies, nucleon substructure is resolved
- at low energies, details are not resolved
- replace fine structure by something simpler (compare multipole expansion)

effective field theory



Problem: Traditional "hard" NN interactions



- constructed to fit low-energy scattering data
- "hard" NN interactions contain repulsive core at small relative distance
- strong coupling between low and high-momentum components
 - \Rightarrow nuclear many-body problem non-perturbative, hard to solve!

Claim: Problems due to high resolution from interaction!

Problem: Traditional "hard" NN interactions



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- resolution of short-distance structures can obscure this information
- small details have nothing to do with long-wavelength information!



low-pass filter



- long-wavelength information is preserved
- much less information necessary



low-pass filter



- long-wavelength information is preserved
- much less information necessary

... however, it's not that easy in nuclear physics.





60



low-pass filter



• truncated interaction fails completely to reproduce original phase shifts

• problem: low- and high momentum states are coupled by interaction!






























Systematic decoupling of high-momentum physics: the Similarity Renormalization Group



- elimination of coupling between low- and high momentum components,
 —> simplified many-body calculations!
- observables unaffected by resolution change (for exact calculations)
- residual resolution dependences can be used as tool to test calculations

Not the full story:

RG transformations also change three-body (and higher-body) interactions!

Low- and high momentum couplings in interactions



AV18

(^IS₀ channel)

 $({}^{3}S_{1} \text{ channel})$

0.5

0.2

 $V_{\Lambda}(0,0)/a_{\rm s}$

- strong couplings of low- and high-momenta in interactions complicates convergence ab initio many-body calculations
- these couplings are reduced in chiral potentials compared to 'traditional' interactions, but still present!

More on this in the SRG exercise session!













0



0



- force between earth and satellite depends on the position of moon
- tidal deformations represent internal excitations
- when all objects are described as point particles 3N forces inevitable!
- effects for the present classical problem rather small

- nucleons are composite particles, they can also be internally excited
- existence of three-nucleon forces natural
- key questions:
 - »how big are their contributions?
 - »how do they depend on the resolution

Development of nuclear interactions

nuclear structure and reaction observables

validation optimization fitting of LECs

predictions

Chiral effective field theory

nuclear interactions and currents

- remarkable agreement between different many-body frameworks
- very good agreement between theory and experiment for masses of oxygen and calcium isotopes based on specific chiral interactions
- contributions from 3N force play important role for drip line

Ab initio calculations of heavier nuclei

Ab initio calculations of heavier nuclei

5.0 PE

- spectacular increase in range of applicability of ab initio many body frameworks
- significant discrepancies to experimental data for heavy nuclei for

(most of) presently used nuclear interactions

• need to quantify theoretical uncertainties

Applications of NN plus 3N forces to atomic nuclei

• contributions from 3N force play important role for location of drip lines

- remarkable agreement between different many-body frameworks
- excellent agreement between theory and experiment for energies of oxygen isotopes based on specific chiral interactions
- challenge: correct description of different observables over wide range of the nuclear chart

Applications of NN plus 3N forces to atomic nuclei

remarkable reproduction of energies over wide range of the nuclear chart based on a single NN+3N interaction

KH et al., PRC 83, 031301 (2011) Stroberg et al., PRL 126, 022501 (2021)

order-by-order calculations of light nuclei based on semilocal NN+3N interactions

E. Epelbaum, PRC 99, 024313 (2019)

First inclusions of subleading 3N contributions

3N forces fitted to empirical saturation properties of nuclear matter:

Hoppe et al. PRC 100, 024318 (2019)

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3N forces fitted few-body systems and medium-mass nuclei:

First inclusions of subleading 3N contributions

3N forces fitted to empirical saturation properties of nuclear matter:

3N forces fitted few-body systems and medium-mass nuclei:

no simultaneous description of matter and nuclei possible for these NN forces

The size of the atomic nucleus: challenges from novel high-precision measurements

Hagen. et al.. Nature Phys. 12, 186 (2015)

The size of the atomic nucleus: challenges from novel high-precision measurements

Garcia Ruiz. et al., Nature Phys. 12, 594 (2016)

The size of the atomic nucleus: challenges from novel high-precision measurements

The equation of state of high-density matter: constraints for neutron stars from nuclear physics











A two-solar-mass neutron star measured using Shapiro delay

Science A Massive Pulsar in a Compact Relativistic Binary Demorest et al., Nature 467, 1081 (2010) Antoniadis et al., Science 340, 448 (2013)







 $M_{\rm max} = 2.0 \pm 0.04 \ M_{\odot}$ $R \sim 10 \ {\rm km}$



• consider forces on a mass element:

gravity: $F_g = -\frac{GM(r)\rho(r)A dr}{r^2}$

pressure difference

F_p =
$$A (p_{out} - p_{in}) = A dp$$

ce:



• consider forces on a mass element:

gravity: $F_g = -\frac{GM(r)\rho(r)A dr}{r^2}$ pressure
difference: $F_p = A (p_{out} - p_{in}) = A dp$

• hydrostatic equilibrium condition:

$$F_g = F_p \Rightarrow \frac{dp}{dr} = -\frac{GM(r)\rho(r)}{r^2}$$



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gravity: $F_g = -\frac{GM(r)\rho(r)A dr}{r^2}$ pressure difference: $F_p = A \left(p_{out} - p_{in} \right) = A dp$

• hydrostatic equilibrium condition:

$$F_g = F_p \Rightarrow \frac{dp}{dr} = -\frac{GM(r)\rho(r)}{r^2}$$

• include general-relativistic corrections:

$$\frac{dp}{dr} = -\frac{GM(r)\varepsilon(r)}{r^2} \left[1 + \frac{p(r)}{\varepsilon(r)c^2}\right] \left[1 + \frac{4\pi r^3 p(r)}{M(r)c^2}\right] \left[1 - \frac{2GM(r)}{c^2 r}\right]$$

'Tolman-Oppenheimer-Volkov' equation



Microscopic calculations of the equation of state



- microscopic framework to calculate equation of state for general proton fractions
- uncertainty bands determined
 by set of 7 Hamiltonians



 many-body framework allows treatment of general
 3N interaction

Drischler, KH, Schwenk, PRC 054314 (2016)

Microscopic calculations of the equation of state



Neutron star radius constraints

incorporation of beta-equilibrium: neutron matter \longrightarrow neutron star matter

parametrize our ignorance via piecewise high-density extensions of EOS:

- use polytropic ansatz $~p\sim
 ho^{\Gamma}$ (results insensitive to particular form)
- range of parameters $\ \Gamma_1, \rho_{12}, \Gamma_2, \rho_{23}, \Gamma_3$ limited by physics



KH, Lattimer, Pethick, Schwenk, ApJ 773, 11 (2013) KH, Lattimer, Pethick, Schwenk, PRL 105, 161102 (2010)

The equation of state of high-density matter: constraints from neutron star observations

observation of heavy neutron stars

Demorest et al., Nature 467, 1081 (2010) Antoniadis et al., Science 340, 448 (2013) Cromartie et al., Nature Astron. 4, 72 (2020)





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• detection of gravitational waves from neutron star merger event

Abbott et al., PRL 119, 161101 (2017)





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14.0

3.5

2.5

2.0

1.0

X-ray Color

Normalized amplitude

Color

0.6

0.8

detection of gravitational waves from neutron star merger event

Abbott et al., PRL 119, 161101 (2017)



• radius measurements from pulsar x-ray timing

Watts et al., RMP 88, 021001 (2016) Riley at al., APJL 887, 21 (2019) Raaijmakers et al., APJL 887, 22 (2019)





500

100 50

500

LIGO-Hanford

Constraints on the nuclear equation of state



constraints lead to significant reduction of EOS uncertainty band

Constraints on neutron star radii



- low-density part of EOS sets scale for allowed high-density extensions
- current radius prediction for typical $1.4 M_{\odot}$ neutron star: $9.7 13.9 \,\mathrm{km}$

Constraints on neutron star radii PCL2 WFF1 3 WFF2 SQM1 36 WFF3 SQM2 AP4 SQM3 AP3 PS 2.5 causalit MS1 MS3 $\log_{10} P \ [dyne/cm^2]$ GM3 Mass [Msub 2 35 ENG PAL GS1 1.5 GS2 34 0.5 33 () 8 10 12 14 16 14.6 14.8 15.0 15.2 14.4 15.4 14.2 $\log_{10}\rho [g/cm^3]$ Radius [km]

KH, Lattimer, Pethick, Schwenk, ApJ 773, 11 (2013) KH, Lattimer, Pethick, Schwenk, PRL 105, 161102 (2010)

- low-density part of EOS sets scale for allowed high-density extensions
- current radius prediction for typical $1.4 M_{\odot}$ neutron star: 9.7 13.9 km
- proposed missions (LOFT,NICER...) could significantly improve constraints

Constraints on neutron star radii constraints on EOS and NS radii from first NICER observations:



additionally incorporating constraints from LIGO and mass measurements:



Constraints on neutron star radii constraints on EOS and NS radii from first NICER observations:



additionally incorporating constraints from LIGO and mass measurements:



Status and achievements

significant increase in scope of ab initio many-body frameworks

remarkable agreement between different ab intio many-body methods

discrepancies to experiment dominated by deficiencies of present nuclear interactions

Current developments and open questions

presently active efforts to develop improved NN and 3N interactions (improved fits of LECs, power counting, regularization...)

Key goals

unified study of atomic nuclei, nuclear matter and reactions based on novel interactions

systematic estimates of theoretical uncertainties