



LABORATÓRIO DE INSTRUMENTAÇÃO  
E FÍSICA EXPERIMENTAL DE PARTÍCULAS  
*partículas e tecnologia*



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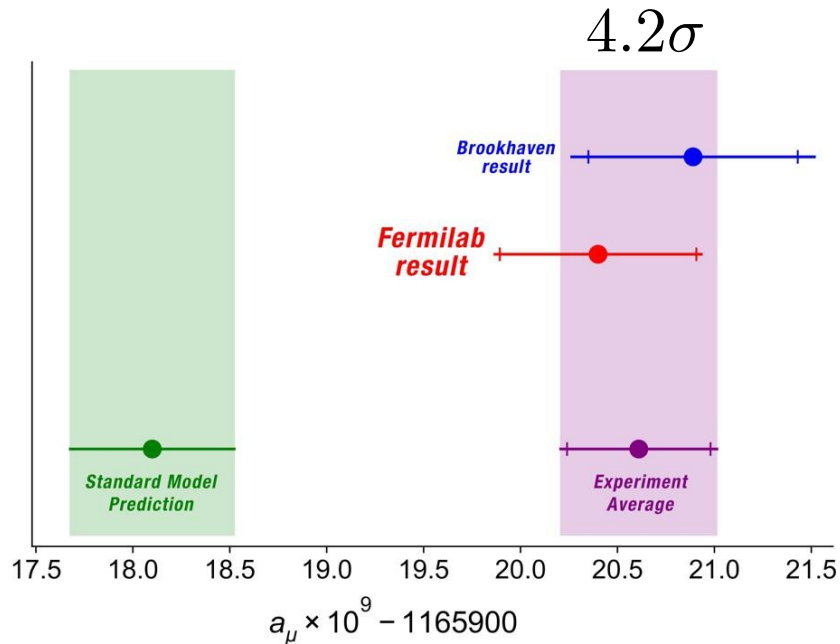
# A bridge to new physics

Explaining ( $g-2$ ) and connecting it to other flavour anomalies

**Guilherme Guedes, Pablo Olgoso**

**gguedes@lip.pt**

# The anomalous $g-2$



Big effort to explain this discrepancy in **SM extensions**

For a comprehensive review of the status of solutions, see:

P. Athron, C. Balázs, D. Jacob, W. Kotlarski, D. Stöckinger, H. Stöckinger-Kim 2104.03691

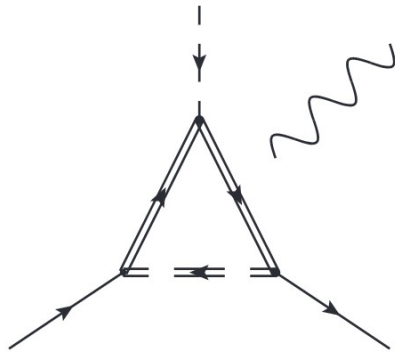
$$\mathcal{O}_{eB} = (\bar{\ell}\sigma^{\mu\nu}e)HB_{\mu\nu} + \text{h.c.},$$

$$\mathcal{O}_{eW} = (\bar{\ell}\sigma^{\mu\nu}e)\sigma^I HW_{\mu\nu}^I + \text{h.c.}$$

# Chirally enhanced solutions

$\mathcal{O}(\text{TeV})$  solutions need chirally enhanced contributions

NOT proportional to the muon's Yukawa



A. Crivellin and M. Hoferichter, 2104.03202

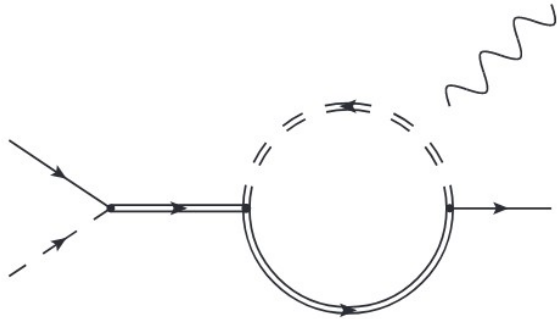
L. Allwicher, L. Luzio, M. Fedele, F. Mescia, M. Nardecchia, 2105.13981

- Chirality flip comes either from top Yukawa ( $S_1$  leptoquark)
- Heavy fermion yukawa-like coupling (Vector like leptons)

# Chirally enhanced solutions

$\mathcal{O}(\text{TeV})$  solutions need chirally enhanced contributions

NOT proportional to the muon's Yukawa



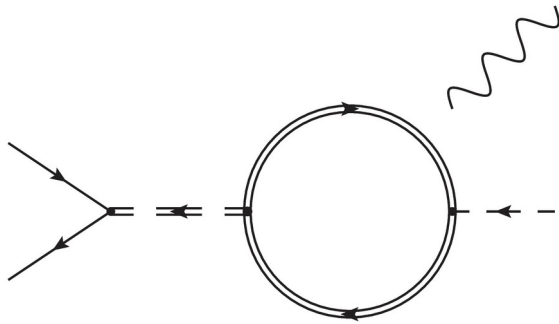
- We will focus on the less studied bridge topology

**In this talk:** Classification of the UV extensions which generate non-zero contribution to  $(g-2)$  through bridge

N. Arkani-Hamed and K. Harigaya, 2106.01373  
L. Rose, B. Harling and A. Pomarol, 2201.10572

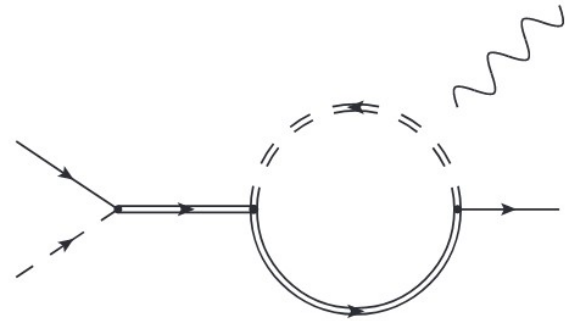
# The bridge

The field running in the bridge can be fixed:



$$\Phi \sim (1, 2, 1/2)$$

**No contribution**



$$E \sim (1, 1, -1)$$

$$\Delta \sim (1, 2, -1/2)$$

$$\Sigma \sim (1, 3, -1)$$

# General results

To see an example, let us focus on the doublet bridge:

$$\alpha_{e\gamma}^{2,2} = \frac{iN_c e}{4} y_M y_F y_b^R \sum_{IJ} T_{I2J} \left[ \gamma_\Psi T_{I'I}^{\gamma,\Psi} T'_{2JI'} + \gamma_\Phi T_{JJ'}^{\gamma,\Phi} T'_{2IJ'} \right]$$

$$\gamma_\Psi = \frac{-iM_\Psi}{(4\pi)^2 M_\Delta} \frac{M_\Psi^4 - 4M_\Psi^2 M_\Phi^2 + 3M_\Phi^4 + 2M_\Phi^4 \text{Log} [M_\Psi^2/M_\Phi^2]}{(M_\Psi^2 - M_\Phi^2)^3}$$

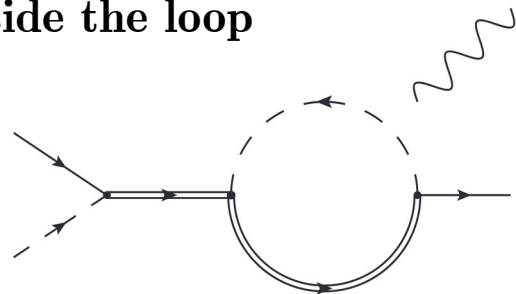
$$\gamma_\Phi = -\frac{iM_\Psi}{(4\pi)^2 M_\Delta} \frac{M_\Psi^4 - M_\Phi^4 - 2M_\Psi^2 M_\Phi^2 \text{Log} [M_\Psi^2/M_\Phi^2]}{(M_\Psi^2 - M_\Phi^2)^3}$$

# 2-fermion extensions

**Discussed in:**  
 A. Freitas, J. Lykken, S. Kell, S. Westhoff  
 1402.7065

Bridge	Other Fermion
$E \sim (1, 1, -1)$	$\Delta \sim (1, 2, -1/2)$ $\Delta_3 \sim (1, 2, -3/2)$
$\Delta \sim (1, 2, -1/2)$	$E \sim (1, 1, -1)$ $\Sigma \sim (1, 3, -1)$ $N \sim (1, 1, 0)$ $\Sigma_0 \sim (1, 3, 0)$
$\Sigma \sim (1, 3, -1)$	$\Delta \sim (1, 2, -1/2)$ $\Delta_3 \sim (1, 2, -3/2)$

**SM Higgs as the scalar inside the loop**

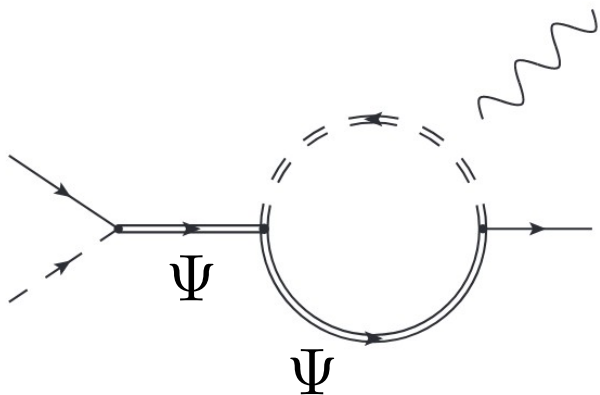


N. Arkani-Hamed and K. Harigaya, 2106.01373

N. Craig, I. Garcia, A. Vainshtein, Z. Zhang  
 2112.05770

L. Rose, B. Harling and A. Pomarol, 2201.10572

# 2-field fermion & scalar extensions



Fermion	Scalar
$E \sim (1, 1, -1)$	$\mathcal{S}_0 \sim (1, 1, 0)$
	$\mathcal{S}_2 \sim (1, 1, -2)$
$\Delta \sim (1, 2, -1/2)$	$\mathcal{S}_0 \sim (1, 1, 0)$
	$\mathcal{S}_1 \sim (1, 1, -1)$
	$\Xi_0 \sim (1, 3, 0)$
	$\Xi_1 \sim (1, 3, -1)$
$\Sigma \sim (1, 3, -1)$	$\Xi_0 \sim (1, 3, 0)$
	$\Xi_2 \sim (1, 3, -2)$

**Excluded in  
the literature**

*but*

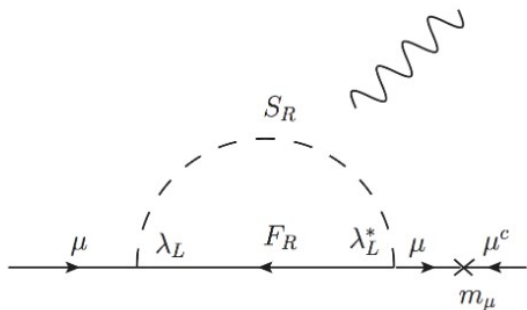
**only Yukawa  
suppressed  
terms**



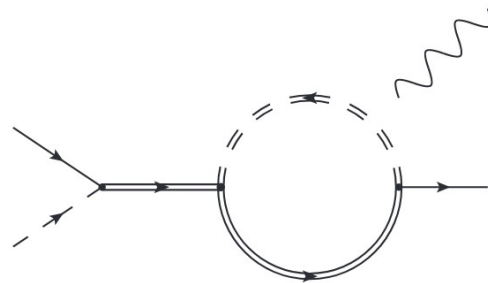
# 2-field fermion & scalar extensions

P. Athron, C. Balázs, D. Jacob, W. Kotlarski, D. Stöckinger, H. Stöckinger-Kim 2104.03691

$(\mathbf{1}, \mathbf{3}, 0)_0$  and  $(\mathbf{1}, \mathbf{2}, -1/2)_{1/2} \implies \Delta a_\mu < 0$  irrespective of  $\mathbb{Z}_2$



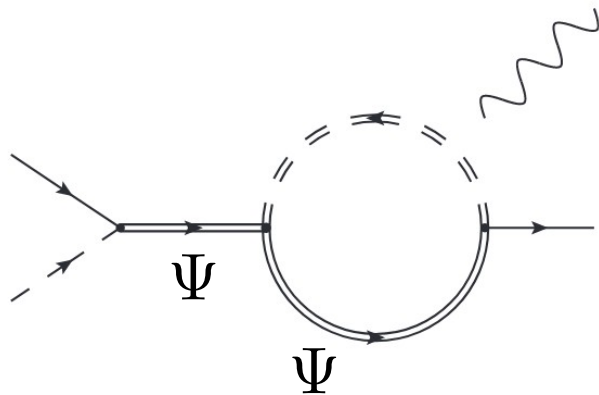
**Yukawa-suppressed:  $< 0$**



**Bridge-like: no definite sign**

$$\alpha_{e\gamma} = y_b y_M y_F f(M_\Delta, M_\Xi)$$

# 2-field fermion & scalar extensions



Fermion	Scalar
$E \sim (1, 1, -1)$	$\mathcal{S}_0 \sim (1, 1, 0)$
	$\mathcal{S}_2 \sim (1, 1, -2)$
$\Delta \sim (1, 2, -1/2)$	$\mathcal{S}_0 \sim (1, 1, 0)$
	$\mathcal{S}_1 \sim (1, 1, -1)$
	$\Xi_0 \sim (1, 3, 0)$
	$\Xi_1 \sim (1, 3, -1)$
$\Sigma \sim (1, 3, -1)$	$\Xi_0 \sim (1, 3, 0)$
	$\Xi_2 \sim (1, 3, -2)$



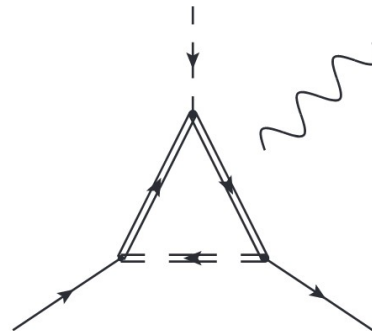
# 3-field extensions

Bridge	$(SU(2)_\Psi, SU(2)_\Phi)$
$E \sim (1, 1, -1)$	(1,1)
	(2,2)
	(3,3)
$\Delta \sim (1, 2, -1/2)$	(2,1)
	(2,3)
$\Sigma \sim (1, 3, -1)$	(2,2)
	(3,3)

A. Crivellin and M. Hoferichter, 2104.03202

L. Allwicher, L. Luzio, M. Fedele, F. Mescia, M. Nardecchia, 2105.13981

Not the same as those contributing through

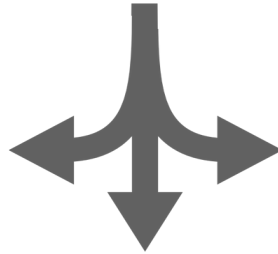


New class of 3-field extensions

# Connecting trees and bridges



Neutral B-anomalies



Cabibbo angle anomaly



$(g-2)$

# The triple triplet model



$S_3 \sim (3, 3, -1/3)$  as an explanation to  $R_K^{(*)}$

# The triple triplet model



$S_3 \sim (3, 3, -1/3)$  as an explanation to  $R_K^{(*)}$



$\Sigma \sim (1, 3, -1)$  as an explanation for C.A.A.

A. Crivellin, M. Hoferichter 2002.07184

$$R(V_{us}) = 1 - \left( \frac{V_{ud}}{V_{us}} \right)^2 v^2 [C_{H\ell}^{(3)}]_{22}$$

$$R(V_{us}) \equiv \frac{V_{us}^{K\mu 2}}{V_{us}^\beta} \equiv \frac{V_{us}^{K\mu 2}}{\sqrt{1 - |V_{ud}^\beta|^2 - |V_{ub}|^2}}$$

**Tension with EWPD  
(worsened by CDF  
measurement)**

M. Kirk, 2008.03261

A. Crivellin, F. Kirk, C. A. Manzari, M. Montull,  
2008.01113

# The triple triplet model



$S_3 \sim (3, 3, -1/3)$  as an explanation to  $R_K^{(*)}$



$\Sigma \sim (1, 3, -1)$  as an explanation for C.A.A.



$\Psi \sim (3, 3, -4/3)$  to construct the bridge of  $(g - 2)$

# One-loop phenomenology

**Matchmakereft**

Full one loop matching  
onto the Warsaw basis

A. Carmona, A. Lazopoulos, P. Olgoso, J. Santiago  
2112.10787

&

**smelli**

Fit to observables

P. Stangl 2012.12211

Only take as *non-zero* the BSM couplings needed to  
account for the anomalies



# Best-fit point

$$\mathcal{L} \supset y_T^i \bar{\ell}_{Li} \phi \sigma^I \Sigma_R^I + y_Q^i \bar{\Psi}_{QL}^I S_3^I \ell_{Ri} + y_b^L \epsilon^{IJK} \bar{\Sigma}_R^I \Psi_{Q,L}^J S_3^{K\dagger} \\ + y_b^R \epsilon^{IJK} \bar{\Sigma}_L^I \Psi_{Q,R}^J S_3^{K\dagger} + \lambda_S^{ij} \bar{Q}_{Li}^c i \sigma^2 \sigma^I \ell_{Lj} S_3^{I\dagger} + \text{h.c.}$$

$$M_{S_3} = 2 \text{ TeV}$$

$$M_{\Sigma} = 3.4 \text{ TeV}$$

$$M_{\Psi_Q} = 4.6 \text{ TeV}$$

$$x_F = 0.2 \text{ TeV}^{-1}$$

$$x_T = 0.17 \text{ TeV}^{-1}$$

$$y_b^L = 0.10$$

$$x_S = 0.00078 \text{ TeV}^{-2}$$

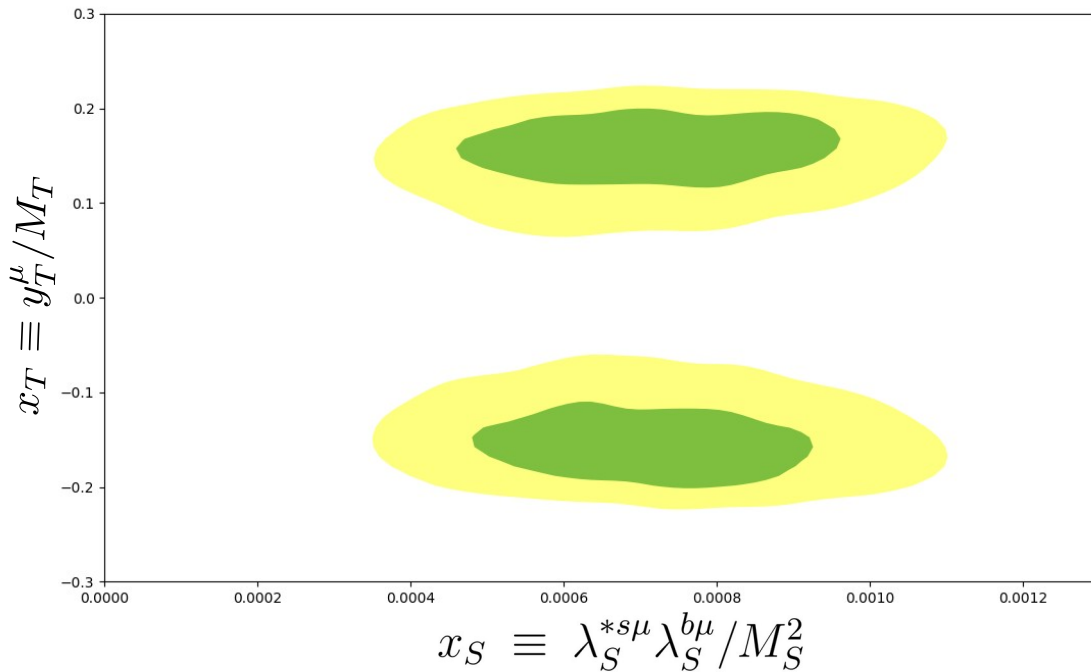
$$\lambda_S^{b\mu} = 0.07$$

$$y_b^R = 0.13$$

defining

$$x_S \equiv \lambda_S^{*s\mu} \lambda_S^{b\mu} / M_S^2 \quad x_T \equiv y_T^\mu / M_T \quad x_F \equiv y_Q^\mu / M_F$$

# Best-fit point



**Results as expected  
from the tree-level  
explanations**

**Introduces some  
tension with  
EWPD, especially  
with W mass**

# Conclusions

- We classified all possible extensions which can generate a chirally enhanced contribution to  $g-2$  through the bridge
- Further pheno studies would be needed
- A complete classification of one-loop solutions to anomalies is helpful in connecting tree-level explanations

# Thanks

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