

Overview of neutral-current B anomalies at LHCb

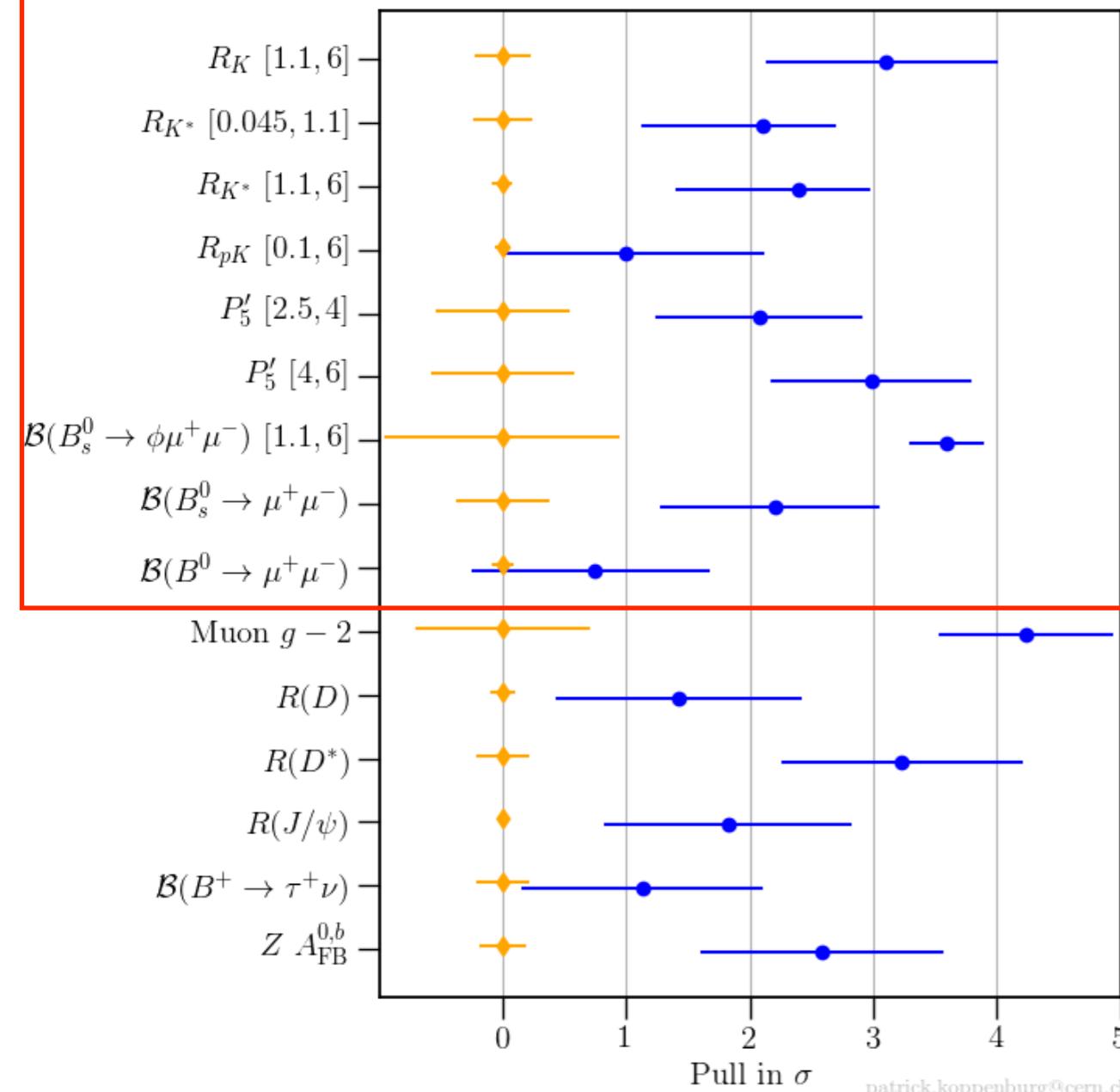
Flavour at the Crossroads, MITP

Eluned Smith / Ambizione Fellow, UZH Zürich

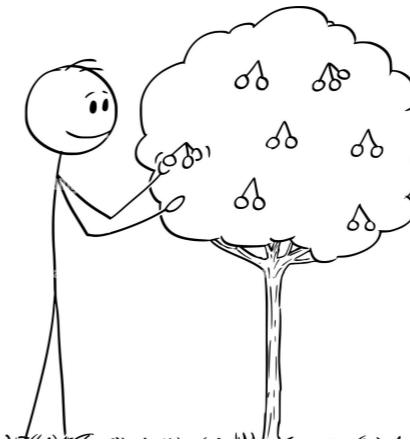
25.04.2022

What I will talk about

Cherry-picked examples



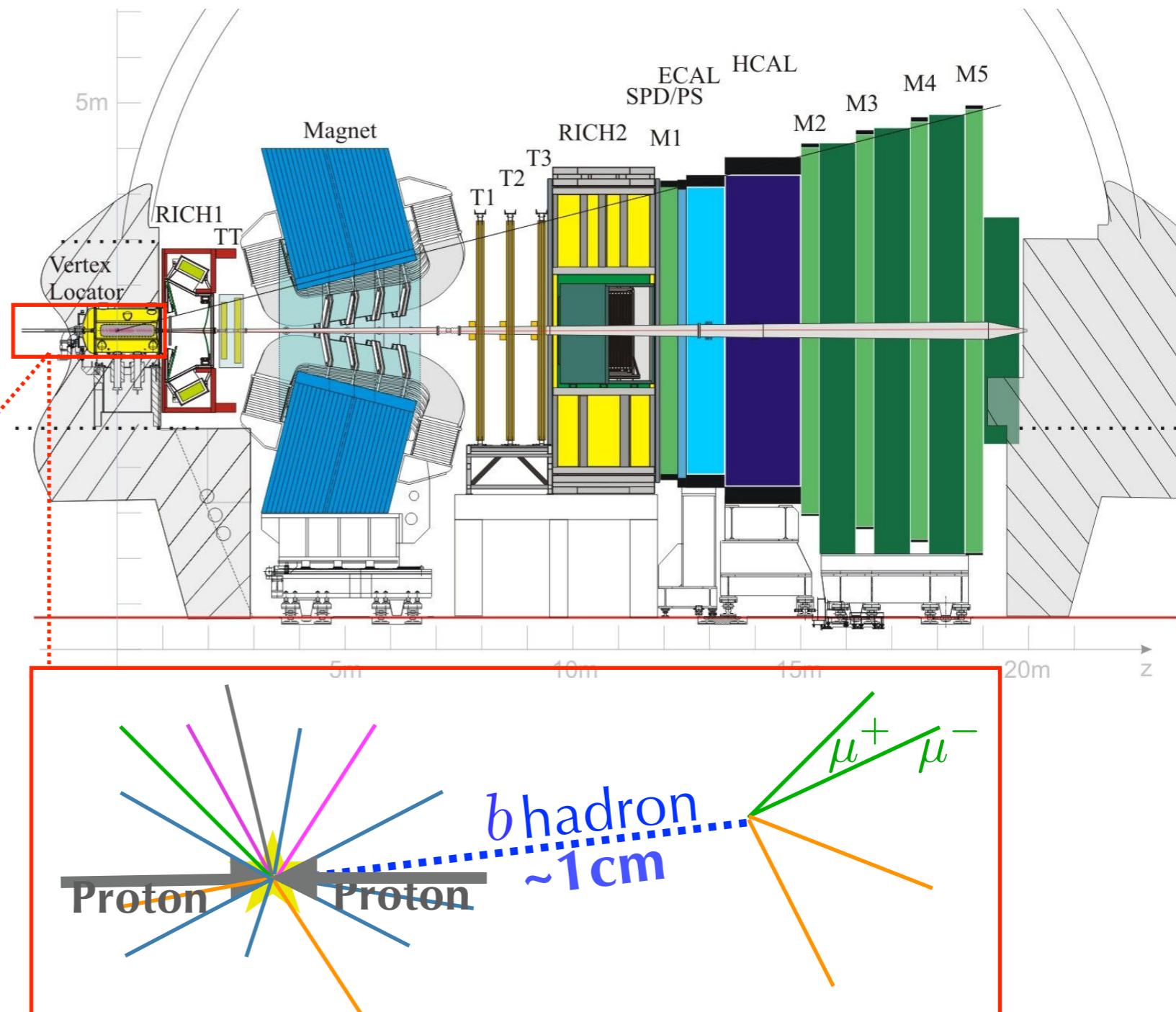
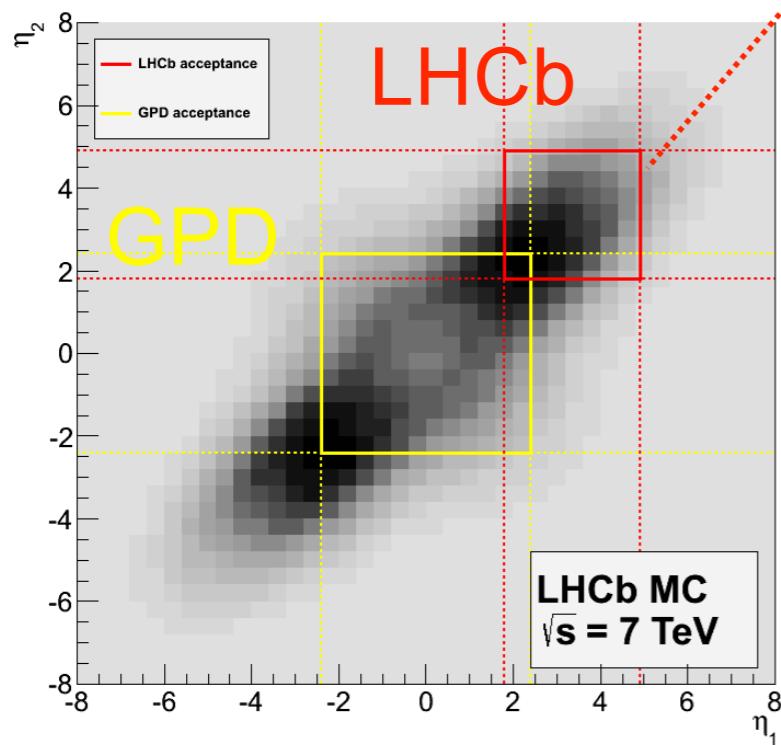
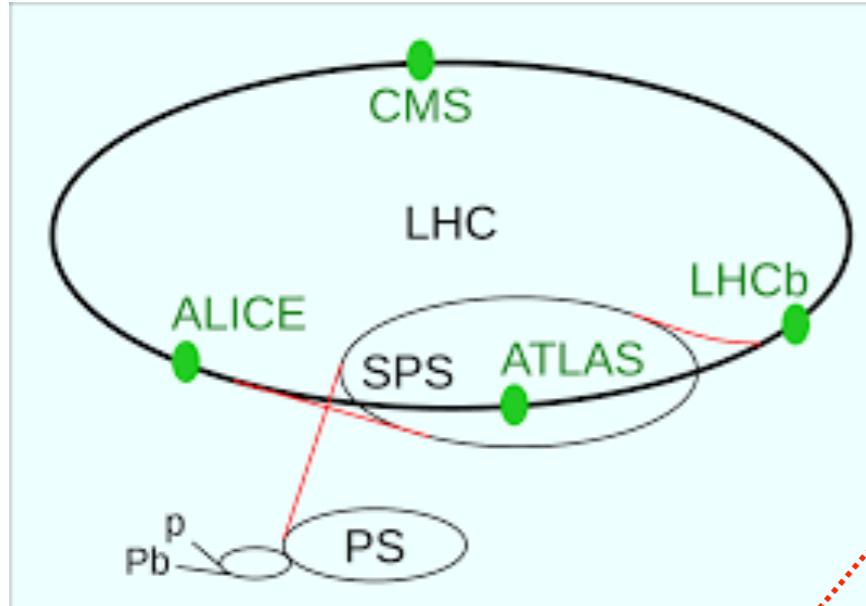
<https://www.nikhet.nl/~pkoppenb/anomalies.html>



- Brief introduction
- Recent results from LHCb on $b \rightarrow s\ell^+\ell^-$ decays
- Remaining Run 2 measurements expected in near-future
- Run 3 prospects

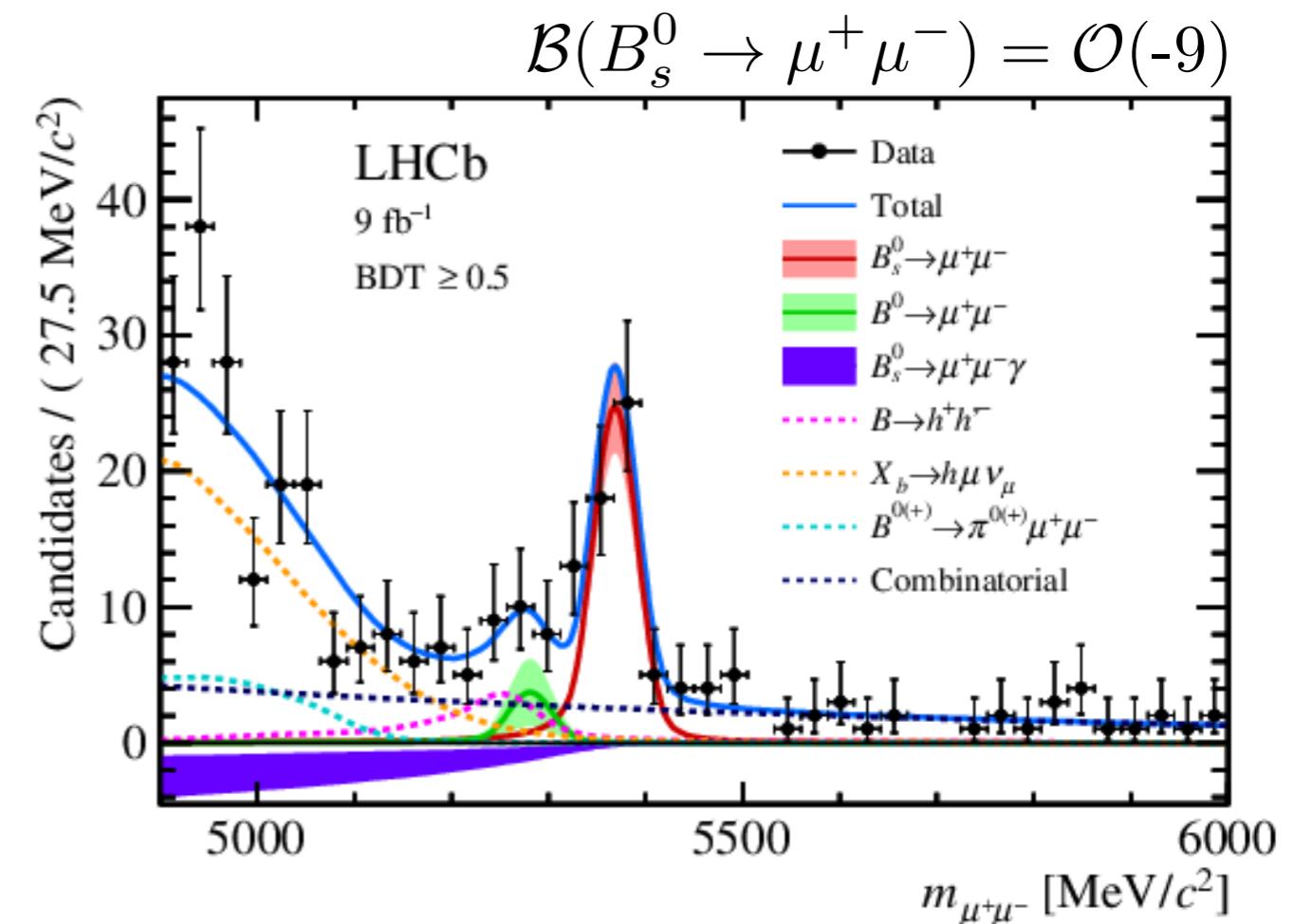
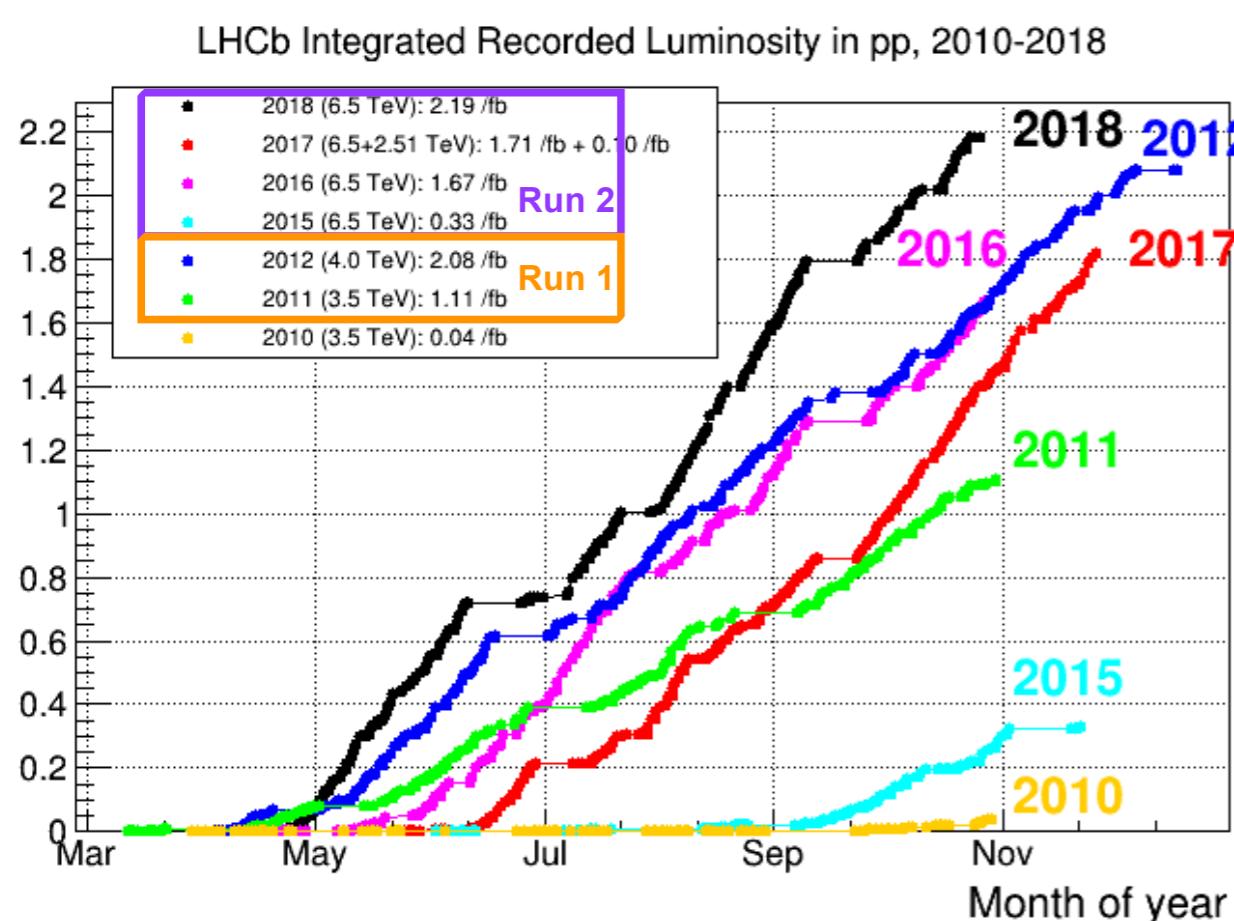
Why $b \rightarrow s(d)\ell^+\ell^-$ decays at LHCb?

- B-quarks produced at the LHC have a significant **boost in the forward direction**, exploited by LHCb experiment



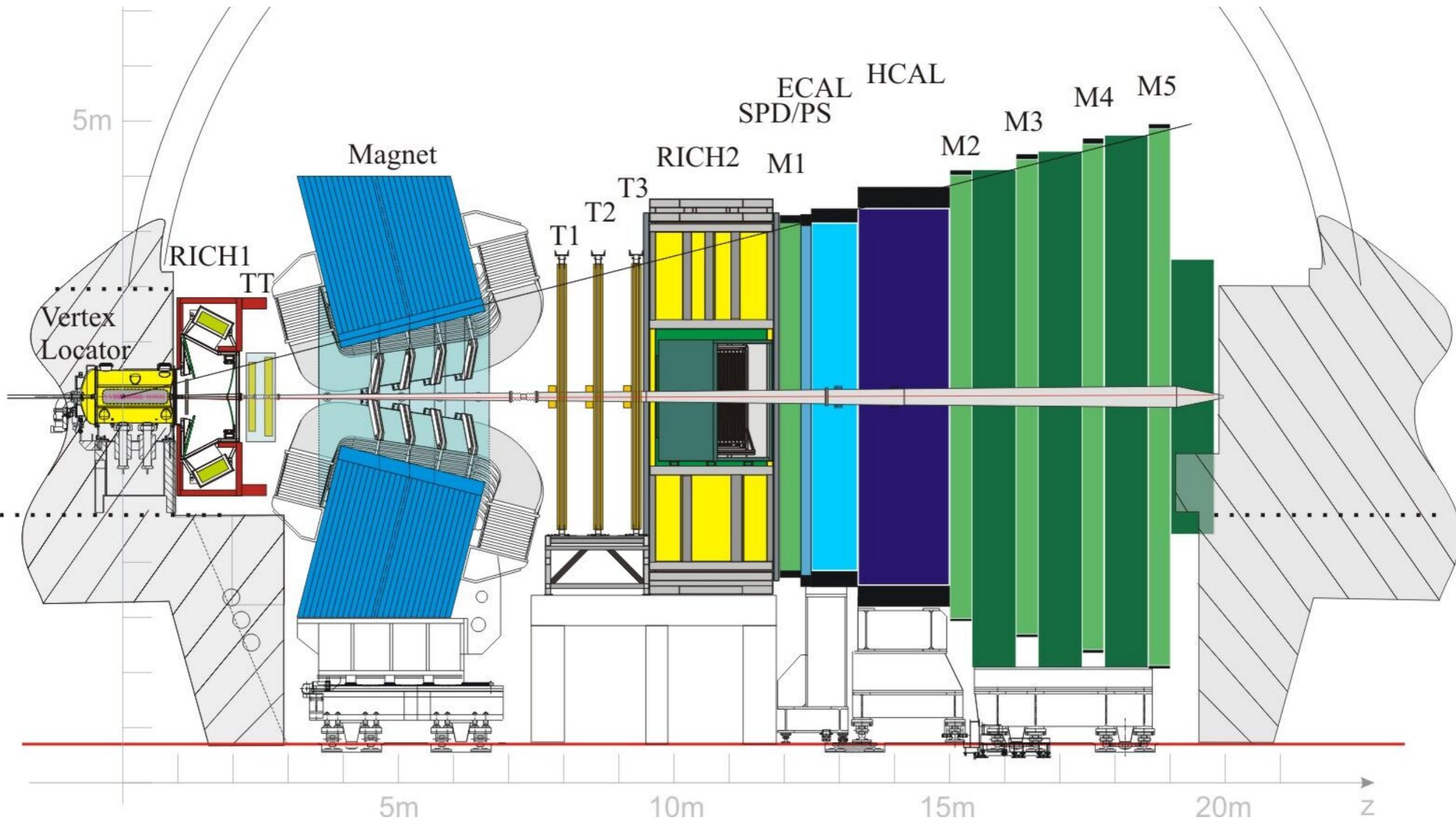
Why $b \rightarrow s(d)\ell^+\ell^-$ decays at LHCb?

- B-quarks produced at the LHC have a significant **boost in the forward direction**, exploited by LHCb experiment

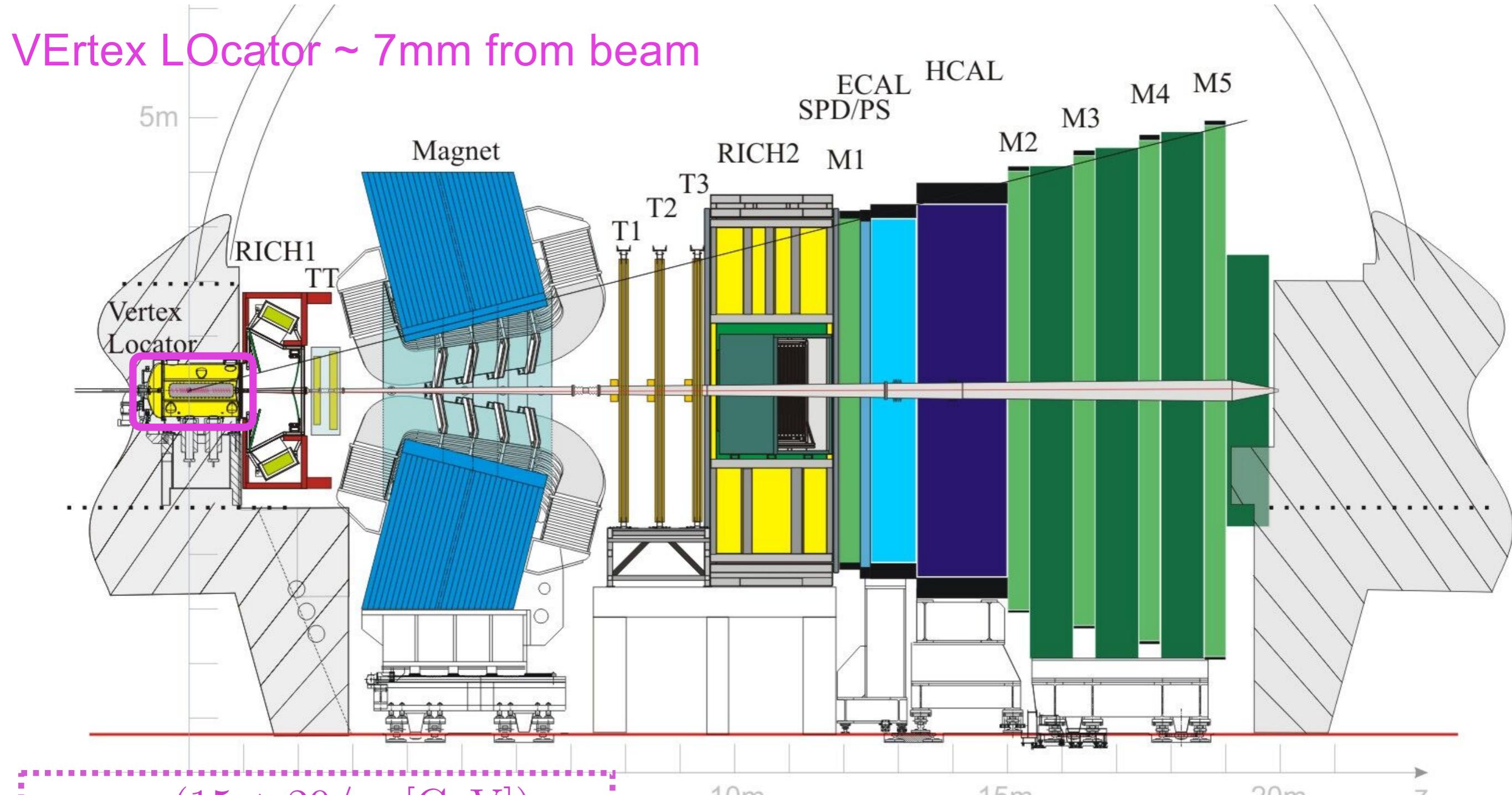


Current available LHCb data (LHC Run 1 (2011-2012) and Run 2 (2015-2018)) gives **upto 1% precision** on NP-sensitive $b \rightarrow s\ell^+\ell^-$ observables

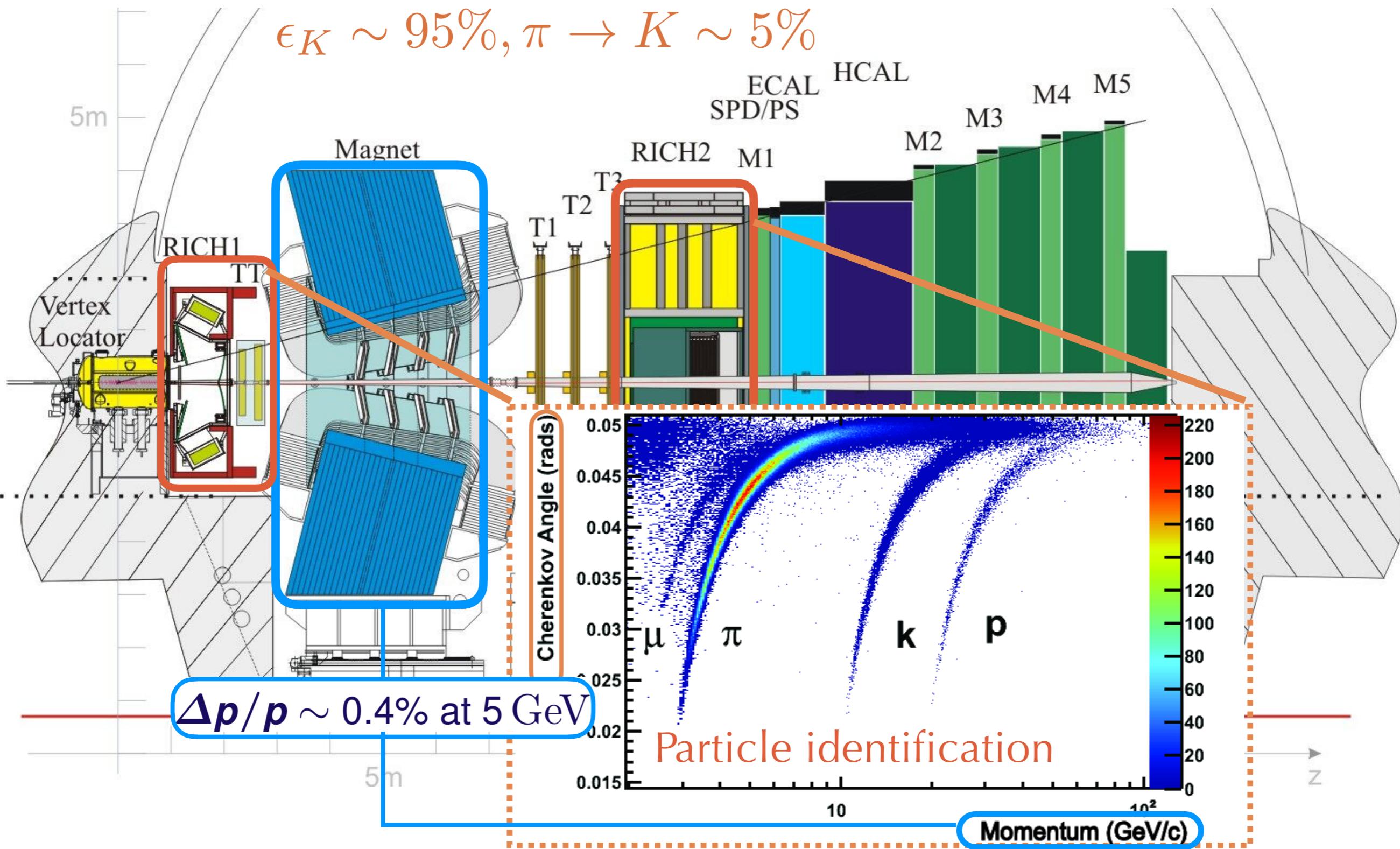
The LHCb detector



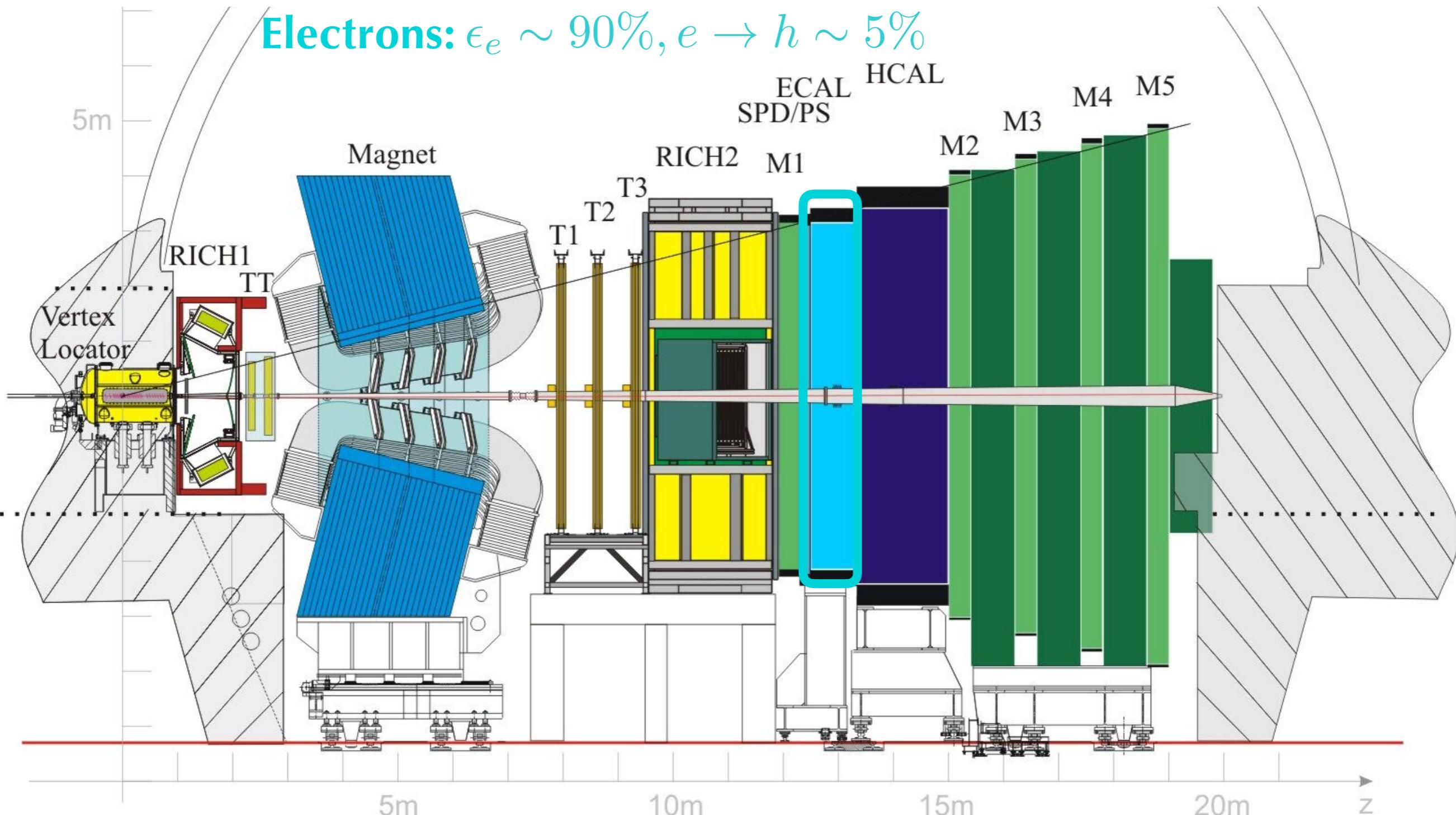
The LHCb detector



The LHCb detector



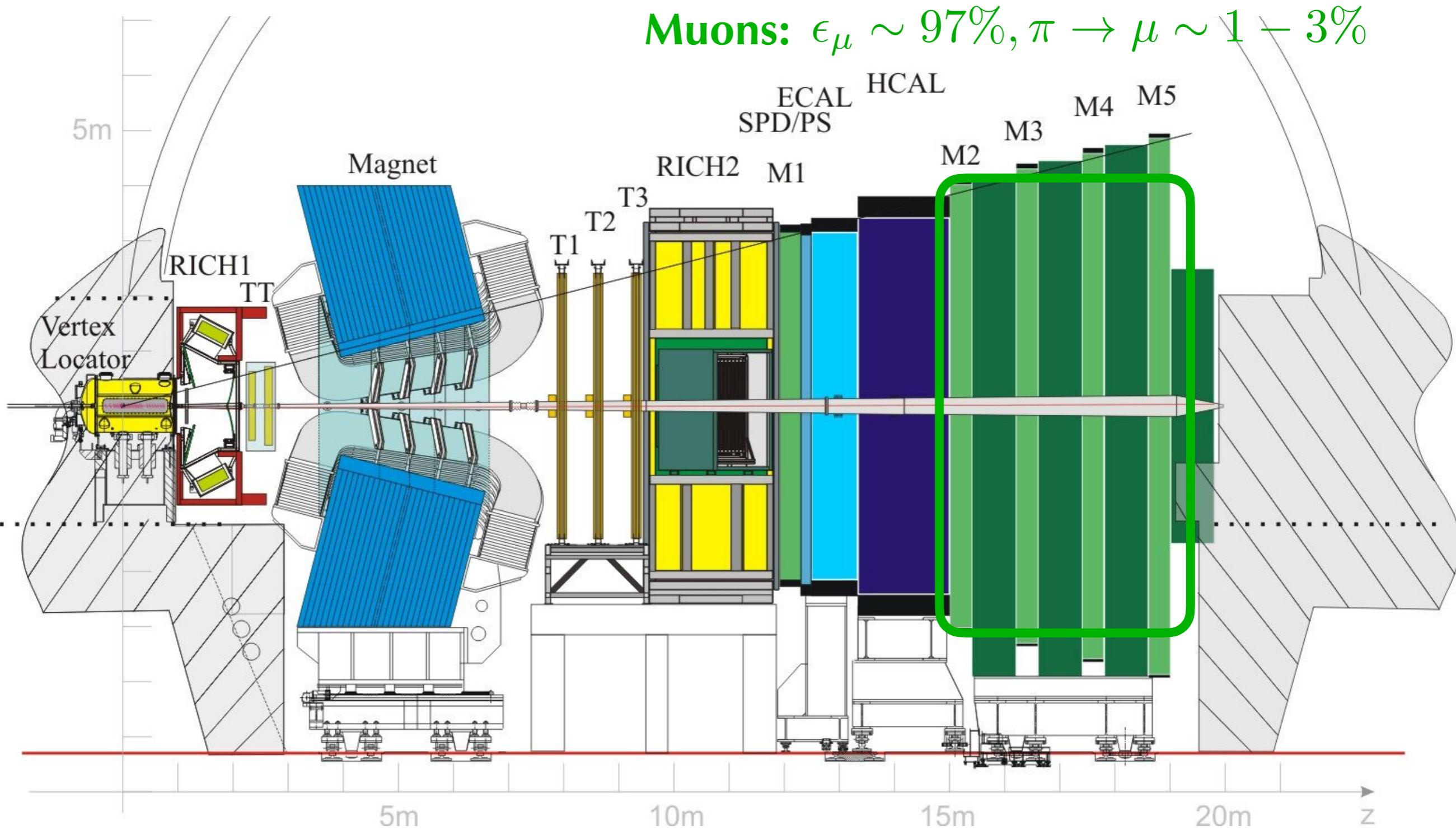
The LHCb detector



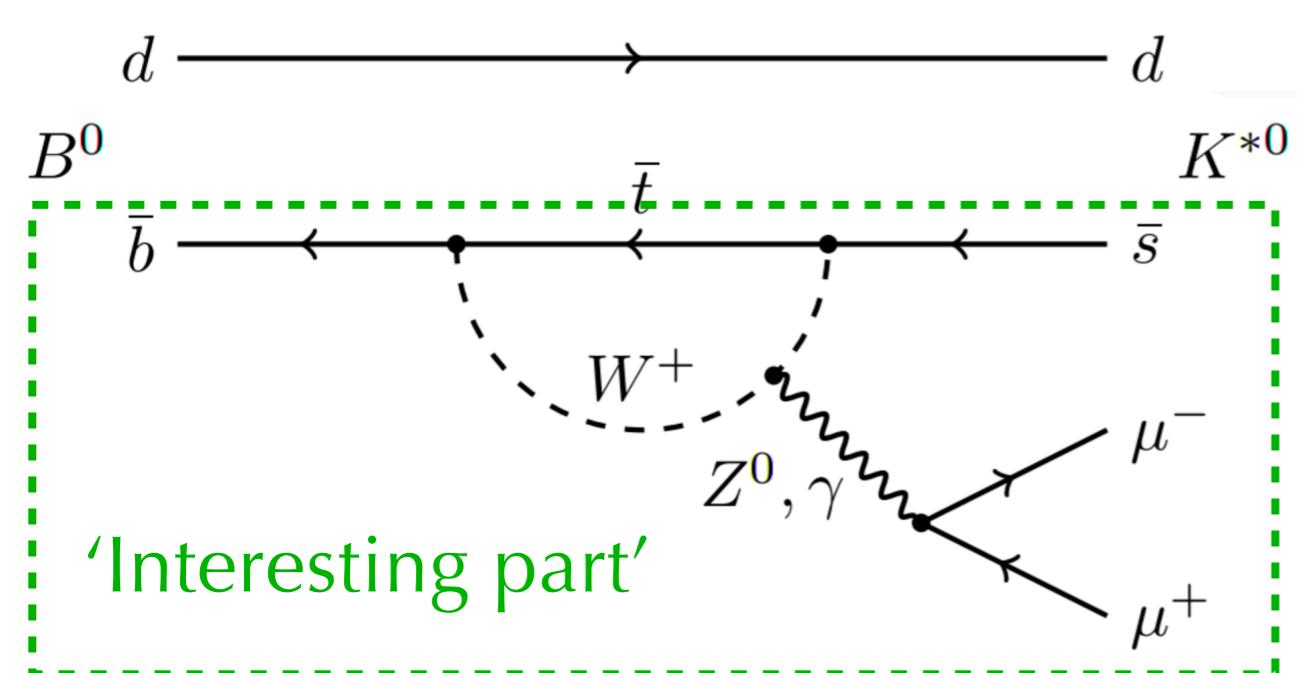
Electrons: $\epsilon_e \sim 90\%, e \rightarrow h \sim 5\%$

ECAL resolution: $1\% \pm \frac{10\%}{\sqrt{(E[GeV])}}$

The LHCb detector

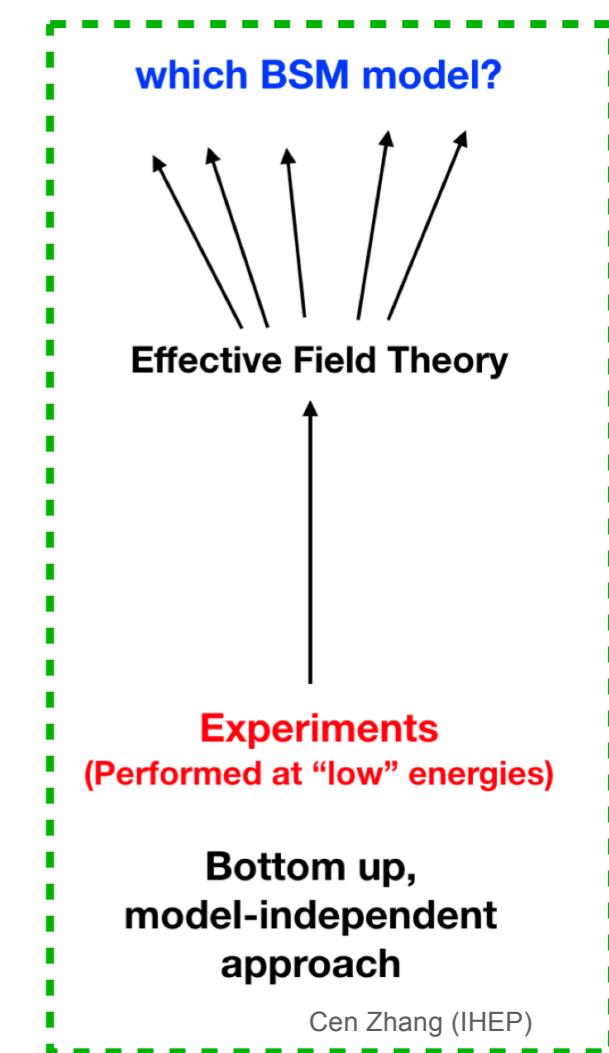
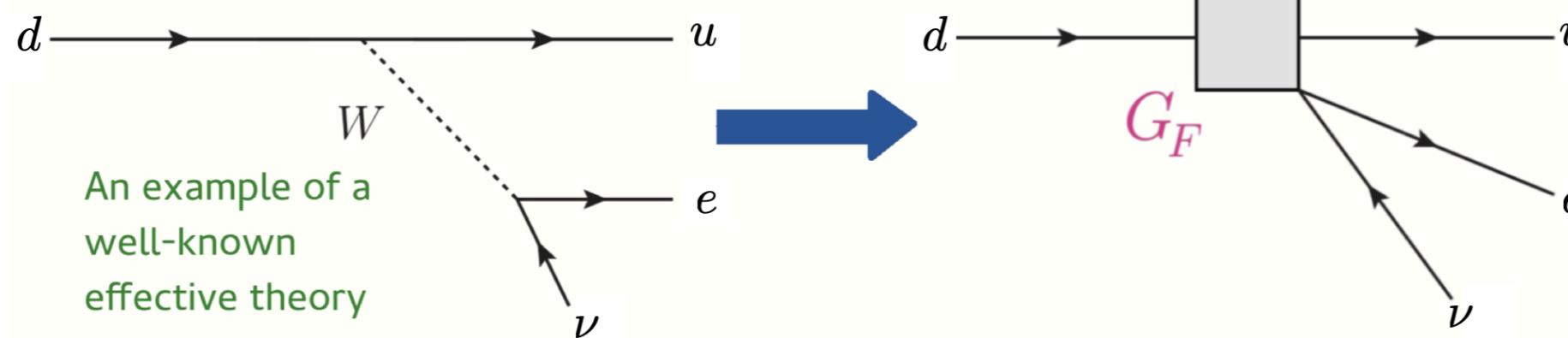


What do we actually want to measure?

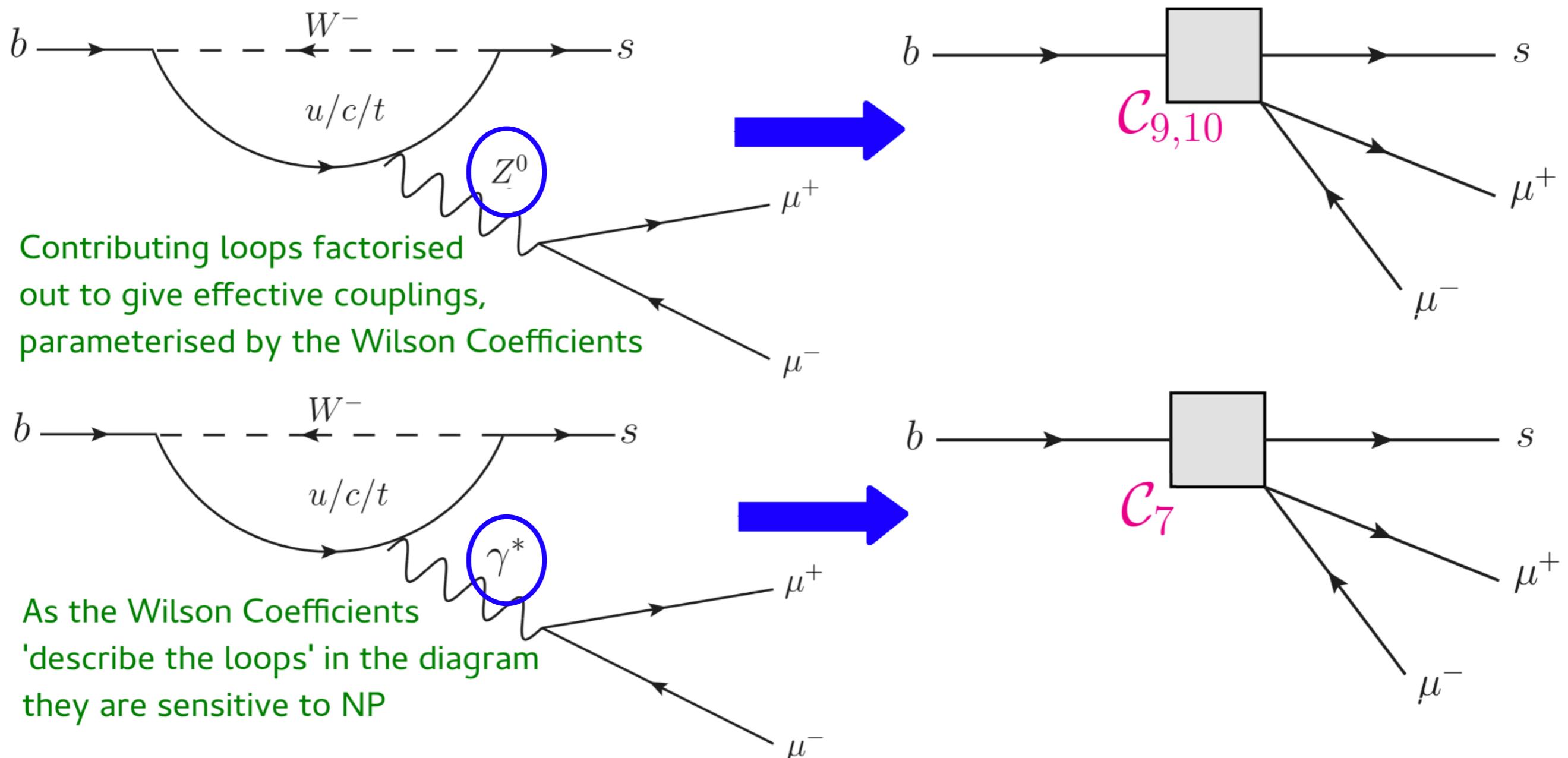


Loop (or box) part of the diagram is sensitive to heavy NP

Much heavier energy scale than rest of diagram, use **effective field theory**

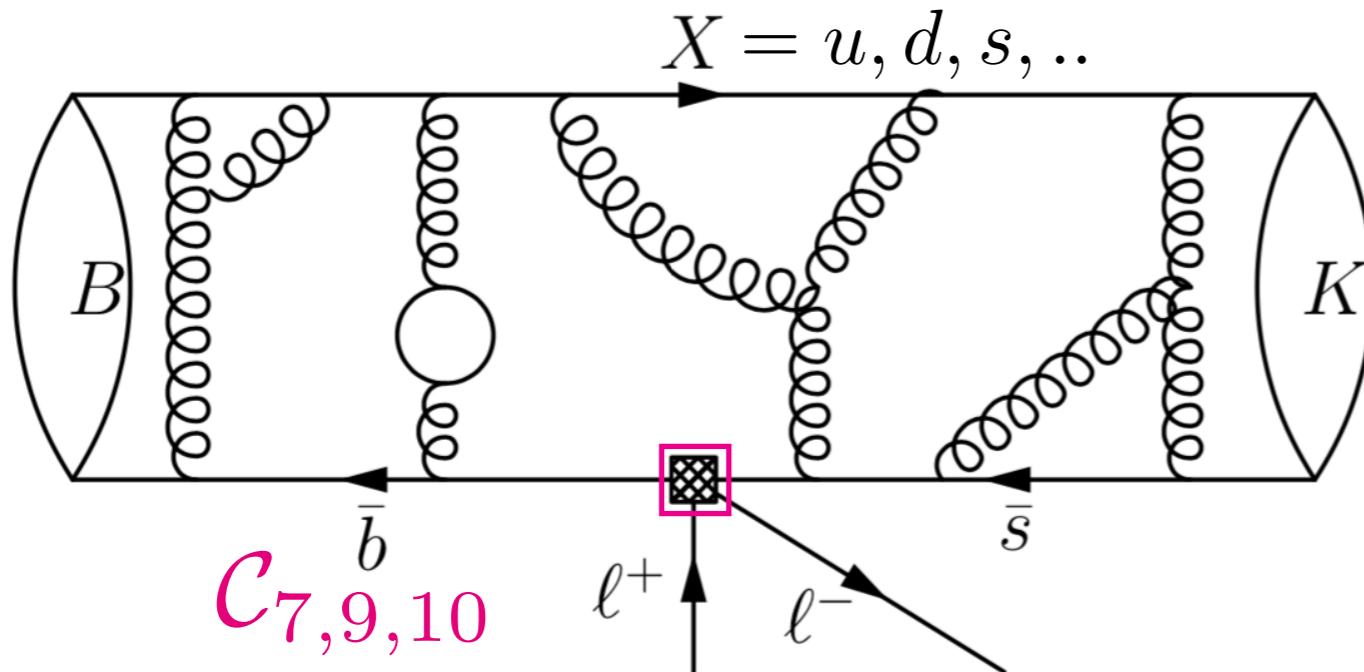


What do we actually want to measure?

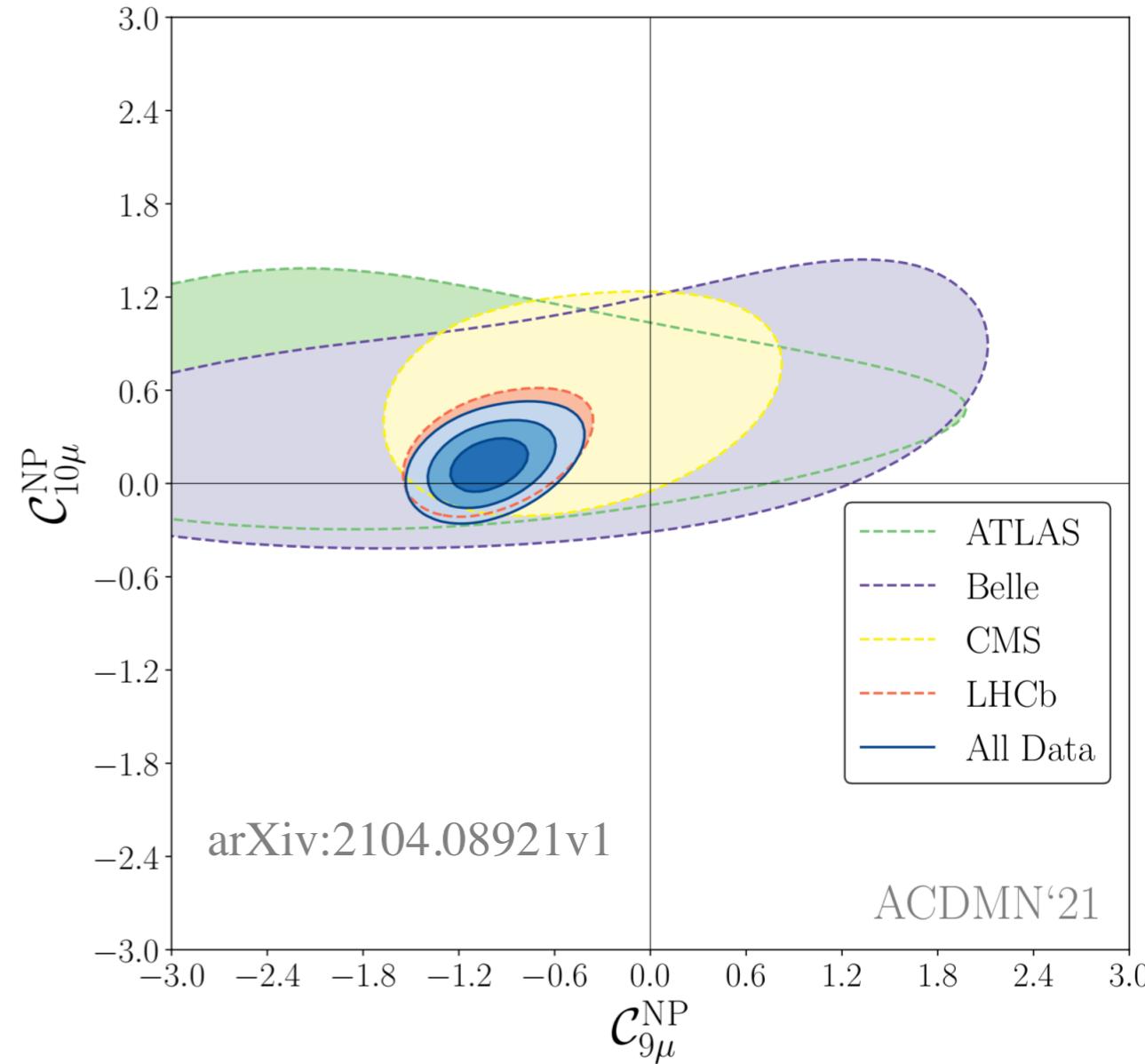


Combining observables

Combine all $b \rightarrow s\ell^+\ell^-$ measurements + observables together

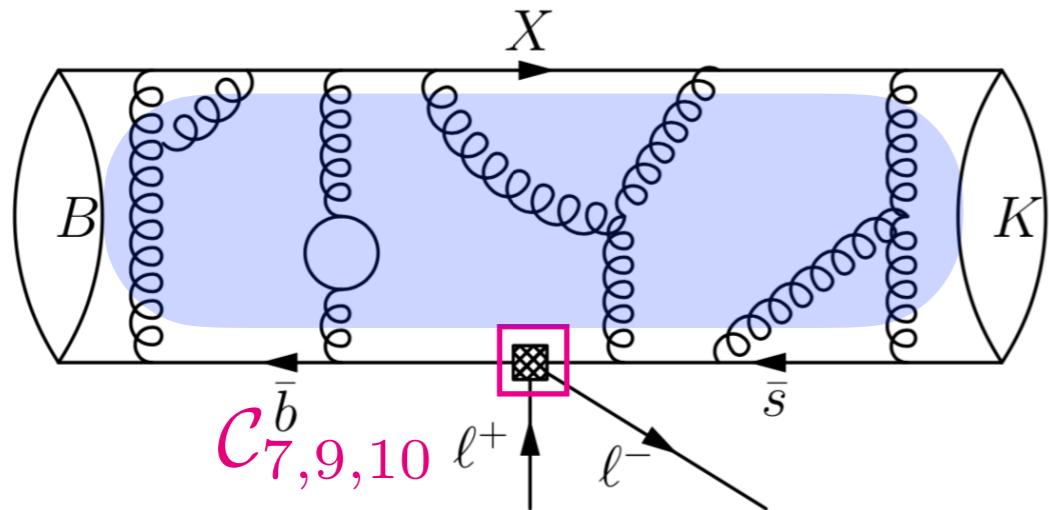


$$\mathcal{H}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum_i (C_i \mathcal{O}_i + C'_i \mathcal{O}'_i)$$

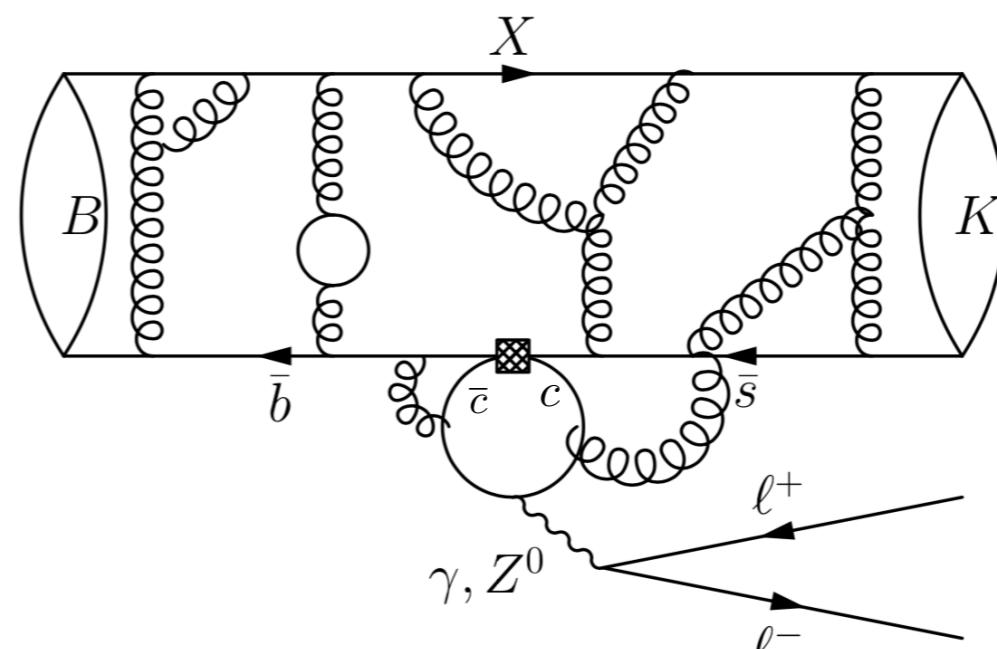
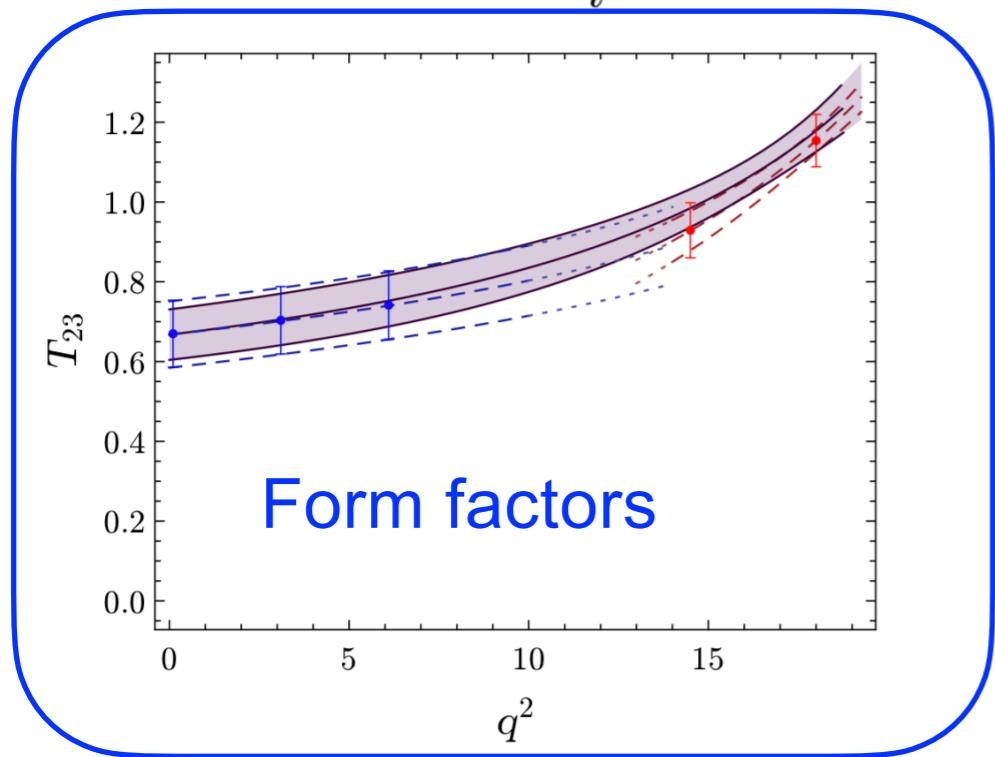


>5 σ - why aren't we claiming discovery?

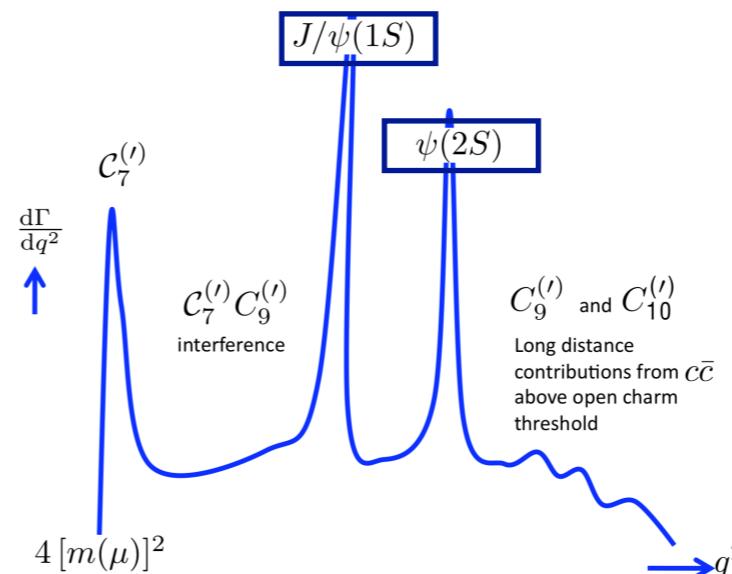
- Not all observables are made equal: robustness of predictions



$$\mathcal{H}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum_i (C_i \mathcal{O}_i + C'_i \mathcal{O}'_i)$$



Non-perturbative “charm-loop” contributions



Mimic C_9

The more sensitive the variable to hadronic effects, the less “clean” the SM prediction

Hadronic cleanliness (not to scale)



Lepton Flavour Universality



Angular analyses



Branching fractions

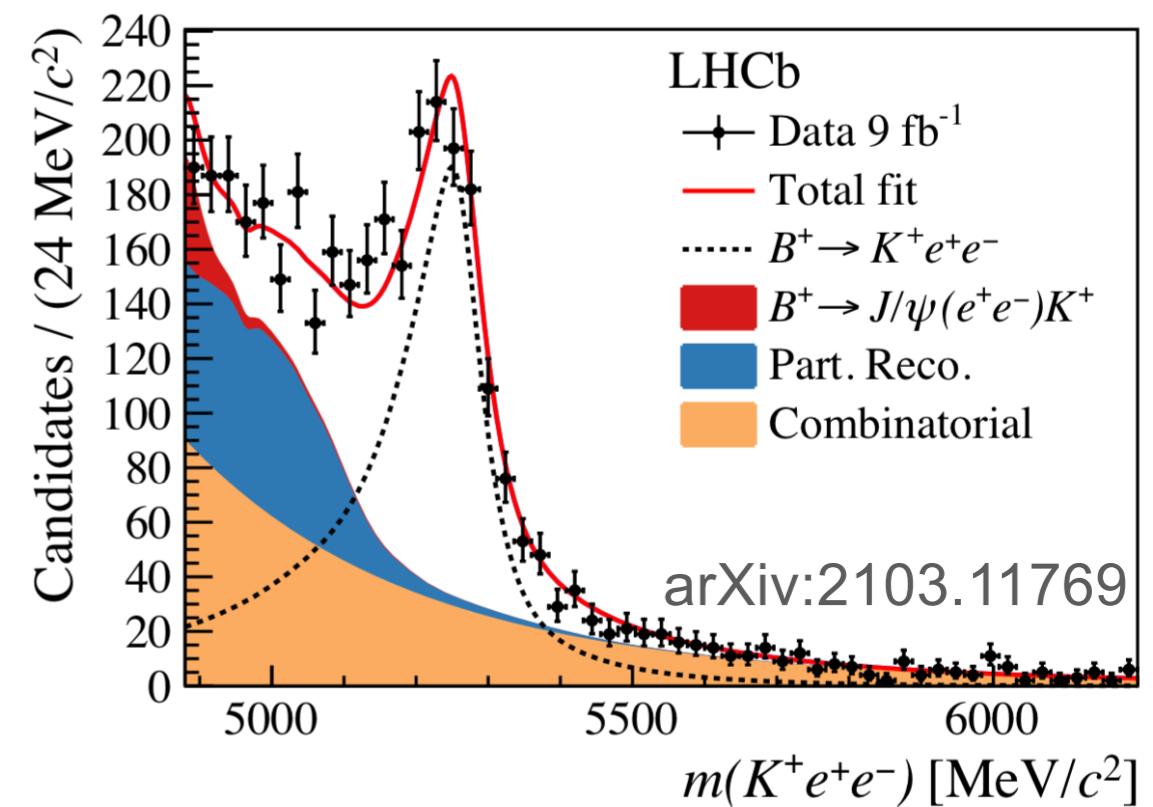
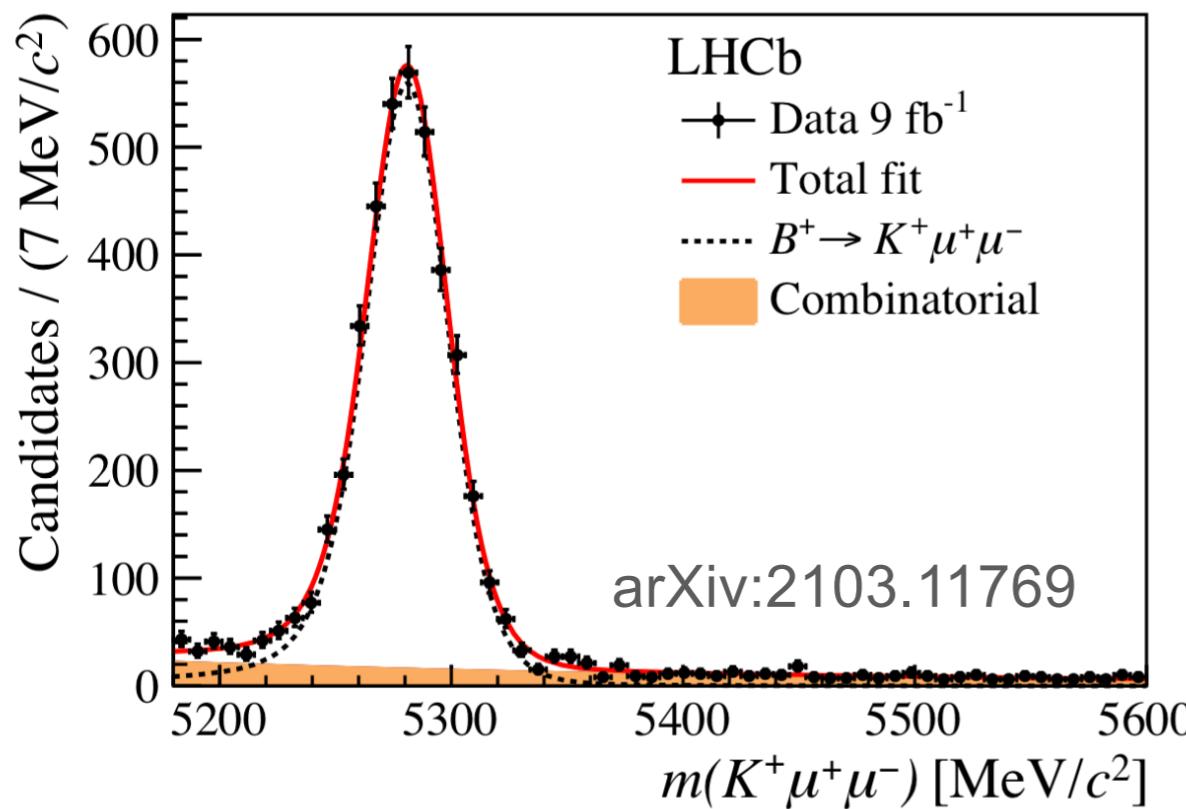
LFU and LFV

“Clean” Lepton Flavour Universality (LFU) observables

- Muons vs electron decay rates, **hadron uncertainties cancel**
- **Unambiguous sign of NP** if deviates from SM expectation

“Clean” observables:

$$R(X) = \frac{\mathcal{B}(B \rightarrow X\mu\mu)}{\mathcal{B}(B \rightarrow Xee)}$$



LFU tests + electrons

Lepton Flavour Universality tests defined as $R(X) = \frac{\mathcal{B}(B \rightarrow X\mu\mu)}{\mathcal{B}(B \rightarrow Xee)}$

In practice measure double-ratio:

$$R(X) = \frac{\mathcal{B}(B \rightarrow X\mu\mu)}{\mathcal{B}(B \rightarrow Xee)} / \frac{\mathcal{B}(B \rightarrow XJ/\psi[\rightarrow \mu\mu])}{\mathcal{B}(B \rightarrow XJ/\psi[\rightarrow ee])}$$

- Double ratio very robust against systematic effects, single ratio:

$$r(J/\psi) = 0.981 \pm 0.020$$



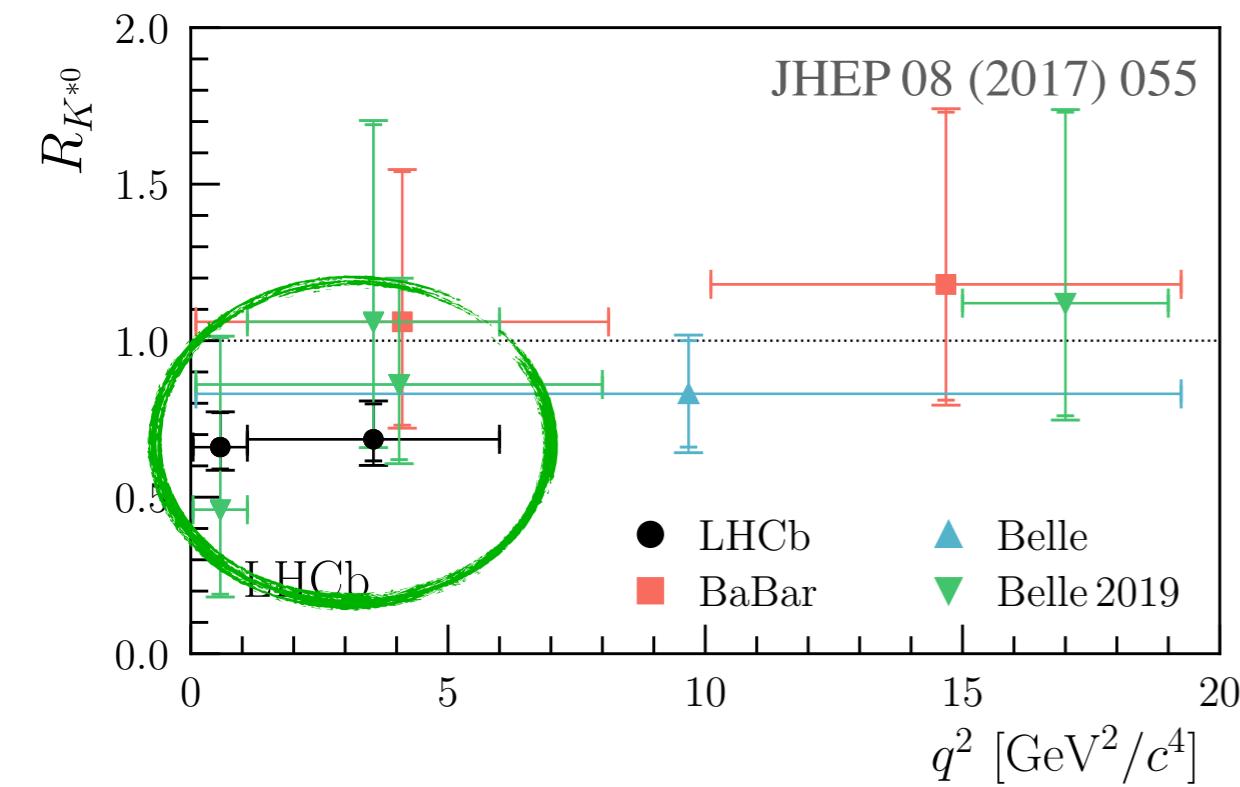
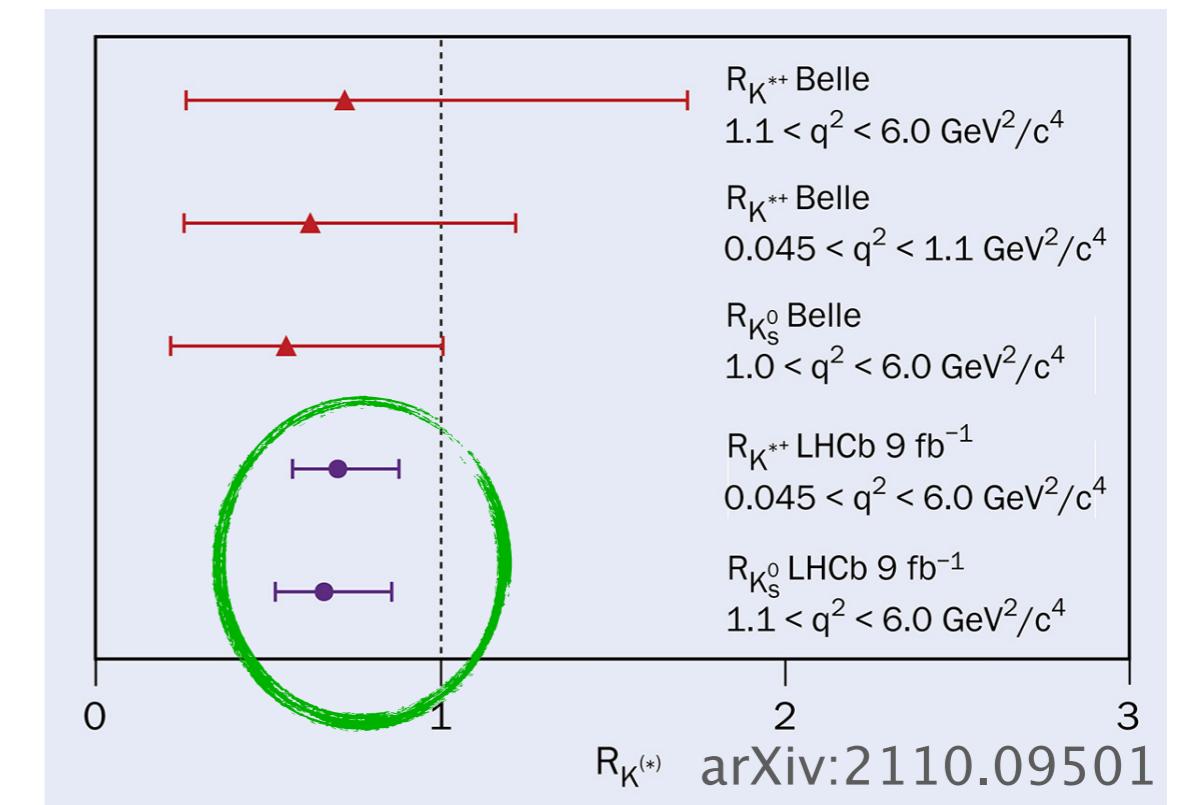
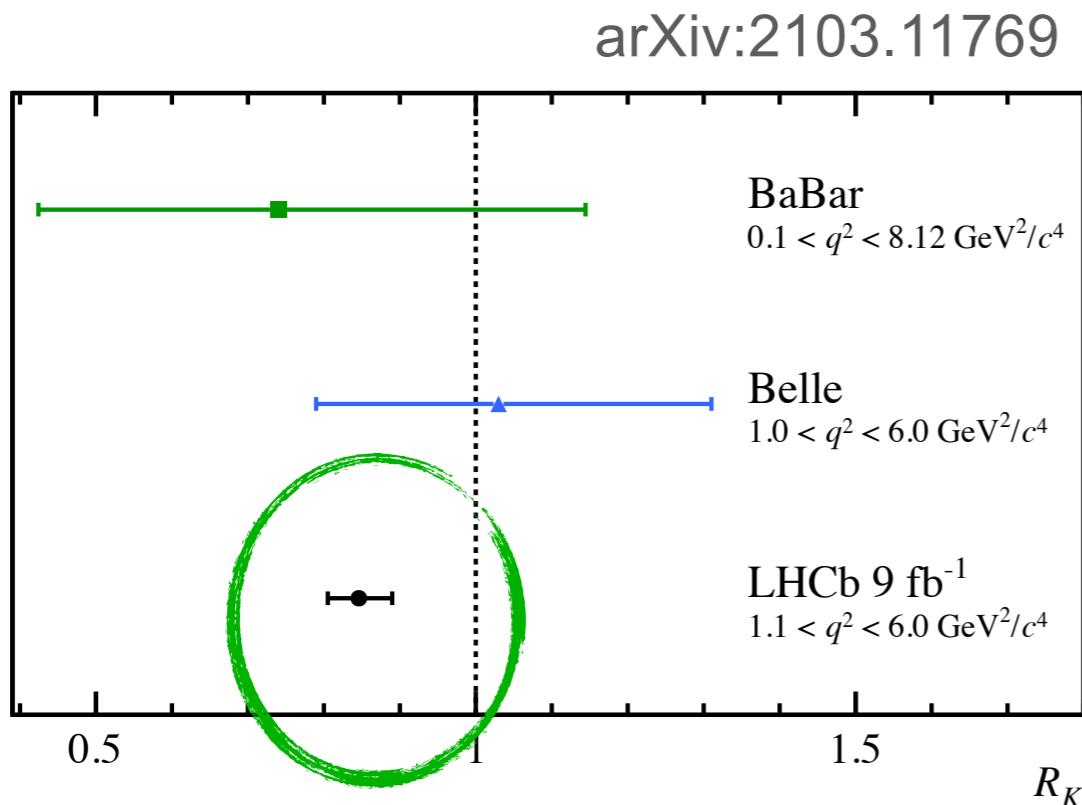
Although electrons more challenging, deviation from SM is largely due to the muon modes, not electrons

$$R_K(1.1 < q^2 < 6.0 \text{ GeV}^2/c^4) = 0.846^{+0.042}_{-0.039}{}^{+0.013}_{-0.012}$$

$$\frac{d\mathcal{B}(B^+ \rightarrow K^+ e^+ e^-)}{dq^2}(1.1 < q^2 < 6.0 \text{ GeV}^2/c^4) = (28.6^{+1.5}_{-1.4} \pm 1.3) \times 10^{-9} c^4/\text{GeV}^2$$

(arXiv:2103.11769)

Summary: Lepton Flavour Universality



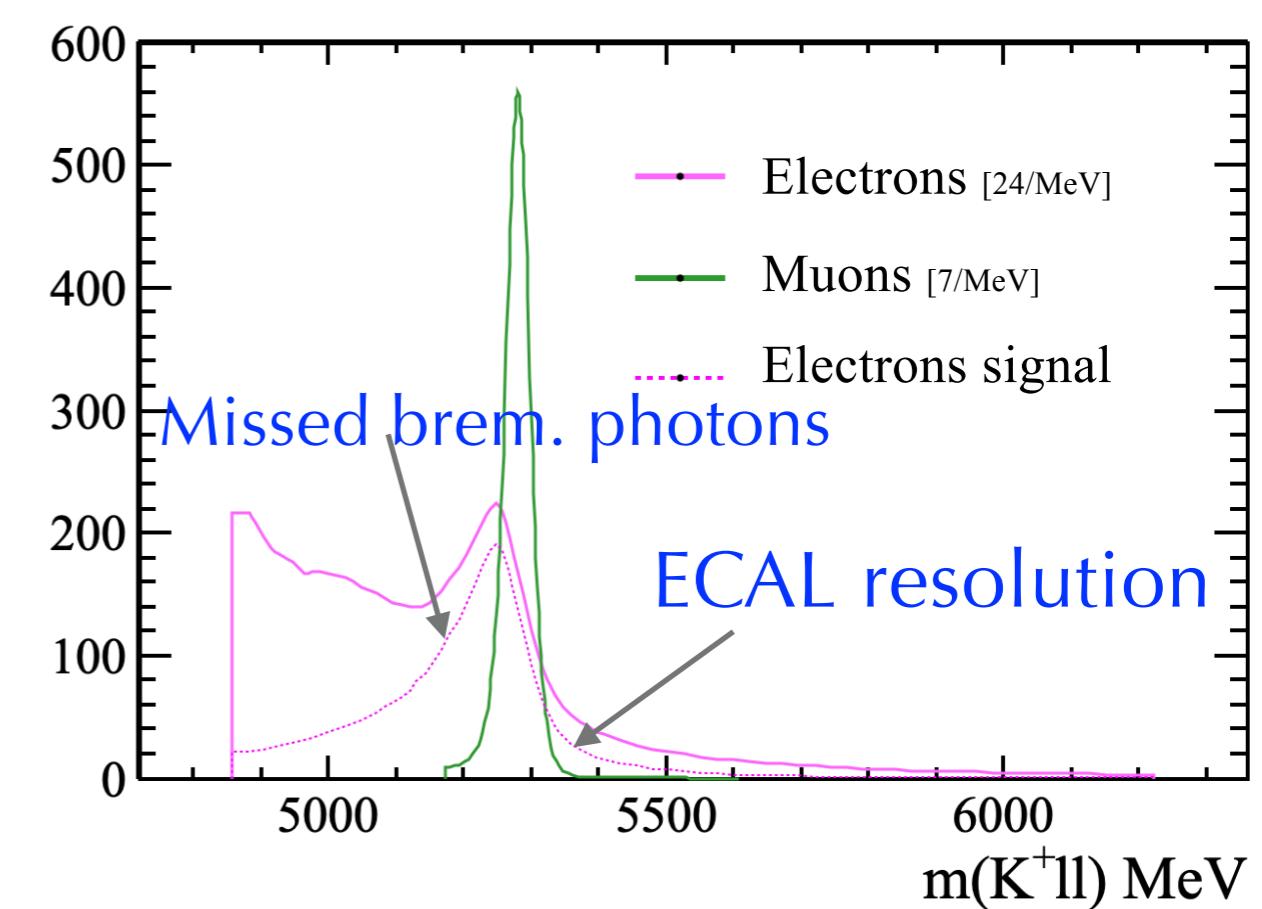
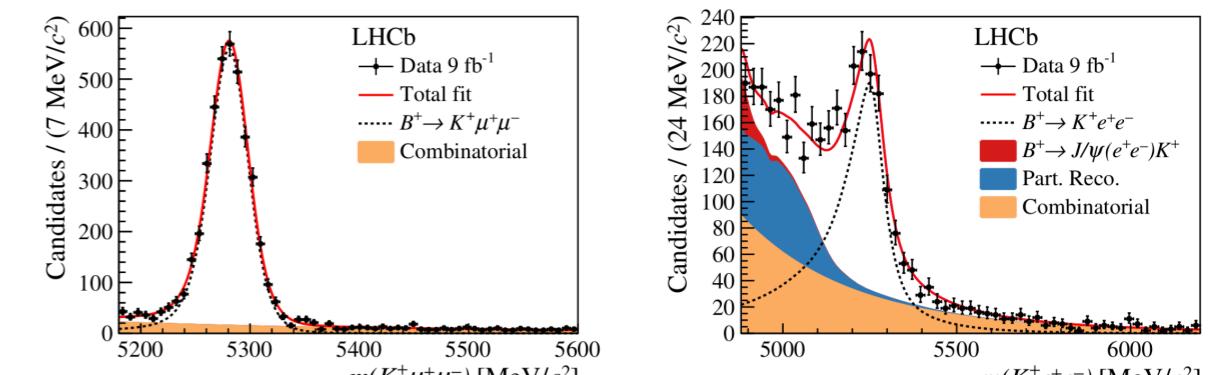
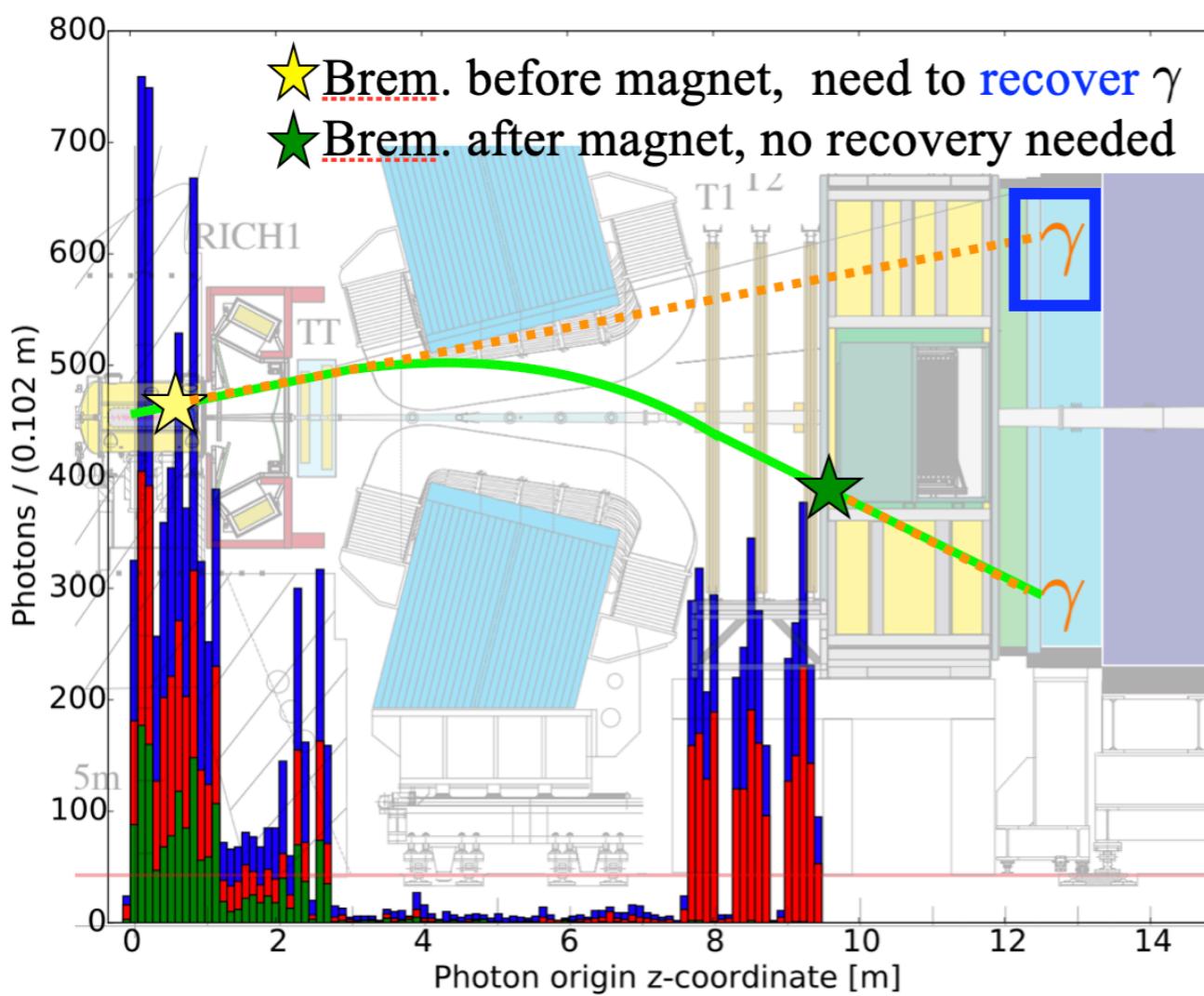
$\Lambda_b^0 \rightarrow p K \ell^+ \ell^-$: JHEP 2020, 40 (2020)

+ $R_{pK} = 0.86^{+0.14}_{-0.11} \pm 0.05$

Same pattern, ratios
below the SM prediction

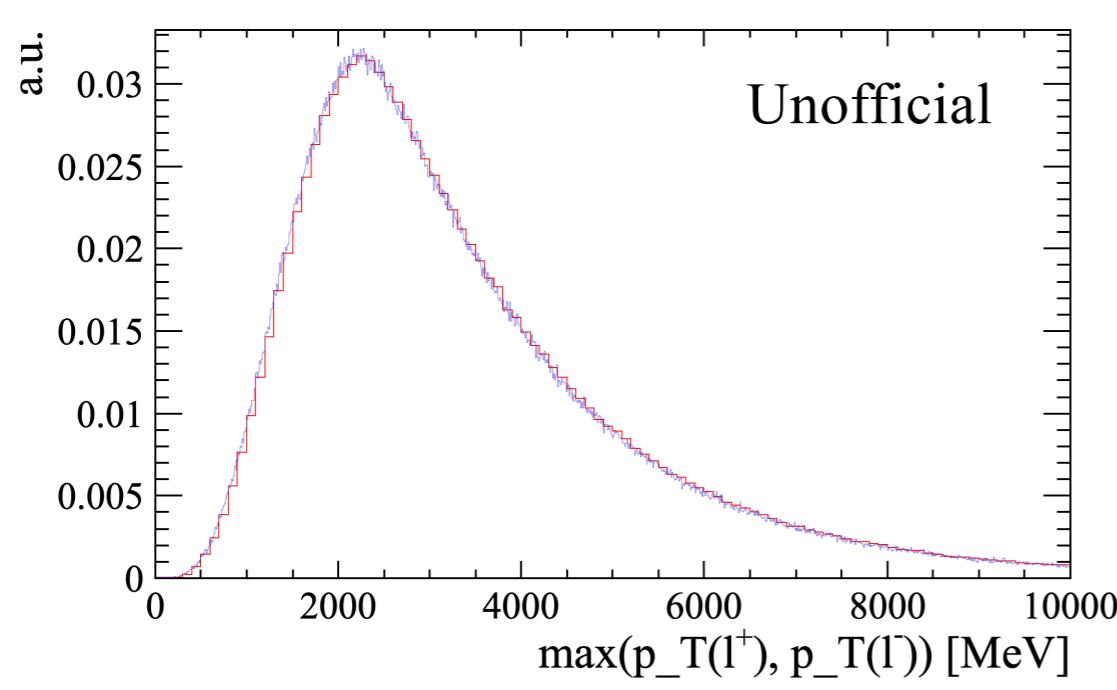
Measuring electrons: Bremsstrahlung

- Electrons at LHCb more challenging, smaller mass, much more Bremsstrahlung radiation

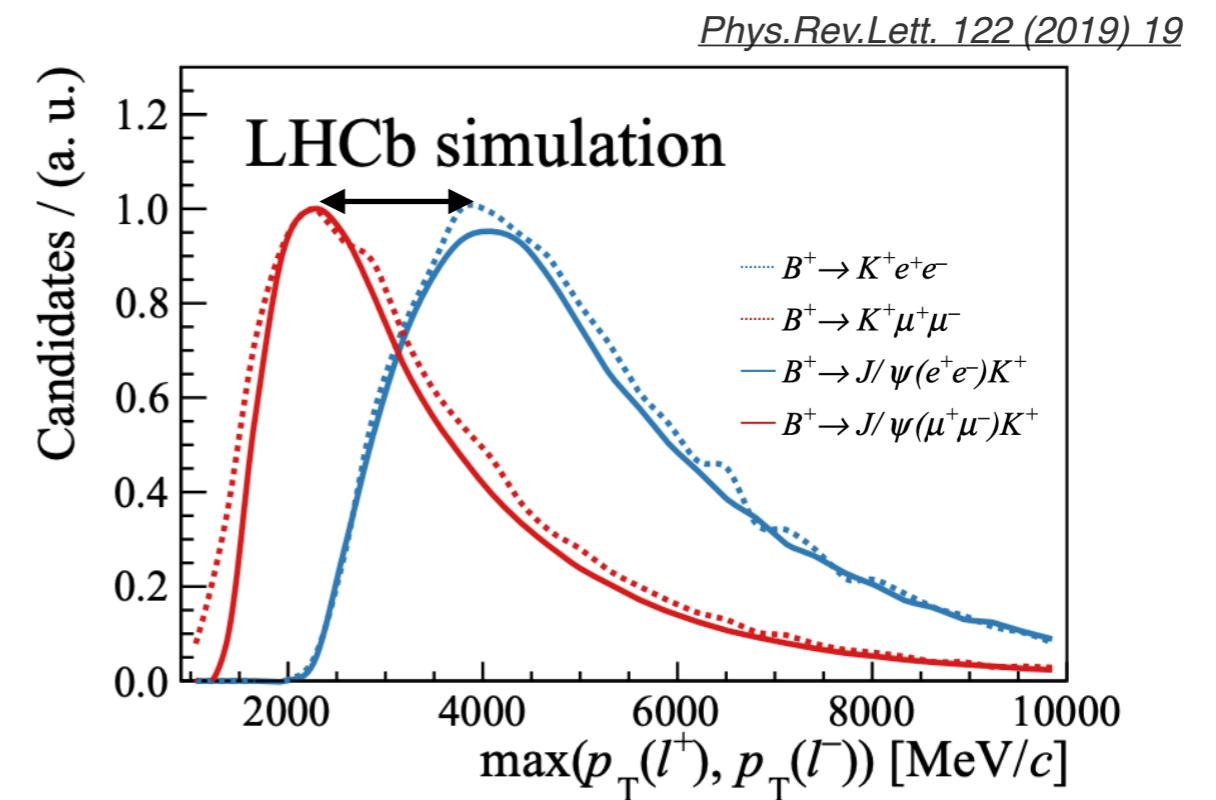


Measuring electrons: trigger

- Electrons are triggered via the signatures they leave in the ECAL
- High occupancy in the ECAL-> need higher trigger threshold to reduce throughput to acceptable level, **~40% of muon efficiency**



Before passing through detector

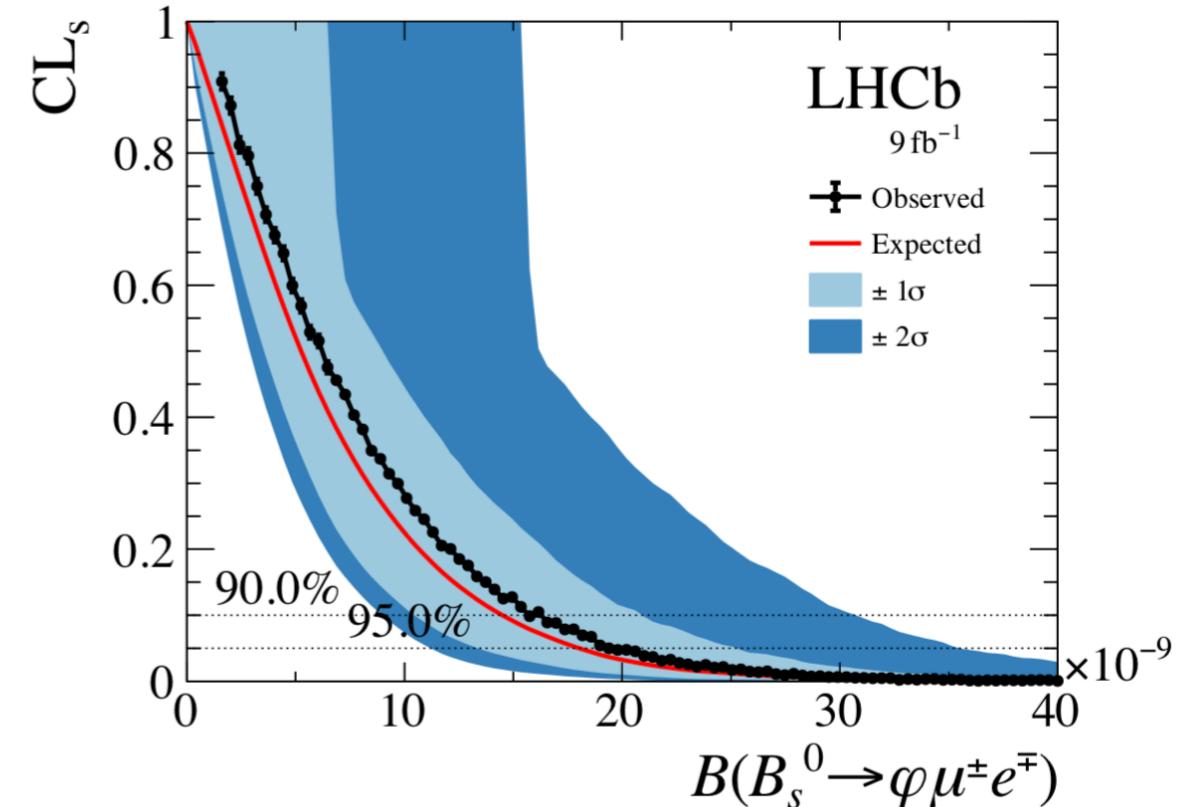
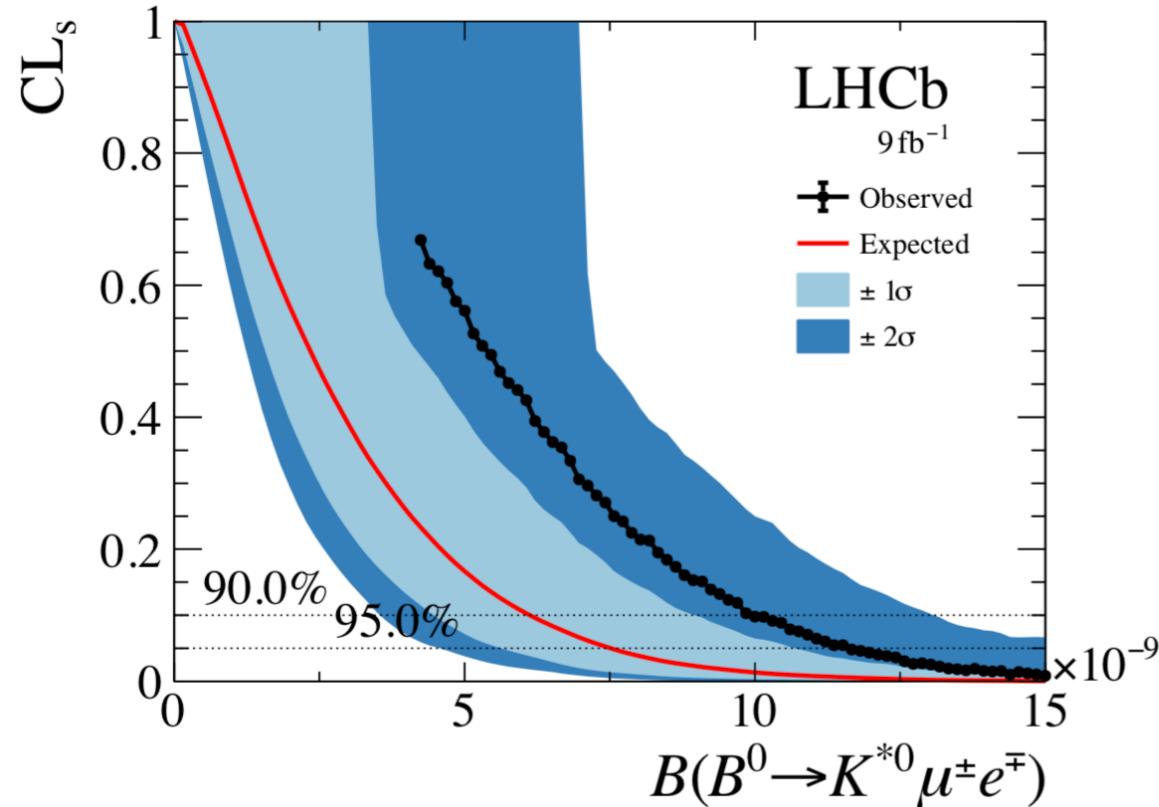


After trigger + selection

- Additionally, electrons loose energy through brem., increasing chance off being bent of acceptance by magnet

Tests of lepton flavour violation

- New preliminary results on $B^0 \rightarrow K^{*0} \mu^\pm e^\mp$, $B_s^0 \rightarrow \phi \mu^\pm e^\mp$



$$\mathcal{B}(B^0 \rightarrow K^{*0} \mu^+ e^-) < 5.7 \times 10^{-9} \quad (7.0 \times 10^{-9}),$$

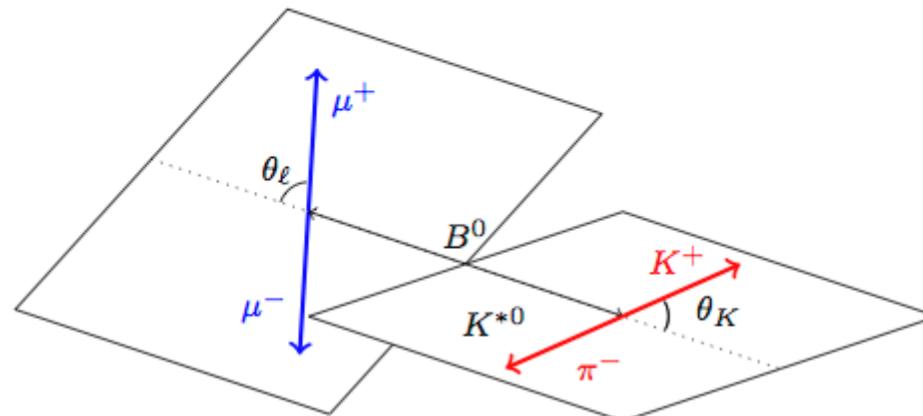
$$\mathcal{B}(B^0 \rightarrow K^{*0} \mu^- e^+) < 6.7 \times 10^{-9} \quad (7.9 \times 10^{-9}),$$

$$\mathcal{B}(B^0 \rightarrow K^{*0} \mu^\pm e^\mp) < 9.9 \times 10^{-9} \quad (11.6 \times 10^{-9}),$$

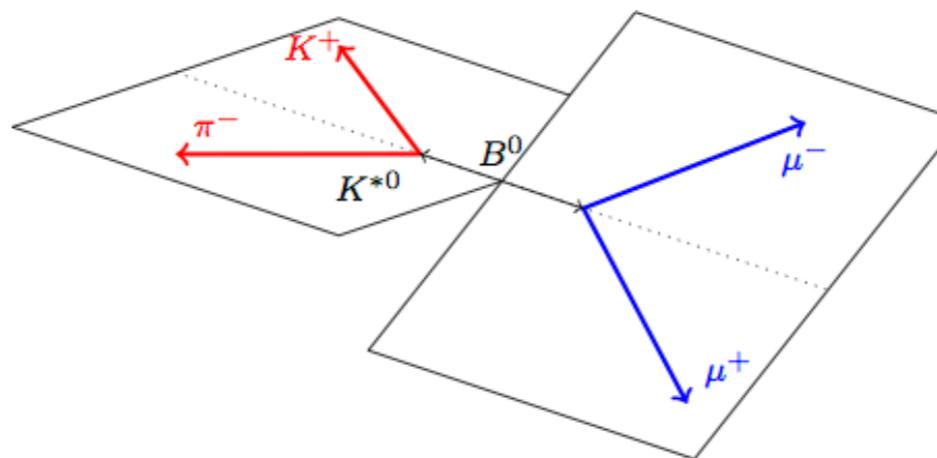
$$\mathcal{B}(B_s^0 \rightarrow \phi \mu^\pm e^\mp) < 15.9 \times 10^{-9} \quad (19.4 \times 10^{-9})$$

Angular analysis

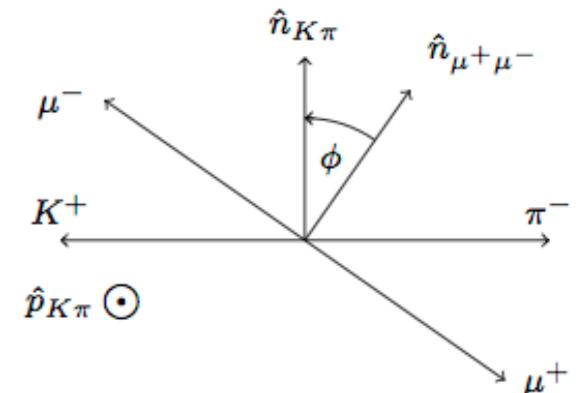
Angular analyses ($B \rightarrow V(\rightarrow hh)\ell^+\ell^-$)



(a) θ_K and θ_ℓ definitions for the B^0 decay



(b) ϕ definition for the B^0 decay



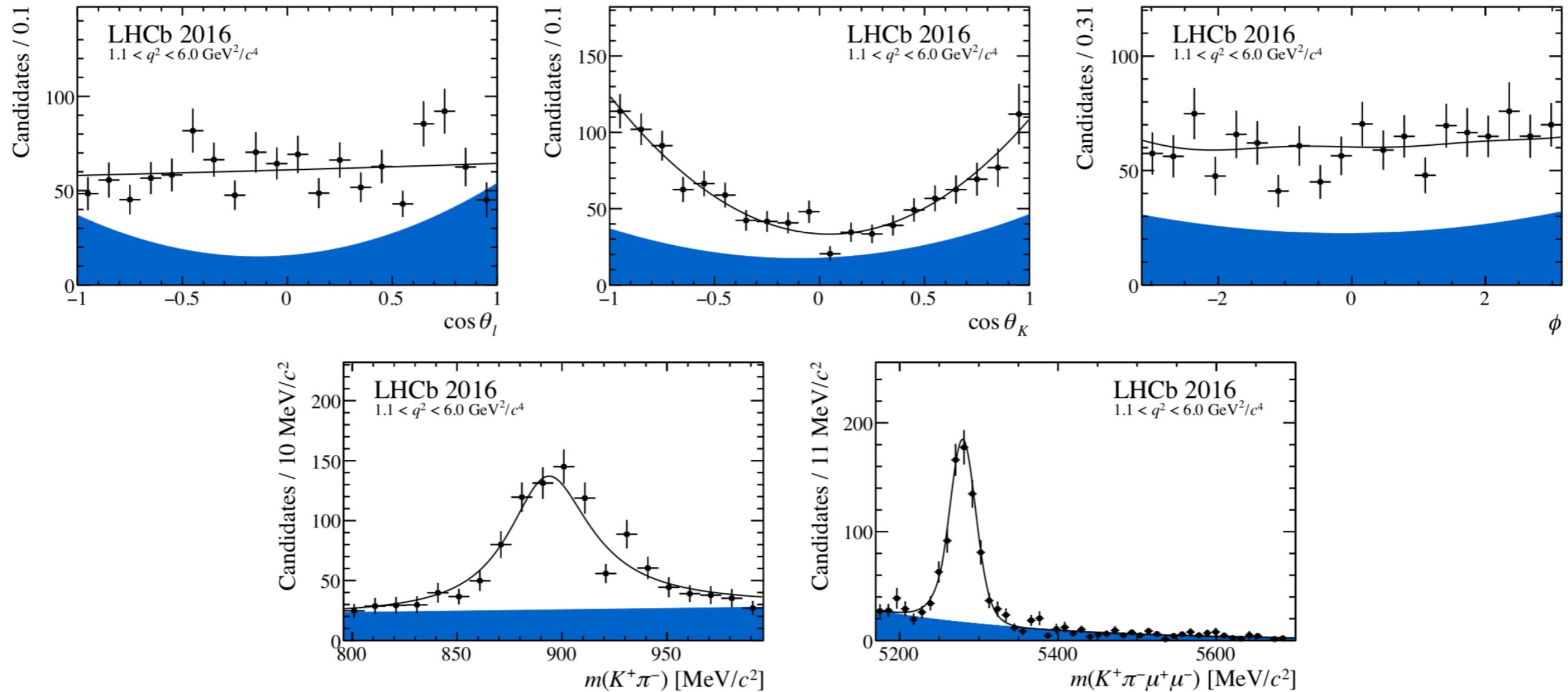
$\vdots S_i$ basis \vdots 8 q^2 dependent observables describe 4D (3 angles + q^2) distribution

$$\frac{1}{d(\Gamma + \bar{\Gamma})/dq^2} \left. \frac{d(\Gamma + \bar{\Gamma})}{dcos\theta_l \, dcos\theta_K \, d\phi} \right|_P = \frac{9}{32\pi} \left[\begin{aligned} & \frac{3}{4}(1 - F_L) \sin^2 \theta_K \\ & + F_L \cos^2 \theta_K + \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_l \\ & - F_L \cos^2 \theta_K \cos 2\theta_l + S_3 \sin^2 \theta_K \sin^2 \theta_l \cos 2\phi \\ & + S_4 \sin 2\theta_K \sin 2\theta_l \cos \phi + S_5 \sin 2\theta_K \sin \theta_l \cos \phi \\ & + \frac{4}{3} A_{FB} \sin^2 \theta_K \cos \theta_l + S_7 \sin 2\theta_K \sin \theta_l \sin \phi \\ & + S_8 \sin 2\theta_K \sin 2\theta_l \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_l \sin 2\phi \end{aligned} \right]. \quad (29)$$

F_L : fraction of longitudinal polarisation

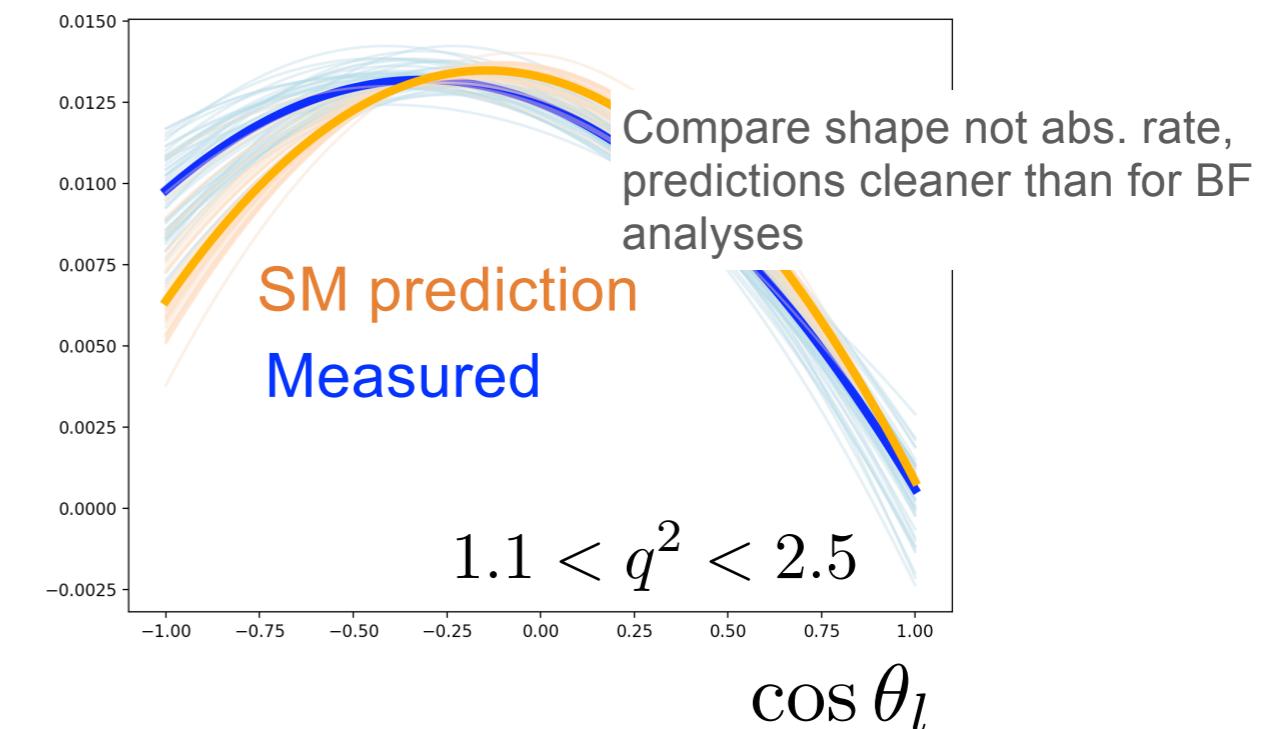
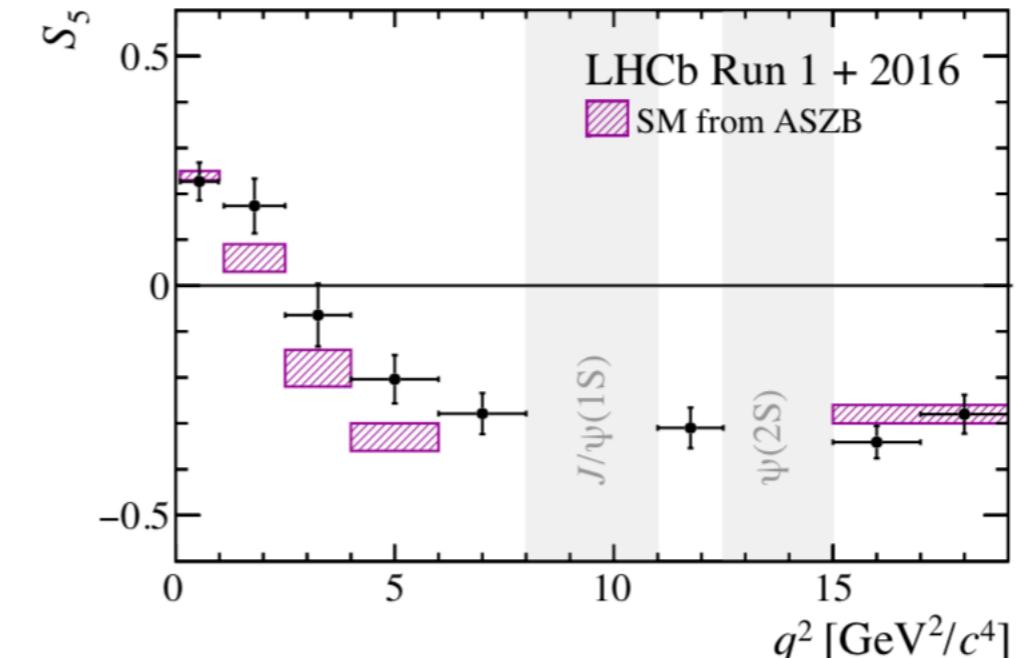
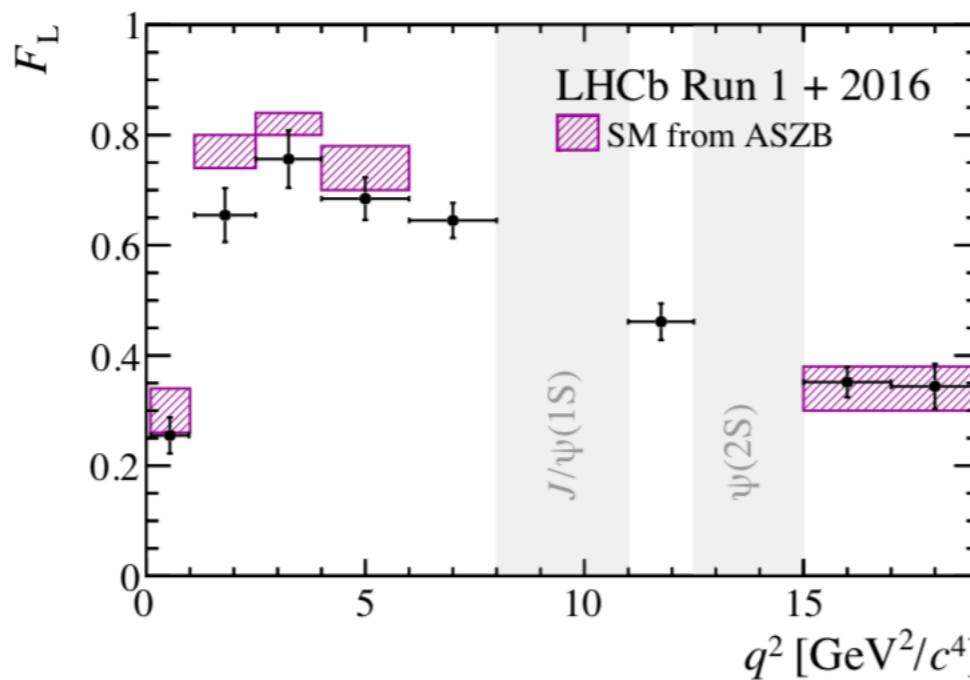
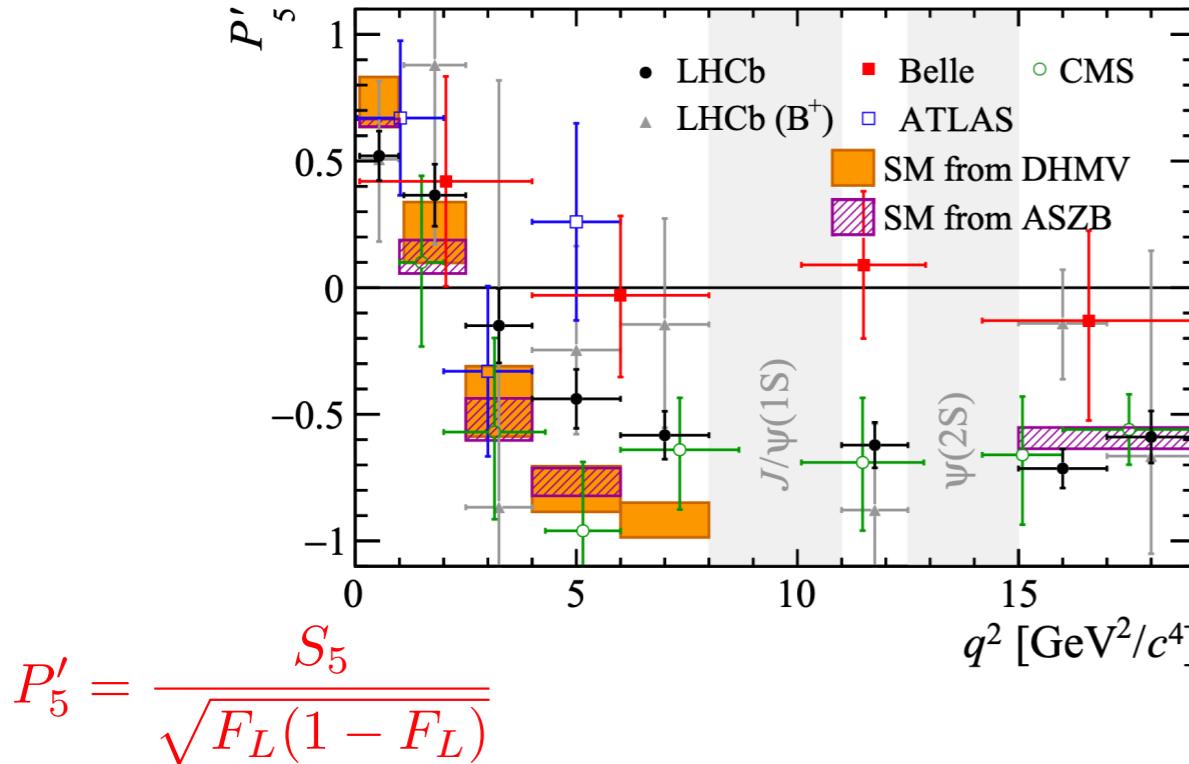
A_{FB} : forward-backward asymmetry of di-muon system

Example of projections from $B^0 \rightarrow K^{*0}(\rightarrow K^+\pi^-)\mu^+\mu^-$



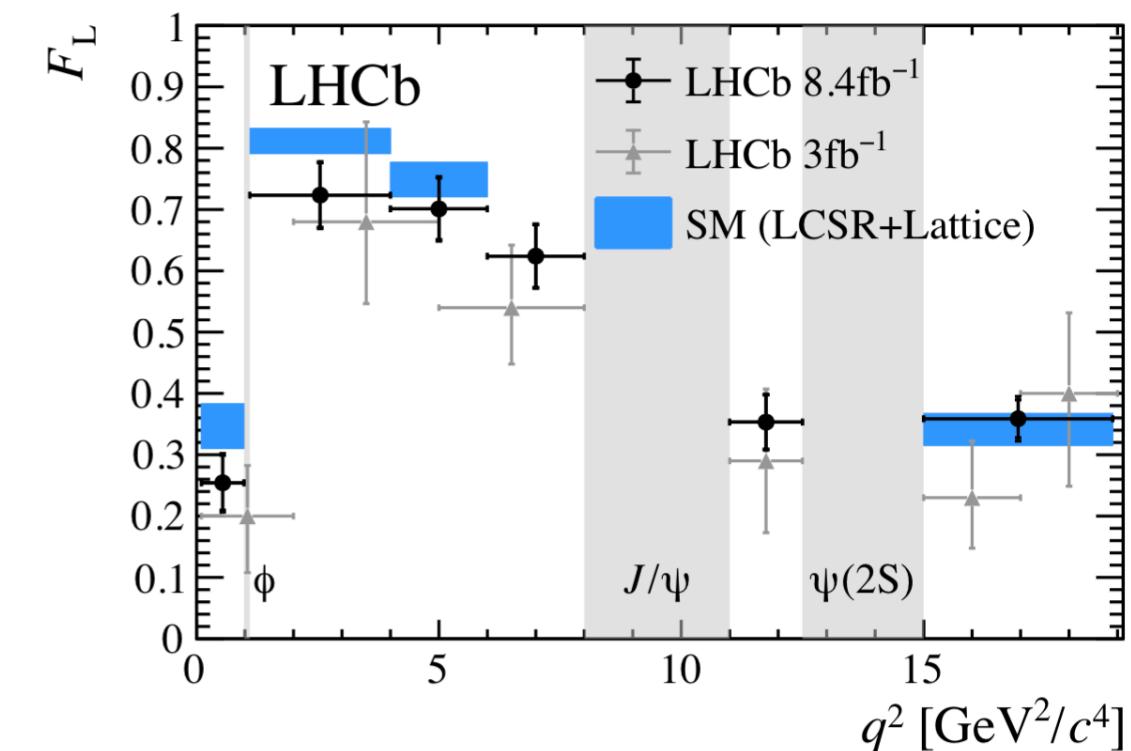
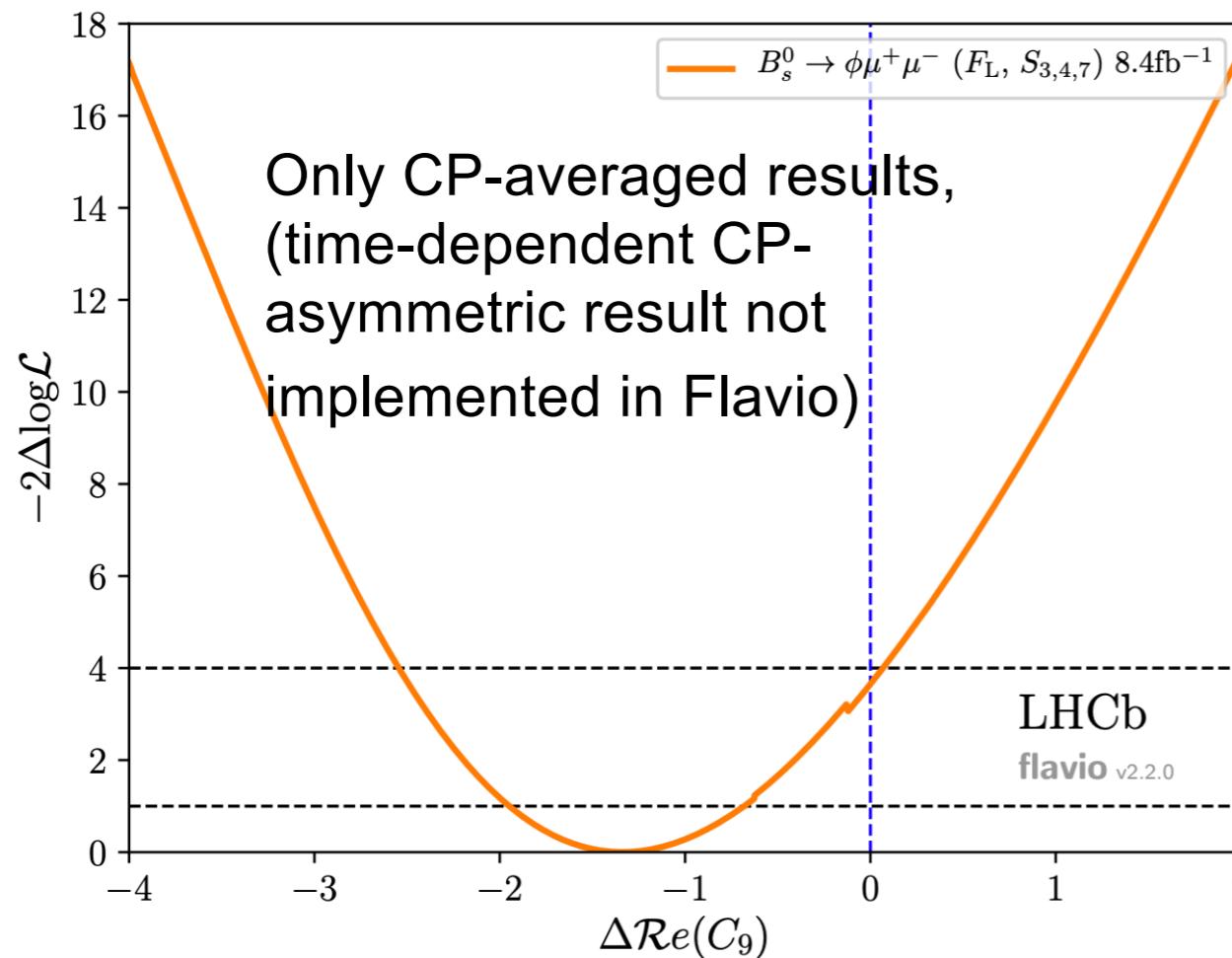
Example of results from $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

LHCb B0 PRL 125, 011802 (2020) . LHCb B+ PRL 161802 (2021) ATLAS: JHEP 10 (2018) 047
 Belle: PRL 118 (2017), CMS:PLB 781 (2018) 517541



Results from $B_s^0 \rightarrow \phi(\rightarrow K^+K^-)\mu^+\mu^-$

Flavour-symmetric final-state, can only measure CP-averages (asymmetries) for CP-even (odd) terms, no P'_5 term as CP-odd



Summary of angular analyses (LHCb)

$$B_s^0 \rightarrow \phi \mu^+ \mu^-$$

$$\Delta \mathcal{R}e(\mathcal{C}_9) = -1.3^{+0.7}_{-0.6}$$

$$B^+ \rightarrow K^{*+} \mu^+ \mu^-$$

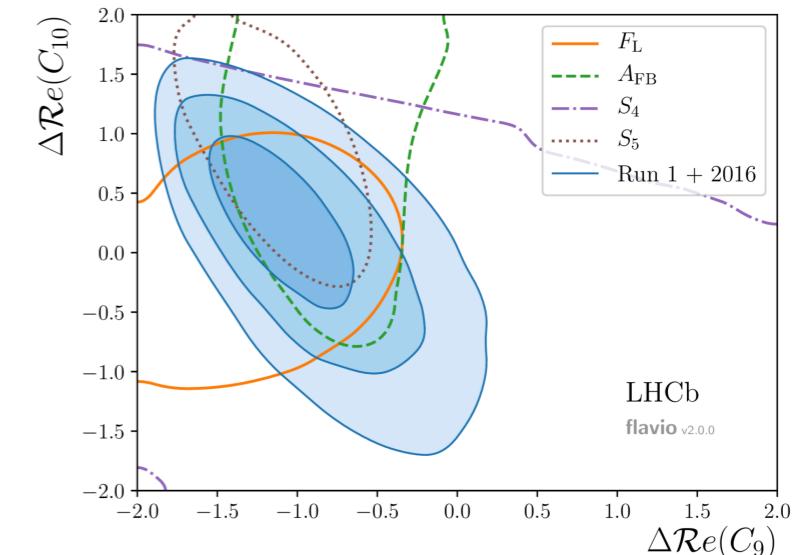
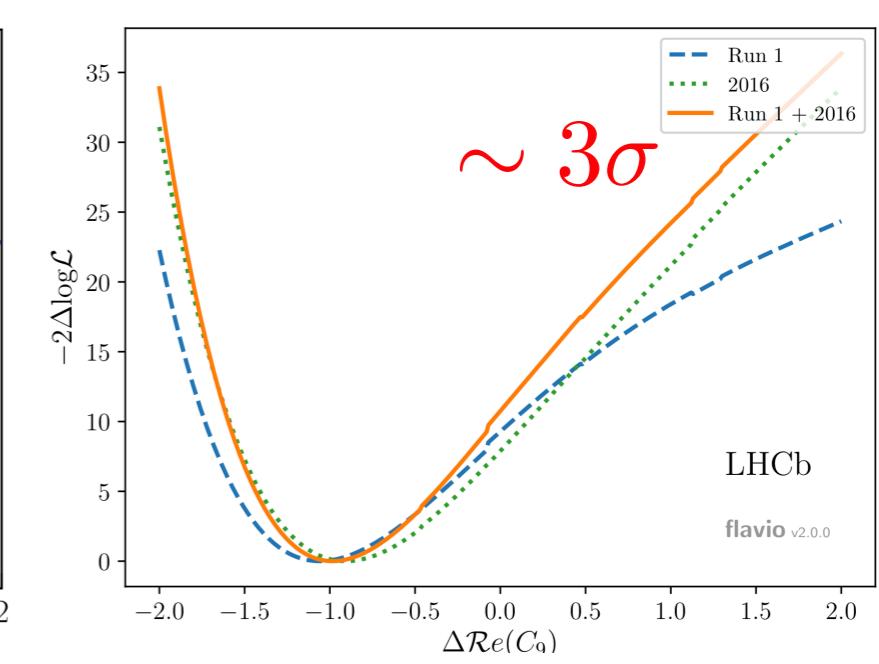
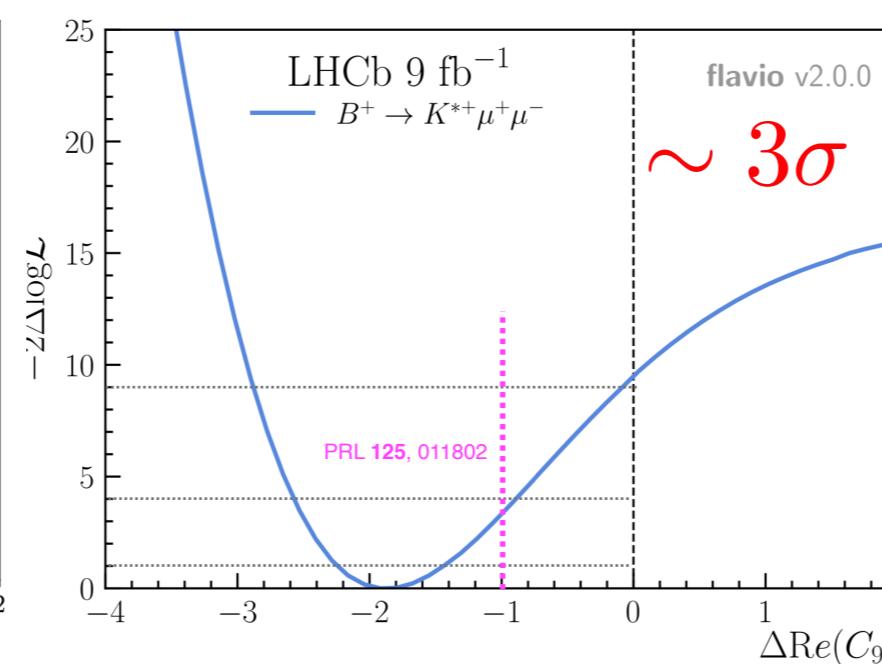
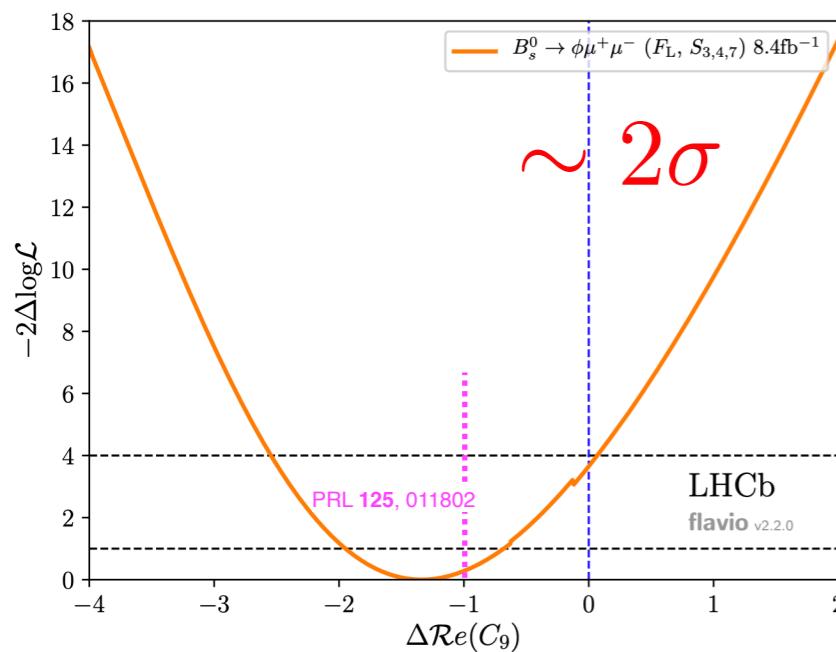
$$\Delta \mathcal{R}e(\mathcal{C}_9) = -1.9$$

Phys. Rev. Lett. **126**, 161802

$$B^0 \rightarrow K^{*0} \mu^+ \mu^-$$

$$\Delta \mathcal{R}e(\mathcal{C}_9) = -0.99^{+0.25}_{-0.21}$$

Phys. Rev. Lett. **125**, 011802

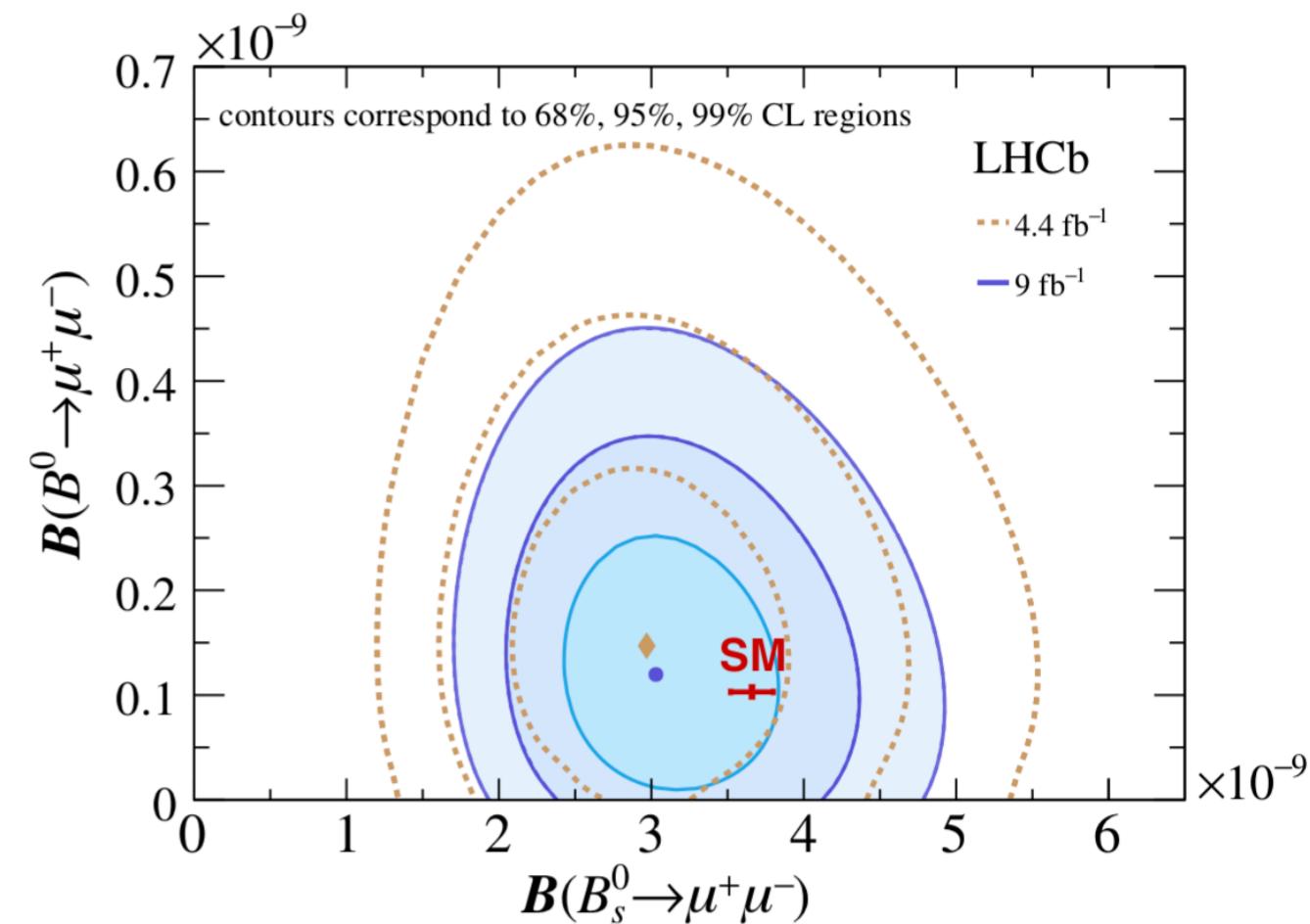
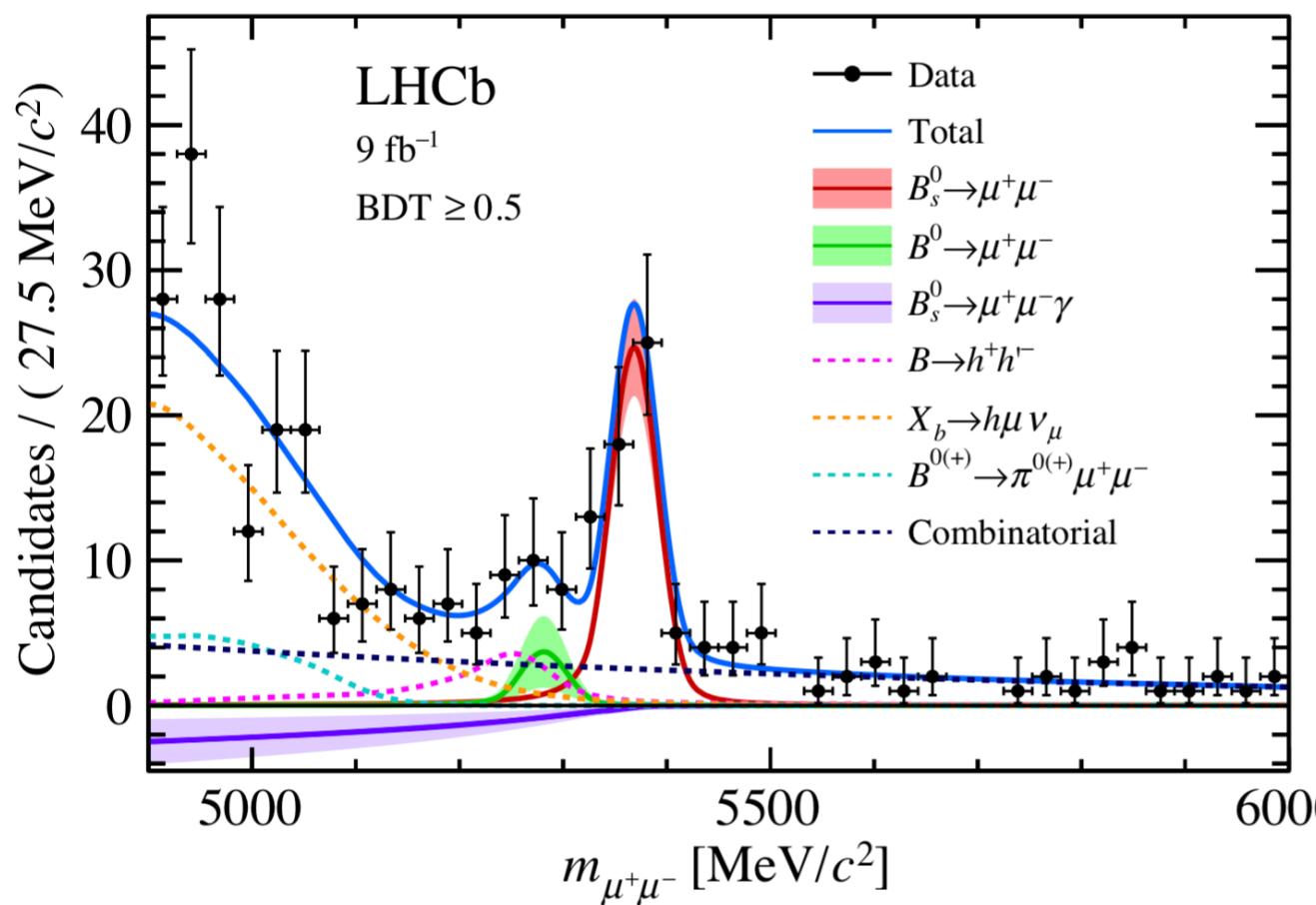


- Compare all 8 angular observables to SM using the underlying WC's
- Look at shift from the SM $\Delta \mathcal{R}e(\mathcal{C}_9) = 0$

Branching fractions

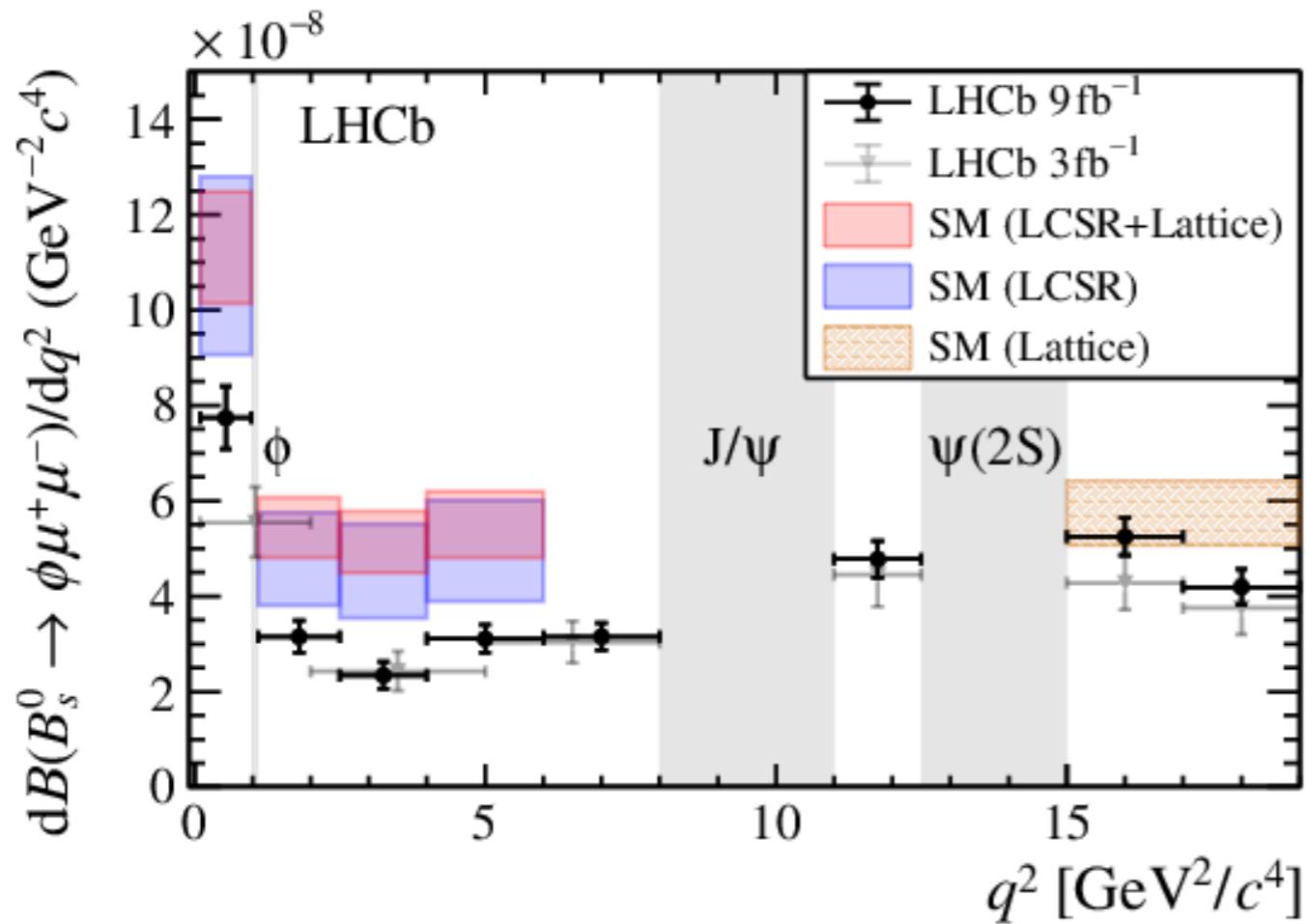
$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-)$

[PRL 128, (2022) 041801]



- Full Run 1 and Run 2 data sample
- Effective lifetime also measured: $2.07 \pm 0.29 \pm 0.03 \text{ ps}$

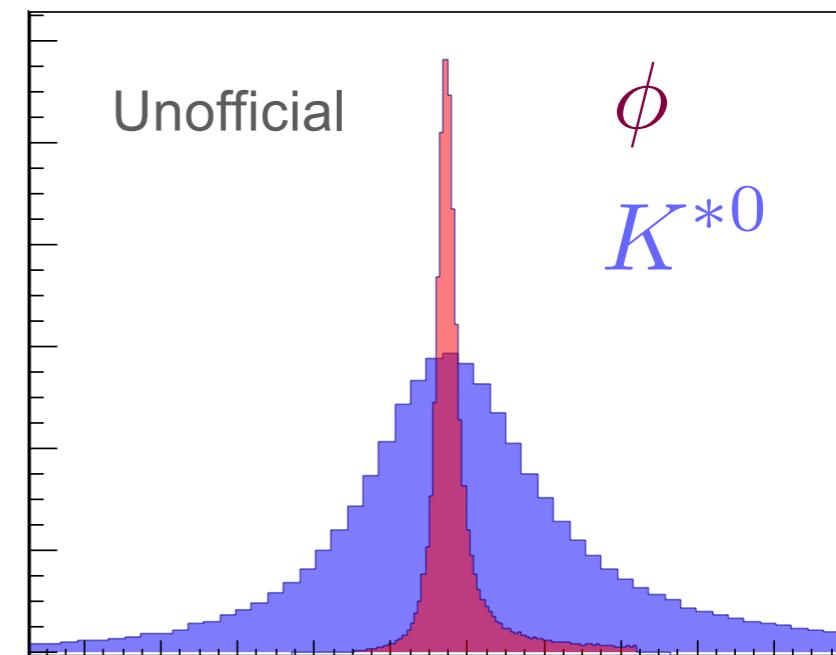
$\mathcal{B}(B_s^0 \rightarrow \phi \mu^+ \mu^-)$



$q^2 \in [1.1, 6.0] \quad d\mathcal{B}(B_s^0 \rightarrow \phi \mu^+ \mu^-)/dq^2 = (2.88 \pm 0.21) \times 10^{-8} \text{ GeV}^2/\text{c}^4$

Tension with SM at **3.6 σ (LCSR+Lattice)** and **1.8 σ (LCSR)**

- WC pulled further from SM when adding to global fits, but overall significance drops
- Use inclusive Vcb for SM prediction



Narrow width approximation more valid
Less background

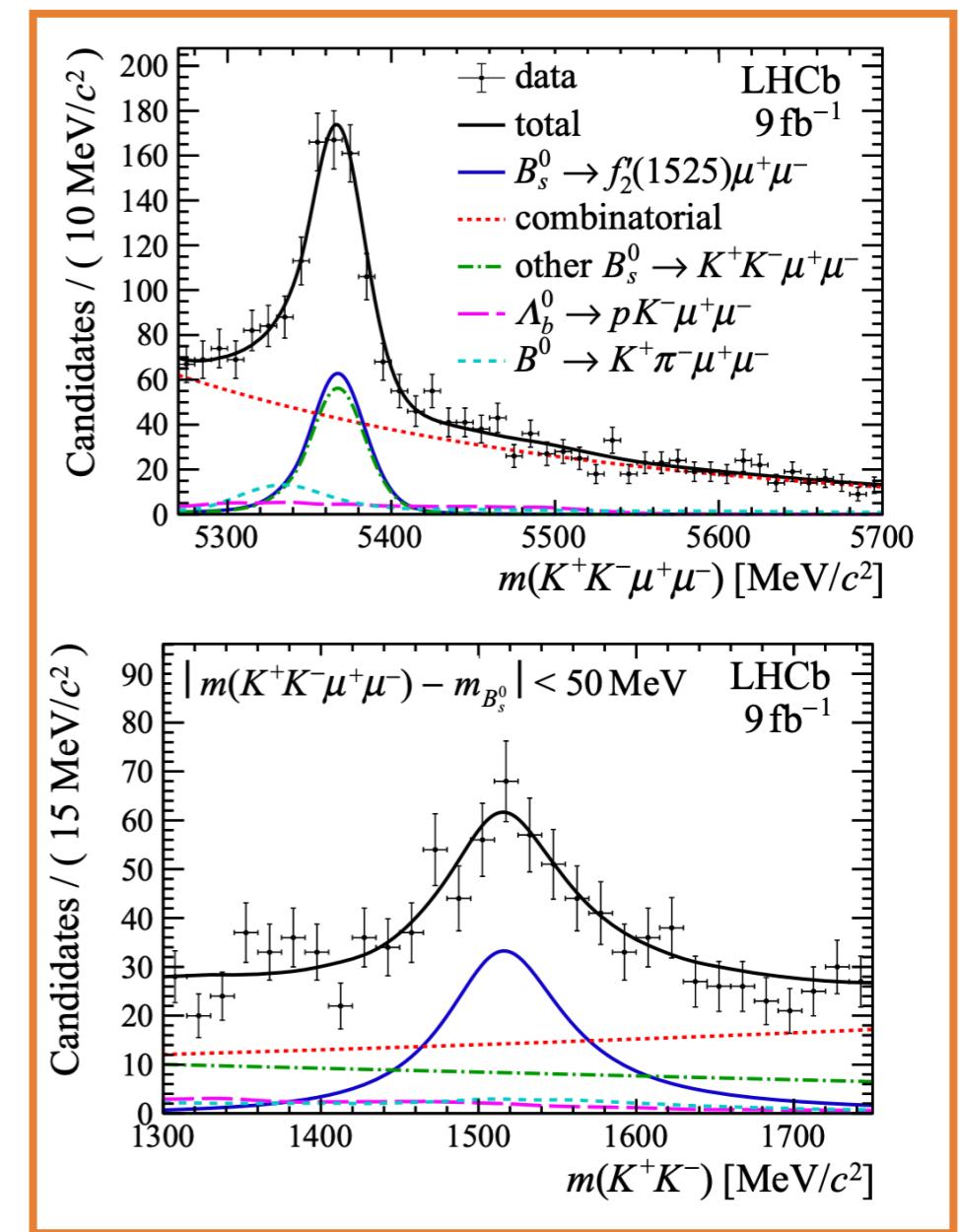
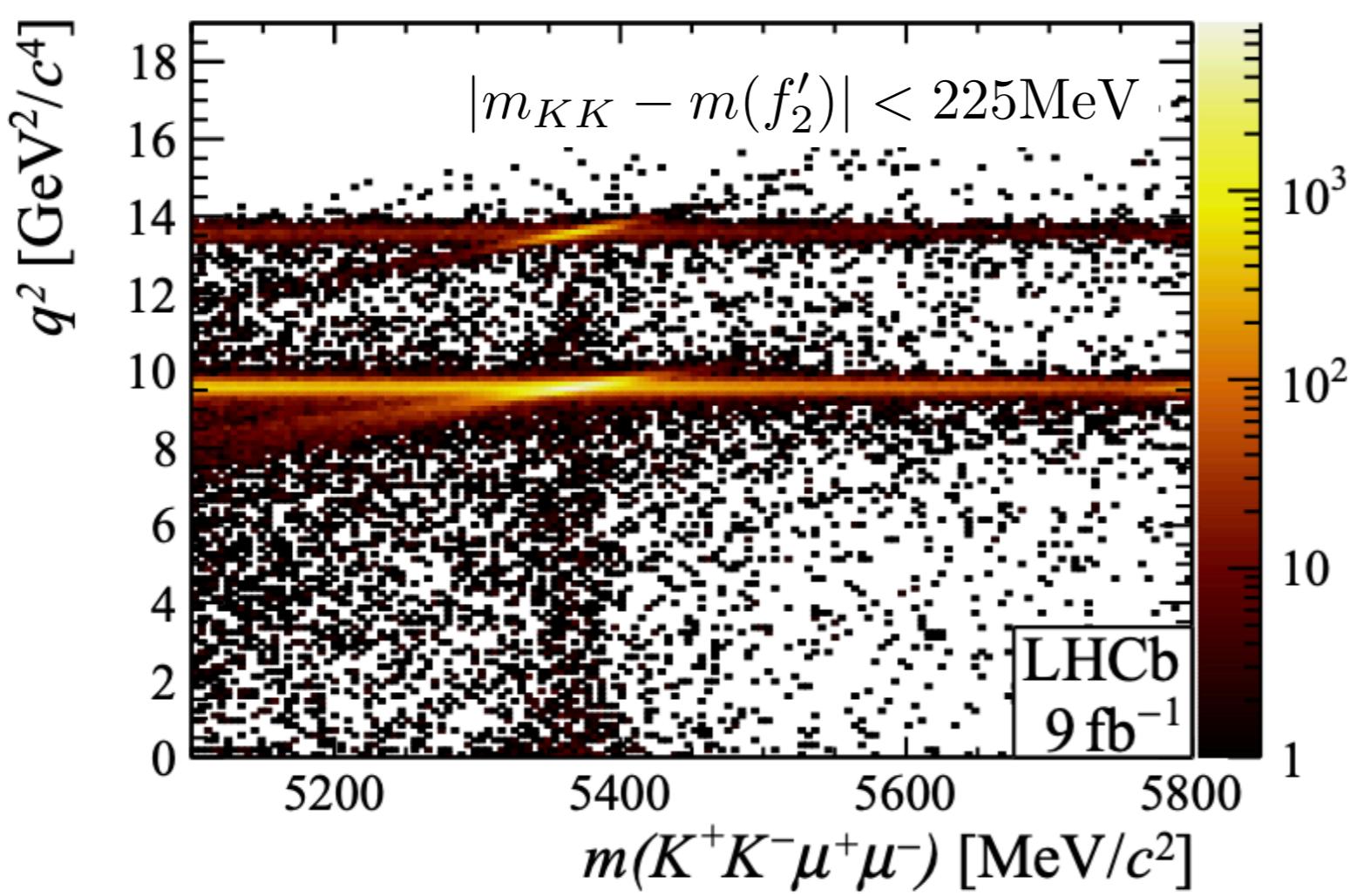
$$\mathcal{B}(B_s^0 \rightarrow f_2' \mu^+ \mu^-)$$

- Same final state, higher dikaon mass, **first observation of a spin-2 FCNC**

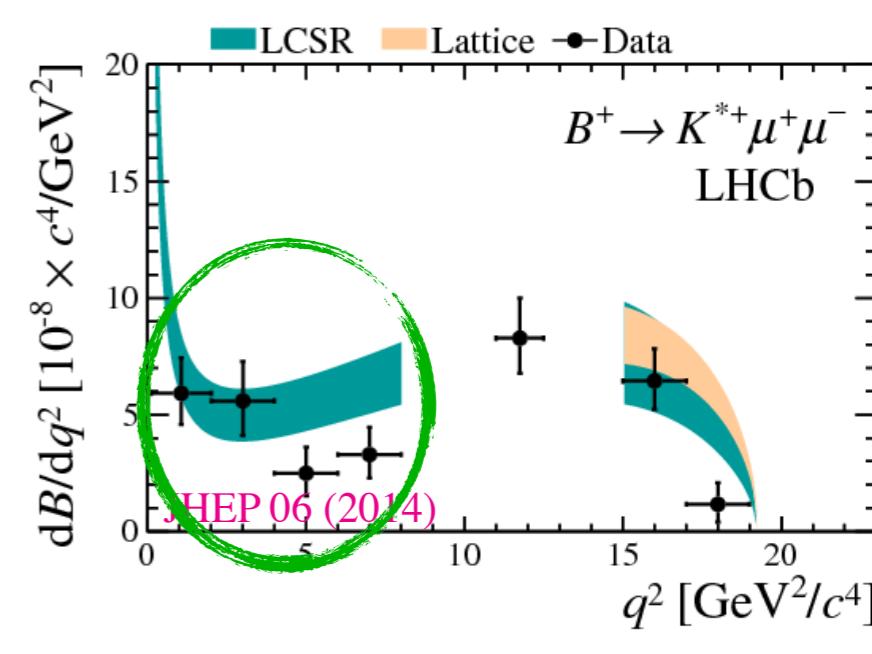
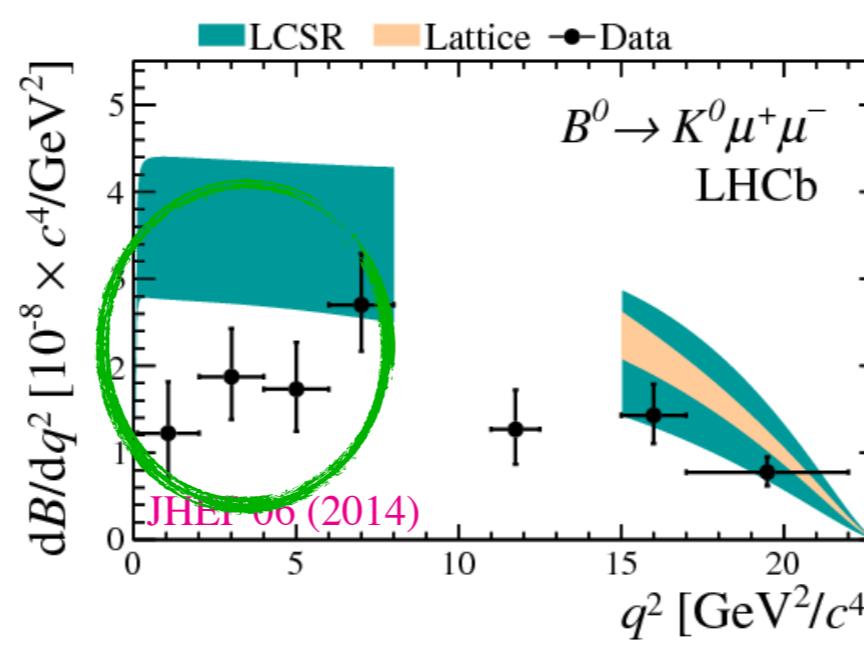
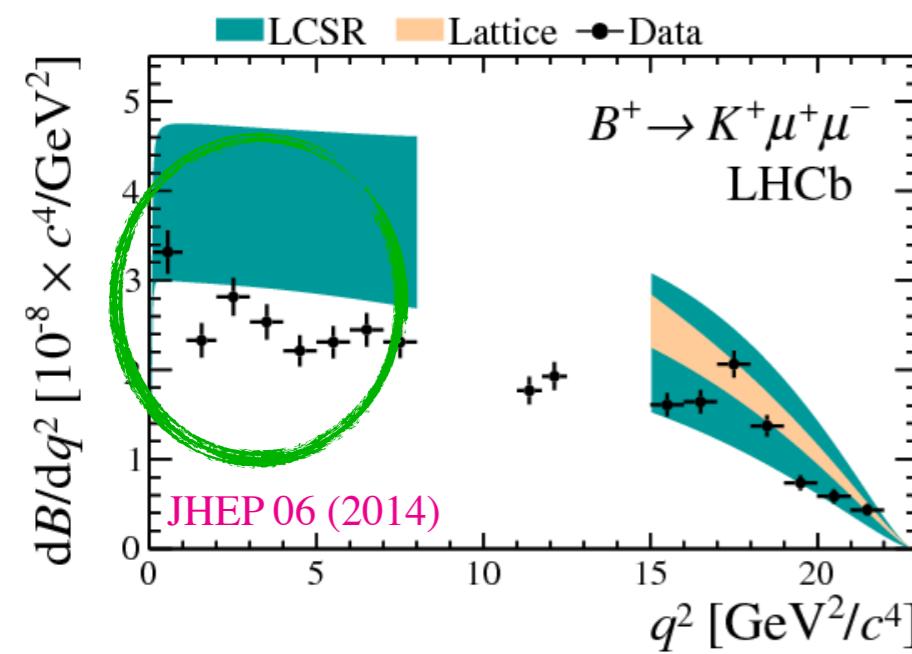
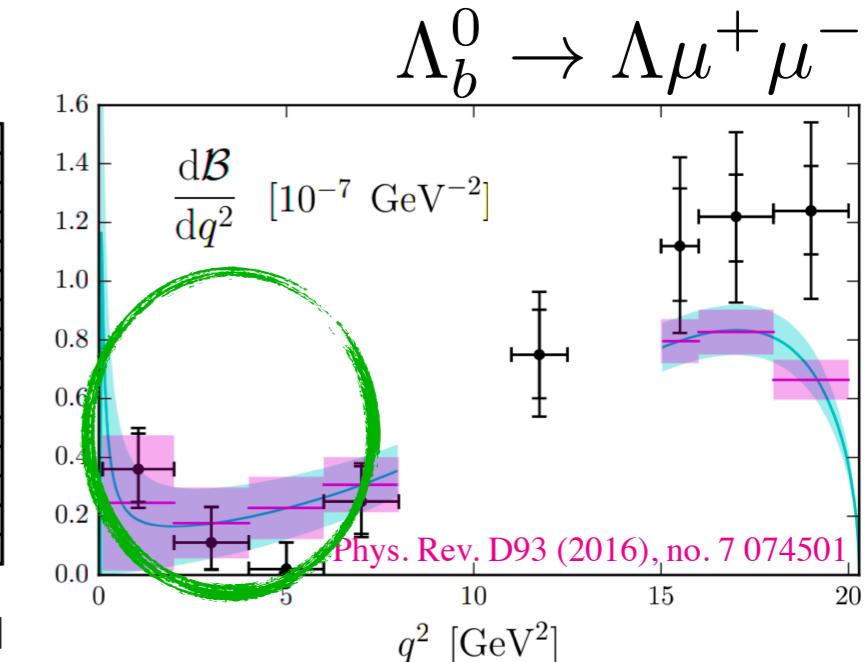
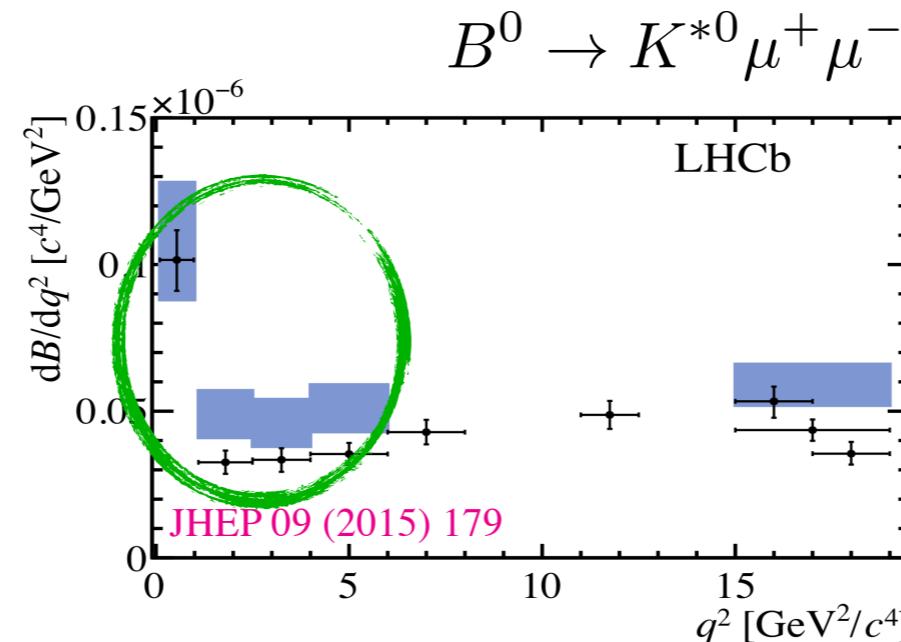
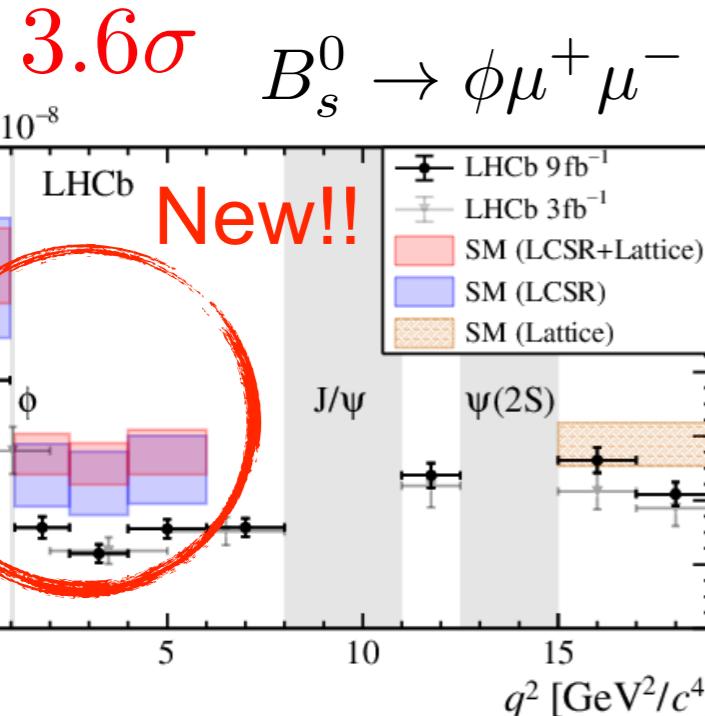
$$\mathcal{B}(B_s^0 \rightarrow f_2' \mu^+ \mu^-) = (1.57 \pm 0.19 \pm 0.06 \pm 0.06 \pm 0.08) \times 10^{-7}$$

$$\text{SM: } 1.2 - 1.7 \times 10^{-7}$$

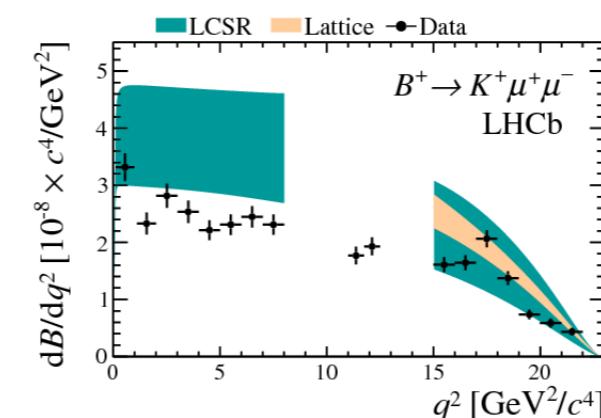
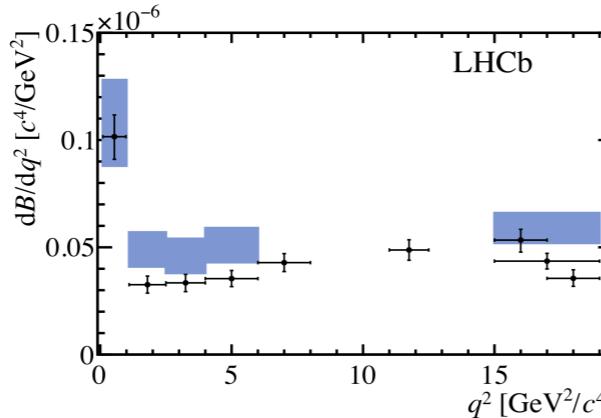
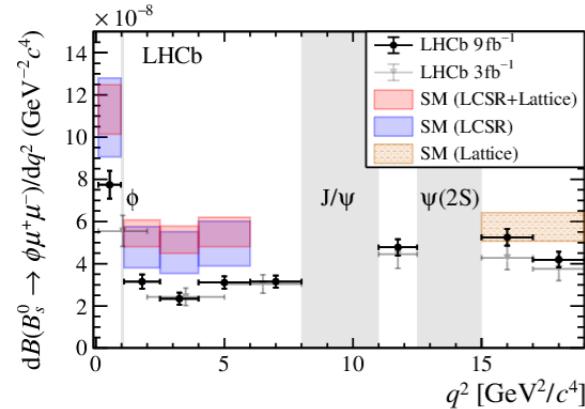
[Phys. Rev. D83 (2011) 034034, Eur. Phys. J. C81 (2021) 30, arXiv: 2009.06213v2]



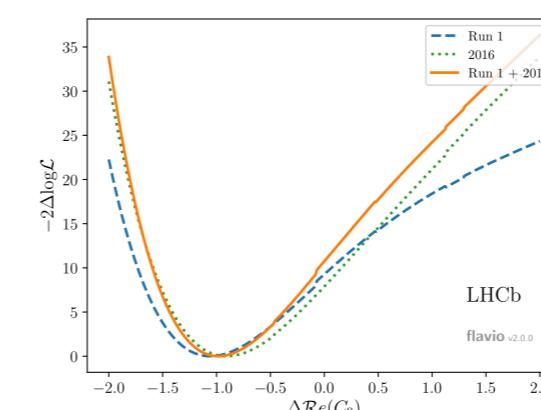
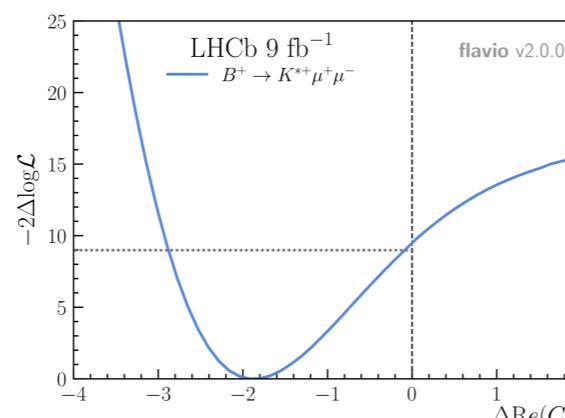
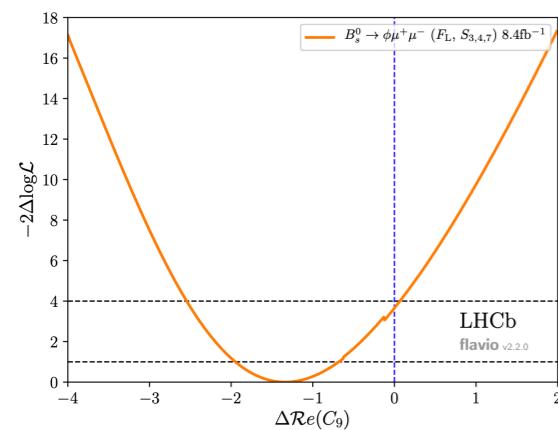
Branching fractions summary



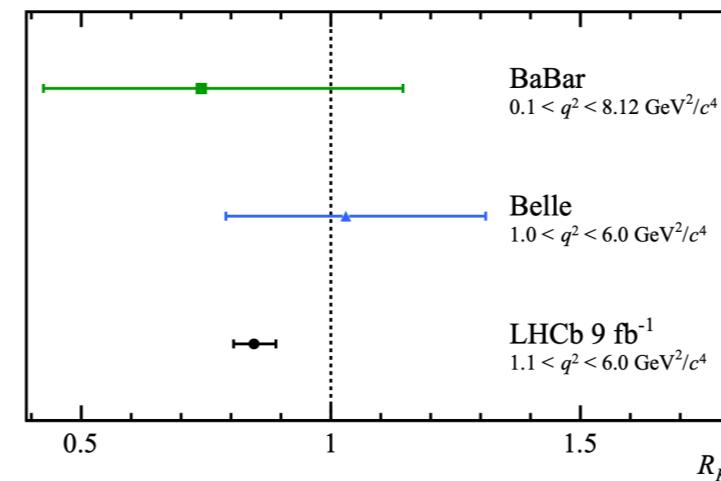
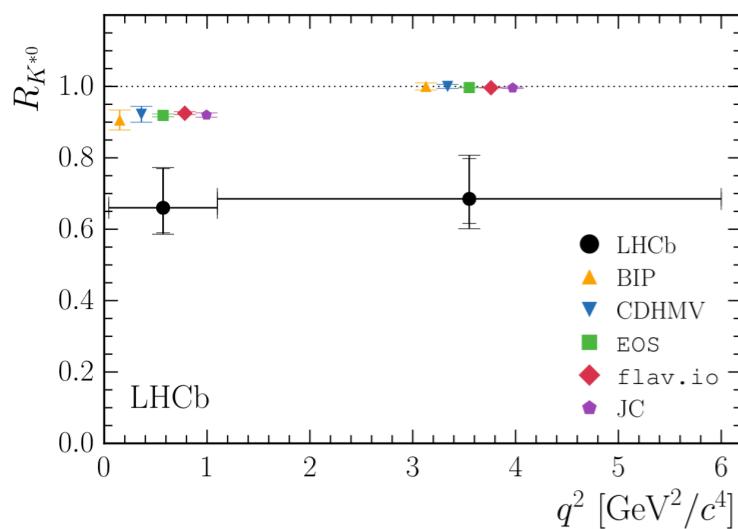
Interim recap: what $b \rightarrow s\ell^+\ell^-$ observables we have



Branching fractions
 $> 3\sigma$

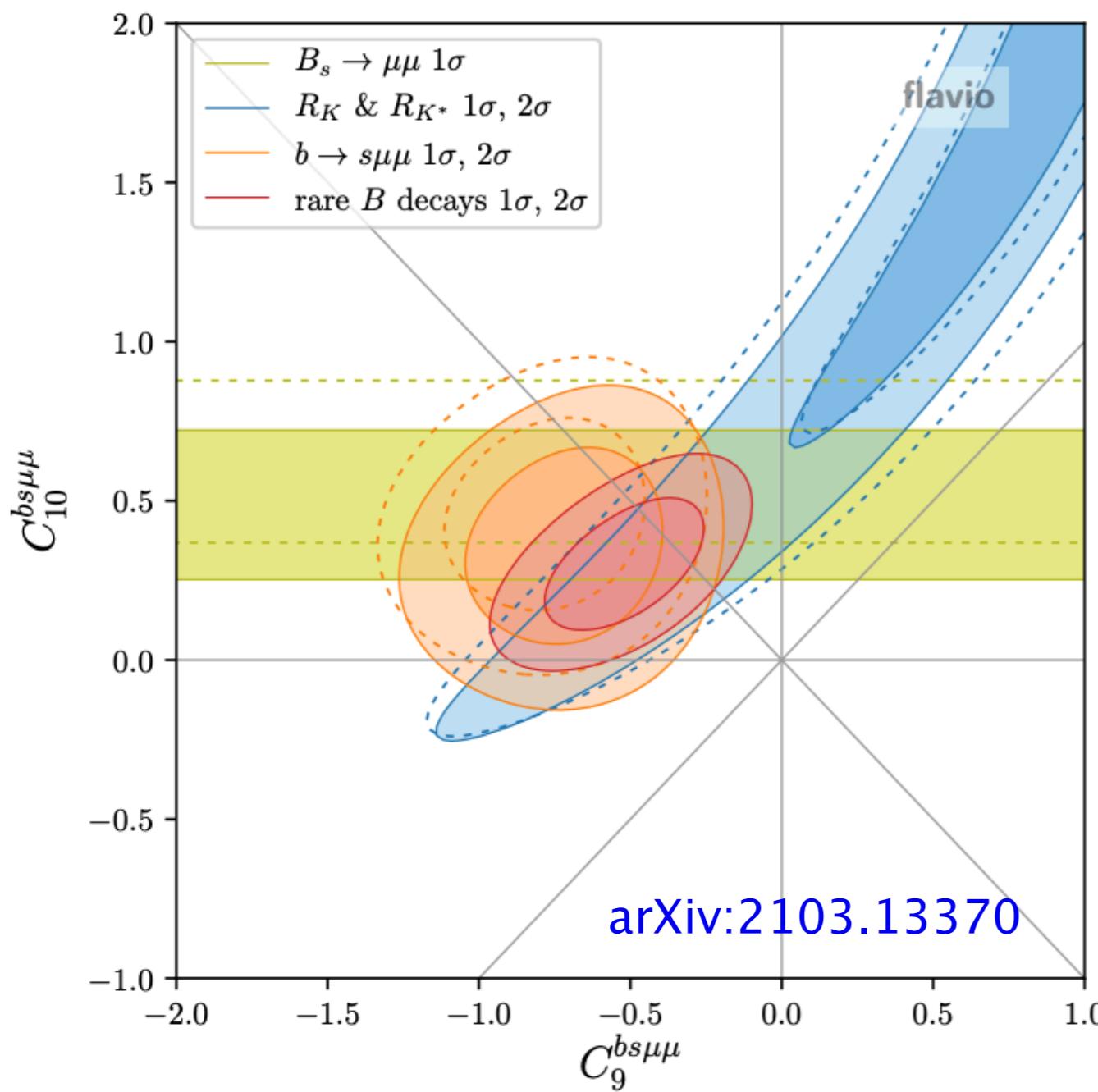


Angular analysis
 $> 3\sigma$



Lepton Flavour Universality (LFU)
 $> 3\sigma$

Global fits summary



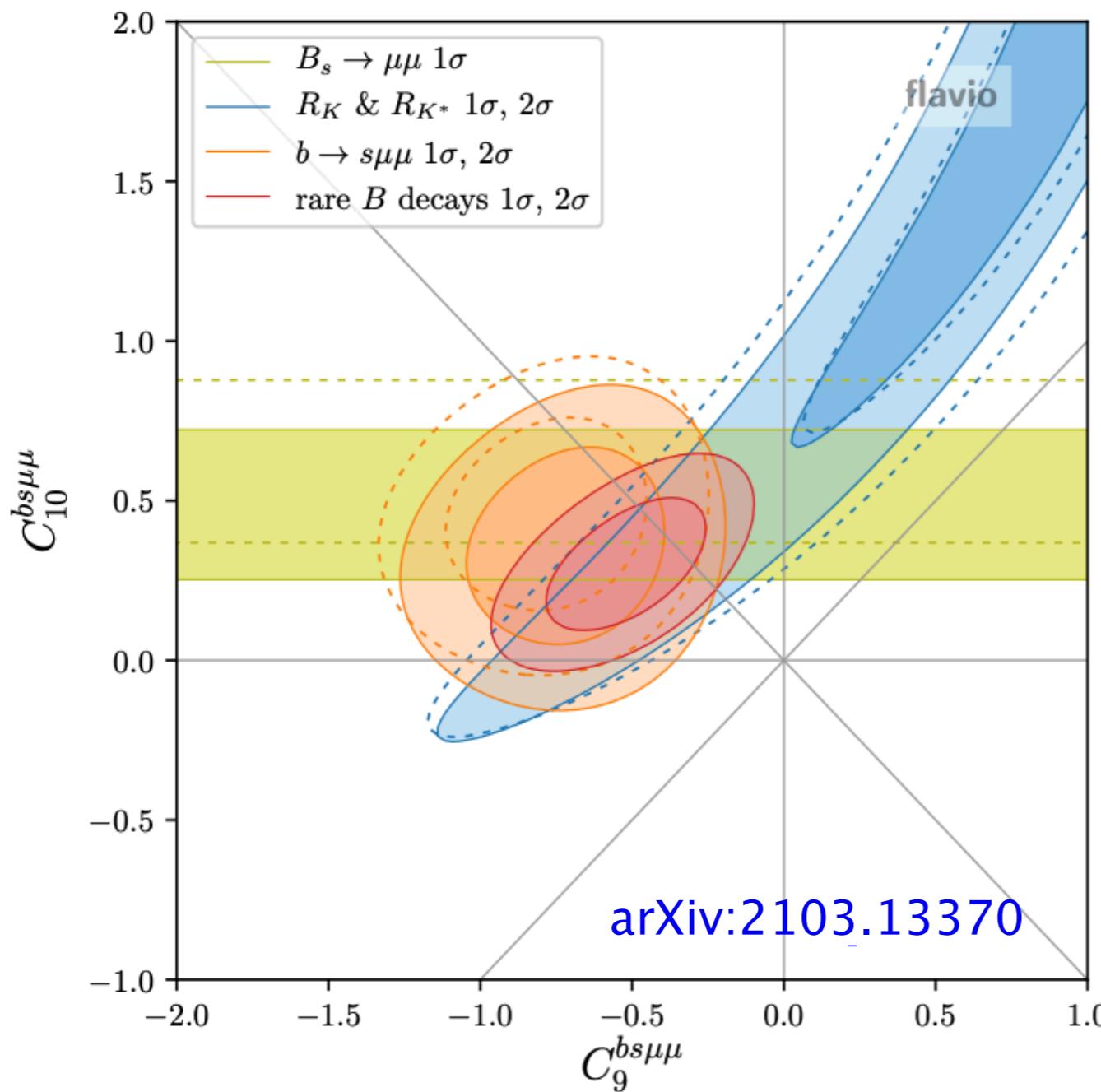
Lepton Flavour Universality

$$R(X) = \frac{\mathcal{B}(B \rightarrow X\mu\mu)}{\mathcal{B}(B \rightarrow Xee)}$$

Very precisely known in SM

Gives a 4 σ tension

Global fits summary



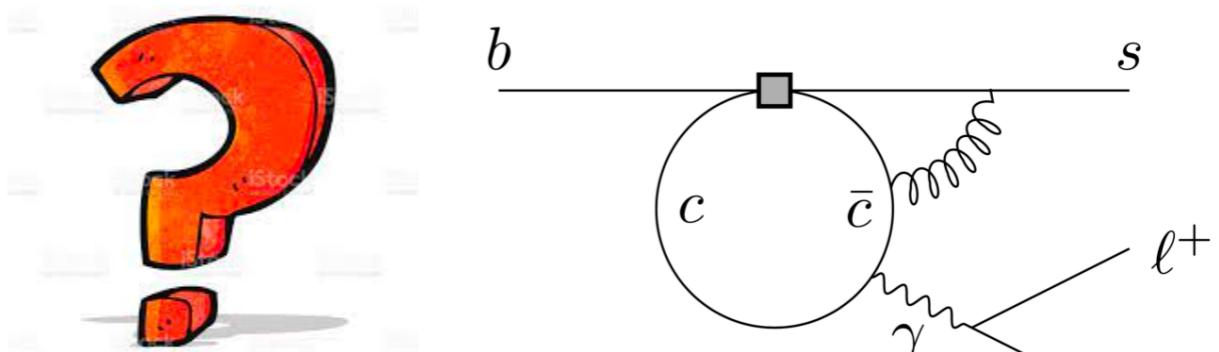
Lepton Flavour Universality

$$R(X) = \frac{\mathcal{B}(B \rightarrow X \mu\mu)}{\mathcal{B}(B \rightarrow X ee)}$$

Very precisely known in SM

Gives a 4σ tension

$\mathcal{B}(b \rightarrow s \mu \mu)$, $b \rightarrow s \mu \mu$ angular



Non-local charm-loop

Cannot be derived from first principles

Other things with Run 2 data

$B^0 \rightarrow K^{*0} \mu^+ \mu^-$ unbinned analysis

Binned analysis, extract $\int I_i(q^2) dq^2$ (normalised to decay rate)

Unbinned, directly fit for underlying Wilson Coefficients

i	$I_i(q^2)$	$f_i(\vec{\Omega})$
1s	$\frac{3}{4} \left[\mathcal{A}_{\parallel}^L ^2 + \mathcal{A}_{\perp}^L ^2 + \mathcal{A}_{\parallel}^R ^2 + \mathcal{A}_{\perp}^R ^2 \right]$	$\sin^2 \theta_K$
1c	$ \mathcal{A}_0^L ^2 + \mathcal{A}_0^R ^2$	$\cos^2 \theta_K$
2s	$\frac{1}{4} \left[\mathcal{A}_{\parallel}^L ^2 + \mathcal{A}_{\perp}^L ^2 + \mathcal{A}_{\parallel}^R ^2 + \mathcal{A}_{\perp}^R ^2 \right]$	$\sin^2 \theta_K \cos 2\theta_\ell$
2c	$- \mathcal{A}_0^L ^2 - \mathcal{A}_0^R ^2$	$\cos^2 \theta_K \cos 2\theta_\ell$
3	$\frac{1}{2} \left[\mathcal{A}_{\perp}^L ^2 - \mathcal{A}_{\parallel}^L ^2 + \mathcal{A}_{\perp}^R ^2 - \mathcal{A}_{\parallel}^R ^2 \right]$	$\sin^2 \theta_K \sin^2 \theta_\ell \cos 2\phi$
4	$\sqrt{\frac{1}{2}} \text{Re} \left(\mathcal{A}_0^L \mathcal{A}_{\parallel}^{L*} + \mathcal{A}_0^R \mathcal{A}_{\parallel}^{R*} \right)$	$\sin 2\theta_K \sin 2\theta_\ell \cos \phi$
5	$\sqrt{2} \text{Re} \left(\mathcal{A}_0^L \mathcal{A}_{\perp}^{L*} - \mathcal{A}_0^R \mathcal{A}_{\perp}^{R*} \right)$	$\sin 2\theta_K \sin \theta_\ell \cos \phi$
6s	$2 \text{Re} \left(\mathcal{A}_{\parallel}^L \mathcal{A}_{\perp}^{L*} - \mathcal{A}_{\parallel}^R \mathcal{A}_{\perp}^{R*} \right)$	$\sin^2 \theta_K \cos \theta_\ell$
7	$\sqrt{2} \text{Im} \left(\mathcal{A}_0^L \mathcal{A}_{\parallel}^{L*} - \mathcal{A}_0^R \mathcal{A}_{\parallel}^{R*} \right)$	$\sin 2\theta_K \sin \theta_\ell \sin \phi$
8	$\sqrt{\frac{1}{2}} \text{Im} \left(\mathcal{A}_0^L \mathcal{A}_{\perp}^{L*} + \mathcal{A}_0^R \mathcal{A}_{\perp}^{R*} \right)$	$\sin 2\theta_K \sin 2\theta_\ell \sin \phi$
9	$\text{Im} \left(\mathcal{A}_{\parallel}^{L*} \mathcal{A}_{\perp}^L + \mathcal{A}_{\parallel}^{R*} \mathcal{A}_{\perp}^R \right)$	$\sin^2 \theta_K \sin^2 \theta_\ell \sin 2\phi$

$B^0 \rightarrow K^{*0} \mu^+ \mu^-$ unbinned analysis

Binned analysis, extract $\int I_i(q^2) dq^2$ (normalised to decay rate)

Unbinned, directly fit for underlying Wilson Coefficients

$$\mathcal{A}_0^{\text{L,R}}(q^2) = -8N \frac{m_B m_{K^*}}{\sqrt{q^2}} \left\{ (C_9 \mp C_{10}) A_{12}(q^2) + \frac{m_b}{m_B + m_{K^*}} C_7 T_{23}(q^2) + \boxed{\mathcal{G}_0(q^2)} \right\}, \quad (1)$$

$$\mathcal{A}_{\parallel}^{\text{L,R}}(q^2) = -N\sqrt{2}(m_B^2 - m_{K^*}^2) \left\{ (C_9 \mp C_{10}) \frac{A_1(q^2)}{m_B - m_{K^*}} + \frac{2m_b}{q^2} C_7 T_2(q^2) + \boxed{\mathcal{G}_{\parallel}(q^2)} \right\}, \quad (2)$$

$$\mathcal{A}_{\perp}^{\text{L,R}}(q^2) = N\sqrt{2\lambda} \left\{ (C_9 \mp C_{10}) \frac{V(q^2)}{m_B + m_{K^*}} + \frac{2m_b}{q^2} C_7 T_1(q^2) + \boxed{\mathcal{G}_{\perp}(q^2)} \right\}, \quad (3)$$

$B^0 \rightarrow K^{*0} \mu^+ \mu^-$ unbinned analysis

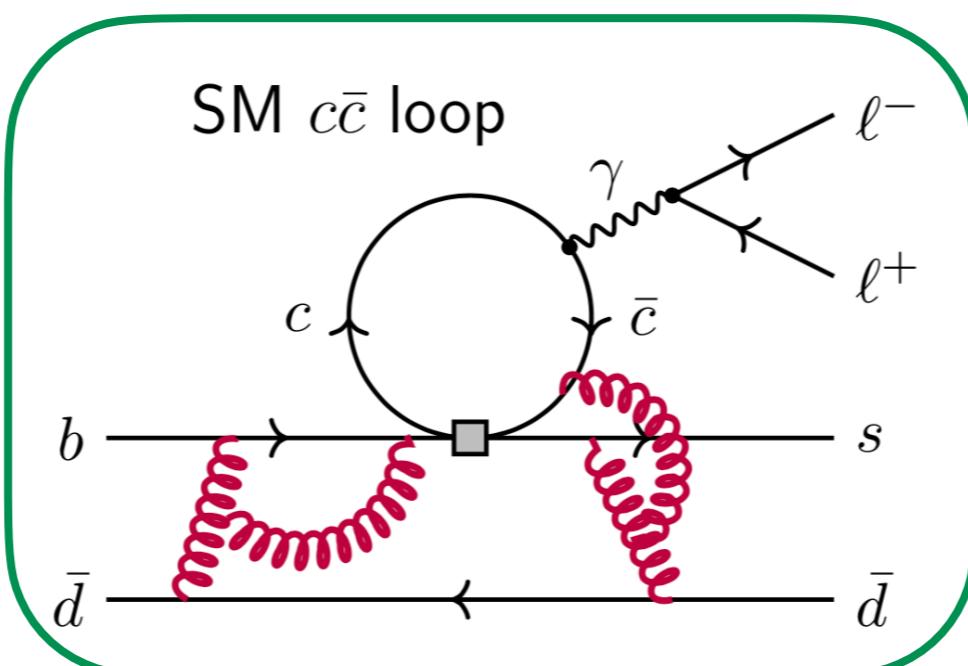
Binned analysis, extract $\int I_i(q^2) dq^2$ (normalised to decay rate)

Unbinned, directly fit for underlying Wilson Coefficients

$$\mathcal{A}_0^{\text{L,R}}(q^2) = -8N \frac{m_B m_{K^*}}{\sqrt{q^2}} \left\{ (C_9 \mp C_{10}) A_{12}(q^2) + \frac{m_b}{m_B + m_{K^*}} C_7 T_{23}(q^2) + \boxed{\mathcal{G}_0(q^2)} \right\}, \quad (1)$$

$$\mathcal{A}_{\parallel}^{\text{L,R}}(q^2) = -N\sqrt{2}(m_B^2 - m_{K^*}^2) \left\{ (C_9 \mp C_{10}) \frac{A_1(q^2)}{m_B - m_{K^*}} + \frac{2m_b}{q^2} C_7 T_2(q^2) + \boxed{\mathcal{G}_{\parallel}(q^2)} \right\}, \quad (2)$$

$$\mathcal{A}_{\perp}^{\text{L,R}}(q^2) = N\sqrt{2\lambda} \left\{ (C_9 \mp C_{10}) \frac{V(q^2)}{m_B + m_{K^*}} + \frac{2m_b}{q^2} C_7 T_1(q^2) + \boxed{\mathcal{G}_{\perp}(q^2)} \right\}, \quad (3)$$



$B^0 \rightarrow K^{*0} \mu^+ \mu^-$ unbinned analysis

Eur. Phys. J. C (2018) 78: 453

Model non-local effects as distortion to C_9^μ

Eur. Phys. J. C 80, 1095 (2020)

Fit for relative phase
and magnitude

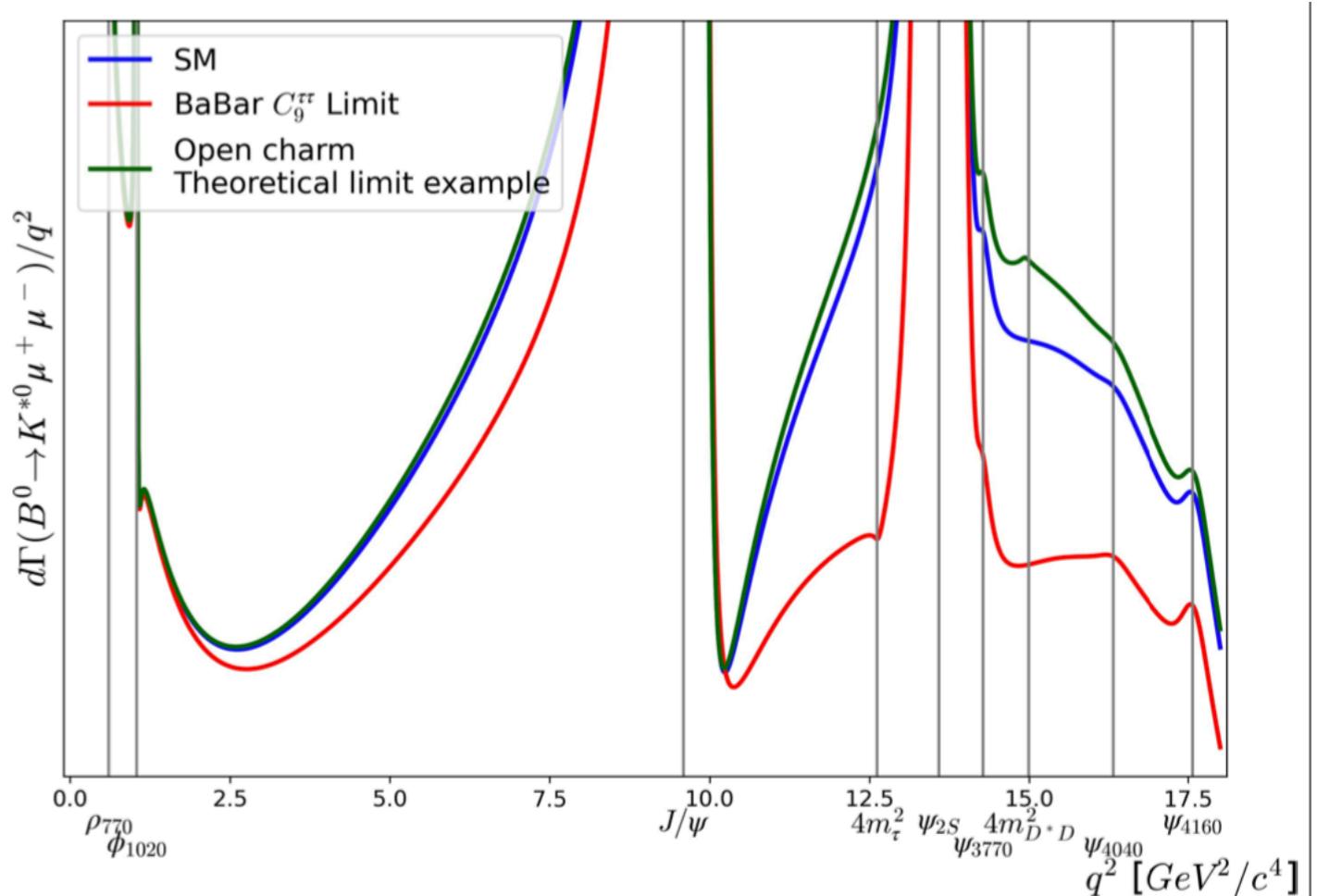
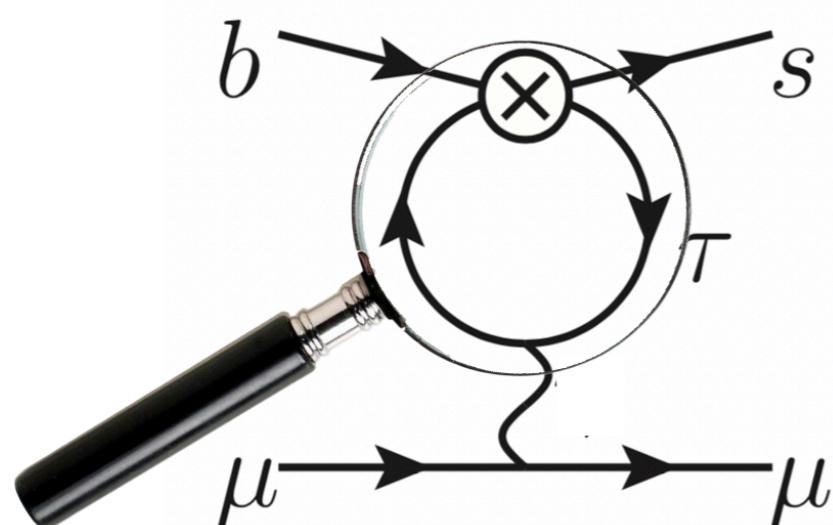
$$C_9^{eff} = C_9 + \sum_j \eta_j e^{i\delta_j} A_j^{res}(q^2)$$

relative phase
magnitude lineshape

Lineshape modelled
by Breitwigner

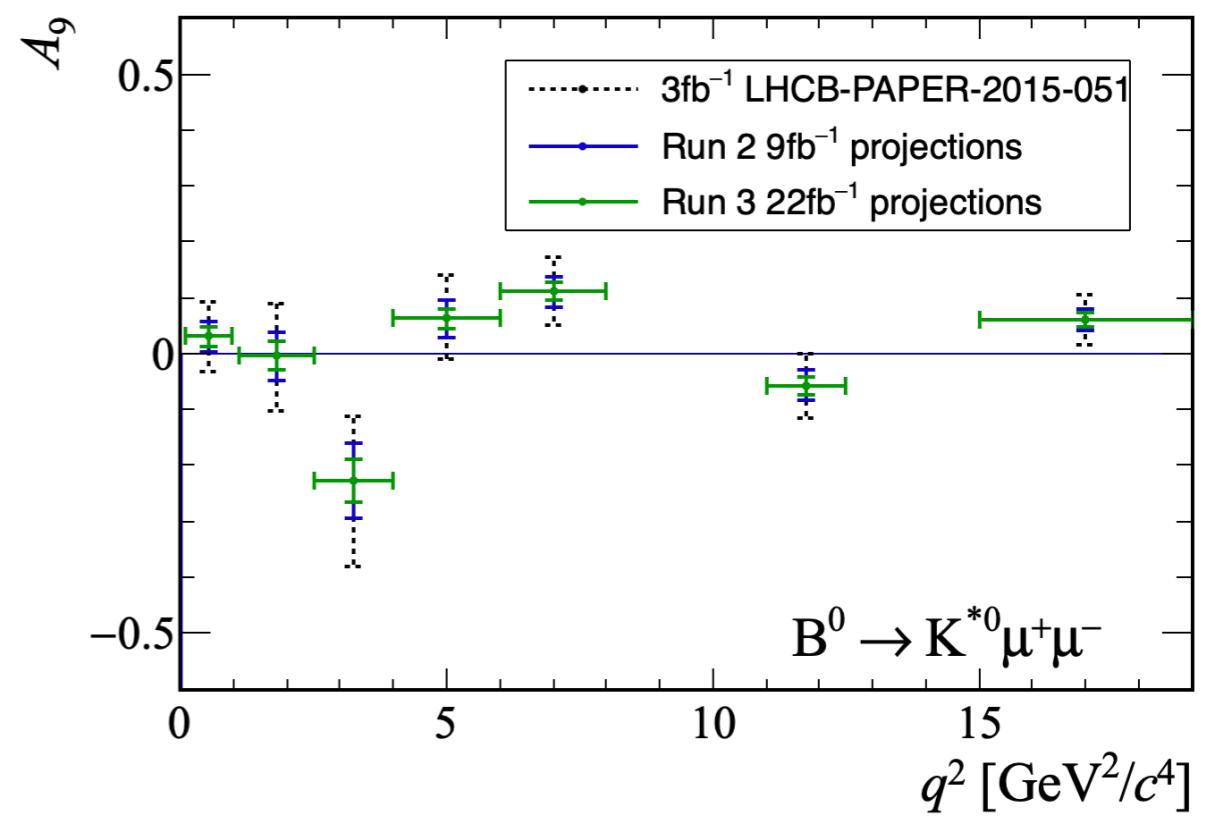
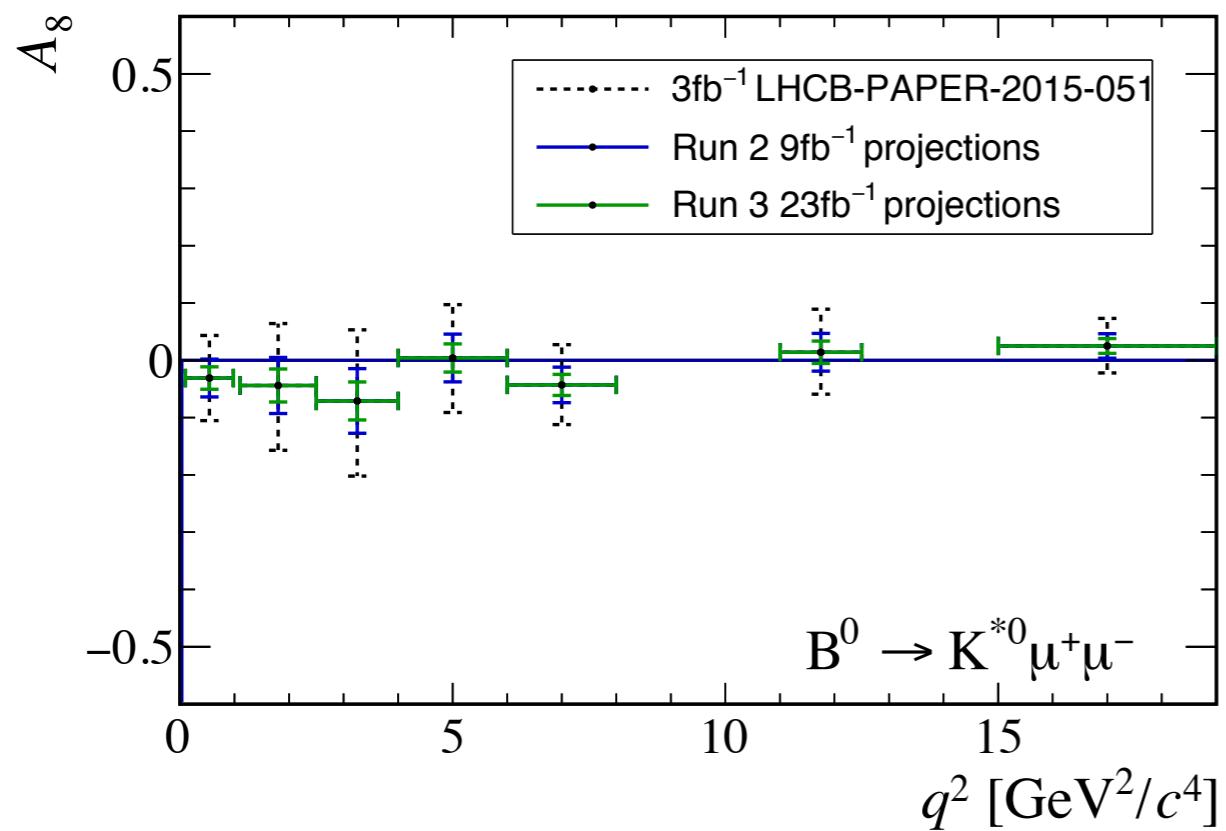
$(\rho, \omega, \phi, J/\psi, \psi(X))$ 1-particle states, modelled with BW

Model contributions above open-charm threshold and $B^0 \rightarrow K^{*0} \tau^+ \tau^-$



$B^0 \rightarrow K^{*0} \mu^+ \mu^-$ binned analysis

- Full Run 1 and 2 data legacy analysis
- Provide CP-averages, asymmetries and correlations between them
- Also measure branching fraction

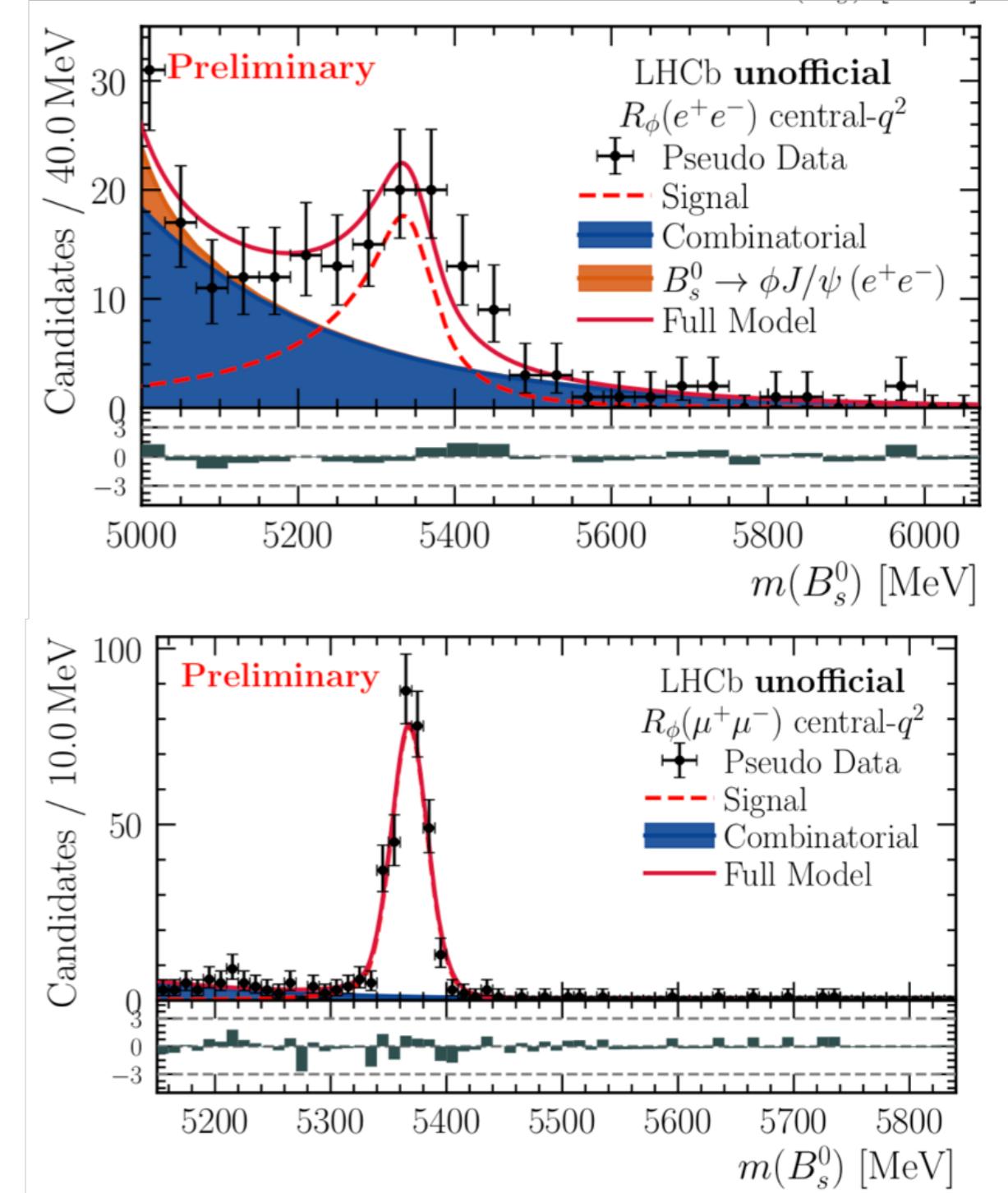


$R(\phi)$

$$R_\phi = \frac{\mathcal{B}(B_s^0 \rightarrow \phi \mu^+ \mu^-)}{\mathcal{B}(B_s^0 \rightarrow \phi e^+ e^-)} \Bigg/ \frac{\mathcal{B}(B_s^0 \rightarrow \phi J/\psi (\mu^+ \mu^-))}{\mathcal{B}(B_s^0 \rightarrow \phi J/\psi (e^+ e^-))}$$

- low q^2 : $0.1 < q^2 < 1.1 \text{ GeV}^2$
- central q^2 : $1.1 < q^2 < 6 \text{ GeV}^2$
- high q^2 : $15 < q^2 < 19 \text{ GeV}^2$

- **Expected Sensitivity** $\mathcal{O}(15\%)$



Run 3 data

What can we expect from Run 3?

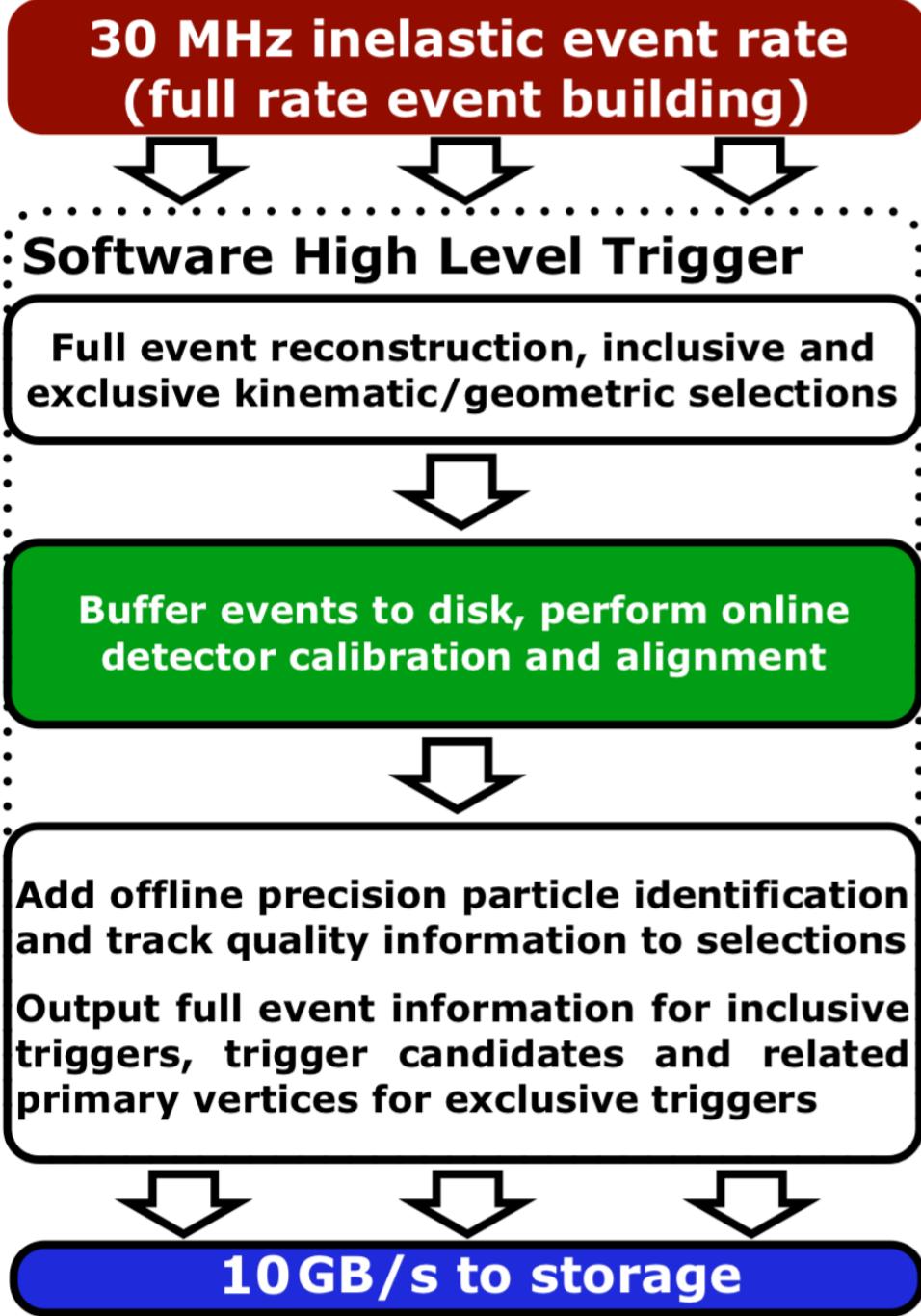
- We expect around 5 times the number of $b\bar{b}$ pairs by end of Run 3 compared to end of Run 2

Run 1&2	LS2	Run 3	LS3	Run 4
$\mathcal{L} = 4 \times 10^{32} / cm^2 s$ $\int \mathcal{L} dt = 9 fb^{-1}$	LHCb Upgrade I	$\mathcal{L} = 2 \times 10^{33} / cm^2 s$ $\int \mathcal{L} dt \approx 23 fb^{-1}$	LHCb Upgrade Ib	$\mathcal{L} = 2 \times 10^{33} / cm^2 s$ $\int \mathcal{L} dt \approx 50 fb^{-1}$
2011-2018	2019-2021	2022-2025	2026-2028	2029-2032

- Significant increase in the number of pp collisions per second -> different problems compared to Run 1+2
- The increase in luminosity in Run 3 means that ~24% of all events with have a reconstructable $c\bar{c}$ pair and 2% have a reconstructable $b\bar{b}$ pair (!)

New trigger for Run 3

LHCb Upgrade Trigger Diagram



- Remove hardware trigger!
- Make decision with more info, improve efficiencies
- Implement the trigger entirely in software
- First-level software trigger (HLT1)
MVA based on inclusive one and two track selections

What does this mean for $b \rightarrow s\ell\ell$ decays?

- The ECAL hardware trigger is currently the major issue for electron analyses
- Removing this bottleneck should increase trigger efficiency relative to the muon mode

Comput. Softw. Big Sci. 4 (2020) 1, 7

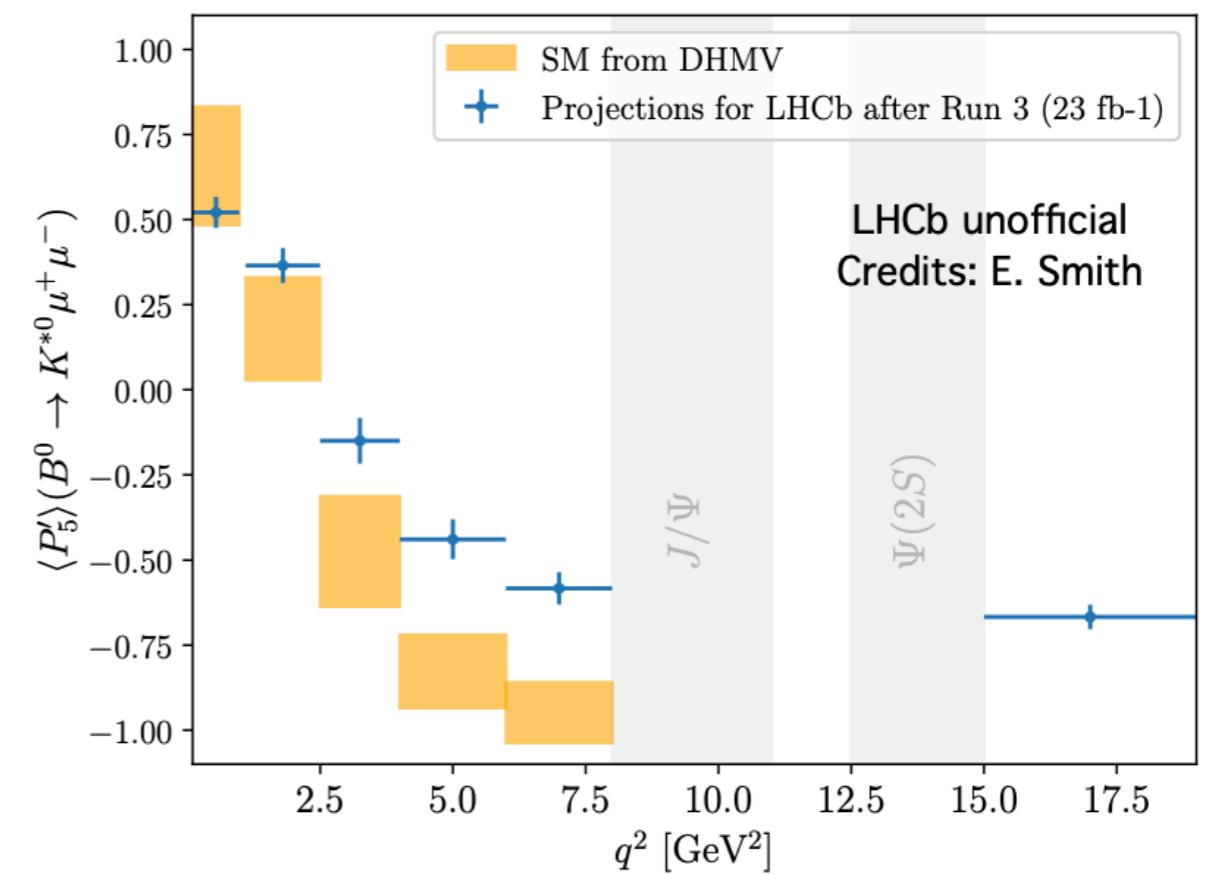
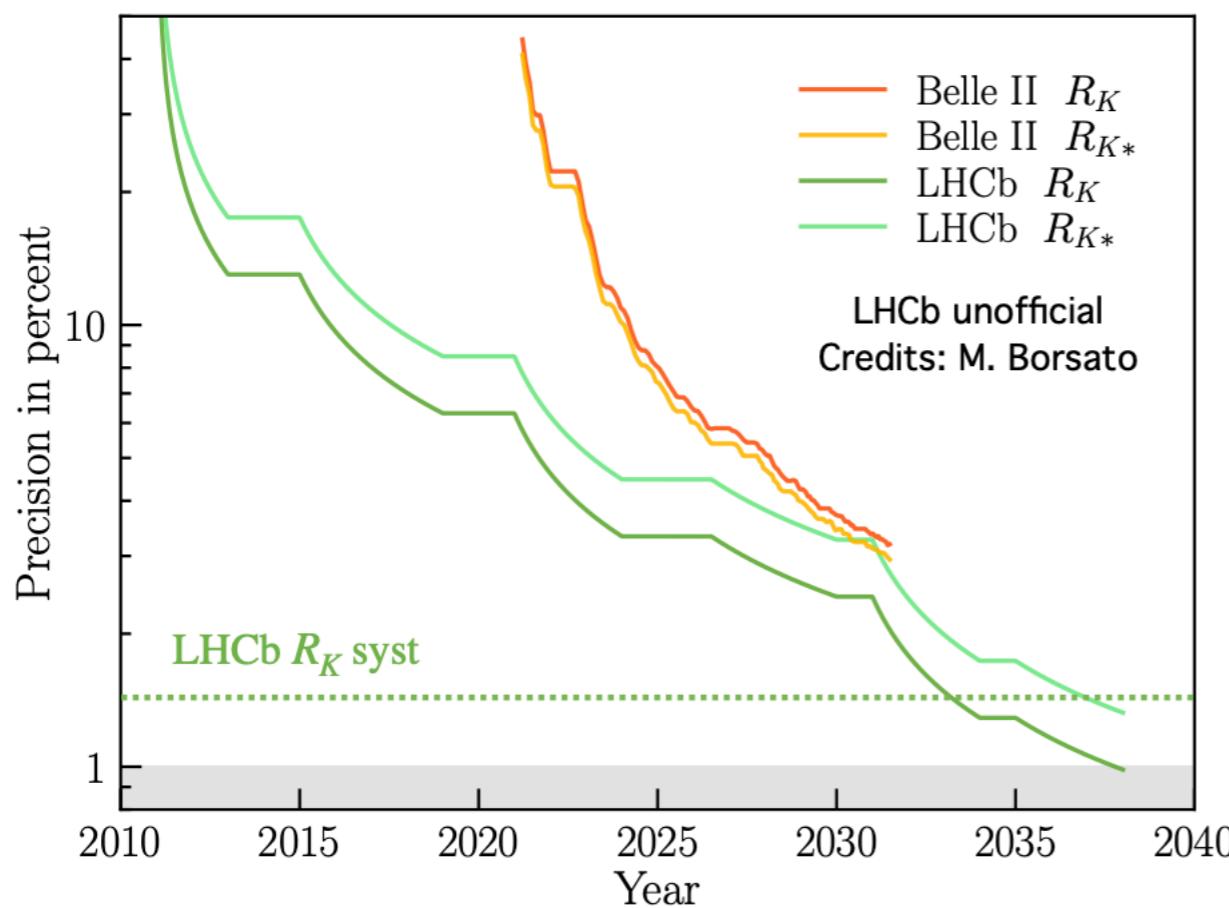
Signal	GEC	TIS -OR- TOS	TOS	GEC × TOS
$B^0 \rightarrow K^{*0} \mu^+ \mu^-$	88.9 ± 2.0	90.6 ± 2.0	88.8 ± 2.1	79.0 ± 2.6
$B^0 \rightarrow K^{*0} e^+ e^-$	84.2 ± 2.7	69.1 ± 3.8	61.7 ± 4.0	52.0 ± 3.8

GEC: Global Event Cut, TIS: Trigger Independent of Signal, TOS: Trigger on Signal

- From ~40% of muon mode currently to ~60% of muon mode

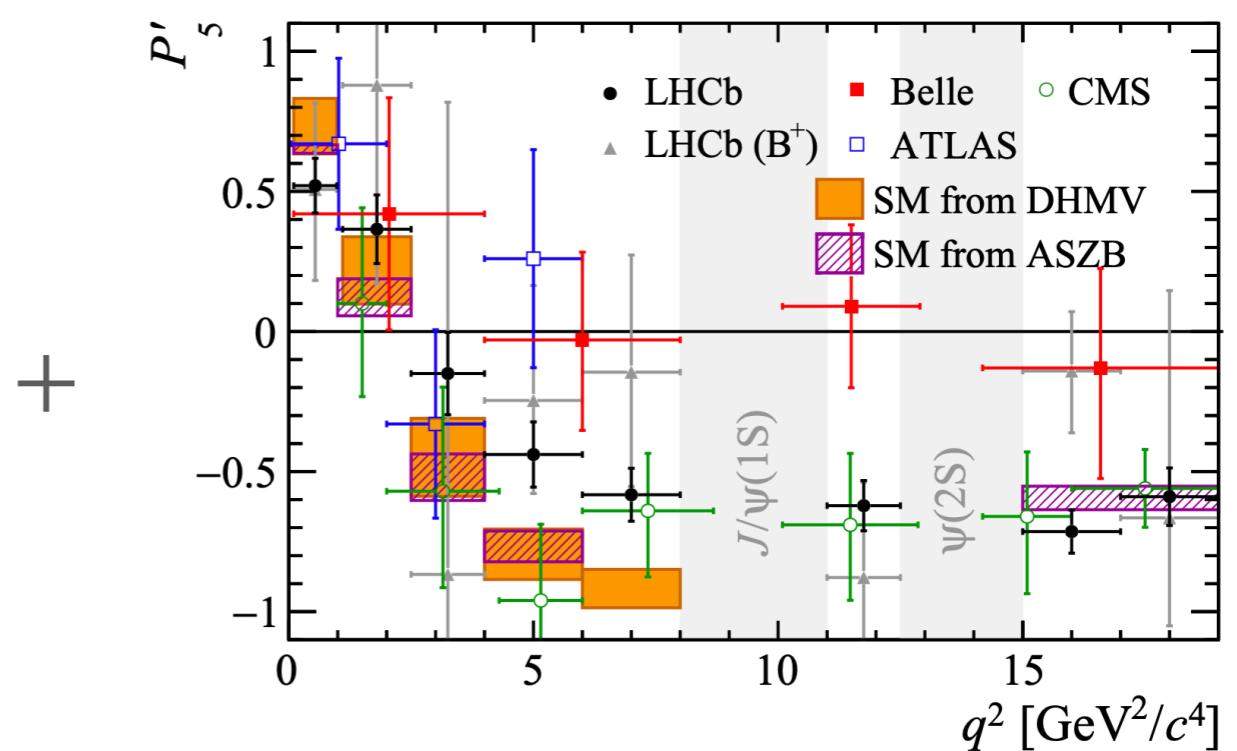
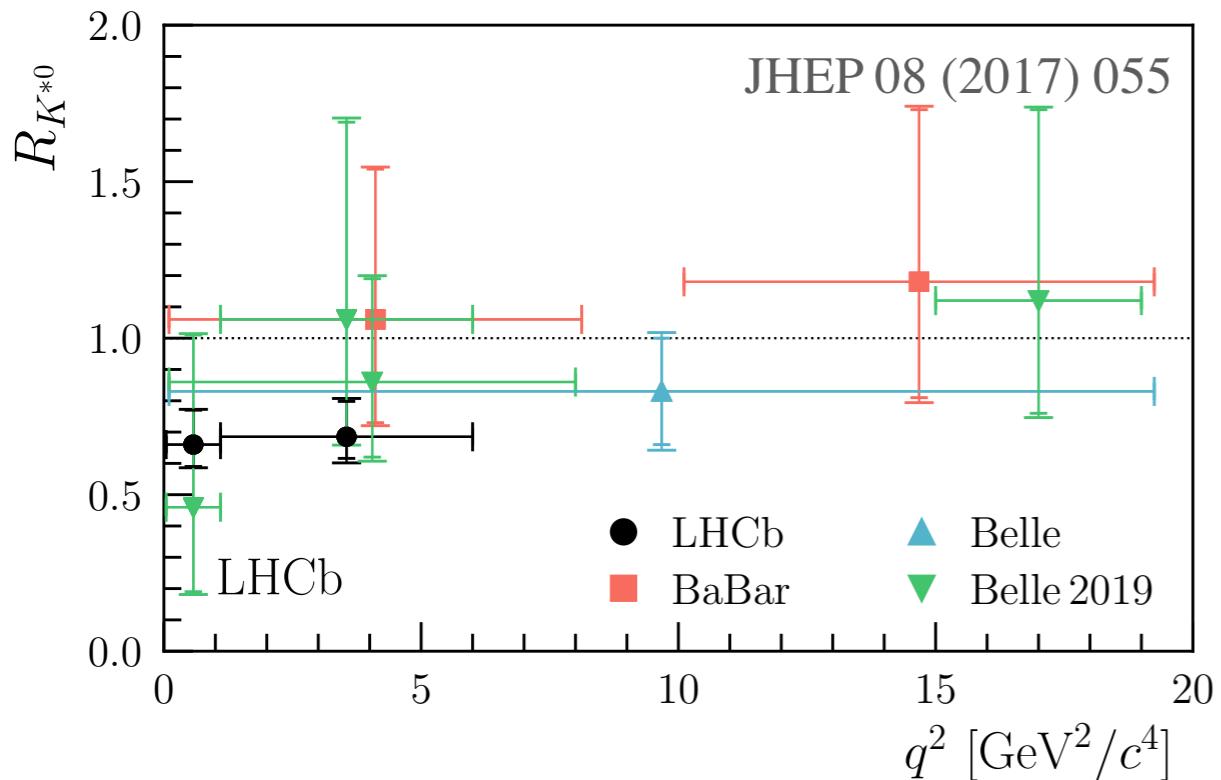
Some outlook plots for Run 3

- Expect around 2.5% statistical uncertainty on RK by end of Run 3
- Angular muon modes will also significantly increase precision



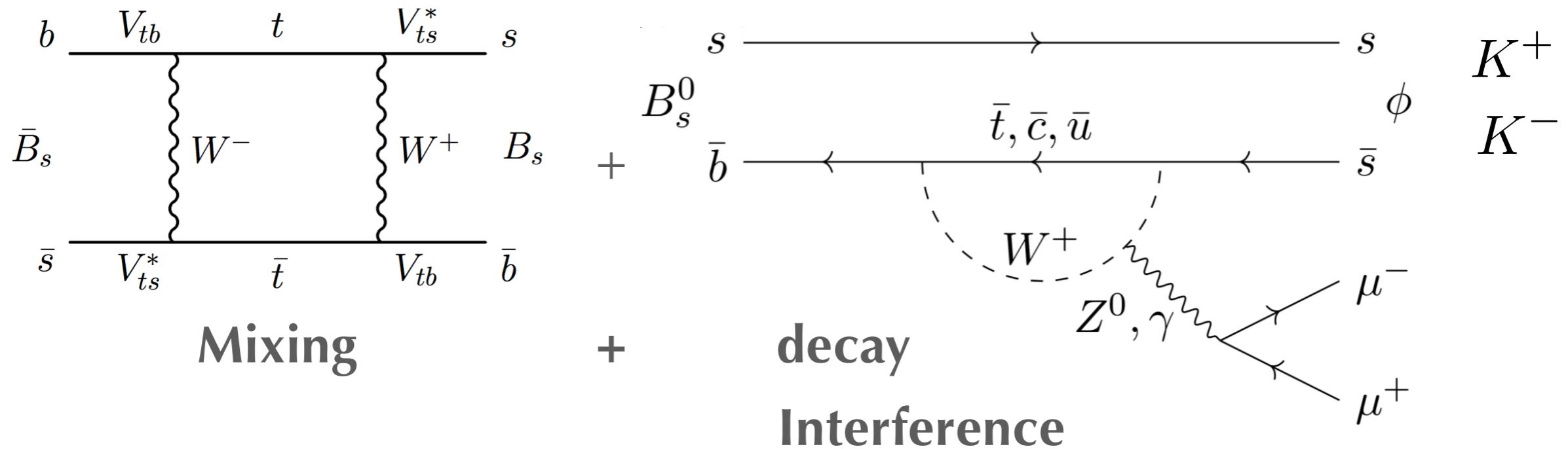
Measurements with Run 3 data and beyond

Angular analysis of $b \rightarrow se^+e^-$ decays

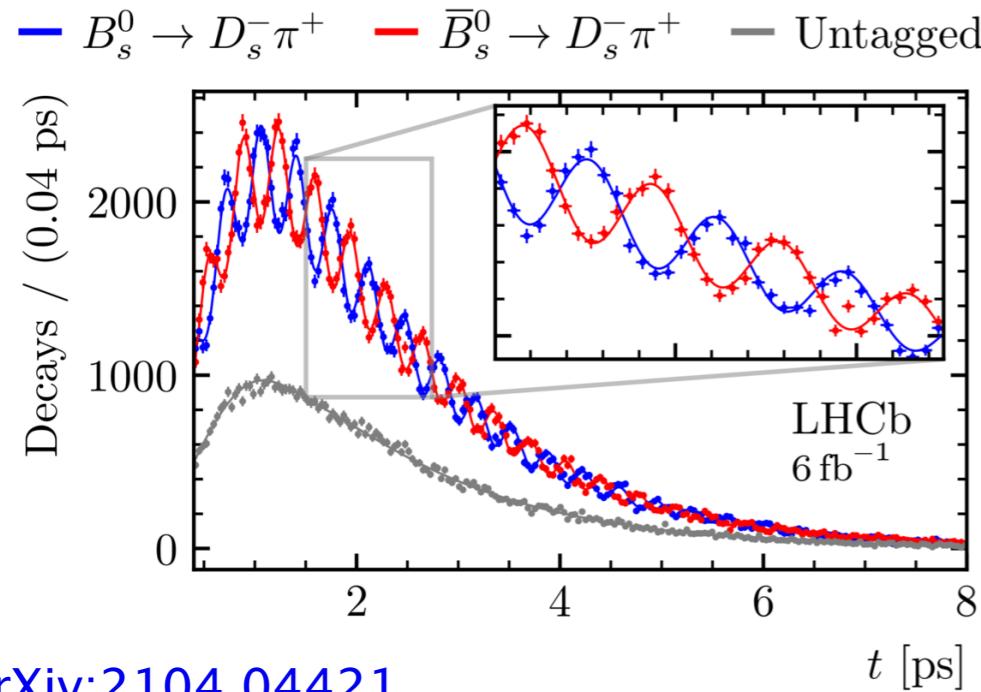


- A full angular analysis of $B \rightarrow V(\rightarrow hh)e^+e^-$ modes:
 - Confirm LFU results in **experimentally orthogonal way**
 - Gives far more in-depth info on the structure of NP
 - Can construct observables between electrons and muons with less dependence on charm loop

Time-dependent angular analysis



= new observables from $b \rightarrow s\mu^+\mu^-$ decays with flavour-symmetric final-states



$$J_i(t) + \tilde{J}_i(t) = e^{-\Gamma t} \left[(J_i + \tilde{J}_i) \cosh(y\Gamma t) - h_i \sinh(y\Gamma t) \right]$$

$$J_i(t) - \tilde{J}_i(t) = e^{-\Gamma t} \left[(J_i - \tilde{J}_i) \cos(x\Gamma t) - s_i \sin(x\Gamma t) \right],$$

$$x \equiv \Delta m/\Gamma, y \equiv \Delta\Gamma/(2\Gamma)$$

Use rest of event to figure out the B_s flavour at production, this is called **Flavour-tagging**

$b \rightarrow s\mu^+\mu^-$ flavour-tagging

Yields, $\epsilon_{tag} \equiv 5\%$		Run 1 observed		Run 3 expected	
		Full q^2	$1.1 < q^2 < 6.0$	Full q^2	$1.1 < q^2 < 6.0$
$B_s^0 \rightarrow \phi(1020)\mu^+\mu^-$	untagged	432	101	5230	1220
	tagged	22	5	262	60
$B_d^0 \rightarrow K_s\mu^+\mu^-$	untagged	176	70	2200	850
	tagged	9	4	110	43

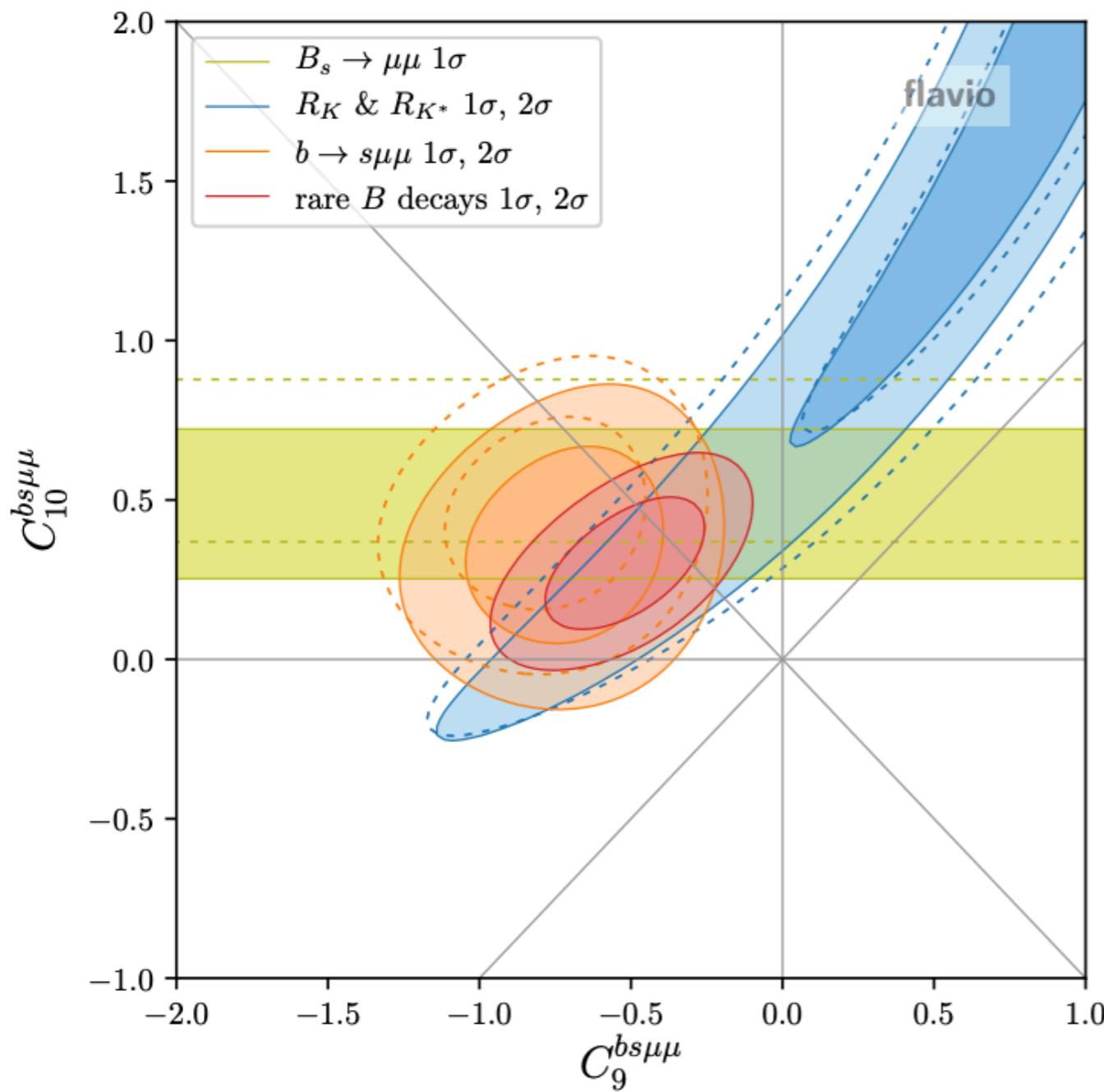
- Tagged angular analysis possible by end of Run 3 in wider q^2 bins at LHCb, full lifetime + angular analysis still somewhat limited
- Data collected in Run 4,5 and beyond needed to properly explore time-dependent angular analysis

What about $b \rightarrow d\ell^+\ell^-$ decays?

- Decay rates around $|V_{ts}/V_{td}|^2 \approx 25$ smaller than $b \rightarrow s\ell^+\ell^-$
- LFU tests possible by end of Run 3 but not angular analysis
- Many explanations for $b \rightarrow s\ell^+\ell^-$ anomalies predict effects in $b \rightarrow d\ell^+\ell^-$

R_X precision	Run 1 result	9 fb^{-1}	23 fb^{-1}	50 fb^{-1}	300 fb^{-1}
R_K	$0.745 \pm 0.090 \pm 0.036$ [274]	0.043	0.025	0.017	0.007
$R_{K^{*0}}$	$0.69 \pm 0.11 \pm 0.05$ [275]	0.052	0.031	0.020	0.008
R_ϕ	—	0.130	0.076	0.050	0.020
R_{pK}	—	0.105	0.061	0.041	0.016
R_π	—	0.302	0.176	0.117	0.047

Conclusions

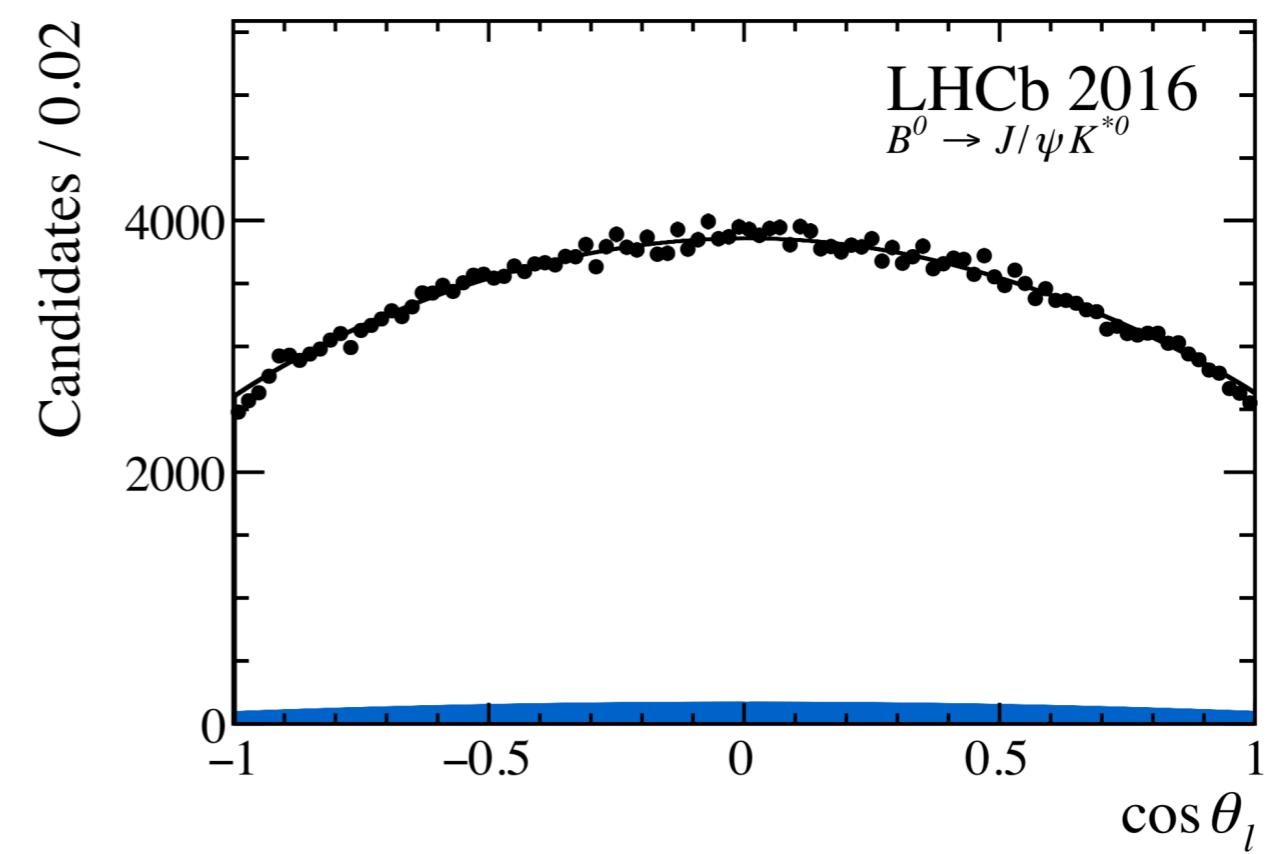
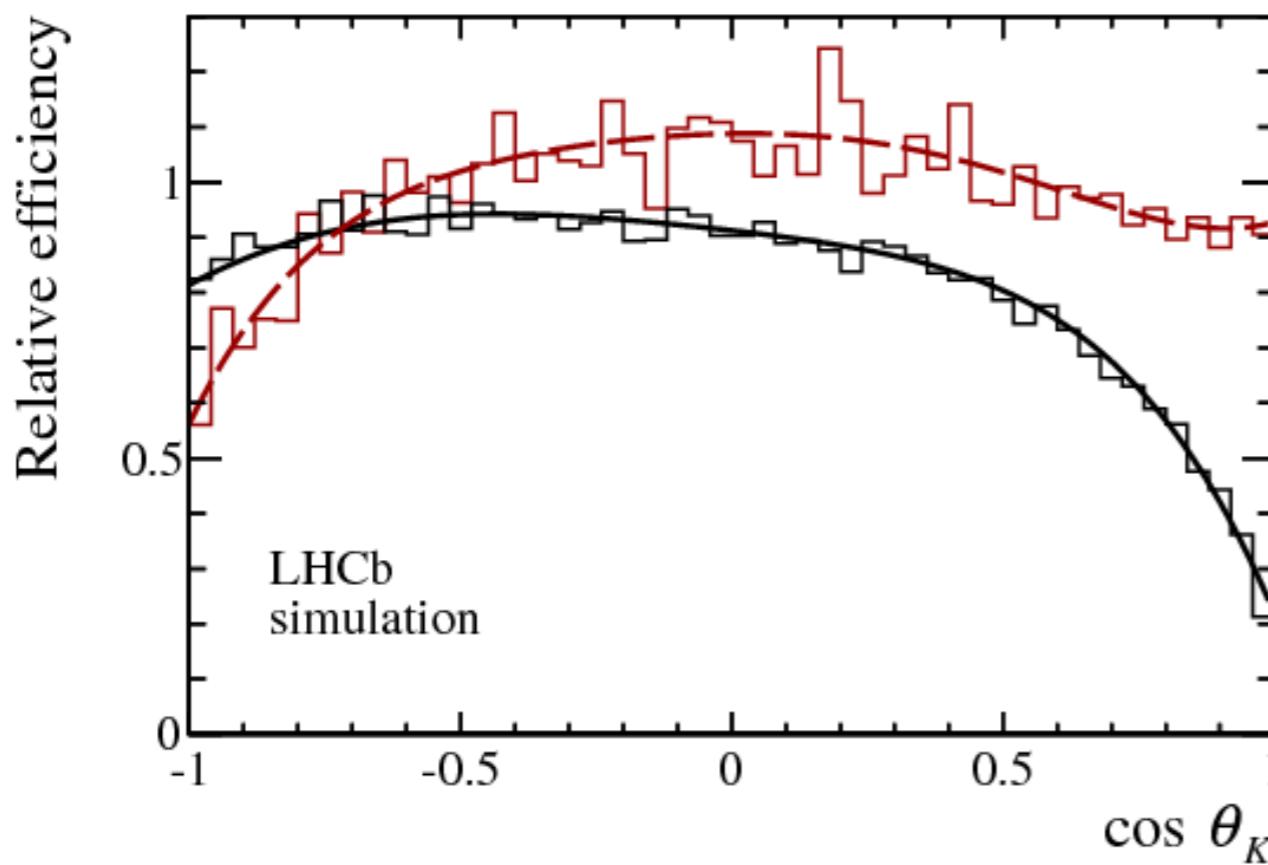


- Run 2 has been an exciting time for the neutral current anomalies at LHCb
- Still remains many measurements that can be performed with both existing and new data
- New measurements will shed more light on both key experimental and theory aspects of flavour anomalies

Back-ups

Experimental summary: angular analyses for muons

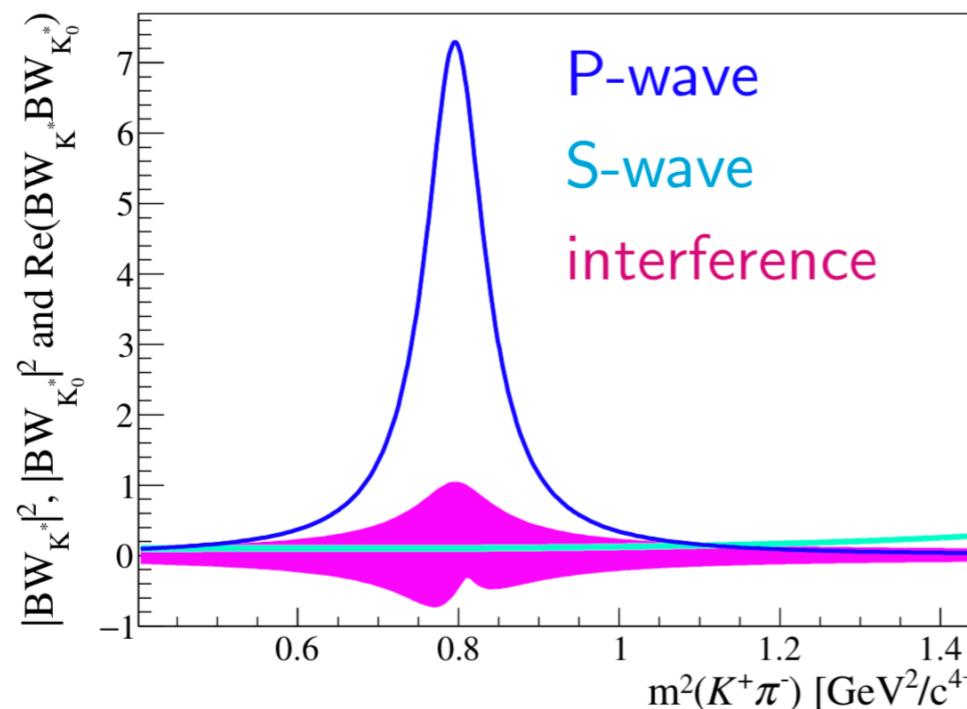
- Uncertainties dominated by statistics
- The efficiency shape as a function of all the angles and q^2 is derived from simulation and validated on high-yield control modes in data
- Not dependent on absolute efficiency, no single dominate systematic



Complications: S-wave contribution

- Contribution from non-resonant $K\pi$'s and spin 0 resonances
- Must include additional angular terms (as nuisances)

$$\frac{1}{d(\Gamma + \bar{\Gamma})/dq^2} \frac{d(\Gamma + \bar{\Gamma})}{dcos\theta_l dcos\theta_K d\phi} \Big|_{S+P} = (1 - F_S) \frac{1}{d(\Gamma + \bar{\Gamma})/dq^2} \frac{d(\Gamma + \bar{\Gamma})}{dcos\theta_l dcos\theta_K d\phi} \Big|_P$$



+ interference terms P-wave

P-wave observables scaled by $1 - F_S$

- Use the $m_{K^+\pi^-}$ distribution to constrain S-wave

Complications: angular acceptance

- The reconstruction and selection efficiency must be calculated as a function of angles and q^2 .
- Efficiency can be parametrised using Legendre polynomials

$$\varepsilon(\cos \theta_\ell, \cos \theta_K, \phi, q^2) = \sum_{k,l,m,n} c_{k,l,m,n} P(\cos \theta_\ell, k) P(\cos \theta_K, l) P(\phi, m) P(q^2, n)$$

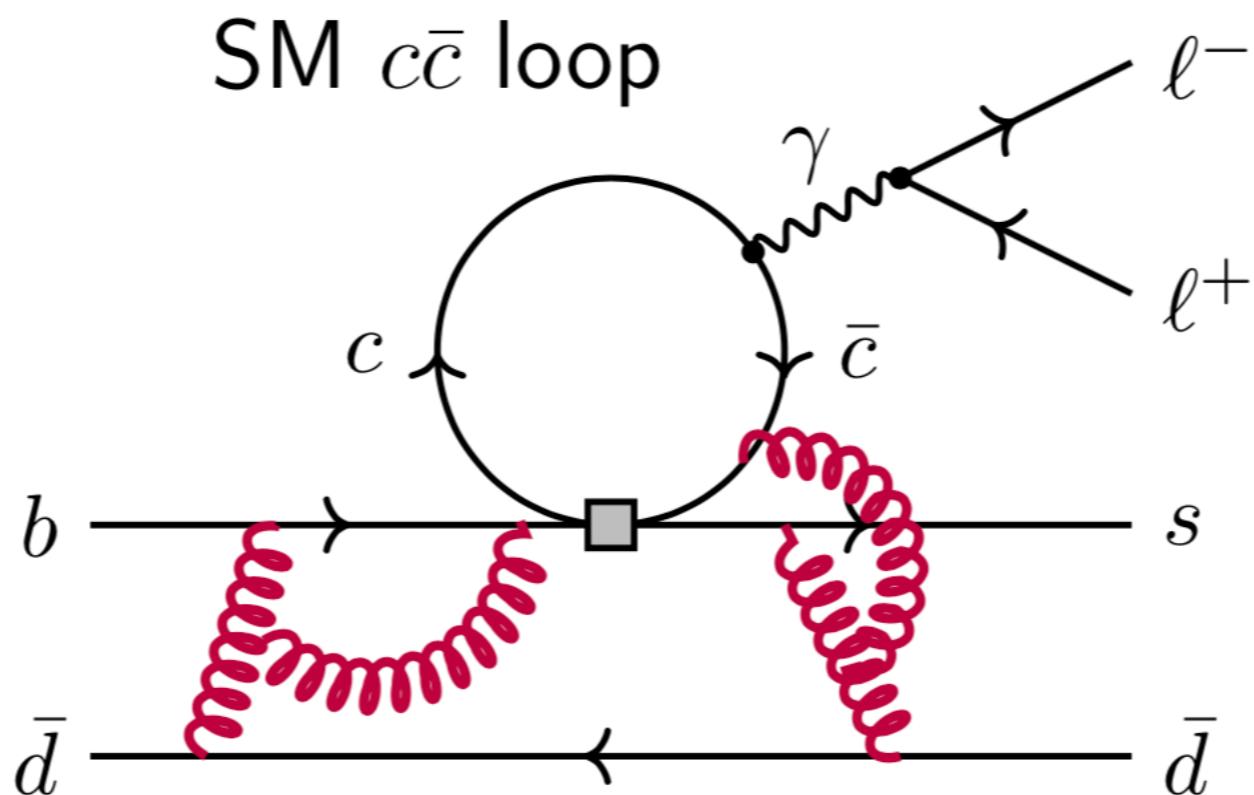
- The coefficients $c_{k,l,m,n}$ are calculated via the method of moments using large statistic MC samples

$$c_{k,l,m,n} = \frac{1}{N'} \sum_{i=1}^N w_i \left[\left(\frac{2k+1}{2} \right) \left(\frac{2l+1}{2} \right) \left(\frac{2m+1}{2} \right) \left(\frac{2n+1}{2} \right) \right. \\ \left. \times P(\cos \theta_\ell, k) P(\cos \theta_K, l) P(\phi, m) P(q^2, n) \right]$$

Writing out expression for complex amplitudes in full:

$$\mathcal{A}_{\lambda=\perp,\parallel,0}^{L,R} = N_\lambda \left\{ (C_9 \mp C_{10}) \mathcal{F}_\lambda(q^2) + \frac{2m_b M_B}{q^2} \left[C_7 \mathcal{F}_\lambda^T(q^2) - 16\pi^2 \frac{M_B}{m_b} \mathcal{H}_\lambda(q^2) \right] \right\}$$

Wilson coefficients, form factors, effects from charm loop



General idea -> parameterise the charm loops: Taylor expandable

1. Perform some **tricks** to make $H_\lambda(q^2)$ an analytical function

Namely removing poles^[*]: $J/\psi, \psi(2S)$

2. Exploit similar $H_\lambda(q^2), F_\lambda(q^2)$ properties, parametrise $H_\lambda(q^2)/F_\lambda(q^2)$

Need to get α_k^λ

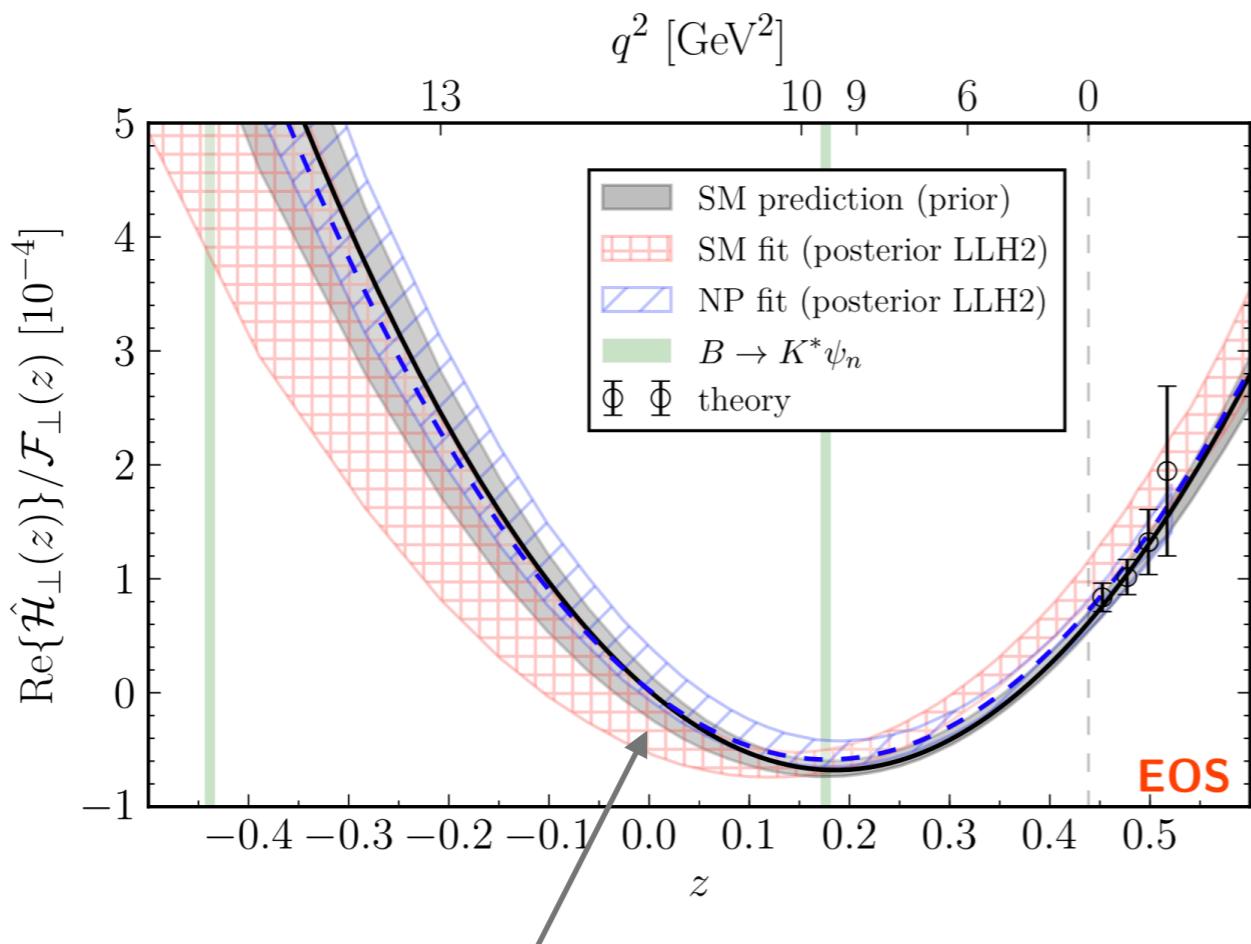
$$\hat{\mathcal{H}}_\lambda(z) = \left[\sum_{k=0}^2 \alpha_k^\lambda z^k \right] \mathcal{F}_\lambda(z)$$

Taylor expansion

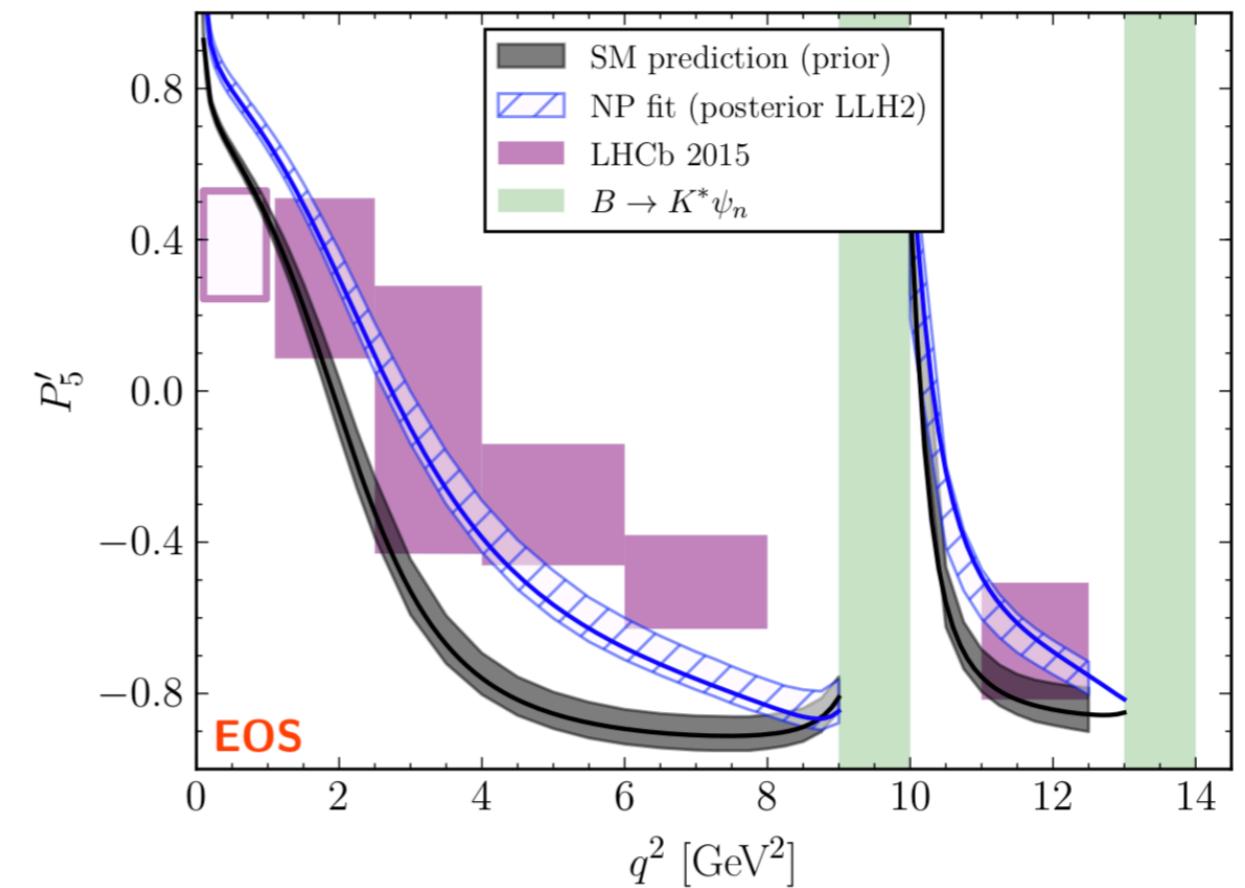
z is just remapping of q^2

3. Use information from theory where there is no charm: negative q^2
4. Use information from data (LHCb, Belle, Babar) for q^2 region corresponding to the poles $J/\psi, \psi(2S)$
5. Interpolate using info from [3][4] to get α_k^λ
6. Using knowledge of α_k^λ , apply to $B_0 \rightarrow K^{*0} \mu^+ \mu^-$ region to get C_9

[*] and multi-branch decays, less dominate



Interpolation between data and theory to extract $\vec{\alpha}^{\perp}$



Modelling the charm loop in fits

arXiv:1612.06764

Following the notation of Ref. [40], the CP -averaged differential decay rate of $B^+ \rightarrow K^+ \mu^+ \mu^-$ decays as a function of the dimuon mass squared, $q^2 \equiv m_{\mu\mu}^2$, is given by

$$\frac{d\Gamma}{dq^2} = \frac{G_F^2 \alpha^2 |V_{tb} V_{ts}^*|^2}{128\pi^5} |\mathbf{k}| \beta \left\{ \frac{2}{3} |\mathbf{k}|^2 \beta^2 \left| \mathcal{C}_{10} f_+(q^2) \right|^2 + \frac{4m_\mu^2(m_B^2 - m_K^2)^2}{q^2 m_B^2} \left| \mathcal{C}_{10} f_0(q^2) \right|^2 \right. \\ \left. + |\mathbf{k}|^2 \left[1 - \frac{1}{3} \beta^2 \right] \left| \mathcal{C}_9 f_+(q^2) + 2\mathcal{C}_7 \frac{m_b + m_s}{m_B + m_K} f_T(q^2) \right|^2 \right\}, \quad (1)$$

where $|\mathbf{k}|$ is the kaon momentum in the B^+ meson rest frame.

The parameters $f_{0,+T}$ denote the scalar, vector and tensor $B \rightarrow K$ form factors.

$$\mathcal{C}_9^{\text{eff}} = \mathcal{C}_9 + Y(q^2),$$

Insert term into eq. above

where the term $Y(q^2)$ describes the sum of resonant and continuum hadronic states appearing in the dimuon mass spectrum. In this analysis $Y(q^2)$ is replaced by the sum of vector meson resonances j such that

If $n^* \pi/2$ term disappears in eq.1

**assumes no continuum
hadronic states (e.g. no Dbarbar)**

$$\mathcal{C}_9^{\text{eff}} = \mathcal{C}_9 + \sum_j \eta_j e^{i\delta_j} A_j^{\text{res}}(q^2), \quad (3)$$

where η_j is the magnitude of the resonance amplitude and δ_j its phase relative to C_9 .

1D Hyp.	All				LFUV			
	Best fit	1 σ /2 σ	Pull _{SM}	p-value	Best fit	1 σ /2 σ	Pull _{SM}	p-value
$\mathcal{C}_{9\mu}^{\text{NP}}$	-1.02	[−1.18, −0.85] [−1.34, −0.68]	5.8	65.1 %	-1.02	[−1.38, −0.69] [−1.80, −0.40]	3.5	50.6 %
$\mathcal{C}_{9\mu}^{\text{NP}} = -\mathcal{C}_{10\mu}^{\text{NP}}$	-0.49	[−0.59, −0.40] [−0.69, −0.30]	5.4	55.5 %	-0.44	[−0.55, −0.32] [−0.68, −0.21]	4.0	74.0 %
$\mathcal{C}_{9\mu}^{\text{NP}} = -\mathcal{C}_{9'\mu}$	-1.02	[−1.18, −0.85] [−1.33, −0.67]	5.7	61.3 %	-1.66	[−2.15, −1.05] [−2.54, −0.47]	3.1	35.4 %
$\mathcal{C}_{9\mu}^{\text{NP}} = -3\mathcal{C}_{9e}^{\text{NP}}$	-0.92	[−1.08, −0.76] [−1.23, −0.60]	5.7	62.7 %	-0.76	[−1.02, −0.52] [−1.30, −0.30]	3.5	50.8 %

Table 1. Most prominent 1D patterns of New Physics in $b \rightarrow s\mu\mu$. The Pull_{SM} is quoted in units of standard deviation. The p -value of the SM hypothesis is 8.6% for the fit “All” and 4.5% for the fit LFUV. We have checked also the scenario with only $\mathcal{C}_{10\mu}^{\text{NP}}$ but its significance in the “All” fit is only at the 4.0σ level and 3.9σ for the LFUV fit.