



NOVEL CPV PHASES IN B-PHYSICS ANOMALIES

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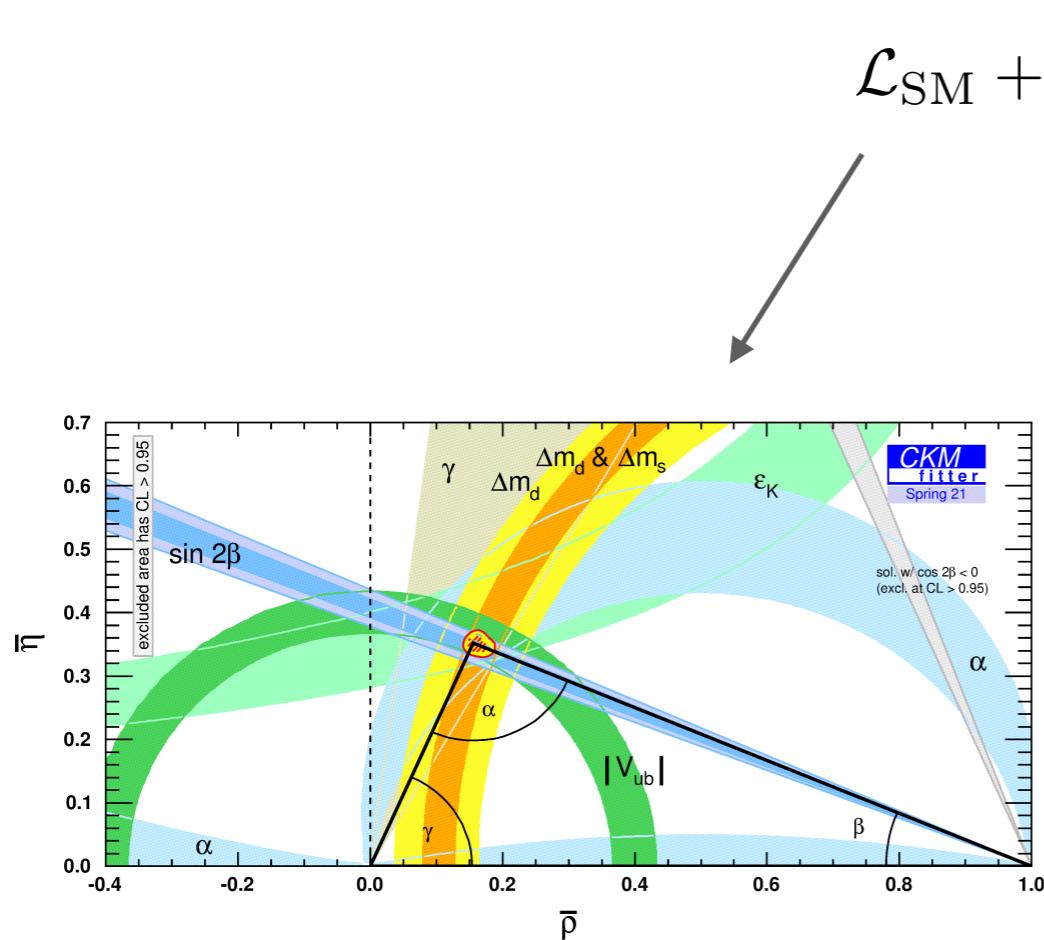
21.4.2022

OUTLINE

- Flavour and CP violation in the SM(EFT)
- Lepton flavour universality and CPV
- Model dependent CP-sensitive observables

FLAVOUR AND CP VIOLATION IN THE SM(EFT)

SM(EFT)



1 CPV + 18 CP even parameters

$$\det(i[M_d, M_u]) = J(m_t - m_c)(m_t - m_u) \dots$$

$$J \approx 3 \times 10^{-5} \quad \text{Jarlskog '85}$$

flavour (universality)
violation from Yukawas

$$\mathcal{L}_{\text{SM}} + \frac{1}{\Lambda^2} \sum_i C_i Q_i$$

$(\bar{L}L)(\bar{L}L)$	
Q_{ll}	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$
\dots	

59 operators (not counting flavor)

1149 CPV + 1350 CP even flavor
couplings

Grzadkowski et al '10
Alonso et al '13

699 Jarlskog-like invariants

Bonnefoy et al. '21

FLAVOR PUZZLE

$$\mathcal{L}_{\text{SM}} + \frac{1}{\Lambda^2} \sum_i C_i Q_i$$



If scale Λ is low, why do we only see CPV effect of a single Jarlskog invariant?

Do the SM flavour patterns encode more fundamental dynamics?

$(\bar{L}L)(\bar{L}L)$	
Q_{ll}	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$
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\dots	

59 operators (not counting flavor)

with flavour:

1149 CPV + 1350 CP

Grzadkowski et al '10

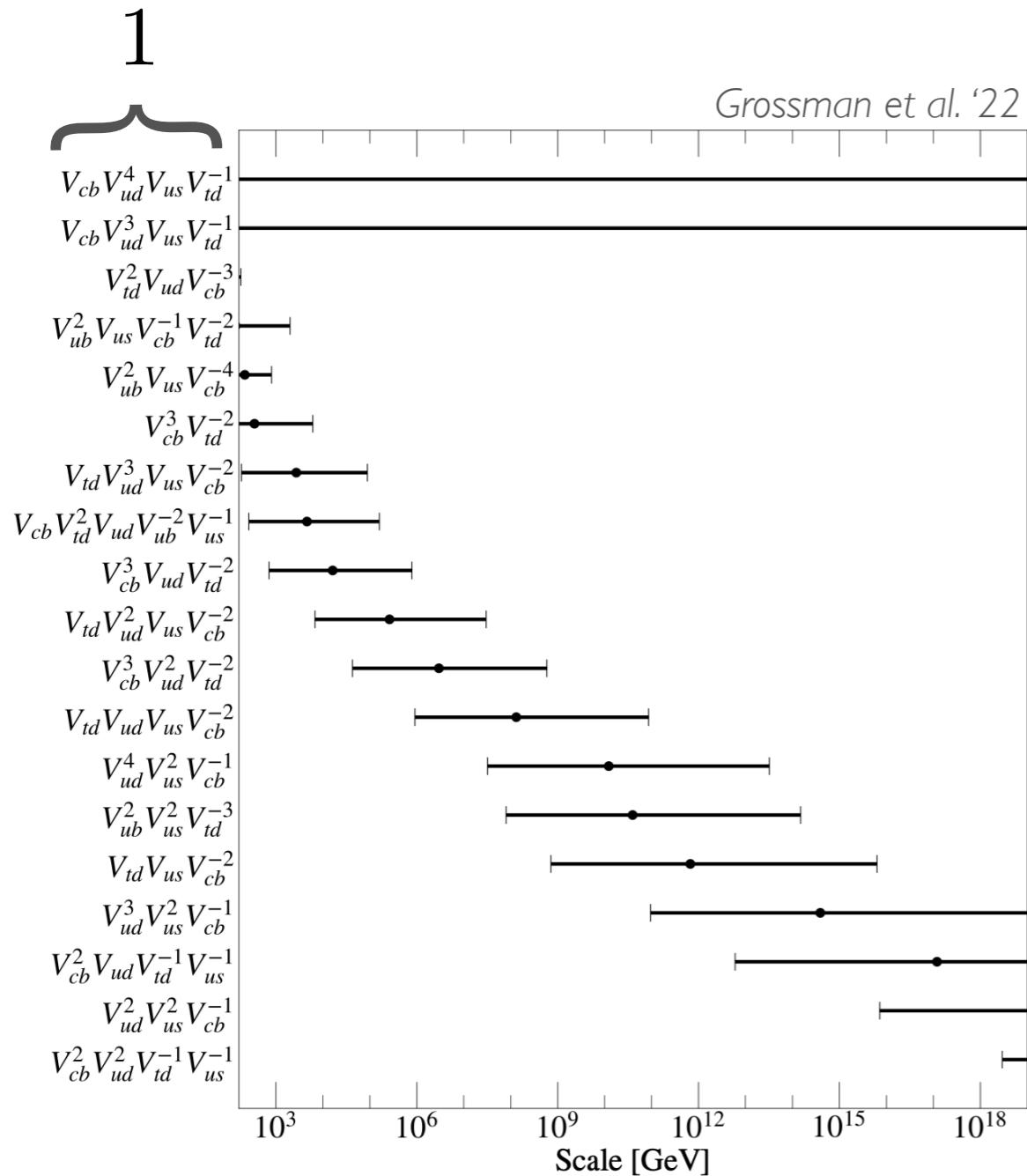
Alonso et al '13

699 Jarlskog-like invariants

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FLAVOR PUZZLE

Pattern in the CKM (besides Cabibbo hierarchy)?



Yukawa and CKM elements run

$$|V_{td} V_{us}| = |V_{cb}^2| \quad \text{at scale } 10^9 - 10^{15} \text{ GeV}$$

Relation reproduced by

$$M_u = m_t \begin{pmatrix} 0 & x\lambda_u^3 & 0 \\ x\lambda_u^3 & x\lambda_u^2 & x\lambda_u \\ 0 & x\lambda_u & 1 \end{pmatrix}, \quad M_d = m_b \begin{pmatrix} 0 & w\lambda_d^3 & 0 \\ w\lambda_d^3 & w\lambda_d^2 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

What can we learn from this? Difficult to go beyond this texture.

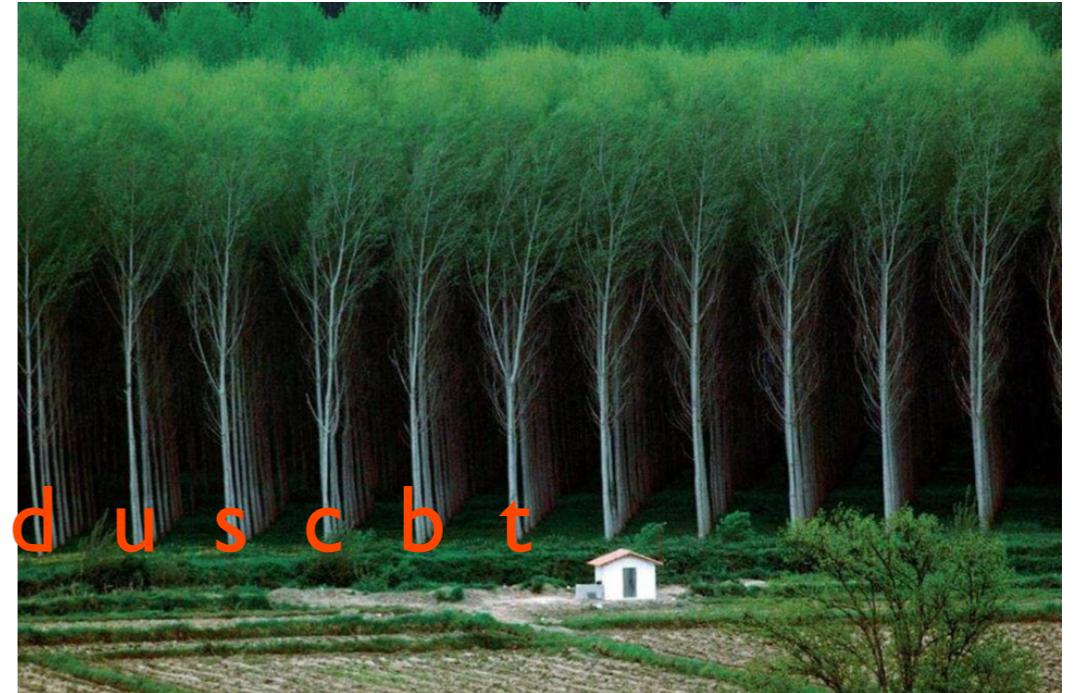
FLAVOR PUZZLE

Minimal flavour violation (and variations) ~ embrace the fact that BSM flavour is aligned with the SM

Flavour violation is broken only by (higher powers of)
Yukawa couplings

$$G_{\text{flavour}} = \begin{cases} SU(3)^5 & Y_{e,u,d} \neq 0 \\ U(1)^5 & \end{cases} \begin{matrix} U(1)_{e-\mu} \otimes U(1)_{\tau-\mu} \\ U(1)_B \otimes U(1)_L \otimes U(1)_Y \end{matrix}$$

$$Y_u \rightarrow U_q Y_u U_u^\dagger, \quad Y_d \rightarrow U_q Y_d U_d^\dagger$$



“as flavour symmetric as the SM”

Chirality flipping SMEFT operators: Yukawa, dim-6 Yukawa, dipole operators

$$\frac{C^{rs}}{\Lambda^2} \bar{q}_r u_s \Rightarrow C^{rs} \sim Y_u^{rs} + \#(Y_u Y_u^\dagger Y_u)^{rs} + \dots + \#(Y_d Y_d^\dagger Y_u)^{rs} + \dots$$

FLAVOR PUZZLE

Minimal flavour violation (and variations) \sim embrace the fact that BSM flavour is aligned with the SM

Reduced number of parameters.

SMEFT $\mathcal{O}(1)$ terms (dim-6, $\Delta B = 0$)		Lepton sector										CP even/odd
		MFV _L	U(3) _V	U(2) ² \times U(1) ²	U(2) ²	U(2) _V	U(1) ⁶	U(1) ³	No symm.			
Quark sector	MFV _Q	41 6	45 9	59 6	62 9	67 13	81 6	93 18	207 132	321 1350 1149	281 169 305 175 168 38 1350 1149	
	U(2) ² \times U(3) _d	72 10	78 15	95 10	100 15	107 21	122 10	140 28	281 169			
	U(2) ³ \times U(1) _{d₃}	86 10	92 15	111 10	116 12	123 21	140 10	158 28	305 175			
	U(2) ³	93 17	100 23	118 17	124 23	132 30	147 17	168 38	321 191			
	No symmetry	703 570	734 600	756 591	786 621	818 652	813 612	906 705	1350 1149			

Greljo, Palavrić, Thomsen '22

see also
Faroughy, Isidori, Wilsch,
Yamamoto '21

Even in the full MFV case there are many new flavor and CPV effects waiting to be discovered.

Why not present already in hints of LFUV?

LEPTON FLAVOUR UNIVERSALITY AND CPV

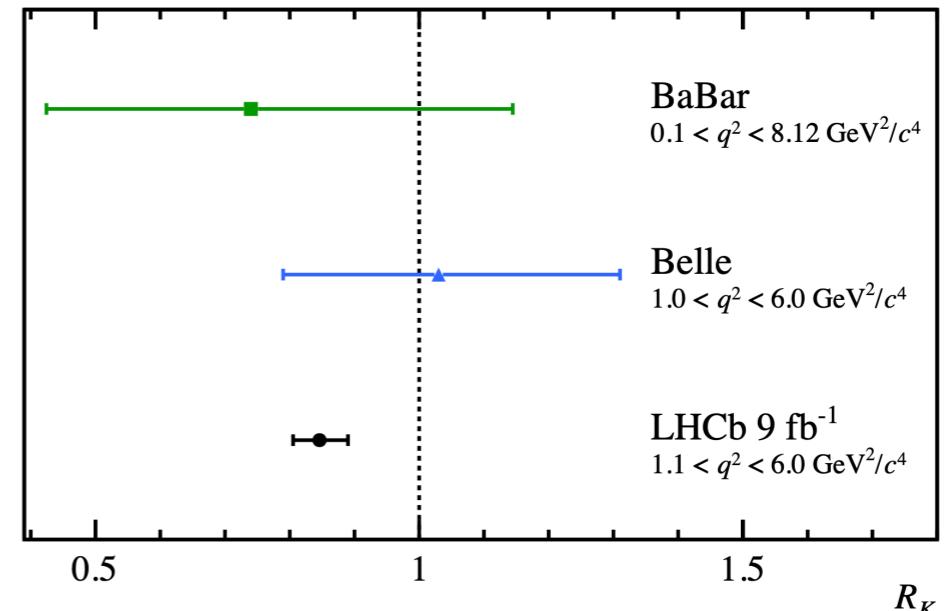
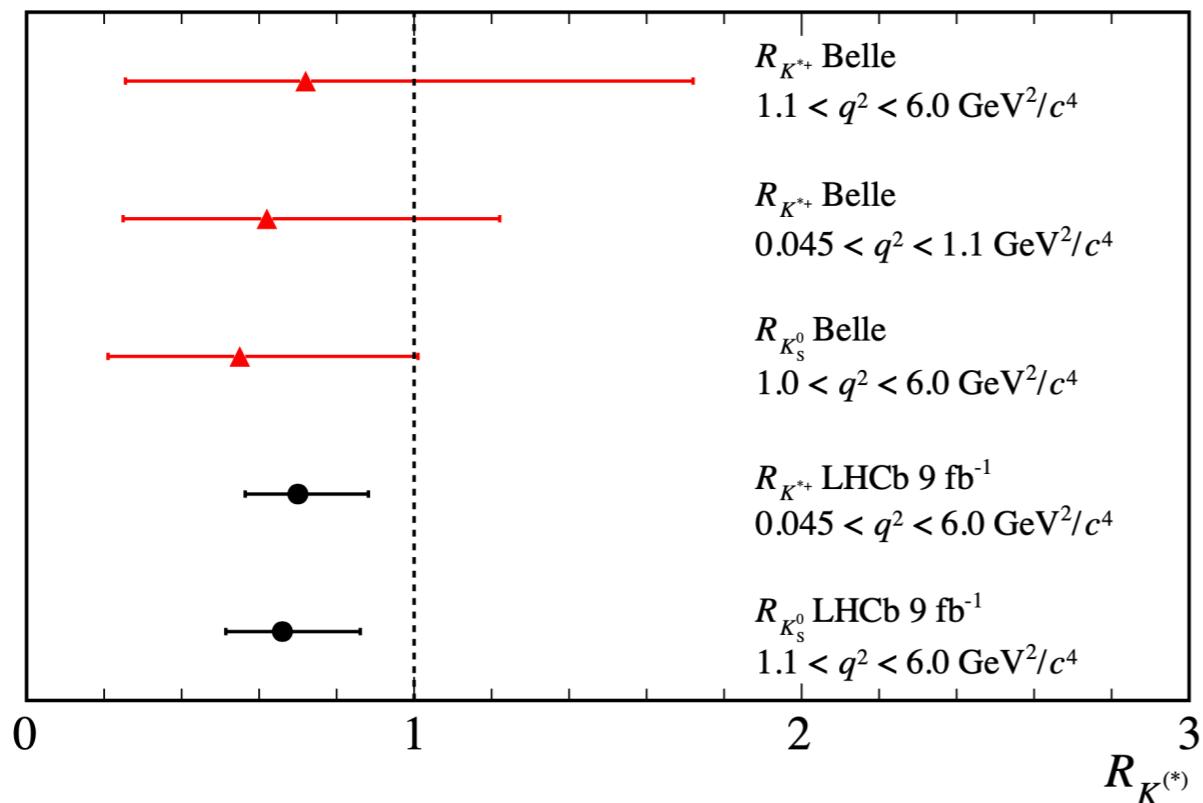
R_K

- Lepton flavour universality ratios (LFU) of $b \rightarrow sll$

$$R_K = \frac{\Gamma(B \rightarrow K\mu^+\mu^-)}{\Gamma(B \rightarrow Ke^+e^-)} \Big|_{[q^2_{\min}, q^2_{\max}]}$$

$$R_K = 0.846^{+0.042}_{-0.039} \text{ (stat.)} \quad {}^{+0.013}_{-0.012} \text{ (syst.)}$$

$$R_K^{\text{SM}} = 1.00 \pm 0.01$$



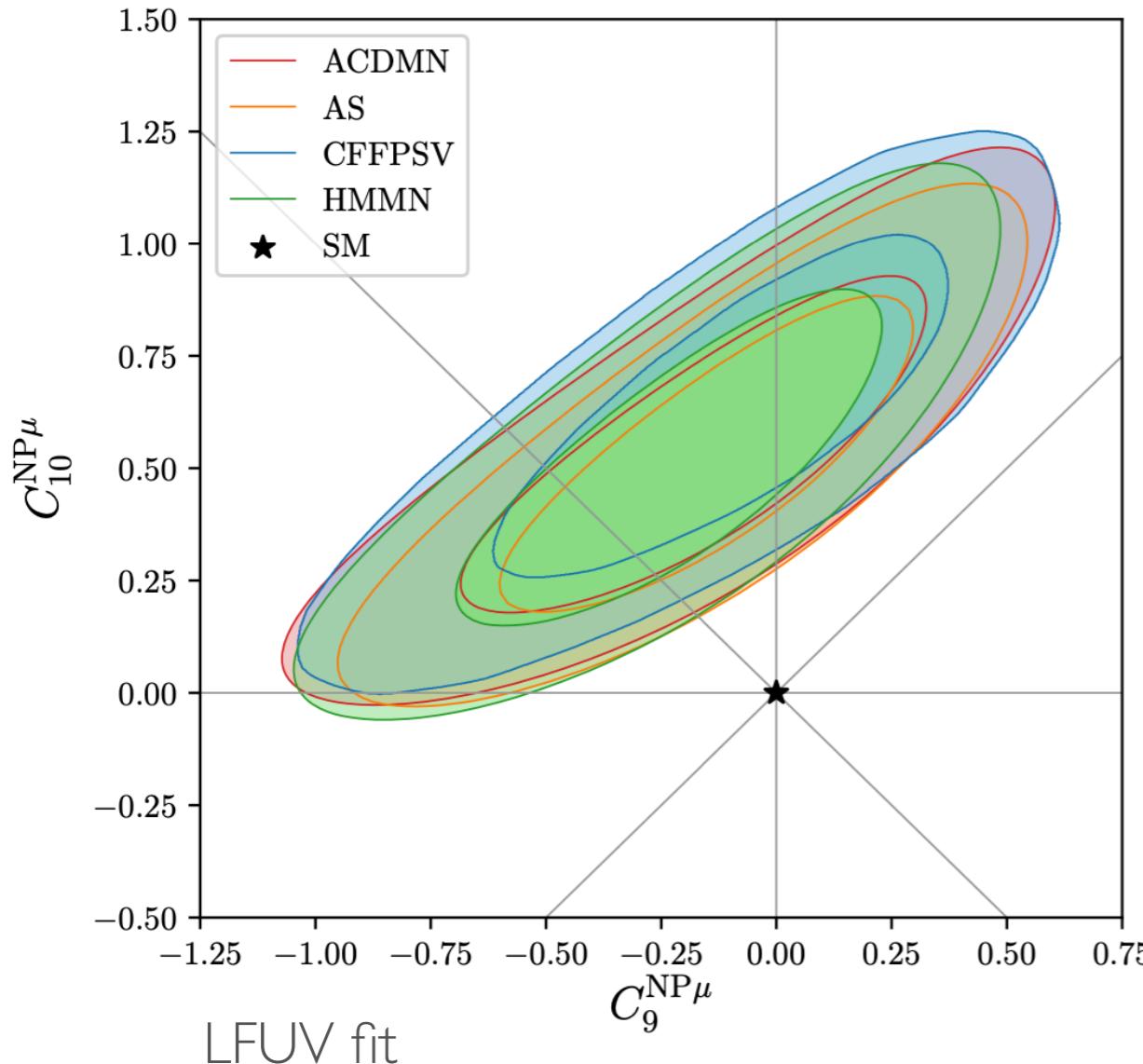
R_K

R_K is a ratio of CP-averaged rates

$$\mathcal{O}_{9(10)} = \frac{e^2}{(4\pi)^2} (\bar{s}_L \gamma_\nu b_L)(\bar{\mu} \gamma^\nu (\gamma^5) \mu)$$

SM amplitude is \sim CP even ($V_{tb} V_{ts}^*$)

$$|\mathcal{A}_{\text{SM}} + \mathcal{A}_{\text{NP}}|^2 + |\mathcal{A}_{\text{SM}} + \mathcal{A}_{\text{NP}}^*|^2 \propto |\mathcal{A}_{\text{SM}}|^2 + |\mathcal{A}_{\text{NP}}|^2 + 2\Re(\mathcal{A}_{\text{SM}}(\mathcal{A}_{\text{NP}}^* + \mathcal{A}_{\text{NP}}))$$

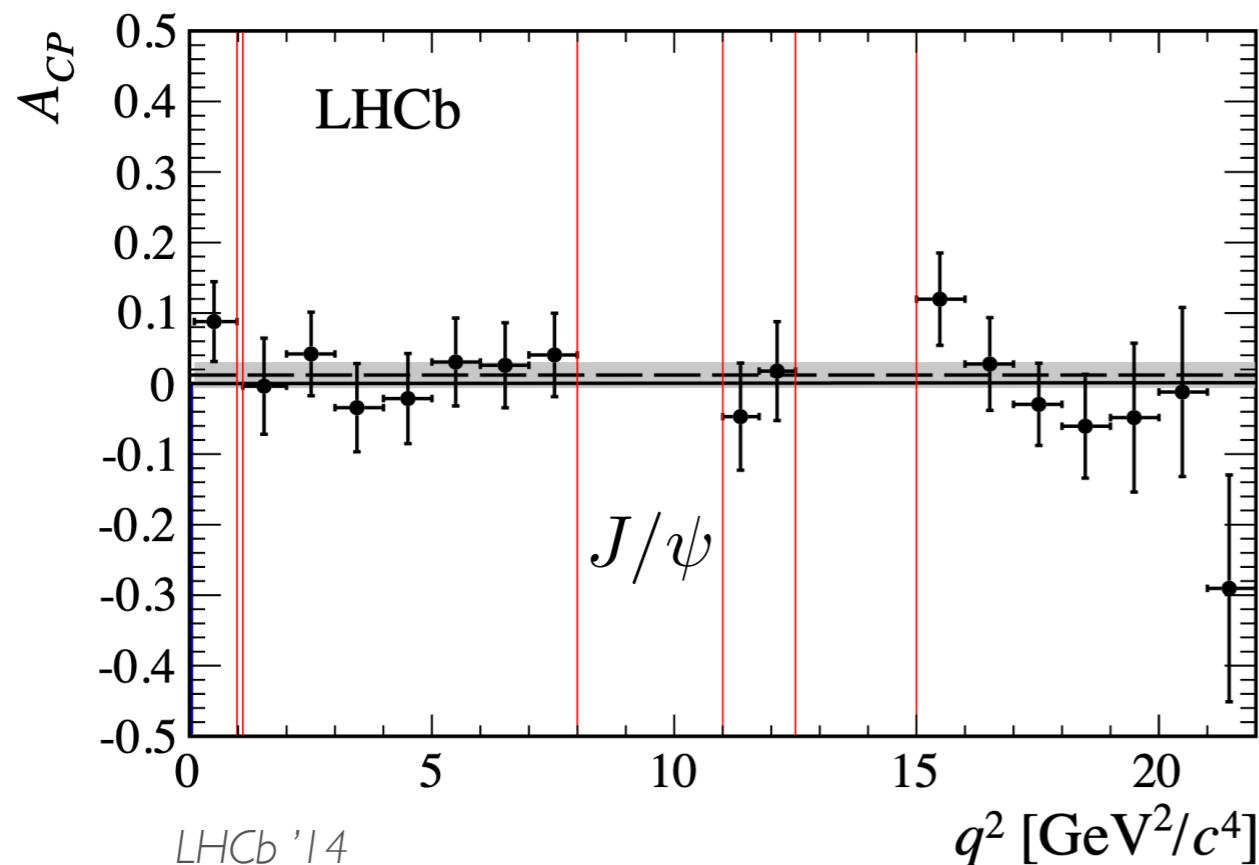


Consider $\delta C_9 = -\delta C_{10}$:

$$R_K = 1.00 + 0.48 \operatorname{Re}(\delta C_9) - 8.3 \times 10^{-3} \operatorname{Im}(\delta C_9) + 0.057 |\delta C_9|^2.$$

Inensitive to New Physics
CPV phases

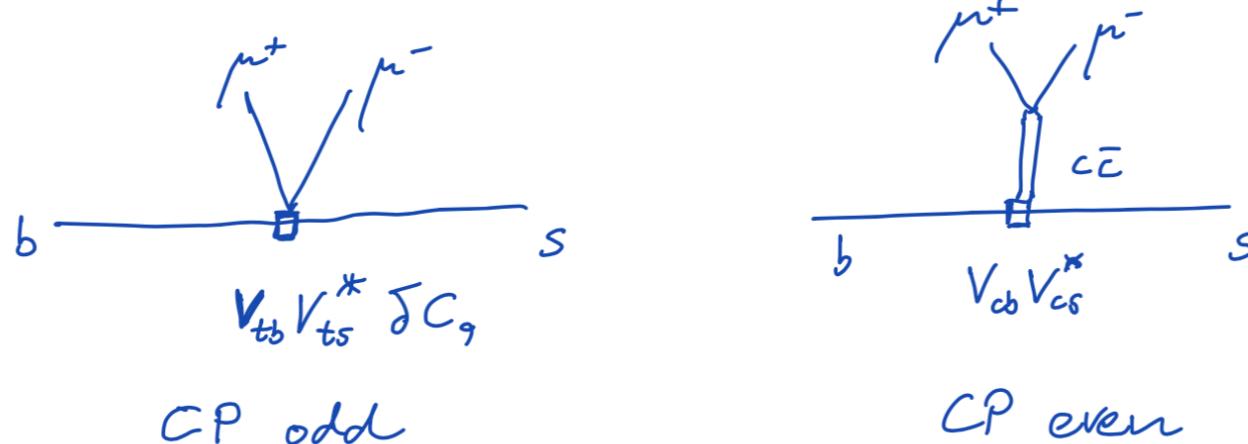
R_K : DIRECT ASYMMETRIES



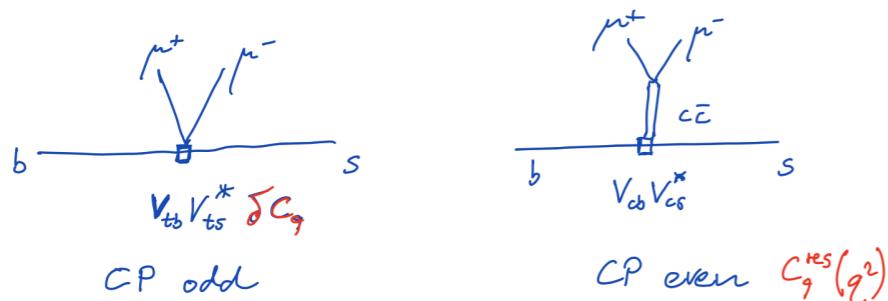
$$\mathcal{A}_{CP}^{K^{(*)}} = \frac{\mathcal{B}(\bar{B} \rightarrow \bar{K}^{(*)}\mu\mu) - \mathcal{B}(B \rightarrow K^{(*)}\mu\mu)}{\mathcal{B}(\bar{B} \rightarrow \bar{K}^{(*)}\mu\mu) + \mathcal{B}(B \rightarrow K^{(*)}\mu\mu)}$$

$$\mathcal{A}_{CP}^{K^+} = 0.012(17)(1)$$

Interfering amplitudes with strong and weak phases difference?

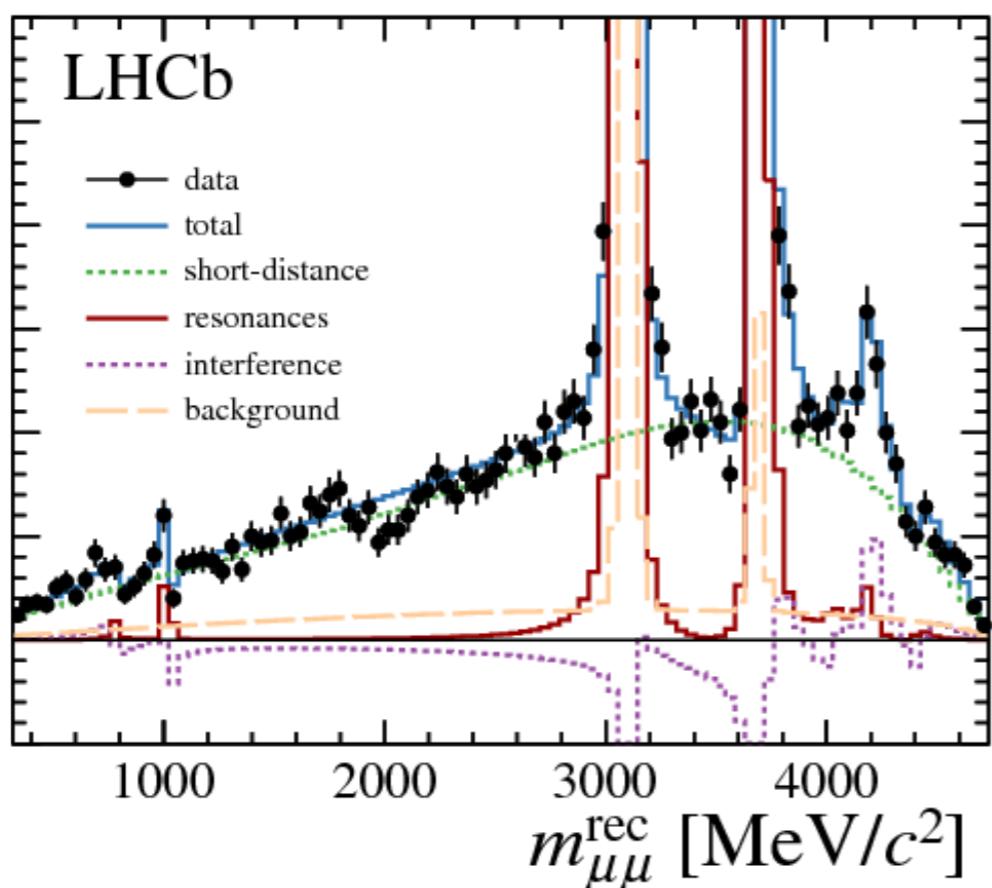


R_K : STRONG PHASE



$$C_9^{\text{res}}(q^2) \approx \frac{m_j \Gamma_j \eta_j e^{i\delta_j}}{m_j^2 - q^2 - im_j \Gamma_j}$$

δ_j : extract from CP-averaged non-blinded spectrum



4-fold degeneracy of fit to the spectrum:

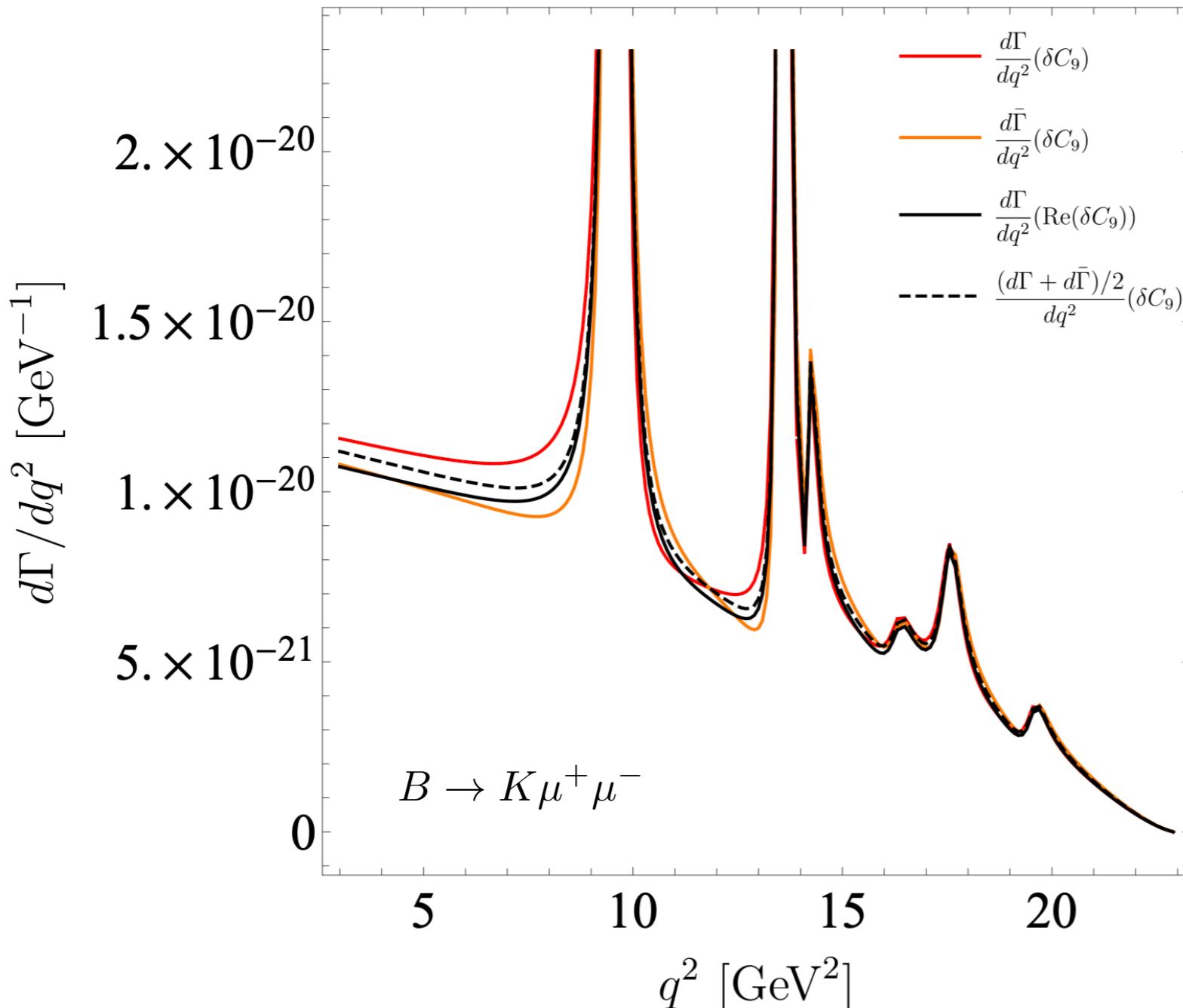
- Branch 1: $\delta_{J/\psi} = -1.66$, $\delta_{\psi(2S)} = -1.93$,
 Branch 2: $\delta_{J/\psi} = -1.50$, $\delta_{\psi(2S)} = 2.08$.

Branch 3,4 ~ Branch 1,2

LHCb '16
 see also Blake, Egede, Owen, Petridis, Pomery '17

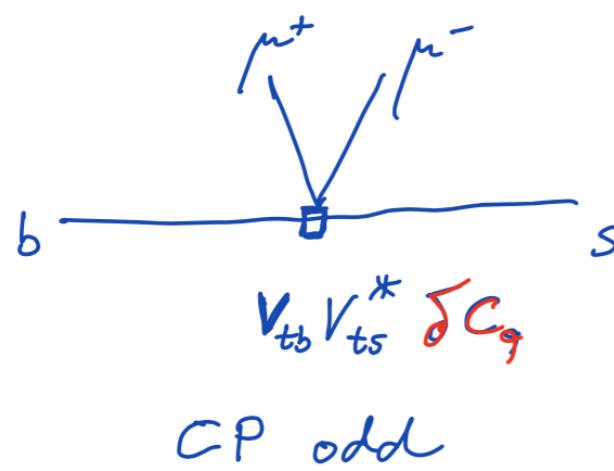
NO CP VS. CP-AVERAGE

$$\delta C_9 = -\delta C_{10} = -0.48 - 0.7i$$

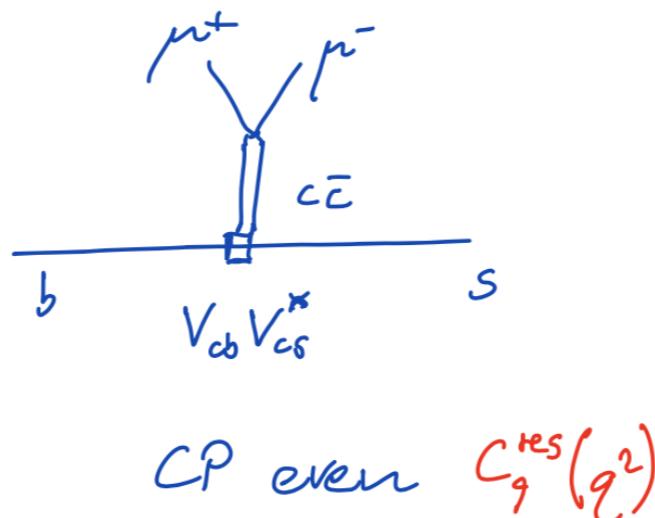


Resonant parameters taken from the LHCb fit to CP averaged rates.

R_K : DIRECT ASYMMETRIES



CP odd

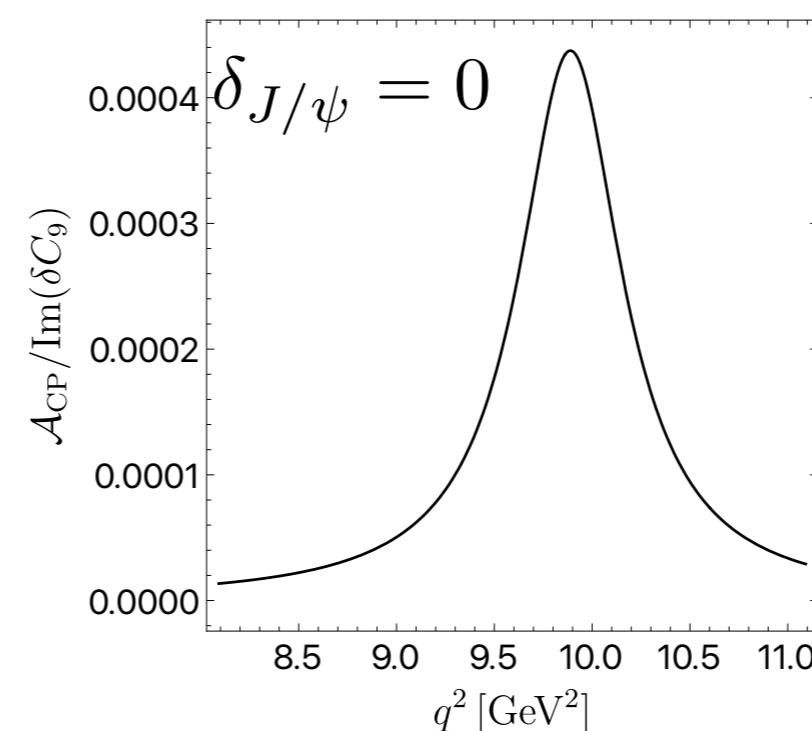
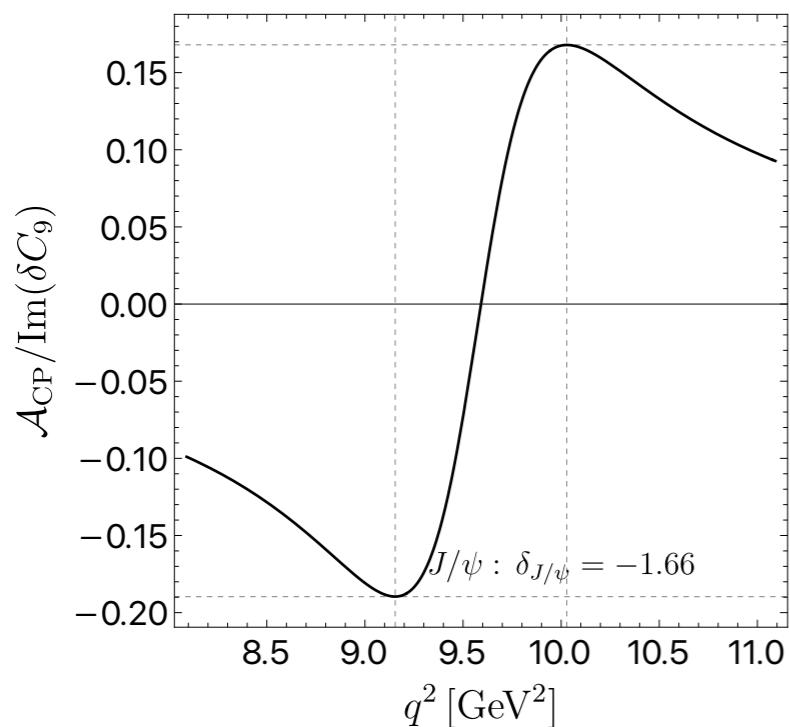


$$C_9^{\text{res}}(q^2) \approx \frac{m_j \Gamma_j \eta_j e^{i\delta_j}}{m_j^2 - q^2 - im_j \Gamma_j}$$

$$\mathcal{A}_{\text{CP}} = \text{Im}(\delta C_9) \frac{2\eta_j (\cos \delta_j - x \sin \delta_j)}{\eta_j^2 - 2\eta_j B [\sin \delta_j + x \cos \delta_j] + A [1 + x^2]}$$

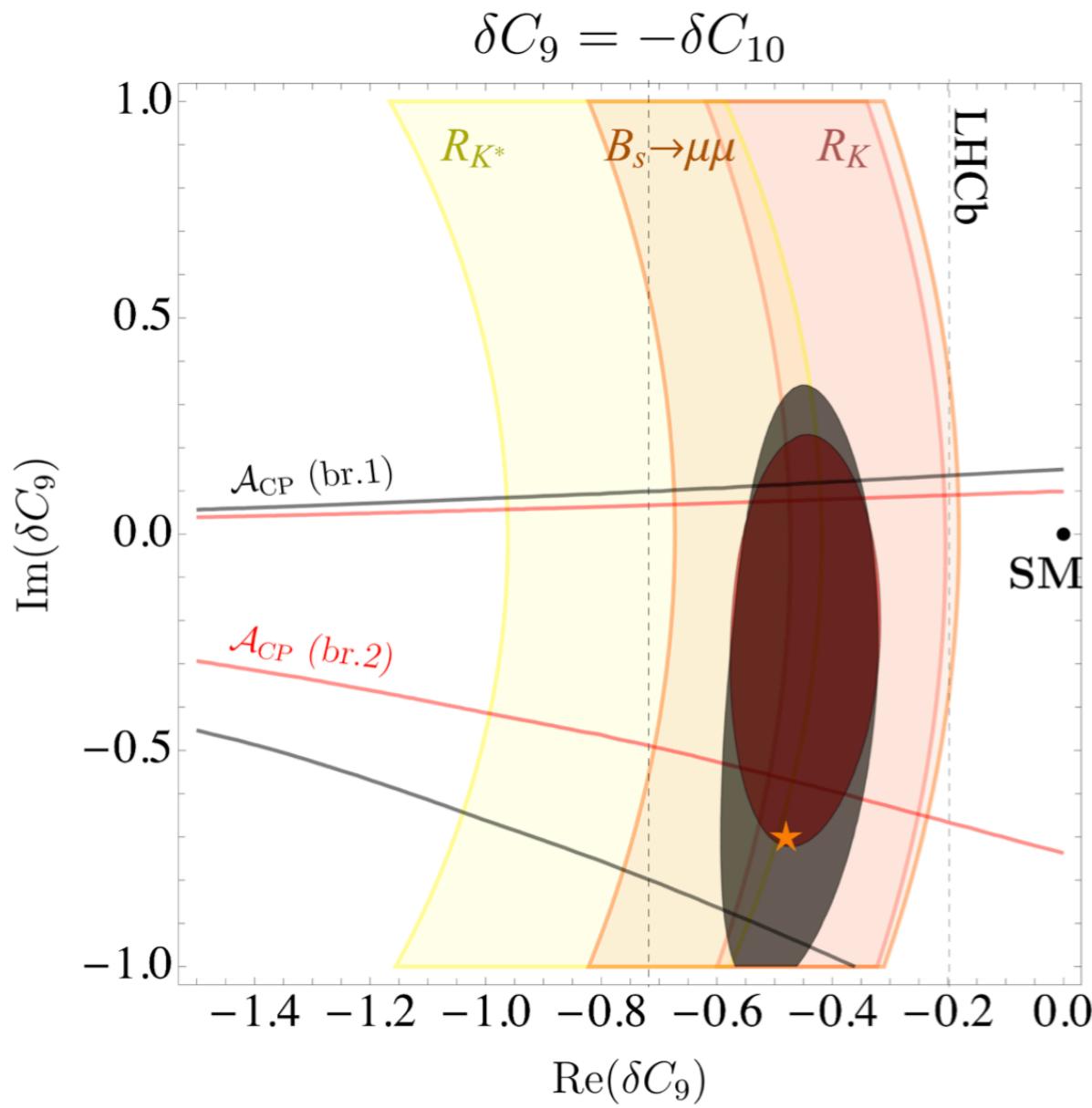
$$x \equiv (q^2 - m_j^2)/(m_j \Gamma_j)$$

Input: off-peak strong phase δ_j



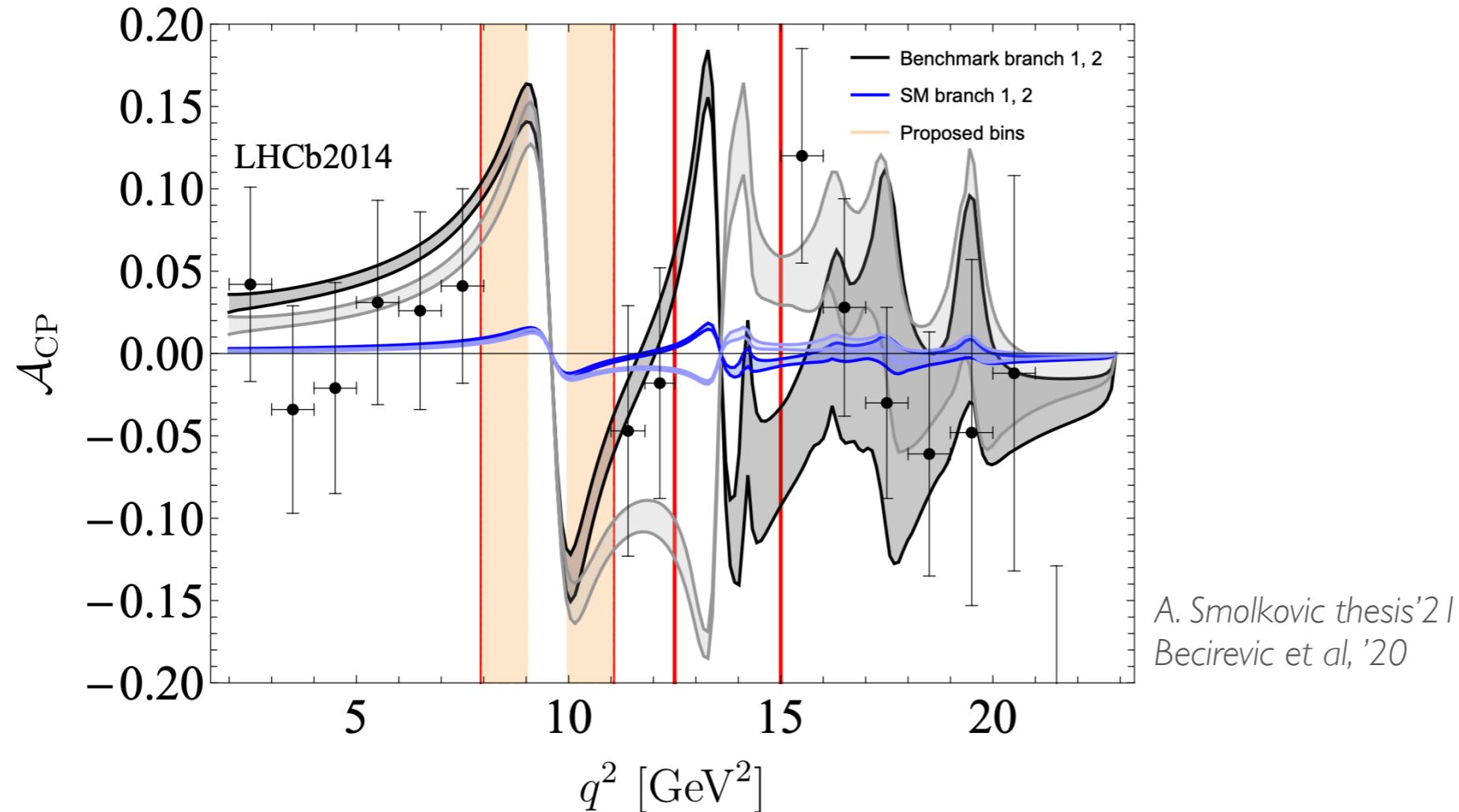
Sensitive to CPV in δC_9

R_K AND DIRECT CPV



R_K AND DIRECT CPV

$$\delta C_9 = -\delta C_{10} = -0.46 - 0.71i$$



Interesting region to look for direct CPV

$$\Delta A_{CP} \equiv \frac{\bar{\Gamma}_{[8,9]} - \Gamma_{[8,9]} - \bar{\Gamma}_{[10,11]} + \Gamma_{[10,11]}}{\bar{\Gamma}_{[8,9]} + \Gamma_{[8,9]} + \bar{\Gamma}_{[10,11]} + \Gamma_{[10,11]}}$$

$$\Delta A_{CP} = \frac{0.0108(2) - 0.139(3) \operatorname{Im}(\delta C_9)}{1 + 0.414(5) \operatorname{Re}(\delta C_9) - 0.0082(1) \operatorname{Im}(\delta C_9) + 0.054(1) |\delta C_9|^2}$$

NK, A. Smolkovic, '21
for other CPV constraints see also
Descotes-Genon, Novoa-Brunet, Vos '20
Carvunis, Dettori, Gangal, Guadagnoli, Normand '21

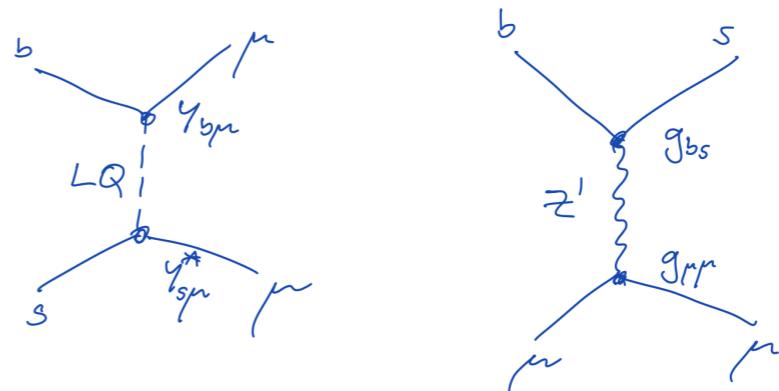
MODEL DEPENDENT CP-SENSITIVE OBSERVABLES

MODELS AND PREDICTIVITY

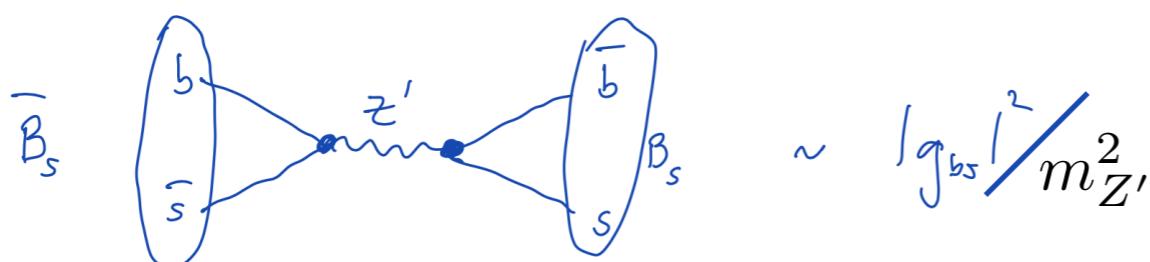
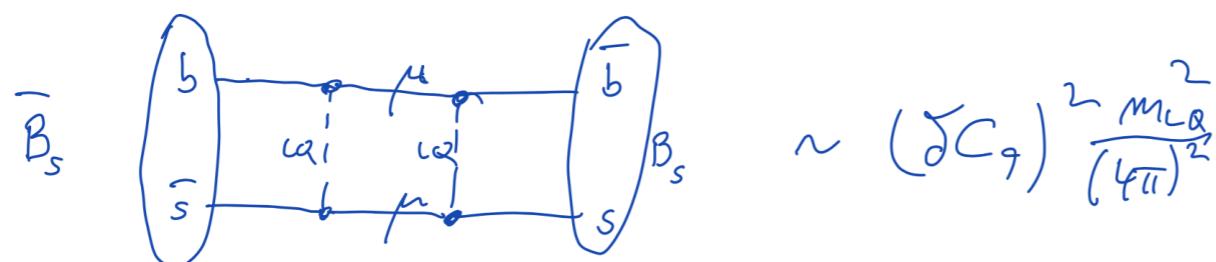
- Tree-level leptoquark or Z' models can explain $R_K^{(*)}$
- SMEFT operators

$$Q_{lq}^{(1)} = (\bar{L}_p \gamma^\mu L_r)(\bar{Q}_s \gamma_\mu Q_t),$$

$$Q_{lq}^{(3)} = (\bar{L}_p \gamma^\mu \tau^I L_r)(\bar{Q}_s \gamma_\mu \tau^I Q_t)$$



- LQ contrib. is correlated to small effect in $\Delta B=2$
- Z' models allow for more tuning

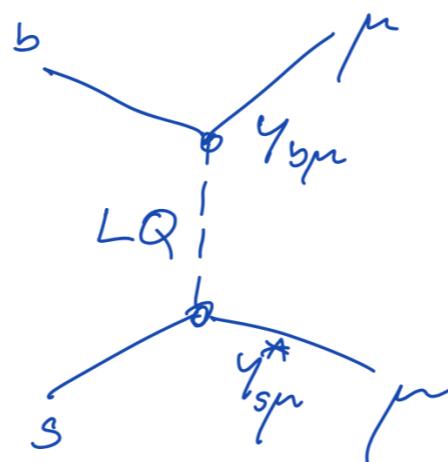


S_3 LEPTOQUARK

- SMEFT semileptonic operators leading to $\delta C_9 = -\delta C_{10}$

$$Q_{lq}^{(1)} = (\bar{L}_p \gamma^\mu L_r)(\bar{Q}_s \gamma_\mu Q_t),$$

$$Q_{lq}^{(3)} = (\bar{L}_p \gamma^\mu \tau^I L_r)(\bar{Q}_s \gamma_\mu \tau^I Q_t)$$



$$S_3 = (\bar{3}, 3)_{1/3}$$

$$C_{lq}^{(1)} = \frac{3y_{b\mu}y_{s\mu}^*}{4m_{S_3}^2}, \quad C_{lq}^{(3)} = \frac{y_{b\mu}y_{s\mu}^*}{4m_{S_3}^2}$$

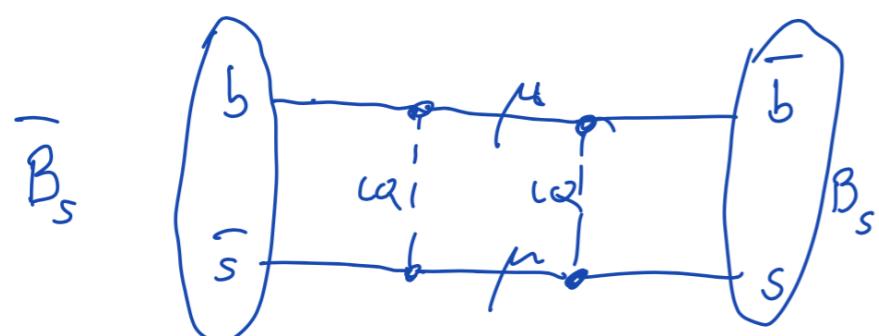
- $\Delta B=2$

$$Q_{qq}^{(1)} = (\bar{Q}_p \gamma^\mu Q_r)(\bar{Q}_s \gamma_\mu Q_t),$$

$$Q_{qq}^{(3)} = (\bar{Q}_p \gamma^\mu \tau^I Q_r)(\bar{Q}_s \gamma_\mu \tau^I Q_t)$$

$$C_{qq}^{(1)} = -\frac{9(y_{b\mu}y_{s\mu}^*)^2}{256\pi^2 m_{S_3}^2},$$

$$C_{qq}^{(3)} = -\frac{(y_{b\mu}y_{s\mu}^*)^2}{256\pi^2 m_{S_3}^2}$$



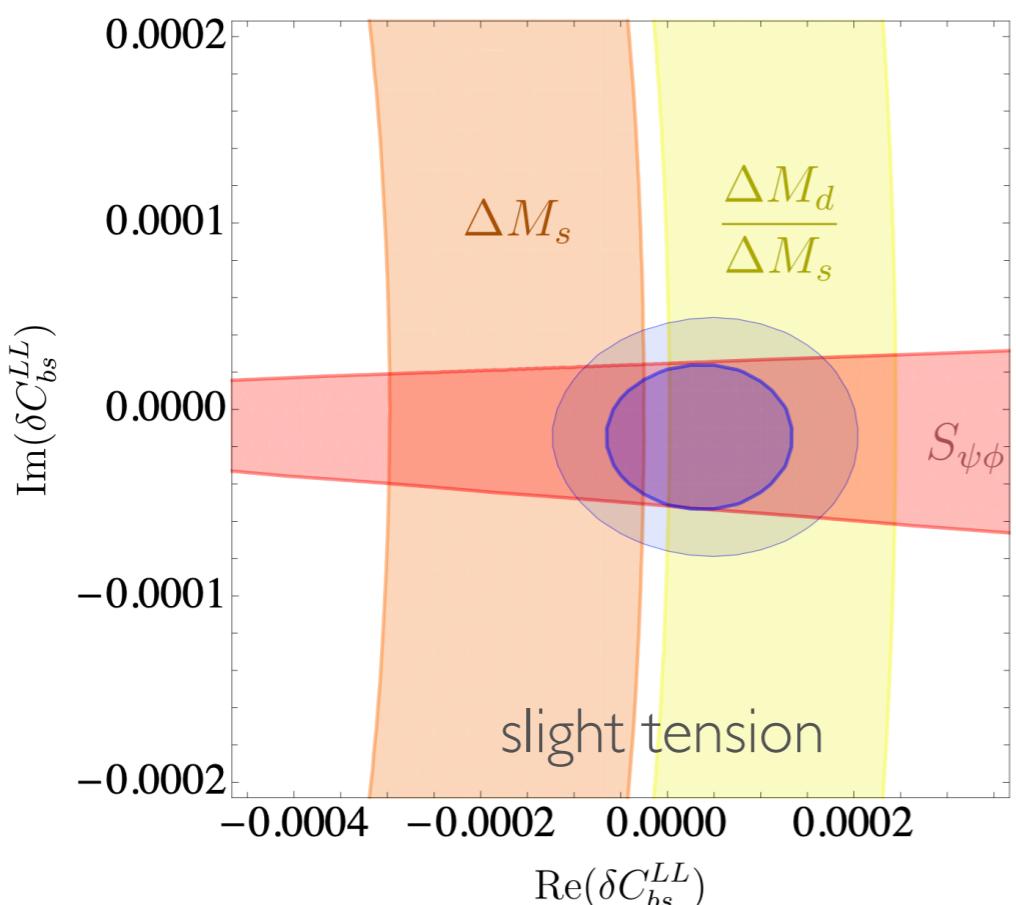
CP(V) effect in Δm_s and $S_{\psi\varphi}$?

S_3 LEPTOQUARK AND $\Delta B=2$

- left-left currents

$$\mathcal{L}_{bs} = -\frac{4G_F}{\sqrt{2}}(V_{tb}V_{ts}^*)^2 C_{bs}^{LL}(\mu) (\bar{s}_L \gamma^\mu b_L)^2 \quad C_{bs}^{LL(\text{SM})} + \delta C_{bs}^{LL}$$

$$\delta C_{bs}^{LL}(\mu = m_b) = \eta^{6/23} \frac{5(y_{b\mu}y_{s\mu}^*)^2}{256\sqrt{2}\pi^2 m_{S_3}^2 G_F (V_{tb}V_{ts}^*)^2} \sim (\delta C_9)^2 m_{S_3}^2$$



$$\Delta M_s^{\text{SM}} = \frac{4\sqrt{2}}{3} G_F m_{B_s} C_{bs}^{LL(\text{SM})} |V_{tb}V_{ts}^*|^2 (f_{B_s} \sqrt{B_{B_s}})^2$$

$$\left(\frac{\Delta M_d}{\Delta M_s}\right)^{\text{SM}} = \frac{1}{\xi^2} \left| \frac{V_{td}}{V_{ts}} \right|^2 \frac{M_{B_d}}{M_{B_s}} = 0.0311^{+0.0018}_{-0.0017}$$

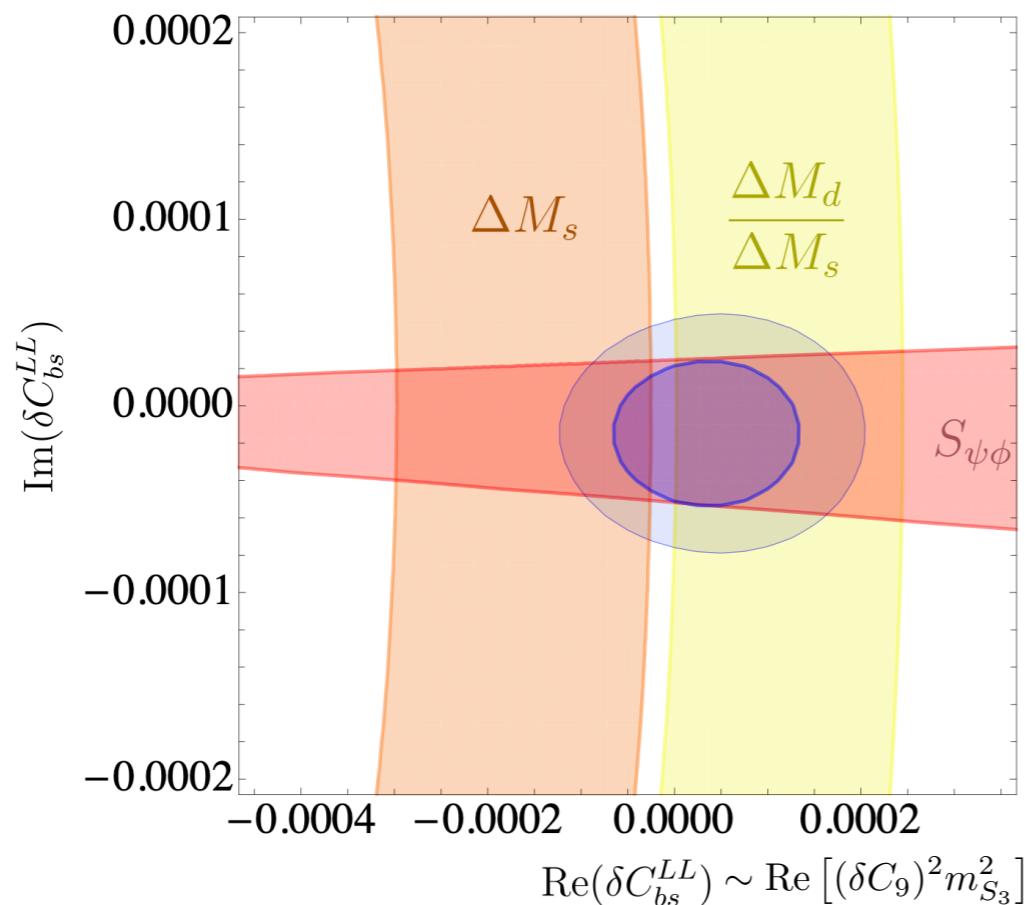
$$S_{\psi\phi} \equiv \sin(-2\beta_s + \delta\phi),$$

$$\delta\phi = \text{Arg} \left(1 + \frac{\delta C_{bs}^{LL}(m_b)}{C_{bs}^{LL(\text{SM})}(m_b)} \right)$$

Huge thanks to
 FLAG lattice averaging group
 HFLAV
and those contributing

S_3 LEPTOQUARK AND $\Delta B=2$

$$\delta C_{bs}^{LL}(\mu = m_b) = \eta^{6/23} \frac{5(y_{b\mu}y_{s\mu}^*)^2}{256\sqrt{2}\pi^2 m_{S_3}^2 G_F (V_{tb}V_{ts}^*)^2} \sim (\delta C_9)^2 m_{S_3}^2$$

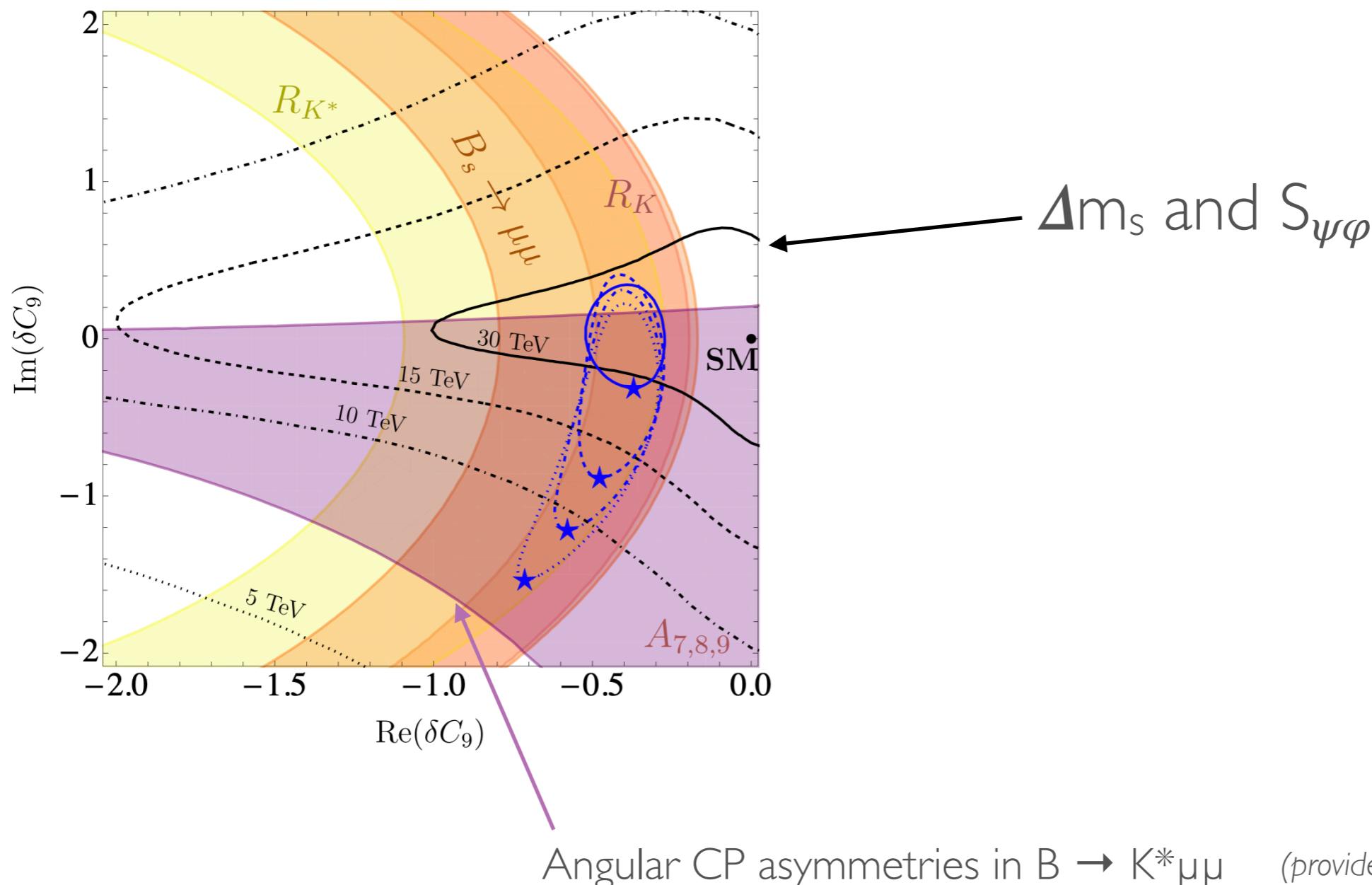


$\Delta M_s < \Delta M_s^{\text{SM}}$ requires $\text{Im}(\delta C_9)$!

$S_{\psi\phi}$ is sensitive to $\text{Re}(\delta C_9)$ $\text{Im}(\delta C_9)$

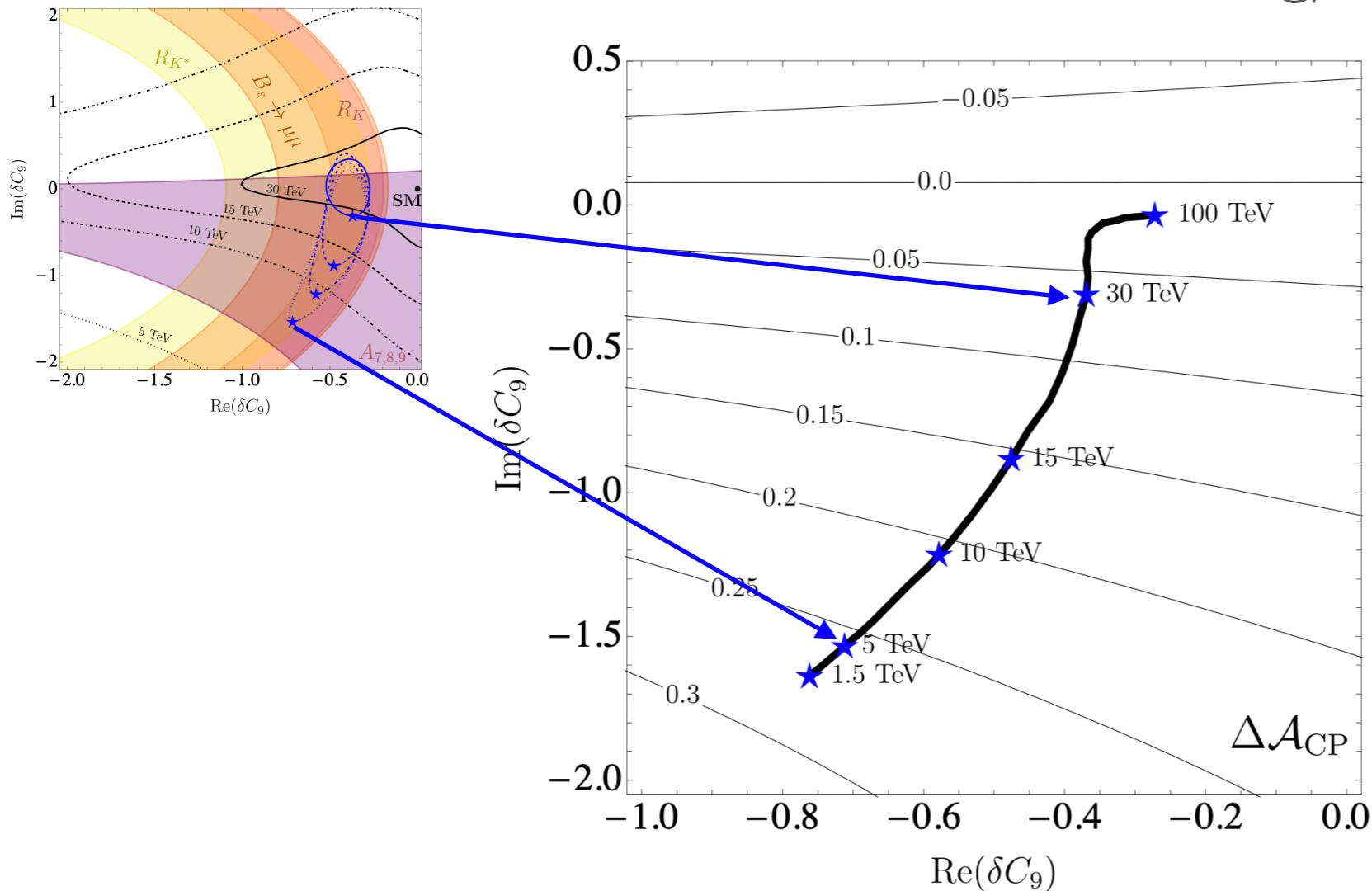
S_3 : PUTTING IT TOGETHER

Black contours from $\Delta B=2$



S_3 : PUTTING IT TOGETHER

Predicted maximal A_{CP}



$$\Delta A_{CP} \equiv \frac{\bar{\Gamma}_{[8,9]} - \Gamma_{[8,9]} - \bar{\Gamma}_{[10,11]} + \Gamma_{[10,11]}}{\bar{\Gamma}_{[8,9]} + \Gamma_{[8,9]} + \bar{\Gamma}_{[10,11]} + \Gamma_{[10,11]}}$$

SUMMARY AND CONCLUSIONS

- There are strong hints of NP in lepton flavour universality ratios.
- These observables are insensitive to CP.
- If this is indeed a NP effect CPV should be probed.
- The proposal is to measure potentially large CPV around J/ψ .
- LQ model: large effects possible with small LQ mass.
- CPV effects also possible for $R_D^{(*)}$, R_2 leptoquark solution entails CPV.
- Testable in high-pT angular correlations/asymmetries.

Thanks!