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Chiral EFT for direct detection

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- EST.1943 —

Outline

- Introduction: EFT framework for direct detection
- Chiral EFT for scalar quark-WIMP interactions
 - Matching to NLO
 - Phenomenology
- Conclusions

Based on: VC, M. Graesser, G. Ovanesyan, JHEP 1210 (2012) 025, arXiv:1205.2695 [hep-ph] VC, M. Graesser, G. Ovanesyan, I. Shoemaker, PLB 739 (2014) 293, arXiv:1311.5886 [hep-ph]

Introduction

WIMP direct detection (1)

• Typical scales involved in direct detection process:



$$|\vec{q}|_{\max} = 2 \,\mu \, v_{
m rel} < 2 \, m_A \, v_0 \sim 200 {
m MeV}$$

 $E_R < \frac{|\vec{q}|_{\max}^2}{2m_A} \sim 200 {
m KeV}$
 $m_A \sim 100 {
m GeV}$ $v_0 \sim 10^{-3}$

"Right" kinematics for (chiral) expansion in $p \sim q/m_N \sim m_\pi/m_N$

WIMP direct detection (II)



 Here focus on hadronic / nuclear physics effects, using chiral EFT power counting as organizing principle

EFT framework for direct detection



<mark>∧</mark>н (~GeV)

EFT framework for direct detection



EFT framework for direct detection



Strategy

- For a given quark-level operator:
 - I. Chiral symmetry \rightarrow WIMP couplings to π , N at small q
 - 2. Chiral power counting for $XN_1...N_A \rightarrow XN_1...N_A$ amplitudes $\Rightarrow V_{XN}, V_{XNN}, ...$ to a given order in $p \sim q/m_N \sim m_{\pi}/m_N$
 - 3. Nuclear matrix elements

Same strategy as in electron-nucleus or neutrino-nucleus scattering (difference is in the operator structure, kinematic regime, target nuclei)

Chiral EFT for scalar interactions

For a discussion of other operators, see Hoferichter-Klos-Schwenk 1503.04811 and references therein

Scalar interactions

• GeV-scale effective Lagrangian* involves 4 short-distance couplings

$$\mathcal{L}_{\rm SM} + \frac{1}{v} \frac{XX}{\Lambda^{[XX]-1}} \left[\sum_{q=u,d,s} \lambda_q \ m_q \ \bar{q}q \ + \ \lambda_\theta \ \theta_\mu^\mu \right] + \dots$$

• Hadronic realization of

$$\mathcal{L}_{\text{QCD}} + \sum_{q=u,d,s} s_q \,\bar{q}q + s_\theta \,\theta^\mu_\mu$$

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$$\mathcal{L}_{\text{QCD}} + \sum_{q=u,d,s} s_q \,\bar{q}q + s_\theta \,\theta^\mu_\mu$$

 Usual chiral Lagrangian, organized as expansion in derivatives ∂~O(p) and chiral symmetry breaking m_q~O(p²)

$$\begin{pmatrix} \mathcal{L}_M = \mathcal{L}_M^{(2)} + \mathcal{L}_M^{(4)} + \dots \\ \pi & \downarrow & \pi \\ & \downarrow & \pi \\ & \downarrow & \uparrow & \sim \frac{p_i \cdot p_j}{F_\pi^2} \\ \pi & \pi & \pi \end{pmatrix}$$

• Hadronic realization of

$$\mathcal{L}_{\text{QCD}} + \sum_{q=u,d,s} s_q \,\bar{q}q + s_\theta \,\theta^\mu_\mu$$

$$s_q = \lambda_q \frac{m_q}{v} \frac{XX}{\Lambda^{[XX]-1}}$$

 Scalar source appears in chiral effective Lagrangian in the same way as quark mass matrix

• Hadronic realization of

$$\mathcal{L}_{\text{QCD}} + \sum_{q=u,d,s} s_q \,\bar{q}q + s_\theta \theta^\mu_\mu$$
$$s_\theta = \lambda_\theta \frac{1}{v} \frac{XX}{\Lambda^{[XX]-1}}$$

 Energy-momentum tensor operator identified by coupling chiral EFT to external metric

Donoghue-Leutwyler 1991

....

2. Power counting and V_{XN} , V_{XNN} , ...

• Non-perturbative amplitude T: sum of ladder diagrams

- <u>One insertion</u> of A-nucleon irreducible amplitude with external probe attached

- Has well defined power counting (no IR enhancements $\sim M_n/q$)

- <u>Arbitrary many insertions</u> of A-nucleon irreducible amplitude with only strong vertices

2. Power counting and V_{XN} , V_{XNN} , ...

• Non-perturbative amplitude T: sum of ladder diagrams

• Match T to non-rel. Lippmann-Schwinger description

Fourier Transform

$$M_{A,X}(\vec{q}_1,...,\vec{q}_A,\vec{q}_X) \quad \longleftrightarrow \quad H_I(\vec{x}_1,...,\vec{x}_A,\vec{x}_X) = V_{XN} + V_{XNN} + \ldots$$

Leading terms in H_1 (potentials) determined by power counting of $M_{A,X}$

2. Power counting and V_{XN} , V_{XNN} , ...

• Scalar density:

• Energy-momentum tensor: first corrections arise in principle to NNLO

• NLO amplitude: I-nucleon

$$M_{1,X} = f_N(q^2) X X \bar{N} N \qquad N = p, n$$

$$f_{p/n}(q^2) = \frac{1}{v \Lambda_{np}^2} \left[\sum_{q=u,d,s} \lambda_q \sigma_q^{(p/n)} + \lambda_\Theta m_{p/n} - \frac{g_A^2}{64\pi F_\pi^2} \left(A(q^2) \pm B(q^2) \right) \right]$$
Usual q=0 term, controlled by sigma terms:

$$\left[\langle i | m_q q \bar{q} | i \rangle = \sigma_q^{(i)} \bar{\psi}_i \psi_i \right]$$

Crivellin-Hoferichter-Procura 1312.4951

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Usual q=0 term,
controlled by sigma terms:
Slope term: no new couplings

$$\langle i | m_q q \bar{q} | i \rangle = \sigma_q^{(i)} \bar{\psi}_i \psi_i$$

Giedt-Thomas-Young 0907.4177 Kronfeld 1203.1204

Crivellin-Hoferichter-Procura 1312.4951

• NLO amplitude: 2-nucleons

$$M_{2,X} = \mathcal{M}_{\pi\pi} + \mathcal{M}_{\eta\eta}$$

ππ contribution first considered in Kamionkoski-Kurylov-Prezeau-Vogel, 2003

3. Nuclear matrix elements

 $\langle f|\hat{T}|i\rangle = (2\pi)^3 \delta^{(3)} (\vec{q}_X + \vec{q}_A) T(\vec{q}_X) \qquad T(\vec{q}_X) = T_1 + T_2$

$$T_1 = \sum_{i=1,A} \int d\vec{x}_i \ \rho_1(\vec{x}_i) \otimes \tilde{V}_1(\vec{q}_X; \vec{x}_i)$$
$$T_2 = \sum_{i < j} \int d\vec{x}_i d\vec{x}_j \ \rho_2(\vec{x}_i, \vec{x}_j) \otimes \tilde{V}_2(\vec{q}_X; \vec{x}_i, \vec{x}_j)$$

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q-dependent "potentials", related to momentum-space amplitudes

$$\begin{split} \tilde{V}_{1}(\vec{q}_{X};\vec{x}_{i}) &= -\int \frac{d\vec{q}_{i}}{(2\pi)^{3}} e^{-i\vec{q}_{i}\cdot\vec{x}_{i}} \ (2\pi)^{3} \delta^{(3)}(\vec{q}_{i}+\vec{q}_{X}) \ \overline{M}_{1,X}(\vec{q}_{i},\vec{q}_{X}) \\ \tilde{V}_{2}(\vec{q}_{X};\vec{x}_{i},\vec{x}_{j}) &= -\int \frac{d\vec{q}_{i}}{(2\pi)^{3}} \frac{d\vec{q}_{j}}{(2\pi)^{3}} e^{-i\vec{q}_{i}\cdot\vec{x}_{i}} e^{-i\vec{q}_{j}\cdot\vec{x}_{j}} \ (2\pi)^{3} \delta^{(3)}(\vec{q}_{i}+\vec{q}_{j}+\vec{q}_{X}) \ \overline{M}_{2,X}(\vec{q}_{i},\vec{q}_{j},\vec{q}_{X}) \end{split}$$

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$$T_2 = \sum_{i < j} \int d\vec{x}_i \, d\vec{x}_j \left(\rho_2(\vec{x}_i, \vec{x}_j) \otimes \tilde{V}_2(\vec{q}_X; \vec{x}_i, \vec{x}_j) \right)$$

Nuclear structure input: one- and two-body densities in the ground state

$$\rho_1(\vec{x}) = \int d\vec{x}_1 \dots d\vec{x}_{A-1} \ |\psi_0(\vec{x}_1, \dots, \vec{x}_{A-1}, \vec{x})|^2$$
$$\rho_2(\vec{x}, \vec{y}) = \int d\vec{x}_1 \dots d\vec{x}_{A-2} \ |\psi_0(\vec{x}_1, \dots, \vec{x}_{A-2}, \vec{x}, \vec{y})|^2$$

• One-body: factorization of nucleon and nuclear effects

• One-body: factorization of nucleon and nuclear effects

• Two-body: use shell model to get first rough estimate

$$\begin{aligned}
T_2^{(\pi\pi)} &= -\frac{\lambda_+}{v \Lambda_{\rm np}^2} \frac{g_A^2 m_\pi^3}{96 \pi F_\pi^2} \mathcal{N}_{\pi\pi} \times \exp\left(-\frac{|\vec{q}_X|^2 R^2(A)}{6}\right) \\
\mathcal{N}_{\pi\pi} &= -1.19 \, A
\end{aligned}$$

Phenomenology: scalar interactions

$$\frac{dR}{dE_R} = \frac{\kappa_X \rho_X}{\pi m_X} \left| \left[Z f_p(\boldsymbol{E_R}) + (A - Z) f_n(\boldsymbol{E_R}) \right] F(E_R) - T_2(\boldsymbol{E_R}, \boldsymbol{A}, \boldsymbol{Z}) \right|^2 \eta(E_R) \right|^2$$

The stuff in red is absent in the LO analysis

$$\frac{dR}{dE_R} = \frac{\kappa_X \rho_X}{\pi m_X} \left| \left[Zf_p(\boldsymbol{E_R}) + (A - Z)f_n(\boldsymbol{E_R}) \right] F(E_R) - T_2(\boldsymbol{E_R}, \boldsymbol{A}, \boldsymbol{Z}) \right|^2 \eta(E_R) \right|^2$$

• Anatomy of recoil spectrum: "astrophysics" factor

$$\frac{dR}{dE_R} = \frac{\kappa_X \rho_X}{\pi m_X} \left| \left[Z f_p(E_R) + (A - Z) f_n(E_R) \right] F(E_R) - T_2(E_R, A, Z) \right|^2 \eta \left(E_R \right) \right|^2$$

• Anatomy of recoil spectrum: hadronic / nuclear effects at LO

$$\frac{dR}{dE_R} = \frac{\kappa_X \rho_X}{\pi m_X} \left| \left[Z f_p(\boldsymbol{E_R}) + (A - Z) f_n(\boldsymbol{E_R}) \right] F(E_R) - T_2(\boldsymbol{E_R}, \boldsymbol{A}, \boldsymbol{Z}) \right|^2 \eta(E_R) \right|^2$$

• Anatomy of recoil spectrum: hadronic / nuclear effects at NLO

 $f(\mathbf{\Gamma})$

-
$$f_{p,n} (E_R) = f_{p,n} [\lambda_{q,\theta}] + k_{n,p} [\lambda_q] A E_R$$

Different linear combinations of λ 's

$$A = 133, \text{ slope is proportional to } A$$

$$E_R (keV)$$

$$\frac{dR}{dE_R} = \frac{\kappa_X \rho_X}{\pi m_X} \left| \left[Z f_p(\boldsymbol{E_R}) + (A - Z) f_n(\boldsymbol{E_R}) \right] F(E_R) - T_2(\boldsymbol{E_R}, \boldsymbol{A}, \boldsymbol{Z}) \right|^2 \eta(E_R) \right|^2$$

• Anatomy of recoil spectrum: hadronic / nuclear effects at NLO

C (D)

-
$$f_{p,n} (E_R) = f_{p,n} [\lambda_{q,\theta}] + k_{n,p} [\lambda_q] A E_R$$

Different linear combinations of λ 's
- $T_2(0,A,Z)/(A f_p (0)) \sim 5\%$
Similar to LQCD* estimate I306.6939
 $f_p(E_R)$
 $f_p(0)$
 $\lambda_u \neq 0$
 $\lambda_s \neq 0$
 λ_s

NLO vs LO: integrated rates

$$R = \left\langle \frac{dR}{dE_R} \right\rangle_{E_R}$$

- Huge effects along "singular" lines where LO is suppressed: $f_p \rightarrow 0$ (at finite r) and Z + (A-Z) r = 0
- Similar features for different targets and λ_s/λ_θ , m_X

$m_X = 10 \text{ GeV}$ NLO vs LO: spectra

$m_X = 100 \text{ GeV}$ NLO vs LO: spectra

Impact of NLO corrections

• While consistent with power counting, NLO effects can have significant impact

- Description of scalar-mediated WIMP-nucleus scattering involves 4 parameters $(\lambda_{u,d,s,\theta}/\Lambda^2)$ rather than 2 $(\sigma_P \text{ and } r = f_n/f_P)$
- LO and NLO contributions depend differently on λ 's \rightarrow corrections to amplitude can be larger than what expected by power counting, for certain choices of λ 's, <u>especially along LO "blind spot" directions</u>

"Isospin-violating dark matter"

 n and p do not have to couple to DM in the same way

Kurylov-Kamionkowski 2003 Giuliani 2005 Chang-Liu-Pierce-Weiner-Yavin 2010 Feng-Kumar-Marfatia-Sanford 2011

• Idea revived by conflicts in searches using different nuclei, when interpreted at LO with $r = f_n/f_p = I$

Can one reconcile experiments by having f_n ≠ f_p? (i.e. destructive interference in Xe, Ge but not-so-destructive for other nuclei, eg. Si?)

Degradation factors: LO

LO fit to data

- LO fit with r = -0.7 shows compatibility between CMDS-Si and LUX
- But it relies on large suppression of LO Xe cross-section
- What about NLO chiral corrections?

Fits use 2013 input from CDMS-Si and LUX. Super CDMS (Ge) 2014 input not included

Degradation factors: NLO

$$D^{NLO}(r,\overline{\lambda}_s,\overline{\lambda}_\theta) = \frac{\overline{R}^{NLO}\left(r,\sigma_p,\overline{\lambda}_s,\overline{\lambda}_\theta\right)}{\overline{R}^{LO}\left(1,\sigma_p\right)}$$

- D^{NLO} still quadratic in r
- Location of the minimum shifts, depending on

$$\bar{\lambda}_{s,\theta} \equiv \frac{\lambda_{s,\theta}}{\lambda_u}$$

(couplings to heavy quarks)

1311.5886

Location and depth of the "dip" vs heavy-quark coupling:

r_{MIN} can take any value

In most cases "degradation"

This points to a manifold of "Xe-phobic" couplings (beyond r=-0.7)

NLO fit to data (I)

NLO fit to data (II)

- New compatibility regions at r ≠-0.7
- Characterized by quite different values of $\lambda_{u,d,s,\theta}$
- Different collider and indirect-detection signatures: richer structure!

What about N^2LO , ... ?

 At small recoil energy, to all orders in χEFT

$$dR \sim \left(Z + \Delta_{\mathcal{X}} + r\left(A - Z - \Delta_{\mathcal{Y}}\right)\right)^2$$

$$r_{\min} = \frac{\bar{Z}}{1 - \bar{Z}} \cdot \frac{1 + \frac{\Delta_{\chi}}{\bar{Z}}}{1 - \frac{\Delta_{\chi}}{1 - \bar{Z}}}$$

$$\bar{Z} = \frac{Z}{A}$$

What about N^2LO , ... ?

At small recoil energy, $dR \sim \left(Z + \Delta_{\chi} + r\left(A - Z - \Delta_{\chi}\right)\right)$ to all orders in χEFT $r_{\min} = \frac{\bar{Z}}{1 - \bar{Z}} \cdot \frac{1 + \frac{\Delta_{\chi}}{\bar{Z}}}{1 - \frac{\Delta_{\chi}}{1 - \frac{\bar{Z}}{1 - \bar{Z}}}}$ $\Delta_{\rm X} = 0.15, 0.17,..$ Xe, $\overline{\rm Z} \sim 0.4$ $\bar{Z} = \frac{Z}{\Lambda}$ 0.1 0.01 As long as Δ_X has well behaved expansion, r_{min} and LO dR(r) are stable against NLO 0.001 NNLO higher order corrections 10^{-4}

-2.0

-1.5

-1.0

r

-0.5

0.0

Conclusions

 Chiral EFT: systematic tool to analyze WIMP-Nucleus scattering and reconstruct or bound WIMP-quark couplings

- Impact of chiral corrections
 - Quantitative: precision DM phenomenology (post discovery)
 - Qualitative: sizable effects possible through interplay of short-distance parameters and hadronic effects.
 Dramatic effects on "blind spots", such as IVDM