



Muon $g-2$: experimental status

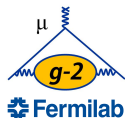
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on behalf of the Muon $g-2$ Collaboration



UNIVERSITÀ DI PISA



MITP
TOPICAL
WORKSHOP

The Evaluation of the Leading Hadronic
Contribution to the Muon $g-2$:
Toward the MUonE Experiment
14 – 18 November 2022



<https://indico.mitp.uni-mainz.de/event/>

μ ONE

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Theoretical Physics

Introduction: the muon anomaly

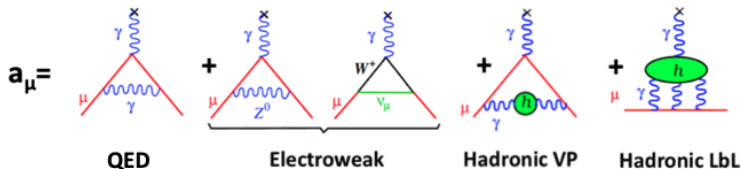
- **Muon:** elementary particle with spin-1/2 and magnetic moment proportional to spin through the **g-factor**:

$$\vec{\mu} = g \frac{q}{2m_{\mu}} \vec{S}$$

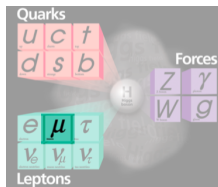
- At first order (Dirac theory for $s = 1/2$ particles) $g = 2$ but with higher order corrections $g > 2$:

$$\underbrace{g_{\mu} = 2 (1 + a_{\mu})}_{\text{Dirac}} \Rightarrow \boxed{a_{\mu} = \frac{g - 2}{2}} \quad \text{muon anomaly}$$

→ Theoretically calculated using the Standard Model (SM) :

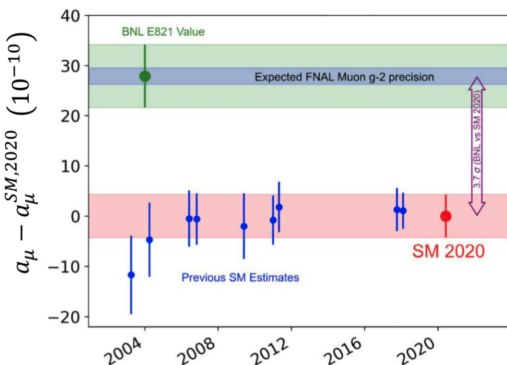


→ Comparison to measurement allows for a **precise test of the SM and to look for new physics**



Experimental measurement vs. SM calculation

- Long-standing $> 3\sigma$ discrepancy



- **E821 (BNL) experimental value:**

$$a_\mu^{E821,BNL} = 116592080(63) \times 10^{-11}$$

[Phys. Rev. D, 73 (2006) 072003]

- **SM value** re-evaluated in 2020 by Muon g-2 Theory Initiative:

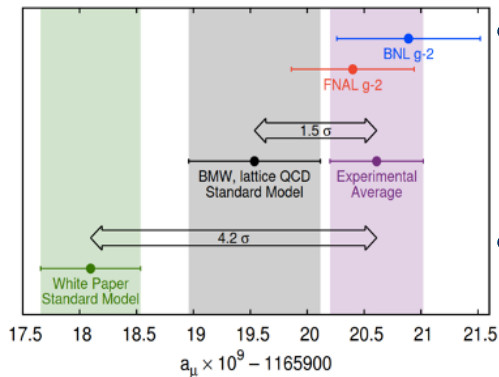
$$a_\mu^{SM,2020} = 116591810(43) \times 10^{-11}$$

[Phys. Rept. 887, 1 (2020)]

- In the meantime: **FNAL Exp.** was build and is collecting data since 2018 aiming to **improve uncertainty** with 140 ppb goal

Experimental measurement vs. SM calculation

- In April 2021 were published:



- a new measurement from **FNAL Muon g – 2 Exp. Run-1 data** that confirmed result from BNL:

$$a_\mu(\text{FNAL}) = 116592040(54) \cdot 10^{-11} \text{ (460 ppb)}$$

$$a_\mu(\text{BNL}) = 116592089(63) \cdot 10^{-11} \text{ (540 ppb)}$$

$$a_\mu(\text{Exp}) = 116592061(41) \cdot 10^{-11} \text{ (350 ppb)}$$

[Phys. Rev. Lett. **126**, no.14, 141801 (2021)]

- a new theoretical calculation $a_\mu(\text{BMW, SM})$ based on Lattice QCD in tension with $a_\mu(\text{WP, SM})$ calculation based on e^+e^- data

[Nature **593** (2021) 51-55]

- This talk: status of the FNAL Muon g – 2 exp. – Run-1 result and beyond

Experimental technique

1. Inject polarized muons into a magnetic storage ring
2. Muons circulate around the ring at the cyclotron frequency:

$$\vec{\omega}_C = \frac{q}{\gamma m_\mu} \vec{B}$$

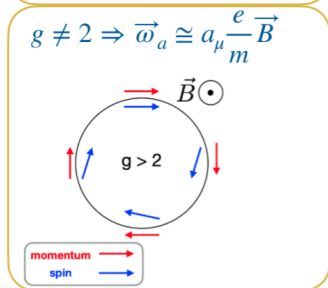
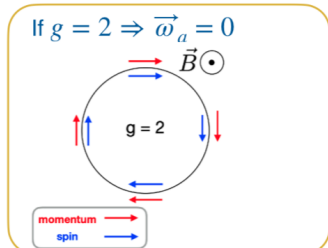
3. Muon spin precession frequency (Larmor) is given by:

$$\vec{\omega}_S = \frac{q}{\gamma m_\mu} \vec{B} (1 + \gamma a_\mu)$$

4. Muon anomaly is related to **anomalous precession frequency**:

$$\vec{\omega}_a \cong \vec{\omega}_S - \vec{\omega}_C \cong a_\mu \frac{q}{m_\mu} \vec{B}$$

5. Measure B and ω_a to extract the anomaly



Final formula

Muon anomaly is determined with:

$$a_\mu = \underbrace{\frac{\omega_a}{\tilde{\omega}'_p(T_r)}}_{\text{ratio of frequencies } (R_\mu) \text{ measured by us}} \underbrace{\frac{\mu'_p(T_r)}{\mu_e(H)} \frac{\mu_e(H)}{\mu_e} \frac{m_\mu}{m_e} \frac{g_e}{2}}_{\text{fundamental factors (combined uncertainty 25 ppb):}}$$

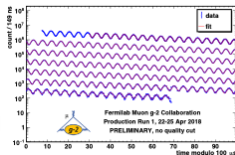
ratio of frequencies (R_μ)
measured by us

fundamental factors
(combined uncertainty 25 ppb):

ω_a : muon anomalous precession frequency

Extract from decay positron time spectra

$$N(t) = N_0 e^{-t/\tau_\mu} [1 + A \cos(\omega_a t + \phi)]$$



$\tilde{\omega}'_p(\mathbf{T}_r)$: magnetic field B in terms of (shielded) proton precession frequency (proton NMR $\hbar\omega_p = 2\mu_p B$) and weighted by the muon distribution

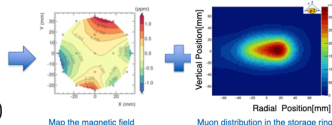
(shielded = measured in spherical water sample at $T_r = 34.7^\circ\text{C}$)

$\mu'_p(T_r)/\mu_e(H)$ from [Metrologia **13**, 179 (1977)]

$\mu_e(H)/\mu_e$ from [Rev. Mod. Phys. **88** 035009 (2016)]

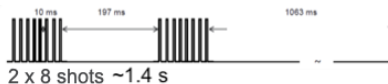
m_μ/m_e from [Phys. Rev. Lett. **82**, 711 (1999)]

$g_e/2$ from [Phys. Rev. A **83** 052122 (2011)]



Production of the muon beam

- **Recycler Ring:** 8 GeV protons from Booster are divided in 4 bunches
- **Target Station:** p -bunches are collided with target and π^+ with $3.1 \text{ GeV}/c$ ($\pm 10\%$) are collected
- **Beam Transport and Delivery Ring:** magnetic lenses select μ^+ from $\pi^+ \rightarrow \mu^+ \nu_\mu$ then μ^+ are separated from p and π^+ in circular ring
- **Muon Campus:** polarized μ^+ are ready to be injected into the storage ring

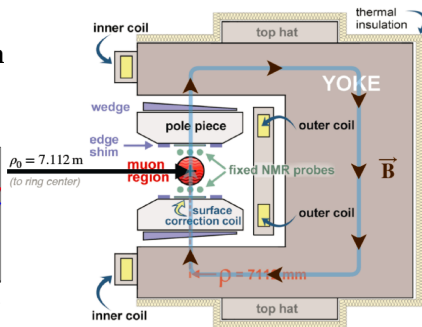
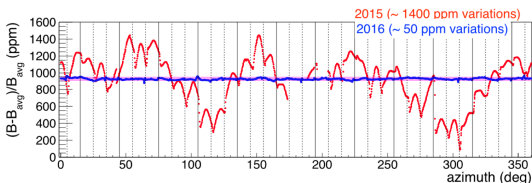
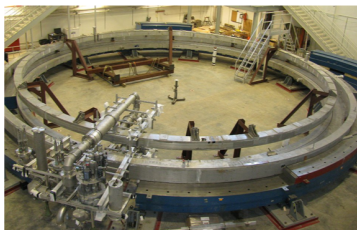


The storage ring journey: from BNL to FNAL in Summer 2013



Storage ring magnet

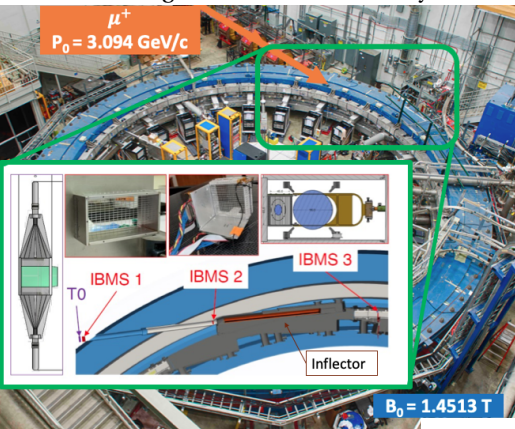
- Three superconducting coils provide 1.45 T vertical magnetic field
- Vacuum chambers surrounded by a cryosystem and C-shaped **yokes** to allow the decay positrons to reach the detectors.
- Achieved 50 ppm on field uniformity thanks to low-carbon steel **poles, edge shims, steel wedges, surface correction coil**



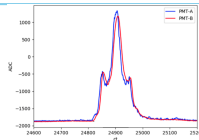
final field ~ 3 times more uniform than at BNL

Injection of the muons into the ring

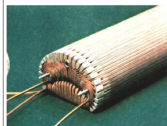
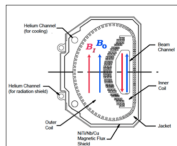
- Beam enters the ring through a 2.2 m-long 10 cm hole in the iron yoke



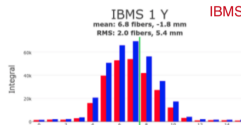
- **T0 Counter** (thin scintillator read out by PMTs) to measure **beam time profile**



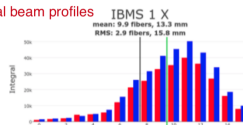
- **Inflector magnet** provides nearly field free region for muons to enter the storage region



- **Inflector Beam Monitoring System** (scintillator fiber grids) to measure **beam spatial profile**

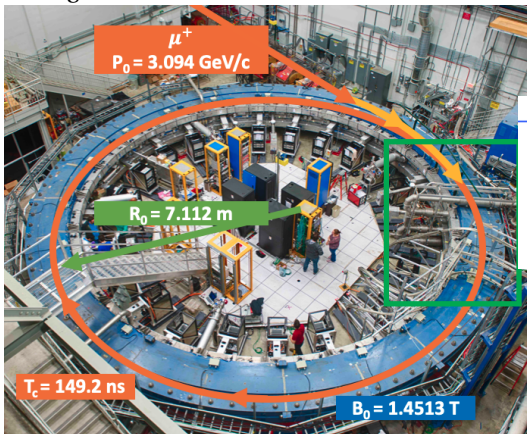


IBMS spatial beam profiles



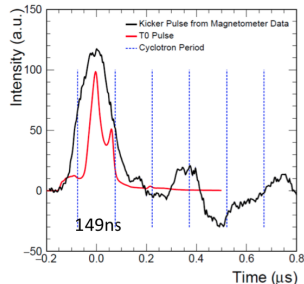
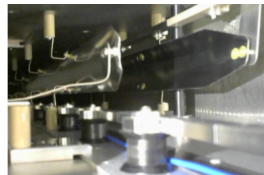
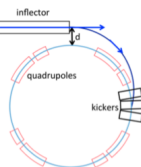
Muon storage

- Injected beam is 77 mm off from storage region center

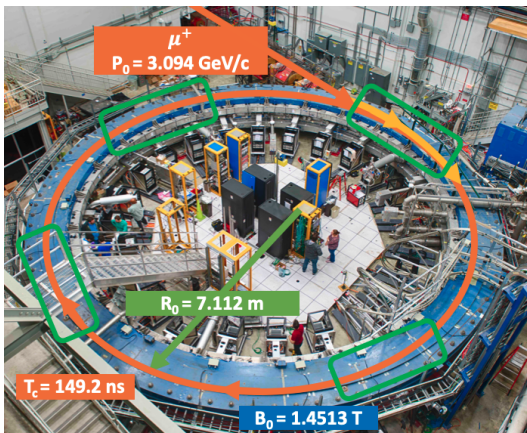


Kicker Magnets

- 3 pulsed magnets deflect beam $\sim 10 \text{ mrad}$ onto the closed storage orbit in less than 150 ns

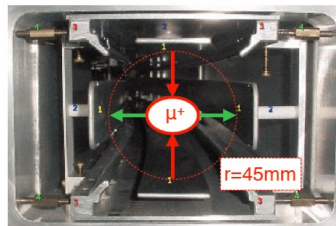


Vertical focusing



Electrostatic Quadrupoles

- 4 sets of quads provide vertical beam focusing

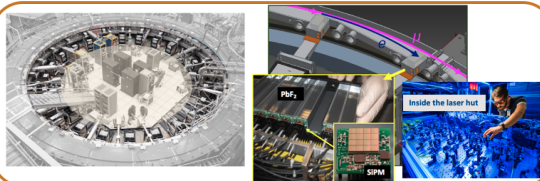


- E -field component cancels out (at first order) when muons at *magic momentum*:

$$\vec{\omega}_a \cong -\frac{e}{m} \left[a_\mu \vec{B} - \left(a_\mu - \underbrace{\frac{1}{\gamma^2 - 1}} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right]$$

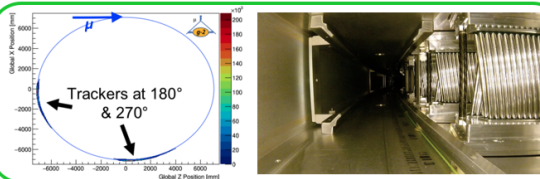
~ 0 if $\gamma = 29.3$ i.e., $p_\mu = 3.094 \text{ GeV}/c$

Detectors and field probes



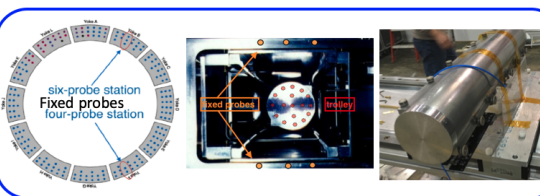
24 Calos around the ring

- Each made of 6×9 PbF_2 crystals read out by large-area SiPMs
- 1296 channels individually calibrated by 405nm-laser system



2 in-vacuum straw trackers

- Each with 8 modules consisting of 128 gas filled straws



2 types of field probes

- 378 fixed NMR probes above and below storage region
 - measure B-field 24/7
- Trolley with 17-probe NMR
 - 2D profile of B over the entire azimuth when beam is OFF

First production run

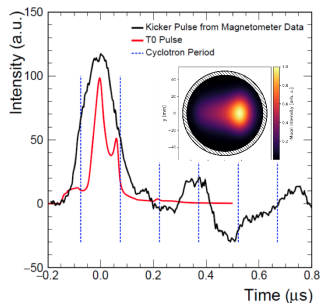
Statistics:

- March 26 – July 7 2018 : **Run1**
- $1.2 \times$ BNL after data quality selection

Main challenges:

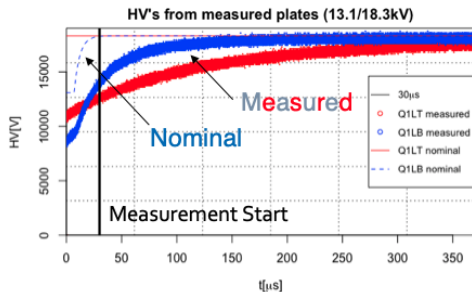
- Non-ideal kick

- low amplitude and ringing
- beam not centered in storage region



- 2 of 32 HV Quad resistors were damaged

- slow recovery time



- Temperature variations larger than 1°C

Master formula for analysis of Run 1

$$R_{\mu} = \left(\frac{\overbrace{f_{clock} \cdot \omega_a^{meas}}^{\omega_a} \cdot \overbrace{(1 + C_e + C_p + C_{ml} + C_{pa})}^{\text{beam dynamics corrections}}}{\underbrace{f_{calib} \cdot \omega'_p(x, y, \phi)}_{\tilde{\omega}'_p(T_r)} \otimes \underbrace{M(x, y, \phi) \cdot (1 + B_k + B_q)}_{\text{field corrections}}} \right)$$

f_{clock} : blinded clock
 ω_a^{meas} : measured precession frequency

f_{calib} : absolute magnetic field calibration
 $\omega'_p(x, y, \phi)$: field maps
 $M(x, y, \phi)$: muon beam distribution

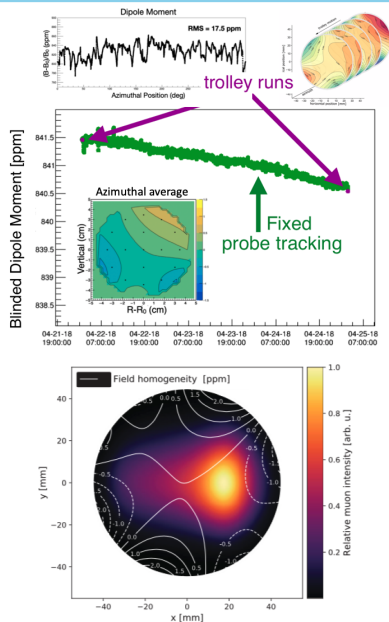
C_e : electric field correction
 C_p : pitch correction
 C_{ml} : muon loss correction
 C_{pa} : phase-acceptance correction

B_k : transient field from eddy current in kicker
 B_q : transient field from quad vibration

Measuring the magnetic field seen by the muons

$$R_\mu = \left(\frac{f_{\text{clock}} \cdot \omega_a^{\text{meas}} \cdot (1 + C_e + C_p + C_{ml} + C_{pa})}{f_{\text{calib}} \cdot \omega'_p(x, y, \phi) \otimes M(x, y, \phi) \cdot (1 + B_k + B_q)} \right)$$

- ω'_p is proportional to the magnetic field and it is mapped every 3 days using 17 NMR probes on a trolley
- During data taking fixed NMR probes located above and below the storage region monitor the field
- Fixed probes to interpolate the field between trolley runs
- Field maps are weighted by beam distribution (extrapolated from the decay e^+ trajectory measured by the trackers and simulations)



Magnetic field corrections

Kicker transient field

- due to eddy currents produced by kicker pulses
- measured using Faraday magnetometers

$$B_k \sim 30 \text{ ppb} \quad \delta_{B_k} \sim 40 \text{ ppb}$$

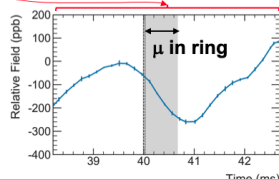
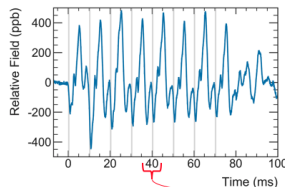
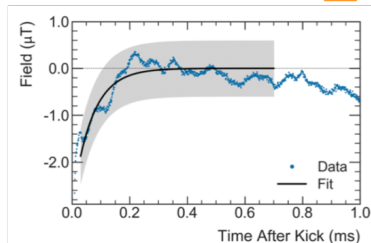
Quads transient field

- due to mechanical vibrations from pulsing the quads
- mapped using special NMR probes

$$B_q \sim 17 \text{ ppb} \quad \delta_{B_q} \sim 92 \text{ ppb}$$

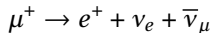
- δ_{B_q} dominated by incomplete map
- expected to be reduced by factor 2 for Run 2 and after

$$R_\mu = \left(\frac{f_{\text{clock}} \cdot \omega_a^{\text{meas}} \cdot (1 + C_e + C_p + C_{ml} + C_{pa})}{f_{\text{calib}} \cdot \omega_p'(x, y, \phi) \otimes M(x, y, \phi) \cdot (1 + B_k + B_q)} \right)$$



Measuring ω_a

- Polarized muon decay:



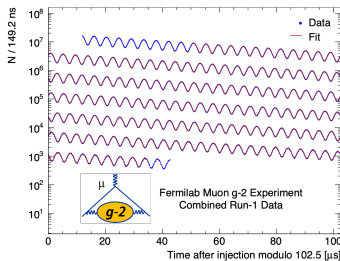
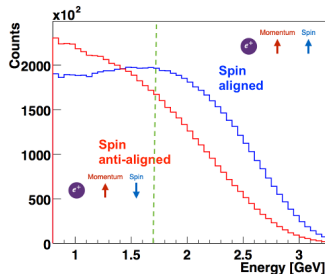
- High energy e^+ are preferentially emitted in direction of μ^+ spin (parity violation of the weak decay)
- Energy spectrum modulates at the ω_a frequency
- Counting the number of e^+ with $E_{e^+} > E_{\text{threshold}}$ as a function of time (wobble plot) leads to ω_a :

$$N(t) = \underbrace{N_0}_{\text{normalization}} e^{-t/\tau} \left[1 + \underbrace{A}_{\text{g-2 asymmetry}} \cos(\underbrace{\omega_a t + \varphi}_{\text{g-2 phase}}) \right]$$

muon lab-frame lifetime
g-2 phase

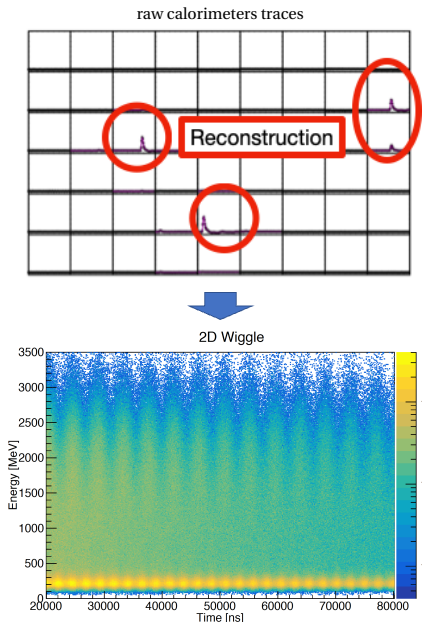
E_{e^+} and t are measured by the calorimeters with a blinding factor applied to the digitization rate

$$R_\mu = \left(\frac{f_{\text{clock}} \cdot \omega_a^{\text{meas}} \cdot (1 + C_e + C_p + C_{ml} + C_{pa})}{f_{\text{calib}} \cdot \omega_p'(x, y, \phi) \otimes M(x, y, \phi) \cdot (1 + B_k + B_q)} \right)$$



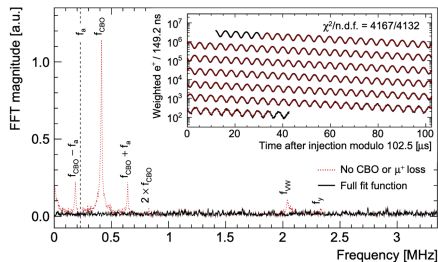
Wiggle plot

- Calorimeters data is reconstructed into energies and times
 - Two independent reconstruction routines
- Different analysis techniques used to reduce systematic errors :
 - **Threshold (T) Method**
 - only energy threshold applied to select positrons
 - **Asymmetry-Weighted (A) Method:**
 - positrons divided into energy bins and weighted by $g-2$ asymmetry
 - **Ratio (R) Method**
 - exponential decay due to muon lifetime is removed before fitting
 - **Integrated Charge (Q) Method:**
 - sum of raw calorimeter traces (unique method independent of reconstruction)
- 11 independent analysis performed



Fitting procedure

- Fit \rightarrow Residuals \rightarrow Fast Fourier Transform (FFT)
- Analyses of FFT fit residuals shows that simple 5-parameter model is inadequate
- Flat FFT of residuals using a 22-parameter fit function that includes beam dynamics effects



$$N_0 e^{-\frac{t}{\tau}} (1 + A \cdot A_{BO}(t) \cos(\omega_a t + \phi \cdot \phi_{BO}(t))) \cdot N_{CBO}(t) \cdot N_{VW}(t) \cdot N_y(t) \cdot N_{2CBO}(t) \cdot J(t)$$

$$A_{BO}(t) = 1 + A_A \cos(\omega_{CBO}(t) + \phi_A) e^{-\frac{t}{\tau_{CBO}}}$$

$$\phi_{BO}(t) = 1 + A_\phi \cos(\omega_{CBO}(t) + \phi_\phi) e^{-\frac{t}{\tau_{CBO}}} \quad \omega_{CBO}, \omega_{2CBO} \text{ radial oscillations}$$

$$N_{CBO}(t) = 1 + A_{CBO} \cos(\omega_{CBO}(t) + \phi_{CBO}) e^{-\frac{t}{\tau_{CBO}}}$$

$$N_{2CBO}(t) = 1 + A_{2CBO} \cos(2\omega_{CBO}(t) + \phi_{2CBO}) e^{-\frac{t}{2\tau_{CBO}}}$$

$$N_{VW}(t) = 1 + A_{VW} \cos(\omega_{VW}(t) + \phi_{VW}) e^{-\frac{t}{\tau_{VW}}} \quad \omega_y, \omega_{VW} \text{ vertical oscillations}$$

$$N_y(t) = 1 + A_y \cos(\omega_y(t) + \phi_y) e^{-\frac{t}{\tau_y}}$$

Red = free parameters

Blue = fixed parameters

$$J(t) = 1 - k_{LM} \int_{t_0}^t \Lambda(t) dt \quad \text{Lost muons}$$

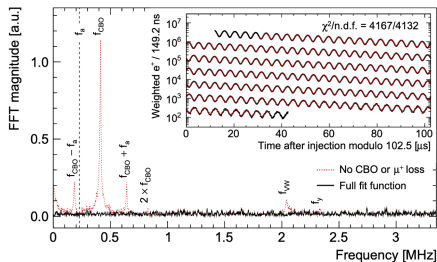
$$\omega_{CBO}(t) = \omega_0 t + A e^{-\frac{t}{\tau_A}} + B e^{-\frac{t}{\tau_B}}$$

$$\omega_y(t) = F \omega_{CBO}(t) \sqrt{2\omega_c / F \omega_{CBO}(t) - 1}$$

$$\omega_{VW}(t) = \omega_c - 2\omega_y(t)$$

Fitting procedure

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- Flat FFT of residuals using a 22-parameter fit function that includes beam dynamics effects



$$N_0 e^{-\frac{t}{\tau}} (1 + A \cdot A_{BO}(t) \cos(\omega_0 t + \phi \cdot \phi_{BO}(t))) \cdot N_{CBO}(t) \cdot N_{VW}(t) \cdot N_y(t) \cdot N_{2CBO}(t) \cdot J(t)$$

$$A_{BO}(t) = 1 + A_A \cos(\omega_{CBO}(t) + \phi_A) e^{-\frac{t}{\tau_{CBO}}}$$

$$\phi_{BO}(t) = 1 + A_\phi \cos(\omega_{CBO}(t) + \phi_\phi) e^{-\frac{t}{\tau_{CBO}}}$$

$\omega_{CBO}, \omega_{2CBO}$ radial oscillations

$$N_{CBO}(t) = 1 + A_{CBO} \cos(\omega_{CBO}(t) + \phi_{CBO}) e^{-\frac{t}{\tau_{CBO}}}$$

$$N_{2CBO}(t) = 1 + A_{2CBO} \cos(2\omega_{CBO}(t) + \phi_{2CBO}) e^{-\frac{t}{\tau_{2CBO}}}$$

$$N_{VW}(t) = 1 + A_{VW} \cos(\omega_{VW}(t) + \phi_{VW}) e^{-\frac{t}{\tau_{VW}}}$$

$$N_y(t) = 1 + A_y \cos(\omega_y(t) + \phi_y) e^{-\frac{t}{\tau_y}}$$

ω_y, ω_{VW} vertical oscillations

Red = free parameters
Blue = fixed parameters

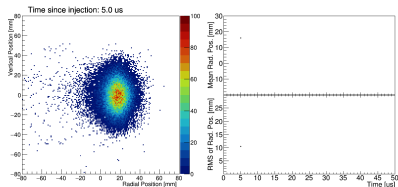
$$J(t) = 1 - k_{LM} \int_{t_0}^t \Lambda(t) dt \quad \text{Lost muons}$$

$$\omega_{CBO}(t) = \omega_0 t + A e^{-\frac{t}{\tau_A}} + B e^{-\frac{t}{\tau_B}}$$

$$\omega_y(t) = F \omega_{CBO}(t) \sqrt{2\omega_c / F \omega_{CBO}(t) - 1}$$

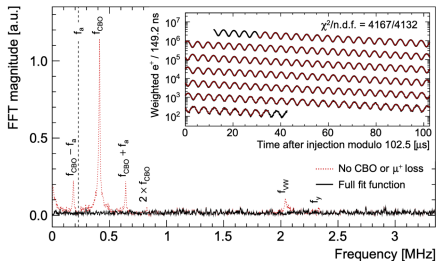
$$\omega_{VW}(t) = \omega_c - 2\omega_y(t)$$

The muon beam oscillates and breathes:



Fitting procedure

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- Analyses of FFT fit residuals shows that simple 5-parameter model is inadequate
- Flat FFT of residuals using a 22-parameter fit function that includes beam dynamics effects



$$N_0 e^{-\frac{t}{\tau}} (1 + A \cdot A_{BO}(t) \cos(\omega_0 t + \phi + \phi_{BO}(t))) \cdot N_{CBO}(t) \cdot N_{VW}(t) \cdot N_y(t) \cdot N_{2CBO}(t) \cdot J(t)$$

$$A_{BO}(t) = 1 + A_A \cos(\omega_{CBO}(t) + \phi_A) e^{-\frac{t}{\tau_{CBO}}}$$

$$\phi_{BO}(t) = 1 + A_\phi \cos(\omega_{CBO}(t) + \phi_\phi) e^{-\frac{t}{\tau_{CBO}}}$$

$\omega_{CBO}, \omega_{2CBO}$ radial oscillations

$$N_{CBO}(t) = 1 + A_{CBO} \cos(\omega_{CBO}(t) + \phi_{CBO}) e^{-\frac{t}{\tau_{CBO}}}$$

$$N_{2CBO}(t) = 1 + A_{2CBO} \cos(2\omega_{CBO}(t) + \phi_{2CBO}) e^{-\frac{t}{\tau_{2CBO}}}$$

$$N_{VW}(t) = 1 + A_{VW} \cos(\omega_{VW}(t) + \phi_{VW}) e^{-\frac{t}{\tau_{VW}}}$$

ω_y, ω_{VW} vertical oscillations

$$N_y(t) = 1 + A_y \cos(\omega_y t + \phi_y) e^{-\frac{t}{\tau_y}}$$

Red = free parameters

Blue = fixed parameters

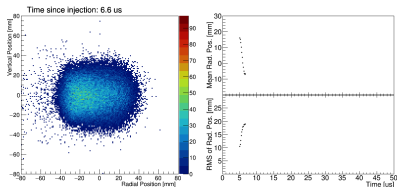
$$J(t) = 1 - k_{LM} \int_{t_0}^t \Lambda(t) dt \quad \text{Lost muons}$$

$$\omega_{CBO}(t) = \omega_0 t + A e^{-\frac{t}{\tau_A}} + B e^{-\frac{t}{\tau_B}}$$

$$\omega_y(t) = F \omega_{CBO}(t) \sqrt{2\omega_c / F \omega_{CBO}(t)} - 1$$

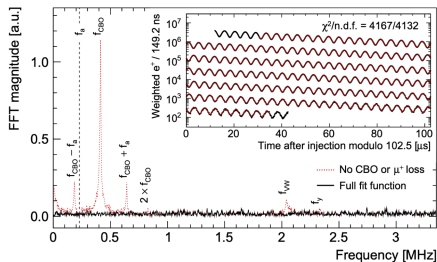
$$\omega_{VW}(t) = \omega_c - 2\omega_y(t)$$

The muon beam oscillates and breathes:



Fitting procedure

- Fit → Residuals → Fast Fourier Transform (FFT)
- Analyses of FFT fit residuals shows that simple 5-parameter model is inadequate
- Flat FFT of residuals using a 22-parameter fit function that includes beam dynamics effects



$$N_{\beta} e^{-\frac{t}{\tau}} (1 + A \cdot A_{BO}(t) \cos(\omega_{\beta} t + \phi_{\beta} \cdot \phi_{BO}(t))) \cdot N_{CBO}(t) \cdot N_{VW}(t) \cdot N_{\beta}(t) \cdot N_{2CBO}(t) \cdot J(t)$$

$$A_{BO}(t) = 1 + A_A \cos(\omega_{CBO}(t) + \phi_A) e^{-\frac{t}{\tau_{CBO}}}$$

$$\phi_{BO}(t) = 1 + A_{\phi} \cos(\omega_{CBO}(t) + \phi_{\phi}) e^{-\frac{t}{\tau_{CBO}}}$$

$\omega_{CBO}, \omega_{2CBO}$ radial oscillations

$$N_{CBO}(t) = 1 + A_{CBO} \cos(\omega_{CBO}(t) + \phi_{CBO}) e^{-\frac{t}{\tau_{CBO}}}$$

$$N_{2CBO}(t) = 1 + A_{2CBO} \cos(2\omega_{CBO}(t) + \phi_{2CBO}) e^{-\frac{t}{\tau_{2CBO}}}$$

$$N_{VW}(t) = 1 + A_{VW} \cos(\omega_{VW}(t) + \phi_{VW}) e^{-\frac{t}{\tau_{VW}}}$$

ω_y, ω_{VW} vertical oscillations

$$N_{\beta}(t) = 1 + A_{\beta} \cos(\omega_{\beta}(t) + \phi_{\beta}) e^{-\frac{t}{\tau_{\beta}}}$$

Red = free parameters

Blue = fixed parameters

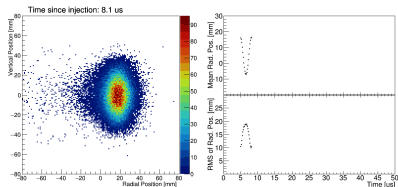
$$J(t) = 1 - k_{LM} \int_{t_0}^t \Lambda(t) dt \quad \text{Lost muons}$$

$$\omega_{CBO}(t) = \omega_0 t + A e^{-\frac{t}{\tau_A}} + B e^{-\frac{t}{\tau_B}}$$

$$\omega_y(t) = F \omega_{CBO}(t) \sqrt{2\omega_c / F \omega_{CBO}(t)} - 1$$

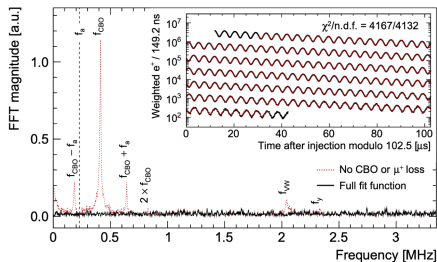
$$\omega_{VW}(t) = \omega_c - 2\omega_y(t)$$

The muon beam oscillates and breathes:



Fitting procedure

- Fit → Residuals → Fast Fourier Transform (FFT)
- Analyses of FFT fit residuals shows that simple 5-parameter model is inadequate
- Flat FFT of residuals using a 22-parameter fit function that includes beam dynamics effects



$$N_B e^{-\frac{t}{\tau}} (1 + A \cdot A_{BO}(t) \cos(\omega_B t + \phi + \phi_{BO}(t))) \cdot N_{CBO}(t) \cdot N_{VW}(t) \cdot N_Y(t) \cdot N_{2CBO}(t) \cdot J(t)$$

$$A_{BO}(t) = 1 + A_A \cos(\omega_{CBO}(t) + \phi_A) e^{-\frac{t}{\tau_{CBO}}}$$

$$\phi_{BO}(t) = 1 + A_\phi \cos(\omega_{CBO}(t) + \phi_\phi) e^{-\frac{t}{\tau_{CBO}}}$$

$\omega_{CBO}, \omega_{2CBO}$ radial oscillations

$$N_{CBO}(t) = 1 + A_{CBO} \cos(\omega_{CBO}(t) + \phi_{CBO}) e^{-\frac{t}{\tau_{CBO}}}$$

$$N_{2CBO}(t) = 1 + A_{2CBO} \cos(2\omega_{CBO}(t) + \phi_{2CBO}) e^{-\frac{t}{\tau_{CBO}}}$$

$$N_{VW}(t) = 1 + A_{VW} \cos(\omega_{VW}(t) + \phi_{VW}) e^{-\frac{t}{\tau_{VW}}}$$

$$N_Y(t) = 1 + A_Y \cos(\omega_Y(t) + \phi_Y) e^{-\frac{t}{\tau_Y}}$$

ω_Y, ω_{VW} vertical oscillations

Red = free parameters

Blue = fixed parameters

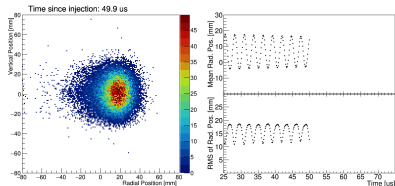
$$J(t) = 1 - k_{LM} \int_{t_0}^t \Lambda(t) dt \quad \text{Lost muons}$$

$$\omega_{CBO}(t) = \omega_0 t + A e^{-\frac{t}{\tau_A}} + B e^{-\frac{t}{\tau_B}}$$

$$\omega_Y(t) = F \omega_{CBO}(t) \sqrt{2\omega_c / F \omega_{CBO}(t) - 1}$$

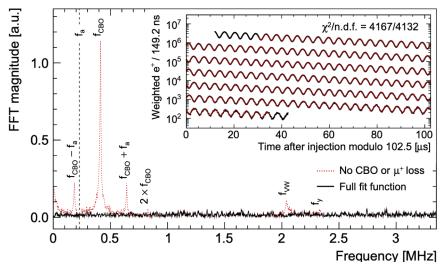
$$\omega_{VW}(t) = \omega_c - 2\omega_Y(t)$$

The muon beam oscillates and breathes:



Fitting procedure

- Fit → Residuals → Fast Fourier Transform (FFT)
- Analyses of FFT fit residuals shows that simple 5-parameter model is inadequate
- Flat FFT of residuals using a 22-parameter fit function that includes beam dynamics effects



Additional term to account for muons that hit the collimators and are lost:

$$N_0 e^{-\frac{t}{\tau}} (1 + A \cdot A_{BO}(t) \cos(\omega_B t + \phi) \cdot \phi_{BO}(t)) \cdot N_{CBO}(t) \cdot N_{VW}(t) \cdot N_y(t) \cdot N_{2CBO}(t) \cdot J(t)$$

$$A_{BO}(t) = 1 + A_A \cos(\omega_{CBO}(t) + \phi_A) e^{-\frac{t}{\tau_{CBO}}}$$

$$\phi_{BO}(t) = 1 + A_\phi \cos(\omega_{CBO}(t) + \phi_\phi) e^{-\frac{t}{\tau_{CBO}}} \quad \omega_{CBO}, \omega_{2CBO} \text{ radial oscillations}$$

$$N_{CBO}(t) = 1 + A_{CBO} \cos(\omega_{CBO}(t) + \phi_{CBO}) e^{-\frac{t}{\tau_{CBO}}}$$

$$N_{2CBO}(t) = 1 + A_{2CBO} \cos(2\omega_{CBO}(t) + \phi_{2CBO}) e^{-\frac{t}{\tau_{CBO}}}$$

$$N_{VW}(t) = 1 + A_{VW} \cos(\omega_{VW}(t) + \phi_{VW}) e^{-\frac{t}{\tau_{VW}}} \quad \omega_y, \omega_{VW} \text{ vertical oscillations}$$

$$N_y(t) = 1 + A_y \cos(\omega_y(t) + \phi_y) e^{-\frac{t}{\tau_y}}$$

Red = free parameters

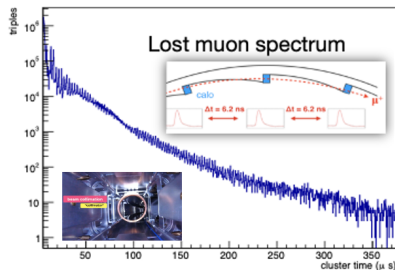
Blue = fixed parameters

$$J(t) = 1 - k_{LM} \int_{t_0}^t \Lambda(t) dt \quad \text{Lost muons}$$

$$\omega_{CBO}(t) = \omega_0 t + A e^{-\frac{t}{\tau_A}} + B e^{-\frac{t}{\tau_B}}$$

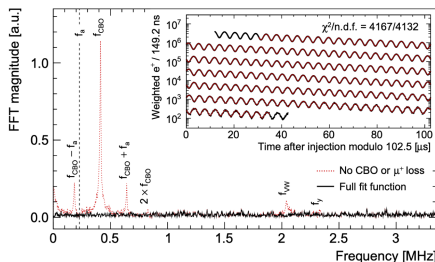
$$\omega_y(t) = F \omega_{CBO}(t) \sqrt{2\omega_c / F \omega_{CBO}(t) - 1}$$

$$\omega_{VW}(t) = \omega_c - 2\omega_y(t)$$



Fitting procedure

- Fit → Residuals → Fast Fourier Transform (FFT)
- Analyses of FFT fit residuals shows that simple 5-parameter model is inadequate
- Flat FFT of residuals using a 22-parameter fit function that includes beam dynamics effects



$$N_0 e^{-\frac{t}{\tau}} (1 + A \cdot A_{BO}(t) \cos(\omega_a t + \phi + \phi_{BO}(t))) \cdot N_{CBO}(t) \cdot N_{VW}(t) \cdot N_y(t) \cdot N_{2CBO}(t) \cdot J(t)$$

$$A_{BO}(t) = 1 + A_A \cos(\omega_{CBO}(t) + \phi_A) e^{-\frac{t}{\tau_{CBO}}}$$

$$\phi_{BO}(t) = 1 + A_\phi \cos(\omega_{CBO}(t) + \phi_\phi) e^{-\frac{t}{\tau_{CBO}}} \quad \omega_{CBO}, \omega_{2CBO} \text{ radial oscillations}$$

$$N_{CBO}(t) = 1 + A_{CBO} \cos(\omega_{CBO}(t) + \phi_{CBO}) e^{-\frac{t}{\tau_{CBO}}}$$

$$N_{2CBO}(t) = 1 + A_{2CBO} \cos(2\omega_{CBO}(t) + \phi_{2CBO}) e^{-\frac{t}{\tau_{2CBO}}}$$

$$N_{VW}(t) = 1 + A_{VW} \cos(\omega_{VW}(t) + \phi_{VW}) e^{-\frac{t}{\tau_{VW}}} \quad \omega_y, \omega_{VW} \text{ vertical oscillation}$$

$$N_y(t) = 1 + A_y \cos(\omega_y(t) + \phi_y) e^{-\frac{t}{\tau_y}}$$

$$J(t) = 1 - k_{LM} \int_{t_0}^t \Lambda(t) dt \quad \text{Lost muons}$$

$$\omega_{CBO}(t) = \omega_0 t + A e^{-\frac{t}{\tau_A}} + B e^{-\frac{t}{\tau_B}}$$

$$\omega_y(t) = F \omega_{CBO}(t) \sqrt{2\omega_c / F \omega_{CBO}(t) - 1}$$

$$\omega_{VW}(t) = \omega_c - 2\omega_y(t)$$

Red = free parameters
Blue = fixed parameters

+ beam dynamics corrections:

$$\omega_a = \omega_a^{meas} \cdot (1 + C_e + C_p + C_{ml} + C_{pa})$$

Electric Field Pitch Muon Loss Phase Acceptance

Electric field and pitch corrections

Electric Field

- due to momentum spread around p_{magic}

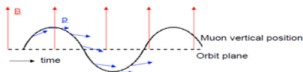
$$\vec{\omega}_a \cong -\frac{e}{m} \left[a_\mu \vec{B} - \left(a_\mu - \frac{1}{\gamma^2 - 1} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right]$$

- measured using momentum distribution provided by the calorimeters in terms of equilibrium radius

$$C_e \sim 450 \text{ ppb} \quad \delta_{C_e} \sim 50 \text{ ppb}$$

Pitch

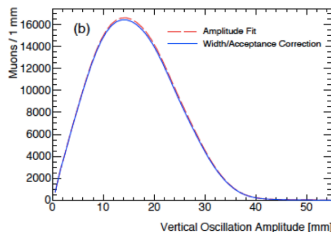
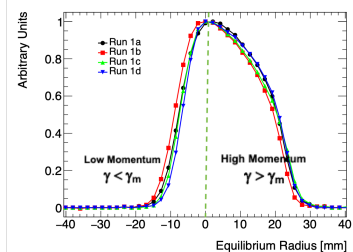
- due to vertical beam oscillation



- measured using the beam vertical amplitude from the trackers, calorimeter data, and simulations

$$C_p \sim 200 \text{ ppb} \quad \delta_{C_p} \sim 20 \text{ ppb}$$

$$R_\mu = \left(\frac{f_{clock} \cdot \omega_a^{meas} \cdot (1 + C_e + C_p + C_{ml} + C_{pa})}{f_{calib} \cdot \omega'_p(x, y, \phi) \otimes M(x, y, \phi) \cdot (1 + B_k + B_q)} \right)$$



Muon loss and phase acceptance corrections

$$R_\mu = \left(\frac{f_{\text{clock}} \cdot \omega_a^{\text{meas}} \cdot (1 + C_e + C_p + C_{ml} + C_{pa})}{f_{\text{calib}} \cdot \omega'_p(x, y, \phi) \otimes M(x, y, \phi) \cdot (1 + B_k + B_q)} \right)$$

Muon losses cause a phase shift

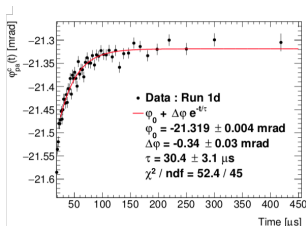
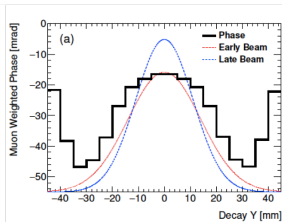
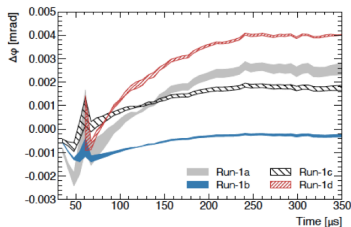
- because muon-phase and muon loss rate are momentum-dependent
- measured using data-driven technique

$$C_{ml} < 20 \text{ ppb} \quad \delta_{C_{ml}} \sim 5 \text{ ppb}$$

Phase acceptance

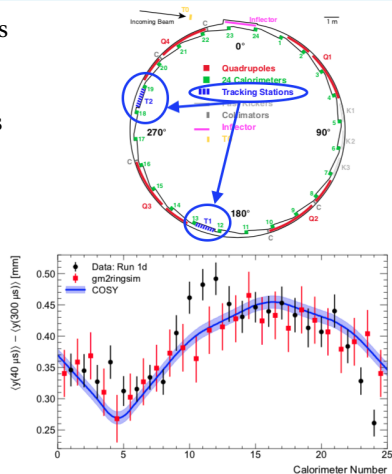
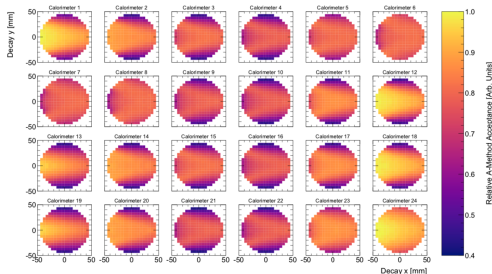
- phase changes due to early to late variations of the beam
- worsened by damaged quads resistors
- measured using tracker data and simulations

$$C_{pa} \sim 200 \text{ ppb} \quad \delta_{C_{pa}} \sim 80 \text{ ppb}$$



Simulations for phase-acceptance

- Time-dependence of beam spatial distributions are measured by trackers in two locations
- Two independent **simulations** are used to extrapolate beam profile from tracker locations around the ring
 - based on **COSY-INFINITY** and **GEANT-4**
 - cross-checked against data
- The beam profiles in the ring are then folded with calorimeter acceptance maps produced with the **GEANT-4** based simulation



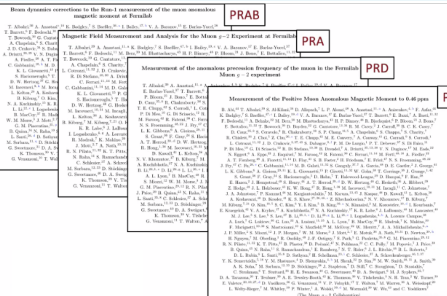
$$R_{\mu} = \left(\frac{f_{clock} \cdot \omega_a^{meas} \cdot (1 + C_e + C_p + C_{ml} + C_{pa})}{f_{calib} \cdot \omega_p'(x, y, \phi) \otimes M(x, y, \phi) \cdot (1 + B_k + B_q)} \right)$$

Clock frequency (f_{clock}):

- frequency that our DAQ clock ticks
- **stable** at ppt level
- hardware-blinded to have $(40 - \epsilon)$ MHz
 - ϵ kept **secret** from all collaborators
- **revealed** only when physics analysis is completed
 - Run-1 result was unblinded on Feb 25, 2021 during a virtual meeting:



Run-1 Result



- First **FNAL** $g-2$ result:

$$a_\mu = 116592040(54) \times 10^{-11} \text{ (462 ppb)}$$

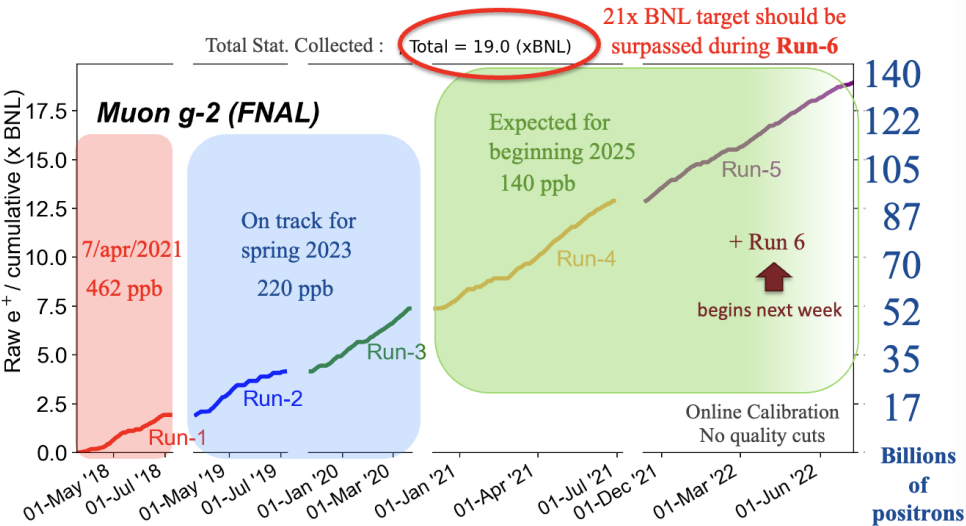
- Good agreement with **BNL** $g-2$

More details in the papers!

- Run-1 result uncertainty is **statistics dominated**
- Major systematic uncertainties: **PA and field transients**
- **Next:** reduce as much as possible the experimental uncertainty on $g-2$!

Quantity	Correction Terms (ppb)	Uncertainty (ppb)
ω_a (statistical)	–	434
ω_a (systematic)	–	56
C_e	489	53
C_p	180	13
C_{ml}	-11	5
C_{pa}	-158	75
$f_{\text{calib}}(\omega'_p(x, y, \phi) \times M(x, y, \phi))$	–	56
B_k	-27	37
B_q	-17	92
$\mu'_p(34.7^\circ)/\mu_e$	–	10
m_μ/m_e	–	22
$g_e/2$	–	0
Total systematic	–	157
Total fundamental factors	–	25
Totals	544	462

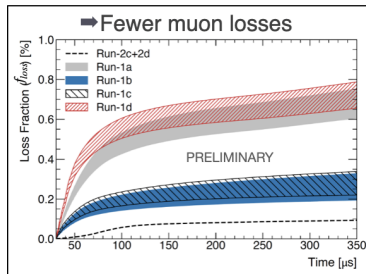
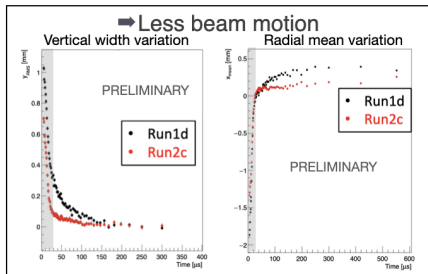
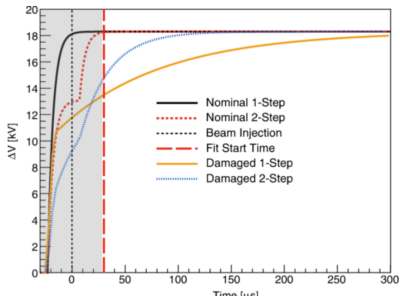
Statistics and Publications Plan



Run-2 and Run-3 Hardware Improvements

● Before Run-2:

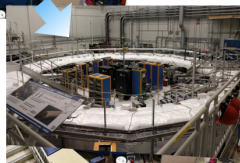
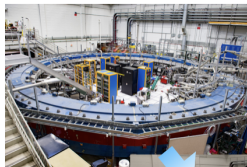
→ Replaced bad quads HV resistors



Run-2 and Run-3 Hardware Improvements

● Before Run-2:

- > Replaced bad quads HV resistors
- > Magnet covered with a thermal blanket



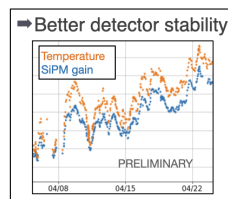
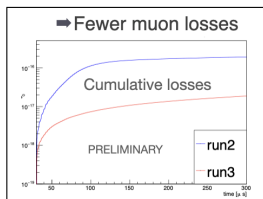
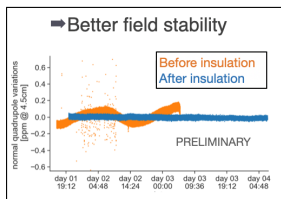
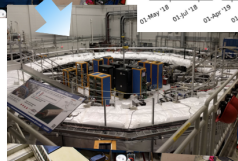
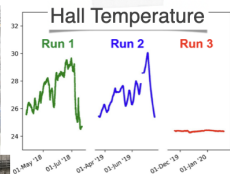
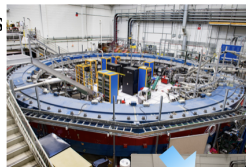
Run-2 and Run-3 Hardware Improvements

● Before Run-2:

- Replaced bad quads HV resistors
- Magnet covered with a thermal blanket

● Before Run-3:

- Hall temperature control improved



Run-2 and Run-3 Hardware Improvements

● Before Run-2:

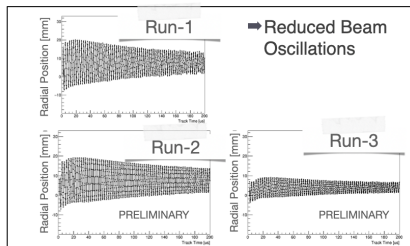
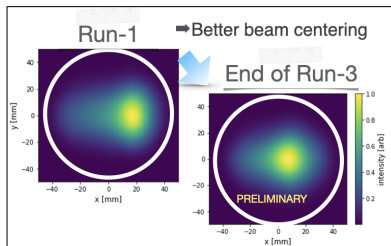
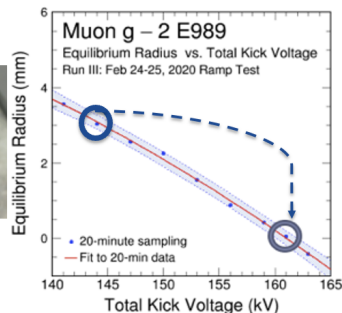
- Replaced bad quads HV resistors
- Magnet covered with a thermal blanket

● Before Run-3:

- Hall temperature control improved

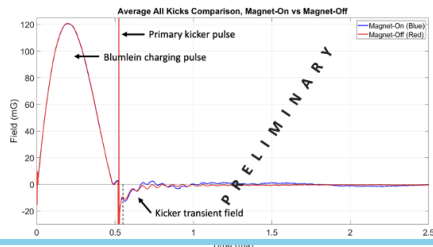
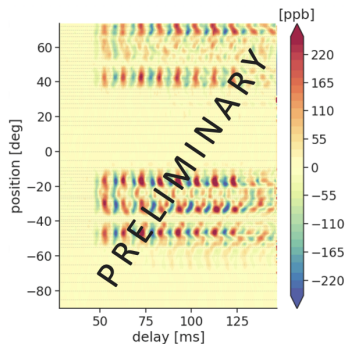
● During Run-2 and Run-3:

- Replaced kicker cables ⇒ kickers at HV design value



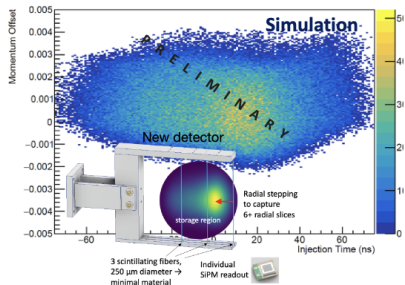
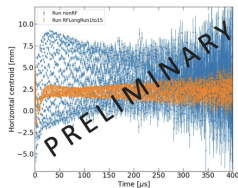
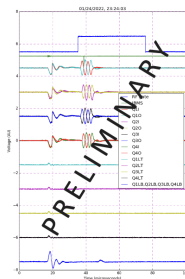
Run-2 and Run-3 Systematics Improvements

- Improved **quadrupole field transient** (B_q) by measuring both time and space
- Improved **kicker field transient** (B_k) by performing new measurement also with a new magnetometer



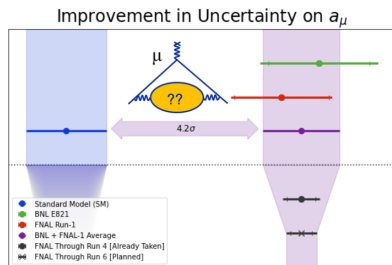
Run-4 and beyond Improvements

- New **Radio Frequency System** mounted on quadrupoles which reduces Beam Betatron oscillations
 - damps beam oscillations in the first 10 μs
 - tested during Run-4 and in use during Run-5 (and Run-6)
- Improved knowledge of the **time-momentum correlation** with simulation and a new detector



Summary and Conclusions

- FNAL $g - 2$ Experiment goal is to measure a_μ with a precision of 140 ppb (4×BNL precision)
- The result from the analysis of the Run-1 data confirmed result from BNL experiment
- Run-2 and Run-3 measurement in progress: we expected to achieve a factor 2 uncertainty reduction!
- With Run-4, Run-5 and Run-6 (on going now) we expect to achieve the uncertainty goal!



Thanks!

