

# Perspectives of the X(3872) line shape measurement at PANDA

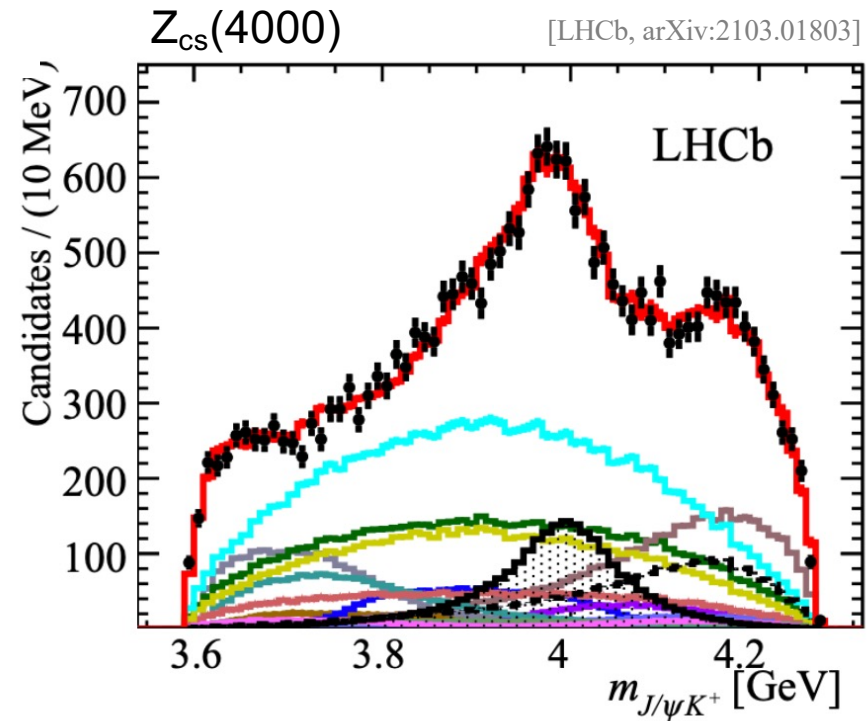
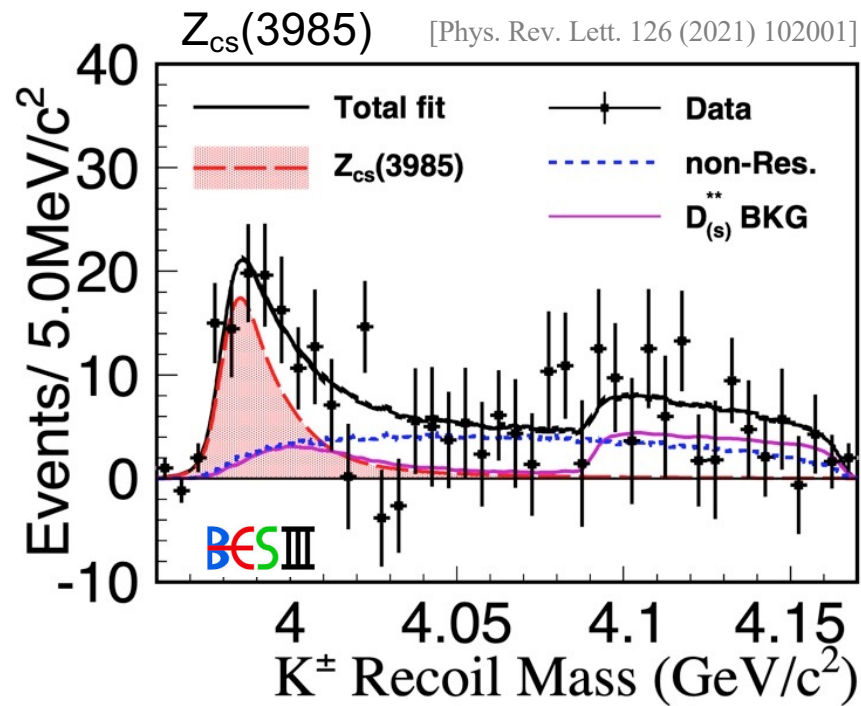
**Frank Nerling**  
HFHF, Campus Frankfurt,  
GSI Darmstadt & GU Frankfurt  
**on behalf of the PANDA collaboration**

**"Hadron Spectroscopy: The Next Big Steps"**  
2022, March 14<sup>th</sup> - 25<sup>th</sup>

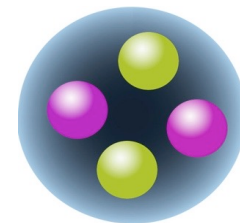
## Outline

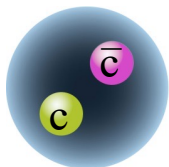
- **Introduction & Motivation**
  - PANDA physics programme
  - Advantage of anti-protons
- **Energy scans of very narrow resonances**
  - The X(3872) experimentally, line shape
  - Comprehensive performance study
- **Summary & outlook**

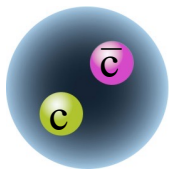
## Hadron Spectroscopy



**Strange partner of the famous,  
unexpected, manifestly exotic  $Z_c(3900)$ ?**

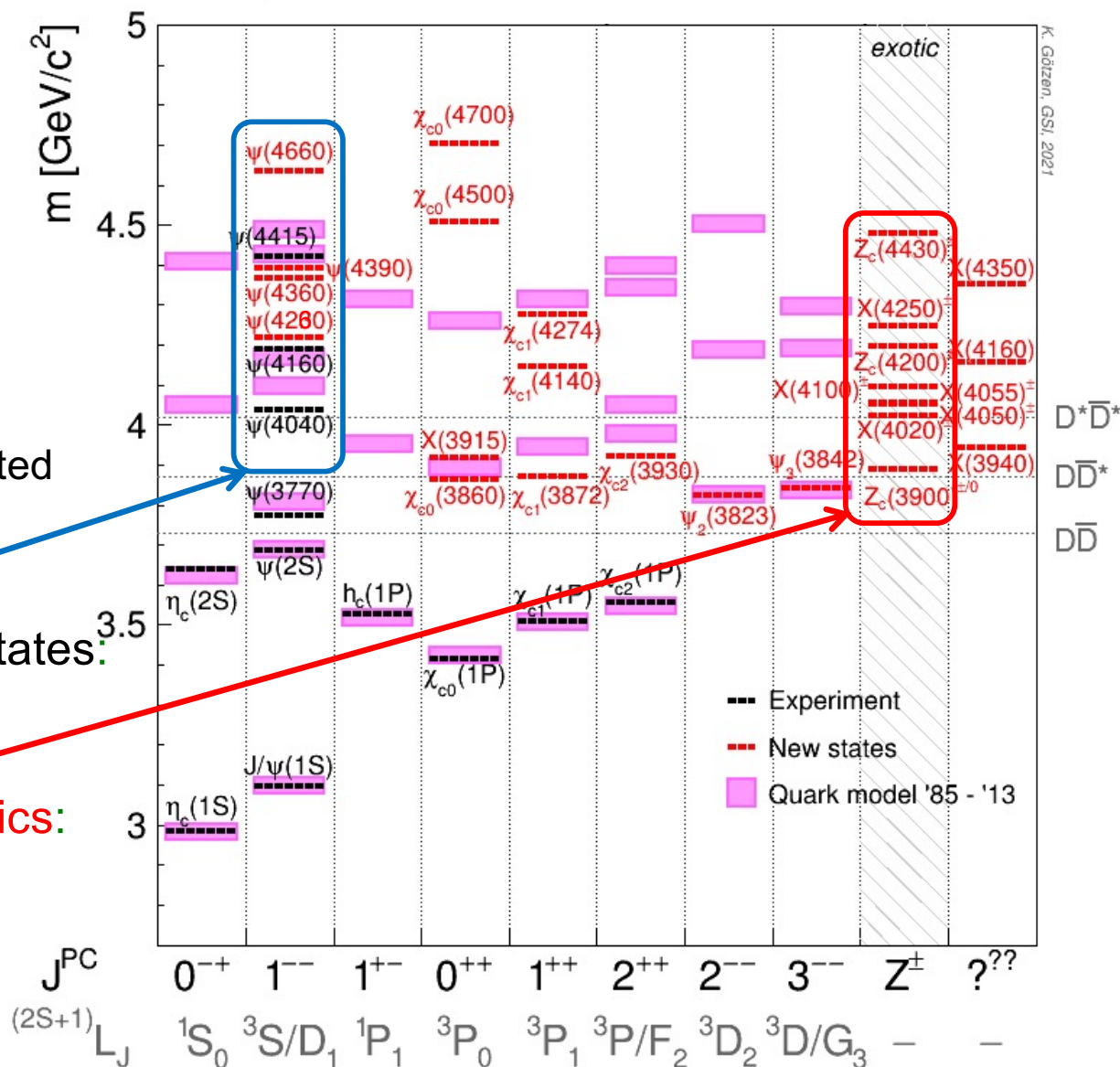




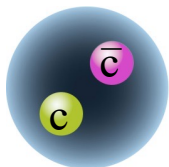


# Charmonium spectrum ( $c\bar{c}$ )

- Before 2003:
  - Good agreement between theory and experiment, particularly beneath open charm thresholds
- After 2003:
  - Severe mismatch between predicted and observed spectrum
- Several supernumerary vector states:  $Y(4260)$ , ...,  $Y(4660)$
- Several charged **manifestly exotics**:  $Z_c(3900)^{+/-}$ , ...,  $Z_c(4430)^{+/-}$

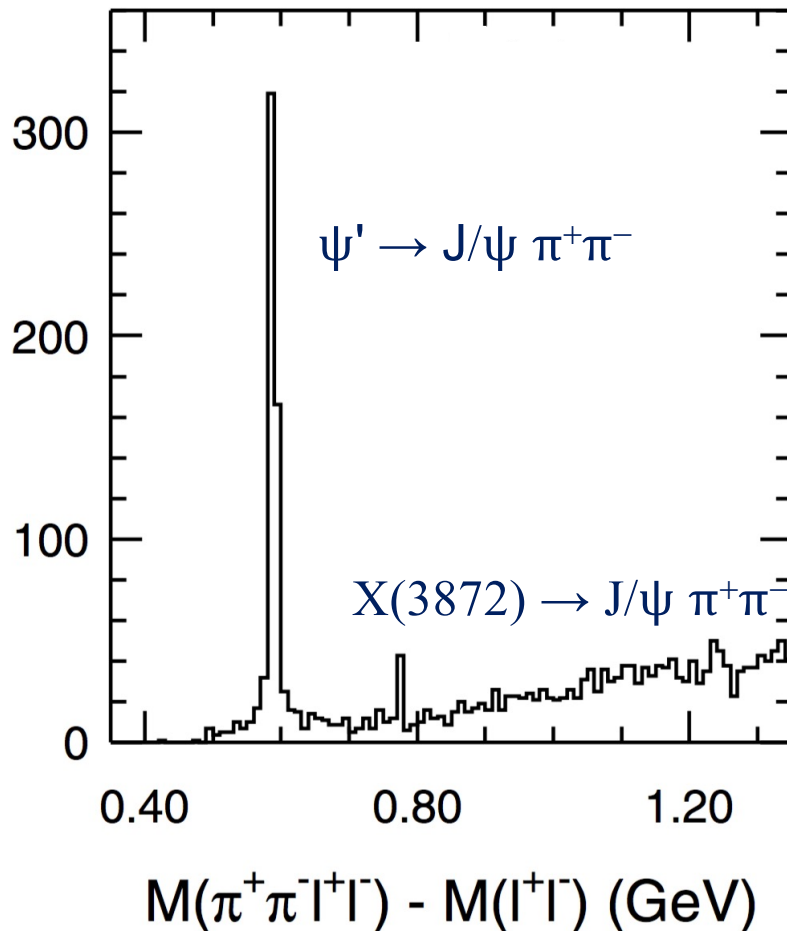






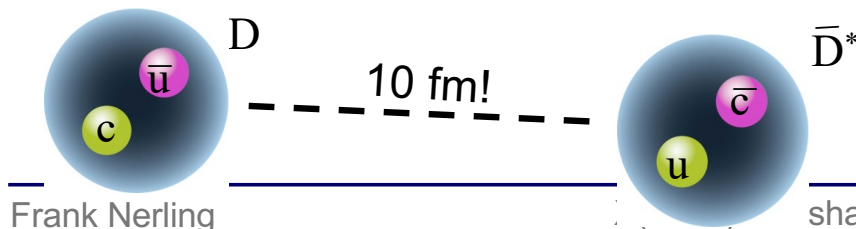
# Experimental review of the X(3872)

[Belle Collab., PRL 91 (2003) 262001]



- First observed by Belle in 2003
  - $X(3872) \rightarrow J/\psi \pi^+ \pi^-$
  - very narrow state with  $J^{PC} = 1^{++}$
- Belle & BaBar report signal in
  - $X(3872) \rightarrow D^0 \bar{D}^{*0}$
- Mass  $m[X(3872)] - m[D^{*0}] - m[D^0]$   
 $= (-0.07 \pm 0.12) \text{ MeV}/c^2$  (LHCb 2020)
- Width measurement:
  - $\Gamma_{X(3872)} < 1.2 \text{ MeV}$  (2011, Belle)
  - $\Gamma_{X(3872)} = 1.39 \text{ MeV}$  (2020, LHCb)

Analogy to deuteron:

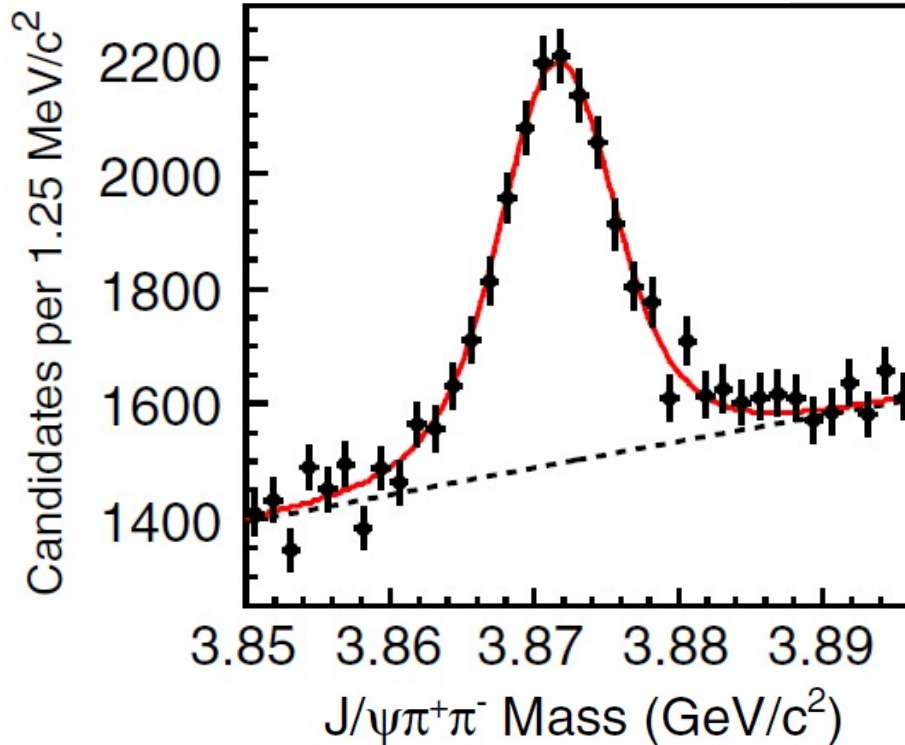


For clarification:

=> Precision measurement with  
sub-MeV resolution needed!

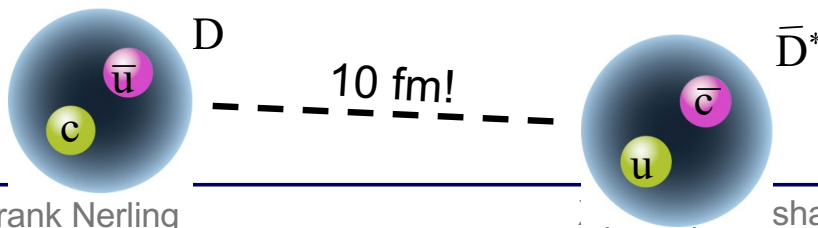
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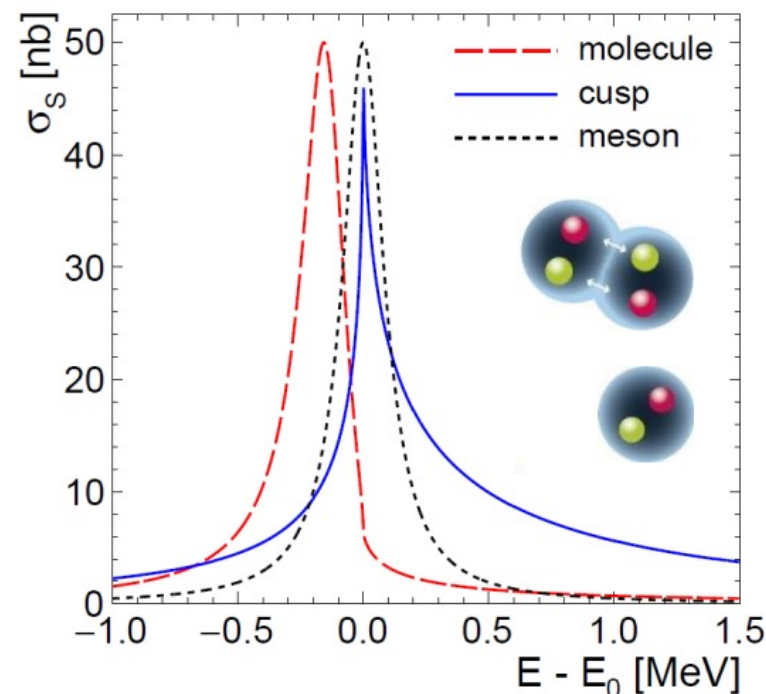
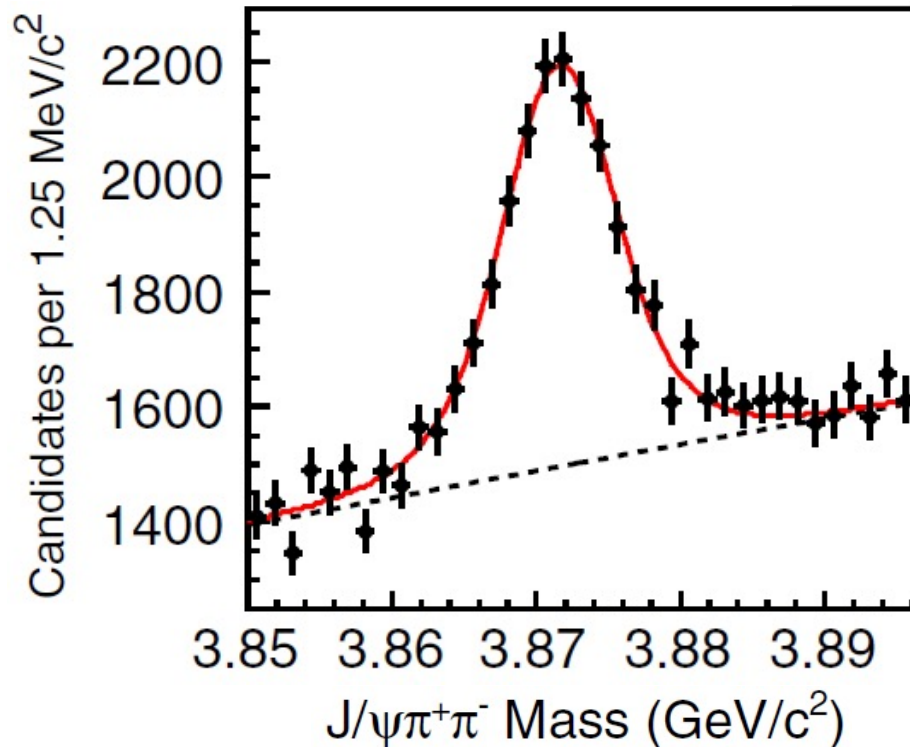


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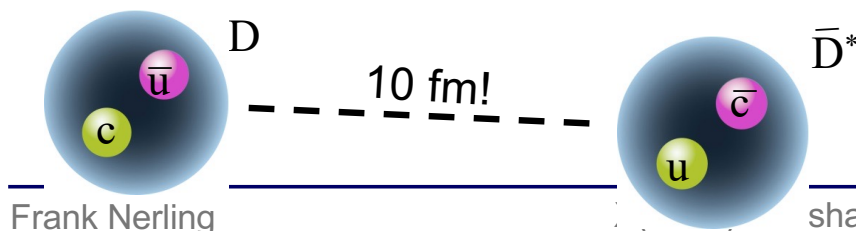
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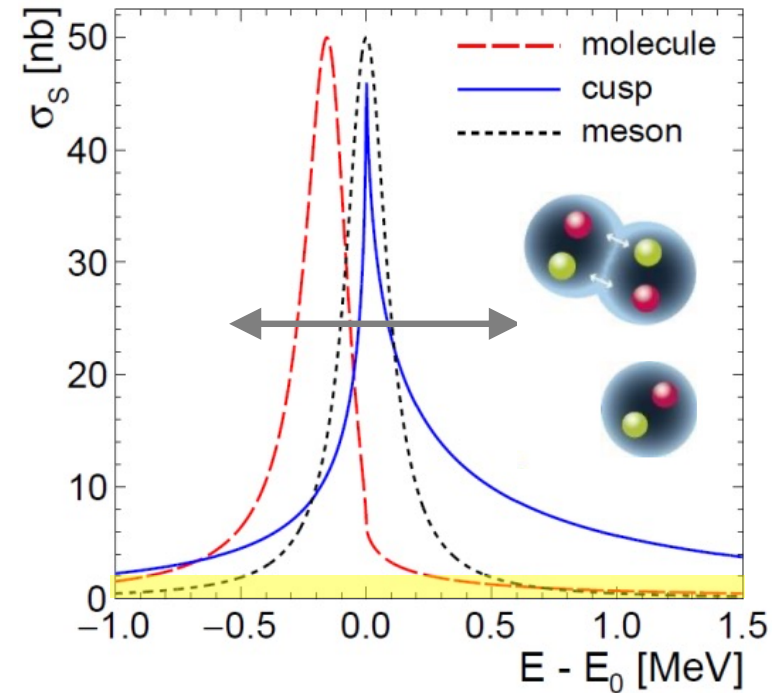
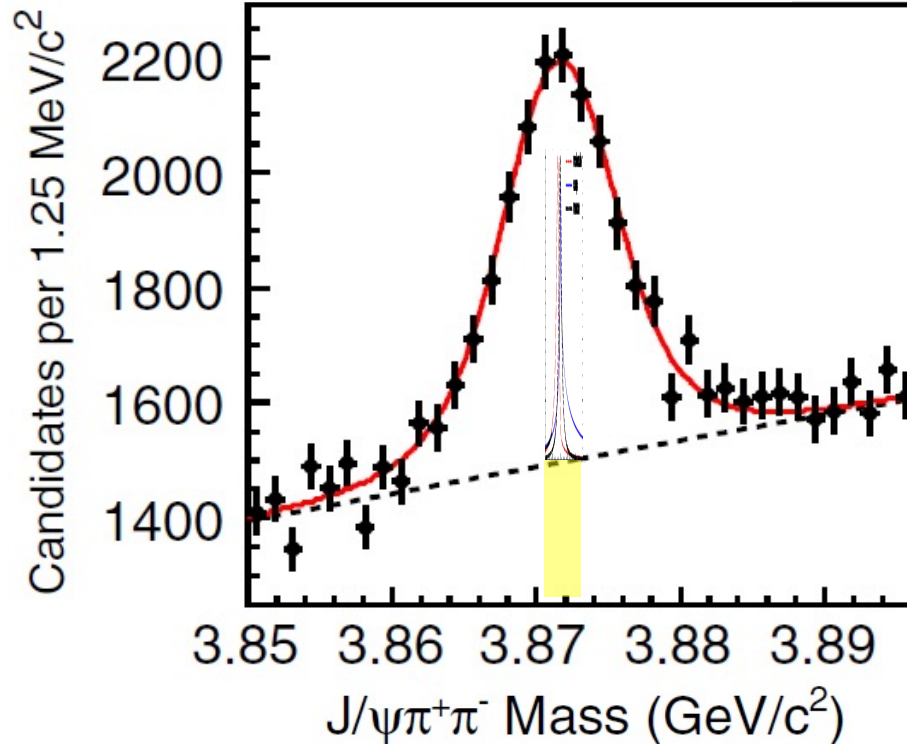
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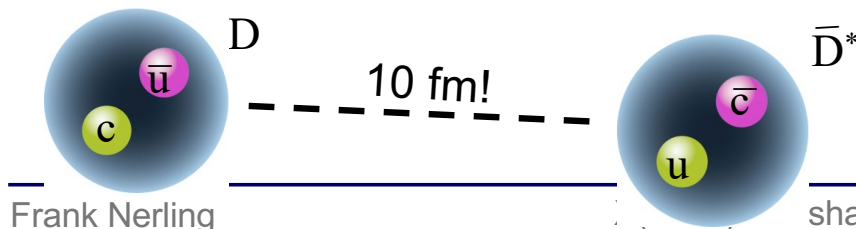
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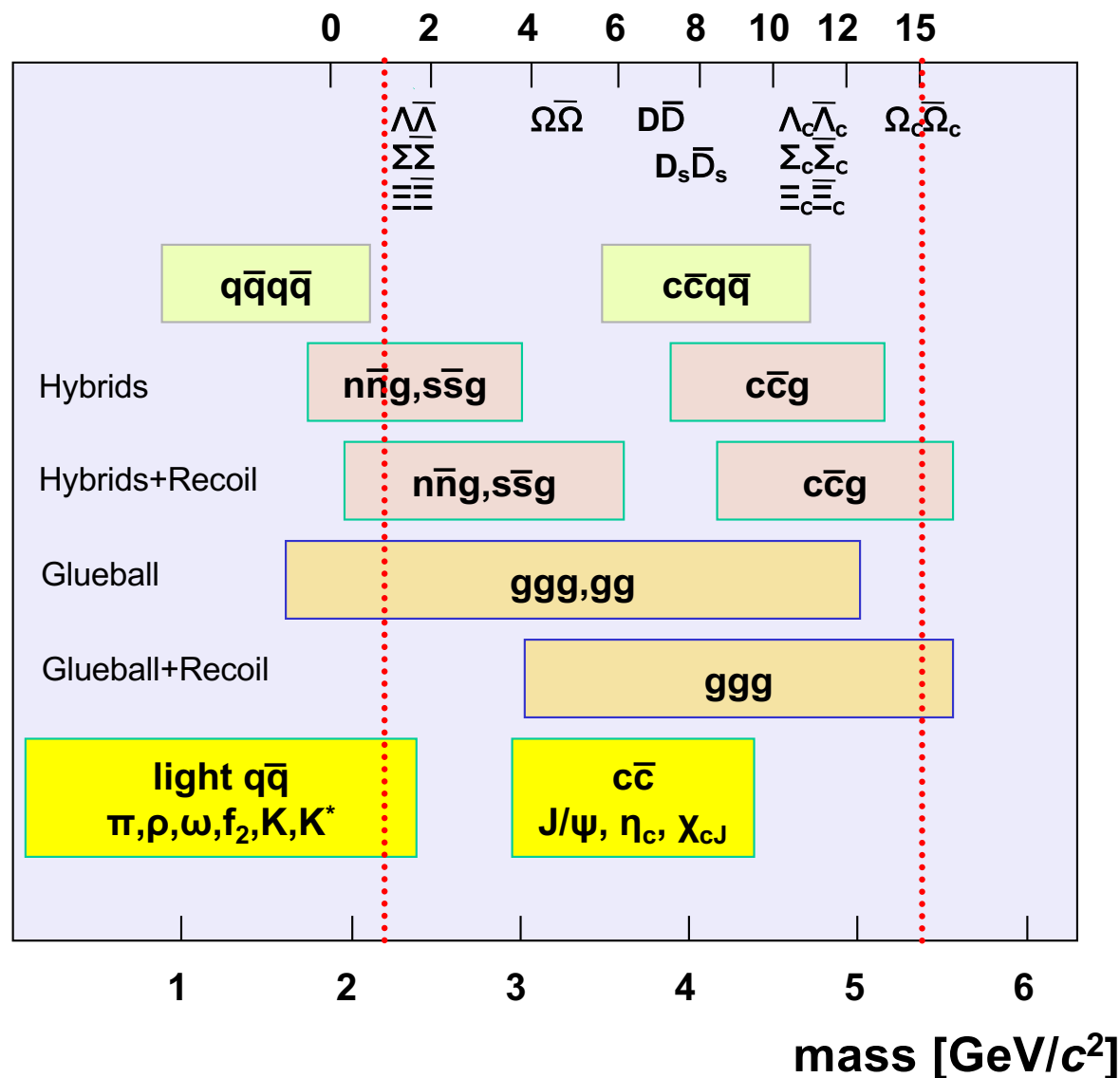
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## Anti-Proton **AN**ihilation in **DA**rmstadt

$\bar{p}$  momentum [GeV/c]

- **Meson spectroscopy**
  - Light mesons
  - Open charm
  - Charmonium
  - Exotic states:  
glue-balls, hybrids,  
molecules / multi-quarks
- **(Anti-) Baryon production**
- **Nucleon structure**
- **Charm in nuclei**
- **Strangeness physics**
  - Hypernuclei,
  - $S = -2$  nuclear system



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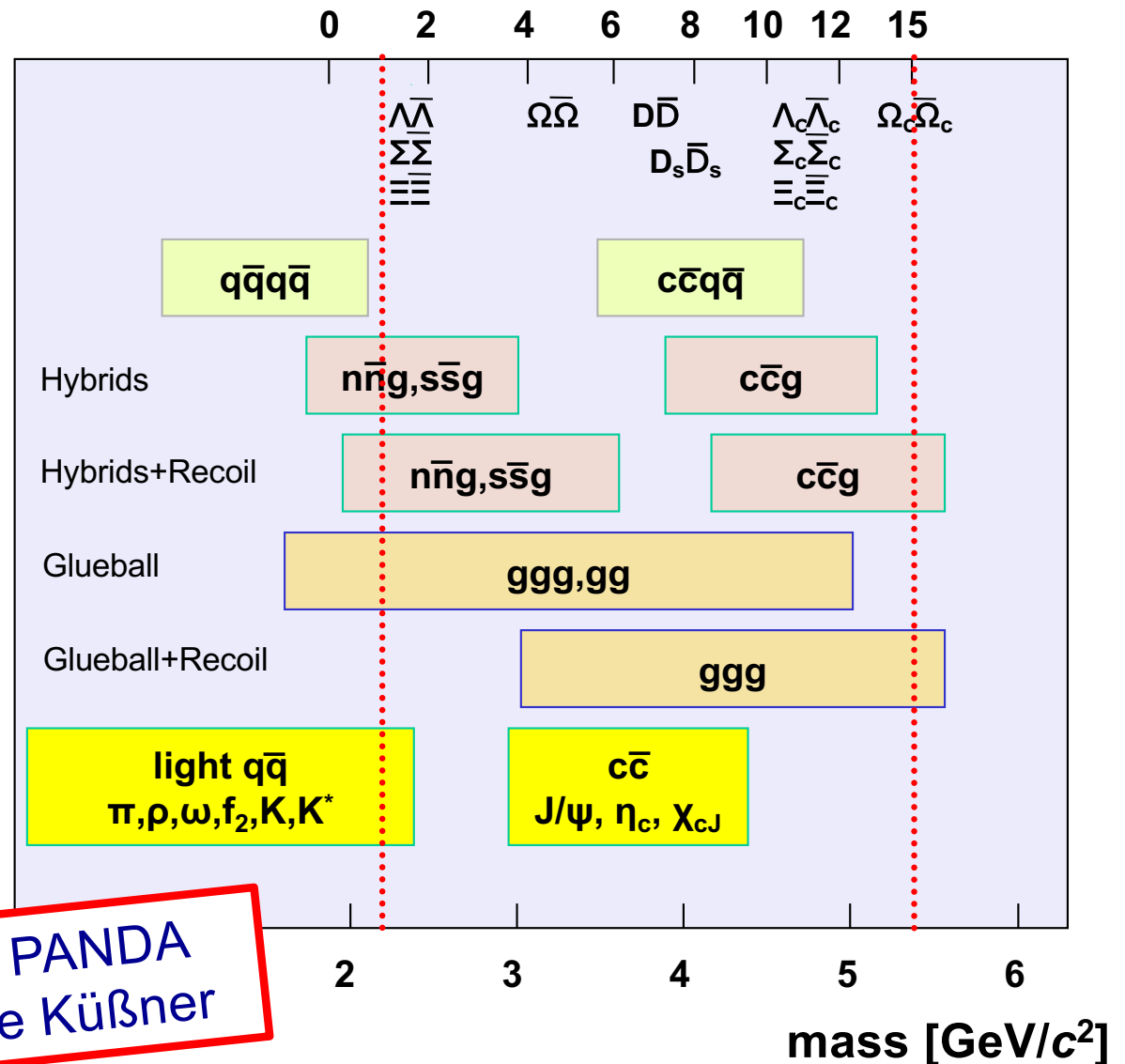
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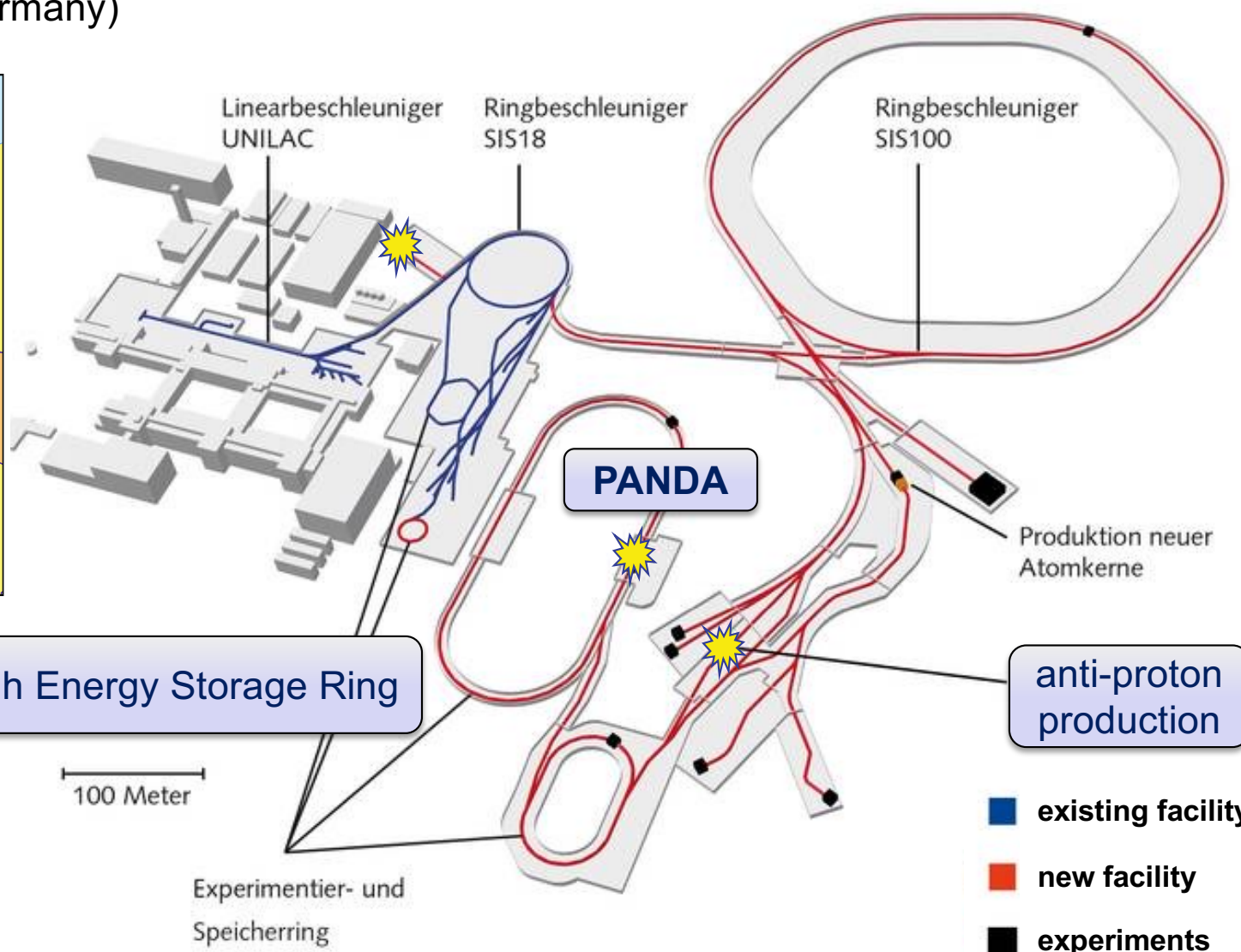


See the more general PANDA  
overview talk by Meike Küßner

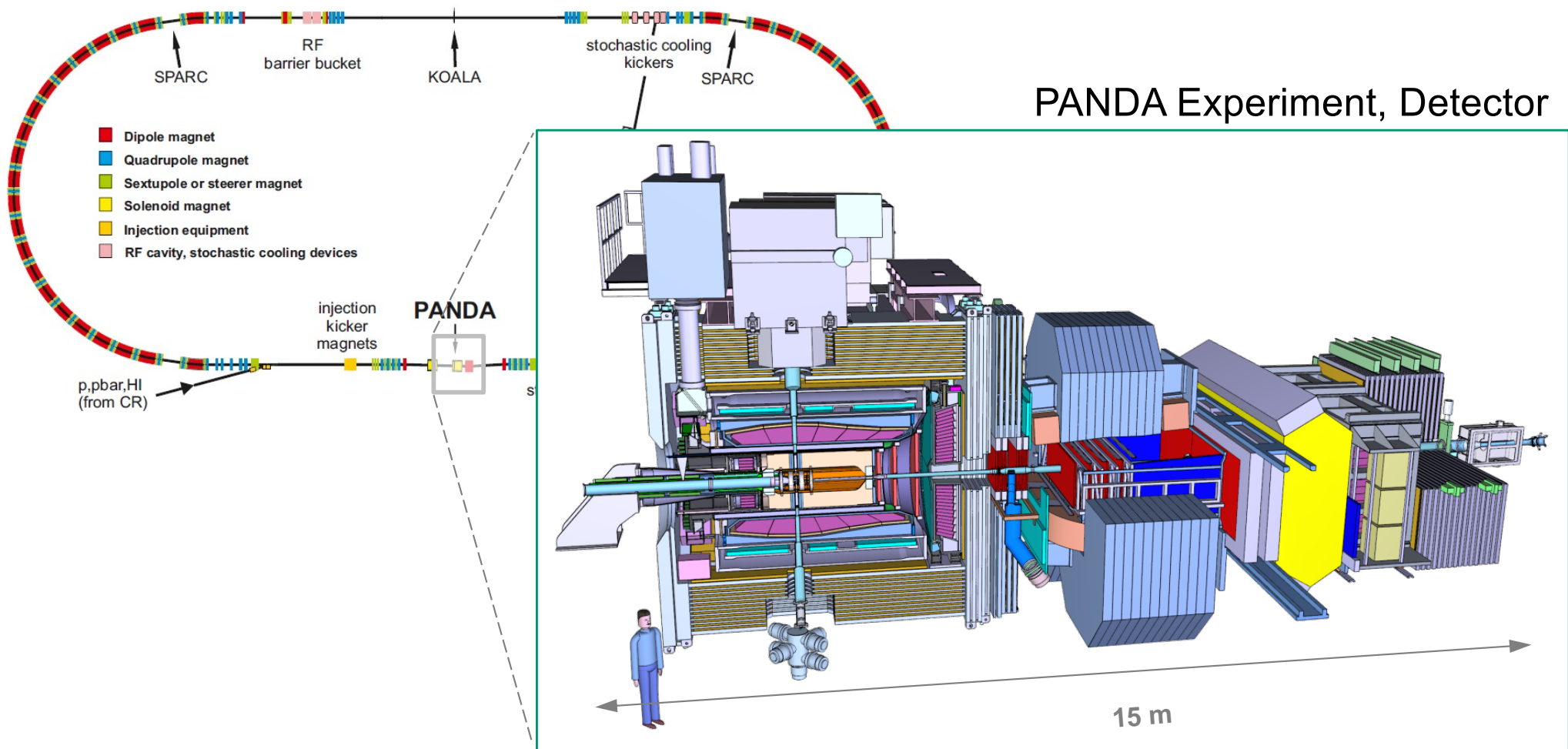
## PANDA at FAIR (GSI, Darmstadt, Germany)



**HESR High Energy Storage Ring**





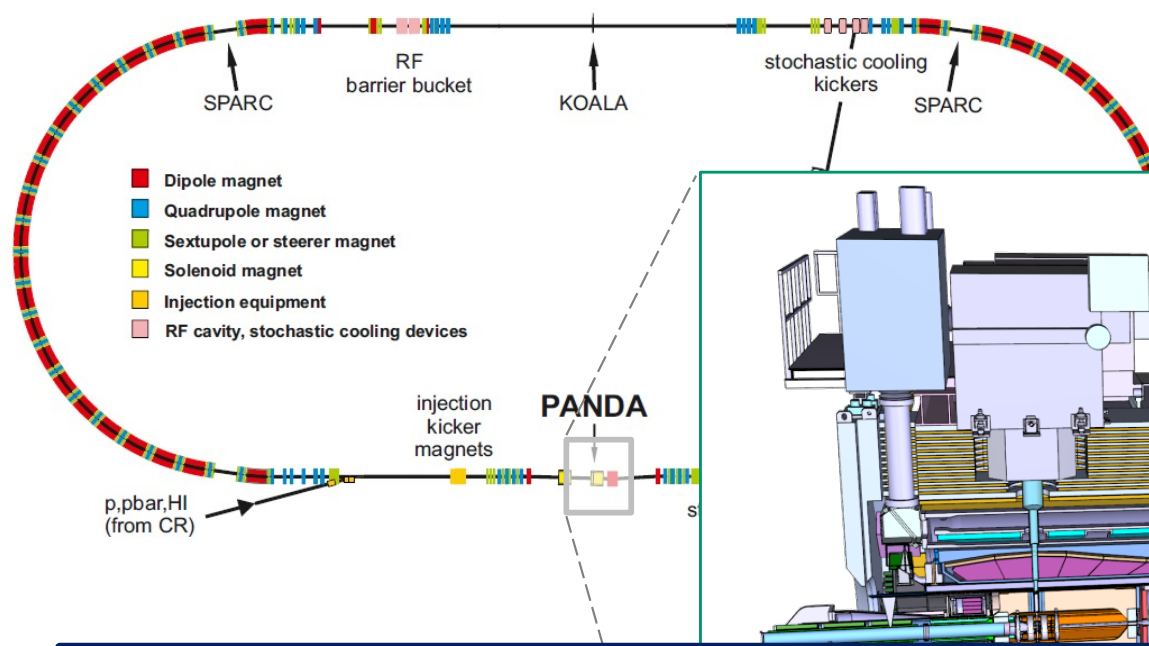


## High Resolution (HR) mode:

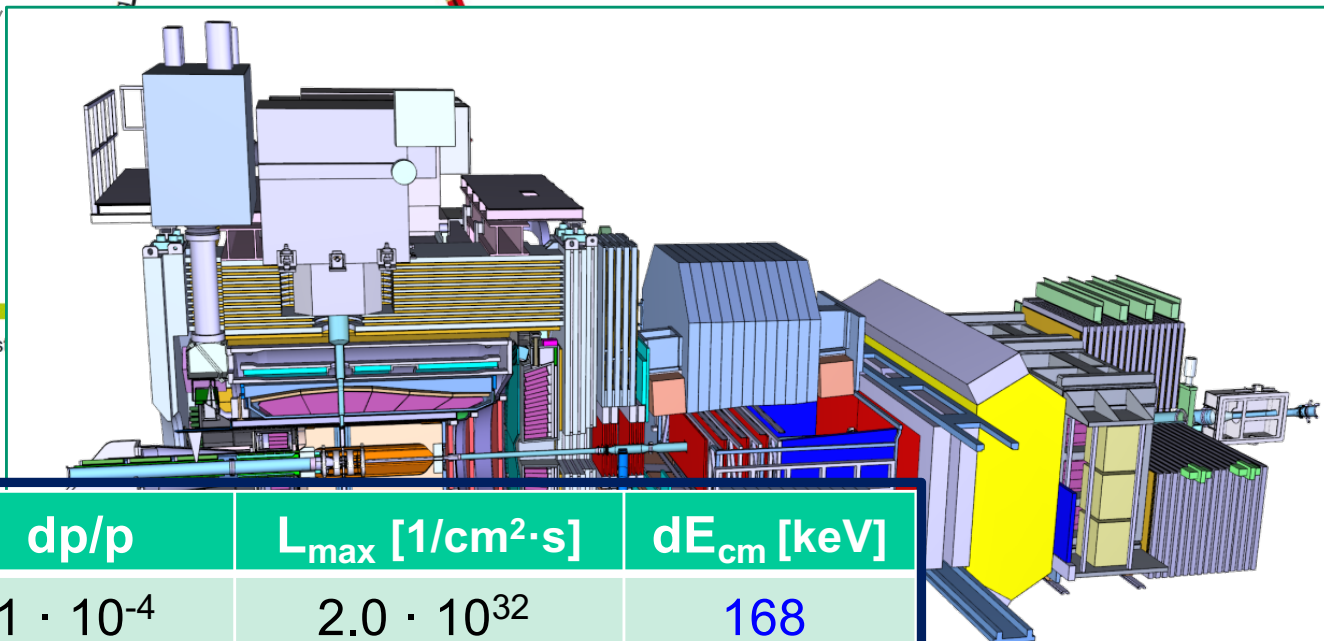
- Luminosity up to  $2 \times 10^{31} \text{ cm}^{-2} \text{ s}^{-1}$
- $\Delta p/p = 2 \times 10^{-5}$

## High Luminosity (HL) mode:

- Luminosity up to  $2 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$
- $\Delta p/p = 1 \times 10^{-4}$



PANDA Experiment, Detector



HESR mode	$dp/p$	$L_{\max}$ [ $1/\text{cm}^2 \cdot \text{s}$ ]	$dE_{\text{cm}}$ [keV]
High Luminosity (HL)	$1 \cdot 10^{-4}$	$2.0 \cdot 10^{32}$	168
High Resolution (HR)	$2 \cdot 10^{-5}$	$2.0 \cdot 10^{31}$	34
Phase 1 Mode (P1)	$5 \cdot 10^{-5}$	$2.0 \cdot 10^{31}$	84

## High Resolution (HR) mode:

- Luminosity up to  $2 \times 10^{31} \text{ cm}^{-2} \text{ s}^{-1}$
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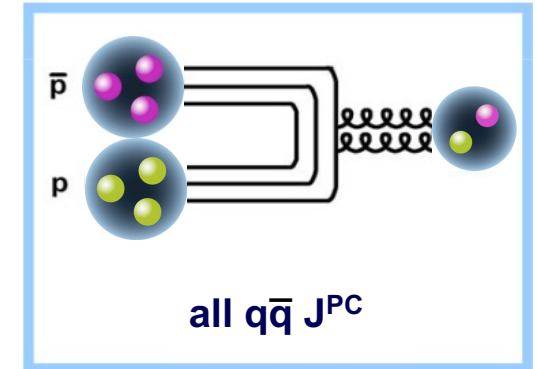
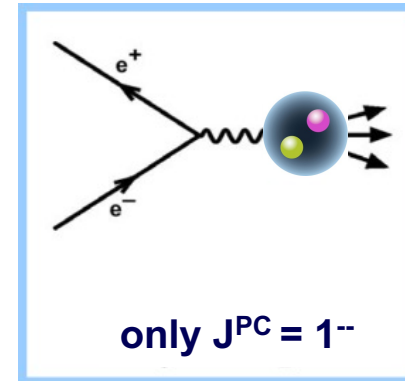
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# Some Advantages of Anti-Protons

- Access to all fermion-antifermion quantum numbers (*not in  $e^+e^-$* )
- Access to states of high spin  $J$

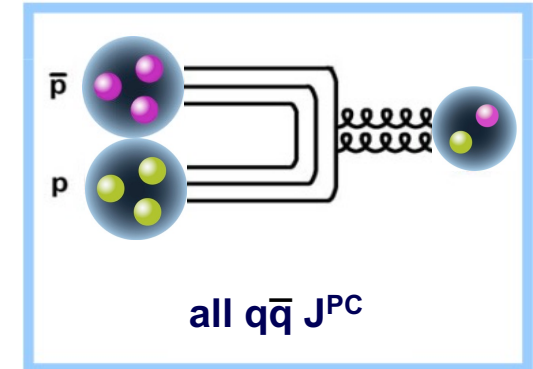
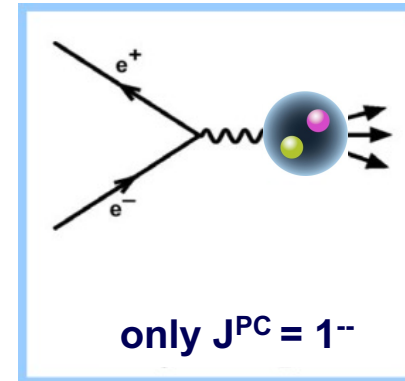
## Formation:



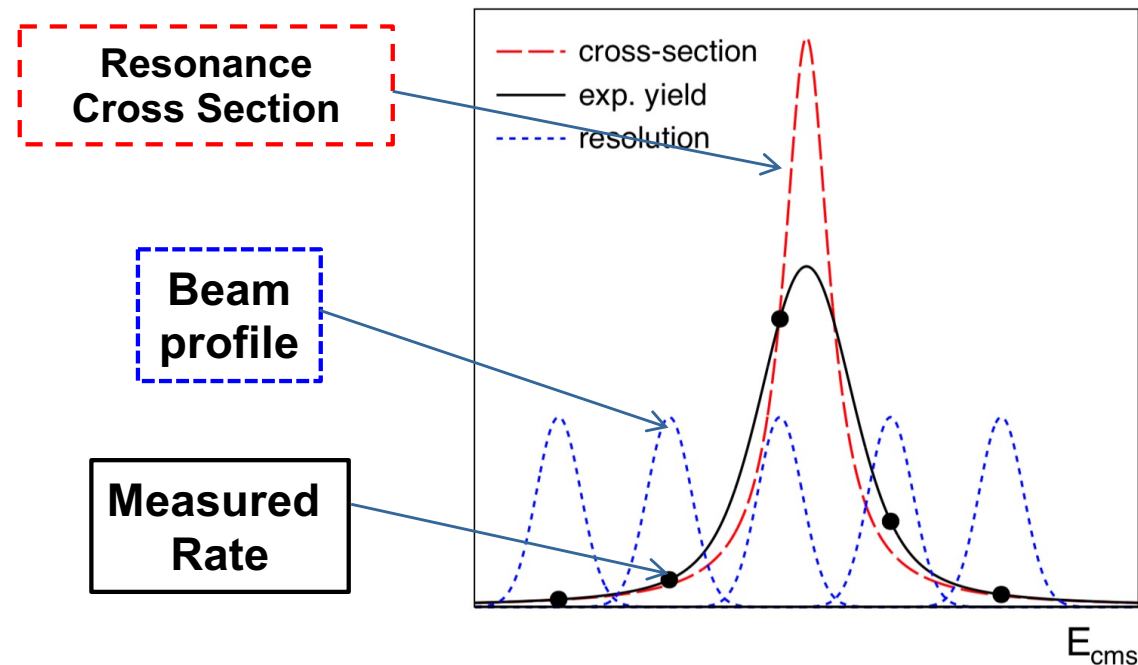
# Some Advantages of Anti-Protons

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- Access to states of high spin J
- Precise mass resolution in formation reactions

## Formation:



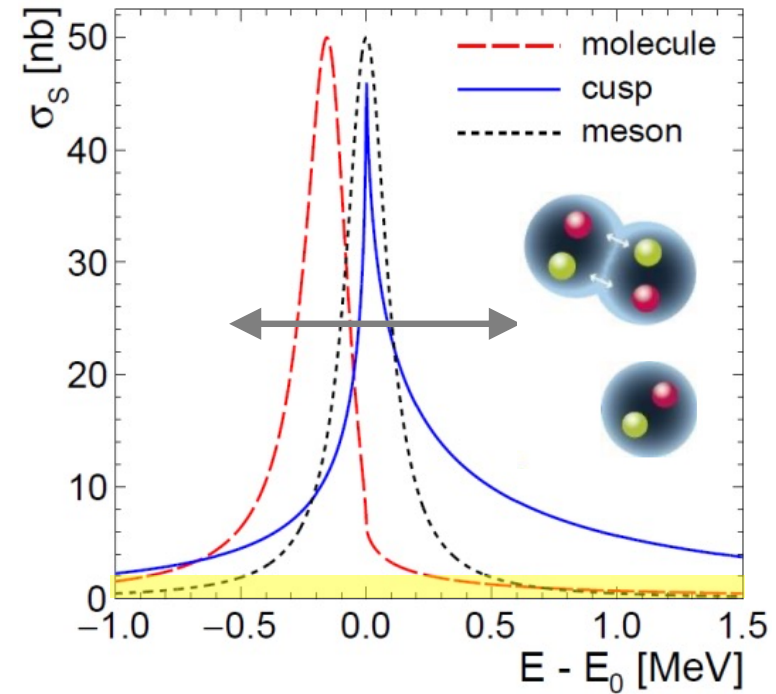
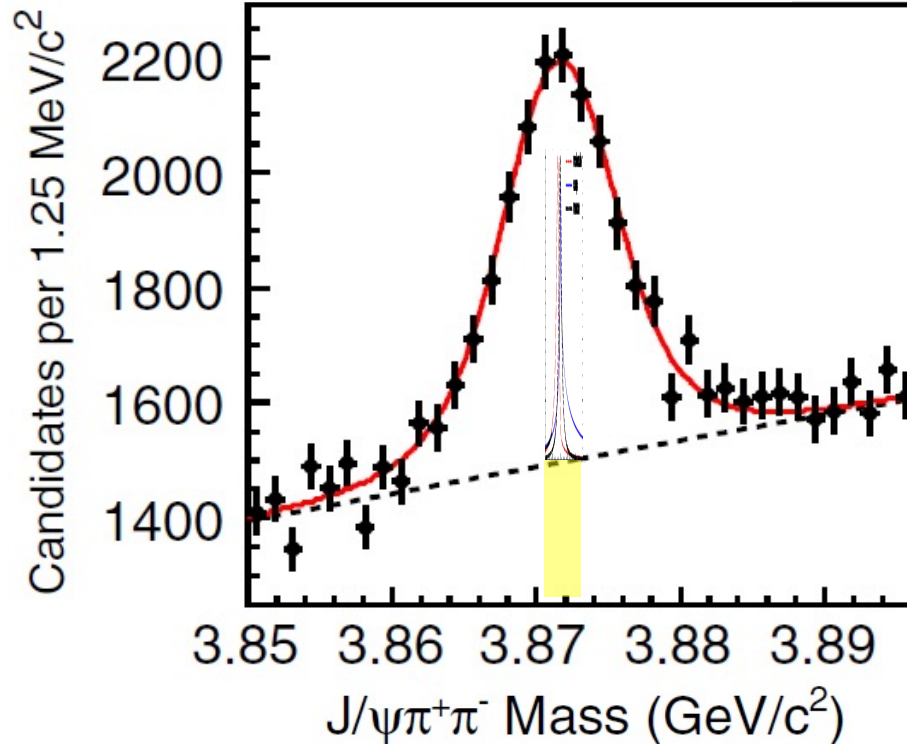
E760/835@Fermilab  $\approx$  240 keV  
PANDA@FAIR  $\approx$  50 keV





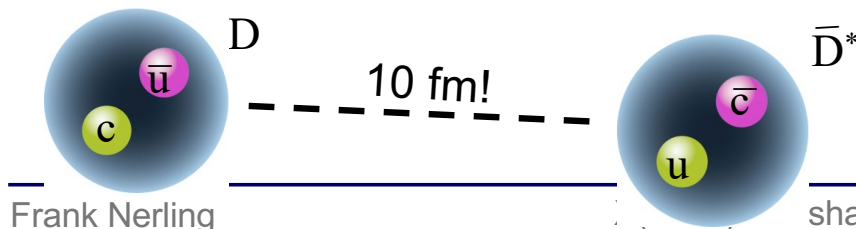
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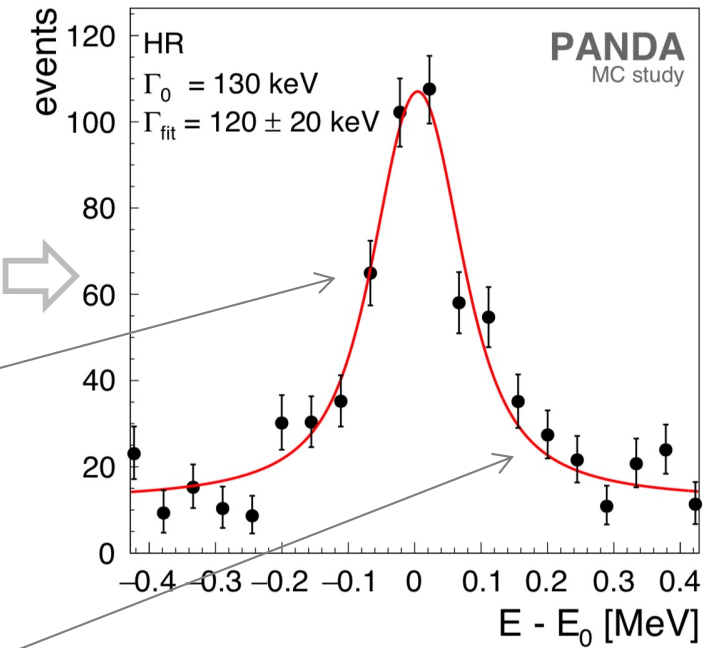
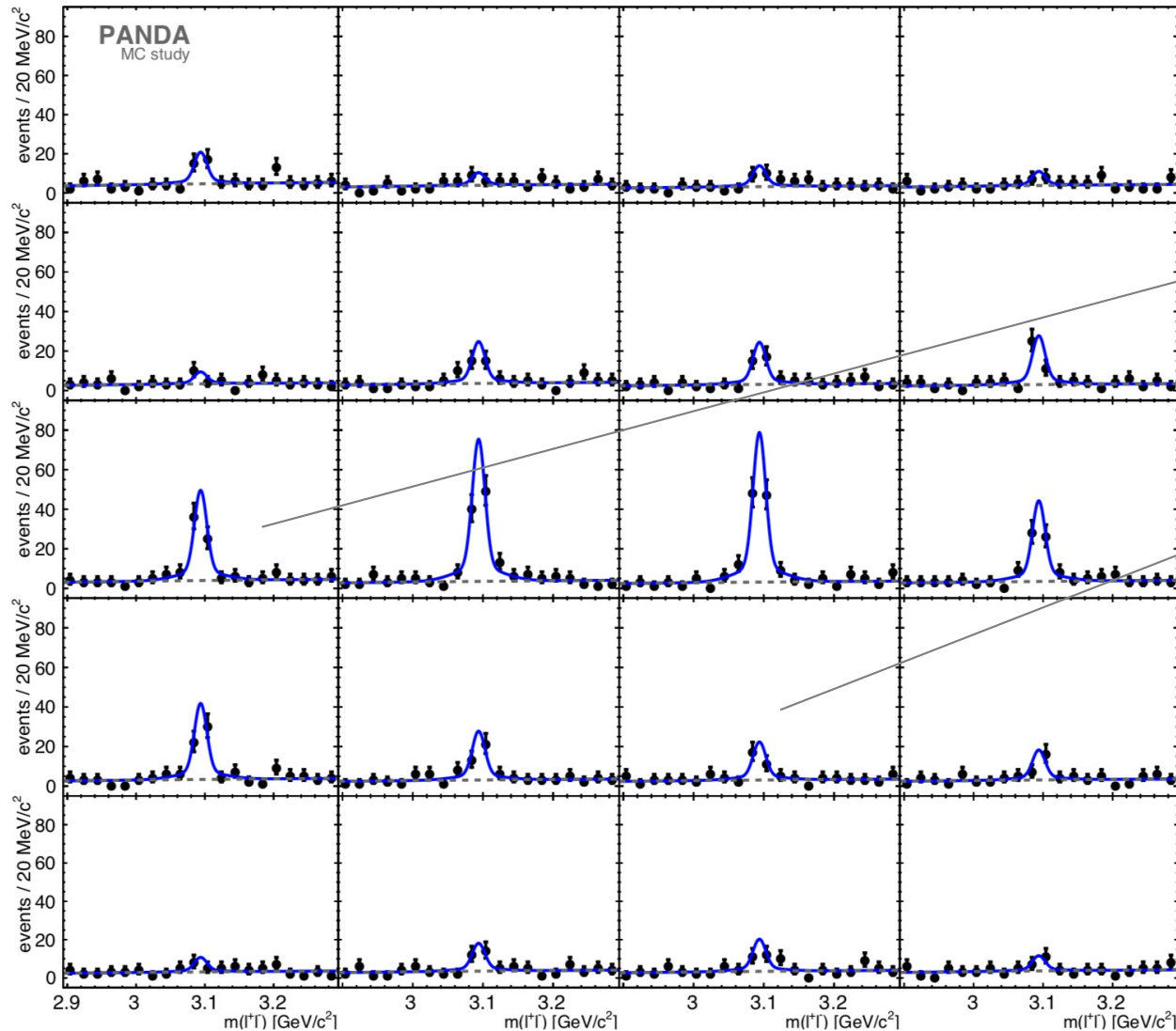
=> Precision measurement with  
sub-MeV resolution needed!

## Performance Study for energy resonance scans of narrow resonances, like the X(3872)

**Reminder:**  
Sub-MeV resolution needed to clarify nature  
=> 

# Scan Procedure Principle (Example)

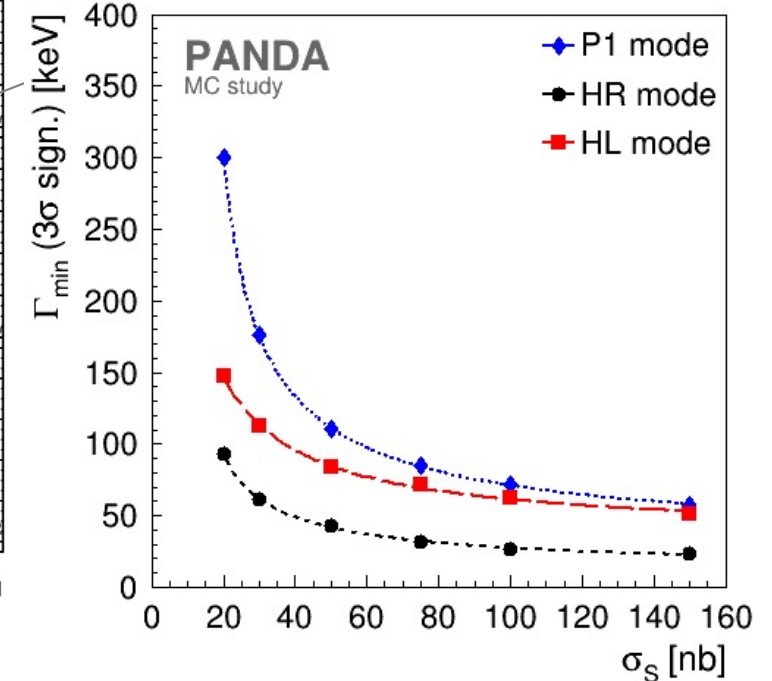
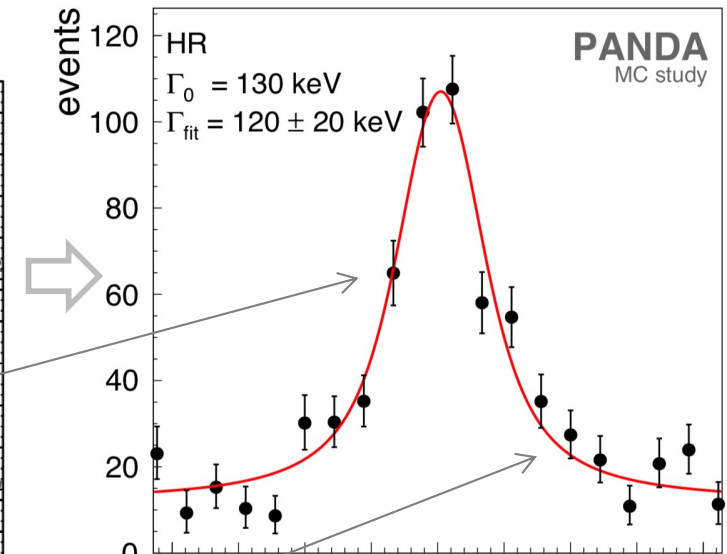
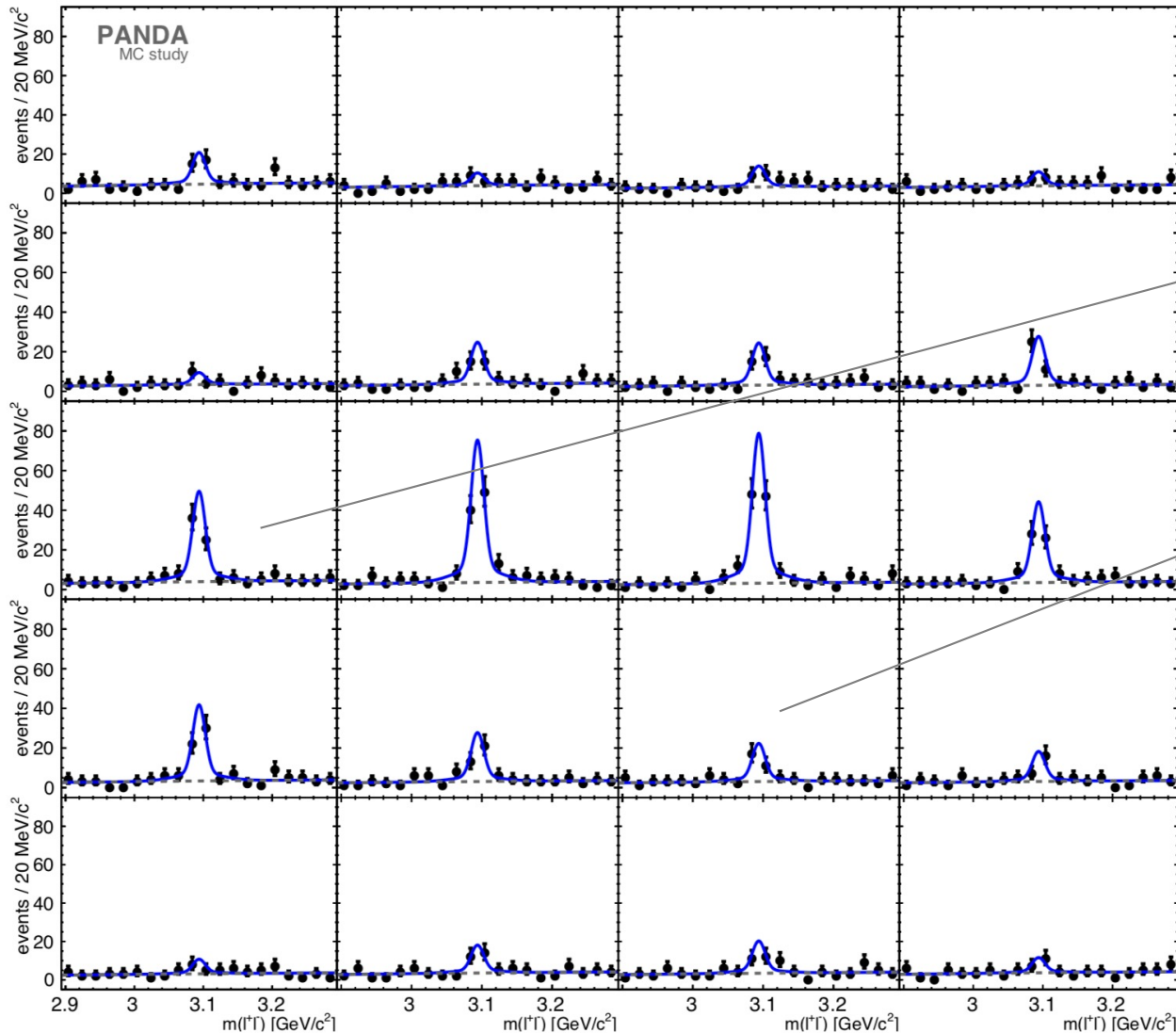
20  $E_{\text{cms}}$  scan point within  $\pm 0.4$  MeV window around nominal mass



[PANDA, Eur. Phys. J. A 55 (2019) 42]

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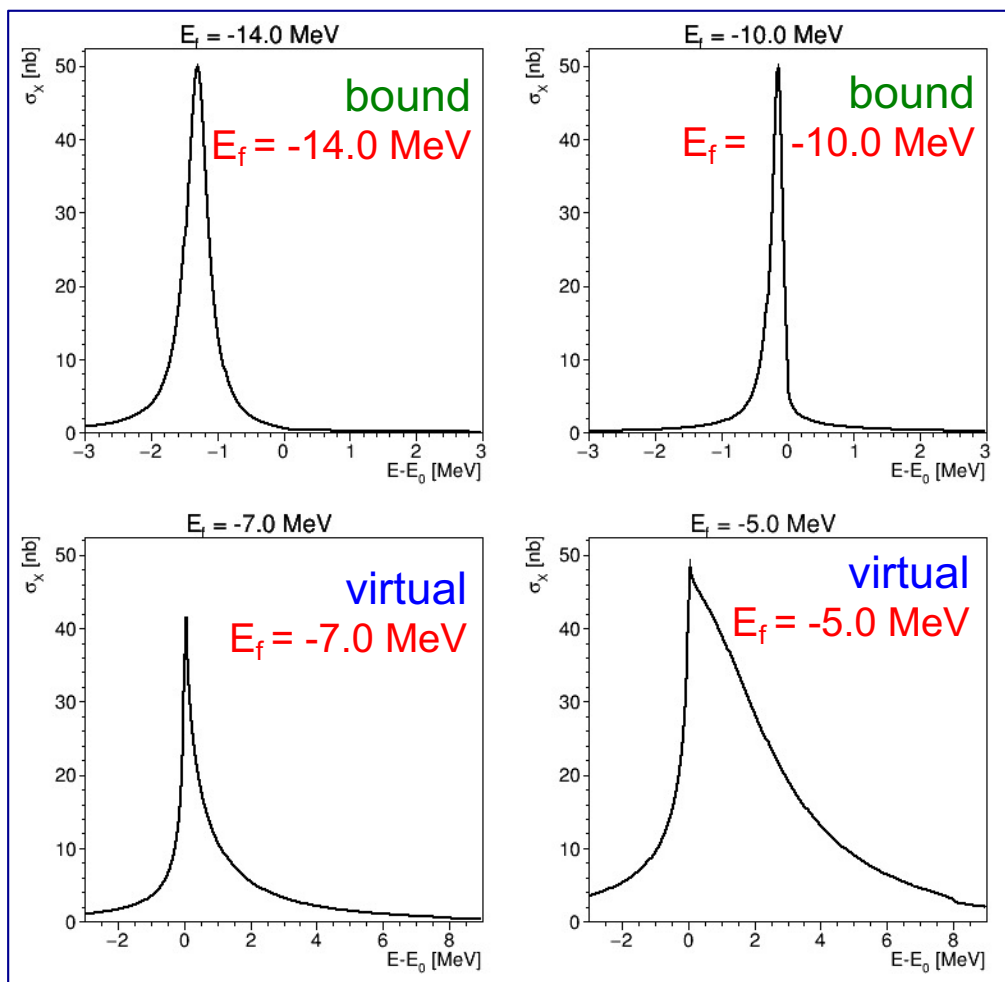
# Distinction of Lineshapes (40 x 2d)

- How well can **virtual** vs **bound** state be distinguished?

[Phys. Atom. Nucl. 73 (2010) 1592]

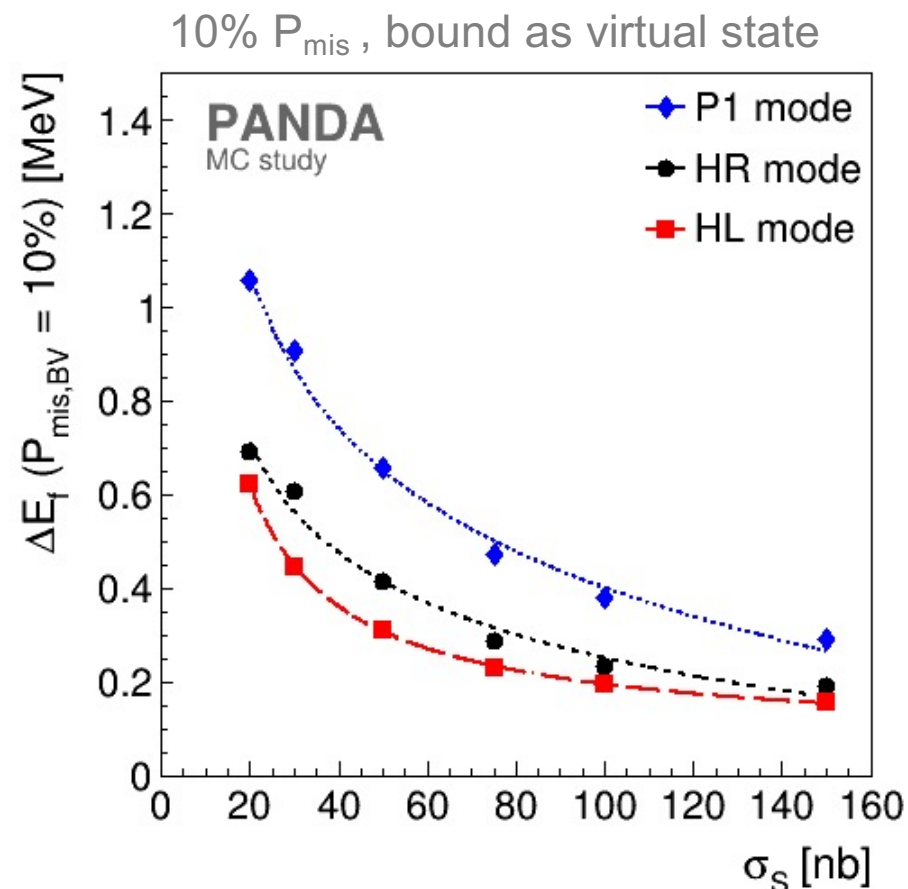
$$\sigma(E; E_f) \sim \frac{\Gamma_{\pi^+\pi^- J/\psi}(E)}{|D(E; E_f)|^2}$$

Flatté line shape depends on  $E_f$



[PANDA, Eur. Phys. J. A 55 (2019) 42]

## Sensitivity





[Phys.Rev.D 102 (2020) 9, 092005]  
[https://arxiv.org/abs/2005.13419]

CERN-EP-2020-086  
LHCb-PAPER-2020-008  
May 27, 2020

## Study of the lineshape of the $\chi_{c1}(3872)$ state

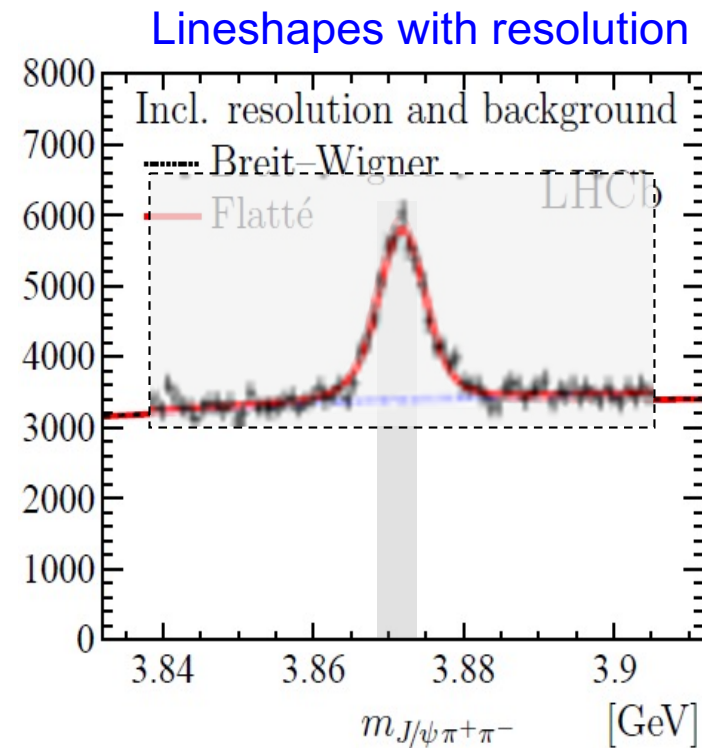
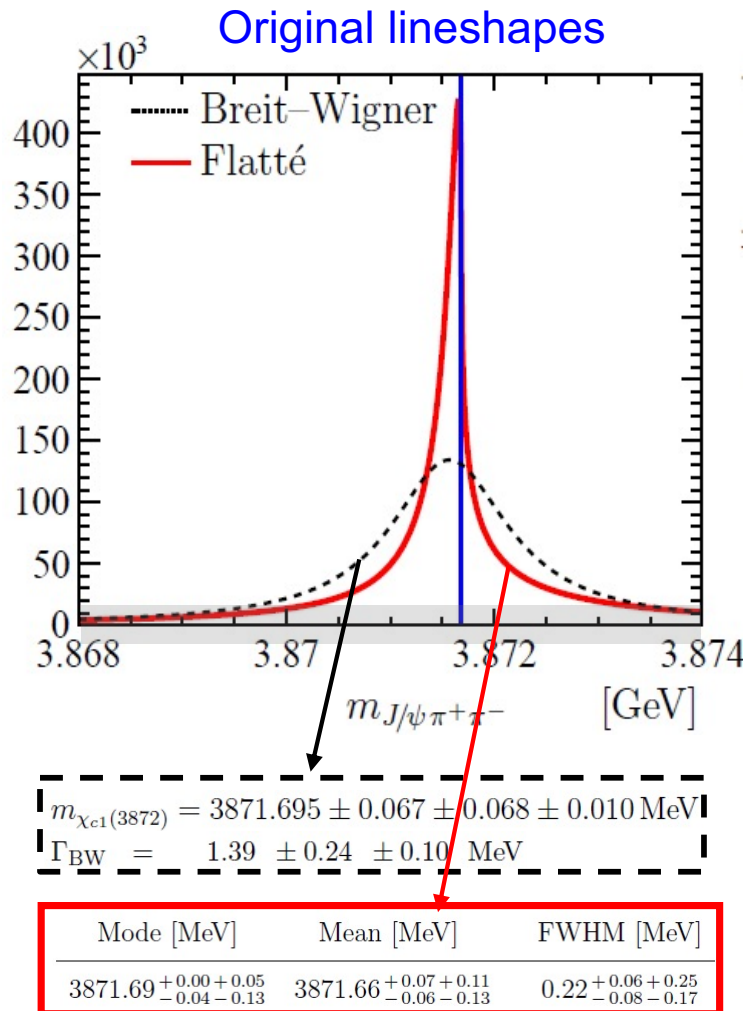
### Abstract

A study of the lineshape of the  $\chi_{c1}(3872)$  state is made using a data sample corresponding to an integrated luminosity of  $3\text{ fb}^{-1}$  collected in  $pp$  collisions at centre-of-mass energies of 7 and 8 TeV with the LHCb detector. Candidate  $\chi_{c1}(3872)$  mesons from  $b$ -hadron decays are selected in the  $J/\psi\pi^+\pi^-$  decay mode. Describing the lineshape with a Breit–Wigner function, the mass splitting between the  $\chi_{c1}(3872)$  and  $\psi(2S)$  states,  $\Delta m$ , and the width of the  $\chi_{c1}(3872)$  state,  $\Gamma_{\text{BW}}$ , are determined to be

$$\begin{aligned}\Delta m &= 185.588 \pm 0.067 \pm 0.068 \text{ MeV}, \\ \Gamma_{\text{BW}} &= 1.39 \pm 0.24 \pm 0.10 \text{ MeV},\end{aligned}$$

where the first uncertainty is statistical and the second systematic. Using a Flatté-inspired lineshape, two poles for the  $\chi_{c1}(3872)$  state in the complex energy plane are found. The dominant pole is compatible with a quasi-bound  $D^0\bar{D}^{*0}$  state but a quasi-virtual state is still allowed at the level of 2 standard deviations.

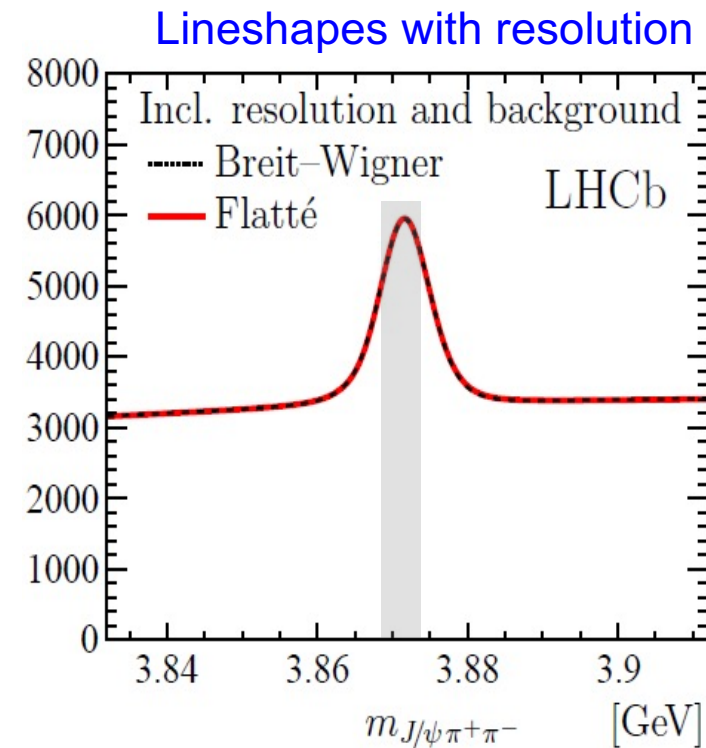
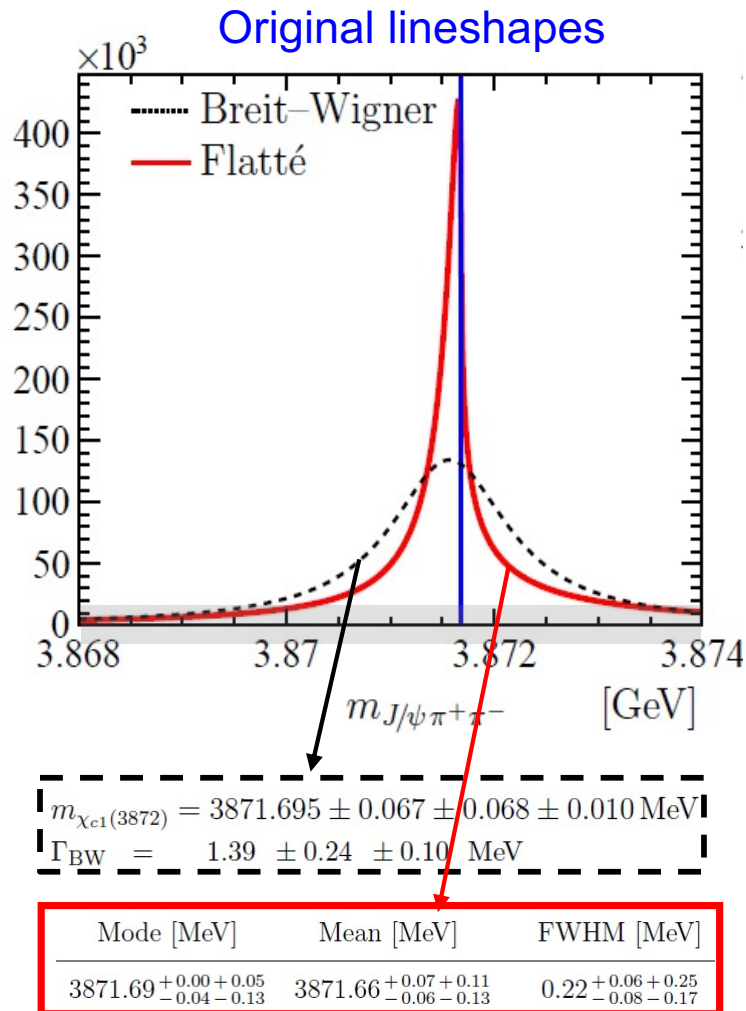
# LHCb lineshapes (incl. resolution)



## 7.3 Comparison between Breit-Wigner and Flatté lineshapes

Figure 4 shows the comparison between the Breit-Wigner and the Flatté lineshapes. While in both cases the signal peaks at the same mass, the Flatté model results in a significantly narrower lineshape. However, after folding with the resolution function and adding the background, the observable distributions are indistinguishable.

# LHCb lineshapes (incl. resolution)



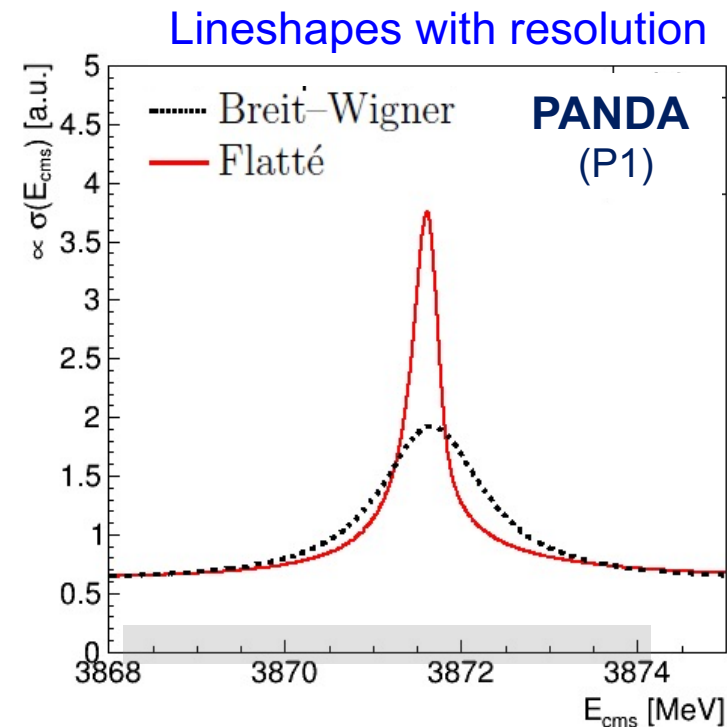
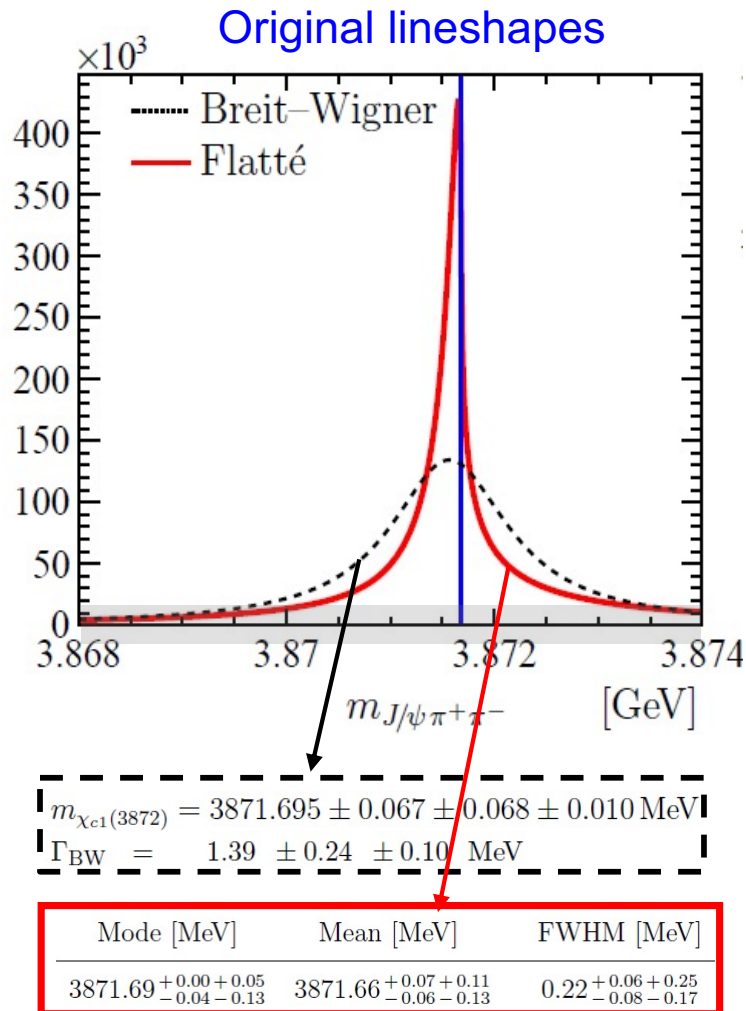
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- Due to detector resolution both models cannot be distinguished at LHCb
  - 1.39 MeV (BW) vs. 0.22 MeV (Flatté) => factor of ~5



# LHCb lineshapes (incl. resolution)



- Due to the excellent beam resolution  $O(50-100 \text{ keV})$  at PANDA
  - Models are well distinguishable  
=> Let's quantify

- Due to detector resolution both models cannot be distinguished at LHCb
  - 1.39 MeV (BW) vs. 0.22 MeV (Flatté) => factor of ~5



**Precision resonance energy scans with the PANDA experiment  
at FAIR** Sensitivity study for width and line shape measurements of the X(3872)

- Addendum:  
Investigate separation power  
→  $E_f$  (Flatté) vs.  $\Gamma$  (BW)
- Key parameters from  
→ EPJ A 55 (2019) 42
- Total beam time  
→  $40 \times 2d = 80 d$
- Generate many (toy) spectra  
for Flatté & BW model
- Fit both line shapes to each  
generated distribution
- Determine fit probabilities  
 $P_F$  &  $P_{BW}$  and fractions of  
incorrect assignments →  $P_{mis}$

Branching  
Fractions

Cross  
sections

Luminosities

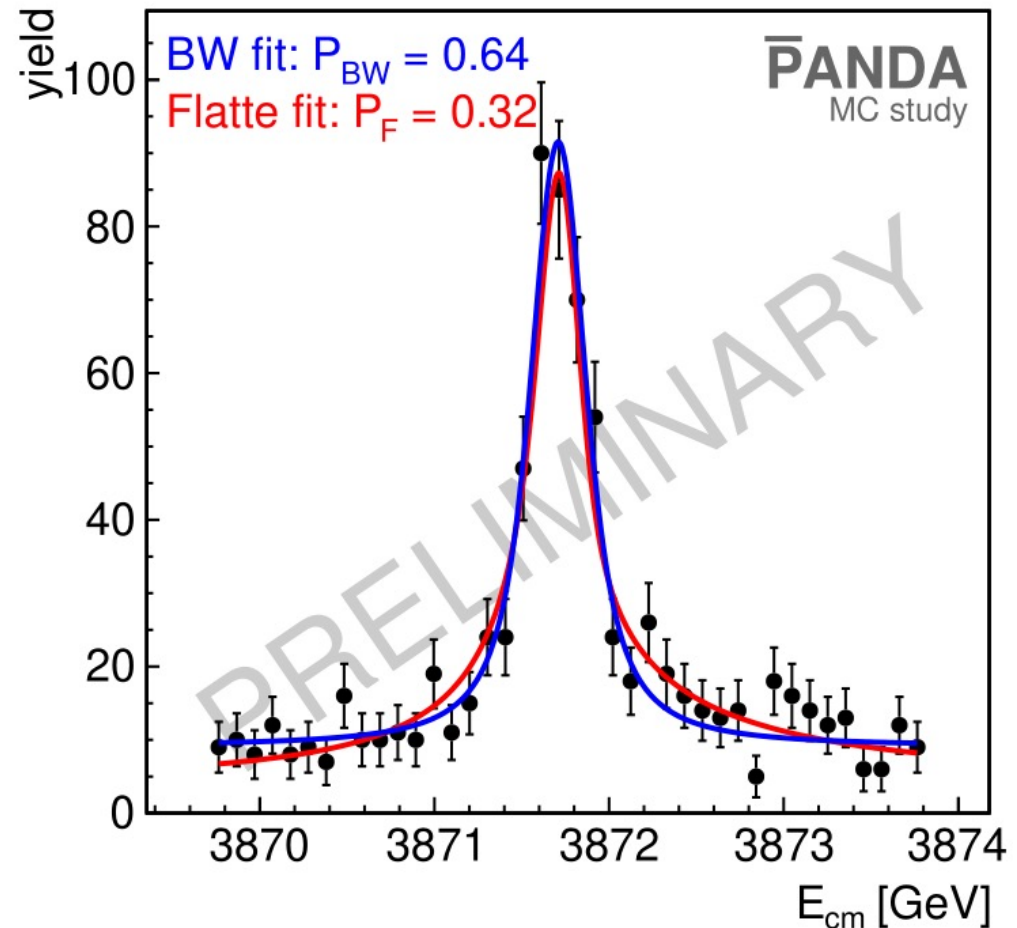
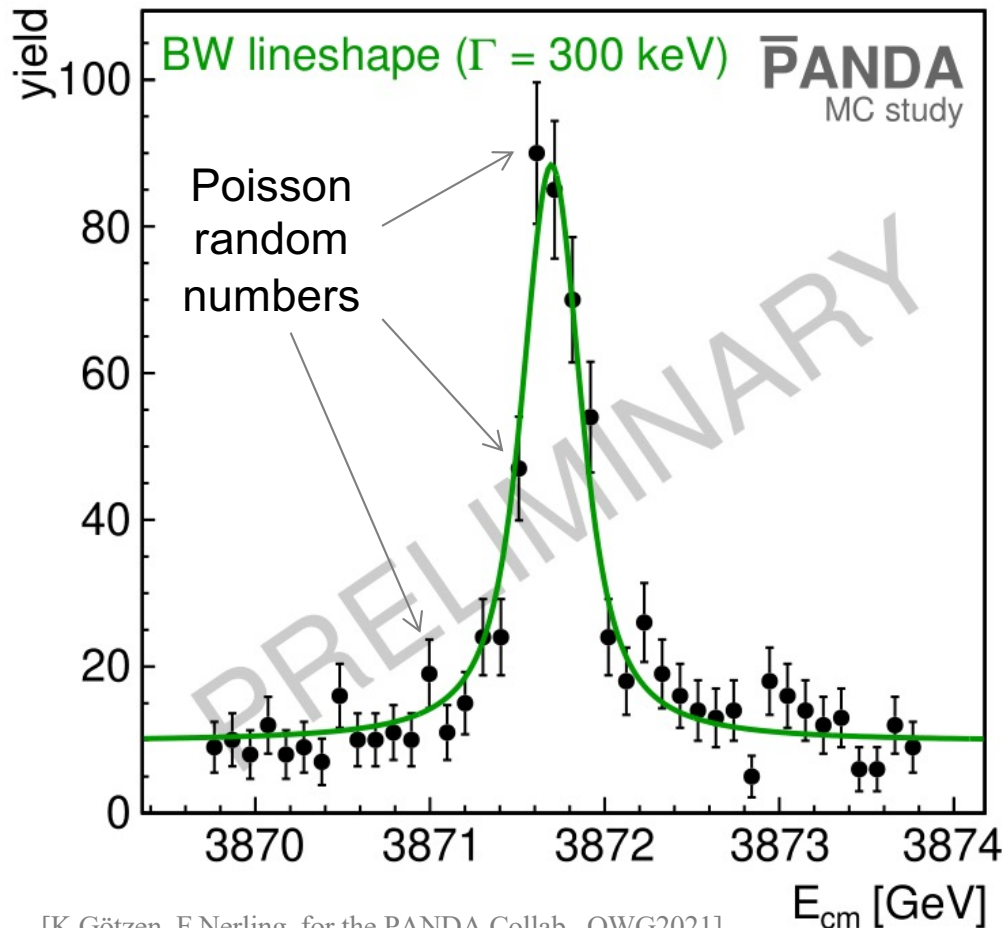
Resolutions

Parameter	Value
BR( $J/\psi \rightarrow e^+ e^-$ )	5.97 %
BR( $J/\psi \rightarrow \mu^+ \mu^-$ )	5.96 %
BR( $\rho^0 \rightarrow \pi^+ \pi^-$ )	100%
BR( $X \rightarrow J/\psi \rho^0$ )	5 % (UL: 6.6%)
$\sigma_{peak}(p\bar{p} \rightarrow X)$	[20,30,50,75,100,150] nb
$\sigma(p\bar{p} \rightarrow J/\psi \pi^+ \pi^- \text{ non-res})$	1.2 nb [theory]
$\sigma(p\bar{p} \rightarrow \text{inelastic}) @ 3.872 \text{ GeV}$	46 mb [CERN-HERA-84-01 (1984)]
$L_{HL} (3.872 \text{ GeV})$	$13683 \text{ (nb} \cdot \text{d)}^{-1}$
$L_{HR} (3.872 \text{ GeV})$	$1368 \text{ (nb} \cdot \text{d)}^{-1}$
$L_{P1} (3.872 \text{ GeV})$	$1170 \text{ (nb} \cdot \text{d)}^{-1}$
$\Delta E_{abs} \text{ (energy prec. w/ calibration)}$	168 keV ( $dp/p = 10^{-4}$ )
$\Delta E_{rel} \text{ (relative energy positioning)}$	1.7 keV ( $dp/p = 10^{-6}$ )
$\Delta E_{mom} \text{ (HL)}$	168 keV ( $dp/p = 10^{-4}$ )
$\Delta E_{mom} \text{ (HR)}$	34 keV ( $dp/p = 2 \cdot 10^{-5}$ )
$\Delta E_{mom} \text{ (P1)}$	84 keV ( $dp/p = 5 \cdot 10^{-5}$ )

# Scan Procedure Principle (Example)

Example: Breit-Wigner,  $\Gamma = 300$  keV (P1 mode)

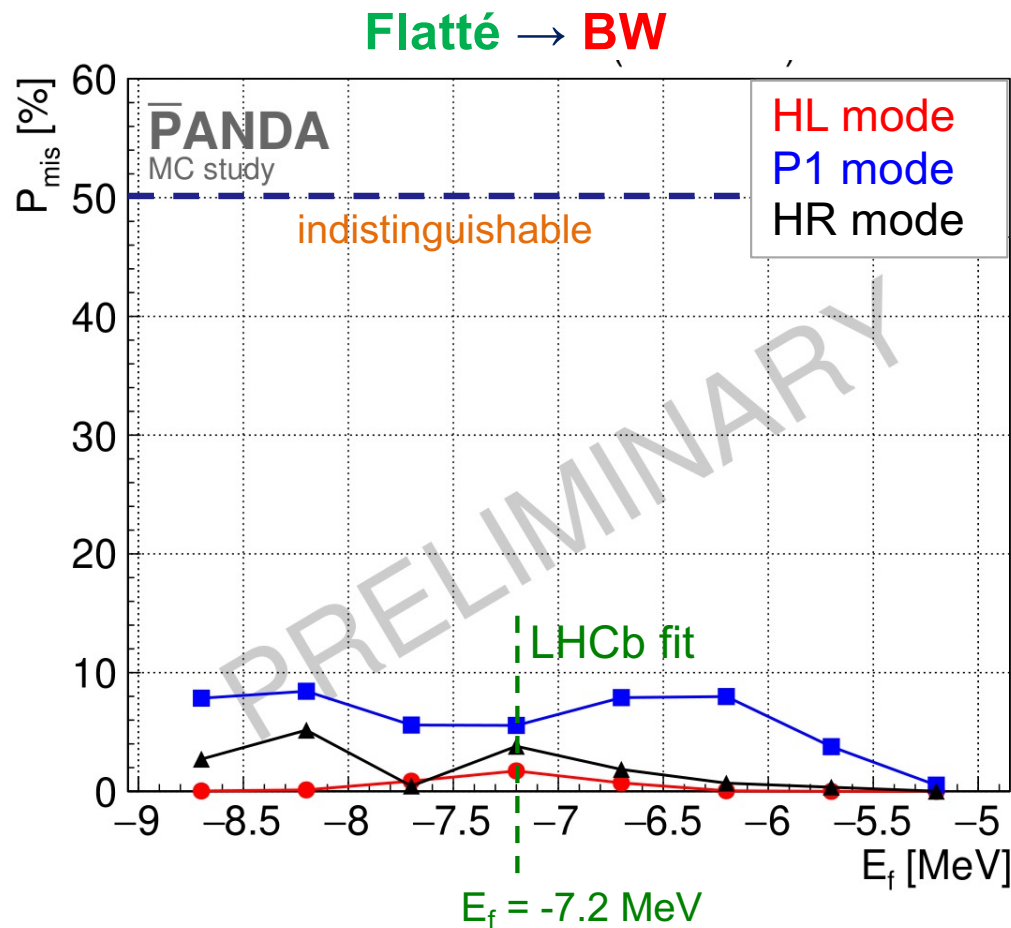
- Compute true line shape (BW or Flatté)
- Generate poisson random number  $N_{\text{poisson}}$  for each  $E_{\text{cm}}$  and fill into graph
- Fit line shapes to extract fit probabilities  $P_{\text{BW}}$  and  $P_{\text{F}}$



[K.Götzen, F.Nerling, for the PANDA Collab., QWG2021]

# Parameter dependent performance

Performance across **Flatté energy**  $E_f$  range (LHCb:  $E_f = -7.2 \text{ MeV}$ ),



Performance as **Mis-ID** of **Flatté** as **BW**

- Mis-identification probability  $P_{\text{mis}}$  vs.  $E_f$
- For three **beam modes** (HL, HR, P1)
- $P_{\text{mis}} = 50\% \Rightarrow$  "indistinguishable"

Distinguish between models:

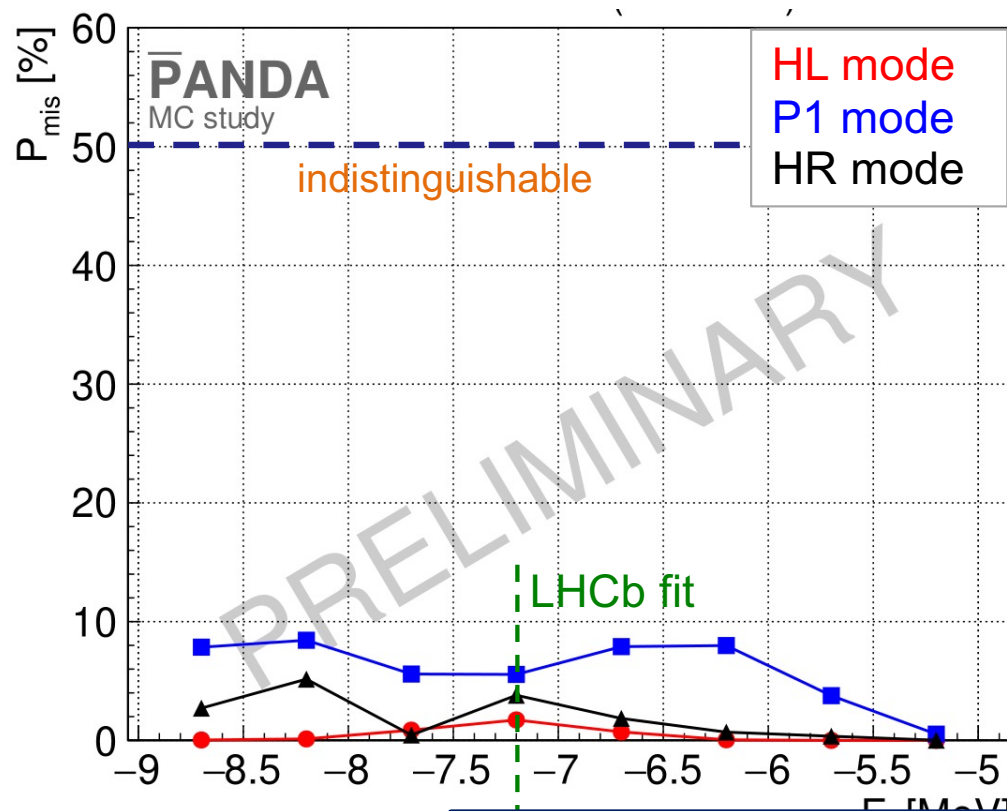
**HL Mode** :  $\geq 98\%$  correct  
**HR Mode** :  $\geq 95\%$  correct  
**P1 Mode** :  $\geq 90\%$  correct

# Parameter dependent performance

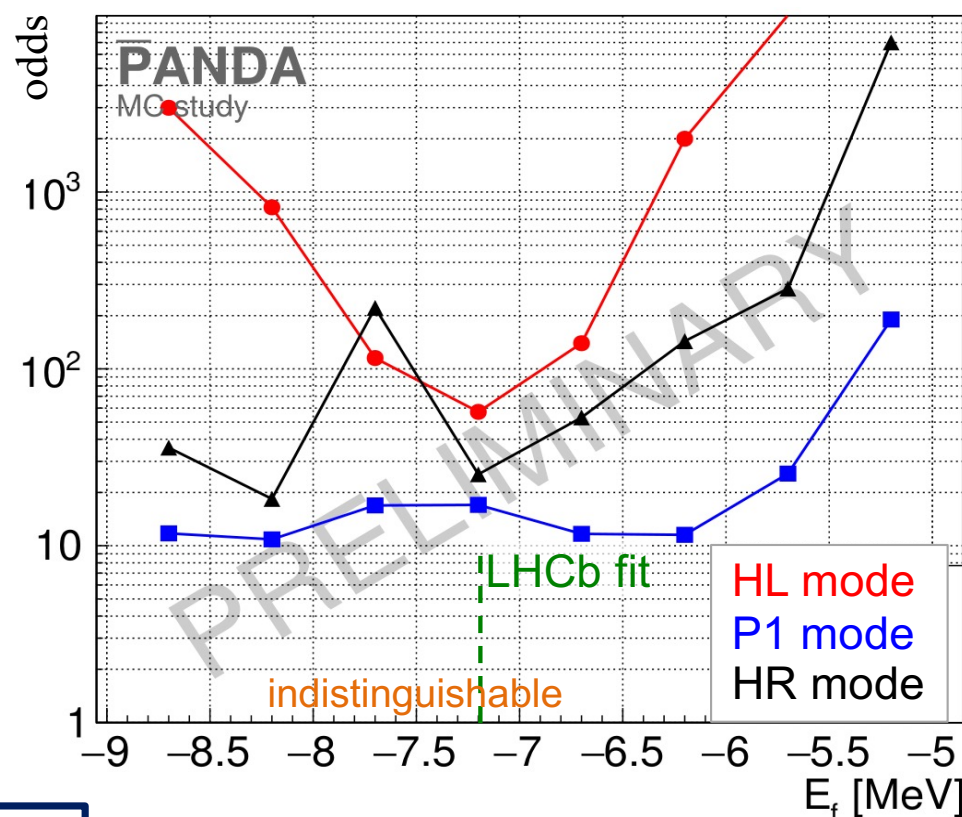
How much better are we than "indistinguishable"?

Idea: Consider so-called **odds** := correct identifications per wrong one

Flatté → BW



At least ~10x better than indistinguishable (full range)



$$\text{odds} = (1 - P_{\text{mis}}) / P_{\text{mis}}$$

# Summary & Conclusions

- Feasibility study for resonance energy scans at PANDA
  - Lineshape and width measurements for  $X(3872)$
  - Achievable performance quantified
- Determined sensitivity for BW width measurement
  - Sensitivity  $\Gamma/\Delta\Gamma > 5$  at  $\Gamma \gtrsim 50 \dots 120$  keV
  - HR mode performs better for smaller widths
- Determined sensitivity for molecular line-shape measurement
  - Possible to distinguish bound/virtual state
  - $P_{\text{HR,HL}} > 90\%$  for  $|E_f - E_{f,\text{th}}| \gtrsim 700$  keV
  - Sub-MeV resolution on  $|E_f - E_{f,\text{th}}|$  already for Phase-1 (P1)
  - HL mode performs better over investigated

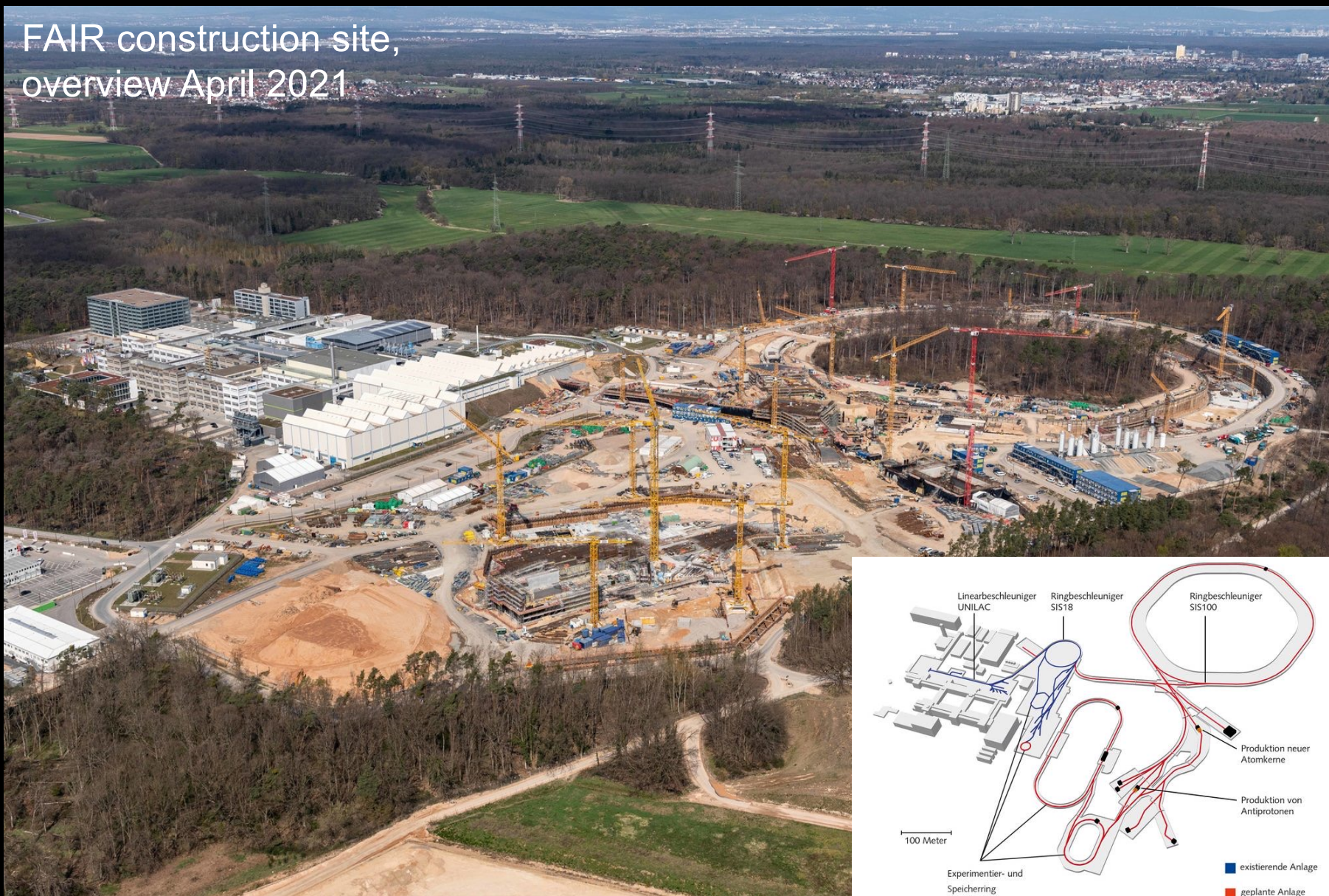


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- Comparison to recent LHCb result
  - Simulation of  $X(3872)$  line shape measurement at PANDA extended  
=> Different models can be well distinguished
  - Correct assignment of fit model over full range between  $\gtrsim 90\%$  (P1) and  $\gtrsim 98\%$  (HL) depending on beam mode
  - At least  $\sim 10\times$  higher odds to identify correct model than LHCb



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overview April 2021





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